

ILC at Z-Pole – A reminder

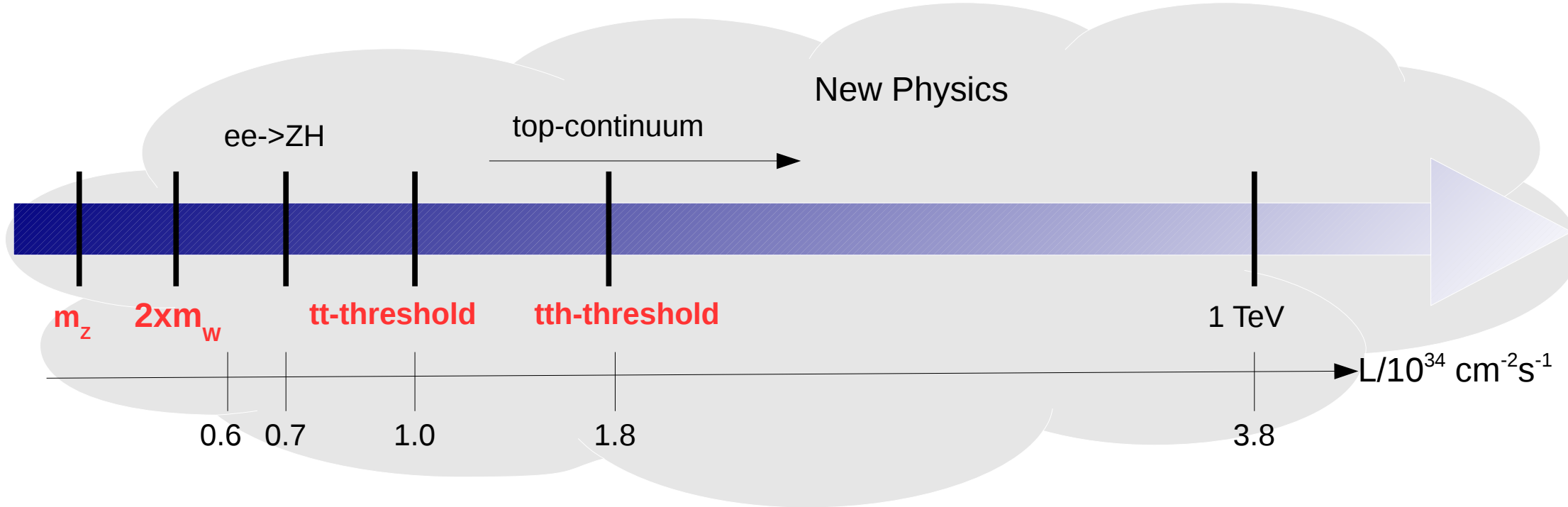
for a more comprehensive assessment see 1908.08212 and/or 2203.07622

Roman Pöschl



ECFA Higgs/elw./top study– November 2023

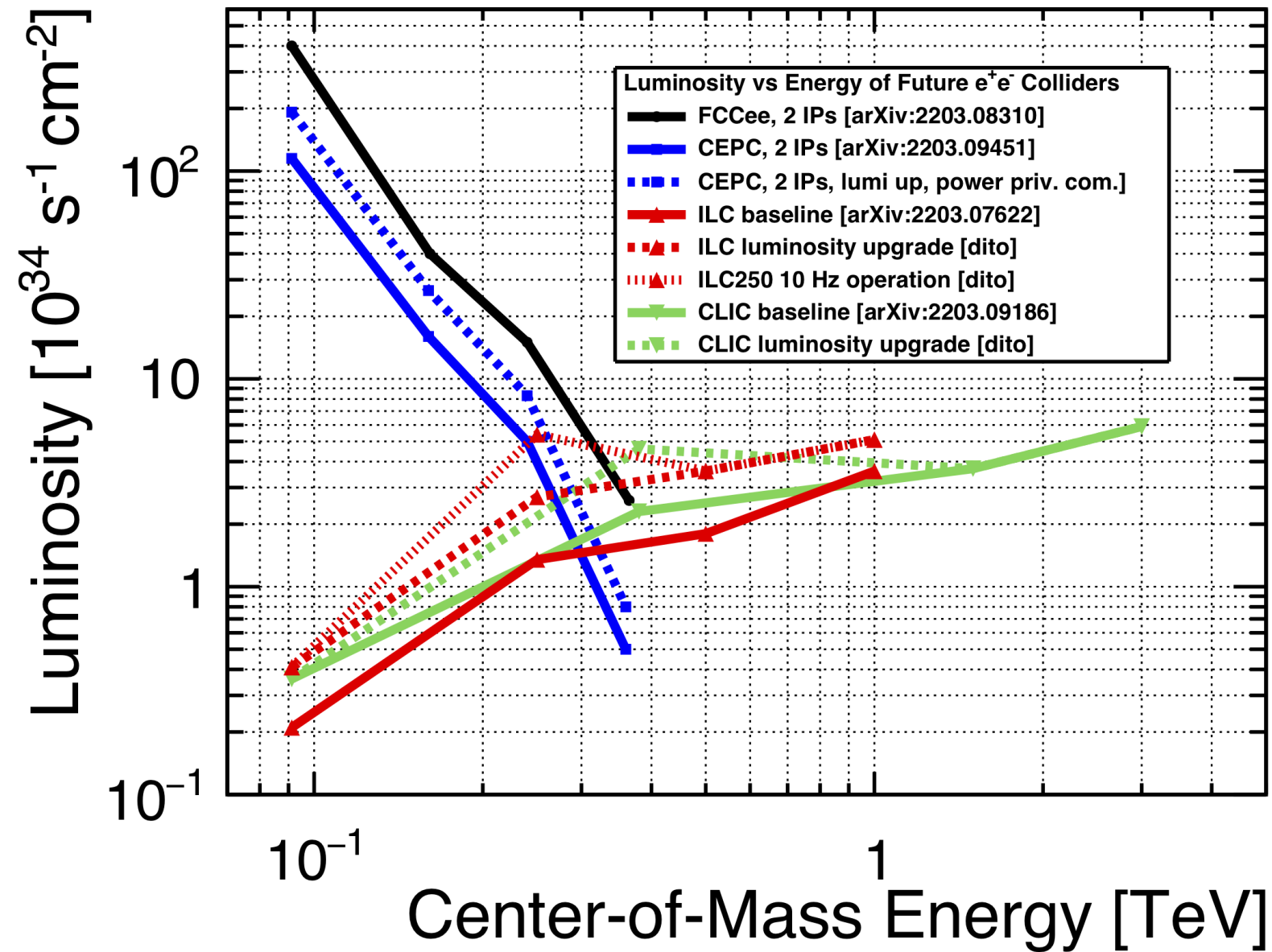
Disclaimer: I mainly show material that I have already shown more than 1.5 years ago at meetings of similar scope. I hope that it's not too outdated. If it is I apologise and please raise your hand



- All Standard Model particles within reach of planned e+e- colliders
- High precision tests of Standard Model over wide range to detect onset of New Physics
- Machine settings can be “tailored” for specific processes
 - Centre-of-Mass energy
 - Beam polarisation (straightforward at linear colliders)

$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

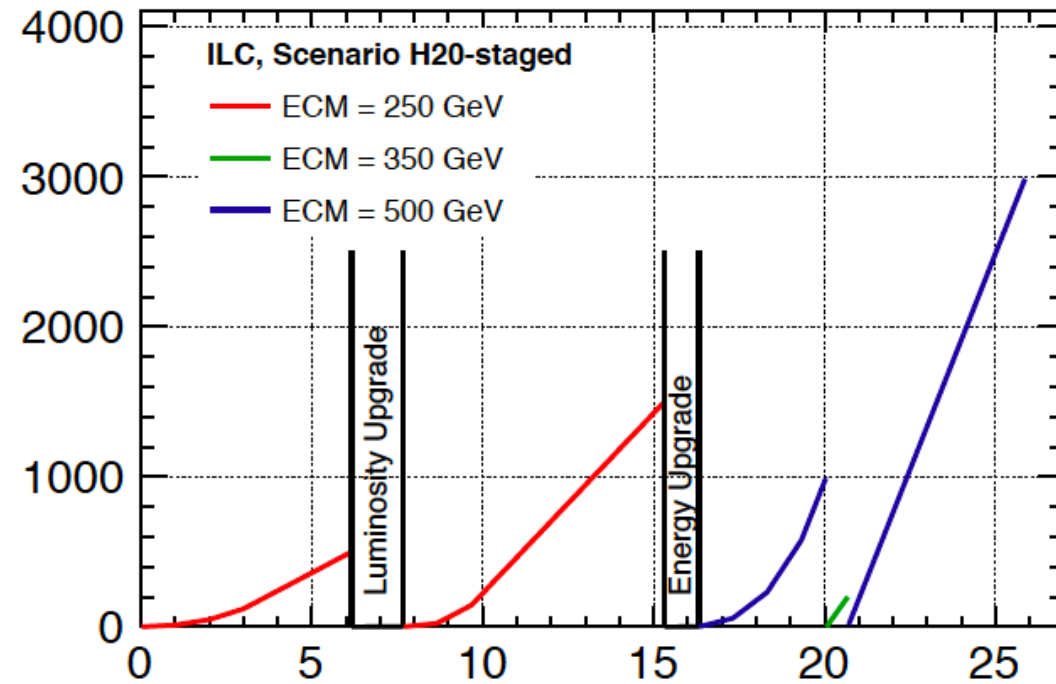
- **Background free** searches for BSM through beam polarisation



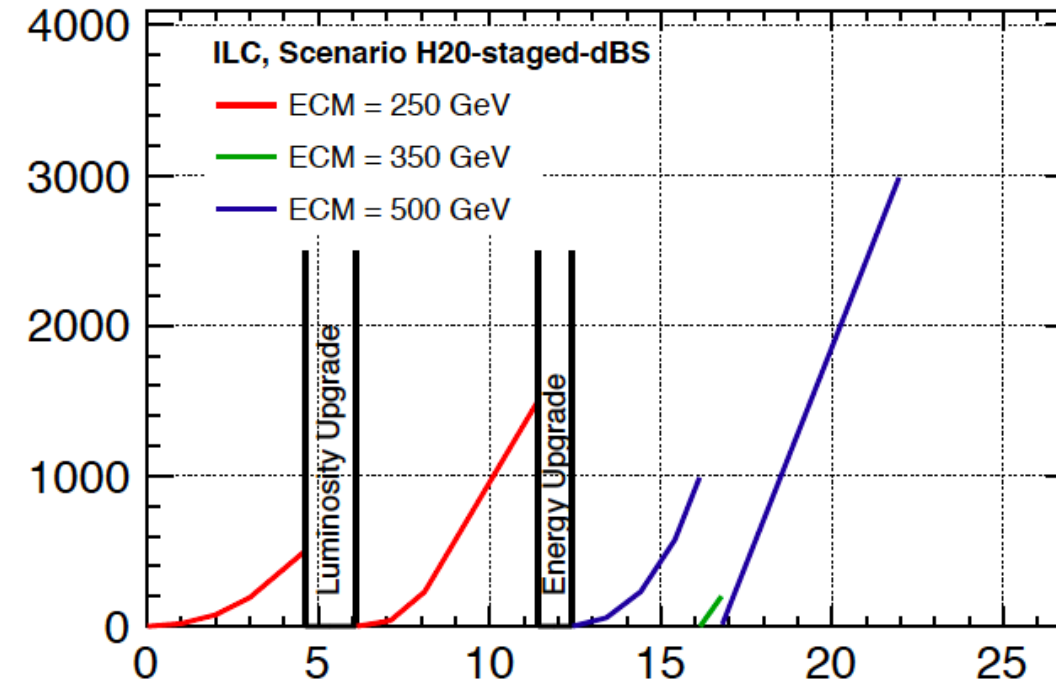
- High energies ~above tt-threshold
Domain of linear colliders
- Low energies e.g. Z-pole
Domain of circular machines
However, see later ...
- Transition region, i.e. HZ threshold
... not so clear
**Comparable numbers for all proposals
and $N = \sigma L$**
- Linear colliders are more versatile
to test chiral theory due to polarised
beams
- Plot on power consumption see backup

Figure J. List

Integrated Luminosities [fb^{-1}]



Integrated Luminosities [fb^{-1}]



In 2019 – Revision of capabilities to run on the Z Pole - GigaZ

	$\text{sgn}(P(e^-), P(e^+)) =$				sum
	(-,+)	(+,-)	(-,-)	(+,+)	
luminosity [fb^{-1}]	40	40	10	10	
$\sigma(P_{e^-}, P_{e^+})$ [nb]	83.5	63.7	50.0	40.6	
Z events [10^9]	2.4	1.8	0.36	0.29	4.9
hadronic Z events [10^9]	1.7	1.3	0.25	0.21	3.4

- Pole running can happen before and after the luminosity upgrade
- Further details see arxiv: 1908.08212

Track momentum: $\sigma_{1/p} < 5 \times 10^{-5}/\text{GeV}$ (1/10 x LEP)

(e.g. Measurement of Z boson mass in Higgs Recoil)

Impact parameter: $\sigma_{d0} < [5 \oplus 10/(p[\text{GeV}]\sin^{3/2}\theta)] \mu\text{m}$ (1/3 x SLD)

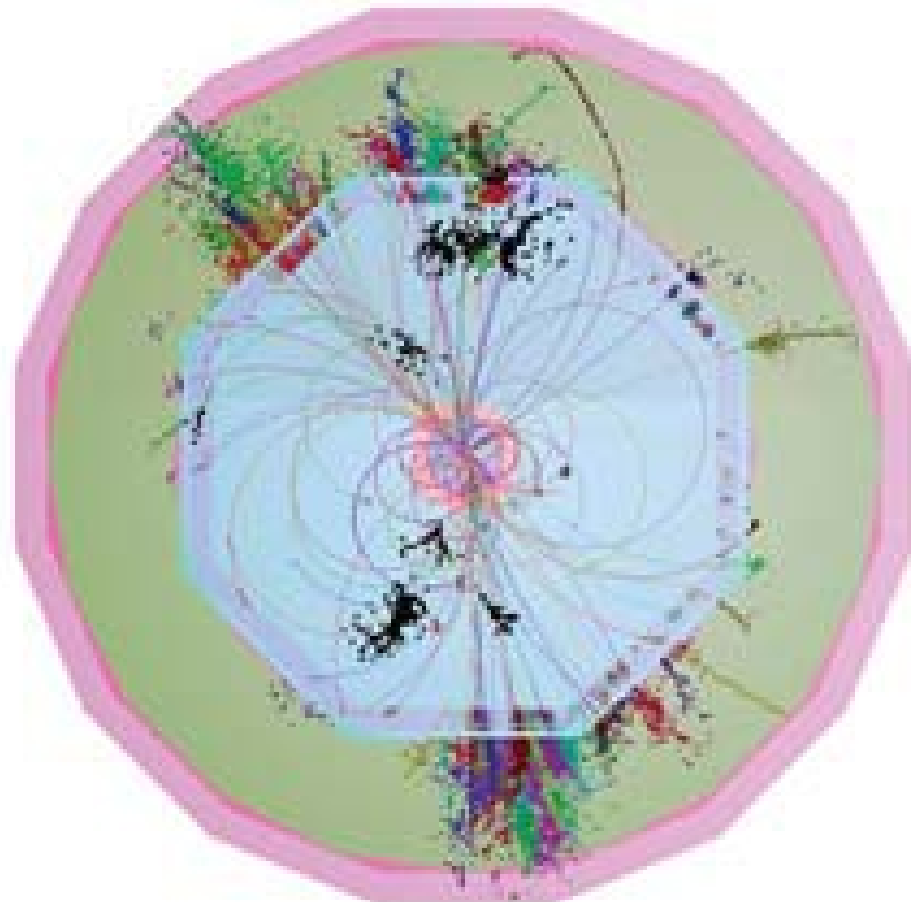
(Quark tagging c/b)

Jet energy resolution : $dE/E = 0.3/(E(\text{GeV}))^{1/2}$ (1/2 x LEP)

(W/Z masses with jets)

Hermeticity : $\theta_{\min} = 5 \text{ mrad}$

(for events with missing energy e.g. dark sector/ invisible decays)



Final state will comprise events with a large number of charged tracks and jets(6+)

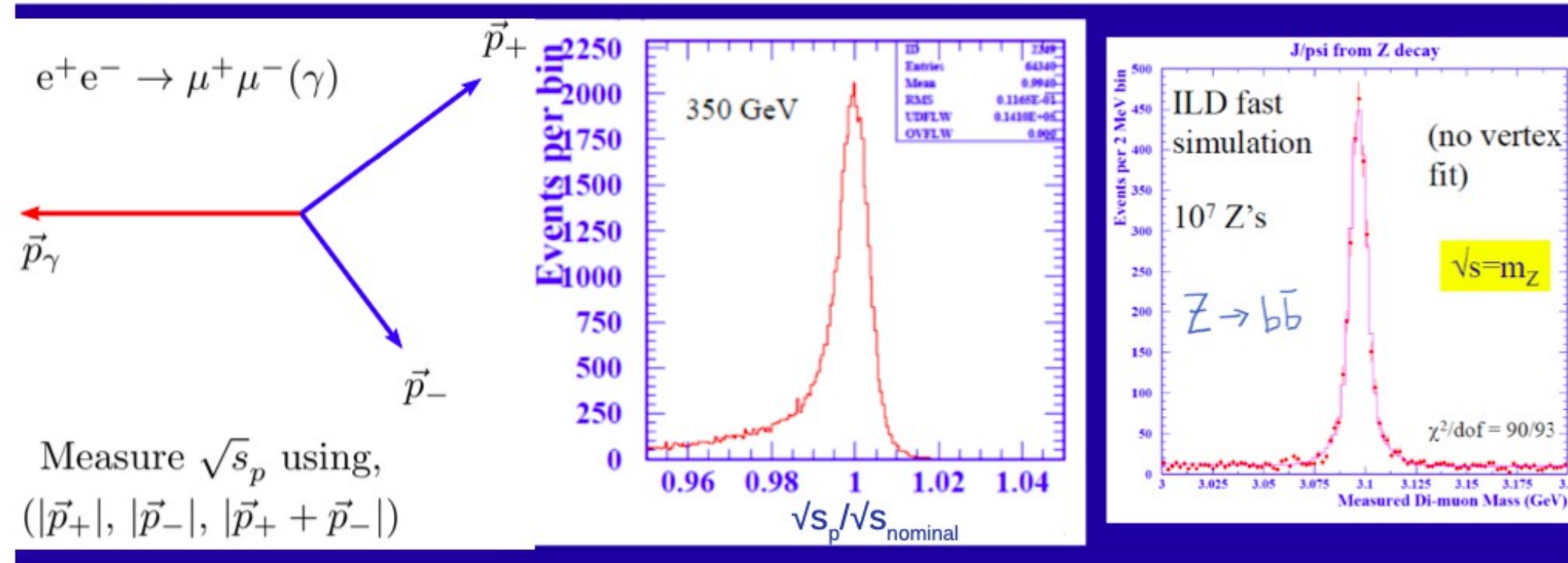
- High granularity
- Excellent momentum measurement
- High separation power for particles
- **Particle Flow Detectors**

Core Program				
Observable	M_H	M_t	M_W	M_X
Method	Recoil mass	Scan	Reconstruction	Scan?
Best \sqrt{s} [GeV]	250	350	250	Highest?
Current precision [MeV]	170	300	12	–
Target precision [MeV]	10	20	2	?
\sqrt{s} contribution [MeV]	3	6	0.5	?
\sqrt{s} uncertainty goal [ppm]	100	200	10	100?

Ultimate Impact/Reach				
Observable	M_W	M_Z	Γ_Z	A_{LR}
Method	Scan	Scan	Scan	Count/Scan
Best \sqrt{s} [GeV]	161	91	91	91
Current precision	12	2.1	2.3	1.9×10^{-3}
Target precision	2 MeV	0.2 MeV	0.11 MeV	3.5×10^{-5}
\sqrt{s} contribution	0.8 MeV	0.2 MeV	small	1.8×10^{-5}
\sqrt{s} uncertainty goal [ppm]	10	2	5*	10

Today

Use dilepton momenta, with $\sqrt{s}_p \equiv E_+ + E_- + |\vec{p}_{+-}|$ as \sqrt{s} estimator.



Tie detector p -scale to particle masses (know J/ψ , π^+ , p to 1.9, 1.3, 0.006 ppm)

Measure $\langle \sqrt{s} \rangle$ and luminosity spectrum with same events. Expect statistical uncertainty of 1.0 ppm on p -scale per 1.2M $J/\psi \rightarrow \mu^+\mu^-$ (4×10^9 hadronic Z's).

- excellent tracker momentum resolution - can resolve beam energy spread.
- feasible for $\mu^+\mu^-$ and e^+e^- (and ... 4l etc).

