

Navigating Phase Space for Event Generation – interfacing Sherpa with BAT.jl

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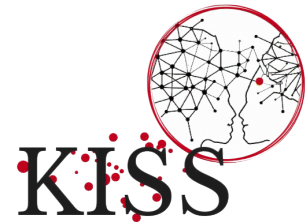
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Track 5: Simulation and Analysis Tools



Motivation - Improving Sampling Efficiency

- high-energy physics heavily relies on simulated events \Rightarrow Monte Carlo simulations
- we need high-statistic samples to precisely investigate tails of distributions and more complex final states
- MC simulation efficiency and speed need to improve for precision era, e.g. for HL-LHC (factor ~ 25 more simulated data required)
- multiple efforts made such as ML, nested sampling, MCMC sampling

[Yallup et al. [2205.02030](#)]
[Danziger et al. [2109.11964](#)]
[Kröninger et al. [1404.4328](#)]

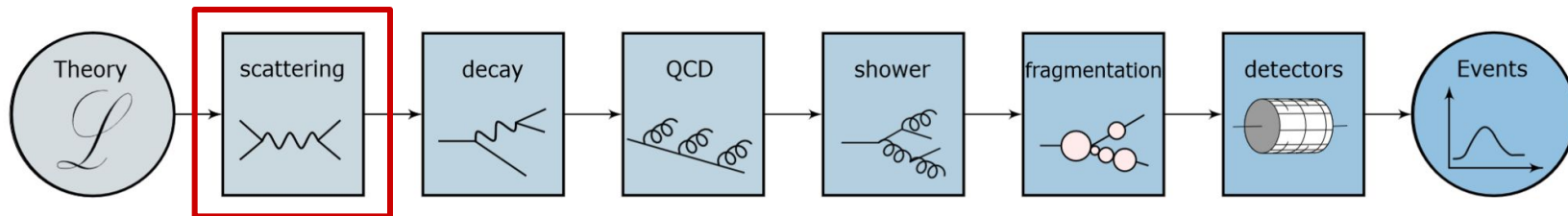
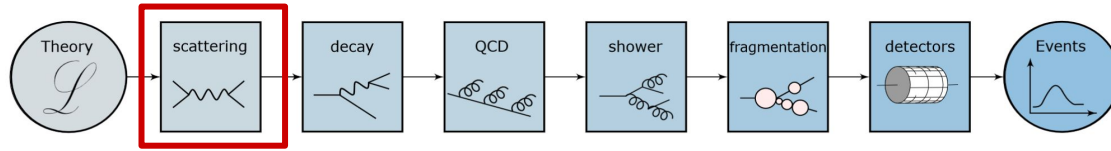


Image: Machine learning and LHC event generation, Butter et al., [10.21468/SciPostPhys.14.4.079](#), SciPost Physics 14 (2021)

The Challenge - Expensive event generation



Computational bottleneck: the hard scattering component

$$\sigma_{pp \rightarrow X_n} = \sum_{ab} \int dx_a dx_b d\Phi_n f_a(x_a, \mu_F^2) f_b(x_b, \mu_F^2) |\mathcal{M}_{ab \rightarrow X_n}|^2 \Theta_n(p_1, \dots, p_n)$$

Difficulty:

- $|\mathcal{M}|^2$ is typically multi-modal, wildly fluctuating & computationally expensive

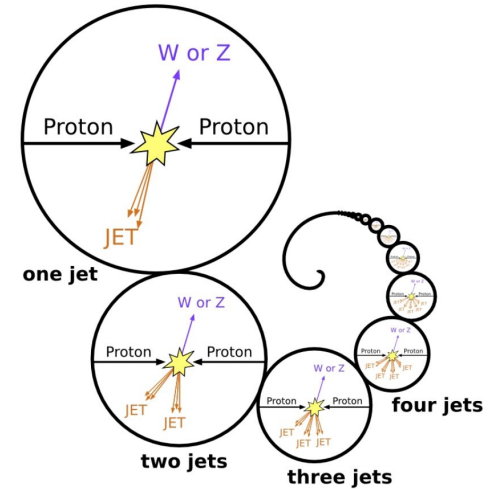


Image by Jim Pivarski

<https://www.fnal.gov/pub/today/images/images12/figure.jpg>

Sherpa

- MC event generator for collision events
 - Built-in matrix element generators AMEGIC & COMIX
- Sherpa v.3.0 released 3 months ago
- user-friendly configuration files for selecting processes and setting cuts
- main sampling method: importance sampling within physics-informed channel mappings

