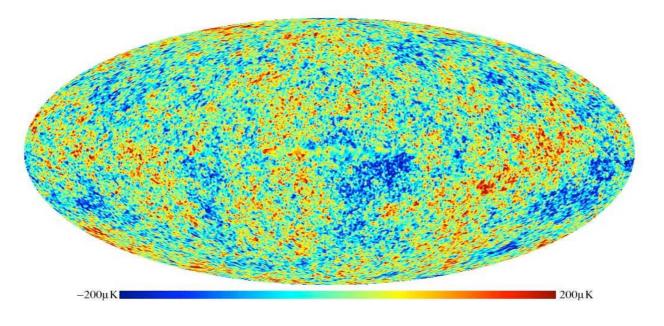
Leonardo Senatore (ETH)

Large Scale Structure Cosmology with the Effective Field Theory

Current Picture of Initial Perturbation

• Quantum Vacuum Fluctuations of a field, the inflaton, created the initial perturbations:

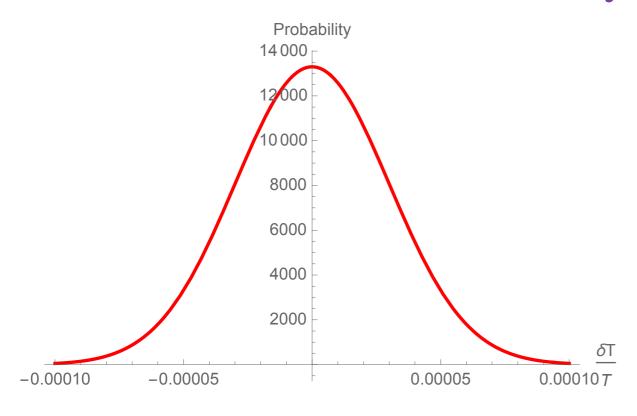


credit: NASA/WMAP

- Knowledge of initial conditions and components $\sim 10^{-2}~{
 m or}~\sim 10^{-3}$
- Primordial Non-Gaussianities: we know the initial distribution of the fluctuations is Gaussian to about $\sim 10^{-3}$
- What does that mean?

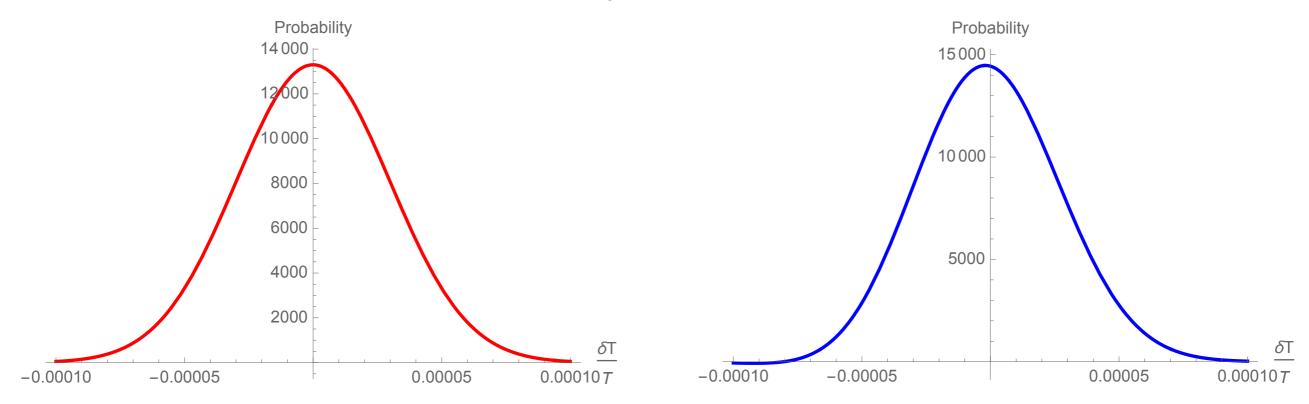
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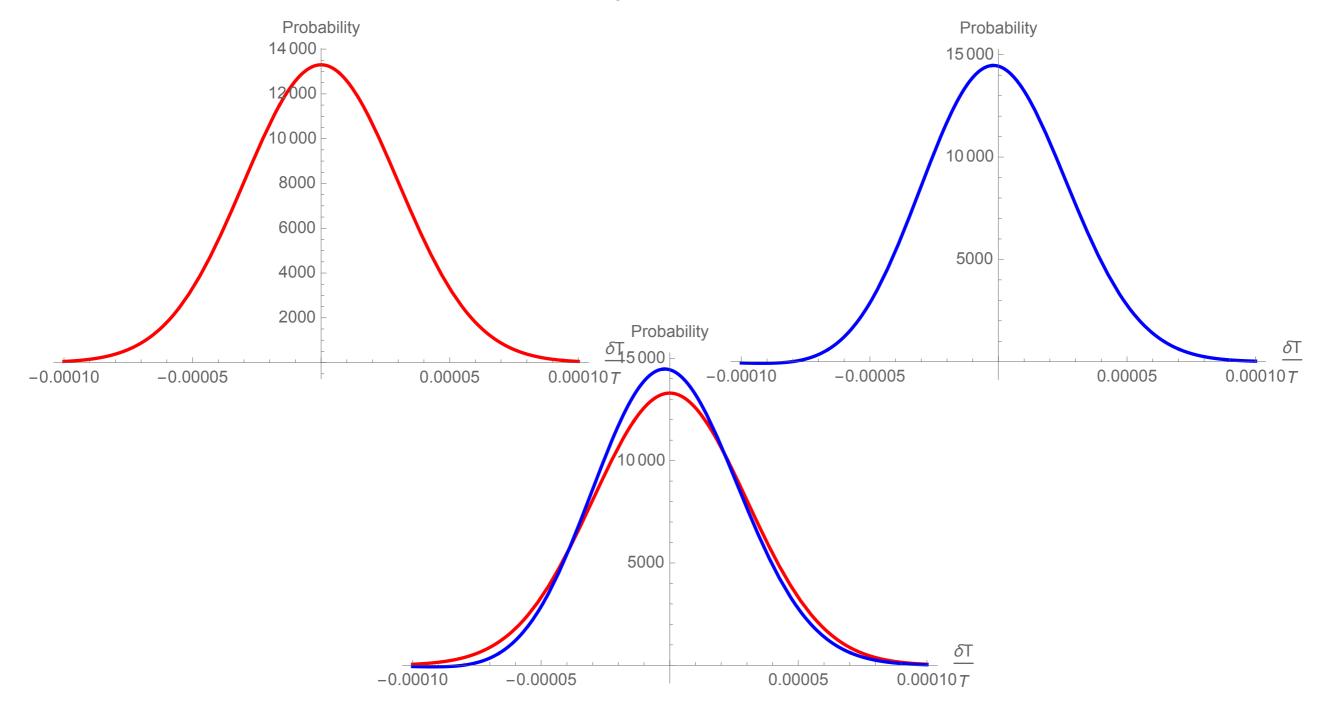
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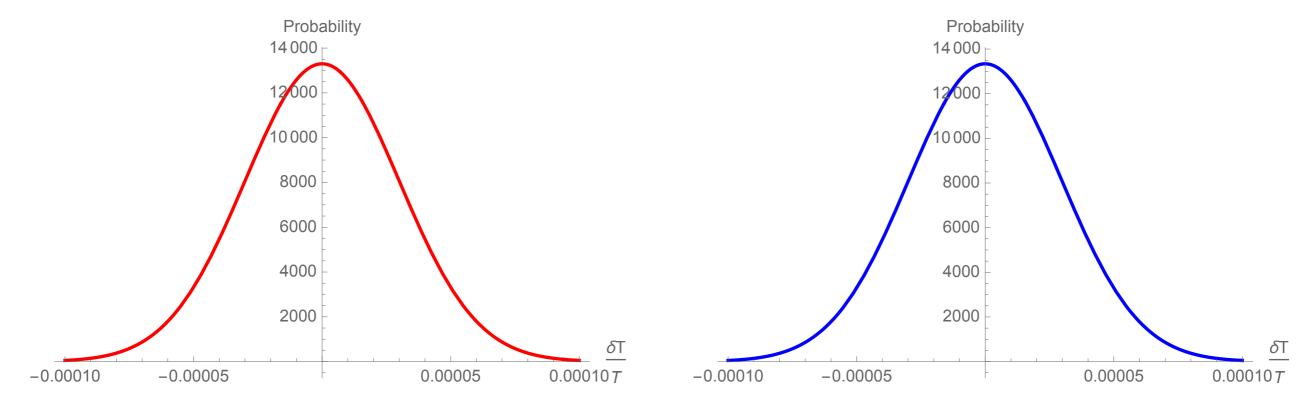


Very Non-Gaussian



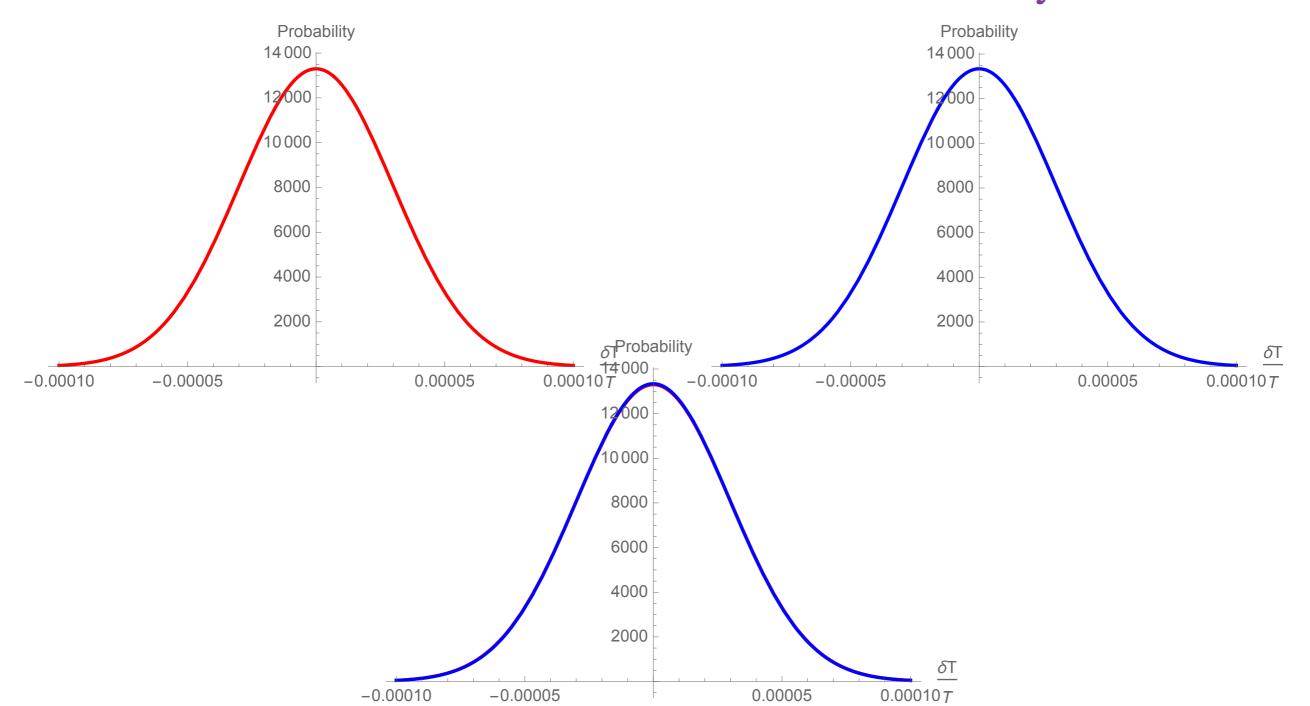
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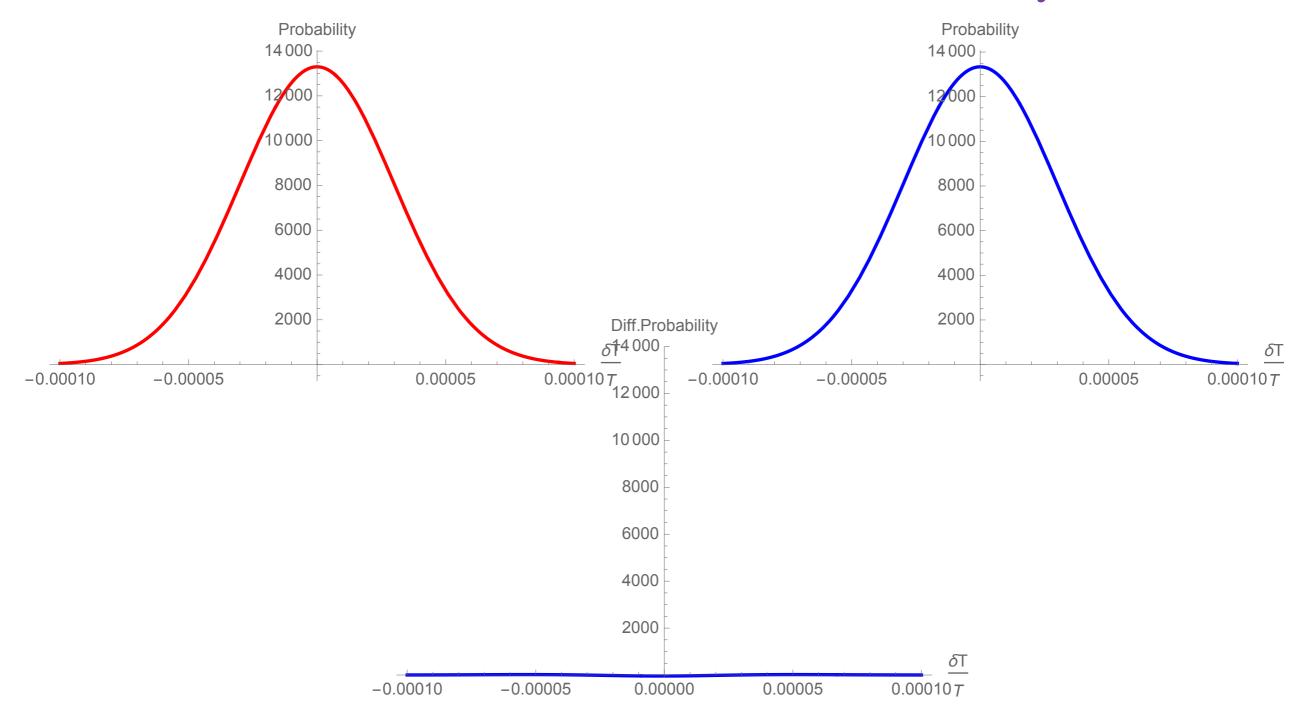
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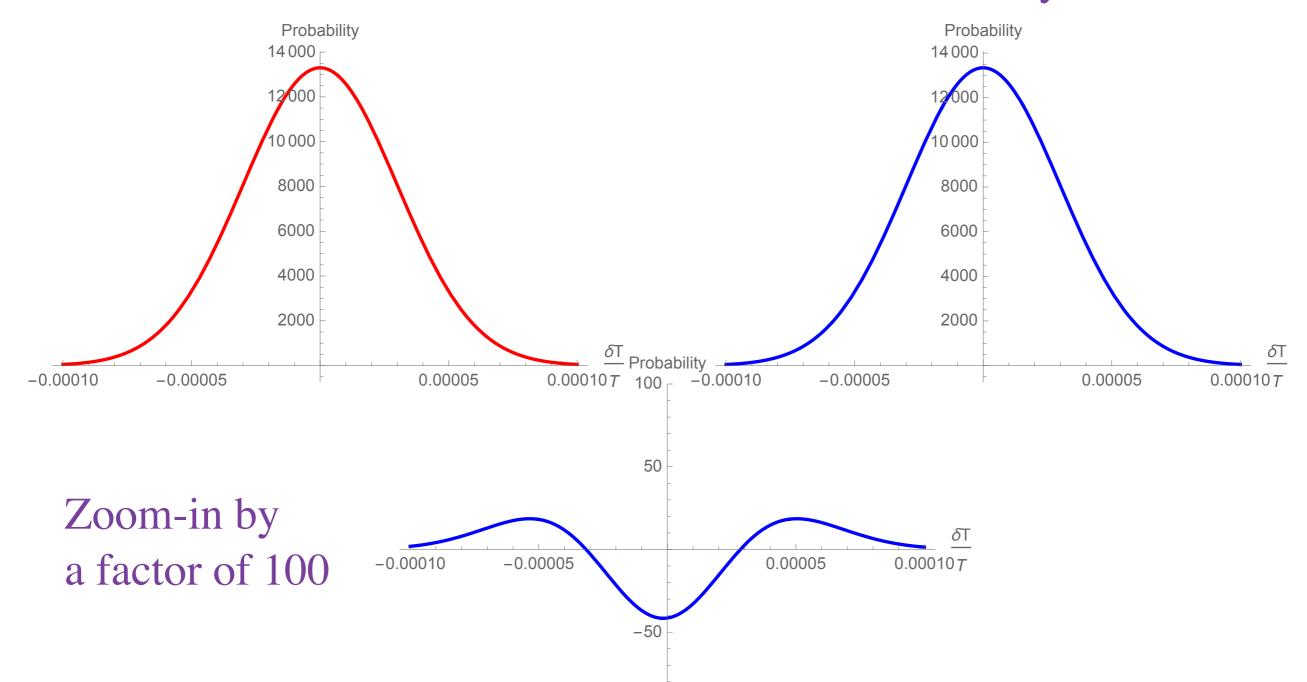
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Quantum Fields at the origin of Universe

- How could we achieve such a Gaussian distribution?
- If Inflation is made of a quantum field

with Cheung et al. 2008

$$S_{\pi} = \int d^4 \sqrt{-g} \left[\frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} \left(\dot{\pi}^2 - c_s^2 (\partial_i \pi)^2 \right) + \frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} \left[\dot{\pi} (\partial_i \pi)^2 + \tilde{c}_3 \, \dot{\pi}^3 \right] \right]$$

• in its vacuum state:

$$|0\rangle$$
, $|\Omega\rangle$, $\Psi(\pi)$

- and the non-linear term are small.
- Then we can!
 - vacuum quantum fluctuations are Gaussian!
- Less self-interacting than Quantum Electro Dyn.

