

Cooling Demonstrator Design Studies

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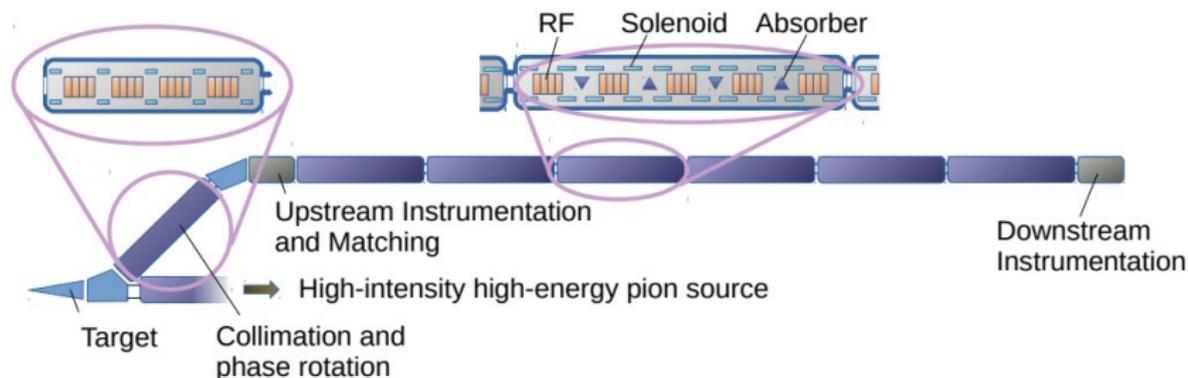
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MuCol WP8 Cooling Cell Workshop, 18 - 19 Jan 2024

Muon Cooling Demonstrator

- Ionisation cooling proof-of-principle demonstrated by MICE (2020)
 - Only one pass through an absorber
 - No acceleration
 - Transverse (4D) cooling only
- Study of 6D cooling a natural follow-up
 - Demonstrate 6D cooling
 - Stage multiple cooling cells
 - Accelerate with RF cavities
 - Achieve suitable cooling performance

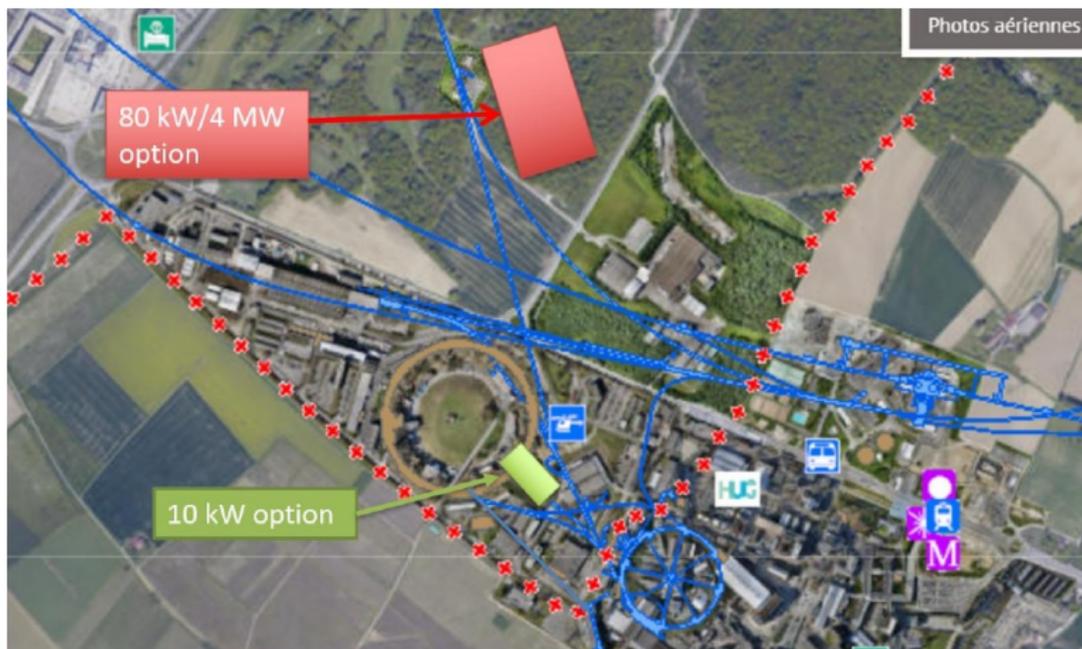
Muon Cooling Demonstrator



- Design in progress

- Preliminary cooling cell - done (C. Rogers)
- Preliminary phase rotation & collimation - done (C. Rogers)
- Muon (pion) production and transport - work in progress
 - Design informed/impacted by the siting options