Further remarks:

- Realistic study has to take real beam energy spread and crossing angle into account
 - Ongoing
- Momentum scale can be further constrained by with K_0 and Λ using Armenteros-Podolanski Method
 - See e.g. 2012.03620
- 10ppm at $s=250$ GeV and 1ppm on Z pole seem to be in reach

W Mass from:

- Constrained WW reconstruction
- Hadronic mass from hadronic W decays
- Lepton endpoints: $m_W^2 = E_l(E_b - E_l)$, $E_l = E_b(1 \pm \beta_W)/2$
- Dilepton pseudo mass from constrained fit
- Polarised W scan

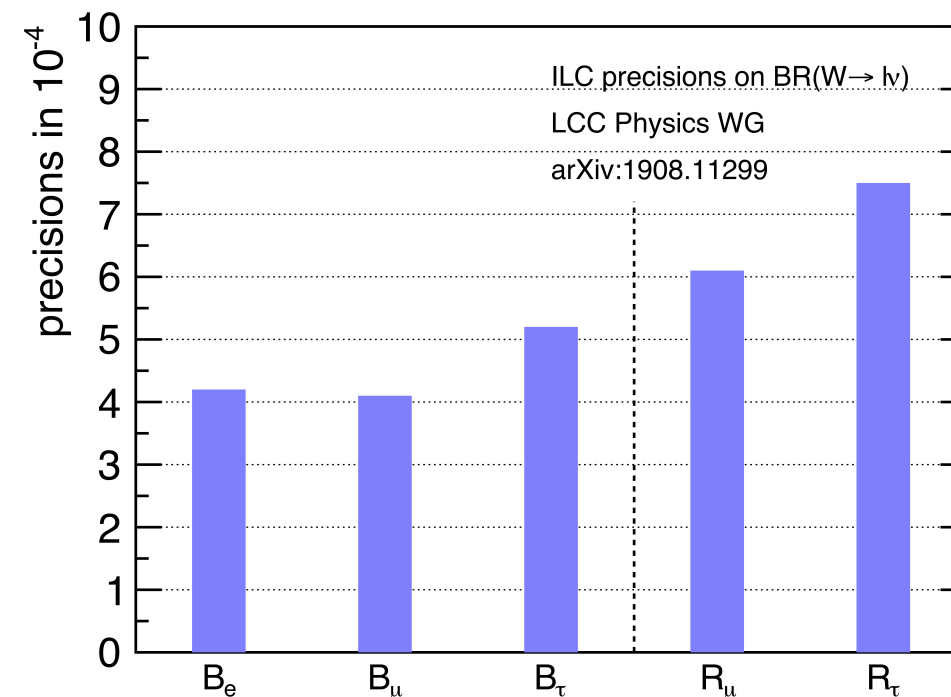
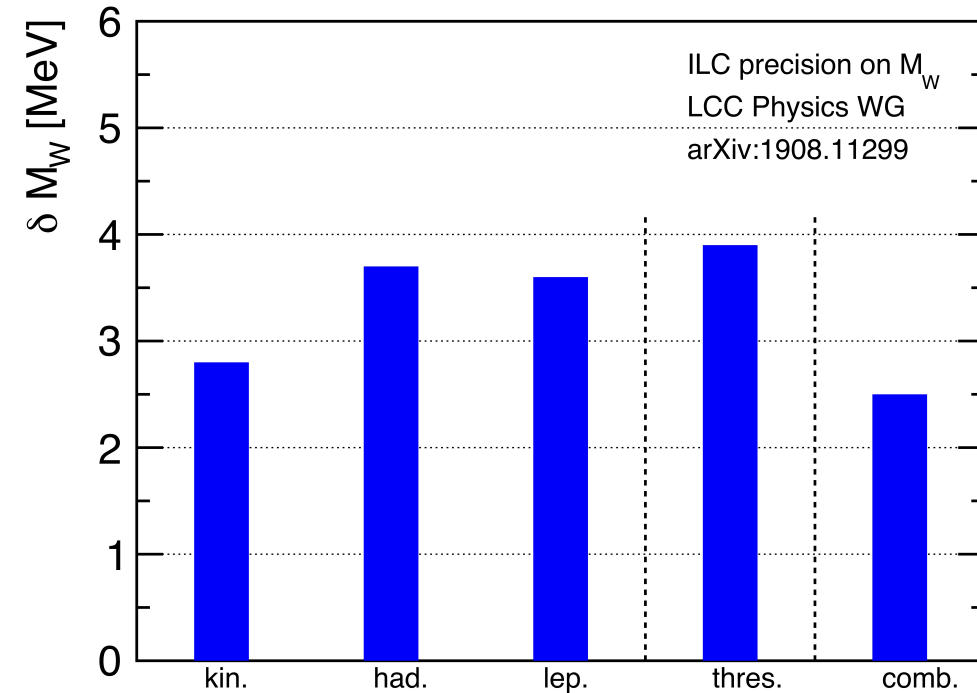
$$\Delta m_W (MeV) = 2.4(stat.) \oplus 3.2(syst.) \oplus 0.8(\sqrt{s}) \oplus theory$$

Branching ratios

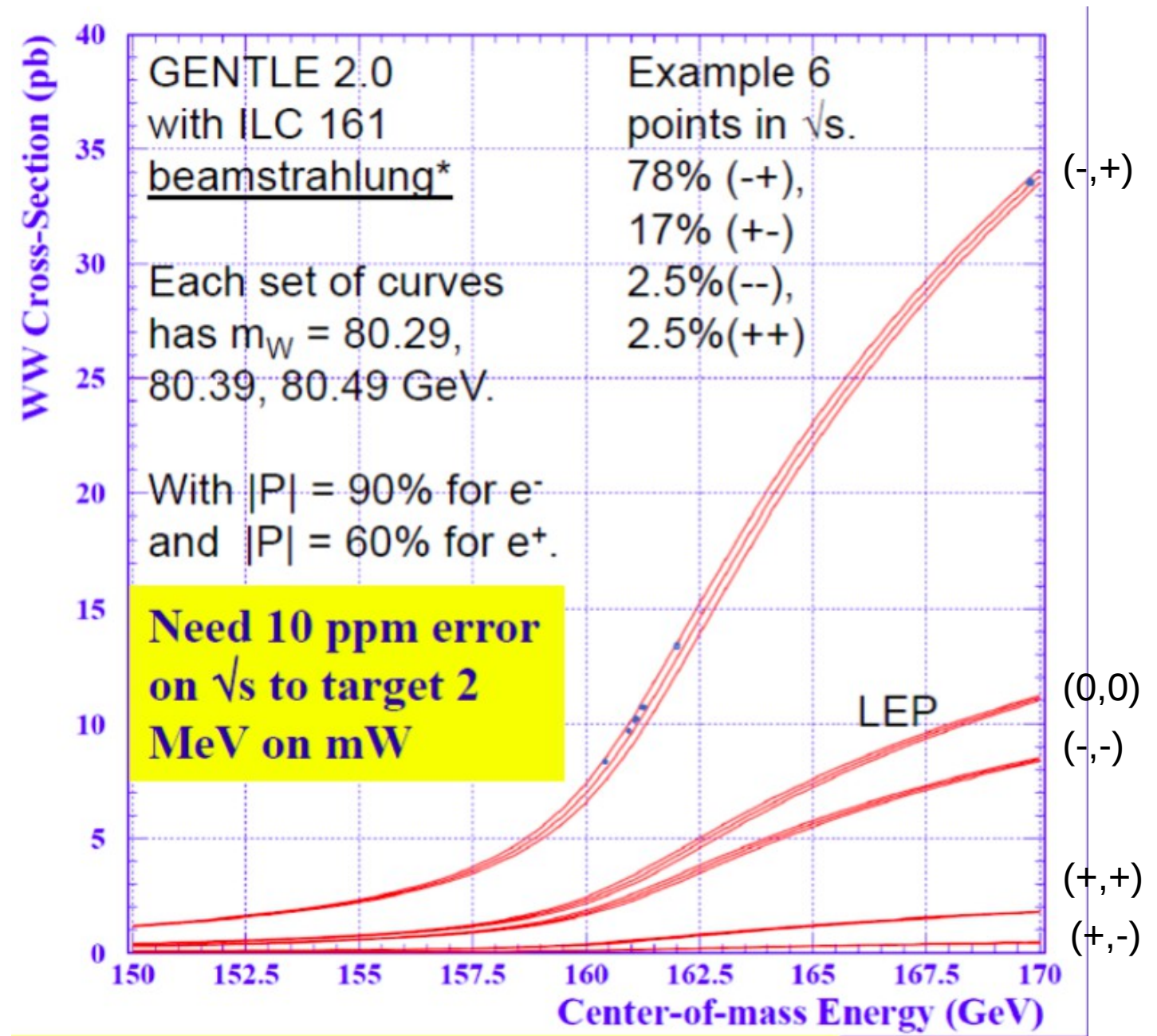
From simultaneous fit to all 10 decay combinations

$$\Rightarrow \sigma_{tot} \text{ and } B_{e,\mu,\tau} \text{ and } B_{had} = 1 - B_e - B_\mu - B_\tau$$

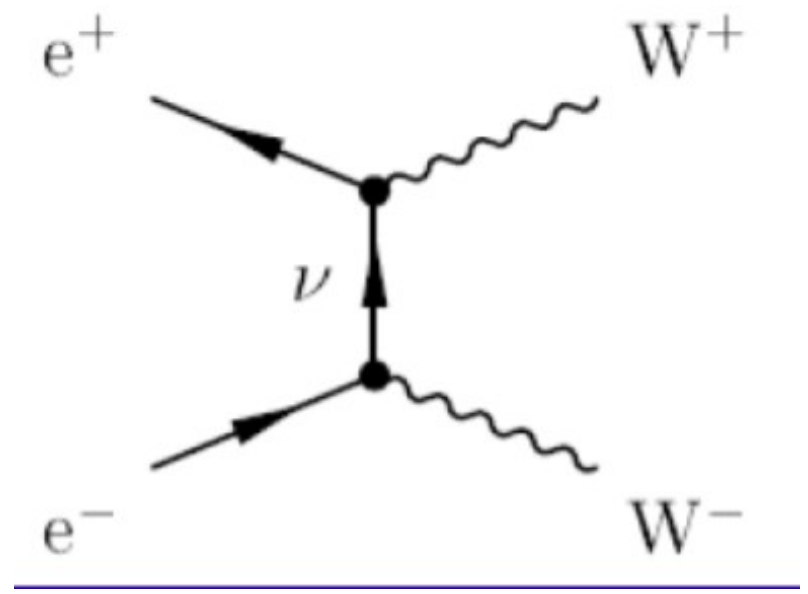
W width: $\Delta\Gamma_W = 3.2 MeV$



W - Parameters

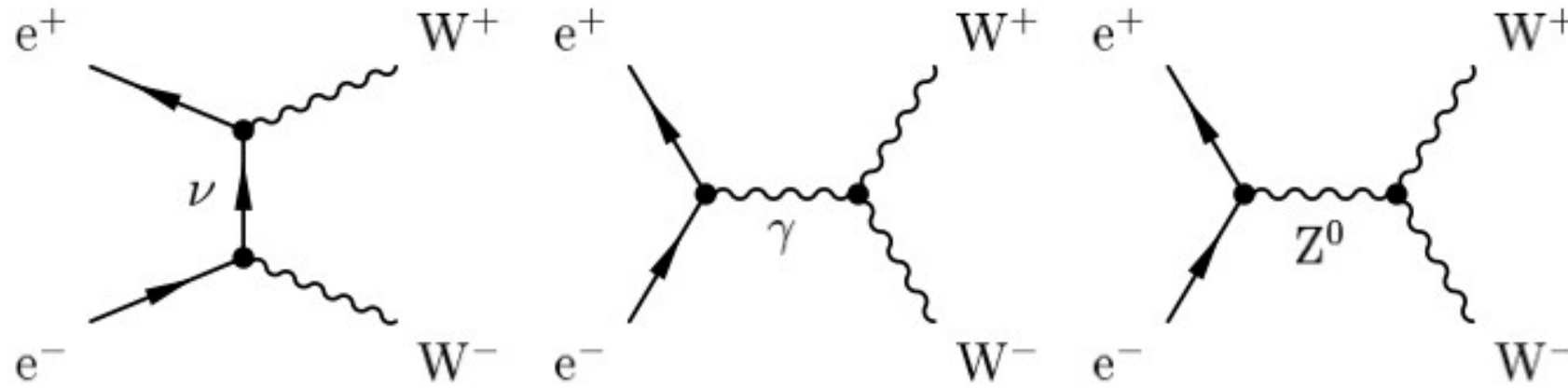


G. Wilson



- Robust method
- Beam polarisation essential to control background
- Need extreme good control of beam energy

Anomalous Triple Gauge Couplings

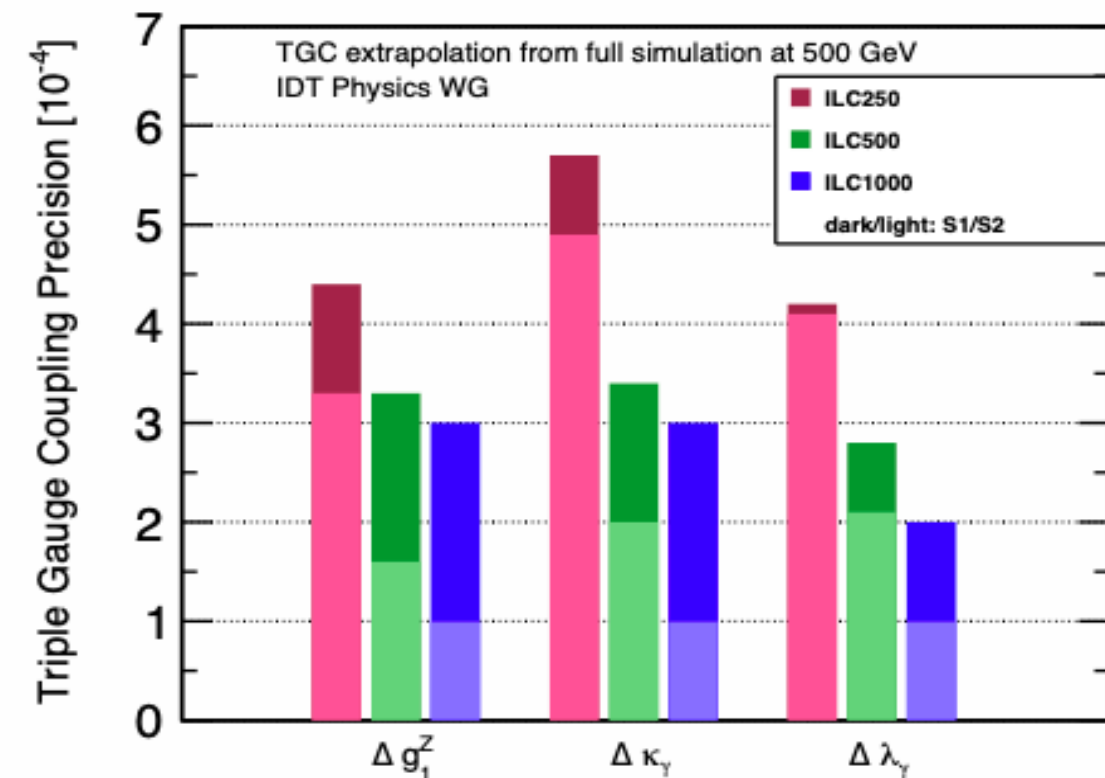
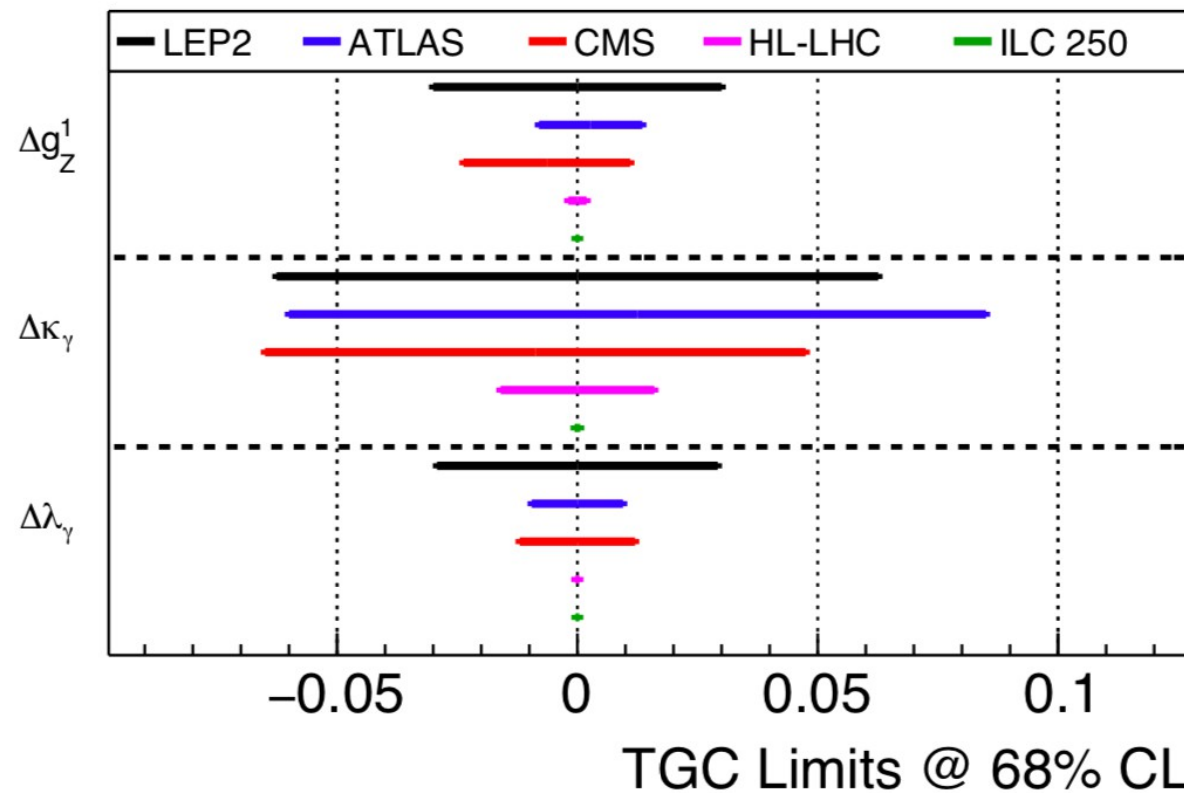


- Sensitivity to triple and quartic gauge Boson couplings (TGC and QGC)

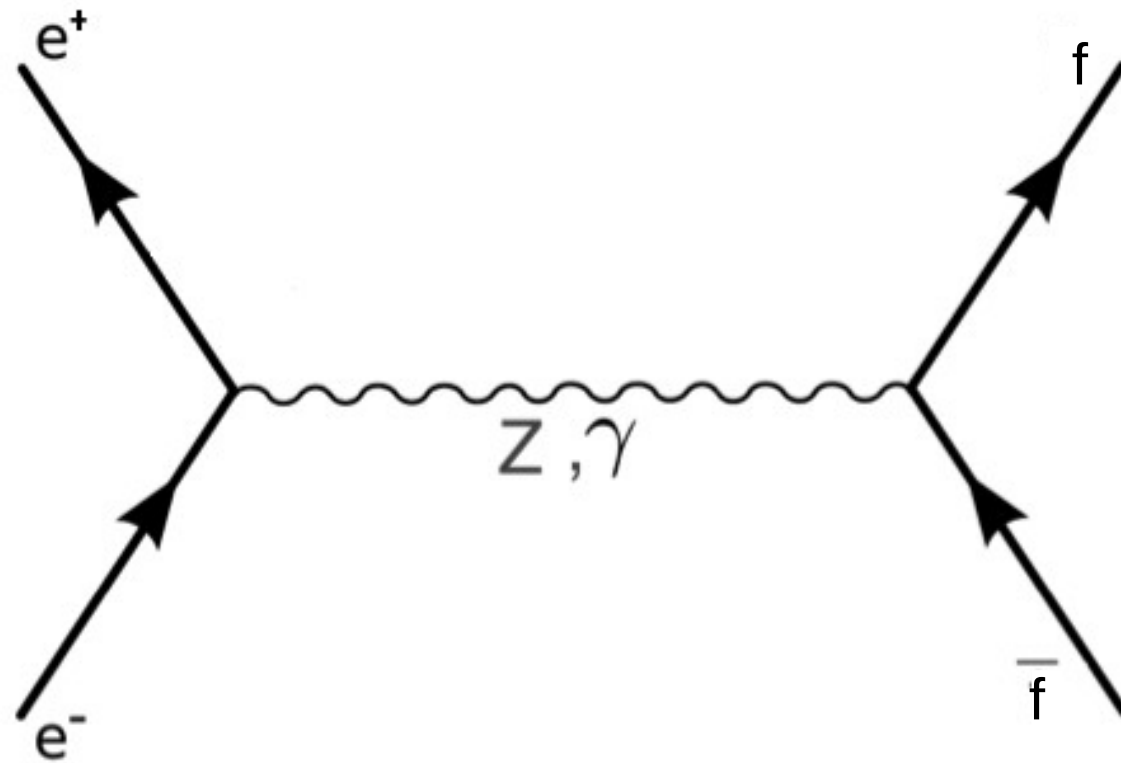
- Observables depend strongly on beam polarisation

