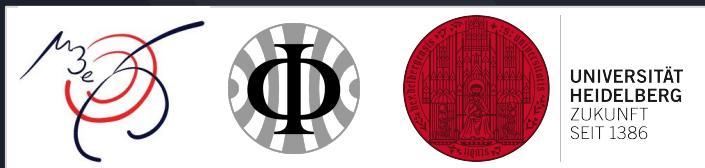


Feasibility Study of a Graph-Neural-Network-Based Cosmic Muon Trigger for the Mu3e Experiment

David Karres

On behalf of the Mu3e collaboration
Physikalisches Institut - Heidelberg University
CHEP 2024 - Kraków
October 19.-25. 2024

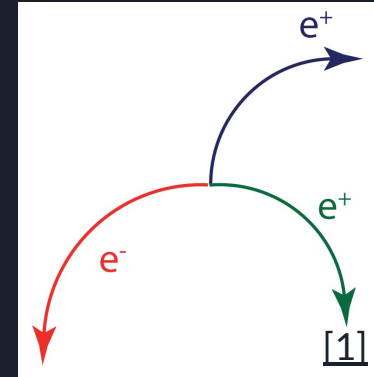




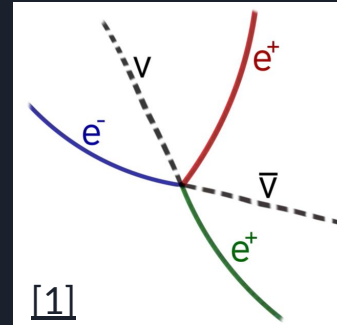
The Mu3e Experiment

- Located at the Paul Scherrer Institute (PSI) in Switzerland
- Planned to search for the lepton flavour violating decay $\mu^+ \rightarrow e^+ e^- e^+$
 - Standard Model branching ratio $< 10^{-54}$
 - Observation would point towards physics beyond the SM
- Goal:
 - Directly observe the decay, or
 - Set a new upper limit for the branching ratio of $< 10^{-16}$
- Background suppression requirements:
 - Momentum resolution $< 0.5 \text{ MeV}/c$
 - Precise vertex finding

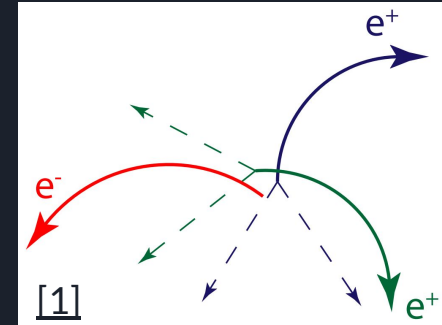
Signal topology



Internal conversion background ($\mu^+ \rightarrow e^+ e^- e^+ \nu \bar{\nu}$)



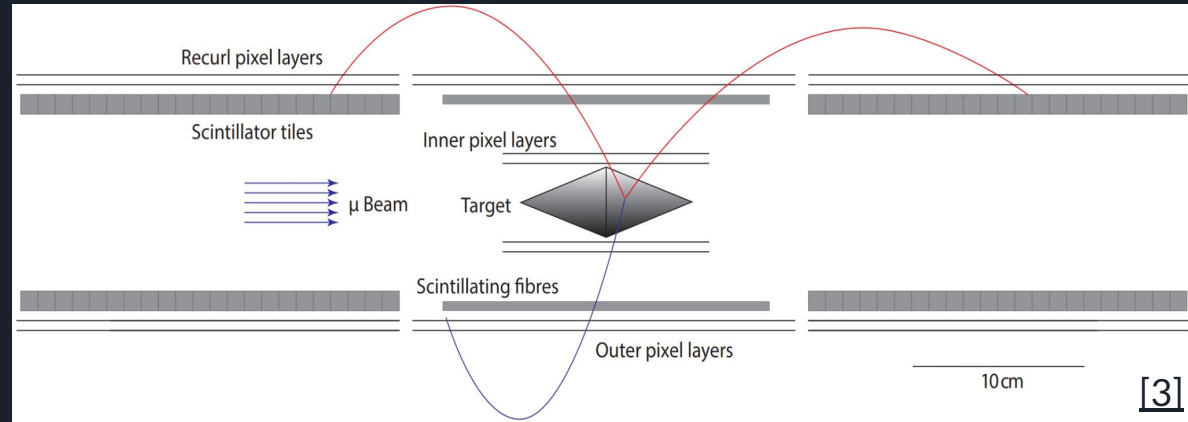
Combinatorial background Michel decay ($\mu^+ \rightarrow e^+ \nu \bar{\nu}$) + Bhabha