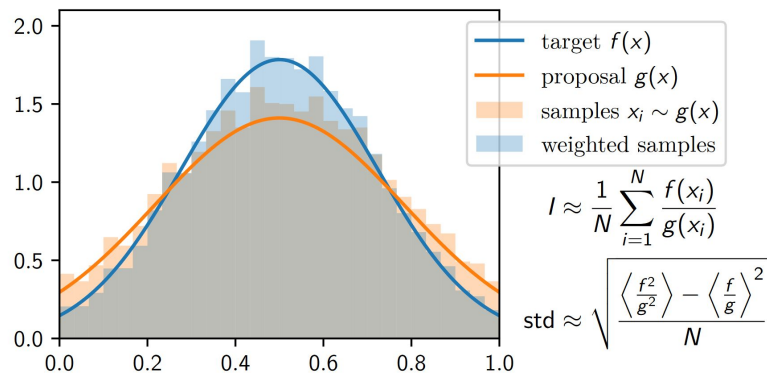


<https://sherpa-team.gitlab.io>

[Bothmann et al., [SciPost Phys.7 \(2019\)](#)]

Sherpa.yaml

```
33 TAGS: {
34   MCUT: 66.0,
35   NJETS: 3,
36   PTMIN: 20.0
37 }
38
39 BEAMS: 2212
40 BEAM_ENERGIES: 6500.
41
42 EVENTS: 100000
43
44 PROCESSES:
45 - 21 21 -> 11 -11 1 -1 21:
46   ME_Generator: Amegic
47   Order: {QCD: Any, EW: 2}
48
49 SELECTORS:
50 - [Mass, 11, -11, $(MCUT), E_CMS]
51 - NJetFinder:
52   N: $(NJETS)
53   PTMin: $(PTMIN)
54   R: 0.4
55   Exp: -1
56
```



Rambo & Multichannel Mappings

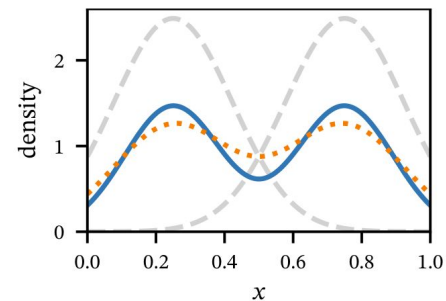
- task: generate four-momenta of incoming & outgoing particles from random numbers
- need to fulfill constraints like energy conservation & on shell conditions
- RAMBO mapping: [\[1308.2922\]](#)

$$d\Phi_n(P, p_1, \dots, p_n) = \prod_{i=1}^n \frac{d^3 p_i}{(2\pi)^3 2E_i} (2\pi)^4 \delta^4\left(P - \sum_{i=1}^n p_i\right) \quad d = 3n - 4$$

- Multichannel interface:

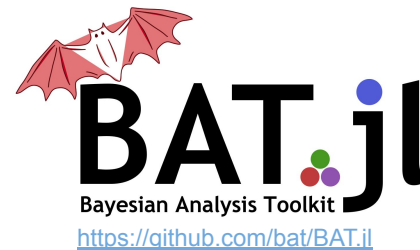
$$g(x) = \sum_i^{N_c} \alpha_i g_i(x), \quad \sum_i \alpha_i = 1$$

- use mixture distribution for multimodal targets
- construct channels based on physics knowledge
- automatic channel weight optimization



The Bayesian Analysis Toolkit - BAT.jl

- collection of state-of-the-art algorithms for Bayesian data analysis in Julia
- focusing on **efficiently sampling distributions** (particularly via MCMC)
- not relying on a specific modelling language / domain specific language
- provides modern sampling approaches & new algorithms



user-specified:

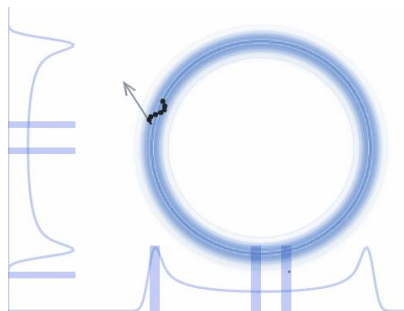
- target (likelihood & data)
- parameters & prior

provided by BAT.jl:

- sampling algorithms
 - MCMC sampling
 - Nested Sampling
- integration algorithms
- optimization algorithms

automated posterior exploration

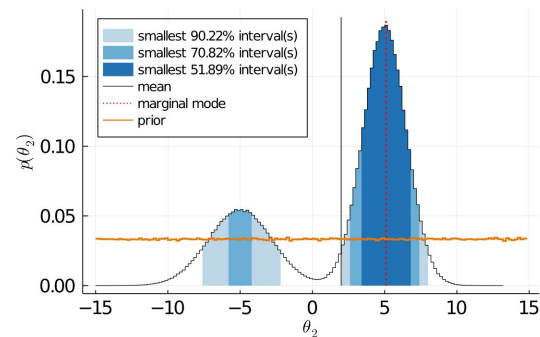
(tuning, parameter space transformations, parallelization, ...)