=> Enrich different helicity modes of W
 => Disentangling of couplings to Z and γ
 => in situ measurement of beam polarisation (and luminosity)

Limits on Triple Gauge Couplings @ 250 GeV



J. List, ILC Snowmass White Paper



$$\frac{d\sigma}{d\cos\theta}(e_L^- e_R^+ \rightarrow f \bar{f}) = \Sigma_{LL}(1 + \cos\theta)^2 + \Sigma_{LR}(1 - \cos\theta)^2$$

$$\frac{d\sigma}{d\cos\theta}(e_R^- e_L^+ \rightarrow f \bar{f}) = \Sigma_{RL}(1 - \cos\theta)^2 + \Sigma_{RR}(1 + \cos\theta)^2$$

*add term $\sim \sin^2\theta$ in case of non-relativistic fermions e.g. top close to threshold

- Σ_{IJ} are helicity amplitudes that contain couplings g_L, g_R (or F_V, F_A)
- $\Sigma_{IJ} \neq \Sigma_{I'J'}$ => (characteristic) asymmetries for each fermion
- Forward-backward in angle, general left-right in cross section
- **All four helicity amplitudes for all fermions only available with polarised beams**

Helicity amplitudes can be analysed in several ways (not mutually exclusive):

Oblique Parameters W, Z:

$$Q_{eifj} = Q_e^\gamma Q_f^\gamma + \frac{g_{e_i}^Z g_{f_j}^Z}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_Z^2 + i\Gamma_Z M_Z} + \frac{s}{m_W^2} f_{i,j}(W, Y)$$

Contact interactions with e.g. compositeness scale Λ :

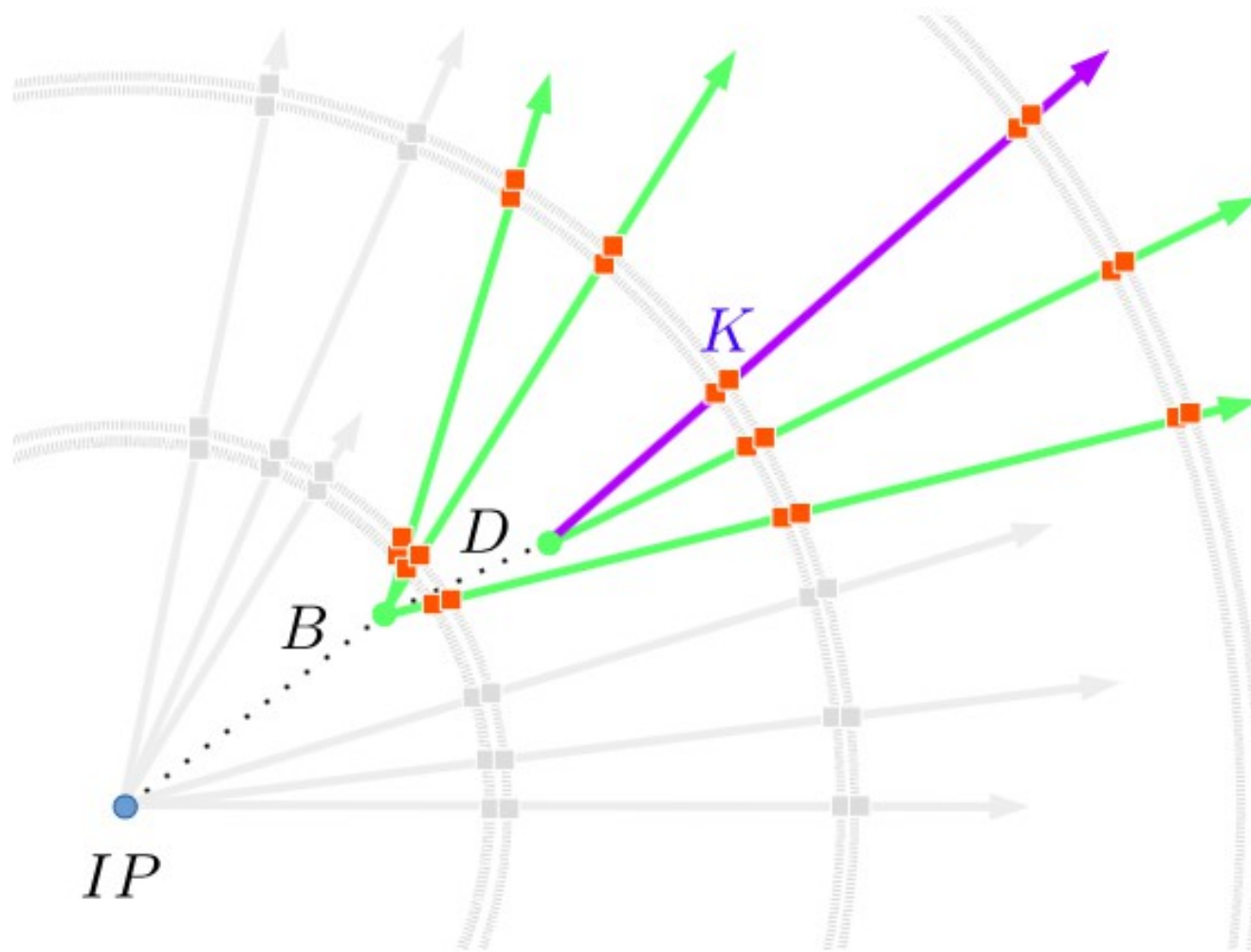
$$Q_{eifj} = Q_e^\gamma Q_f^\gamma + \frac{g_{e_i}^Z g_{f_j}^Z}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_Z^2 + i\Gamma_Z M_Z} + \frac{g_{\text{contact}}^2}{2\Lambda^2} \eta_{eifj}$$

New propagators in concrete models of new physics:

$$Q_{eifj} = Q_e^\gamma Q_f^\gamma + \frac{g_{e_i}^Z g_{f_j}^Z}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_Z^2 + i\Gamma_Z M_Z} + \sum \frac{g_{e_i}^{Z'} g_{f_j}^{Z'}}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_{Z'}^2 + i\Gamma_{Z'} M_{Z'}}$$

Always with I,j being the helicities of the initial state electron e and the final state fermion f

Remark: Have to exchange g → Q to be consistent with conventions

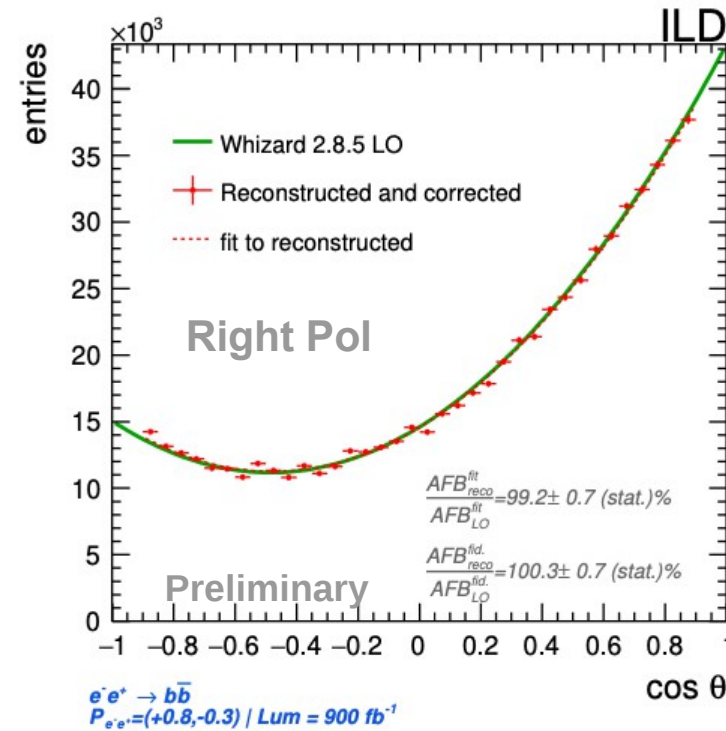
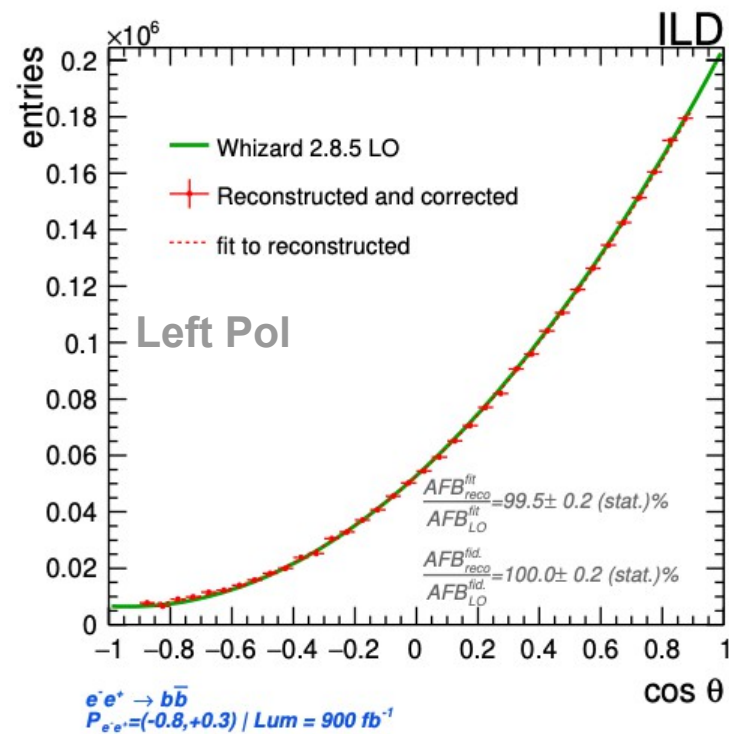


- flavor tagging
- b-quark charge measurement
 - Important for top quark studies, indispensable for $ee \rightarrow bb$
- Control of migrations:
 - Correct measurement of vertex charge
 - Requires excellent forward acceptance
 - Kaon identification by dE/dx (and more)
- ILC/ILD can base the entire measurements on double Tagging and vertex charge
 - LEP/SLC had to include single tags and semi-leptonic events

PhD thesis: S. Bilokin
 A. Irles



Full simulation study within ILD Concept at $\sqrt{s}=250$ GeV allows for educated guess on uncertainties on Z-Pole

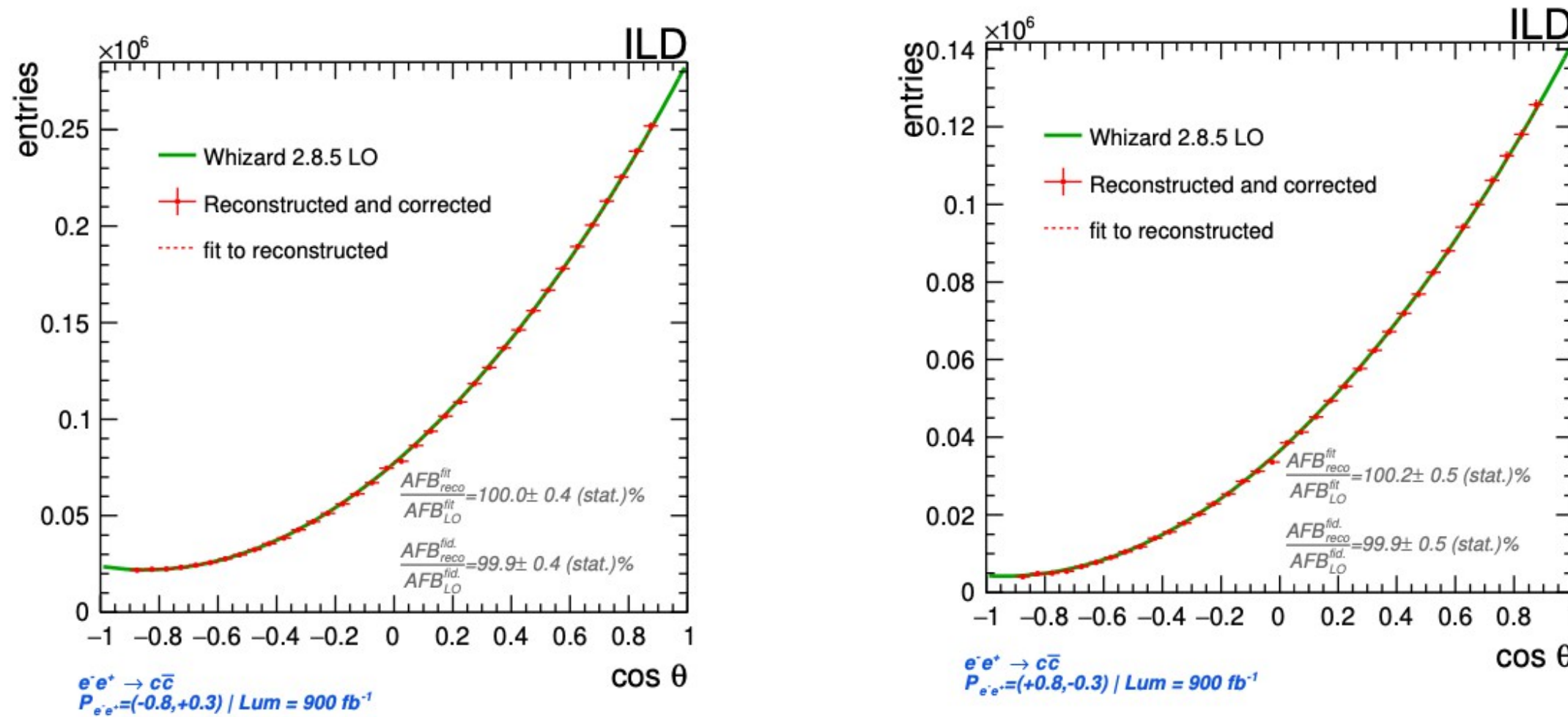


Arxiv:2306.11413

Excellent agreement between predicted and reconstructed distributions

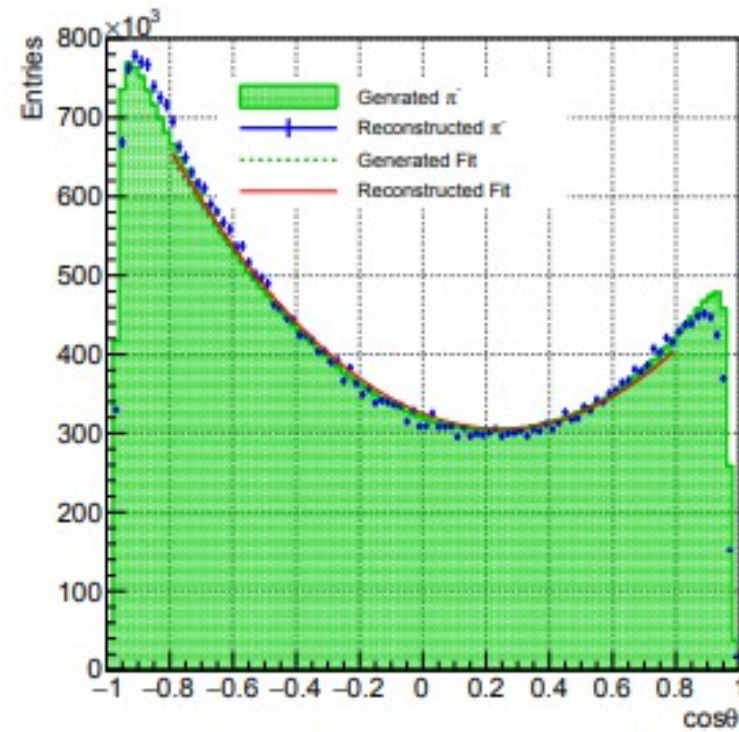
Source	$e^-e^+ \rightarrow c\bar{c}$				$e^-e^+ \rightarrow b\bar{b}$			
	$P_{e^-e^+}(-0.8, +0.3)$		$P_{e^-e^+}(+0.8, -0.3)$		$P_{e^-e^+}(-0.8, +0.3)$		$P_{e^-e^+}(+0.8, -0.3)$	
	R_c	$A_{FB}^{c\bar{c}}$	R_c	$A_{FB}^{c\bar{c}}$	R_b	$A_{FB}^{b\bar{b}}$	R_b	$A_{FB}^{b\bar{b}}$
Statistics	0.18%	0.38%	0.27%	0.52%	0.12%	0.24%	0.23%	0.70%
Preselection eff.	<0.01%	0.12%	0.02%	0.16%	<0.01%	0.08%	0.06%	0.12%
Background	0.01%	0.01%	0.02%	0.02%	0.01%	0.01%	0.06%	<0.01%
heavy quark mistag	0.11%	<0.01%	0.06%	<0.01%	0.12%	<0.01%	0.22%	<0.01%
<i>uds</i> mistag	0.03%	<0.01%	0.02%	<0.01%	0.08%	<0.01%	0.14%	<0.01%
Angular correlations	0.10%	0.10%	0.10%	0.10%	0.10%	0.10%	0.10%	0.10%
Beam Polarisation	<0.01%	<0.01%	0.02%	0.01%	<0.01%	0.01%	0.03%	0.15%
Systematics	0.15%	0.16%	0.12%	0.19%	0.18%	0.13%	0.29%	0.22%
Total	0.24%	0.41%	0.30%	0.55%	0.21%	0.27%	0.37%	0.73%

Additional complication in continuum compared with Z-Pole: Rejection of ISR events)

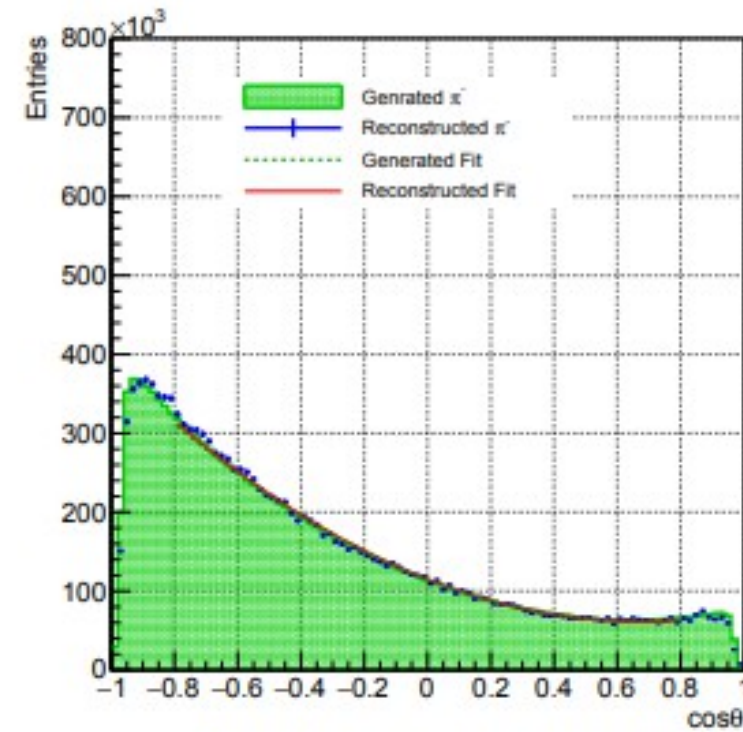


- Full simulation study (with ILD concept)
- Long lever arm in $\cos \theta_c$ to extract from factors or couplings

Polar Angle Distribution



(a)

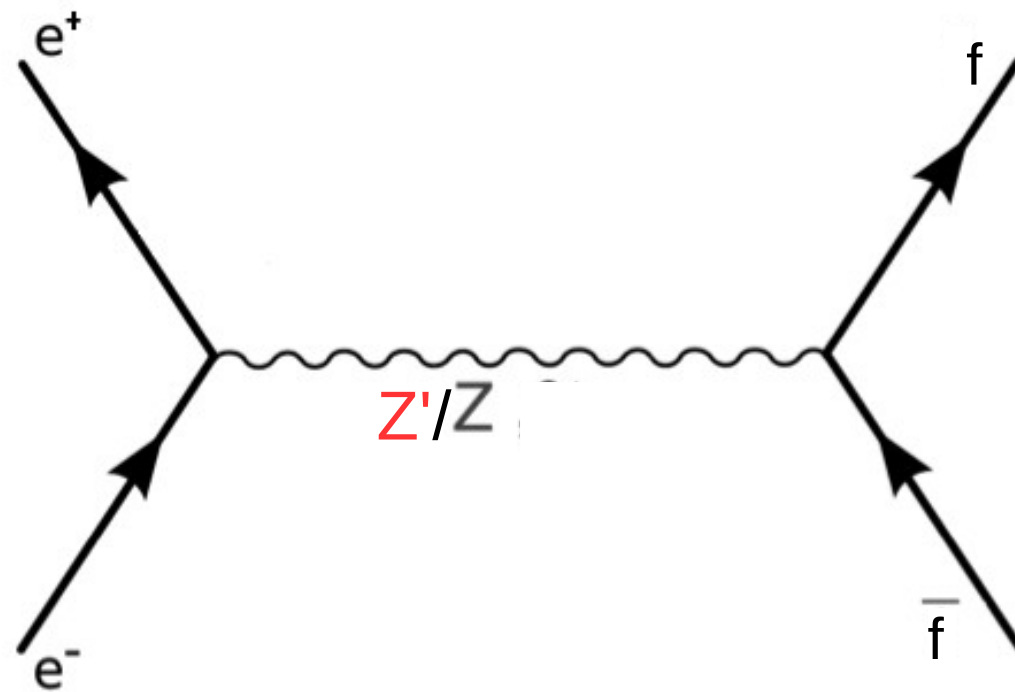


(b)

Figure 4: Reconstructed polar angle distribution for the u and d mixed samples with (a) left-handed and (b) right-handed electron beam.