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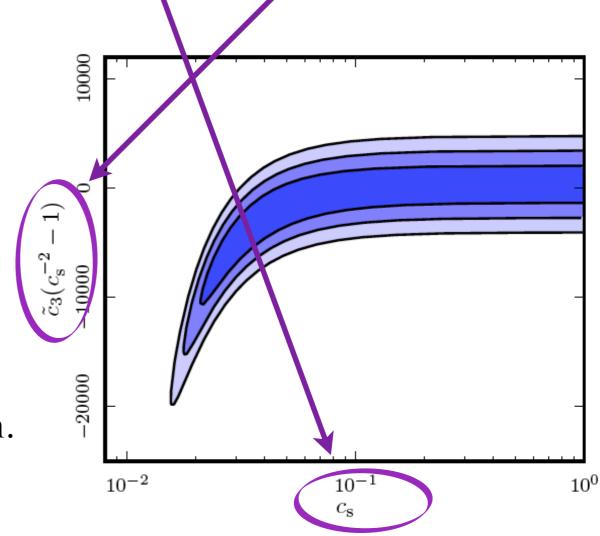
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with Smith and Zaldarriaga, 2010 WMAP final 2012

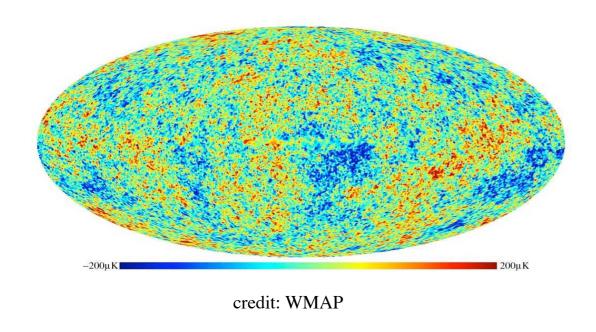
Planck Collaboration 2013, 2015, 2018

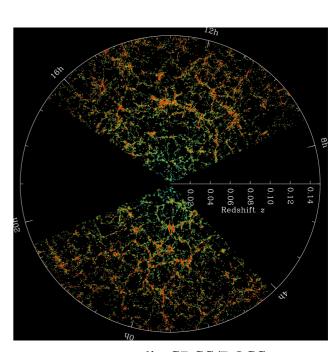
The way ahead

Cosmology is a luminosity experiment

- Progress through observation of the primordial fluctuations
- They are statically distributed:
 - -To increase knowledge: more modes:

$$\Delta (\text{everything}) \propto \frac{1}{\sqrt{N_{\text{pixel}}}}$$





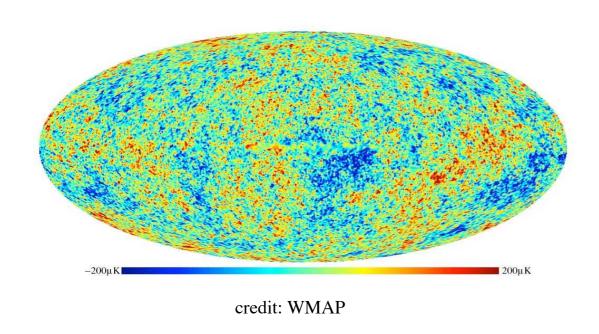
credit: SDSS/BOSS

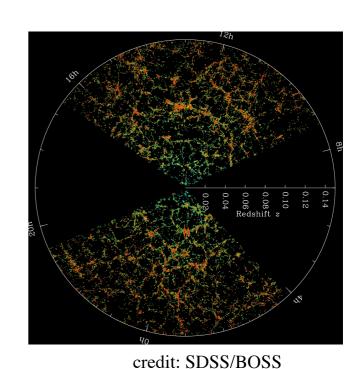
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Planck, STPpol, ... has observed almost all the modes in CMB





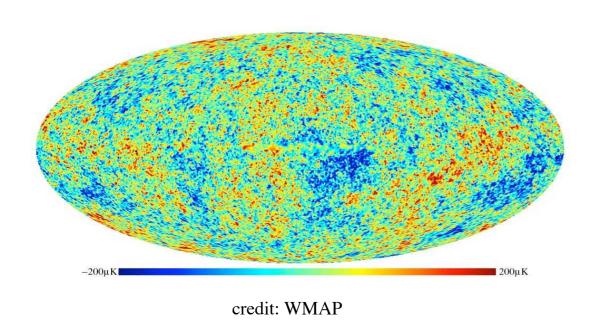
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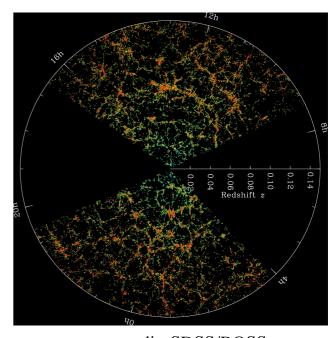
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Large-Scale Structure (LSS) offer the only medium-term opportunity





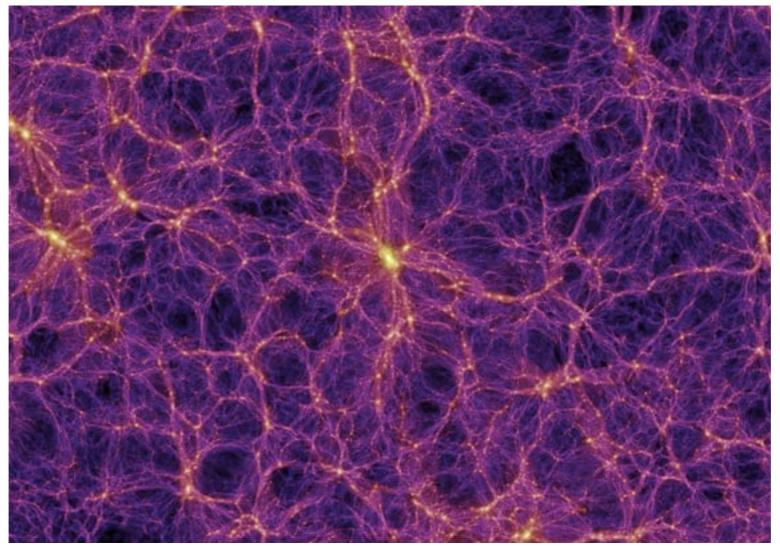
credit: SDSS/BOSS

What is the challenge?

– As many modes as possible:

$$N_{\text{modes}} \sim \int^{k_{\text{max}}} d^3k \sim k_{\text{max}}^3$$

Need to understand short distances



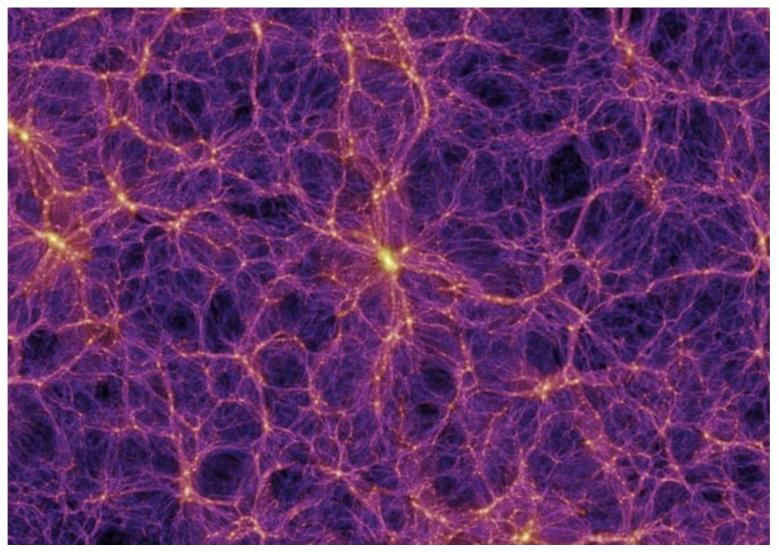
credit: Millenium Simulation, Springel et al. (2005)

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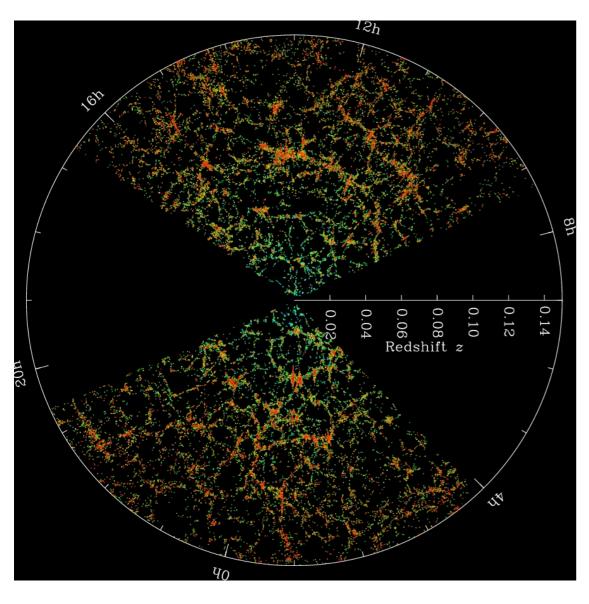
- Need to understand short distances
 - Like having LHC but not having QCD



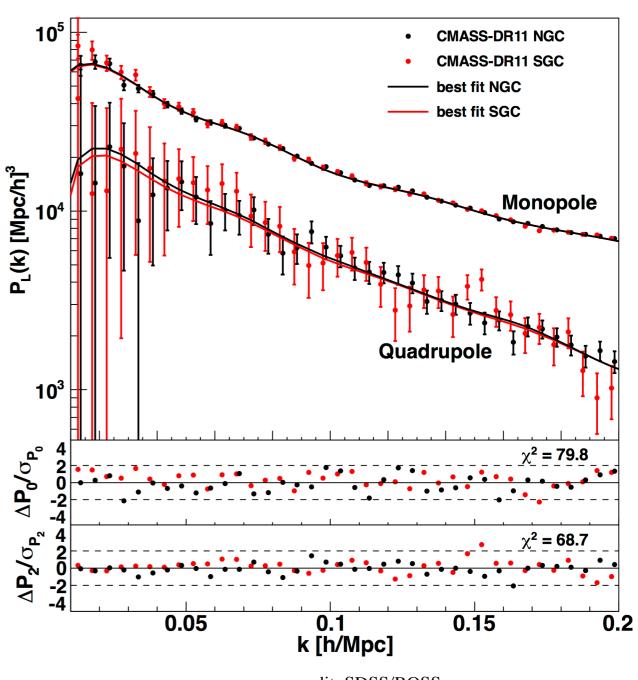
credit: Millenium Simulation, Springel et al. (2005)

The Observables

$$\langle n_{\rm gal}(\vec{x}) n_{\rm gal}(\vec{y}) \rangle \iff \langle n_{\rm gal}(\vec{k}) n_{\rm gal}(\vec{k}') \rangle \equiv P(\vec{k}) \, \delta^{(3)} \left(\vec{k} + \vec{k}' \right)$$