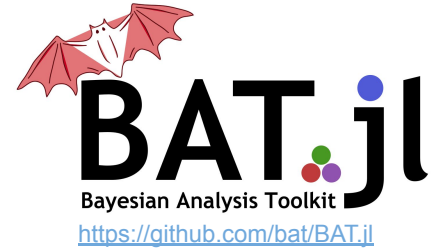
<https://github.com/chi-feng/mcmc-demo>

outputs

- samples
- plots
- modes, mean values, intervals



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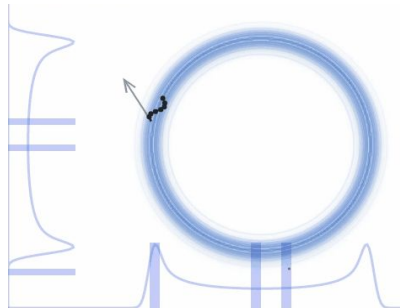
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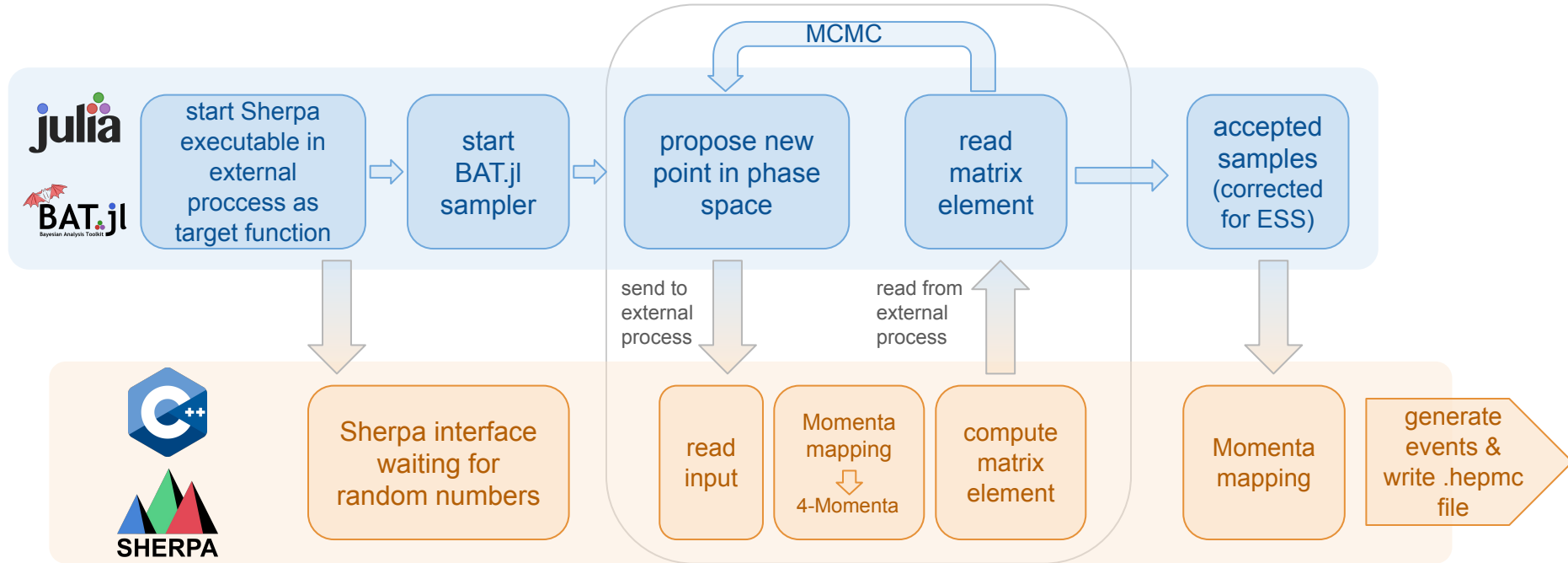
outputs

