

SM & MSSM CORRECTIONS TO TOP-QUARK HADRO-PRODUCTION IN DOUBLE & SINGLE TOP CHANNELS

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IN COLLABORATION WITH

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DISCLAIMER

- WILL NOT DESCRIBE SM QCD EFFECTS (APART FROM $A_{FB}(t\bar{t})$)
- WILL CONCENTRATE ON: SM EW, MSSM EW & QCD
- ONLY LHC 14 TEV RESULTS

OUTLINE

- WHY EW CORRECTIONS CAN BE IMPORTANT IN HADRONIC PROCESSES
- SM EW EFFECTS IN TOP-QUARKS HADRO-PRODUCTION
- MSSM QCD & EW EFFECTS THEREIN
- SUMMARY

CORRECTIONS TO HADRONIC OBSERVABLES: QCD vs EW

- LARGE SCALE DEPENDENCE OF HIGHER ORDER CORRECTIONS OFTEN DOMINATES THEORETICAL UNCERTAINTIES !
- QCD CORRECTIONS TYPICALLY LARGEST:

$$\alpha_S \approx 10 \alpha_{EW} \quad (\alpha_{EW} = \alpha_{EM} / \sin^2 \theta_W).$$

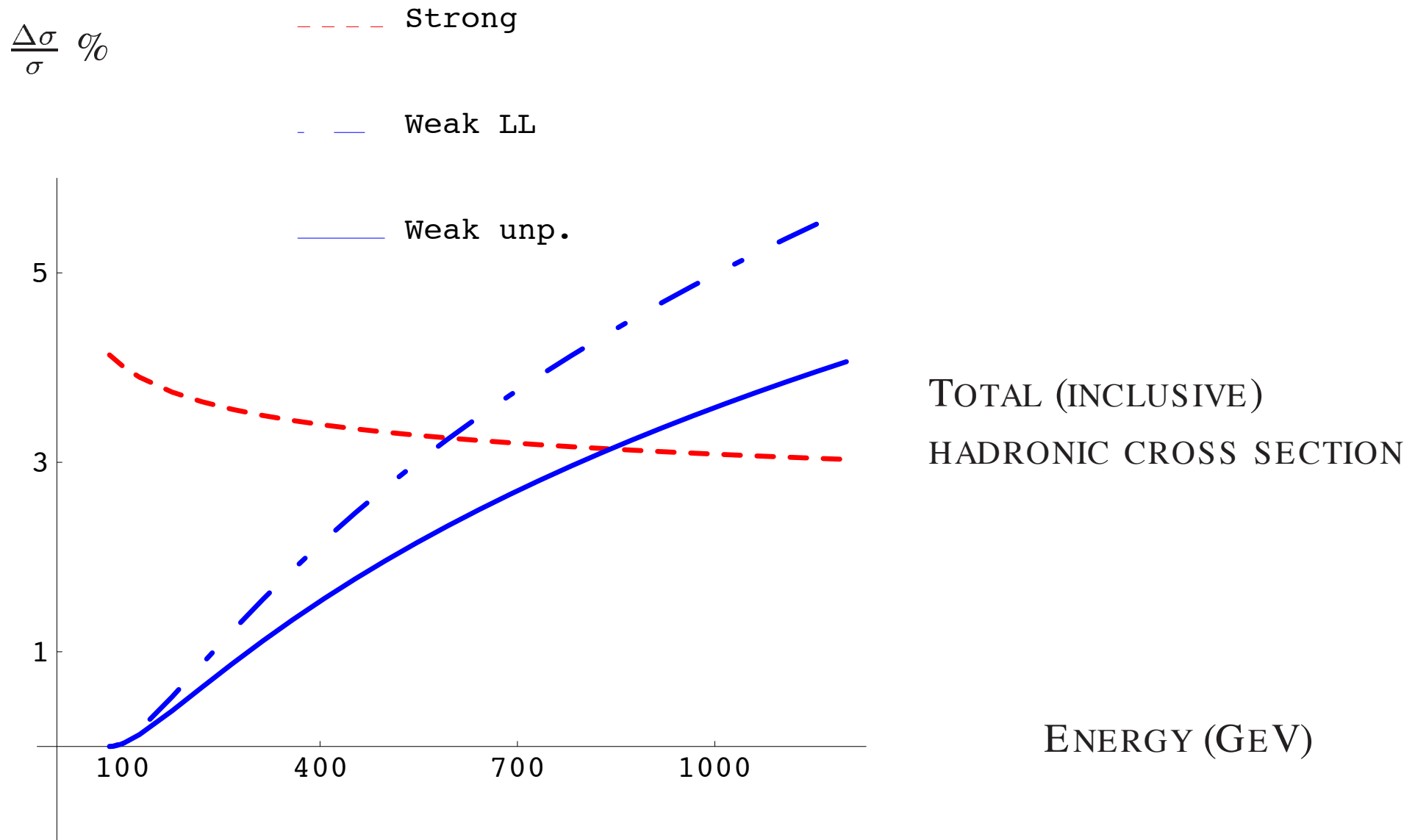
BUT

- THERE ARE LARGE LOG AROUND IN EW CASE: AT $\sqrt{s} = 1 \text{ TeV}$

$$\frac{\alpha}{4\pi s_W^2} \log^2 \frac{s}{M_W^2} = 6.6\%, \quad \frac{\alpha}{4\pi s_W^2} \log \frac{s}{M_W^2} = 1.3\%.$$

- NNLO QCD CORRECTIONS WILL SOON BE AVAILABLE: RECALL $\alpha_S^2 \approx \alpha_{EW}$!

- CONSIDER LEPTONIC COLLISIONS: AT HIGH ENERGIES, $\sqrt{s} \gg M_W$ (ILC, 0.5 TO 3 TeV), EW INTERACTIONS BECOME STRONG:

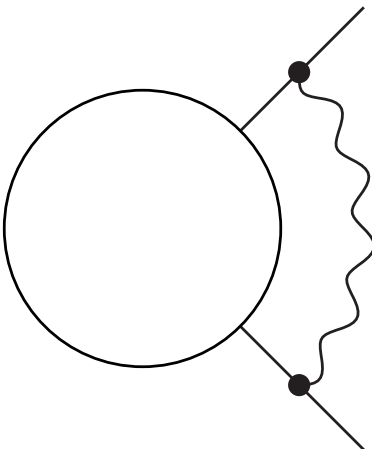


SUDAKOV LOGS² IN A NUTSHELL

- CORRESPOND TO SOFT AND COLLINEAR SINGULARITIES IN THEORIES WITH MASSLESS BOSONS, WHERE THEY ARE CANCELED BY REAL RADIATION.
- REGULATED BY BOSON MASS IN EW CASE: THEY ARE FINITE !

PHYSICAL DEPENDENCE ON IR CUT-OFF M_W REMAINS

- IN FEYNMAN GAUGE THEY ARE ASSOCIATED WITH VIRTUAL GRAPHS WHERE SOFT-COLLINEAR BOSONS ARE EXCHANGED BETWEEN EXTERNAL LEGS. (IN AXIAL GAUGE THEY ARE ASSOCIATED WITH SELF ENERGY GRAPHS ON EXTERNAL LEGS.)
- DL ARE UNIVERSAL: ONLY DEPEND ON EXTERNAL PARTICLES !

$$\sum_{k=1}^n \sum_{l < k} \sum_{V_a = A, Z, W^\pm}$$


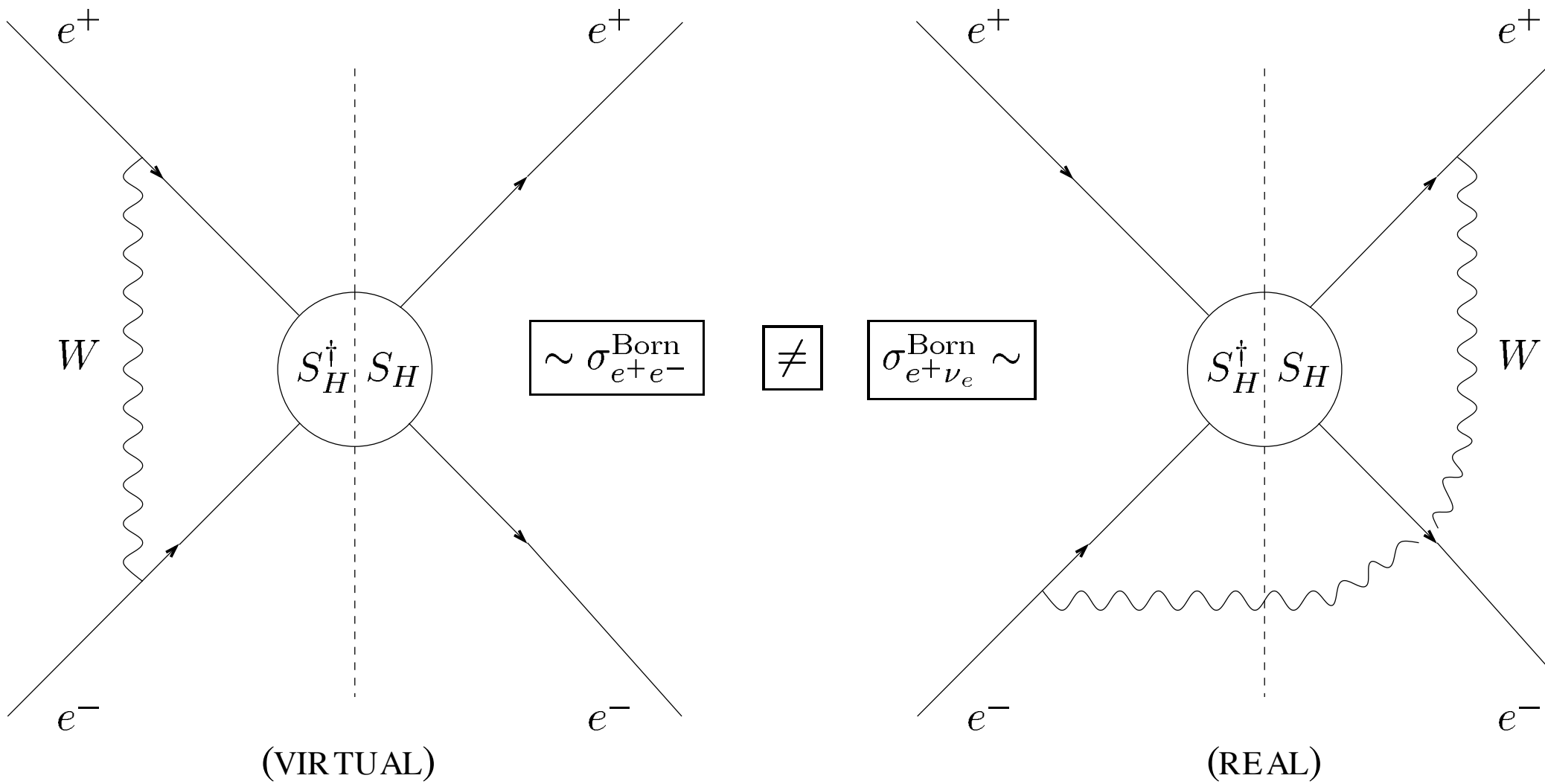
The diagram shows a circle representing a loop. Two external lines, labeled k and l , enter and exit the circle at two vertices marked with black dots. A wavy line, labeled V_a , connects these two vertices, forming a loop with the circle.

$$= \sum_{k=1}^n \sum_{l < k} \sum_{V_a = A, Z, W^\pm} \alpha/4\pi \log^2(r_{kl}/M^2) T_{kl}$$

$$\log^2 \frac{r_{kl}}{M^2} = \log^2 \frac{s}{M^2} + 2 \log \frac{s}{M^2} \log \frac{r_{kl}}{s} + \log^2 \frac{r_{kl}}{s} \quad r_{kl} = (p_k \pm p_l)^2$$

- NUMERICALLY AT TeV ENERGIES THERE ARE LARGE CANCELLATIONS BETWEEN DOUBLE LOG (DL) AND SINGLE LOG (SL) CONTRIBUTIONS.

- DL (AND SL) DO NOT CANCEL IN INCLUSIVE MEASUREMENTS (AKA VIOLATION OF BLOCH-NORDSIECK THEOREM IN NON-ABELIAN THEORIES).
- COLOURLESS HADRONS FORCE SUMMATION/ AVERAGING OVER INITIAL COLOUR STATES: CANCELLATION IS RECOVERED IN QCD (KLN THEOREM).
- EW CASE: ANALOGOUS WOULD BE FLAVOUR/ ISOSPIN SUMMATION/ AVERAGING, IMPOSSIBLE EXPERIMENTALLY.
- SL ARE NON-UNIVERSAL !
- NON-LOG (FINITE) TERMS ARE ALSO PROCESS DEPENDENT.



- EXAMPLE: e^+e^- WOULD CANCEL AGAINST $e^+\nu_e$

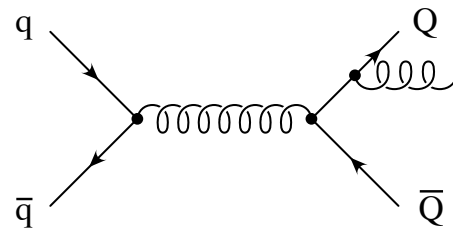
- CONSIDER EXCLUSIVE FINAL STATES, Z/W RADIATION EASILY RESOLVED EXPERIMENTALLY:

REAL & VIRTUAL LOGS ARE FINITE, NEED NOT BE RESUMMED.

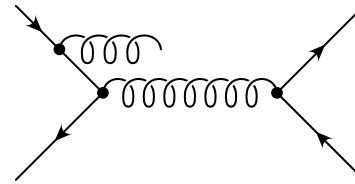
- HENCE ADDITIONAL DL AND SL IN CASE OF Z EXCHANGE.
- COMPUTE ONLY VIRTUAL CONTRIBUTIONS: NEGATIVE EFFECTS DOMINATE INCLUSIVELY.
- NON-TRIVIAL HELICITY STRUCTURE: INTRODUCE PARITY-VIOLATING & SPIN ASYMMETRIES (BACKGROUND TO NEW PHYSICS).
- LEADING ($\sim \alpha_W^n \log^{2n}(s/M_W^2)$), SUB-LEADING ($\sim \alpha_W^n \log^{2n-1}(s/M_W^2)$) AND SUB-SUB-LEADING ($\sim \alpha_W^n \log^{2n-2}(s/M_W^2)$) LOGS CAN BE RESUMMED (INCLUSIVE FINAL STATES).
- CONSIDER HERE FIXED ORDER (INCLUDING FINITE TERMS).
- (CAN SEPARATE WEAK FROM QED CORRECTIONS IN SOME PROCESSES).

