

## GOAL

Perform a physics-informed Bayesian Analysis (BA) to test hybrid star EOS under modern astrophysical constraints.

## HYBRID EOS

The hybrid EOS allowing a first-order phase transition from hadronic to two-flavor color-superconducting (2SC) quark matter, was constructed with a two-phase approach:

- The hadronic phase is represented by the **DD2 density-dependent relativistic mean-field EOS**.
- The quark matter phase is described by a **nonlocal chiral quark model with 2SC phase**.

## NONLOCAL CHIRAL 2SC

The effective Euclidean action for quark matter is given by:

$$S_E = \int d^4x \left\{ \bar{\psi}(x) (-i\partial + \hat{m} - \gamma_0 \hat{\mu}) \psi(x) - \frac{G_S}{2} [j_S^f(x) j_S^f(x) + \eta_D [j_D^a(x)]^\dagger j_D^a(x) - \eta_V j_V^\mu(x) j_V^\mu(x)] \right\}$$

with scalar and diquark nonlocal currents:

$$j_S^f(x) = \int d^4z g_S(z) \bar{\psi}(x + \frac{z}{2}) \Gamma_f \psi(x - \frac{z}{2}),$$

$$j_D^a(x) = \int d^4z g_D(z) \bar{\psi}_C(x + \frac{z}{2}) i\gamma_5 \tau_2 \lambda_a \psi(x - \frac{z}{2}),$$

$$j_V^\mu(x) = \int d^4z g_V(z) \bar{\psi}(x + \frac{z}{2}) i\gamma^\mu \psi(x - \frac{z}{2}),$$

For the nonlocality a **Gaussian ansatz is employed** which after Fourier transformation to the momentum space reads (the vector current is taken local!):

$$g_i(\vec{p}) = \exp(-\vec{p}^2 / \Lambda_i^2), \quad i = S, D$$

The quark matter EOS is parameterized by the **dimensionless couplings** ( $G_S = 9.92 \text{ GeV}^{-2}$ ):

$$\eta_V = G_V / G_S \quad \text{and} \quad \eta_D = G_D / G_S$$

## BA WITH MULTI-MESS. ASTRO.

A physics-informed Bayesian analysis is then performed to constrain  $(\eta_D, \eta_V)$  using observational data:

- NICER **mass-radius measurements** (e.g. PSR J0030+0451)
- Gravitational-wave **tidal deformability** from GW170817
- Precise pulsar **mass measurements** (e.g. PSR J0348+0432)
- **Additionally: highest mass** (PSR J0952-0607 "BW") and **highly compact object** (low mass-radius) (HESS J1731-347)

## RESULTS

The Bayesian posterior favors:

- Low-to-moderate  $\eta_V \lesssim 0.6 \rightarrow$  **moderate stiffness**
- High  $\eta_D (\gtrsim 1.1) \rightarrow$  **early deconfinement** at  $M \approx 0.5-0.7 M_\odot$
- Hybrid stars are favored to have:
  - Maximum masses up to  $\approx 2.2 M_\odot$
  - Mass-insensitive radii  $R \approx 12 \text{ km}$  for  $M \approx 1.2-2.0 M_\odot$
- **Large  $\eta_V$  (stiff EOS) are disfavored** due to failure to match tidal deformability constraints.
- **Twin star configurations are allowed** in a narrow region.

## CONCLUSION

This analysis supports the scenario of **early quark deconfinement to 2SC matter** in the cores of neutron stars, consistent with all current astrophysical constraints.

