

# Nb<sub>3</sub>Sn cable modelling

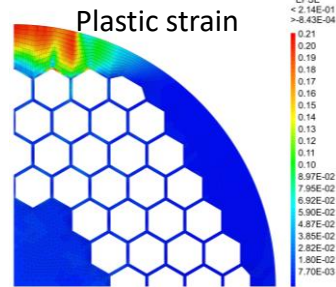
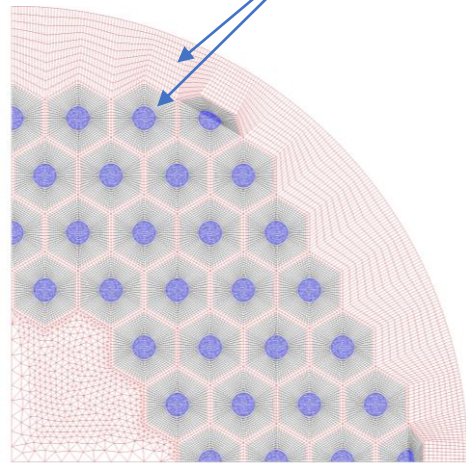
CG, 19/10/2023

Update on:

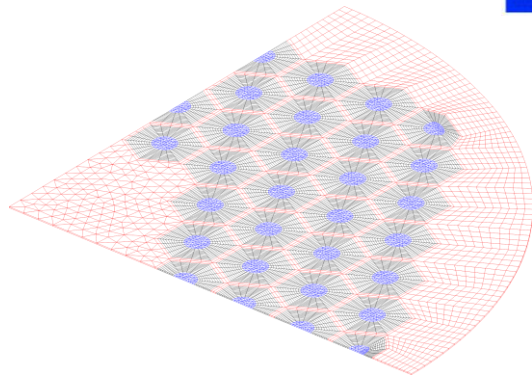
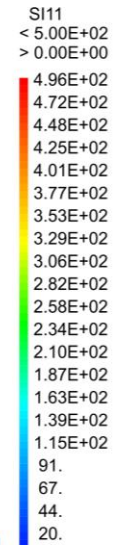
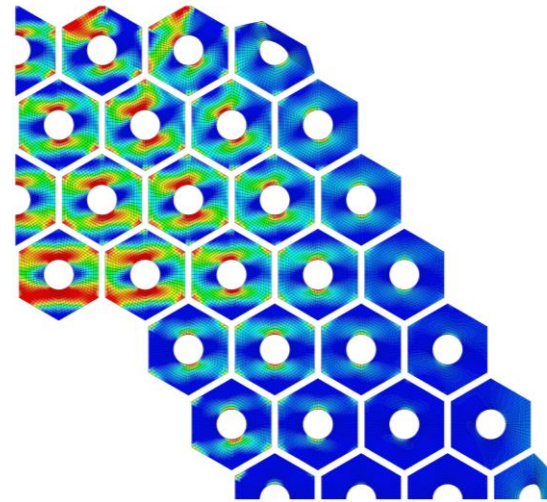
1. Model
2. Experimental activities

# Microscopic and equivalent wire models

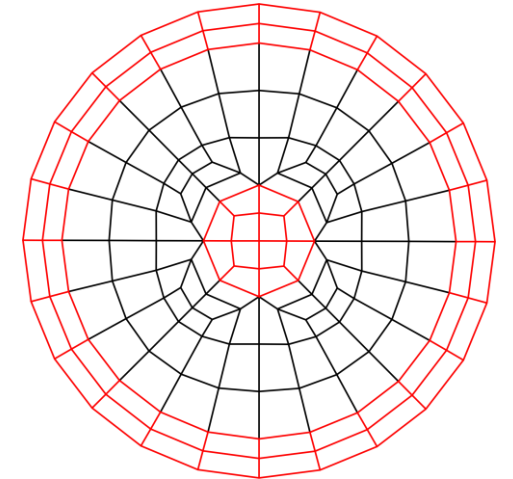
“Simple” elastic-plastic model



Principal stress [Mpa]



Pending material data.

