

# $D^0$ -mixing and CPV in charm

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FLAVOR PHYSICS AND CP VIOLATION  
KIBBUTZ MAALE HACHAMISHA, ISRAEL  
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## $D^0$ -mixing: **Calm before the storm**

- no new result since last year's FPCP
- but eagerly expecting final results (first observations?) from  $B$ -factories, updates from CDF and first results from LHCb

## Search for CPV in charm: **all thunder but no lightning**

- Many new results since last year
  - $A_{CP}$  in  $D^0 \rightarrow \pi^+\pi^-, K^+K^-$  from CDF
  - $A_{CP}$  difference between  $D^0 \rightarrow \pi^+\pi^-$  and  $D^0 \rightarrow K^+K^-$  from LHCb
  - $A_{CP}$  difference between  $D^+ \rightarrow \phi\pi^+$  and  $D_s^+ \rightarrow \phi\pi^+$  from Belle
- **See also M. Martinelli's talk on Thursday**

# Phenomenology

- flavor eigenstate  $\neq \mathcal{H}_{\text{eff}}$  eigenstate (with defined mass  $m_{1,2}$  and width  $\Gamma_{1,2}$ )

$$i \frac{\partial}{\partial t} \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix} = \mathcal{H}_{\text{eff}} \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix} \quad |D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle \quad (|p|^2 + |q|^2 = 1)$$

- time evolution of flavor eigenstate

$$|D^0(t)\rangle = \left[ |D^0\rangle \cosh\left(\frac{i\mathbf{x} + \mathbf{y}}{2} t\right) + \frac{q}{p} |\bar{D}^0\rangle \sinh\left(\frac{i\mathbf{x} + \mathbf{y}}{2} t\right) \right] \times e^{-\frac{1}{2}(1 + \frac{i\mathbf{m}}{\Gamma})t}$$

$$\text{Mixing parameters: } \mathbf{x} = \frac{m_1 - m_2}{\Gamma}, \quad \mathbf{y} = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}, \quad \Gamma = \frac{1}{2}(\Gamma_1 + \Gamma_2)$$

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- time evolution of flavor eigenstate

$$|D^0(t)\rangle = \left[ |D^0\rangle \cosh\left(\frac{ix+y}{2}t\right) + \frac{q}{p} |\bar{D}^0\rangle \sinh\left(\frac{ix+y}{2}t\right) \right] \times e^{-\frac{1}{2}(1+\frac{im}{\Gamma})t}$$

$$\text{Mixing parameters: } \mathbf{x} = \frac{m_1 - m_2}{\Gamma}, \quad \mathbf{y} = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}, \quad \Gamma = \frac{1}{2}(\Gamma_1 + \Gamma_2)$$

- Classification of CP-violating effects:**

$$\mathbf{A}_{\text{CP}} = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} = \mathbf{a}_f^d + \mathbf{a}_f^m + \mathbf{a}_f^i$$

- ①  $\mathbf{a}_f^d$ : CP violation in decay

$$\hookrightarrow \left| \frac{\mathcal{A}_f}{\bar{\mathcal{A}}_f} \right| \equiv 1 + \frac{A_D}{2} \quad (A_D \neq 0)$$

- ②  $\mathbf{a}_f^m$ : CP violation in mixing

$$\hookrightarrow \left| \frac{q}{p} \right| \equiv 1 + \frac{A_M}{2} \quad (A_M \neq 0)$$

- ③  $\mathbf{a}_f^i$ : CP violation in interference ( $f = \bar{f}$ )  $\rightarrow \phi = \arg\left(\frac{q}{p} \frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f}\right)$  ( $\phi \neq 0$ )

In SM both mixing ( $x \sim y \sim 1\%$ ) and CPV ( $\mathcal{O}(1)$ ) in charm system small.

# Available Charm Samples

## B-factories:

- continuum production @  $\Upsilon(4S)$ :  
 $\sigma(c\bar{c}) \approx 1.3 \text{ nb}$
- Belle:  $\sim 1.3 \cdot 10^9$   $c\bar{c}$  pairs
- Babar:  $\sim 0.7 \cdot 10^9$   $c\bar{c}$  pairs

## Tevatron:

- $p\bar{p}$  @  $\sim 2 \text{ TeV}$
- CDF:  $\sim 70 \cdot 10^9$   $D^0$ 's

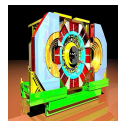
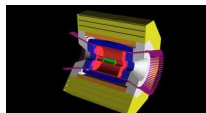
## Charm factories:

- $\psi(3770) \rightarrow D^0\bar{D}^0, D^+D^-$
- CLEO:  $\sim 2.8 \cdot 10^6$   $D^0\bar{D}^0$  pairs
- BESIII:  $\sim 12 \cdot 10^6$   $D^0\bar{D}^0$  pairs

## LHC:

- pp @ 7 TeV
- LHCb: first results

Diverse exp. conditions!



$D^0$ -mixing  
and  
 $t$ -dependent CPV measurements

# Mixing measurements

Decay time distribution sensitive to mixing parameters  $x$  and  $y$  and depends on the final state:

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto \left| \langle f | D^0 \rangle + \frac{q}{p} \left( \frac{ix+y}{2} \langle f | \bar{D}^0 \rangle \right) \right|^2$$

Final state	Belle	BaBar	CDF	Cleo	E791	Focus
$K^+ \pi^-$	✓	★	★	✓	✓	✓
$KK, \pi\pi$	★	★		✓	✓	✓
$K_S^0 \pi\pi$	✓	✓		✓		
$K_S^0 KK$	✓	✓				
$K^+ \pi^- \pi^0$		★				
$K^+ \pi^- \pi^- \pi^+$		✓				
$K^+ \ell^- \nu_\ell$	✓	✓		✓	✓	
quantum corr. in $\psi(3770) \rightarrow D^0 \bar{D}^0$				✓		

✓ – measurement performed; ★ – evidence for mixing

Full list of all  $D^0 - \bar{D}^0$  mixing measurements is available at:  
<http://www.slac.stanford.edu/xorg/hfag/charm/index.html>

# Time dependent Dalitz analyses: $D^0 \rightarrow P^0 h^+ h^-$

- Many quasi 2-body intermediate states, e.g. in

$D^0 \rightarrow K_S^0 \pi^+ \pi^-$  decays:

↪ CF:  $D^0 \rightarrow K^{*-} \pi^+$

↪ DCS:  $D^0 \rightarrow K^{*+} \pi^-$

↪ CP:  $D^0 \rightarrow \rho^0 K_S^0$

$$D^0 : \mathcal{A}(m_-^2, m_+^2) = \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_-^2, m_+^2) + a_{nr} e^{i\phi_{nr}}$$

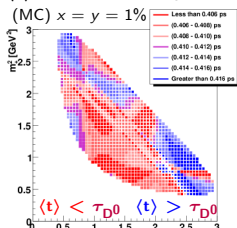
$$\bar{D}^0 : \bar{\mathcal{A}}(m_-^2, m_+^2) = \sum_r \bar{a}_r e^{i\bar{\phi}_r} \bar{\mathcal{A}}_r(m_-^2, m_+^2) + a_{nr} e^{i\phi_{nr}}$$

- Time dependent decay rate ( $\mathcal{A}_{1,2} = \frac{1}{2}(\mathcal{A} \pm \bar{\mathcal{A}})$ )

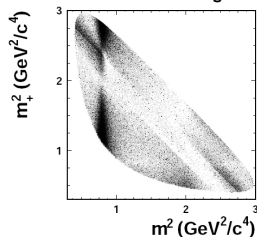
$$\Gamma(m_-^2, m_+^2, t) = e^{-\Gamma t} (|\mathcal{A}_1|^2 e^{-y\Gamma t} + |\mathcal{A}_2|^2 e^{y\Gamma t} + 2\mathcal{R}[\mathcal{A}_1 \mathcal{A}_2^*] \cos(x\Gamma t) + 2\mathcal{I}[\mathcal{A}_1 \mathcal{A}_2^*] \sin(x\Gamma t))$$

Simultaneous determination of  $x$  and  $y$ !

$\langle t \rangle$  across Dalitz plot



Dalitz plot for  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$



(Relative) Intrinsic sensitivities to mixing

Mode	$\mathcal{B} \cdot \epsilon$	$\sigma(x)$	$\sigma(y)$	
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	100	10	9	★ ★ ★
$D^0 \rightarrow K_S^0 K^+ K^-$	15	33	23	★ ★ ★
$D^0 \rightarrow \pi^0 \pi^+ \pi^-$	20	45	22	★

Taking into account  $\mathcal{B}$ 's and efficiencies (@ B-factories) but neglecting different purities

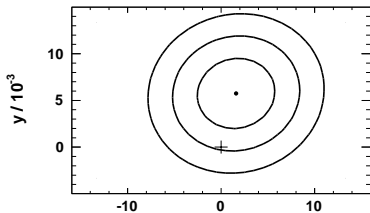


# Mixing and CPV $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ , $D^0 \rightarrow K_S^0 K^+ K^-$ decays

BaBar@469 fb<sup>-1</sup> [PRL105,081803]

$D^0 \rightarrow K_S^0 \pi^+ \pi^-$  and  $D^0 \rightarrow K_S^0 K^+ K^-$

68%, 95% and 99.9% confidence level contours



Conserved  $CP$  symmetry ( $|q/p| = 1$  &  $\phi = 0$ )

$$x = (0.16 \pm 0.23 \pm 0.14)\%$$

$$y = (0.57 \pm 0.20 \pm 0.15)\%$$

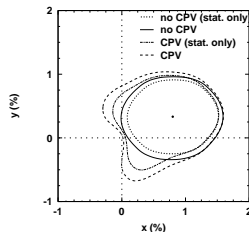
Most accurate determinations of  $x$  and  $y$ !