The Mu3e Pixel Tracking Detector

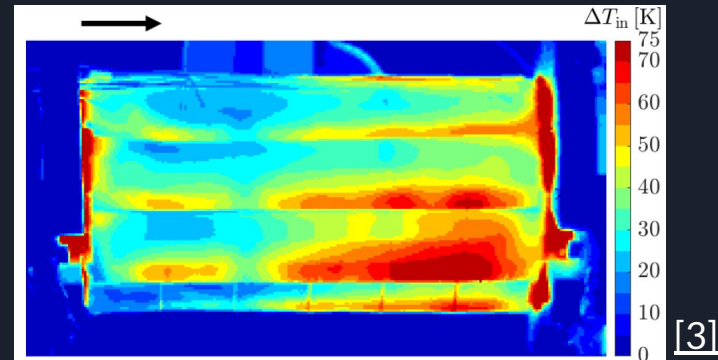
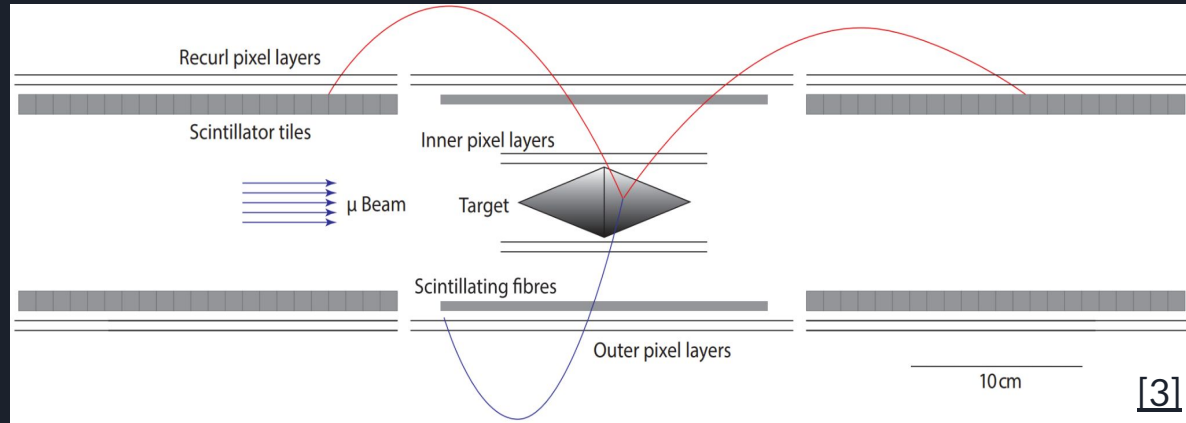
- Muon beam with 10^8 muons/second for phase I
 - Muons decay at rest on the target
- Ultra-thin silicon pixel sensors (MuPix)
- Solenoidal magnetic field, $B = 1\text{T}$
- Gaseous helium cooling





The Mu3e Pixel Tracking Detector

- Muon beam with 10^8 muons/second for phase I
 - Muons decay at rest on the target
- Ultra-thin silicon pixel sensors (MuPix)
- Solenoidal magnetic field, $B = 1T$
- Gaseous helium cooling
- Time-dependent misalignment factors:
 - Thermal expansion
 - Helium flow
 - Magnetic field
- Online detector alignment system required





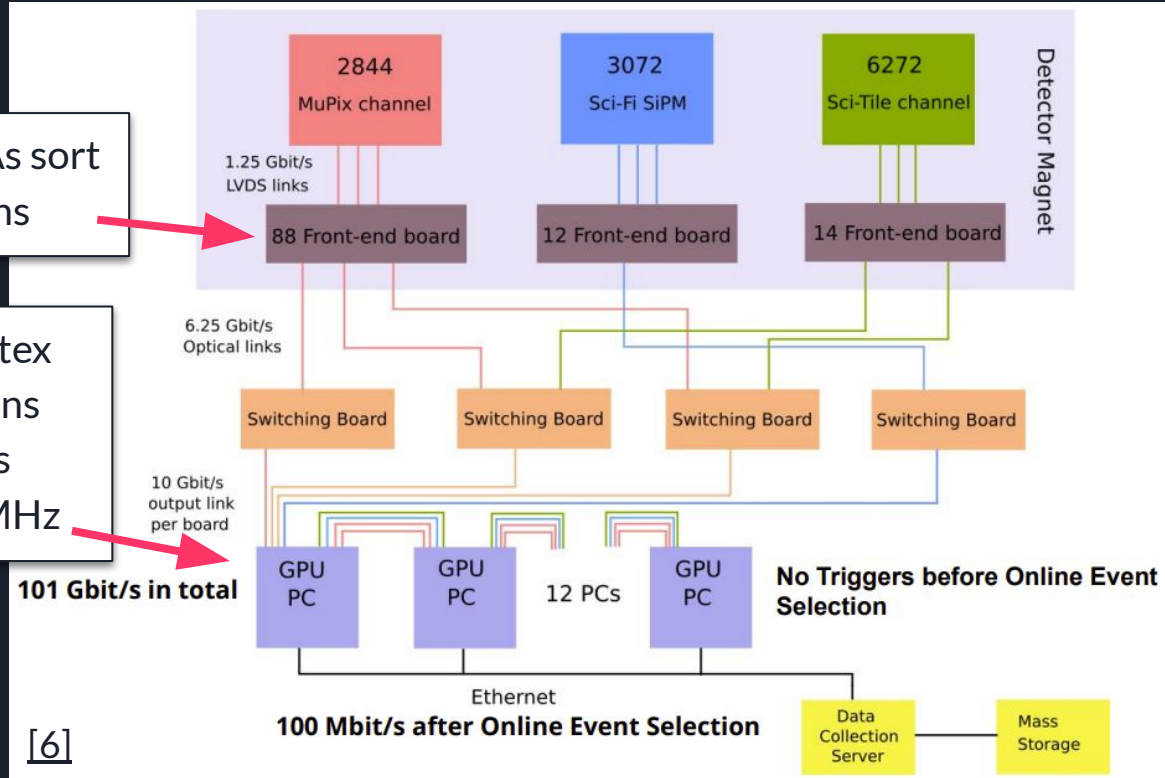
Data Acquisition at Mu3e

Front-end FPGAs sort data into 8 ns bins

Online track and vertex reconstruction of 64ns time frames on GPUs
↔ Frame rate 15.6 MHz

