

Signatures of ultralight bosons in the orbital eccentricity of binary black holes [2403.02415]

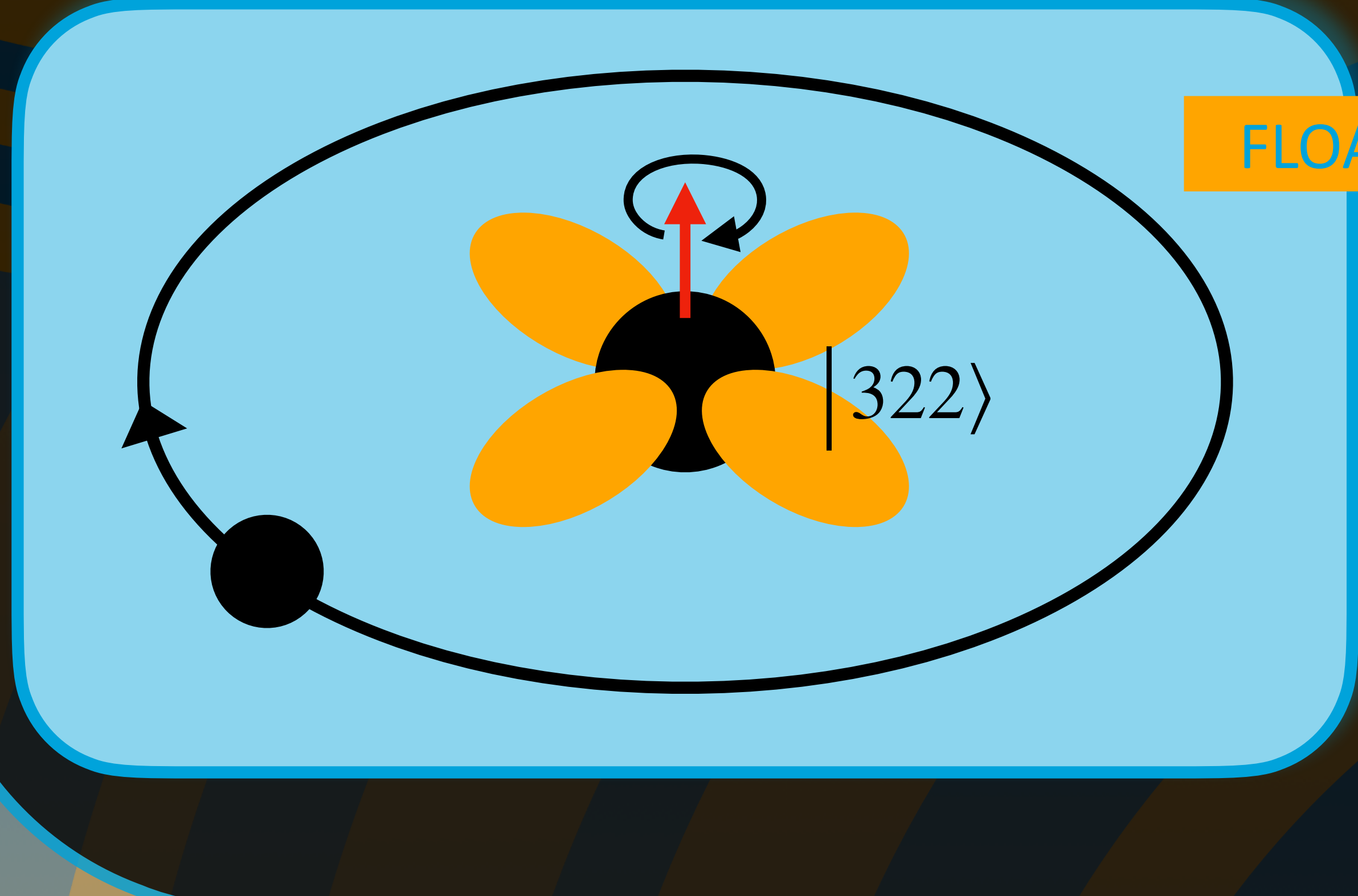
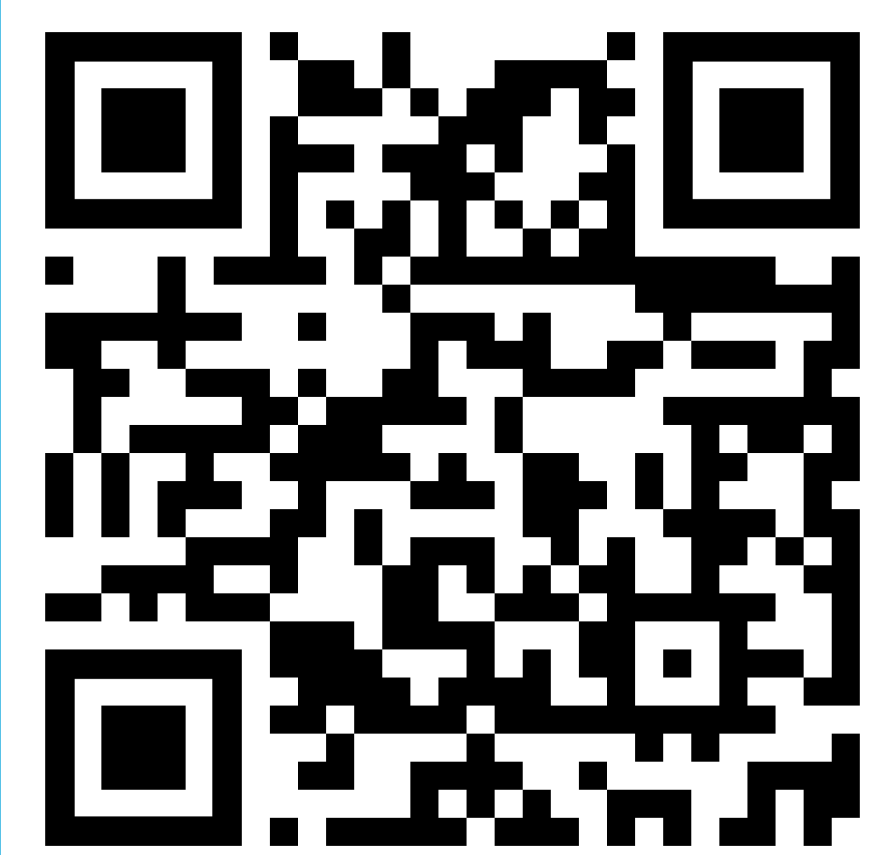
Mateja Bošković¹, Matthias Koschnitzke^{1, 2}, and Rafael A. Porto¹

