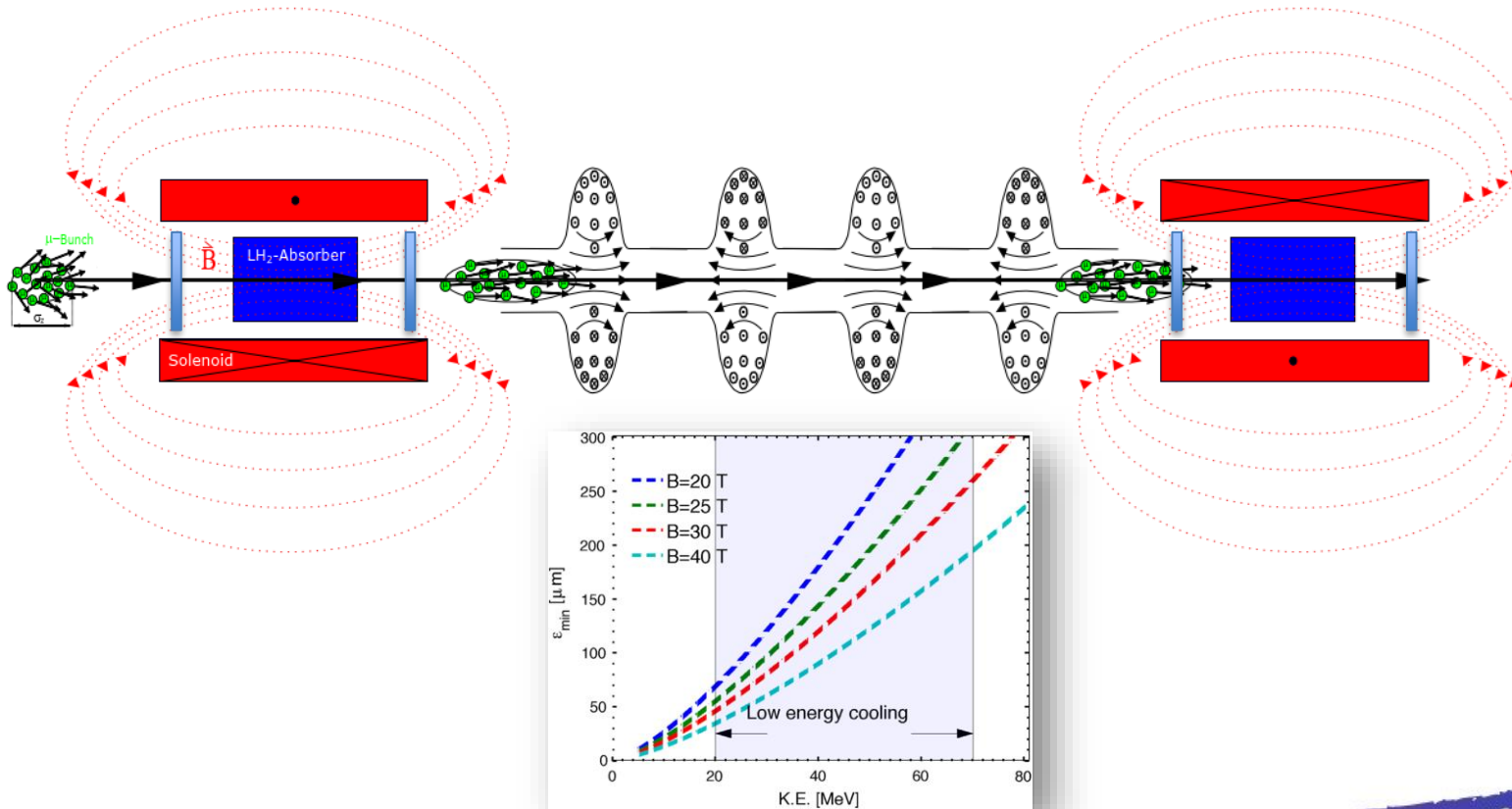
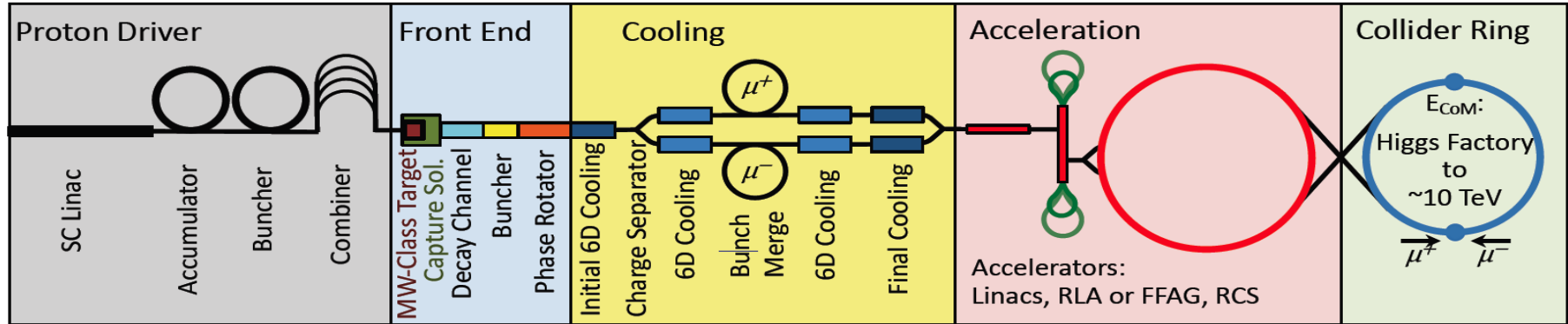
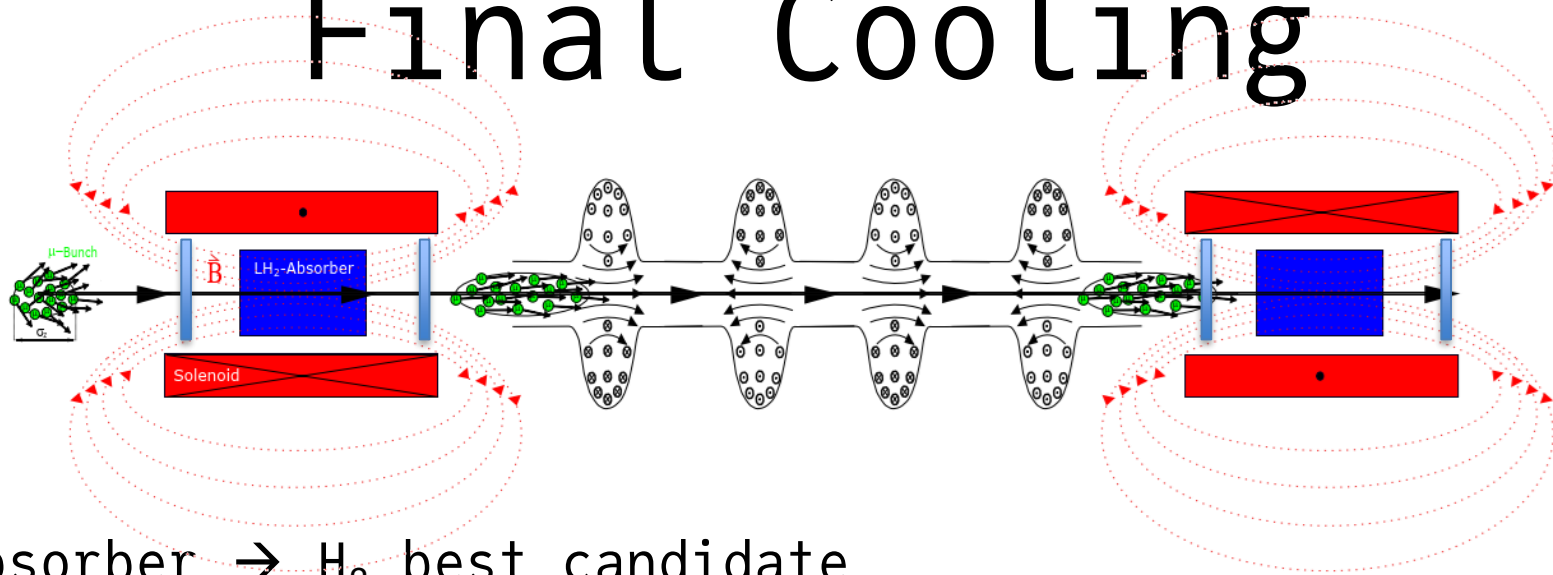


Windows for final cooling

Introduction



Final Cooling



- ❑ Absorber → H₂ best candidate
- ❑ For liquid/gas absorber → Vacuum windows are required^[1]
- ❑ Windows may be required even for solids (thermal desorption)
- ❑ Low energy → Thin windows

TABLE II. Parameters of the high-field low-energy cooling channel.

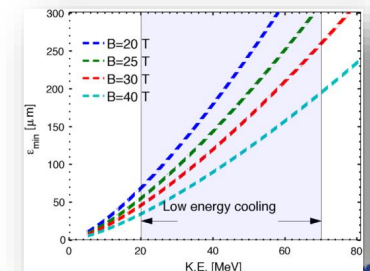
Stage [N]	P [MeV/c]	Energy spread σ_E [MeV]	LH ₂ thickness [cm]	Drift length [m]	rf length [m]	rf frequency [MHz]	Field flip
1	135.0	2.29	65	0.434	2.25	325	Yes
2	130.0	2.48	60	0.459	2.25	250	Yes
3	129.0	2.78	60	0.450	2.5	220	No
4	129.0	3.10	59	0.458	2.5	201	No
5	122.0	3.60	57	1.629	5.0	201	Yes
6	124.0	4.90	53	2.22	4.5	180	No
7	116.0	3.40	42	2.21	3.25	150	No
8	111.0	3.90	40	2.0	3.5	150	No
9	106.0	3.50	40	3.13	5.0	125	Yes
10	98.0	3.07	35	3.13	5.0	120	No
11	89.4	3.11	20	3.12	5.0	110	No
12	87.9	2.76	20	3.1	8.0	100	No
13	85.9	2.67	20	3.0	7.5	100	Yes
14	79.7	3.08	15	2.7	7.0	70	No
15	71.1	4.0	15	2.6	6.0	50	No
16	71.0	3.80	13	2.5	6.0	20	No
17	70.0	3.80	10	20	...