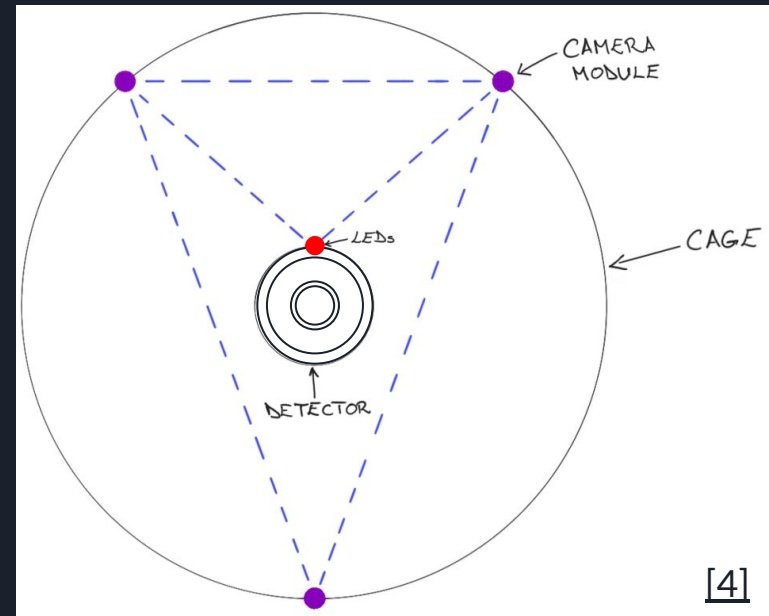
101 Gbit/s in total

[6]



Online Alignment at Mu3e

- Camera tracking system
 - Outer layer is tracked with cameras
 - Provide reference layer for alignment



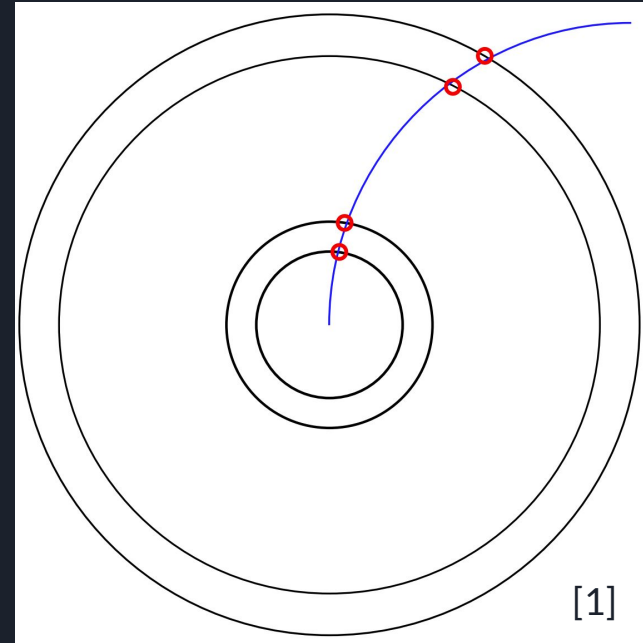
[4]



Online Alignment at Mu3e

- Camera tracking system
 - Outer layer is tracked with cameras
 - Provide reference layer for alignment
- Track-based alignment
 - Use tracks originating from the target in the central barrel
 - Minimize Chi2 by adjusting track and alignment parameters

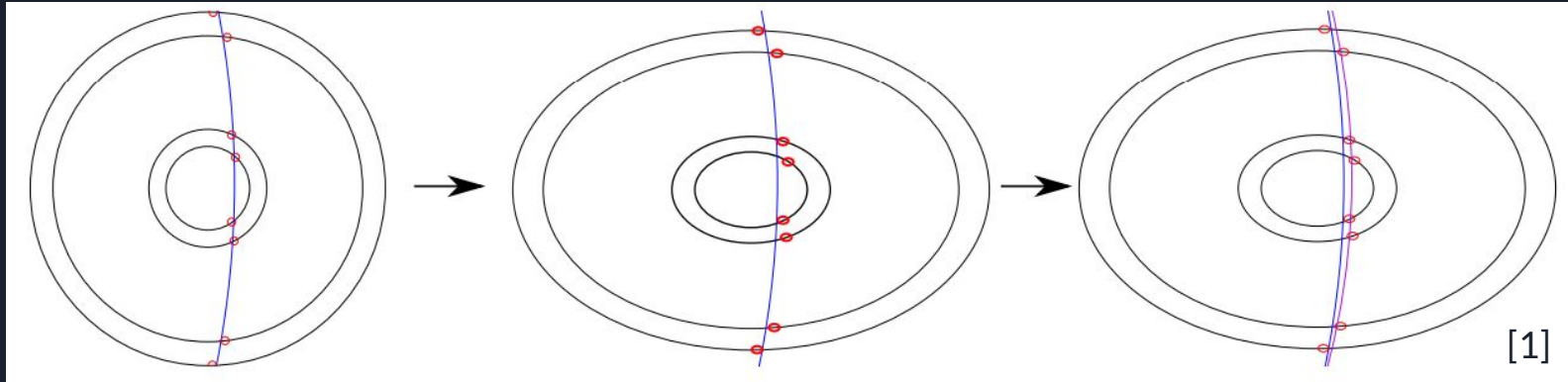
$$\chi^2(\mathbf{q}_j, \mathbf{p}) = \sum_j^{\text{tracks}} \sum_i^{\text{hits}} \left(\frac{m_{ij} - f(\mathbf{q}_j, \mathbf{p})}{\sigma_{ij}} \right)^2$$