Demonstrator facility siting options at CERN

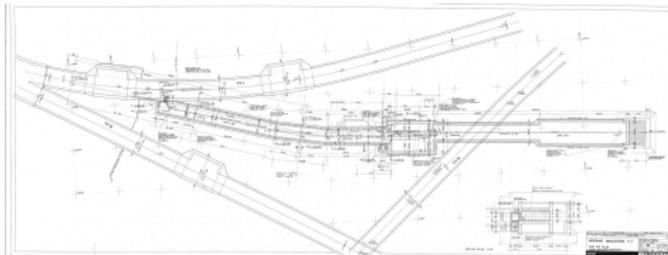


Demonstrator facility siting options at CERN

Two siting options at CERN are currently considered

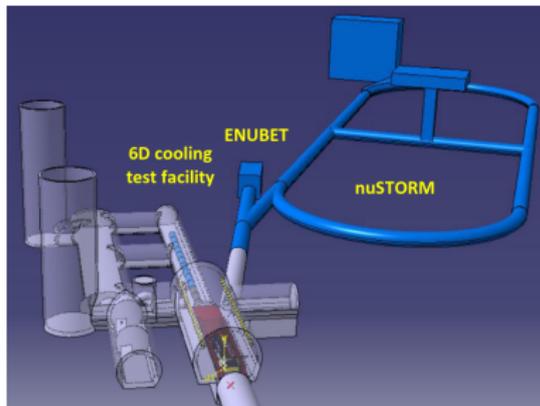
- Intersection Storage Rings (ISR) complex

- In the TT7 extraction line
- Proton beam from the PS
- Near surface level, lower proton beam power required (10kW), 14 GeV



- TT10

- Pion production system could be shared with the nuSTORM facility
- Proton beam from the PS (26 GeV) or SPS (100 GeV)
- Underground, beam power up to 80 kW (first phase)



Target & Capture System

- Protons impinge on a target \rightarrow pions \rightarrow muons
- Muon yield can be improved by:
 - Choosing a suitable target geometry and material
 - Improving the pion capture efficiency
- Pion capture usually achieved using:
 - Magnetic horns
 - Solenoid channel

Pion momentum range

- Aim to produce muons with 190-210 MeV/c momentum
- Which pions are we interested in?

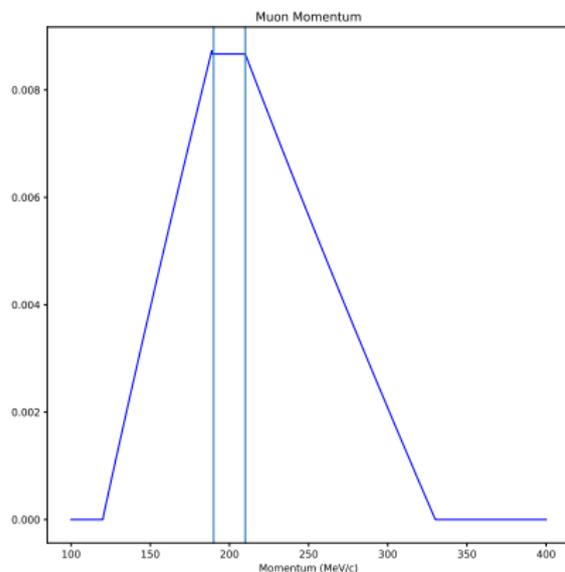
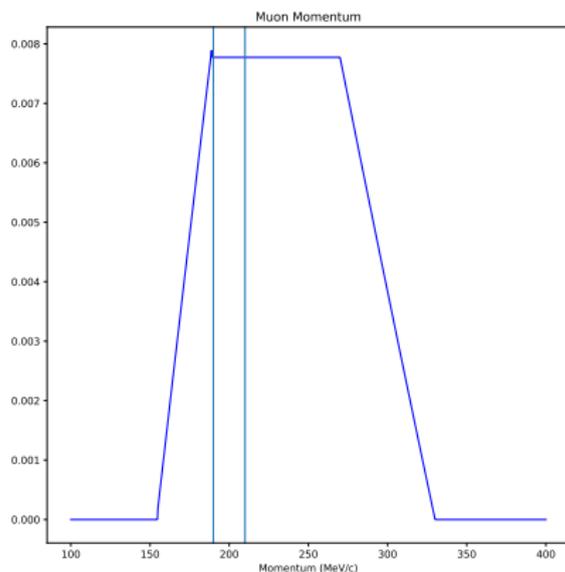
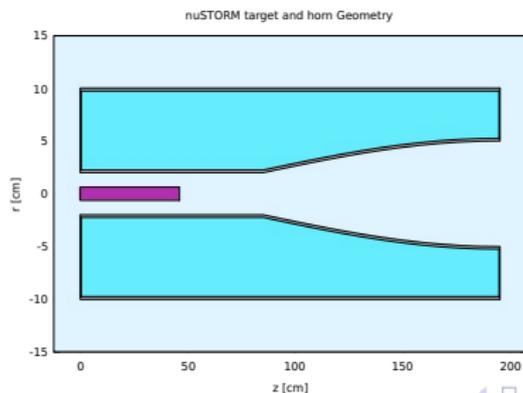


Figure: Muon distribution from a (left) 270-330 MeV/c and (right) 210-330 MeV/c pion beam.

