



Radboud  
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e l l i s



SURF

Nikhef

# Efficient ML-Assisted Particle Track Reconstruction Designs

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Radboud University



<https://arxiv.org/abs/2407.07179>

# Team

- **The project collaborators:**

- Radboud University (Nadezhda Dobрева)
- Nikhef (Sascha Caron, Zef Wolffs, Uraz Odyurt)
- SURF (Yue Zhao)
- University of Valencia (Antonio Ferrer Sanchez, Roberto Ruiz de Austri Bazan, Jose D. Martin-Guerrero)

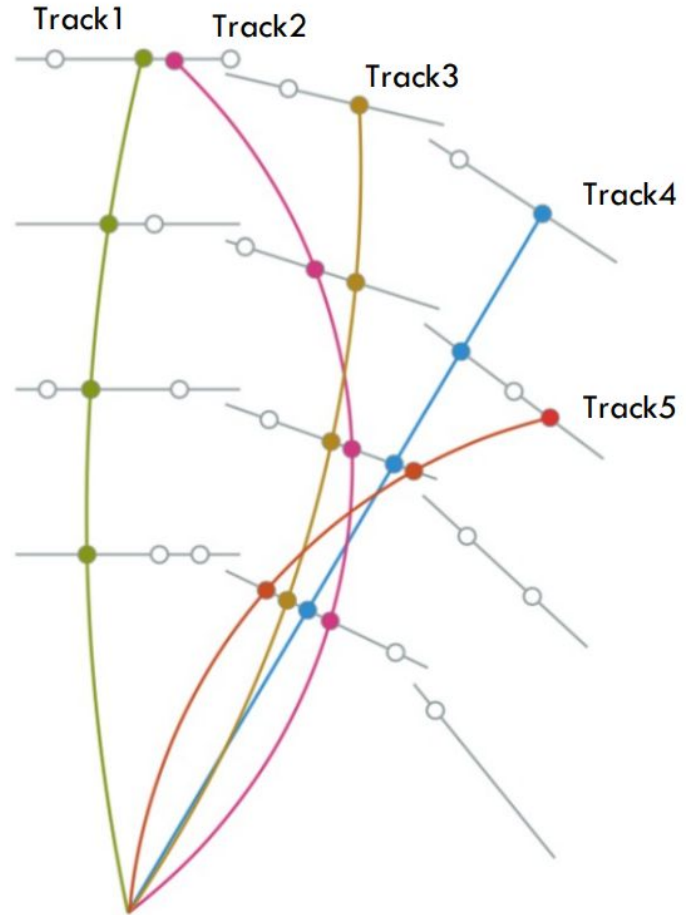
*Transformers*

*U-nets*

# Problem Definition

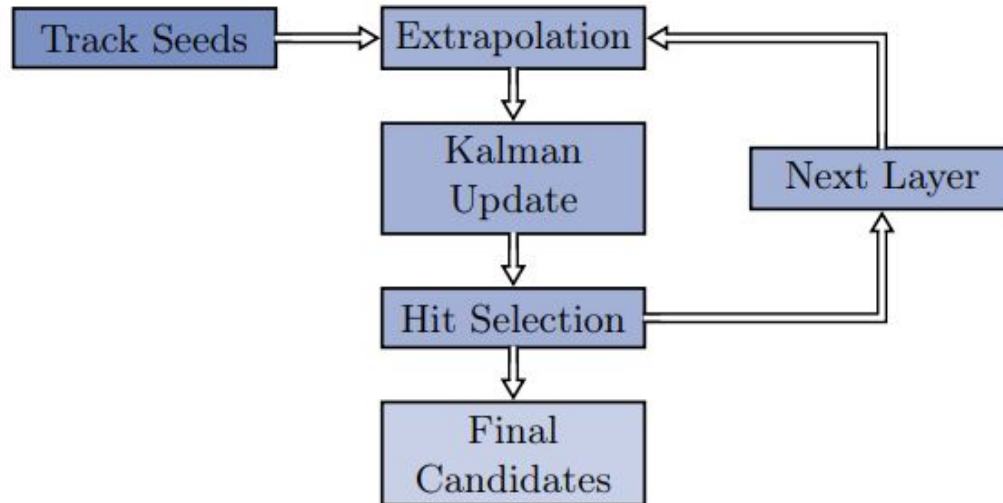
# Track Reconstruction

- **Track finding**
  - Grouping hits that likely originate from the same particle
- **Track fitting**
  - The derivation of track parameter of a group of hits
- **Track parameters**
  - Describe the particle trajectory



# Kalman Filters (KF)

- **Traditional algorithm for the task, used in LHC**
- **Track finding needs a combinatorial KF**



# Scalability Issue

- **KF and CKF scale poorly, inherently sequential [1]**
- **High Luminosity LHC**
  - Number of generated particles and recorded hits to increase manyfold [3]
- **12s per event [2] \***
- **Fast KF: 1.8s per event [2] \***

\* Used CPU: Intel Xeon E5-2620v2

# Active Field of Research

- **Graph neural networks**
  - Goal is to identify connections between the hits that represent actual physical trajectories
  - 2.2s\* per event [5]
- **U-nets**
  - A convolutional neural network for image segmentation
  - Investigated within our team: pixel segmentation

