

MAX-PLANCK-INSTITUT
FÜR PHYSIK



Recent results for LHC simulations matched with Parton Shower using MiNNLOPS

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LHC event

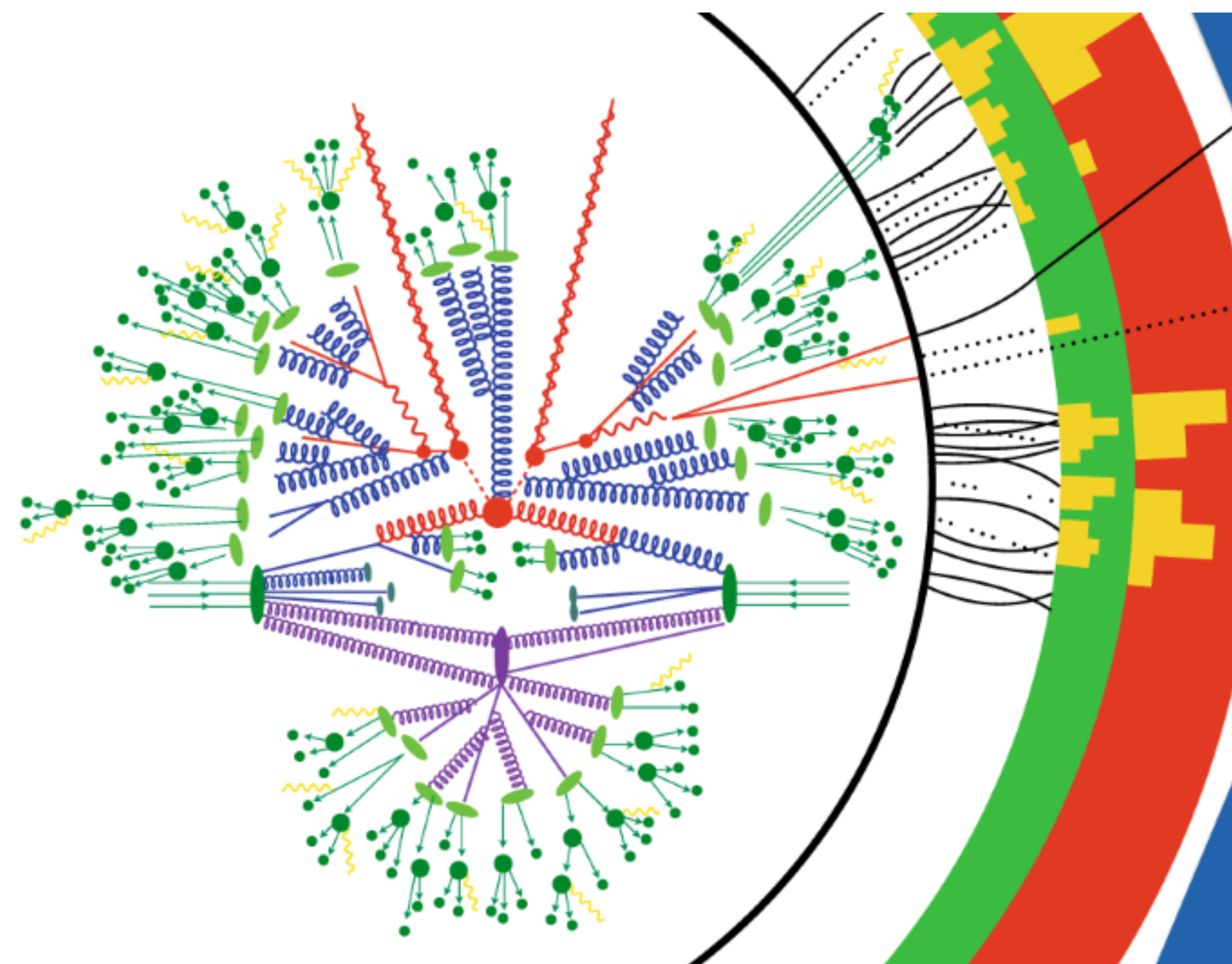


Image credit: Nature

LHC event



α_s^3
 α_s^2
 α_s^1
 α_s^0

N^3LO

$NNLO$

NLO

LO

Hard Process N^xLO

High precision

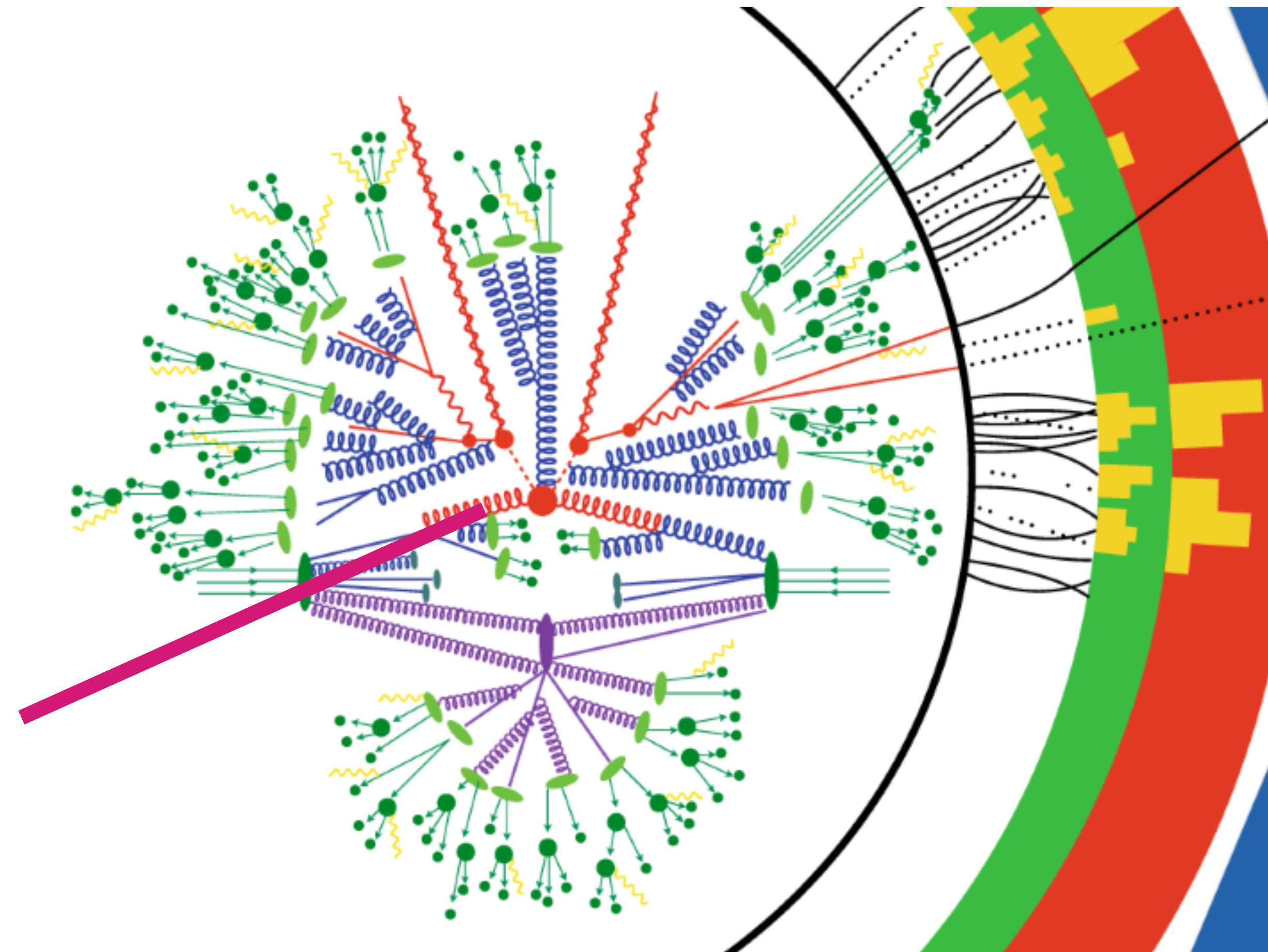


Image credit: Nature



LHC event

$$\alpha_s^n \log^{n-1}$$

$$\alpha_s^n \log^n$$

$$\alpha_s^n \log^{n+1}$$



NNLL

NLL

LL

Parton shower PS_{N^yLL}
and hadronisation

Realistic description

N^yLL resummation

$$\alpha_s^3$$

$$\alpha_s^2$$

$$\alpha_s^1$$

$$\alpha_s^0$$



N³LO

NNLO

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Hard Process N^xLO

High precision

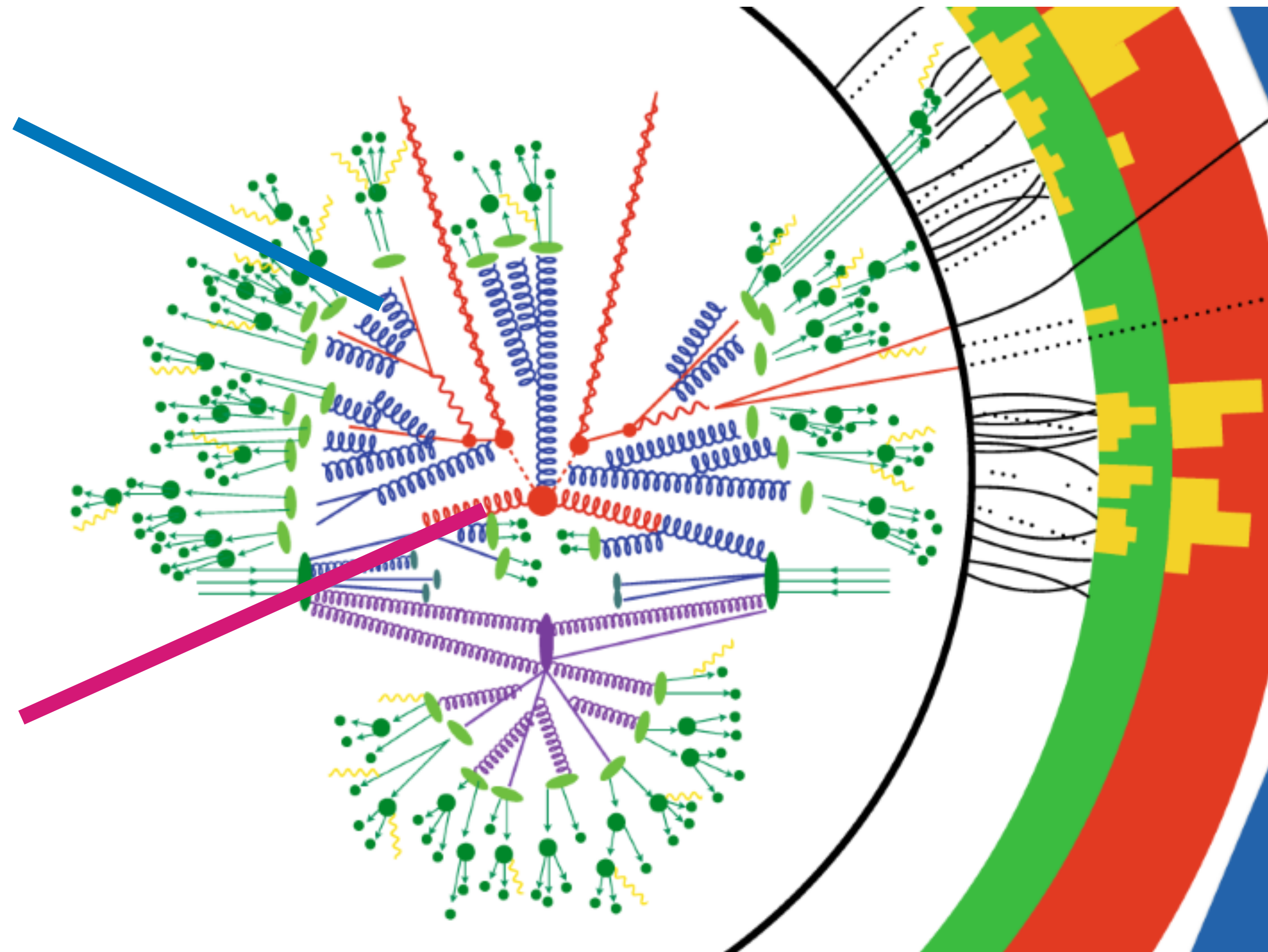


Image credit: Nature



LHC event

$$\alpha_s^n \log^{n-1}$$

$$\alpha_s^n \log^n$$

$$\alpha_s^n \log^{n+1}$$

NNLL

NLL

LL

$$\alpha_s^3$$

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N³LO

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Parton shower PS_{N^yLL}
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- Realistic description
- N^yLL resummation

Hard Process N^xLO

- High precision

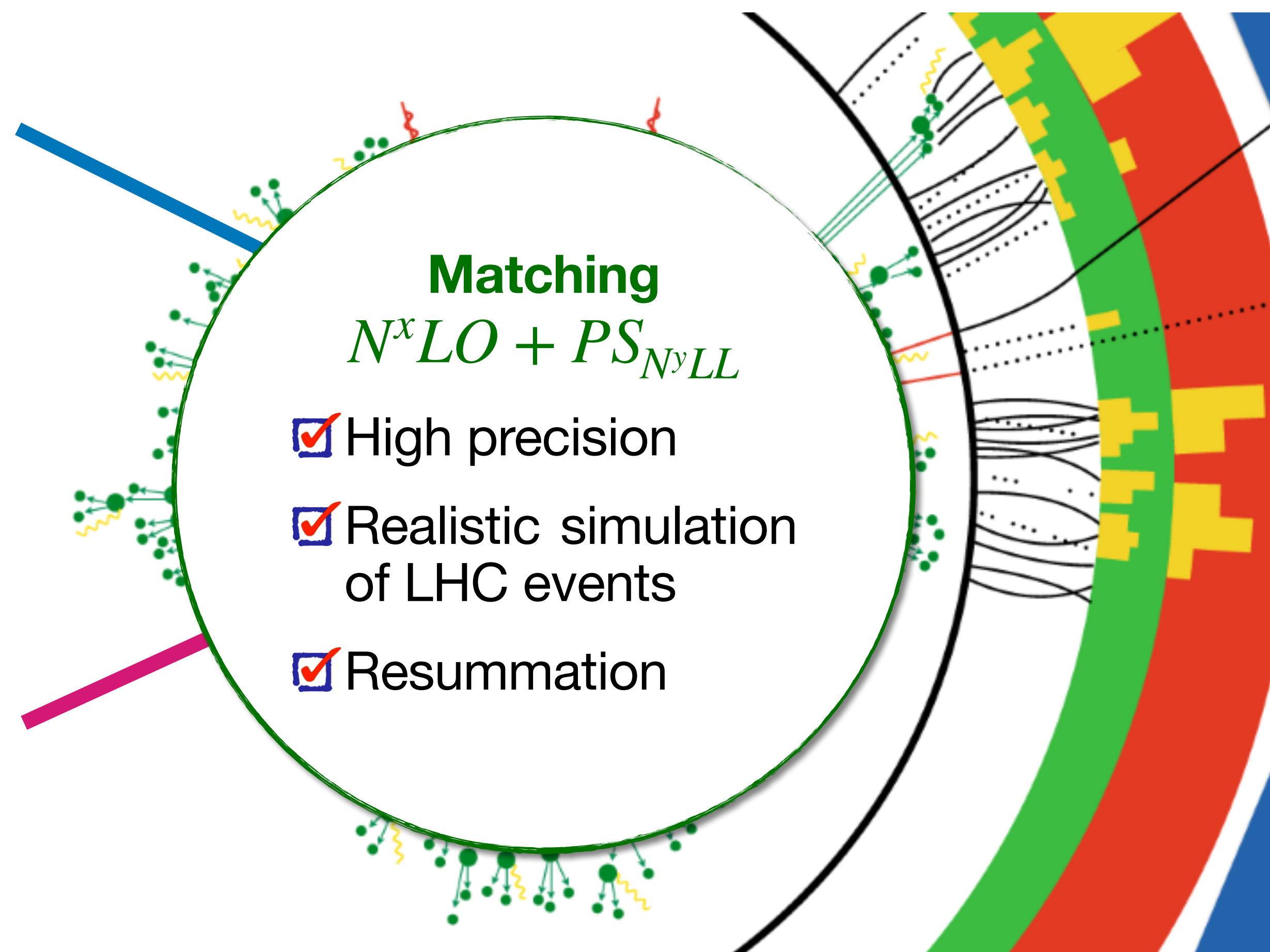


Image credit: Nature

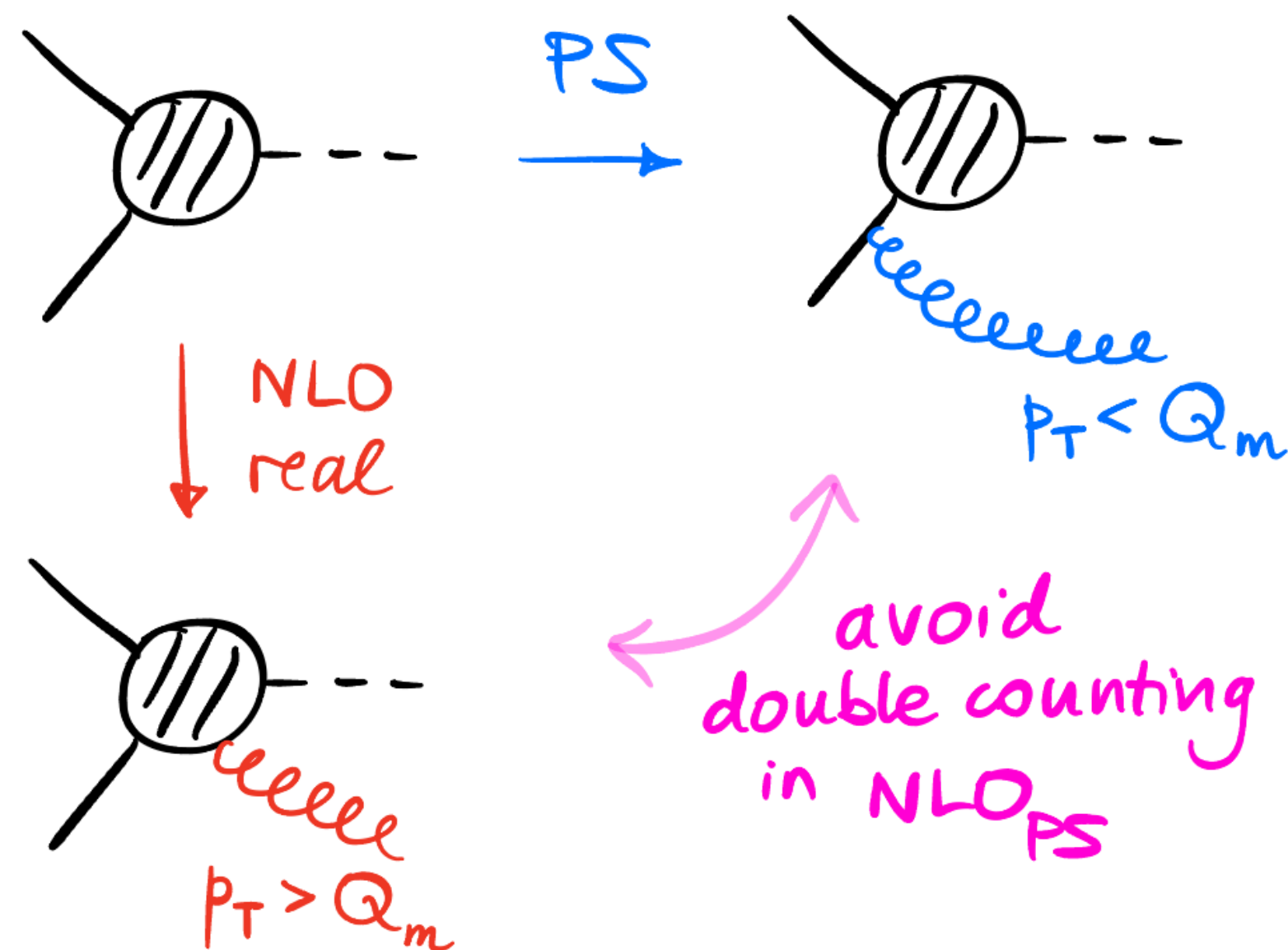


NLO+PS_{LL}

Solved problem for long time.
Completely understood and fully automated.