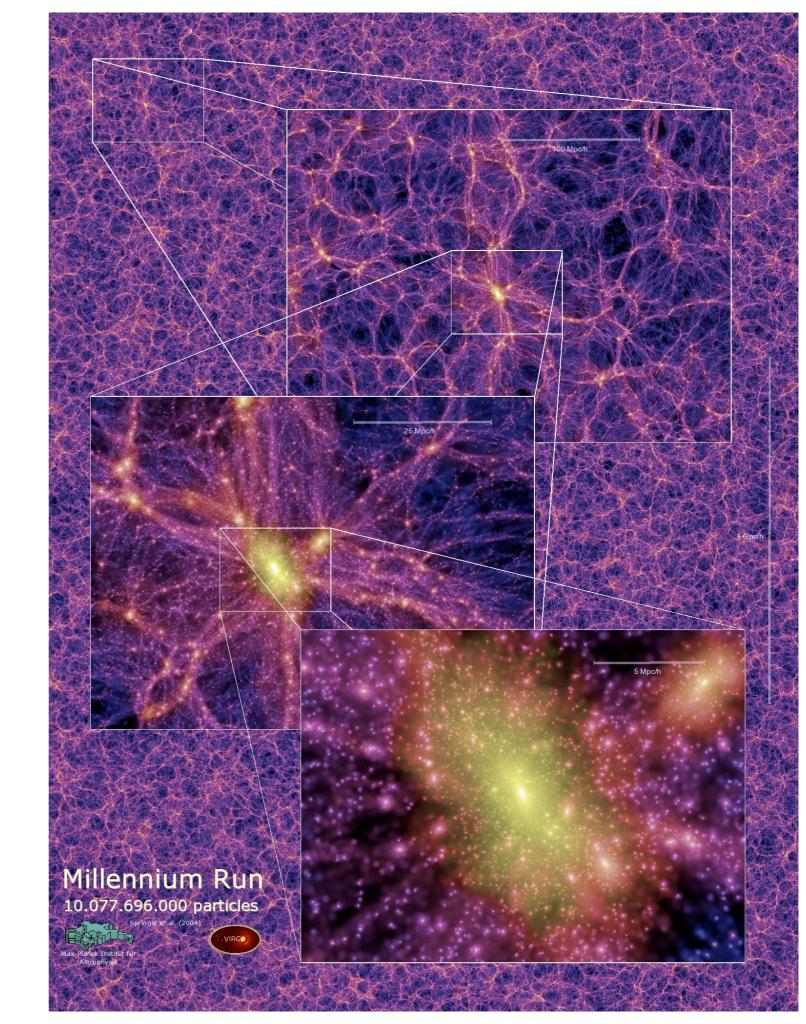


credit: SDSS/BOSS

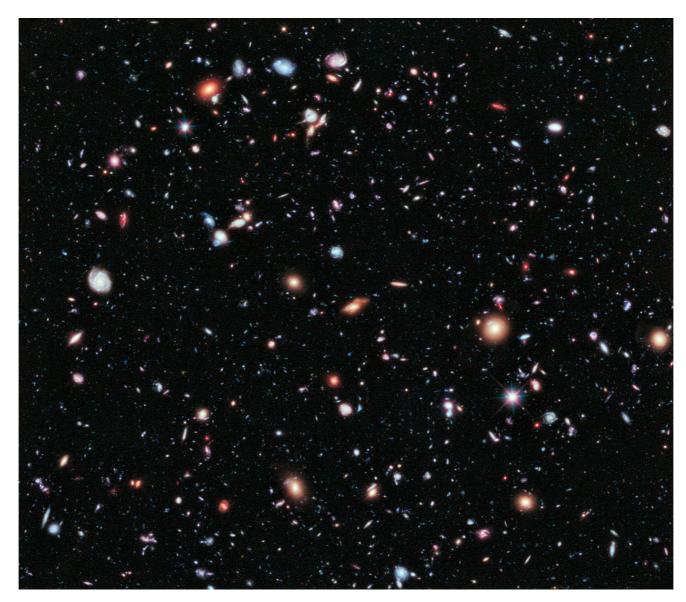


credit: SDSS/BOSS

Normal Approach: numerics

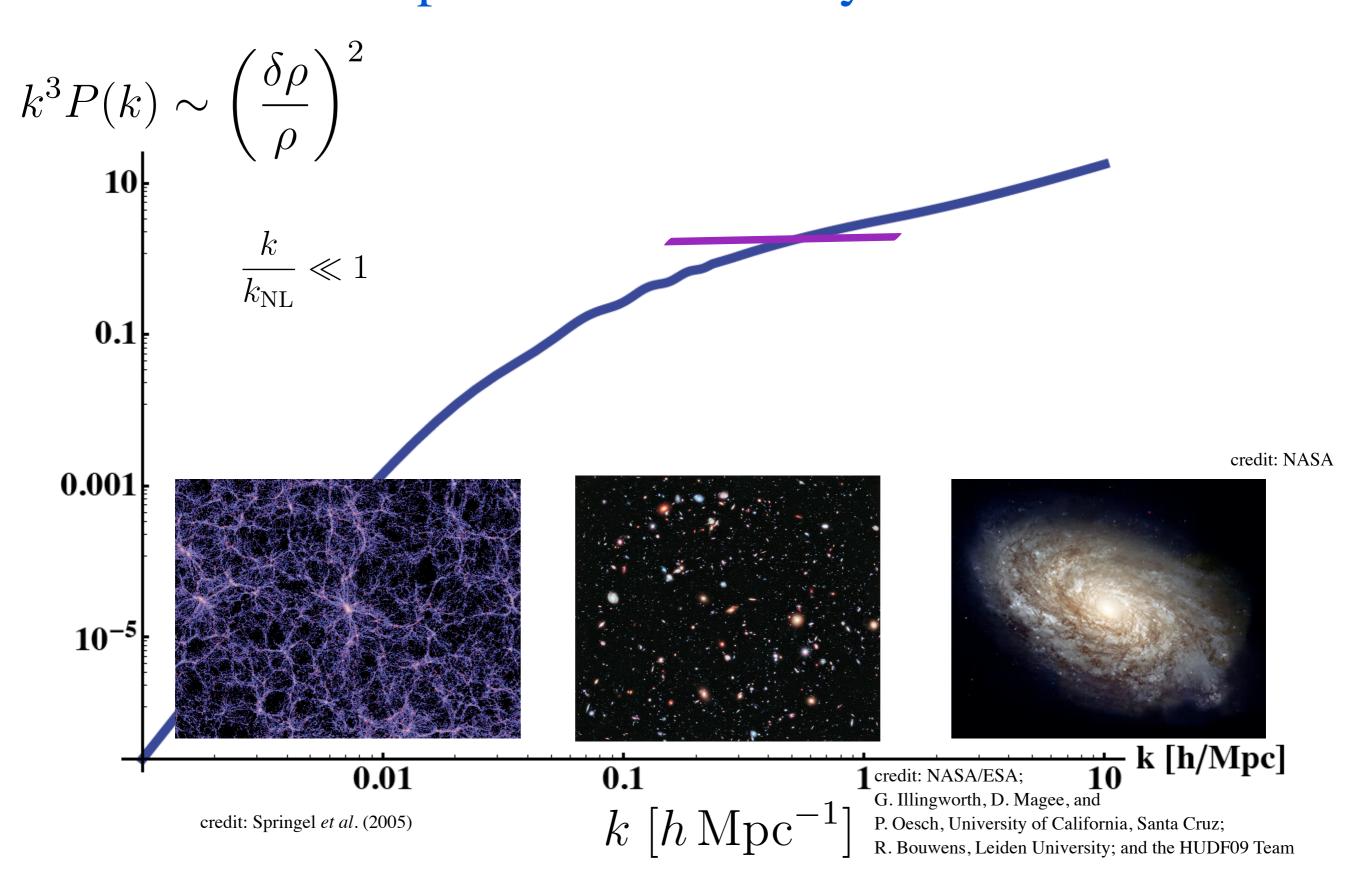


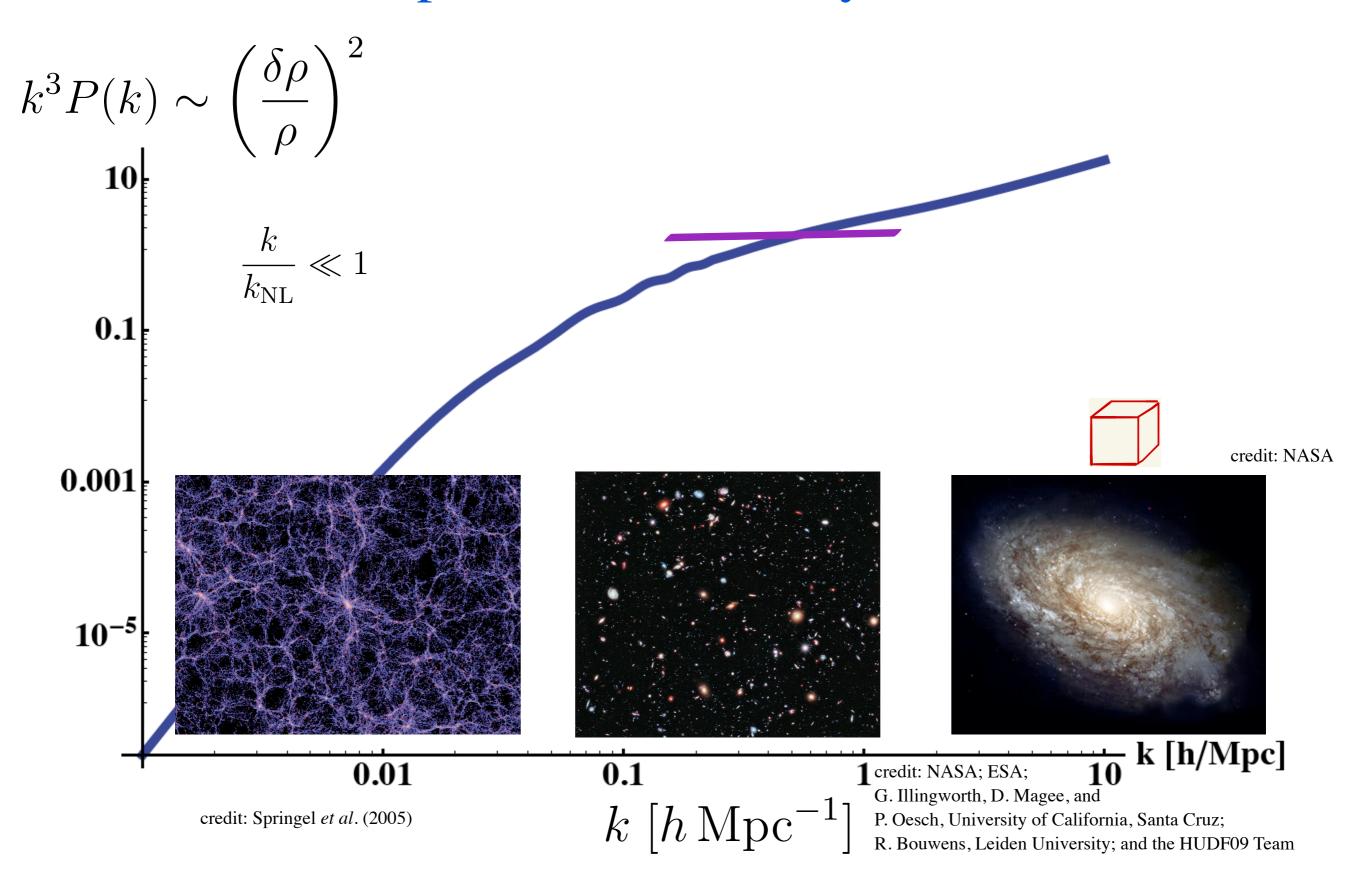
Large-Scale Structure

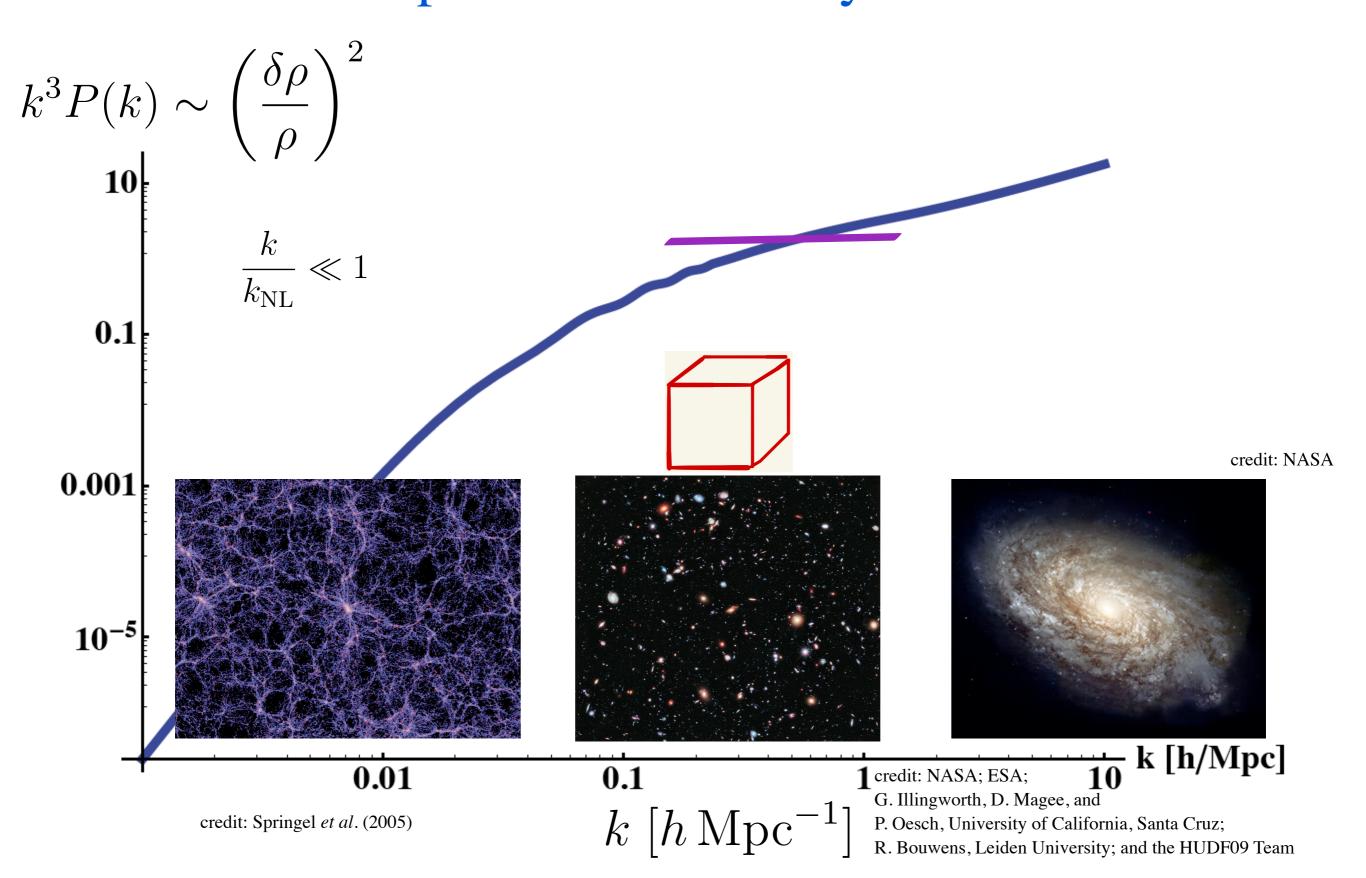


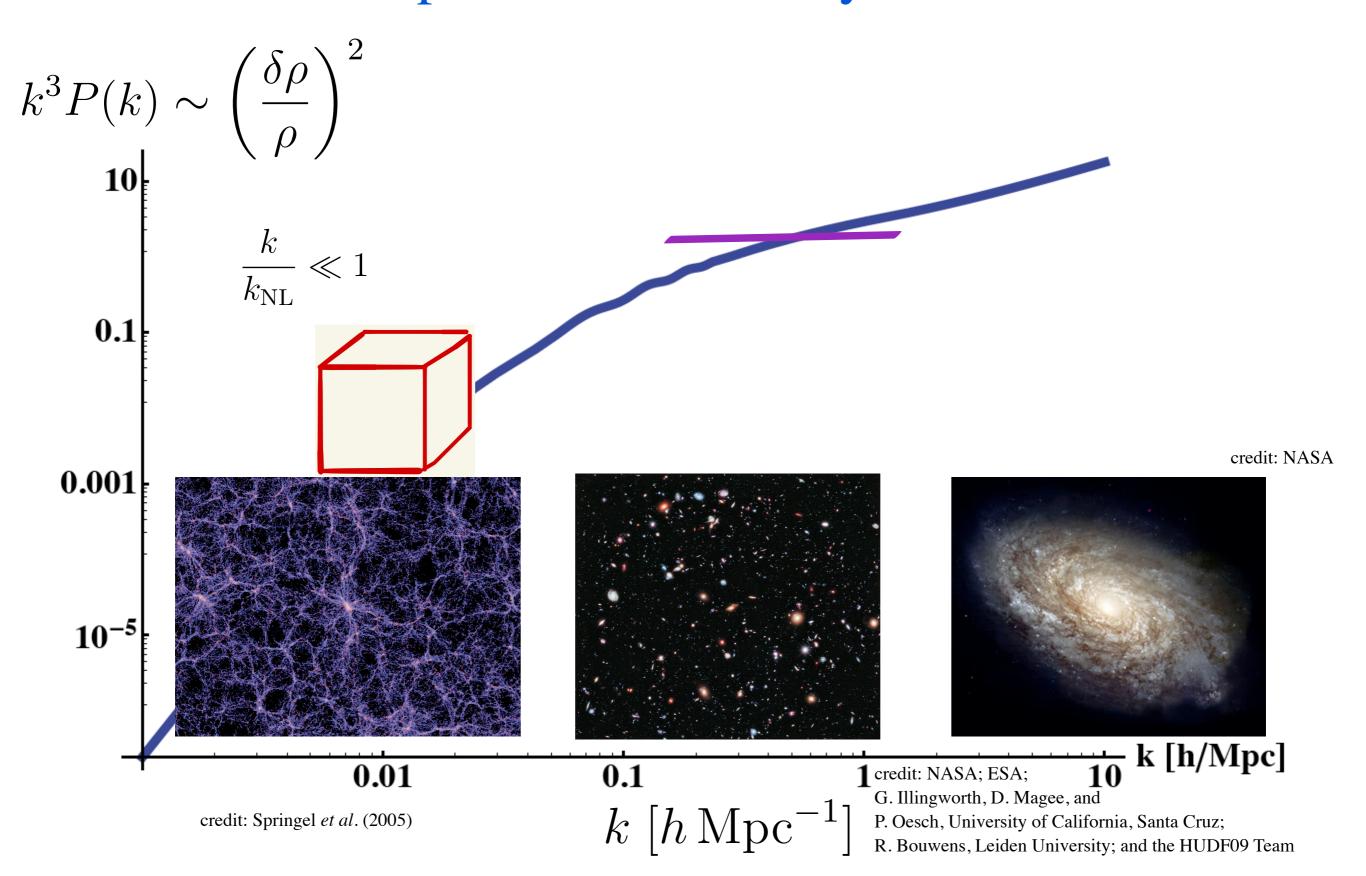
credit NASA/ESA

- -DESI, Euclid, Vera Rubin, Megamapper...
- Can we use them to make a lot of fundamental physics?
 - -in CMB, we use simplicity of universe at early time, can we now use its simplicity at long distances?

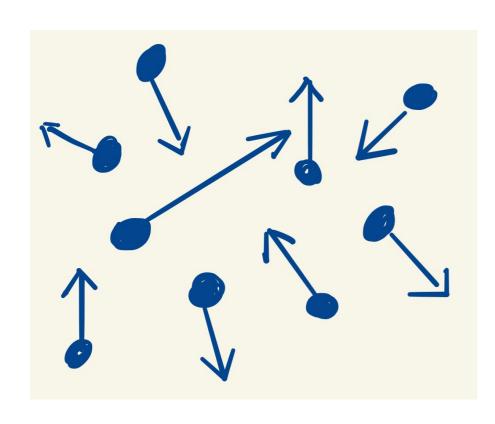








What is a fluid?



