

# Phenomenology of Jet Drift in Heavy Ion Collisions

*Supported in part by DoE Grant (DE-SC0024560)  
Supported in part by a start-up grand from NMSU*

Hard Probes 2024  
24<sup>th</sup> September, 2024

Jo Bahder

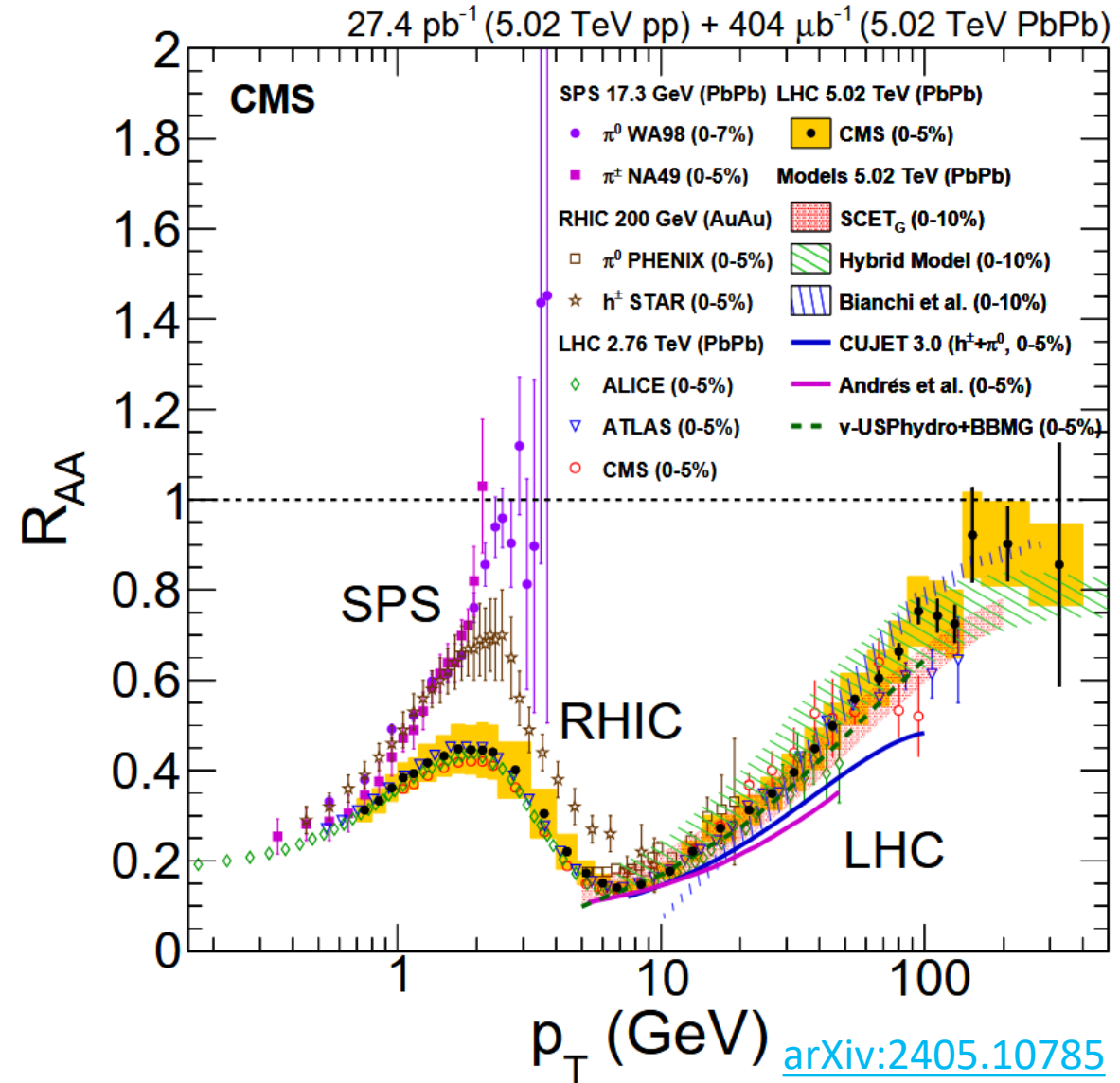


In collaboration with  
Hasan Rahman, Matthew Sievert,  
and Ivan Vitev

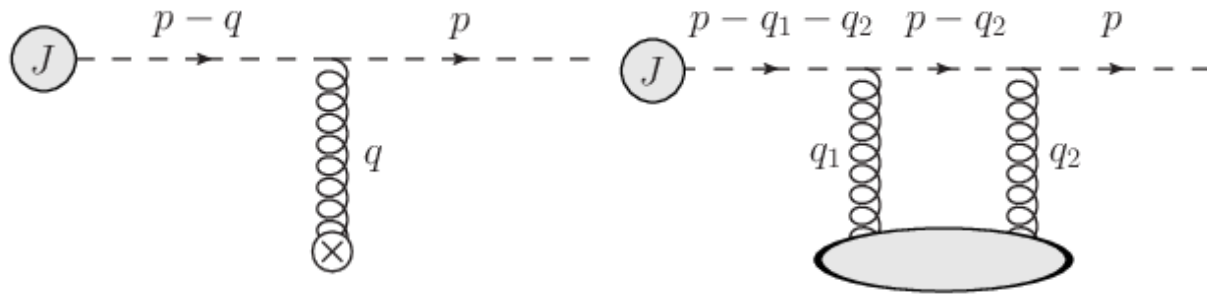


# The State of Hard Probe Tomography

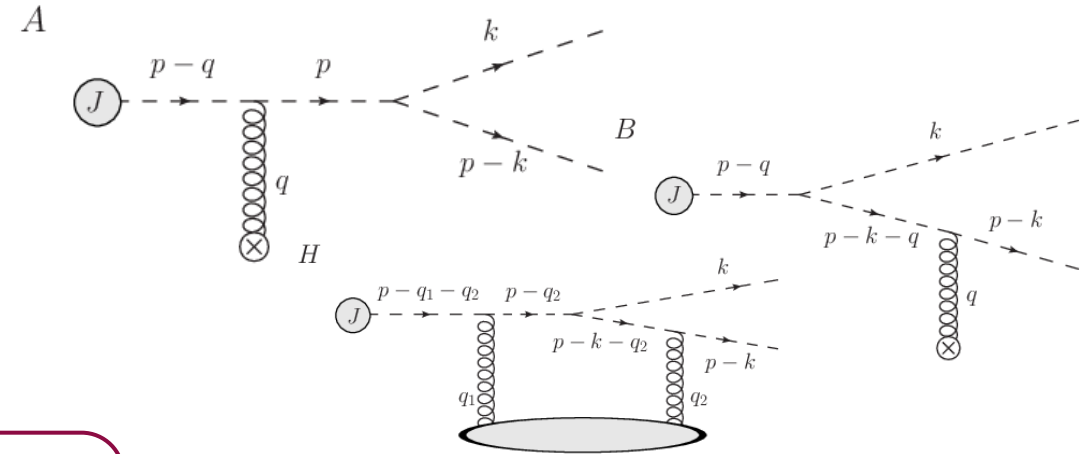
- Delivery of hard probe tomography lackluster
  - Many microscopic models obtain results similar to data (e.g. ch. had.  $R_{AA}$ )
- Two options for successful hard probe tomography
  - New observables (EECs & jet substructure)
  - Regions of phase space where hard probes interact in more discriminating ways (e.g.  $< 10$  GeV)
- Both require new precision perturbative calculations, e.g.  $\mathcal{O}\left(\frac{\mu}{E}\right)$  corrections & precise calculation inputs



# Momentum Broadening & Radiation in the Presence of Flow

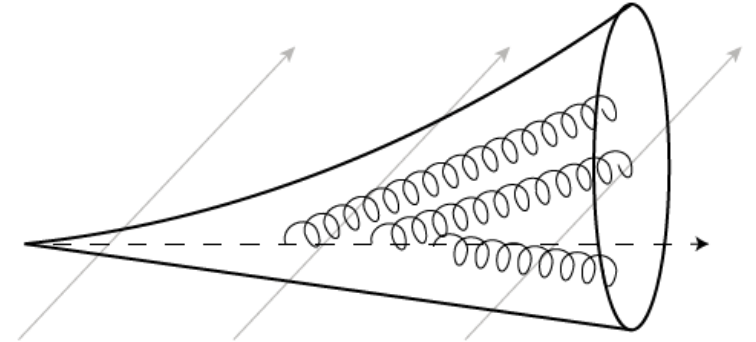
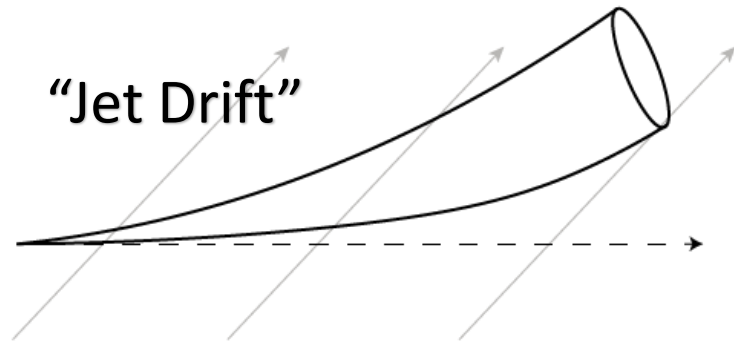
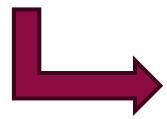


Born & Double-Born Momentum Broadening Diagrams



E.G. Born & Double-Born Radiation Diagrams

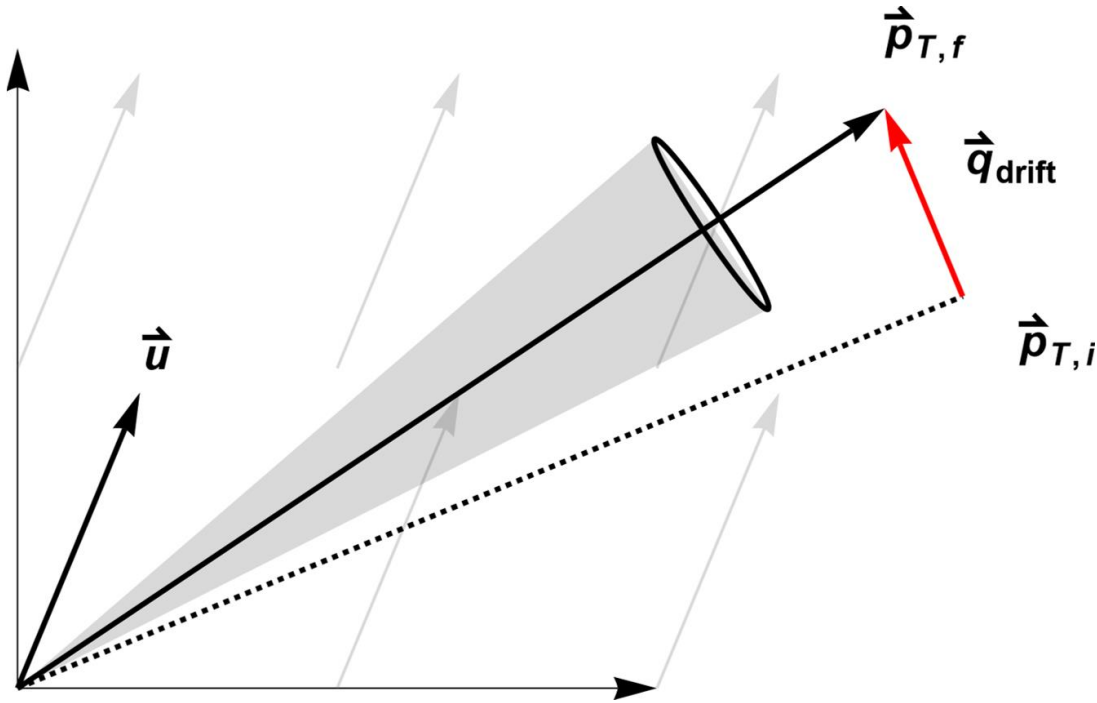
**Derivation**  
 A. V. Sadofyev, I. Vitev,  
 & M. D. Sievert  
 Phys.Rev.D 104 (2021)  
[arXiv:2104.09513](https://arxiv.org/abs/2104.09513)



New systematic behavior at  $\mathcal{O}\left(\frac{\mu}{E}\right)$



# Anisotropic Jet Broadening: Jet Drift



- “Jet Drift”: Preferential broadening in direction of medium flow
- Part of a "New" class of  $\mathcal{O}\left(\frac{\mu}{E}\right)$  pQCD effects: asymmetric / anisotropic