Two main approaches:

- **POWHEG** [0409146, 0709.2092, 1002.2581]
- **MC@NLO** [0204244]



Problem: Match fixed-order predictions with Parton Shower avoiding an unphysical **matching scale**.

POWHEG idea: implement a Monte Carlo generator that produces just one emission (the hardest one) which alone gives the correct NLO result.

Nason [hep-ph/0409146]



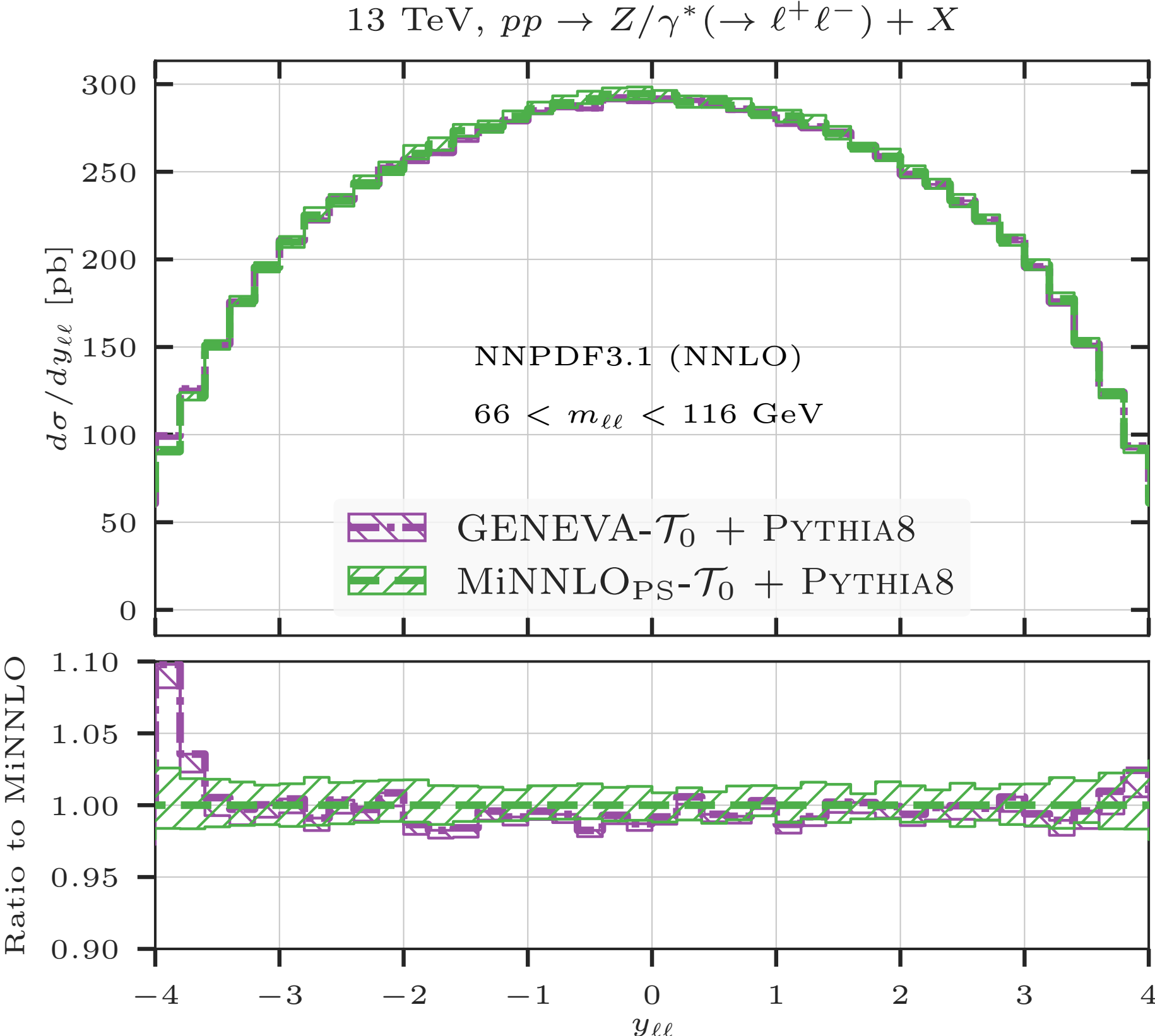
NNLO+PS_{LL}

State-of-the-art for precision LHC phenomenology.

Lots of ongoing efforts. **Many processes** already implemented, beyond the color-singlet production.

Two main approaches:

- **MiNNLOPS** [1908.06987]
 - in the POWHEG framework
- **GENEVA** [1311.0286]



Ebert, Rottoli, Wiesemann, Zanderighi, Zanolini [2402.00596]



2004
POWHEG

2008
NLO+PS
for color
singlet (F)

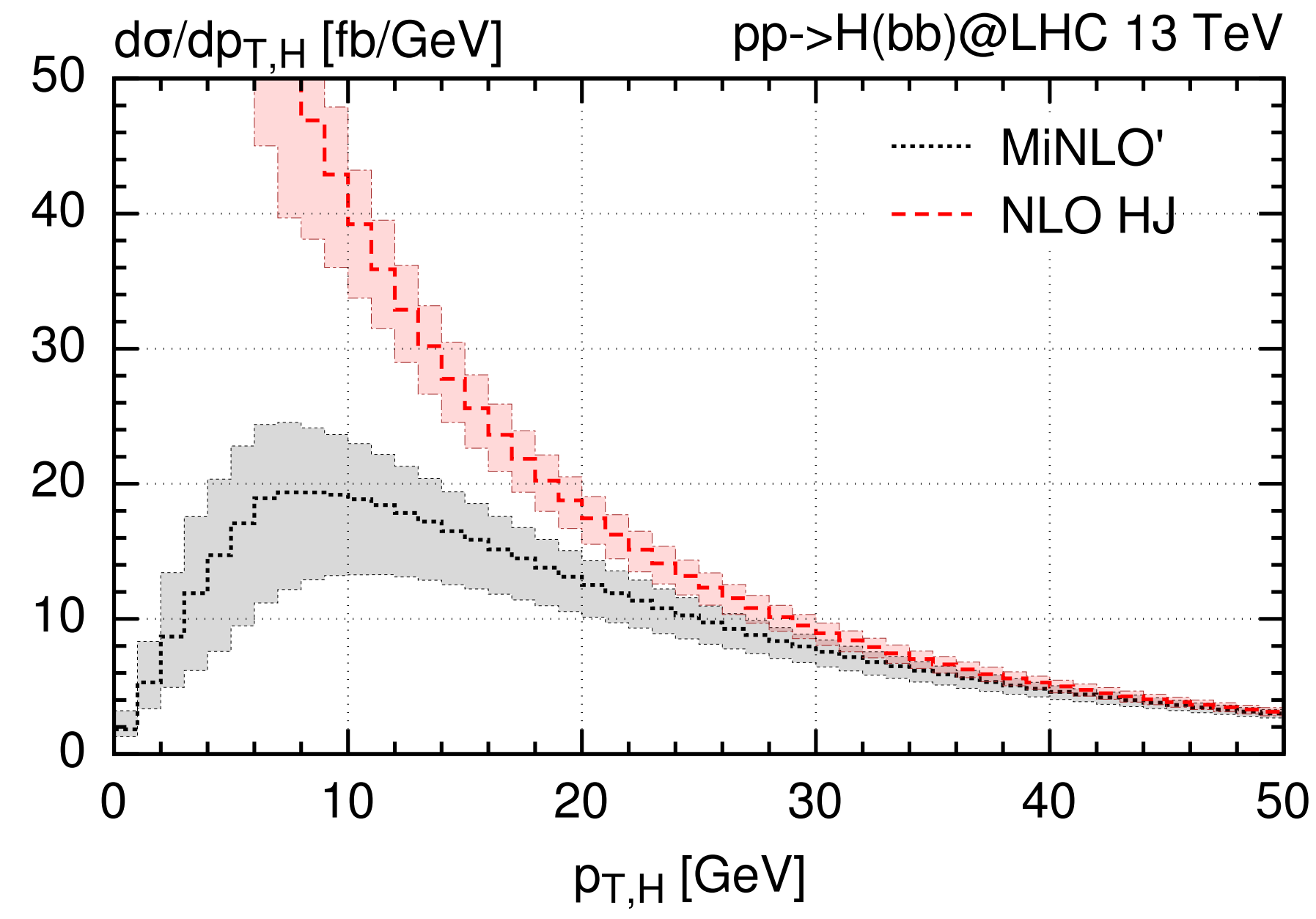
2010
NLO+PS
 F_j

2012
MiNLO'
NNLO a posteriori
reweighing of
MiNLO'

2019
MiNNLOPS

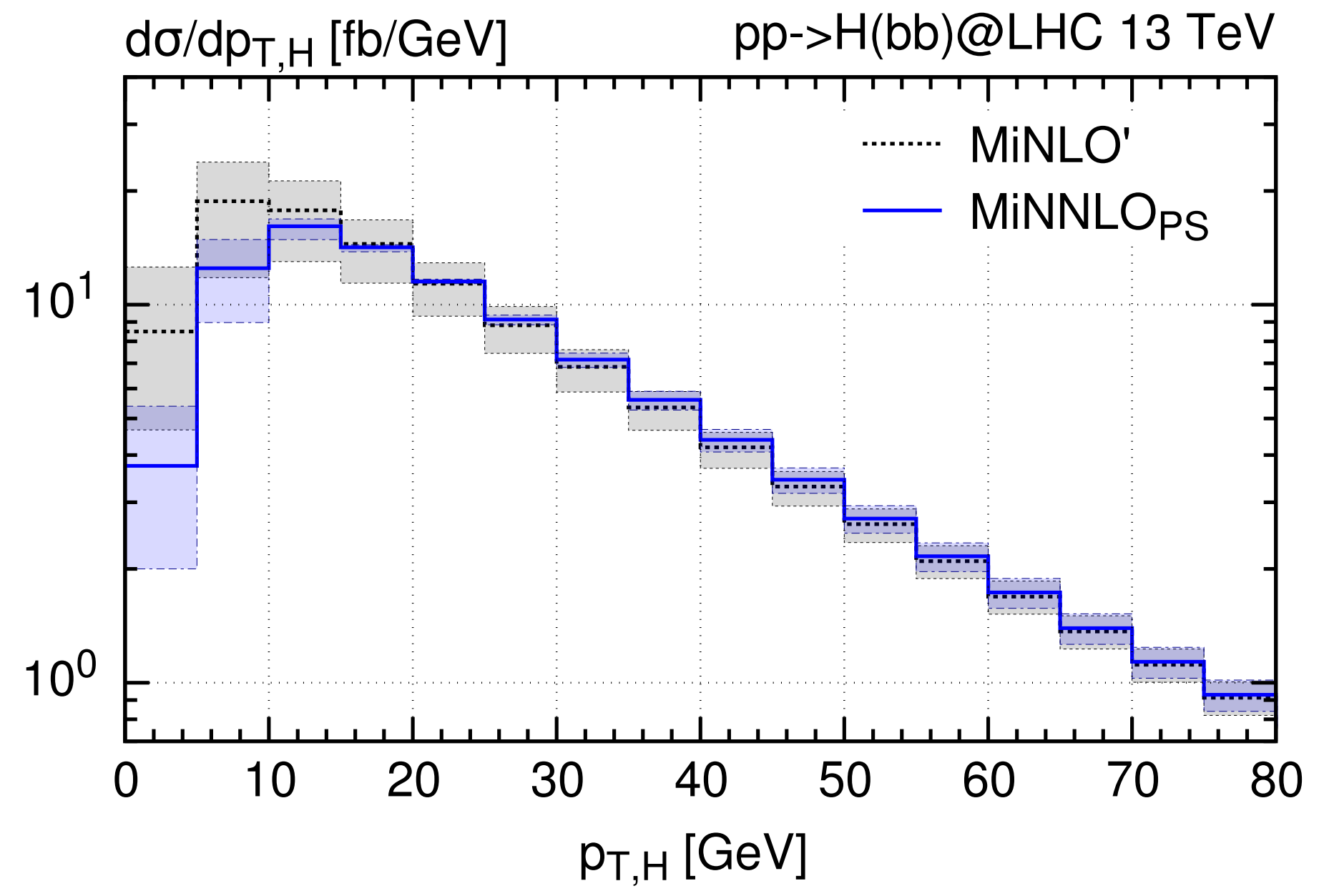
MiNLO'

Hamilton, Nason, Oleari,
Zanderighi [1212.4504]



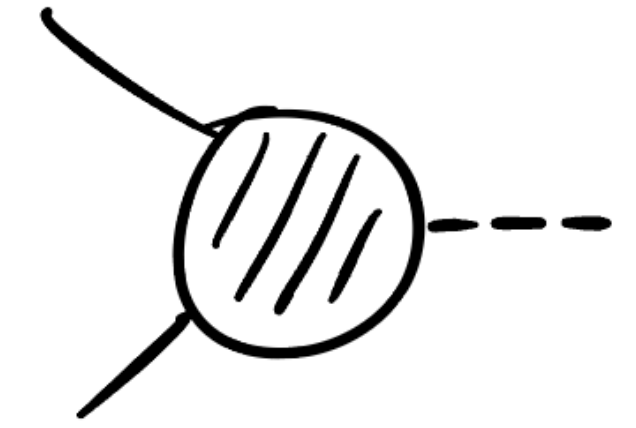
MiNNLOPS

Monni, Nason, Re, Wieseemann,
Zanderighi [1908.06987]

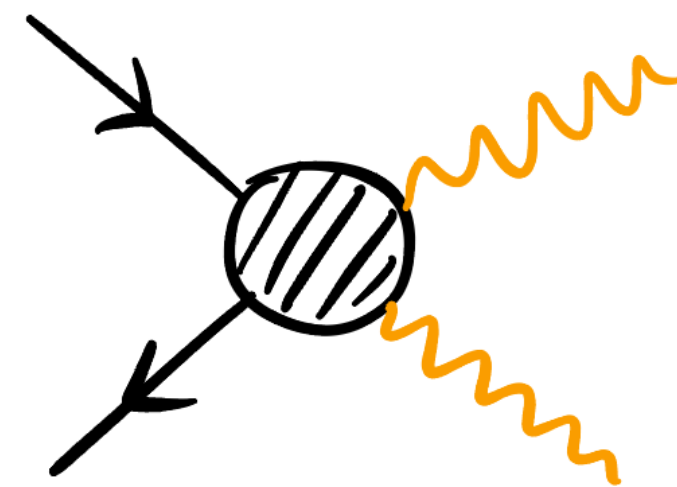




Classes of processes in MiNNLOPs



DIBOSON PROCESSES



$Z\gamma$ [2010.10478, 2108.11315]

WW [2103.12077]

ZZ [2108.05337]

$WH/ZH(H \rightarrow b\bar{b})$ [2112.04168]

$\gamma\gamma$ [2204.12602]

WZ [2208.12660]

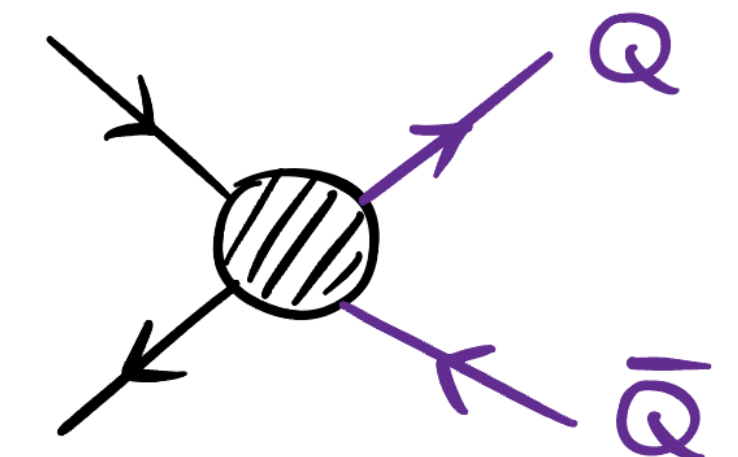
SMEFT studies [2204.00663, 2311.06107]

$gg \rightarrow H, W/Z$ [1908.06987, 2006.04133, 2402.00596, 2407.01354]

$b\bar{b} \rightarrow H$ [2402.04025]

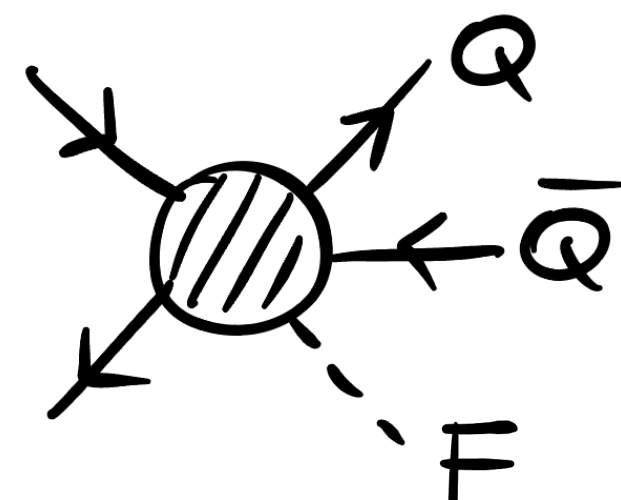
first (and currently only) NNLO+PS method for heavy-quark final states

HEAVY-QUARK PRODUCTION



$b\bar{b}Z$ [2404.08598]

$b\bar{b}H$ [in progress]

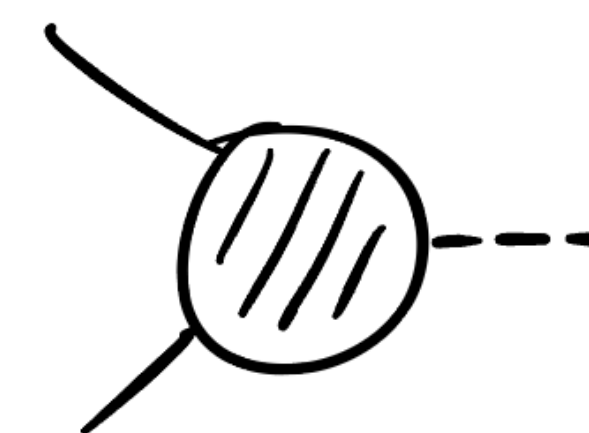


$t\bar{t}$ [2012.14267, 2112.12135]

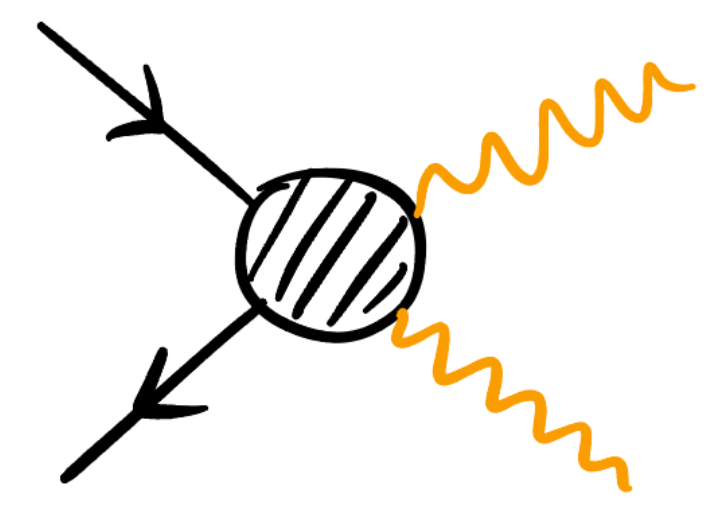
$b\bar{b}$ [2302.01645, in progress]



