

The two-point energy correlator in the QGP: from gamma+jet to inclusive jets

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MIT

Hard Probes 2024

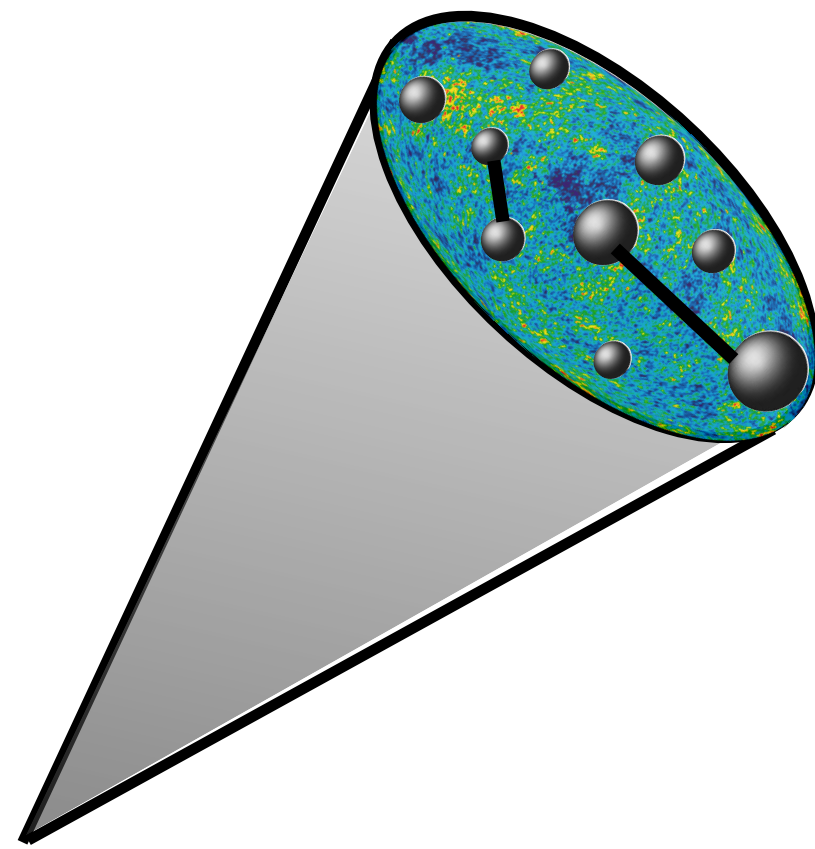
Nagasaki, September 23-27, 2024



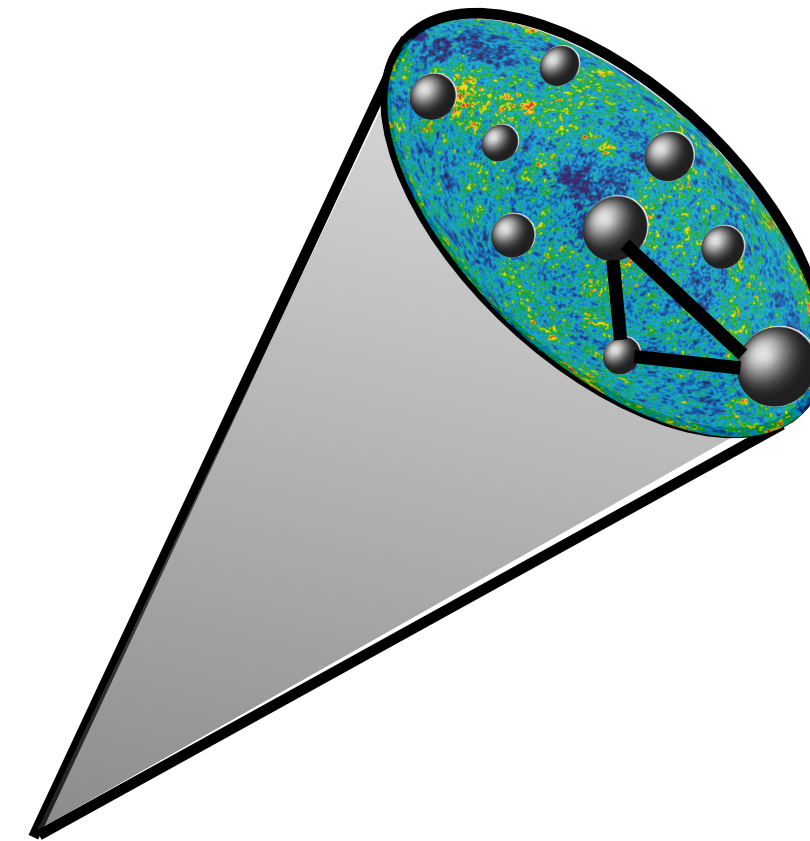
Energy correlators within jets

- Correlators $\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \cdots \mathcal{E}(\vec{n}_k) \rangle$ of the **energy flux**:
- **Exceptional angular resolution** of modern detectors provide us with an unprecedented opportunity to analyze the **energy flow within jets**