Expected statistical sensitivity using full Belle data sample  $\sigma(x) = 0.18$  and  $\sigma(y) = 0.15$

Belle@540 fb<sup>-1</sup> [PRL99,131803]

$D^0 \rightarrow K_S^0 \pi^+ \pi^-$

95% confidence level contours



Conserved  $CP$  symmetry ( $|q/p| = 1$  &  $\phi = 0$ )

$$x = (0.80 \pm 0.29^{+0.13}_{-0.16})\%$$

$$y = (0.33 \pm 0.24^{+0.10}_{-0.14})\%$$

CPV allowed ( $|q/p|$  &  $\phi$  free parameters of the fit)

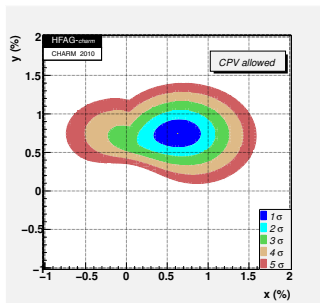
$$|q/p| = 0.86 \pm 0.30 \pm 0.09$$

$$\phi = -0.24 \pm 0.30 \pm 0.09$$

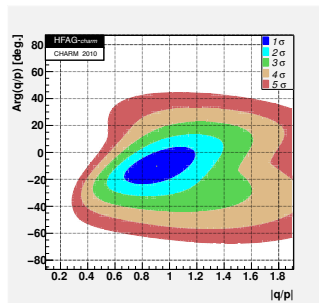
Consistent with no CPV!

# World average of mixing parameters

Heavy Flavor Averaging Group (HFAG) performs an average of 8 underlying physics parameters from currently 30 observables. [[www.slac.stanford.edu/xorg/hfag/](http://www.slac.stanford.edu/xorg/hfag/)]



$$x = (0.63 \pm 0.20)\%$$
$$y = (0.80 \pm 0.13)\%$$



$$|q/p| = 0.91^{+0.18}_{-0.16}$$
$$\phi(^{\circ}) = -10.0^{+9.4}_{-8.9}$$

No mixing point  $(x, y) = (0, 0)$  is excluded at  $10.2\sigma$ , while no  $CP$  violation point  $(|q/p|, \phi) = (1, 0)$  is consistent within  $1\sigma$ .

# $t$ -integrated CPV measurements

*Reminder: looking for signals at  $\sim 0.1\%$*

# Time-integrated searches of $CP$ Violation

Key is to distinguish possible  $CPV$  asymmetry from detector effects and production asymmetry in reconstructed asymmetry

$$A^{\text{reco}} = \frac{N_D^{\text{reco}} - N_{\bar{D}}^{\text{reco}}}{N_D^{\text{reco}} + N_{\bar{D}}^{\text{reco}}}$$

$$N_D^{\text{reco}} = N_D^{\text{prod}} \cdot \mathcal{B}(D \rightarrow f) \cdot \varepsilon_f \implies \text{if } A_i \ll 1 \implies A^{\text{reco}} = A_P^D + A_{CP}^f + A_\varepsilon^f$$

$A_{CP}$   
CP asymmetry

independent of any kinematic variable

LHCb:

$pp \neq CP$  symmetric



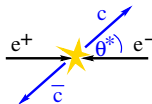
Production asymmetry

CDF:

No production asymmetry ( $p\bar{p}$ )

$A_P$   
Production asymmetry

due to  $\gamma/Z$  interference in  $e^+e^- \rightarrow c\bar{c}$



(anti-symmetric in  $\cos\theta_D^*$ )

$A_\varepsilon^f$   
Reconstruction asymmetry

$h^\pm$  reconstruction efficiency asymmetry



( $p^{\text{lab}}, \cos\theta^{\text{lab}}$ )

In order to control systematics  $A_i$ 's are estimated on real data sample!

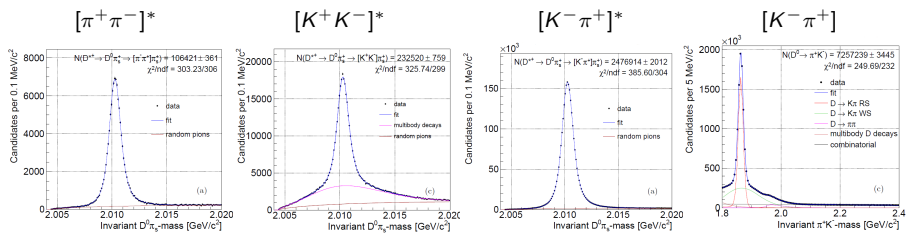
# $A_{CP}$ in $D^0 \rightarrow K^+K^-$ and $D^0 \rightarrow \pi^+\pi^-$ at CDF ( $5.94 \text{ fb}^{-1}$ )

Use three different samples to correct for detector asymmetry and minimize systematics:

- 1  $D^{*+} \rightarrow D^0 \pi_s^+ \rightarrow [h^+ h^-] \pi_s^+ \Rightarrow A^{\text{reco}}(hh)^* = A_{CP}(hh) + A_\epsilon(\pi_s)$
- 2  $D^{*+} \rightarrow D^0 \pi_s^+ \rightarrow [K^- \pi^+] \pi_s^+ \Rightarrow A^{\text{reco}}(K\pi)^* = A_{CP}(K\pi) + A_\epsilon(\pi_s) + A_\epsilon(K\pi)$
- 3  $D^0 \rightarrow [K^- \pi^+] \Rightarrow A^{\text{reco}}(K\pi) = A_{CP}(K\pi) + A_\epsilon(K\pi)$

$$A_{CP}(hh)^* = A^{\text{reco}}(hh)^* - A^{\text{reco}}(K\pi)^* + A^{\text{reco}}(K\pi)$$

Assuming  $A_P = 0$ ,  $\epsilon(D^*) = \epsilon(D^0) \cdot \epsilon(\pi_s)$ , and kinematic distributions equal across samples



# $A_{CP}$ in $D^0 \rightarrow K^+K^-$ and $D^0 \rightarrow \pi^+\pi^-$ at CDF (5.94 fb<sup>-1</sup>)

Preliminary results [CDF-NOTE-10296]:

- ①  $A^{\text{reco}}(\pi^+\pi^-)^* = (-1.86 \pm 0.23)\%$
- ②  $A^{\text{reco}}(K^+K^-)^* = (-2.32 \pm 0.21)\%$
- ③  $A^{\text{reco}}(K^-\pi^+)^* = (-2.91 \pm 0.05)\%$
- ④  $A^{\text{reco}}(K^-\pi^+) = (-0.83 \pm 0.03)\%$

Most precise measurements up to date

$$A_{CP}(\pi\pi)^* = (+0.22 \pm 0.24 \pm 0.11)\%$$

$$A_{CP}(KK)^* = (-0.24 \pm 0.22 \pm 0.10)\%$$

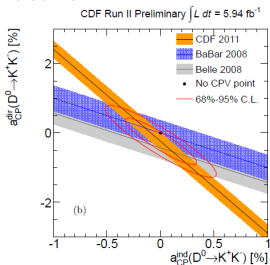
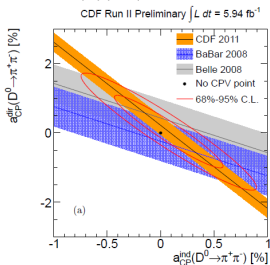
Systematics: largest contributions from charge dependent differences in mass shape and possible contamination of  $CPV$

from  $B \rightarrow DX$  decays

$$\text{NB: } A_{CP} = a_{CP}^{\text{dir}} + \frac{\langle t \rangle}{\tau} a_{CP}^{\text{ind}}$$

Complementary to B-factories

$$\langle t \rangle / \tau |_{\text{CDF}} > 1 \text{ vs. } \langle t \rangle / \tau |_{\text{B-fact.}} = 1$$



Averages:

- Assuming  $a_{CP}^{\text{ind}} = 0$

$$a_{CP}^{\text{dir}}(\pi\pi) = (0.19 \pm 0.22)\%$$

$$a_{CP}^{\text{dir}}(KK) = (-0.24 \pm 0.17)\%$$

- Assuming  $a_{CP}^{\text{dir}}(hh) = 0$

$$a_{CP}^{\text{ind}} = (-0.01 \pm 0.08)\%$$

Possible to include it in the global HFAG fit.