Classes of processes in MiNNLOPs



DIBOSON PROCESSES



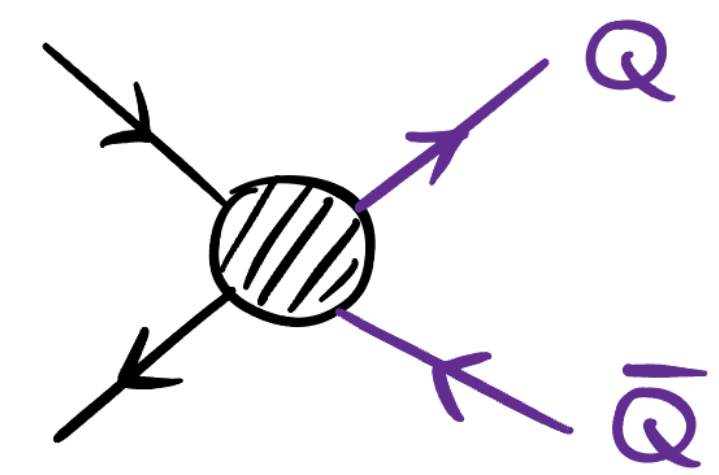
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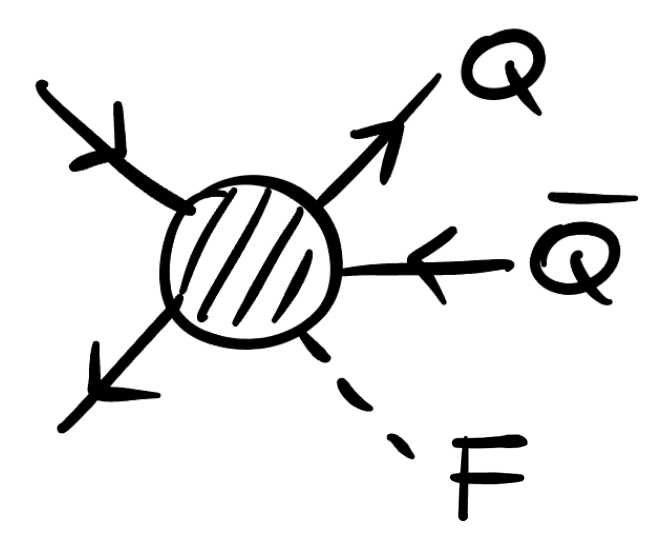
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$b\bar{b}Z$ [2404.08598]
 $b\bar{b}H$ [in progress]



Recent results discussed in this talk

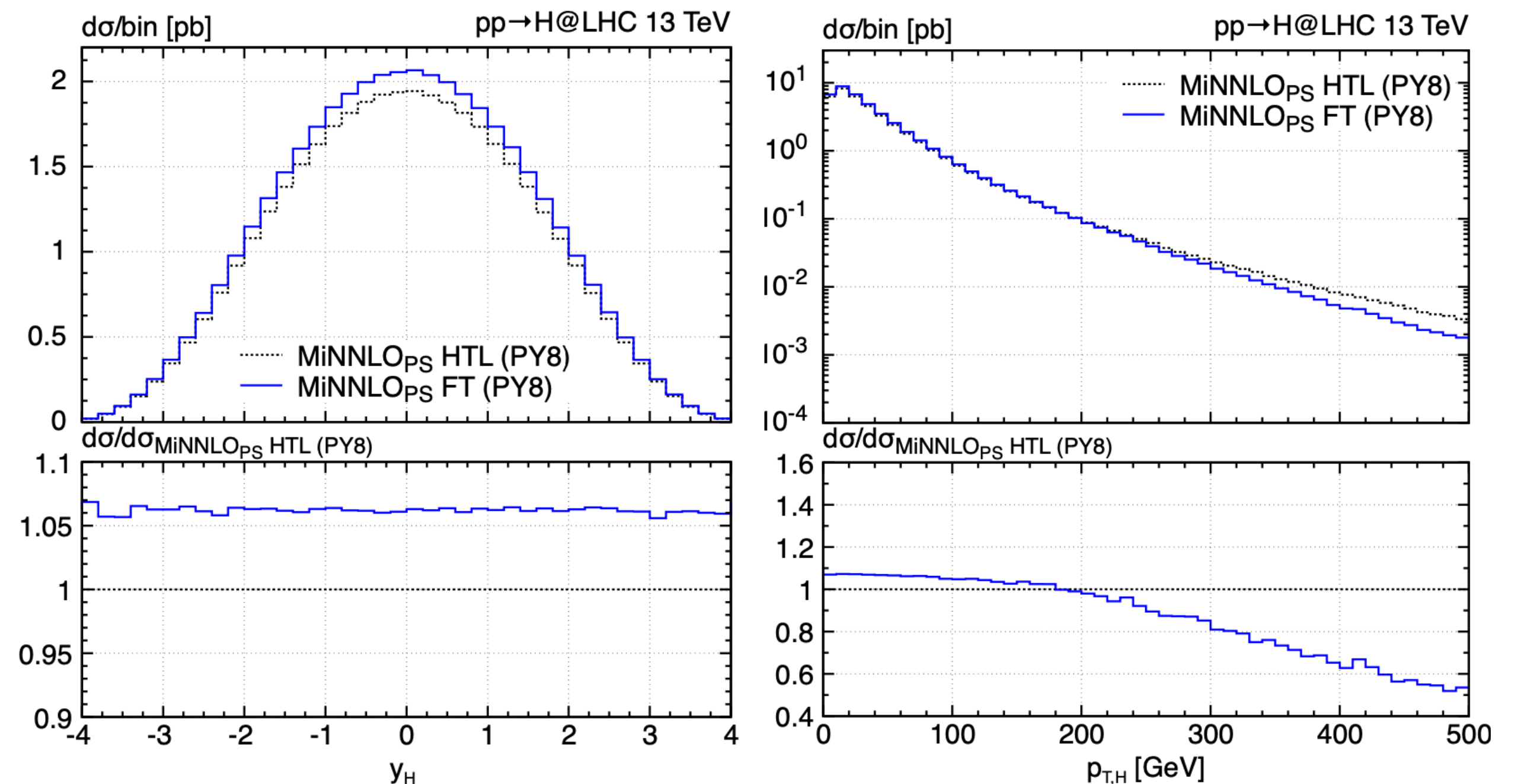
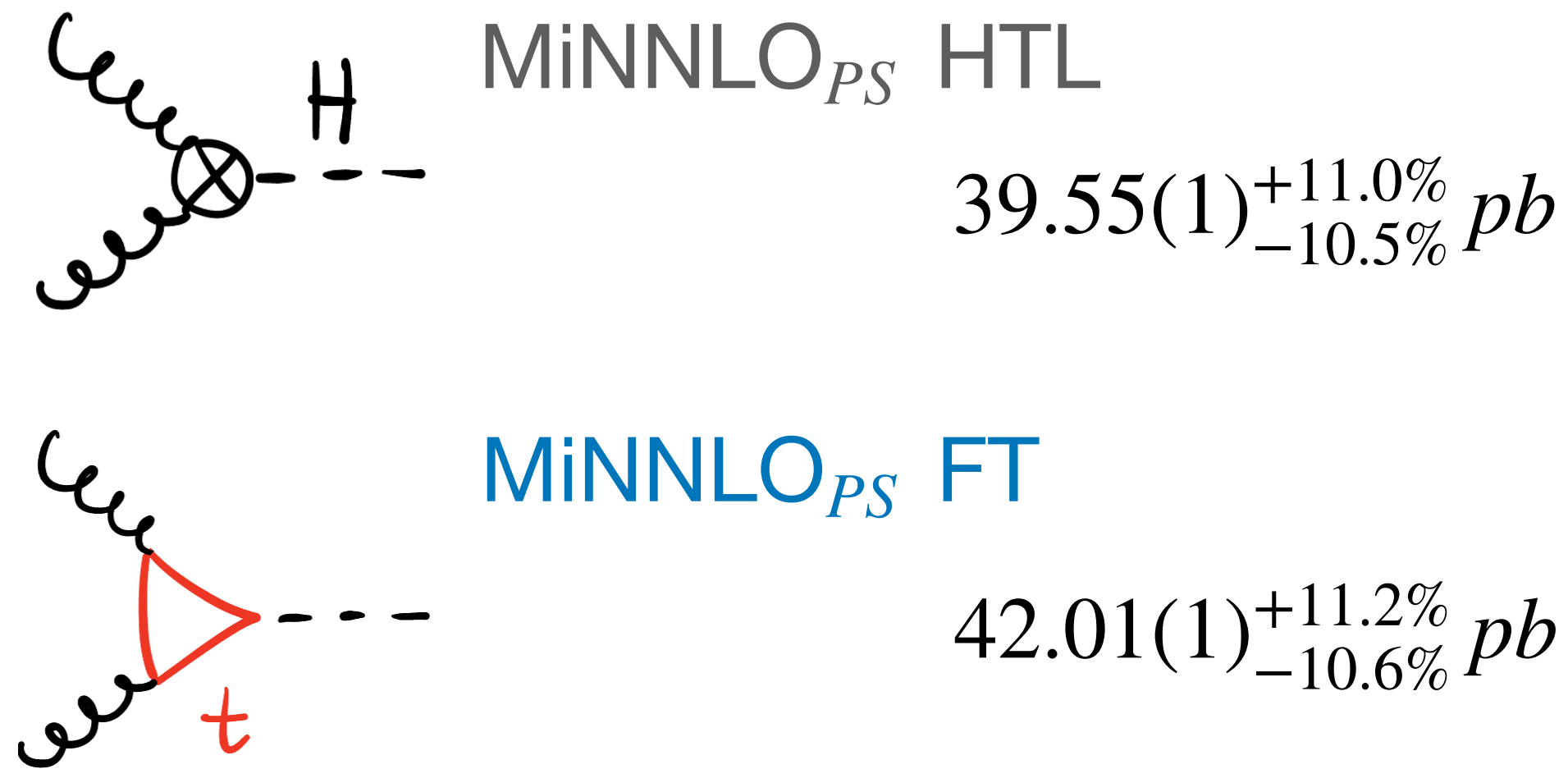
$t\bar{t}$ [2012.14267, 2112.12135]
 $b\bar{b}$ [2302.01645, in progress]

Full top dependence



Why? Increasing precision calls for the inclusion of effects, like mass corrections!

The Higgs production via gluon fusion with **exact top-quark mass** dependence has been recently implemented in the MiNNLOPS generator.

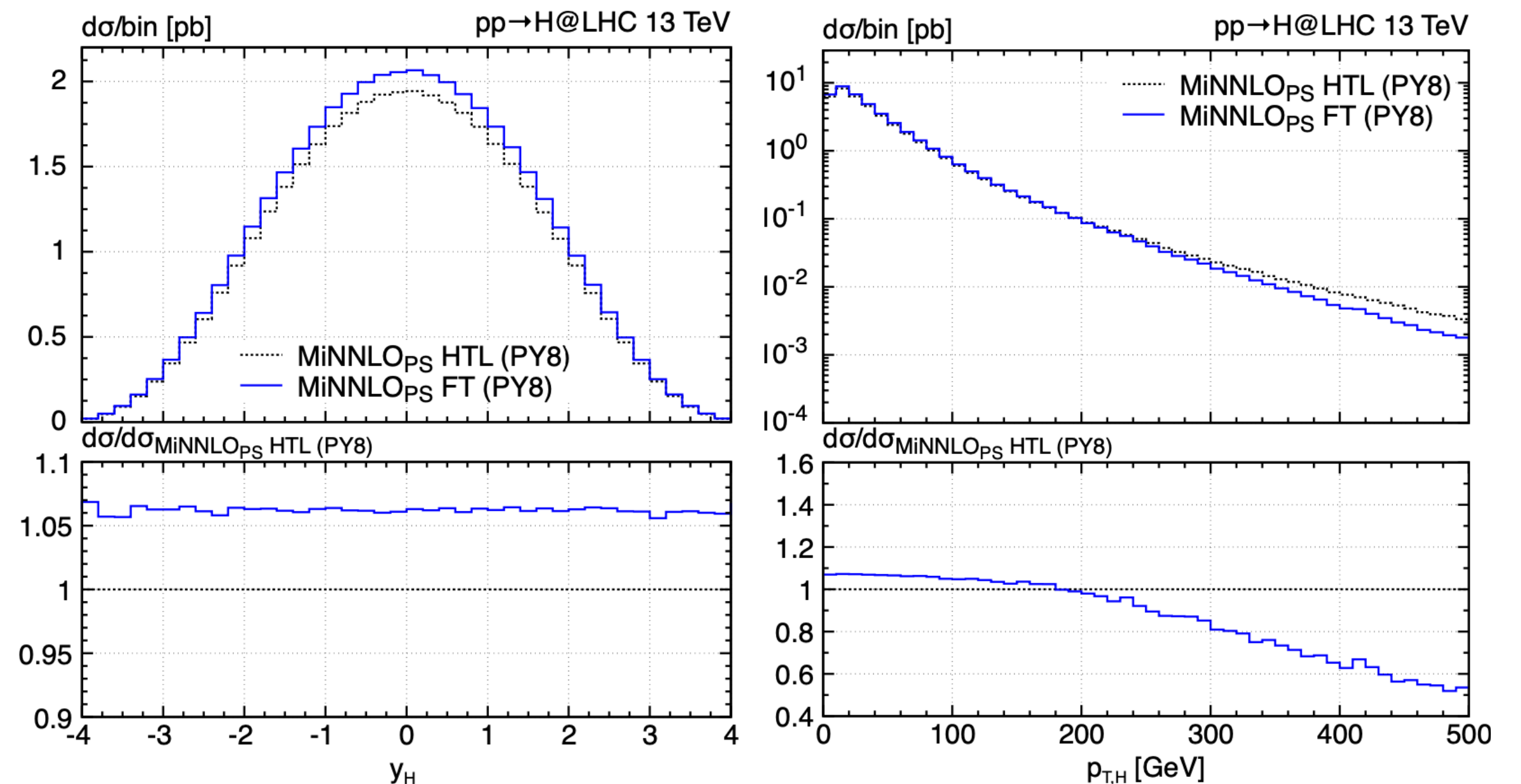
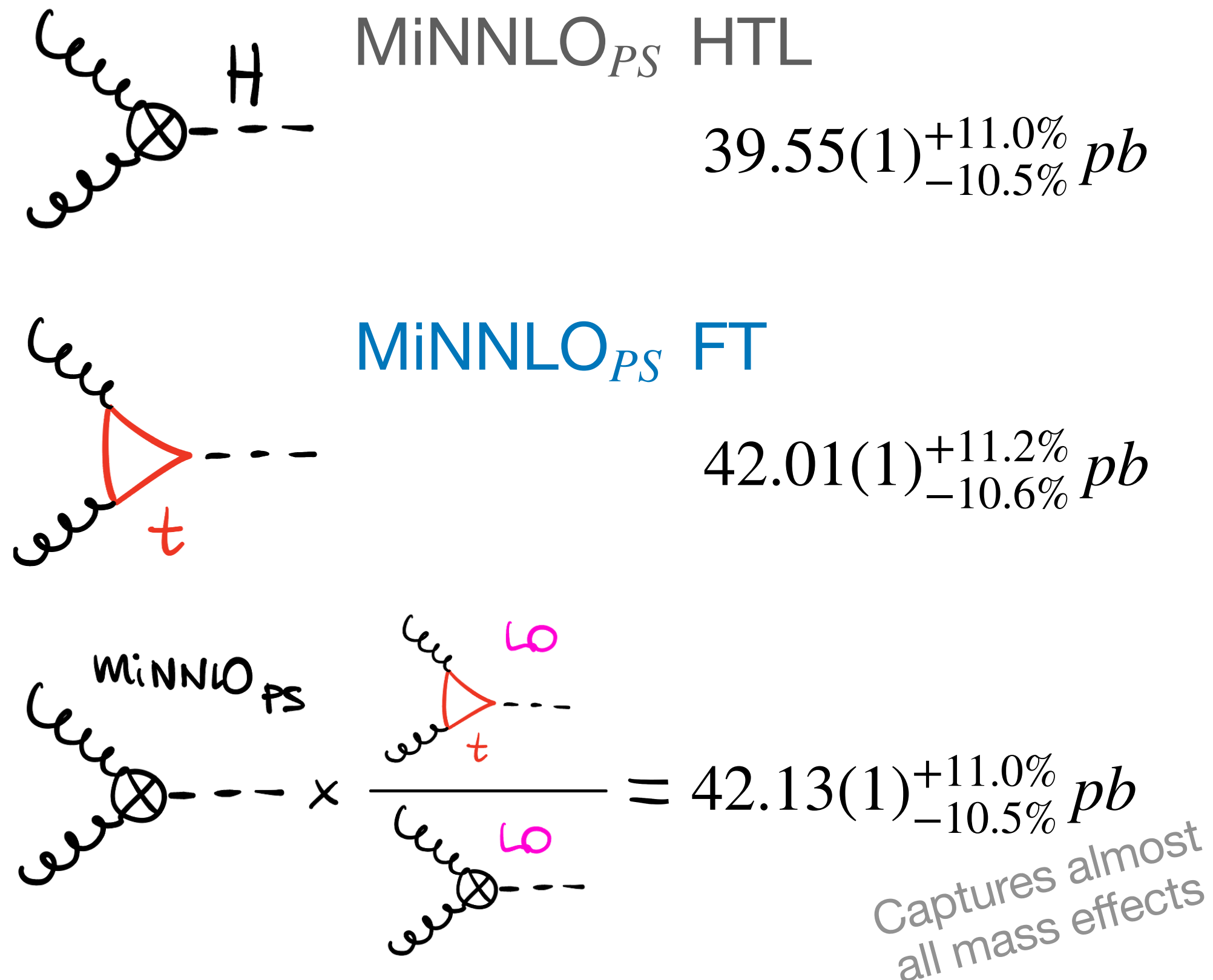


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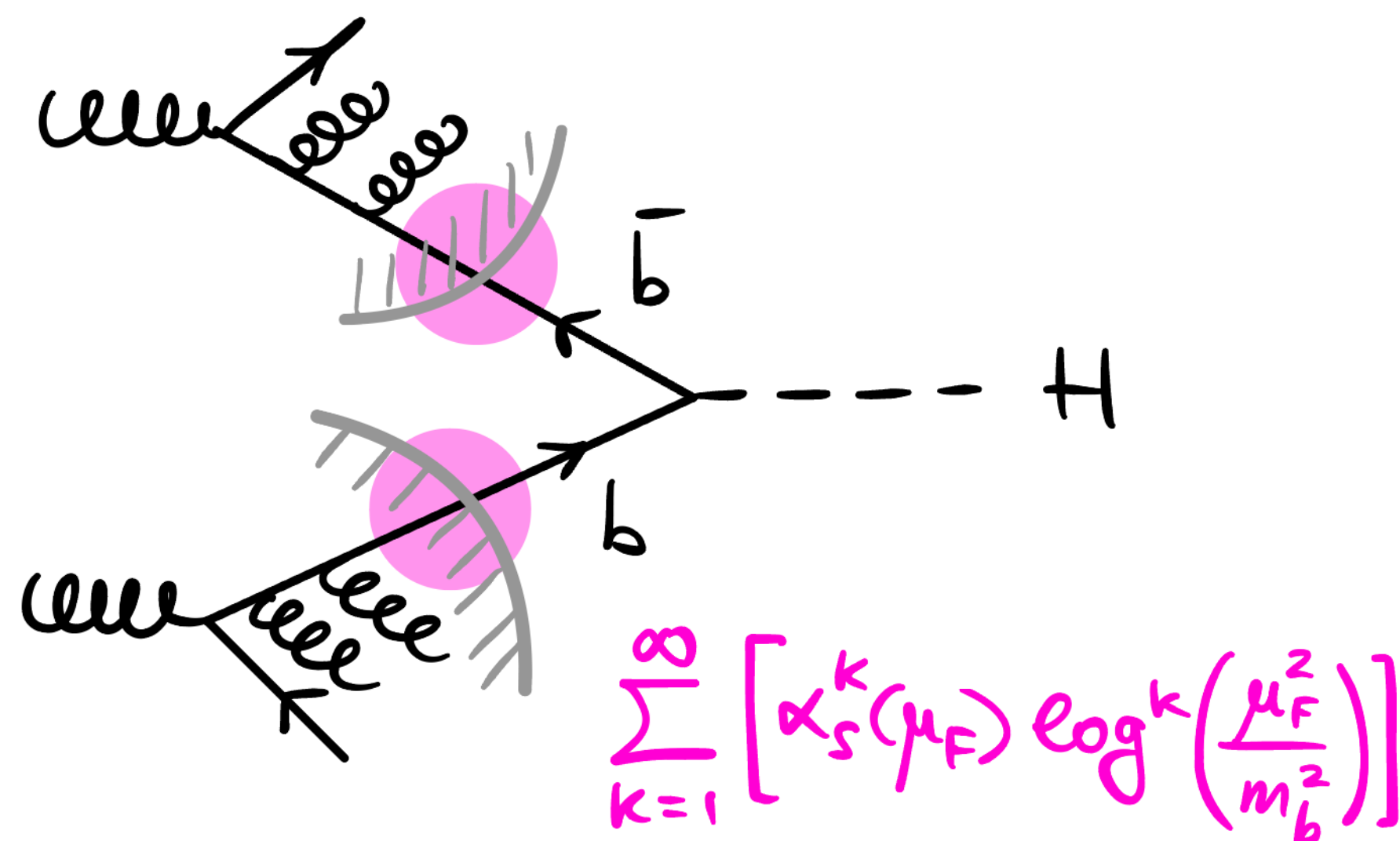
bb → **H**

