

Neutrino masses and mixing

Michele Maltoni

Instituto de Física Teórica UAM/CSIC

35th Rencontres de Blois on “Particle Physics and Cosmology”

Château de Blois, France – October 24th, 2024



Project PID2022-142545NB-C21
funded by MCIN/AEI/10.13039/
/501100011033/ FEDER, UE

SM with ν masses: general three-neutrino framework

- Equation of motion: **6 parameters** (including **Dirac** and neglecting **Majorana** phases):

$$i \frac{d\vec{\nu}}{dt} = H \vec{\nu}; \quad H = U_{\text{vac}} \cdot D_{\text{vac}} \cdot U_{\text{vac}}^\dagger \pm V_{\text{mat}};$$

$$U_{\text{vac}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \vec{\nu} = \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix};$$

$$D_{\text{vac}} = \frac{1}{2E_\nu} \left[\text{diag} (0, \Delta m_{21}^2, \Delta m_{31}^2) + \cancel{m_1^2} \mathbf{I} \right]; \quad V_{\text{mat}} = \sqrt{2} G_F N_e \text{diag} (1, 0, 0).$$

6 parameters \iff 6 types of experiments

- MeV** sources:

– solar experiments (mainly SNO)	→ θ_{12}
– reactor LBL (KamLAND)	→ Δm_{21}^2
– reactor MBL (Double-Chooz, Daya-Bay, Reno)	→ θ_{13} [Δm_{31}^2]
- GeV** sources:

– atmospheric experiments (SK, DC)	→ θ_{23}
– accelerator LBL-DIS $\nu_\mu \rightarrow \nu_\mu$ (T2K, NOvA)	→ Δm_{31}^2 [θ_{23}]
– accelerator LBL-APP $\nu_\mu \rightarrow \nu_e$ (T2K, NOvA)	→ δ_{CP}

Solar and reactor neutrinos

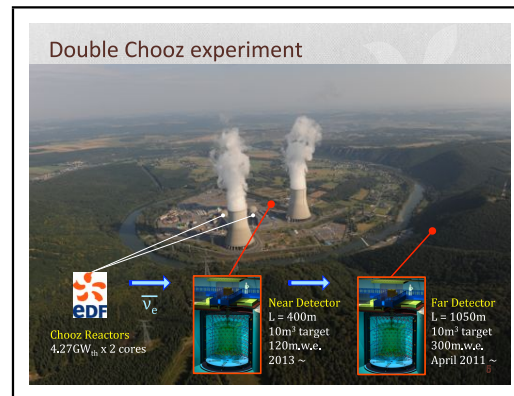
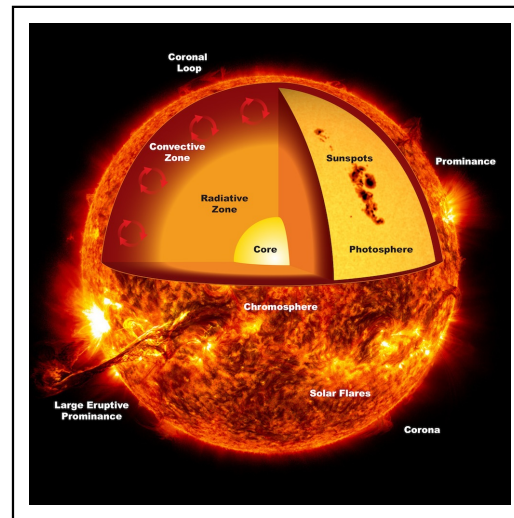
- ν_e from **nuclear** reactions \Rightarrow energy in the MeV range;
- ν_μ and ν_τ indistinguishable \Rightarrow no sensitivity to θ_{23} or δ_{CP} .

Reactor neutrinos

- $\bar{\nu}_e$ produced by nuclear **fission** in reactor's core;
- detection: inverse beta decay ($\bar{\nu}_e + p \rightarrow e^+ + n$), both e^+ and n observed in coincidence;
- negligible matter effects \Rightarrow mostly vacuum params.

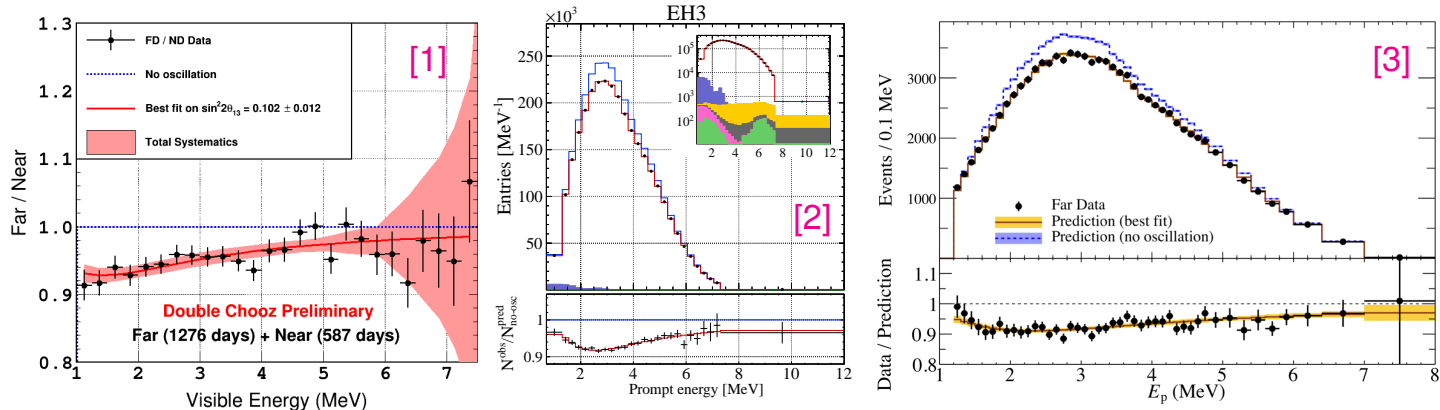
Solar neutrinos

- ν_e produced by nuclear **fusion** in the core of the Sun;
- two different mechanisms at work: **p-p chain** and **CNO cycle**. Both give $4p \rightarrow {}^4\text{He} + 2e^+ + 2\nu_e + \gamma \Rightarrow$ solar light and **neutrinos** in well-defined mutual proportions;
- detection: various processes (**CC- ν_e** , **NC**, **ES**);
- matter effects very important (MSW effect).



Medium-baseline reactor neutrino disappearance and θ_{13}

- Positive $\bar{\nu}_e$ disappearance (≈ 1 km) in DOUBLE-CHOOZ [1], DAYA-BAY [2], RENO [3];
- experimental results are mutually consistent \Rightarrow it is now a firmly established fact that $\theta_{13} \neq 0$
 \Rightarrow full 3ν oscillation phenomenology;
- all these experiments have spectral capabilities and detector units placed at different baselines
 \Rightarrow uncertainties in the reactor flux predictions do **not** affect the results.