Initial Momentum (MeV/c)	Initial kinetic energy (MeV)	Final kinetic energy MeV
135	65.8	39.3
130	61.9	36.7
129	61.1	35.7
129	61.1	36.2
122	55.7	30.1
124	57.3	34.2
116	51.2	32.1
111	47.6	28.5
106	44.0	23.5
98	38.5	18.6
89.4	32.7	21.1
87.9	31.8	19.8
85.9	30.5	18.0
79.7	26.7	16.6
71.1	21.7	8.8
71	21.6	11.0
70	21.1	13.2

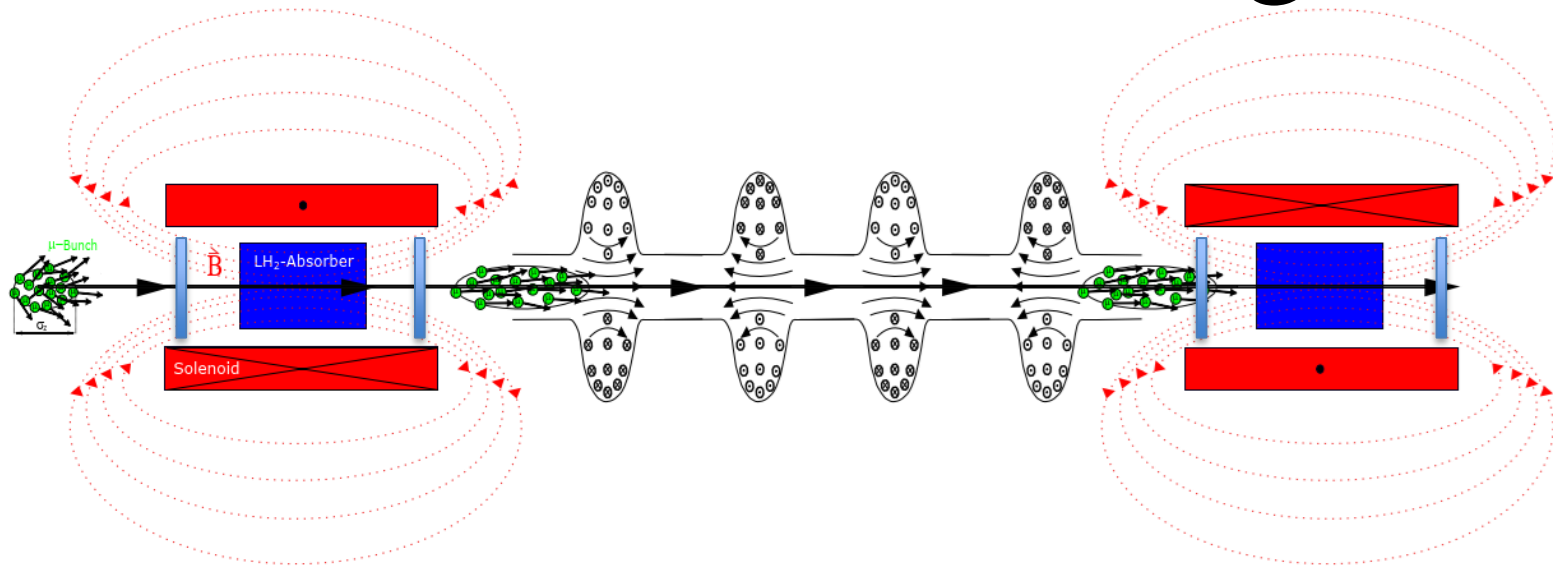
Parameters:

- 20 to 5 MeV cooling
- 4e12 muons/pulse
- 5 Hz repetition rate
- $\sigma_{RMS}=0.6$ mm



[2]

Final Cooling



[10]

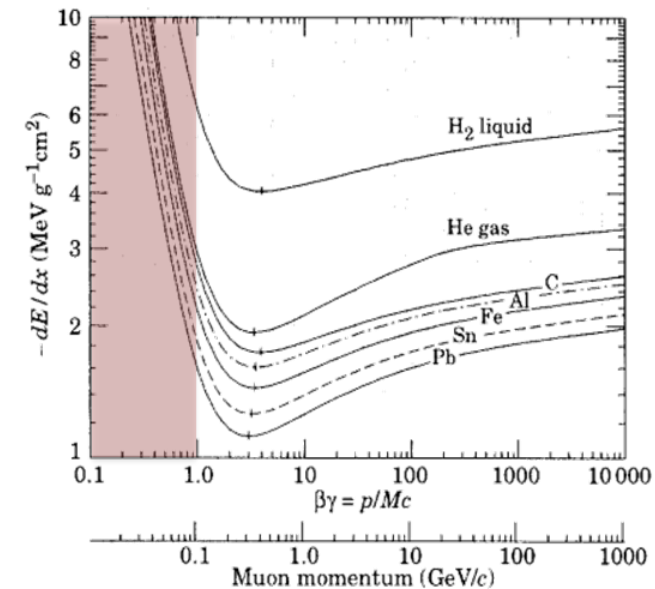
- ❑ At 5 MeV \rightarrow Be range < 1.5 mm [3]
- ❑ Conventional windows typical at CERN 0.254 mm $> 15\%$ muon range

Thin windows

- Possible materials:
 - Be, Si₃N₄, C, SiC, etc.?
- To limit beam perturbation <15μm (approx. <1% of power absorbed in the window for 3keV/μm)
- Thin window → Small window → 10×σ_{RMS}

$$\left\langle -\frac{dE}{dx} \right\rangle_{\text{electronic}} = K \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 Q_{\text{max}}}{I^2} - \beta^2 - \frac{\delta}{2} + \frac{1}{8} \frac{Q_{\text{max}}^2}{(\gamma M c^2)^2} \right] + \Delta \left| \frac{dE}{dx} \right|$$

		5 MeV	20 MeV
Be	Stopping power [MeV×cm ² /g]	11.2	4.0
	Linear stopping power [keV/μm]	2.1	0.7
C	Stopping power [MeV×cm ² /g]	12.2	4.3
	Linear stopping power [keV/μm]	2.7	1.0
Si ₃ N ₄	Stopping power [MeV×cm ² /g]	11.2	4.0
	Linear stopping power [keV/μm]	3.1	1.1
SiC	Stopping power [MeV×cm ² /g]	11.1	4.0
	Linear stopping power [keV/μm]	3.5	1.3



Thin windows: Be

- ❑ Well known material
- ❑ As thin as 8 μm in commercial x-ray windows[5]
- ❑ Aperture 7 mm
- ❑ $\Delta P > 1$ bar
- ❑ Commercial, but no many suppliers



Figure 1 Typical Assembly of Beryllium Window

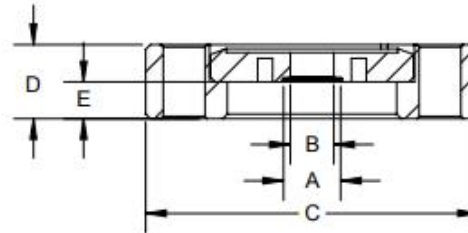


Figure 2 Conflat Flange Geometry



Table 1 Dimensions of Conflat Flange Options (Refer to Figure 2 above)								
CF	Foil Thickness (μm)	Foil Diameter (mm) - A	Through Hole Diameter (mm) - B	CF Outer Diameter (mm) - C	CF Thickness (mm) - D	Window Height (mm) - E	Coating	Part ID
1-1/3" OD	8.0	9.2	7.0	33.8	7.2	0.5	DuraCoat Plus	DBM-08-9.2-CF1.3-P
	25.0	16.0	13.0	33.8	7.2	0.5	DuraCoat	DBM-25-16.0-CF1.3
2-1/8" OD	8.0	9.2	7.0	53.6	11.9	6.5	DuraCoat Plus	DBM-08-9.2-CF2.1-P
	25.0	16.0	13.0	53.6	11.9	6.5	DuraCoat	DBM-25-16.0-CF2.1

Thin windows: C

- ❑ Thickness $< 1 \mu\text{m}$
- ❑ Different options: Graphenic carbon [6] or diamond [7]
- ❑ Research phase

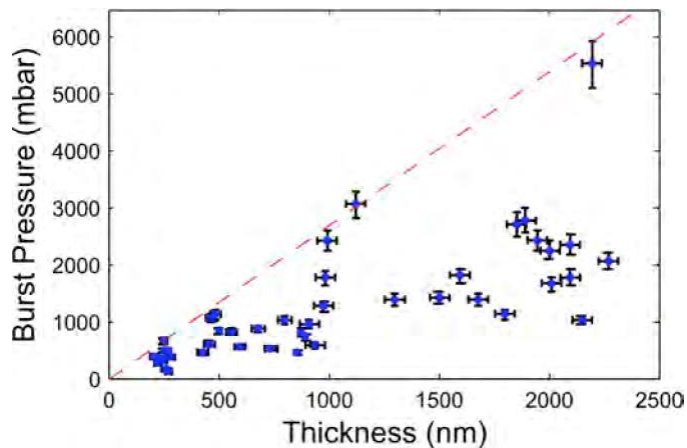


Fig. 4. Measured thickness dependent burst strength of fabricated GC transmission windows with a diameter of 7 mm.

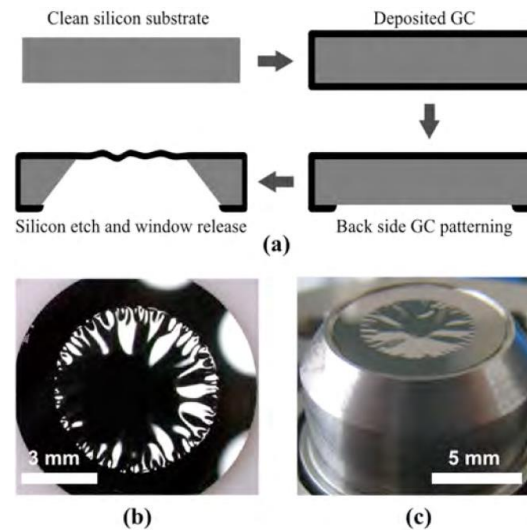


Fig. 2. (a) sketches the fabrication process of the transmission window. (b) shows a top view image of a fabricated GC window. (c) depicts a TO8 housing with a GC window glued into the top of the housing

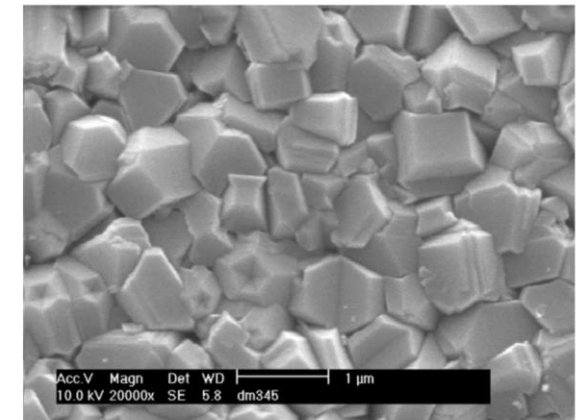
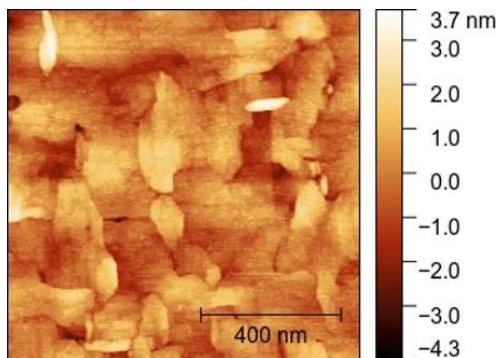


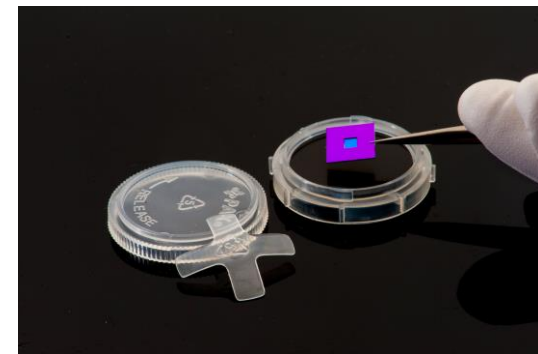
Fig. 4. SEM picture of the diamond film 345#.