Target & Capture System - Magnetic Horn

Baseline target and horn design derived from the FNAL nuSTORM horn optimization study [1]

- Target: Inconel, cylindrical rod, $L = 46$ cm (3 interaction lengths), $r = 0.63$ cm
- Capture: Magnetic horn, optimised to deliver 5 GeV pions (!) from a 120 GeV proton beam impinging on the target
- Currently under study @nuSTORM



π^+ yield: different proton beam energies

- Simulated 10^6 protons-on-target for the three proton beam energies considered at CERN:
 - 14, 26 and 100 GeV (all with $\sigma_{x,y} = 2.67$ mm)
- Horn current: $I = 220$ kA
- Estimated the yield of π^+ with momenta in the 270 - 330 MeV/c range and within a transverse acceptance cut of 2 mm rad

π^+ yield: different proton beam energies

Table: Pion yield in the 270 - 330 MeV/c range

E_0 [GeV]	14	26	100
At target [/POT]	0.10	0.15	0.35
At horn exit [10^{-2} /POT]	1.06	1.63	4.01
Within 2 mm rad [10^{-4} /POT]	3.24	5.16	13.75
Energy normalised [10^{-5} /POT/GeV]	2.31	1.99	1.38

- Number of pions produced at target scale with the proton beam energy
- Pion yield per proton energy largest at 14 GeV
- N.B. Capture efficiency to be improved

π^+ at target: Angle Distribution

π^+ in the 270-330 MeV/c momentum range

Angle: $\theta = \arctan(p_T/p_z)$

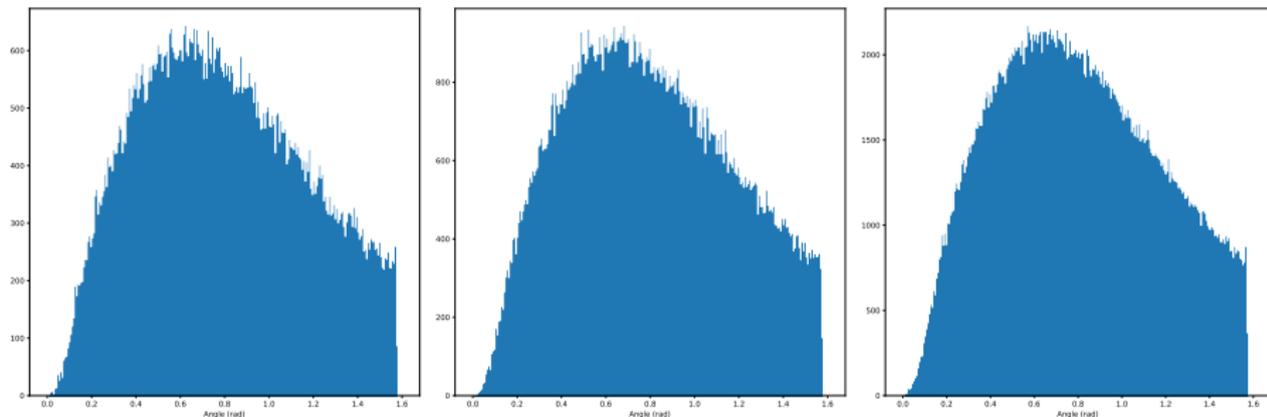


Figure: (left) 14 GeV, (middle) 26 GeV, (right) 100 GeV proton beam energy

π^+ yield: different proton energies - graphite

Choice of material motivated by the extensive knowledge and use of graphite targets.