Jet substructure: energy flow operators are brought together (collinear limit)



$$\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \rangle$$



$$\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \mathcal{E}(\vec{n}_3) \rangle$$

- Jet substructure: **study of multi-point energy correlators** within jets (collinear limit)

E2C within p-p jets

$$\frac{d\Sigma_{\text{E2C}}}{dR_L} = \frac{1}{\sigma} \sum_{i,j} \int dE_i dE_j \frac{d\sigma}{dE_i dE_j dR_L} \frac{E_i E_j}{Q^2}$$

- Within jets: **collinear** (or OPE) limit of E2C

$$\langle X | \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) | X \rangle \xrightarrow{R_L \rightarrow 0} \sum_i R_L^{(\tau_i - 4)/2} \mathcal{O}_i(\vec{n}_1)$$

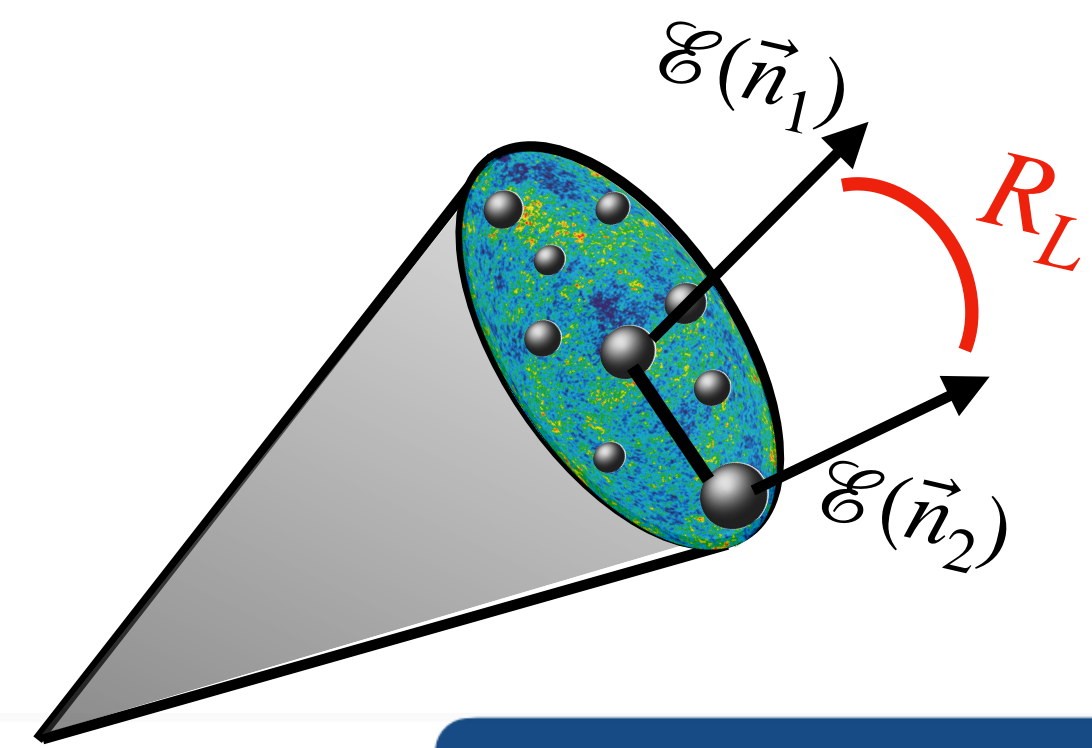
Hoffman, Maldacena,
[0803.1467](#)

Dixon, Moult,
Zhu, [1905.01310](#)