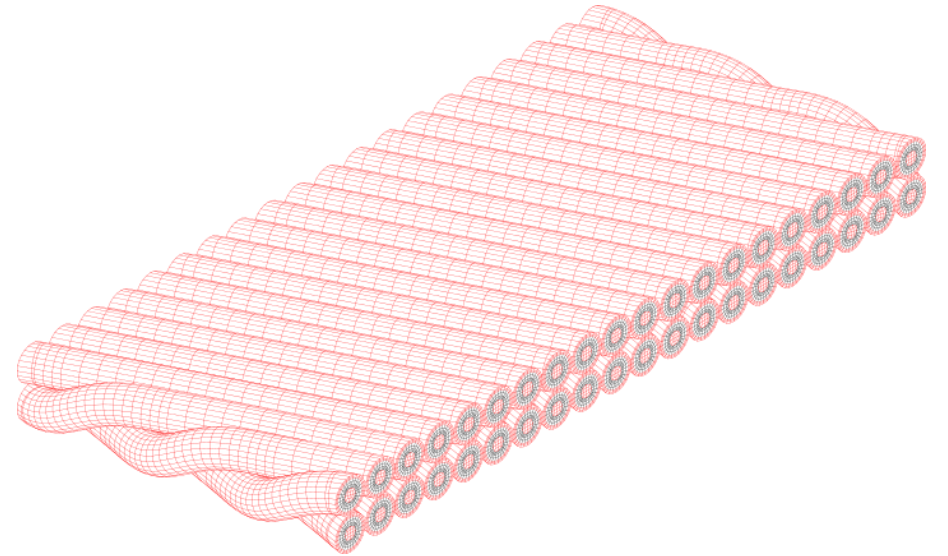
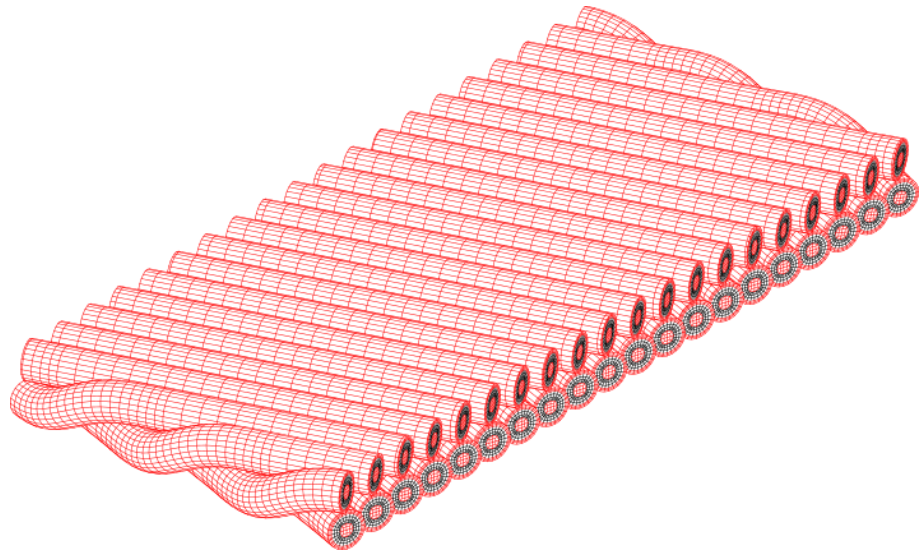


Equivalent wire



## Mesososcopic cable model

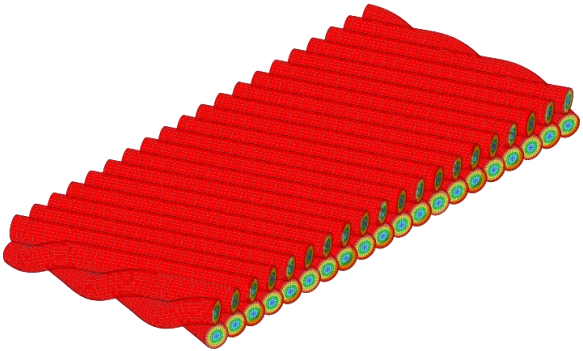
Modification of the cross sections at the interfaces to ease the application of the boundary conditions