- samples



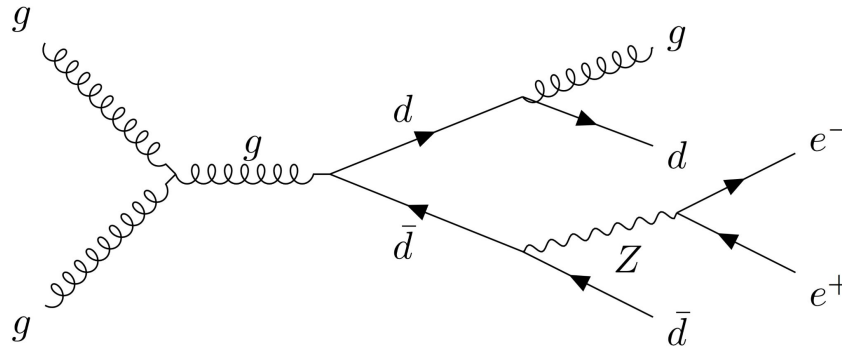
The BAT.jl - Sherpa Interface

Current interface: Run BAT.jl and call Sherpa as the target distribution



Example Process: Z + 3 Jets

Z+3jets : $g g \rightarrow d d e^+ e^- g$ @ 13GeV pp collisions



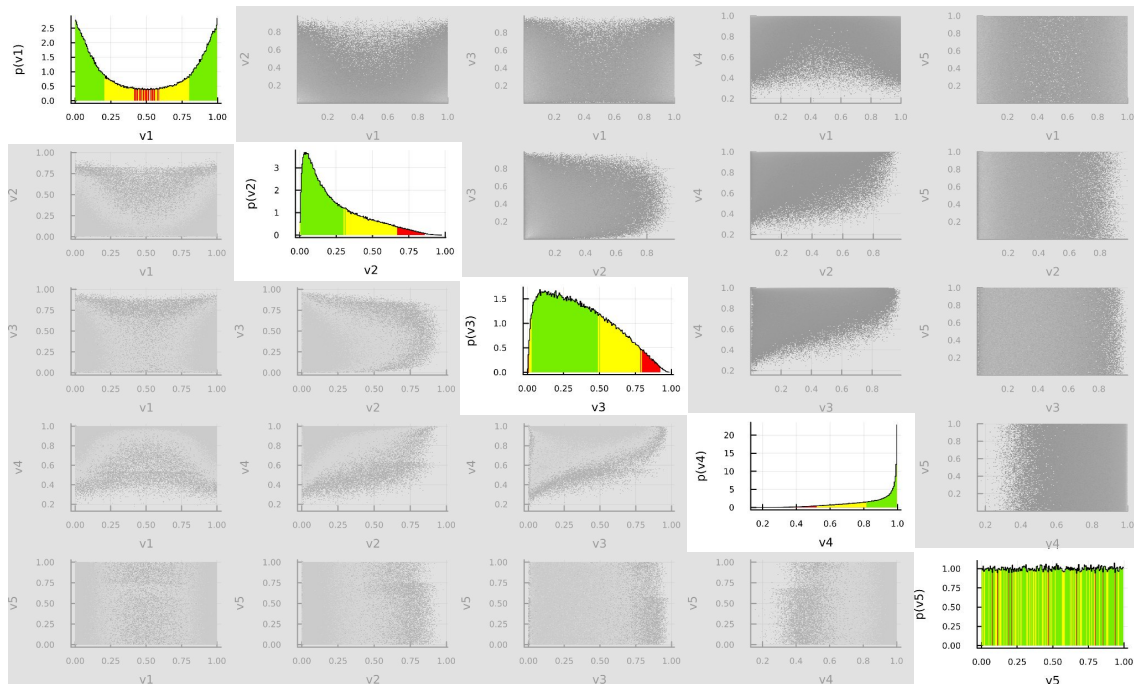
2 parameters for the **incoming** momenta fractions

11 parameters for the momenta of the **5 outgoing particles**

⇒ **13 dimensional sampling space**

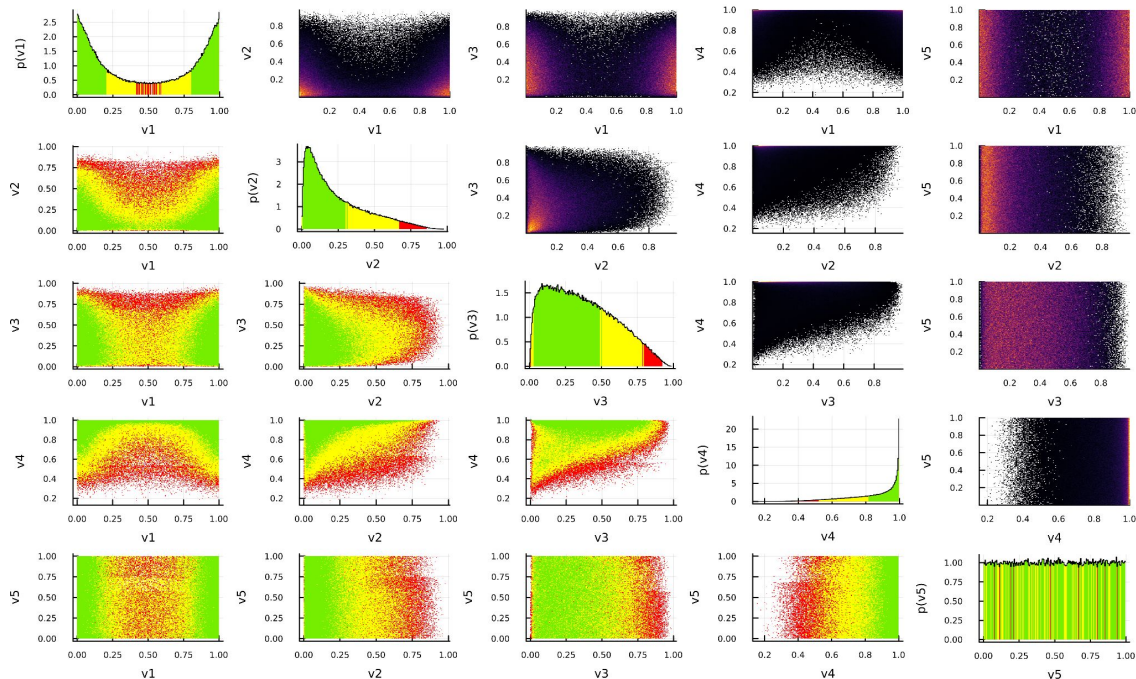
Phase space when sampling in a selected channel (1D)