FORWARD-BACKWARD ASYMMETRY FROM QCD

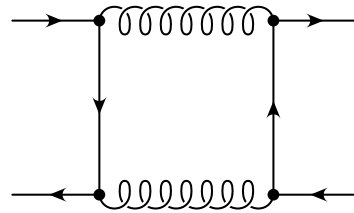
[J .H. KÜHN, G. RODRIGO, PRL81:49,1998 & PRD59:054017,1999]



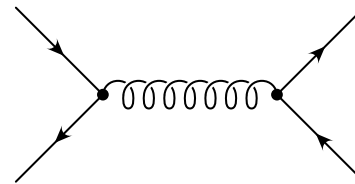
(a)



(b)



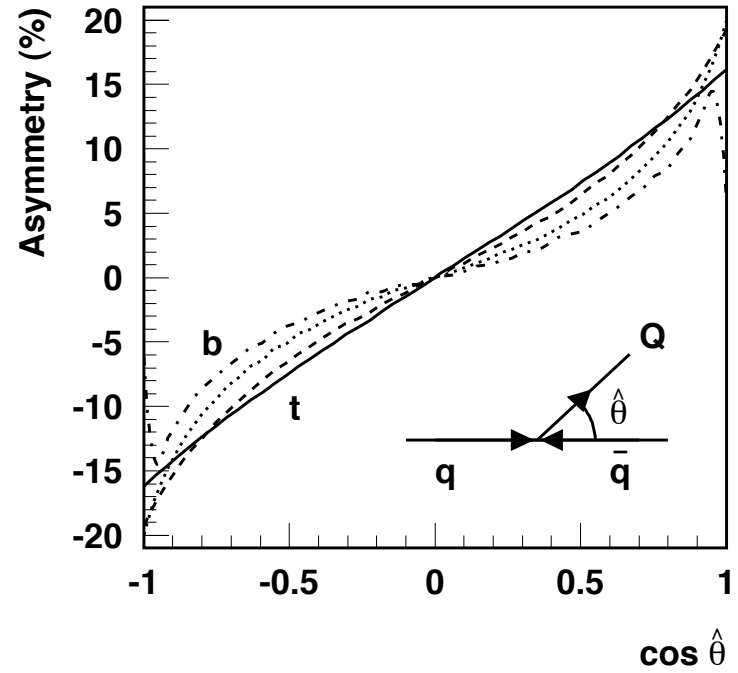
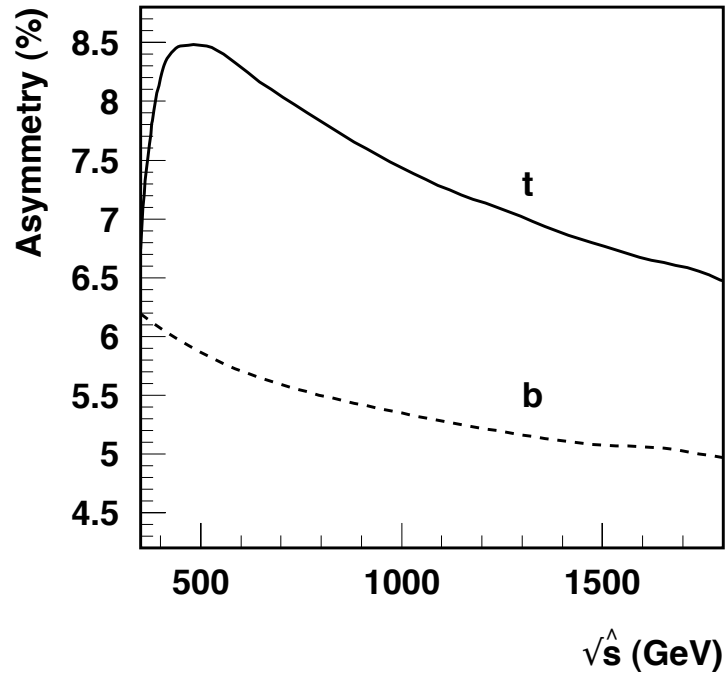
(c)



(d)

INTERFERENCES GIVE RISE TO FORWARD-BACKWARD ASYMMETRY (A_{FB})
 PROPORTIONAL TO:

$$\{\tau^a \tau^b \tau^c\} = d^{abc}$$



FORWARD-BACKWARD ASYMMETRY IS ENHANCED AT $\cos \theta = \pm 1$.

DOUBLE-TOP PRODUCTION AT HADRON COLLIDERS

- UNDER STUDY AT TEVATRON & LHC

SALIENT FEATURES

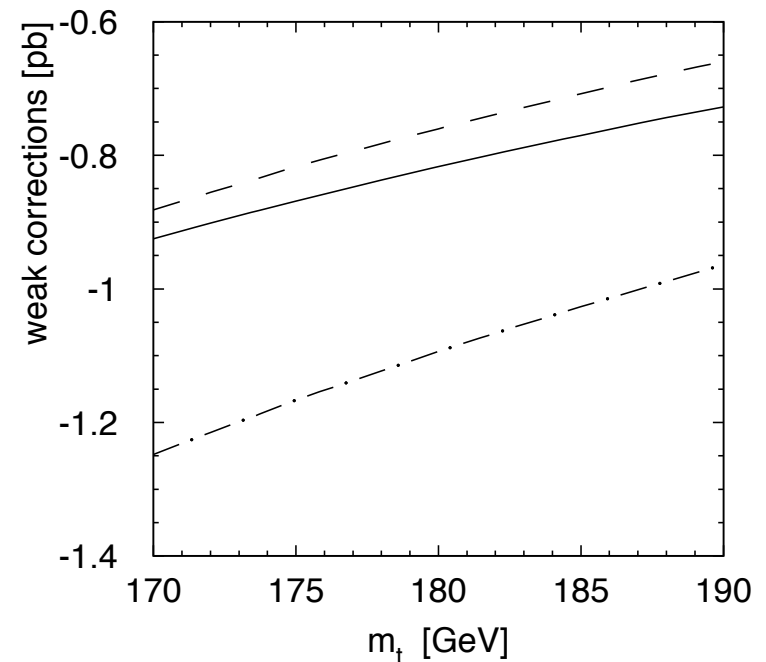
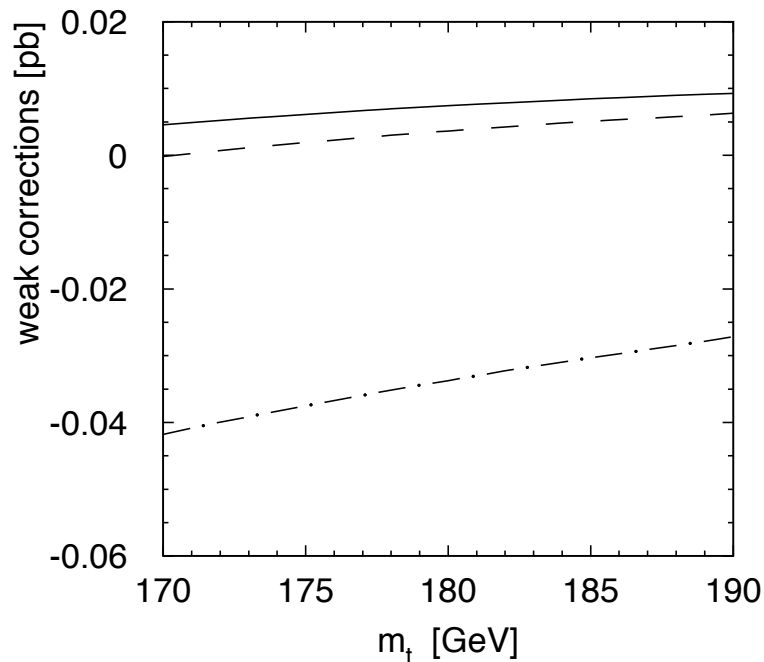
- MEASURED BY ALL EXPERIMENTS (CDF/ DO@FNAL & ATLAS/ CMS@LHC).
 - ACHIEVED CONSISTENCY WITH SM PREDICTION (REQUIRED NLO QCD AND RESUMMATION, NNLO QCD EXPECTED)
1. MANY DIFFERENT DECAY CHANNELS
 2. COMPARE TO THEORY TO LOOK FOR NP – HADRONIC PRECISION EXPERIMENT
 3. LARGE DATA SAMPLE – SMALL STATISTICAL ERROR
 4. NEED TO CONTROL JET ENERGY SCALE – TO REDUCE SYSTEMATICAL ERROR
 5. POSSIBLE TO STUDY SPIN EFFECTS (TOP DECAYS BEFORE HADRONISING !)

NLO EW EFFECTS IN $t\bar{t}$ HADRO-PRODUCTION

$$q\bar{q} \rightarrow t\bar{t}$$

[KUHN ET AL, EPJ C45:139,2006; BERNREUTHER ET AL, PLB633:54,2006]

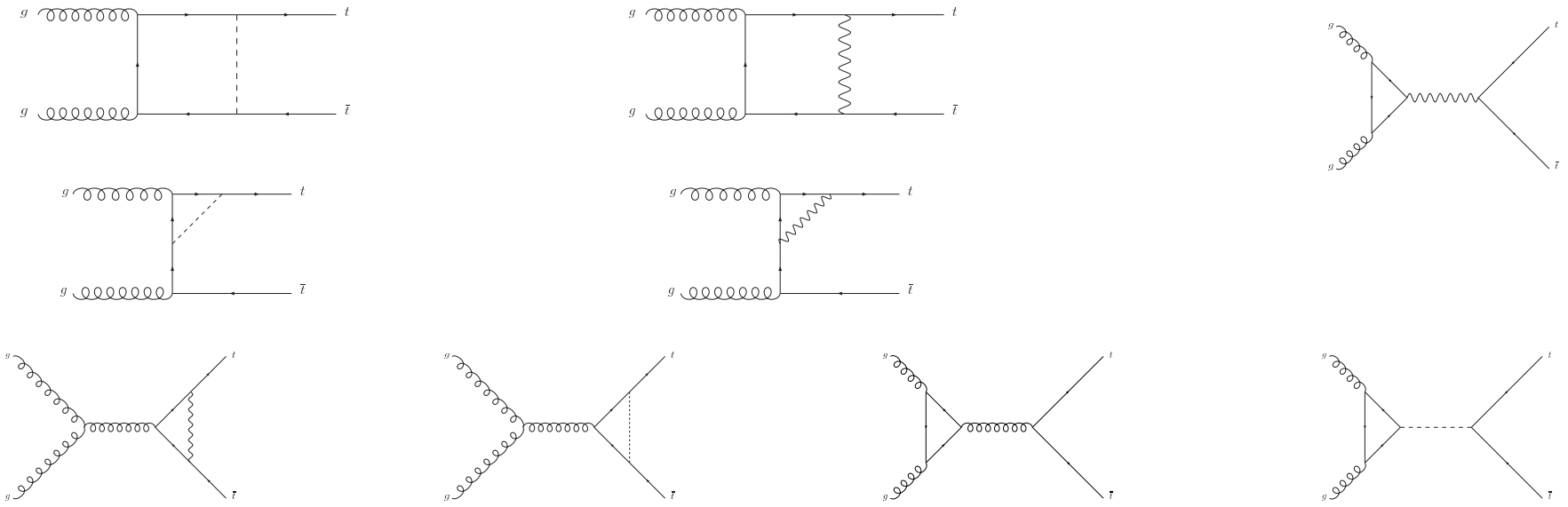
- LO IS 5.15(0.23)[0.034] PB FOR $q\bar{q}$ QCD(gg QCD)[$q\bar{q}$ EW] @ TEVATRON
- LO IS 80.2(384.4)[0.49] PB FOR $q\bar{q}$ QCD(gg QCD)[$q\bar{q}$ EW] @ LHC



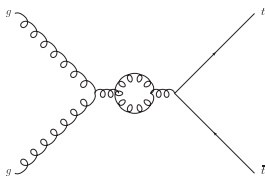
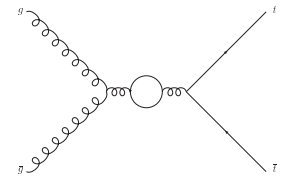
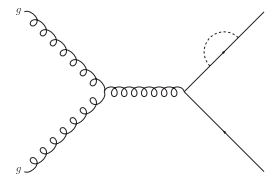
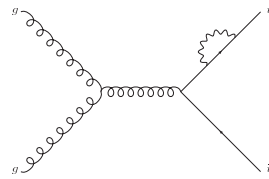
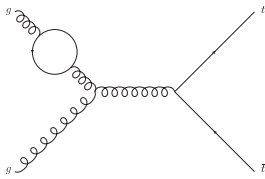
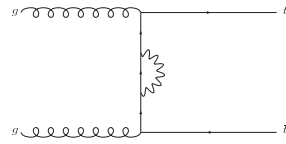
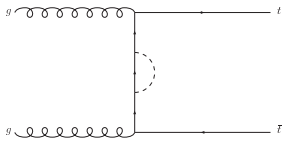
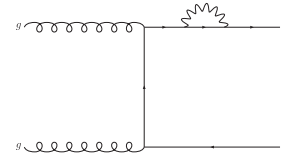
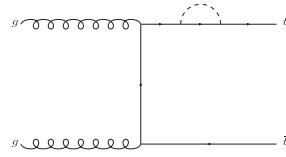
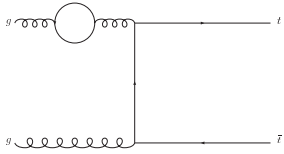
$\sigma(q\bar{q} \rightarrow t\bar{t})(\text{NLO-W})$ vs m_t FOR $M_H = 120(200)[1000]$ GEV,
SOLID(DASHED)[DASHED-DOTTED]: LEFT@TEVATRON, RIGHT@LHC.