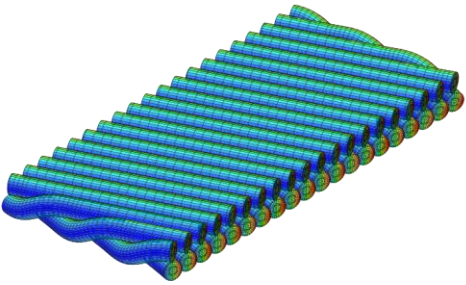
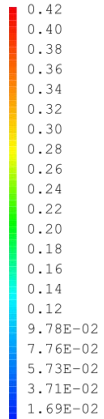
Definition of local coordinate system to enable the definition of initial stresses:

- Elastic (tensile, torsion),
- Residual stress,
- Back stress.

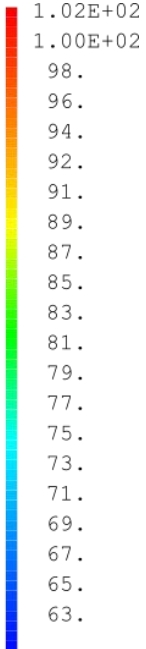
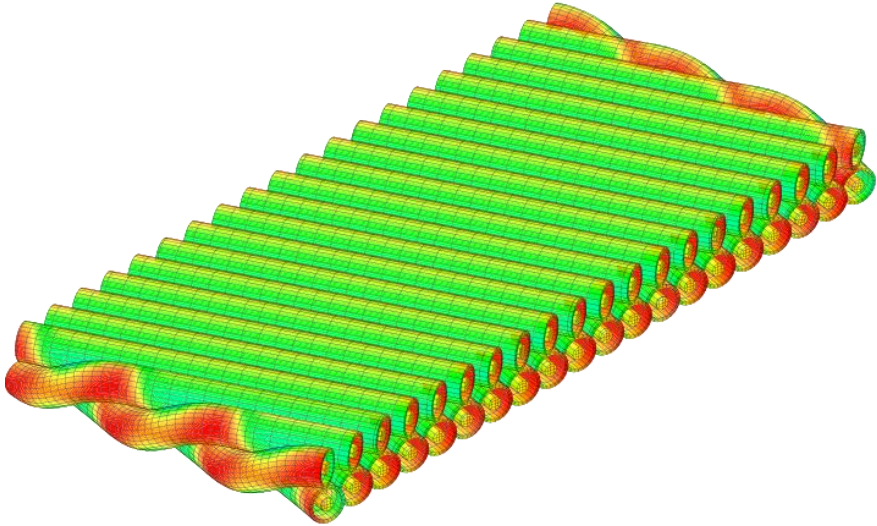
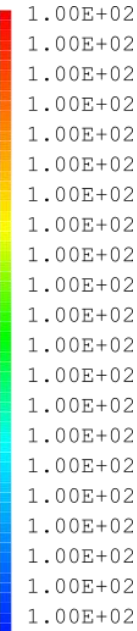
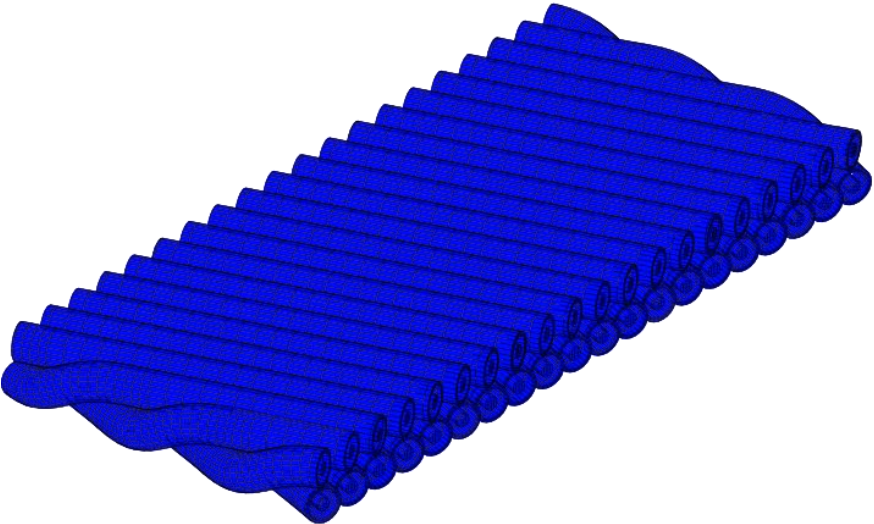
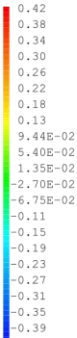
In local and global coordinate system