[1] T. Bezerra [DOUBLE-CHOOZ], online talk at Neutrino 2020, Fermilab, USA, June 22–July 2, 2020.

[2] F.P. An *et al.* [DAYA BAY], Phys. Rev. Lett. **130** (2023) 161802 [arXiv:2211.14988].

[3] J. Yoo [RENO], online talk presented at Neutrino 2020, Fermilab, USA, June 22–July 2, 2020.

Troubles with reactor fluxes

Reactor antineutrino anomaly

- In [4, 5] the reactor $\bar{\nu}$ fluxes was reevaluated;
- new calculations: small increase by about **3.5%**;
- impact [6]: **no evidence** (before) \rightarrow **deficit** (now);
- origin [8, 9]: ^{239}Pu mostly OK, deficit from ^{235}U .

5 MeV excess

- RENO [7]: **excess** of events around 5 MeV;
- both in NEAR and FAR detector \rightarrow independent of L ;
- confirmed by Daya-Bay, Double-Chooz, and others;
- DB+Prospect [10]: affect **both** ^{235}U & ^{239}Pu .

[4] T.A. Mueller *et al.*, PRC **83** 054615 [arXiv:1101.2663]

[5] P. Huber, PRC **84** 024617 [arXiv:1106.0687]

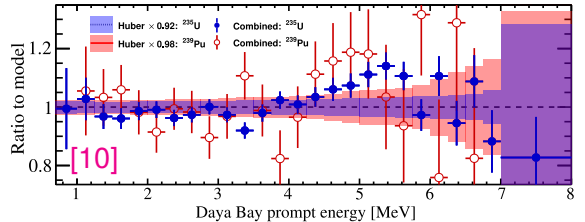
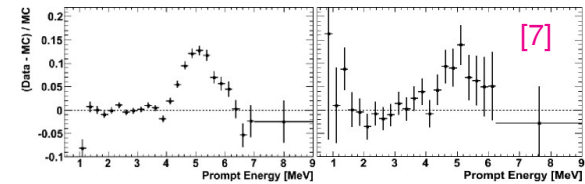
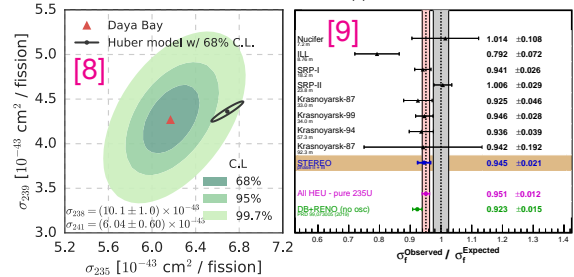
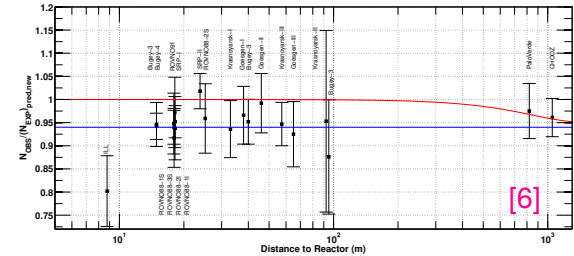
[6] G. Mention *et al.*, PRD **83** 073006 [arXiv:1101.2755]

[7] S.H Seo [RENO], talk at Neutrino 2014, USA, 2–7/06/2014

[8] [Daya-Bay], PRL **118** 251801 [arXiv:1704.01082]

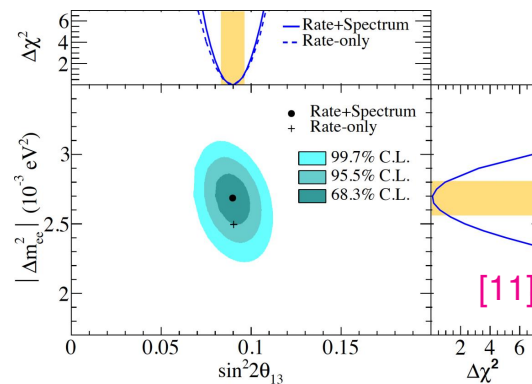
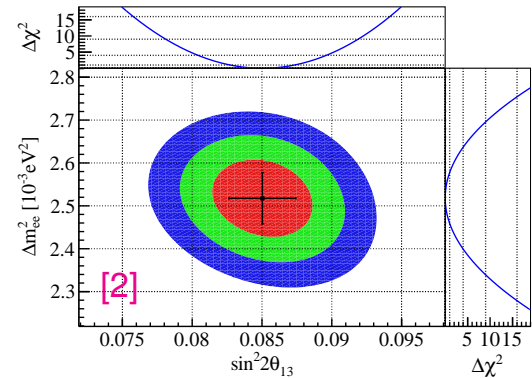
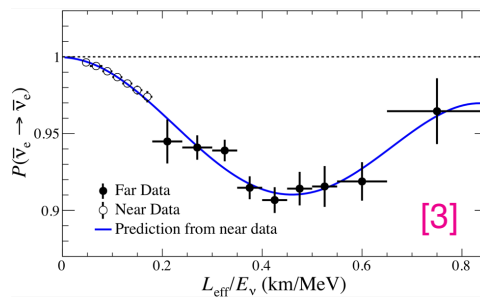
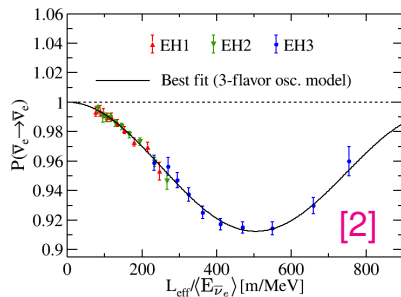
[9] [STEREO], Nature **613** 257 [arXiv:2210.07664]

[10] [DB+Prospect], PRL **128** 081801 [arXiv:2106.12251]



Measuring θ_{13} and Δm_{31}^2 from reactor data

- FAR/NEAR spectral ratio \Rightarrow flux shape irrelevant;
- spectral information from Double-Chooz, Daya-Bay and Reno \Rightarrow oscillation pattern clearly visible $\Rightarrow \theta_{13}$ and Δm_{31}^2 accurately determined by reactor data;
- accuracy from reactor $\nu_e \rightarrow \nu_e$ comparable with LBL $\nu_\mu \rightarrow \nu_\mu$, but oscillation channel is different \Rightarrow important **complementary** information available.



[2] F.P. An *et al.* [DAYA BAY], Phys. Rev. Lett. **130** (2023) 161802 [arXiv:2211.14988].

[3] J. Yoo [RENO], online talk at Neutrino 2020, Fermilab, USA, 22/06–2/07/2020.

[11] K.K. Joo [RENO], online talk at Neutrino 2022, Virtual Seoul, Korea, 30/05–4/06/2022.