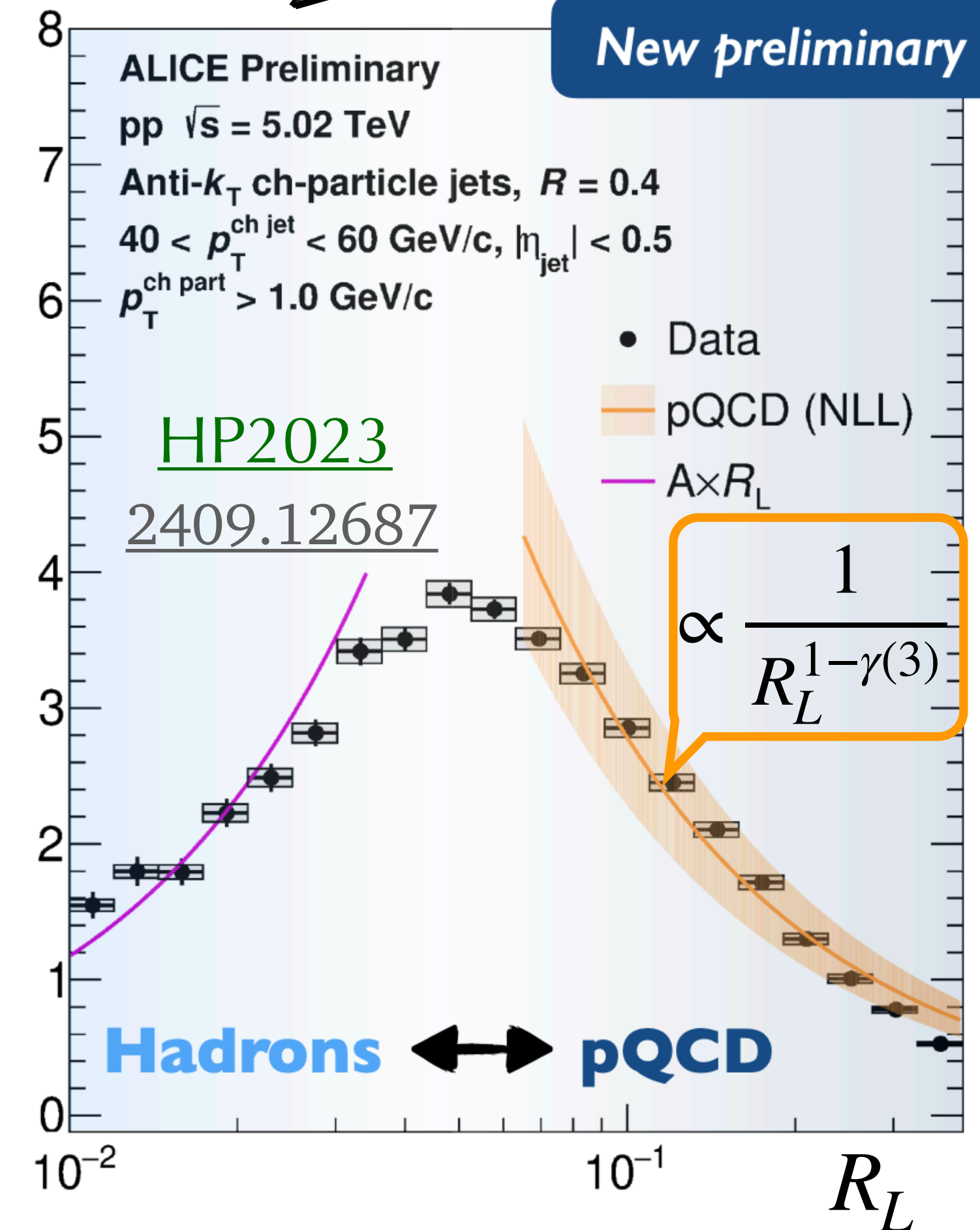
$$\frac{d\Sigma_{\text{E2C}}}{dR_L} \propto \frac{1}{R_L^{1-\gamma(3)}}$$

Power-law scaling according to CFT!

QCD scaling observed by STAR, ALICE, and CMS in jets
from 15 GeV to ~2TeV!