\* GPU used: Nvidia A100 Tensor Core

# The Transformer



# What is a Transformer?

- **Deep learning architecture**
- **Success in NLP (and many other fields)**

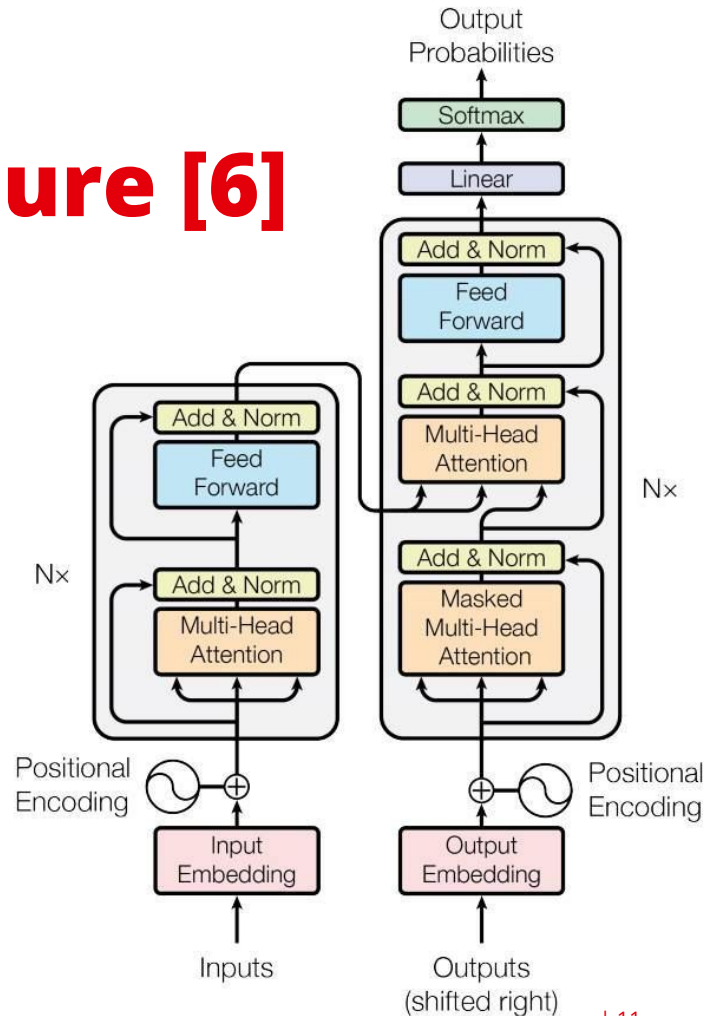
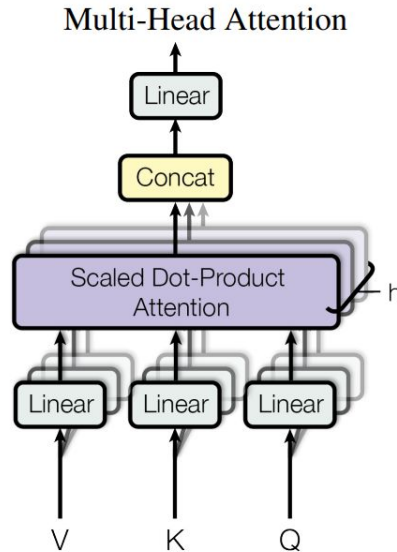
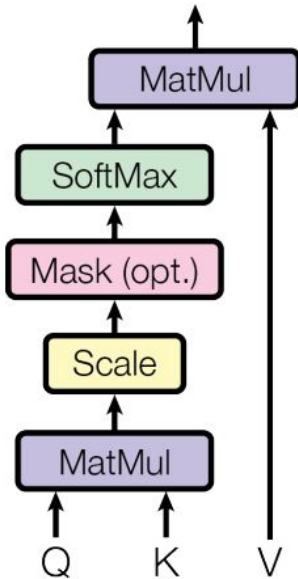


# Why Use a Transformer?

- Can be parallelized
- Can handle variable length input
- Equivariant to input order
- Captures complex non-linear dynamics in data

# Transformer Architecture [6]

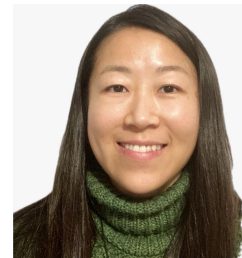
## Scaled Dot-Product Attention



# Proposed Approaches

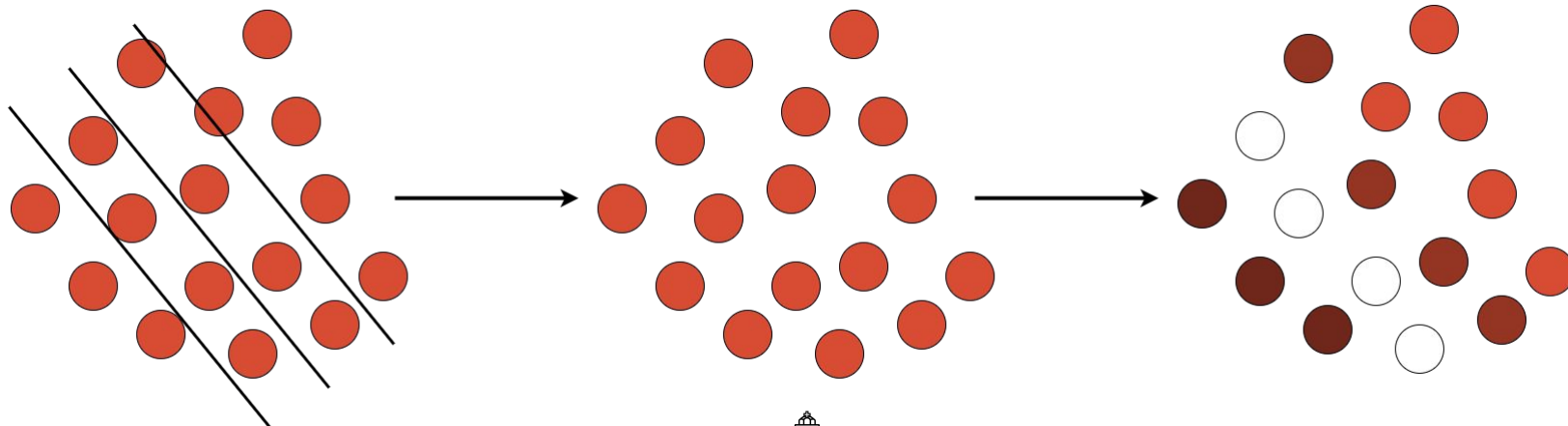
# Four Pipelines [11]

- **U-Net:** Segments digital image representation of event into segments representing the different tracks
- **Encoder-Decoder Model (EncDec):** Autoregressively builds the full track, starting from a given seed
- **Encoder-only Classifier (EncCla):** Based on distribution of track parameters among classes, predict the class of each hit
- **Encoder-only Regressor (EncReg):** Regress track parameters of each hit and cluster together based on proximity