Measuring θ_{12} and Δm_{21}^2 with KamLAND data

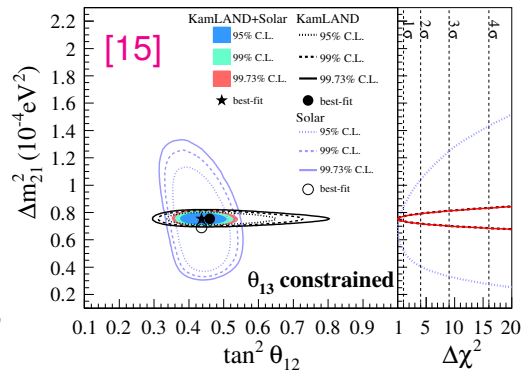
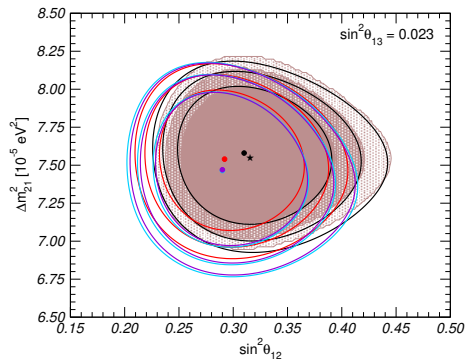
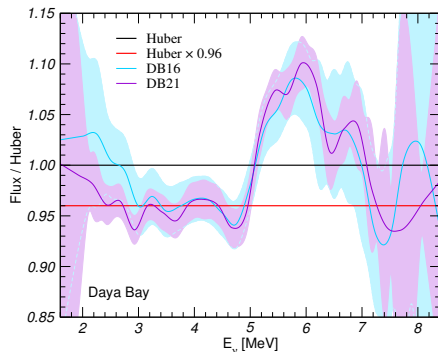
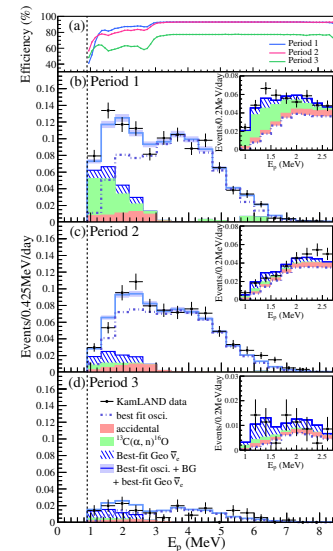
- Much longer baseline (≈ 180 km) \Rightarrow sensitive to θ_{12} and Δm_{21}^2 ;
- lack of a near detector \Rightarrow spectral distortions may be an issue;
- problem discussed in [12, 13] \Rightarrow impact on Δm_{21}^2 found to be small;
- solution: bind KamLAND spectrum to Daya-Bay measurement [14].

[12] M. Maltoni, A.Yu. Smirnov, EPJA **52** (2016) 87 [arXiv:1507.05287].

[13] F. Capozzi *et al.*, NPB **908** (2016) 218 [arXiv:1601.07777].

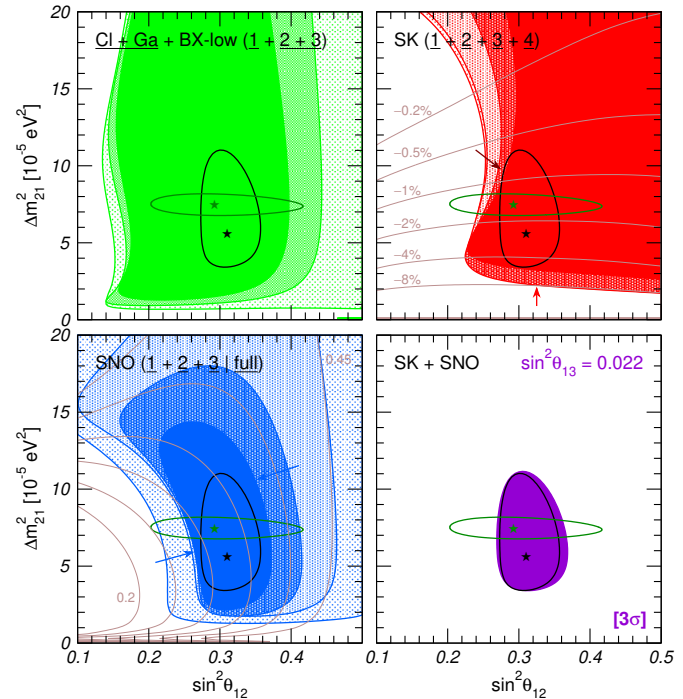
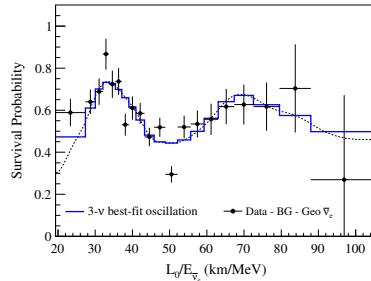
[14] F.P. An *et al.* [Daya-Bay], CPC **45** (2021) 073001 [arXiv:2102.04614].

[15] A. Gando *et al.* [KamLAND], PRD **88** (2013) 033001 [arXiv:1303.4667].



Determination of θ_{12} and Δm_{21}^2 from solar neutrino data

- $P_{ee} = c_{13}^4 P_{\text{eff}} + s_{13}^4$, $i \frac{d\vec{v}}{dt} = \left[\frac{\Delta m_{21}^2}{4E_\nu} \begin{pmatrix} -\cos 2\theta_{12} & \sin 2\theta_{12} \\ \sin 2\theta_{12} & \cos 2\theta_{12} \end{pmatrix} \pm \sqrt{2} G_F N_e \begin{pmatrix} c_{13}^2 & 0 \\ 0 & 0 \end{pmatrix} \right] \vec{v}$, $\vec{v} = \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$;
 - $\nu_\mu \equiv \nu_\tau \Rightarrow$ no sensitivity to θ_{23} and δ_{CP} ;
 - $\Delta m_{31}^2 \approx \infty \Rightarrow$ specific Δm_{31}^2 value irrelevant;
- \Rightarrow data only depend on Δm_{21}^2 , θ_{12} and θ_{13} ;
- param's: $\begin{cases} \theta_{12} \text{ dominated by SNO;} \\ \Delta m_{21}^2 \text{ dominated by KamLAND;} \end{cases}$
 - solar region determined by high-E data, low-E contribution marginal;
 - SNO-NC measurement confirms SSM;
 - KamLAND precisely determines the oscillation pattern.