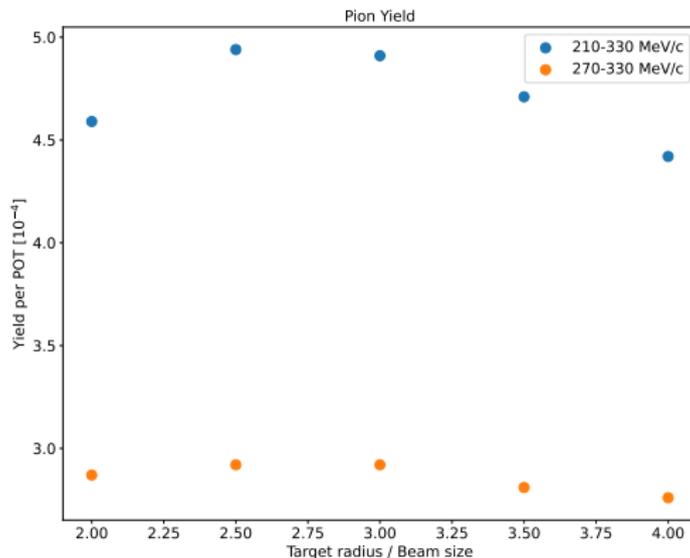
- Target: Graphite, cylindrical, $L = 80$ cm (1.78 interaction lengths), $r = 0.63$ cm
- Capture: Horn, $I = 220$ kA

Table: Pion yield in the 270 - 330 MeV/c range

E_0 [GeV]	14	26	100
At target [/POT]	0.07	0.09	0.16
At horn exit [10^{-2} /POT]	0.79	1.05	2.07
Within 2 mm rad [10^{-4} /POT]	2.80	4.27	7.53
Energy normalised [10^{-5} /POT/GeV]	2.00	1.64	0.75

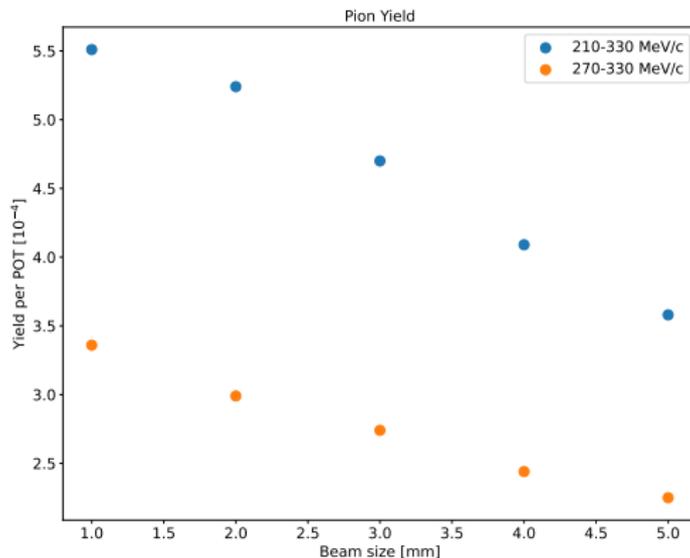
Graphite target: radius/beam size optimisation

- Proton beam: $E = 14 \text{ GeV}$, $\sigma_{x,y} = 2.67 \text{ mm}$
- Target: Graphite, cylindrical
- Target radius varied between 2 and 4 times the beam size
- Capture: Horn, $I = 220 \text{ kA}$
- Simulated $5.0 \times 10^6 \text{ POT}$ for each configuration



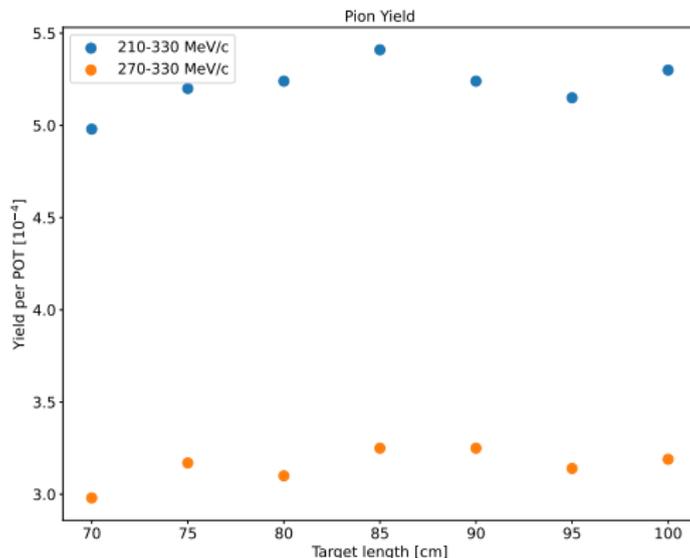
Graphite target: proton beam size optimisation

- Proton beam: $E = 14$ GeV
- Target: Graphite, cylindrical, $r = 3\sigma_{x,y}$
- Proton beam size varied between 1 and 5 mm
- Capture: Horn, $I = 220$ kA
- Simulated 2.0×10^6 POT for each configuration