- one dimensional marginalized distributions of samples
- shown first five parameters of phase space
- abstract parameter space
- wide variety of shapes

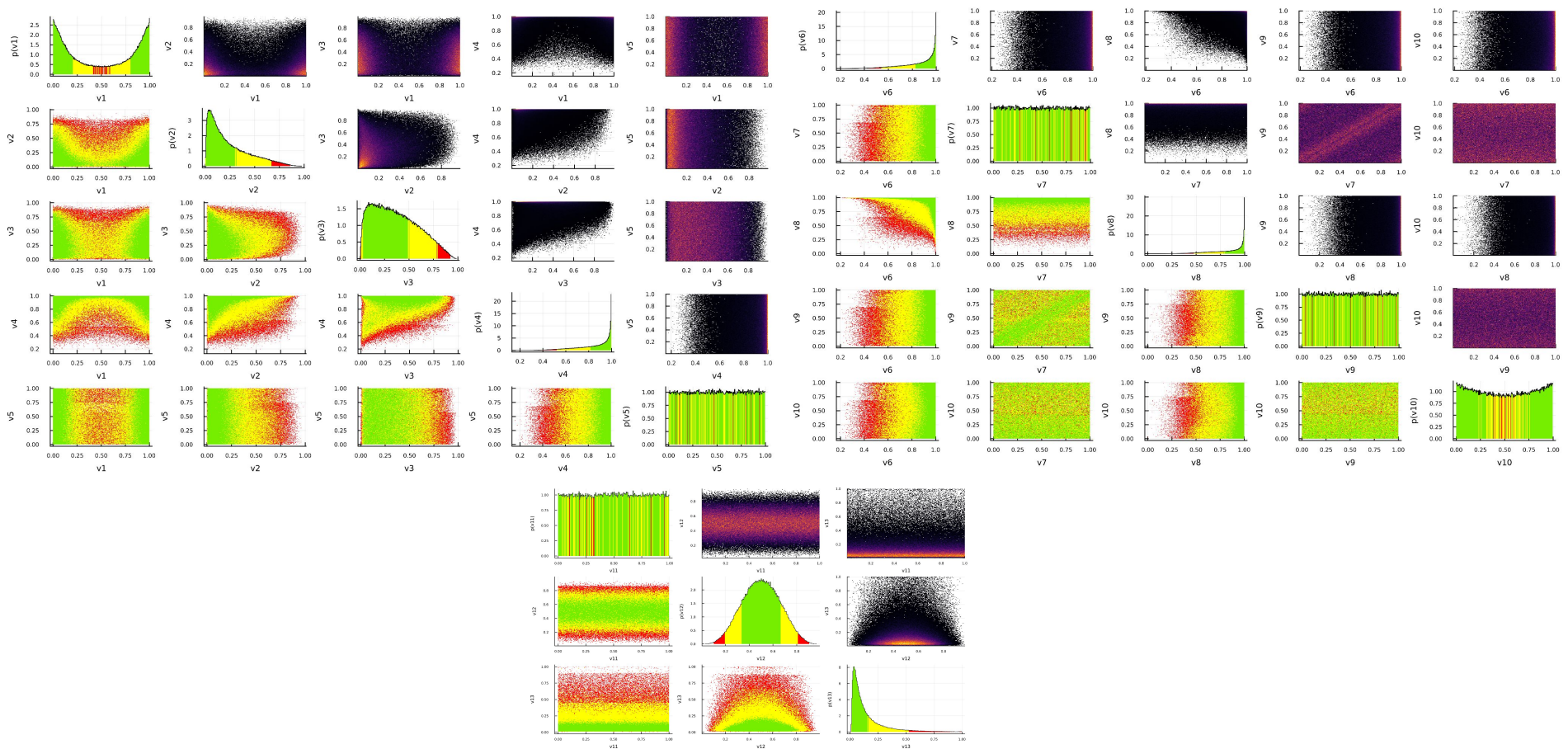


Phase space when sampling in a selected channel (2D)