$$gg \rightarrow t\bar{t}$$

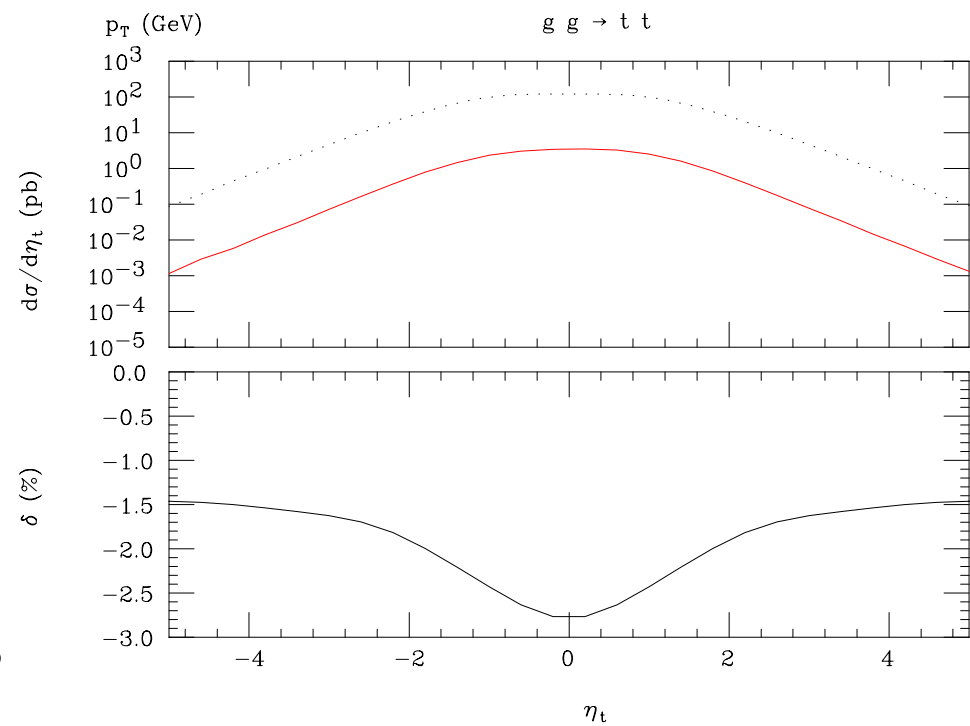
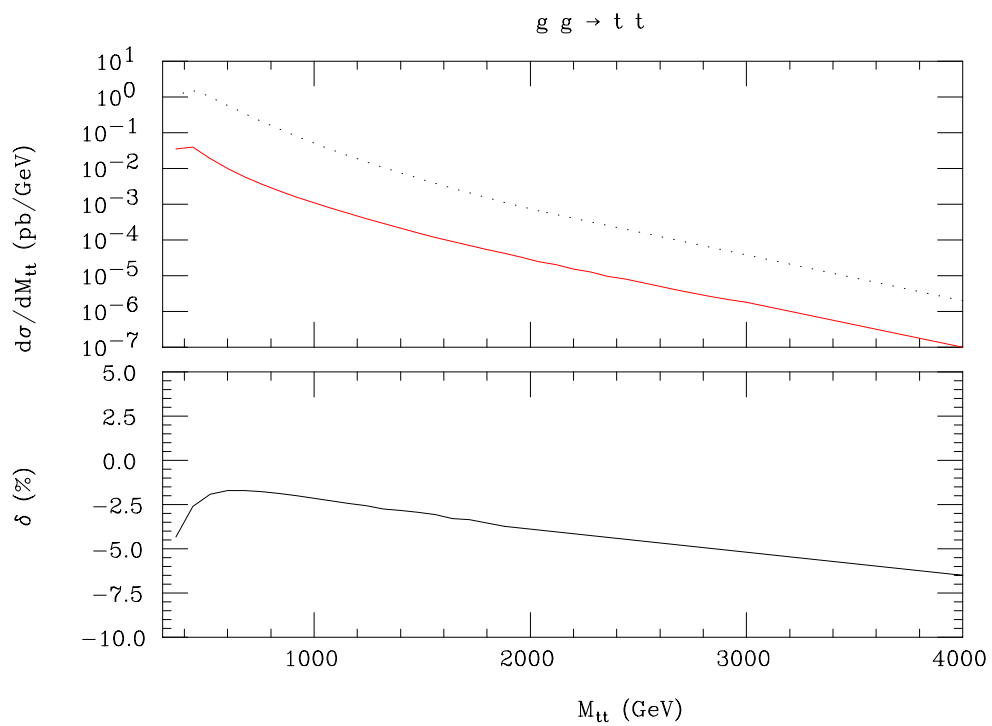
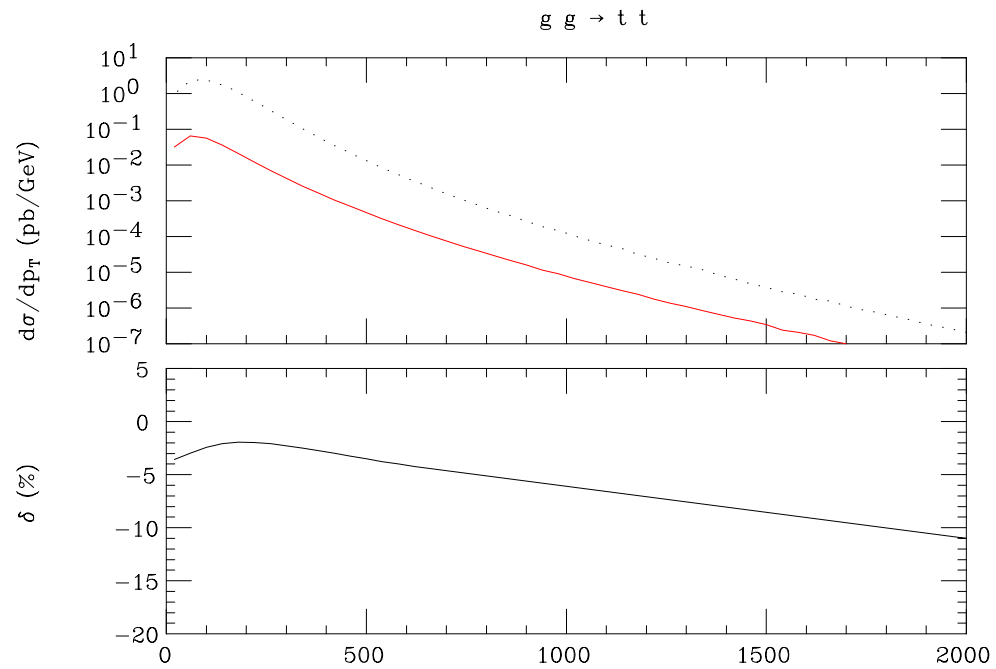
[NOLTEN, MORETTI AND ROSS, PLB639:513,2006 & PLB660:607,2008; KUHN ET AL, EPJC51:37,2007; BERNREUTHER ET AL, PRD74:113005,2006]



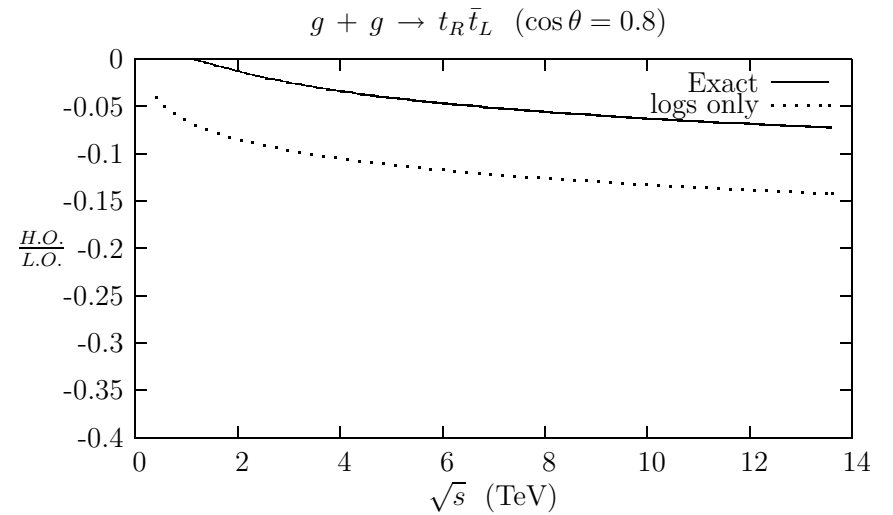
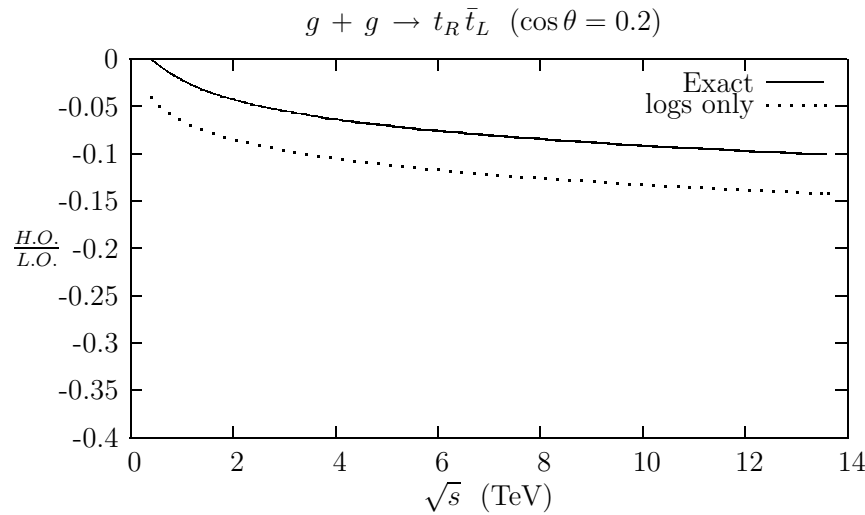
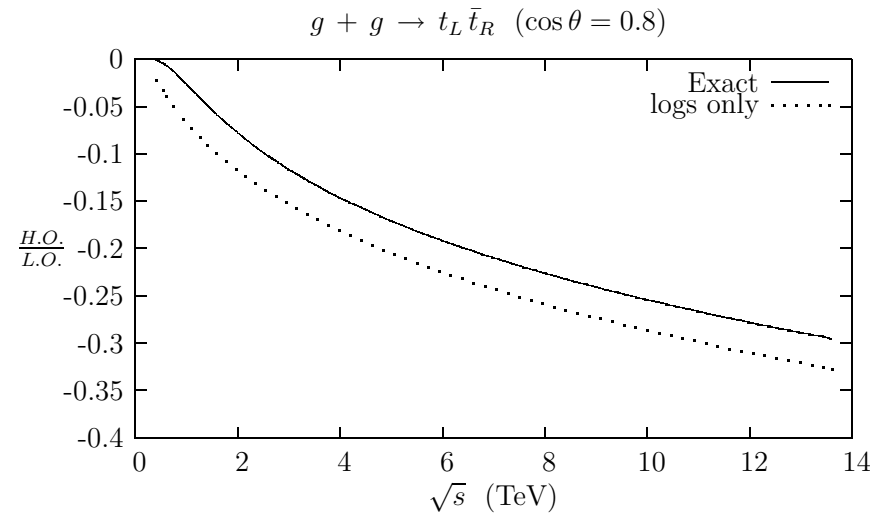
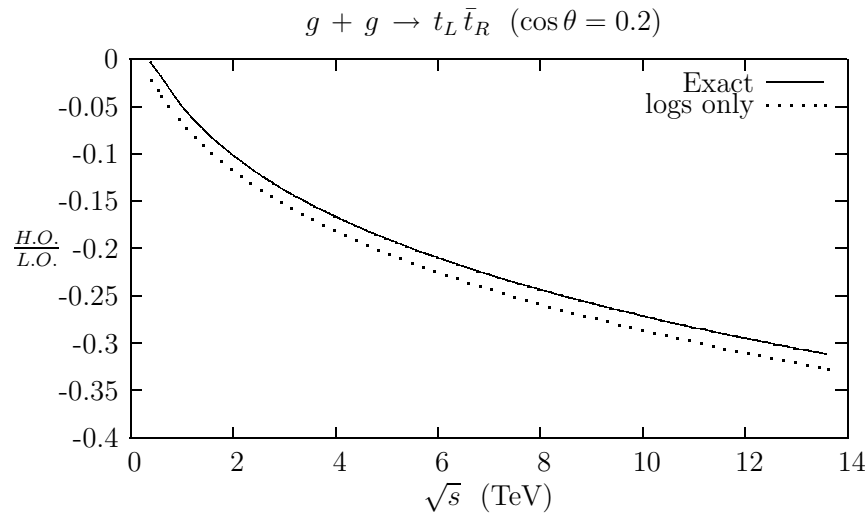
BOXES AND TRIANGLES



SELF-ENERGIES



• COMPARE FULL ONE-LOOP AGAINST DL AND (ANGULAR INDEPENDENT) SL:



POLARISED $t\bar{t}$ PRODUCTION

W. BERNREUTHER, A. BRANDENBURG, Z.G. SI, P. UWER, HEP-PH/0111346

CANNOT MEASURE t -POLARISATIONS DIRECTLY, BUT CAN DETERMINE IF SPINS ARE ALIGNED OR ANTI-ALIGNED FROM ANGULAR DISTRIBUTIONS OF DECAY PRODUCTS.

$$t\bar{t} \rightarrow bW^+ \bar{b}W^- \rightarrow be^+ \nu \bar{b}e^- \bar{\nu}$$

- CAN DEFINE SINGLE AND DOUBLE TOP-SPIN ASYMMETRIES:

$$A_{LL} d\sigma \equiv d\sigma_{++} - d\sigma_{+-} + d\sigma_{--} - d\sigma_{-+},$$