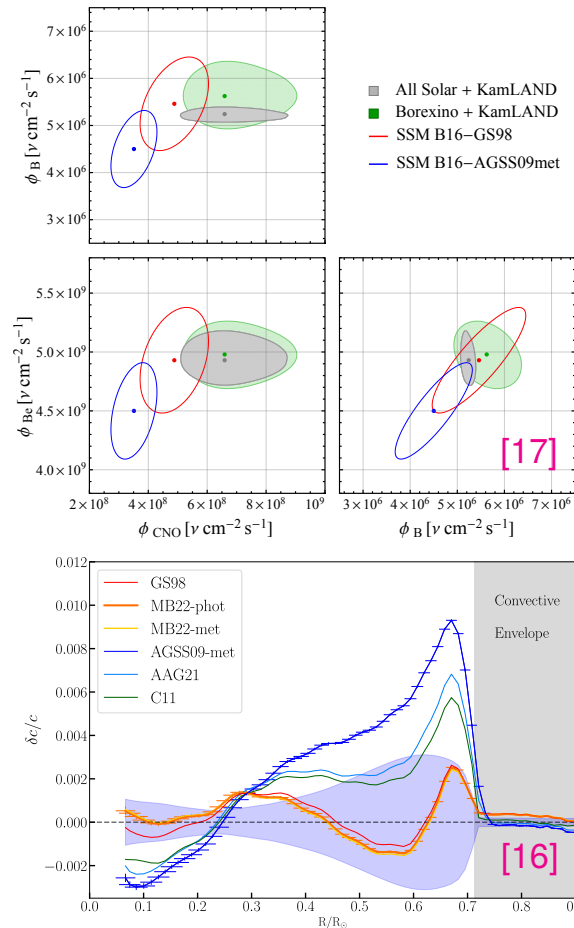


Uncertainties in the solar fluxes

- Long-standing tension between **surface** and **internal** composition of the Sun. Two types of models:
 - **high-metallicity** (GS98 → MB22): good agreement with *helioseismology*, but historically poor description of the *Sun's atmosphere*;
 - **low-metallicity** (AGSS09 → AAG21): solve issues with *surface* modelling, but fails to properly reproduce *helioseismic* results;
- recent CNO measurement by Borexino [17] ⇒ experimental determination of *all* solar fluxes ⇒ data indicate preference for **high-metallicity** models;
- new MB22 model [16] reconciles *surface* data with the high metallicity required by *helioseismology*.

[16] E. Magg *et al.*, A&A **661** A140 [arXiv:2203.02255].

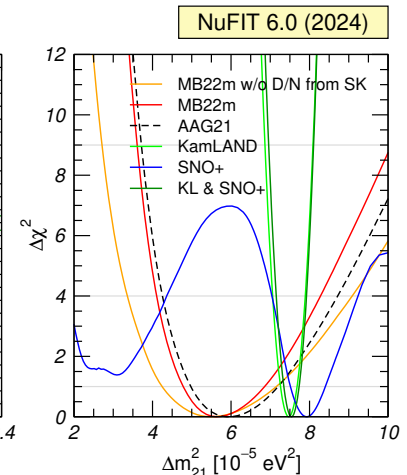
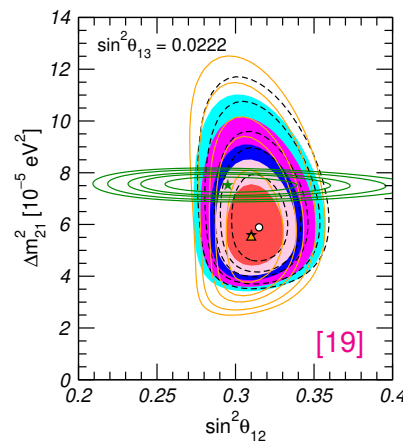
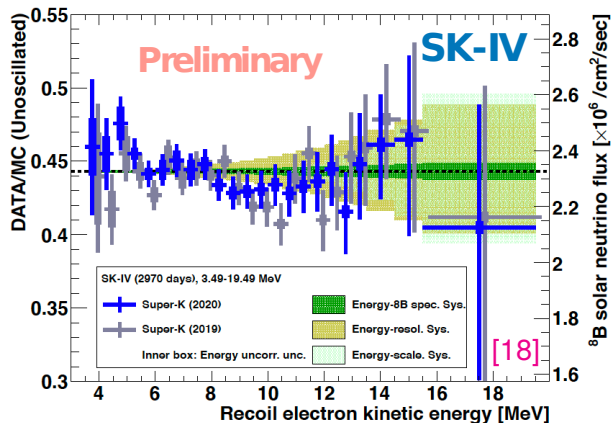
[17] S. Appel *et al.* [BOREXINO], PRL [arXiv:2205.15975].



Comparison between solar and KamLAND measurements

- Long-standing weak tension on preferred Δm_{21}^2 from solar and KamLAND data;
- choice of the assumed solar model (GS, AGSS, MB22, ...) has little impact on the issue;
- cause:
 - too much D/N asymmetry in SK
 - no indication of low-E turn-up
- new data [18]:
 - D/N: 3.6% \rightarrow 2.1%,
 - “hints” of turn-up.

\Rightarrow tension considerably reduced after Neutrino 2020 conference.



[18] Y. Nakajima [SK], online talk at Neutrino 2020, Fermilab, USA, June 22–July 2, 2020.

[19] I. Esteban *et al.*, arXiv:2410.05380 & NuFIT 6.0 [<http://www.nu-fit.org>].

Atmospheric and accelerator neutrinos

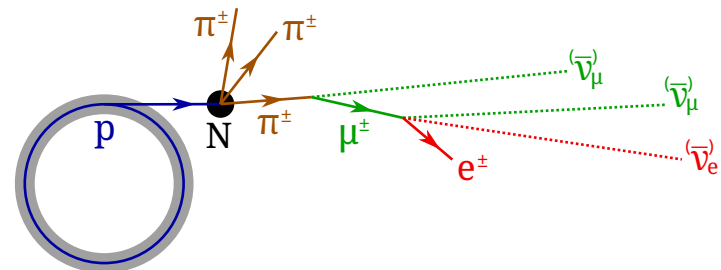
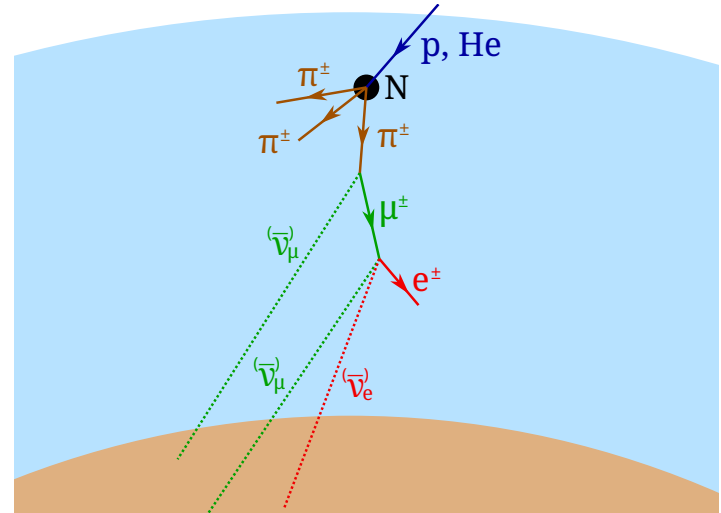
- Atmospheric (accelerator) neutrinos are produced by the interaction of *cosmic rays* (*protons*) with the *Earth's atmosphere* (*target*):