Flow enhanced and flow direction controlled

$$\langle \vec{q}_{drift} \rangle = \hat{e}_\perp \int d\tau \begin{matrix} 3 \\ E(\tau) \end{matrix} \begin{matrix} \mu^2(\tau) \\ \lambda(\tau) \end{matrix} \ln \frac{E(\tau)}{\mu(\tau)} \begin{matrix} u_\perp(\tau) \\ 1 - u_\parallel(\tau) \end{matrix}$$

$$\frac{1}{\lambda} = \sigma \rho$$

$$\rho \propto T^3$$

$$\mu \propto T$$

Energy suppressed

Temperature/Density Enhanced

## Derivation

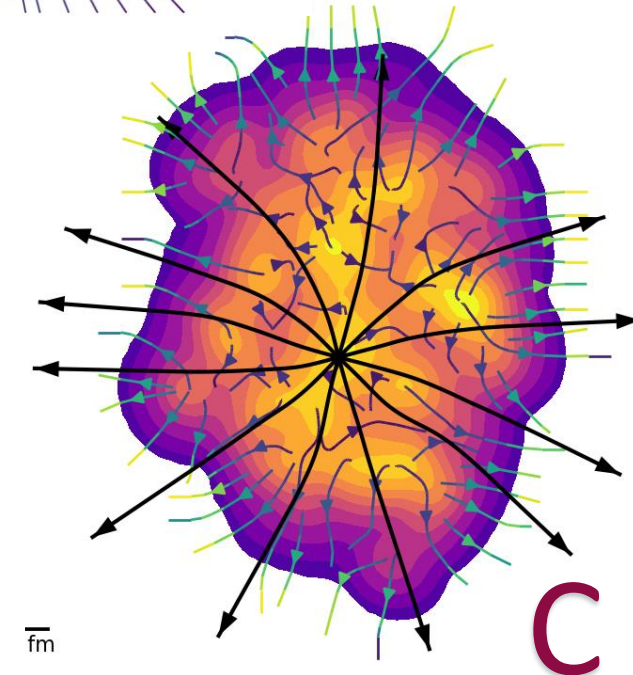
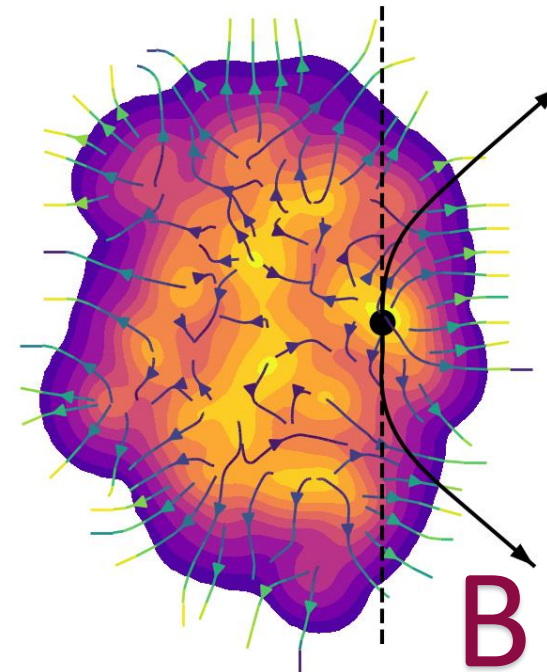
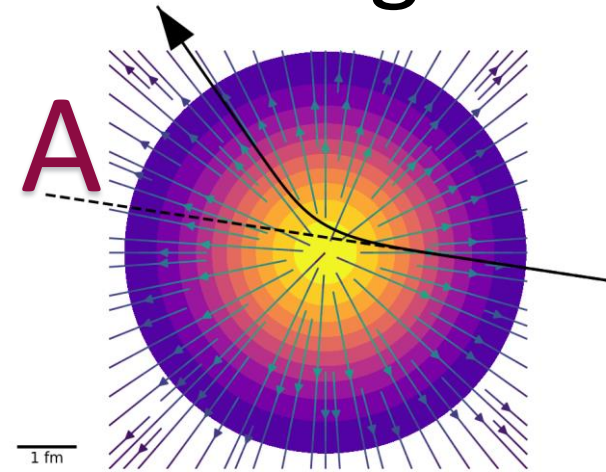
A. V. Sadofyev, I. Vitev,  
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Phys.Rev.D 104 (2021)  
([arXiv:2104.09513](https://arxiv.org/abs/2104.09513))

## Analytic Pheno.

L. Antiporda, J. Bahder, H.  
Rahman  
& M. D. Sievert  
Phys.Rev.D 105 (2022)  
([arXiv: 2110.03590](https://arxiv.org/abs/2110.03590))

# Possible Signatures of Jet Drift in Leading Hadrons

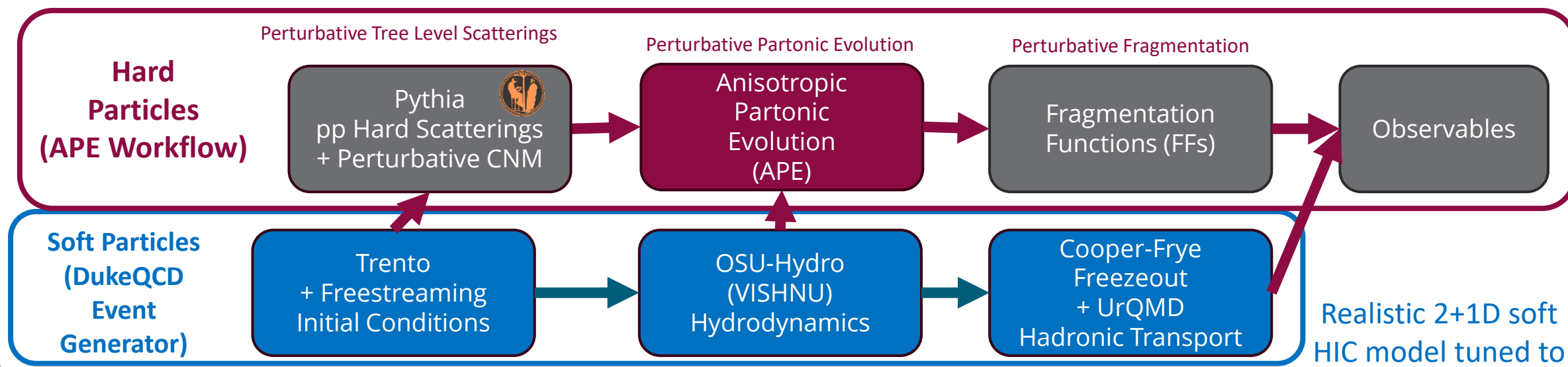
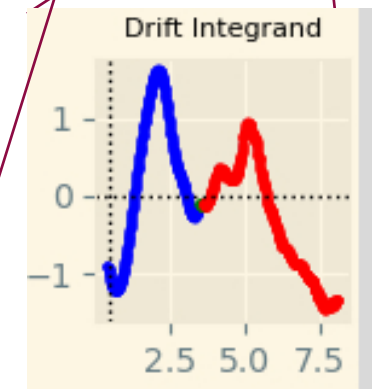
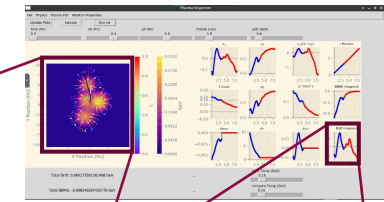
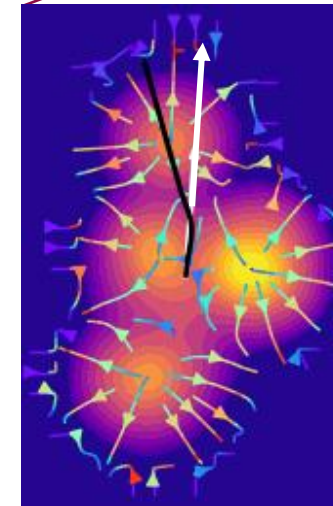
- Modification of suppression (A)
  - Deflecting away from flowing hot spots
  - Particle sees reduced integrated density
- Dihadron/dijet acoplanarity enhancements (B)
  - Particles couple to same “attractor” in the medium
- Anisotropic flow modification (C)
  - Particles couple to soft anisotropic flow



# APE: A Primitive Monte Carlo

Test effect of addition of jet drift to realistic event-by-event jet-medium simulations on hard probes of heavy ion collisions

Study in  $\sqrt{s} = 5.02$  TeV PbPb



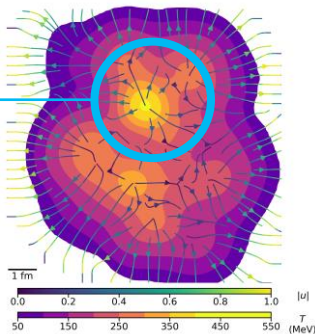
[arXiv:1808.02106](https://arxiv.org/abs/1808.02106)

Realistic 2+1D soft HIC model tuned to pPb & PbPb data



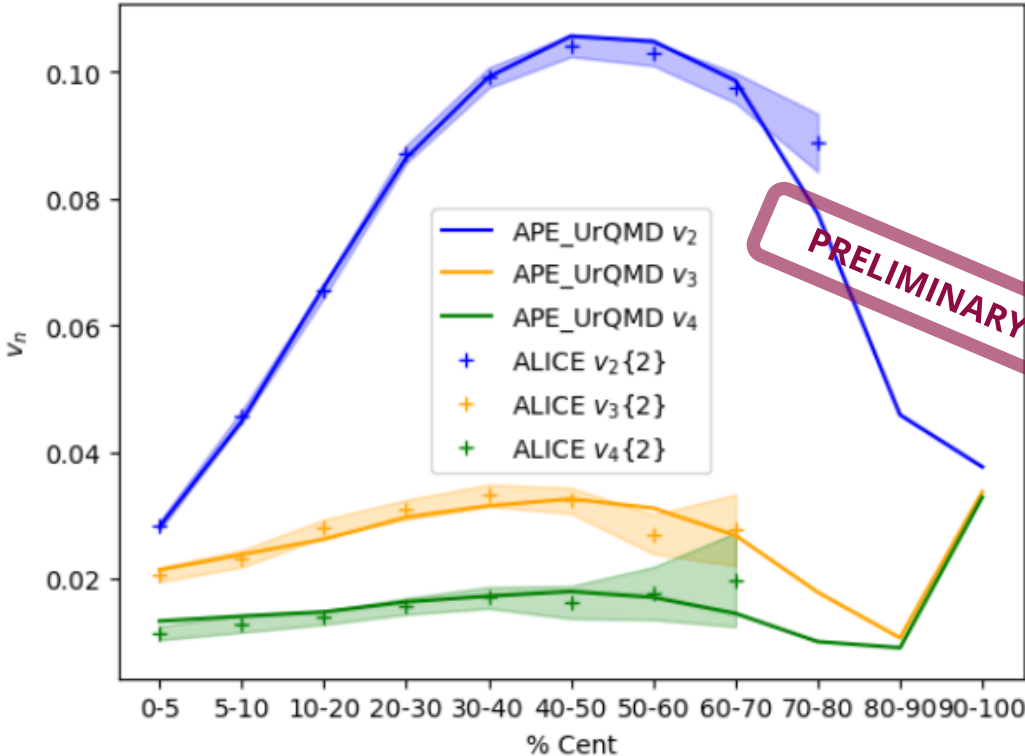
# DukeQCD's HIC Event Generator

- Highly tuned to soft sector observables
  - Reliable picture of final state
  - Not necessarily good description of intermediate dynamics – drift distinguishes
- Large event-by-event fluctuations
  - Maximizes disruption of event-correlated drift



$$\langle \vec{q}_{drift} \rangle = \hat{e}_\perp \int d\tau \frac{3}{E(\tau)} \frac{\mu^2(\tau)}{\lambda(\tau)} \ln \frac{E(\tau)}{\mu(\tau)} \frac{u_\perp(\tau)}{1 - u_\parallel(\tau)}$$

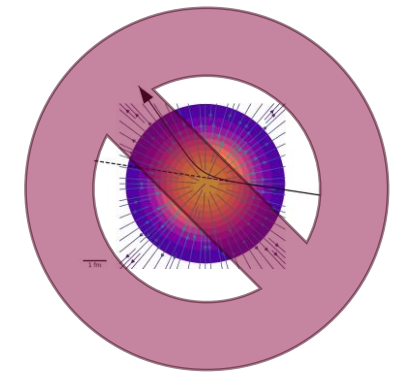
Energy suppressed



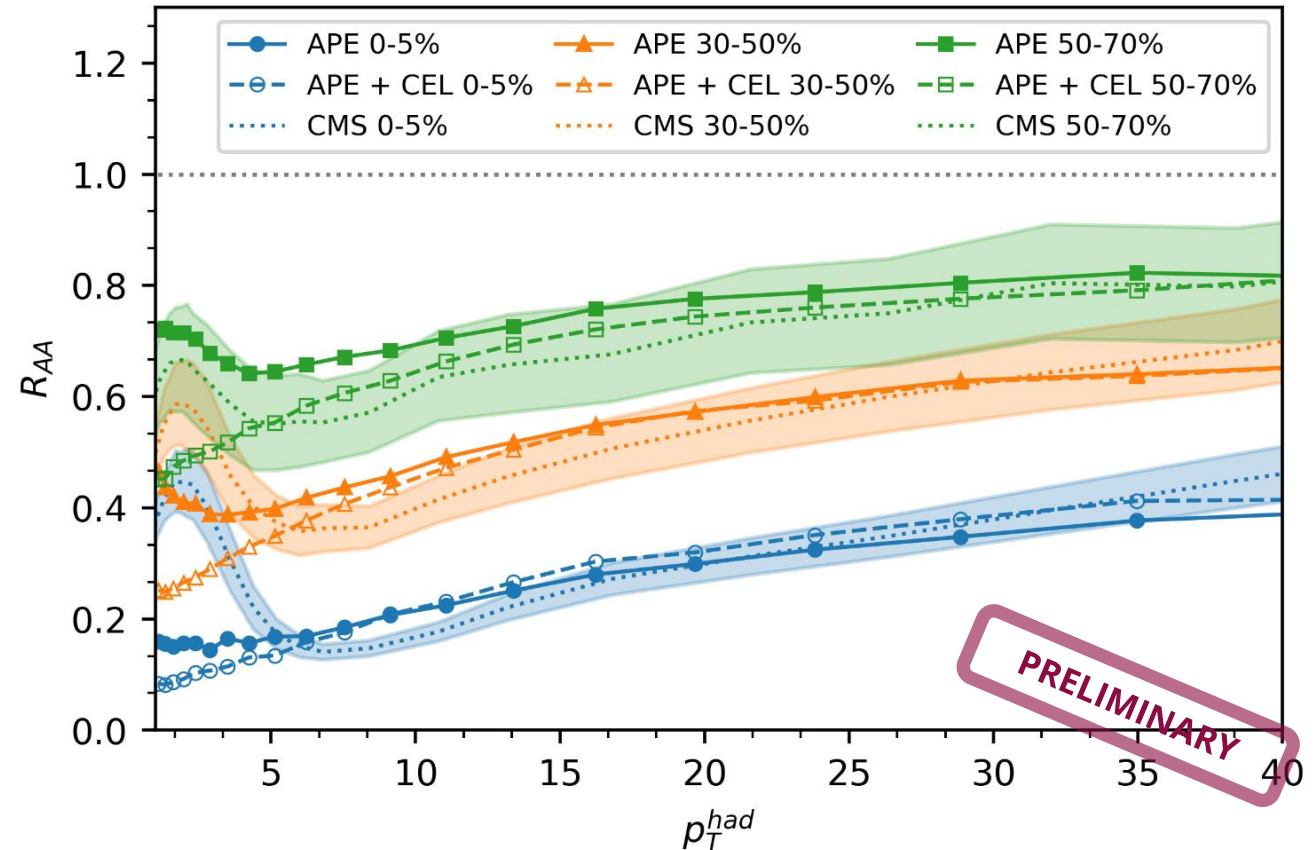
Target: Lower Bound of Drift

See also multiplicities, mean pT, pT fluctuation, etc.: [arXiv:1808.02106](https://arxiv.org/abs/1808.02106)

# No Suppression Reduction



- Drift does not measurably modify  $R_{AA}(p_T)$ 
  - Very useful – can tune coupling
  - Rad:  $g=2.0$ , Rad + Coll:  $g=1.6$
- Additional sources of high- $p_T$  energy loss reduce effective drift coupling
- Better performance at low- $p_T$  can only enhance drift