Weak Modes

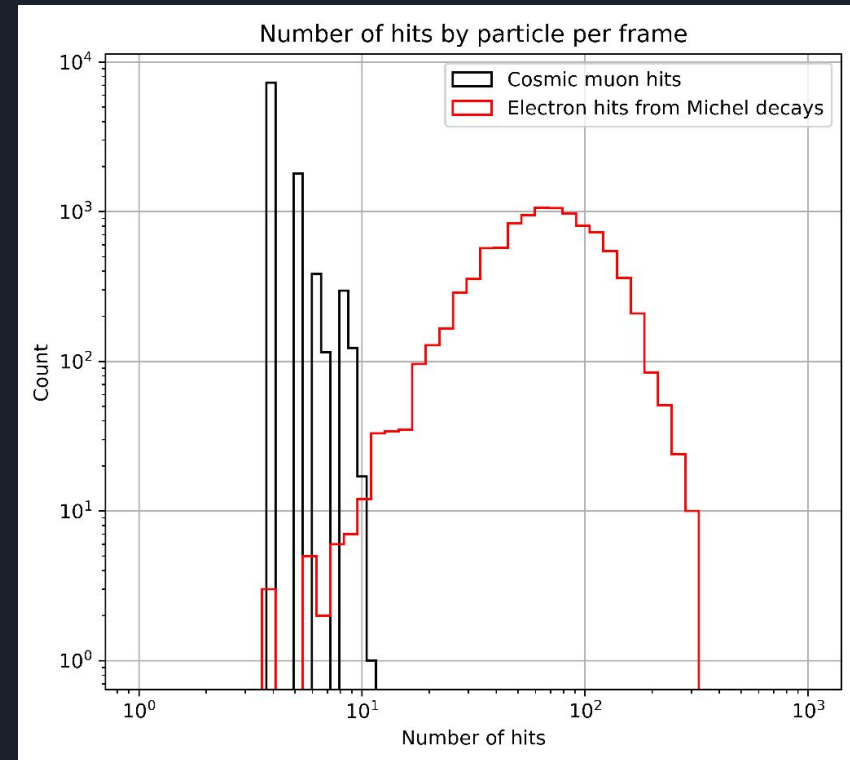
- Problem of track-based alignment: Weak modes
 - Global tracker deformations like bowing, twisting, etc.
 - Able to fit a track with equal Chi2 as for the aligned case
- Solution: Cosmic ray muons
 - Fundamentally different track topology
 - High momentum \Rightarrow Almost no deflection inside magnetic field
 - Even distribution over whole detector





Challenges for a Cosmic Muon Trigger

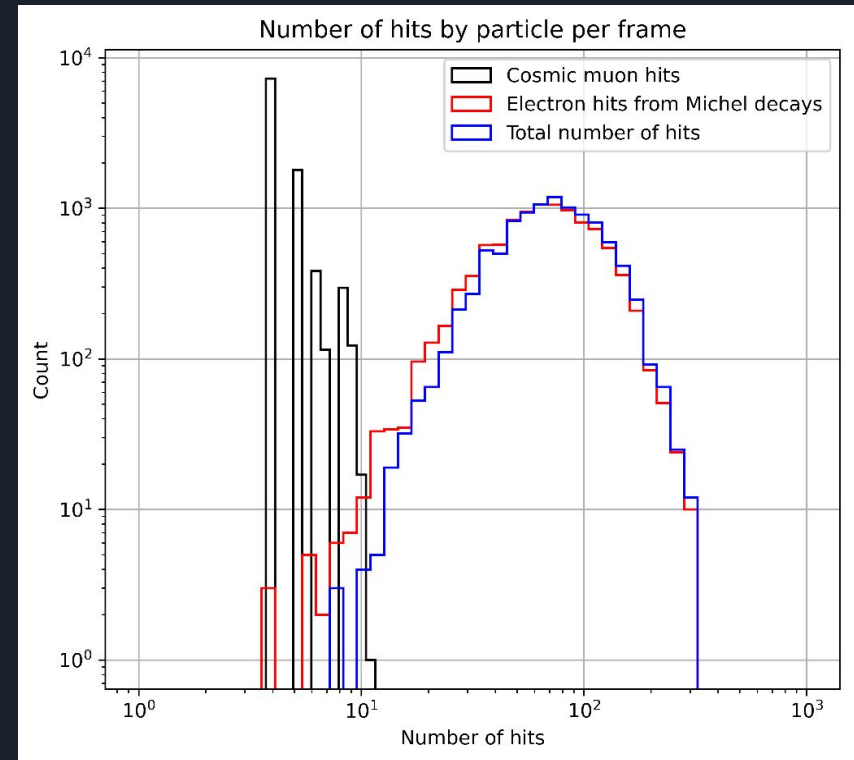
- Cosmics rate 10 Hz \leftrightarrow Beam rate 100 MHz:
Only 1 in 10^6 frames (64 ns) contain a cosmic muon
- Background suppression: 10^{-3} - 10^{-4} frames
- High trigger efficiency
- Most cosmics leave ~ 4 hits among $O(100)$ background hits per frame