# Encoder-only Classifier: EncCla

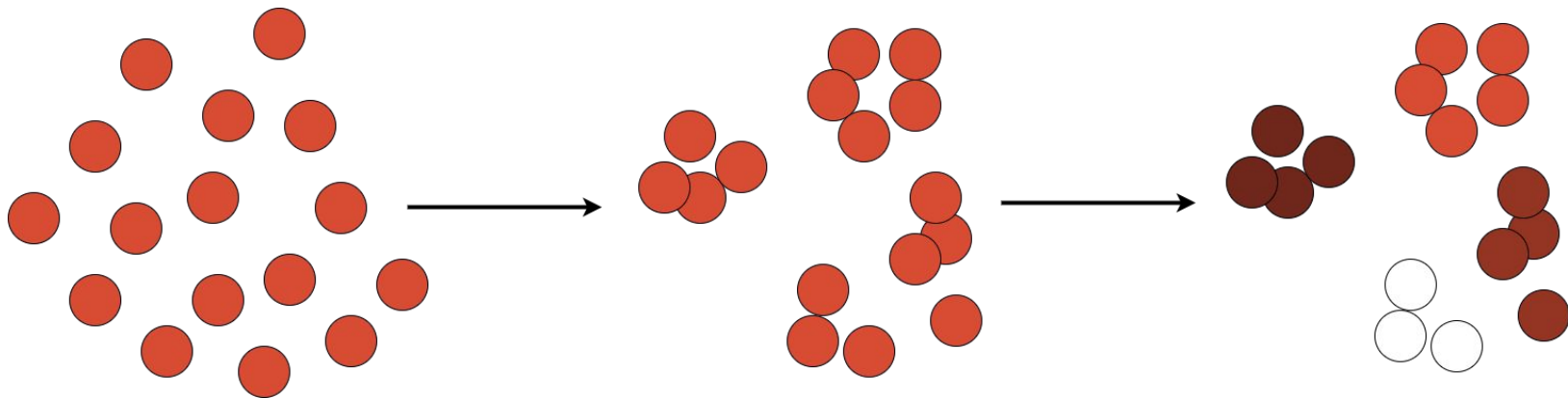
- Track defining parameters placed in balanced bins (i.e. classes)
- Transformer predicts the class of each hit





# Encoder-only Regressor: EncReg

- Used for regressing track-defining parameters
- Clustering hits based on regressed parameters



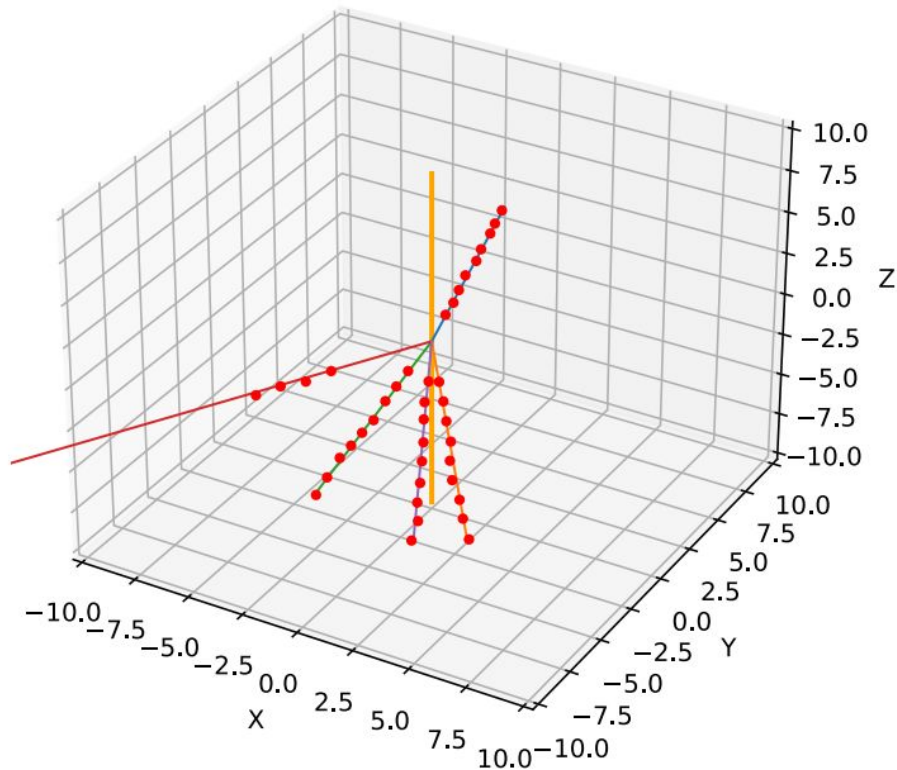
# Simulations



# Complexity-Reduced Approach

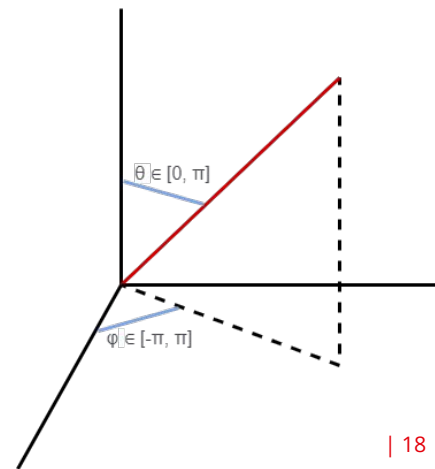
- **Iterative increase of complexity**
- **REDuced Virtual Detector (REDVID) [9]**
  - <https://virtualdetector.com/redvid/>
  - <https://indico.cern.ch/event/1338689/contributions/6015906/>
- **TrackML-derived subsets [4]**