CB, Sankar, Wiesemann,
Zanderighi [2402.04025]

A rare but interesting channel

Why bbH? Higgs production via bottom fusion is a rare but crucial channel, **background of HH searches.**

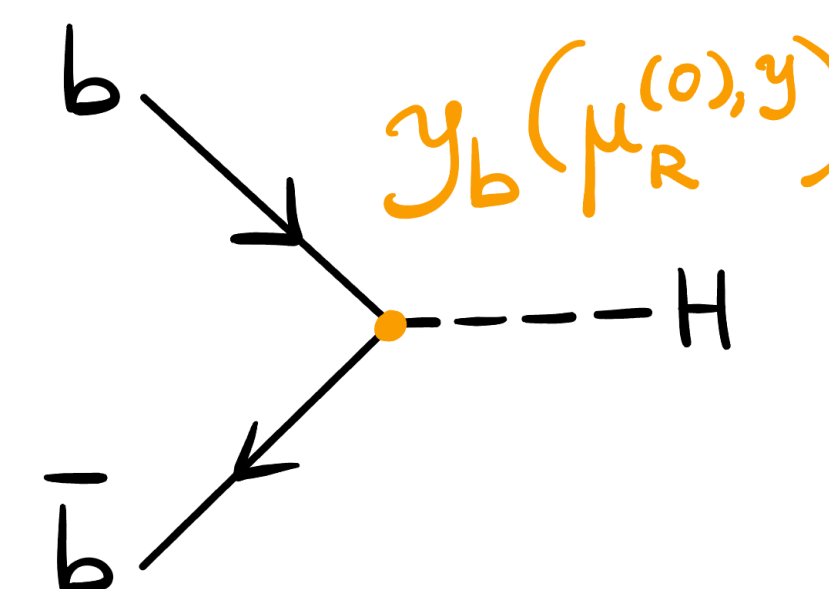
SFS



massless bottoms (5 flavour scheme)

- ✓ Collinear initial-state logs are resummed into bottom PDFs
- $\mathcal{O}(m_b/m_H)$ are neglected: low accurate description of bottom kinematic distribution

Feature. Adaptation of the MiNNLOPS method to account for the extra scale dependence induced by an overall **Yukawa coupling** that is $\overline{\text{MS}}$ renormalised



See Moriond 2024

$bb \rightarrow H$

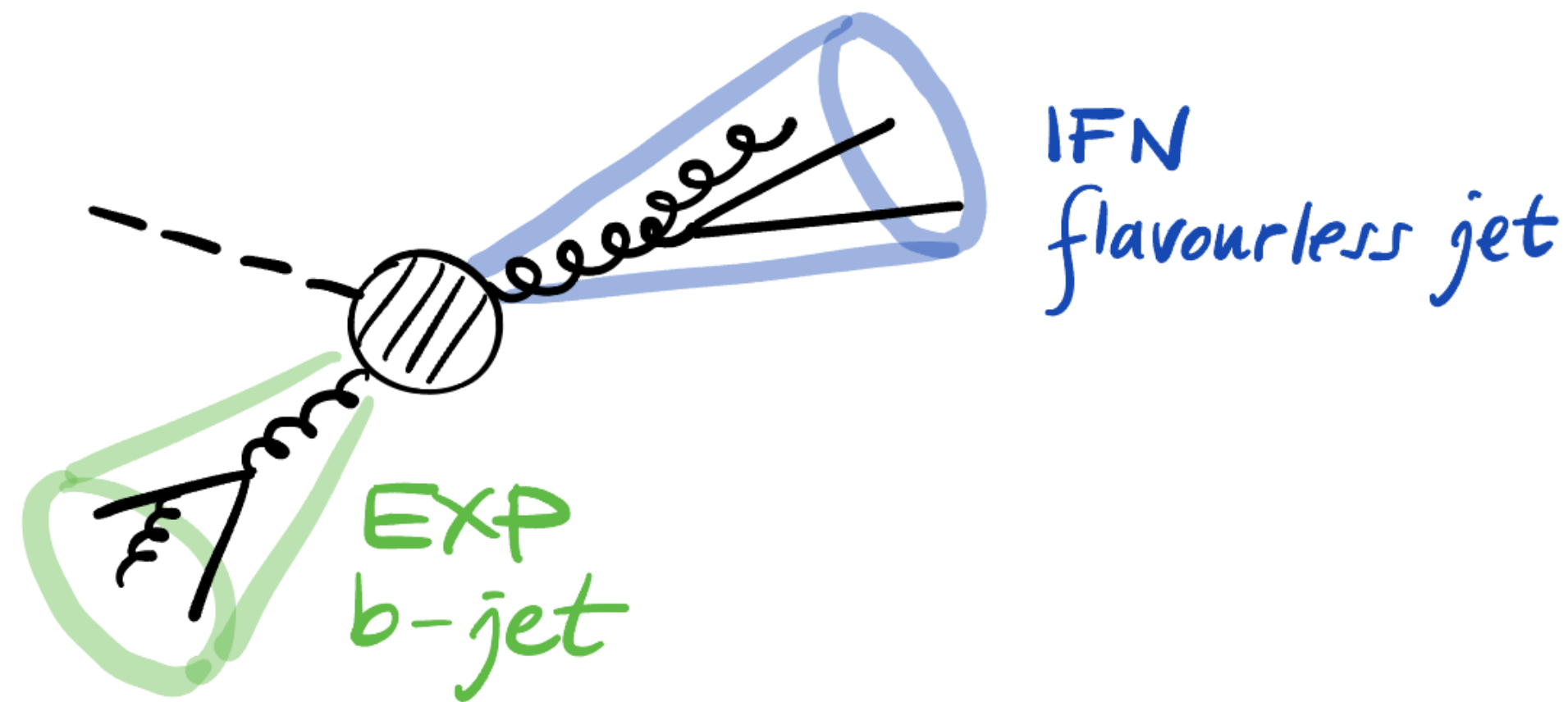


CB, Sankar, Wiesemann,
Zanderighi [in progress]

event generator \rightarrow fully-exclusive results

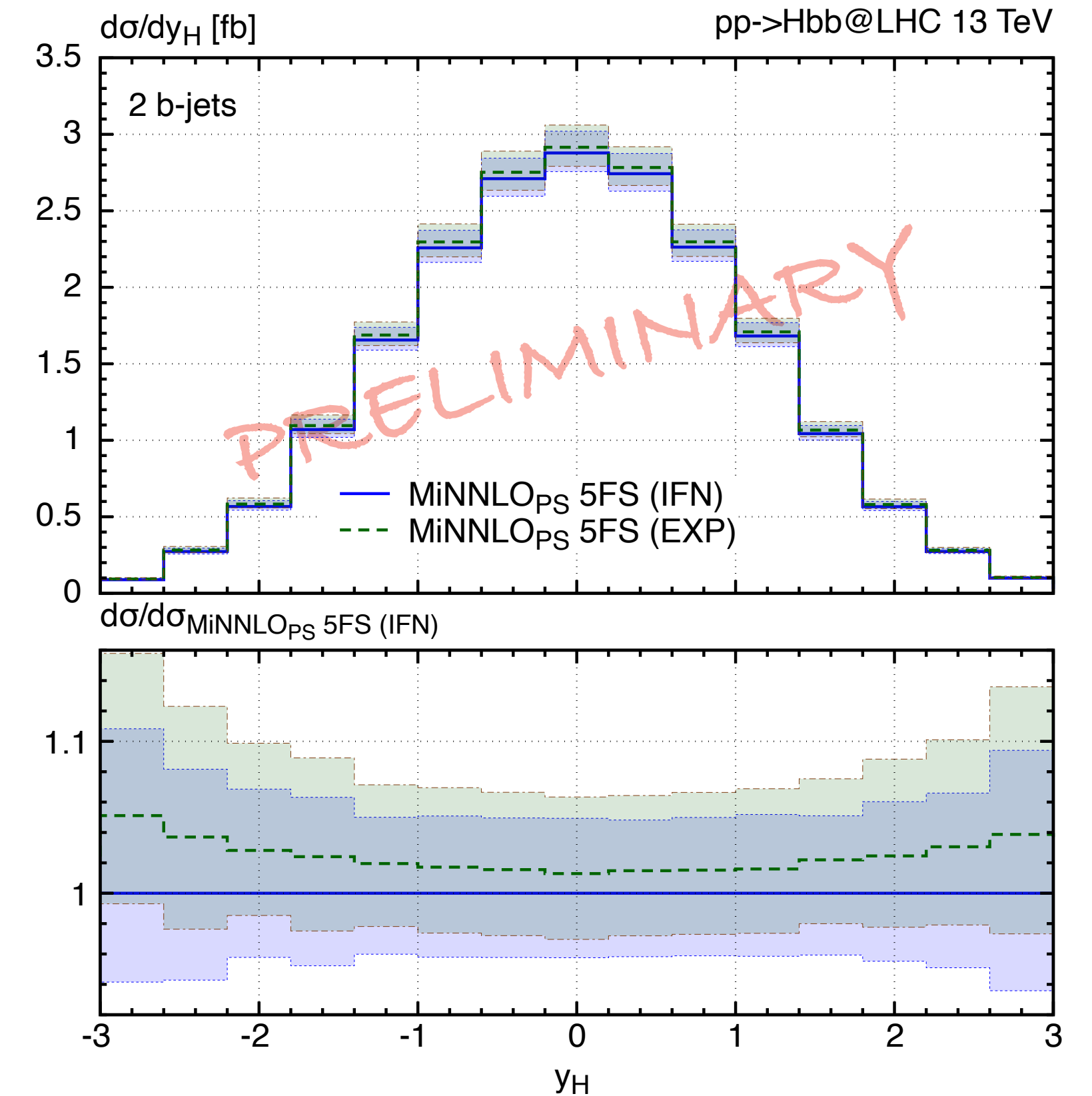
With the generated events, we have the opportunity to explore a lot of physics!

Several pheno studies can be conducted, such as the **b-tagging of jets**.



News. We have investigated the properties of the flavour jets in $bb \rightarrow H$

- **EXP**, a bjet contains at least a B-hadron
- **IFN**, IR-safe method called Interleaved Flavour Neutralisation
Caola, Grabarczyk, Hutt, Salam, Scyboz, Thaler [2306.07314]



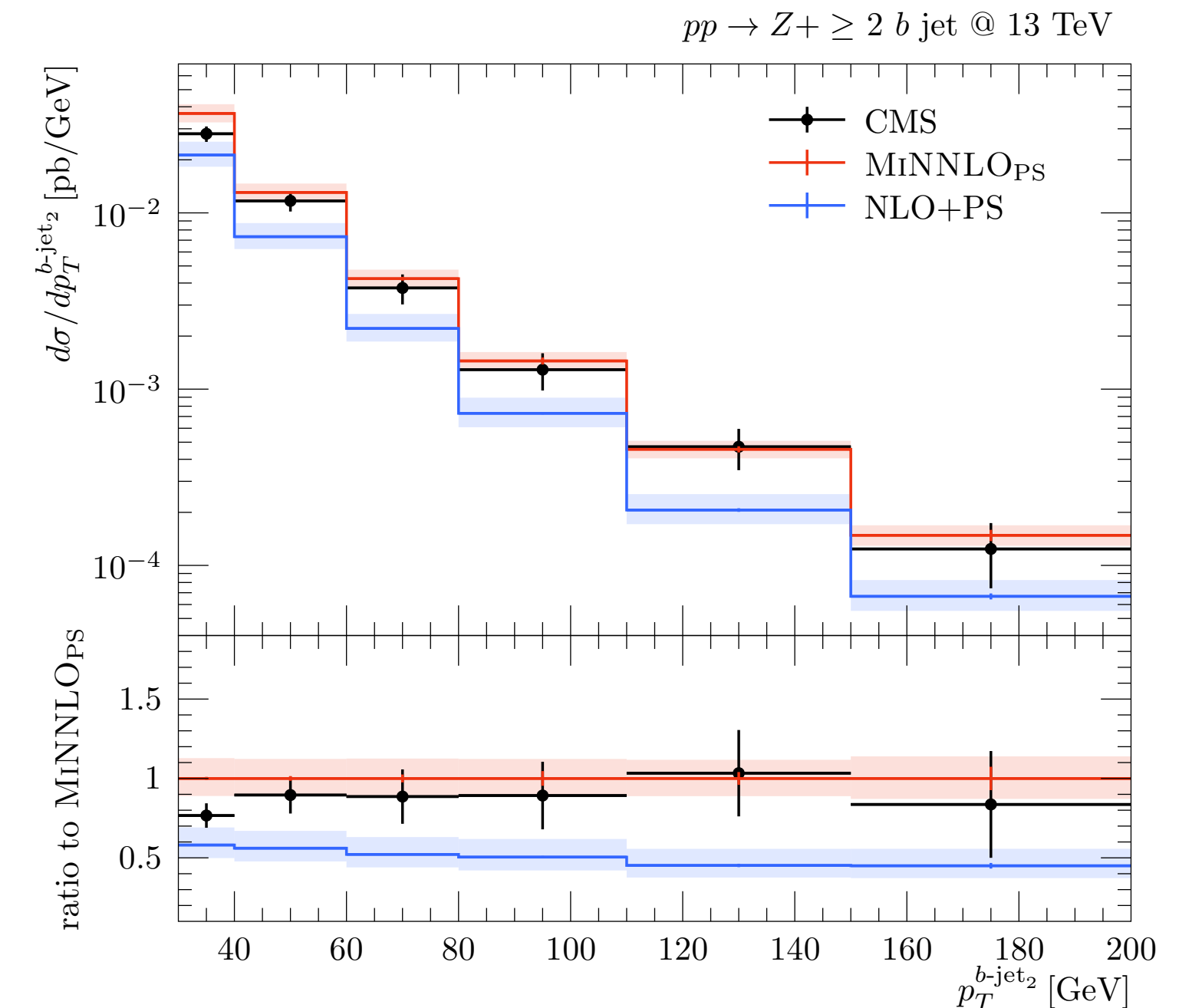
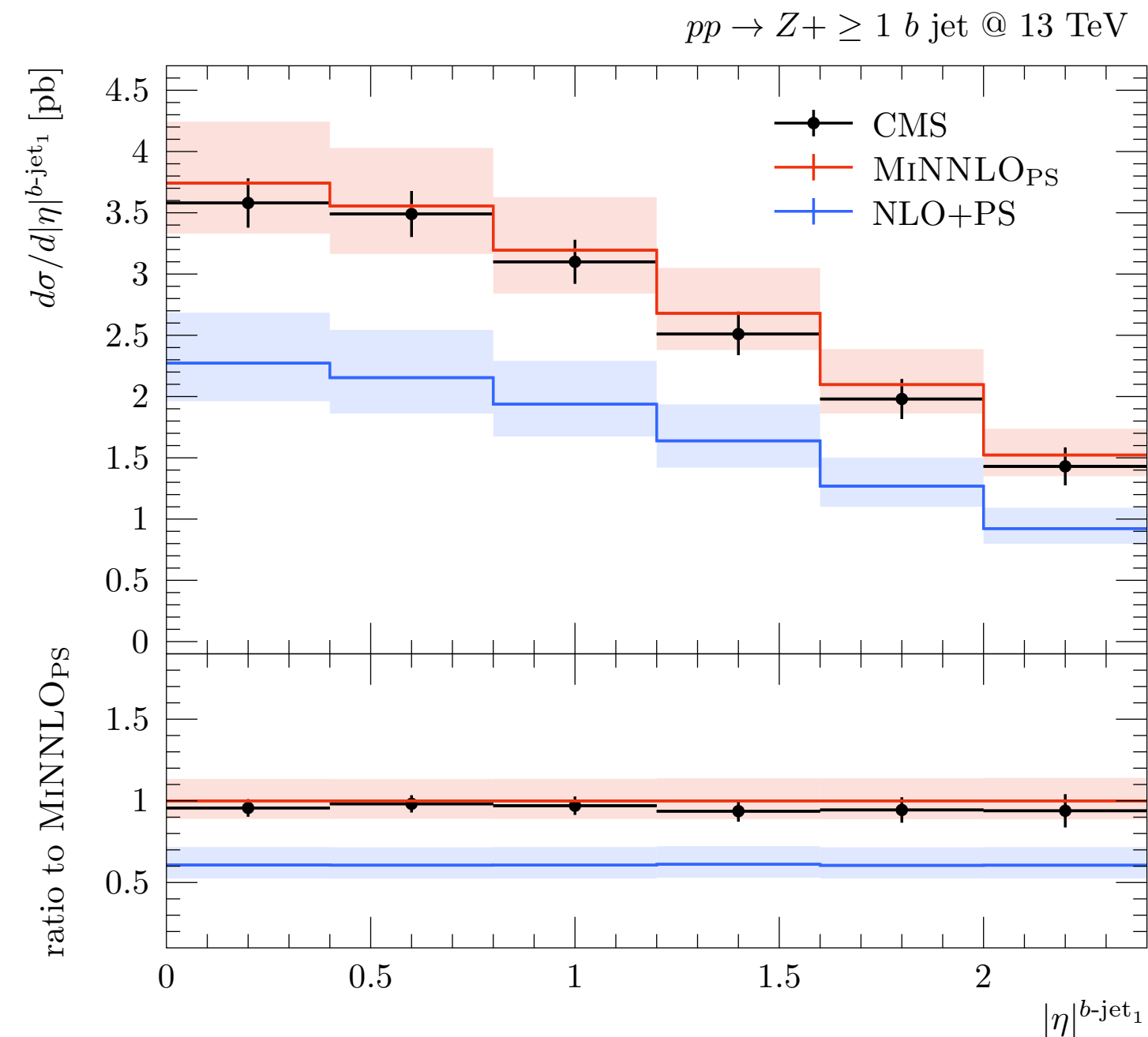
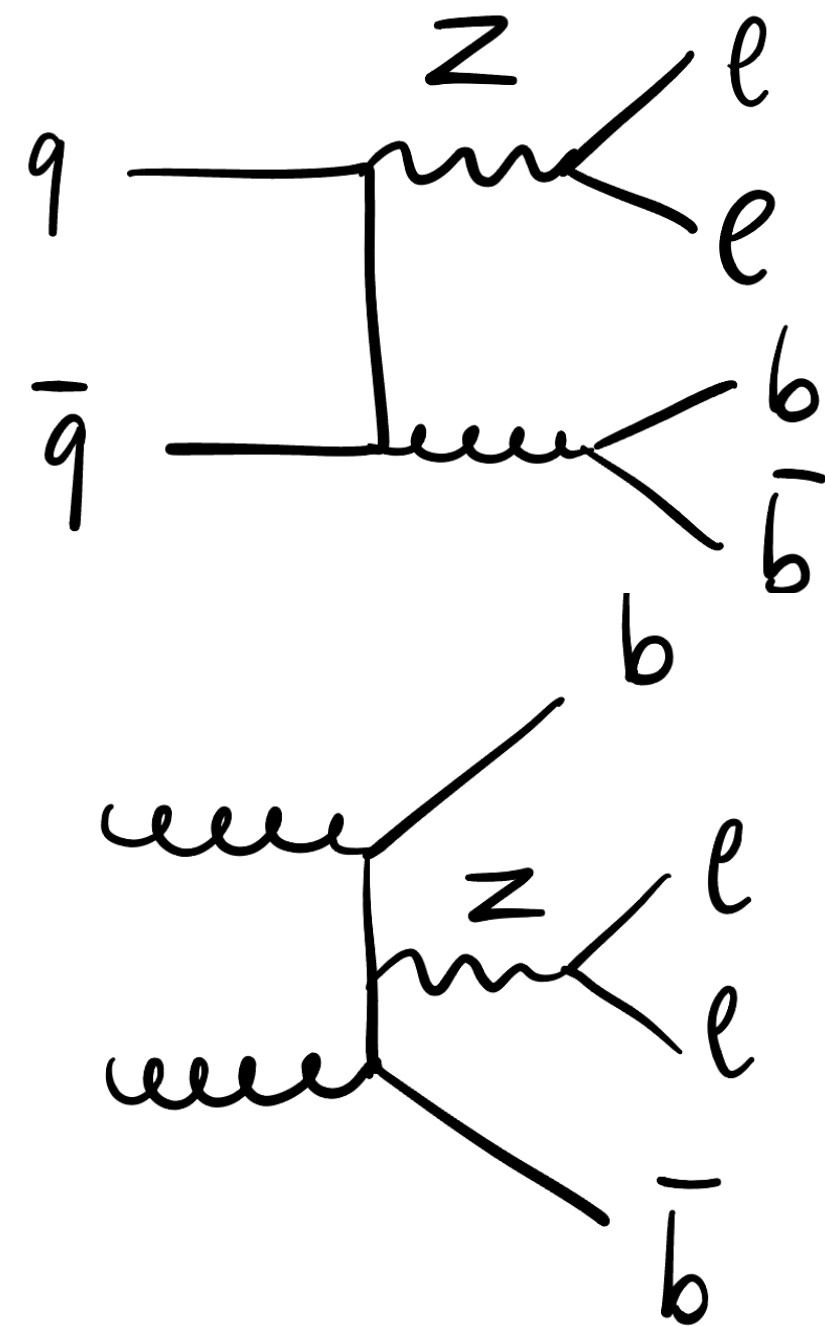