Challenges for a Cosmic Muon Trigger

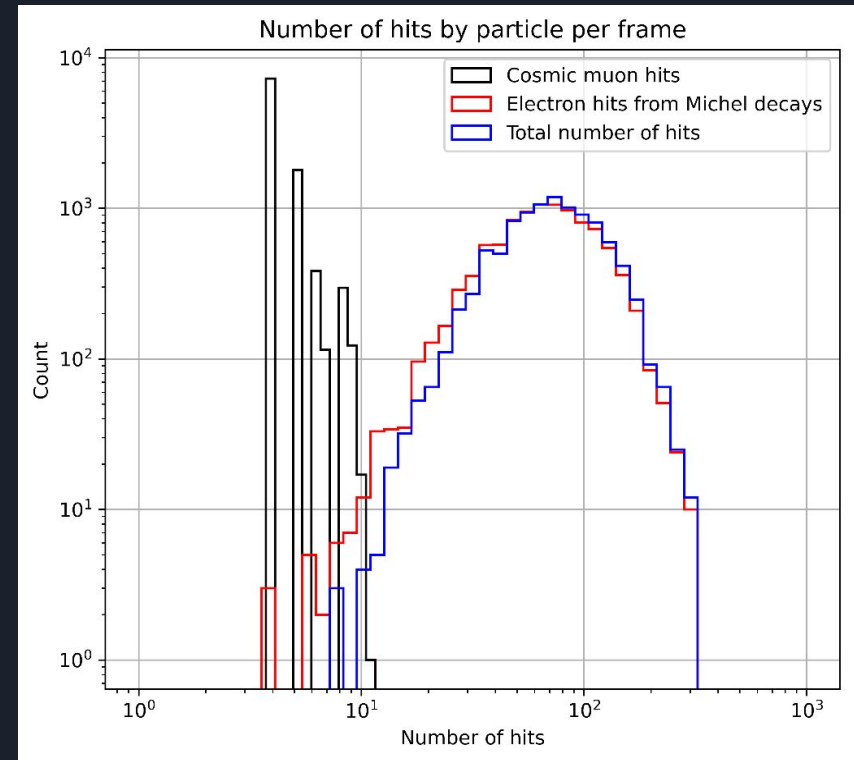
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Challenges for a Cosmic Muon Trigger

- Cosmics rate 10 Hz \leftrightarrow Beam rate 100 MHz:
Only 1 in 10^6 frames (64 ns) contain a cosmic muon
- Background suppression: 10^{-3} - 10^{-4} frames
- High trigger efficiency
- Most cosmics leave ~ 4 hits among
 $O(100)$ background hits per frame
- Previously studied: Hardware-based pattern
recognition with associative memory chips [\[5\]](#)
- This study: **Graph neural networks (GNNs) for
cosmic muon track reconstruction**

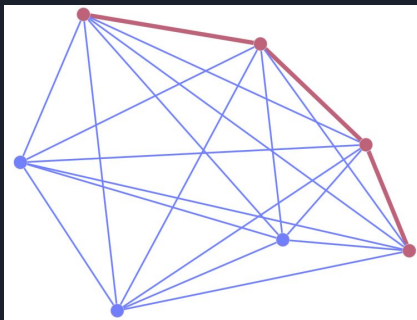




Track Reconstruction with Graph Neural Networks

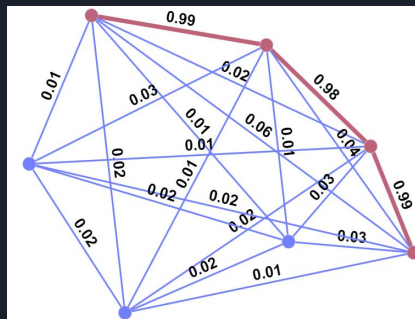
Graph Construction

- Represent frames as graphs
- Hits \leftrightarrow Nodes
- Track segments \leftrightarrow Edges
- Frames contain $O(10^2)$ hits
 \Rightarrow Fully connected graphs
 $\Rightarrow O(10^4)$ edges/graph



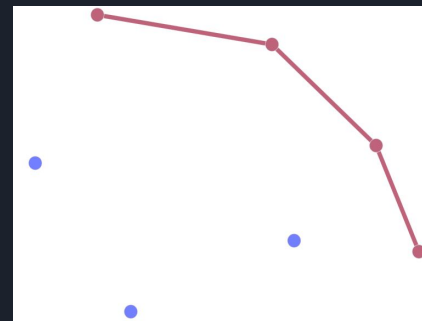
Edge Labeling

- Infer edge-classifying GNN to obtain edge scores $\in [0,1]$
- High score \leftrightarrow Muon edge
- Low score \leftrightarrow Fake/electron edge



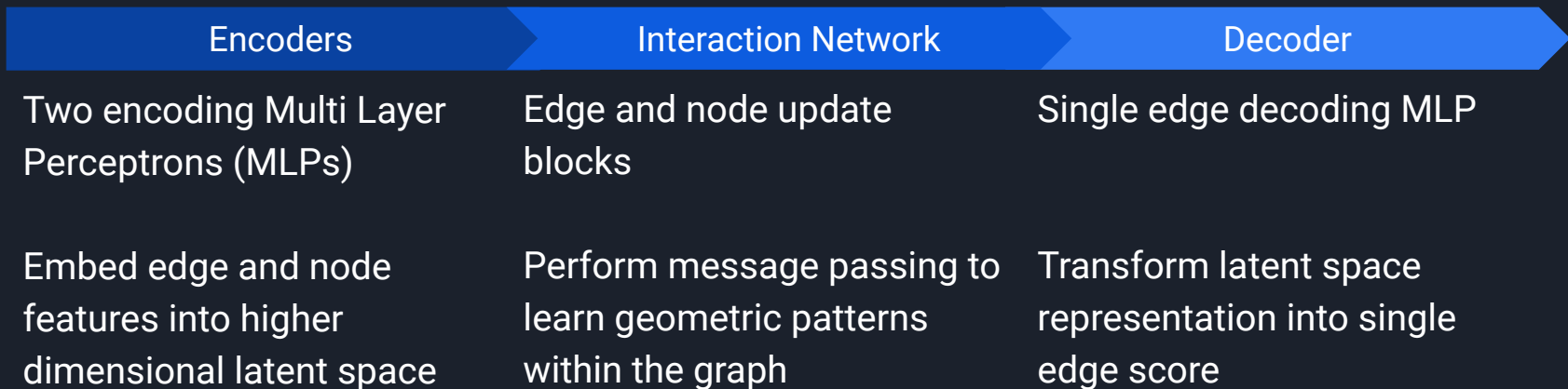
Track Reconstruction

- Cut edges below threshold
- Run connected components algorithm to obtain track candidates
- Keep candidates with ≥ 4 hits