SCAL  
< 4.25E-01  
> 0.00E+00



SCAL  
< 4.25E-01  
> -4.25E-01



Possible initial variables accounted in the model:

## WIRE

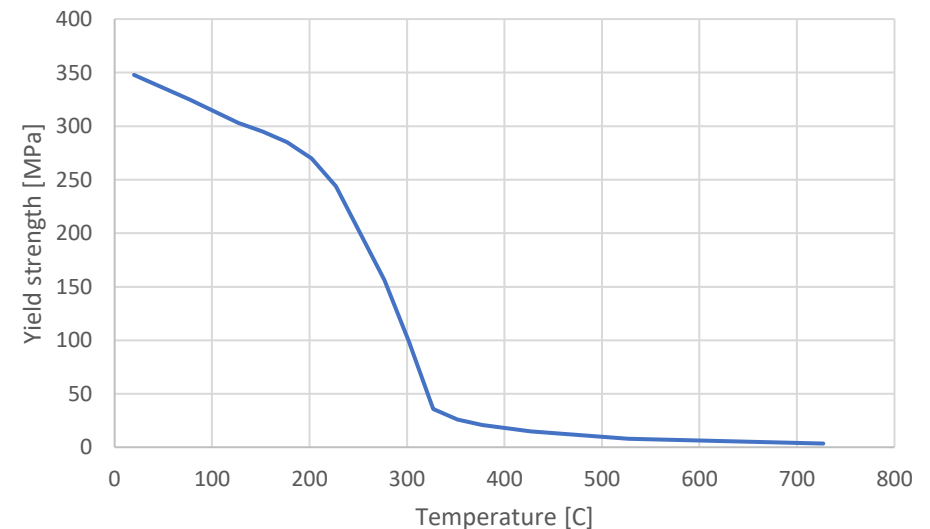
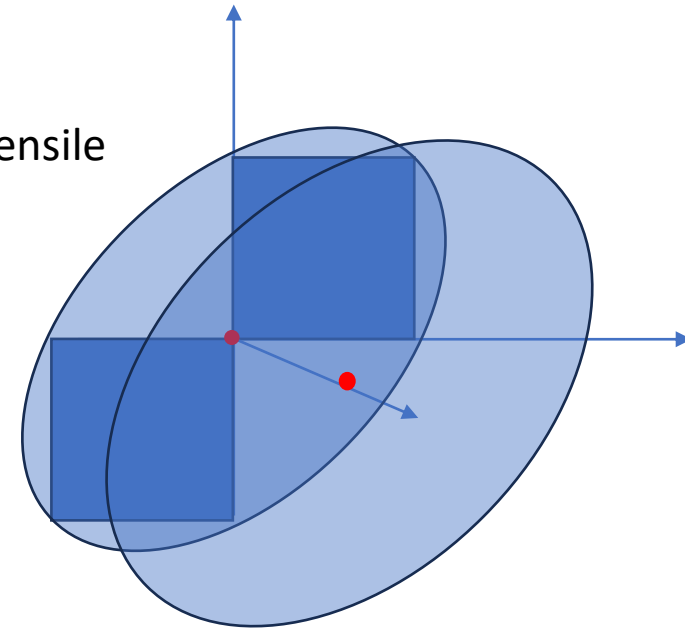
- Cold work Hardening
  - Kinematic or isotropic?
- Residual stress. If Nb exhibits higher yield strength , compressive/tensile residual stress is expected in copper/Nb, respectively.