# $A_{CP}(KK) - A_{CP}(\pi\pi)$ at LHCb ( $37 \text{ pb}^{-1}$ ; preliminary)

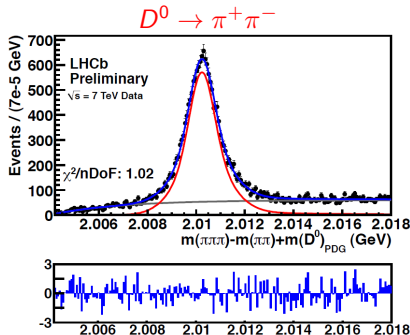
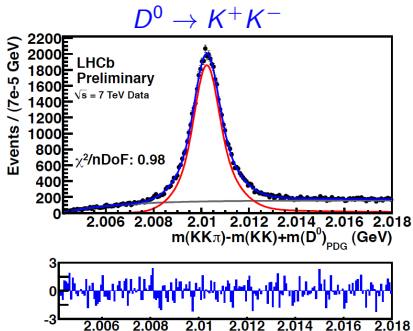
Search for direct CPV in SCS  $D^0 \rightarrow K^+K^-$  and  $D^0 \rightarrow \pi^+\pi^-$  produced in  $D^{*+} \rightarrow D^0\pi_s^+$  decays

$$A^{\text{reco}}(KK)^* = A_{CP}(KK)^* + A_\varepsilon(\pi_s) + A_P(D^*) \quad A^{\text{reco}}(\pi\pi)^* = A_{CP}(\pi\pi)^* + A_\varepsilon(\pi_s) + A_P(D^*)$$

↓

$$A_{CP}(KK)^* - A_{CP}(\pi\pi)^* = A^{\text{reco}}(KK)^* - A^{\text{reco}}(\pi\pi)^*$$

$$\text{NB: } A_{CP} = a_{CP}^{\text{dir}} + \frac{\langle t \rangle}{\tau} a_{CP}^{\text{ind}}$$



Signal extracted in bins of  $p_T$  (3),  $\eta$  (4), split magnet polarity (2) and trigger conditions (2)

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$$A^{\text{reco}}(KK)^* = A_{CP}(KK)^* + A_\varepsilon(\pi_S) + A_P(D^*) \quad A^{\text{reco}}(\pi\pi)^* = A_{CP}(\pi\pi)^* + A_\varepsilon(\pi_S) + A_P(D^*)$$

↓

$$A_{CP}(KK)^* - A_{CP}(\pi\pi)^* = A^{\text{reco}}(KK)^* - A^{\text{reco}}(\pi\pi)^*$$

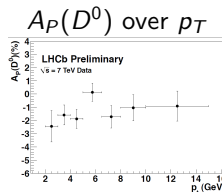
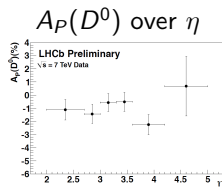
$$\Delta A_{CP} = (-0.28 \pm 0.70 \pm 0.25)\%$$

Systematics:

- $D^0$  mass window: 0.20%
- Best cand. sel.: 0.13%
- Fit model: 0.06%
- Binning: 0.01%

Using external measurements of  $A_{CP}(hh)$  production asymmetry can be determined

$$A_P(D^0) = (-1.08 \pm 0.32 \pm 0.12)\%$$





# $A_{CP}(D^+ \rightarrow \phi\pi^+) - A_{CP}(D_s^+ \rightarrow \phi\pi^+)$ at Belle [955 fb<sup>-1</sup>]

Measuring difference of  $A_{CP}$  in SCS  $D^+ \rightarrow \phi\pi^+$  and CF  $D_s^+ \rightarrow \phi\pi^+$  decays in bins of  $\cos\theta^*$ ,  $p_\pi$  and  $\cos(\theta_\pi)$ :

$$D_{(s)}: A^{\text{rec}} = A_{CP} + A_P(\cos\theta^*) + A_\epsilon^{KK} + A_\epsilon^\pi(p_\pi, \cos\theta_\pi)$$

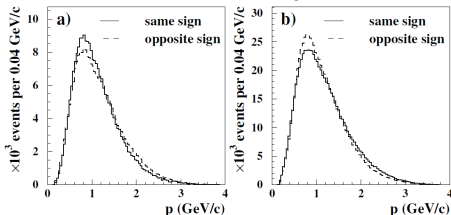
$$\Downarrow$$

$$D - D_s: \Delta A^{\text{rec}} = \Delta A_{CP} + \Delta A_P(\cos\theta^*) + \Delta A_\epsilon^{KK}$$

$$A_\epsilon^{KK} \neq 0!$$

$D^\pm$

$D_s^\pm$



Due to interference of  $\phi$  with  $K\pi$  S-wave ( $f_0(980)$ ) in case of D ( $D_s$ )

Effect in opposite directions  $\Rightarrow \Delta A_\epsilon^{KK} \neq 0!$

Determining  $A_\epsilon^{KK}$ :

$$A_\epsilon^{KK} = \int [P_{K^+}(x) - P_{K^-}(x)] A_\epsilon^K(x) dx$$

$P_K(x)$  - kaon phase space distr. in lab frame  $x = (p, \cos\theta)$

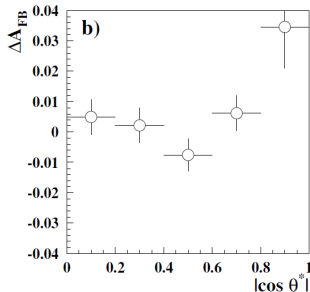
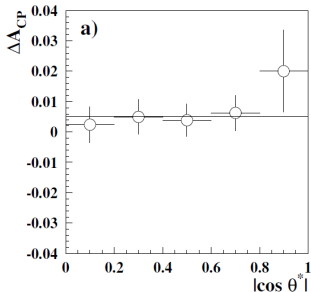
$A_\epsilon^K(x)$  measured using  $D_s \rightarrow \phi\pi$  and  $D^0 \rightarrow K\pi$

$$\Delta A_\epsilon^{KK} = (+0.111 \pm 0.025)\%$$

# $A_{CP}(D^+ \rightarrow \phi\pi^+) - A_{CP}(D_s^+ \rightarrow \phi\pi^+)$ at Belle [955 fb<sup>-1</sup>]

to be submitted soon to PRL

$$\Delta A_{CP} = \frac{\Delta A_{CORR}^{RECO}(\cos\theta^*) + \Delta A_{CORR}^{RECO}(-\cos\theta^*)}{2} \quad \Delta A_P = \frac{\Delta A_{CORR}^{RECO}(\cos\theta^*) - \Delta A_{CORR}^{RECO}(-\cos\theta^*)}{2}$$



Most precise measurements up to date

$$\Delta A_{CP} = (0.51 \pm 0.28 \pm 0.05)\%$$

$\Delta A_P$  consistent with 0 (C.L. 6%)

Results important for LHCb's measurement of flavor-specific asymmetry ( $a_{fs}$ ) using the subtraction method (see R. Lambert's talk at Beauty'11):

- need to take possible CPV in charm into account
- detector asymmetry, which does not cancel entirely when subtracting

# Conclusions

- Collective evidence for  $D^0 - \bar{D}^0$  mixing are compelling
  - No single measurement exceeds  $5\sigma$
  - The no-mixing point is excluded at around  $10\sigma$
  - The WA of  $x$  and  $y$  seem consistent with SM expectations
  - Providing strong constraints for some New Physics models
- No evidence of  $CP$  violation (at the level of 0.2%)
  - Large CPV ( $\mathcal{O}(1\%)$ ) already excluded in many modes from Belle, Babar and CDF
  - Possible signal of CPV at  $\mathcal{O}(0.1\%)$  will be exciting but not evidence of New physics

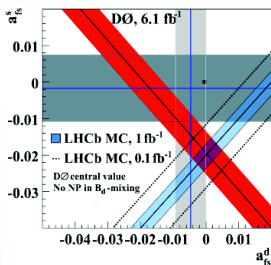
# Backup slides

# Flavor specific asymmetry at LHCb

taken from M. Calvi's talk on Monday

## $A_{sl}$

Di-muon charge asymmetry measured by D0, giving hints of anomalous CPV in the mixing of neutral B mesons.



$$\Delta A_{fs} = \frac{a_{fs}^s - a_{fs}^d}{2} \rightarrow (2.1 \pm 0.3) \times 10^{-4} [S.M.]$$

- > LHCb will measure  $a_{sl}^s - a_{sl}^d$  from difference in asymmetry in  $B_s \rightarrow D_s(KK\pi)\mu\nu$ ,  $B^0 \rightarrow D^+(KK\pi)\mu\nu$ .
- > Orthogonal constraint to D0.