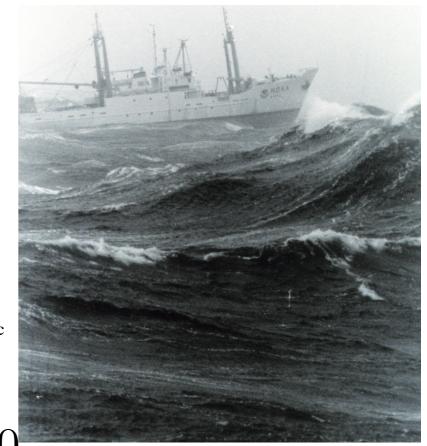
wikipedia: credit National Oceanic and Atmospheric Administration/ Department of Commerce

$$\partial_t \rho_\ell + \partial_i \left(\rho_\ell v_\ell^i \right) = 0$$

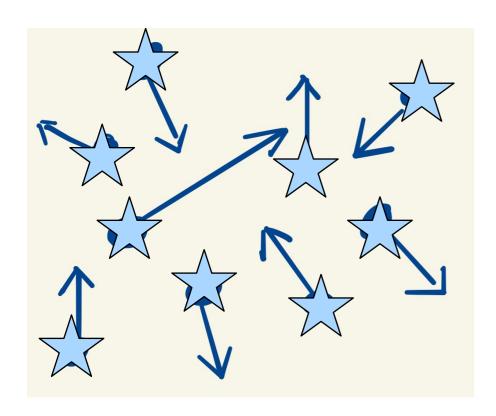
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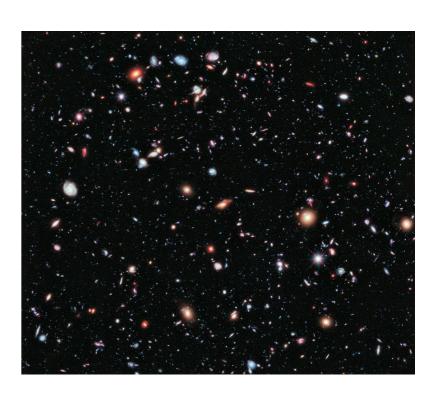
$$\partial_t v_\ell^i + v_\ell^j \partial_j v_\ell^i + \frac{1}{\rho_\ell} \partial_i p_\ell = \text{viscous terms}$$

- -From short to long
- The resulting equations are simpler
- -Description arbitrarily accurate
 - -construction can be made without knowing the nature of the particles.
- -short distance physics appears as a non trivial stress tensor for the long-distance fluid



Do the same for matter in our Universe





credit NASA

with Baumann, Nicolis and Zaldarriaga JCAP 2012 with Carrasco and Hertzberg JHEP 2012

- -From short to long
- -The resulting equations are simpler
- -Description arbitrarily accurate

- $\nabla^2 \Phi_{\ell} = H^2 \left(\delta \rho_{\ell} / \rho \right)$ $\partial_t \rho_{\ell} + H \rho_{\ell} + \partial_i \left(\rho_{\ell} v_{\ell}^i \right) = 0$ $\partial_t v_{\ell}^i + v_{\ell}^j \partial_j v_{\ell}^i + \partial_i \Phi_{\ell} = \partial_j \tau^{ij}$
- -construction can be made without knowing the nature of the particles.
- -short distance physics appears as a non trivial stress tensor for the long-distance fluid

$$\tau_{ij} \sim \delta_{ij} \, \rho_{\rm short} \, \left(v_{\rm short}^2 + \Phi_{\rm short} \right)$$

Dealing with the Effective Stress Tensor

• For long distances: expectation value over short modes (integrate them out)

$$\langle \tau_{ij}(\vec{x},t) \rangle_{\text{long fixed}} = f_{\text{very complicated}} \left(\{H, \Omega_m, \dots, m_{\text{dm}}, \dots, \rho_{\ell}(x) \}_{\text{past light cone}} \right)$$



$$\langle \tau_{ij}(\vec{x},t) \rangle_{\text{long fixed}} = \int^t dt' \left[c(t,t') \frac{\delta \rho_{\ell}}{\rho} (\vec{x}_{\text{fl}},t') + \mathcal{O}\left((\delta \rho_{\ell}/\rho)^2 \right) \right]$$

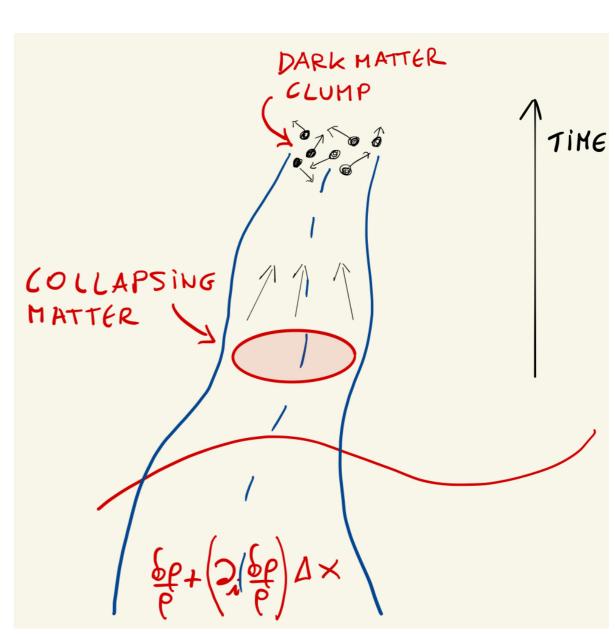
Equations with only long-modes

$$\partial_t v^i_\ell + v^j_\ell \partial_j v^i_\ell + \partial_i \Phi_\ell = \partial_j \tau^{ij}$$

$$\tau_{ij} \sim \delta \rho_\ell / \rho + \dots$$
 every term allowed by symmetries

each term contributes as factor of

$$\frac{\delta \rho_l}{\rho} \sim \frac{k}{k_{\rm NL}} \ll 1$$



Perturbation Theory within the EFT

• In the EFT we can solve iteratively $\delta_\ell, v_\ell, \Phi_\ell \ll 1$, where $\delta_\ell = \frac{\delta \rho_\ell}{\rho}$

$$\nabla^{2}\Phi_{\ell} = H^{2} \left(\delta \rho_{\ell}/\rho\right)$$

$$\partial_{t}\rho_{\ell} + H\rho_{\ell} + \partial_{i} \left(\rho_{\ell}v_{\ell}^{i}\right) = 0$$

$$\partial_{t}v_{\ell}^{i} + v_{\ell}^{j}\partial_{j}v_{\ell}^{i} + \partial_{i}\Phi_{\ell} = \partial_{j}\tau^{ij}$$

$$\tau_{ij} \sim \delta \rho_{\ell}/\rho + \dots$$

• Two scales:

$$k \, [\text{Mean Free Path Scale}] \sim k \, \left[\left(\frac{\delta \rho}{\rho} \right) \sim 1 \right] \sim k_{\text{NL}}$$

Perturbation Theory within the EFT

- Solve iteratively some non-linear eq. $\delta_\ell = \delta_\ell^{(1)} + \delta_\ell^{(2)} + \ldots \ll 1$
- Second order:

$$\partial^2 \delta_\ell^{(2)} = \left(\delta_\ell^{(1)}\right)^2 \quad \Rightarrow \quad \delta_\ell^{(2)}(x) = \int d^4 x' \operatorname{Greens}(x, x') \left(\delta_\ell^{(1)}(x')\right)^2$$

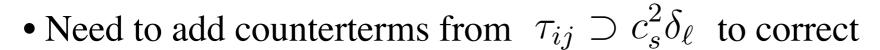
• Compute observable:

$$\langle \delta_{\ell}(x_1)\delta_{\ell}(x_2)\rangle \supset \langle \delta_{\ell}^{(2)}(x_1)\delta_{\ell}^{(2)}(x_2)\rangle \sim \int d^4x_1'd^4x_2' \text{ (Green's)}^2 \langle \delta_{\ell}^{(1)}(x_1')^2\delta_{\ell}^{(1)}(x_2')^2\rangle$$

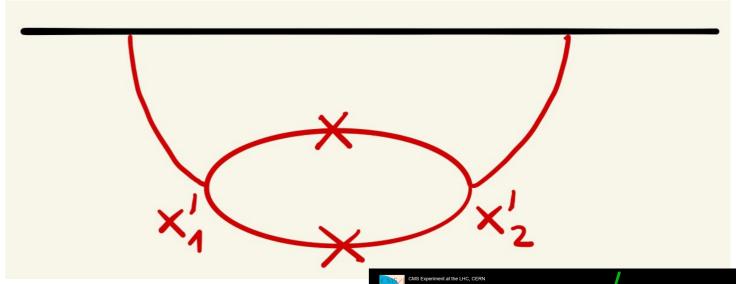
• We obtain Feynman diagrams

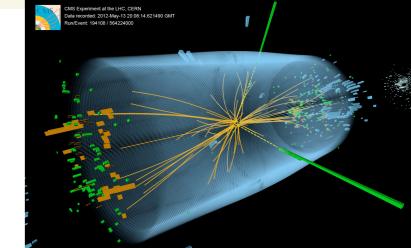


$$x_2' \to x_1'$$



• Loops and renormalization applied to galaxies





.... lots of work

Galaxy Statistics

Senatore **1406** with Lewandowsky *et al* **1512** with Perko *et al* **. 1610**

Galaxies in the EFTofLSS

- On galaxies, a long history before us, summarized by McDonald, Roy 2010.
 - Senatore 1406 provided first complete parametrization.

• Nature of Galaxies is very complicated

$$n_{\rm gal}(x) = f_{\rm very\ complicated}\left(\left\{H, \Omega_m, \dots, m_e, g_{ew}, \dots, \rho(x)\right\}_{\rm past\ light\ cone}\right)$$

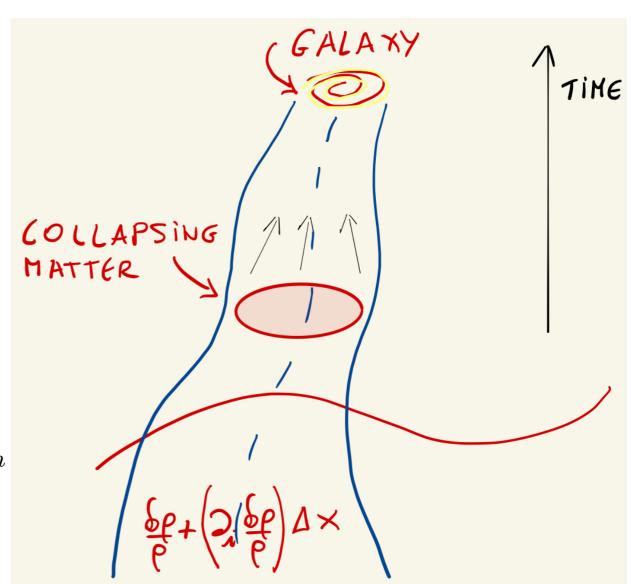
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$$n_{\rm gal}(x) = f_{\rm very\ complicated}\left(\left\{H, \Omega_m, \dots, m_e, g_{ew}, \dots, \rho(x)\right\}_{\rm past\ light\ cone}\right)$$



$$\left(\frac{\delta n}{n}\right)_{\text{gal},\ell}(x) \sim \int^t dt' \left[c(t,t') \left(\frac{\delta \rho}{\rho}\right)(\vec{x}_{\text{fl}},t') + \ldots\right]$$

- all terms allowed by symmetries
- all physical effects included
 - −e.g. assembly bias
- $\left\langle \left(\frac{\delta n}{n}\right)_{\text{gal.}\ell}(x)\left(\frac{\delta n}{n}\right)_{\text{gal.}\ell}(y)\right\rangle =$ $= \sum \operatorname{Coeff}_n \cdot \langle \operatorname{matter correlation function} \rangle_n$



It is familiar in dielectric E&M

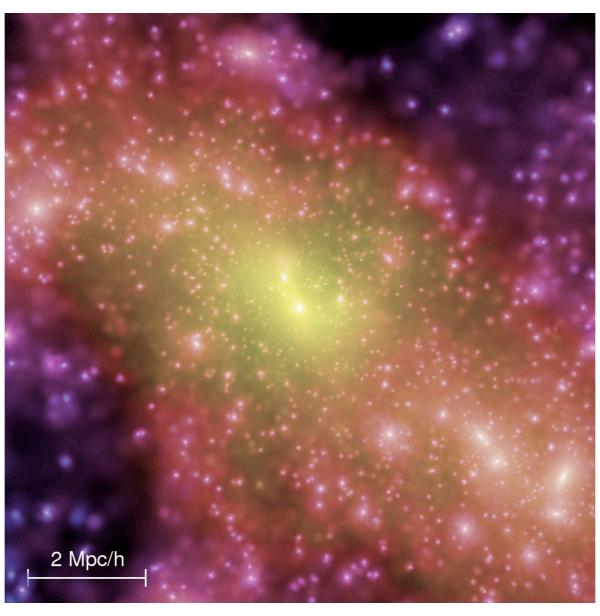
• Polarizability:

$$\vec{P}(\omega) = \chi(\omega)\vec{E}(\omega) \implies \vec{P}(t) = \int dt' \chi(t-t')\vec{E}(t')$$

- -Here we work in time-Fourier space, and theory is practically linear.
- The EFT of Non-Relativistic binaries Goldberger and Rothstein 2004 is non-local in time
 - -Here we solve perturbatively the inspiralling regime, and feed it into the long-distance theory (again time-Fourier space).

Baryonic effects

• When stars explode, baryons behave differently than dark matter

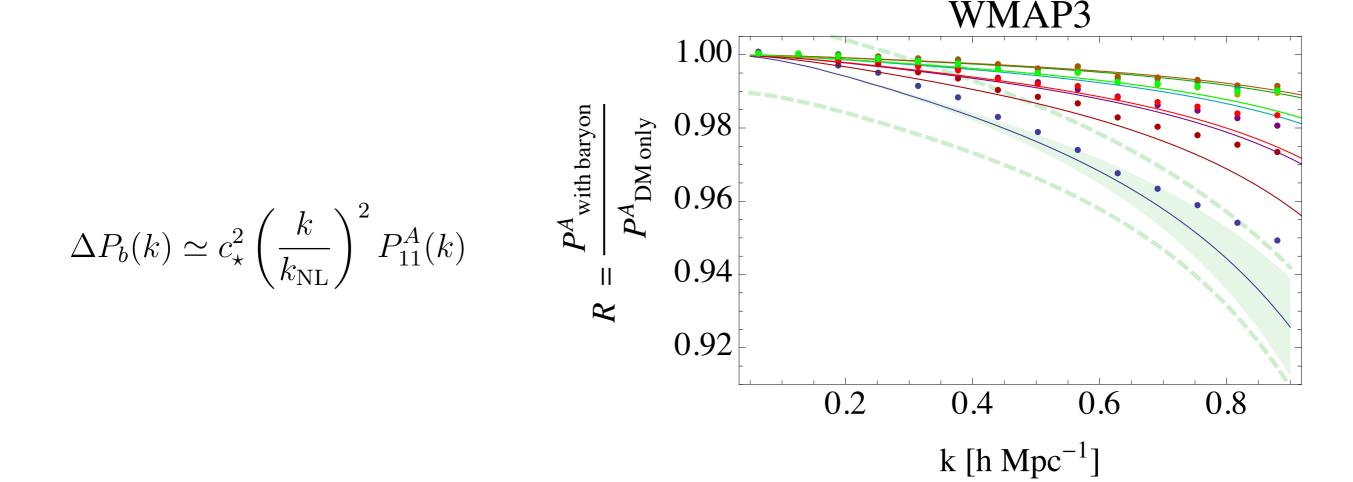


credit: Millenium Simulation, Springel *et al*. (2005)

• They cannot be reliably simulated due to large range of scales

Baryons

- Idea for EFT for dark matter:
 - Dark Matter moves $1/k_{\rm NL} \sim 10\,{\rm Mpc}$
 - \implies an effective fluid-like system with mean free path $\sim 1/k_{\rm NL}$
- Baryons heat due to star formation, but move the same:
 - Universe with CDM+Baryons ⇒ EFTofLSS with 2 specie



Baryons

• EFT Equations:

Continuity:
$$\dot{\rho}_{\sigma} + 3H\rho_{\sigma} + a^{-1}\partial_{i}\pi_{\sigma}^{i} = 0$$
,

Momentum:
$$\dot{\pi}_c^i + 4H\pi_c^i + a^{-1}\partial_j \left(\frac{\pi_c^i \pi_c^j}{\rho_c}\right) + a^{-1}\rho_c\partial_i \Phi = +a^{-1}\gamma^i - a^{-1}\partial_j \tau_c^{ij}$$
,

$$\dot{\pi}_b^i + 4H\pi_b^i + a^{-1}\partial_j \left(\frac{\pi_b^i \pi_b^j}{\rho_b}\right) + a^{-1}\rho_b \partial_i \Phi = -a^{-1}\gamma^i - a^{-1}\partial_j \tau_b^{ij} .$$

Baryons

• EFT Equations:

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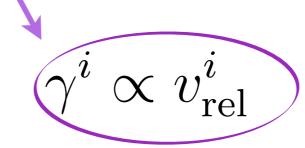
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$$\dot{\pi}_c^i + 4H\pi_c^i + a^{-1}\partial_j \left(\frac{\pi_c^i\pi_c^j}{\rho_c}\right) + a^{-1}\rho_c\partial_i\Phi = \left(+a^{-1}\gamma^i\right) - a^{-1}\partial_j\tau_c^{ij}$$

$$\dot{\pi}_b^i + 4H\pi_b^i + a^{-1}\partial_j \left(\frac{\pi_b^i \pi_b^j}{\rho_b}\right) + a^{-1}\rho_b \partial_i \Phi = (-a^{-1}\gamma^i) - a^{-1}\partial_j \tau_b^{ij} .$$

dynamical friction

effective force

Counterterms:



no derivative: marginal operator

A marginal operator

• Dynamical friction term is indeed needed for renormalization of the theory, i.e. it is generated.