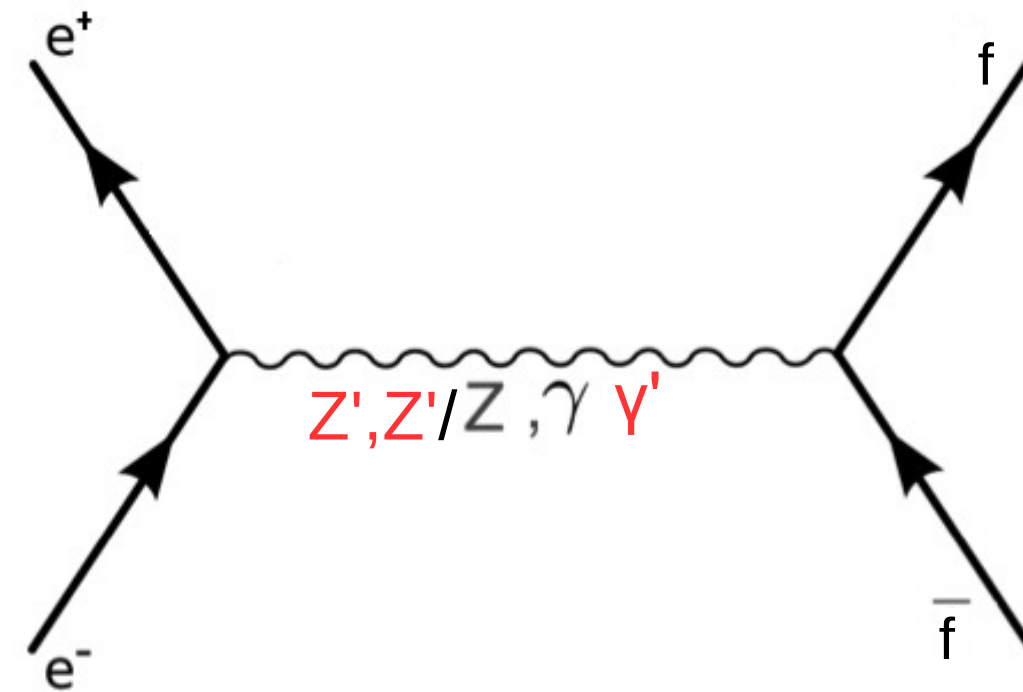
PhD thesis
Y. Okugawa
See also talk at
Paestum

On the Z-pole



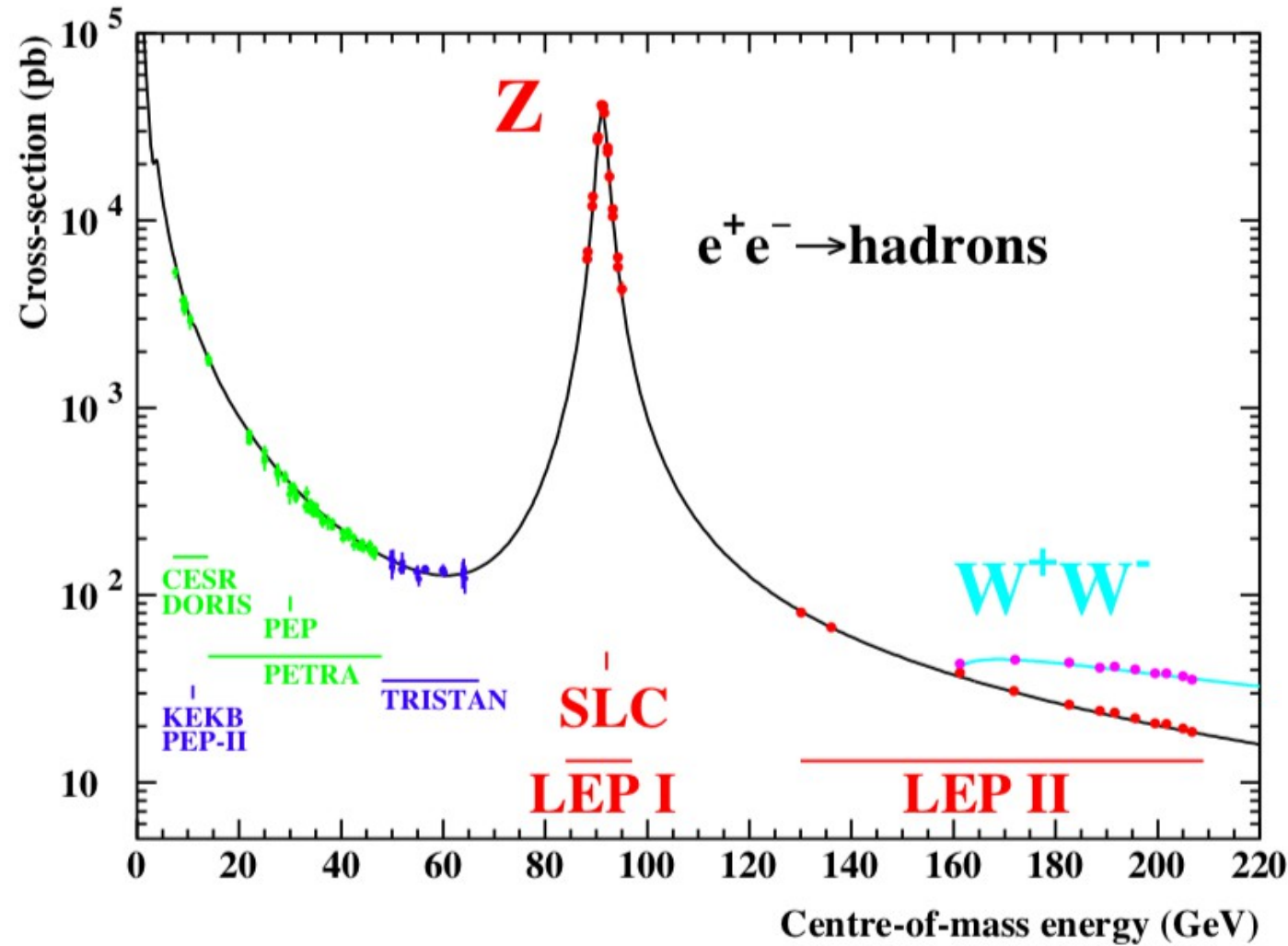
- **ILC/GigaZ with $\sim 10^9 Z$**
- Sensitivity to Z/Z' mixing
- Sensitivity to vector (and tensor?) couplings of the Z
 - the photon does not “disturb”

Above the Z-pole



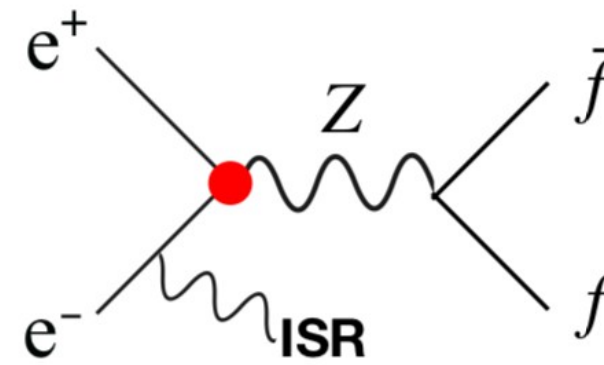
- Sensitivity to interference effects of Z and photon!!
- Measured couplings of photon and Z can be influenced by new physics effects
- Interpretation of result is greatly supported by precise input from Z pole

Running on Z pole "GigaZ"



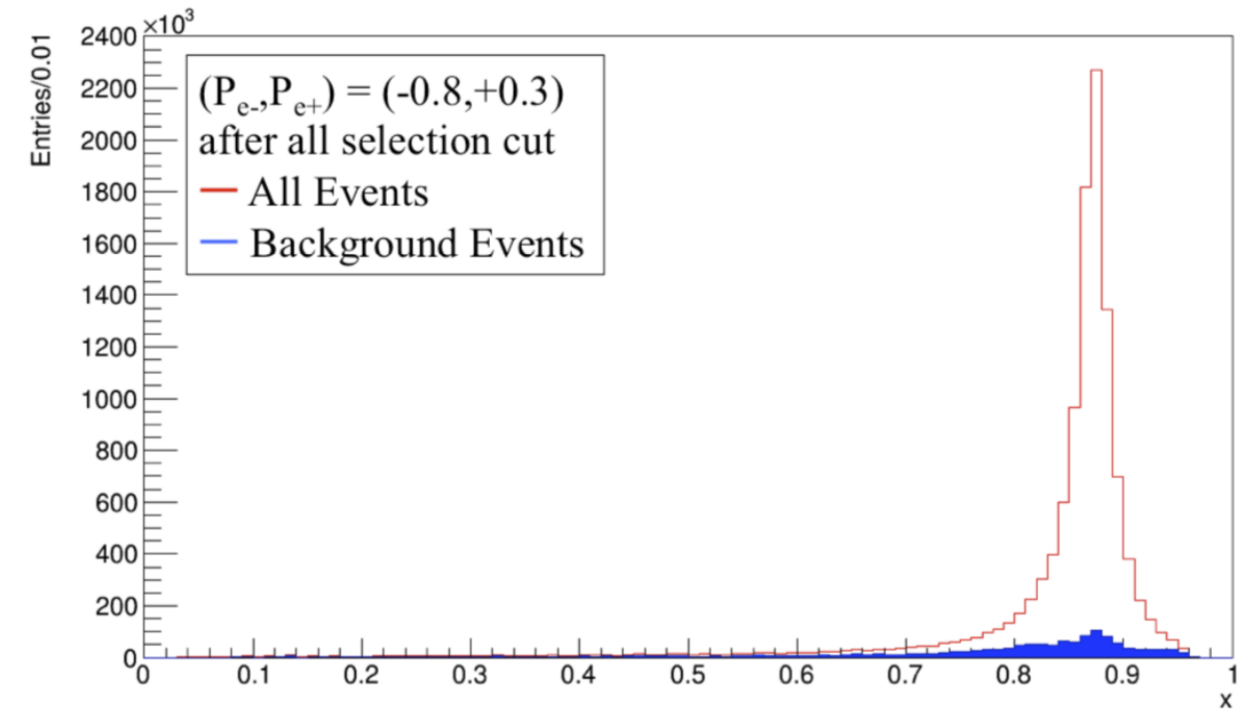
- Around 5×10^9 Z events (250xLEP)
- With beam polarisation
 $\sim 30 \times 250 = 7500$ LEP!

Radiative return at higher energies



$$m_Z^2 = \frac{1 - |\beta|}{1 + |\beta|} \cdot s$$

$$\beta = \frac{|\sin(\theta_1 + \sin \theta_2)|}{\sin \theta_1 + \sin \theta_2}$$



- $\sim 10^8$ events at 250 GeV with 2 ab^{-1}
- Beam polarisation

Partial fermion width:

$$R_f = \frac{N_f}{N_{had}} = \frac{(g_f^L)^2 + (g_f^R)^2}{\sum_{i=1}^{n_q} [(g_i^L)^2 + (g_i^R)^2]}$$

- Sensitive to sum of coupling constants
- Available at linear and circular colliders

Left-right asymmetry:

$$A_{LR} = \frac{1}{|\mathcal{P}_{eff.}|} \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \mathcal{A}_e = \frac{(g_f^L)^2 - (g_f^R)^2}{(g_f^L)^2 + (g_f^R)^2} \sim 1 - 4\sin^2 \theta_{eff.}^l$$

- Direct sensitivity to Zee vertex
- Only available at linear colliders due to beam polarisation
- Circular colliders need auxiliary measurement
 - e.g. $P_r \sim A_e$

Forward-backward asymmetry:

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f \quad \text{for } \mathcal{P}_e = 0.$$

- “Classical” observable to study P-violating effects in ee->ff
- Available at circular and linear colliders
- Without beam polarisation interpretation is always model dependent

Left-right-forward-backward asymmetry:

$$A_{FB,LR}^f = \frac{(\sigma_F - \sigma_B)_L - (\sigma_F - \sigma_B)_R}{(\sigma_F + \sigma_B)_L + (\sigma_F + \sigma_B)_R} = -\frac{3}{4} \mathcal{A}_f$$

- Combination of asymmetries above
- Only available linear colliders due to beam polarisation
- Direct and model independent measurement of A_f

$$\mathcal{A}_e = \frac{(g_{eL}^Z)^2 - (g_{eR}^Z)^2}{(g_{eL}^Z)^2 + (g_{eR}^Z)^2} = \frac{2g_{eV}/g_{eA}}{1 + (g_{eV}/g_{eA})^2} \quad \text{with } g_{eV}/g_{eA} = 1 - 4 \sin^2 \theta_{\text{eff}}^{\ell}.$$

How to determine \mathcal{A}_e ?

Left Right Asymmetry
 Requires polarised beams

$$A_{LR} = \frac{1}{|\mathcal{P}_{eff.}|} \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \mathcal{A}_e$$

Available at LC

Using all hadronic decays of Z!!!

Forward backward asymmetry
 Has to assume lepton universality!!!

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f \quad \text{for } \mathcal{P}_e = 0.$$

Available at LC, CC

Used e.g. In EPJC (2019) 79:474
 with $f = \mu$

Final state polarisation (r,l)
 e.g. with τ

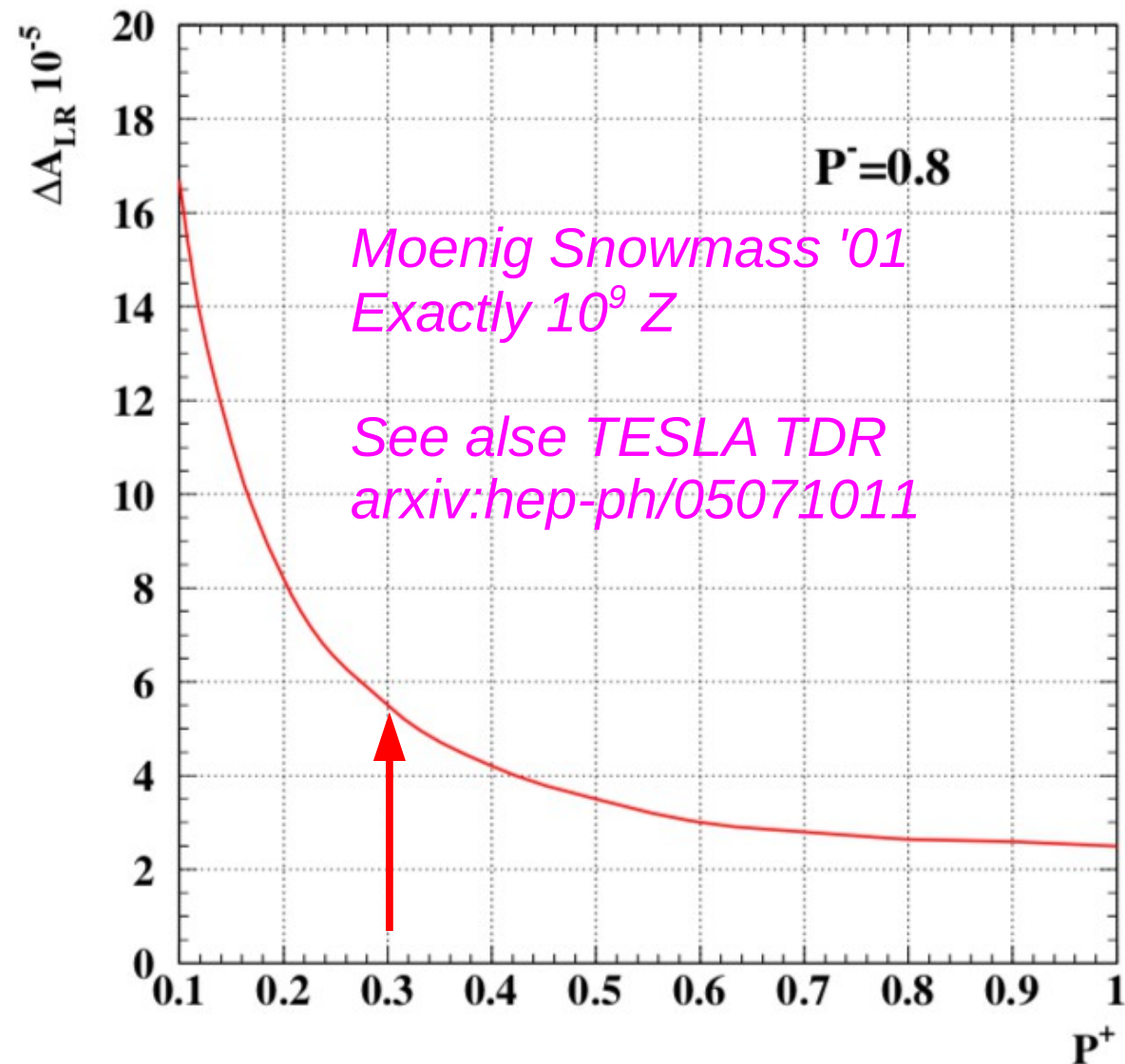
$$A_{FB}^{pol} = \frac{(\sigma_r - \sigma_l)_F - (\sigma_r - \sigma_l)_B}{(\sigma_r + \sigma_l)_F + (\sigma_r + \sigma_l)_B} = -\frac{3}{4} \mathcal{A}_e$$

Available at LC, CC

Beam polarisation is key: Remember SLC delivered most precise value of $\sin^2 \theta_{\text{eff}}^{\ell}$
 despite of 30 times less lumi

Measurement of $\sin^2\theta_{\text{eff}}^{\ell}$.