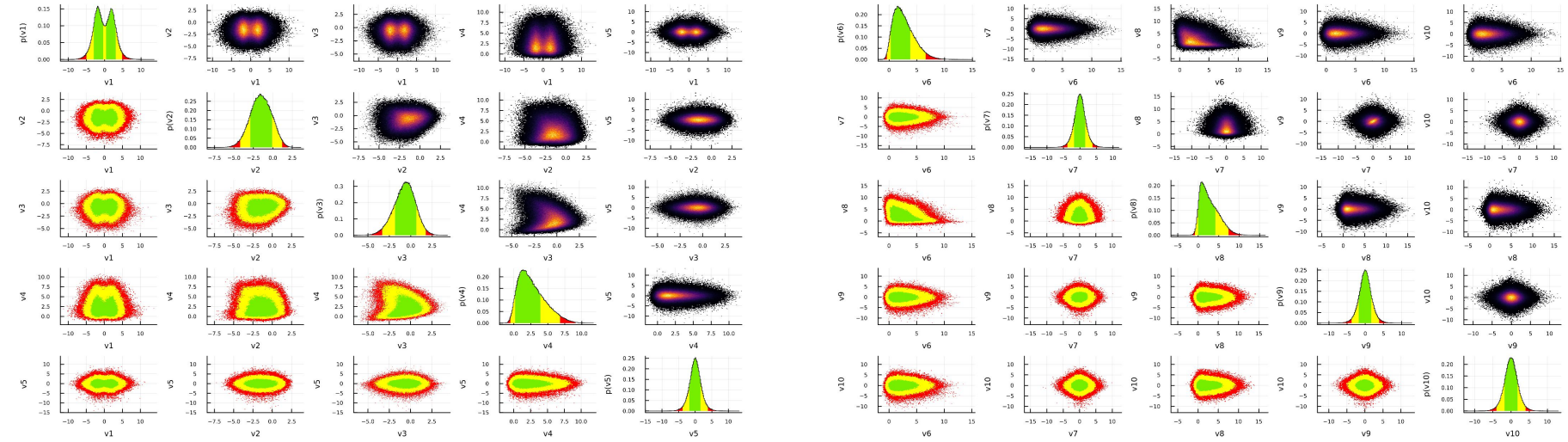
- one and two dimensional marginalized distributions of samples
- shown first five parameters of phase space
- abstract parameter space
- wide variety of shapes



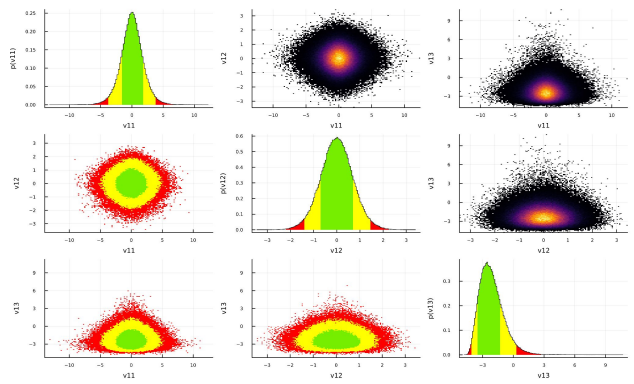
Full phase space when sampling in a selected channel