1): Deutsches Elektronen-Synchrotron DESY, Notkestr. 85, 22607 Hamburg, Germany

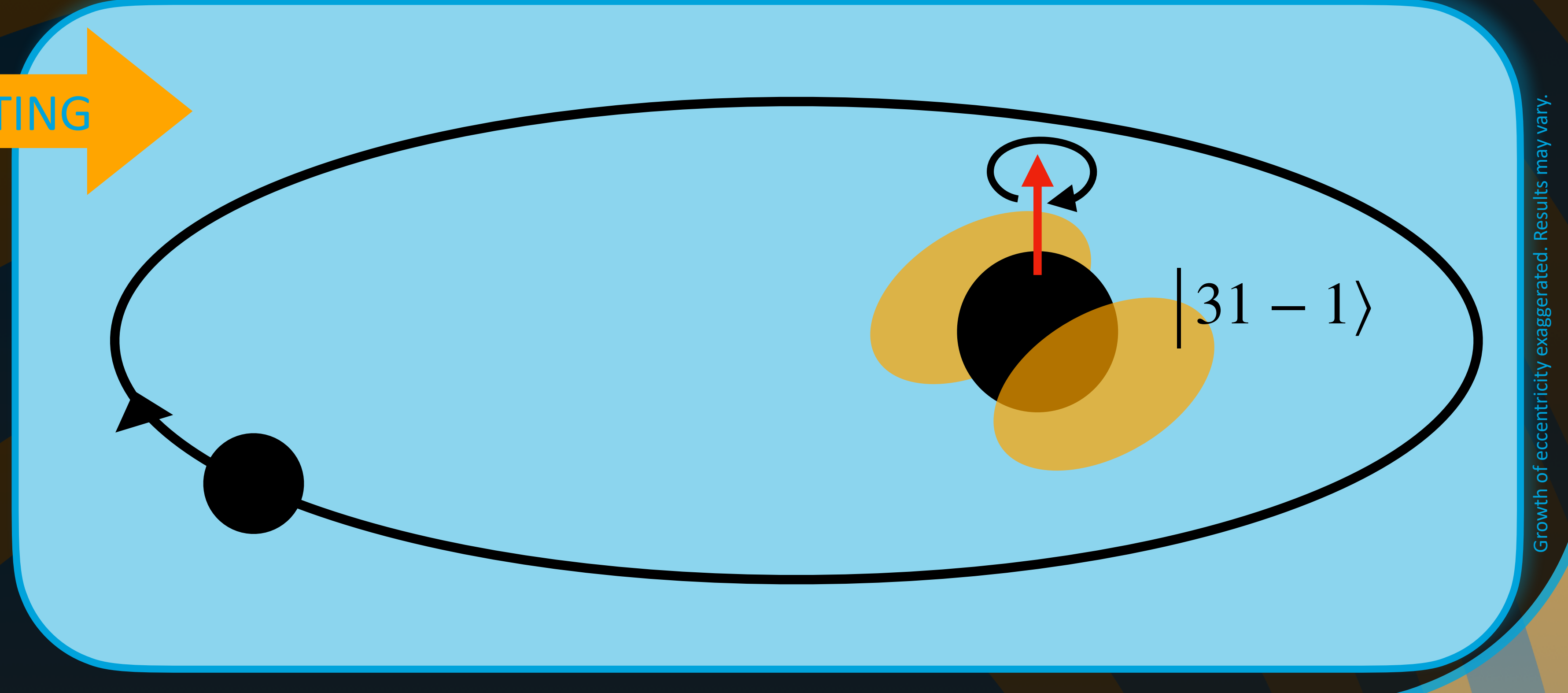
2): II. Institut für Theoretische Physik, Universität Hamburg, Luruper Chaussee 149, 22761 Hamburg, Germany