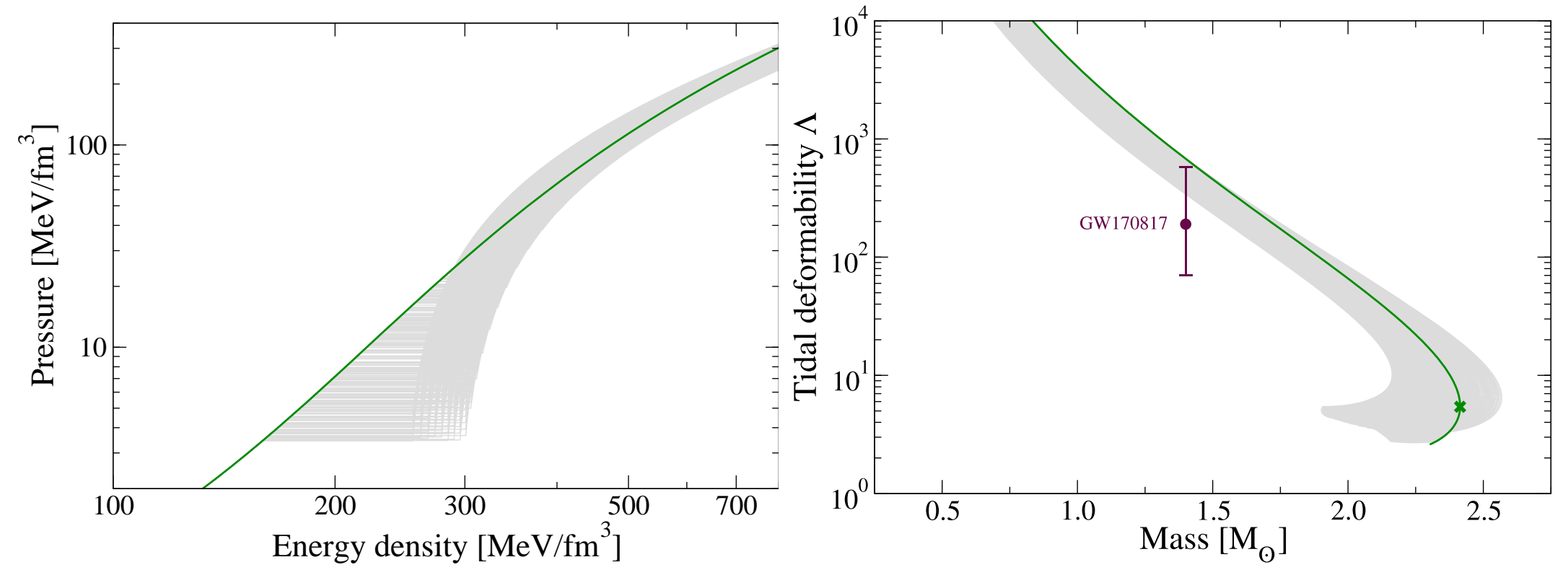


Figure 1: Pressure vs. Energy Density (left) and Tidal Deformability vs. Star Mass (right).