$$\frac{1}{N_{\text{jet}}} \times \frac{dN_{\text{EEC}}}{d\theta}$$



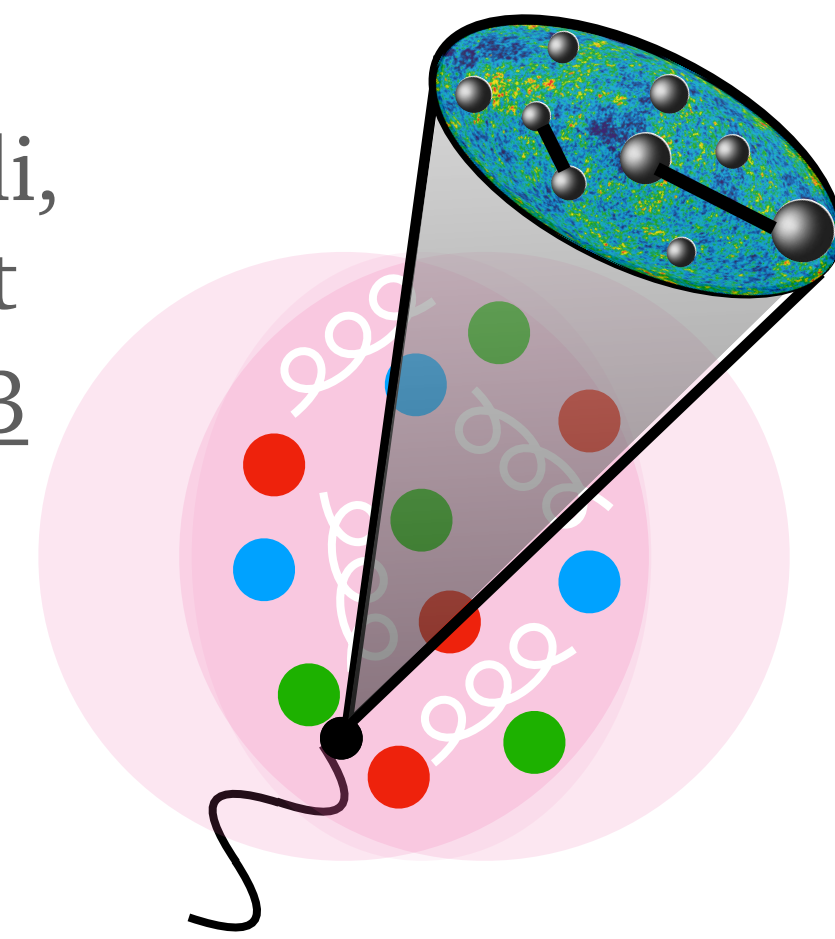
See also: CMS, [2402.13864](#), and STAR [2309.0576](#)

Proof of principle in HICs

CA, Dominguez, Elayavalli,
Holguin, Marquet, Moul
2209.11236, 2303.03413

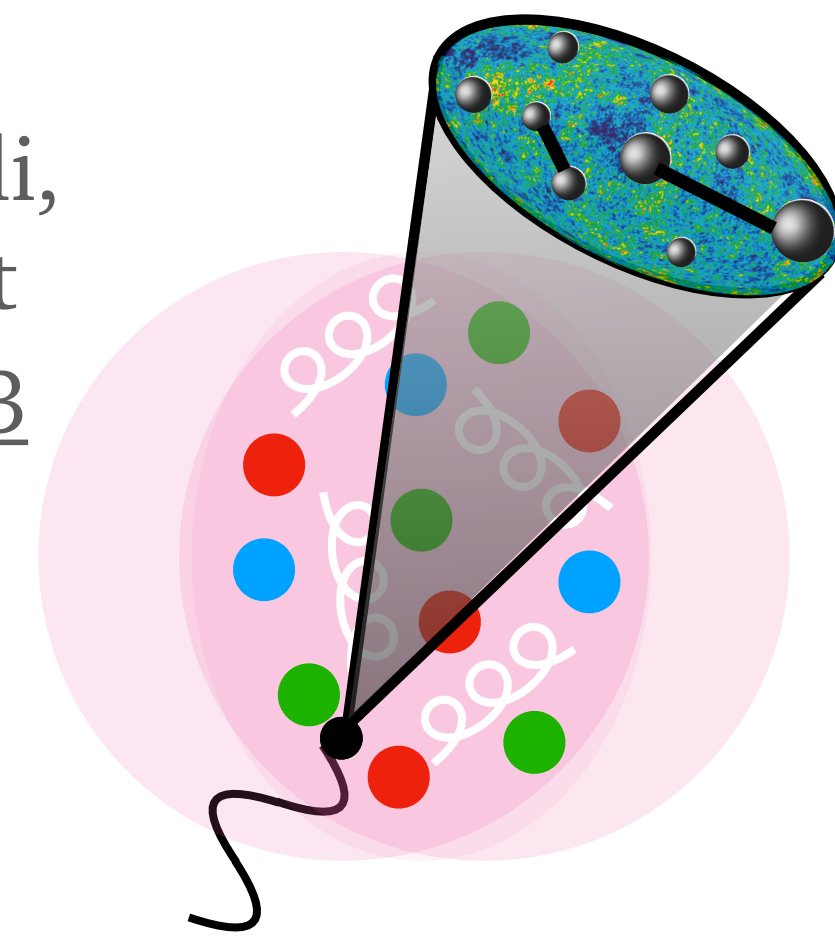
- Quark-initiated jet with known initial energy $Q = E$ (γ/Z -jet)

$$\frac{d\Sigma_{E2C}}{dR_L} = \frac{1}{\sigma_{qg}} \int dz \left(\frac{d\sigma_{qg}^{\text{vac}}}{dzdR_L} + \frac{d\sigma_{qg}^{\text{med}}}{dzdR_L} \right) z(1-z) + \mathcal{O}\left(\frac{\mu_s}{E}\right)$$