A new class of processes

Why? Modelling high-multiplicity processes is mandatory for LHC studies. We must go beyond $2 \rightarrow 2$ processes.

MiNNLOPS now can perform predictions for **heavy-quark pair production in association to a color singlet.**

Feature. Treatment of the singular structure for heavy quarks in generic kinematics. Applied for the first time to $b\bar{b}l\bar{l}$.

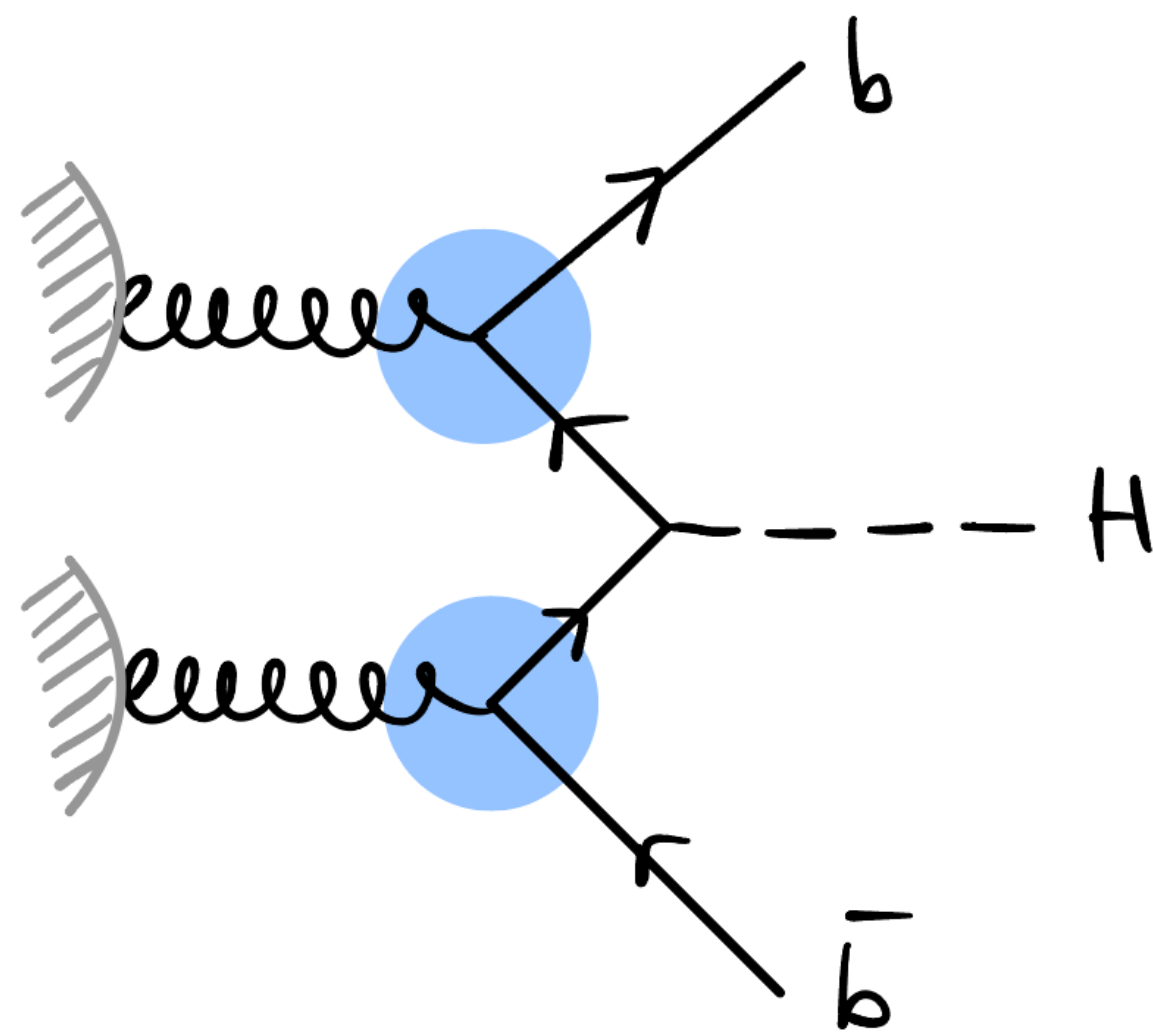


The massive calculation



Why bbH with massive quarks? The massless calculation is not accurate in some region of the phase-space and for B-hadron observables.

4FS



massive calculation (four-flavour scheme)

- Computing higher orders is extremely non-trivial due to higher multiplicity
- ✓ Mass effects $O(m_b/m_H)$ are present at any order

Feature. It requires both the MiNNLOPS extensions for Yukawa induced processes and heavy quarks in final state.

Theoretical bottleneck. Two-loop amplitude \rightsquigarrow implement a reliable and well-tested approximation

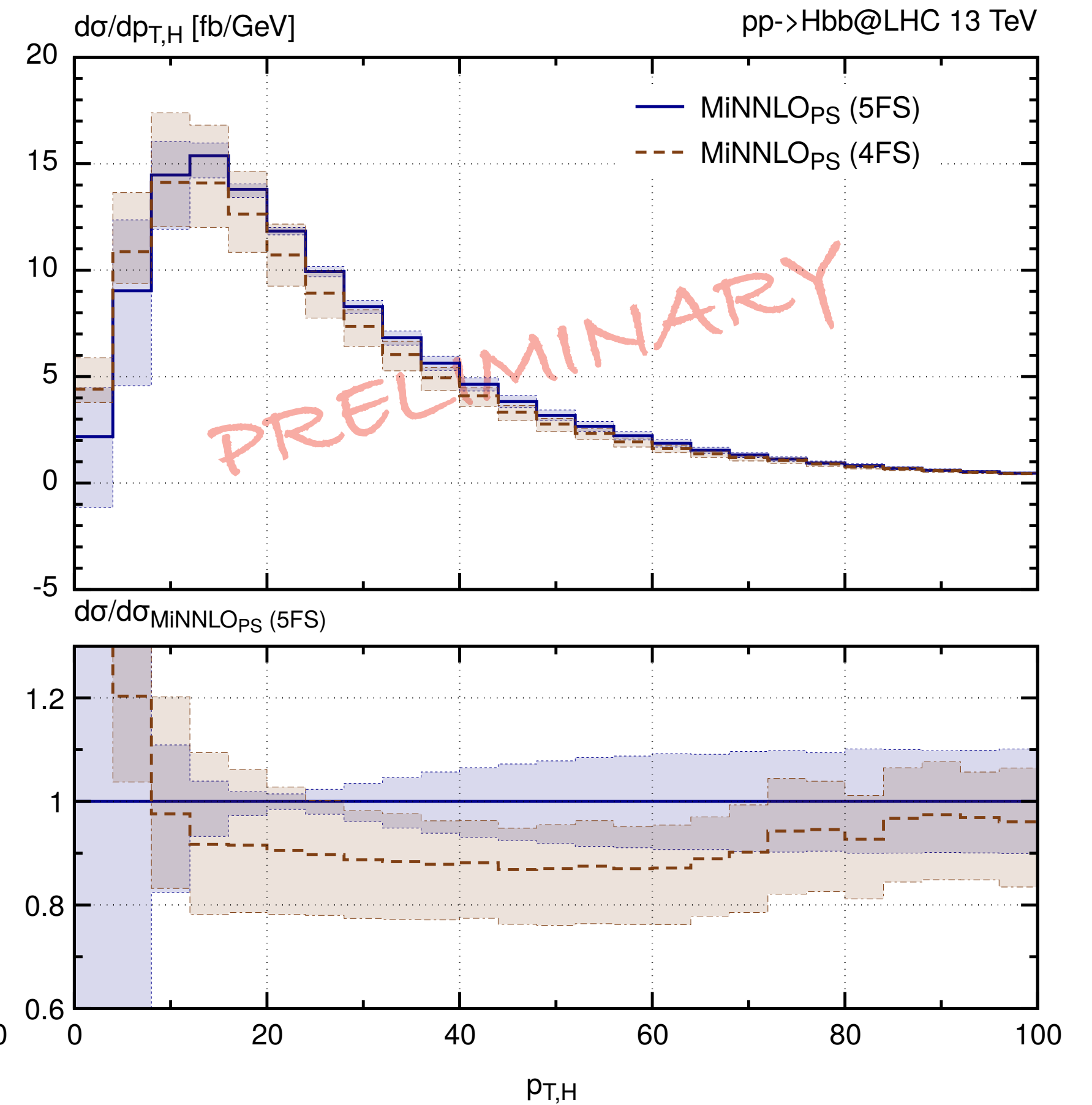
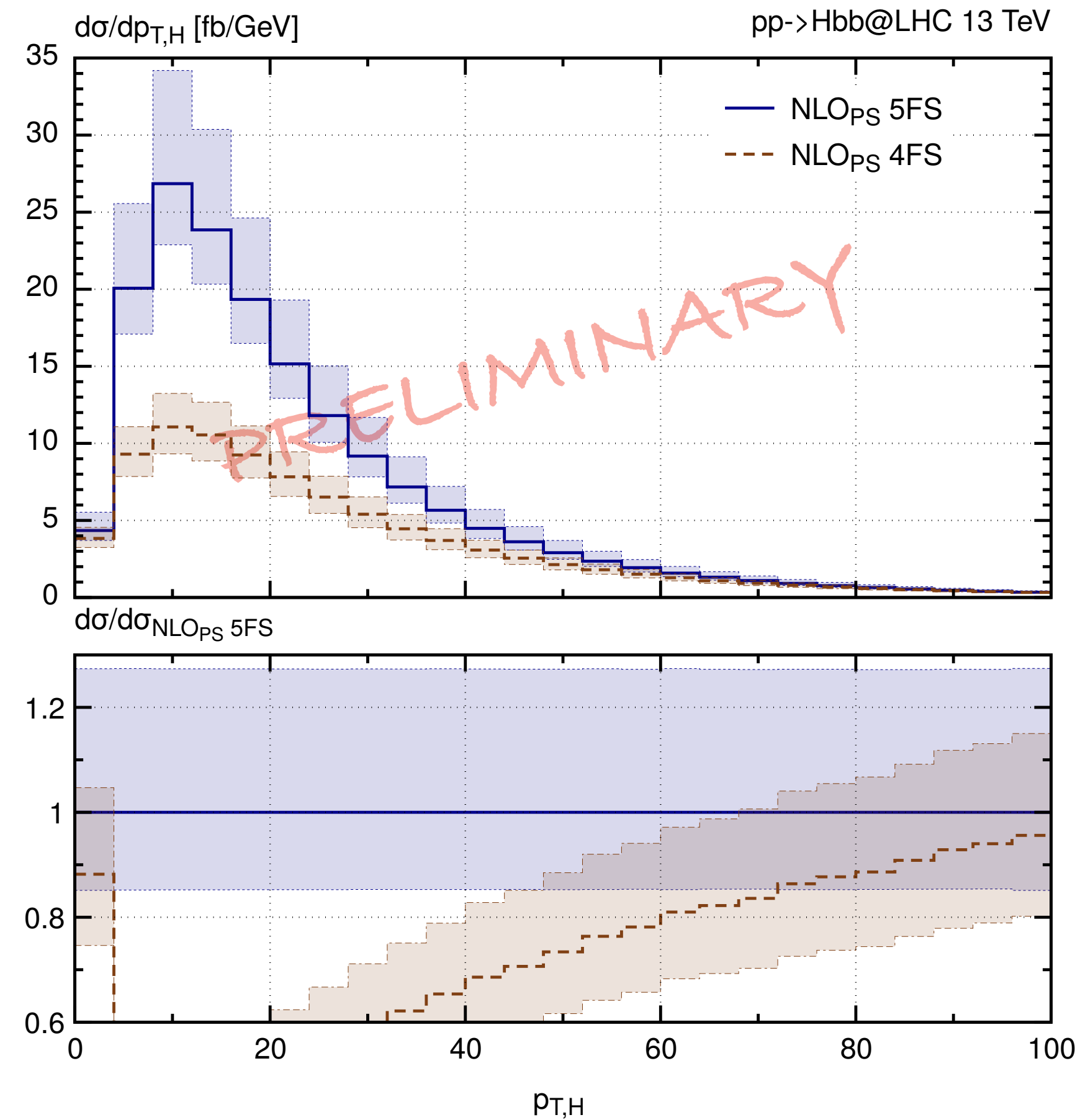
$$\mathcal{A}^{(2)} = \log(m_b)\text{-terms} + \text{const.} + \mathcal{O}\left(\frac{m_b}{Q}\right)$$

Massive vs massless



NNLO corrections in the 4FS solve the long-standing issue of discrepancies between the flavour-scheme predictions.

Higgs and one b-jet observables are in agreement between the two MiNNLOPS generators.





$NLO+PS_{LL}$

$NNLO+PS_{LL}$

$N^xLO+PS_{N^yLL}$

- NLO+PS are the standard of any analysis for a realistic modelling at colliders
- MiNNLOPS is a flexible and adaptive method to be applied to several processes with different features!
- Thanks to the accuracy of novel parton showers and the improvements in fixed-order calculations, we are in a promising period for the matching



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Thank you for the attention!

Backup slides

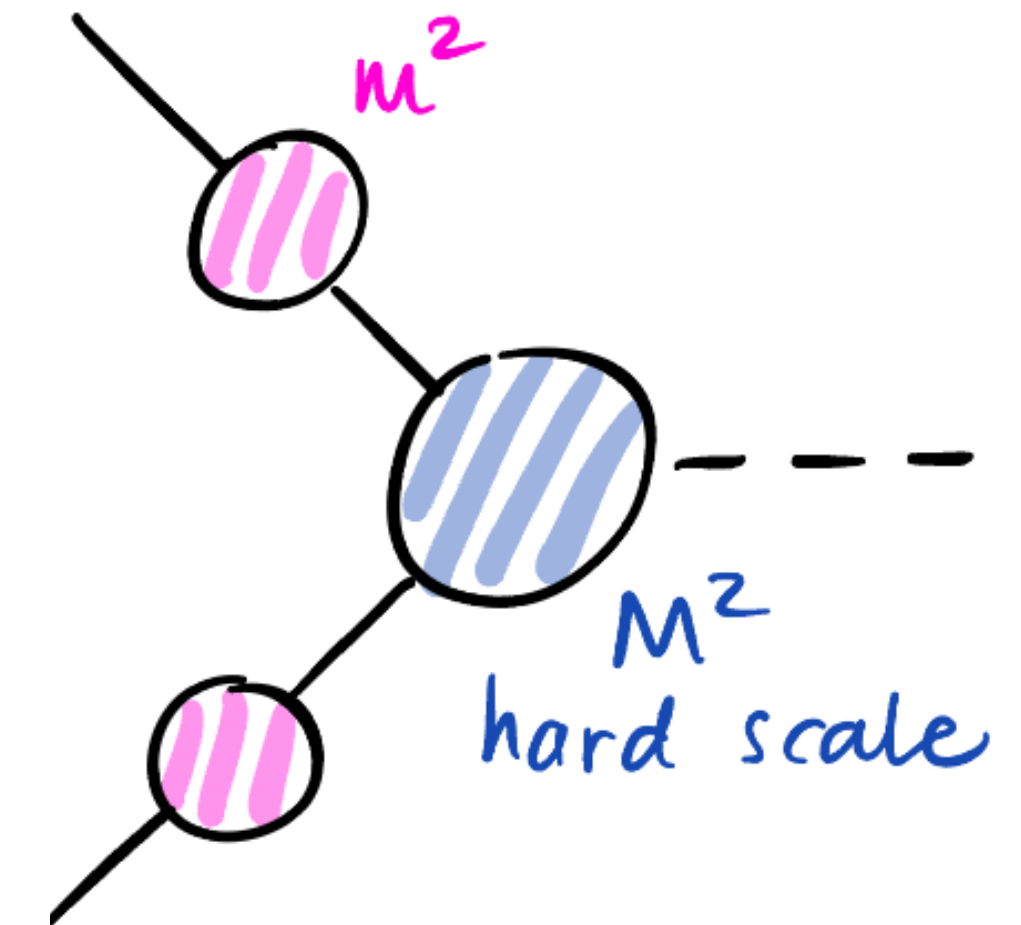


Resummation from factorisation

Consider a physical quantity $\mathcal{O}(M^2, m^2)$ in which m^2 measures the distance from the IR region.

$$\text{If } m^2 \ll M^2, \quad \mathcal{O}(M^2, m^2) = H \left(\frac{M^2}{\mu^2} \right) S \left(\frac{m^2}{\mu^2} \right)$$

Hard Soft



$$\mathcal{O} \text{ is } \mu \text{ - independent} \Rightarrow \frac{1}{H} \frac{d \ln H}{d \ln \mu^2} = - \frac{1}{S} \frac{d \ln S}{d \ln \mu^2} =: \gamma(\mu^2)$$