$$1 \quad A_{\text{in}} + A_{\text{tgt}} \rightarrow \pi^{\pm}, K^{\pm}, K^0, \dots$$

$$2 \quad \pi^{\pm} \rightarrow \mu^{\pm} + \nu_{\mu},$$

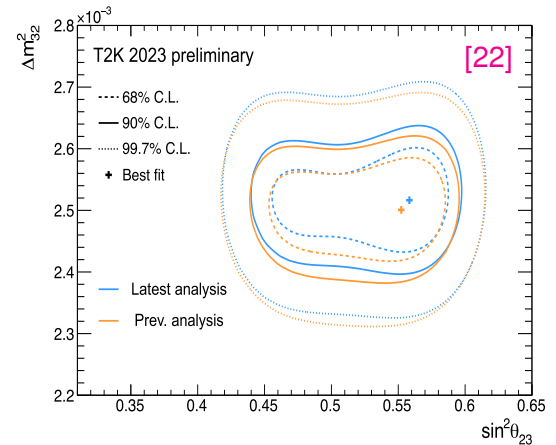
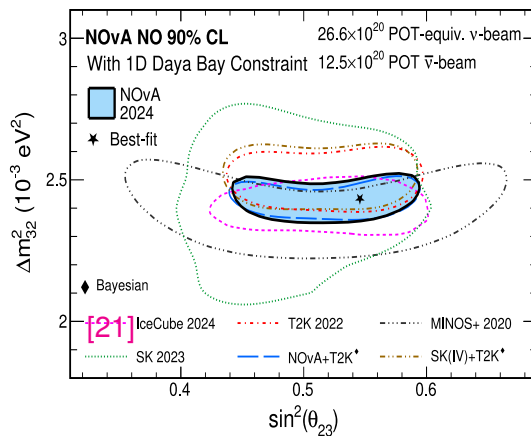
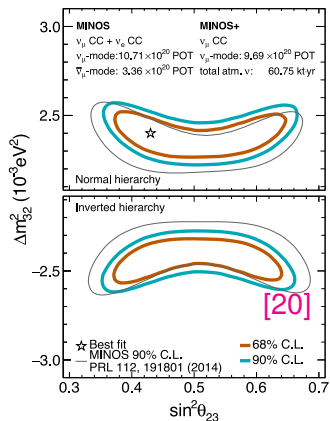
$$3 \quad \mu^{\pm} \rightarrow e^{\pm} + \nu_e + \nu_{\mu};$$

- at the detector, some ν interacts and produces a **charged lepton**, which is observed;
- atmospheric**: fluxes of ν_{μ} and ν_e are known with poor precision ($\approx 20\%$), but the accuracy on the ν_{μ}/ν_e ratio is better ($\approx 5\%$);
- accelerator**: a **near detector** allow to characterize the unoscillated ν flux.



Determination of Δm_{31}^2 and θ_{23} from accelerator data

- Δm_{31}^2 & θ_{23} dominated by LBL disappearance ($\nu_\mu \rightarrow \nu_\mu$) data;
- Δm_{21}^2 & θ_{12} subleading contributions to LBL appearance ($\nu_\mu \rightarrow \nu_e$) \Rightarrow relevant for δ_{CP} ;
- reasonably good agreement between all experiments in the allowed regions, although some small differences are visible.



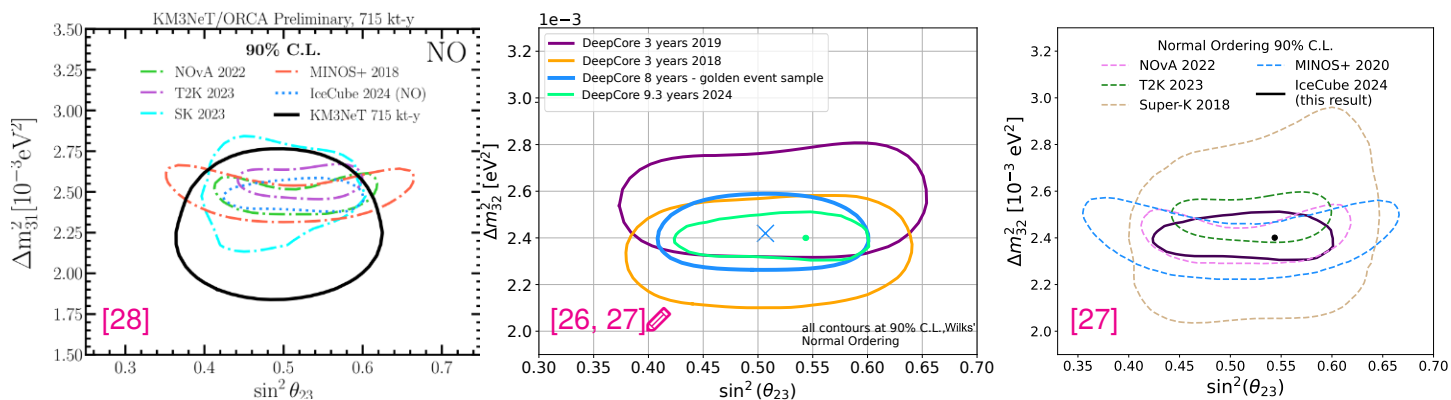
[20] T. Carroll [MINOS], online talk at Neutrino 2020, Fermilab, USA, June 22–July 2, 2020.

[21] J. Wolcott [NOvA], talk at Neutrino 2024, Milan, Italy, June 16–22, 2024.

[22] D. Carabadjac [T2K], talk at ICHEP 2024, Prague, Czech Republic, July 17–24, 2024.

The contribution of neutrino telescopes through atmospheric data

- IceCUBE/DeepCore: after many 3-year “calibration” fits [23, 24, 25], updated 8-year [26] and 9.3-year [27] results presented (but not “released”) ⇒ competitive with reactors and LBL;
- Km3NET/ORCA: under deployment (23/115 strings so far [28]), fit (ORCA6+11) catching up.



[23] M.G. Aartsen *et al.* [ICECUBE], PRD **91** (2015) 072004 [arXiv:1410.7227], updated Oct. 2016. [IC16]

[24] M.G. Aartsen *et al.* [ICECUBE], PRL **120** (2018) 071801 [arXiv:1707.07081].