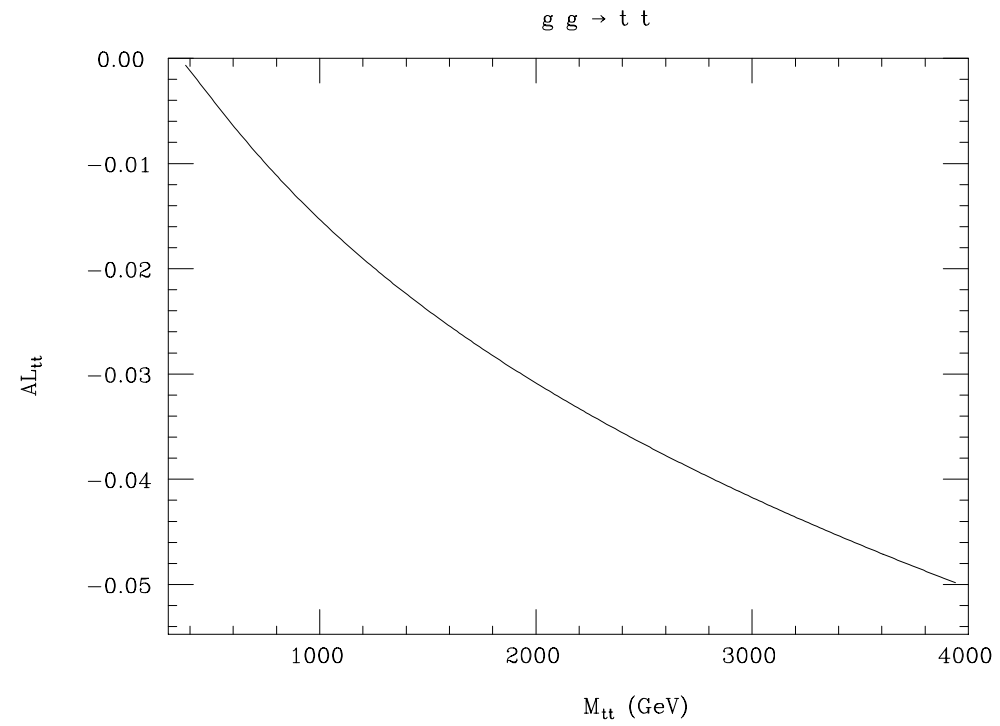
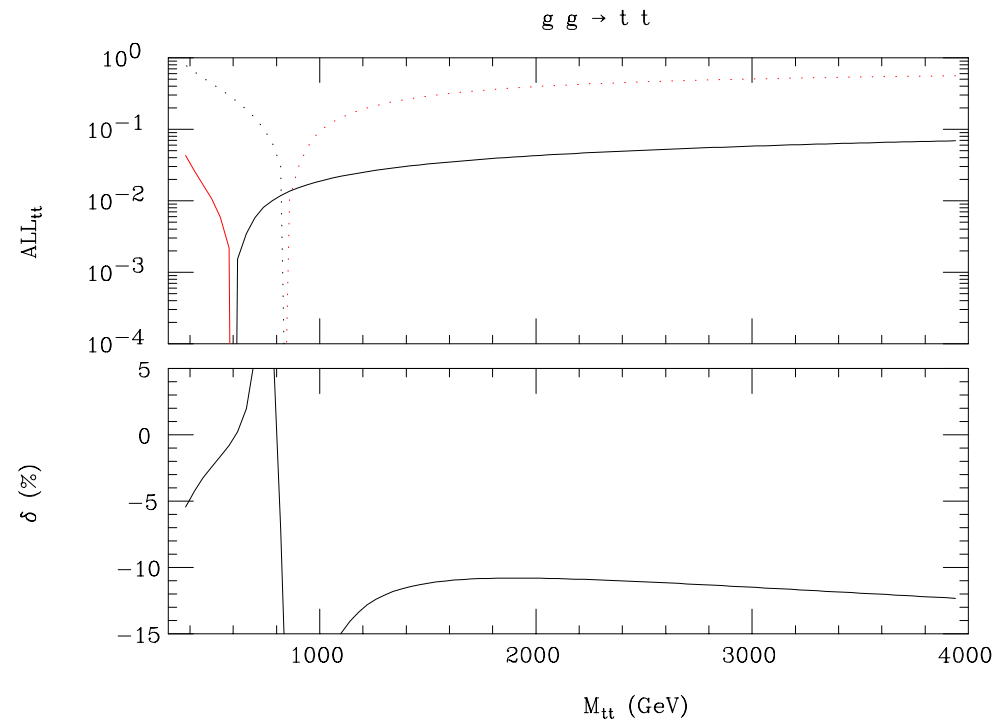
$$A_L d\sigma \equiv d\sigma_- - d\sigma_+,$$

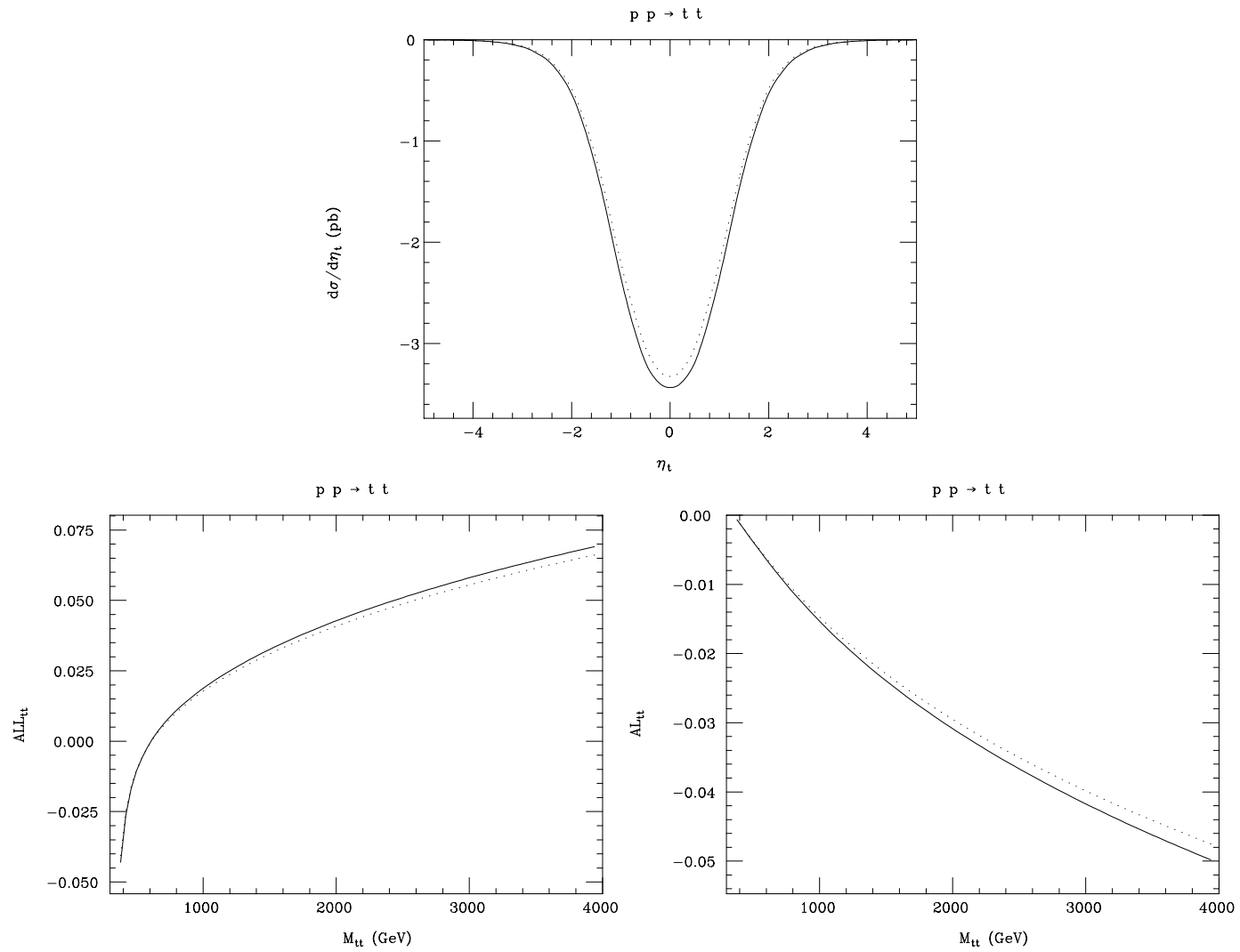
$$A_{PV} d\sigma \equiv d\sigma_{--} - d\sigma_{++}.$$

- FIRST IS PARITY-CONSERVING, LAST TWO ARE PARITY-VIOLATING
- INDICES + AND - REFER TO HELICITIES OF RIGHT (R) AND LEFT (L) t 'S

NLO QCD CONTRIBUTIONS TO A_{LL}, A_L, A_{PV} HAVE BEEN CALCULATED.

WEAK CONTRIBUTIONS EXPECTED TO BE OF SIMILAR MAGNITUDE





(SOME DEPENDENCE ON THE H MASS: SOLID(DOTTED) FOR $M_H = 150(200)$ GEV.)

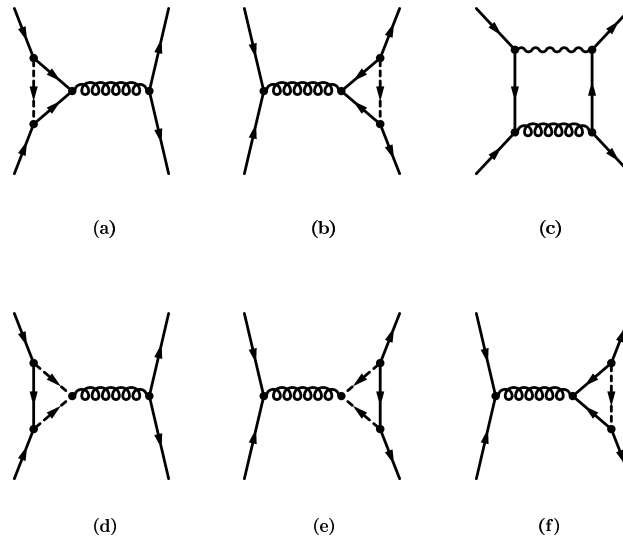
MSSM CORRECTIONS TO HEAVY QUARK PAIR PRODUCTION

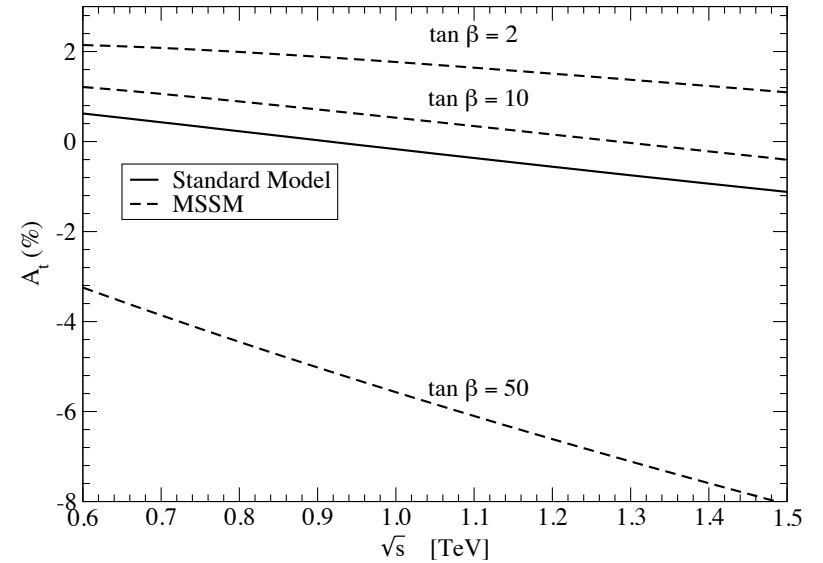
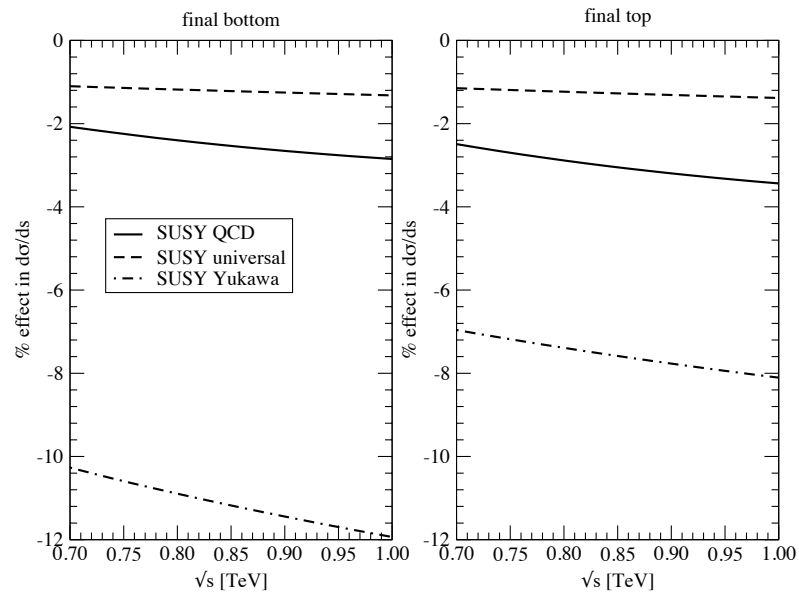
[BECCARIA ET AL, PRD69:113004,2004 & HEP-PH/0405036 &
PHYS.REV.D71:073003,2005]

ONE-LOOP CORRECTIONS (QCD & EW) WITH (VIRTUAL) SUSY PARTICLES
AFFECT PRODUCTION CROSS-SECTIONS.

THE MAGNITUDE OF THESE EFFECTS DEPEND ON SUSY PARAMETERS:

PRECISION PHYSICS PROGRAMME AT LHC TO FIT UNDERLYING SUSY MODEL ?