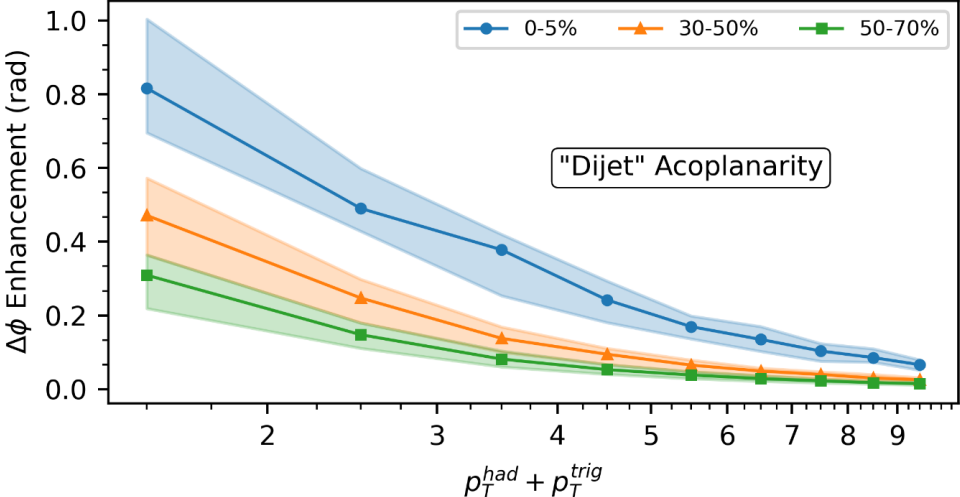
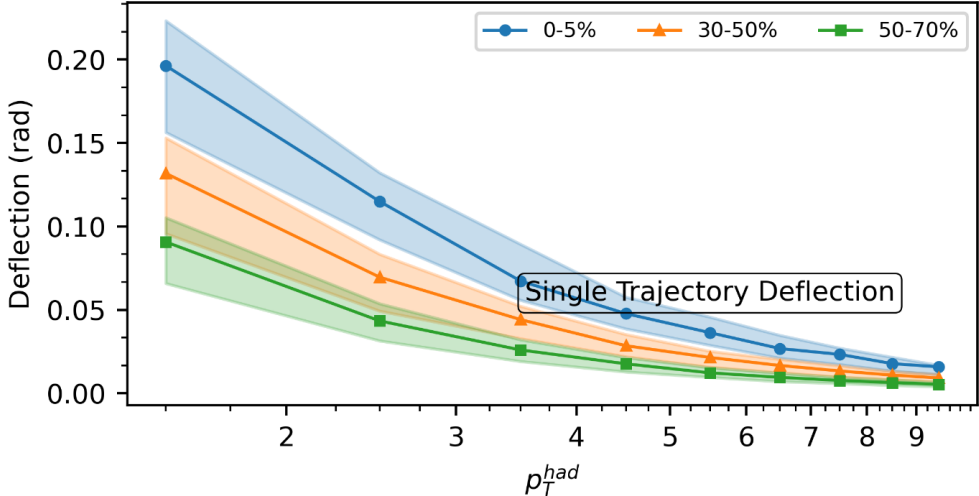
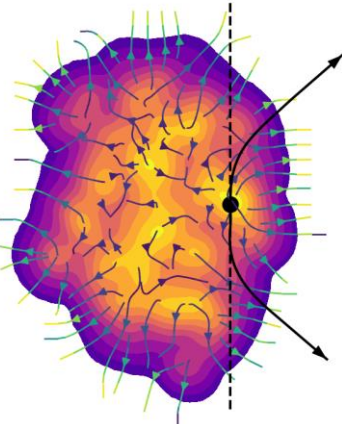


PRELIMINARY



# Deflection Size & Acoplanarity Enhancement

- Note centrality reversal
  - $V_2$  correlated to event plane
  - Acoplanarities access absolute deflections
- Initial acoplanarity fluctuation will change magnitude
  - Currently tree-level scattering: coplanar “dijets”



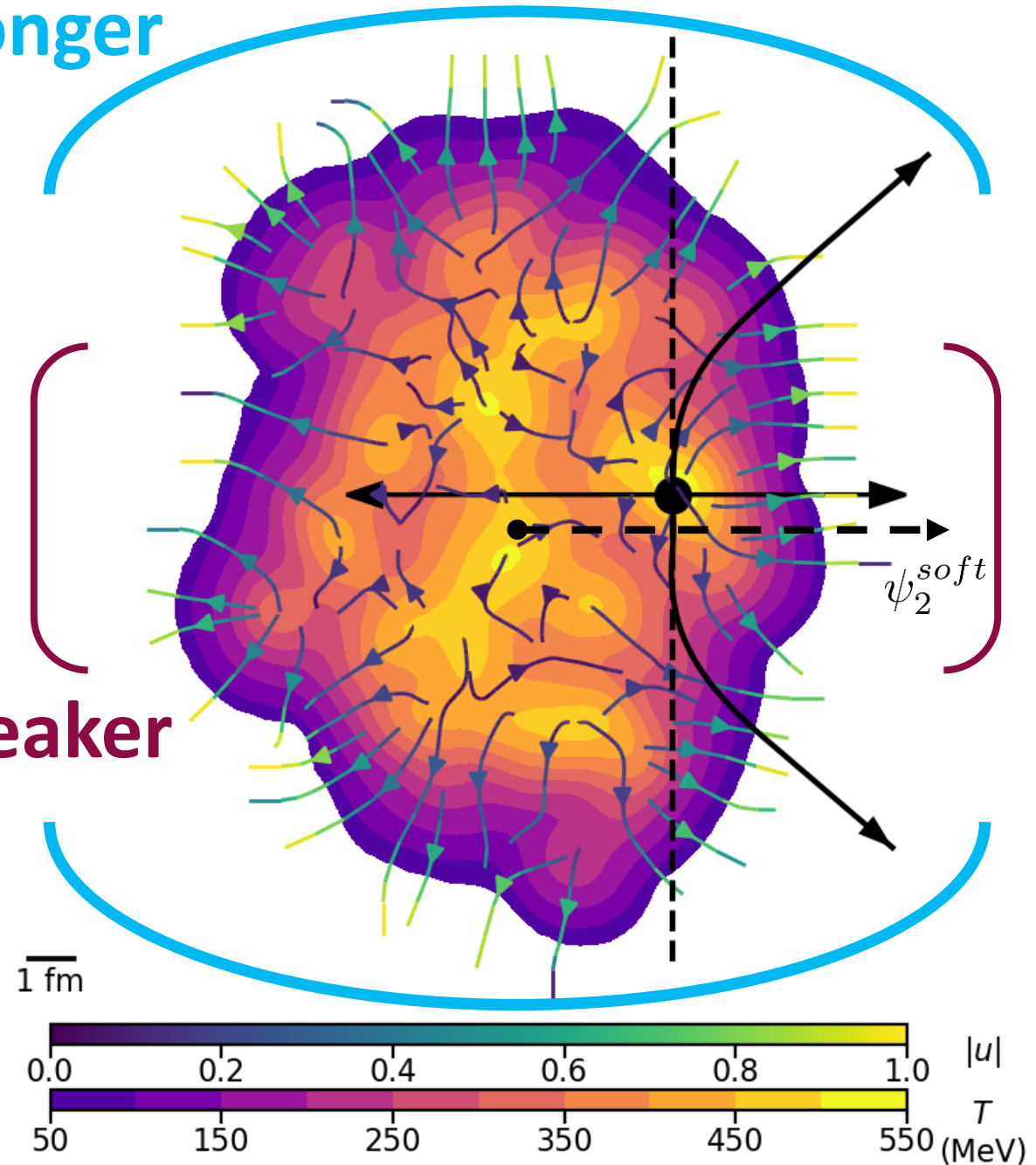
Colored band: drift +/- 25 % strength

# Acoplanarity Cuts

- Acoplanarity modulation still tied to event plane
  - Possible selection cuts for velocity tomography
  - Difficult to measure independent of pathlength effects
- Collimation effect possible along event plane

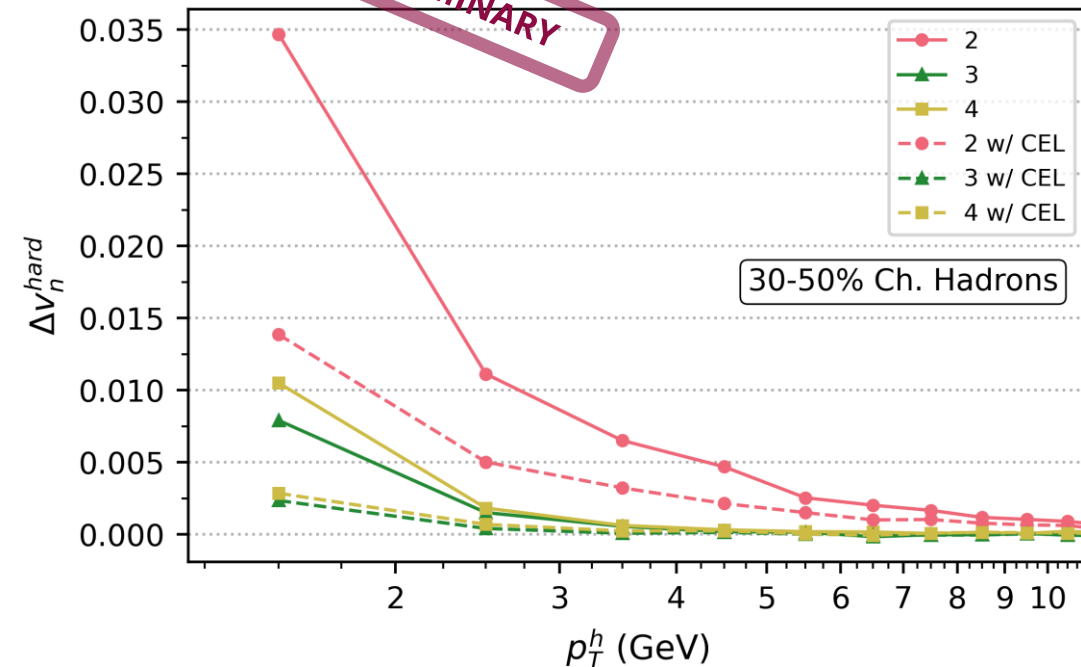
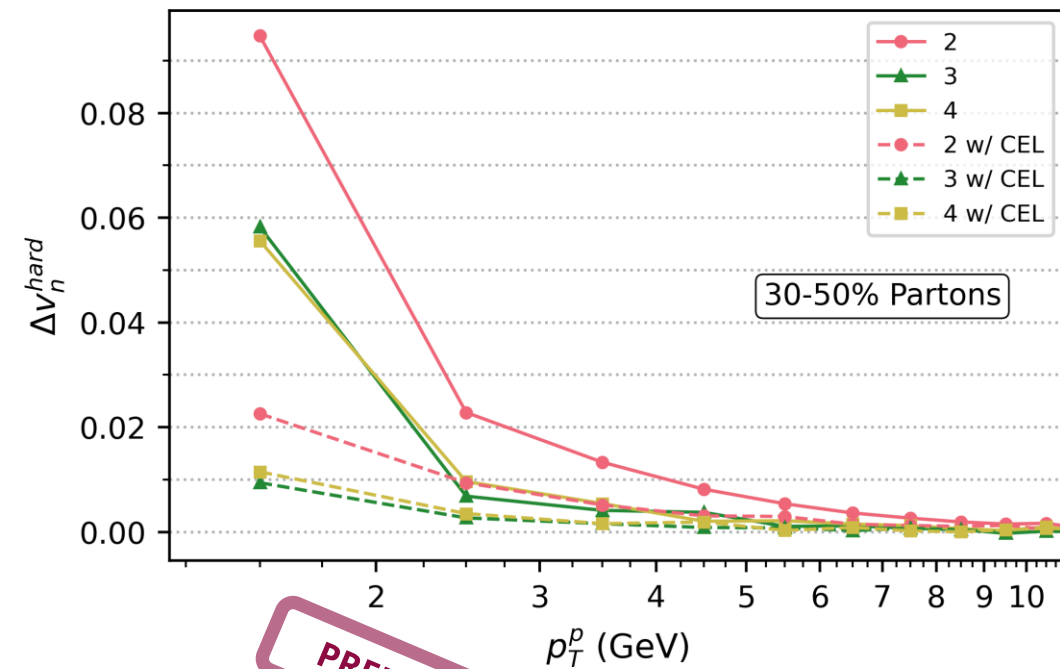
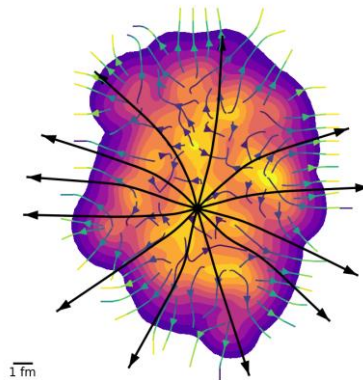
Stronger