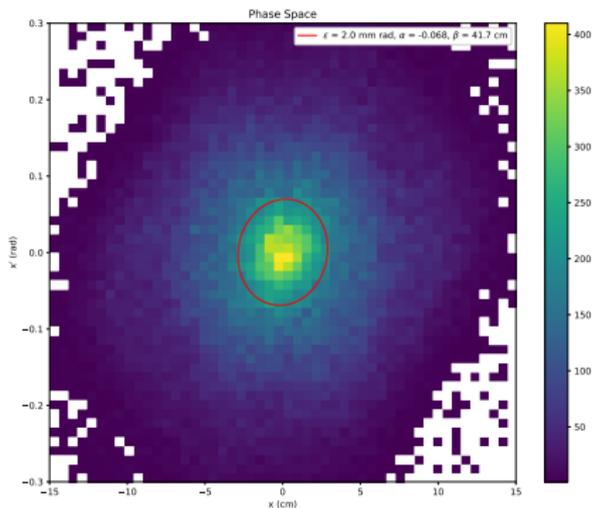
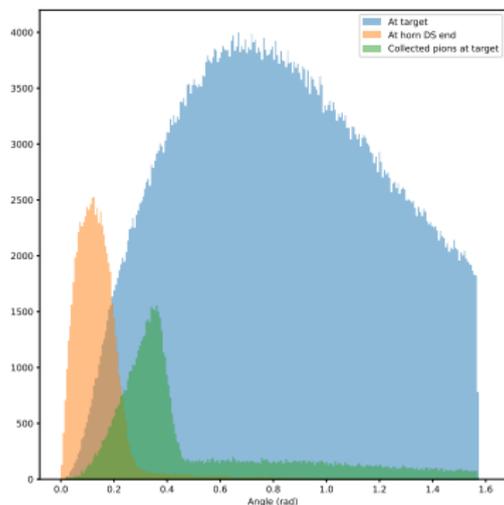


Graphite target: Length optimisation

- Proton beam: $E = 14 \text{ GeV}$, $\sigma_{x,y} = 2 \text{ mm}$
- Target: Graphite, cylindrical, $r = 3\sigma_{x,y}$
- Capture: Horn, $I = 220 \text{ kA}$
- Simulated $5.0 \times 10^6 \text{ POT}$ for each configuration



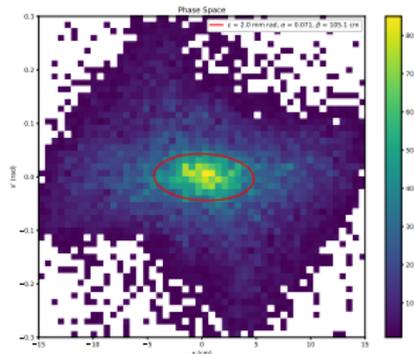
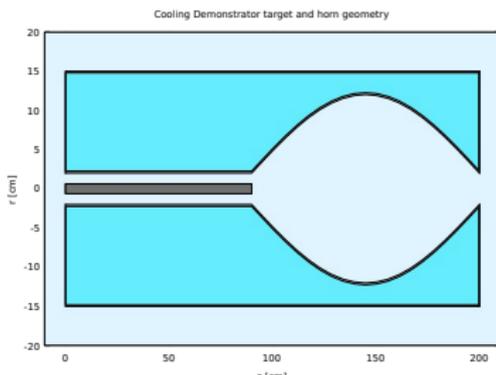
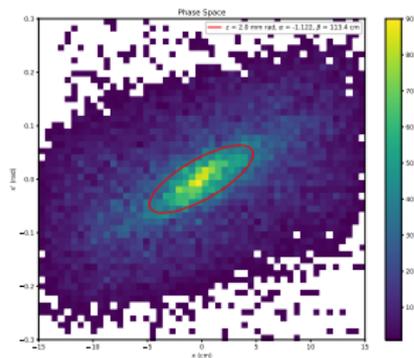
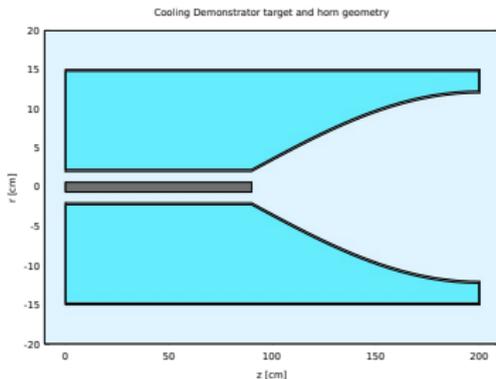
Capture: challenges



- Large pion angles, with a majority of pions produced outside the effective angular acceptance of existing horn
- Small fraction of captured pions useful for producing muons within the transverse emittance required