If there is NP in  $B_s$  mixing it will be seen by LHCb also in the  $\phi_s$  measurement

M. Calvi - FPCP 2011

allowing for possible contribution of CPV in charm  $\rightarrow$

need external input to extract  $a_{fs}$  from  $b$

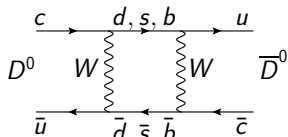
$$\Delta A_{fs} = \frac{1}{2}(a_{fs}^s - a_{fs}^d) - \frac{1}{2}(A_{CP}(Ds) - A_{CP}(D))$$

# Contributions to $x$ and $y$

## Standard Model

Burdman, Shipsey, Ann.Rev.Nucl.Part.Sci.53,431; Falk et al., PRD65, 054034; Bigi, Uraltsev, Nucl. Phys. B592, 92;

### Short distance



Effective CKM and GIM suppression

$$|x|, |y| \leq 10^{-3}$$

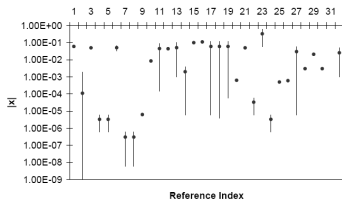
### Long distance



Contribution from hadronic intermediate states

$$x, y \sim \text{up to } 1\%$$

## New Physics predictions for $|x|$



A. Petrov, Int.J.Mod.Phys.A21, 5686;

A. Zupanc (KIT)

- Large uncertainty in SM mixing rate  
 $\hookrightarrow$  difficult to identify New Physics contributions
- however, measurements of  $x$  and  $y$  still provide useful constraints on many New Physics models
- See also A. Kagan's talk later today

# Mixing probability

- probability to observe an initial  $M^0$  as  $M^0$  or  $\bar{M}^0$  after time  $t$

$$\mathcal{P}_{\text{non-mix}}(t) = |\langle M^0(t) | M^0 \rangle|^2 = \frac{1}{2} e^{-\Gamma t} [\cosh(y\Gamma t) + \cos(x\Gamma t)]$$

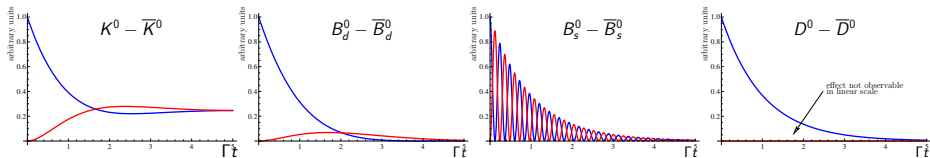
$$\mathcal{P}_{\text{mix}}(t) = |\langle M^0(t) | \bar{M}^0 \rangle|^2 = \frac{1}{2} e^{-\Gamma t} [\cosh(y\Gamma t) - \cos(x\Gamma t)]$$

- time integrated mixing rate

$$R_M = \frac{\int_0^\infty \mathcal{P}_{\text{mix}}(t) dt}{\int_0^\infty \mathcal{P}_{\text{non-mix}}(t) dt} = \frac{x^2 + y^2}{2 + x^2 - y^2}$$

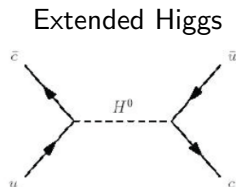
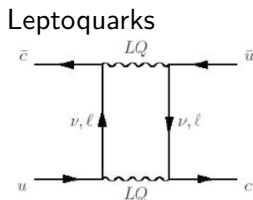
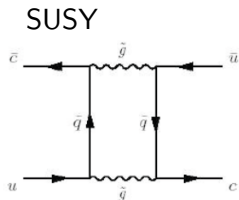
$M^0$	$x$	$y$	$R_M$
$K^0$	0.946	0.997	0.994
$B_d^0$	0.776	< 0.01	0.23
$B_s^0$	26.1	0.15	0.997
$D^0$	0.01	0.01	$10^{-4}$

1 out of  $10^4$   $D^0$  mesons oscillates before it decays



Large sample of  $D^0$  mesons needed to observe  $D^0 - \bar{D}^0$  mixing

# New Physics in Charm Mixing



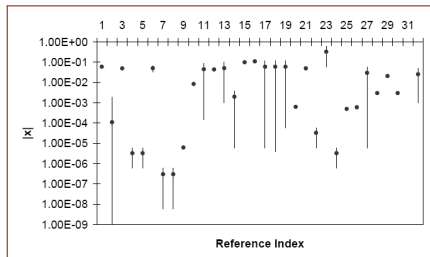
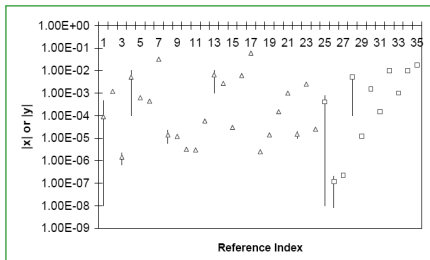
- Possible New Physics contributions can increase  $x$ , while  $y$  is mostly unaffected

$\hookrightarrow |x| \gg |y|$  would be a hint of New Physics



# Compilation of predictions for $x$ and $y$

Compilation of SM predictions for  $|x|$  ( $\triangle$ ) and  $|y|$  ( $\square$ )  
and New Physics predictions for  $|x|$  ( $\bullet$ )



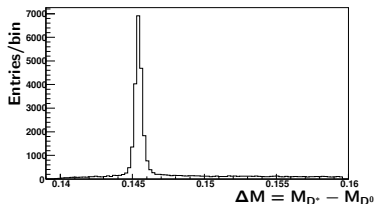
A. Petrov, Int.J.Mod.Phys.A21, 5686;

# Common steps in $D^0 - \bar{D}^0$ mixing and $CPV$ measurements

- 1 Tag the flavor of the produced neutral  $D$  meson
- 2 Measure proper decay time

## Flavor tagging

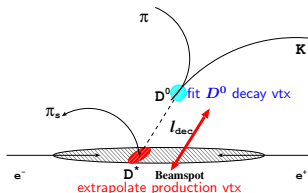
- require  $D^{*+} \rightarrow D^0 \pi^+$ 
  - ↪ flavor tagging with  $\pi$ 's charge
  - ↪ background suppression with  $\Delta M = M_{D^*} - M_{D^0}$



eliminate  $D^0$ s from  $b \rightarrow c$  with  $p_{\text{CMS}}^{D^*} > 2.5 \text{ GeV}/c^2$  (B-fact.) or use impact parameter (hadron col.)

## Proper decay time

- Vertexing with beam point constraint



$$t = \frac{l_{\text{dec}}}{c\beta\gamma}, \quad \beta\gamma = \frac{p_{D^0}}{M_{D^0}}$$

$\sigma_t$  uncertainty of the measurement typically between  $1/6\tau_{D^0}$  and  $1/2\tau_{D^0}$

# Mixing and CPV in $D^0 \rightarrow K^+K^-$ , $\pi^+\pi^-$ decays

- Measurement of lifetime difference between  $D^0 \rightarrow K^-\pi^+$  (*CP-mixed*) and  $D^0 \rightarrow K^+K^-$ ,  $\pi^+\pi^-$  (*CP-even*) decays (tagged and untagged samples)

$$\hookrightarrow \Gamma(D^0, \bar{D}^0 \rightarrow K^-, +\pi^+, -) \propto e^{-t/\tau_{D^0}}$$

$$\hookrightarrow \Gamma(D^0, \bar{D}^0 \rightarrow K^+K^-, \pi^+\pi^-) \propto e^{-(1+y_{CP})t/\tau_{D^0}}$$

$$y_{CP} \equiv \frac{\tau_{K^\mp, \pi^\pm}}{\tau_{K^+K^-, \pi^+\pi^-}} - 1 = \frac{1}{2} \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) y \cos \phi - \frac{1}{2} \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) x \sin \phi$$

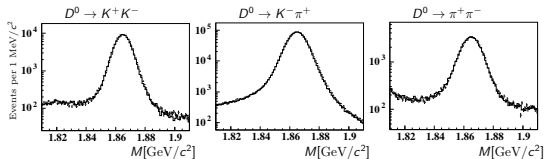
In limit of no CPV  $y_{CP} = y$

- In untagged sample contribution of wrong sign (DCS  $D^0 \rightarrow K^+\pi^-$ ) decays introduces negligible bias in  $y_{CP}$
- CP Violation  
 $\hookrightarrow \tau(D^0 \rightarrow f_{CP}) \neq \tau(\bar{D}^0 \rightarrow f_{CP})$

$$A_\Gamma = \frac{\tau(\bar{D}^0 \rightarrow f_{CP}) - \tau(D^0 \rightarrow f_{CP})}{\tau(\bar{D}^0 \rightarrow f_{CP}) + \tau(D^0 \rightarrow f_{CP})} = \frac{1}{2} \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) y \cos \phi - \frac{1}{2} \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) x \sin \phi$$

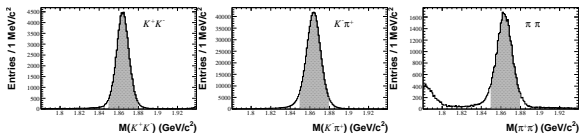
# Mixing and CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$ decays

- Belle tagged analysis ( $540 \text{ fb}^{-1}$ ): PRL98, 211803 (2007)



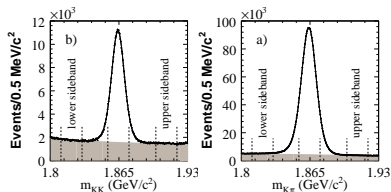
$D^0 \rightarrow$	Sig. yield	Purity
$K^-\pi^+$	1.22M	99%
$K^+K^-$	111k	98%
$\pi^+\pi^-$	49k	92%