Edge Labeling with Graph Neural Networks



Preliminary model size optimization:

- 24 dimensional edge- and node feature embeddings
- 4 message passing steps
- 2 hidden layers per MLP

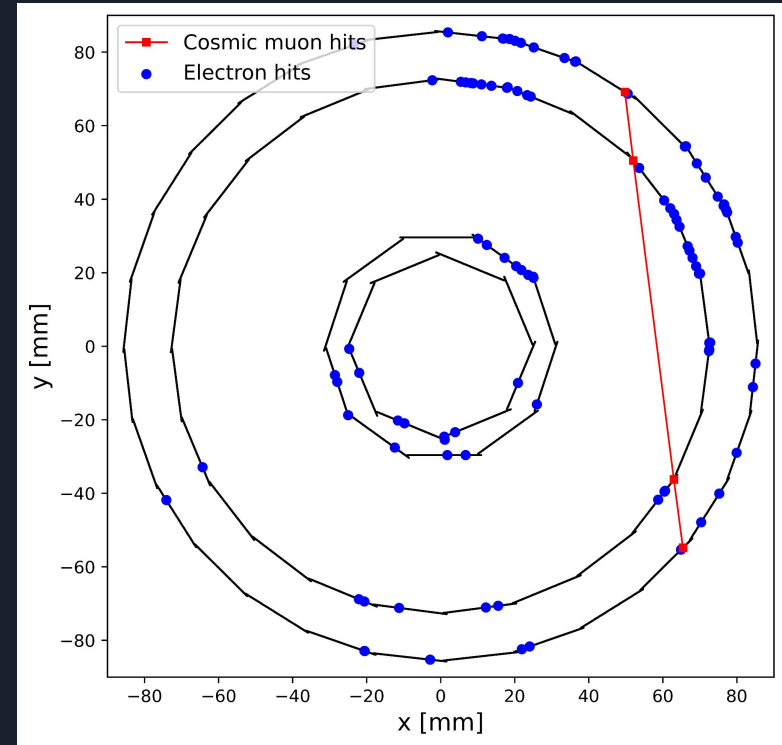
Based on the Acorn framework [\[7\]](#)





Data Samples for Training and Inference

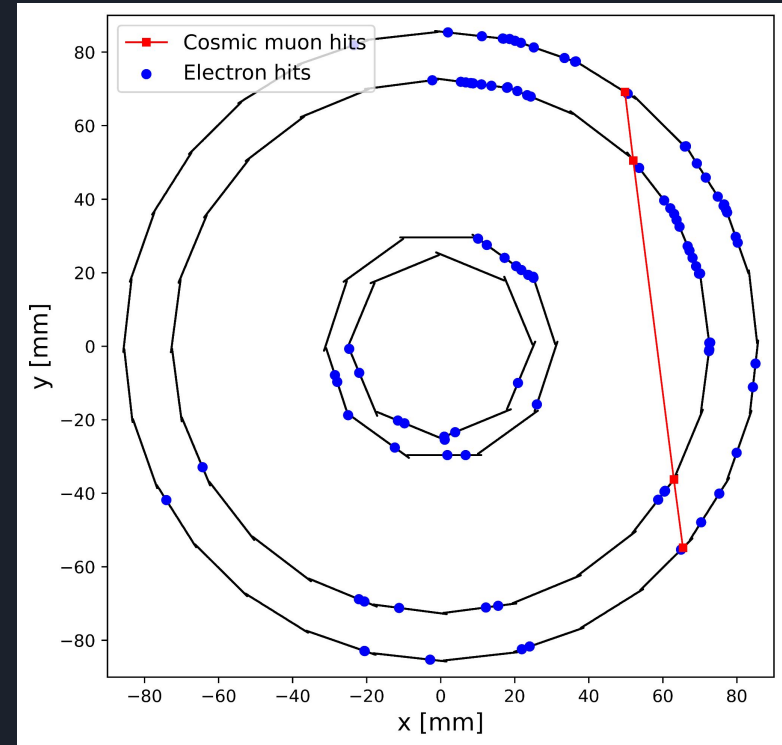
- Simulated samples for training and inference via Mu3e simulation package (based on Geant4)
- Data samples:
 - Cosmic muons mixed with Michel decays (signal)
 - Michel decays only (background)
- Train on:
 - 100% Cosmics with Michel
 - 50% Cosmics with Michel + 50% Michel only (boost background rejection)
 - 10k training frames/epoch
 - 1k frames/epoch for validation and testing