• Dynamical friction is a relevant operator: i.e. it cannot be treated perturbatively: it is an essential part of the linear *equations*:

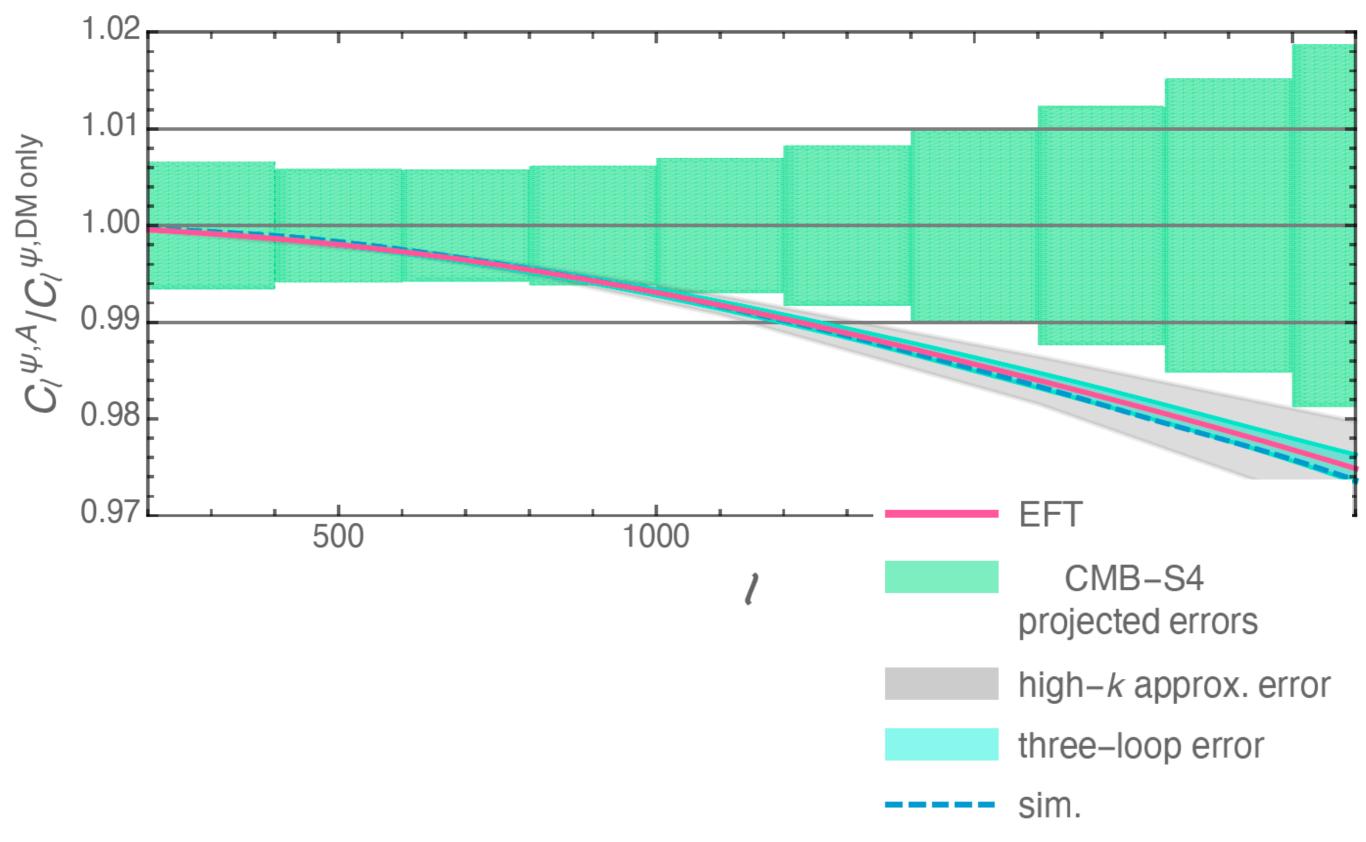
$$a^{2}\delta_{I}^{(1)"}(a,\vec{k}) + \left(2 + \frac{a\mathcal{H}'(a)}{\mathcal{H}(a)}\right)a\delta_{I}^{(1)"}(a,\vec{k}) = \int^{a} da_{1}g(a,a_{1})a_{1}\delta_{I}^{(1)"}(a_{1},\vec{k}) .$$

- - we can make some guesses

• Luckily: it only affect the decaying mode of the isocurvature, which is very very very very very small by the time this effect kicks in.

Predictions for CMB Lensing

• Baryon corrections are detectable in next CMB S-4 experiments. But we can predict it:



Bispectrum at one loop

with D'Amico, Donath, Lewandowski, Zhang 2206

Bispectrum

• The tree level bispectrum had been already used for cosmological parameter analysis in

with Guido D'Amico, Jerome Gleyzes,

Nickolas Kockron, Dida Markovic, Pierre Zhang, Florian Beutler, Hector Gill-Marin 1909

Philcox, Ivanov 2112

• ~10% improvement on A_s

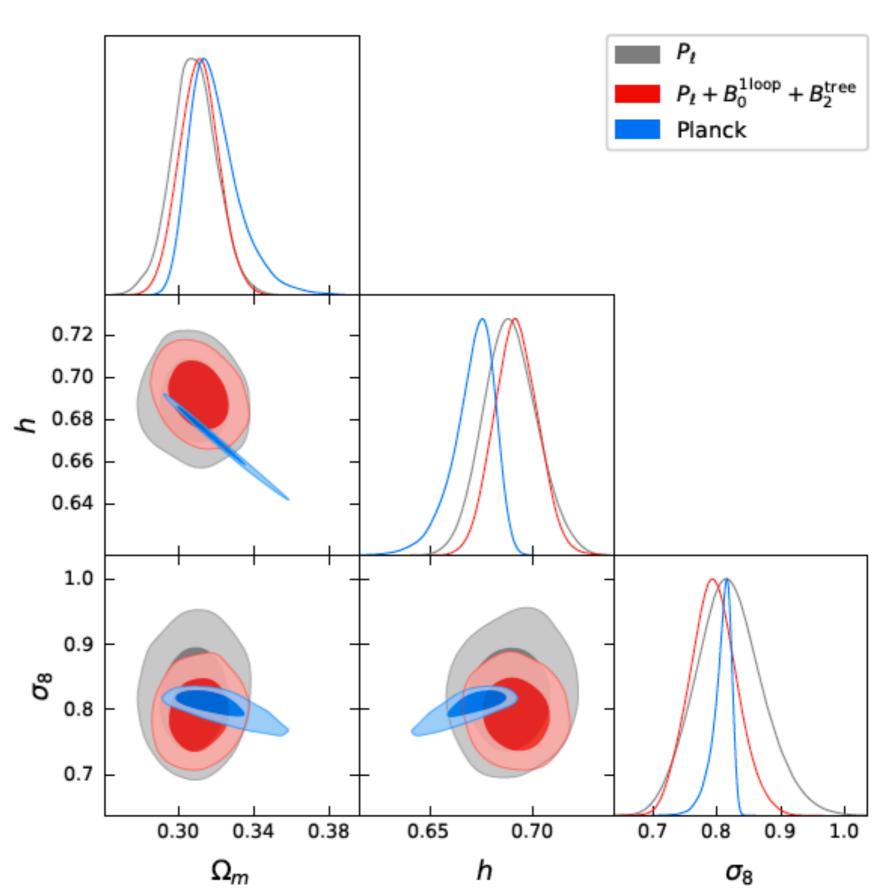
- Time to move to one-loop:
 - -Large effort:
 - data analysis with D'Amico, Donath, Lewandowski, Zhang 2206
 - theory model with D'Amico, Donath, Lewandowski, Zhang JCAP 2024
 - theory integration with Anastasiou, Braganca, Zheng JHEP 2024

Data Analysis ΛCDM

with D'Amico, Donath, Lewandowski, Zhang 2206

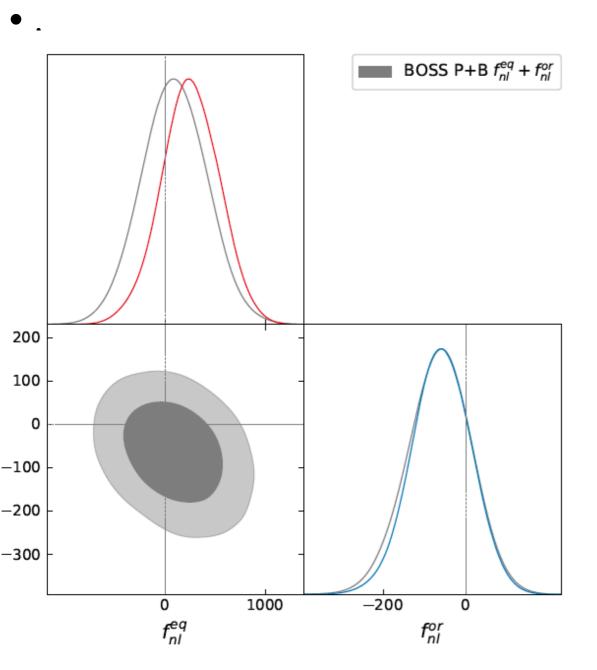
- Main result: ΛCDM
 - Improvements:
 - 30% on σ_8
 - 18% on h
 - 13% on Ω_m

- Compatible with Planck
 - -no tensions
- Often Planck Comparable



Data Analysis Non-Gaussianities

with D'Amico, Lewandowski, Zhang 2201



	BOSS	WMAP	Planck		
$f_{ m NL}^{ m equil.}$	245 ± 293	51 ± 136	-26 ± 47		
$f_{ m NL}^{ m orth.}$	-60 ± 72	-245 ± 100	-38 ± 24		
$f_{ m NL}^{ m ioc.}$	7 ± 31	37.2 ± 19.9	-0.9 ± 5.1		

see also contemporary Cabass, Ivanov, Simonovic, Zaldarriaga for only-tree-level analysis **2201**

$$S_{\pi} = \int d^4 \sqrt{-g} \left[\frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} \left(\dot{\pi}^2 - c_s^2 (\partial_i \pi)^2 \right) + \frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} \left(\dot{\pi} (\partial_i \pi)^2 \right) + \tilde{c}_s \left(\dot{\pi}^3 \right) \right]$$

Theory Model

• We add all the relevant biases (4th order) and counterterms (2nd order):

$$P_{11}^{r,h}[b_{1}], \quad P_{13}^{r,h}[b_{1},b_{3},b_{8}], \quad P_{22}^{r,h}[b_{1},b_{2},b_{5}],$$

$$B_{211}^{r,h}[b_{1},b_{2},b_{5}], \quad B_{321}^{r,h,(II)}[b_{1},b_{2},b_{3},b_{5},b_{8}], \quad B_{411}^{r,h}[b_{1},\dots,b_{11}],$$

$$B_{222}^{r,h}[b_{1},b_{2},b_{5}], \quad B_{321}^{r,h,(I)}[b_{1},b_{2},b_{3},b_{5},b_{6},b_{8},b_{10}],$$

$$P_{13}^{r,h,ct}[b_{1},c_{h,1},c_{\pi,1},c_{\pi v,1},c_{\pi v,3}], \quad P_{22}^{r,h,\epsilon}[c_{1}^{St},c_{2}^{St},c_{3}^{St}],$$

$$B_{321}^{r,h,(II),ct}[b_{1},b_{2},b_{5},c_{h,1},c_{\pi,1},c_{\pi v,1},c_{\pi v,3}], \quad B_{321}^{r,h,\epsilon,(I)}[b_{1},c_{1}^{St},c_{2}^{St},\{c_{i}^{St}\}_{i=4,\dots,13}],$$

$$B_{411}^{r,h,ct}[b_{1},\{c_{h,i}\}_{i=1,\dots,5},c_{\pi,1},c_{\pi,5},\{c_{\pi v,j}\}_{j=1,\dots,7}], \quad B_{222}^{r,h,\epsilon}[c_{1}^{(222)},c_{2}^{(222)},c_{5}^{(222)}].$$

- IR-resummation:
 - For the power spectrum, we use the correct and controlled IR-resummation.
 - For the bispectrum, we use an approximate method

Ivanov and Sibiryakov 2018

Derivation of theory model

with D'Amico, Donath, Lewandowski, Zhang **2211**

- Counterterms: major algebraic effort for 4th order and some theoretical subtle aspects.
- Renormalization of velocity
 - In the EFTofLSS, the velocity is a composite operator $v^i(x)=\frac{\pi^i(x)}{\rho(x)}$, so, it needs to be renormalized:

$$[v^i]_R = v^i + \mathcal{O}_v^i ,$$

• Under a diffeomorphisms:

$$v^i \to v^i + \chi^i \quad \Rightarrow \quad \mathcal{O}_v^i \text{ is a scalar}$$

• In redshift space, we have local product of velocities, which need to be renormalized but have non-trivial transformations under diff.s:

$$[v^i v^j]_R \to [v^i v^j]_R + [v^i]_R \chi^j + [v^j]_R \chi^i + \chi^i \chi^j$$

ullet To achieve this, one can do: (so must include products $v^i\cdot\mathcal{O}^i_v$)

$$[v^i v^j]_R = [v^i]_R [v^j]_R + \mathcal{O}_{v^2}^{ij}$$
, where $\mathcal{O}_{v^2}^{ij}$ is a scalar

- Counterterms: major algebraic effort for 4th order and some theoretical subtle aspects.
- Spatially non-locally-contributing counterterm:
 - This is a normal effect, just strange-looking in the EFTofLSS context.
 - Normally, counterterms are local, but, contributing through non-local Green's functions, they contribute non-locally.

Derivation of theory model

- Counterterms: major algebraic effort for 4th order and some theoretical subtle aspects.
- Spatially non-locally-contributing counterterm:
 - In the EFTofLSS, the Green's function is simple: $\frac{1}{\partial^2}$
 - Counterterms typically come with $\partial^2 \mathcal{O}_{local}$ \Rightarrow $\delta_{counter} \sim \frac{1}{\partial^2} \partial^2 \mathcal{O}_{local} \sim \mathcal{O}_{local}$
 - result almost trivial
 - But at second order, and for velocity fields, contracted along the line of sight, derivatives do not simplify, so we get

$$\delta_{\text{counter}}(\vec{x}) \sim \hat{z}^{i} \hat{z}^{j} \partial_{i} \pi_{(2)}^{j}(\vec{x}) \sim \hat{z}^{i} \hat{z}^{j} \frac{\partial_{i} \partial_{j} \partial_{k} \partial_{m}}{\partial^{2}} \mathcal{O}_{\text{local}}$$

$$\sim \hat{z}^{i} \hat{z}^{j} \frac{\partial_{i} \partial_{j} \partial_{k} \partial_{m}}{\partial^{2}} \left(\frac{\partial_{k} \partial_{l}}{H^{2}} \Phi(\vec{x}) \frac{\partial_{l} \partial_{m}}{H^{2}} \Phi(\vec{x}) \right)$$

• This is truly non-locally contributing, truly non-trivial.