Capture: optimisation

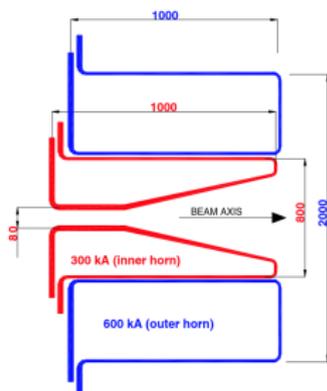
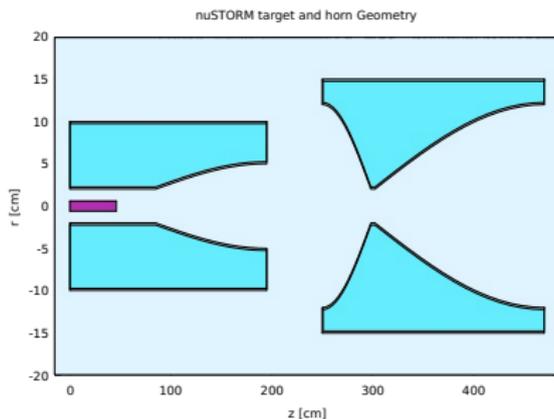
- Horn geometry can be further optimised → currently under study



Capture: optimisation

Can pursue higher yields using:

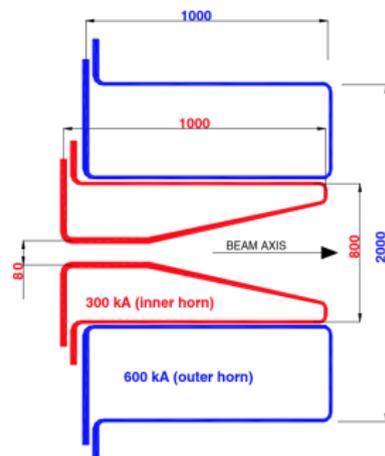
- Multiple horns



- Solenoid capture - more challenging for the low power option (and expensive regardless)
 - To be explored

Neutrino Factory horn prototype

- Simone Gilardoni thesis
- Proton beam: $E = 2.2 \text{ GeV}$, $\sigma_{x,y} = 2.2 \text{ mm}$
- Target: Mercury, cylindrical, $L = 30 \text{ cm}$, $r = 0.75 \text{ cm}$
- Yield for pions in 200-800 MeV and 4.2 mm rad transverse acceptance:
 - $1.4 \times 10^{-3} \pi^+/\text{POT}$
 - $0.6 \times 10^{-3} \pi^+/\text{POT}/\text{GeV}$
- Yield for the TT7 option – 10 kW (14 GeV) proton beam, graphite target, one horn 220 kA – in the same momentum and transverse acceptances:
 - $1.9 \times 10^{-2} \pi^+/\text{POT}$
 - $1.4 \times 10^{-3} \pi^+/\text{POT}/\text{GeV}$



How many muons/POT in 190-210 MeV/c?

TT7 - Graphite

- Proton beam: $E = 14 \text{ GeV}$, $\sigma_{x,y} = 2 \text{ mm}$
- Target: Graphite, $L = 80 \text{ cm}$, $r = 3\sigma_{x,y}$
- Horn: $I = 220 \text{ kA}$

For a pion momentum bite of 210-330 MeV/c:

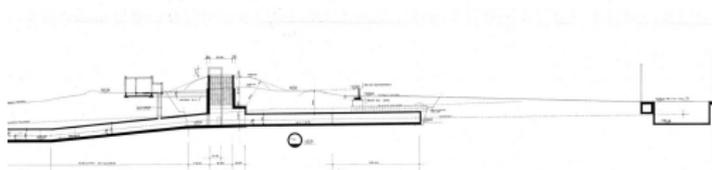
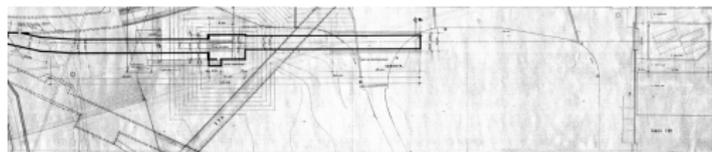
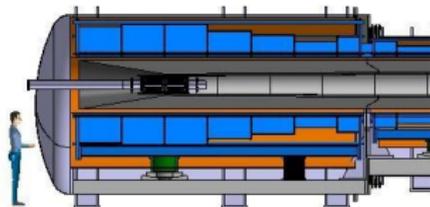
- 2 mm rad $\rightarrow 7.9 \times 10^{-4} \pi^+/\text{POT} \rightarrow 1.53 \times 10^{-4} \mu^+/\text{POT}$

N.B.

