

Indirect constraints on Top Quark operators

Based on «Indirect constraints on top quark operators from a global SMEFT analysis»

F. Garosi, D. Marzocca, A. Rodriguez-Sanchez, A. Stanzione [2310.00047] *JHEP* 12 (2023) 129



EFT framework

We work within the **(SM)EFT** framework: higher-dim operators built out of the SM fields and allowed by its symmetries (plus B and L conservation)

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots \quad \text{e.g.}$$

$$\mathcal{O}_{Hq}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{q}^3 \gamma^\mu q^3)$$

$$\mathcal{O}_{\ell q}^{(1), \alpha\beta} = (\bar{\ell}^\alpha \gamma_\mu \ell^\beta) (\bar{q}^3 \gamma^\mu q^3)$$

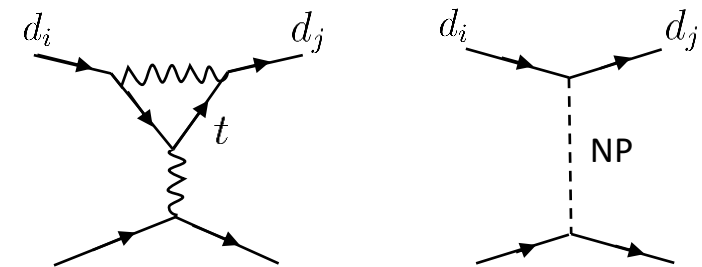
$$\mathcal{O}_{qq}^{(1)} = (\bar{q}^3 \gamma^\mu q^3) (\bar{q}^3 \gamma_\mu q^3)$$

$$\mathcal{O}_{uW} = (\bar{q}^3 \sigma^{\mu\nu} u^3) \tau^a \tilde{H} W_{\mu\nu}^a$$

Top-philic assumption: only top quark operators generated at tree level, i.e. 19 SMEFT operators up to flavour indices (including LFV cases)

B. Grzadkowski, M. Iskrzynski, M. Misiak, J. Rosiek [1008.4884]

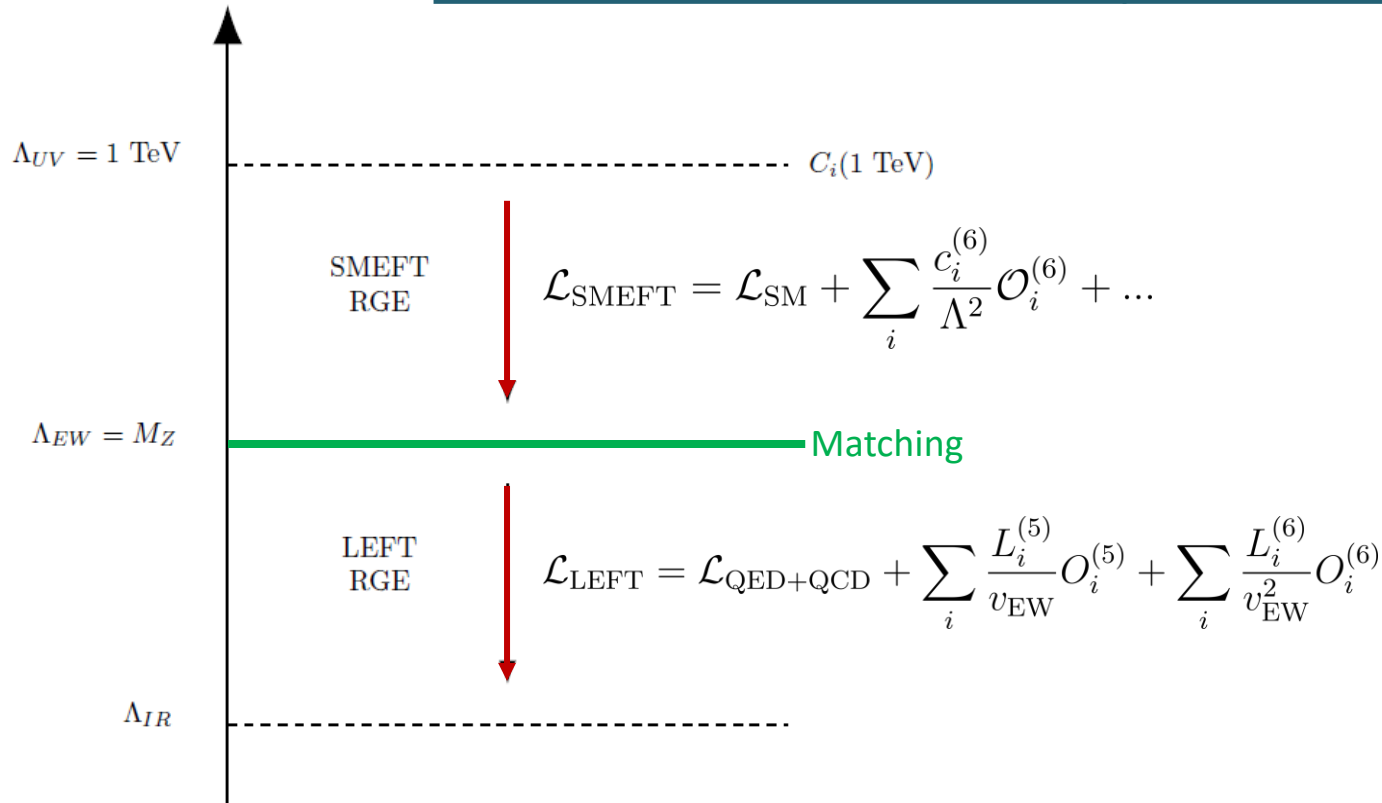
We work in the up-type quark basis $q^i = (u_L^i, V_{ij} d_L^j)$:
 FCNC $d_L^i \rightarrow d_L^j$ processes allowed at tree level, suppressed by $V_{tj}^* V_{ti}$ factors