• We check that all these terms are needed and sufficient for renormalization

Evaluational/Computational Challenge

with Anastasiou, Braganca, Zheng 2212

The best approach so far

Simonovic, Baldauf, Zaldarriaga, Carrasco, Kollmeier **2018**

- Nice trick for fast evaluation of the loops integrals
- The power spectrum is a numerically computed function
- Decompose linear power spectrum

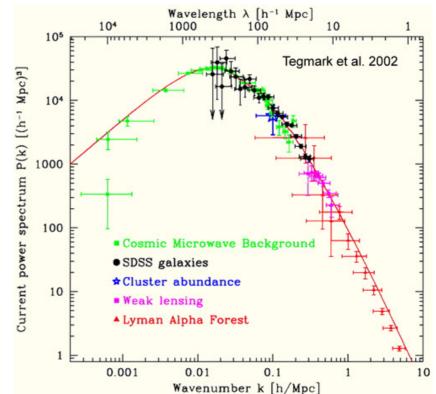
$$P_{11}(k) = \sum_{n} c_n k^{\mu + i\alpha n}$$

• Loop can be evaluated analytically

$$P_{1-\text{loop}}(k) = \int_{\vec{q}} K(\vec{q}, \vec{k}) P_{11}(k - q) P_{11}(q) =$$

$$= \sum_{n_1, n_2} c_{n_1} c_{n_2} \left(\int_{\vec{q}} K(\vec{q}, \vec{k}) k^{\mu + i\alpha n_1} k^{\mu + i\alpha n_2} \right) = \sum_{n_1, n_2} c_{n_1} c_{n_2} M_{n_1, n_2}(k)$$

- -using quantum field theory techniques
- $M_{n_1n_2}$ is cosmology independent \Rightarrow so computed once



• Two difficulties:

$$P_{1-\text{loop}}(k) = \int_{\vec{q}} K(\vec{q}, \vec{k}) P_{11}(k - q) P_{11}(q) =$$

$$= \sum_{n_1, n_2} c_{n_1} c_{n_2} \left(\int_{\vec{q}} K(\vec{q}, \vec{k}) k^{\mu + i\alpha n_1} k^{\mu + i\alpha n_2} \right) = \sum_{n_1, n_2} c_{n_1} c_{n_2} M_{n_1, n_2}(k)$$

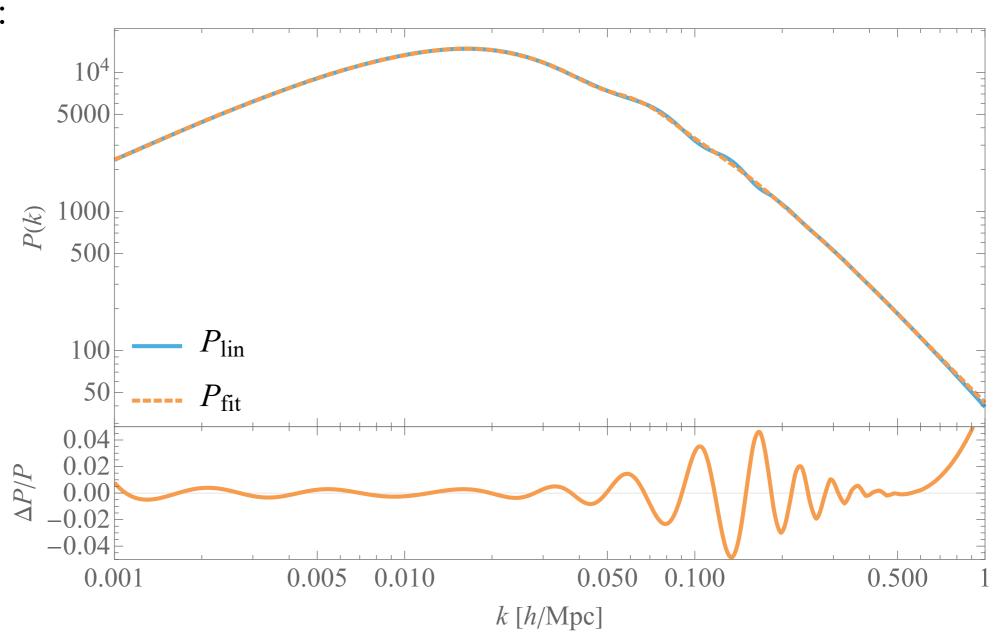
- integrals are complicated due to fractional, complex exponents
- many functions needed, the matrix $M_{n_1n_2n_3}$ for bispectrum is about 50Gb, so, ~impossible to load on CPU for data analysis

• In order to ameliorate (solve) these issues, we use a different basis of functions.

• Use as basis:

$$f(k^2, k_{\text{peak}}^2, k_{\text{UV}}^2, i, j) \equiv \frac{\left(k^2/k_0^2\right)^i}{\left(1 + \frac{(k^2 - k_{\text{peak}}^2)^2}{k_{\text{UV}}^4}\right)^j},$$

• With just 16 functions:



• This basis is equivalent to massive propagators to integer powers

$$\frac{1}{\left(1 + \frac{(k^2 - k_{\text{peak}}^2)^2}{k_{\text{UV}}^4}\right)^j} = \frac{k_{\text{UV}}^{4j}}{\left(k^2 - k_{\text{peak}}^2 - i k_{\text{UV}}^2\right)^j \left(k^2 - k_{\text{peak}}^2 + i k_{\text{UV}}^2\right)^j},$$

$$\frac{k_{\text{UV}}^2}{\left(k^2 - k_{\text{peak}}^2 - i\,k_{\text{UV}}^2\right)\left(k^2 - k_{\text{peak}}^2 + i\,k_{\text{UV}}^2\right)} = -\frac{i/2}{k^2 - k_{\text{peak}}^2 - i\,k_{\text{UV}}^2} + \frac{i/2}{k^2 - k_{\text{peak}}^2 + i\,k_{\text{UV}}^2}$$

• So, each basis function:

$$f(k^2, k_{\text{peak}}^2, k_{\text{UV}}^2, i, j) = \sum_{n=1}^{j} k_{\text{UV}}^{2(n-i)} k^{2i} \left(\frac{\kappa_n}{(k^2 + M)^n} + \frac{\kappa_n^*}{(k^2 + M^*)^n} \right)$$

• This basis is equivalent to massive propagators to integer powers

$$\frac{1}{\left(1 + \frac{(k^2 - k_{\text{peak}}^2)^2}{k_{\text{UV}}^4}\right)^j} = \frac{k_{\text{UV}}^{4j}}{\left(k^2 - k_{\text{peak}}^2 - i k_{\text{UV}}^2\right)^j \left(k^2 - k_{\text{peak}}^2 + i k_{\text{UV}}^2\right)^j}, \\
\frac{k_{\text{UV}}^2}{\left(k^2 - k_{\text{peak}}^2 - i k_{\text{UV}}^2\right) \left(k^2 - k_{\text{peak}}^2 + i k_{\text{UV}}^2\right)} = \frac{i/2}{k^2 - k_{\text{peak}}^2 - i k_{\text{UV}}^2} + \frac{i/2}{k^2 - k_{\text{peak}}^2 + i k_{\text{UV}}^2}$$

Complex-Mass propagator

• So, each basis function:

$$f(k^2, k_{\text{peak}}^2, k_{\text{UV}}^2, i, j) = \sum_{n=1}^{j} k_{\text{UV}}^{2(n-i)} k^{2i} \left(\frac{\kappa_n}{(k^2 + M)^n} + \frac{\kappa_n^*}{(k^2 + M^*)^n} \right)$$

• We end up with integral like this:

$$L(n_1, d_1, n_2, d_2, n_3, d_3) = \int_q \frac{(\mathbf{k}_1 - \mathbf{q})^{2n_1} \mathbf{q}^{2n_2} (\mathbf{k}_2 + \mathbf{q})^{2n_3}}{((\mathbf{k}_1 - \mathbf{q})^2 + M_1)^{d_1} (\mathbf{q}^2 + M_2)^{d_2} ((\mathbf{k}_2 + \mathbf{q})^2 + M_3)^{d_3}}$$

- with integer exponents.
- First we manipulate the numerator to reduce to:

$$T(d_1, d_2, d_3) = \int_q \frac{1}{((\mathbf{k}_1 - \mathbf{q})^2 + M_1)^{d_1} (\mathbf{q}^2 + M_2)^{d_2} ((\mathbf{k}_2 + \mathbf{q})^2 + M_3)^{d_3}},$$

• Then, by integration by parts, we find (i.e. QCD teaches us how to) recursion relations

$$\int_{q} \frac{\partial}{\partial q_{\mu}} \cdot (q_{\mu}t(d_1, d_2, d_3)) = 0$$

$$\Rightarrow (3 - d_{1223})\hat{0} + d_1k_{1s}\widehat{1^+} + d_3(k_{2s})\widehat{3^+} + 2M_2d_2\widehat{2^+} - d_1\widehat{1^+}\widehat{2^-} - d_3\widehat{2^-}\widehat{3^+} = 0$$

• relating same integrals with raised or lowered the exponents (easy terminate due to integer exponents).

- We end up to three master integrals:
- Tadpole:

$$Tad(M_j, n, d) = \int \frac{d^3 \mathbf{q}}{\pi^{3/2}} \frac{(\mathbf{p}_i^2)^n}{(\mathbf{p}_i^2 + M_i)^d}$$

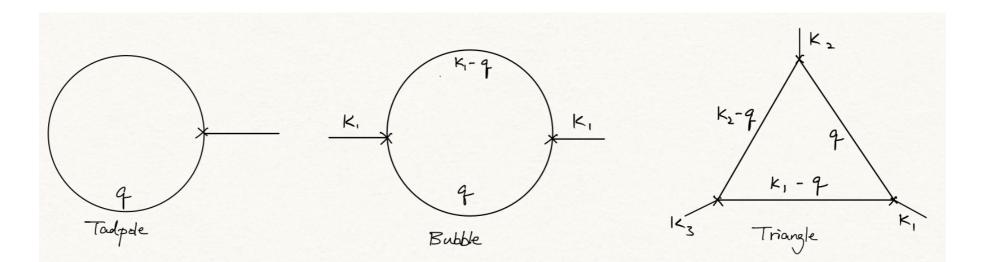
• Bubble:

$$B_{\text{master}}(k^2, M_1, M_2) = \int \frac{d^3 \mathbf{q}}{\pi^{3/2}} \frac{1}{(q^2 + M_1)(|\mathbf{k} - \mathbf{q}|^2 + M_2)}$$

• Triangle:

$$T_{\text{master}}(k_1^2, k_2^2, k_3^2, M_1, M_2, M_3) =$$

$$\int \frac{d^3\mathbf{q}}{\pi^{3/2}} \frac{1}{(q^2 + M_1)(|\mathbf{k}_1 - \mathbf{q}|^2 + M_2)(|\mathbf{k}_2 + \mathbf{q}|^2 + M_3)},$$



- The master integrals are evaluated with Feynman parameters, but with great care of branch cut crossing, which happens because of complex masses.
- Bubble Master:

$$B_{\text{master}}(k^2, M_1, M_2) = \frac{\sqrt{\pi}}{k} i [\log (A(1, m_1, m_2)) - \log (A(0, m_1, m_2)) - 2\pi i H (\text{Im } A(1, m_1, m_2)) H (-\text{Im } A(0, m_1, m_2))],$$

$$A(0, m_1, m_2) = 2\sqrt{m_2} + i(m_1 - m_2 + 1),$$

$$A(1, m_1, m_2) = 2\sqrt{m_1} + i(m_1 - m_2 - 1),$$

$$m_1 = M_1/k^2 \text{ and } m_2 = M_2/k^2$$

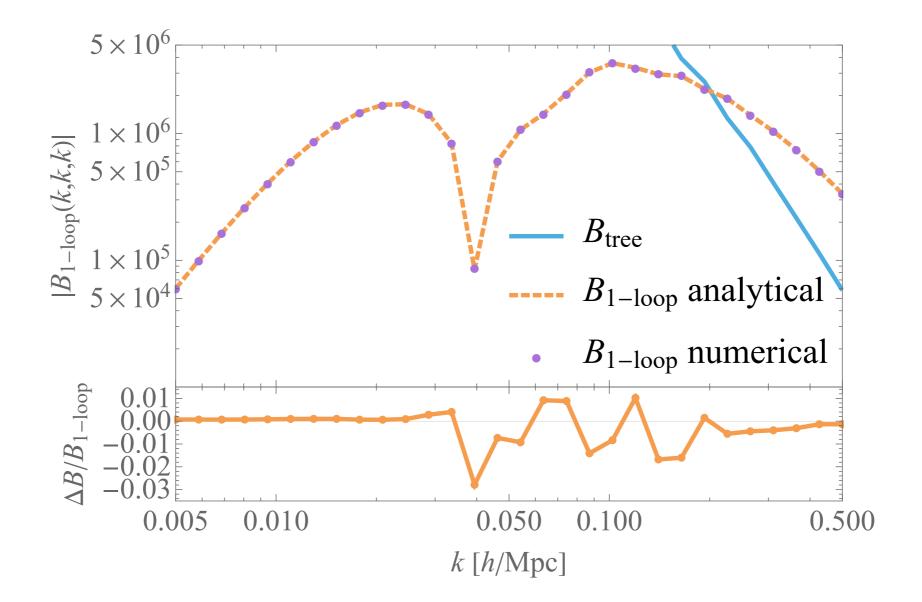
• Triangle Master:

Friangle Master:
$$F_{\text{int}}(R_2, z_+, z_-, x_0) = s(z_+, -z_-) \frac{\sqrt{\pi}}{\sqrt{|R_2|}} \left. \frac{\arctan\left(\frac{\sqrt{z_+ - x}\sqrt{x_0 - z_-}}{\sqrt{x_0 - z_+}\sqrt{x_0 - z_-}}\right)}{\sqrt{x_0 - z_+}\sqrt{x_0 - z_-}} \right|_{x=0}^{x=1}.$$

• Very simple expressions with simple rule for branch cut crossing.

Result of Evaluation

- All automatically coded up.
- For BOSS analysis, evaluation of matrix is 2.5CPU hours and 800 Mb storage, very fast matrix contractions.
- Accuracy with 16 functions:



Back to data-analysis: Pipeline Validation

Scale cut from NNLO

• We can estimate the $k_{\rm max}$ without the use of simulations, by adding NNLO terms, and seeing when they make a difference on the posteriors.

$$P_{\text{NNLO}}(k,\mu) = \frac{1}{4} c_{r,4} b_1^2 \mu^4 \frac{k^4}{k_{\text{NL,R}}^4} P_{11}(k) + \frac{1}{4} c_{r,6} b_1 \mu^6 \frac{k^4}{k_{\text{NL,R}}^4} P_{11}(k) ,$$

$$B_{\text{NNLO}}(k_1, k_2, k_3, \mu, \phi) = 2 c_{\text{NNLO},1} K_2^{r,h}(\vec{k}_1, \vec{k}_2; \hat{z}) K_1^{r,h}(\vec{k}_2; \hat{z}) f \mu_1^2 \frac{k_1^4}{k_{\text{NL,R}}^4} P_{11}(k_1) P_{11}(k_2)$$

$$+ c_{\text{NNLO},2} K_1^{r,h}(\vec{k}_1; \hat{z}) K_1^{r,h}(\vec{k}_2; \hat{z}) P_{11}(k_1) P_{11}(k_2) f \mu_3 k_3 \frac{(k_1^2 + k_2^2)}{4k_1^2 k_2^2 k_{\text{NL,R}}^4} \Big[-2 \vec{k}_1 \cdot \vec{k}_2 (k_1^3 \mu_1 + k_2^3 \mu_2) + 2 f \mu_1 \mu_2 \mu_3 k_1 k_2 k_3 (k_1^2 + k_2^2) \Big] + \text{perm.} ,$$