[25] M.G. Aartsen *et al.* [ICECUBE], PRD **99** (2019) 032007 [arXiv:1901.05366]. [IC19]

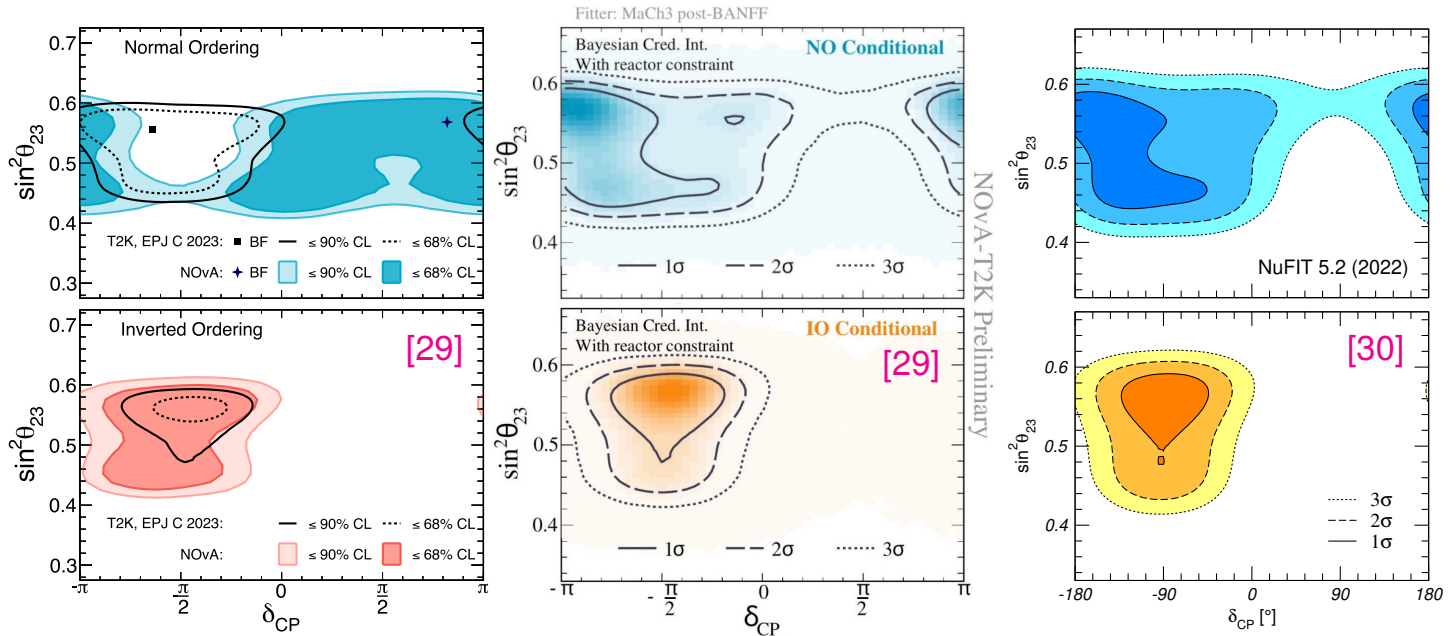
[26] R. Abbasi *et al.* [ICECUBE], PRD **108** (2023) 012014 [arXiv:2304.12236].

[27] R. Abbasi *et al.* [ICECUBE], arXiv:2405.02163. [IC24]

[28] J. Coelho [KM3NET], talk at Neutrino 2024, Milan, Italy, June 16–22, 2024.

Tension between NOvA and T2K data: summer 2020

- Neutrino 2020: tension on δ_{CP} between T2K and NOvA for **NO** (no problem for **IO**);
- official joint T2K/NOvA analysis finally presented [29], results very similar to estimates [30].

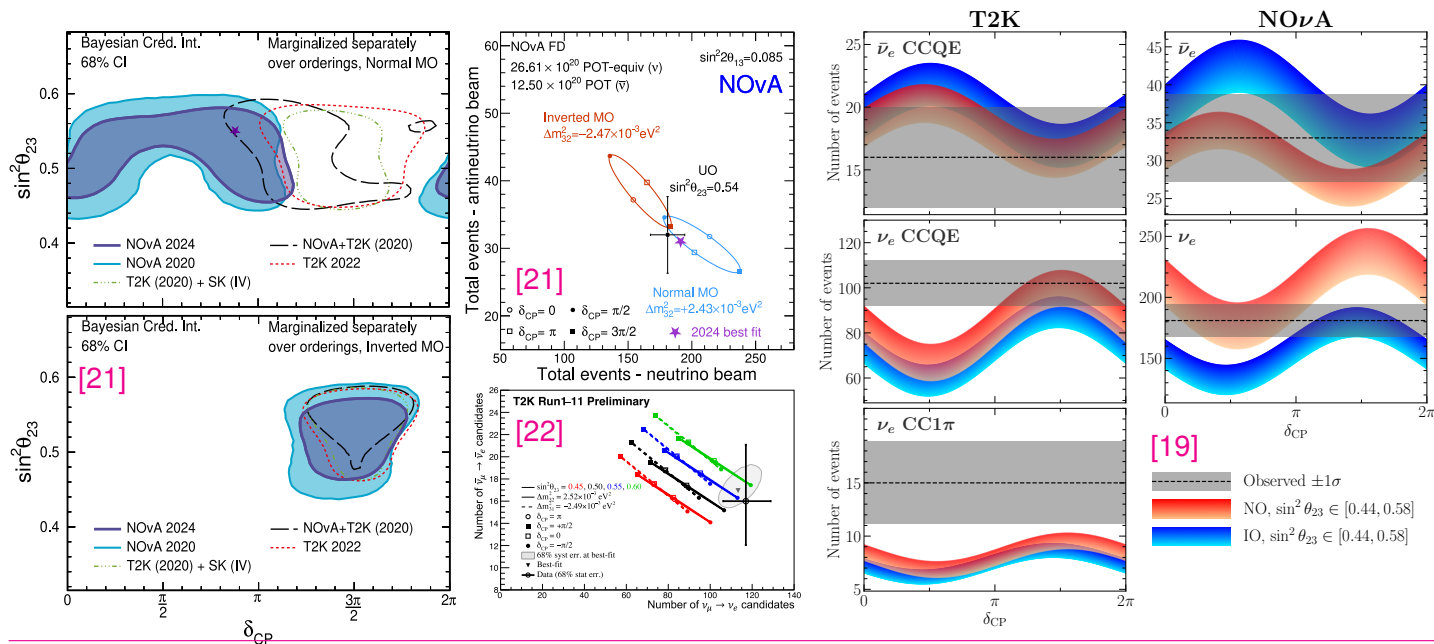


[29] M. Sanchez [NOvA], talk at Moriond-EW 2024, La Thuile, Italy, March 24–31, 2024.

[30] I. Esteban *et al.*, JHEP **09** (2020) 178 [arXiv:2007.14792].

Tension between NOvA and T2K data: today

- Neutrino 2024: NOvA substantially increased ν statistics, but no qualitative change on δ_{CP} .