SMEFT operators

| Semi-leptonic | | Four quarks | |
|--|---|--------------------------|---|
| $\mathcal{O}_{lq}^{(1),\alpha\beta}$ | $(\bar{l}^a \gamma_\mu l^\beta)(\bar{q}^3 \gamma^\mu q^3)$ | $\mathcal{O}_{qq}^{(1)}$ | $(\bar{q}^3 \gamma^\mu q^3)(\bar{q}^3 \gamma_\mu q^3)$ |
| $\mathcal{O}_{lq}^{(3),\alpha\beta}$ | $(\bar{l}^a \gamma_\mu \tau^a l^\beta)(\bar{q}^3 \gamma^\mu \tau^a q^3)$ | $\mathcal{O}_{qq}^{(3)}$ | $(\bar{q}^3 \gamma^\mu \tau^a q^3)(\bar{q}^3 \gamma_\mu \tau^a q^3)$ |
| $\mathcal{O}_{lu}^{\alpha\beta}$ | $(\bar{l}^\alpha \gamma_\mu l^\beta)(\bar{u}^3 \gamma_\mu u^3)$ | \mathcal{O}_{uu} | $(\bar{u}^3 \gamma^\mu u^3)(\bar{u}^3 \gamma_\mu u^3)$ |
| $\mathcal{O}_{qe}^{\alpha\beta}$ | $(\bar{q}^3 \gamma^\mu q^3)(\bar{e}^\alpha \gamma_\mu e^\beta)$ | $\mathcal{O}_{qu}^{(1)}$ | $(\bar{q}^3 \gamma^\mu q^3)(\bar{u}^3 \gamma_\mu u^3)$ |
| $\mathcal{O}_{eu}^{\alpha\beta}$ | $(\bar{e}^\alpha \gamma^\mu e^\beta)(\bar{u}^3 \gamma_\mu u^3)$ | $\mathcal{O}_{qu}^{(8)}$ | $(\bar{q}^3 \gamma^\mu T^A q^3)(\bar{u}^3 \gamma_\mu T^A u^3)$ |
| $\mathcal{O}_{lequ}^{(1),\alpha\beta}$ | $(\bar{l}^\alpha e^\beta)\epsilon(\bar{q}^3 u^3)$ | Higgs-Top | |
| $\mathcal{O}_{lequ}^{(3),\alpha\beta}$ | $(\bar{l}^\alpha \sigma_{\mu\nu} e^\beta)\epsilon(\bar{q}^3 \sigma^{\mu\nu} u^3)$ | | |
| Dipoles | | $\mathcal{O}_{Hq}^{(1)}$ | $(H^\dagger i \overleftrightarrow{\mathcal{D}}_\mu H)(\bar{q}^3 \gamma^\mu q^3)$ |
| | | $\mathcal{O}_{Hq}^{(3)}$ | $(H^\dagger i \overleftrightarrow{\mathcal{D}}_\mu^a H)(\bar{q}^3 \gamma^\mu \tau^a q^3)$ |
| \mathcal{O}_{uG} | $(\bar{q}^3 \sigma^{\mu\nu} T^A u^3) \tilde{H} G_{\mu\nu}^A$ | \mathcal{O}_{Hu} | $(H^\dagger i \overleftrightarrow{\mathcal{D}}_\mu H)(\bar{u}^3 \gamma^\mu u^3)$ |
| \mathcal{O}_{uW} | $(\bar{q}^3 \sigma^{\mu\nu} u^3) \tau^a \tilde{H} W_{\mu\nu}^a$ | \mathcal{O}_{uH} | $(H^\dagger H)(\bar{q}^3 u^3 \tilde{H})$ |
| \mathcal{O}_{uB} | $(\bar{q}^3 \sigma^{\mu\nu} u^3) \tilde{H} B_{\mu\nu}$ | | |

Constrain TeV-scale operators from GeV-scale observables



RGEs connect different energy scales within the range of validity of the EFT:

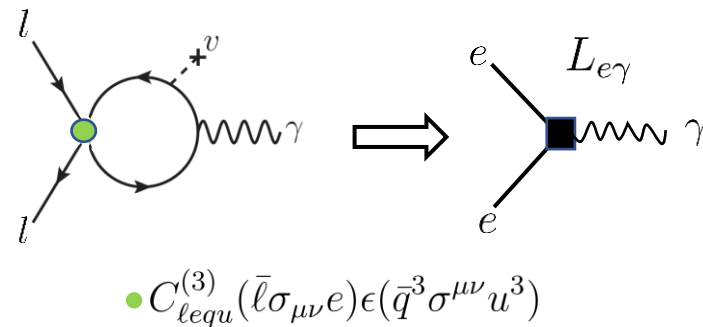
$$[1308.2627] [1310.4838] [1312.2014] [1711.05270] \quad \mu \frac{\partial C_n}{\partial \mu} = \gamma_{nm}(\lambda) C_m$$

Matching procedures allow to integrate out heavy degrees of freedom, linking EFTs valid above or below the threshold

W. Dekens, P. Stoffer [1908.05295]

Use DSixTools!
[2010.16341]

For example:

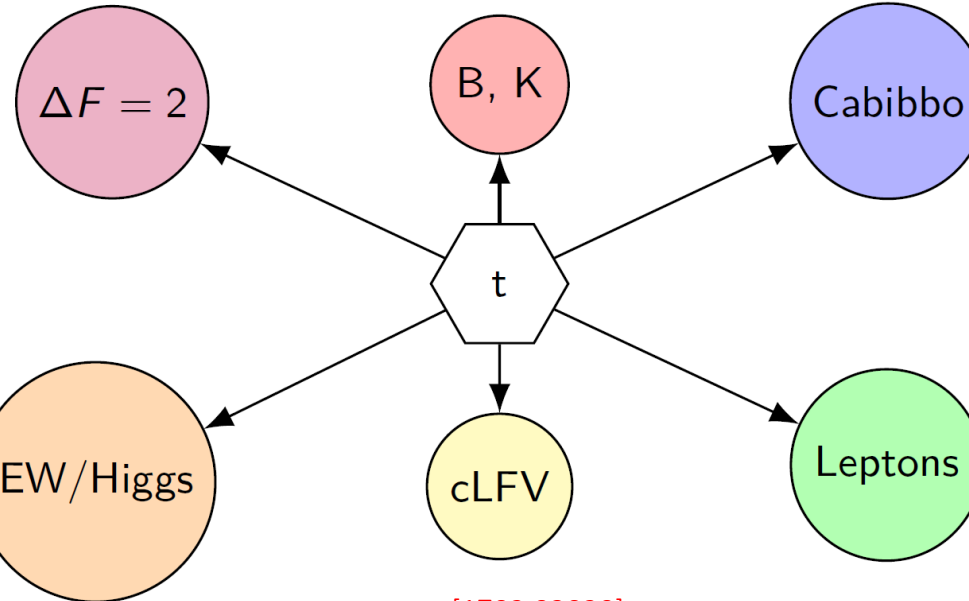


Closing the top quark loop produces an effective dipole operator

We can write predictions for low energy observables in terms of UV Wilson Coefficients and build a global likelihood:

$$-2 \log \mathcal{L}(C_i) \equiv \chi^2(C_i) = \sum_i \frac{(\mathcal{O}_i(C_j) - \mu_i)^2}{\sigma_i^2}$$

[2009.07276]
J. Aebischer et al.



[2112.02087]
V. Cirigliano et al.

[1911.07866]
A. Falkowski, D. Straub

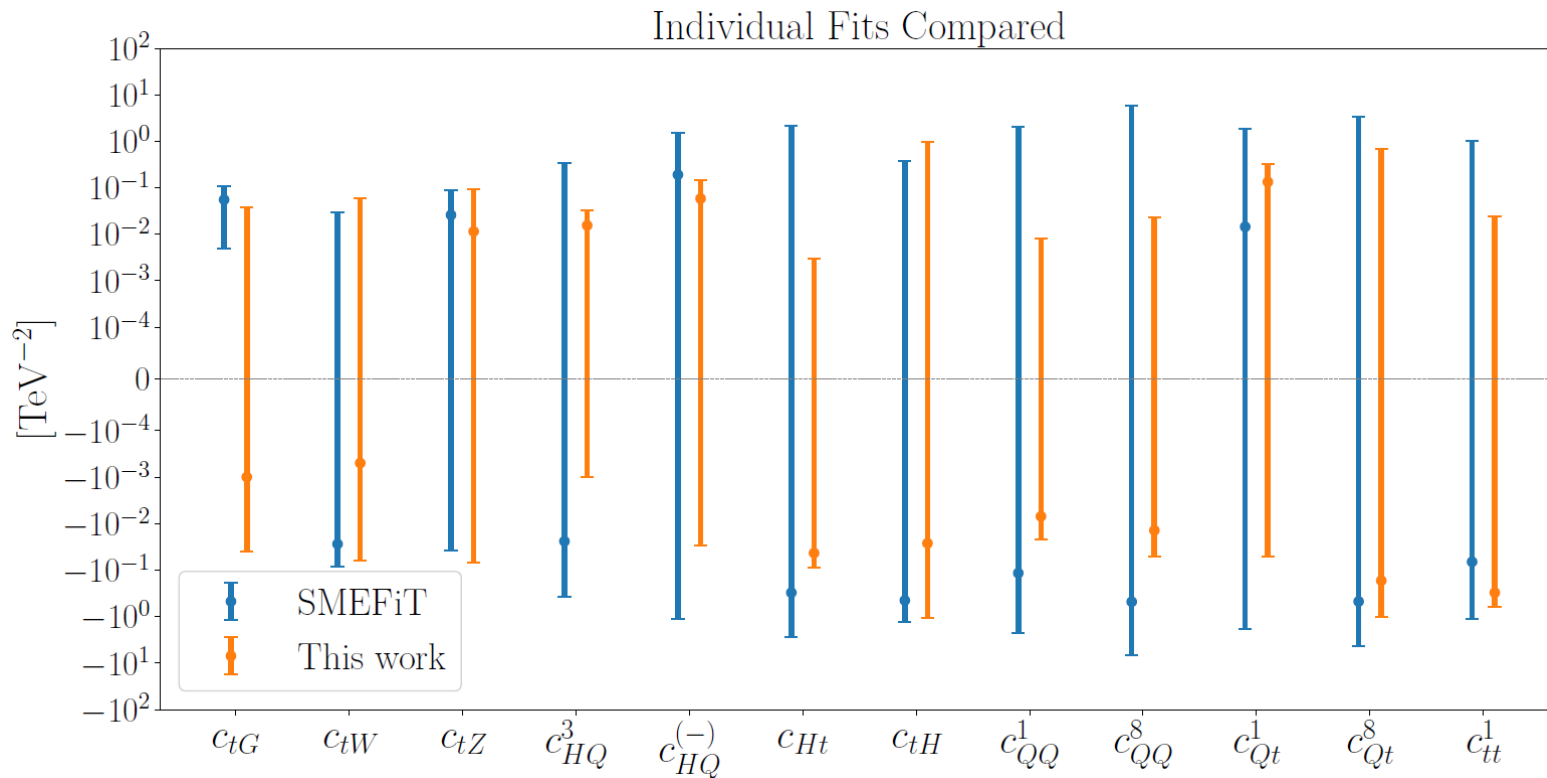
[1702.03020]
A. Crivellin et al.