Solving the differential equation,

$$\mathcal{O}(M^2, m^2) = H(1) S(1) \exp \left[- \int_{m^2}^{M^2} \frac{dq^2}{q^2} \gamma(q^2) \right]$$

✓ for $m^2 \rightarrow 0$

Sudakov form factor:
it captures at *all order*
the log-enhanced terms



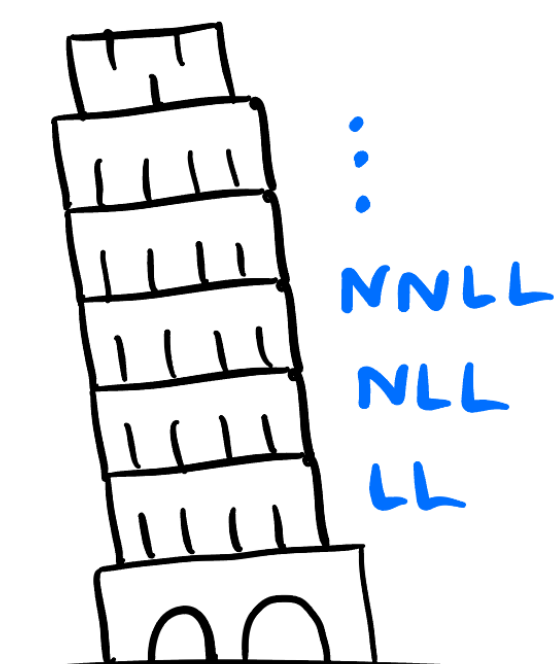
Transverse momentum resummation

What is the probability that a Higgs boson is produced with transverse momentum $< p_T$?

$$\mathcal{P} \simeq -\#\alpha_s \ln^2 \frac{m_H}{p_T} + \mathcal{O}(\alpha_s^2) \rightarrow \exp \left[-\#\alpha_s \ln^2 \frac{m_H}{p_T} \right]$$

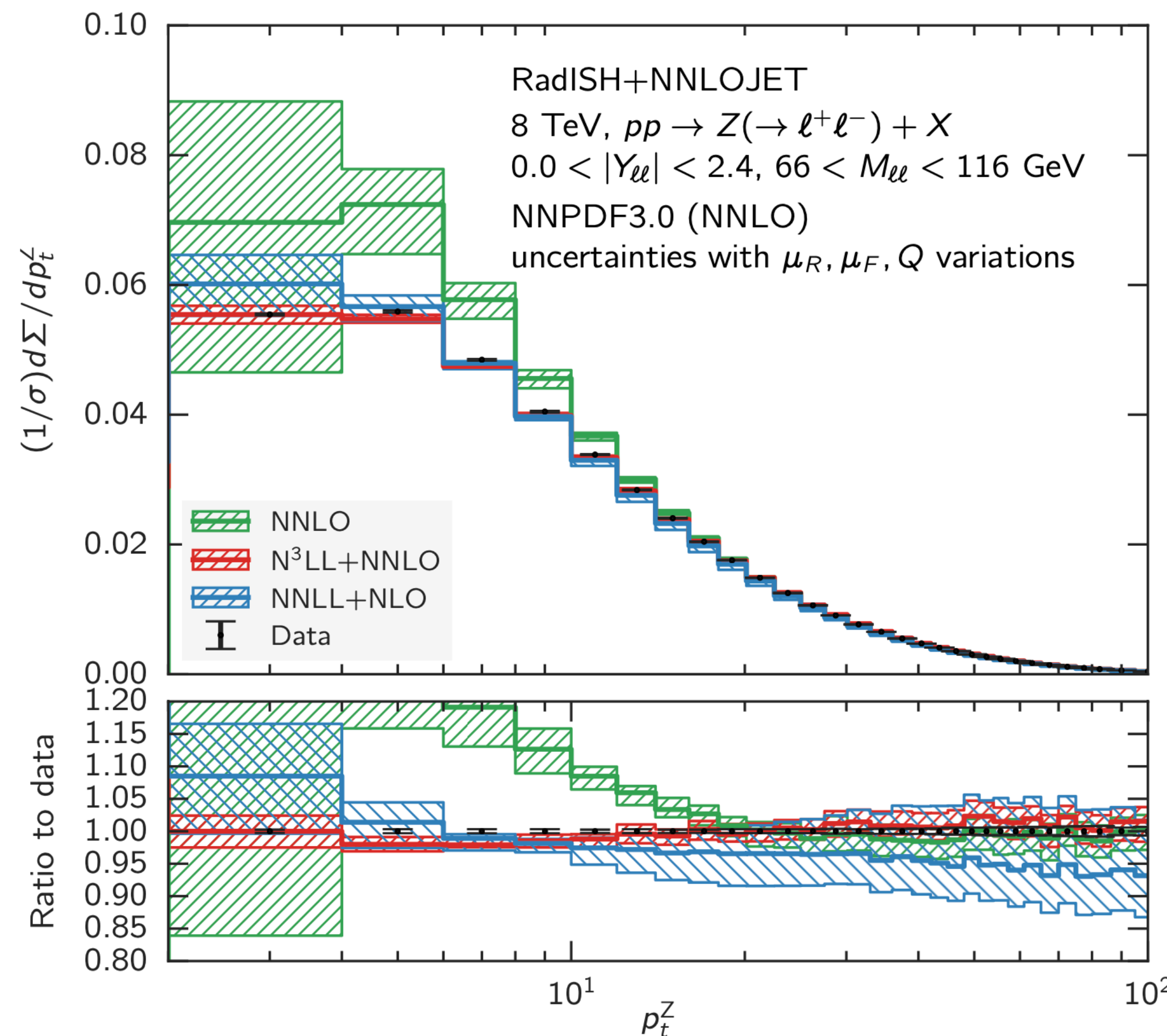
for small p_T we need to sum up the logs

In general we have a tower of logs



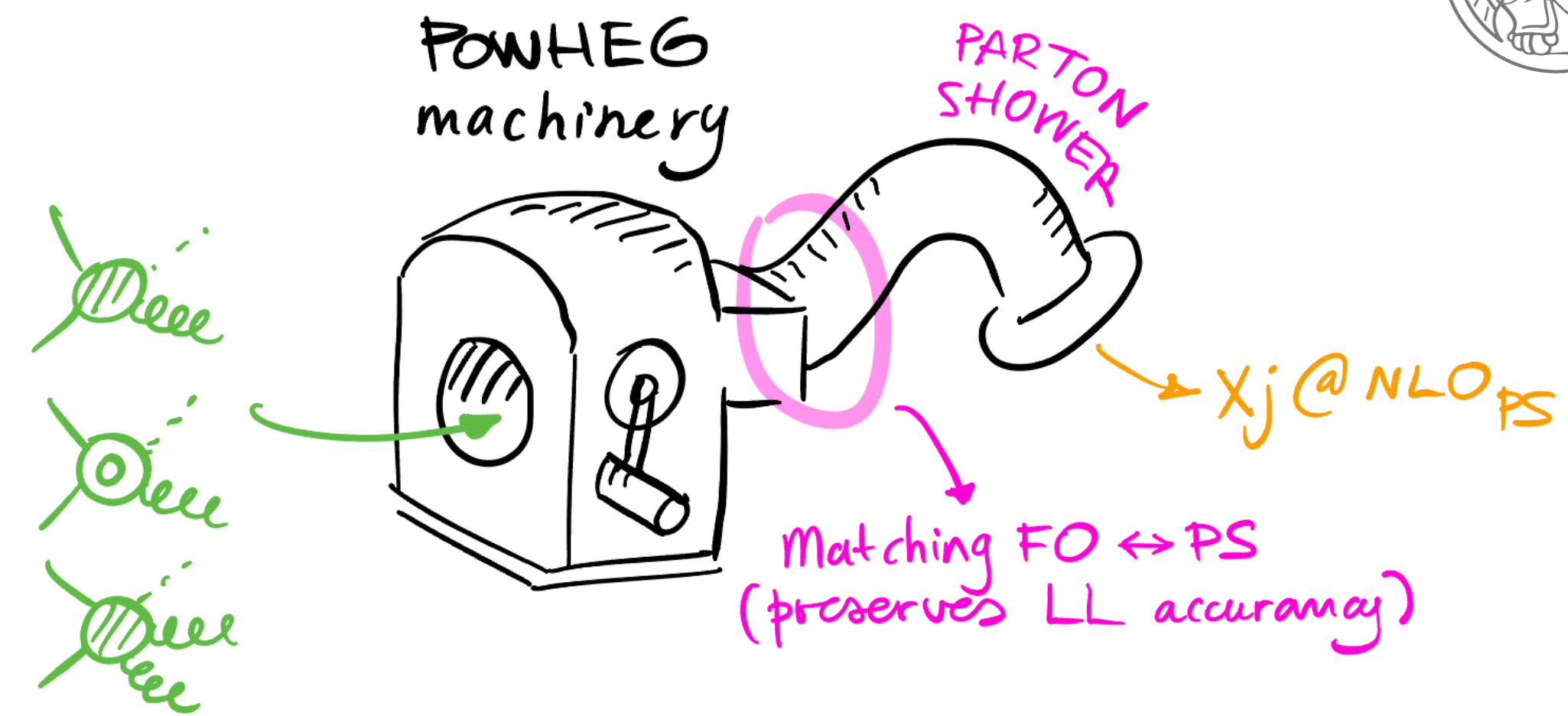
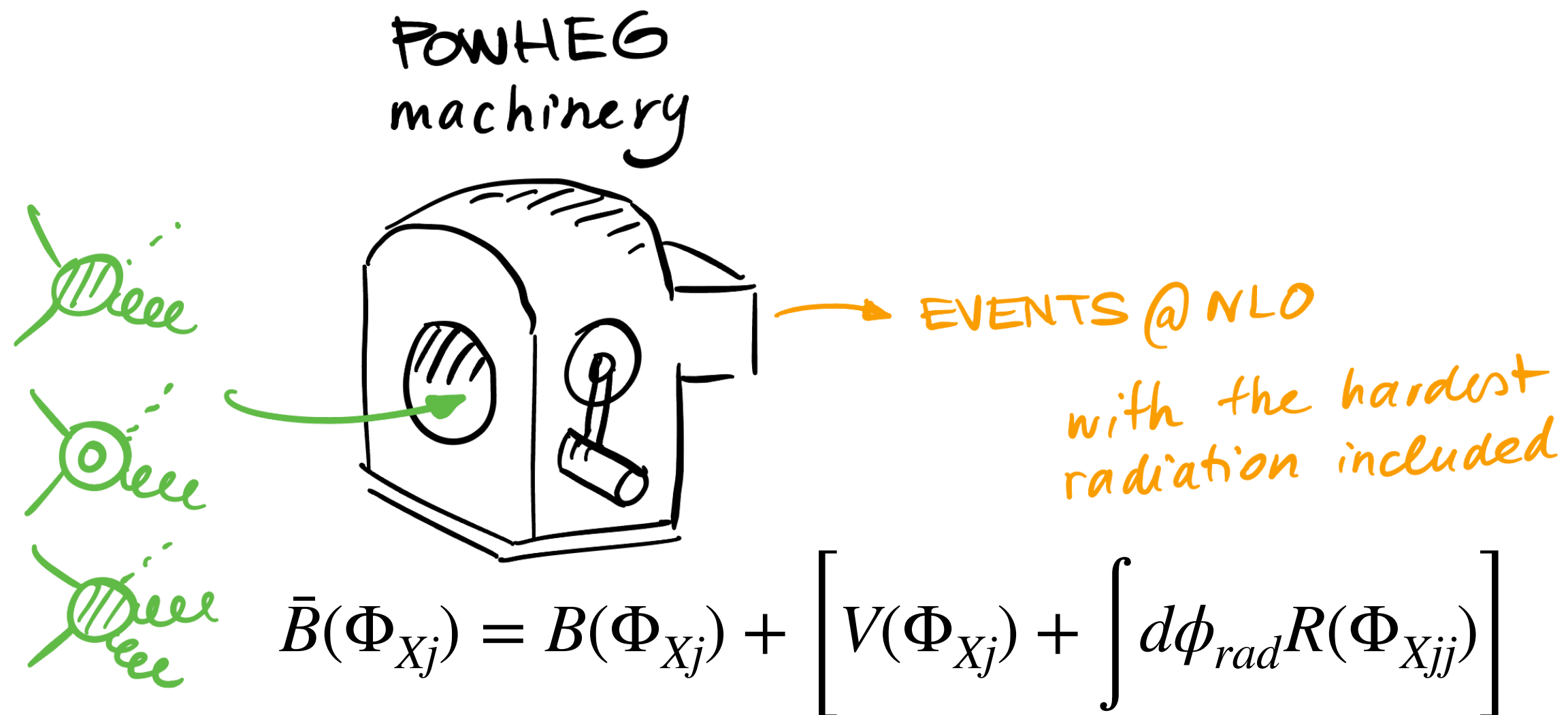
$$\exp \left[-\sum_{n,m} \alpha_s^n \ln^m \frac{m_H}{p_T} \right]$$

- $m = n + 1$ → Leading Logs (LL)
- $m = n$ → Next-To-LL (NLL)
- $m = n - 1$ → Next-To-NLL (NNLL) ...

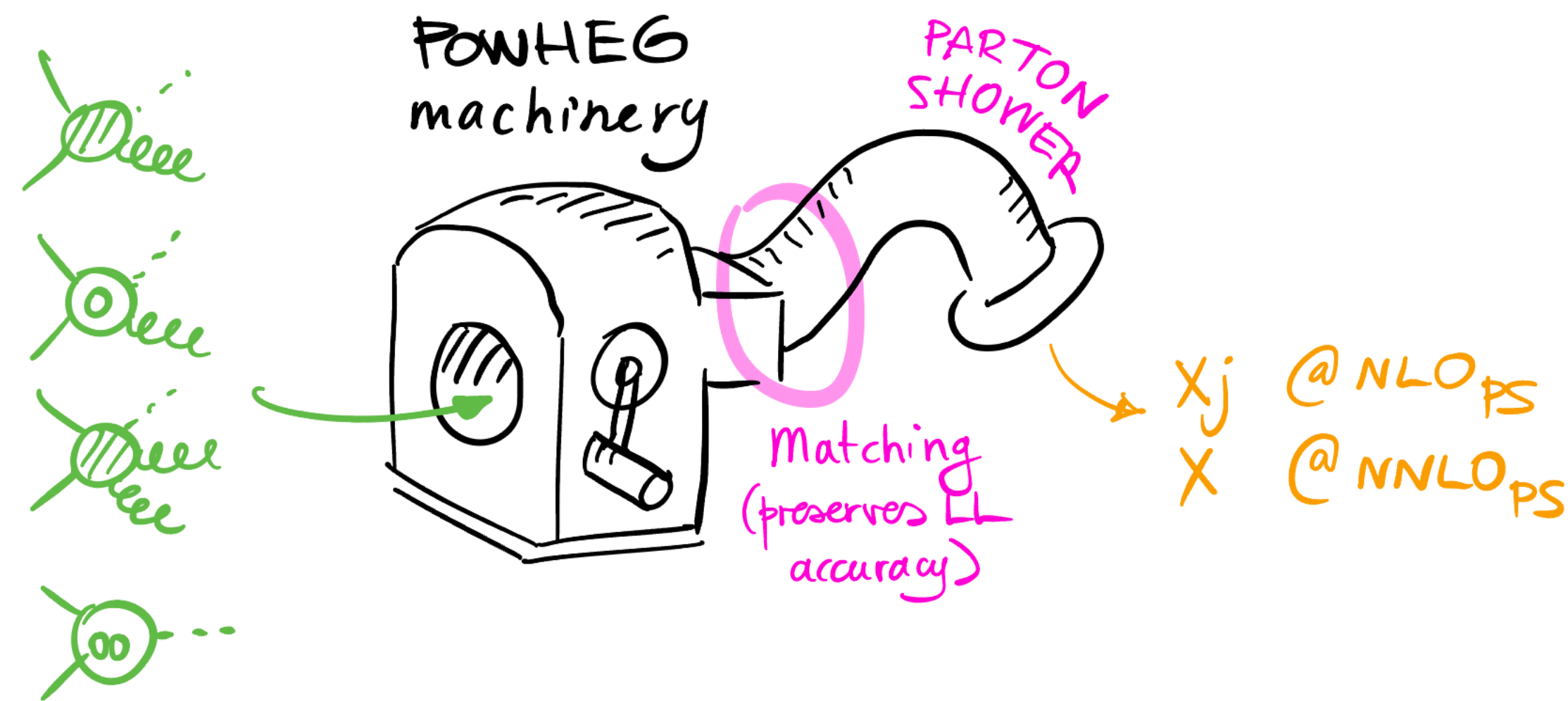
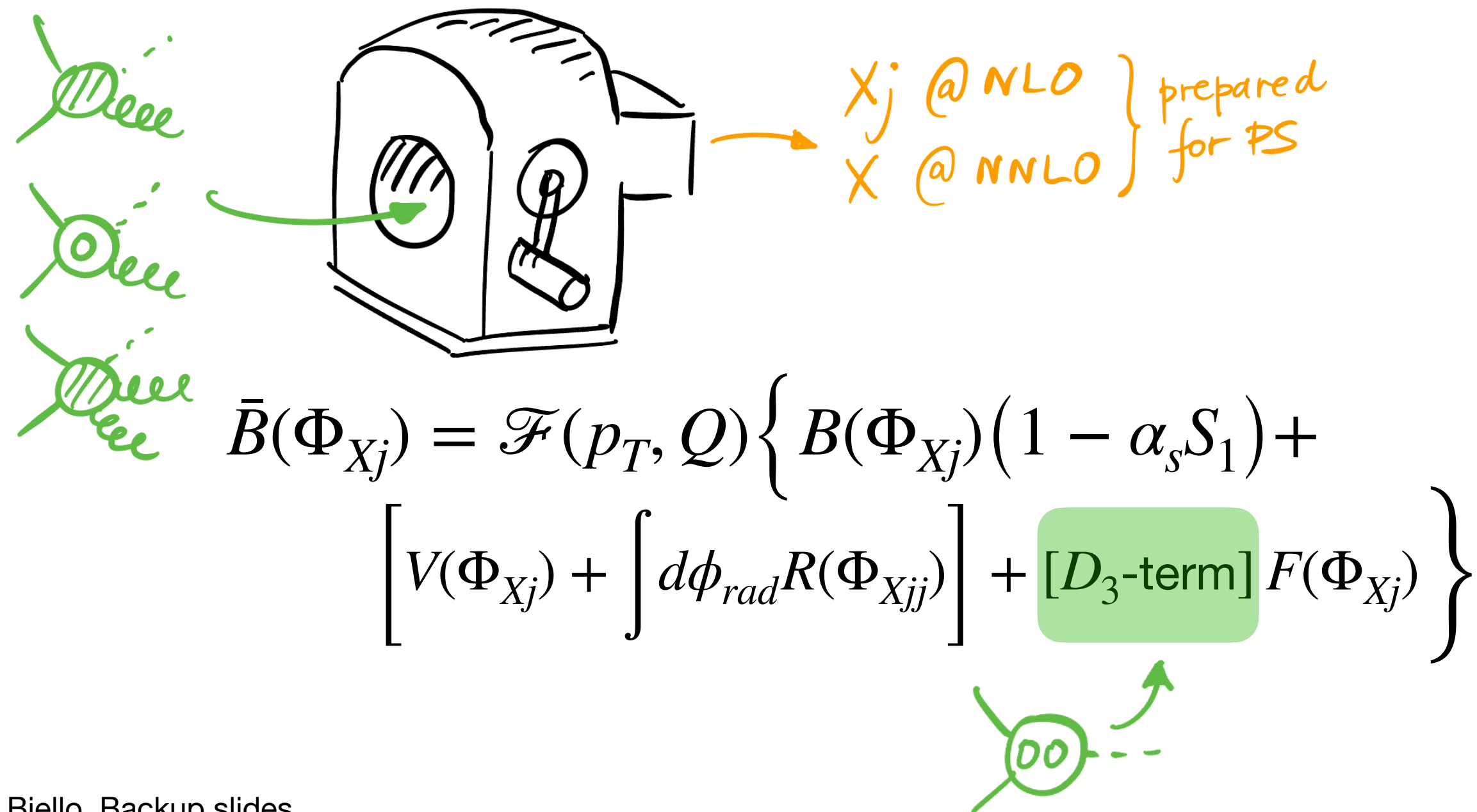




POWHEG



MINNLO+POWHEG





MiNNLOps in a nutshell

$$NLO X_j \longrightarrow NNLO X$$

MiNNLOps is an extension of MiNLO' to achieve NNLO+PS accuracy for inclusive observables.