Weaker



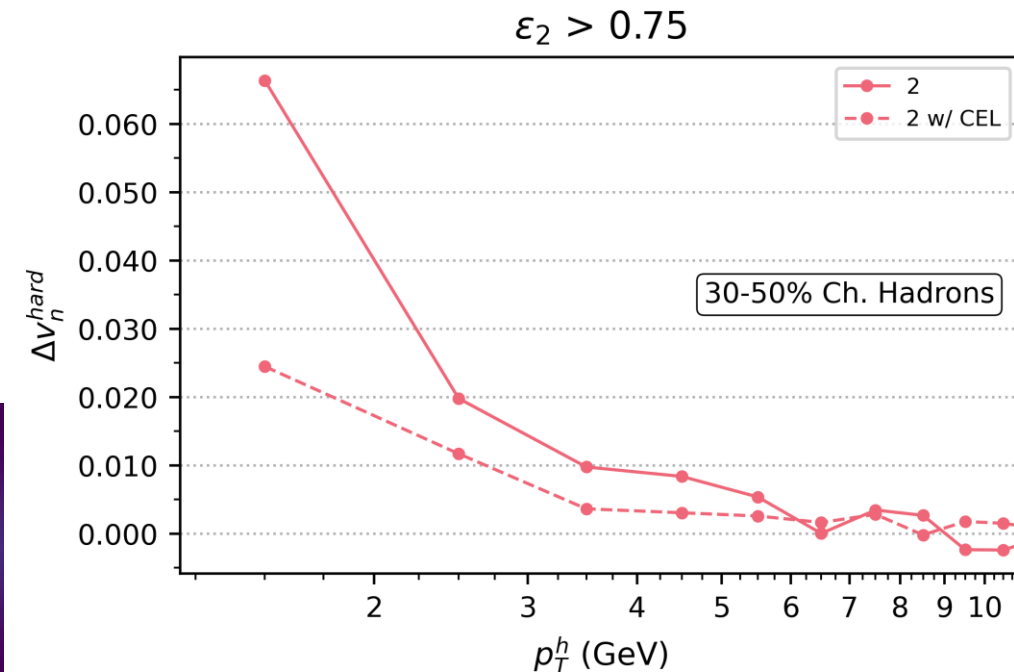
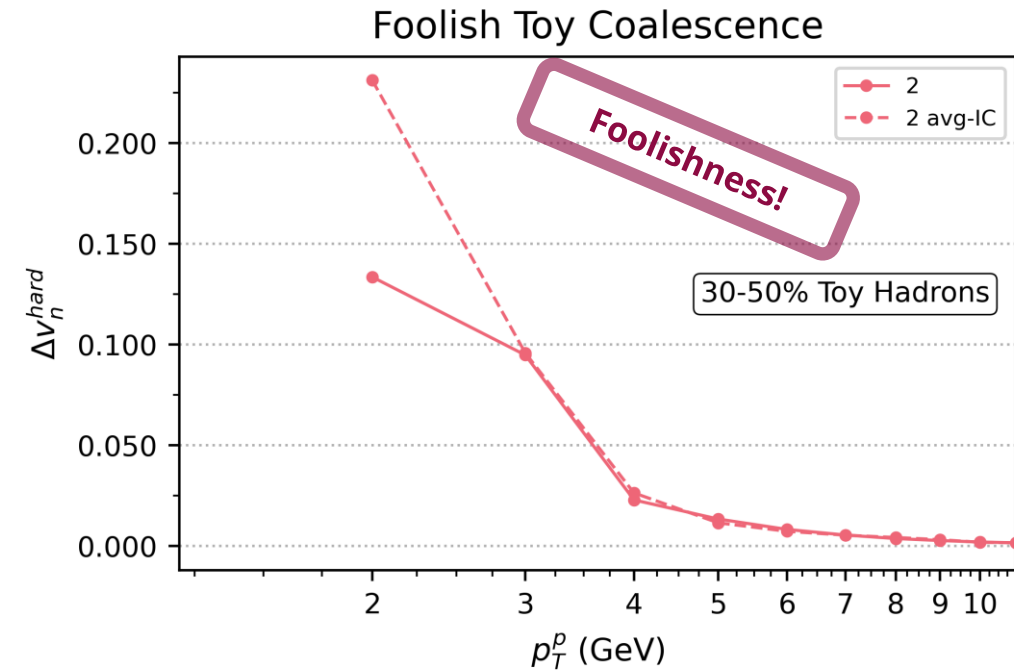
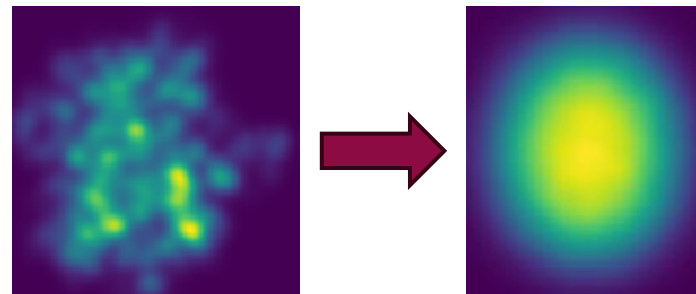
# Vn is Enhanced by Drift

- Large surviving  $v_2$  modulation at low- $p_T$ 
  - Compare to:  $\pm 0.005$  exp. uncertainty
- Conservative estimate of drift
  - Low temp cutoff removes large drift region
  - CNM effects + Coll. Energy loss reduce relative strength



# Effect too Small for You? Many Choices to Enhance!

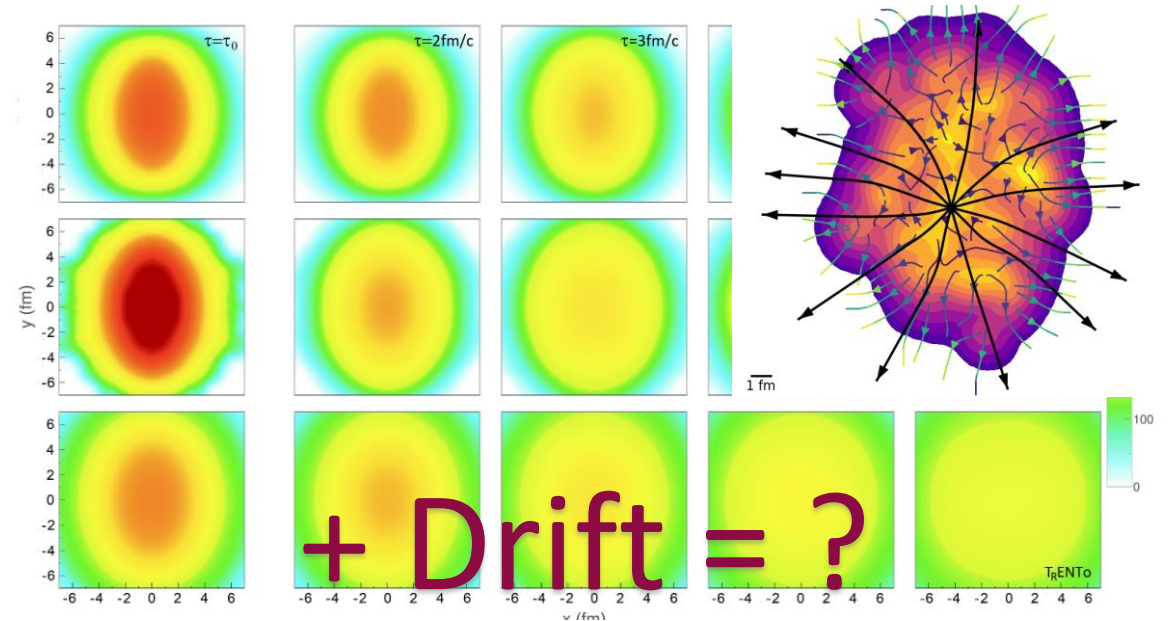
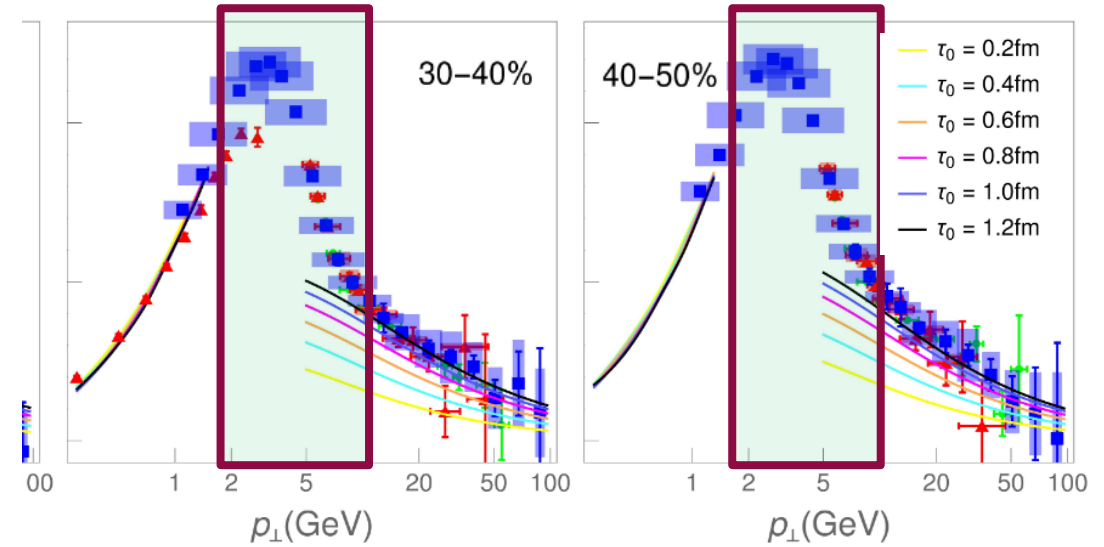
- Take toy coalescence model
  - Say partons pick up collinear 1.5 GeV medium particle, on average
- Fluctuating drift & EL can result in much larger enhancements
- Effect may be large in tuned medium models
  - E.g. enhancement in smoothed events
- Consider cuts on event geometry ( $\epsilon_2$ , or soft  $v_2$ )
  - E.g.  $\epsilon_2 > 0.75$



# Drift $v_n$ sensitive to pathlength ordered internal medium props.

- Drift distinguishes between high anisotropy at early times vs at late times via interplay with energy loss
  - Powerful additional constraint on evolution dynamics!!!
- How would a hard + soft Bayesian parameter extraction like Magdalena's differ with the inclusion of drift?
  - Possibly selects on slightly smaller anisotropy, likely changes story of free streaming parameters

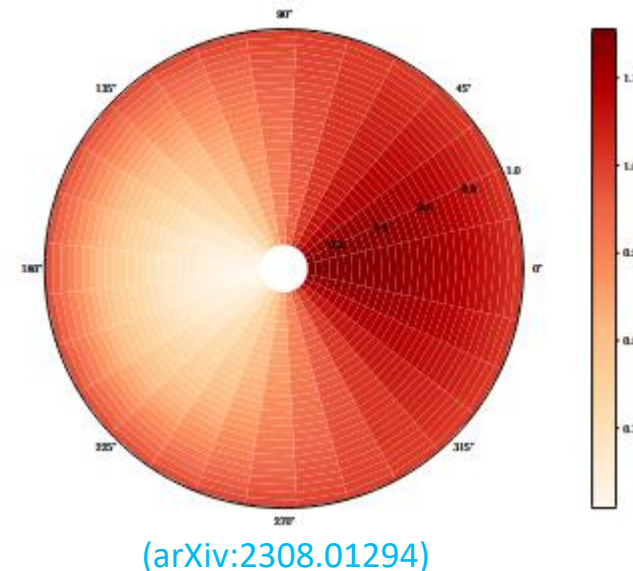
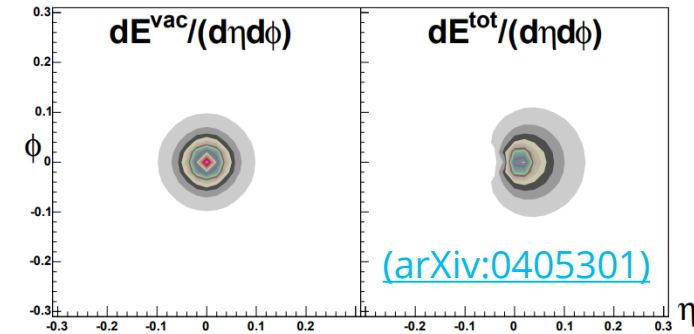
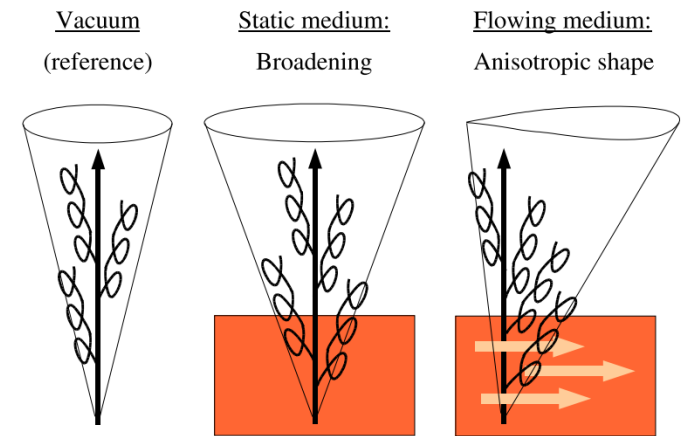
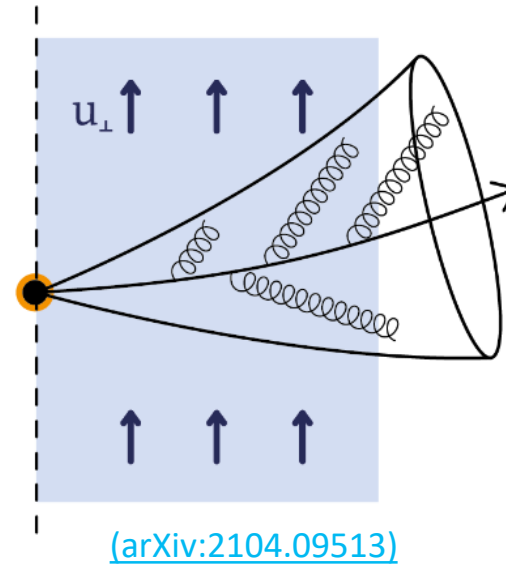
(iNSPIRE:2640923)



(iNSPIRE:2606181)