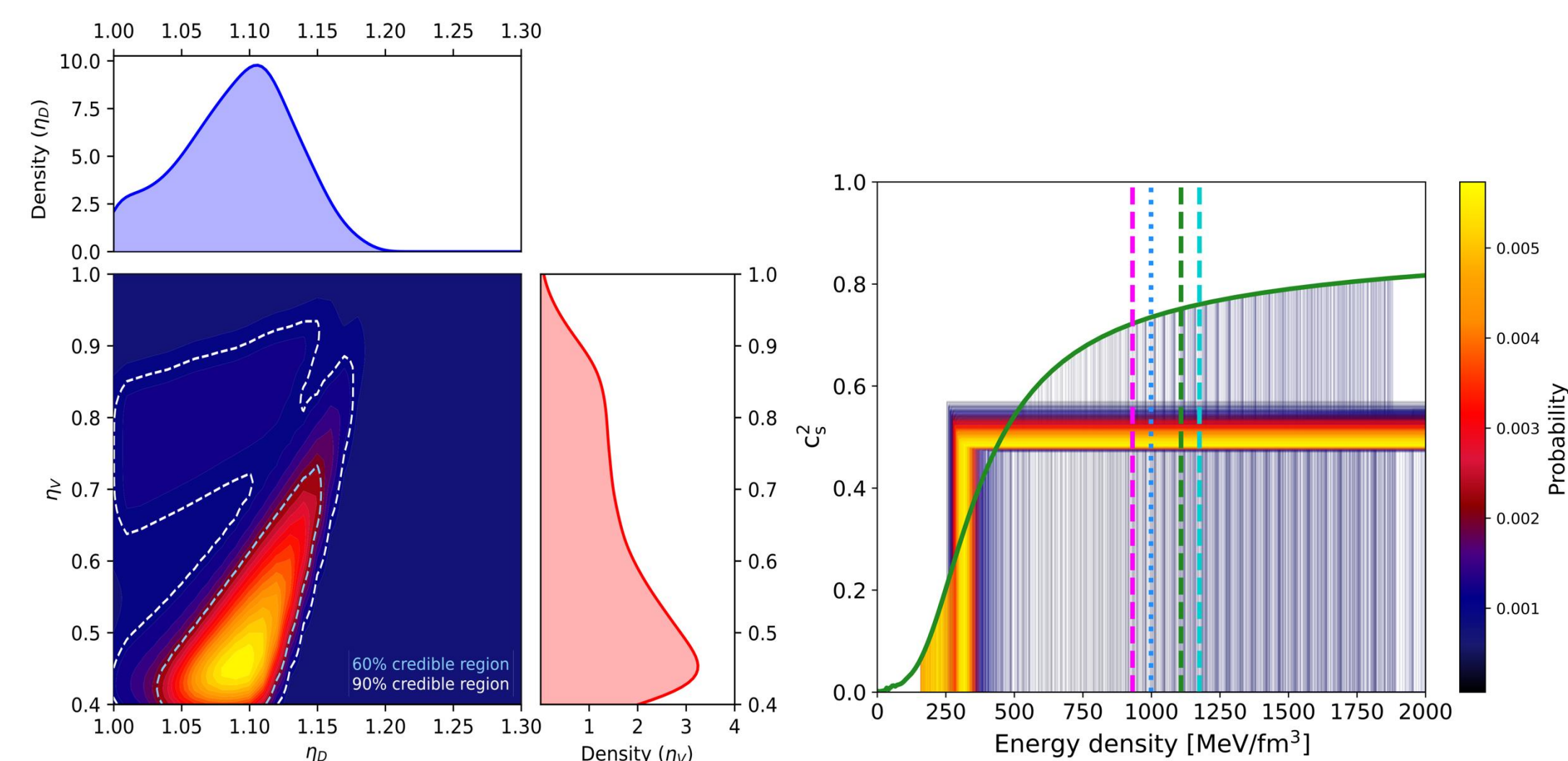


Figure 2: Bayesian Posterior in the  $(\eta_V, \eta_D)$  Plane (left) and Speed of Sound vs. Energy Density (right).