Monni, Nason, Re, Wiesemann, Zanderighi [1206.3572]

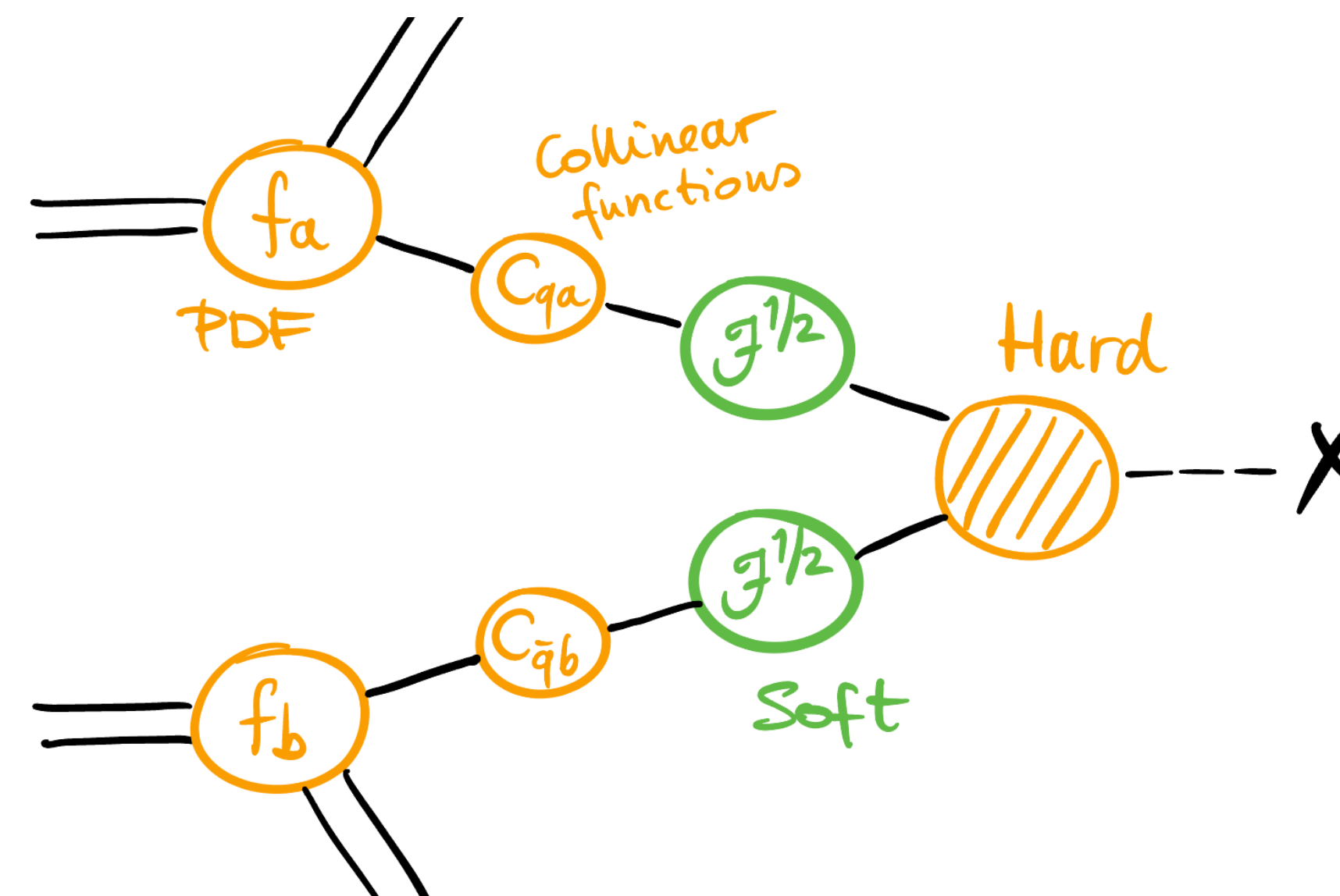
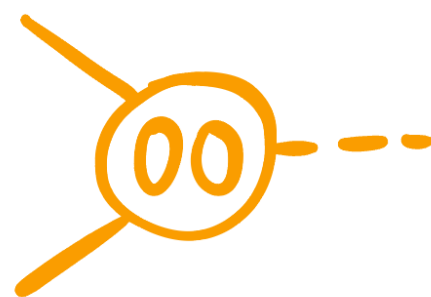
Split the differential inclusive cross-section into the singular and regular part in the small transverse momentum limit: $d\sigma = d\sigma^{sing} + d\sigma^{reg}$.

$$\frac{d\sigma^{sing}}{dp_T d\Phi_X} = \frac{d}{dp_T} \left\{ \mathcal{F}(p_T) \mathcal{L}(p_T) \right\} =: \exp \left[-\tilde{S}(p_T) \right] D(p_T)$$

Sudakov form factor

$$\mathcal{F}(p_T) = \exp \left[-\tilde{S}(p_T) \right]$$

Luminosity: it also contains





MiNNLOps in a nutshell

$$d\sigma = d\sigma^{sing} + d\sigma^{reg}$$

The modified POWHEG function is

$$\bar{B}(\Phi_{XJ}) = e^{-\tilde{S}(p_T)} \left\{ B \left(1 - \alpha_s(p_T) \tilde{S}^{(1)} \right) + V + \int d\phi_{rad} R + \left[D(p_T) - D^{(1)} - D^{(2)} \right] \times F^{corr} \right\}$$

MiNLO' structure

Extra term: it ensures NNLO accuracy.

F^{corr} encodes the spreading of the D-terms upon the full Φ_{XJ} .

- In the singular part, the QCD scales must be $\mu_F \sim \mu_R \sim p_T$.
- For the regular part, different scale choices can be performed:
 - the transverse momentum p_T (original choice)
 - the **hard scale** Q (FOatQ=1)

Gavardi, Oleari, Re [2204.12602]

5FS results

Same PDFs:
NNPDF40_nnlo_as_01180
with 5 active flavours



Comparison of the total inclusive cross section with FO results obtained with the public code **SusHi** with $\mu_R = \mu_F = m_H$

Harlander, Lieber, Mantel [1212.3249]

Process	NLO (SUSHi)	NNLO (SUSHi)	MINLO'	MINNLO _{PS}
$b\bar{b} \rightarrow H$	$0.646(0)^{+10.4\%}_{-10.9\%}$ pb	$0.518(2)^{+7.2\%}_{-7.5\%}$ pb	$0.571(1)^{+17.4\%}_{-22.7\%}$ pb	$0.509(8)^{+2.9\%}_{-5.3\%}$ pb

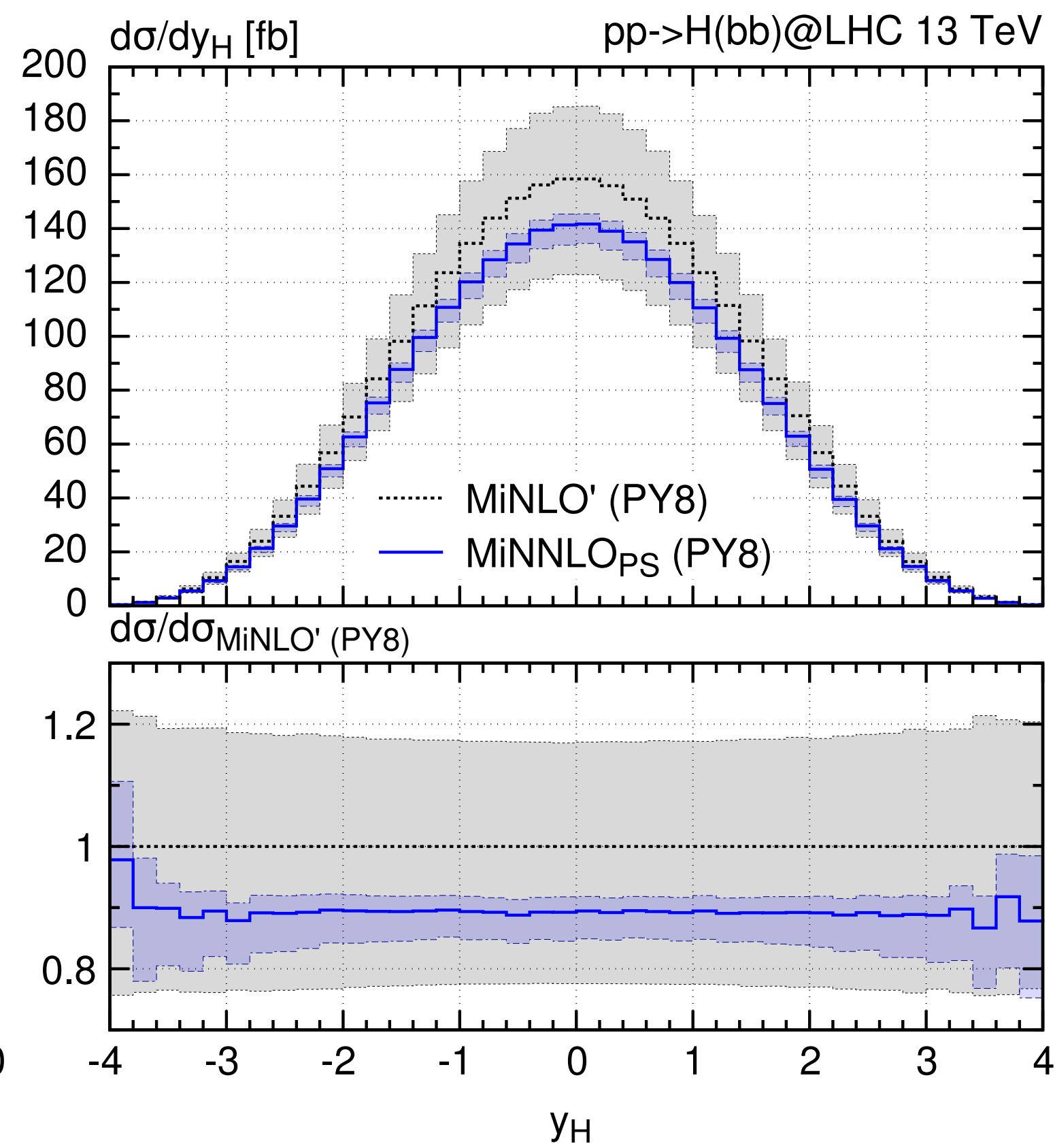
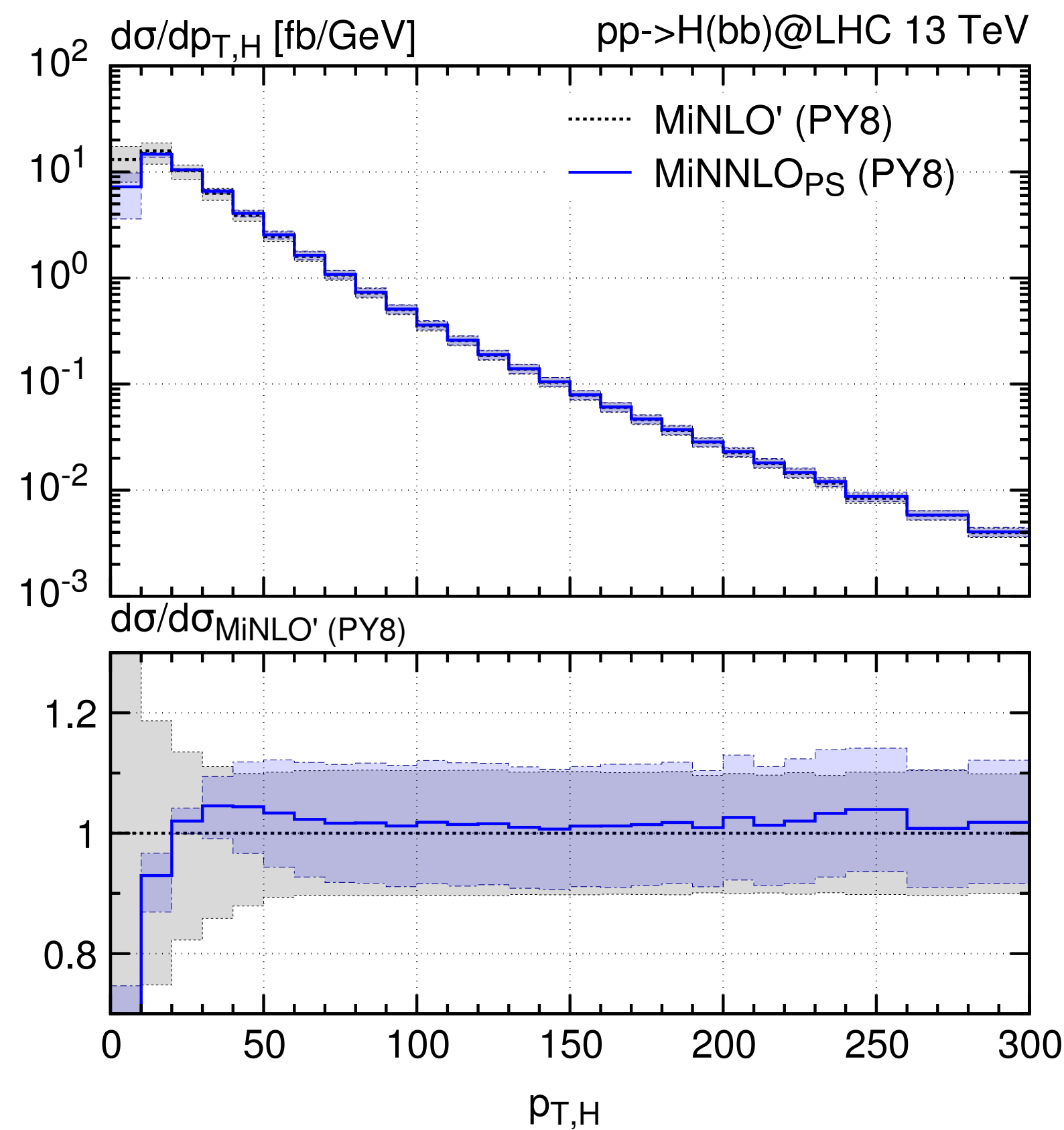
- NNLO cross section is reduced by $\sim 20\%$
- Scale uncertainties significantly reduced at NNLO
- Our MiNNLOPS predictions are in agreement with **SusHi** within the uncertainties



Comparison of MiNLO' and MiNNLOPs

Transverse momentum spectrum of the Higgs boson

Rapidity distribution of the Higgs boson

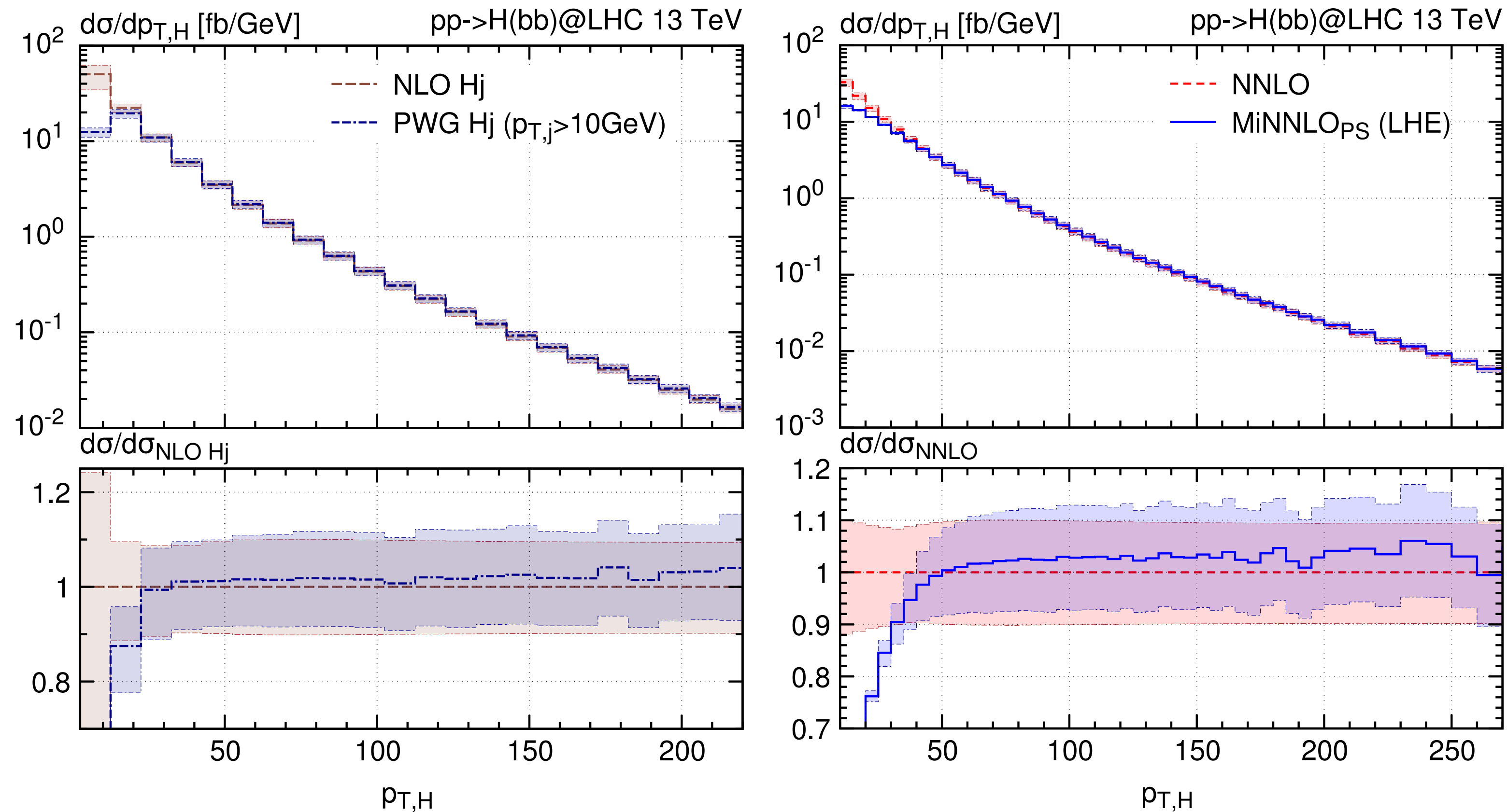


- At small $p_{T,H}$, **MiNNLOPs** significantly damps the distribution
- At high $p_{T,H}$, **MiNNLOPs** and **MiNLO'** coincide, both NLO accurate
- **MiNNLOPs** has a flat negative correction in the rapidity y_H distribution