Proof of principle in HICs

CA, Dominguez, Elayavalli,
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[2209.11236](#), [2303.03413](#)



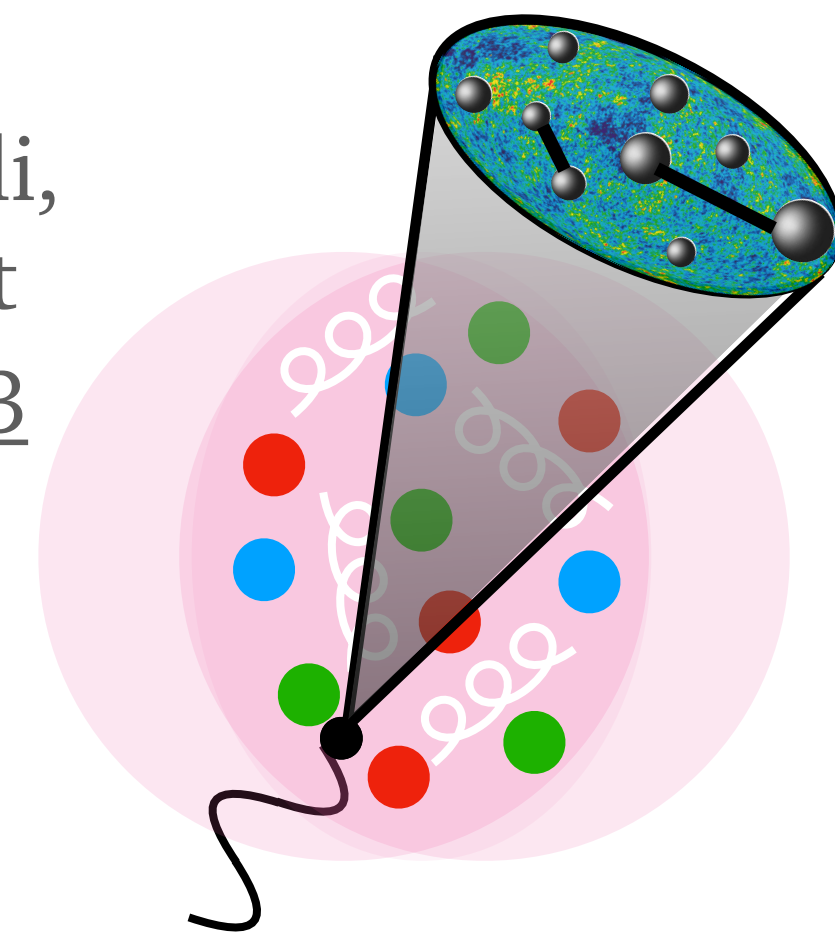
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Includes collinear
resummation

Proof of principle in HICs

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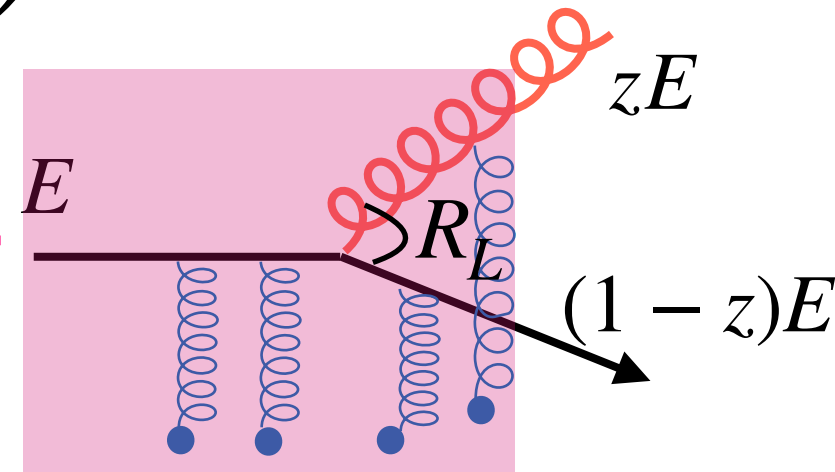