- Bunch time structure not considered yet
- Expect to produce 5 - 10 100 ps bunches from a $\sim 7 \text{ ns}$ pulse

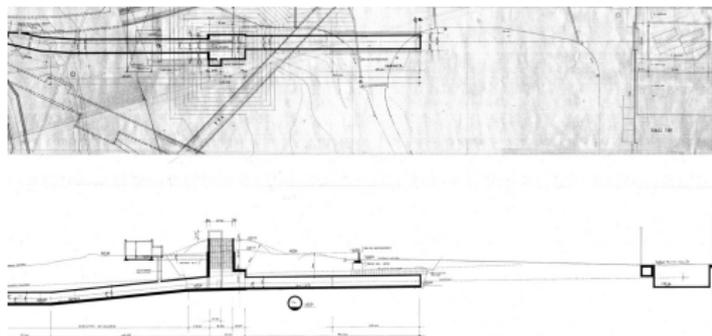
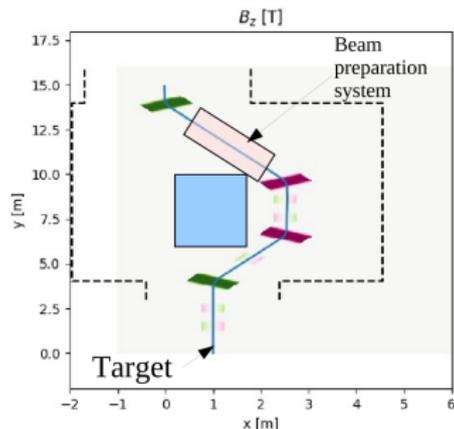
Next Steps: solenoid capture

- Comparative study with the magnetic horn
- Some space concerns:
 - Tunnel only about 2.8 m wide
 - Solenoid + decay channel may require 10 - 20 m in length
 - Current assumption is that the beam dump (and chicane) will be located in the chamber in the middle region of the tunnel → target in region where the tunnel has an incline?



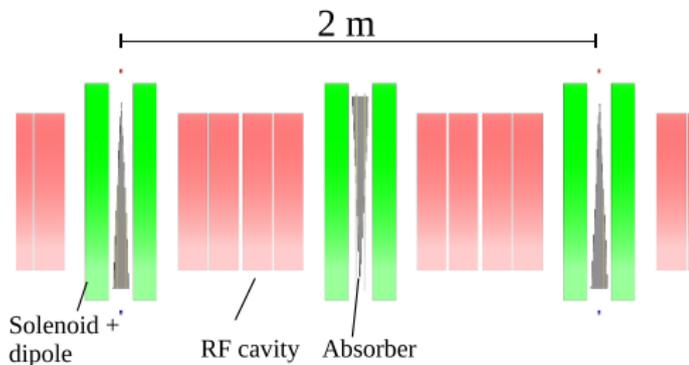
Next Steps: beam transport

- Transport: target → beam preparation system → cooling stage
 - Finalize design, integrate in one simulation



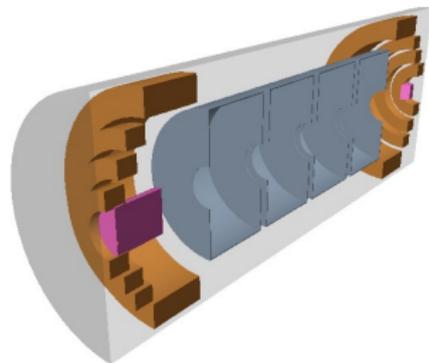
- Ideally pions would decay into muons before the chicane → can we place the target further upstream?

Next Steps: cooling cell



Cooling System	
Cell length	2 m
Peak solenoid field on-axis	7.2 T
Dipole field	0.2 T
Dipole length	0.1 m
RF real estate gradient	22 MV/m
RF nominal phase	20°
RF frequency	704 MHz
Wedge thickness on-axis	0.0342 m
Wedge apex angle	5°
Wedge material	LiH

- Implement preliminary cooling cell lattice design (C. Rogers) in BDSIM
- Study performance and iterate design
- Integrate in a start-to-end simulation



- Target & capture preliminary design done
 - 14 GeV proton beam option feasible for TT7 option provided adequate capture
 - Efficient capture is challenging due to the large pion angles
 - Priority is horn-based capture, with a solenoid comparison study to follow
- 190 - 210 MeV/c muon yield $\sim \mathcal{O}(10^{-4}/POT)$ for a few ns pulse. Further work required to account for:
 - Bunch time structure
 - Pion and muon losses during transport to the cooling channel
- Plans to develop a cooling channel model in BDSIM and integrate it in a start-to-end demonstrator simulation



A. Liu, A. Bross, and D. Neuffer.

Optimization of the magnetic horn for the nustorm non-conventional neutrino beam using the genetic algorithm.

Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, 794:200–205, 2015.

Thank you!