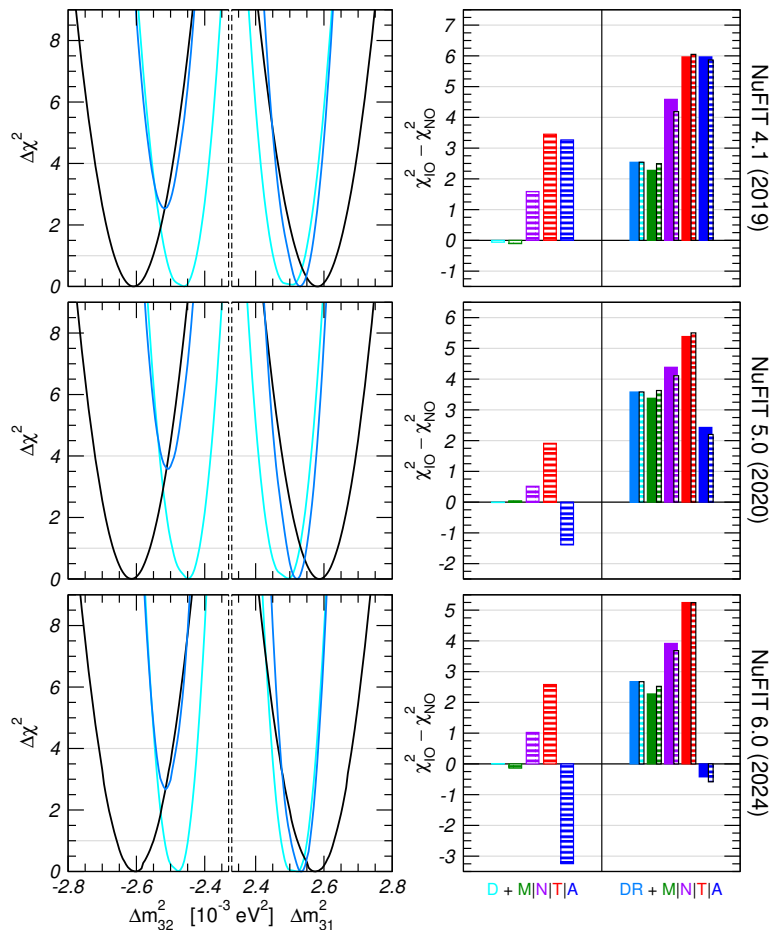
[19] I. Esteban *et al.*, arXiv:2410.05380 & NuFIT 6.0 [<http://www.nu-fit.org>].

[21] J. Wolcott [NOvA], talk at Neutrino 2024, Milan, Italy, June 16–22, 2024.

[22] D. Carabadjac [T2K], talk at ICHEP 2024, Prague, Czech Republic, July 17–24, 2024.

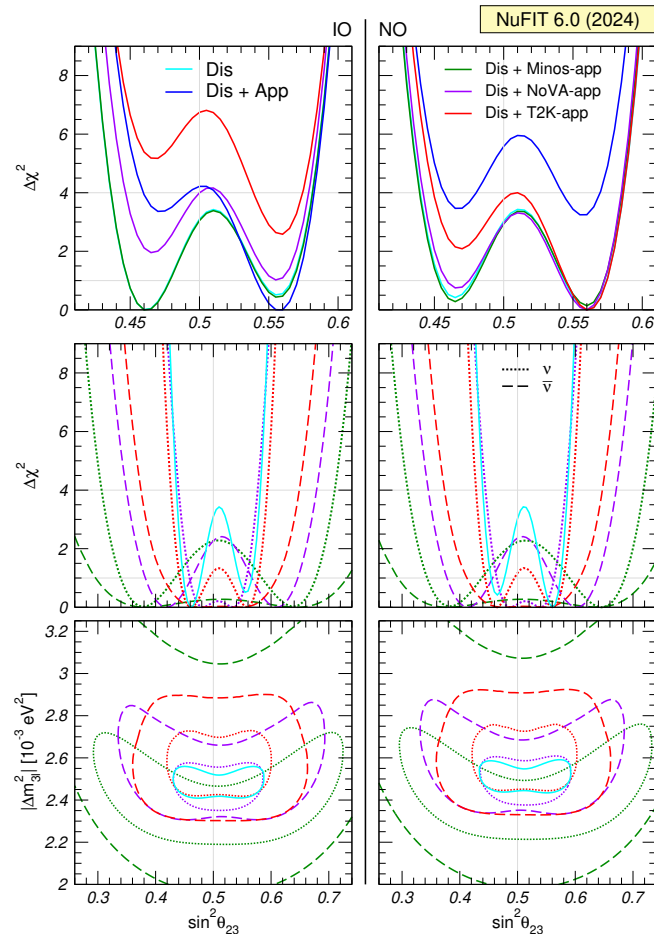
Δm_{31}^2 and mass ordering

- disappearance data: → **NO**
 - Δm_{31}^2 measured both by **reactor** (ν_e) and **accelerator** (ν_μ), but neither is sensitive to the ordering;
 - however, **combination** prefer **NO** due to better compatibility on Δm_{31}^2 range;
- appearance data: → **IO**
 - taken by **themselves** both **T2K** and **NOvA** exhibit a preference for **NO**;
 - but the δ_{CP} tension among them (which has increased over time) implies than **joint** LBL-app data prefer **IO**;
- ★ contrasting preferences of dis. and app. data mutually cancel ⇒ no indication.