TL;DR

- If black holes carry a superradiant cloud of ultralight particles¹ (e.g., axion-like-particles), a perturbation by a binary object on an eccentric orbit can trigger overtones of the well-known Landau-Zener transition.
- If these transitions float (i.e., stall the mean orbital frequency), they can significantly increase the eccentricity of the orbit.



FLOATING



Growth of eccentricity exaggerated. Results may vary.

GRAVITATIONAL ATOM CRASHCOURSE²

= instead of proton + electron \rightarrow black hole + ultralight bosons

$$\alpha_{\text{em}} \rightarrow \alpha_{(\text{grav})} \equiv GM\mu/(\hbar c)$$

$$\alpha \approx 0.1 \left(\frac{M}{15M_{\odot}}\right) \left(\frac{\mu}{10^{-12}\text{eV}}\right)$$

$$\text{Im}(\omega_{nlm}) = 0 \rightarrow \text{Im}(\omega_{nlm}) \neq 0$$

i.e. SUPERRADIANCE³

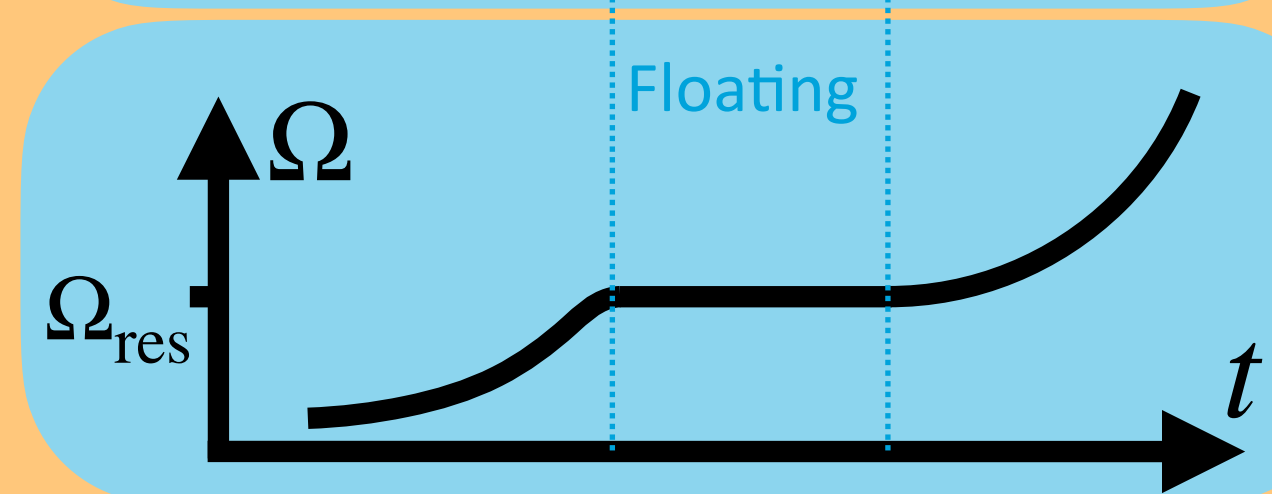
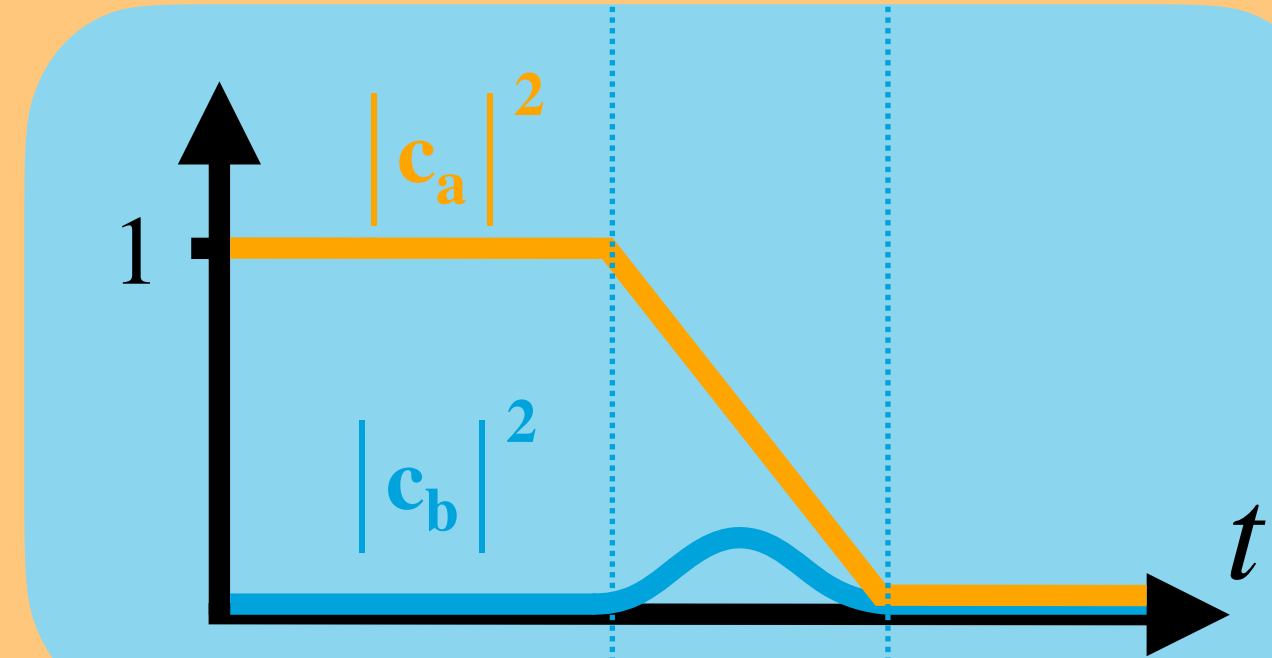
Fastest growing modes: $|211\rangle, |322\rangle$
1 fermion \rightarrow many bosons