- BaBar tagged analysis ( $384 \text{ fb}^{-1}$ ): PRD78, 011105 (2008)



$D^0 \rightarrow$	Sig. yield	Purity
$K^-\pi^+$	731k	99.9%
$K^+K^-$	70k	99.6%
$\pi^+\pi^-$	31k	98%

- BaBar untagged analysis ( $384 \text{ fb}^{-1}$ ): PRD80, 071103 (2009)



$D^0 \rightarrow$	Sig. yield	Purity
$K^-\pi^+$	2.71M	94.2%
$K^+K^-$	264k	80.9%

4× the size of the tagged sample and independent

# Mixing and CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$ decays (Belle)

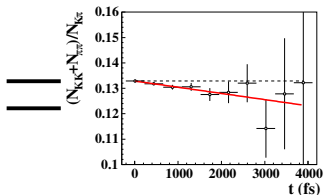
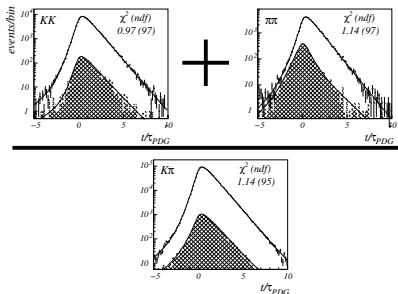
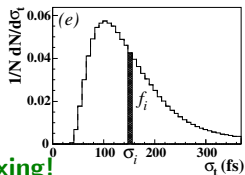
- Fit to the proper decay time distribution

$$\frac{dN}{dt} \propto \int e^{-t'/\tau} \cdot R(t-t') dt' + B(t)$$



$$R(t-t') = \sum_i^N f_i \sum_{k=1}^3 w_k G(t-t', \sigma_{ik}, t_0)$$

First evidence for  $D^0 - \bar{D}^0$  mixing!



$$y_{CP} = (1.31 \pm 0.32 \pm 0.25)\%$$

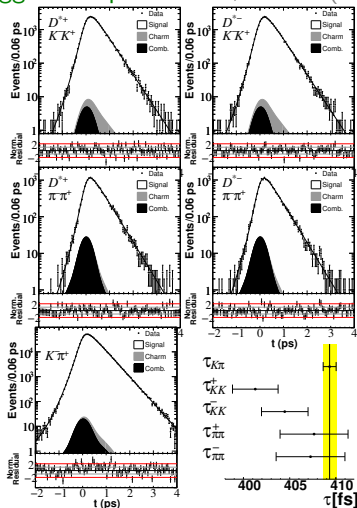
$$A_{\Gamma} = (0.01 \pm 0.30 \pm 0.15)\%$$

PRL98, 211803 (2007)

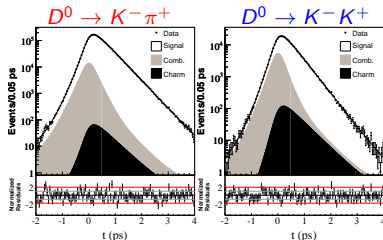
No evidence for CPV.

# Mixing and CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$ decays (BaBar)

Tagged Sample PRD78, 011105 (2008)



Untagged Sample PRD80, 071103 (2009)



$$\tau_{K\pi} = 410.39 \pm 0.38(\text{stat.}) \text{ fs}$$

$$\tau_{KK} = 405.85 \pm 1.00(\text{stat.}) \text{ fs}$$

$$y_{CP} = (1.12 \pm 0.26 \pm 0.22)\%$$

**Combined: tagged + untagged**

$$y_{CP} = (1.16 \pm 0.22 \pm 0.18)\%$$

4.1 $\sigma$  significance!

$$y_{CP} = (1.24 \pm 0.39 \pm 0.13)\%$$

$$\Delta Y = -(0.26 \pm 0.36 \pm 0.08)\%$$

$$\Delta Y = (1 + y_{CP})A_{\Gamma}$$

# Mixing and CPV in WS hadronic decays ( $D^0 \rightarrow K^+ \pi^-$ )

- Right sign (RS) charge combination

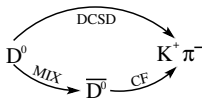
$$D^{*+} \rightarrow D^0(K^- \pi^+) \pi^+$$

$$\Gamma_{RS} \propto e^{-t/\tau_{D^0}}$$

- Wrong sign (WS) charge combination

$$D^{*+} \rightarrow D^0(K^+ \pi^-) \pi^+$$

↪ DCS or mixing



$$\Gamma_{WS} \propto [R_D + y' \sqrt{R_D} (\Gamma t) + \frac{x'^2 + y'^2}{4} (\Gamma t)^2] e^{-\Gamma t}$$

- DCS ● interference ● mixing

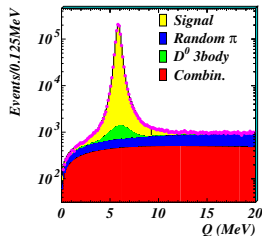
$$\hookrightarrow R_D = (0.331 \pm 0.008)\% \quad \text{DCS/CF rate}$$

$$\hookrightarrow \mathbf{x}' = \mathbf{x} \cos \delta + \mathbf{y} \sin \delta$$

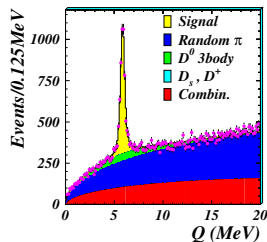
$$\hookrightarrow \mathbf{y}' = \mathbf{y} \cos \delta - \mathbf{x} \sin \delta$$

↪  $\delta$  strong phase between DCS and CF  
(Accessible at charm factory)

## RS events



## WS events

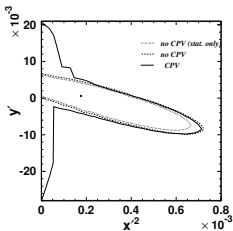
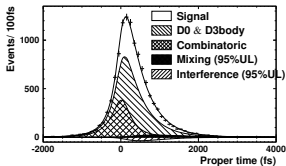


$$Q = M_{K\pi\pi} - M_{K\pi} - m_{\pi}$$

# Mixing and CPV in WS hadronic decays $D^0 \rightarrow K^+ \pi^-$

Belle [400 fb<sup>-1</sup>]

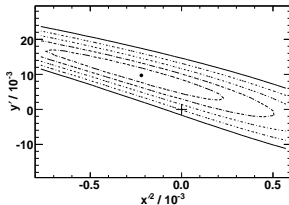
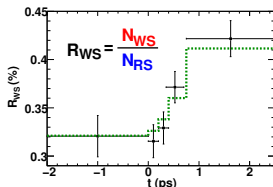
PRL96, 151801 (2006).



BaBar [384 fb<sup>-1</sup>]

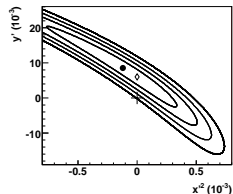
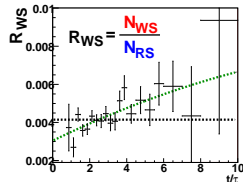
PRL98, 211802 (2007).

First Evidence!



CDF [1.5 fb<sup>-1</sup>]

PRL100, 121802 (2008).



Results assuming conservation of CP symmetry

Experiment	$R_D (10^{-3})$	$y' (10^{-3})$	$x^2 (10^{-3})$	Signif.
CDF	$3.04 \pm 0.55$	$8.5 \pm 7.6$	$-0.12 \pm 0.35$	3.8
BaBar	$3.03 \pm 0.19$	$9.7 \pm 5.4$	$-0.22 \pm 0.37$	3.9
Belle	$3.64 \pm 0.17$	$0.6^{+4.0}_{-3.9}$	$0.18^{+0.21}_{-0.23}$	2.0

No CPV found in DCS or mixing by Belle or Babar.



# Mixing in WS $D^0 \rightarrow K^+\pi^-\pi^0$ decays (BaBar)

PRL103, 211801 (2009) [(384 fb<sup>-1</sup>)]

Analysis similar to the WS  $D^0 \rightarrow K^+\pi^-$  analysis, however the strong phase  $\delta$  varies across the Dalitz plot.