[2102.08954]
J. Aebischer et al.

One-parameter fits

Comparison with LHC direct bounds provided by CMS and ATLAS measurements (SMEFiT package)

T. Giani, G. Magni, and J. Roj [2302.06660]



SMEFiT basis employed, e.g.:

$$c_{QQ}^{(8)} = 8C_{qq}^{(3)}$$

$$c_{QQ}^{(1)} = 2C_{qq}^{(1)} - \frac{2}{3}C_{qq}^{(3)}$$

Indirect constraints are competitive or stronger in most cases!

One parameter fits are also studied for semileptonic operators, including LFV cases. More discussions in [2310.00047].

One-parameter fits: a closer look 1

| Wilson | Global fit [TeV ⁻²] | Dominant |
|----------------|---------------------------------|--------------------------|
| $C_{qq}^{(+)}$ | $(-1.9 \pm 2.3) \times 10^{-3}$ | ΔM_s |
| $C_{qq}^{(-)}$ | $(-2.0 \pm 1.0) \times 10^{-1}$ | $B_s \rightarrow \mu\mu$ |
| $C_{qu}^{(1)}$ | $(1.3 \pm 1.0) \times 10^{-1}$ | ΔM_s |
| $C_{qu}^{(8)}$ | $(-1.7 \pm 4.4) \times 10^{-1}$ | ΔM_s |
| C_{uu} | $(-3.0 \pm 1.7) \times 10^{-1}$ | $\delta g_{L,11}^{Ze}$ |

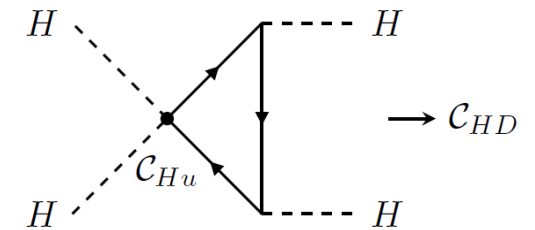
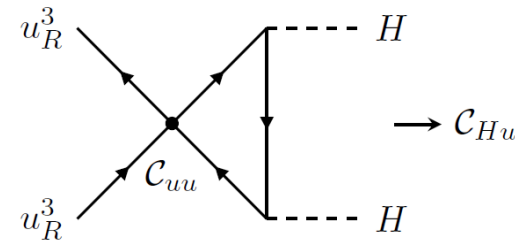
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Indirect bounds from the EW sector, e.g. Z pole observables, can be competitive or stronger than direct limits.

See L. Allwicher, C. Cornella, B. A. Stefanek, G. Isidori [2311.00020]

What is the mechanism?

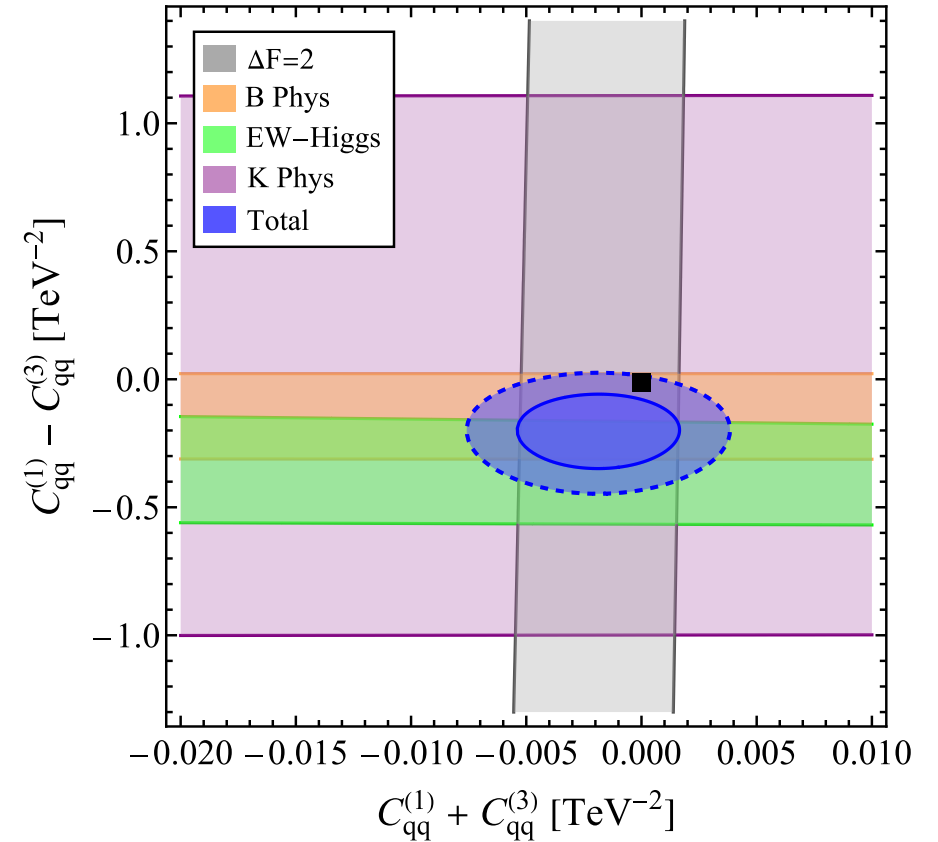
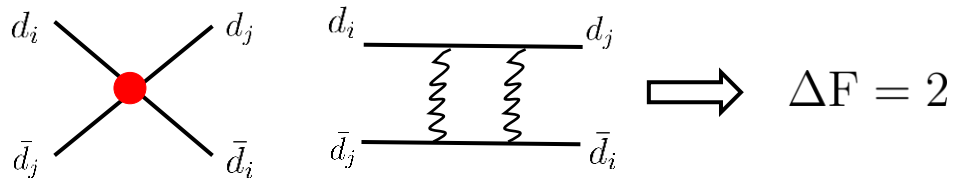