CALCULATED IN THE LEADING (SUDAKOV) LOG APPROXIMATION:

$$\ln \left(\frac{x_1 x_2 s}{M_{SUSY}^2} \right) \gg 1$$

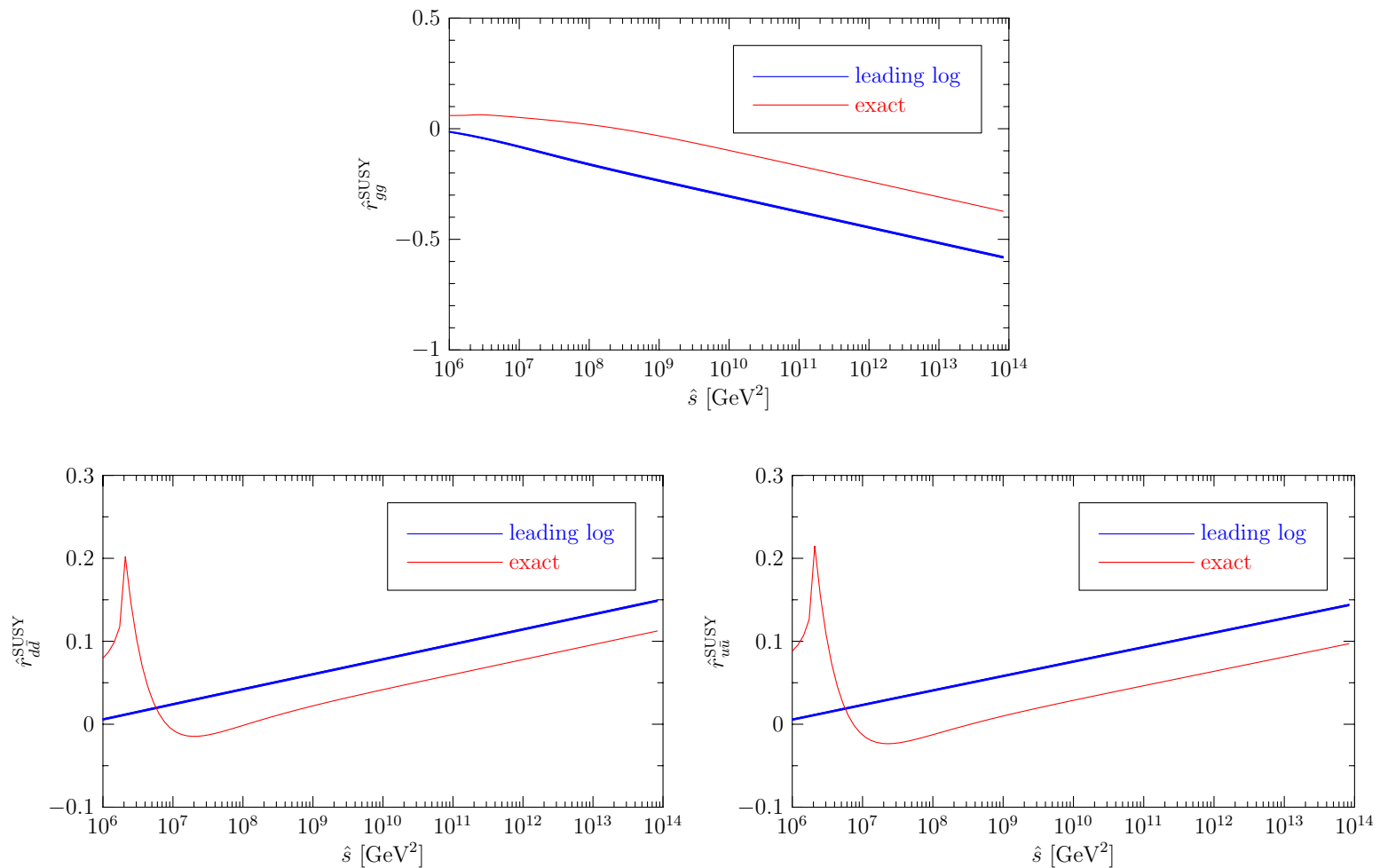
(ALSO, USED HERE LIGHT MSSM SPECTRUM.)

SUM RULES EXIST BETWEEN SINGLE- AND DOUBLE-TOP ASYMMETRIES [BECCARIA ET AL, PRD72:093001,2005]

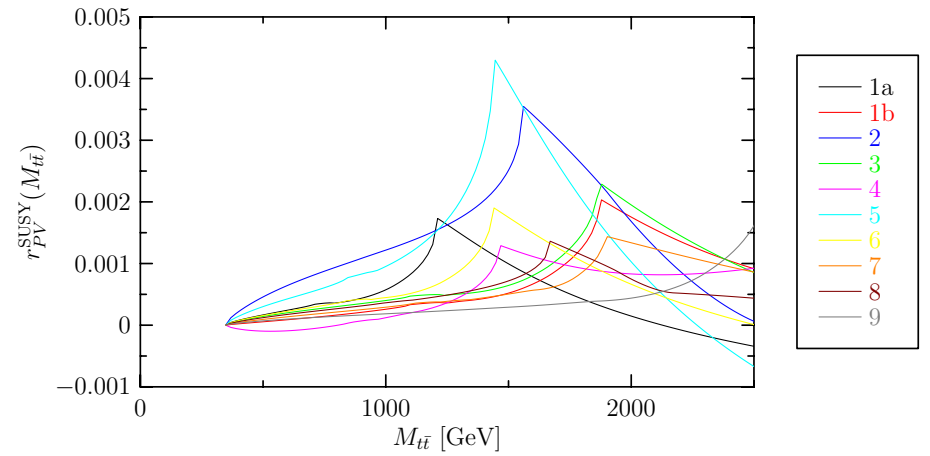
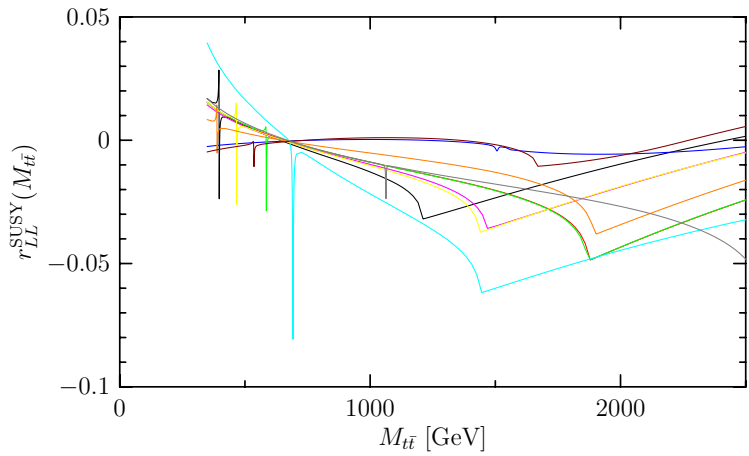
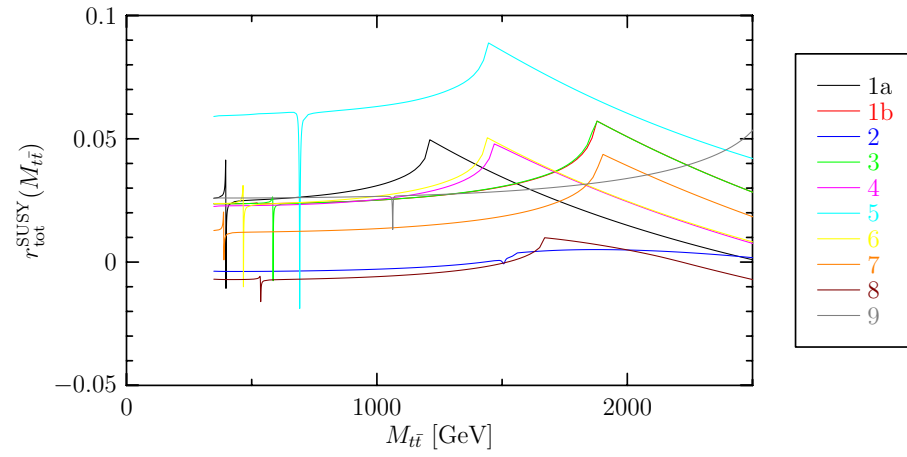
MSSM CORRECTIONS TO HEAVY QUARK PAIR PRODUCTION

[ROSS AND WIEBUSCH, JHEP0711:041,2007]

CONSIDER NOW QCD AND EW NLO IN MSSM:



CLOCKWISE: gg , $u\bar{u}$, $d\bar{d}$ AT THE LHC FOR SPS5.



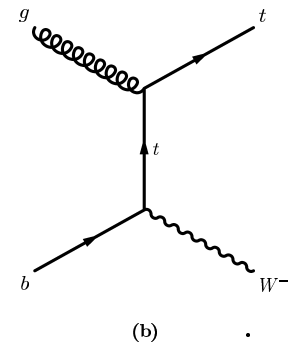
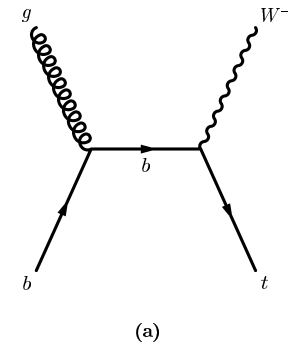
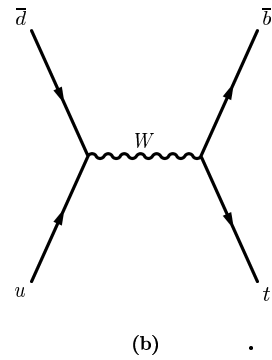
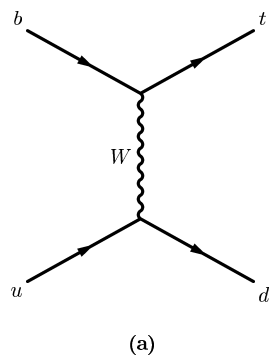
HADRO-PRODUCTION AT THE LHC FOR ALL SPSS.