● DCS ● interference ● mixing

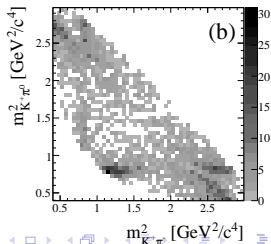
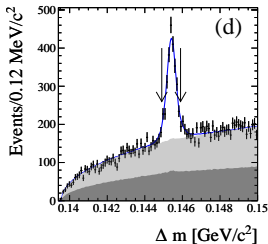
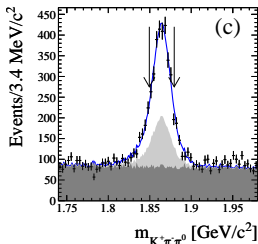
$$\frac{dN_{\bar{f}}(s_0, s_+, t)}{ds_0 ds_+ dt} = e^{-\Gamma t} \left\{ |A_{\bar{f}}|^2 + |A_{\bar{f}}| |\bar{A}_{\bar{f}}| [y'' \cos \delta_{\bar{f}} - x'' \sin \delta_{\bar{f}}] (\Gamma t) + \frac{x''^2 + y''^2}{4} |\bar{A}_{\bar{f}}|^2 (\Gamma t)^2 \right\}$$

$$s_0 = m_{K^+\pi^-}^2; s_+ = m_{K^+\pi^0}^2$$

## ● Mixing parameters

↪

$$x'' = x \cos \delta_{K\pi\pi^0} + y \sin \delta_{K\pi\pi^0} \quad \text{and} \quad y'' = y \cos \delta_{K\pi\pi^0} - x \sin \delta_{K\pi\pi^0}$$



# Mixing in WS $D^0 \rightarrow K^+\pi^-\pi^0$ decays (BaBar)

Assuming no CPV

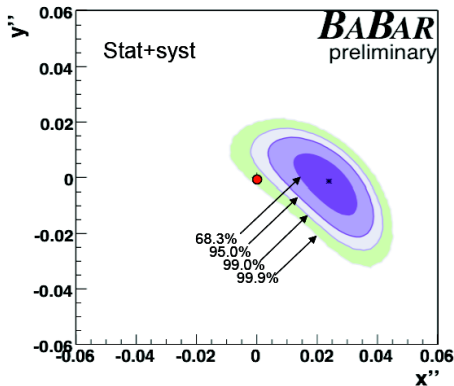
$$\begin{aligned} x'' &= (2.61_{-0.68}^{+0.57} \pm 0.39)\% \\ y'' &= -(0.05_{-0.64}^{+0.55} \pm 0.34)\% \\ R_M &= (2.9 \pm 1.6) \times 10^{-4} \end{aligned}$$

Allowing CPV

$$\begin{aligned} x''^+ &= (2.53_{-0.63}^{+0.54} \pm 0.39)\% \\ y''^+ &= -(0.05_{-0.67}^{+0.63} \pm 0.50)\% \end{aligned}$$

$$\begin{aligned} x''^- &= (3.55_{-0.83}^{+0.73} \pm 0.65)\% \\ y''^- &= -(0.54_{-1.16}^{+0.40} \pm 0.41)\% \end{aligned}$$

Results consistent with no CPV.



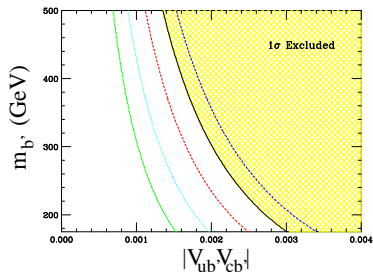
No mixing is excluded at 99% confidence level.

# Impact – Constraints on new physics models from mixing

E. Golowich *et al.*, PRD76,095009

- Constraints on new physics models from  $D^0 - \bar{D}^0$  complementary to those obtained in  $B$  and  $K$  sector  
     $\hookrightarrow$  FCNC transitions with *down-like* quarks in charm sector (unique feature)
- 21 NP models considered  $\rightarrow$  17 with useful constraints

Example: quark  $b'$  from 4<sup>th</sup> generation

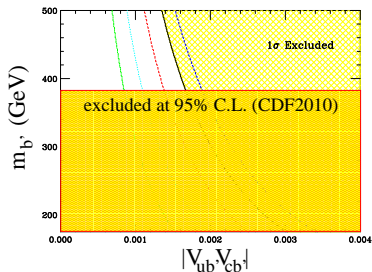


# Impact – Constraints on new physics models from mixing

E. Golowich *et al.*, PRD76,095009

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     $\hookrightarrow$  FCNC transitions with *down-like* quarks in charm sector (unique feature)
- 21 NP models considered  $\rightarrow$  17 with useful constraints

Example: quark  $b'$  from 4<sup>th</sup> generation



$|V_{ub'} V_{cb'}| < 0.002$   
order of magnitude stronger constraint  
as from CKM unitarity

Providing complementary and improved  
constraints!

# Mixing in $D^0 \rightarrow K_S^0 K^+ K^-$ decays (Belle)

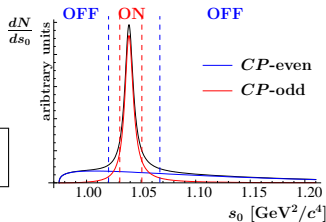
PRD80, 052006 (2009) [673 fb<sup>-1</sup>]

Measurement of lifetime difference between  $CP$ -even and  $CP$ -odd eigenstates

- $\sqrt{s_0} = m_{K^+ K^-}$  dependent  $CP$  mixture
  - ↪ **ON** region: mainly  $CP$ -odd ( $\phi(1020)K_S^0$ )
  - ↪ **OFF** region: mainly  $CP$ -even ( $a_0(980)^0 K_S^0$ )

$$\frac{d^2 N(s_0, t)}{ds_0 dt} \propto a_1(s_0) e^{-(1+y_{CP})t/\tau_{D^0}} + a_2(s_0) e^{-(1-y_{CP})t/\tau_{D^0}}$$

$$a_{1,2}(s_0) = \int |\mathcal{A}_{1,2}(s_0, s_+)|^2 ds_+; \sqrt{s_+} = m_{K_S^0 K^+}; \mathcal{A}_{1,2} = \frac{1}{2}(\mathcal{A} \pm \bar{\mathcal{A}})$$



- Effective lifetimes in **ON** and **OFF** regions

$$\tau_{\text{ON,OFF}} = [1 + (1 - 2f_{\text{ON,OFF}})y_{CP}] \tau_{D^0} \Rightarrow y_{CP} = \frac{1}{f_{\text{ON}} - f_{\text{OFF}}} \left( \frac{\tau_{\text{OFF}} - \tau_{\text{ON}}}{\tau_{\text{OFF}} + \tau_{\text{ON}}} \right)$$

↪  $f_{\text{ON}}, f_{\text{OFF}}$  are  $CP$ -even fractions in **ON** and **OFF** regions, determined using 8-resonant Dalitz model (REF!!!)

$$y_{CP} = +(0.11 \pm 0.61(\text{stat.}) \pm 0.52(\text{syst.}))\%$$

TABLE I: Results from the mixing fits. The first uncertainty is statistical, the second systematic and the third systematic from the amplitude model. For the nominal fit, the corresponding correlation coefficients between  $x$  and  $y$  are 3.5%, 16.0% and  $-2.7\%$ , respectively.

Fit type	$x/10^{-3}$	$y/10^{-3}$
Nominal	$1.6 \pm 2.3 \pm 1.2 \pm 0.8$	$5.7 \pm 2.0 \pm 1.3 \pm 0.7$
$K_S^0 \pi^+ \pi^-$	$2.6 \pm 2.4$	$6.0 \pm 2.1$
$K_S^0 K^+ K^-$	$-13.6 \pm 9.2$	$4.4 \pm 5.7$
$D^0$	$0.0 \pm 3.3$	$5.5 \pm 2.8$
$\bar{D}^0$	$3.3 \pm 3.3$	$5.9 \pm 2.8$

# Mixing in semileptonic decays $D^0 \rightarrow K^{(*)-} \ell^+ \nu_\ell$

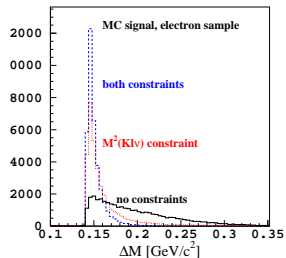
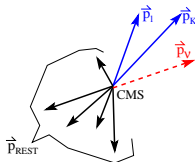
U. Bitenc *et al.* [Belle Collaboration], PRD77, 112003 (2008). [ $\mathcal{L} = 492 \text{ fb}^{-1}$ ]

- Wrong sign (WS) charge combination accessible only via mixing

	Flavor at production		Flavor at decay	
without mixing	$D^{*+} \rightarrow D^0 \pi^+$		$D^0 \rightarrow K^- \ell^+ \nu_\ell$	<b>RS</b>
with mixing	$D^{*+} \rightarrow D^0 \pi^+$	$D^0 - \bar{D}^0$	$\bar{D}^0 \rightarrow K^+ \ell^- \nu_\ell$	<b>WS</b>

Neutrino reconstruction:

- $P_\nu = P_{\text{CMS}} - P_{K\ell} - P_{\text{rest}}$
- $M_{K\ell\nu}^2 = m_{D^0}^2 \text{ \& } (P_\nu^*)^2 = 0$

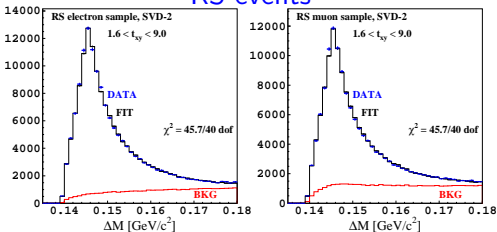


Time integrated mixing rate:

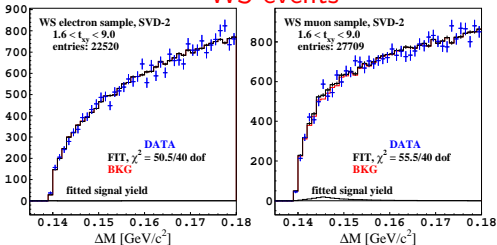
$$R_M \simeq \frac{x^2 + y^2}{2} = \frac{N_{\text{WS}}}{N_{\text{RS}}}$$

# Mixing in semileptonic decays $D^0 \rightarrow K^{(*)-} \ell^+ \nu_\ell$

## RS events



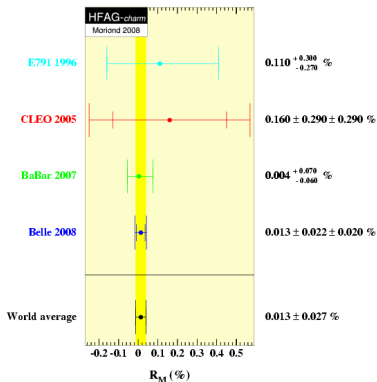
## WS events



No WS charge combinations  
 observed.

$$R_M = (1.3 \pm 2.2 \pm 2.0) \times 10^{-4}$$

$$R_M < 6.1 \times 10^{-4} @ 90\% \text{ C.L.}$$



<http://www.slac.stanford.edu/xorg/hfag/>



# Future Prospects

TABLE V: Expected precision ( $\sigma$ ) on the measured quantities using methods described in the text for SuperB with an integrated luminosity of  $75 \text{ ab}^{-1}$  at SuperB at 10 GeV,  $300 \text{ fb}^{-1}$  ( $\sim$  two months) running at charm threshold with SuperB, and LHCb with  $10 \text{ fb}^{-1}$ [13].

Mode	Observable	$\Upsilon(4S)$ ( $75 \text{ ab}^{-1}$ )	$\psi(3770)$ ( $300 \text{ fb}^{-1}$ )	LHCb ( $10 \text{ fb}^{-1}$ )
$D^0 \rightarrow K^+ \pi^-$	$x'^2$	$3 \times 10^{-5}$		$6 \times 10^{-5}$
	$y'$	$7 \times 10^{-4}$		$9 \times 10^{-4}$
$D^0 \rightarrow K^+ K^-$	$y_{CP}$	$5 \times 10^{-4}$		$5 \times 10^{-4}$
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	$x$	$4.9 \times 10^{-4}$		
	$y$	$3.5 \times 10^{-4}$		
	$ q/p $	$3 \times 10^{-2}$		
	$\phi$	$2^\circ$		
$\psi(3770) \rightarrow D^0 \bar{D}^0$	$x^2$		$(1-2) \times 10^{-5}$	
	$y$		$(1-2) \times 10^{-3}$	
	$\cos \delta$		$(0.01-0.02)$	

arXiv:0810.1312

Table 5.23: Expected number of reconstructed  $D^{*+} \rightarrow D^0\pi^+$ ,  $D^0 \rightarrow K^-\pi^+$  decays at different facilities (projected using [292], [293], [294], [295]). <sup>†</sup>For charm factory the expected yield of  $\Psi(3770) \rightarrow D^0\bar{D}^0$ ,  $D^0 \rightarrow K^-\pi^+$ ,  $\bar{D}^0 \rightarrow K^+\pi^-$  is quoted.

Facility	num. of $D^{*+} \rightarrow D^0\pi^+$ , $D^0 \rightarrow K^-\pi^+$	int. luminosity [ $\text{fb}^{-1}$ ]	Comment
existing B factories	$2.5 \times 10^6$	1000	final data set
Super-KEKB	$14 \times 10^6$	5000	purity $\sim 99\%$
Charm factory <sup>†</sup>	$4 \times 10^4$	20	both $D^0$ 's reconstructed; $D^0\bar{D}^0$ in coherent state
Tevatron	$0.5 \times 10^6$	0.35	
LHCb	$15 \times 10^6$	2	

<http://belle2.kek.jp/physics.html>

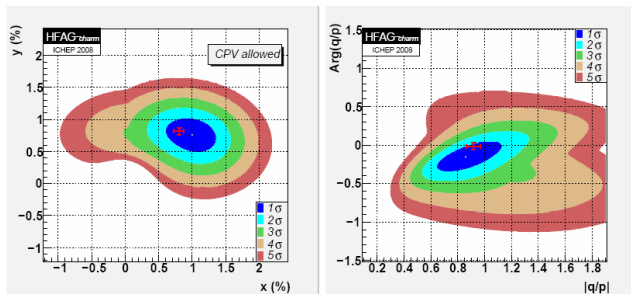


Figure 5.67: Left: The probability contours for the current world average values of the mixing parameters  $x$  and  $y$  [338]. The error bars denote the expected accuracy on the parameters with  $50 \text{ ab}^{-1}$  following from the extrapolation of results using  $K^+K^-$ ,  $\pi^+\pi^-$ ,  $K^+\pi^-$  and  $K_S\pi^+\pi^-$  final states. Right: The probability contours for the current world average values of the  $CPV$  parameters  $|q/p|$  and  $\phi$  [338]. The error bars denote the expected accuracy with the same assumptions as above.

<http://belle2.kek.jp/physics.html>

# Time-integrated searches of $CP$ Violation

- Searches for direct  $CP$  violation performed in total over 30  $D^0$ ,  $D^+$  and  $D_s^+$  decay modes in past 15 years
  - ↪ Belle, BaBar, Cleo, CDF, FOCUS, E796, E687
- No evidence for  $CP$  violation found so far
  - ↪ Sensitivity is in some cases reaching 0.2%
- Measurements statistical limited
  - ↪ All measurements can be significantly improved!

$D^0 \rightarrow$	$A_{CP}$ [%]	$D^+ \rightarrow$	$A_{CP}$ [%]	$D_s^+ \rightarrow$	$A_{CP}$ [%]
$K^+K^-$	$-0.16 \pm 0.23$	$K_S^0\pi^+$	$-0.72 \pm 0.26$	$K_S^0K^+$	$-0.28 \pm 0.41$
$\pi^+\pi^-$	$+0.22 \pm 0.37$	$K_S^0K^+$	$-0.09 \pm 0.63$	$K_S^0\pi^+$	$+6.5 \pm 2.5$
$\pi^+\pi^-\pi^0$	$-0.23 \pm 0.42$	$K^+K^-\pi^+$	$+0.39 \pm 0.61$	$K^+K^-\pi^+$	$+0.3 \pm 1.4$
$K^-\pi^+\pi^0$	$+0.16 \pm 0.89$	$K^-\pi^+\pi^+$	$-0.5 \pm 1.0$	$\pi^+\pi^-\pi^+$	$+2.0 \pm 4.7$
$K_S^0\pi^0$	$+0.10 \pm 1.3$	$K^-\pi^+\pi^+$	$-0.5 \pm 1.0$	$K^+\pi^-\pi^+$	$+11.2 \pm 7.1$
$K^+K^-\pi^0$	$+1.00 \pm 1.7$	$K_S^0\pi^+\pi^0$	$+0.3 \pm 0.9$	$\pi^+\eta$	$-8.2 \pm 5.3$
$\pi^0\pi^0$	$+0.10 \pm 4.8$	$\pi^+\pi^-\pi^+$	$-1.7 \pm 4.2$	$\pi^+\eta'$	$-5.5 \pm 3.9$
⋮	⋮	⋮	⋮	⋮	⋮

Full list of all  $A_{CP}$  measurements is available at:  
<http://www.slac.stanford.edu/xorg/hfag/charm/index.html>

# Search for $CP$ Violation with $T$ -odd correlations

Assuming  $CPT$  invariance:  $T$  violation  $\Rightarrow CP$  violation

- Possible only in  $\geq 4$ -body decay

$$\hookrightarrow D^0 \rightarrow K^- K^+ \pi^- \pi^+$$

- $T$ -odd quantity:

$$C_T \equiv \langle \vec{p}_{K^+} \cdot (\vec{p}_{\pi^+} \times \vec{p}_{\pi^-}) \rangle$$

- $T$  violating asymmetry  $A_T$

$$D^0: A_T = \frac{\Gamma(C_T > 0) - \Gamma(C_T < 0)}{\Gamma(C_T > 0) + \Gamma(C_T < 0)}$$

$$\bar{D}^0: \bar{A}_T = \frac{\Gamma(-\bar{C}_T > 0) - \Gamma(-\bar{C}_T < 0)}{\Gamma(-\bar{C}_T > 0) + \Gamma(-\bar{C}_T < 0)}$$

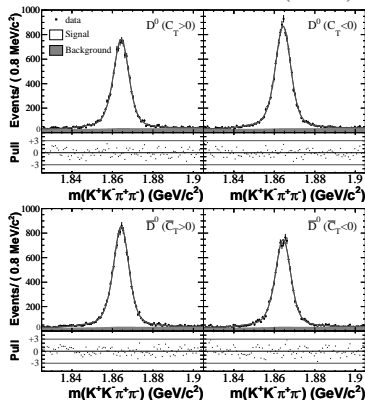
$$A_T = \frac{1}{2} (A_T - \bar{A}_T)$$

Bigi, hep-ph/0107102 (2001)

Bensalem et al., PRD66, 094004 (2002)

$A_T$  can be different from zero due to final state interactions, but  $A_T \neq 0$  represents  $CP$  violation.