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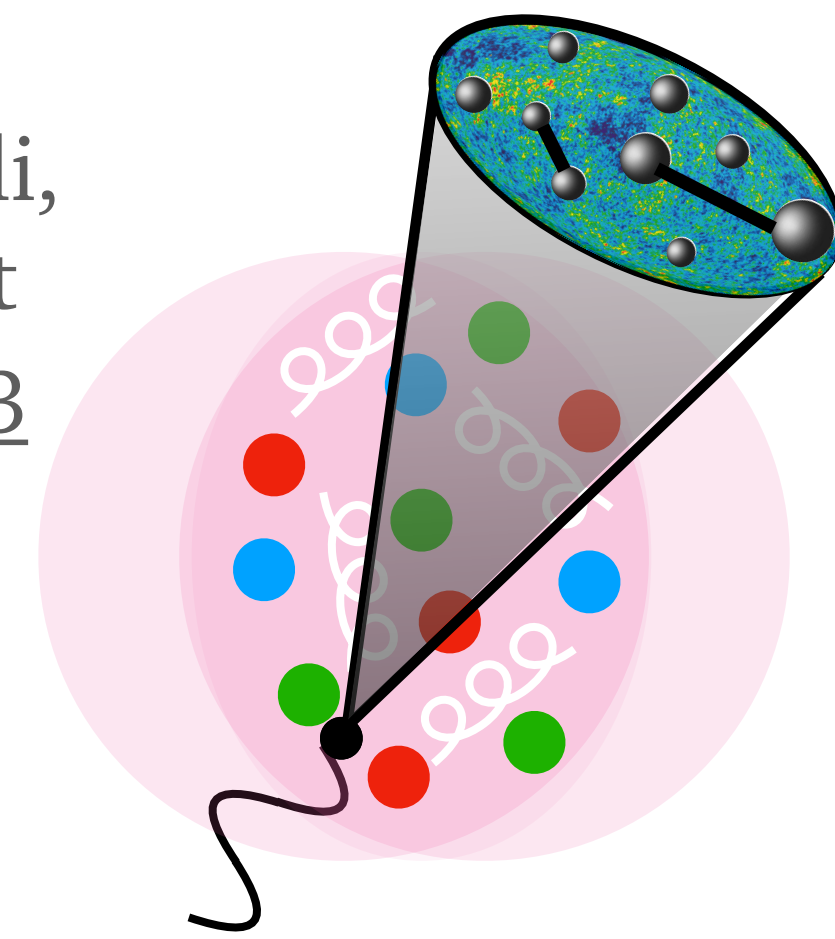
Includes collinear
resummation

LO in the number
of splittings



Proof of principle in HICs

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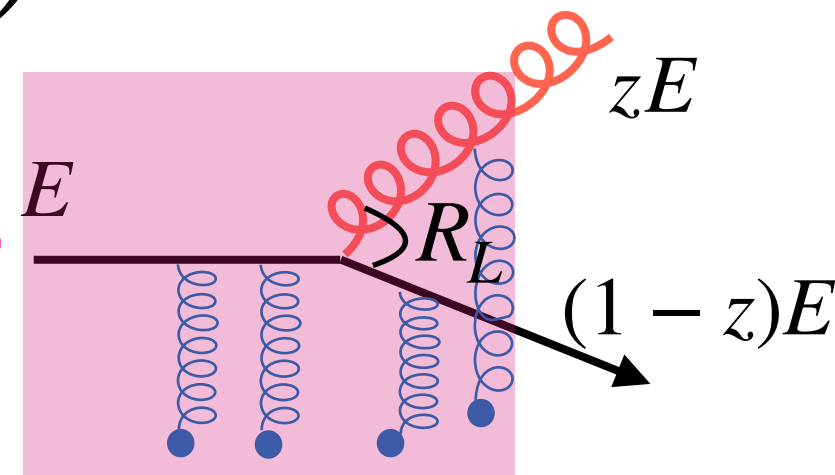