$$\mathcal{O}_{Hu}^{ij} = (H^\dagger i \overleftrightarrow{\mathcal{D}}_\mu H)(\bar{u}_i \gamma^\mu u_j) \quad \mathcal{O}_{HD} = (H^\dagger \mathcal{D}_\mu H)^*(H^\dagger \mathcal{D}^\mu H)$$

One-parameter fits: a closer look 2

| Wilson | Global fit [TeV ⁻²] | Dominant |
|----------------|---------------------------------|--------------------------|
| $C_{qq}^{(+)}$ | $(-1.9 \pm 2.3) \times 10^{-3}$ | ΔM_s |
| $C_{qq}^{(-)}$ | $(-2.0 \pm 1.0) \times 10^{-1}$ | $B_s \rightarrow \mu\mu$ |
| $C_{qu}^{(1)}$ | $(1.3 \pm 1.0) \times 10^{-1}$ | ΔM_s |
| $C_{qu}^{(8)}$ | $(-1.7 \pm 4.4) \times 10^{-1}$ | ΔM_s |
| C_{uu} | $(-3.0 \pm 1.7) \times 10^{-1}$ | $\delta g_{L,11}^{Ze}$ |

Meson oscillations provide strong constraints on 4-quark operators



$$c_{QQ}^{(8)} = 8C_{qq}^{(3)} \quad c_{QQ}^{(1)} = 2C_{qq}^{(1)} - \frac{2}{3}C_{qq}^{(3)}$$

Summary and conclusions

- ❑ We studied the impact of effective top quark operators on low energy observables and found a rich phenomenology
- ❑ Indirect bounds can provide competitive or stronger bounds than direct ones
- ❑ Meson oscillations establish by far the strongest constraint along some direction of the parameter space, e.g. $C_{qq}^{(1)+(3)}$
- ❑ Future sensitivity improvements (e.g. LHCb and Belle II upgrades) will increase the strength of indirect bounds from low energy measurements.
- ❑ More results in 2310.00047 :
 - Semileptonic operators
 - More pairwise fits
 - Global fit
 - Implications for UV models

Thanks for the attention!



Backup slides

SMEFiT results (TeV⁻²)

| Class | Coefficients | Warsaw basis | 95% CL Individual | 95% CL Marginalised |
|-----------|----------------|---|-------------------|---------------------|
| Dipoles | c_{tG} | C_{uG} | [0.01,0.11] | [0.01,0.23] |
| | c_{tW} | C_{uW} | [-0.085,0.030] | [-0.28,0.13] |
| | c_{tZ} | $-s_\theta C_{uB} + c_\theta C_{uW}$ | [-0.038,0.090] | [-0.50,0.14] |
| Higgs-Top | c_{HQ}^3 | $C_{Hq}^{(3)}$ | [-0.39,0.34] | [-0.42,0.31] |
| | $c_{HQ}^{(-)}$ | $C_{Hq}^{(1)} - C_{Hq}^{(3)}$ | [-1.1,1.5] | [-2.7,2.7] |
| | c_{Ht} | C_{Hu} | [-2.8,2.2] | [-15,4] |
| | c_{tH} | C_{uH} | [-1.3,0.4] | [-0.5,2.9] |
| 4 quarks | c_{QQ}^1 | $2C_{qq}^{(1)} - \frac{2}{3}C_{qq}^{(3)}$ | [-2.3,2.0] | [-3.7,4.4] |
| | c_{QQ}^8 | $8C_{qq}^{(3)}$ | [-6.8,5.9] | [-13,10] |
| | c_{Qt}^1 | $C_{qu}^{(1)}$ | [-1.8,1.9] | [-1.5,1.4] |
| | c_{Qt}^8 | $C_{qu}^{(8)}$ | [-4.3,3.3] | [-3.4,2.5] |
| | c_{tt}^1 | C_{uu} | [-1.1,1.0] | [-0.88,0.81] |

Individual fits (TeV⁻²)

| Wilson | Global fit [TeV ⁻²] | Dominant |
|----------------|---------------------------------|--------------------------|
| $C_{qq}^{(+)}$ | $(-1.9 \pm 2.3) \times 10^{-3}$ | ΔM_s |
| $C_{qq}^{(-)}$ | $(-2.0 \pm 1.0) \times 10^{-1}$ | $B_s \rightarrow \mu\mu$ |
| $C_{qu}^{(1)}$ | $(1.3 \pm 1.0) \times 10^{-1}$ | ΔM_s |
| $C_{qu}^{(8)}$ | $(-1.7 \pm 4.4) \times 10^{-1}$ | ΔM_s |
| C_{uu} | $(-3.0 \pm 1.7) \times 10^{-1}$ | $\delta g_{L,11}^{Ze}$ |
| $C_{Hq}^{(+)}$ | $(18.7 \pm 8.8) \times 10^{-3}$ | $B_s \rightarrow \mu\mu$ |
| $C_{Hq}^{(-)}$ | $(5.8 \pm 4.5) \times 10^{-2}$ | $\delta g_{L,11}^{Ze}$ |
| C_{Hu} | $(-4.3 \pm 2.3) \times 10^{-2}$ | $\delta g_{L,11}^{Ze}$ |
| C_{uB} | $(-0.6 \pm 2.0) \times 10^{-2}$ | $c_{\gamma\gamma}$ |
| C_{uG} | $(-0.1 \pm 2.0) \times 10^{-2}$ | c_{gg} |
| C_{uH} | $(-0.3 \pm 5.2) \times 10^{-1}$ | $C_{uH,33}$ |
| C_{uW} | $(-0.1 \pm 3.1) \times 10^{-2}$ | $c_{\gamma\gamma}$ |