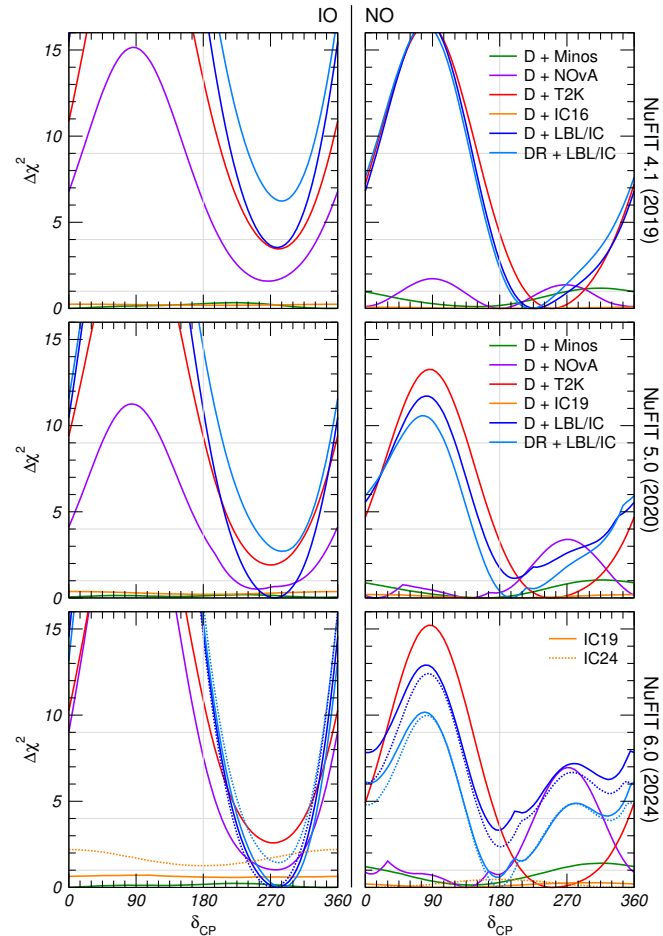
θ_{23} mixing and octant

- disappearance data:
 - each individual LBL-dis ν or $\bar{\nu}$ data slightly favor deviation from maximal mixing, but without any preference for a given octant;
 - **combined** disapp. data disfavor maximal mixing at $\Delta\chi^2 \sim 3.4$, with marginal octant preference (**NO** $> 45^\circ$ & **IO** $< 45^\circ$ at $\Delta\chi^2 \sim 0.4$);
- adding appearance data:
 - **Minos** contribution practically irrelevant;
 - **T2K** (more) and **NOvA** (less) both push for $\theta_{23} > 45^\circ$, irrespective of the mass ordering;
 - **combination** confirms $\theta_{23} > 45^\circ$ for **IO**, but for **NO** the δ_{CP} tension between T2K and NOvA cancels this hint and lead to similar minima.



Status of the CP phase

- **T2K** data show a clear preference for maximal CP violation ($\delta_{CP} \simeq 270^\circ$), irrespective of the assumed mass ordering;
- **NOvA** data also favor such value for **IO**, but for **NO** it disfavors it, preferring instead the CP conserving value $\delta_{CP} \simeq 180^\circ$;
- **NOvA** rejection of $\delta_{CP} \simeq 270^\circ$ has steadily increased over time: $1.2\sigma \rightarrow 1.8\sigma \rightarrow 2.6\sigma$ from the analysis of NuFIT 4.1 \rightarrow 5.0 \rightarrow 6.0 data;
- **Minos** & **IceCube** have practically no sensitivity to δ_{CP} and give negligible contribution;
- combined **LBL+IC** experiments indicate $\delta_{CP} \simeq \pi$ for **NO**, thus dominated by **NOvA**. Further inclusion of **reactors** does not change this picture.



Neutrino oscillations: where we are

- Global 6-parameter fit (including δ_{CP}):
 - **Solar**: Cl + Ga + SK(1–4) + SNO-full (I+II+III) + BX(1–3);
 - **Atmospheric**: IC19 | IC24 + SK(1–5);
 - **Reactor**: KamLAND + SNOplus + DC + DB + Reno;
 - **Accelerator**: Minos + T2K + NOvA;

- best-fit point and 1σ (3σ) ranges:

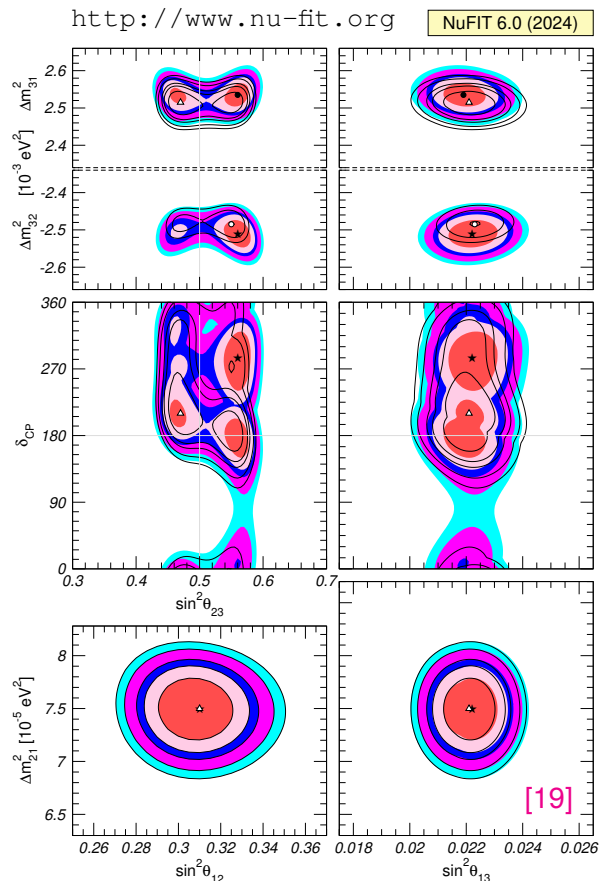
$$\theta_{12} = 33.68_{-0.70}^{+0.73} \left({}_{-2.05}^{+2.27} \right), \quad \Delta m_{21}^2 = 7.49_{-0.19}^{+0.19} \left({}_{-0.57}^{+0.56} \right) \times 10^{-5} \text{ eV}^2,$$

$$\theta_{23} = \begin{cases} 48.5_{-0.9}^{+0.7} \left({}_{-7.6}^{+2.0} \right), \\ 48.6_{-0.9}^{+0.7} \left({}_{-7.2}^{+2.0} \right), \end{cases} \quad \Delta m_{31}^2 = \begin{cases} +2.534_{-0.023}^{+0.025} \left({}_{-0.071}^{+0.072} \right) \times 10^{-3} \text{ eV}^2, \\ -2.510_{-0.025}^{+0.024} \left({}_{-0.073}^{+0.072} \right) \times 10^{-3} \text{ eV}^2, \end{cases}$$

$$\theta_{13} = 8.58_{-0.13}^{+0.11} \left({}_{-0.39}^{+0.33} \right), \quad \delta_{\text{CP}} = 285_{-28}^{+25} \left({}_{-182}^{+129} \right);$$

- neutrino mixing matrix:

$$|U|_{3\sigma} = \begin{pmatrix} 0.801 \rightarrow 0.842 & 0.519 \rightarrow 0.580 & 0.142 \rightarrow 0.155 \\ 0.248 \rightarrow 0.505 & 0.473 \rightarrow 0.682 & 0.649 \rightarrow 0.764 \\ 0.270 \rightarrow 0.521 & 0.483 \rightarrow 0.690 & 0.628 \rightarrow 0.746 \end{pmatrix}.$$



[19] I. Esteban *et al.*, [arXiv:2410.05380](https://arxiv.org/abs/2410.05380) & NuFIT 6.0 [<http://www.nu-fit.org>].

- Most of the present data from **solar**, **atmospheric**, **reactor** and **accelerator** experiments are well explained by the 3ν oscillation hypothesis. The three-neutrino scenario is robust;
- the long-standing “hints” concerning the **mass ordering**, with **NO** favored over **IO** at the $2\sigma \div 3\sigma$ level, are cancelled by the T2K/NOvA tension;
- the discovery of large θ_{13} opened the road to searches for **CP violation**. However, results on this topic need further clarifications;
- deviation from **maximal θ_{23} mixing** is also still an open issue. The region $\theta_{23} > 45^\circ$ seems to be slightly preferred, especially for **IO**;
- synergies between different experiments will be crucial to increase the sensitivity.