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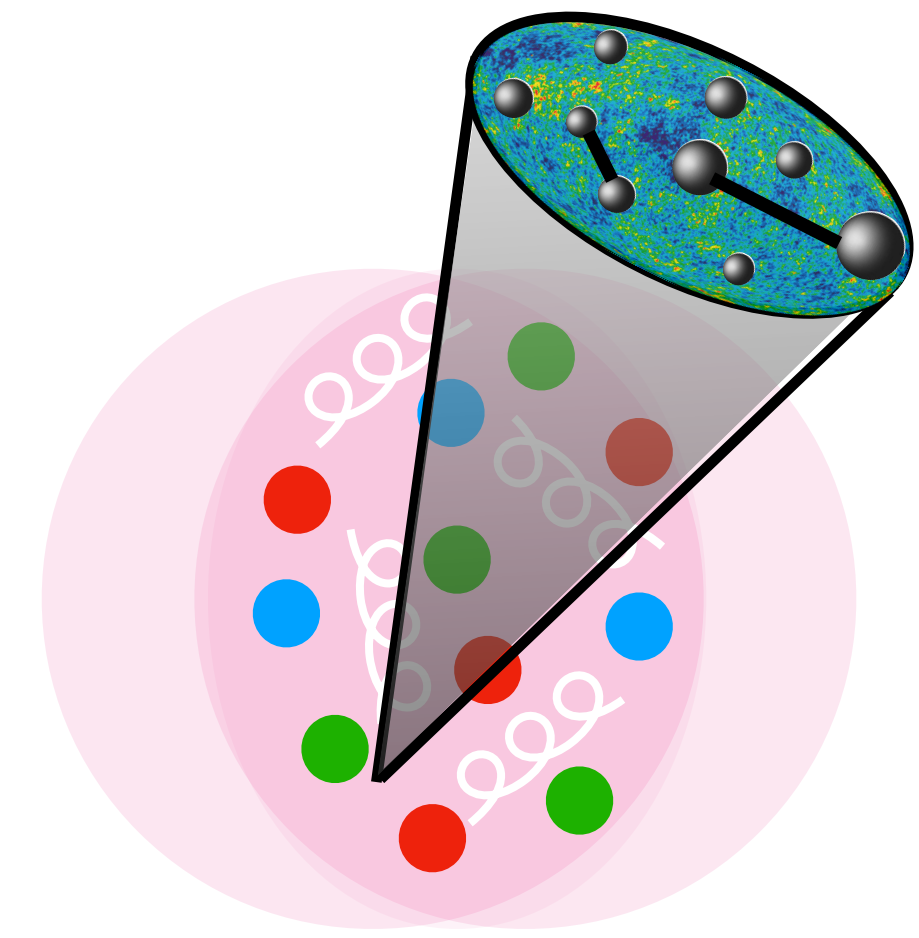
- Soft approximation ($z \rightarrow 0$, zE finite) not suitable
- Two available approximations:
 - **Semi-hard splittings**: eikonal trajectories. Ignores broadening
Isaksen, Tywoniuk, [2107.02542](#)
Dominguez, Milhano, Salgado, Tywoniuk, Vila, [1907.03653](#)
 - **Opacity expansion (GLV)**. No eikonal assumptions
Sievert, Vitev, [1807.03799](#)

Toward a qualitative comparison to inclusive jets data

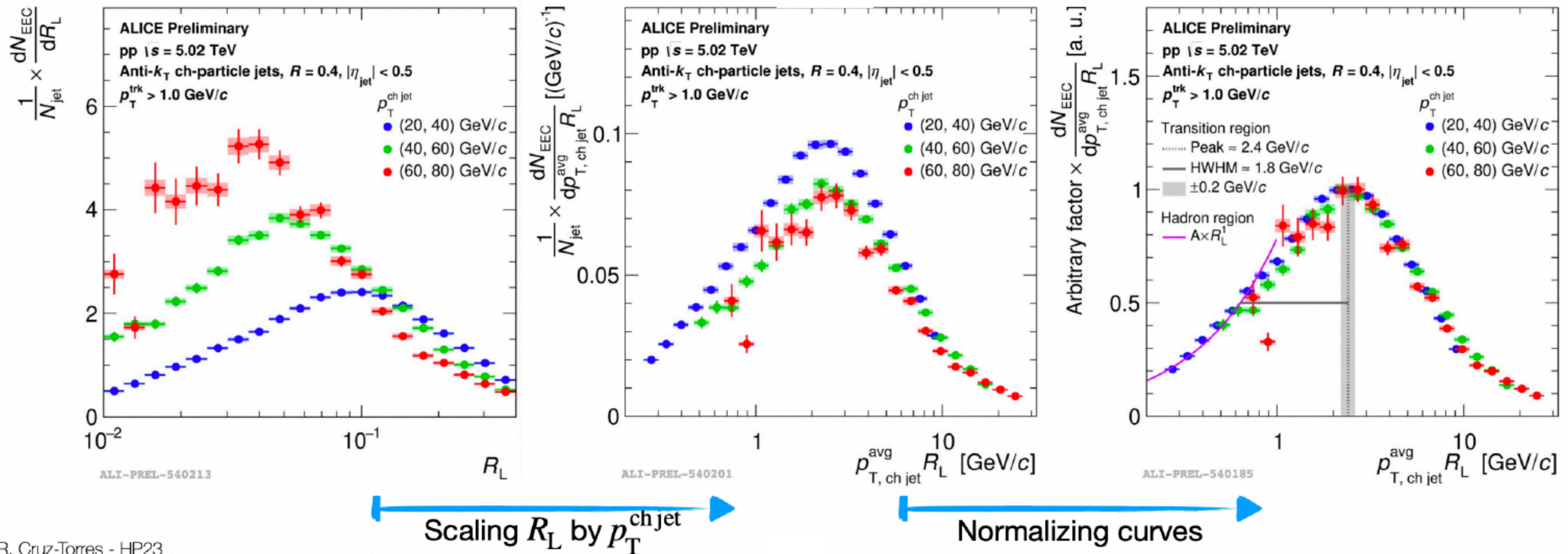
CA, Dominguez, Holguin, Marquet, Moul, [2407.07936](#)