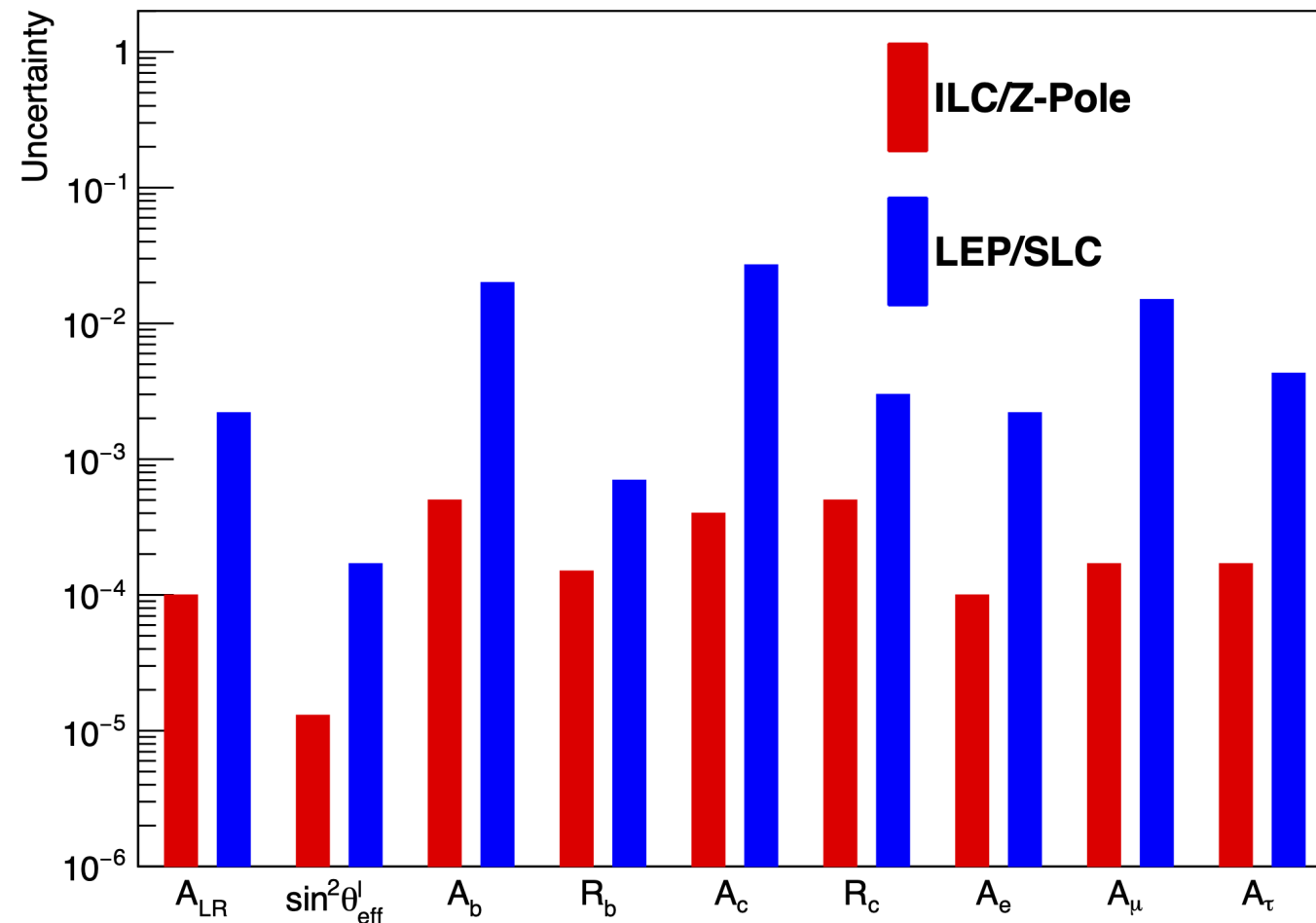
Blondel scheme:
$$A_{LR} = \sqrt{\frac{(\sigma_{++} + \sigma_{-+} - \sigma_{+-} - \sigma_{--})(-\sigma_{++} + \sigma_{-+} - \sigma_{+-} + \sigma_{--})}{(\sigma_{++} + \sigma_{-+} + \sigma_{+-} + \sigma_{--})(-\sigma_{++} + \sigma_{-+} + \sigma_{+-} - \sigma_{--})}}$$



- Blondel scheme independent of polarimeter precision
 - Assumes perfect spin flip for polarised beams
 - Residuals must be monitored by polarimeter
 - Residual uncertainty of $\Delta A_{LR} = 0.5 \times 10^{-4}$ seems possible
 - The more positron polarisation the better
 - Don't forget energy dependency ($dA_{LR}/d\sqrt{s} \sim 2 \times 10^{-5}/\text{MeV}$)
 - 1 MeV precision on \sqrt{s} seems possible (see above)
- Precision $\Delta A_{LR} = 1 \times 10^{-4}$ is a realistic assumption for GigaZ

$$\Rightarrow \delta \sin^2\theta_{\text{eff}}^{\ell} \sim 1.3 \cdot 10^{-5}$$

- Radiative return
 - Mainly limited by statistics $\Delta A_{LR} = 1.4 \times 10^{-4}$
 - Beam polarisation better than $\Delta A_{LR} = 0.5 \times 10^{-4}$ (More processes available)
 - Energy dependence much weaker than on Z-pole

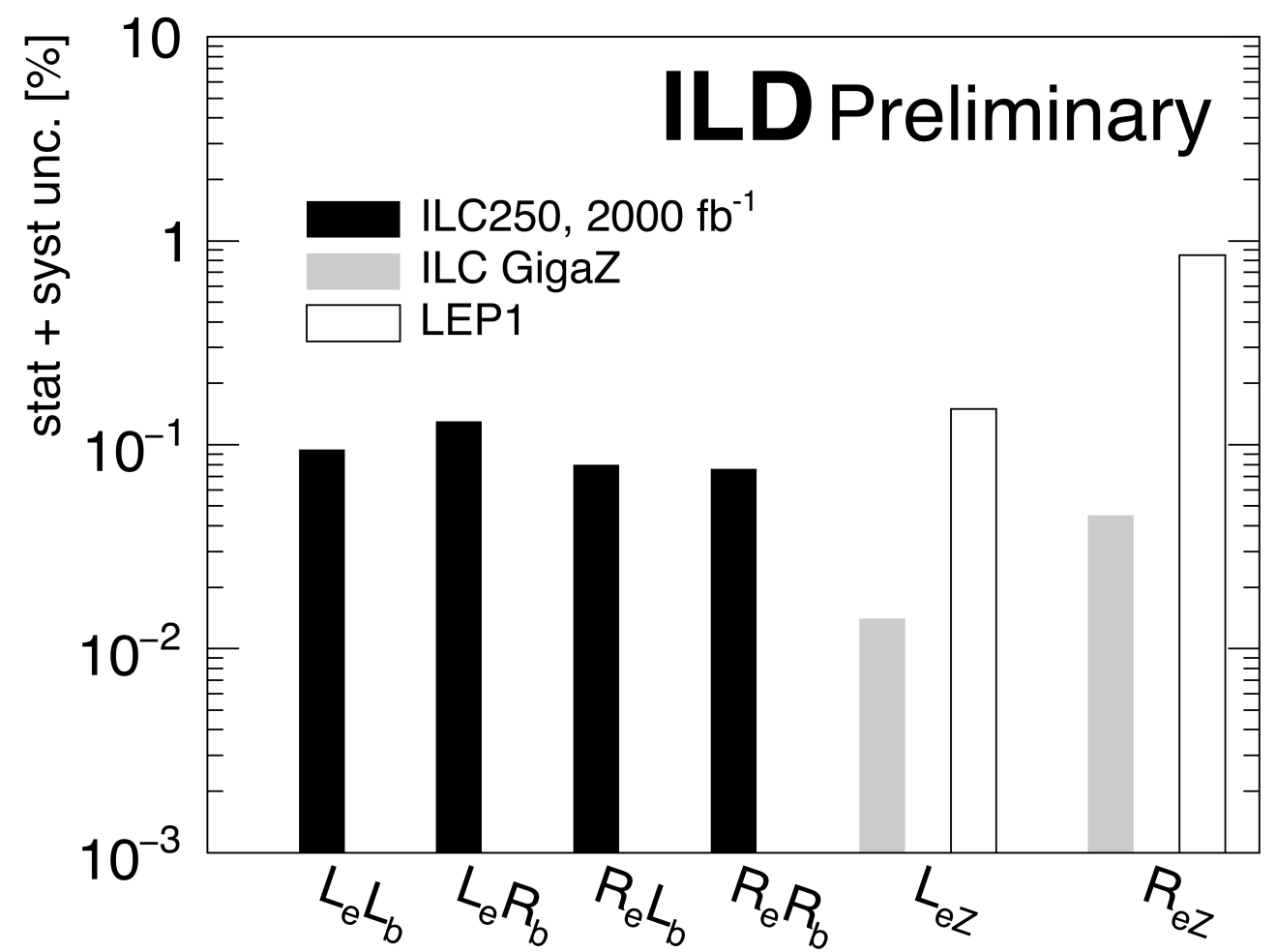


- Z pole running of ILC will improve significantly precision w.r.t. LEP/SLD
- Precise measurement of $\sin^2 \theta_{\text{eff}}^l$.
 - Around 13 times better than LEP/SLD and a factor three better than current world average
- Considerable improvement of fermion asymmetries A_f
 - e.g.: arXiv: 1908.11299
 - $\Delta A_b / A_b \sim 5 \times 10^{-4}$ (compare with $\Delta A_b / A_b \sim 214 \times 10^{-4}$ today)
 - $\Delta A_c / A_c \sim (5 \oplus 5) \times 10^{-4}$ (compare with $\Delta A_c / A_c \sim 404 \times 10^{-4}$ today)
 - For completeness note that a statistical error of 10^{-4} has been assumed for A_b and 3×10^{-4} for A_c
- Main error source
 - Knowledge of beam polarisation
 - QCD corrections that dilute forward backward asymmetry (arXiv:2010.08604) not considered but about to be looked at (once more)

From Slide 7 it follows

$$\frac{\sigma_{A_f}}{A_f} = \frac{\sigma_{\tilde{A}}}{\tilde{A}} \oplus \frac{\sigma_x}{x} \quad \text{with } \tilde{A} = A_{FB}, A' \text{ and } x = P_{eff.}, A_e$$

- $\sigma_{P_{eff}}/P_{eff} = 5 \times 10^{-4}$ assumed for ILC (most likely pessimistic)
- $\sigma_{A_e} = 0.000022$ absolute error (see Alacaraz Slide 9, <https://indico.fnal.gov/event/51940/>)
- $\Rightarrow \sigma_{A_e}/A_e = 0.00002/0.1511 \sim 1.4 \times 10^{-4}$
- Systematic errors on “analysis power” A_e and P_{eff} may considered to be comparable
- Dilution due to QCD effects on A_{FB} . Effect can be controlled at $\Delta A_{FB} \sim 10^{-4}$ (arXiv:2010.08604)
 - **Using “current theoretical knowledge”**
 - $\Rightarrow \sigma_{AFB}/A_{FB} \sim 0.0001/0.1 \sim 10^{-3}$
 - QCD dilution is independent of beam polarisation and may influence A' in the same way as A_{FB}
- **A relative error of 10^{-3} would be the dominant error source in both cases**
 - Remark: In 2019 I have used Table 2 of <https://arxiv.org/pdf/hep-ex/0410042.pdf> which in turn (on QCD corrections) made use of Table 15 of <http://cds.cern.ch/record/426819/files/ep-2000-016.pdf> and references therein
 - At the time I went through the papers and references and have indeed supposed, with some reasoning, that the QCD corrections will become subdominant w.r.t. the error on polarisation



$$LeLb = Q_e Q_b + \frac{LeZLbZ}{s^2 w c^2 w} BWZ + \sum_{Z'} \frac{LeZ'LbZ'}{s^2 w c^2 w} BWZ'$$

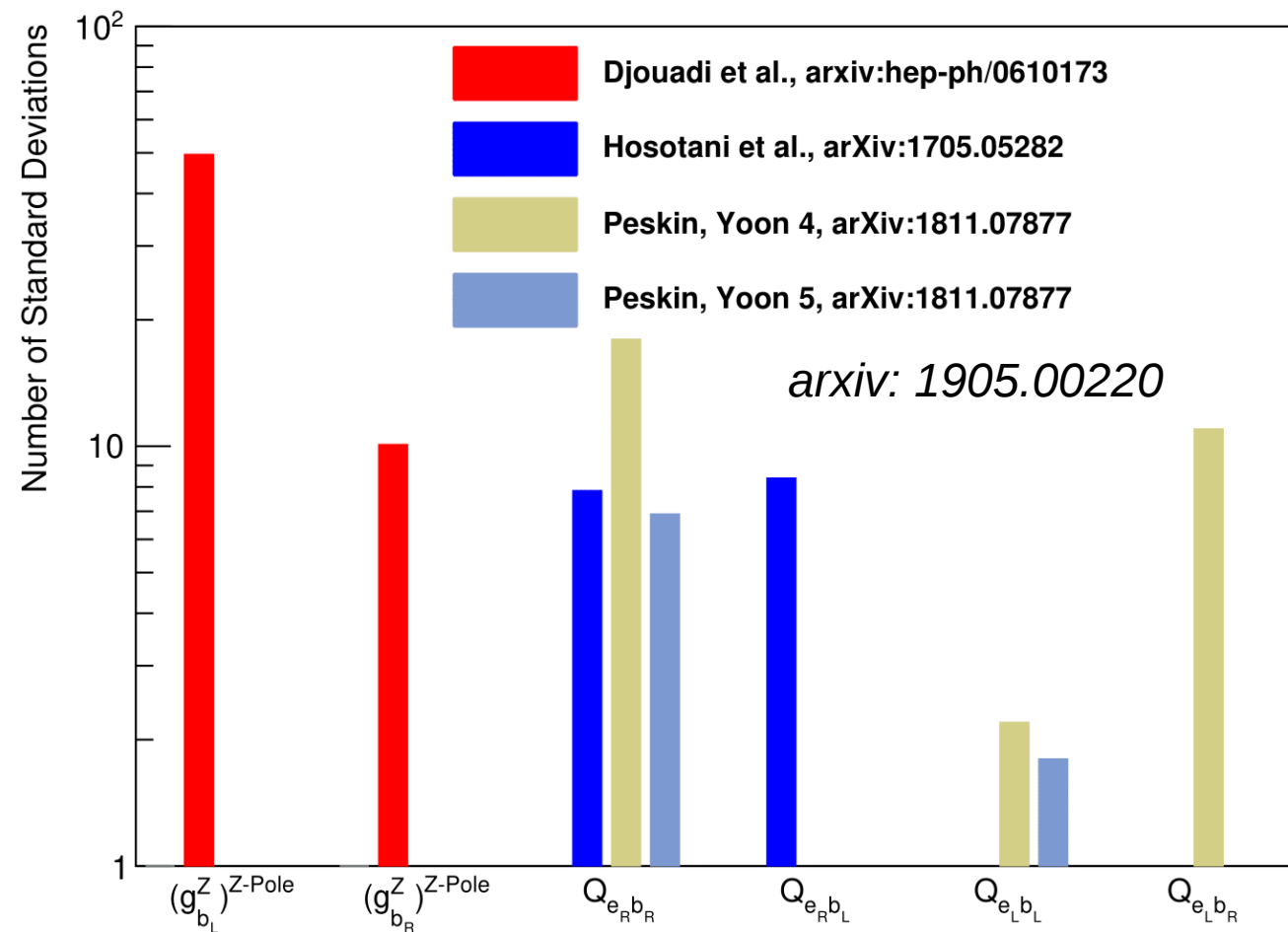
Arrows point from the terms to labels:

- Blue arrow from $Q_e Q_b$ to ILC250
- Blue arrow from $\frac{LeZLbZ}{s^2 w c^2 w} BWZ$ to SM
- Blue arrow from $\frac{LeZ'LbZ'}{s^2 w c^2 w} BWZ'$ to GigaZ
- Red arrow from the sum term to New resonances

- Couplings are order of magnitude better than at LEP
 - In particular right handed couplings are much better constrained
- New physics can also influence the Zee vertex
 - in 'non top-philic' models
- **Full disentangling of helicity structure for all fermions only possible with polarised beams!!**

Figure: A. Irles

Example: b couplings and helicity amplitudes



- Spectacular sensitivity to new physics in Randall Sundrum Models with warped extra dimensions
 - **Complete tests only possible at LC**
 - **Discovery reach $O(10 \text{ TeV})@250 \text{ GeV}$ and $O(20 \text{ TeV})@500 \text{ GeV}$**
- Pole measurements critical input
 - Only poorly constrained by LEP
- Pole measurements will (most likely) influence also top electroweak precision program
 - (t,b) doublet



- **ILC is electroweak precision machine**
 - Electroweak parameters are limited by systematics, not statistics
 - High precision measurements of $M_{Z'}$, $\Gamma_{Z'}$, $M_{W'}$, $\Gamma_{W'}$, M_t and $\sin^2\theta_{\text{eff}}^\ell$.
- **ILC can (should) be run on the Z-pole**
 - Electroweak precision observables deliver decisive input for interpretation at higher energies
- **Full exploitation of physics potential by large energy coverage and polarised beams**
 - Clean model independent measurements due to beam polarisation
 - Tests of lepton universality
 - Measurement of patterns for indirect discovery of new physics
 - Spectacular mass reach for new physics already at 250 GeV demonstrated
 - Flexibility of beam energy allows for systematic tracing of the onset of new physics

Main challenge at future machines will be the control of systematic errors

- Experimentally (non exhaustive list)
 - Vertex charge and particle ID
 - PFO for final state jets
 - Beam energy and polarisation
- Theoretically (not discussed)
 - Need at least NLO electroweak predictions (and MC programs) for correct interpretation of results
 - α_s



1. Can m_W be measured well at center-of-mass energies above ZH production threshold? For ILC this needs a more detailed look with a full kinematic fit to $qq\nu$ events including effects of luminosity spectrum. These events have m_W information from both W's.

Acceptance?

1b. Is it really necessary to use the WW threshold for theoretical reasons?

2. Ultimate precision on center-of-mass energy using radiative return events especially in case momentum-scale systematics dominate \sqrt{s} . Important for Higgs mass, top mass, and W mass.

3. Detector requirements for Z pole observables.

Forward acceptance for $e^+e^- \rightarrow q\bar{q}$ is very important.

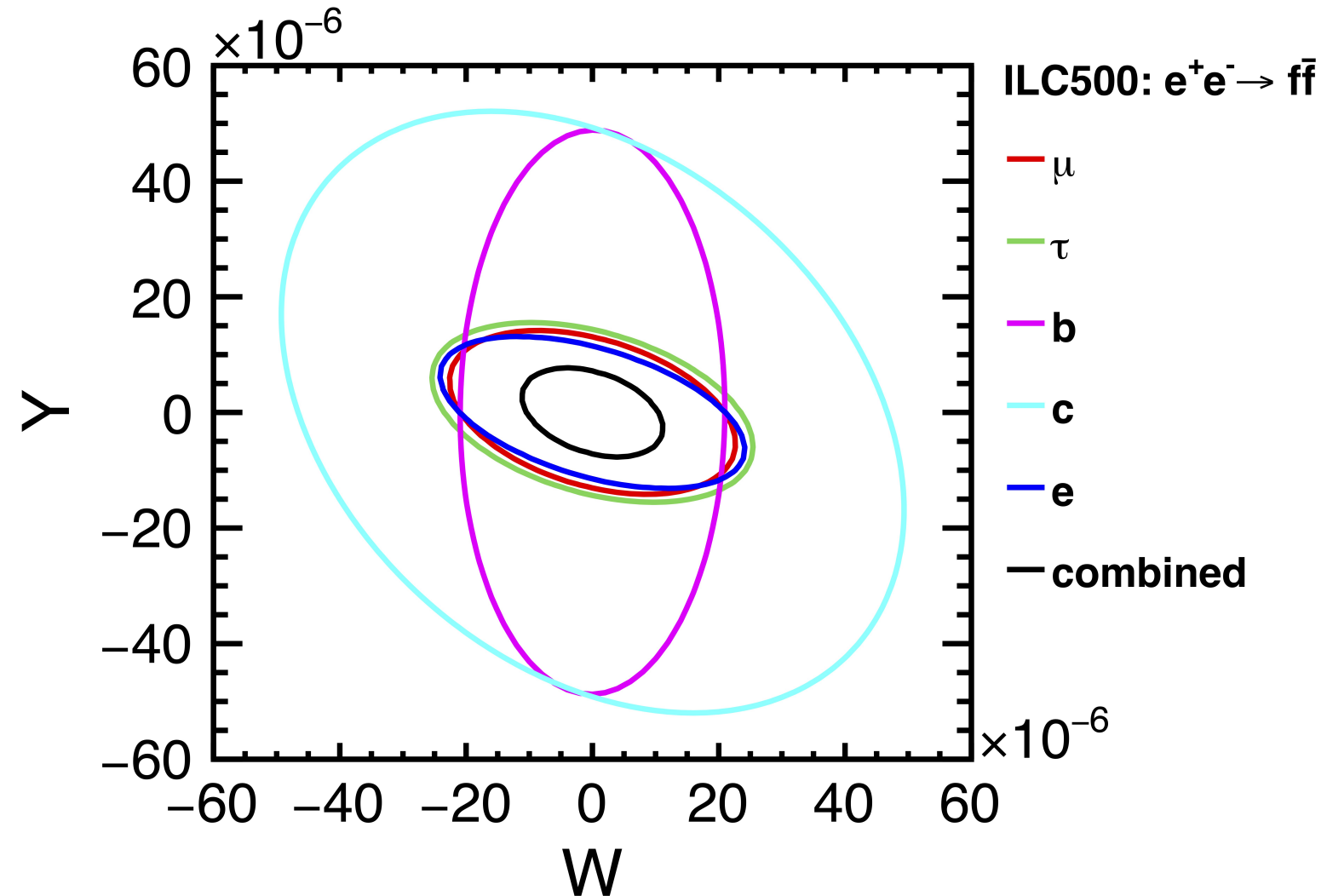
4. Can the background be controlled well enough

for m_W from threshold measurements. Especially for 4-jet case, and without both beams being polarized.