# Anisotropic Jet Substructure

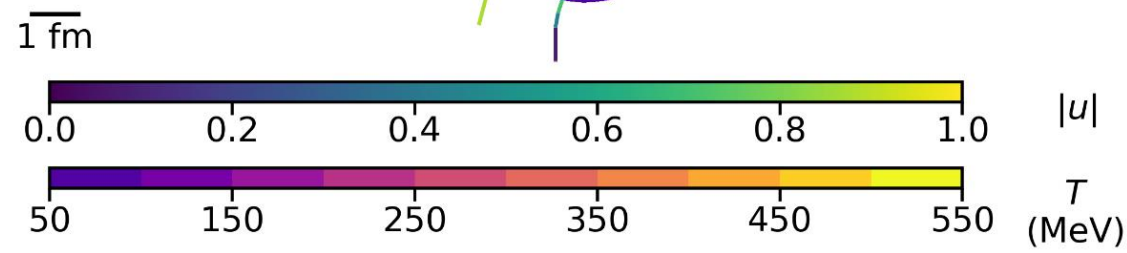
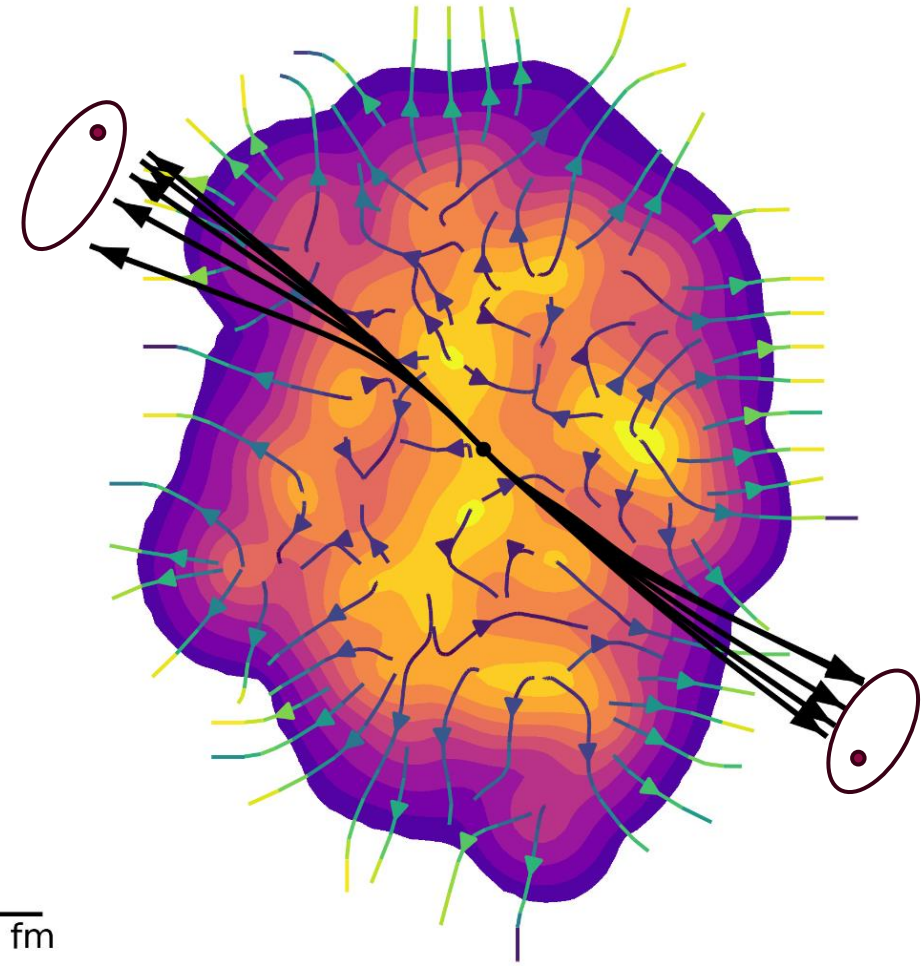
- People have been thinking about anisotropic radiation distribution for some time
  - Armesto, Salgado, & Wiedemann (2004) Flow anisotropy as Lorentz boost: <https://inspirehep.net/literature/651342>
  - Sievert, Sadofyev, Vitev (2021) Perturbative scalar calculation of radiation: <https://inspirehep.net/literature/1859289>
  - Barata, Milhano, & Sadofyev: Jet substructure harmonics: <https://inspirehep.net/literature/2684595>
  - Kuzmin & López Perturbative real gluon calculation of radiation: <https://inspirehep.net/literature/2801226>
- Drift of jet particles is also likely important!



# Drift of Ensemble of Particles

$\Delta j, v_n$  of substructure

- Energy suppression naturally produces dispersion of hard and soft particles within jet
- Sub-eikonal property a detriment for inclusive measurements, but well suited for jet substructure modification



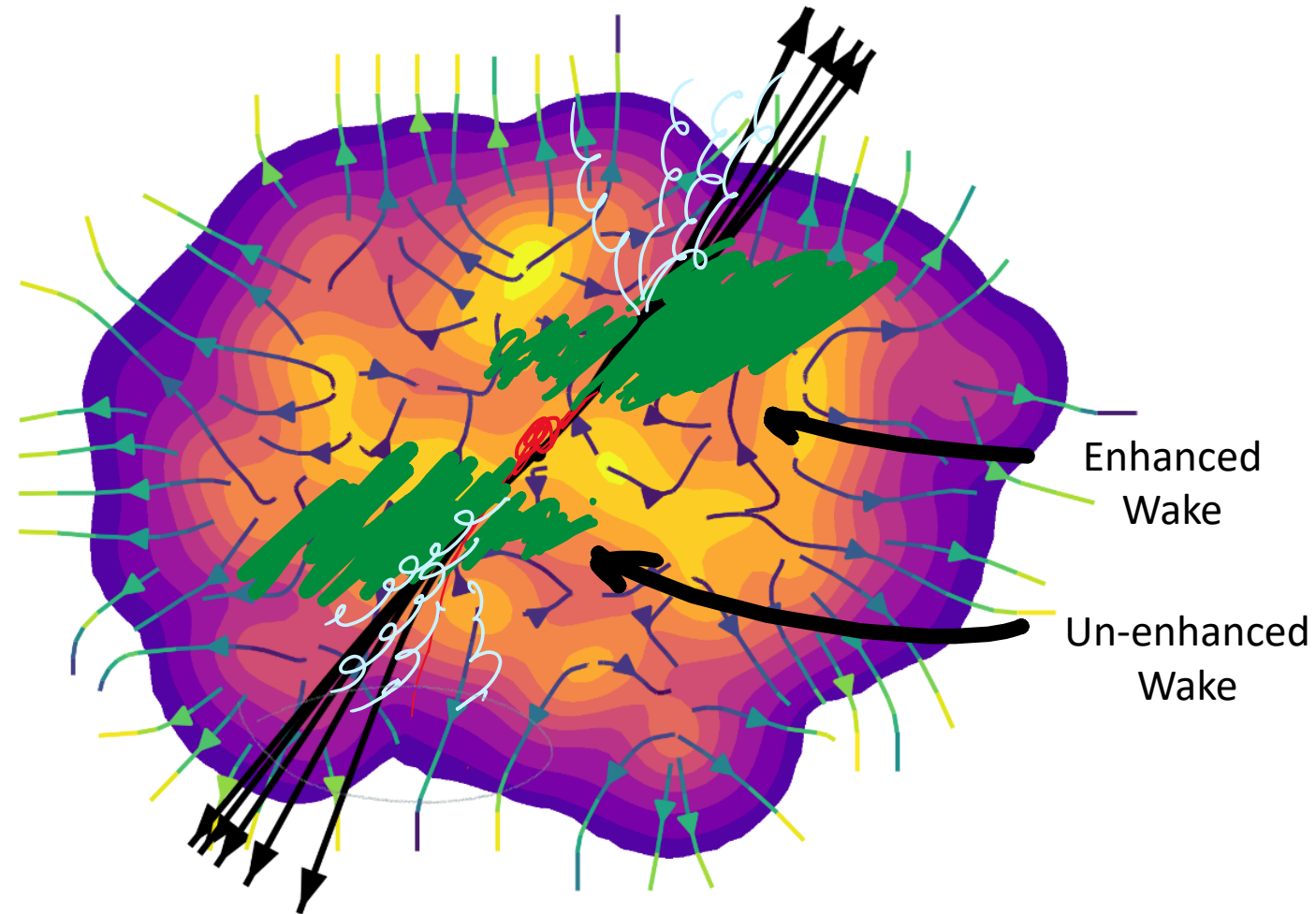
$$\langle \vec{q}_{drift} \rangle = \hat{e}_\perp \int d\tau \frac{3}{E(\tau)} \frac{\mu^2(\tau)}{\lambda(\tau)} \ln \frac{E(\tau)}{\mu(\tau)} \frac{u_\perp(\tau)}{1 - u_\parallel(\tau)}$$

Energy suppressed

# Anisotropic Jet Wake

Does  $Z^0$  wake measurement show anisotropy relative to event plane at any scale???

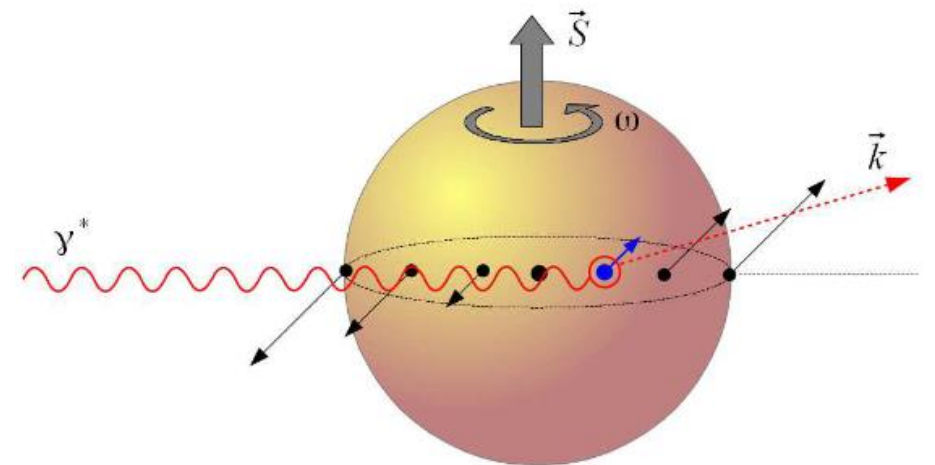
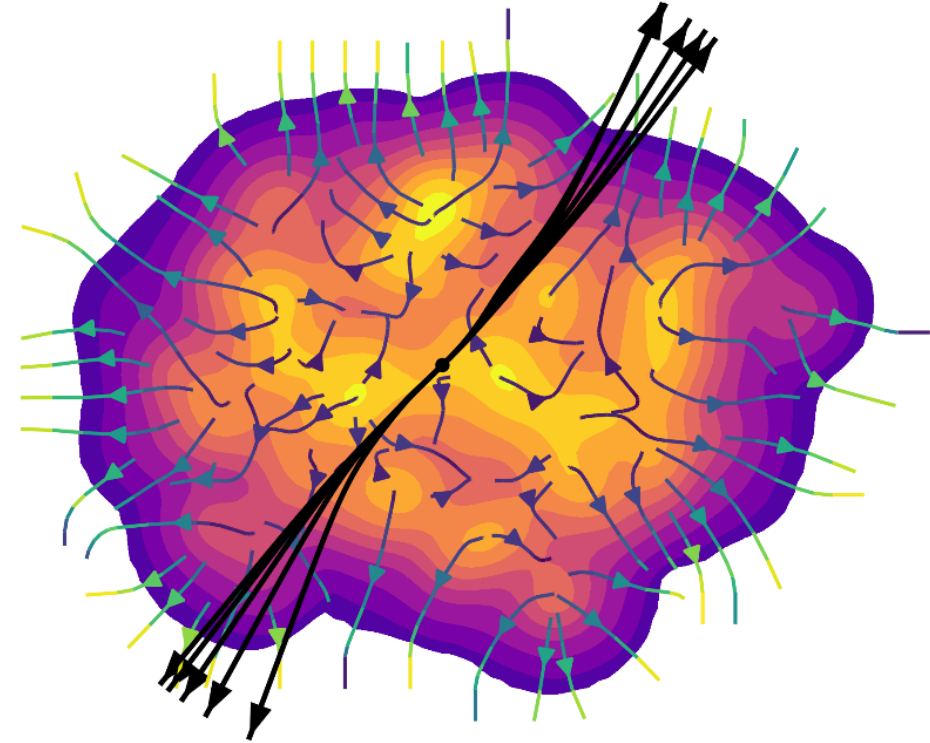
- Conservation of momentum – should be anisotropic wake
  - Constructive with induced radiation anisotropy
- How does this interplay with jet substructure anisotropies?
  - Possible anisotropic background contamination of jet substructure observables





# Next Steps:

- Jet Substructure
  - Drift-dispersion + flow-induced radiation => jet substructure anisotropy
  - Jo Bahder, Hasan Rahman, Matt Sievert, & Ivan Vitev
- CNM drift investigations
  - Drift due to polarized nuclei
  - Nicholas Baldonado, Alex Garcia, & Matt Sievert
  - Add to APE MC for estimate
- Complete survey of important interactions to  $\mathcal{O}\left(\frac{\mu}{E}\right)$

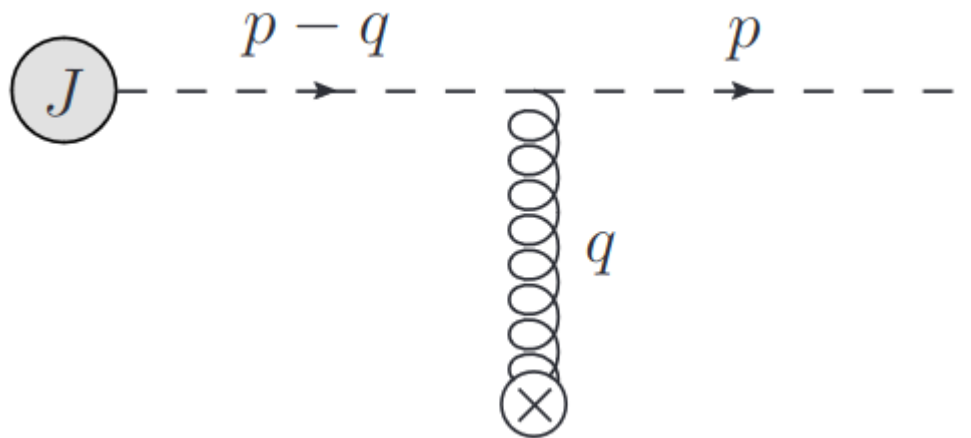


(arXiv:1310.5028)

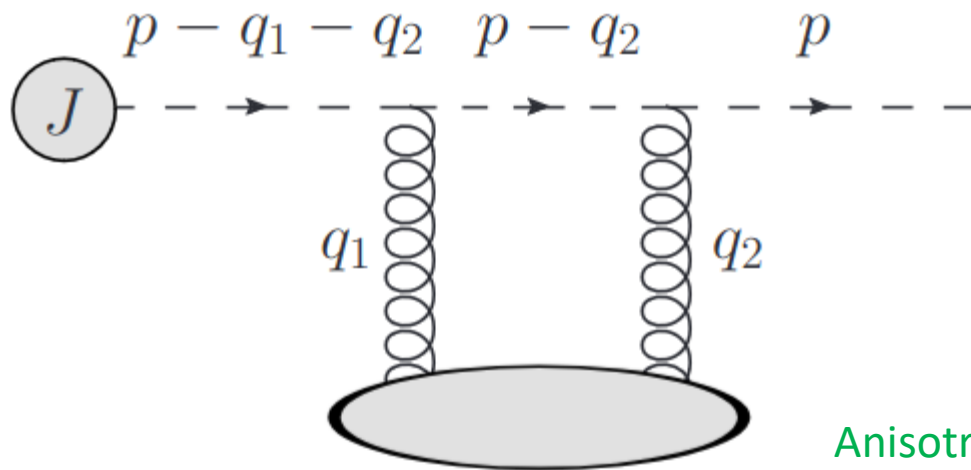
Please Watch Out  
for the Paper in the  
Coming Weeks!