SINGLE-TOP PRODUCTION AT HADRON COLLIDERS

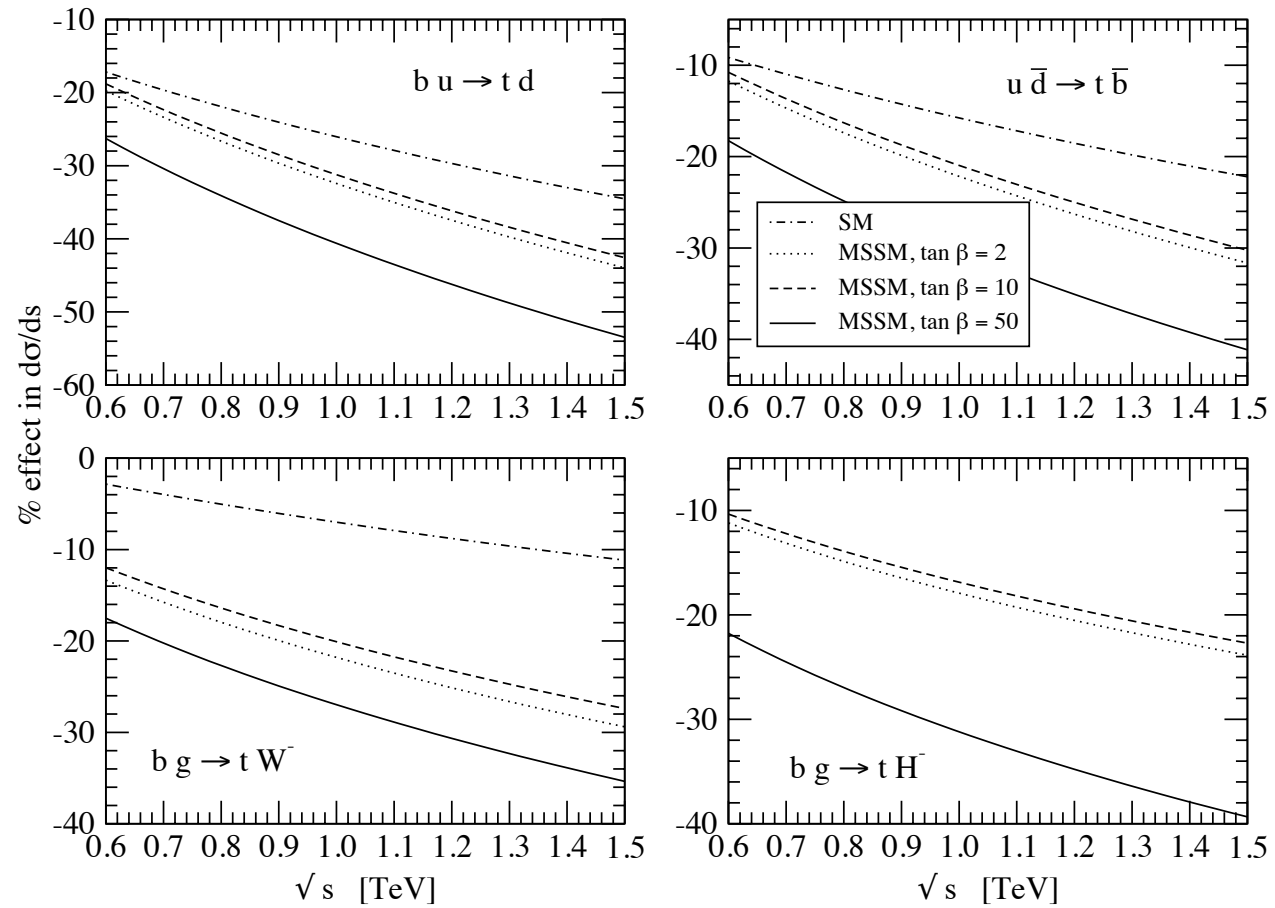
- UNDER STUDY AT TEVATRON & LHC

SALIENT FEATURES

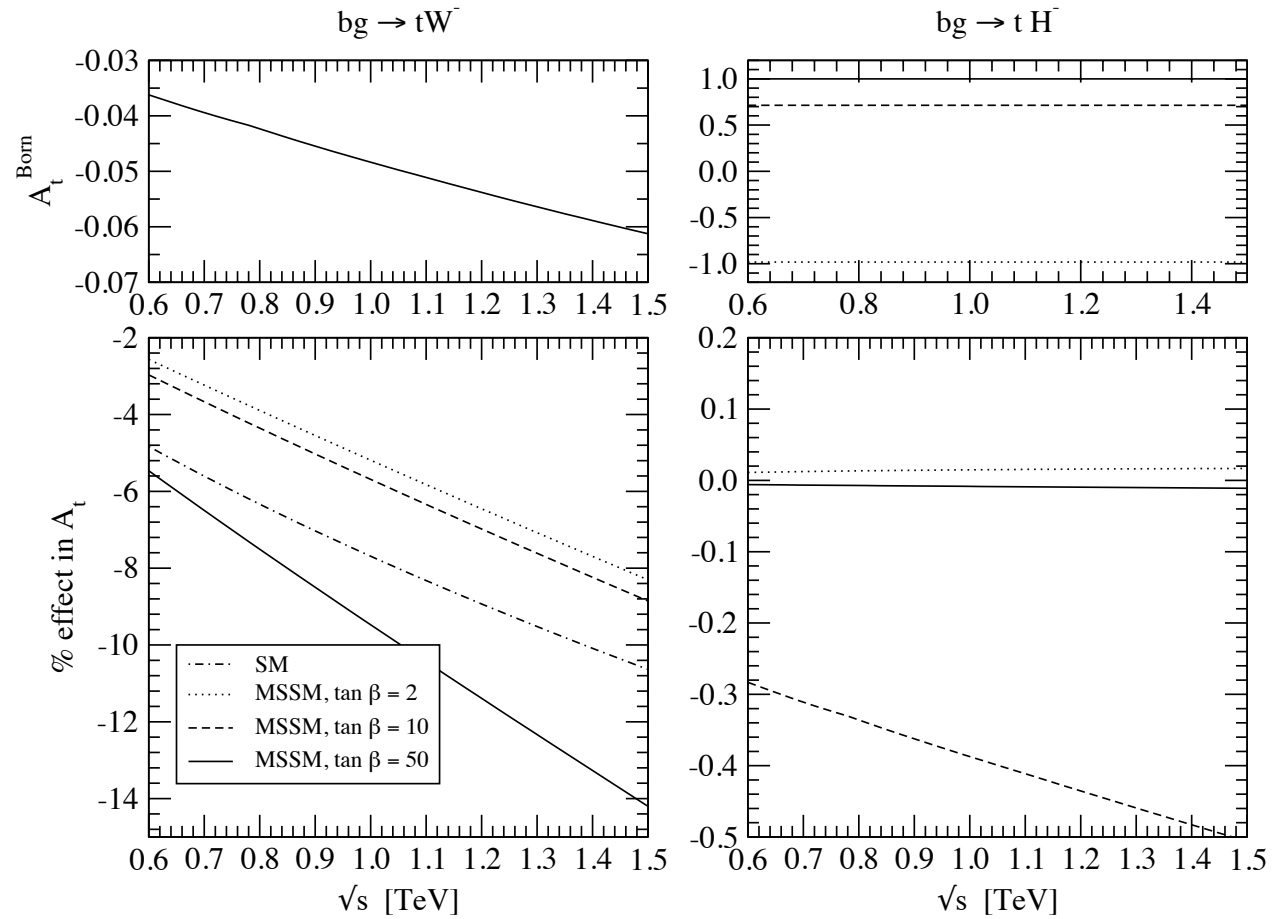
- (BEING) MEASURED BY ALL EXPERIMENTS (CDF/ DO@FNAL & ATLAS/ CMS@LHC).
 - ACHIEVED CONSISTENCY WITH SM PREDICTION
1. REQUIRES DETAILED KNOWLEDGE OF b DYNAMICS INSIDE (ANTI)PROTON
 2. ENABLES MEASURING TOP CKMs FROM CROSS-SECTION
 3. COMPARE TO THEORY TO LOOK FOR NP
 4. LARGE DATA SAMPLE (1/ 3 OF DOUBLE TOP)
 5. AGAIN, NEED TO CONTROL JET ENERGY SCALE
 6. AGAIN, POSSIBLE TO STUDY SPIN EFFECTS (SINGLE ASYMMETRIES)



(LO DIAGRAMS FOR SINGLE-TOP PRODUCTION: bq (A) [245 PB], $q\bar{q}$ (B) [10 PB] & bg (C) [50 PB] FUSION.)



SM & MSSM EW ONLY SUDAKOVs. [BECCARIA ET AL, PRD71:033005,2005]



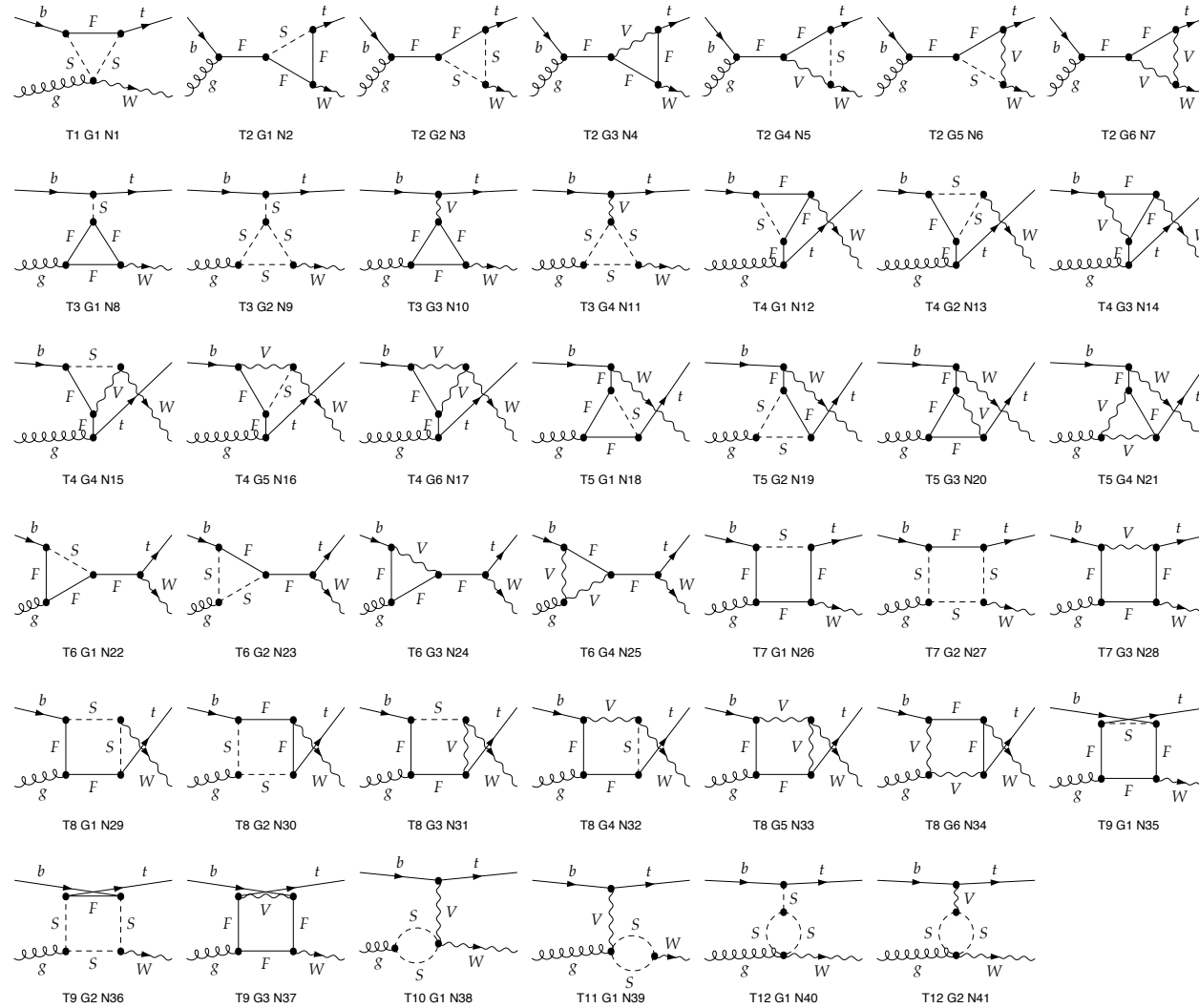
ASYMMETRY $A_L(t)$ FOR bg -FUSION. [BECCARIA ET AL, PRD71:033005,2005]

	SU1	SU6	LS1	LS2
m_0	70	320	300	300
$m_{1/2}$	350	375	150	150
A_0	0	0	-500	-500
$\tan \beta$	10	50	10	50
$\mu/ \mu $	1	1	1	1
α	-0.110	-0.0212	-0.109	-0.015
M_1	144.2	155.8	60.1	60.6
M_2	270.1	291.3	114.8	115.9
μ	474.4	496.6	329.7	309.3
H^\pm	534.3	401.7	450.4	228.9
H^0	528.3	392.5	442.5	211.1
h^0	114.6	115.7	111.4	110.8
A^0	527.9	392.5	443.4	212.0
$\chi_{1\pm}^{\pm}$	262.8	289.3	108.0	111.1
$\chi_{2\pm}^{\pm}$	495.3	514.8	350.1	329.4
χ_1^0	140.1	153.0	57.38	58.92
χ_2^0	263.1	289.4	108.5	111.3
χ_3^0	479.2	501.0	335.3	315.8
χ_4^0	495.4	514.0	348.7	326.5

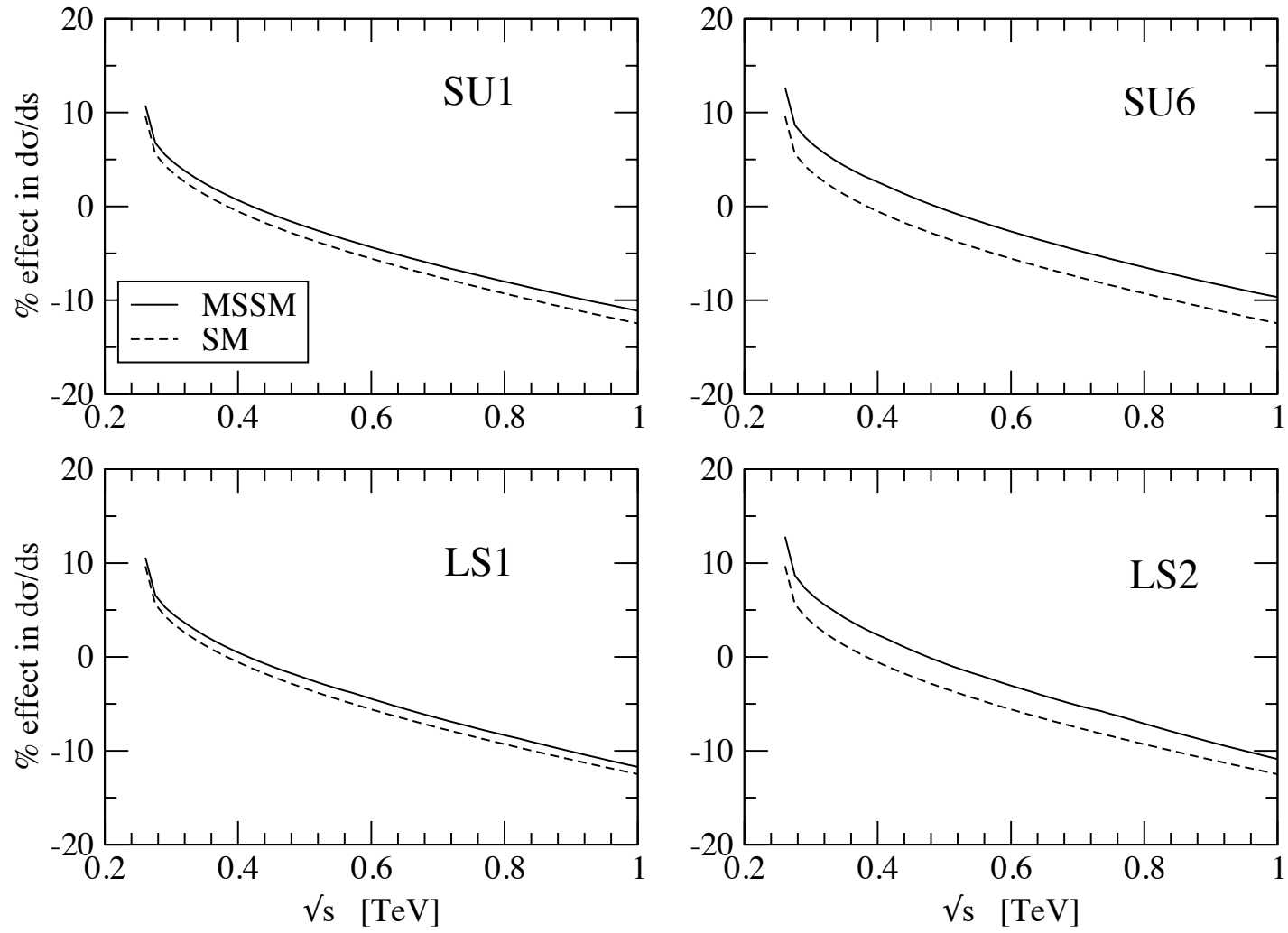
	SU1	SU6	LS1	LS2
\tilde{l}_L	253.3	412.3	321.0	321.2
\tilde{l}_R	157.6	353.4	308.7	308.7
$\tilde{\nu}_e$	241.0	404.8	311.3	311.3
$\tilde{\tau}_L$	149.6	195.8	297.1	078.1
$\tilde{\tau}_R$	256.1	399.2	323.8	282.5
$\tilde{\nu}_\tau$	240.3	362.5	308.4	243.6
\tilde{u}_L	762.9	870.5	459.8	460.2
\tilde{u}_R	732.9	840.7	451.9	452.3
\tilde{d}_L	766.9	874.0	466.4	467.0
\tilde{d}_R	730.2	837.8	452.8	453.2
\tilde{t}_L	562.5	631.5	213.3	223.6
\tilde{t}_R	755.8	796.9	462.9	431.3
\tilde{b}_L	701.0	713.7	380.6	304.0
\tilde{b}_R	730.2	787.6	449.1	401.7
θ_τ	1.366	1.133	1.091	1.117
θ_b	0.3619	0.7837	0.184	0.653
θ_t	1.070	1.050	1.016	0.9313

DEFINE MSUGRA BENCHMARKS.