Thin windows: SiC

- ❑ Thickness $< 1 \mu\text{m}$
- ❑ Bulk material has excellent mechanical properties
- ❑ No many commercial suppliers [8]

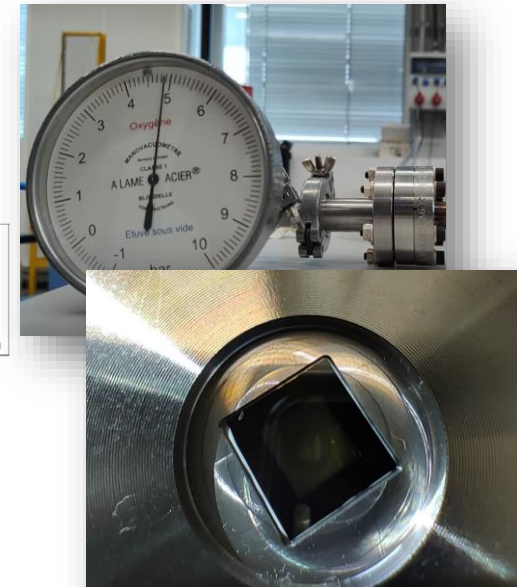
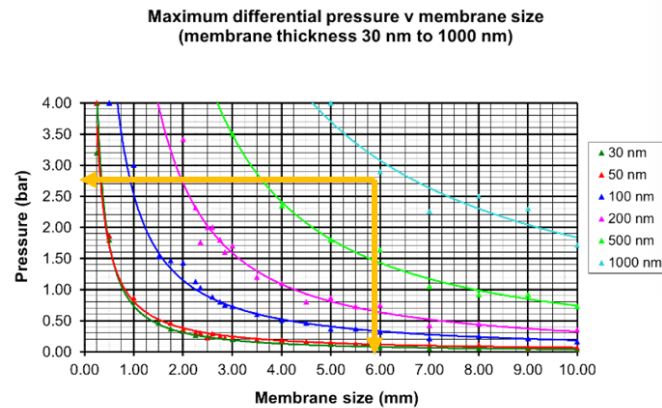
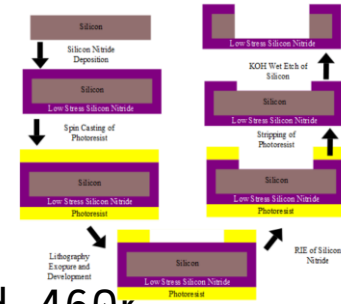


Silson



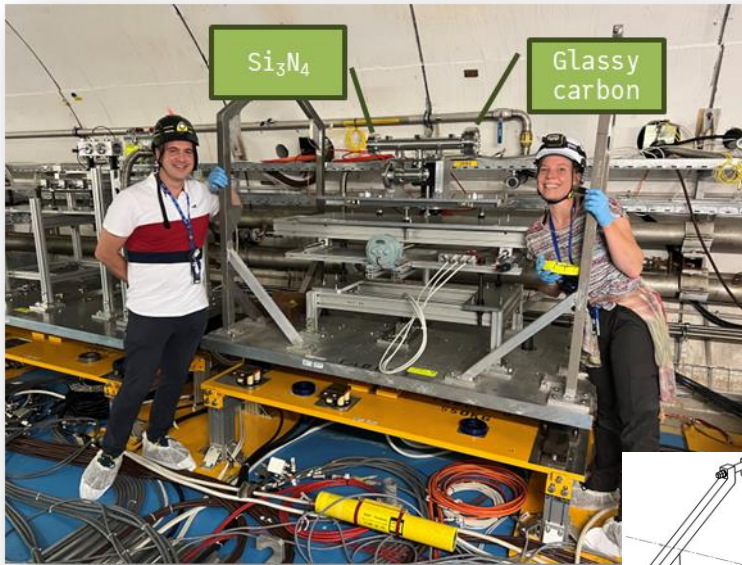
Thin windows: Si_3N_4

- ❑ Commercially available: Xray windows i.e. [9]
- ❑ Thickness <1 μm
- ❑ They can work at cryogenic temperature [10]
- ❑ Bulk material has excellent mechanical properties [11]
- ❑ Expected ΔT at the conditions described before estimated 460K
- ❑ Stress during the pulse reasonable level according to first rough estimate.
- ❑ 1 μm 6x6mm window \rightarrow >5 bar pressure (tested in lab)
- ❑ Thermal cycles at 77K

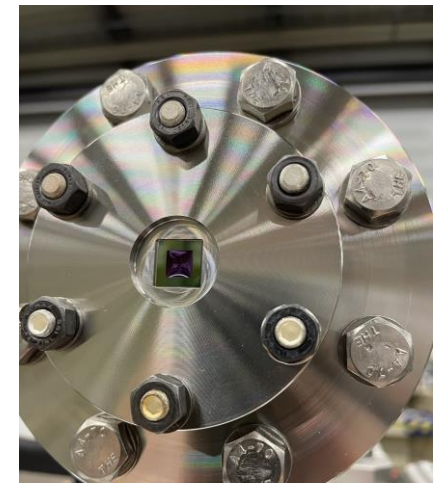
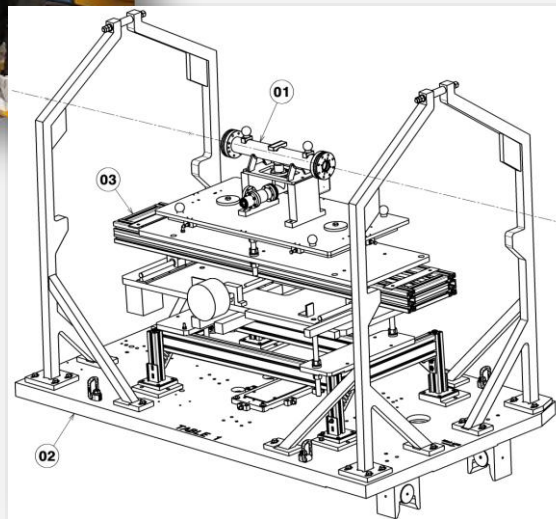


Test of 1 μ m thick Si₃N₄ window in HiRadMat (Baby-SMAUG)

$$\left\langle -\frac{dE}{dx} \right\rangle_{\text{electronic}} = K \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 Q_{\text{max}}}{I^2} - \beta^2 - \frac{\delta}{2} + \frac{1}{8} \frac{Q_{\text{max}}^2}{(\gamma M c^2)^2} \right] + \Delta \left| \frac{dE}{dx} \right| \quad \text{Brightness} \equiv \frac{N_b I_b}{\sigma_x^2 + \sigma_y^2} p^+ / \text{mm}^2 \quad [12]$$



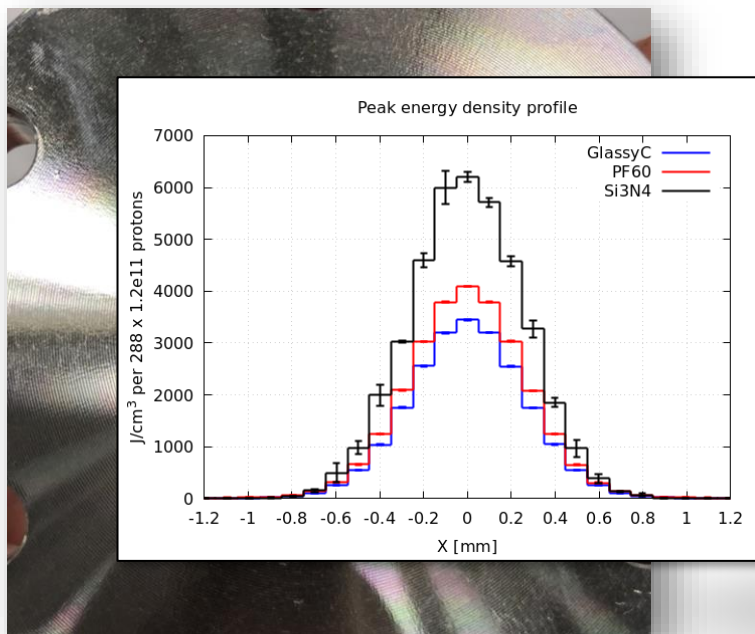
- ❑ Test one membrane irradiated under vacuum
- ❑ 4×10¹² muons/pulse at 5MeV $\sigma_{\text{RMS}}=0.6$ mm → Maximum power deposited 0.89 kJ/cm³
- ❑ p⁺ equivalent with $\sigma_{\text{RMS}}=0.25$ mm at 440 GeV → 3.2×10¹² p⁺/pulse that corresponds to 2.6×10¹³ p⁺/mm²
- Objective: Few shots increasing intensity up to failure. Optics Fp2 0.25 mm



1 μ m 6×6mm window

Results

- Leak rate $< 5 \times 10^{-10}$ mbar \times l/s (both glassy carbon and Si₃N₄ leak tight)
- Not visible damage while under vacuum
- Indentation visible after venting Si₃N₄.