Comparison with FO results

Transverse momentum spectrum of the Higgs



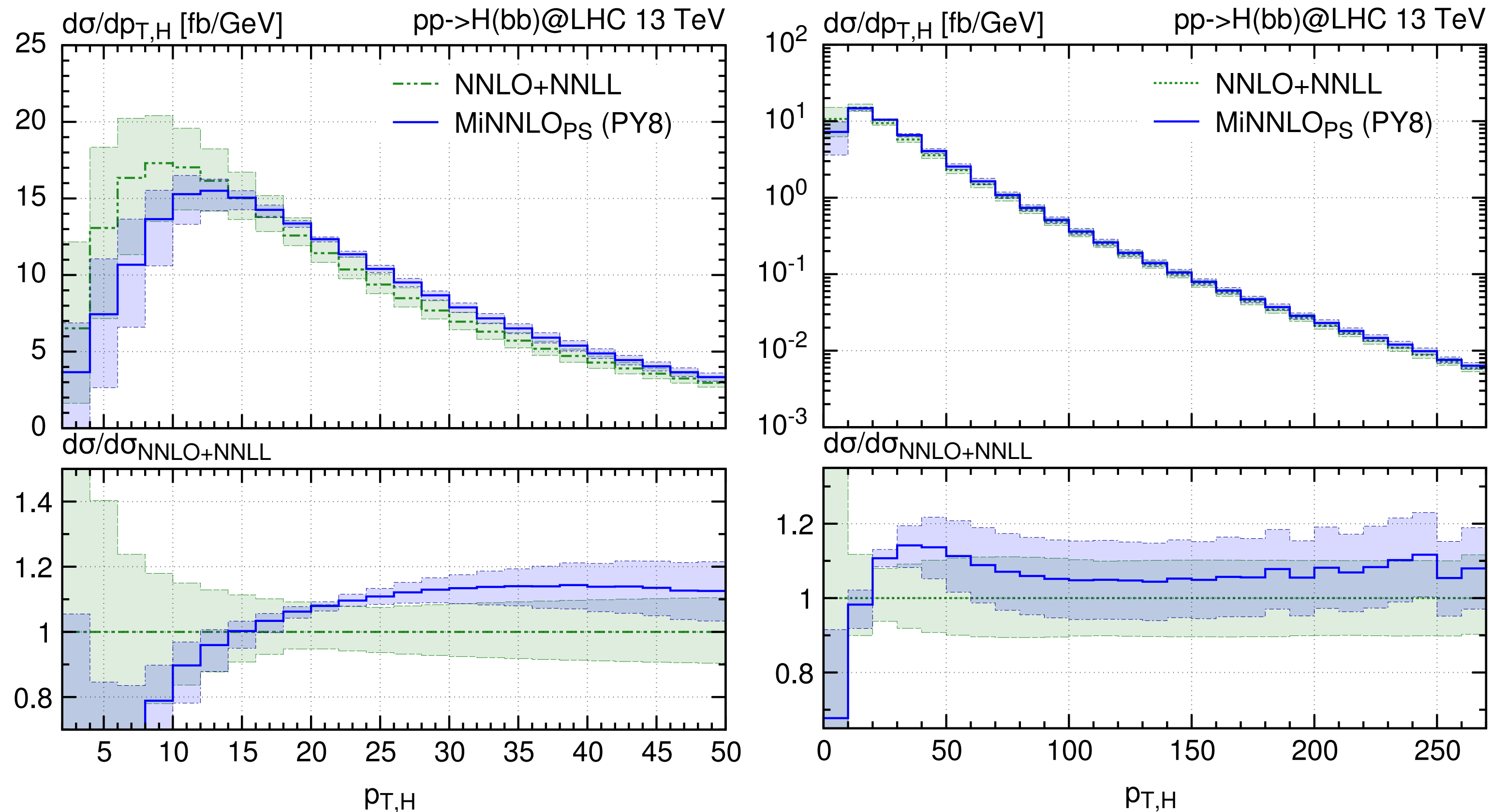
Full **agreement** at large transverse momenta $p_{T,H}$ with analytic **fixed-order** predictions

NLO Higgs Harlander, Ozeren, Wiesemann [1007.5411]
NNLO Harlander, Tripathi, Wiesemann [1403.7196]



Comparison with resummed results

Transverse momentum spectrum of the Higgs



We compare the MiNNLO implementation with the NNLO+NNLL results for low and high $p_{T,H}$

- Acceptable agreement for small $p_{T,H}$
- The shower has an effect on the tail

NNLO+NNLL Harlander, Tripathi, Wieseemann [1403.7196]

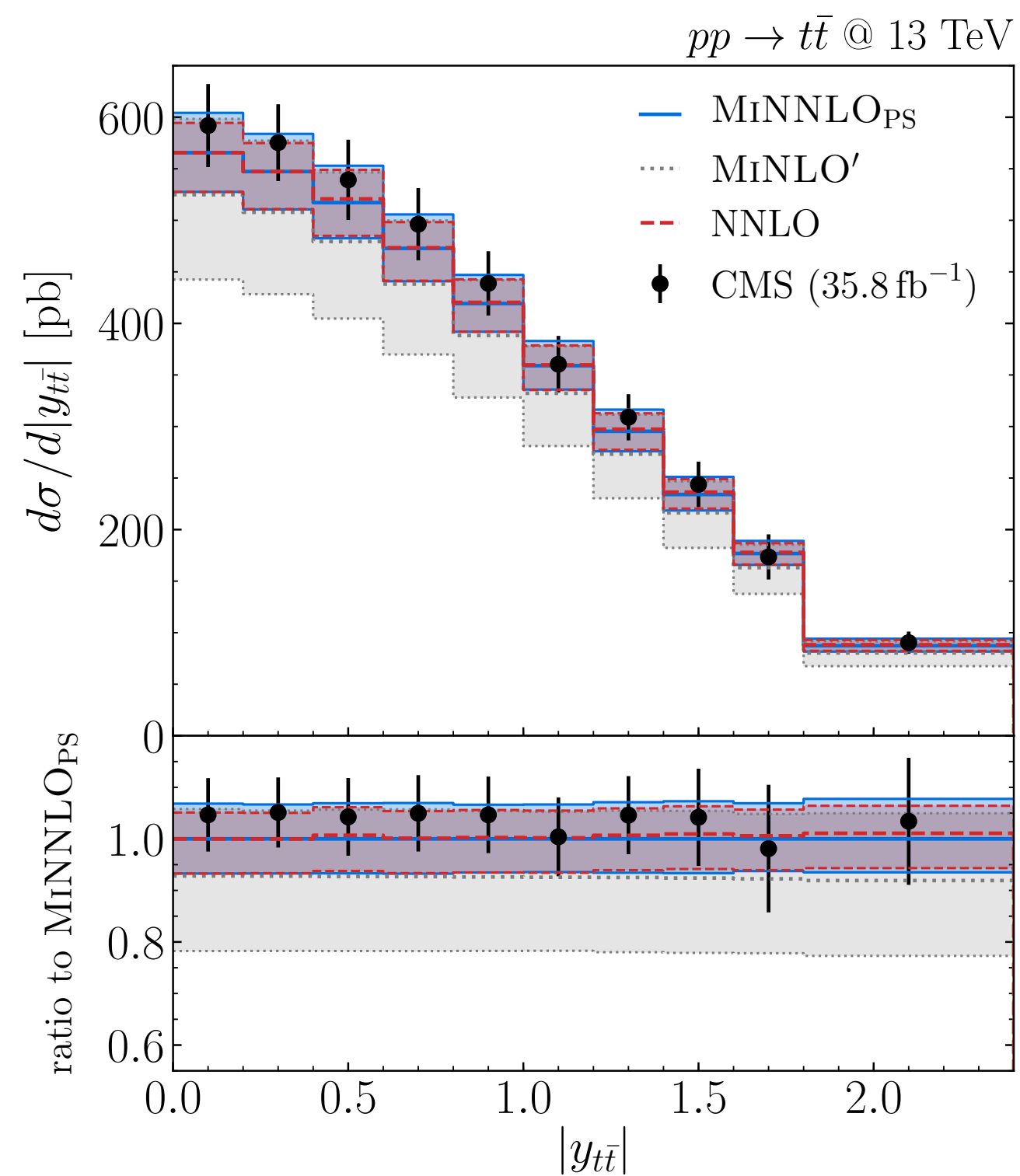
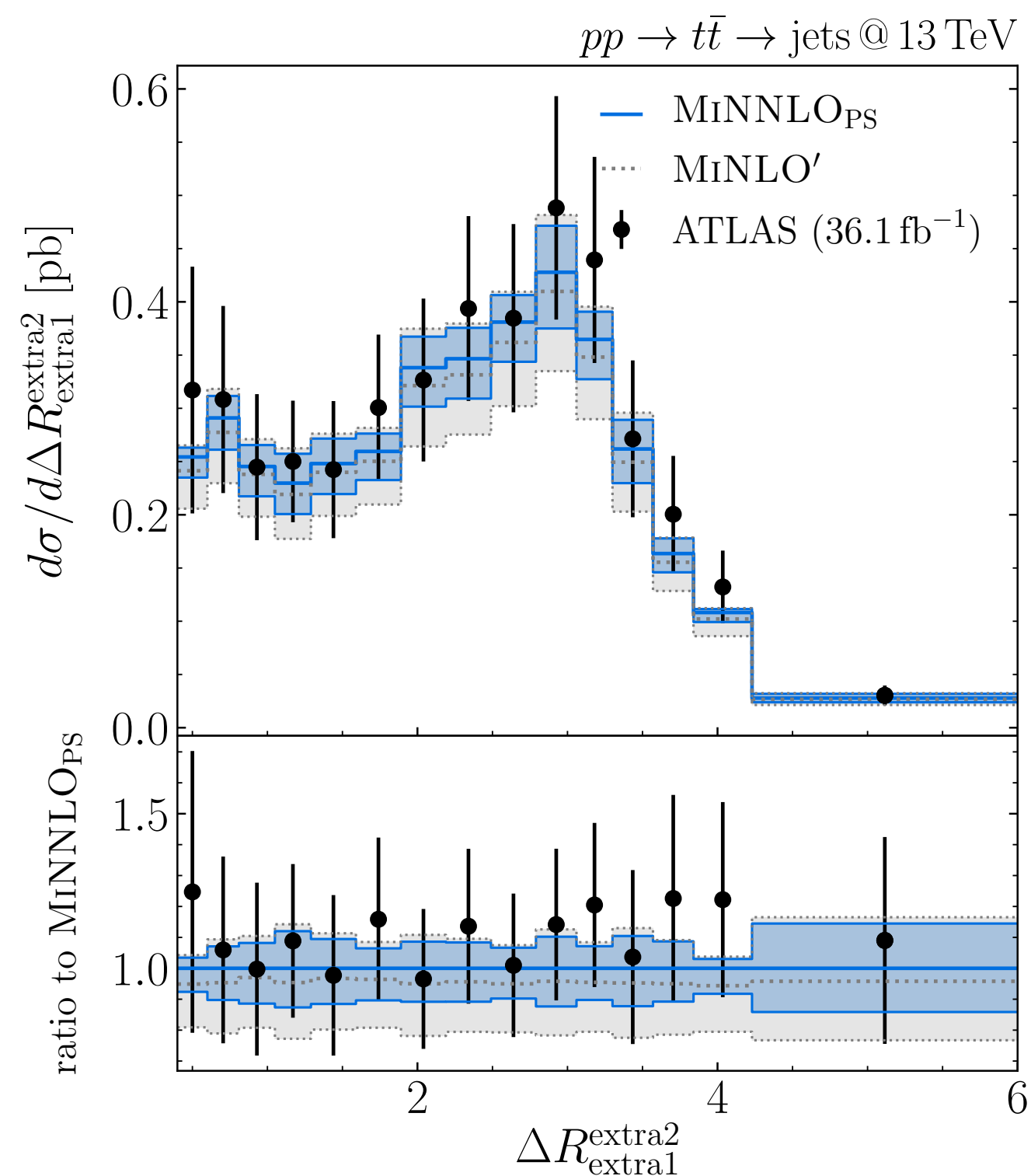


Heavy-quark pair production

The method was generalised for coloured final states with an **intensive phenomenological comparison** against ATLAS, CMS and LHCb data.

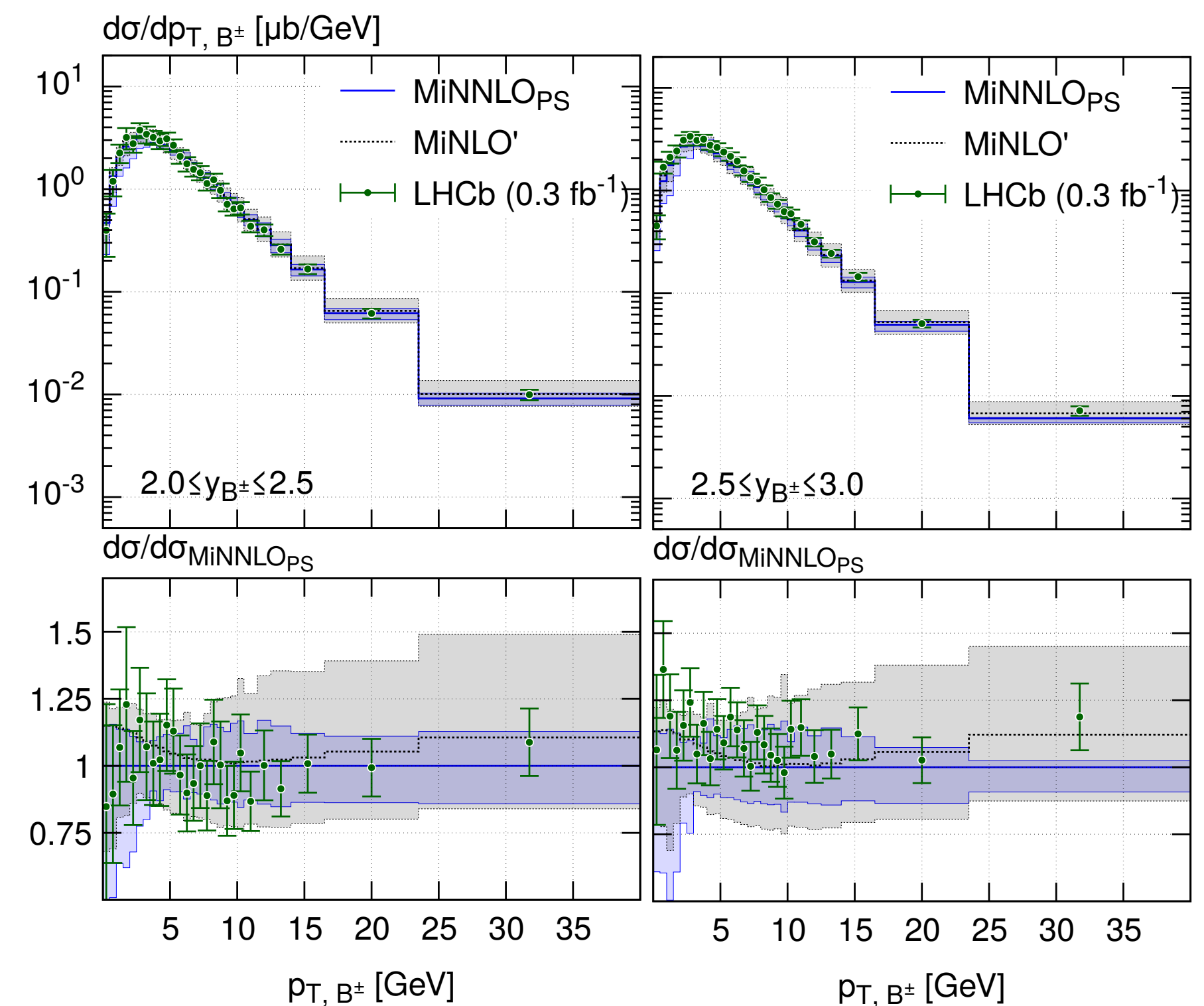
$t\bar{t}$

Mazzitelli, Monni, Nason, Re,
Wiesemann, Zanderighi [2112.12135]



$b\bar{b}$

Mazzitelli, Ratti, Wiesmann,
Zanderighi [2302.01645]



Massification



Biello, Mazzitelli, Sankar, Wiesemann,
Zanderighi [in progress]

First two-loop massification in Bhabha scattering

Penin [hep-ph/0508127]

Extension for non-abelian theories from
factorisation principles

Mitov, Moch [hep-ph/0612149]

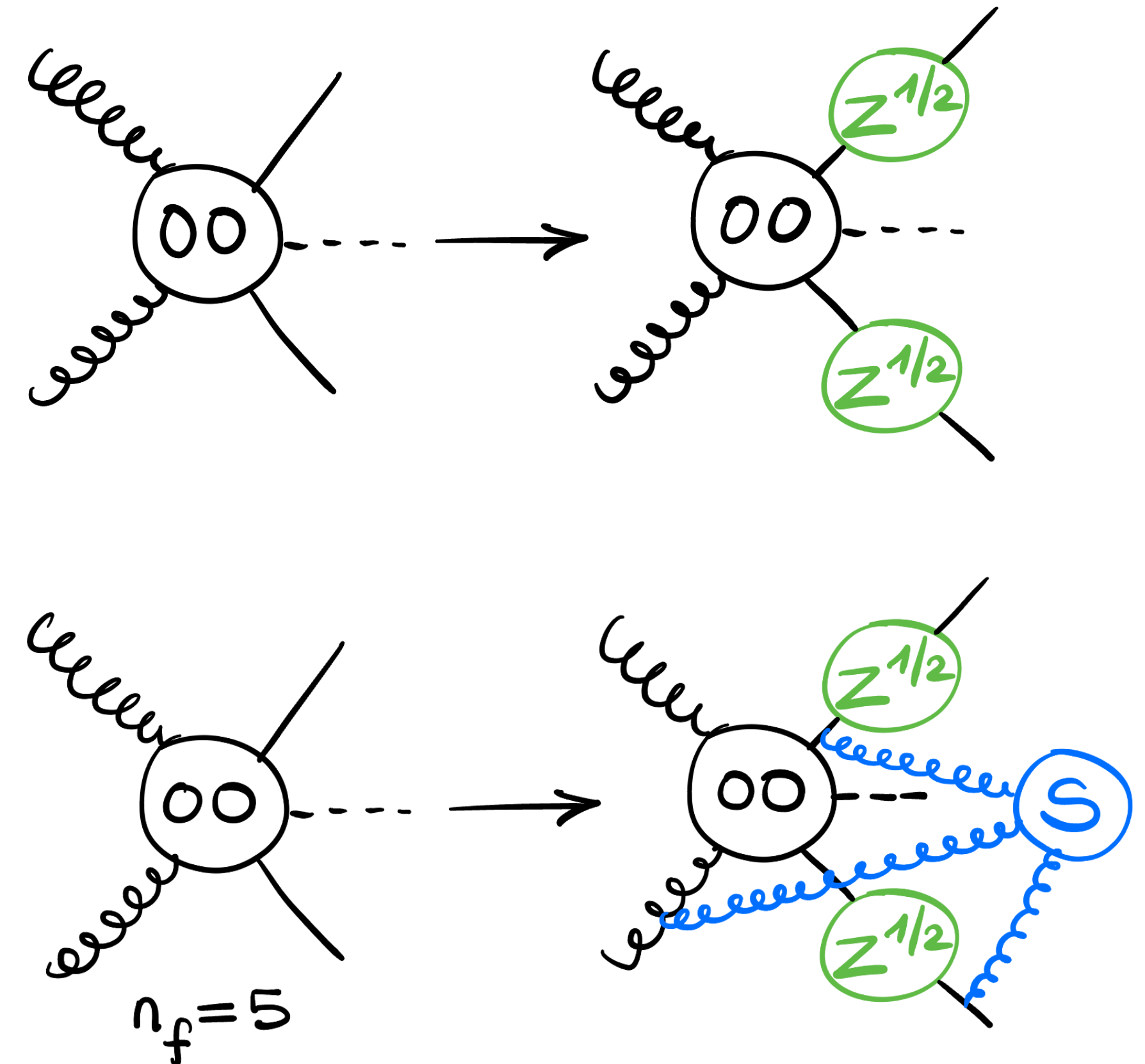
First massification of internal loops in Bhabha
using the SCET formalism

Becher, Melnikov [0704.3582]

Recent application for QCD amplitudes

Wang, Xia, Yang, Ye [2312.12242]

We applied decoupling relations for α_s and $\overline{\text{MS}}$
Yukawa



Cross-checks with the independent implementation of Chiara Savoini