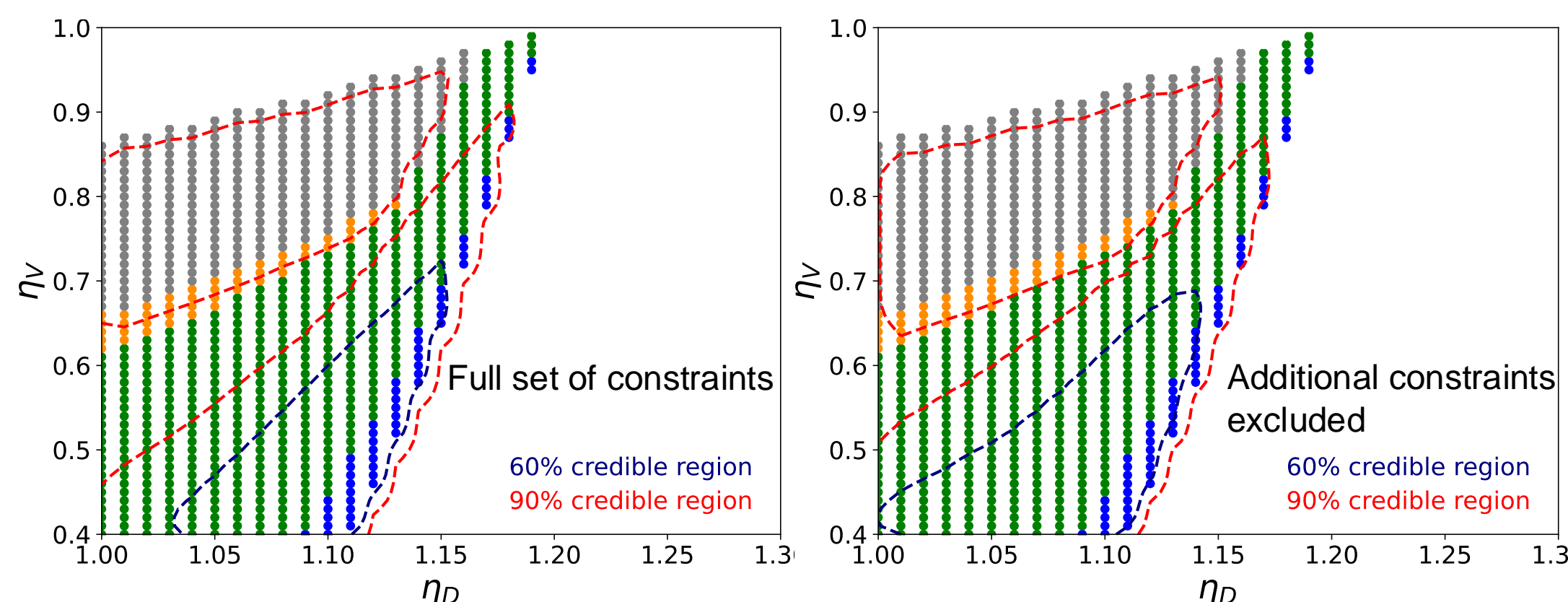


Figure 3: Phase Transition Classification. Color-coded regions in the  $(\eta_V, \eta_D)$  plane show: no hybrid stars (grey and orange), stable hybrid stars (green and blue), blue color indicates twin stars. Overlaid with 60% and 90% credibility contours.

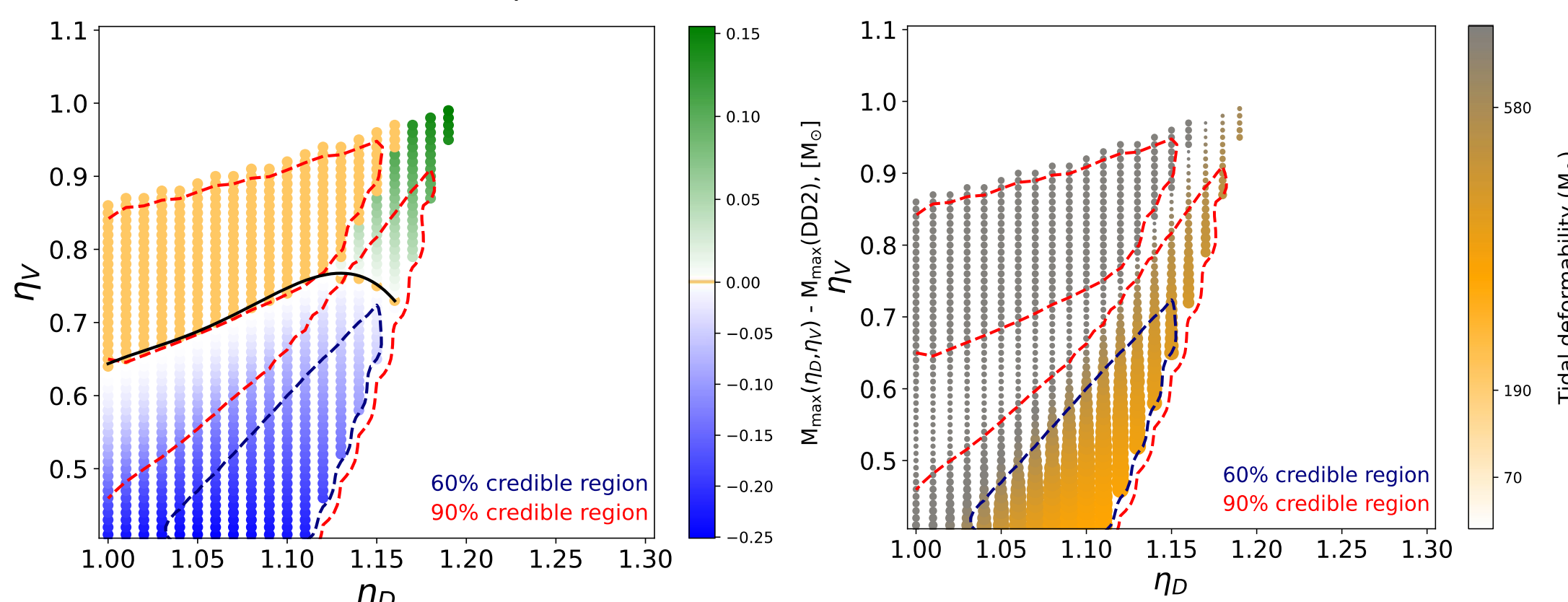


Figure 4: Maximum Mass Difference from Maximum Mass of Hadronic Star (left) and Tidal Deformability  $\Lambda$  for  $1.4 M_\odot$  in  $(\eta_V, \eta_D)$  Plane (right).