5. Can $\gamma\gamma \rightarrow$ hadrons background be controlled at the Z peak?

Backup

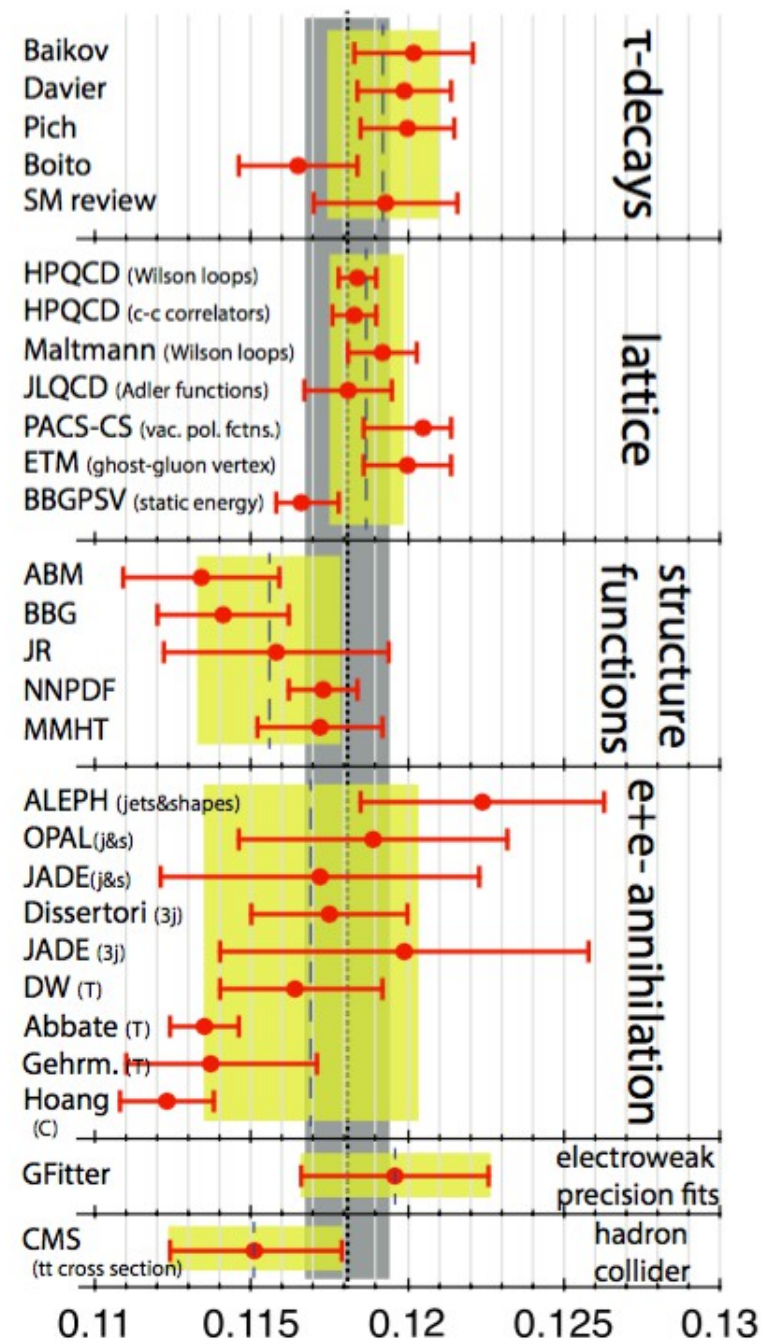
Contributions for different fermion species



\sqrt{s}	ΔW	ΔY	ρ
HL-LHC	15×10^{-5}	20×10^{-5}	-0.97
ILC250	3.4×10^{-5}	2.4×10^{-5}	-0.34
ILC500	1.1×10^{-5}	0.78×10^{-5}	-0.35
ILC1000	0.39×10^{-5}	0.27×10^{-5}	-0.38
500 GeV, no beam pol.	2.0×10^{-5}	1.2×10^{-5}	-0.78

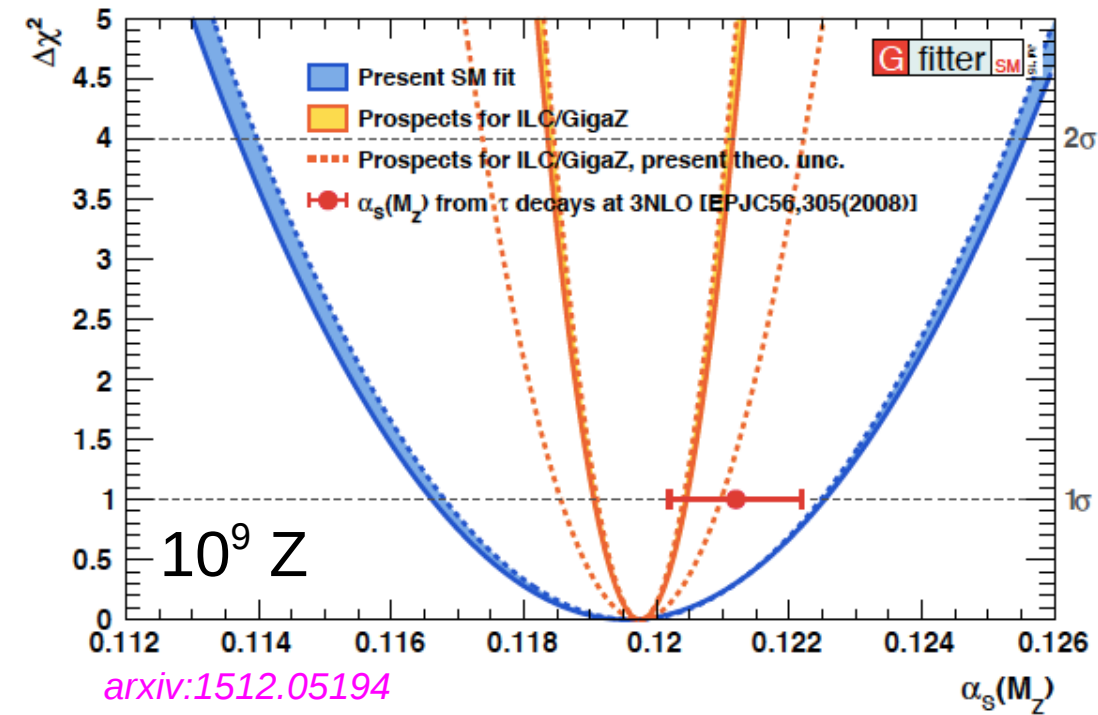
- Beam polarisation essential to disentangle effects from W and Y
- ILC250 outperforms LHC
- ILC500 and above outperforms e^+e^- machines w/o polarisation (at $4ab^{-1}$)

Current status



Dominated by lattice QCD

Prospects Z-running



Slide made in 2016!

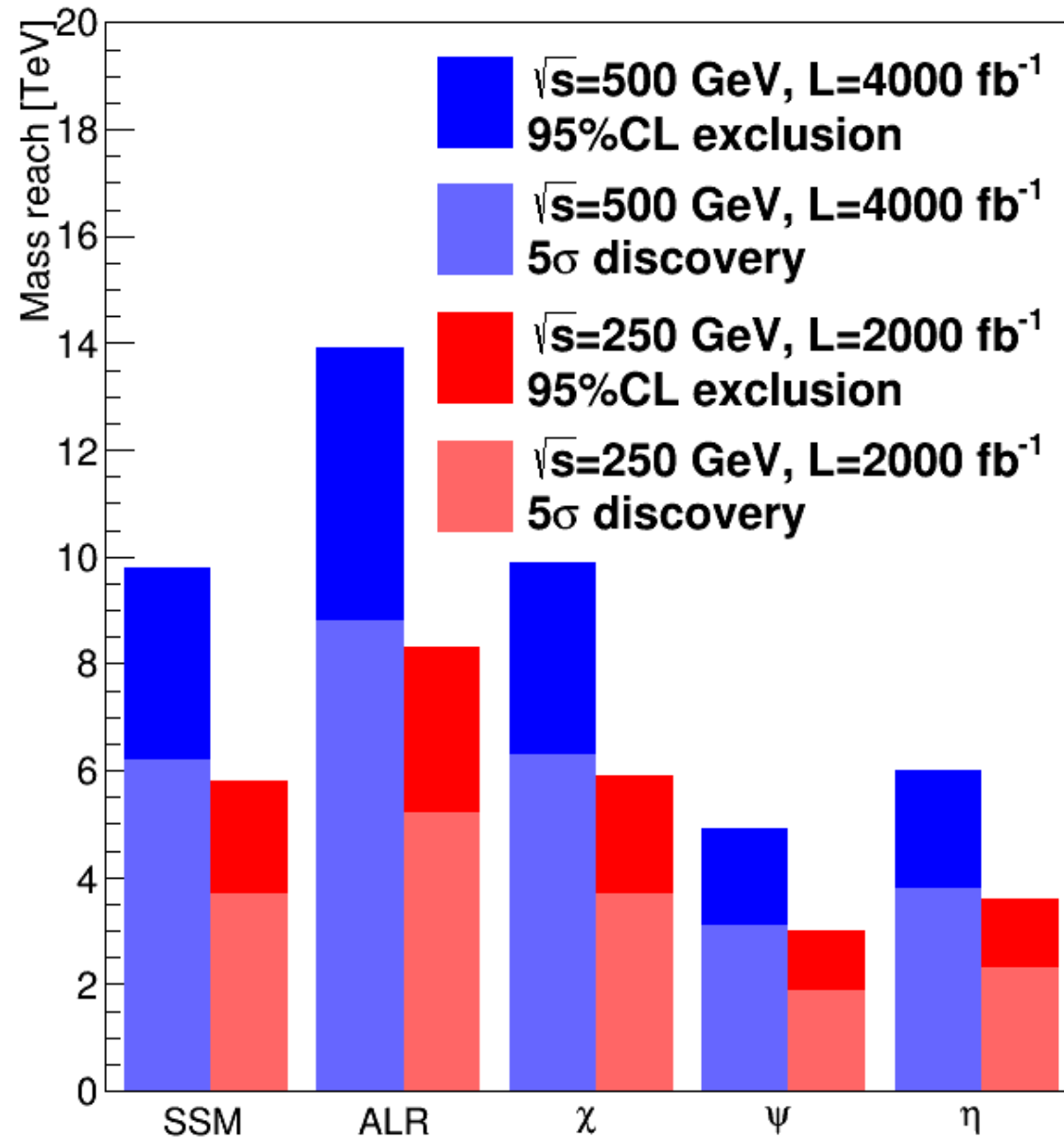
Electroweak fit with updated EWPO and theory uncertainties

$$\delta \alpha_s(M_Z) \sim 0.0007 \text{ for } 10^9 Z$$

$$\delta \alpha_s(M_Z) \sim 0.0003(16) \text{ for } 10^{12} Z$$

Prospects Lattice

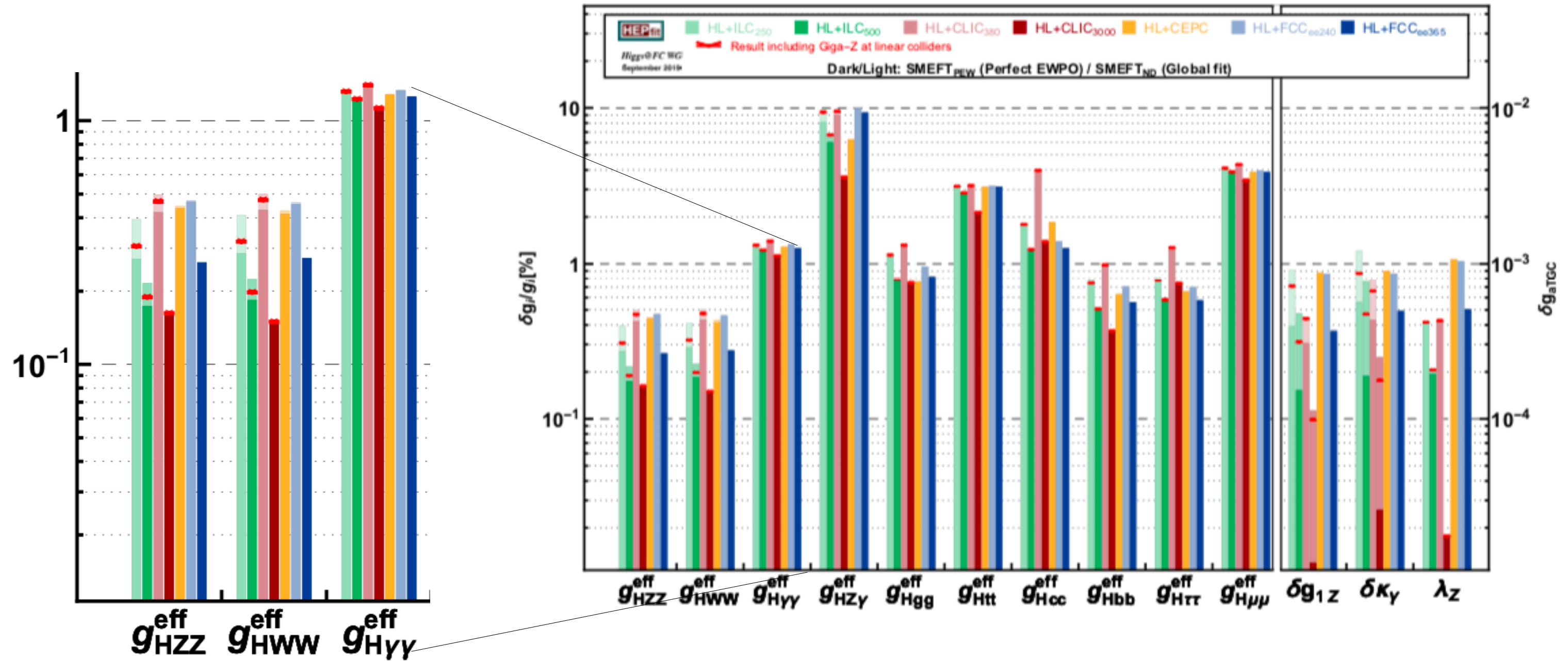
$$\delta \alpha_s(M_Z) \sim 0.0003$$

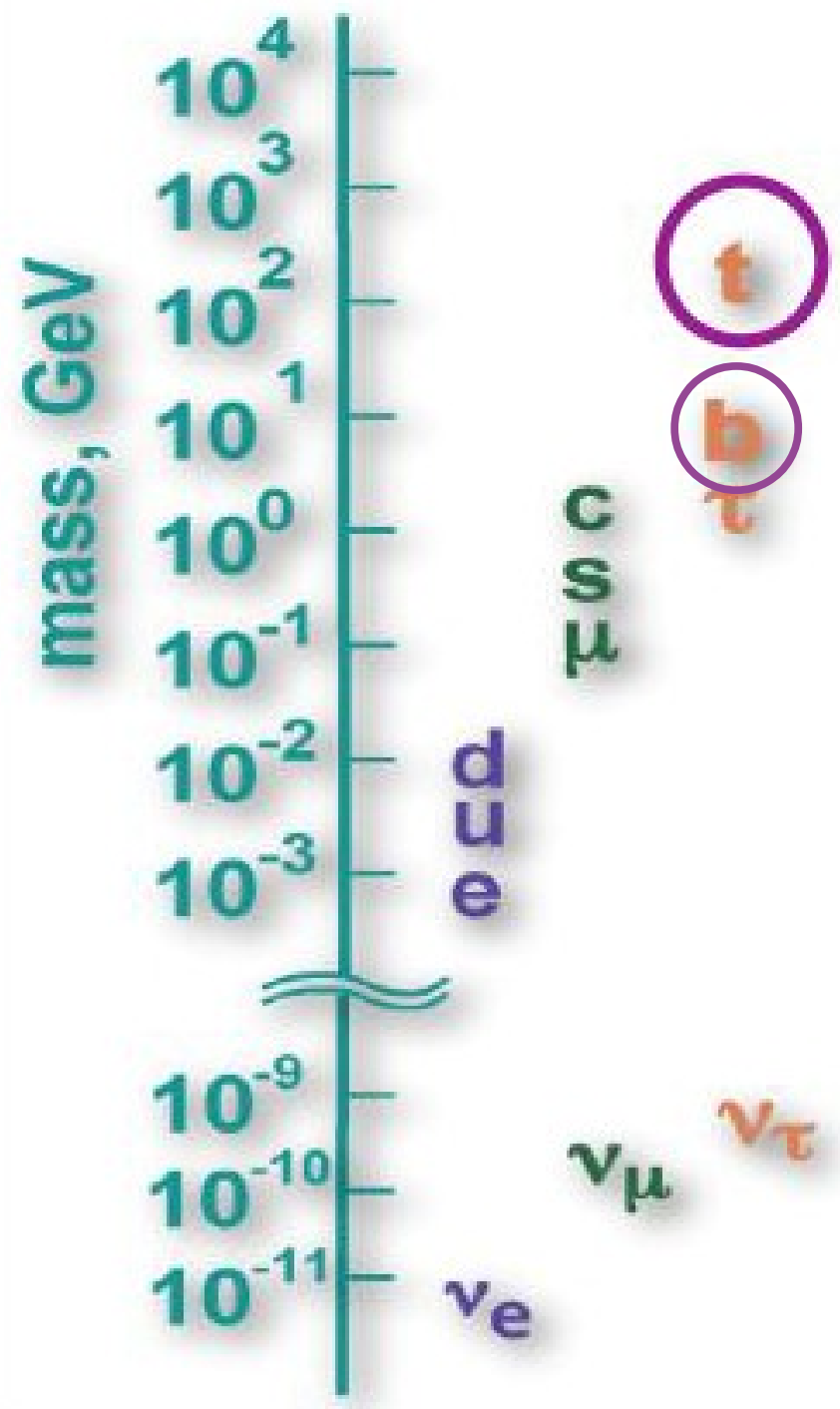


- SSM is “carbon” copy of SM Z and used as common metric in generic Z' searches
- ALR introduces an “ad hoc” $SU(2)_R$ and a Z' with orthogonal couplings to the fermions
- X, ψ, η are linear combinations of bosons appearing in Grand Unified Theories with couplings orthogonal to the SM

Typical mass reach 5-10 TeV

- Reach shown for e, μ, τ
- Adding quarks would improve limits





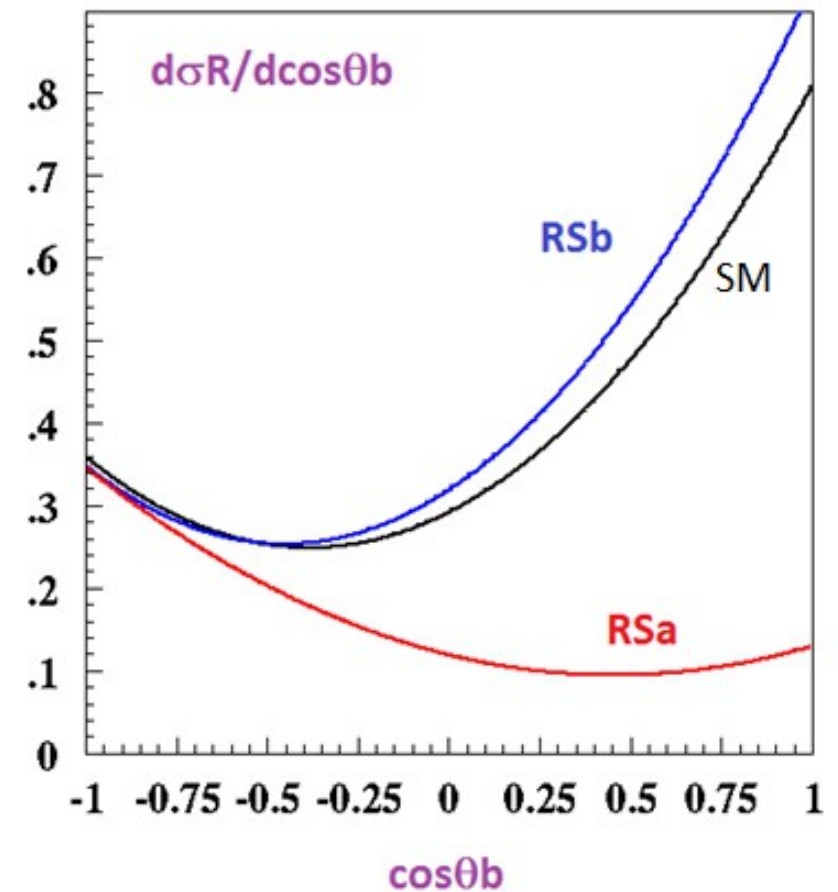
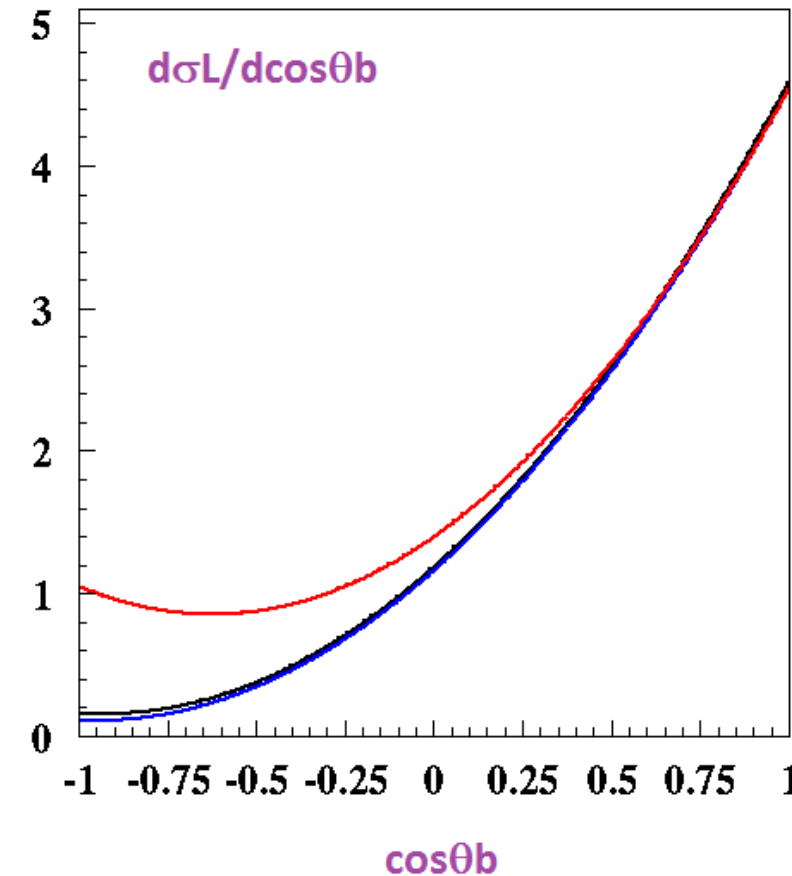
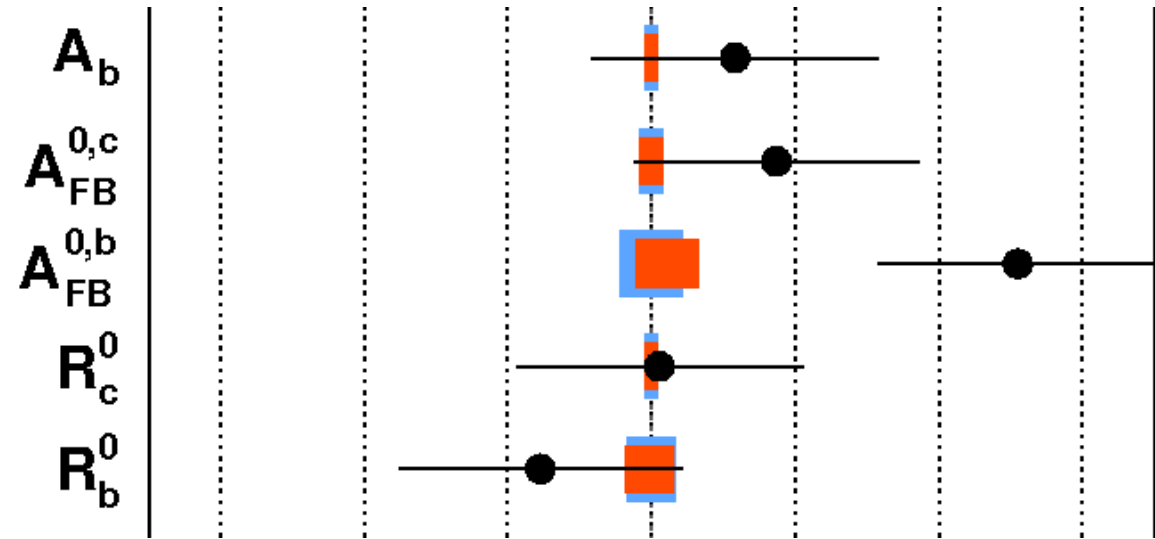
- SM does not provides no explanation for mass spectrum of fermions (and gauge bosons)
- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale

$$\begin{pmatrix} t \\ b \end{pmatrix}_L$$

Strong motivation to study chiral structure of heavy quark vertices in high energy e+e- collisions