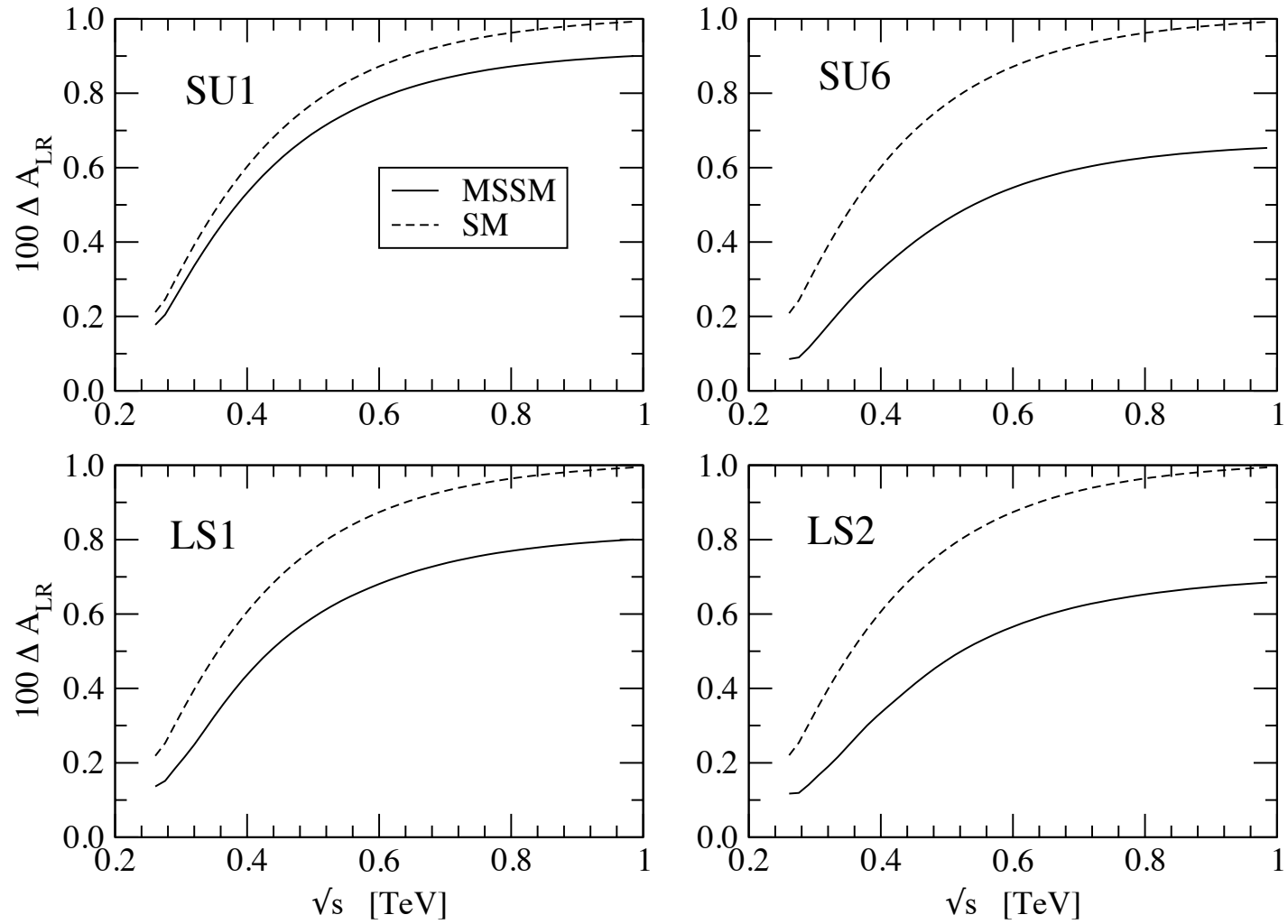
$$b \bar{g} \rightarrow t W$$



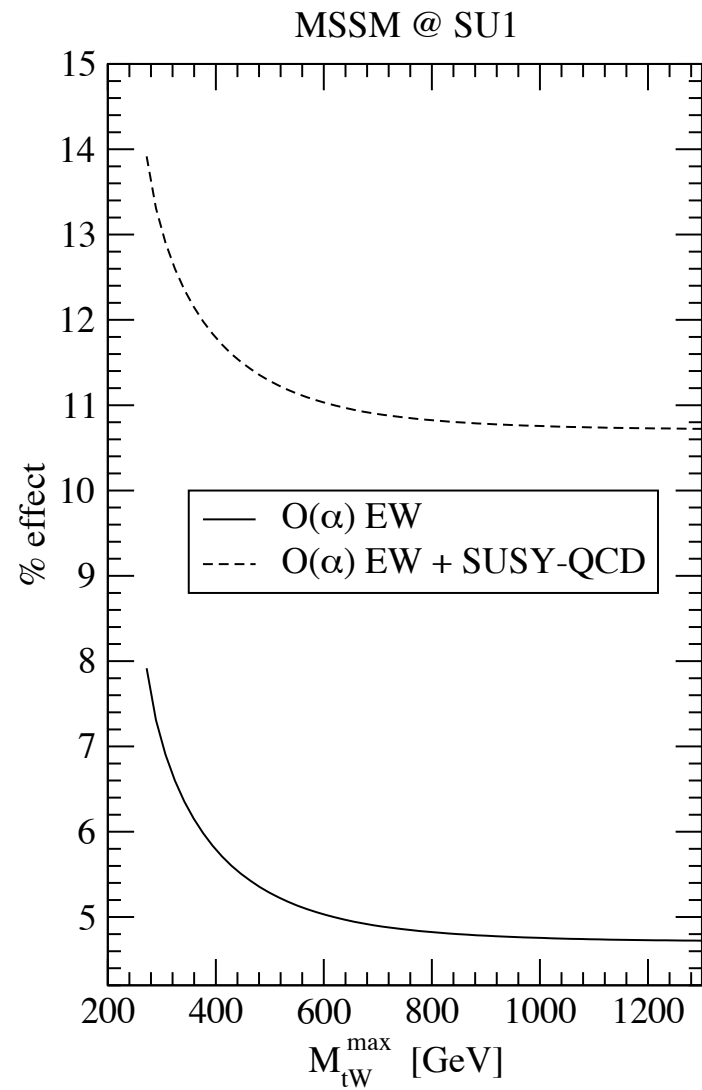
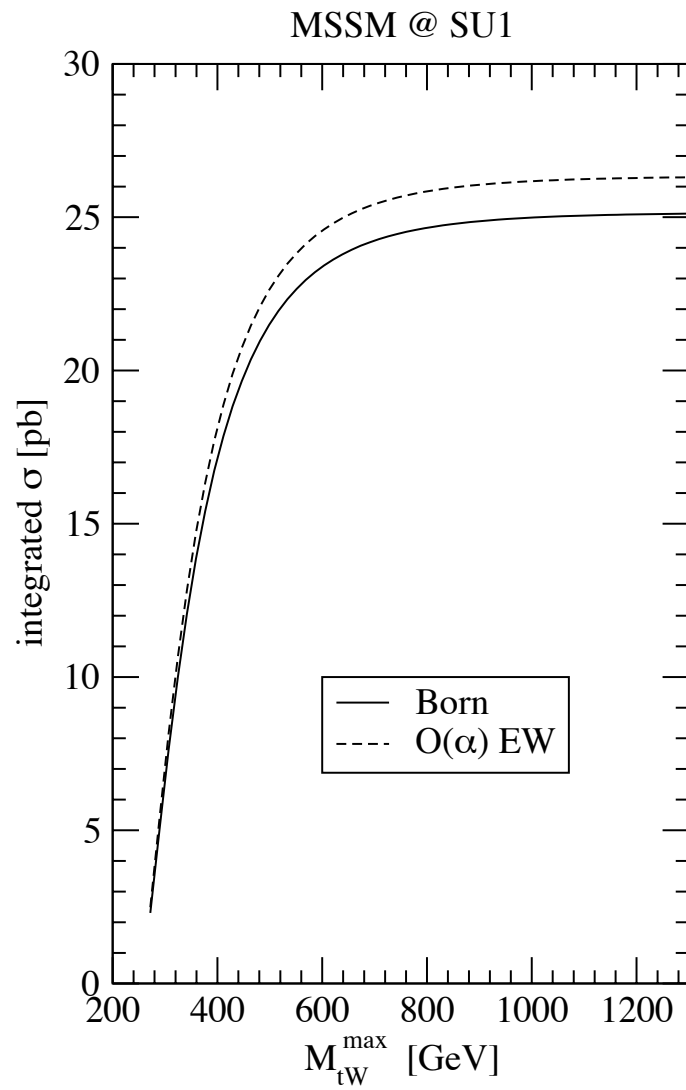
ONE LOOP SM & MSSM EW DIAGRAMS IN $bg \rightarrow tW^-$. [BECCARIA ET AL, PRD73:093001,2006]



ONE LOOP SM & MSSM EW EFFECTS IN $bg \rightarrow tW^-$: CROSS SECTION.

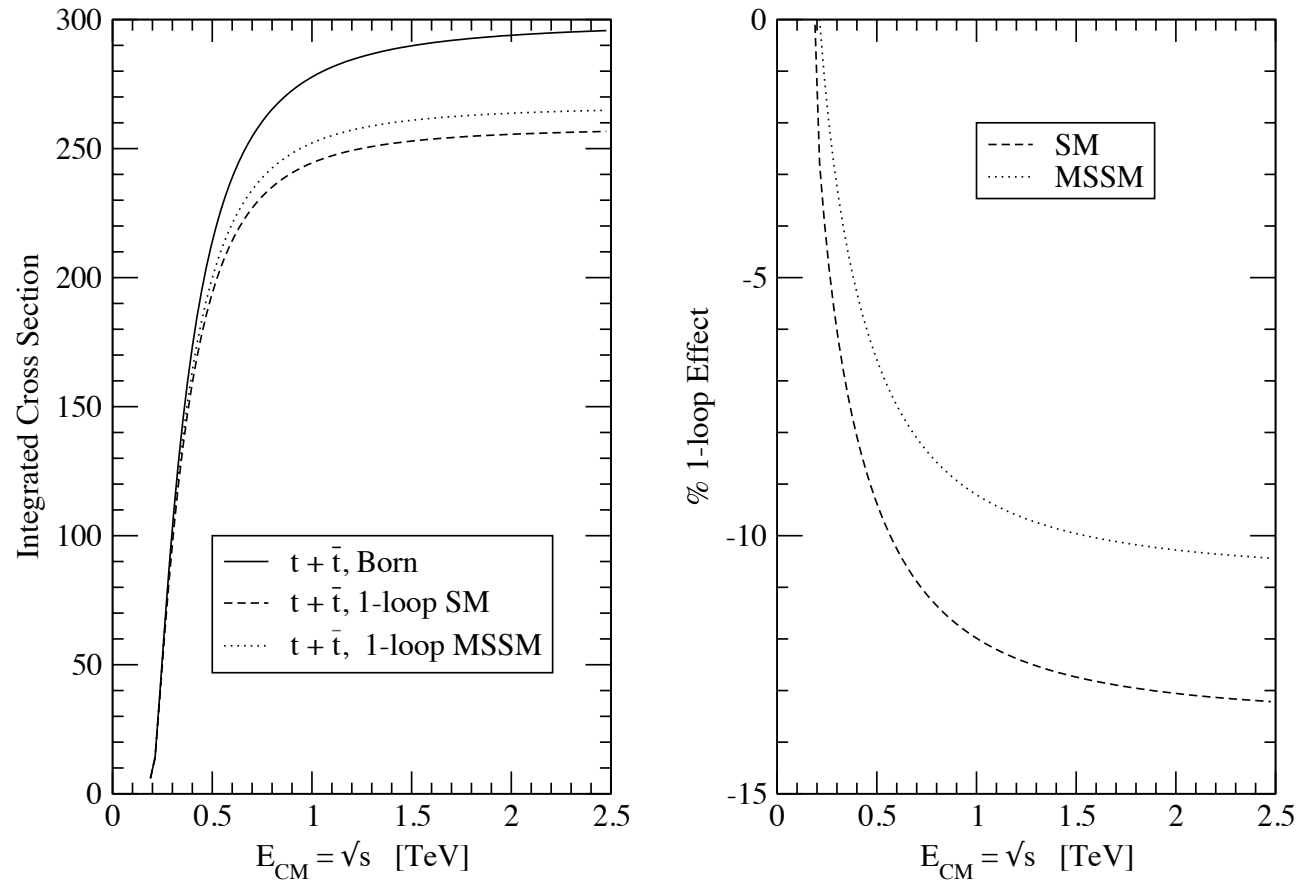


ONE LOOP SM & MSSM EW EFFECTS IN $bg \rightarrow tW^-$: A_L ASYMMETRY.



INCLUDE ONE LOOP MSSM QCD EFFECTS: CROSS SECTION. [EPJ C53:257,2008]

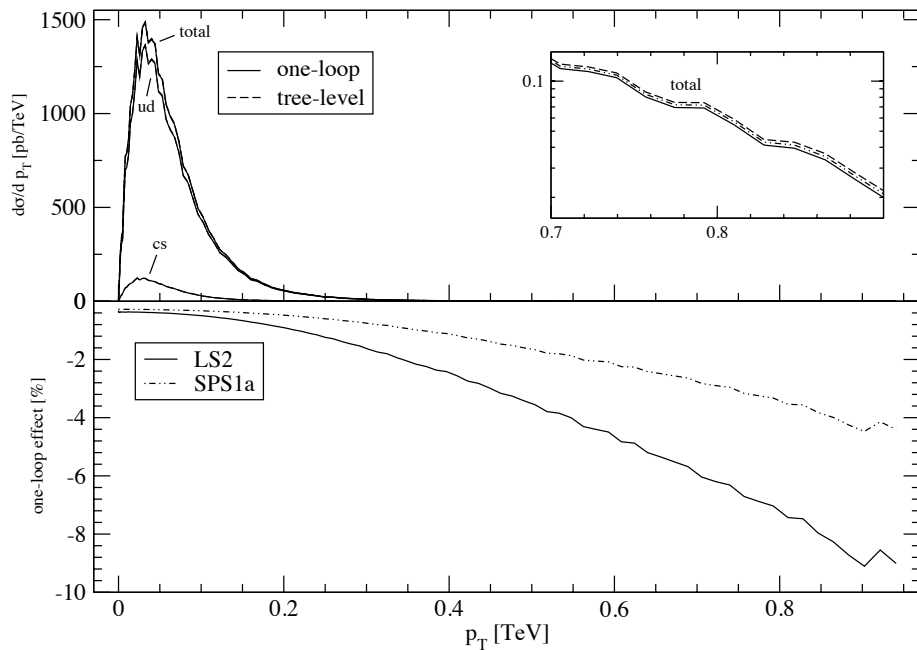
$t + \bar{t}$ production



ONE LOOP SM & MSSM EW EFFECTS IN $bq \rightarrow tq'$: CROSS SECTION. [BECCARIA ET AL, PRD74:013008,2006 & HEP-PH/0609189]