Track Reconstruction: Definitions

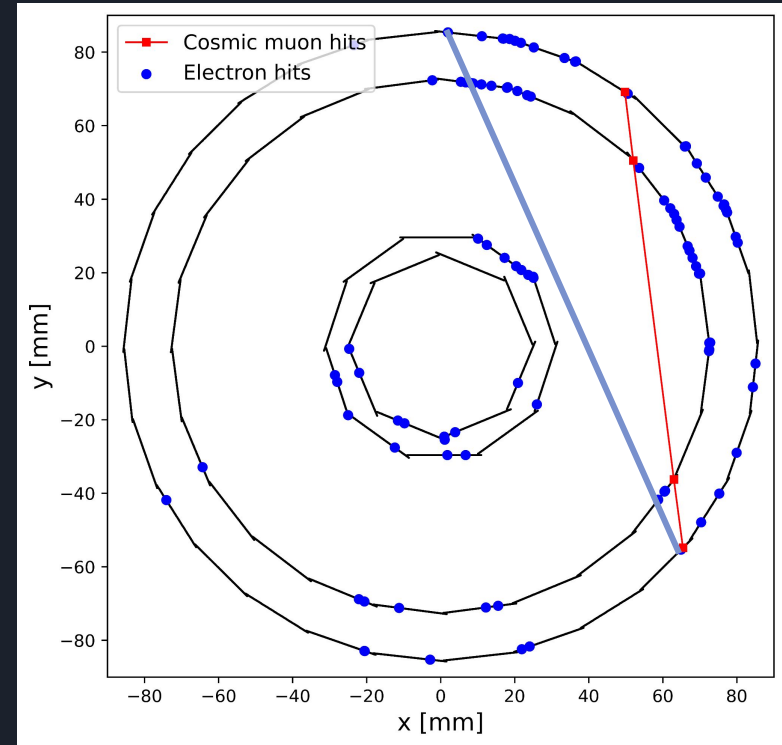
- **True track:** All hits from cosmic muon
- **Fake track:** At least one non-muon hit
⇒ Trigger any frame with at least one reconstructed cosmic muon track
- Track reconstruction efficiency:
 - Evaluate on cosmics with Michel
 - #triggers/ #signal frames
- Background acceptance:
 - Evaluate on Michel only
 - #triggers / #background frames





Track Reconstruction: Definitions

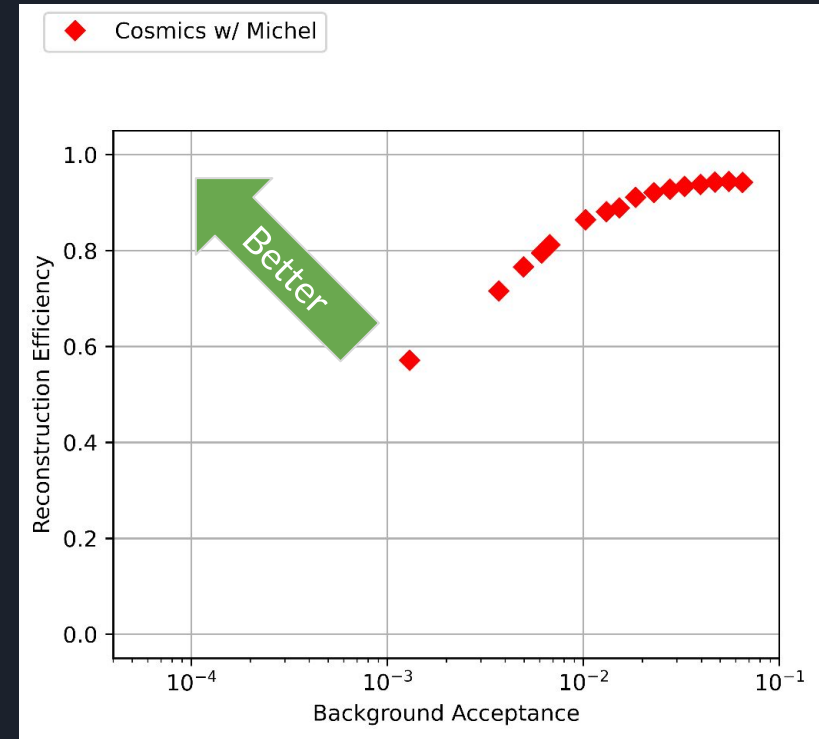
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Track Reconstruction: Evaluation

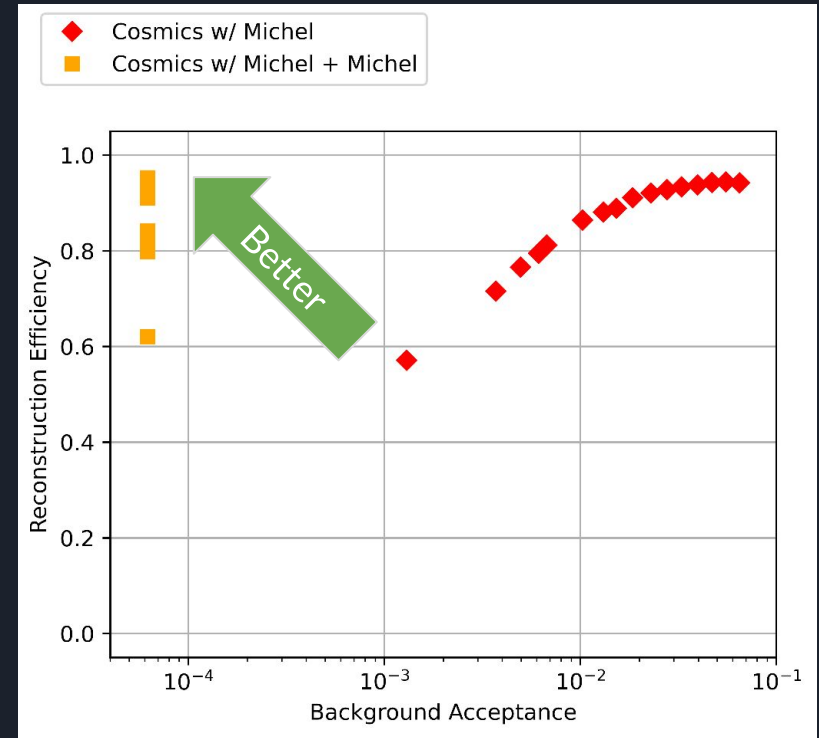
- Inference on 16k Michel frames and 1k cosmics with Michel frames
- **Baseline model**
 - Reconstruction efficiency $\leq 95\%$
 - Efficiency drops below 80% at background acceptance $\sim 6 \times 10^{-3}$