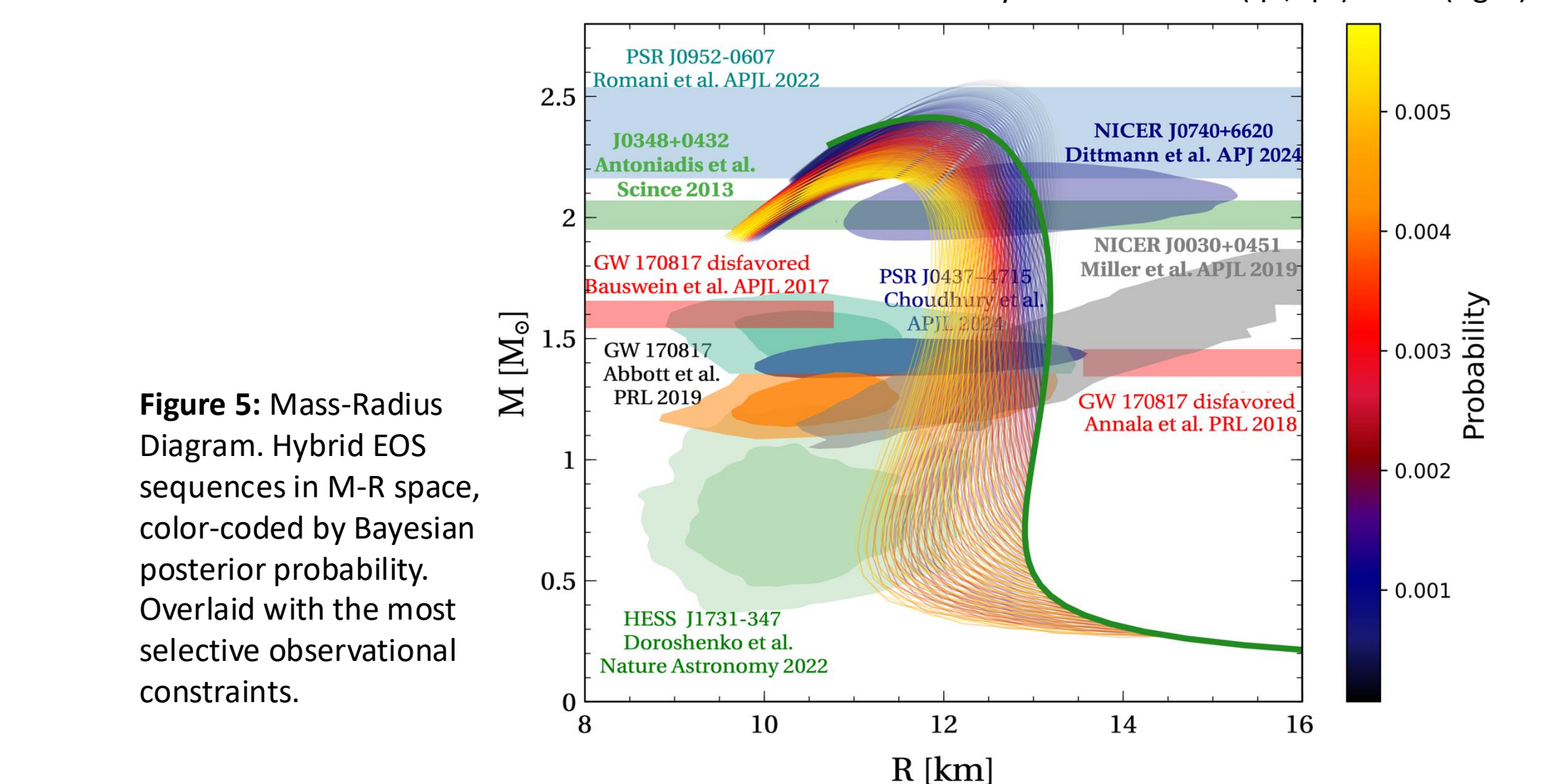


Figure 5: Mass-Radius Diagram. Hybrid EOS sequences in M-R space, color-coded by Bayesian posterior probability. Overlaid with the most selective observational constraints.

We thank Dr. Oleksii Ivanytskyi for valuable discussions. This work was supported by NCN grant No. 2021/43/P/ST2/03319 (A.A. and D.B.). A.G.G., G.A.C., and J.P.C. acknowledge CONICET, ANPCyT and UNLP (Argentina) for financial support under grants No. PIP 2022-2024 GI-11220210100150CO, PICT19-00792, PICT22-03-00799499 and X960, respectively. D.B. acknowledges a travel grant awarded by MDPI Universe.