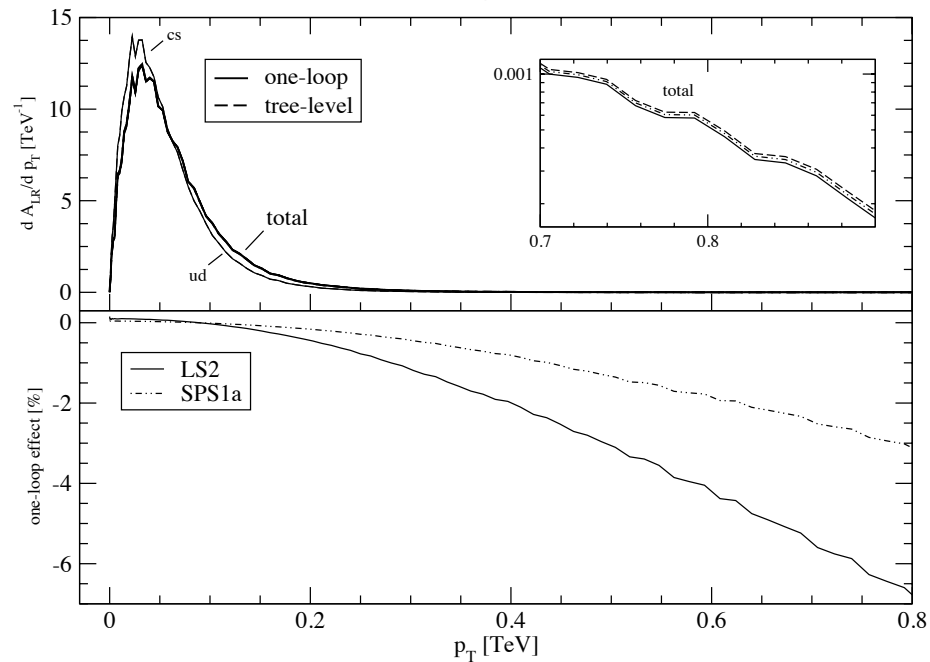
Cross Section - Transverse Momentum Distribution

t-channel - SUSY EW+QCD contribution @ 14 TeV



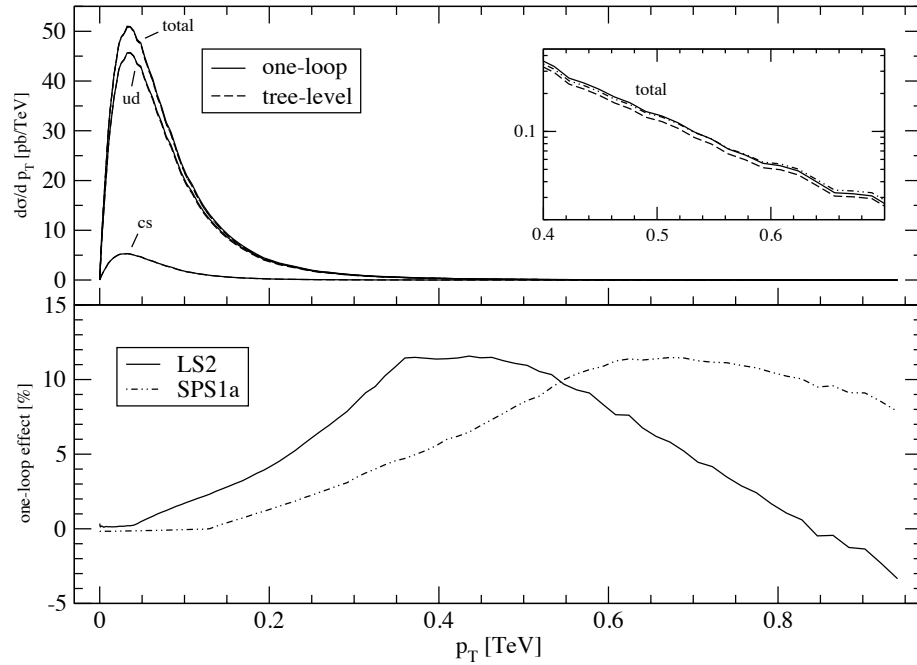
A_{LR} - Transverse Momentum Distribution

t-channel - SUSY EW+QCD contribution @ 14 TeV

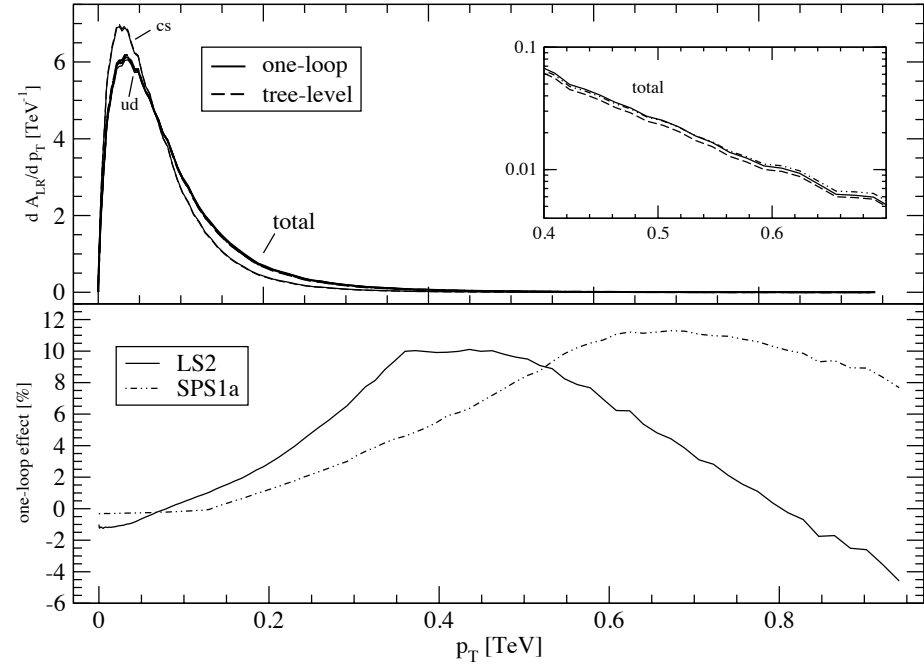


ONE LOOP MSSM QCD & EW EFFECTS IN $bq \rightarrow tq'$: CROSS SECTION & A_L ASYMMETRY. [MACORINI, MORETTI AND PANIZZI, PRD82:054016,2010]

Cross Section - Transverse Momentum Distribution
s-channel - SUSY EW+QCD contribution @ 14 TeV



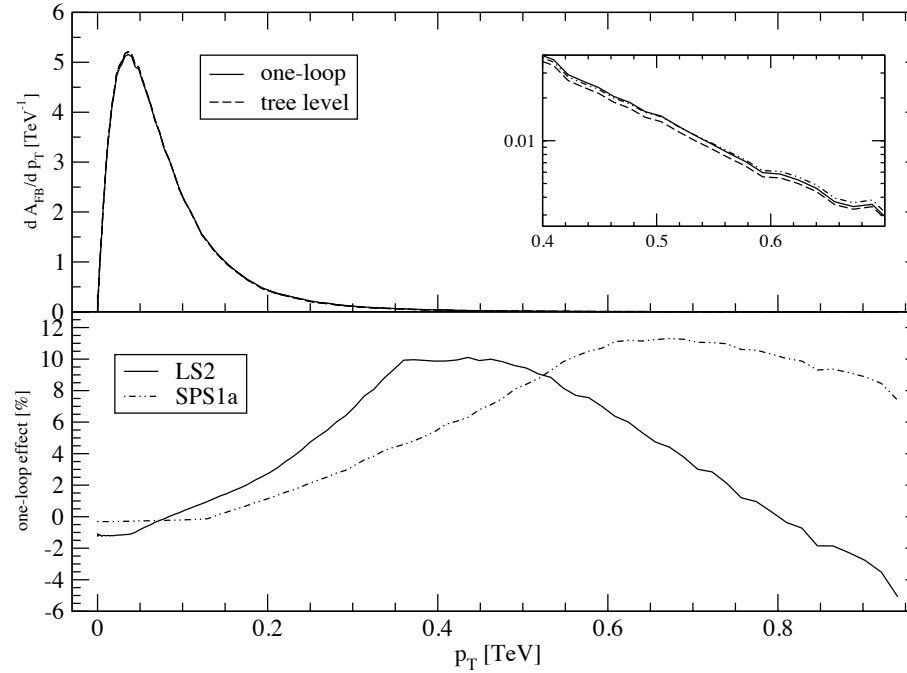
A_{LR} - Transverse Momentum Distribution
s-channel - SUSY EW+QCD contribution @ 14 TeV



ONE LOOP MSSM QCD & EW EFFECTS IN $q\bar{q}' \rightarrow t\bar{b}$: CROSS SECTION & A_L
ASYMMETRY. [MACORINI, MORETTI AND PANIZZI, PRD82:054016,2010]

A_{FB} - Transverse Momentum Distribution

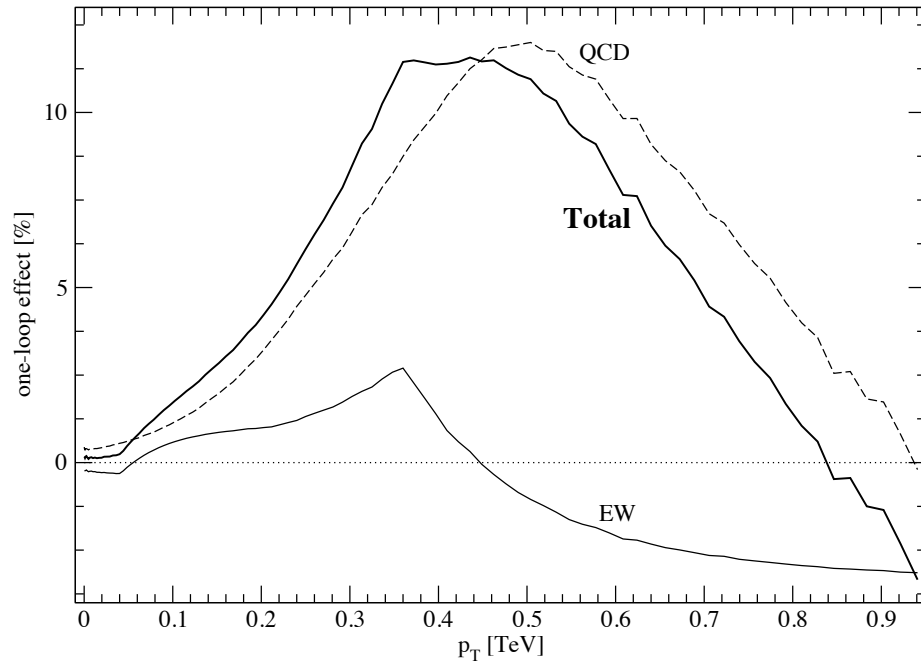
s-channel - SUSY EW+QCD contribution @ 14 TeV



ONE LOOP MSSM QCD & EW EFFECTS IN $q\bar{q}' \rightarrow t\bar{b}$: A_{FB} ASYMMETRY. [MACORINI, MORETTI AND PANIZZI, PRD82:054016,2010]

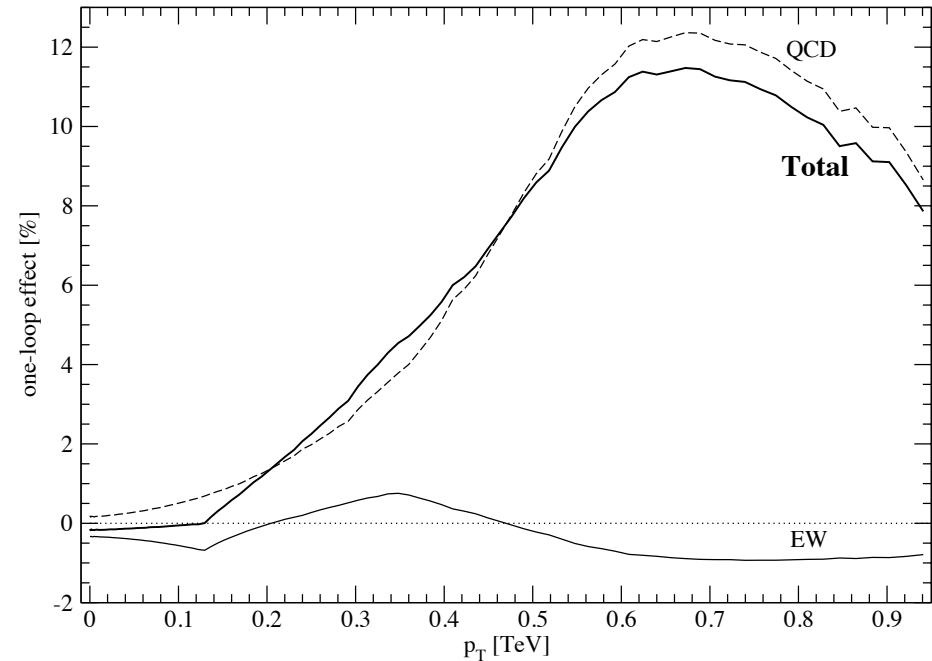
LS2 - Transverse Momentum Distribution

s-channel @ 14 TeV



SPS1a - Transverse Momentum Distribution

s-channel @ 14 TeV



ONE LOOP MSSM QCD & EW (SEPARATE) EFFECTS IN $q\bar{q}' \rightarrow t\bar{b}$: CROSS SECTION.

[MACORINI, MORETTI AND PANIZZI, PRD82:054016,2010]

CONCLUSIONS

- BOTH SM & MSSM, BOTH QCD & EW CORRECTIONS TO BOTH DOUBLE- AND SINGLE-TOP PROCESSES AVAILABLE.
- INCLUDE ALL DIFFERENTIAL DISTRIBUTIONS AND ASYMMETRIES (BOTH SPIN AND FORWARD/ BACKWARD).
- THEY ARE RELEVANT FOR HIGH ENERGY AND HIGH p_T CONFIGURATIONS (EXCEPT SM QCD).

OUTSTANDING ISSUES:

- NEED TO CLARIFY TREATMENT OF W, Z REAL RADIATION: EXP. INPUT.
- EW TOOLS NEEDED: IMPLEMENT RESULTS IN EXCLUSIVE MONTE CARLO. (MC) EVENT GENERATION, EASIER: NO DOUBLE COUNTING FOR W, Z RADIATION WITH PARTON. SHOWER, PROBLEM SOLVED FOR QED RADIATION (ABELIAN QCD).

- DEFINE EW PDFs AND (MORE IMPORTANTLY) PS.
- NEEDED FOR PRECISION MEASUREMENT PROGRAMME: E.G., SEARCH FOR VIRTUAL SUSY EFFECTS.

CURRENT WORK:

- CHECKING OUT TEVATRON ANOMALY IN $A_{FB}(t\bar{t})$ THROUGH $\mathcal{O}(\alpha_s^3)$, $\mathcal{O}(\alpha_s^2\alpha_W)$, $\mathcal{O}(\alpha_s\alpha_W^2)$ & $\mathcal{O}(\alpha_W^2)$ IN BOTH SM & MSSM (PLUS OTHER BSM): WATCH THIS SPACE.