## CABLE

- Initial stress: axial tensile? Torsion?

How to distinguish kinematic and isotropic hardening from measurements?

How hardness and/or yield strength evolutions in temperature translate in isotropic/kinematic hardening evolution?



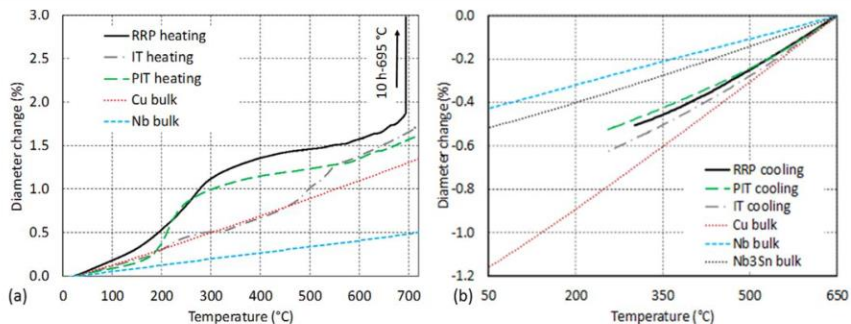
Experimental activities:

Delays due to:

- a failure of the sample holder
- Degradation of the glue with temperature



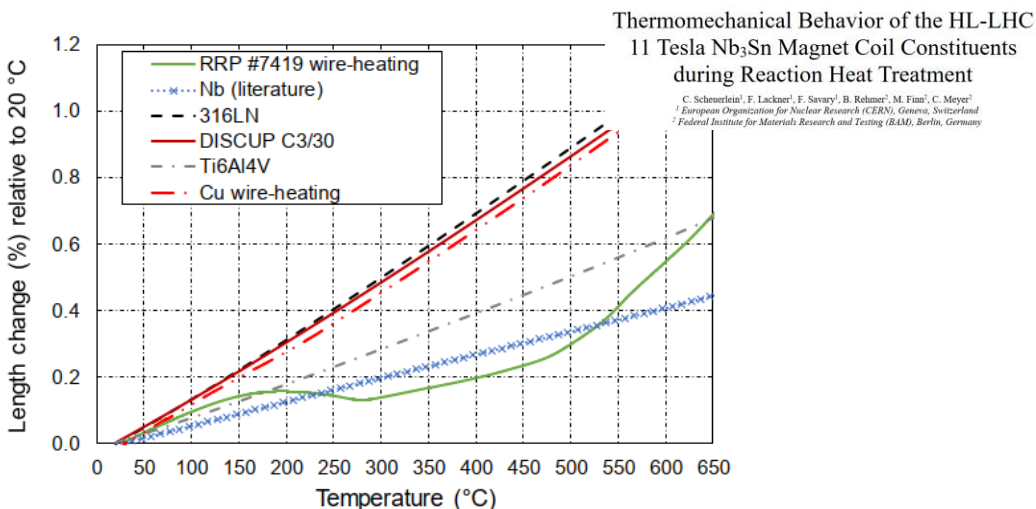




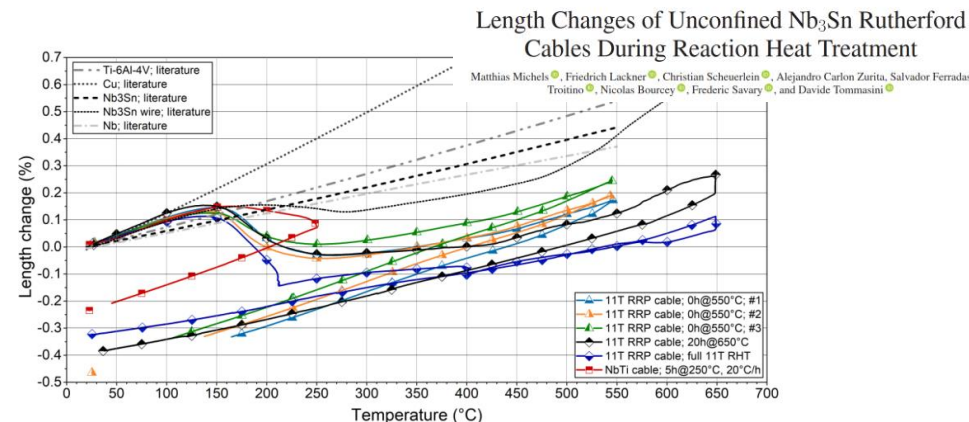
**Figure 1.** (a) Typical evolution of the RRP, PIT and IT wire diameters as measured by dilation during RHT with a ramp rate of  $1.67\text{ }^\circ\text{C min}^{-1}$ . (b) Evolution of the reacted RRP, PIT and IT wire diameters during cooling from  $650\text{ }^\circ\text{C}$  (average of at least two independent measurements). The thermal expansions of Cu, Nb and  $\text{Nb}_3\text{Sn}$  are shown for comparison.