Excitation via photons with $\omega \propto \omega_{n_2 l_2 m_2} - \omega_{n_1 l_1 m_1} \rightarrow$ Excitation via binary companion:⁴

For a two-state system $|a\rangle \equiv |n_a l_a m_a\rangle$ and $|b\rangle \equiv |n_b l_b m_b\rangle$, we get at a Schrödinger eqn.:

$$i \begin{pmatrix} \dot{c}_a \\ \dot{c}_b \end{pmatrix} = \begin{pmatrix} -\frac{\Delta E}{2} & \eta(R_*)e^{i\Delta m\varphi_*} \\ \eta(R_*)e^{-i\Delta m\varphi_*} & \frac{\Delta E}{2} - i\Gamma_b \end{pmatrix} \begin{pmatrix} c_a \\ c_b \end{pmatrix}$$

- $\Delta E, \Delta m$: energy and angular momentum differences, respectively, Γ_b : decay rate of $|b\rangle$
- $\eta(R_*)$: mixing due to the perturbation by the companion, φ_* : the true anomaly of the orbit.
- When $\Omega_{\text{res}} \equiv \dot{\varphi}_* = \Delta E/\Delta m$, we get a Landau-Zener (LZ) transition.
- If the cloud loses energy, its backreaction to the orbit stalls the inspiral \rightarrow the orbit floats!