| Wilson | Global fit [TeV ⁻²] | Dominant |
|-------------------|---------------------------------|-----------------------------|
| $C_{lq}^{(+),11}$ | $(2.4 \pm 3.5) \times 10^{-3}$ | R_K |
| $C_{lq}^{(+),22}$ | $(-4.0 \pm 3.4) \times 10^{-3}$ | R_K |
| $C_{lq}^{(+),33}$ | $(7.2 \pm 4.4) \times 10^{-1}$ | g_τ/g_i |
| $C_{lq}^{(-),11}$ | $(10.9 \pm 7.6) \times 10^{-2}$ | $R_{K(*)}^\nu$ |
| $C_{lq}^{(-),22}$ | $(-6.0 \pm 7.0) \times 10^{-2}$ | $R_{K(*)}^\nu$ |
| $C_{lq}^{(-),33}$ | $(-1.8 \pm 1.0) \times 10^{-1}$ | $R_{K(*)}^\nu$ |
| C_{lu}^{11} | $(-1.7 \pm 7.0) \times 10^{-2}$ | $\delta g_{L,11}^{Ze}$ |
| C_{lu}^{22} | $(-4.3 \pm 1.8) \times 10^{-1}$ | $\delta g_{L,22}^{Ze}, R_K$ |
| C_{lu}^{33} | $(0.5 \pm 2.4) \times 10^{-1}$ | $\Delta g_{L,33}^{Ze}$ |
| C_{qe}^{11} | $(-0.7 \pm 3.9) \times 10^{-2}$ | R_{K^*} |
| C_{qe}^{22} | $(12.1 \pm 9.2) \times 10^{-3}$ | $B_s \rightarrow \mu\mu$ |
| C_{qe}^{33} | $(2.2 \pm 2.4) \times 10^{-1}$ | $\delta g_{R,33}^{Ze}$ |

| Wilson | Global fit [TeV ⁻²] | Dominant |
|---------------------|----------------------------------|------------------------|
| C_{eu}^{11} | $(5.0 \pm 8.1) \times 10^{-2}$ | $\Delta g_{R,11}^{Ze}$ |
| C_{eu}^{22} | $(4.8 \pm 2.1) \times 10^{-1}$ | $\Delta g_{R,22}^{Ze}$ |
| C_{eu}^{33} | $(-2.3 \pm 2.5) \times 10^{-1}$ | $\Delta g_{R,33}^{Ze}$ |
| $C_{lequ}^{(1),11}$ | $(0.4 \pm 1.0) \times 10^{-2}$ | $(g-2)_e$ |
| $C_{lequ}^{(1),22}$ | $(1.8 \pm 1.6) \times 10^{-2}$ | C_{eH22} |
| $C_{lequ}^{(1),33}$ | $(8.0 \pm 9.1) \times 10^{-2}$ | C_{eH33} |
| $C_{lequ}^{(3),11}$ | $(-0.6 \pm 1.5) \times 10^{-5}$ | $(g-2)_e$ |
| $C_{lequ}^{(3),22}$ | $(-19.3 \pm 8.1) \times 10^{-5}$ | $(g-2)_\mu$ |
| $C_{lequ}^{(3),33}$ | $(-7.0 \pm 7.8) \times 10^{-1}$ | C_{eH33} |

B-phys and K-phys observables

| Observable | Experimental value |
|--|--|
| $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ | $(1.14_{-0.33}^{+0.4}) \times 10^{-10}$ NA62 |
| $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$ | $< 3.6 \times 10^{-9}$ KOTO |
| $\mathcal{B}(K_S \rightarrow \mu^+ \mu^-)$ | $< 2.5 \times 10^{-10}$ LHCb |
| $\mathcal{B}(K_L \rightarrow \mu^+ \mu^-)_{SD}$ | $< 2.5 \times 10^{-9}$ Isidori:2003 |
| $\mathcal{B}(K_L \rightarrow \mu^\pm e^\mp)$ | $< 5.6 \times 10^{-12}$ BNL |
| $\mathcal{B}(K_L \rightarrow \pi^0 \mu^+ \mu^-)$ | $< 4.5 \times 10^{-10}$ KTeV |
| $\mathcal{B}(K_L \rightarrow \pi^0 e^+ e^-)$ | $< 3.3 \times 10^{-10}$ KTeV |
| $\mathcal{B}(K_L \rightarrow \pi^0 e^+ \mu^-)$ | $< 9.1 \times 10^{-11}$ KTeV |
| $\mathcal{B}(K^+ \rightarrow \pi^+ e^+ \mu^-)$ | $< 7.9 \times 10^{-11}$ NA62 |