**Table 1.** Comparison of  $\text{Nb}_3\text{Sn}$  wire diameter and wire and cable length changes before and after RHT. The change to the wire's cross-sectional area was calculated from the diameter change.

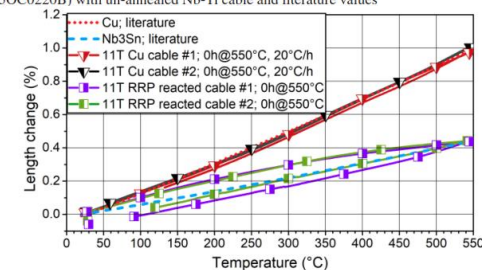
	Wire			Cable [11]
	Diameter change (%)	Cross-sectional area change (%)	Length change (%)	Length change (%)
RRP	+2.5	+4.9	-0.07	-0.32
PIT	+1.6	+3.3	-0.15	-0.40
IT	+1.1	+2.3	not measured	not measured



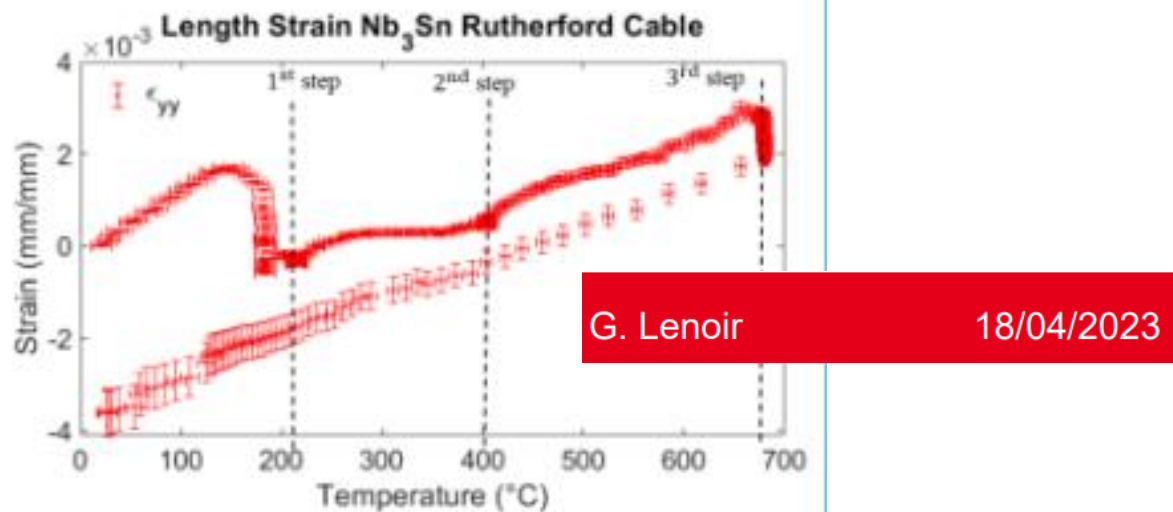
**Fig. 10:** Comparison of RRP #7419  $\text{Nb}_3\text{Sn}$  wire axial length change during first heating with that of DISCUS C3/30, Ti6Al4V, and 316LN. The relative length changes of a Cu wire and the Nb thermal expansion from reference [20] are shown for comparison.