See Hasan Rahman's  
Talk at SoftJet Satellite  
meeting for investigation of drift  
correlations to medium  
properties!

# Jet Broadening – Isotropic vs Anisotropic



A. V. Sadofyev, I. Vitev,  
& M. D. Sievert  
Phys.Rev.D 104 (2021)  
([arXiv:2104.09513](https://arxiv.org/abs/2104.09513))



Anisotropic

$$g a_i^{\mu a}(q) = t_i^a u_i^\mu v_i(q) (2\pi) \delta(q^0 - \mathbf{u}_i \cdot \mathbf{q})$$

Preferred direction!

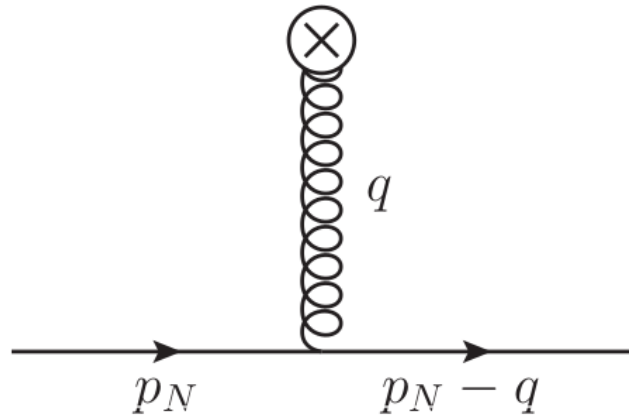
$$a_i^{\mu a}(q) = g^{\mu+} (t^a)_i \left[ 2\pi \delta(q^+) \right] \left[ \frac{-g_{eff}}{q_T^2} \right]$$

No vector info

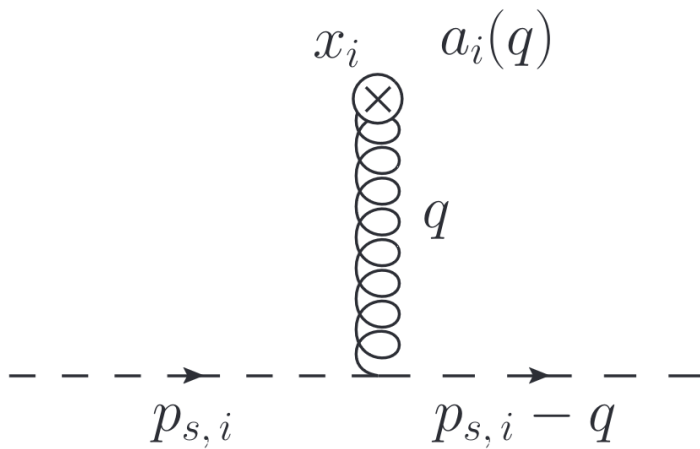
- Difference in setup – constraints on external gluon field
- Isotropic
  - Jet quark moves lightcone (+), medium quark moves lightcone (-)
- Anisotropic
  - Jet quark moves lightcone (+), medium quark moves with medium flow
- Two vector directions associated with the medium
  - Flow
  - Gradients

# Medium Gluon Field Potentials

Simple Isotropic Potential



$$a_i^{\mu a}(q) = g^{\mu+} (t^a)_i \underbrace{[2\pi\delta(q^+)]}_{\text{Eikonal delta function (antiparallel)}} \underbrace{\left[\frac{-g_{eff}}{q_T^2}\right]}_{v(q) \text{ Isotropic scattering centers}}$$



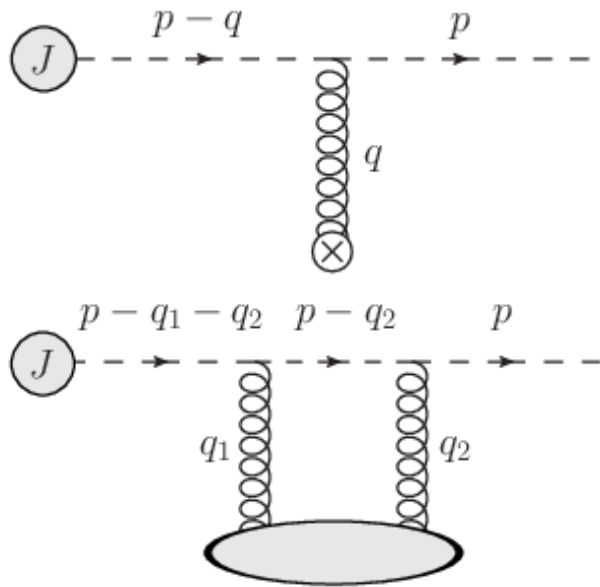
$$g a_i^{\mu a}(q) = t_i^a u_i^\mu v_i(q) (2\pi) \delta(q^0 - \mathbf{u}_i \cdot \mathbf{q}) \left. \vphantom{g a_i^{\mu a}(q)} \right\} \text{Quark moves with medium}$$

$$v_i(q) \equiv v_i(\mathbf{q}^2 - (\mathbf{u}_i \cdot \mathbf{q})^2) \equiv \underbrace{\frac{-g^2}{\mathbf{q}^2 + \mu_i^2 - (\mathbf{u}_i \cdot \mathbf{q})^2 - i\epsilon}}_{v(q) \text{ Directional scattering centers}}$$

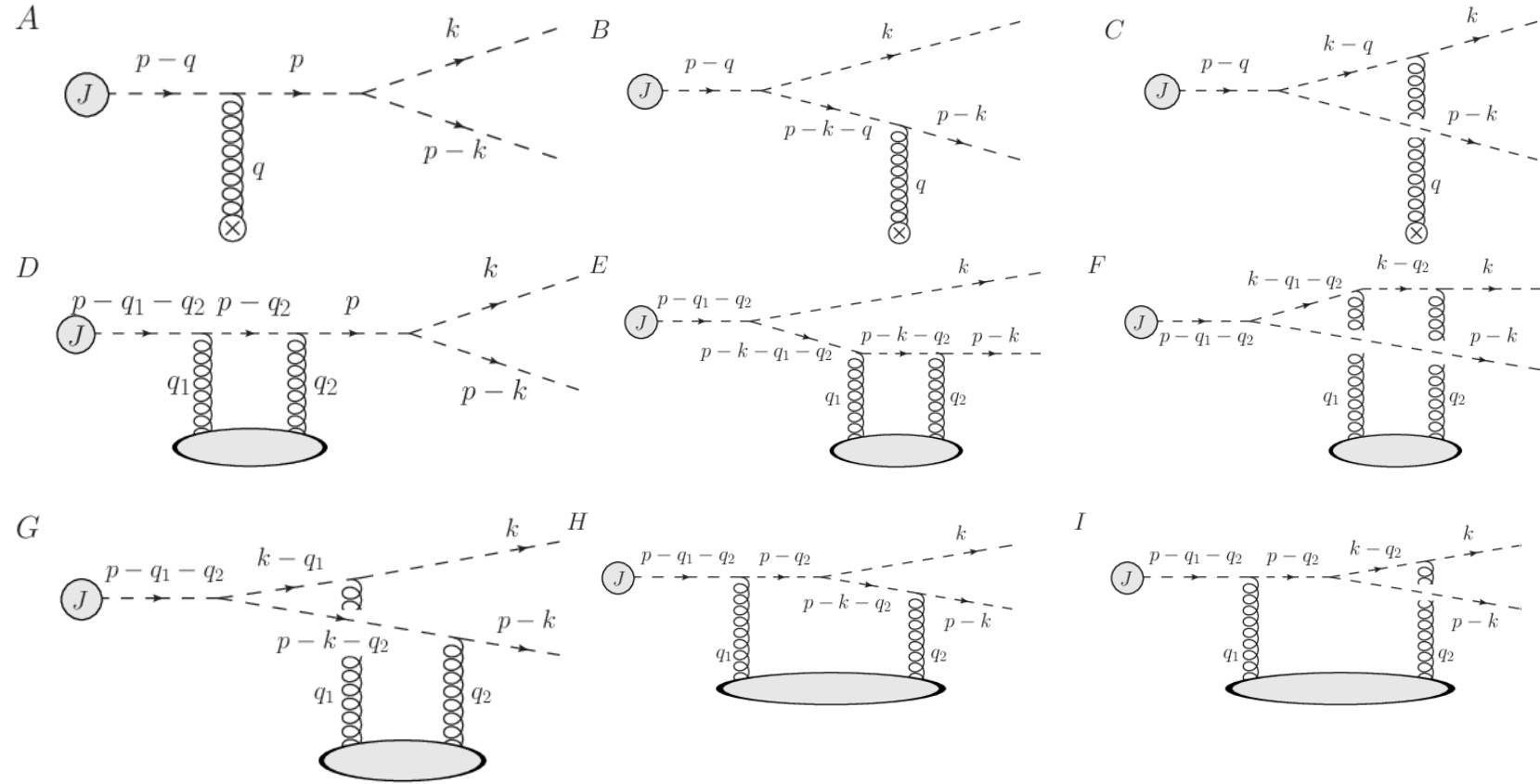
Anisotropic Flow Potential  
Regge Kinematics

A. V. Sadofyev, I. Vitev,  
& M. D. Sievert  
Phys.Rev.D 104 (2021)  
[arXiv:2104.09513](https://arxiv.org/abs/2104.09513)

# All Diagrams



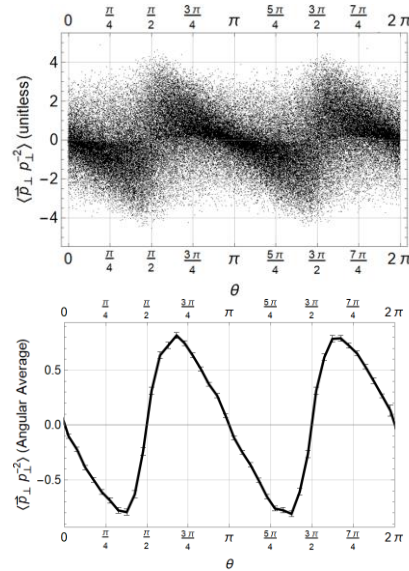
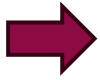
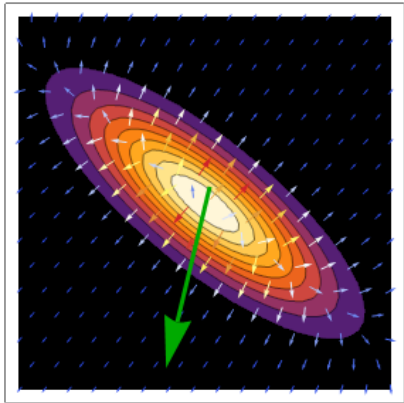
Born & Double-Born  
Momentum Broadening  
Diagrams



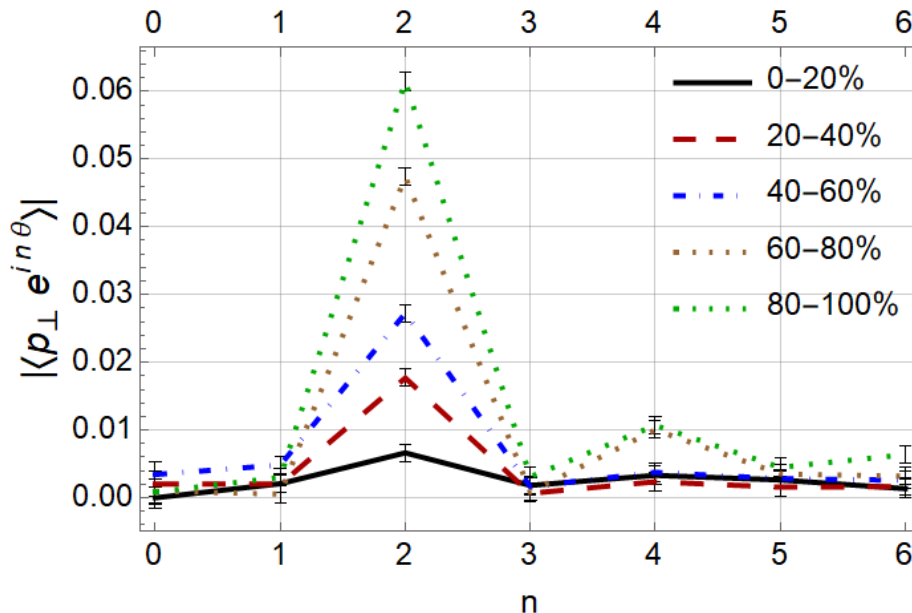
Born & Double-Born  
Radiation Diagrams

# Does Drift Survive Event Averaging?

L. Antiporda, J. Bahder,  
H. Rahman  
& M. D. Sievert  
Phys.Rev.D 105 (2022)  
([arXiv: 2110.03590](https://arxiv.org/abs/2110.03590))



Harmonic  
Analogous to  
 $v_n^{hard}$



- Naively, one might expect cancellation via event averaging
- Coupling to event anisotropic flow shown in glauber elliptic geometry to preserve effect
  - Fluctuating event plane, centrality
- What about in realistic heavy ion collisions?

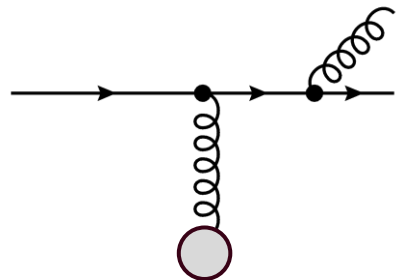
# Energy Loss Effects

## Radiative

$$\frac{dE}{d\ell} = -\frac{d}{dL} \left( \frac{2C_R\alpha_s}{\pi} \frac{L}{\lambda} E \int_{k_{min}}^{k_{max}} \frac{dk}{k} \int_0^{q_{max}} dq q \int_0^{2\pi} d\phi \right. \\ \left. \times \frac{\mu^2}{\pi(q^2 + \mu^2)^2} \frac{2\mathbf{k} \cdot \mathbf{q} (\mathbf{k} - \mathbf{q})^2 L^2}{16x^2 E^2 + (\mathbf{k} - \mathbf{q})^4 L^2} \right)_{L=\ell}$$

- Single Emission GLV @ 1<sup>st</sup> order in opacity w/ finite kinematic bounds (q, k)
- Interpolated tabulated results
- Gyulassy, Levai, Vitev (2000) ([arXiv:0006010](https://arxiv.org/abs/0006010))

E.g.