| Observable | Experimental value |
|---|--------------------------------------|
| $B \rightarrow X_s \gamma$ | $(3.49 \pm 0.19) \times 10^{-4}$ PDG |
| R_K^ν | 2.93 ± 0.90 Belle-II |
| $R_{K^*}^\nu$ | < 3.21 Belle-II |
| $R_K[1.1, 6]$ | 0.949 ± 0.047 LHCb |
| $R_{K^*}[1.1, 6]$ | 1.027 ± 0.077 LHCb |
| $\mathcal{B}(B \rightarrow K e \mu)$ | $< 4.5 \times 10^{-8}$ Belle |
| $\mathcal{B}(B \rightarrow K e \tau)$ | $< 3.6 \times 10^{-5}$ BaBar |
| $\mathcal{B}(B \rightarrow K \mu \tau)$ | $< 4.5 \times 10^{-5}$ LHCb |

| Observable | Experimental value |
|---|---------------------------------------|
| $\mathcal{B}(B_s \rightarrow ee)$ | $< 11.2 \times 10^{-9}$ LHCb |
| $\mathcal{B}(B_s \rightarrow \mu\mu)$ | $(3.01 \pm 0.35) \times 10^{-9}$ LHCb |
| $\mathcal{B}(B_s \rightarrow \tau\tau)$ | $< 6.8 \times 10^{-3}$ LHCb |
| $\mathcal{B}(B_s \rightarrow e\mu)$ | $< 6.3 \times 10^{-9}$ LHCb |
| $\mathcal{B}(B_s \rightarrow \mu\tau)$ | $< 4.2 \times 10^{-5}$ LHCb |
| $\mathcal{B}(B_d \rightarrow ee)$ | $< 3.0 \times 10^{-9}$ LHCb |
| $\mathcal{B}(B_d \rightarrow \mu\mu)$ | $< 2.6 \times 10^{-10}$ LHCb |
| $\mathcal{B}(B_d \rightarrow \tau\tau)$ | $< 2.1 \times 10^{-3}$ LHCb |
| $\mathcal{B}(B_d \rightarrow e\mu)$ | $< 1.3 \times 10^{-9}$ LHCb |
| $\mathcal{B}(B_d \rightarrow \mu\tau)$ | $< 1.4 \times 10^{-5}$ LHCb |

| Observable | Experimental value | SM prediction |
|--------------|---------------------------------------|-------------------------------------|
| ϵ_K | $(2.228 \pm 0.011) \times 10^{-3}$ | $(2.14 \pm 0.12) \times 10^{-3}$ |
| ΔM_s | $(17.765 \pm 0.006) \text{ ps}^{-1}$ | $(17.35 \pm 0.94) \text{ ps}^{-1}$ |
| ΔM_d | $(0.5065 \pm 0.0019) \text{ ps}^{-1}$ | $(0.502 \pm 0.031) \text{ ps}^{-1}$ |

Lepton observables

| Observable | Experimental limit |
|---|----------------------------|
| $\mathcal{B}(\tau \rightarrow e\pi^+\pi^-)$ | 2.7×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow eK^+K^-)$ | 4.1×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow \mu\gamma)$ | 5.0×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow 3\mu)$ | 2.5×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow \mu\bar{e}e)$ | 2.1×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow \mu\pi^0)$ | 1.3×10^{-7} Belle |
| $\mathcal{B}(\tau \rightarrow \mu\eta)$ | 7.7×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow \mu\eta')$ | 1.5×10^{-7} Belle |
| $\mathcal{B}(\tau \rightarrow \mu\pi^+\pi^-)$ | 2.5×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow \mu K^+K^-)$ | 5.2×10^{-8} Belle |

| Observable | Experimental limit |
|--|-------------------------------|
| $\mathcal{B}(\mu \rightarrow e\gamma)$ | 5.0×10^{-13} MEG |
| $\mathcal{B}(\mu \rightarrow 3e)$ | 1.2×10^{-12} SINDRUM |
| $\mathcal{B}(\mu \text{ Au} \rightarrow e \text{ Au})$ | 8.3×10^{-13} SINDRUM |
| $\mathcal{B}(\tau \rightarrow e\gamma)$ | 3.9×10^{-8} BaBar |
| $\mathcal{B}(\tau \rightarrow 3e)$ | 3.2×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow e\bar{\mu}\mu)$ | 3.2×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow e\pi^0)$ | 9.5×10^{-8} Belle |
| $\mathcal{B}(\tau \rightarrow e\eta)$ | 1.1×10^{-7} Belle |
| $\mathcal{B}(\tau \rightarrow e\eta')$ | 1.9×10^{-7} Belle |