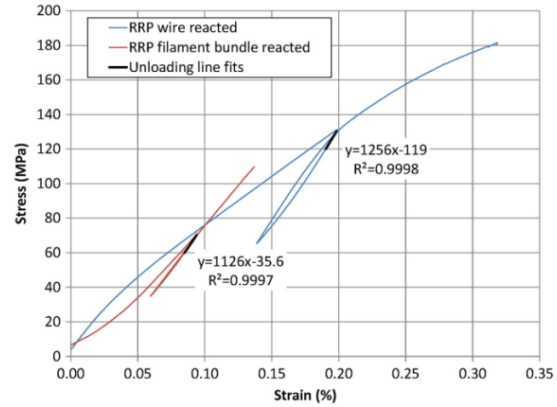
**Fig. 5.** Comparison of length change behaviour of unreacted  $\text{Nb}_3\text{Sn}$  RRP Rutherford cables (H15OC0220B) with un-annealed Nb-Ti cable and literature values for Ti-6Al-4V [6], Cu [16], Nb [21], bulk  $\text{Nb}_3\text{Sn}$  [16] and  $\text{Nb}_3\text{Sn}$  RRP wires [6].



**Fig. 6.** Relative length changes of un-annealed Cu Rutherford cables and reacted  $\text{Nb}_3\text{Sn}$  RRP Rutherford cables during heat treatment up to  $550\text{ }^\circ\text{C}$  and comparison with literature values for Cu and  $\text{Nb}_3\text{Sn}$  [16].



# Elastic modulus of RRP type Nb<sub>3</sub>Sn wire



- E is defined as the initial linear slope of the unloading curve.
- Determined elastic modulus of the reacted RRP wire: **126 GPa**

TABLE II  
Nb<sub>3</sub>Sn ELASTIC MODULI IN AXIAL AND TRANSVERSE DIRECTIONS  
CALCULATED FOR THE RRP AND PIT WIRES AT RT AND AT 4.2 K

		PIT B215	RRP #7419
RT	E <sub>axial</sub>	130	140
	E <sub>trans</sub>	135	129
4.2 K	E <sub>axial</sub>	106	127
	E <sub>trans</sub>	116	104

Fig. 3. Stress-strain curves measured at room temperature on a reacted RRP wire and its extracted filaments.

## Mechanical tests with MME:

Nous proposons une matrice d'essais comme suit :

- essais de dilatométrie 20-650-20C sur brins:
  - direction axiale :
    - 3x essai sous faible force
    - 3x essai sous traction a 3 N (Fmax)
    - 3\*Essai sous traction a 1.5 N
  - Direction transversale
    - 3x Essai à faible force
- Essais de « traction » de cables sous temperature contrôlée
  - 3x Traction à température ambiante → rigidité et Poissons
  - Cycle 20-650-20C :
    - 3x « 0 » force → déformations axiale et transversales
    - 3x F Force → déformations axiale et transversales
    - 3x X déformation axiale (  $F=k.X$  ) → force axiale et déformations transversales

Ici nous procéderons comme discuté pour l'arrimage des éprouvettes (collage céramique ) sur des inserts consommables. Un approche similaire a été décrit dans la littérature pour les basses températures (brin brassé a l'étain) avec des bonnes résultats. La mesure des déformations transversales reste compliquée, mais je pense que possible avec le système de Corrélation Digitale D'image.

Nous travaillons déjà sur le dessin des outillages. Je contacterai prochainement Hervé Rambeau pour planifier la fabrication (même si je pense que c'est un tout petit truc.).

Au niveau de la production des échantillons, il serait nécessaire de prévoir au moins:

- x15 segments d'au moins 30 mm (dilatométrie)
- x15 segments d'au moins 80 mm (traction)

Comme tu le sais, nous devons facturer no activités. Nous estimons le cout de la campagne en 8000 CHF.

To be added:

- Essais de traction sur brins