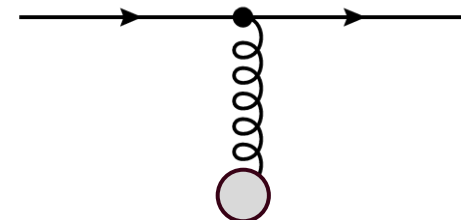


## Collisional

$$\frac{dE}{d\ell} = -C_R \frac{1}{2} \mu^2 \ln \left( 2^{\frac{N_f}{2(6+N_f)}} 0.920 \frac{\sqrt{3ET}}{\mu} \right)$$

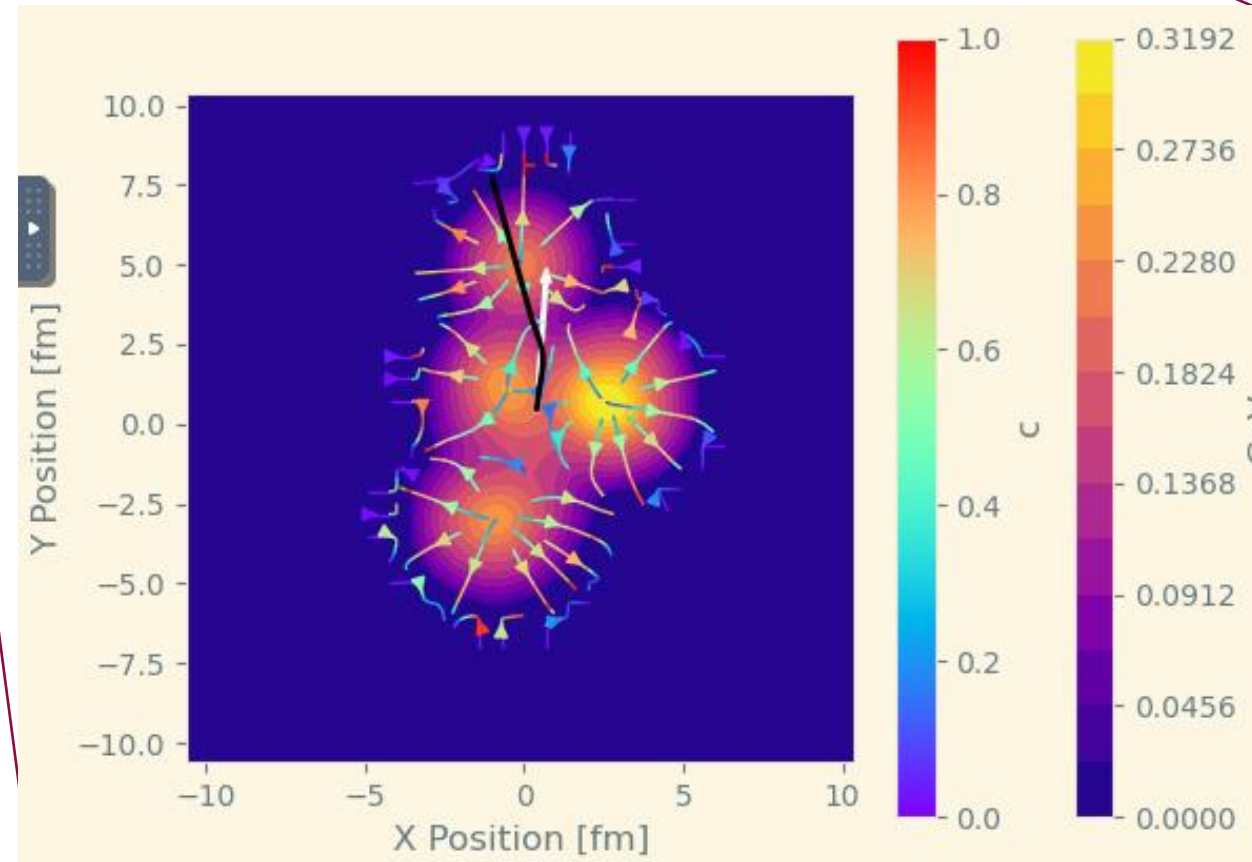
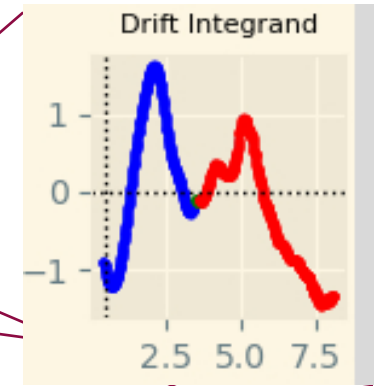
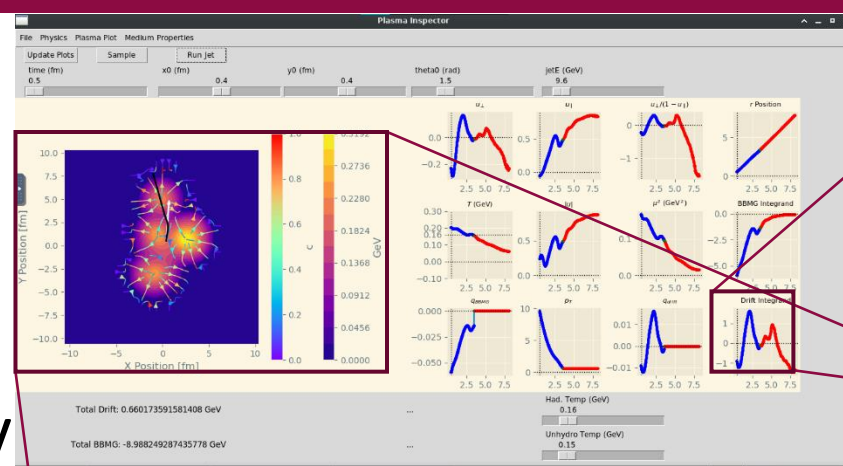
- Braaten & Thoma (1991) ([iNSPIRE:317898](https://arxiv.org/abs/hep-th/9103017))
- Light quarks:  $E \gg m^2/T$  regime
- Gluons:  $CA/CF = 9/4$  ([arXiv:2305.13182](https://arxiv.org/abs/2305.13182))

E.g.



# Ape Trajectories

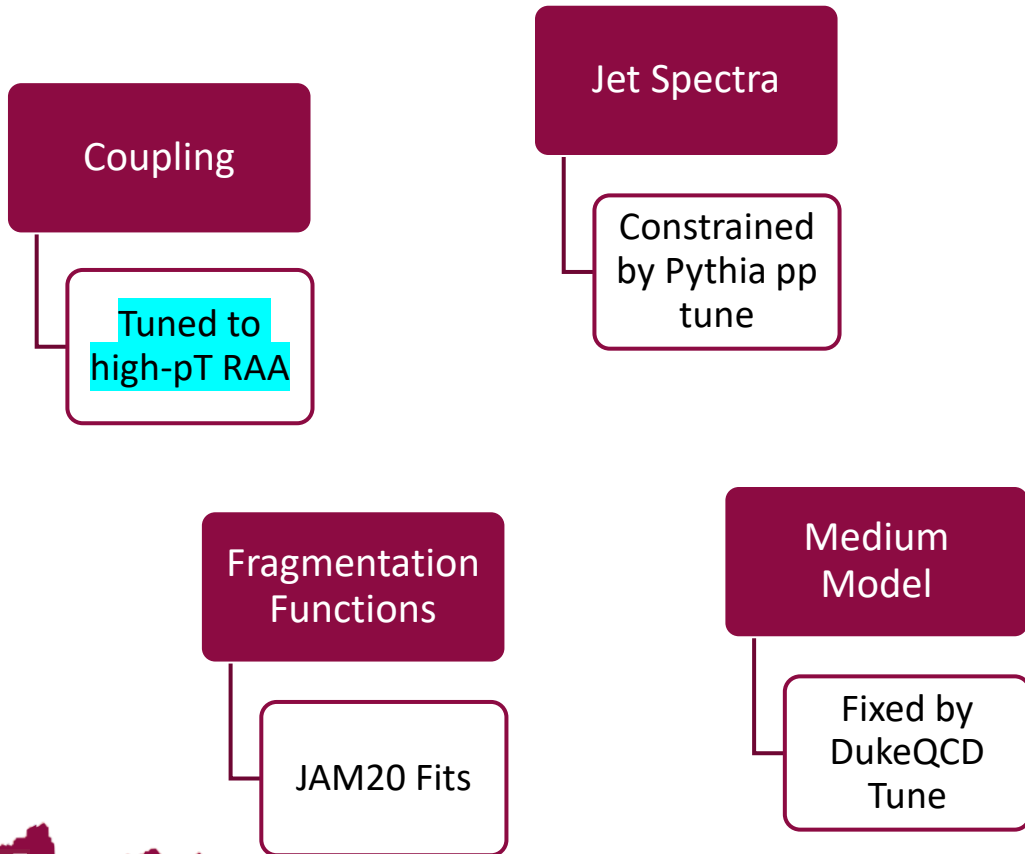
- Approx. Binary collision density weighting of production points
- Computed within QGP phase of hydro backgrounds
  - EL & Drift cut off at  $T < 155$  MeV
  - Cuts off highest flow region!!!
- Dynamic trajectories respond to medium flow
  - Deflections, zigzags, weirdness





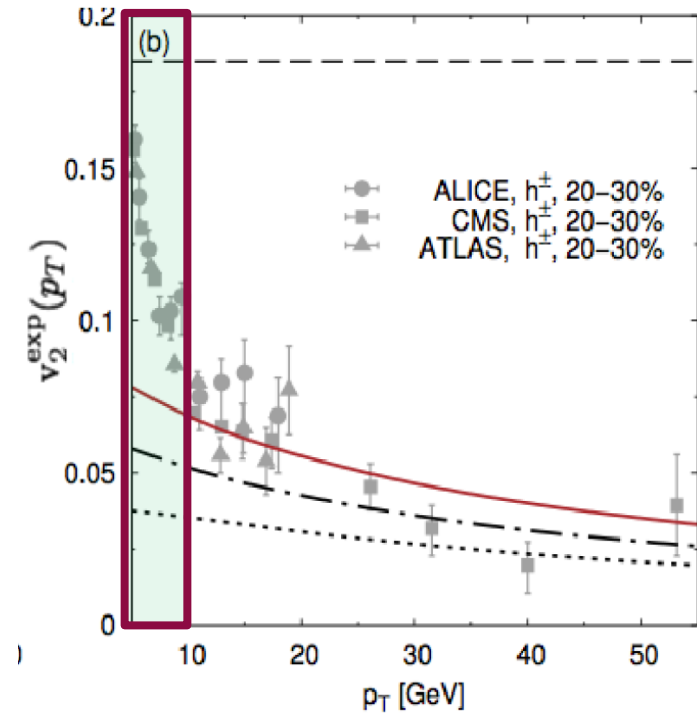
# Parameter Fits & Model Choices

- DukeQCD “hic-eventgen” medium model parameters set by Bayesian parameter estimation  
[arXiv:1804.06469](https://arxiv.org/abs/1804.06469)
- Pythia input + pCNM determines partonic spectra
- Coupling from high pT RAA (30-50%)
- Choice of fragmentation function fits
  - Large change to scale of results!



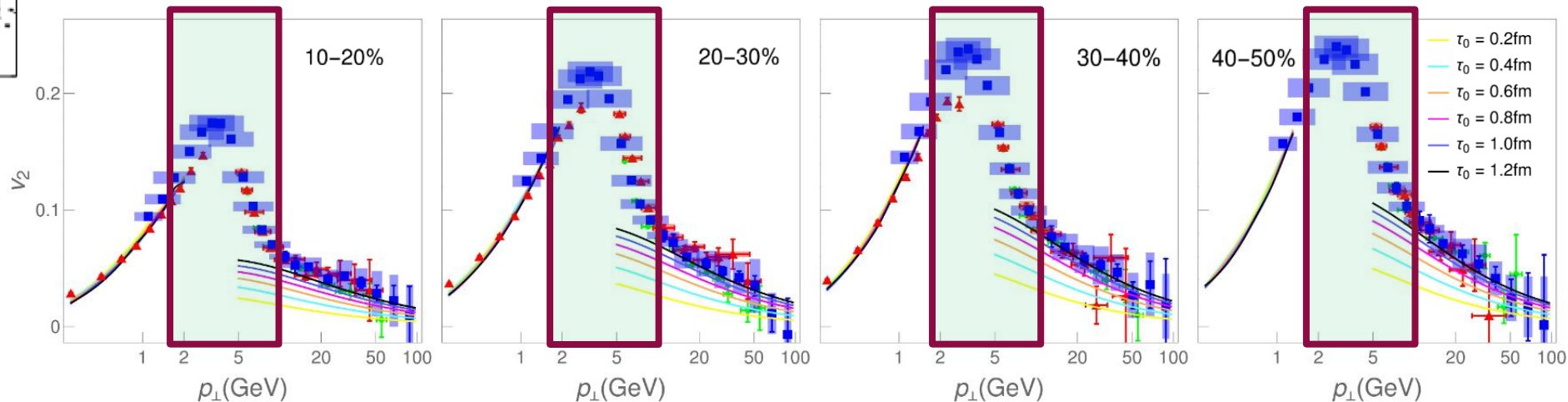
# Importance for the $R_{AA} \times v_2$ Puzzle

Drift produces measurable elliptic modulation at low  $p_T$  that qualitatively matches elliptic flow missing in perturbative & similar calculations!