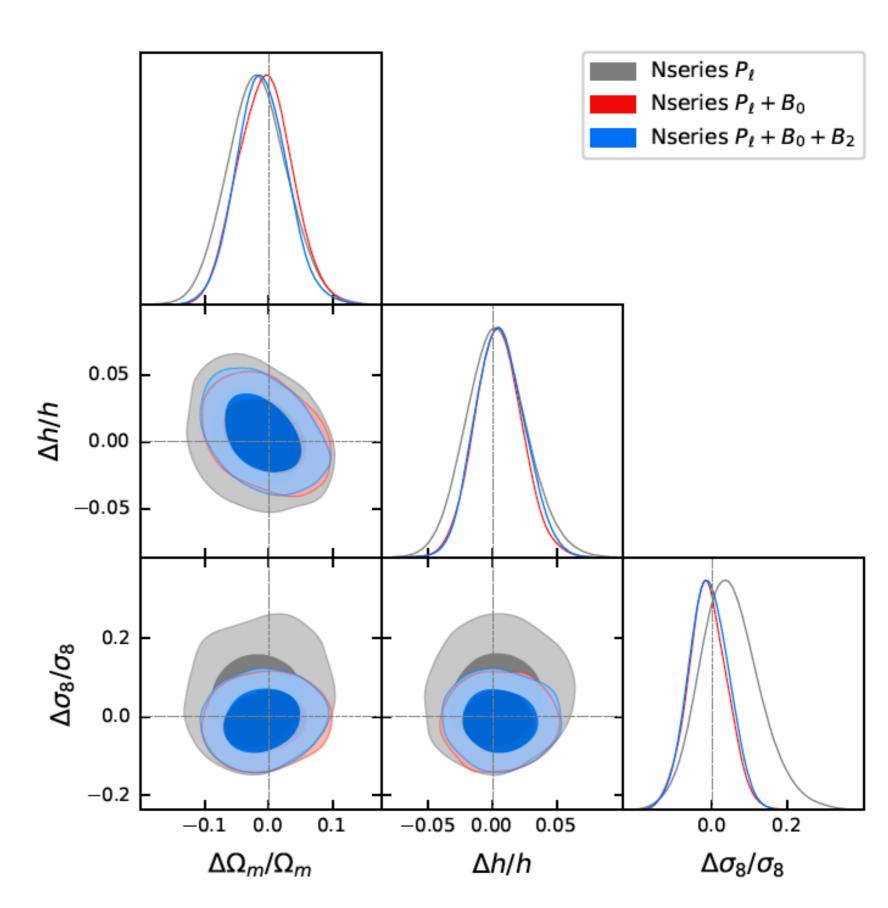
$$(4)$$

• For our k_{max} , we find the following shifts, which are ok:

$\Delta_{ m shift}/\sigma_{ m stat}$	Ω_m	h	σ_8	ω_{cdm}	$\ln(10^{10}A_s)$	S_8
$P_{\ell} + B_0$: base - w/ NNLO	-0.03	-0.09	-0.03	-0.1	0.05	-0.04

Scale-cut from simulations

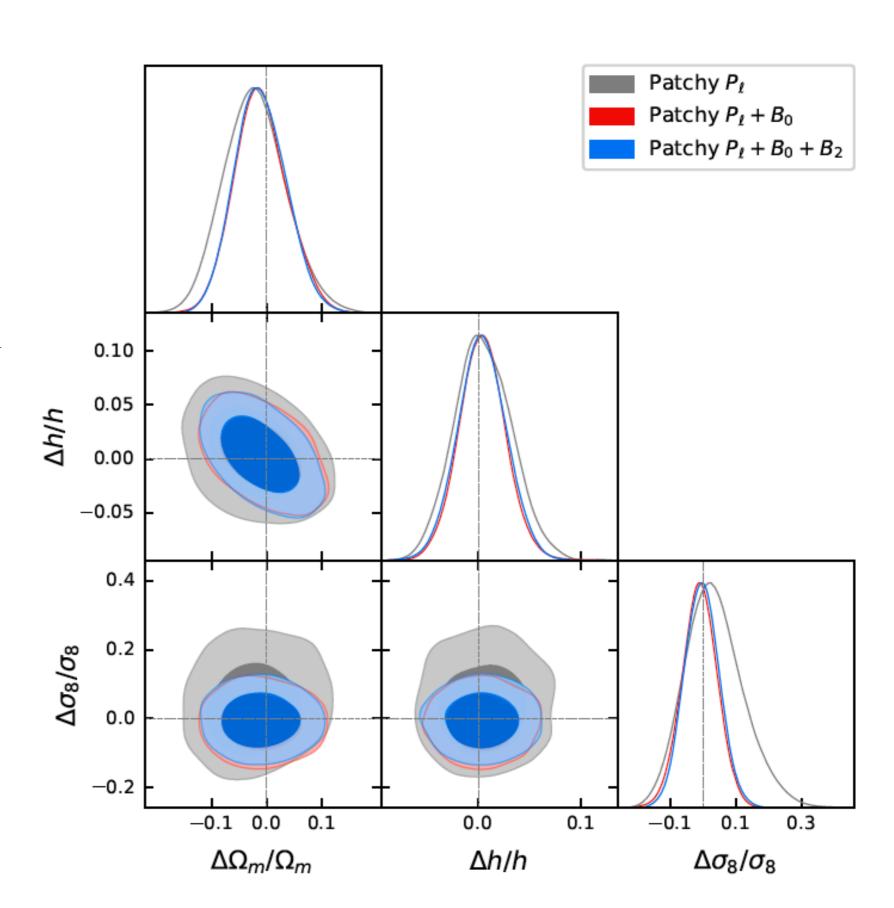
- N-series
 - Volume ~80 BOSS
 - \bullet safely within $\sigma_{\mathrm{data}}/3$
- After phase-space correction



Scale-cut from simulations

- Patchy:
 - Volume ~2000 BOSS
 - safely within $\sigma_{\rm data}/3$

• After phase-space correction



BOSS data

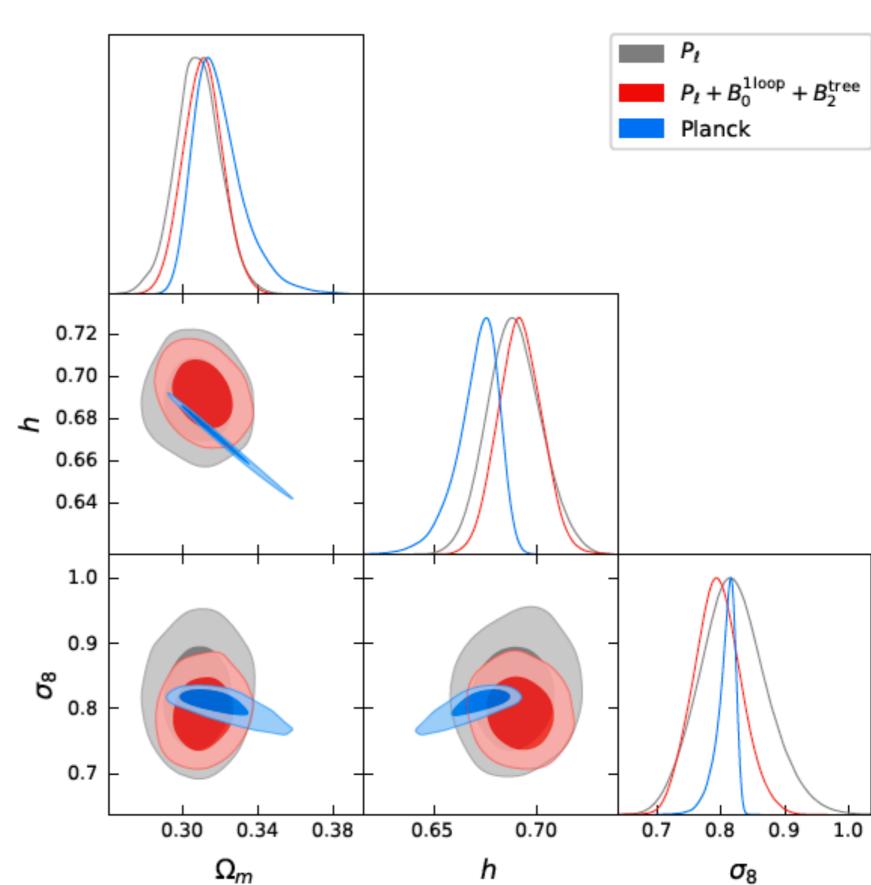
Data Analysis ΛCDM

with D'Amico, Donath, Lewandowski, Zhang 2206

- Main result: ΛCDM
 - Improvements:
 - 30% on σ_8
 - 18% on h
 - 13% on Ω_m

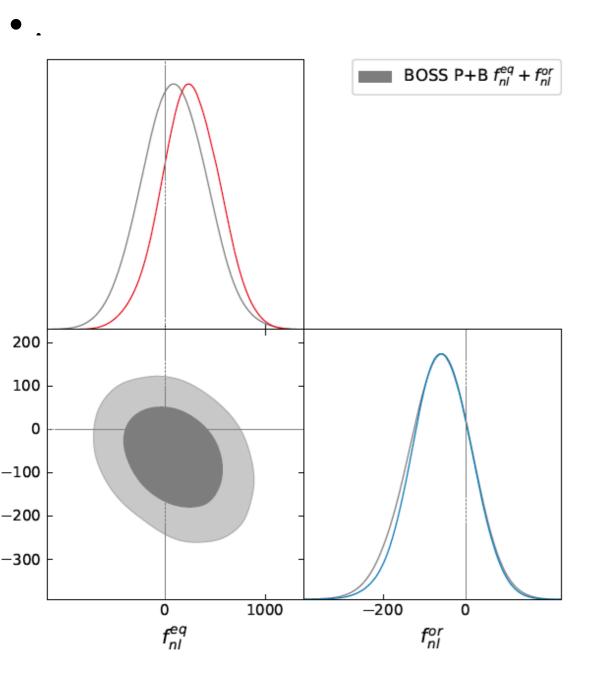
Compatible with Planck–no tensions

Remarkable consistencyof observables



Data Analysis Non-Gaussianities

with D'Amico, Lewandowski, Zhang 2201



	BOSS	WMAP	Planck
$f_{ m NL}^{ m equil.}$	245 ± 293	51 ± 136	-26 ± 47
$f_{ m NL}^{ m orth.}$	-60 ± 72	-245 ± 100	-38 ± 24
$f_{ m NL}^{ m loc.}$	7 ± 31	37.2 ± 19.9	-0.9 ± 5.1

$$S_{\pi} = \int d^4 \sqrt{-g} \left[\frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} \left(\dot{\pi}^2 - c_s^2 (\partial_i \pi)^2 \right) + \frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} \left[\dot{\pi} (\partial_i \pi)^2 + \tilde{c}_s (\dot{\pi}^3) \right] \right]$$

Comment on Large non-Gaussianities

with Donath in progress

- Emerged that we can continue probing large non-Gaussianities. thanks to LSS
- Are they viable?
- Large non-Gaussianities means that breaking of Lorentz invariance is strong: inflationary solution is non-perturbatively far from the Lorentz invariant vacuum.
 - Slow-roll inflation is when the solution is close. $(\partial \phi)^2 \perp$

$$(\partial \phi)^2 + \frac{(\partial \phi)^4}{\Lambda^4}$$

- Explains why hard to find solutions with large non-Gaussianities.
 - -~ as discovering liquid Helium out of the standard model Lagrangian

source Wikipedia



- -Easier to discover the EFT for the fluctuations (and indeed this is the EFTofI)
- To have $S_{\pi} = \int d^{4}\sqrt{-g} \left[\frac{\dot{H}M_{\mathrm{Pl}}^{2}}{c_{s}^{2}} \left(\dot{\pi}^{2} c_{s}^{2}(\partial_{i}\pi)^{2} \right) + \frac{\dot{H}M_{\mathrm{Pl}}^{2}}{c_{s}^{2}} \left[\dot{\pi}(\partial_{i}\pi)^{2} + \tilde{c}_{3} \, \dot{\pi}^{3} \right] \right]$ $\boldsymbol{\varphi} = \int d^{4}\sqrt{-g} \left[\frac{\dot{H}M_{\mathrm{Pl}}^{2}}{c_{s}^{2}} \left(\dot{\pi}^{2} c_{s}^{2}(\partial_{i}\pi)^{2} \right) + \frac{\dot{H}M_{\mathrm{Pl}}^{2}}{c_{s}^{2}} \left[\dot{\pi}(\partial_{i}\pi)^{2} + \tilde{c}_{3} \, \dot{\pi}^{3} \right] \right]$

$$f_{\rm NL}^{\rm equil}, f_{\rm NL}^{\rm orthog} \gtrsim 1 \quad \Leftrightarrow \quad (\Lambda_{\rm cutoff}^{\rm EFT})^4 \lesssim \dot{H} M_{\rm Pl}^2$$

Comment on Large non-Gaussianities

with Donath in progress

- Is it so hard?
 - -At field theory level, there are two models that can derive the inflationary solution out of the Lorentz invariant vacuum:
 - slow roll inflation $(\partial \phi)^2 + \frac{(\partial \phi)}{\Lambda^4}$
 - DBI inflation

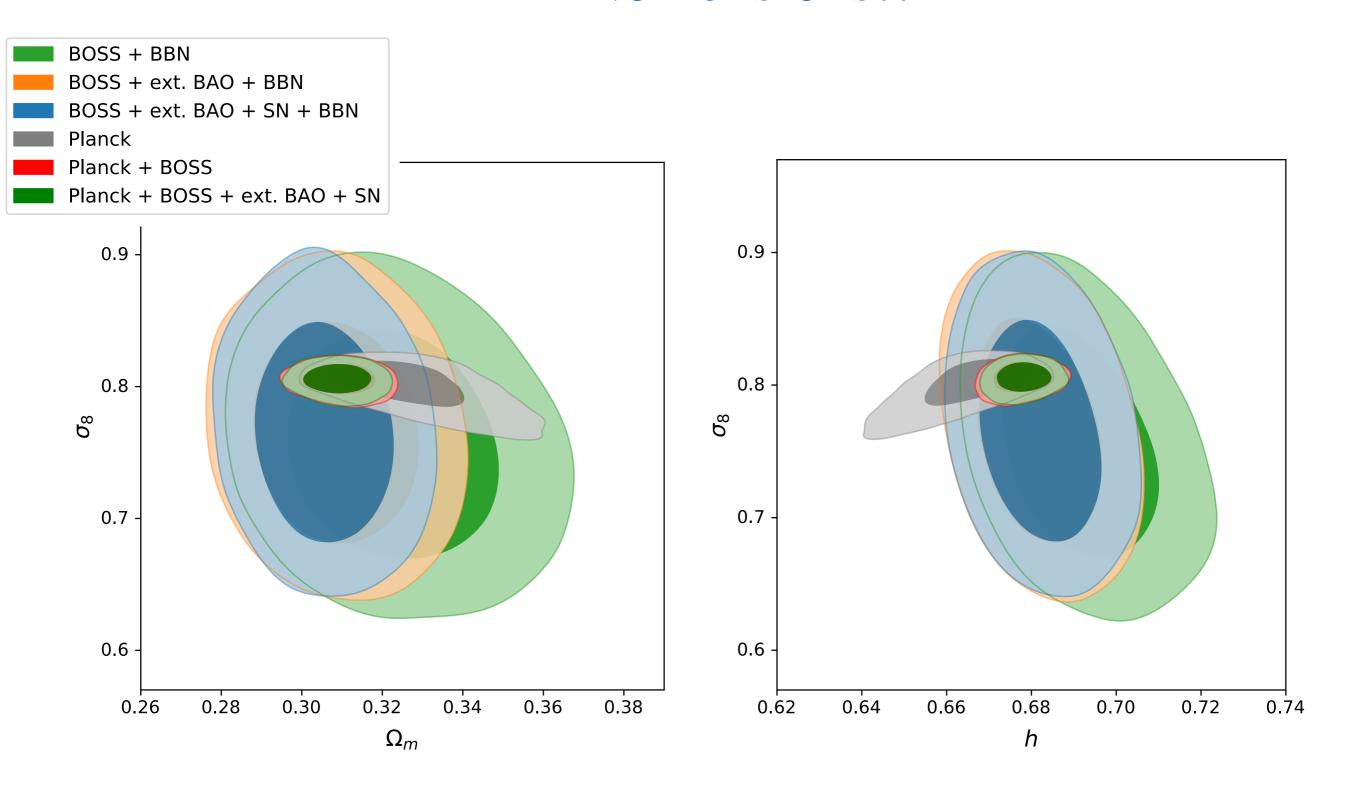
$$\sqrt{1 - \frac{(\partial \phi)^2}{\Lambda^4}}$$

- At string-theory level
 - unclear if one is better than the other

- Summary: I do not currently see any theoretical prejudice towards the fact that inflation should have small non-Gaussianities
 - -as much as I have no theoretical prejudice against the existence on liquid helium, though it is harder to find.