6E+14 

Bethe-Bloch equation

- 15 kJ/cm³
- $\Delta T > 8000$ °C

FLUKA [12]

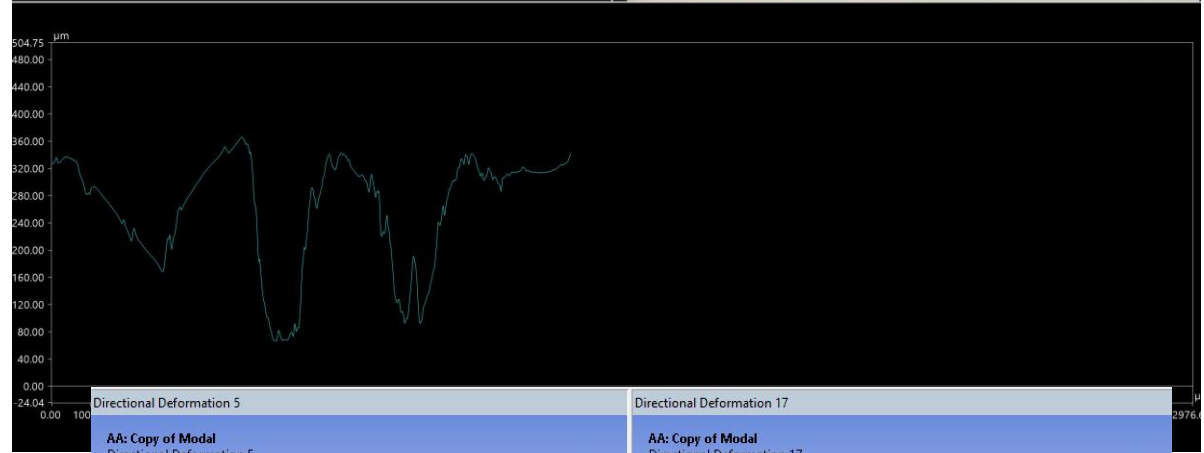
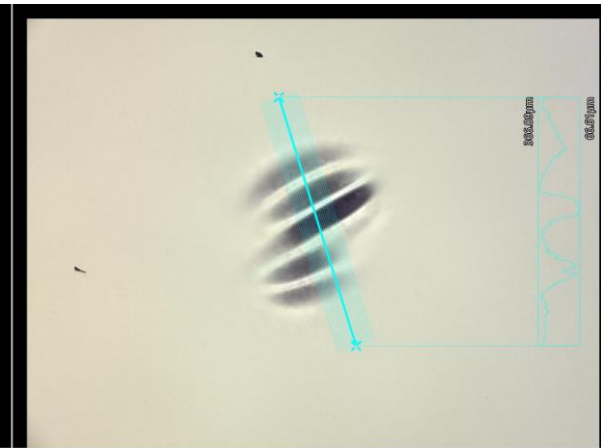
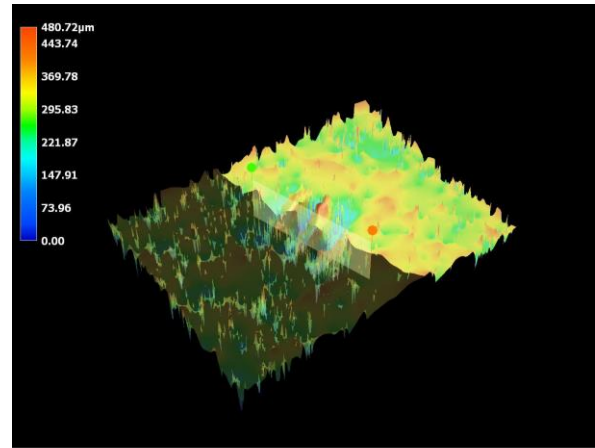
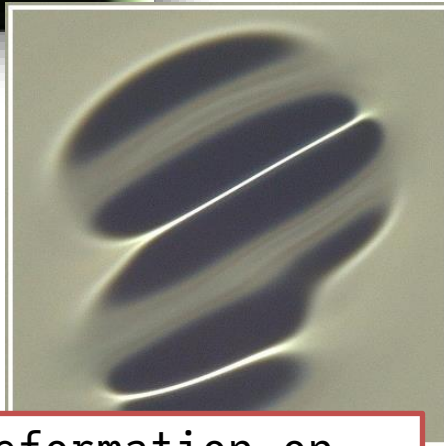
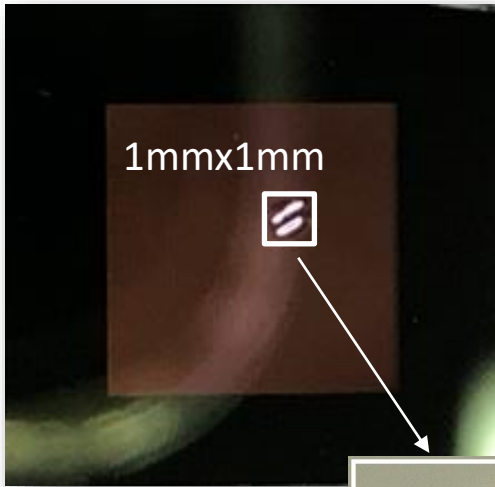
- 6 kJ/cm³
- $\Delta T > 2000$ °C

Operational temperature of bulk Si₃N₄ 1400°C (no load).

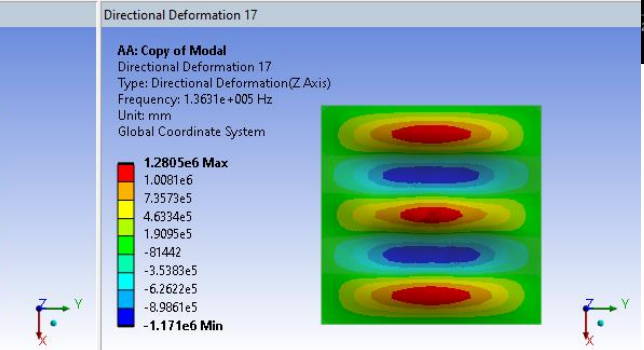
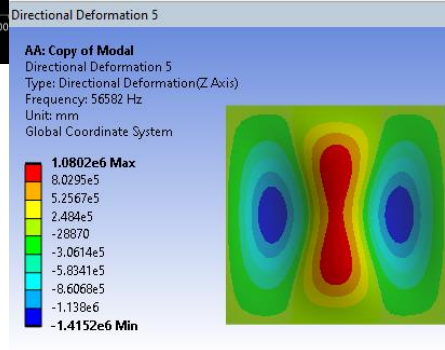
Decomposition at 1900 °C

Why?

Results

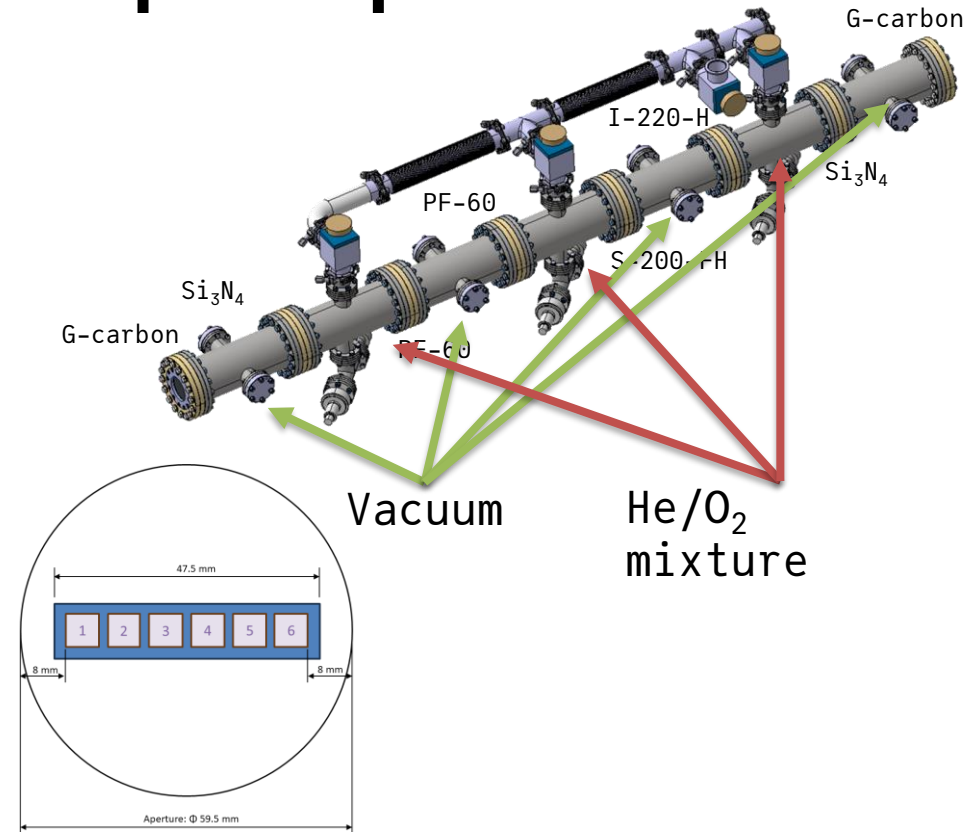


- Strong deformation on beam spot (>300 μm?)
- Buckling? Vibrations?
- SEM imaging was not possible (insulator)



Experimental proposal

- ❑ Continuation of HRMT-59 (SMAUG)
- ❑ Test Nb-Ti coated PF-60 diffusion-bonded windows and Si_3N_4
- ❑ Brightness range between 288 bunches 1.2×10^{11} ppb $\sigma_{\text{RMS}} = 0.4$ mm (5 and 50 pulses)
- ❑ Highest possible brightness fp2 0.25 mm, 288 bunches $> 2.1 \times 10^{11}$ ppb (5 and 50 pulses)
- ❑ Test fp2 0.25 mm $> 2.1 \times 10^{11}$ ppb 72+72 bunches with separations 0.22 and 23 μs

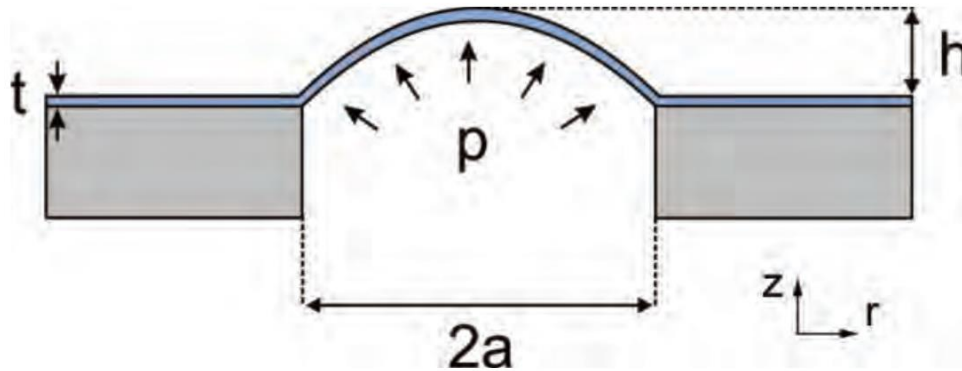


Modifications:

- DN100 → Glue 6 Si_3N_4 windows (10×10 mm frame)
- Low vacuum (10^{-2} mbar) → Pressure difference even with large leaks
- Remotely operated isolation valves
- He/O₂ (Heliox). Oxidation and high sensitivity using leak detector (20% O₂ 80% He) → Early detection of any failure
- Pirani gauges → Leak rate by accumulation
- Remote control: Leak detector, valves and gauges

Mechanical tests

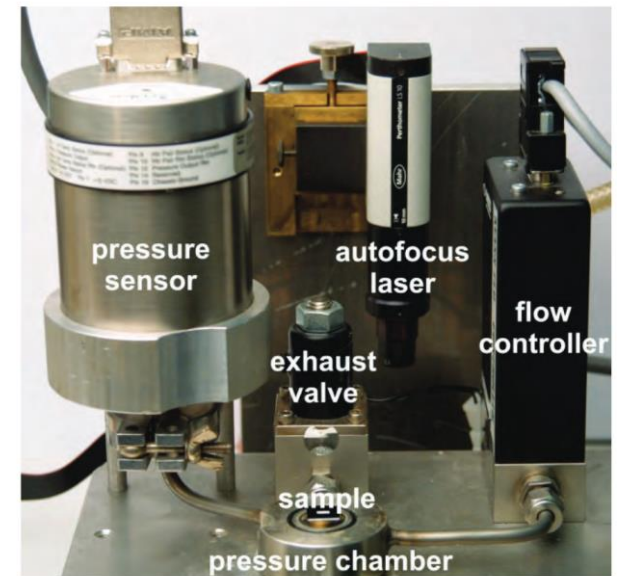
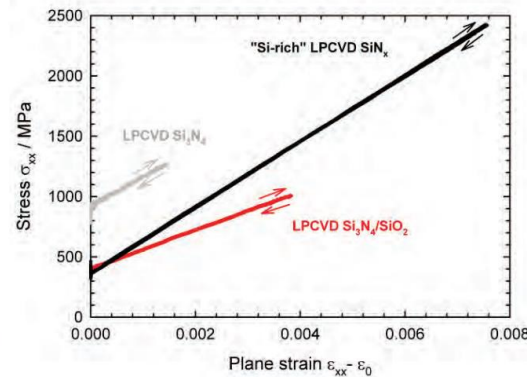
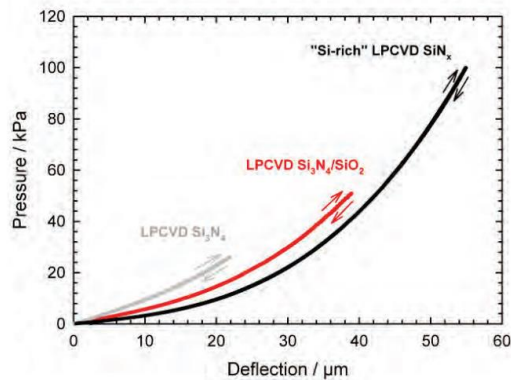
- Mechanical characterization of Si_3N_4 membranes at different temperatures (from cryogenic to high temperature) → Use inputs to better validate thermomechanical models
- For thin membranes Bulge testing is the easiest setup. Measurements of Si_3N_4 membranes at room temperature in [13]



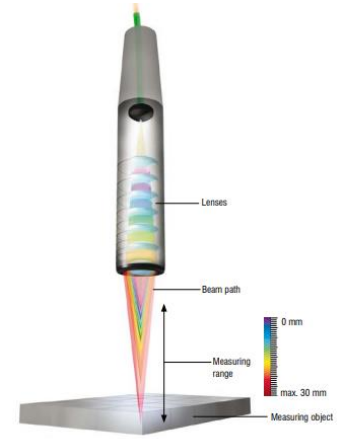
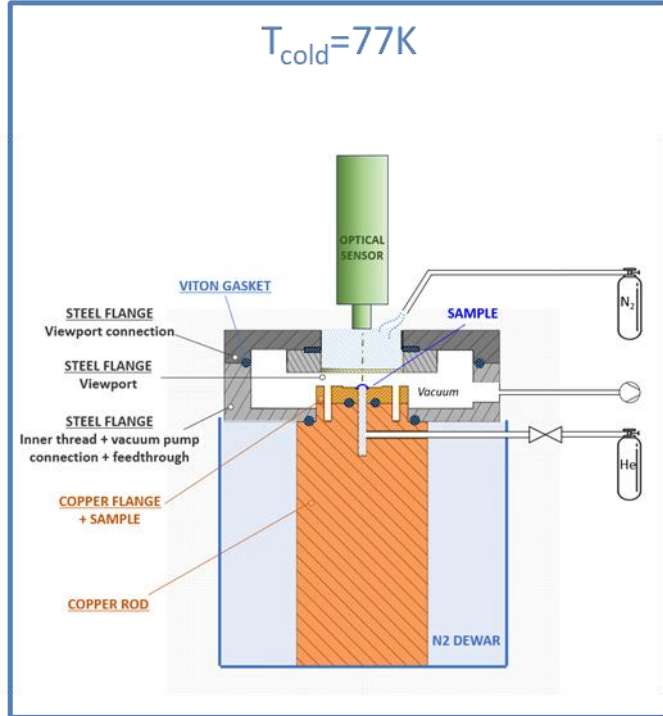
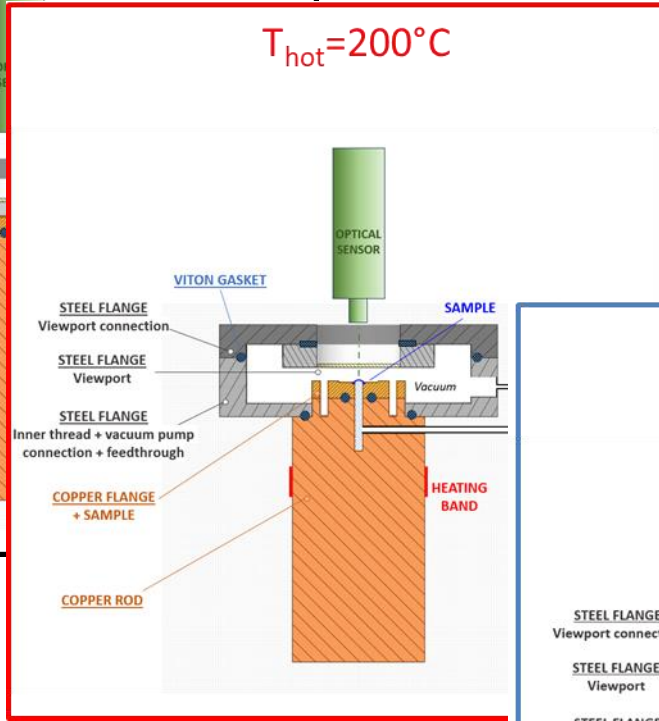
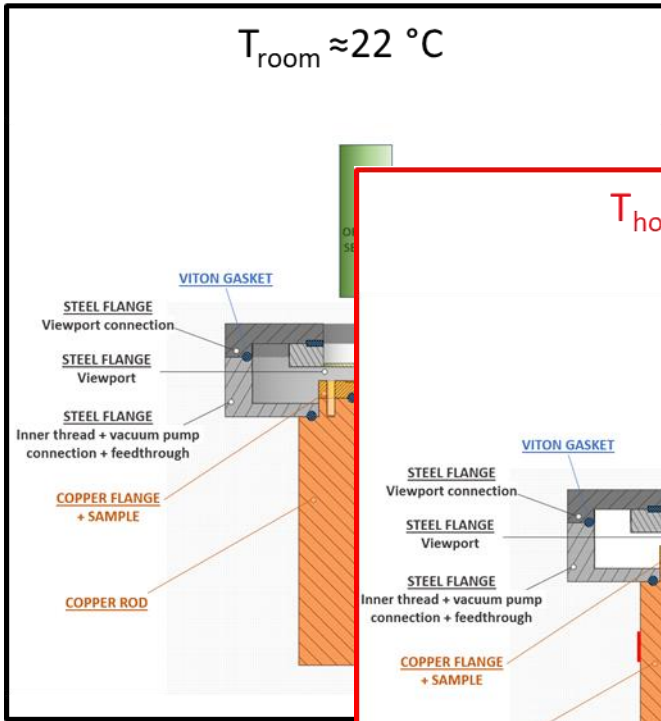
$$p = 4\sigma_0 t \frac{h}{a^2} + \frac{8}{3} \frac{E}{1-\nu} t \frac{h^3}{a^4}$$

$$\sigma_r = \frac{pa^2}{4ht}$$

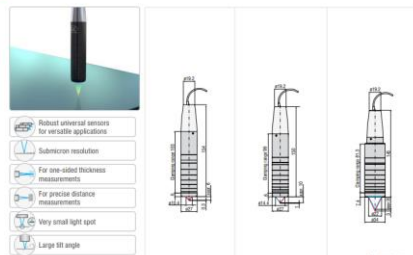
$$\epsilon_r = \frac{2h^2}{3a^2} + \epsilon_0$$



Mechanical tests



Confocal sensors with high precision
confocalDT IFS2405

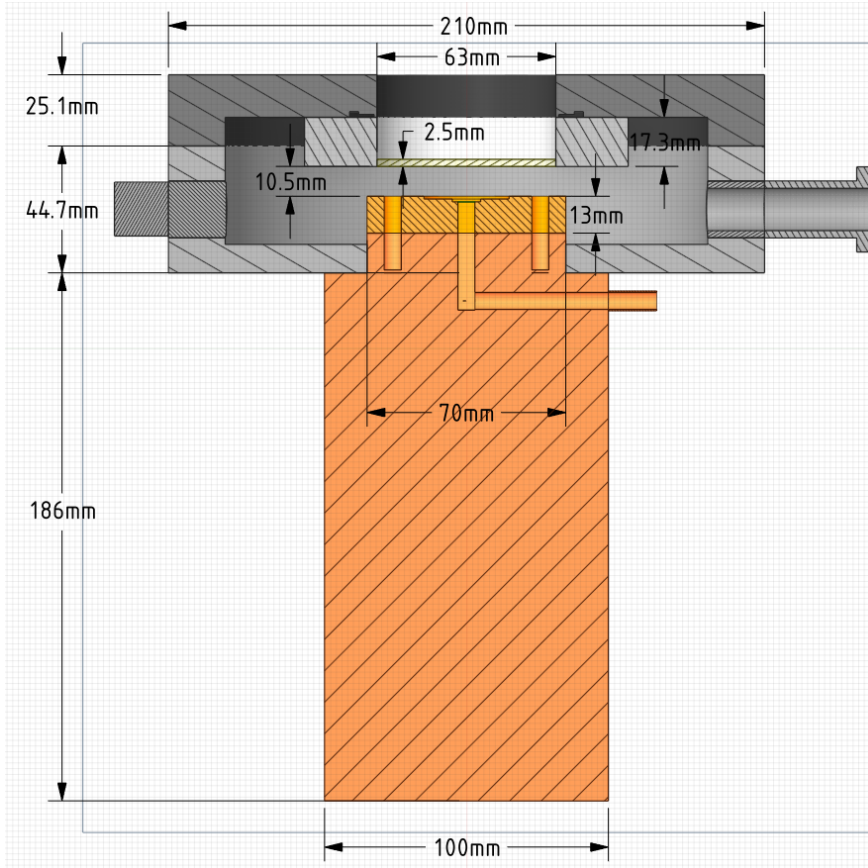


- Robust universal sensors for versatile applications
- Submicron resolution
- For one-sided thickness measurements
- For precise distance measurements
- Very small light spot
- Large tilt angle