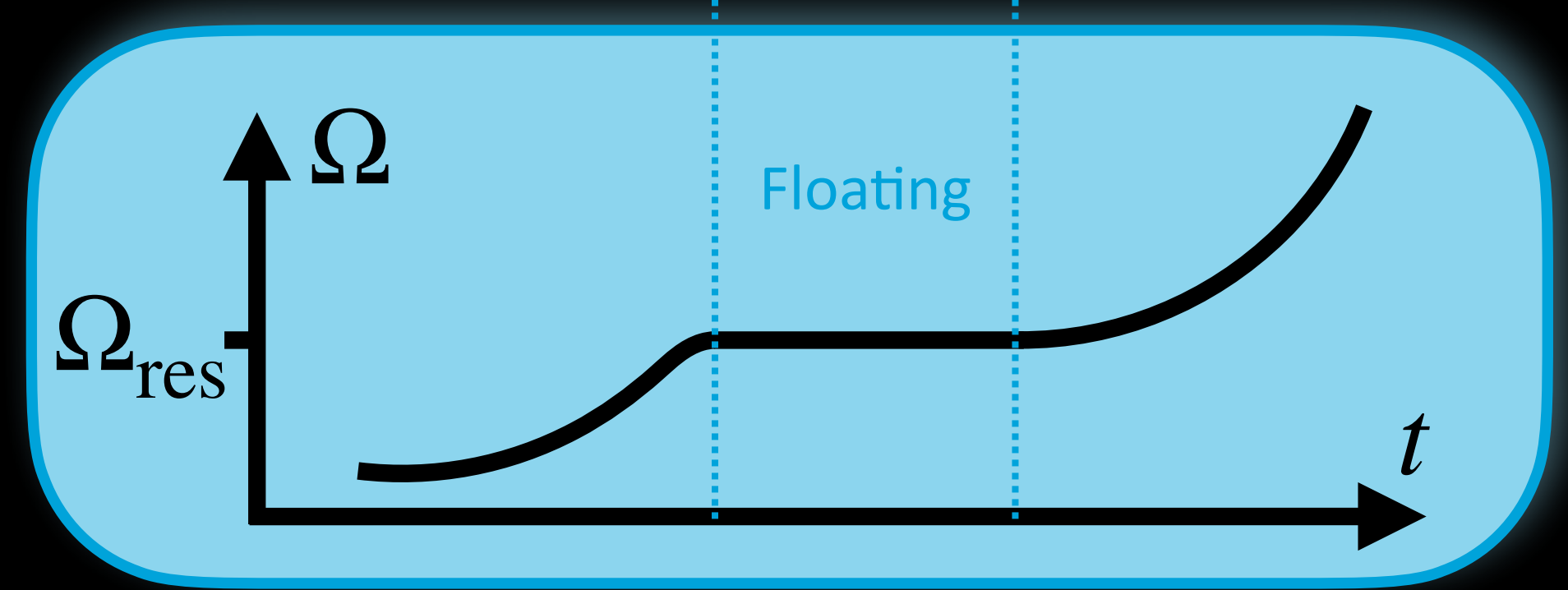