# REDVID Linear Datasets

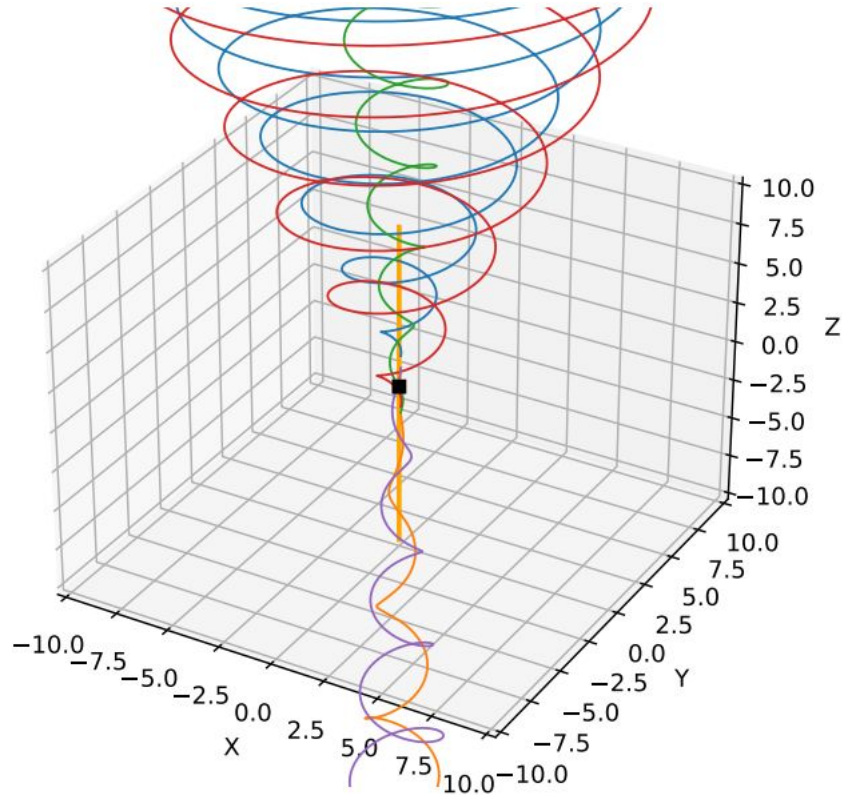


	3D-lin:10-50
Max nr. hits per event	450

**EncCla:** phi, theta, p  
**EncReg:** sin(phi),  
cos(phi), theta

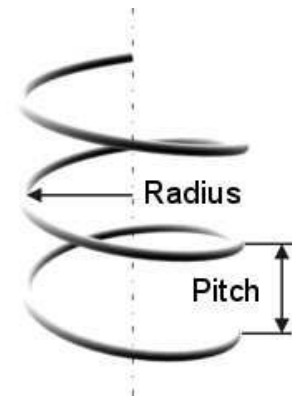


# REDVID Helical Datasets

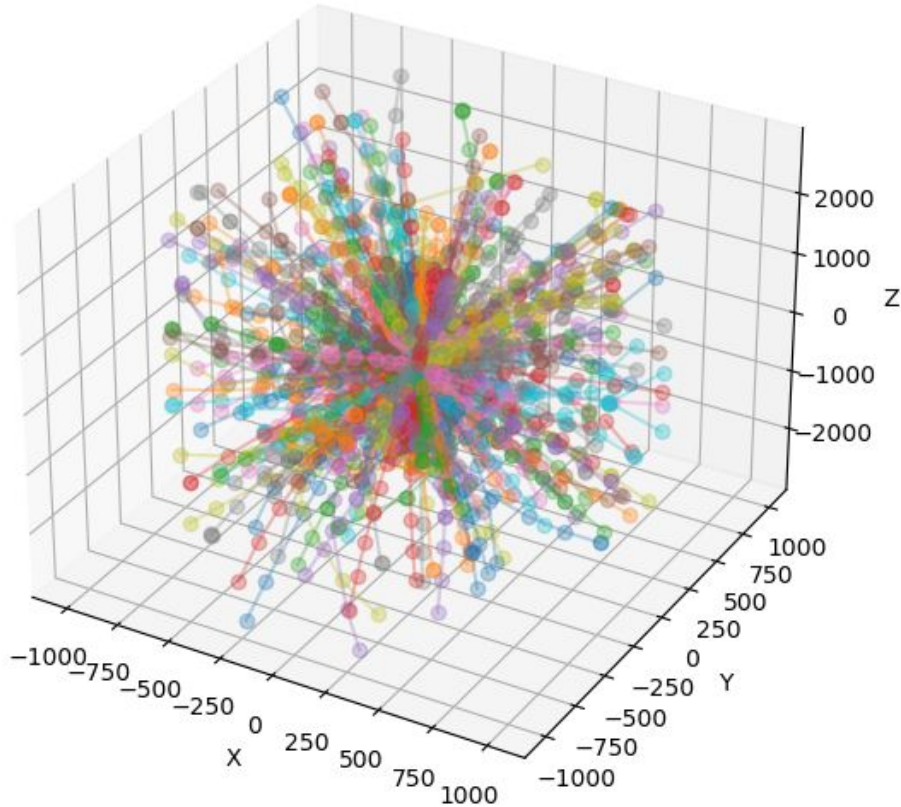


	3D-hel: 10-50	3D-hel: 50-100
Max nr. hits per event	450	900

**EncCla, EncReg, U-net:**  
**radial coefficient**  
**pitch coefficient**  
**azimuthal coefficient**

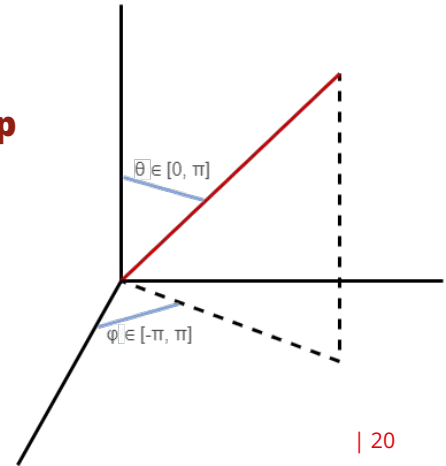


# TrackML-derived Datasets [4]

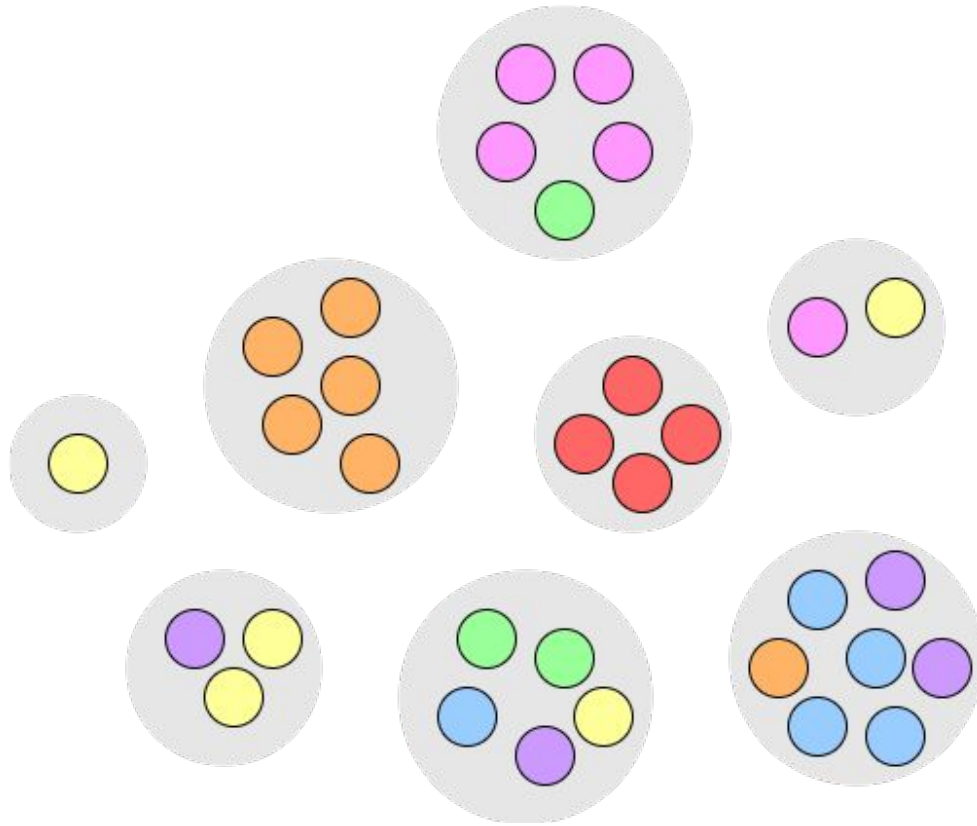


	TML:10-50	TML:200-500
Max nr. hits per event	700	5000