BaBar PRD81, 111103 (2010)



$$A_T = (-68.5 \pm 7.3 \pm 4.5) \times 10^{-3}$$

$$\bar{A}_T = (-70.5 \pm 7.3 \pm 3.9) \times 10^{-3}$$

$$A_T = (1.0 \pm 5.1 \pm 4.4) \times 10^{-3}$$

Number of reconstructed decays:

$$N^{reco} = N_{D^{*+}}^{prod} \cdot \mathcal{B}(D^{*+} \rightarrow D^0 \pi^+) \cdot \mathcal{B}(D^0 \rightarrow h^+ h^-) \cdot \epsilon_{hh} \cdot \epsilon_{\pi}$$

- Contributions to asymmetry in  $N^{reco}$ :
  - production ( $A_{FB}$ )
  - branching fractions ( $A_{CP}$ )
  - efficiencies ( $A_{\epsilon}$ )
- If asymmetries are small ( $A_{FB}, A_{CP}, A_{\epsilon} \ll 1$ ) it is easy to see, that the asymmetry in  $N^{reco}$  is:

$$A^{reco} = A_{FB}^{D^{*+}} + A_{CP}^{D^0 \pi} + A_{CP}^{hh} + A_{\epsilon}^{hh} + A_{\epsilon}^{\pi}$$

- Some are zero:  $A_{CP}^{D^0 \pi} = 0$  (strong decay),  $A_{\epsilon}^{hh} = 0$  (same final state)

- Production asymmetry ( $A_{FB}$ ) is due to interference in  $e^+e^- \rightarrow c\bar{c}$  (mediated by virtual  $\gamma$  or  $Z^0$ )
  - anti-symmetric function of  $\cos\theta^*$  (follows from  $CP$  conservation)

$$A_{FB}(\cos\theta^*) = -A_{FB}(-\cos\theta^*)$$

- Measured asymmetry:

$$A^{reco} = A_{FB}^{D^{*+}}(\cos\theta^*) + A_{CP}^{hh} + A_{\epsilon}^{\pi}(\theta, p)$$

- Asymmetry in  $\pi_{slow}$  efficiency  $A_{\epsilon}^{\pi}(\theta, p)$  can be measured in  $D^0 \rightarrow K^-\pi^+$  by using tagged and untagged decays
- Corrected asymmetry

$$A_{corr}^{reco} = A^{reco} - A_{\epsilon}^{\pi}(\theta, p)$$

$$A_{corr}^{reco}(\cos\theta^*) = A_{FB}^{D^{*+}}(\cos\theta^*) + A_{CP}^{KK}$$

Number of reconstructed tagged and untagged  $D^0 \rightarrow K^- \pi^+$  decays:

$$N^{\text{untag}} = N_{D^0}^{\text{prod}} \cdot \mathcal{B}(D^0 \rightarrow K^- \pi^+) \cdot \epsilon_{K\pi}$$

$$N^{\text{tag}} = N_{D^{*+}}^{\text{prod}} \cdot \mathcal{B}(D^{*+} \rightarrow D^0 \pi_S^+) \cdot \mathcal{B}(D^0 \rightarrow K^- \pi^+) \cdot \epsilon_{K\pi} \cdot \epsilon_{\pi}$$

Measured asymmetry:

$$A^{\text{untag}} = A_{FB}^{D^0} + A_{CP}^{K\pi} + A_{\epsilon}^{K\pi}$$

$$A^{\text{tag}} = A_{FB}^{D^0} + A_{CP}^{K\pi} + A_{\epsilon}^{K\pi} + A_{\epsilon}^{\pi}$$

Assuming  $A_{FB}^{D^0} = A_{FB}^{D^{*+}}$ :

$$A_{\epsilon}^{\pi} = A^{\text{tag}} - A^{\text{untag}}$$

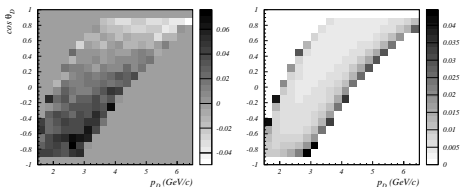
$A_{\epsilon}^{K\pi}$  and  $A_{\epsilon}^{\pi}$  are functions of corresponding phase spaces.



# CPV in $D^0 \rightarrow K^- K^+, \pi^- \pi^+$ decays backup (time-integrated)

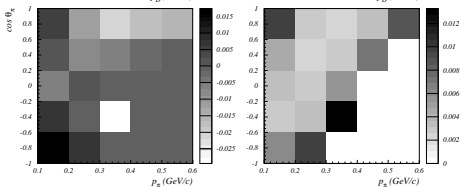
Determination of soft pion  $\pi_s$  asymmetry:

- using tagged and untagged  $D^0 \rightarrow K^- \pi^+$  decays



⇒ asymmetry map of the untagged  $K\pi$  sample (left)  
with uncertainty (right)

↪ weight  $D^0$  candidates in the  $\pi_s$  tagged  $K\pi$  sample

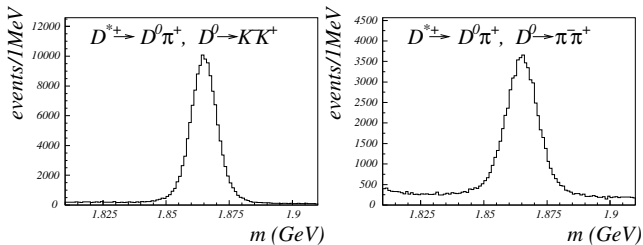


⇒ asymmetry map of the slow pion efficiency (left)  
with uncertainty (right)

↪ weight  $D^0$  yields to correct for tagging asymmetry

Averaging over the phase space the correction due to the  $\pi_s$  efficiency is found to be  $(0.76 \pm 0.09\%)$ .

# CPV in $D^0 \rightarrow K^-K^+, \pi^-\pi^+$ decays backup (time-integrated)



The signal counting was performed by the mass-sideband subtraction.

Systematics:

## Signal counting

	$KK$	$\pi\pi$
Signal shape diff.	0.02%	0.04%
Sideband position	0.01%	0.03%
Random $\pi_{slow}$ bkg.	0.03%	0.03%
Total	0.04%	0.06%

## $\pi_S$ eff. correction

	$KK$	$\pi\pi$
Statistics of $K\pi$	0.09%	0.09%
Binning	0.03%	0.02%
Min. num. events/bin	0.04%	0.03%
Total	0.10%	0.10%

## $A_{CP}$ extraction

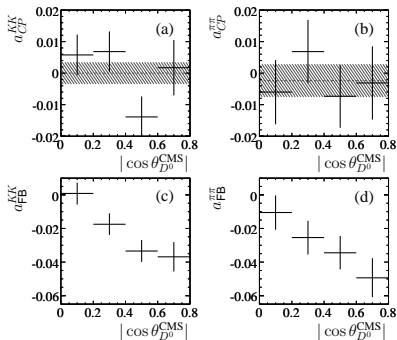
	$KK$	$\pi\pi$
Binning	0.03%	0.03%
SVD1/2	0.03%	0.00%
Total	0.04%	0.03%

# Time integrated CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$ decays

$$A_{\text{corr}}^{\text{reco}}(\cos\theta^*) = \frac{N(D^0) - N(\bar{D}^0)}{N(D^0) + N(\bar{D}^0)}$$

$$= A_{FB}^{D^{*+}} + A_{CP}^{hh}$$

BaBar



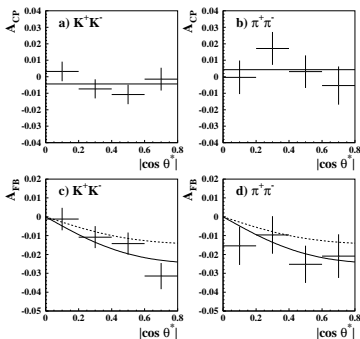
PRL100, 061803

$$A_{CP}^{KK} = (0.00 \pm 0.34(\text{stat}) \pm 0.13(\text{syst}))\%$$

$$A_{CP}^{\pi\pi} = (-0.24 \pm 0.52(\text{stat}) \pm 0.22(\text{syst}))\%$$

- $A_{CP} = \frac{A_{\text{corr}}^{\text{reco}}(\cos\theta^*) + A_{\text{corr}}^{\text{reco}}(-\cos\theta^*)}{2}$
- $A_{FB} = \frac{A_{\text{corr}}^{\text{reco}}(\cos\theta^*) - A_{\text{corr}}^{\text{reco}}(-\cos\theta^*)}{2}$

Belle



PLB670, 190

$$A_{CP}^{KK} = (-0.41 \pm 0.30(\text{stat}) \pm 0.11(\text{syst}))\%$$

$$A_{CP}^{\pi\pi} = (+0.41 \pm 0.52(\text{stat}) \pm 0.12(\text{syst}))\%$$