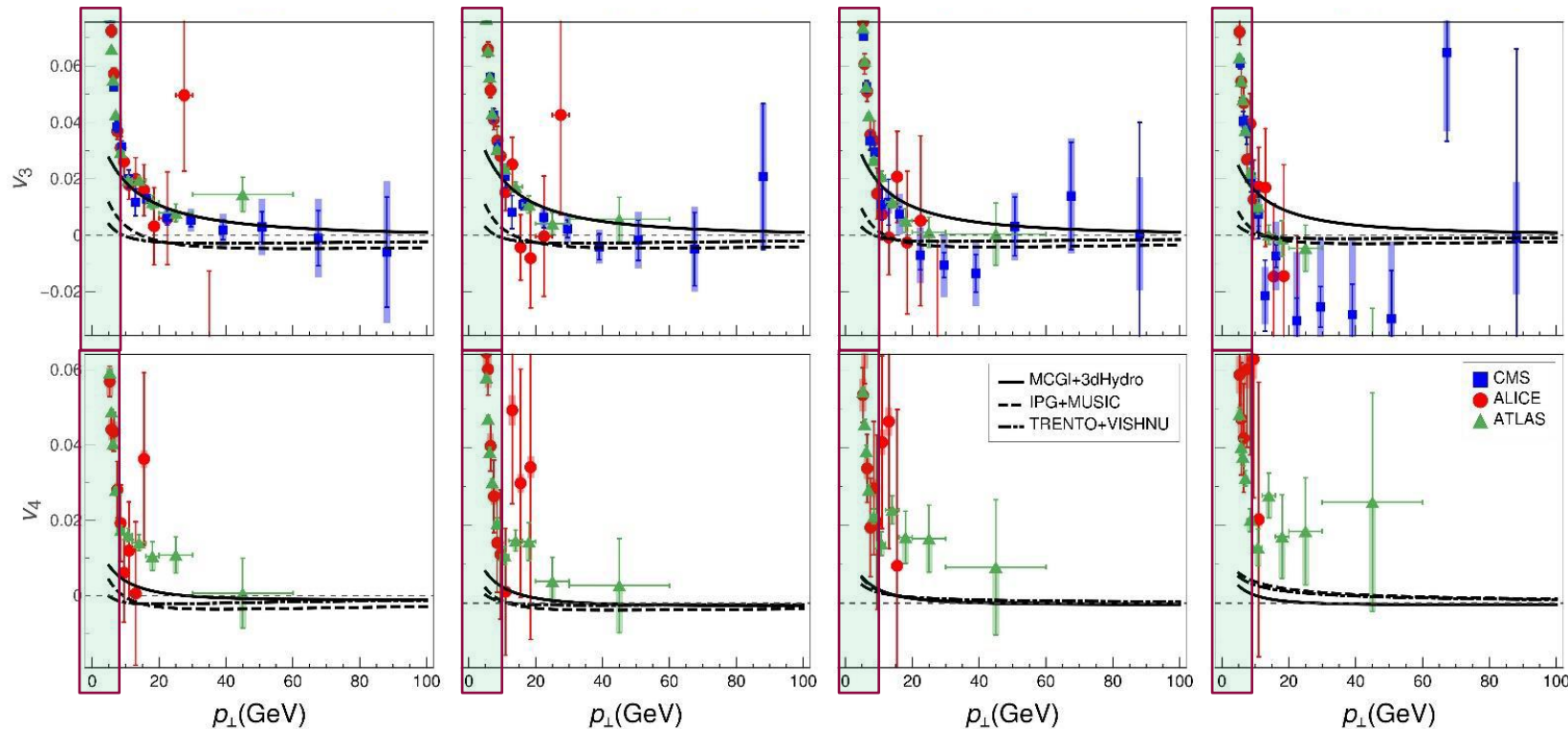


← Parametric Energy Loss  
Noronha-Hostler et al:  
[arXiv: 1602.03788](https://arxiv.org/abs/1602.03788)

↙ DREENA-A Ch. Had.  
LHC PbPb  
sqrt(s) = 5.02 TeV  
Perturbative Energy Loss  
Stojku et al.  
[iNSPIRE:2640923](https://arxiv.org/abs/1602.03788)



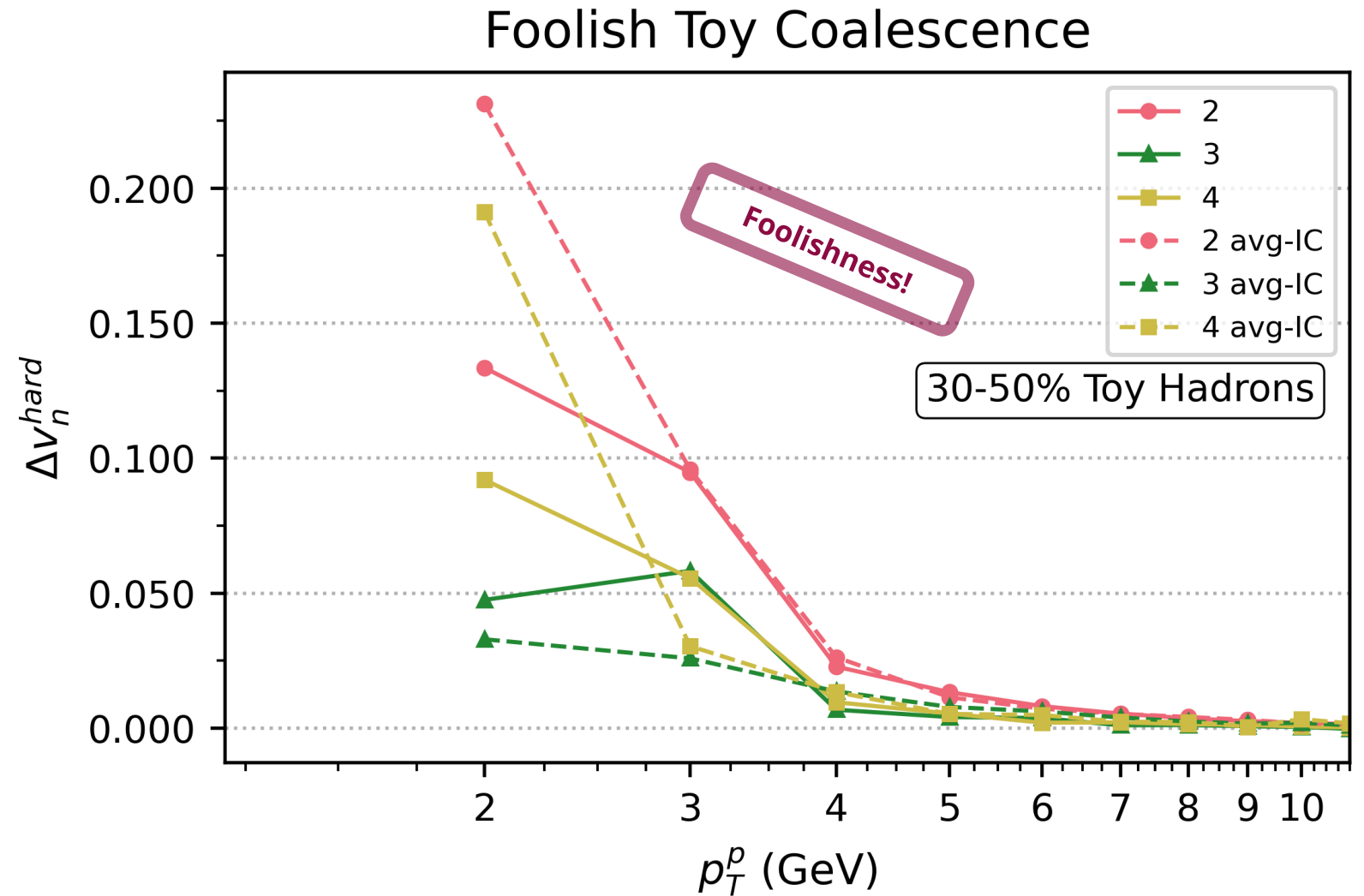
# v3 & v4 from Perturbative Energy Loss



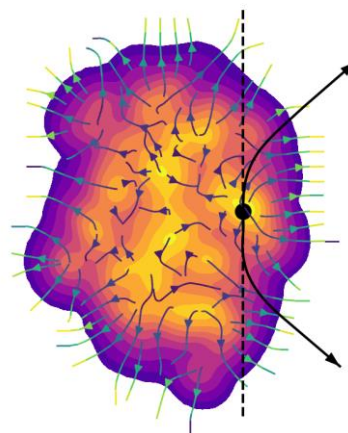
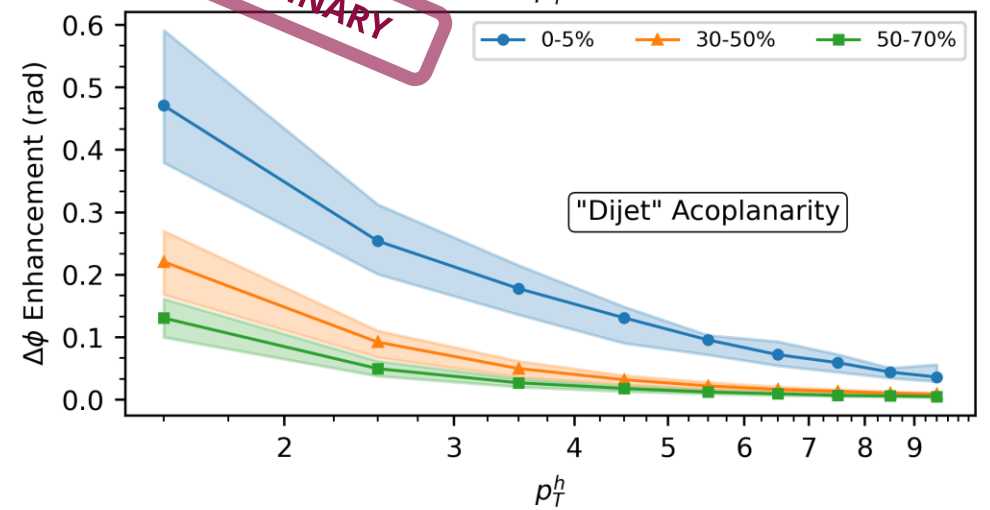
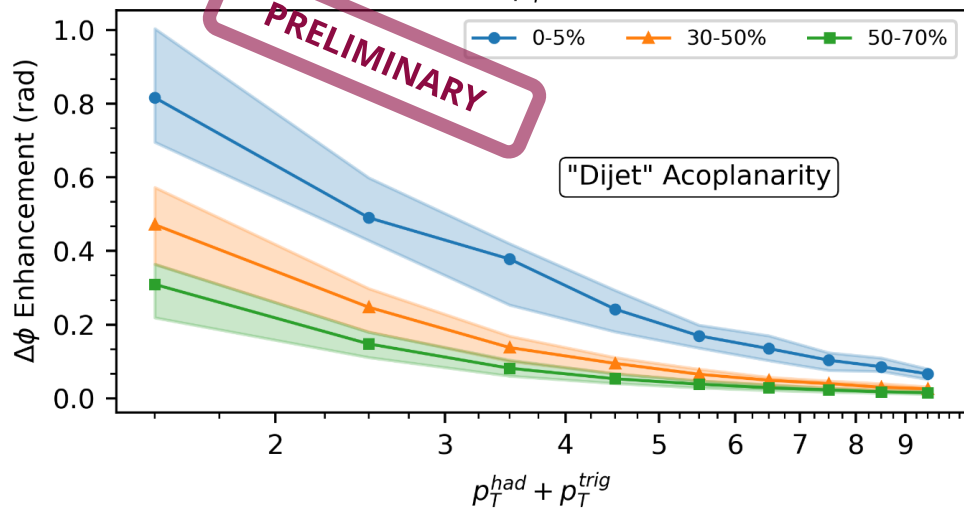
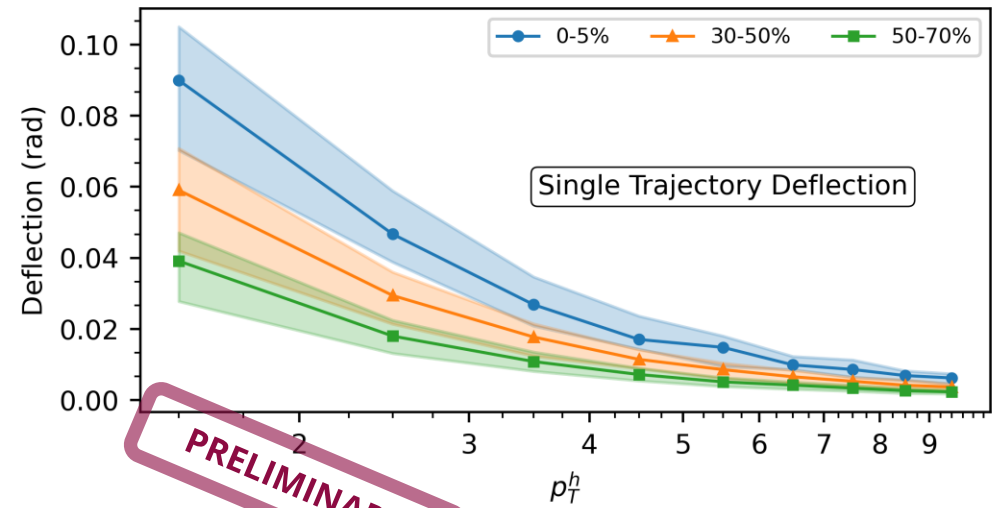
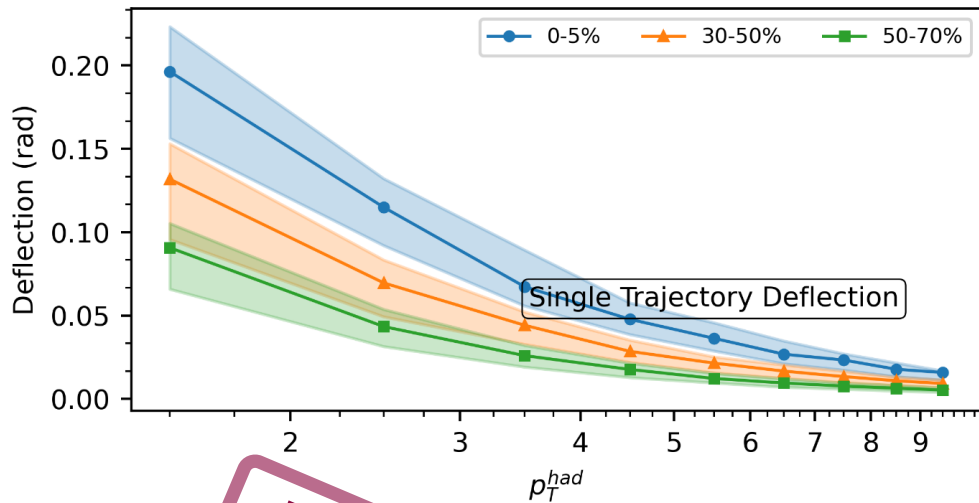
- Drift produces higher harmonic coupling
- Possible importance to  $v_3$  &  $v_4$
- Difficult to couple to small anisotropies with energy loss alone

[arXiv:2208.09886](https://arxiv.org/abs/2208.09886)

# Toy Coalescence with v3 & v4



# Acoplanarity Enhancement RAD + CEL v. RAD



Rad. EL + Drift

Rad. EL + Coll. EL + Drift

# Drift at the EIC

- Cold nuclear matter anisotropies can couple similarly to QGP flow
  - “Spin flow”, gradients, etc.
- Possible distinction between pre-equilibrium and equilibrium anisotropy
  - Could provide constraints on pre-equilibrium qhat
- Possible large impact on tomographic parameter extraction via hard probes
- Comparative laboratory for jet substructure dispersion