$\sim 3\sigma$ in heavy quark observable A_{FB}^b

$ee \rightarrow b\bar{b}$ @ 250 GeV



- Is tension due to underestimation of errors or due to new physics?

- High precision e^+e^- collider will give final word on anomaly

- In case it will persist polarised beams will allow for discrimination between effects on left and right handed couplings

- Randall Sundrum Models generate basically automatically a symmetry group of type $SU(2)_R$

Randall Sundrum Models Djouadi/Richard '06



	\sqrt{s}	beam polarisation	$\int L dt$ for Higgs	R&D phase
ILC	0.1 - 1 TeV	e-: 80% e+: 30%	2000 fb-1 @ 250 GeV 200 fb-1 @ 350 GeV 4000 fb-1 @ 500 GeV	TDR completed in 2013
CLIC	0.35 - 3 TeV	e-: (80%) e+: 0%	1000 fb-1 @ 380 GeV 2500 fb-1 @ 1.5 TeV 5000 fb-1 @ 3 TeV	CDR completed in 2012
CEPC	90 - 240 GeV	e-: 0% e+: 0%	5600 fb-1 @ 240 GeV	CDR completed in 2018
FCC-ee	90 - 350 GeV	e-: 0% e+: 0%	5000 fb-1 @ 250 GeV 1700 fb-1 @ 350 GeV	CDR completed in Jan 2019

Details see talk by Y. Okada

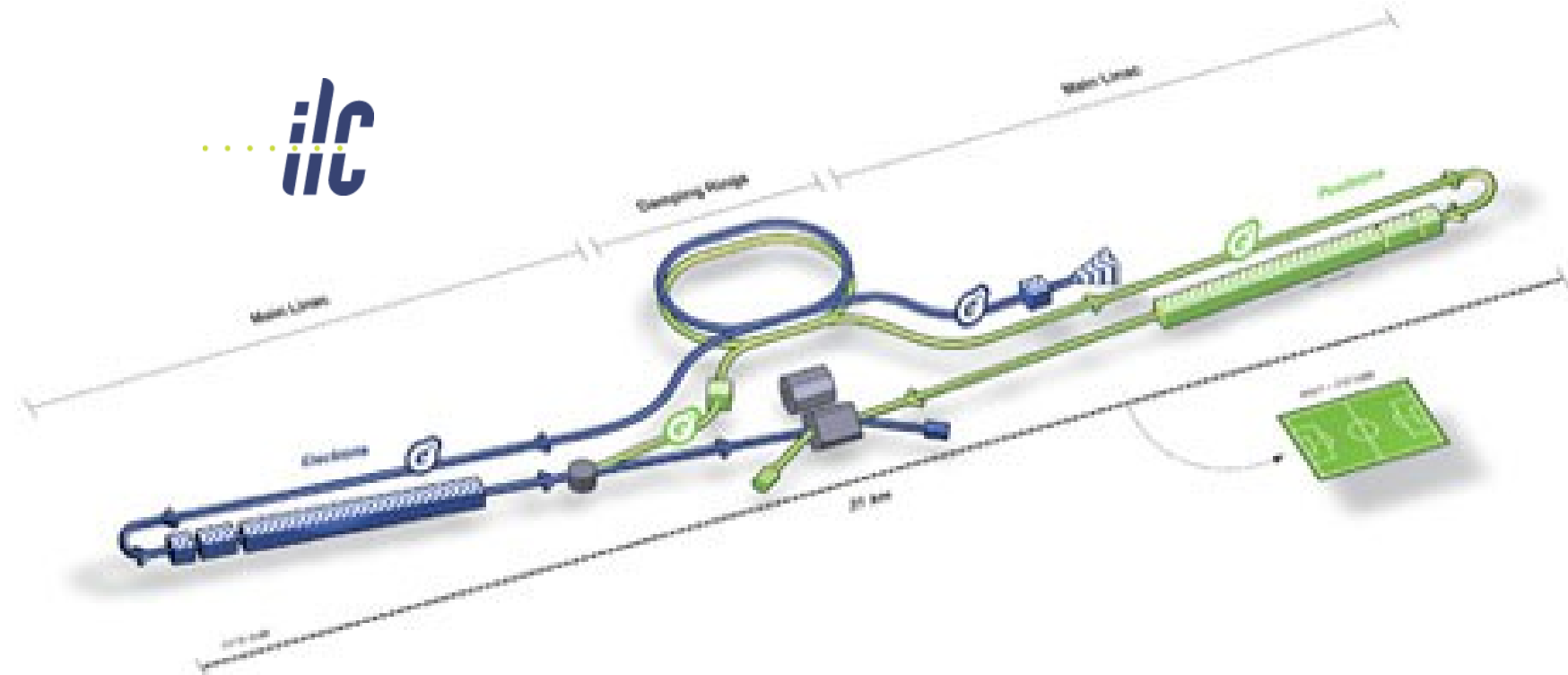
Details see talk by M. Ruan

Table courtesy of J. Brau

Open questions



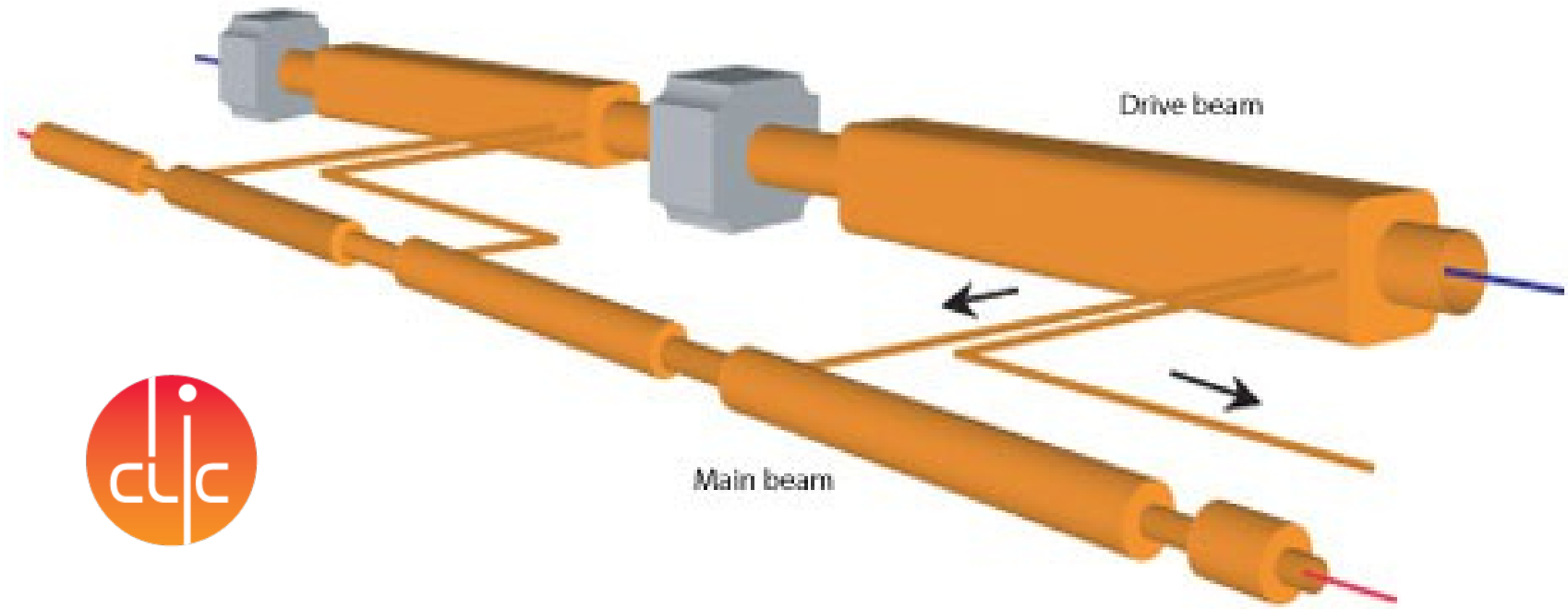
Linear Electron-Positron Colliders



Energy: 0.1 - 1 TeV
Electron (and positron)
polarisation
TDR in 2013
+ DBD for detectors
 Footprint 31 km

Initial Energy 250 GeV – Footprint ~20km

Japanese Government expressed its interest in project in March 2019



Energy: 0.4 - 3 TeV
CDR in 2012
 Footprint 48km
 Initial Energy 380 GeV

EFT: Two distinct observations

Observables at fixed mass m
(e.g. Z pole of Higgs decays)

$$\frac{\sigma}{\sigma_{SM}} \approx \left| 1 + \frac{c_6 m^2}{\Lambda^2} \right|^2$$

Increasing UV scales probed in EFT
achieved solely by increasing the
measurement precision

$$c_6 \sim (g^*)^2$$

Typical experimental precision 0.1-1%

High energy tails of distributions
(e.g. Drell-Yan Productions)

$$\frac{\sigma}{\sigma_{SM}} \approx \left| 1 + \frac{c_6 E^2}{\Lambda^2} \right|^2$$

Increasing UV scales probed in EFT
achieved solely by increasing the
energy scale of measurement precision

Typical experimental precision 10%

- Polarized beams play a crucial role in disentangling the two spin structures

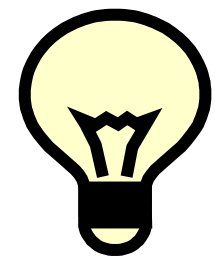
$$\sigma = \frac{2}{3} \frac{\pi \alpha_w^2}{c_w^4} \frac{m_Z^2}{(s - m_Z^2)} \frac{2k_Z}{\sqrt{s}} \left(2 + \frac{E_Z^2}{m_Z^2}\right) \cdot Q_Z^2 \cdot \left[1 + 2a + 2 \frac{3\sqrt{s}E_Z/m_Z^2}{(2 + E_Z^2/m_Z^2)} b\right]$$

The **a** and **b** coefficients depend on beam polarization:

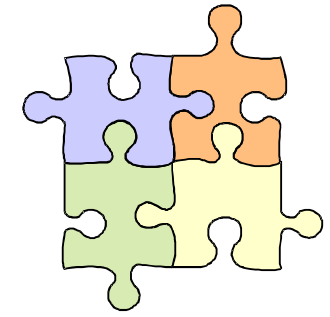
$$\begin{aligned}
 e_L^- e_R^+ & \quad Q_{ZL} = \left(\frac{1}{2} - s_w^2\right), \quad a_L = -c_H \\
 & \quad b_L = c_w^2 \left(1 + \frac{s_w^2}{1/2 - s_w^2} \frac{s - m_Z^2}{s}\right) (8c_{WW})
 \end{aligned}$$

$$\begin{aligned}
 e_R^- e_L^+ & \quad Q_{ZR} = (-s_w^2), \quad a_R = -c_H \\
 & \quad b_R = c_w^2 \left(1 - \frac{s - m_Z^2}{s}\right) (8c_{WW})
 \end{aligned}$$

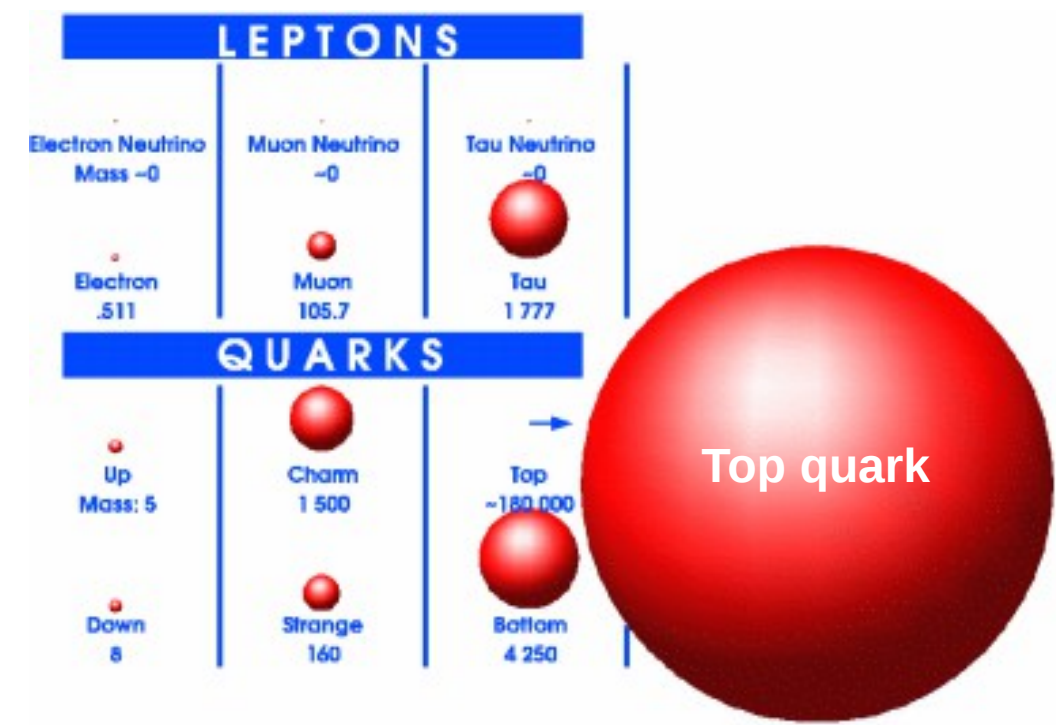
- Angular distributions in $e^+e^- \rightarrow hZ$ can also be used, but have weaker analyzing power and require more luminosity to achieve the same result



Elementary Scalar?



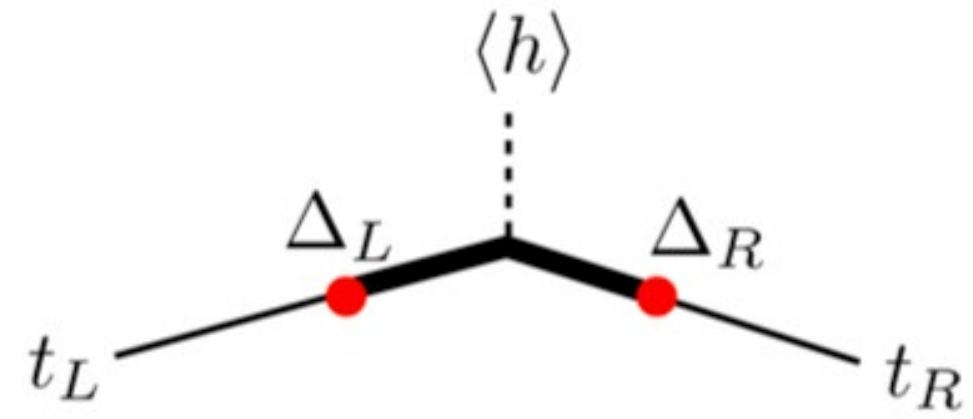
Composite object?



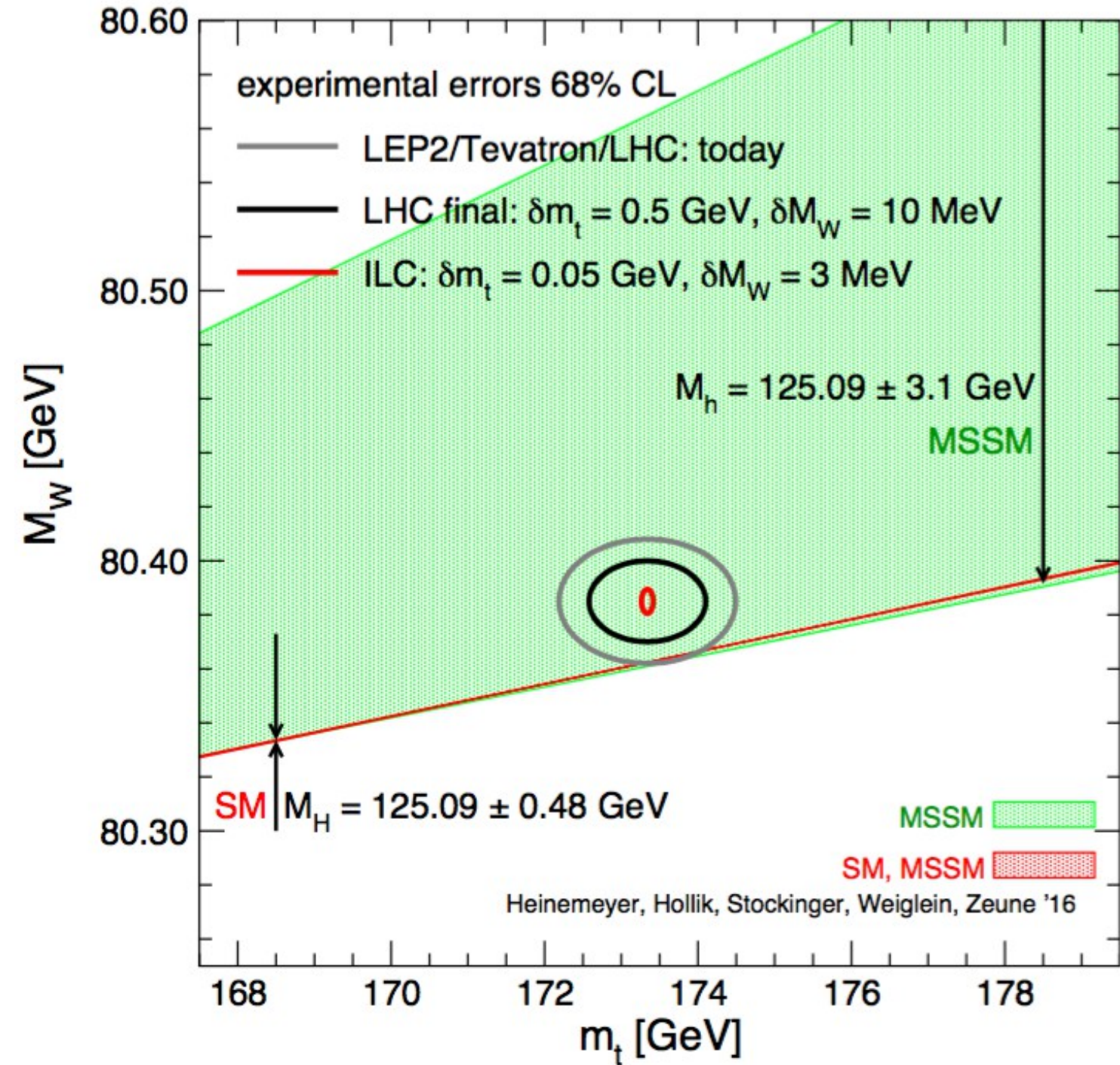
- Higgs and top quark are intimately coupled!
Top Yukawa coupling $O(1)$!
=> Top mass important SM Parameter

- New physics by compositeness?
Higgs and top composite objects?