**EncCla: phi, theta, q, p**  
**EncReg: sin(phi), q, cos(phi), theta**



# Results

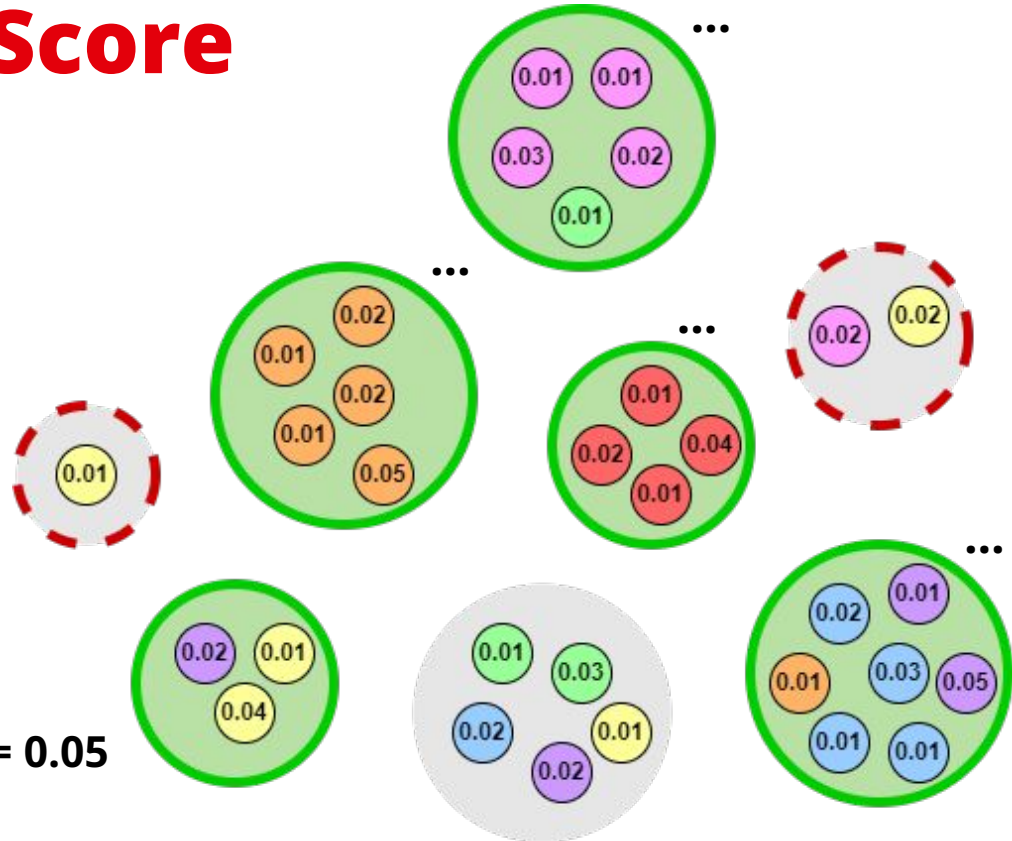


# FitAccuracy Score

## TrackML [4]

sum of weights of majority  
particle (>50% hits in cluster  
come from it)

$$0.04 + 0.01 = 0.05$$



# FitAccuracy Scores [11]

Data set	FitAccuracy score				U-Net
	EncDec	EncCla	EncReg	EncReg-FA	
REDVID - 10-50 linear tracks	93%	93%	<u>97%</u>	-	68%
REDVID - 10-50 helical tracks	85%	<u>93%</u>	92%	-	62%
REDVID - 50-100 helical tracks	85%	<u>88%</u>	85%	-	57%
TrackML - 10-50 tracks	26%	<u>94%</u>	93%	-	-
TrackML - 200-500 tracks	-	<u>78%</u>	70%	67%	-