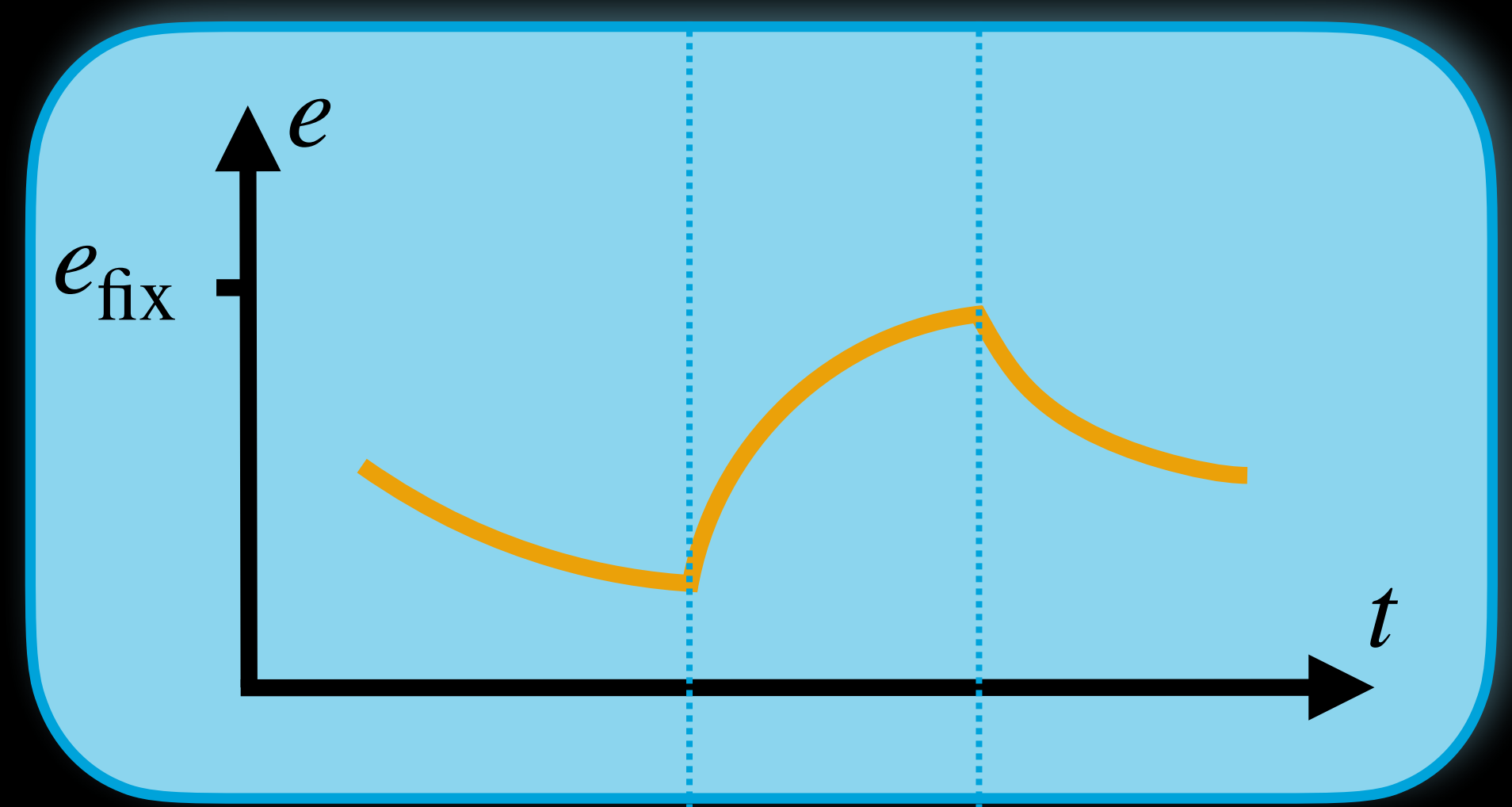