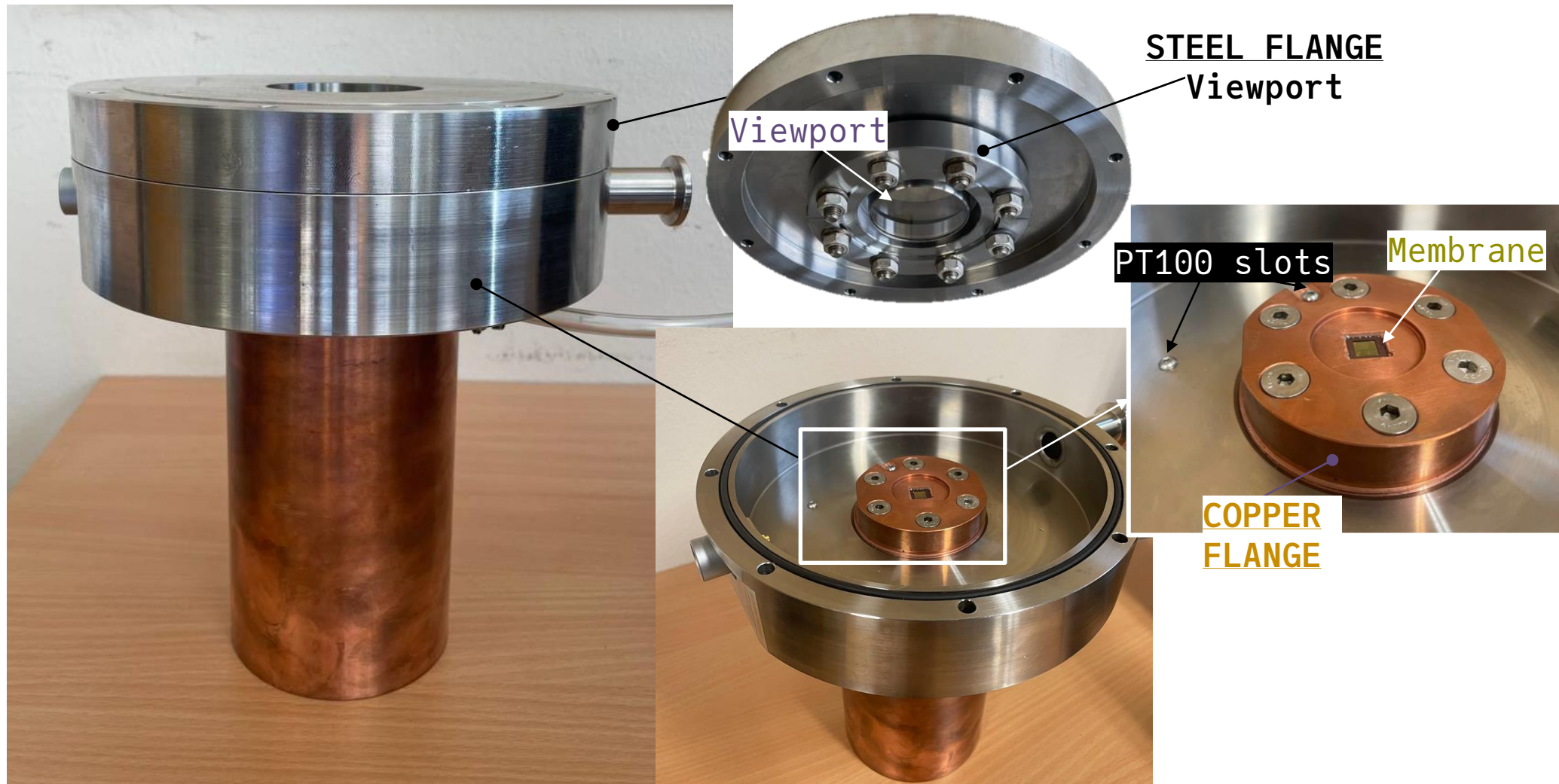
Model	IFS2405-S	IFS2405-T	IFS2405-B
Measuring range	0.2 mm	1 mm	3 mm
Start of measuring range	approx.	8 mm	10 mm
Resolution	static: 1 μm	8 mm	10 mm
Resolution	dynamic: 1 μm	38 mm	80 mm
Linearity*	Displacement and distance: ±0.3 μm	±0.20 μm	±0.70 μm
Technical features (TV)	±0.2 μm	±0.20 μm	±0.5 μm
Light spot diameter	6 μm	6 μm	6 μm
Max. measuring angle**	±34°	±30°	±24°
Technical features (TV)	0.80	0.80	0.80
Min. target thickness*	0.015 mm	0.05 mm	0.10 mm
Connector	plugable optical fiber via FC socket, standard length 3 m, extension up to 60 m		
Mounting	Clamping, mounting adapter (see accessories)		
Temperature range	Storage	-20 ... +70 °C	
Shock (DIN EN 60068-2-21)	Operation	10 g / 10 ms to 57 ms, 1000 shocks each	
Vibration (DIN EN 60068-2-4)		2 g / 20 ... 500 Hz to 97 ms, 10 cycles each	
Production case (DIN EN 60528)	IP64 (steel)		
Material	Aluminum housing, glass lenses		
Weight*	approx. 140 g		approx. 220 g

* Weight from 0.01 mm scale at 100% scale in the middle of the measuring range and 0% deflection.
** Max. value when in the middle of measuring range (1 mm).
*** All data at ambient temperature (20 ± 2 °C) unless stated. For specifications, see change when measuring physical states.
**** Maximum measuring angle of the sensor that produces a stable signal on reflecting surfaces. The tolerance depends on the reflecting surface.
***** Max. target thickness: max. ± 1.5 throughout the entire measuring range. In the end of the measuring range, max. target thickness is 0.5 mm.
***** Max. target thickness: max. ± 1.5 throughout the entire measuring range. In the end of the measuring range, max. target thickness is 0.5 mm.

Mechanical tests

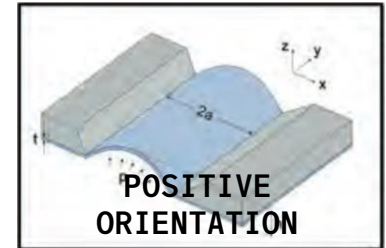


Mechanical tests



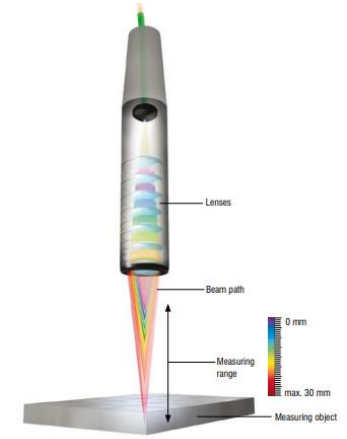
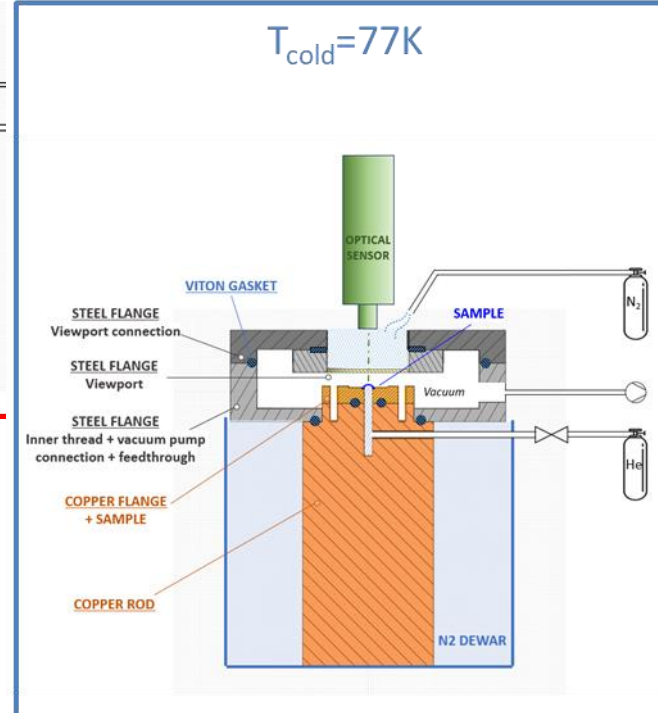
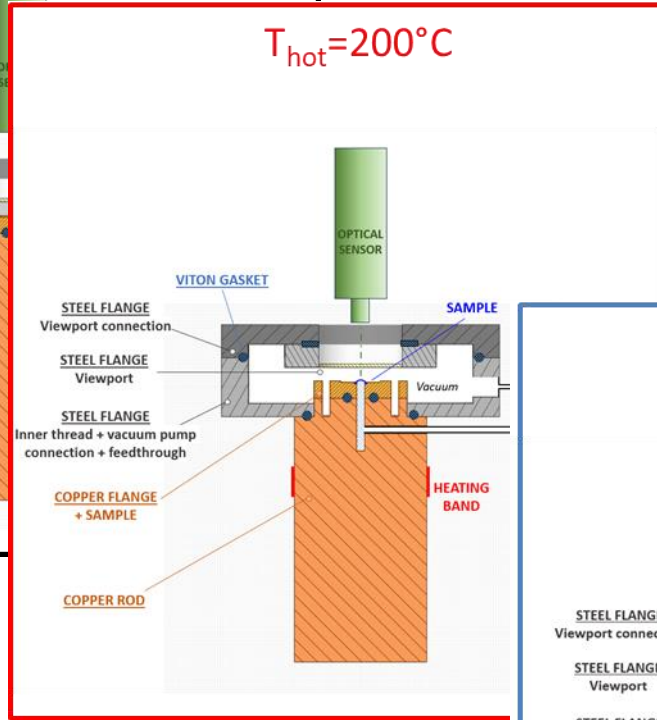
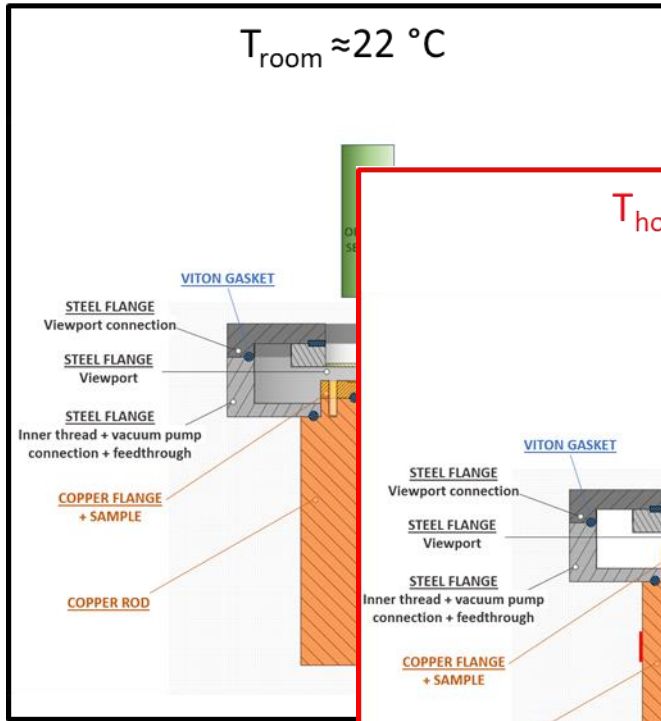
Mechanical tests