Transformed Phase Space



- more favorable sampling conditions using transformed phase space

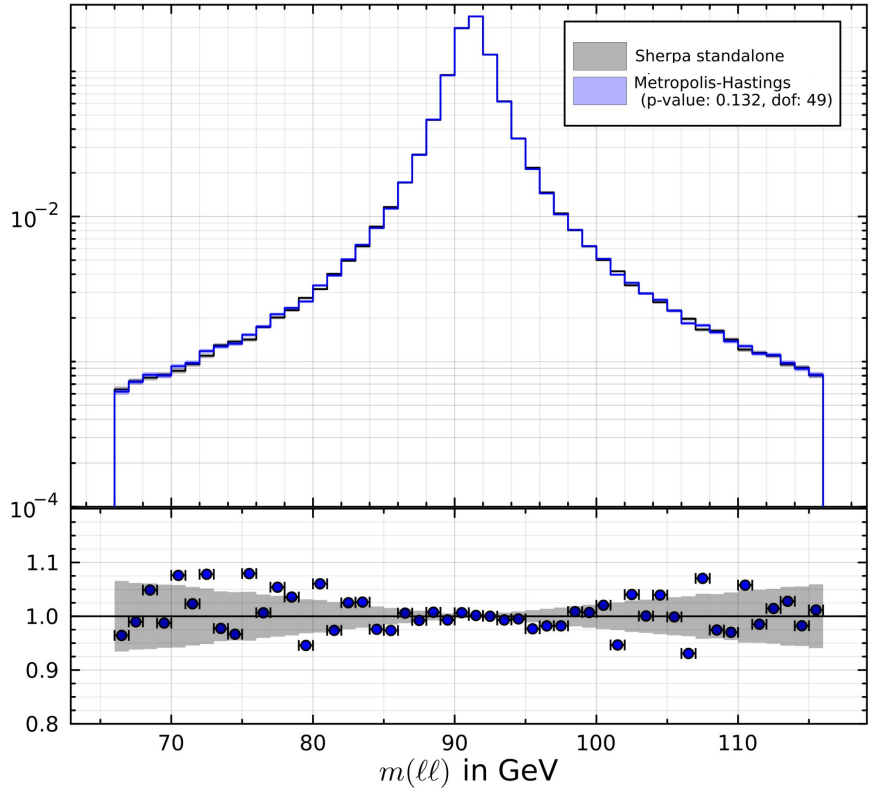


$$\text{logit}(p) = \log\left(\frac{p}{1-p}\right) \quad (0 < p < 1)$$

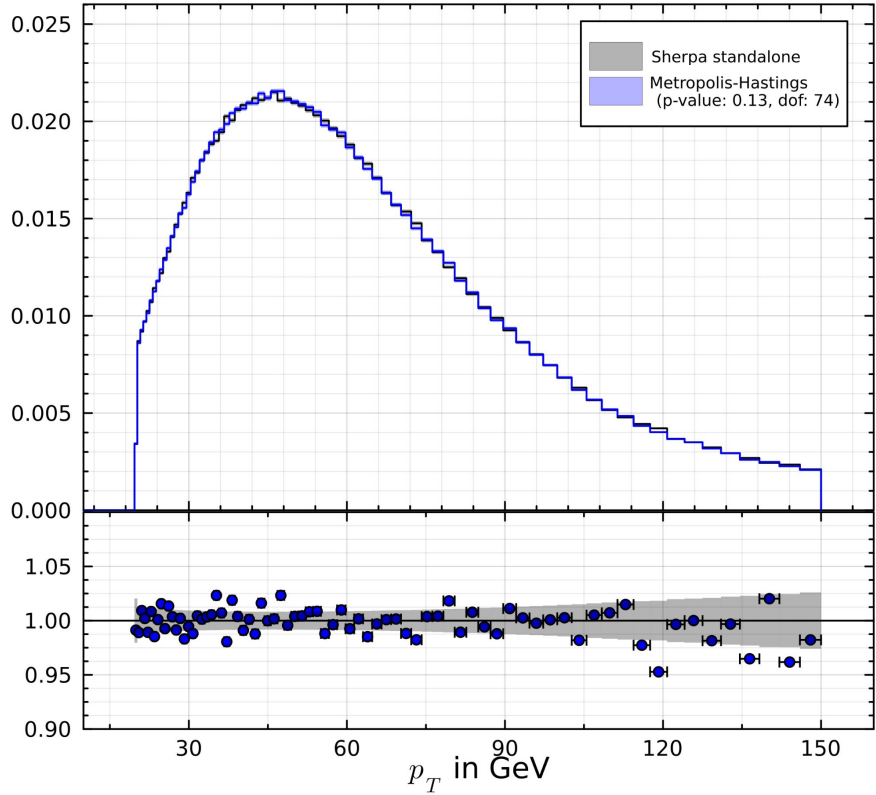
$$\text{logit}^{-1}(x) = \frac{1}{1 + e^{-x}}$$