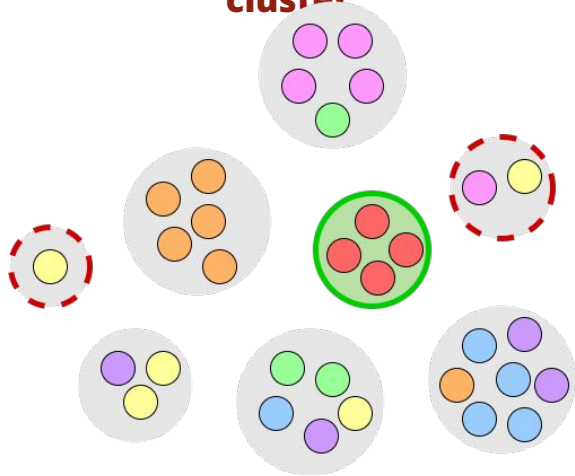
\* FA = Flash attention



# Other Efficiency Scores [5]

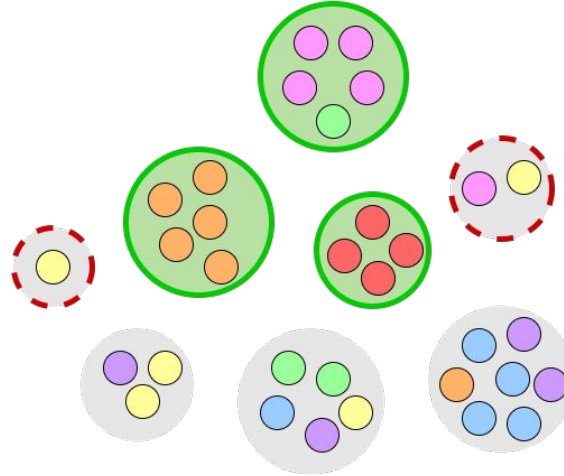
## Perfect

only hits from 1 particle  
no hits of it outside of  
cluster



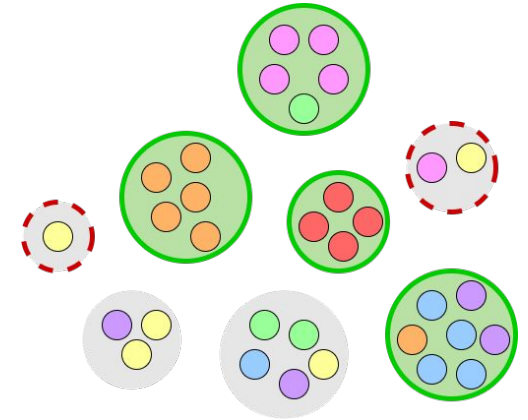
## LHC

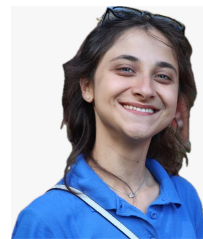
$\geq 75\%$  hits are from 1  
particle



## Double Majority

$\geq 50\%$  hits from 1 particle  
and  $< 50\%$  of its hits outside  
cluster



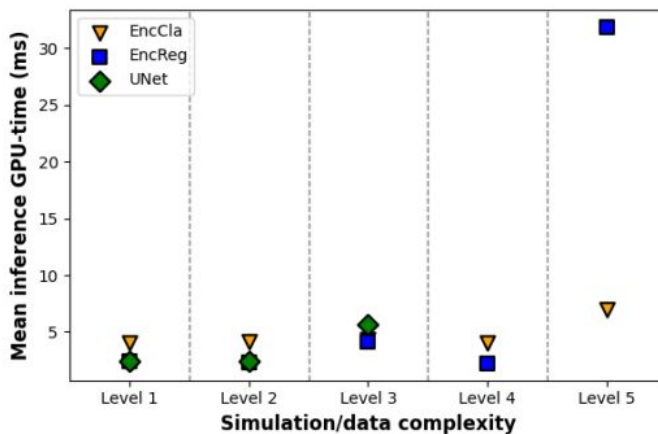
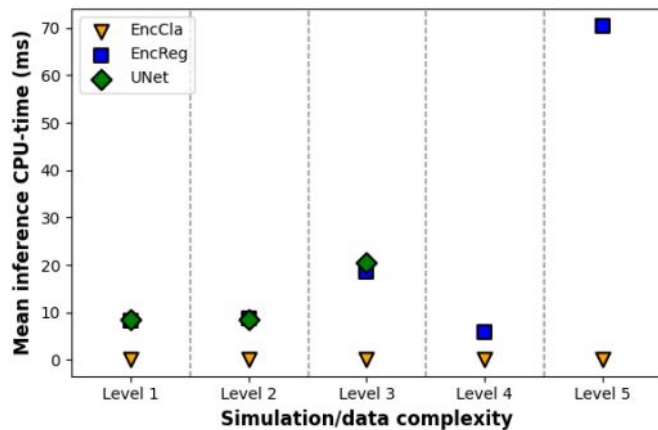


# Physics Performance of EncReg

	3D-lin:10-50	3D-hel:10-50	3D-hel:50-100	TML:10-50	TML:200-500
TrackML score	0.97	0.92	0.85	0.932	0.7 (0.67)
$\epsilon^{perf}$	0.94	0.78	0.6	0.78	0.4 (0.36)
$\epsilon^{DM}$	0.97	0.94	0.89	0.91	0.75 (0.72)
$\epsilon^{LHC}$	0.98	0.96	0.92	0.97	0.82 (0.79)

Table 6.2: Summary of the  $\epsilon^{perf}$ ,  $\epsilon^{DM}$ ,  $\epsilon^{LHC}$  and TrackML scores obtained by the Transformer Regressor models for the 5 used datasets. For the models trained on TML:200-500, the result with Flash attention is in parentheses.

# Computational Performance



Data set	Model	Inference (mean) CPU side	Inference (mean) GPU side	Inference (mean) Wall-clock
REDVID - 10-50 linear tracks	EncDec	n/a	n/a	41 s
	EncCla	0.1 ms	4.0 ms	-
	EncReg	8.3 ms	2.4 ms	-
	U-Net	8.5 ms	2.4 ms	-
REDVID - 10-50 helical tracks	EncDec	n/a	n/a	19 s
	EncCla	0.1 ms	4.1 ms	-
	EncReg	8.7 ms	2.3 ms	-
	U-Net	8.6 ms	2.4 ms	-
REDVID - 50-100 helical tracks	EncDec	n/a	n/a	27 s
	EncCla	0.1 ms	4.3 ms	-
	EncReg	18.6 ms	4.1 ms	-
	U-Net	20.4 ms	5.6 ms	-
TrackML - 10-50 tracks	EncDec	n/a	n/a	16 s
	EncCla	0.1 ms	4.0 ms	-
	EncReg	5.8 ms	2.2 ms	-
	U-Net	n/a	n/a	-
TrackML - 200-500 tracks	EncDec	n/a	n/a	-
	EncCla	0.1 ms	7.0 ms	-
	EncReg	70.5 ms	31.9 ms	-
	EncReg-FA	72.2 ms	3.6 ms	-
	U-Net	n/a	n/a	-