- ❑ Pressure tests were performed on square membranes with the following geometry:
 - ❑ Si frame: 10 mm x 10 mm, thickness=200 μm ,
 - ❑ Si_3N_4 membrane: 6mm x 6mm, thickness=1000nm.
- ❑ Leak-tight tests of the bulge test setup were successfully performed.
- ❑ Different glues were used to bond the sample to the copper flange. This considerably affects the mechanical response of the membrane against the maximum pressure it can withstand.
- ❑ Two different ways to mount the membrane (positive and negative orientation in the figure) were investigated.
- ❑ Results from pressure tests are shown in the table:

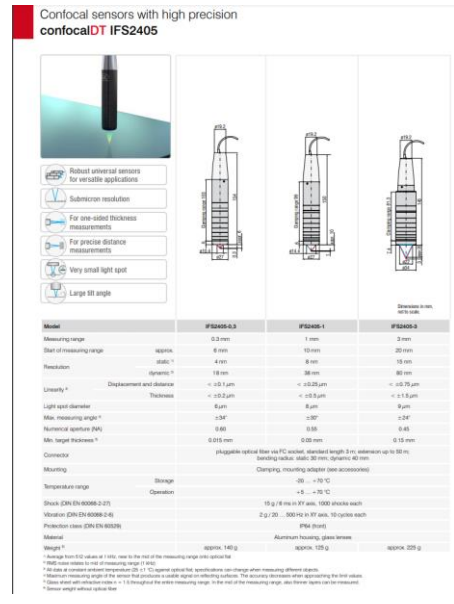


Sample #	Membrane orientation	Glue	Temperature	Max pressure before failure
1	NEGATIVE	Superglue (instantaneous)	295 K	< 1 bar
2	POSITIVE	Superglue (instantaneous)	295 K	2 bar
3	POSITIVE	Araldite bi-component (curing time: 2 h)	295 K	6 bar
4	POSITIVE	Araldite bi-component (curing time: 2 h)	77 K	2 bar

Mechanical tests



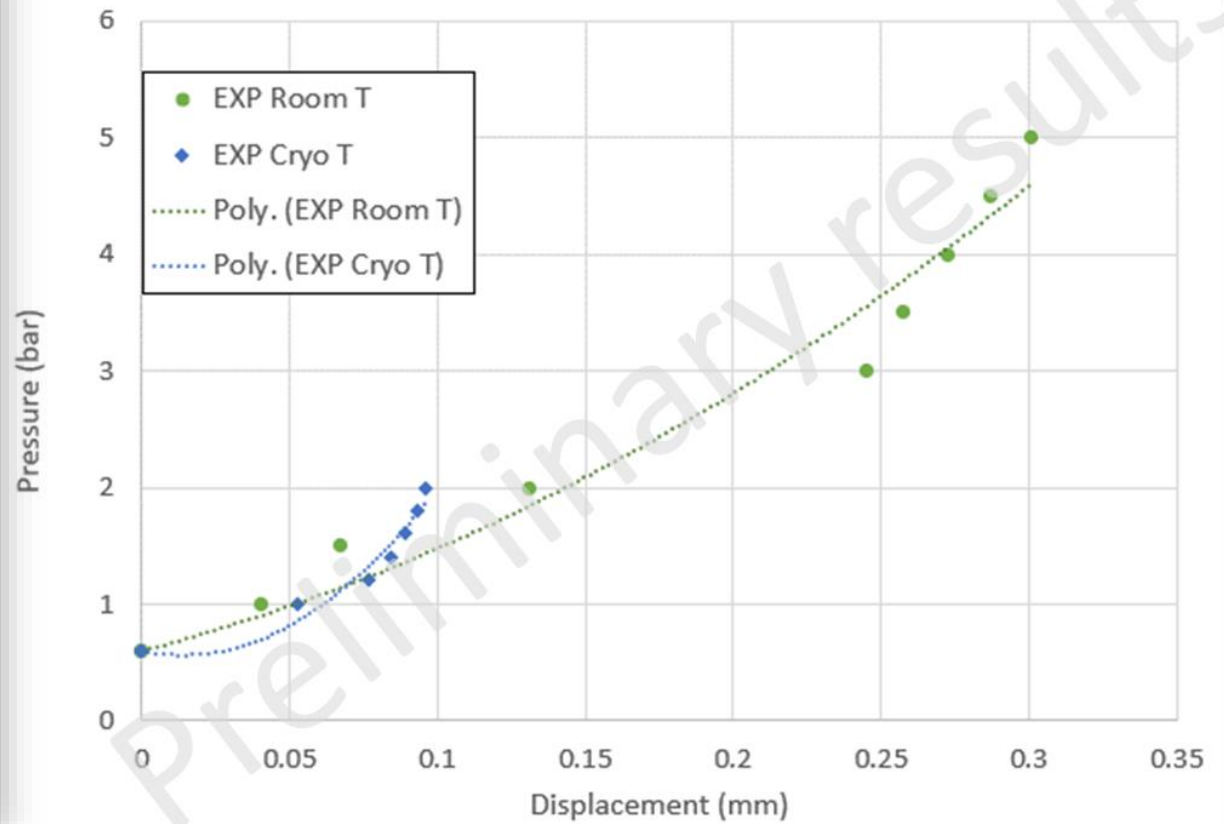
Confocal sensors with high precision
confocalDT IFS2405



Model	IFS2405-S	IFS2405-T	IFS2405-B
Measuring range	0.2 mm	1 mm	3 mm
Start of measuring range	approx.	8 mm	10 mm
End of measuring range	4 mm	8 mm	10 mm
Resolution	18 nm	38 nm	80 nm
Linearity*	Displacement and distance: $\pm 0.3 \mu\text{m}$ Thickness: $\pm 0.2 \mu\text{m}$	$\pm 0.25 \mu\text{m}$	$\pm 0.75 \mu\text{m}$
Light spot diameter	6 μm	8 μm	8 μm
Max. measuring angle**	$\pm 34^\circ$	$\pm 37^\circ$	$\pm 24^\circ$
Horizontal resolution (FWHM)	0.85	0.85	0.85
Min. target thickness*	0.015 mm	0.05 mm	0.15 mm
Connectivity	plugable optical fiber via FC socket, standard length 3 m, extension up to 80 m		
Mounting	Clamping, mounting adapter (see accessories)		
Temperature range	Storage: $-20 \dots +70^\circ\text{C}$ Operation: $-5 \dots +35^\circ\text{C}$		
Shock (DIN EN 60068-2-27)	10 g / 10 ms to 57 ms, 1000 shocks each		
Vibration (DIN EN 60068-2-4)	2 g / 20 ... 500 Hz to 97 ms, 10 cycles each		
Production case (DIN EN 60528)	IP64 (steel)		
Material	Aluminum housing, glass lenses		
Weight*	approx. 145 g		approx. 225 g

* Weight from IFS 2405 with 3 m cable, used in the field of the measuring range and operation.
** Max. value when used in the measuring range (1 mm).
*** All data at ambient temperature (20 \pm 2 $^\circ\text{C}$). Values subject to modifications, see change when measuring physical objects.
**** Maximum measuring angle of the sensor that produces a stable signal on reflecting surfaces. The tolerance depends on the reflecting surface.
***** Max. target thickness: max. ± 1 throughout the entire measuring range. In the end of the measuring range, the max. target thickness is not guaranteed.
***** Same vertical optical axis.