Track Reconstruction: Evaluation

- Inference on 16k Michel frames and 1k cosmics with Michel frames
- **Baseline model**
 - Reconstruction efficiency $\leq 95\%$
 - Efficiency drops below 80% at background acceptance $\sim 6 \times 10^{-3}$
- Adding **Michel only** frames decreases background acceptance by orders of magnitude
 - Reconstruction efficiency $\sim 95\%$ at background acceptance $\leq 6.2 \times 10^{-5}$
 - Only one fake track observed \Rightarrow Statistically limited





Summary

- Utilization of graph neural networks for cosmic muon track reconstruction are studied for the Mu3e experiment
- Massive boost in performance by training on **Cosmics with Michel + Michel only**
 - Track reconstruction efficiency: 95.2% at background acceptance: $\leq 6.2 \times 10^{-5}$
 - Full reconstruction rate of < 1000 frames/s required
- Online trigger deployment on GPU or FPGA is targeted
 - Throughput (and optimization) has to be studied



References

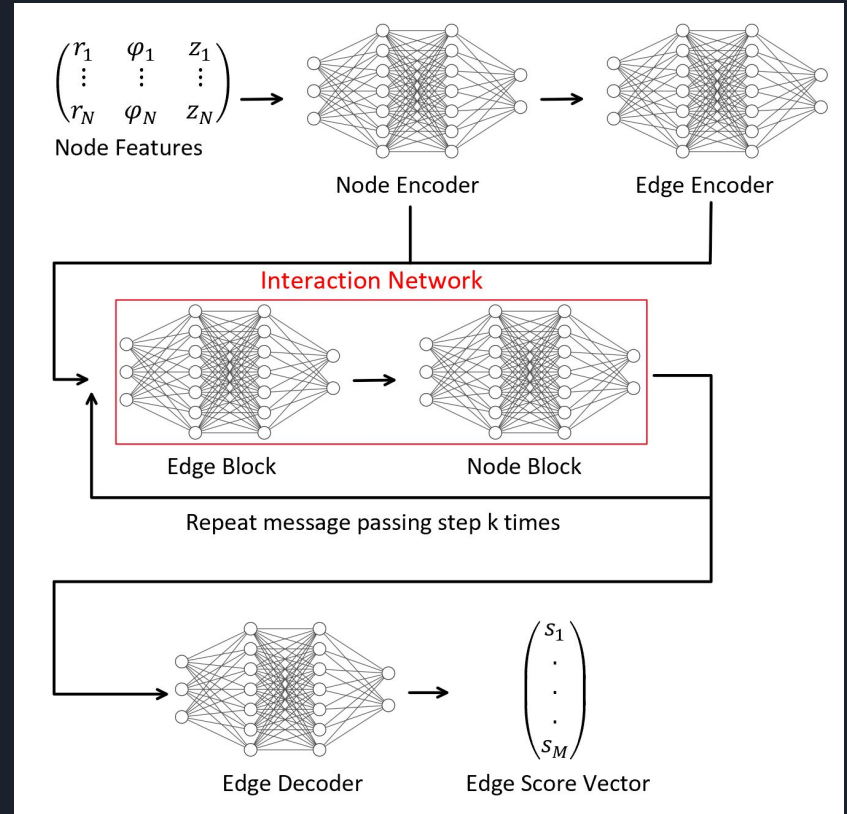
- [1] U. Hartenstein, Track Based Alignment for the Mu3e Pixel Detector, 2019, [Link](#)
- [2] [Mu3e Collaboration Website](#)
- [3] K. Arndt et al., Technical design of the phase I Mu3e experiment, 2020, published in [Nucl.Instrum.MethA. 1014, 165679, 2021](#)
- [4] G. Stanic, A Camera Alignment System for the Mu3e Experiment, 2021, [Link](#)
- [5] K. Neureither, Towards an Online Reconstruction of Cosmic Muons for Mu3e using Hardware-Based Pattern Recognition, 2020, [Link](#)
- [6] H. Murugan, Online Track Reconstruction for the Mu3e Experiment, DPG Spring Meeting, 2024, [Link](#)
- [7] Git Repository of the Acorn framework, [Link](#)

Backup



Edge Labeling with GNNs

- Want to classify edges as true or false
 - Assign edge scores and label all edges below a score cut threshold as false and the rest as true
- Node features (cylindrical hit coordinates) are embedded into a latent space by the node encoder
- Edge encoder takes both embedded node features and generates edge features
- Both embeddings are passed to the interaction network to perform k message passing steps
- Edge decoder takes the transformed embedding and outputs a single number - the edge score



Message Passing in an Interaction Network

- Graph with embedded node and edge features is fed into interaction network
- Edge block MLP takes embedded edge feature and the connected node features and updates it
- Node block MLP takes embedded node feature and an aggregation (e.g. a sum) of the updated edge features to output node update
- Repeat k times to extract higher level geometric patterns