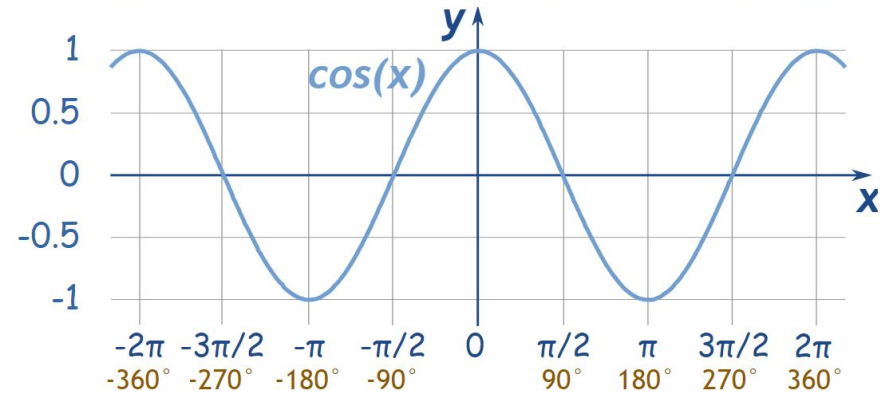
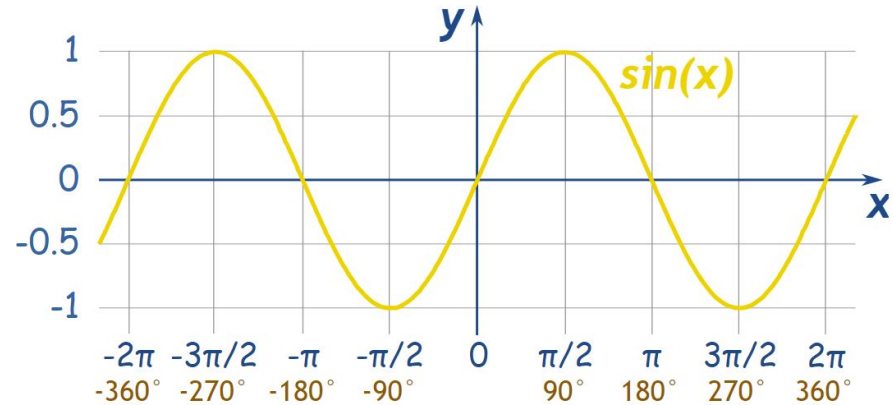
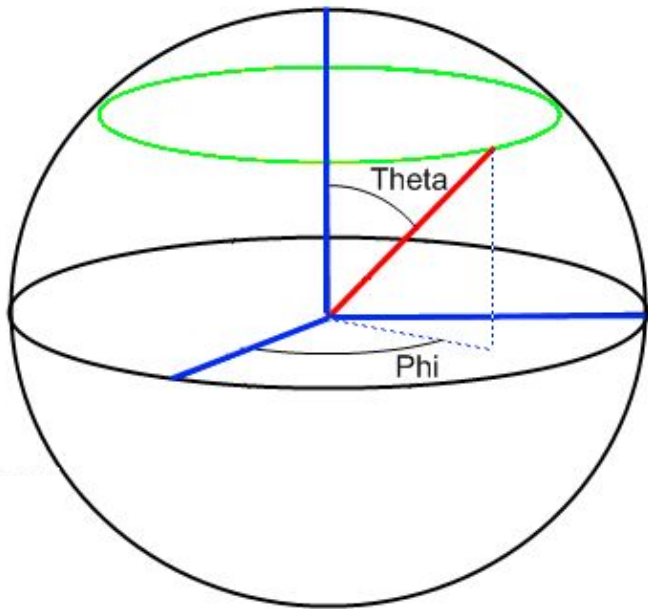
# **Transformers for tracking: promising and worth further research!**

**Thank you.  
Questions?**

# References

- [1] Braun, N. "Combinatorial Kalman filter and high level trigger reconstruction for the Belle II experiment." Springer, 2019.
- [2] ATLAS Collaboration. "Fast track reconstruction for HL-LHC." Tech. Rep. ATL-PHYS-PUB-2019-041, CERN, Geneva, 2019.
- [3] Apollinari, Giorgio, Lucio Rossi, and Oliver Brüning. "High luminosity LHC project description." No. CERN-ACC-2014-0321. 2014.
- [4] Amrouche, Sabrina, et al. "The tracking machine learning challenge: throughput phase." *Computing and Software for Big Science* 7.1 (2023): 1.
- [5] Ju, Xiangyang, et al. "Performance of a geometric deep learning pipeline for HL-LHC particle tracking." *The European Physical Journal C* 81 (2021): 1-14.
- [6] Vaswani, Ashish, et al. "Attention is all you need." *Advances in neural information processing systems*, 30 (2017).
- [7] Dao, Tri, et al. "Flashattention: Fast and memory-efficient exact attention with io-awareness." *Advances in Neural Information Processing Systems* 35 (2022): 16344-16359.
- [8] Stewart, Geoffrey, and Mahmood Al-Khassaweneh. "An implementation of the HDBSCAN\* clustering algorithm." *Applied Sciences* 12.5 (2022): 2405.
- [9] *Reduced Simulations for High-Energy Physics, a Middle Ground for Data-Driven Physics Research*, Uraz Odyurt, Stephen Nicholas Swatman, Ana-Lucia Varbanescu, Sascha Caron, 2023
- [10] Lieret, Kilian, et al. "High Pileup Particle Tracking with Object Condensation." arXiv preprint arXiv:2312.03823 (2023).
- [11] Caron, Sascha, et al. "TrackFormers: In Search of Transformer-Based Particle Tracking for the High-Luminosity LHC Era." (2024) <https://arxiv.org/abs/2407.07179>