- e+e- collider perfectly suited to decipher both particles

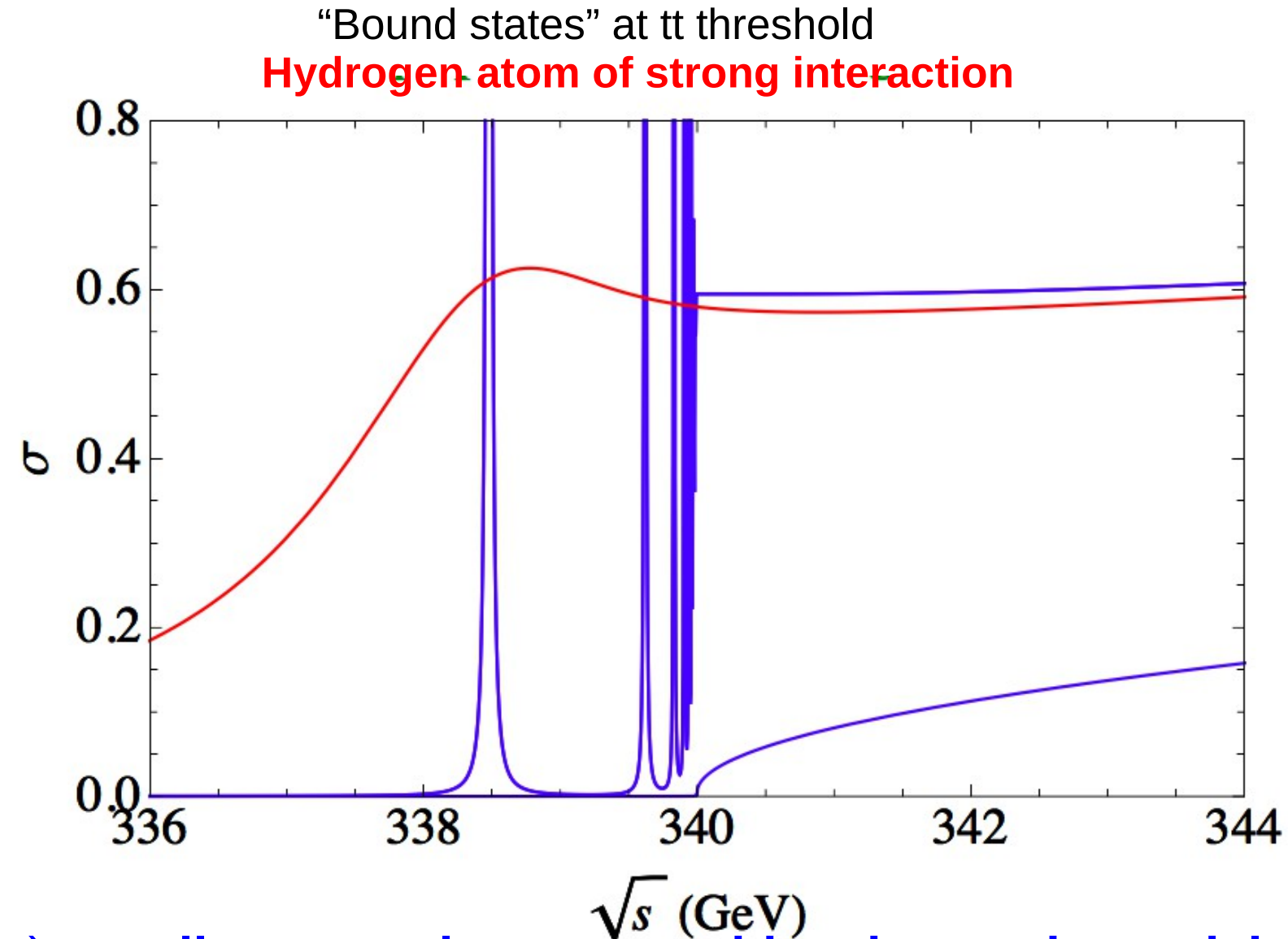


Courtesy of S. Rychkov



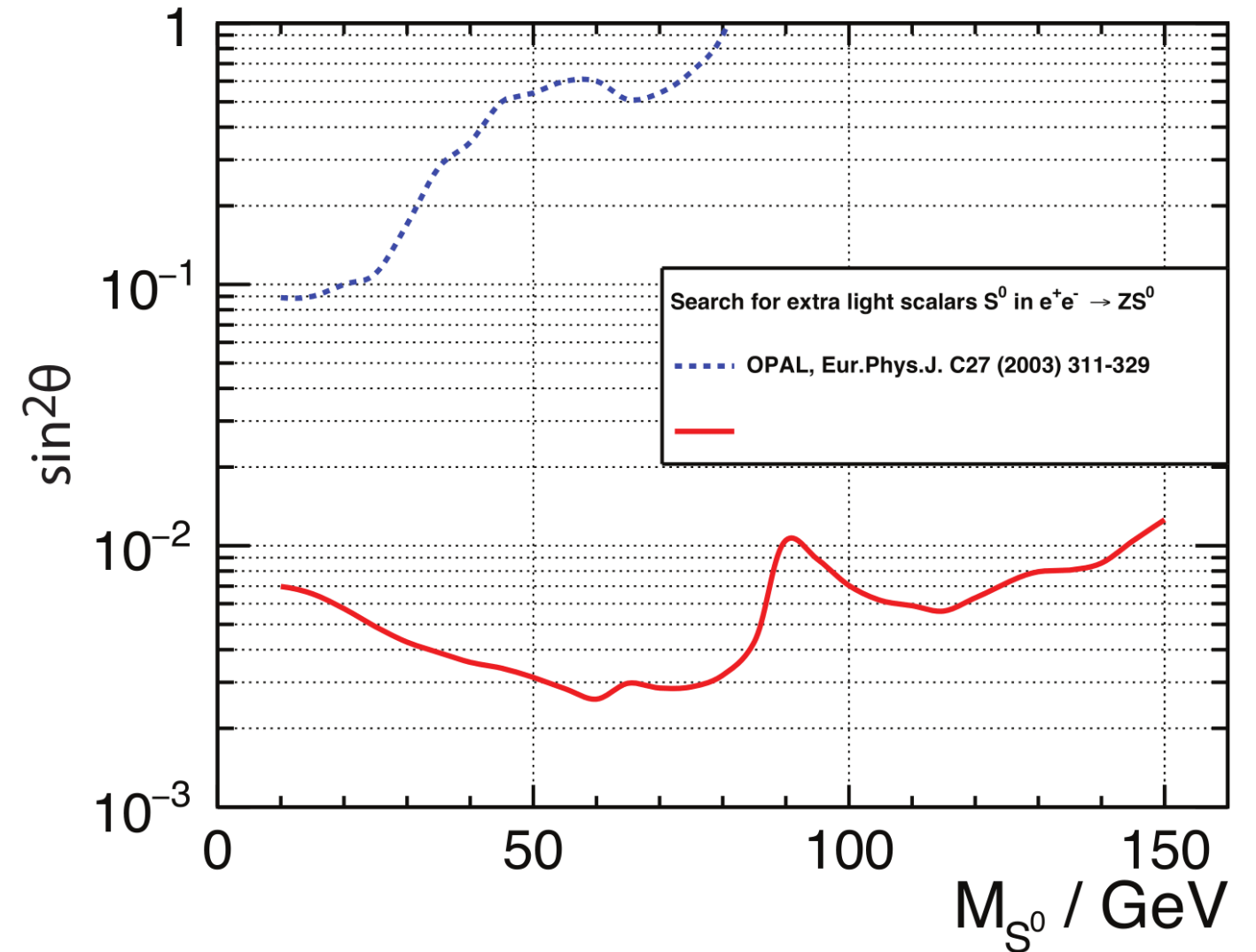
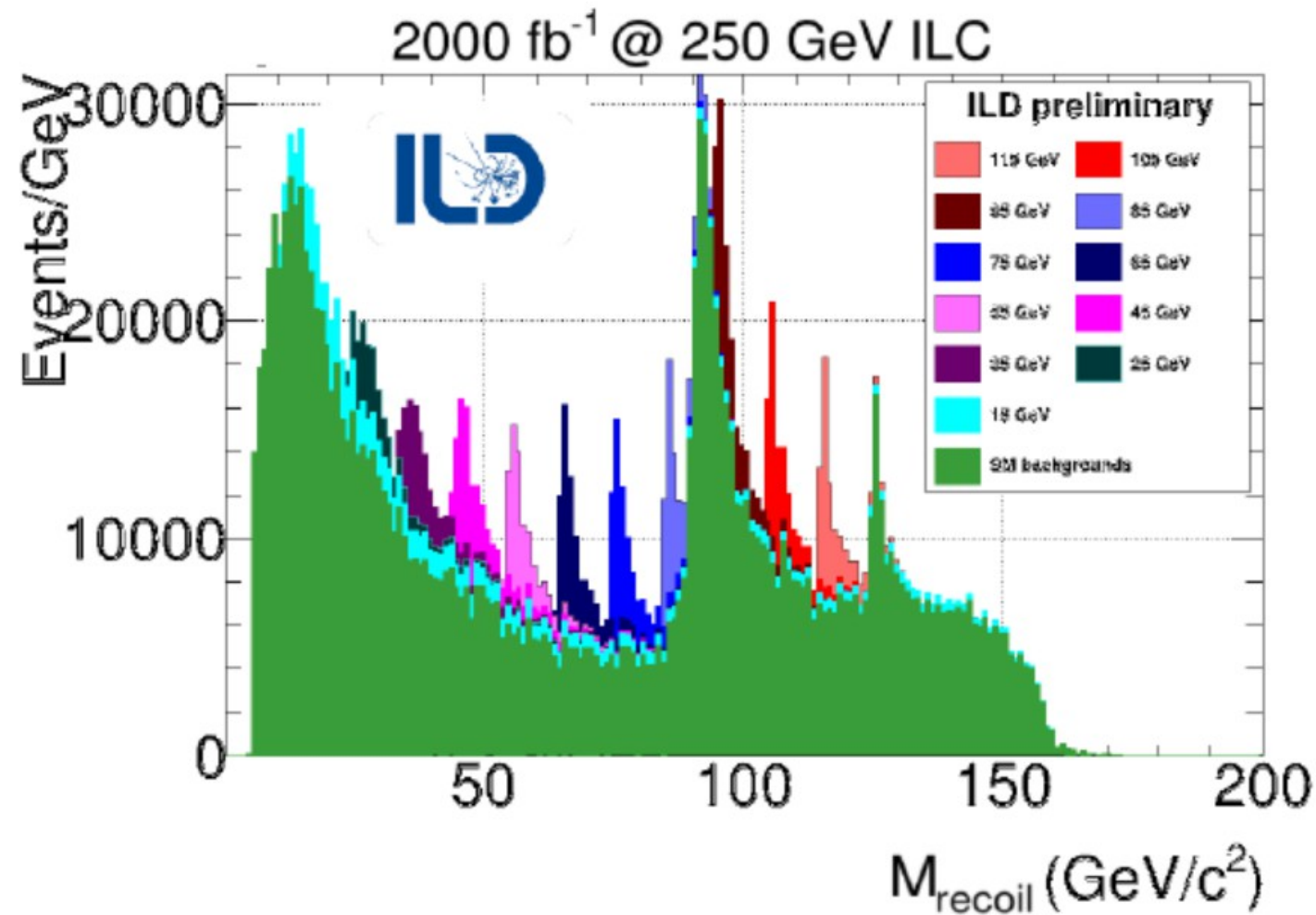
- Precise Top (and W) mass crucial to test compatibility of measured Higgs mass
- SM might not be sufficient to explain Higgs mass
- LHC may not reach sufficient discriminative power
- A lepton collider will for sure

Top pair production at threshold



- Size $O(10^{-17}\text{m})$, **smallest non-elementary object known in particle physics**
 Small scale \Rightarrow Free of confinement effects \Rightarrow Ideal premise for precision calculations
 Measurement of (a hypothetical) 1^3S_1 State
- Decay of top quark smears out resonances in a well defined way

Light scalar may be missing piece to trigger first order 1st transition and/or the being the radion in extra dimension theories

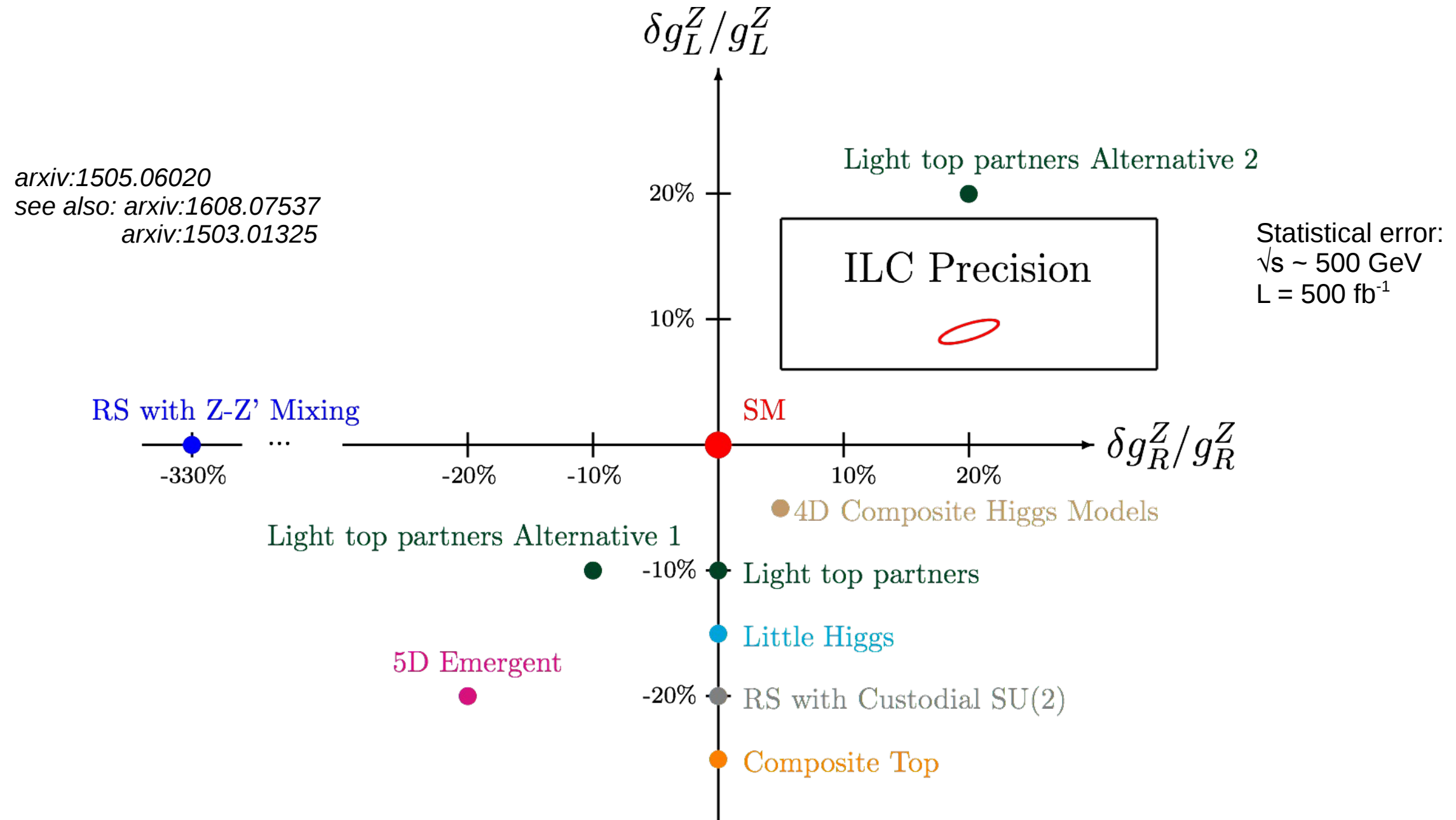


- New resonances cleanly distinguishable for large range of masses
- Sensitivity to mixing angle θ down to 10^{-2} (taking all relevant backgrounds into account)
- ^Lnew scalar would count as “Feebly interacting Particle” (FIPS)

Electroweak top couplings

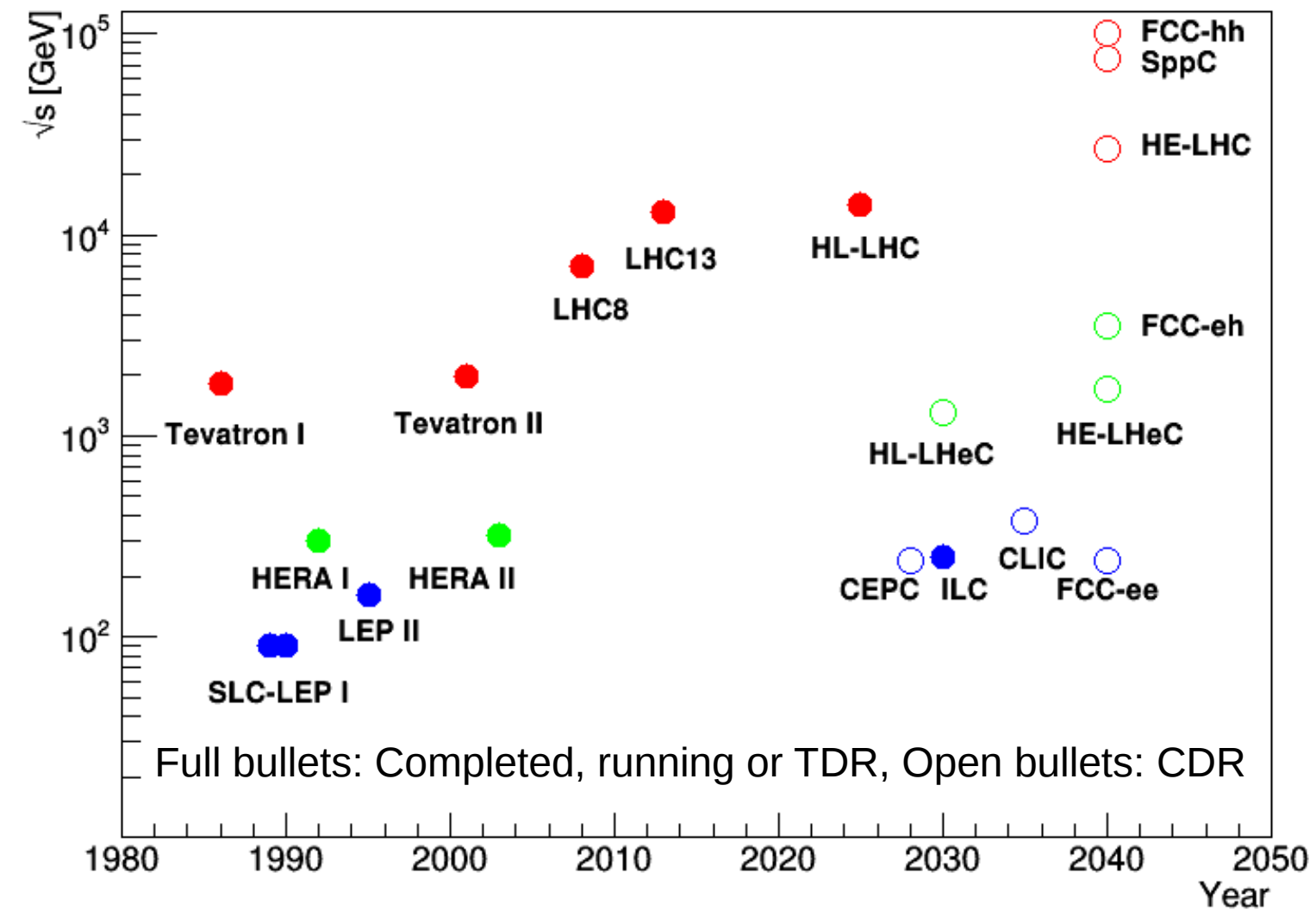


Top is primary candidate to be a messenger new physics in many BSM models



Precision expected for top quark couplings will allow to distinguish between models

Remark: All presented models are compatible with LEP elw. precision data



- ILC is the only machine that can be built now
 - European XFEL gives credibility for construction