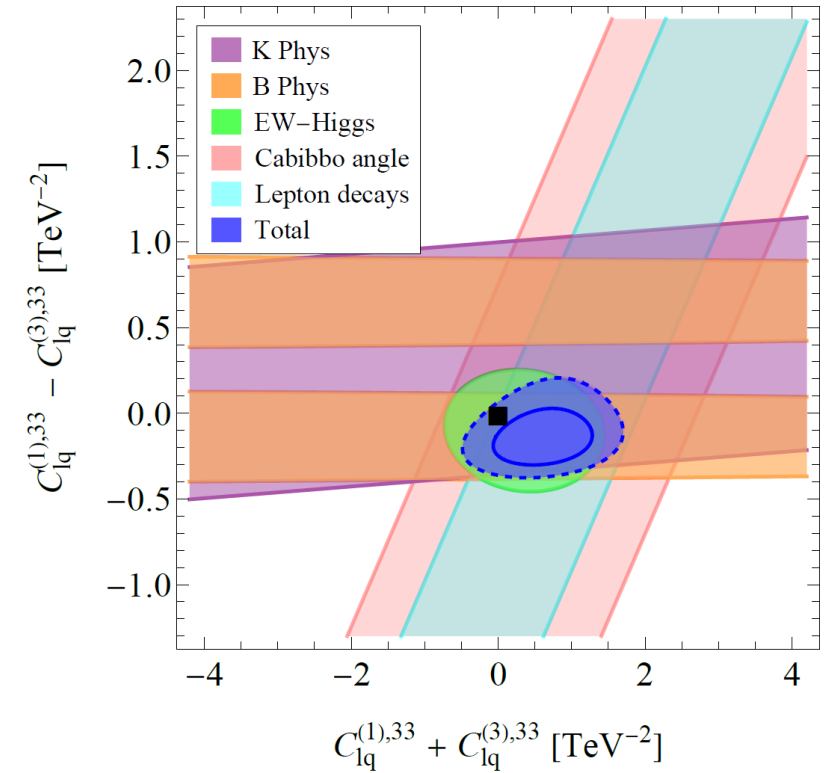
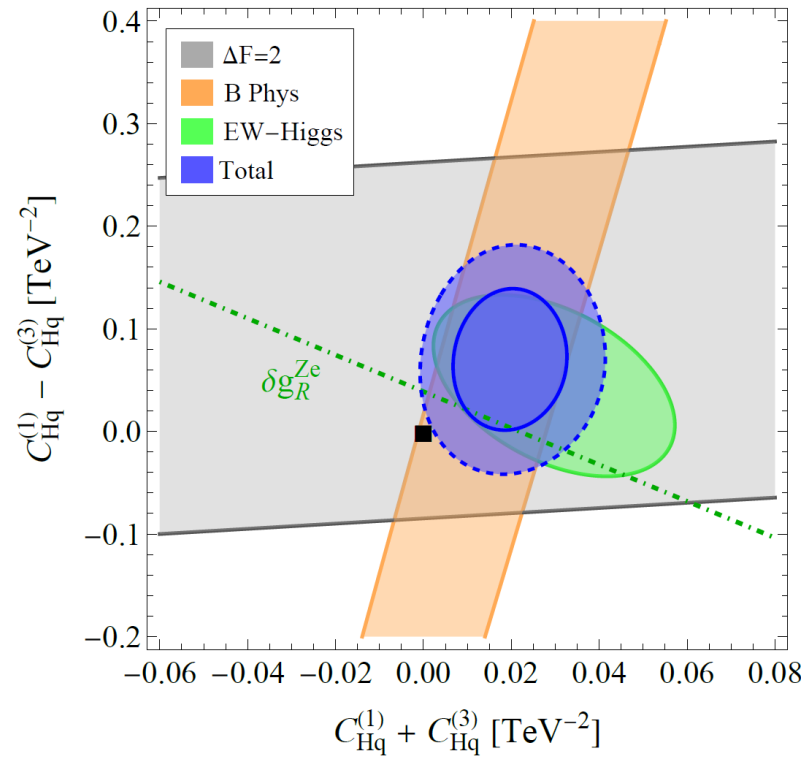
| Observable | Experimental value | |
|-----------------|---------------------------------|----------------------------------|
| | $\ell = e$ | $\ell = \mu$ |
| Δa_ℓ | $(2.8 \pm 7.4) \times 10^{-13}$ | $(20.0 \pm 8.4) \times 10^{-10}$ |

| Observable | Experimental value | |
|---------------------|--------------------------------|--------------------------------|
| | $\ell = e$ | $\ell = \mu$ |
| $g_\tau/g_\ell - 1$ | $(2.7 \pm 1.4) \times 10^{-3}$ | $(0.9 \pm 1.4) \times 10^{-3}$ |

Beyond one-parameter fits

More results in 2310.00047

- Two parameter fits



Beyond one-parameter fits

We perform a Gaussian global fit

More results in 2310.00047

$$\chi^2 = \chi_{\text{best-fit}}^2 + (C_i - \mu_{C_i})(\sigma^2)_{ij}^{-1}(C_j - \mu_{C_j}) = \chi_{\text{best-fit}}^2 + \frac{(K_i - \mu_{K_i})^2}{\sigma_{K_i}^2}.$$

- Two parameter fits
- Global fits

| Coefficient | Gaussian fit [TeV ⁻²] | Coefficient | Gaussian fit [TeV ⁻²] |
|-------------|-----------------------------------|-------------|-----------------------------------|
| K_1 | 0.0019 ± 0.0023 | K_7 | 0.56 ± 0.79 |
| K_2 | 0.0169 ± 0.0083 | K_8 | 0.80 ± 0.88 |
| K_3 | -0.001 ± 0.015 | K_9 | -0.8 ± 1.3 |
| K_4 | -0.017 ± 0.021 | K_{10} | -1.1 ± 1.7 |
| K_5 | 0.044 ± 0.029 | K_{11} | 20.5 ± 12 |
| K_6 | -0.26 ± 0.38 | K_{12} | -14 ± 15 |

$$K_{11} \approx -0.86C_{qq}^{(-)} + 0.26C_{uu} - 0.41C_{qu}^{(1)} - 0.10C_{Hu} + \dots ,$$

$$K_{12} \approx +0.23C_{qq}^{(-)} + 0.95C_{uu} + 0.16C_{qu}^{(1)} - 0.12C_{Hu} + \dots .$$

Beyond one-parameter fits

More results in 2310.00047

- Two parameter fits
- Global fits
- Implications on UV

$$S_1 \sim (\bar{3}, 1)_{+1/3}$$

$$\mathcal{L} \supset \lambda_{t\tau} \bar{q}_3^c i \sigma_2 l_3 S_1 + h.c$$