LZ transition to a decaying state

If you can read only one panel today, let it be this one:

Eccentricity Growth!

Because for eccentricity e : $\varphi_* = \vartheta + 2e \sin \vartheta + \mathcal{O}(e^2)$, with φ_* , ϑ the true and mean anomaly, respectively, we get $e^{i2e \sin \vartheta} = \sum_{k=-\infty}^{\infty} e^k / (|k|!) e^{ik\vartheta}$ in the mixing term. The condition for resonance becomes $\Omega_{\text{res},k} \equiv \dot{\vartheta} = \Delta E/(\Delta m + k) \rightarrow$ we get **early and late resonances** due to **overtones** ($k \neq 0$).⁶ During floating, the orbital energy is constant, while the angular momentum scales as $\dot{L}_0 \propto \Omega_{\text{res},k} - \Omega_{\text{res},0} + \mathcal{O}(e^2)$. We have $d(L_0^2) \propto -d(e^2)$, and find that e can change towards a non-zero fixed point! For early resonances, the eccentricity grows.



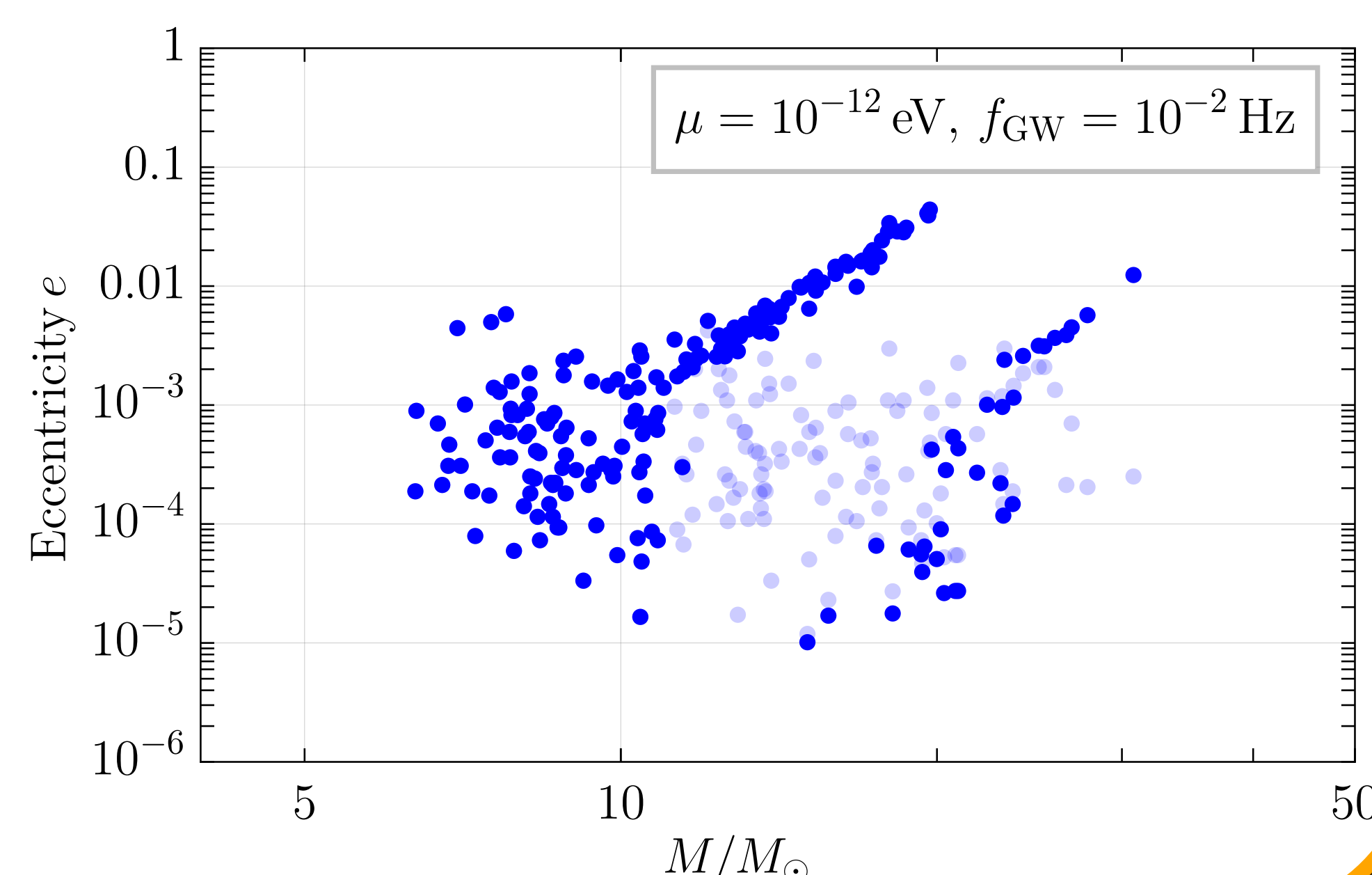
Eccentricity growth during floating

Binary Black Hole Populations in LISA⁷

We take a population of binary BHs with **chirp masses** $< 10M_{\odot}$, formed in isolation at an orbital frequency of $10^{-4}\pi\text{Hz}$. If the ultralight particle has a mass of 10^{-12}eV , the binaries experience **hyperfine** and **fine transitions**, mostly from $|322\rangle$ to $|31-1\rangle$.

At the strongest early resonances, $k \leq -1$, the eccentricity can grow. **On the right**, we show the eccentricity distribution at 10^{-2}Hz , **possibly visible in LISA**. Transparent dots show the distribution without the clouds.

For larger masses, $M_1 = 20M_{\odot}$, with companion $M_2 = 40M_{\odot}$, the eccentricity growth can also fall **into the LISA band**, with floating times of $\mathcal{O}(\text{yrs})$.



References:

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- [7] K. G. Arun, et al. (LISA), Living Rev. Rel. 25, 4 (2022)