Back-up

Magnetic Horn Focusing

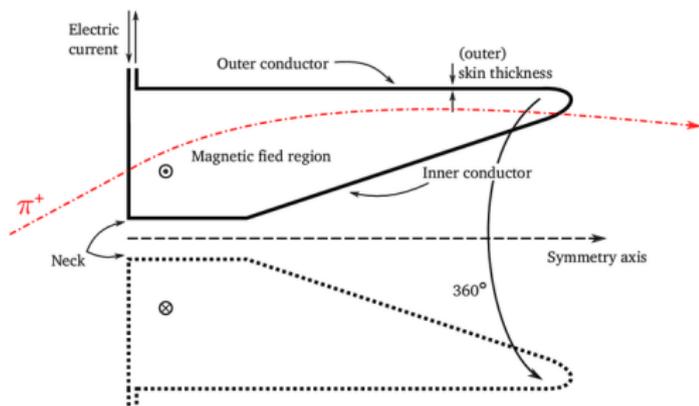
Toroidal magnetic field generated between the inner and outer conductors

$$B_\phi = \frac{\mu_0 I}{2\pi r}; B_z = B_r = 0$$

Induces a radial kick to charged particles passing through the field region

$$\Delta\theta = \frac{B_\phi z}{p} = \frac{\mu_0 I}{2\pi r} \frac{z}{p}$$

Horn geometries generally seek to ensure a larger radial kick for particles entering the field region at larger radii.



- Used FLUKA to simulate the proton-target interaction and tracking of the secondary particles in the magnetic field of the horn
- Horn and target geometries derived from code provided by John Back (nuSTORM GitHub repository)
- Particle position and momentum recorded at:
 - the downstream end of the horn, within the outer conductor radius
 - the target surface

π^+ at target: Longitudinal Position Distribution (z)

π^+ in the 270-330 MeV/c momentum range

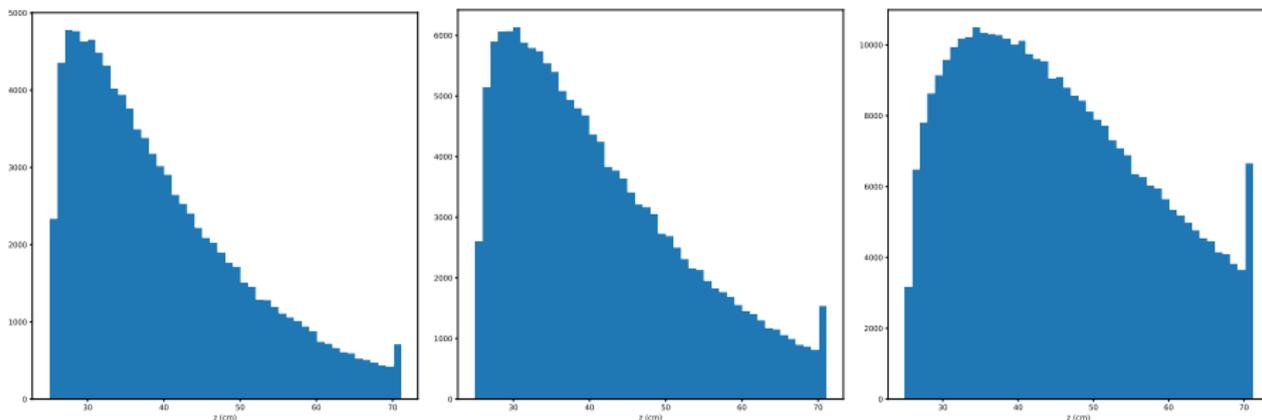


Figure: (left) 14 GeV, (middle) 26 GeV, (right) 100 GeV proton beam energy

At lower proton beam energies, more pions are emitted towards the upstream end of the target. Might inform capture system design.

Pion momentum range

- The wider momentum range (2x) provides $\sim 70\%$ more captured pions in the transverse phase space of interest (2 mm rad)
- Further study required
 - Consider transfer line & cooling channel acceptance. The 190-210 MeV/c muon sample will contain muons that decay backwards and sideways in the pion rest frame. Muons that decay orthogonally to the pion momentum will have a divergence of ~ 150 mrad ($p_T \approx 30$ MeV/c)
 - PID implications?

Muon yield estimation: Horn Capture

TT10 (nuSTORM) - Inconel

- Proton beam: $E = 100 \text{ GeV}$, $\sigma_{x,y} = 2.67 \text{ mm}$
- Target: Inconel, $L = 46 \text{ cm}$, $r = 0.63 \text{ cm}$
- Horn: $I = 220 \text{ kA}$

For a pion momentum bite of 270-330 MeV/c:

- 2 mm rad $\rightarrow 13.8 \times 10^{-4} \pi^+/\text{POT} \rightarrow 2.4 \times 10^{-4} \mu^+/\text{POT}$

N.B.

- Bunch time structure not considered yet
- Pion capture efficiency can be improved