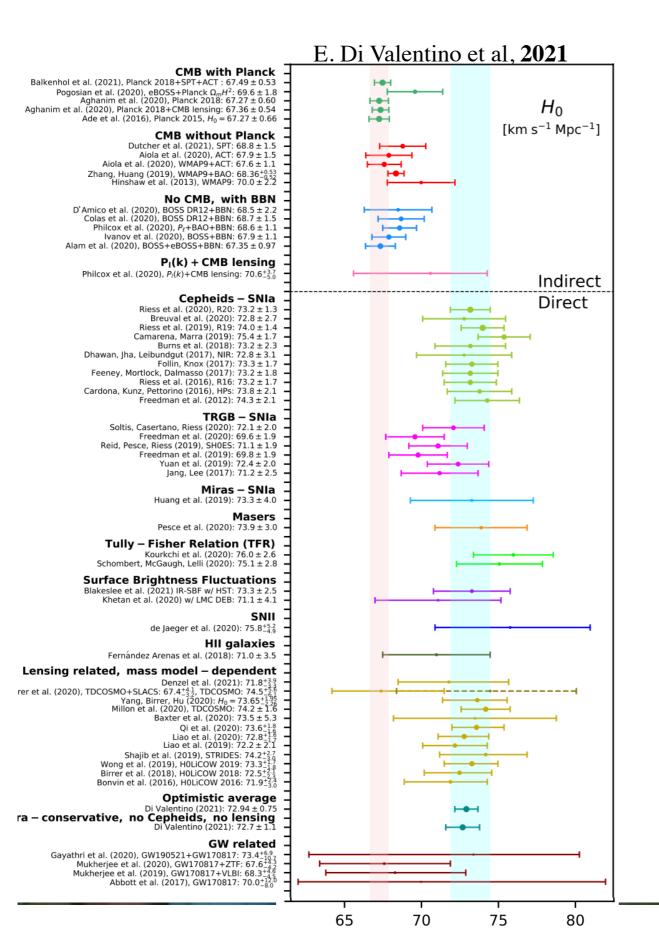
No tensions?!

No Tensions!!



with Pierre Zhang, Guido D'Amico, Cheng Zhao, Yifu Can 2110

The Hubble Tension as of yesterday



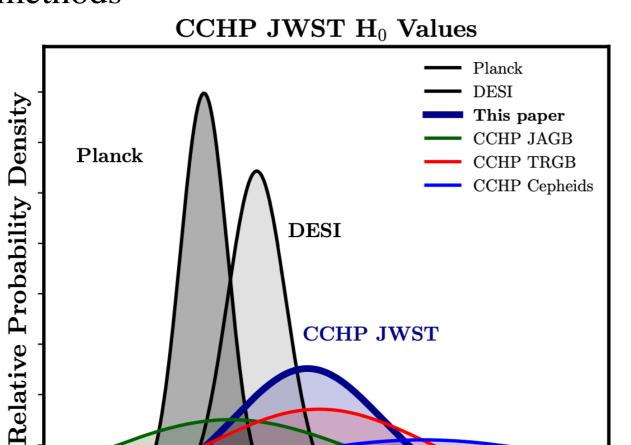


JWST sheds light

• 3 methods W. Freedman et al, 2024

74

76



70

 \mathbf{H}_0

72

• Most important:

64

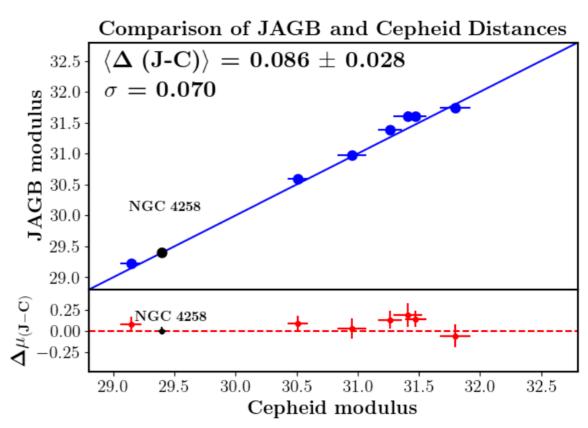
• Cepheids are systematically offset

68

• wrt JAGB

66

-I do find Riess et al, 2024 addresses this



• To me, they should address/decide on these systematics.

Direct Measurement of formation time of galaxies

with Donath and Lewandowski 2307

Galaxies in the EFTofLSS

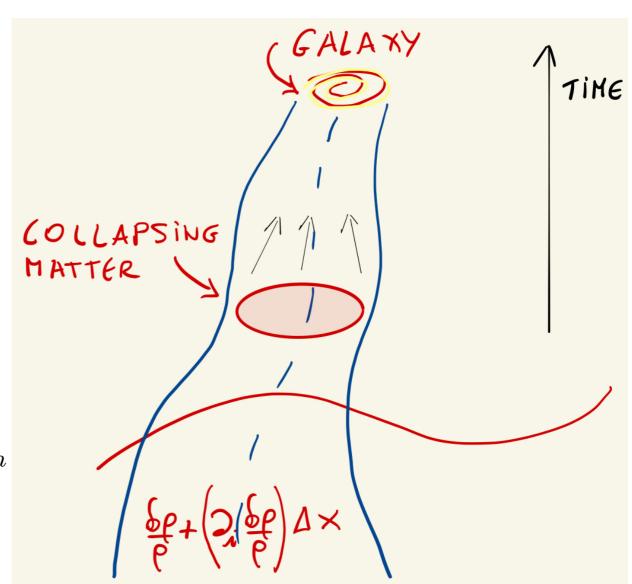
Senatore 1406 Mirbabayi et al. 1412

$$n_{\rm gal}(x) = f_{\rm very\ complicated}\left(\left\{H, \Omega_m, \dots, m_e, g_{ew}, \dots, \rho(x)\right\}_{\rm past\ light\ cone}\right)$$



$$\left(\frac{\delta n}{n}\right)_{\text{gal},\ell}(x) \sim \int^t dt' \left[c(t,t') \left(\frac{\delta \rho}{\rho}\right)(\vec{x}_{\text{fl}},t') + \ldots\right]$$

- all terms allowed by symmetries
- all physical effects included
 - −e.g. assembly bias
- $\left\langle \left(\frac{\delta n}{n}\right)_{\text{gal},\ell}(x)\left(\frac{\delta n}{n}\right)_{\text{gal},\ell}(y)\right\rangle =$ $= \sum \operatorname{Coeff}_n \cdot \langle \operatorname{matter correlation function} \rangle_n$



Consequences of non-locality in time

• Mathematics again:

• non-local in time:

$$\delta_g^{(n)}(\vec{x}, t) = \sum_{\mathcal{O}_m} \int_0^t dt' H(t') c_{\mathcal{O}_m}(t, t') \times \left[\mathcal{O}_m(\vec{x}_{fl}(\vec{x}, t, t'), t') \right]^{(n)},$$

$$\mathcal{O}_{m=3} \supset \delta^2 \theta, \delta^3, \dots$$

• local in time:

$$\delta_{g,\text{loc}}^{(n)}(\vec{x},t) = \sum_{\mathcal{O}_m} c_{\mathcal{O}_m}(t) \, \mathcal{O}_m^{(n)}(\vec{x},t) ,$$

Consequences of non-locality in time

• This means that one *does not* get the same terms as in the local-in-time expansion

- If we could measure one of these terms, we could *measure* that Galaxies take an Hubble time to form. We have never measured this: we take pictures of different galaxies at different stages of their evolution. But we have never *seen* a galaxy form in an Hubble time.
 - -This would be the first direct evidence that the universe lasted an Hubble time.

• So, detecting a non-local-in-time bias would allow us to measure that, and from the size, the formation time. Unfortunately, so far, not yet.

Consequences of non-locality in time

$$\delta_{g,\text{loc}}^{(n)}(\vec{x},t) = \sum_{\mathcal{O}_m} c_{\mathcal{O}_m}(t) \, \mathcal{O}_m^{(n)}(\vec{x},t) \;, \qquad \delta_g^{(n)}(\vec{x},t) = \sum_{\mathcal{O}_m} \sum_{\alpha=1}^{n-m+1} c_{\mathcal{O}_m,\alpha}(t) \, \mathbb{C}_{\mathcal{O}_m,\alpha}^{(n)}(\vec{x},t)$$

- it turns out that up to 4th order, the two basis of operators were identical.
- but at 5th order they are not!
 - out of 29 independent operators, 3 cannot be written as local in time ones.
- \Rightarrow By looking at, eg,

$$\langle \delta_{g_1}^{(5)}(\vec{x}_1) \delta_{g_2}^{(1)}(\vec{x}_2) \delta_{g_3}^{(1)}(\vec{x}_3) \delta_{g_4}^{(1)}(\vec{x}_4) \delta_{g_5}^{(1)}(\vec{x}_5) \delta_{g_6}^{(1)}(\vec{x}_6) \rangle$$

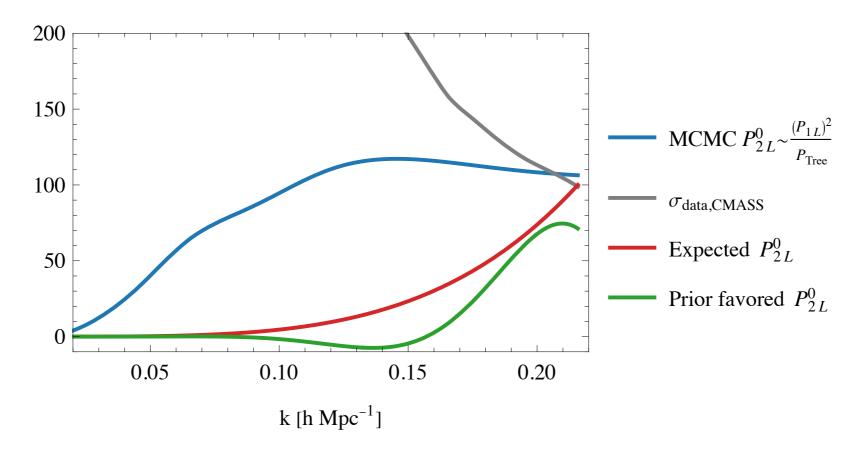
- we can detect these biases, and, from their size, determine:
 - -the order of magnitude of the formation time of galaxies
 - -direct evidence that the universe lasted 13 Billion years

Peeking into the next Decade

with Donath, Bracanga and Zheng 2307

Next Decade

- After validating our technique against the MCMC's on BOSS data, we Fisher forecast for DESI and Megamapper
- Prediction of one-loop Power Spectrum and Bispectrum
- Here, and in the NG analysis, introduce a `perturbativity prior': impose expected size and scaling of loop



• Also a `galaxy formation prior', 0.3 in each EFT-parameter

0.66 0.67 0.68 1.0 1.2 1.4 2 0 2 -400 0 400 0.66 0.67 1.0 1.1 1.2 -1 0 1 $\log(b_1)$ c_2 c_4 $\log(b_1)$ c_2 c_4

Results: Non-Gaussianities

with Donath, Bracanga and Zheng 2307

BOSS: $\sigma(\cdot)$	$f_{ m NL}^{ m loc.}$	$f_{ m NL}^{ m eq.}$	$f_{ m NL}^{ m orth.}$
$P+B_{\mathrm{Tree}}$	37	357	142
P+B	23	253	67
P+B+p.p.	17	228	62
P+B+p.p.+g.p.	15	163	49

DESI: $\sigma(\cdot)$	$f_{ m NL}^{ m loc.}$	$f_{ m NL}^{ m eq.}$	$f_{ m NL}^{ m orth.}$
$P+B_{\mathrm{Tree}}$	3.61	142	71.5
P+B	3.46	114	30.2
P+B+p.p.	3.26	91.5	27.0
P+B+p.p.+g.p.	3.19	77.0	21.8

MMo: $\sigma(\cdot)$	$f_{ m NL}^{ m loc.}$	$f_{ m NL}^{ m eq.}$	$f_{ m NL}^{ m orth.}$
$P+B_{\mathrm{Tree}}$	0.29	23.4	8.7
P+B	0.27	17.7	4.6
P + B + p.p.	0.26	16.0	4.2
P+B+p.p.+g.p.	0.26	12.6	3.4

10

with Donath in progress

• Just using perturbativity prior, potentially a factor of 20, 5, 6 over Planck!!

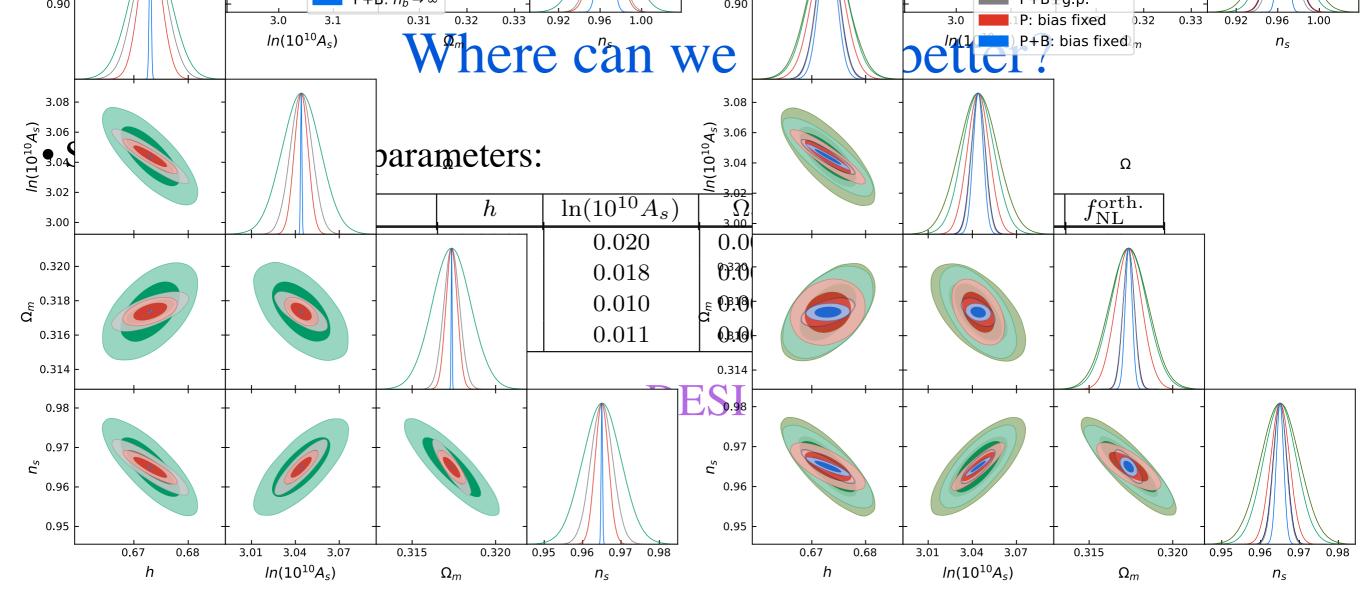
Results: Curvature and Neutrinos

DESI: $\sigma(\cdot)$	h	$\ln(10^{10}A_s)$	Ω_m	n_s	Ω_k
P+B	0.004	0.035	0.002	0.01/1	0.013
P + B + p.p.	0.004	0.032	0.002	0.008	0.012
P+B+p.p.+g.p.	0.004	0.025	0.002	0.007	0.009

	, ,	Δl_m	$\mid n_s \mid$	Ω_k
P+B 0.002	0.0052	0.0003	0.002	0.0015
P + B + p.p. 0.002	0.0046	0.0003	0.002	0.0012
P+B+p.p.+g.p. 0.002	0.0044	0.0003	0.001	0.0011

- Just using perturbativity prior, potentially factor of 5 over Planck!
 - Important for the landscape of string theory.
- Neutrinos: guaranteed evidence/detection:

 2σ DESI, 14σ MegaMapper



Ω

$\sigma(\cdot)$	h	$\ln(10^{10}A_s)$	Ω_m	n_s	$f_{ m NL}^{ m loc.}$	$f_{ m NL}^{ m eq.}$	$f_{ m NL}^{ m orth.}$
P+B	0.0021	0.0047	0.00034	0.0017	0.27	18	4.6
P+B+g.p.:	0.0020	0.0045	0.00033	0.016	0.26	13	3.6
P+B: bias fixed	0.0016	0.0034	0.00021	0.0010	0.17	3.6	1.7
$P+B:n_b\to\infty$	0.00019	0.00045	0.000029	0.00017	0.11	5.4	1.5

Ω

MegaMapper

Summary

- After the initial, successful, application to BOSS data:
 - -measurement of cosmological parameters
 - -new method to measure Hubble
 - -perhaps fixing tensions
- the EFTofLSS is starting to look ahead to
 - -higher-order and higher-n point functions
 - -enlightening what next surveys could do, and how to design them
 - an eye to BSM: primordial non-Gaussianities, neutrinos, curvature, etc..
 - -learning about some astrophysics, qualitative facts on the universe