Physical Observables

dilepton mass

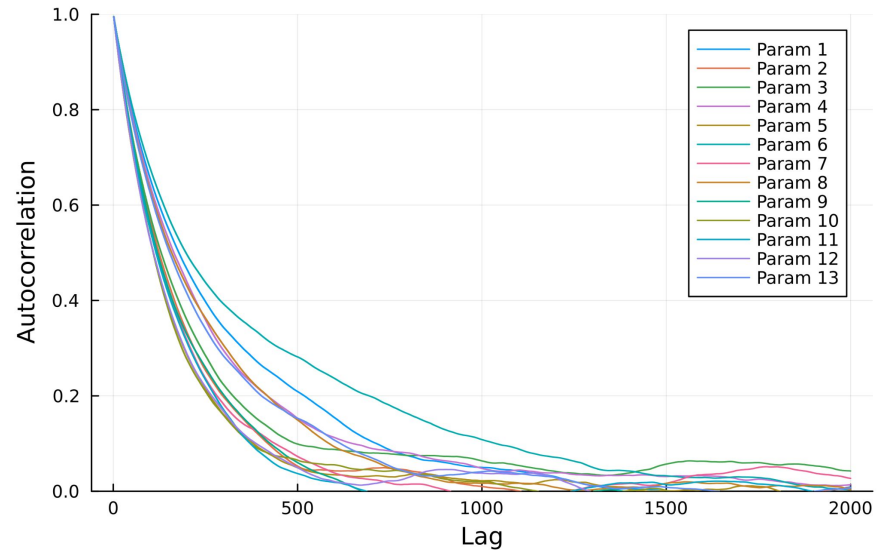
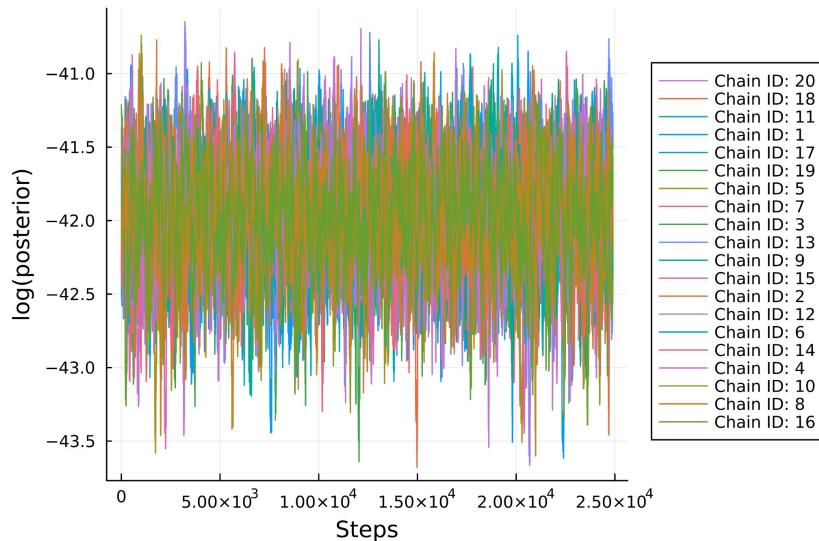


Lepton p_T



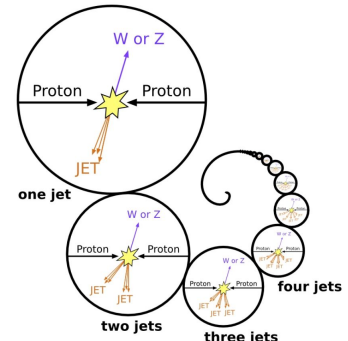
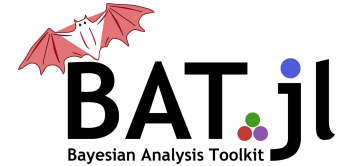
MCMC Diagnostics

- trace plots shows good chain mixing and no more visible burn-in
- events generated by MCMC methods are not independent
- autocorrelation plots allow to visualize this effect
- effective sample size (ESS) can be used to account for correlated samples



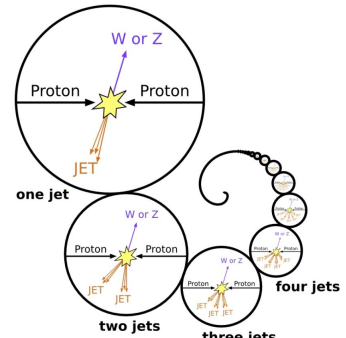
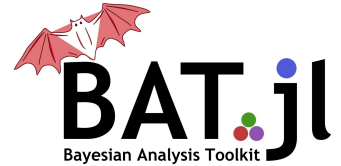
Summary & Outlook

- hard scattering process and matrix element calculation costly step in the simulation chain for (future) experiments
- improve efficiency using MCMC sampling techniques for event generation instead of importance sampling



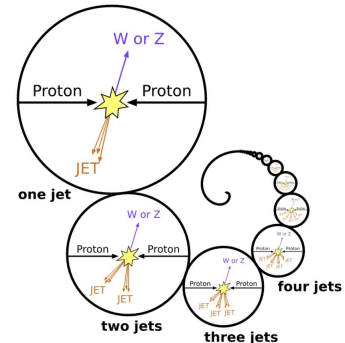
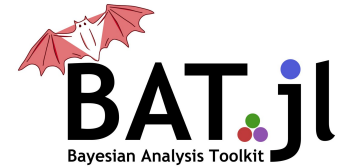
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- we developed a functioning interface between the BAT.jl tool and the Sherpa MC generator
- successful phase space sampling resulting in matching distributions
- possible to use different parametrizations of the phase space, e.g. Rambo mapping or the process-dependent multichannel mappings



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 - successful phase space sampling resulting in matching distributions
 - possible to use different parametrizations of the phase space, e.g. Rambo mapping or the process-dependent multichannel mappings
- need to overcome high autocorrelation to improve sampling efficiency
 - investigate more-complex processes: correcting for autocorrelation is expected to scale more preferably than unweighting efficiency in importance sampling



Thank you for your attention !