Mechanical tests



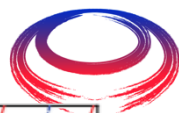
Si_3N_4 windows

- ❖ Low energy muons would require very thin windows to limit the impact of the window itself
- ❖ Si_3N_4 windows seem a good candidate:
 - ❖ Cheap and available
 - ❖ Good properties already with on the shelf products
 - ❖ Compatible with bright beams
 - ❖ Compatible at cryogenic temperature
- ❖ Thermomechanical characterization is ongoing, and more beam tests are planned
- ❖ The window should separate vacuum from the absorber, at low energy ideally hydrogen. The configuration of the absorber will define the maximum differential pressure the window should sustain

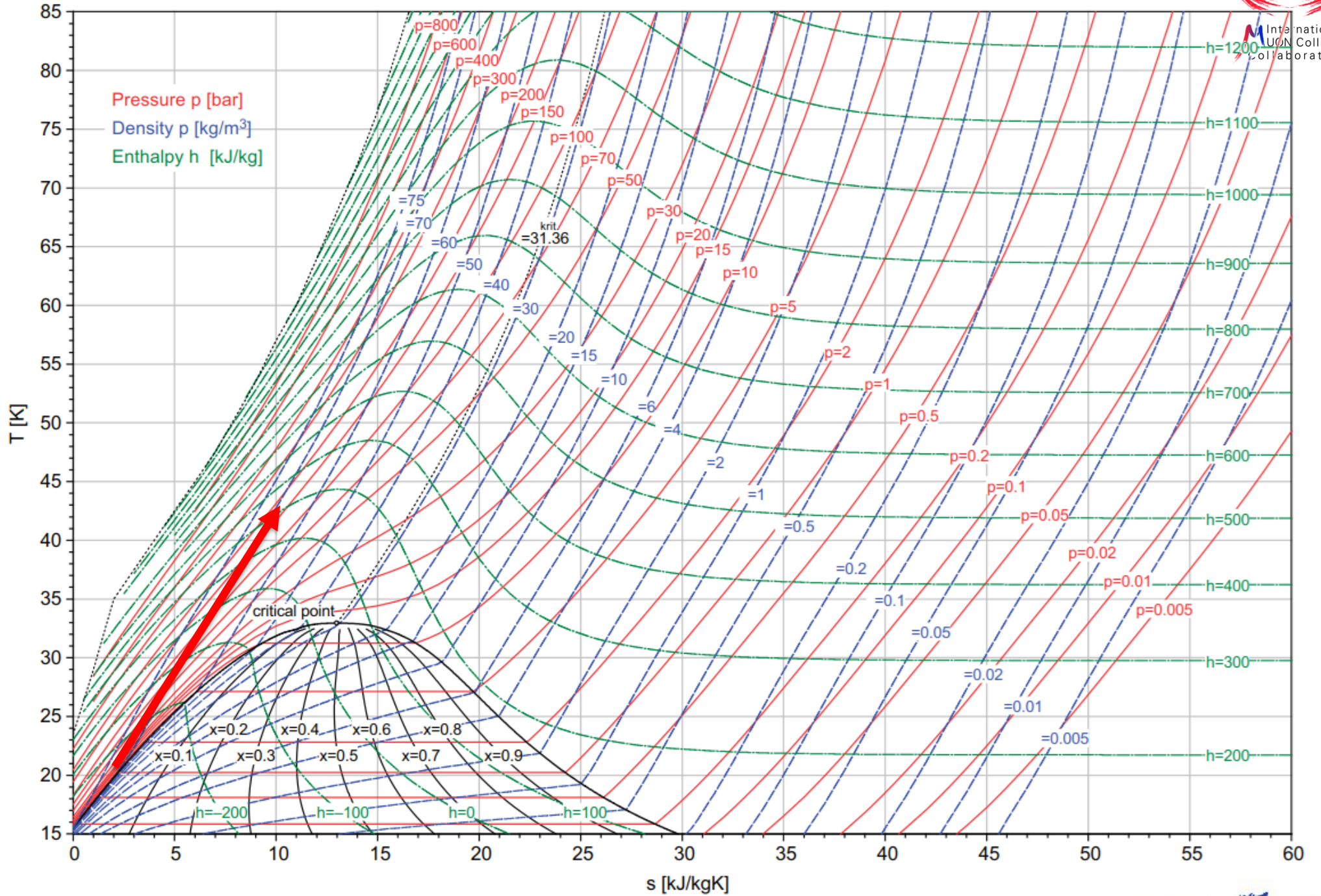
Absorber

$$\epsilon_{min,N} \propto \frac{E}{BL_R(dE/ds)} \quad [2]$$

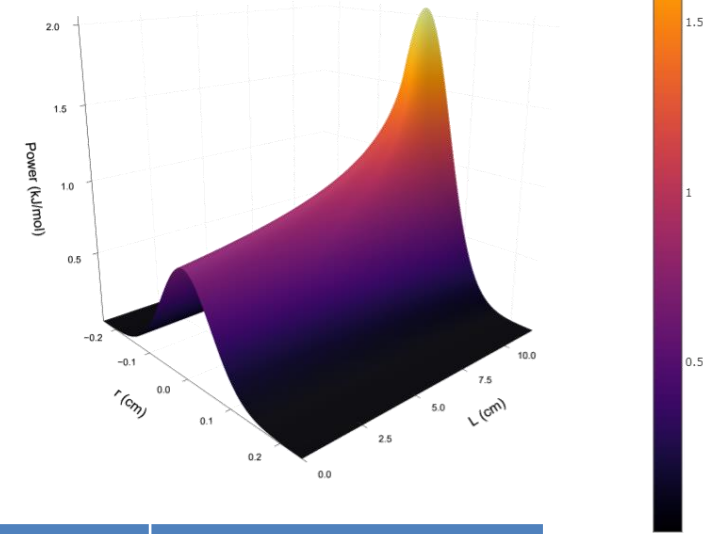
- ❑ H₂ best absorber material (out of the scope of MuCol?)
- ❑ What is the required density?
- ❑ Which length can we expect?
- ❑ What is the effect on the window?



Ts-Diagram for Hydrogen (Equilibrium H₂)



Absorber Length



20 → 5 MeV from [14][15].
 9.6 J, not including heat
 load from muon decay

H ₂ Absorber	Length	Max P (bar)	Max T (K)	P at 3×σ _{RMS} (bar) (gaussian beam shape)	T at 3×σ _{RMS} (K) (gaussian beam shape)
RT@1bar	124 m	1.3	373	1.04	303
RT@4bar	31 m	5.2	373	4.18	303
20.3K@1bar vapor	8 m	7.5	140	1.8	34
26.1K@4bar vapor	2.1 m	29.2	143	7	40
20.3K@1bar liquid	15 cm	833	128	125	35

$$\left\langle -\frac{dE}{dx} \right\rangle_{\text{electronic}} = K \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 Q_{\max}}{I^2} - \beta^2 - \frac{\delta}{2} + \frac{1}{8} \frac{Q_{\max}^2}{(\gamma M c^2)^2} \right] \quad L = \int_{E_f}^{E_s} \frac{1}{dE/ds} dE$$

Summary

- ❑ Several window candidates for final cooling. Si_3N_4 seems very promising
 - ❑ Commercially available as vacuum window for x-ray transmission
 - ❑ First irradiation tests showed excellent performance, well beyond the requirements
 - ❑ Ongoing effort to better characterise the thermomechanical properties of the membranes at different temperatures and understand its behaviour and produce better models.
 - ❑ Irradiation in proton facilities
- ❑ High density absorber required to have a short solenoid, but high power deposition → High pressure. Compatible with thin window?
- ❑ Shock wave and phase change after power deposition in liquid hydrogen → Very challenging CFD problem out of reach of commercial codes
- ❑ The design of the H_2 absorber will define the requirements and lifetime of the window, is this out of the scope of MuCol?
- ❑ Decouple window and absorber → even thinner windows
 - ❑ Pulsed high density vapor?
 - ❑ Leidenfrost effect?
 - ❑ Staging of steps with different densities (lower at the end)

*THANK YOU FOR YOUR
ATTENTION!*

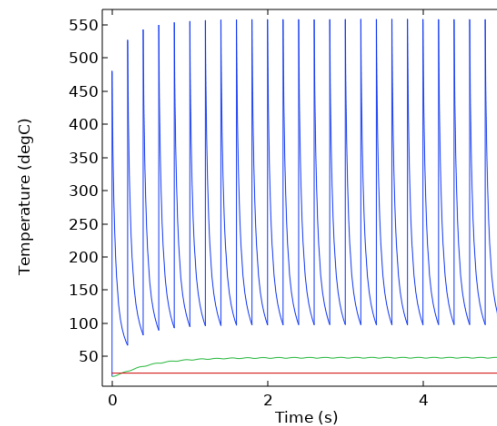
References

- [1] B.M. Stechauner, Final cooling scheme for muon colliders: a door opener for future discovery machines, TU Vienna, 2021.
- [2] H. Kamal Sayed, R.B. Palmer, and D. Neuffer, Phys. Rev. ST Accel. Beams **18**, 091001 (2015).
- [3] [AtomicNuclear Properties \(lbl.gov\)](#)
- [4] D.E. Groom and S.R. Klein, Eur. Phys. J. C **15**, 163 (2000).
- [5] [DuraBeryllium® Windows in Conflat Flanges](#)
- [6] S. Huebner, N. Miyakawa, S. Kapser, A. Pahlke, and F. Kreupl, IEEE Transactions on Nuclear Science **62**, 588 (2015).
- [7] X. Ying, J. Luo, P. Wang, M. Cui, Y. Zhao, G. Li, and P. Zhu, Diamond and Related Materials **12**, 719 (2003).
- [8] [Silson - Silicon Carbide](#)
- [9] [Silson - Differential Pressure Windows](#)
- [10] P.T. Törmä, J. Kostamo, H. Sipilä, M. Mattila, P. Kostamo, E. Kostamo, H. Lipsanen, C. Laubis, F. Scholze, N. Nelms, B. Shortt, and M. Bavdaz, IEEE Transactions on Nuclear Science **61**, 695 (2014).
- [11] R.L. Edwards, G. Coles, and W.N. Sharpe, Experimental Mechanics **44**, 49 (2004).
- [12] N. Solieri et al, TF3: Beam-Intercepting Devices final report, [EDMS 2754370](#)
- [13] B. Merle, *Mechanical Properties of Thin Films Studied by Bulge Testing* (FAU University Press, Erlangen, 2013)
- [14] [Isochoric Properties for Hydrogen \(nist.gov\)](#)
- [15] J.W. Leachman, R.T. Jacobsen, S.G. Penoncello, and E.W. Lemmon, Journal of Physical and Chemical Reference Data **38**, 721 (2009).

Thin windows

- Approx 1 mm stops the beam completely at 5MeV (1.3 mm for Be)
- Several candidates for thin windows
- Better characterization and evaluation required but first numbers look promising
- Measure mechanical properties (cryogenic to high temperature) for precise thermomechanical simulations. Bulge test [14] with interferometry?
- Pressure in the absorber is critical for the window definition

		5 MeV	20 MeV
Be	ΔT_{inst} [K]	174	61
	Cyclic Thermal Stress (MPa)	485	171
Si_3N_4	ΔT_{inst} [K]	470	169
	Cyclic Thermal Stress (MPa)	228	82
C	ΔT_{inst} [K]	507	180
	Cyclic Thermal Stress (MPa)	1013	360
SiC	ΔT_{inst} [K]	467	168
	Cyclic Thermal Stress (MPa)	224	81



Si_3N_4 \varnothing 7 mm $1\mu m$ at 5 MeV - 0.6 mm gaussian beam
Only room temperature ambient radiation

$$\sigma_{cyc} \approx \frac{1}{2} \alpha E \Delta T \quad \Delta T_{inst} = \left(\frac{dE}{dx} \right) \frac{N}{2\pi\sigma^2\rho c}$$