# Rotational Invariance of Phi





# Rotational Invariance of Phi

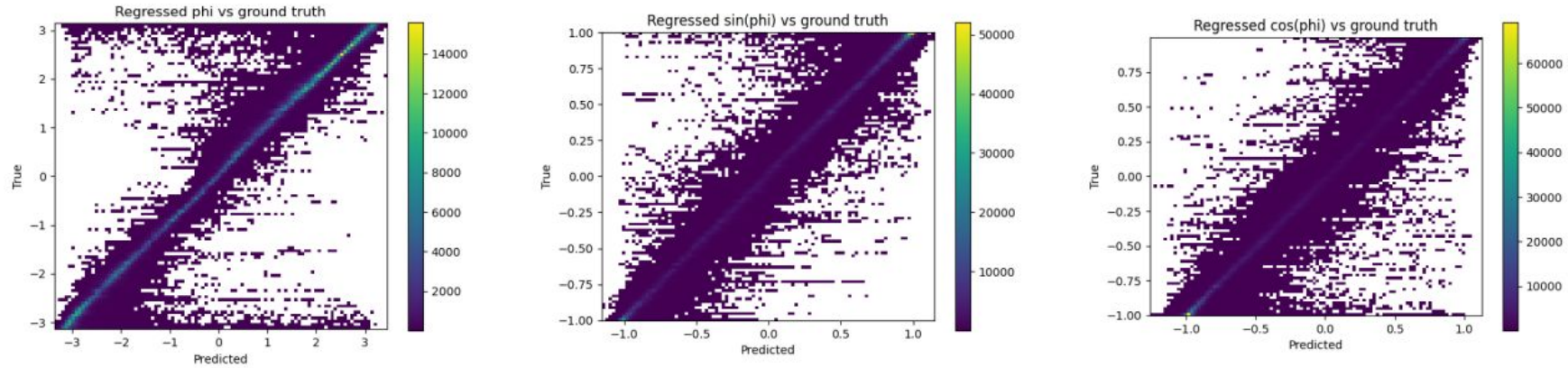
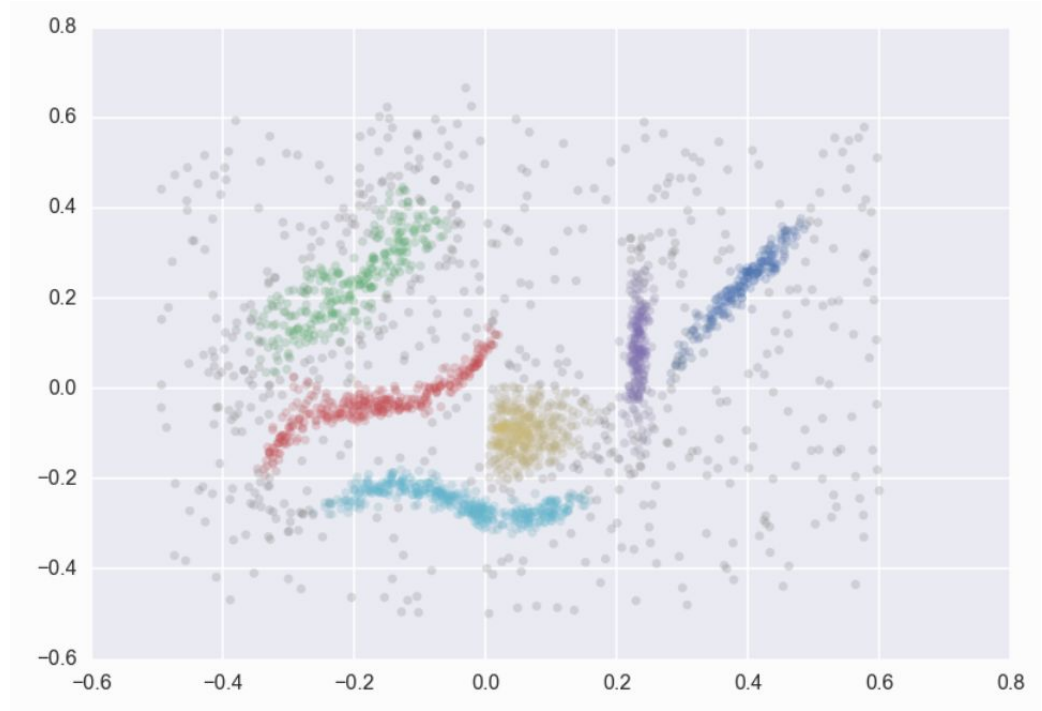


Figure B.1: Visualization of the regressed  $\phi$  plotted against the actual  $\phi$  for a model trained to regress  $\theta, \phi, q$  (left), and of the regressed  $\cos(\phi), \sin(\phi)$  plotted against the actual values for a model trained to regress  $\theta, \sin(\phi), \cos(\phi), q$  (middle, right). The models were trained on the TML:10-50 dataset.



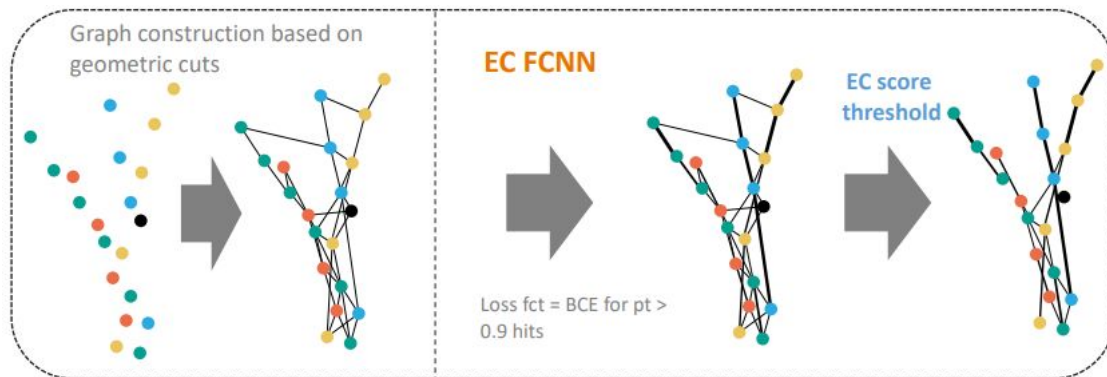
# HDBSCAN [8]

- **No pre-specified number of clusters**
- **No assumptions about the data and cluster distribution**
- **Time complexity in  $O(n^2)$**



# Graph Neural Networks

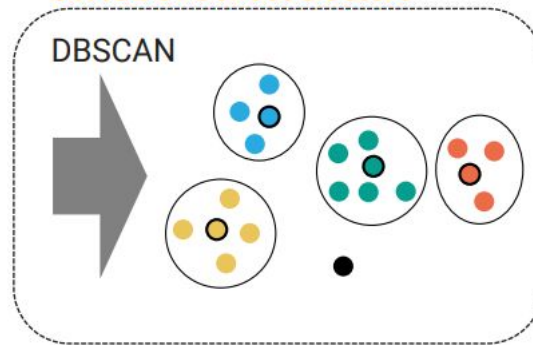
Lieret et al. [10]



## STAGE 2: Object condensation



## STAGE 3: Collect clusters



# Memory Bottleneck

- **MHA - memory intensive**
  - $L \times H$  matrices of  $S \times S$  floating point values
  - $L$  - nr. layers,  $H$  - nr. heads,  $S$  - sequence length
- **Flash attention [7]**
  - Splitting matrix in blocks and doing calculations separately, then combining results
  - 3x faster and 20x more memory efficient

# Refiner Network

- **Autoregressive model**
  - Adds hits to reconstructed tracks that were missed by the pipeline
- **Binary classifier network**
  - Determines whether each hit of a cluster truly belongs there
- **Regressor network**
  - Transformer Regressor, but per-cluster not per-event
  - Hits with track parameters too different from the rest of the group get removed