Energy loss

- Energy loss must be included at LO in inclusive measurements due to the **dependence of the E2C on the hard scale**
- Shift in the hard scale. **Selection bias**



E2C within p-p jets



R. Cruz-Torres - HP23

Energy loss and hadronization transition

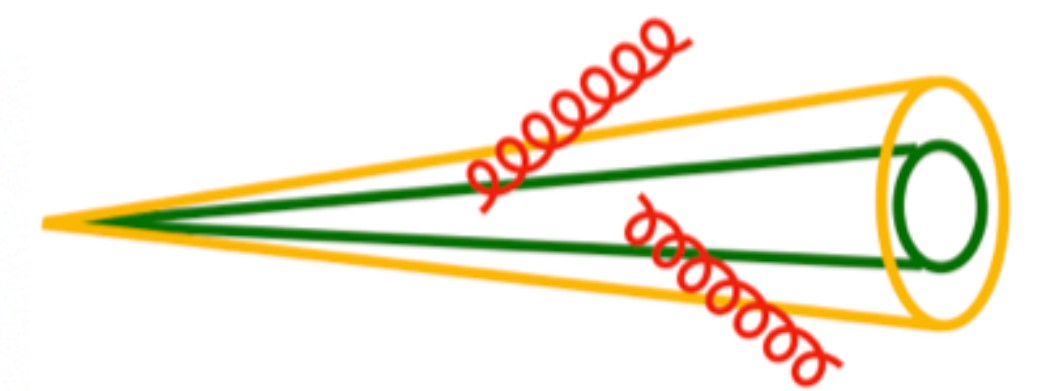
- Analytical model of the **hadronization transition**

$$\begin{array}{ccc}
 \left. \frac{d\Sigma^{\text{E2C}}}{dR_L} \right|_{\text{pQCD}} \sim R_L^{-1+\mathcal{O}(\alpha_s)} & \longrightarrow & \left. \frac{d\Sigma^{\text{E2C}}}{dR_L} \right|_{\text{pQCD}} = \frac{R_L}{B_0 + B_2 R_L^2} \\
 \left. \frac{d\Sigma^{\text{E2C}}}{dR_L} \right|_{\text{free had}} \sim R_L & & \frac{B_0}{B_2} \sim \frac{\Lambda_{\text{QCD}}^2}{Q^2}
 \end{array}$$

- Rough estimate of **energy loss** through Quenching Weights distribution (totally coherent)

Salgado, Wiedemann, [hep-ph/0302184](https://arxiv.org/abs/hep-ph/0302184)

$$P_\xi(\epsilon) = \sum_{N=0}^{\infty} \frac{1}{N!} \prod_{i=1}^N \left[\int d\omega_i \frac{dI_\xi}{d\omega} \right] \delta \left(\epsilon - \sum_{i=1}^N \omega_i \right) \exp \left[- \int_0^\infty d\omega \frac{dI_\xi}{d\omega} \right]$$



For corrections to this approach due to fluctuations see: Mehtar-Tani, Tywoniuk, [1707.07361](https://arxiv.org/abs/1707.07361)

Barata, Caucal, Soto-Ontoso, Szafron, [2312.12527](https://arxiv.org/abs/2312.12527)

E2C in inclusive heavy-ion jets

- **Convolution** of this the **Quenching Weights** with the **E2C at a higher hard scale** and averaged over trajectories

$$\frac{d\Sigma_{\text{E2C}}(p_T)}{dR_L} = \int d\epsilon \left\langle P_\xi(\epsilon) \frac{d\Sigma_{\text{E2C},\xi}^{\text{NP}}(p_T + \epsilon)}{dR_L} \right\rangle_\xi \frac{1}{\sigma_{q+X}} \frac{d\sigma_{q+X}}{dp_{T,q}} \Big|_{p_{T,q} = p_T + \epsilon}$$

- Predictions within two approaches to compute **E2C**:

- Multiple scatterings: **Semi-hard + leading broadening corrections** $\hat{q}(t) = k_{\text{HO}} T^3(\xi(t))$

CA, Dominguez, Holguin, Marquet, Moult, [2407.07936](#)

- Single scattering: **GLV** $n(t) = k_{\text{GLV}} T(\xi(t))$ $\mu^2(t) = 6\pi\alpha_s T^2(\xi(t))$

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E2C at the hard scale $p_T + \epsilon$

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Energy loss E2C at the hard scale $p_T + \epsilon$

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Energy loss E2C at the hard scale $p_T + \epsilon$

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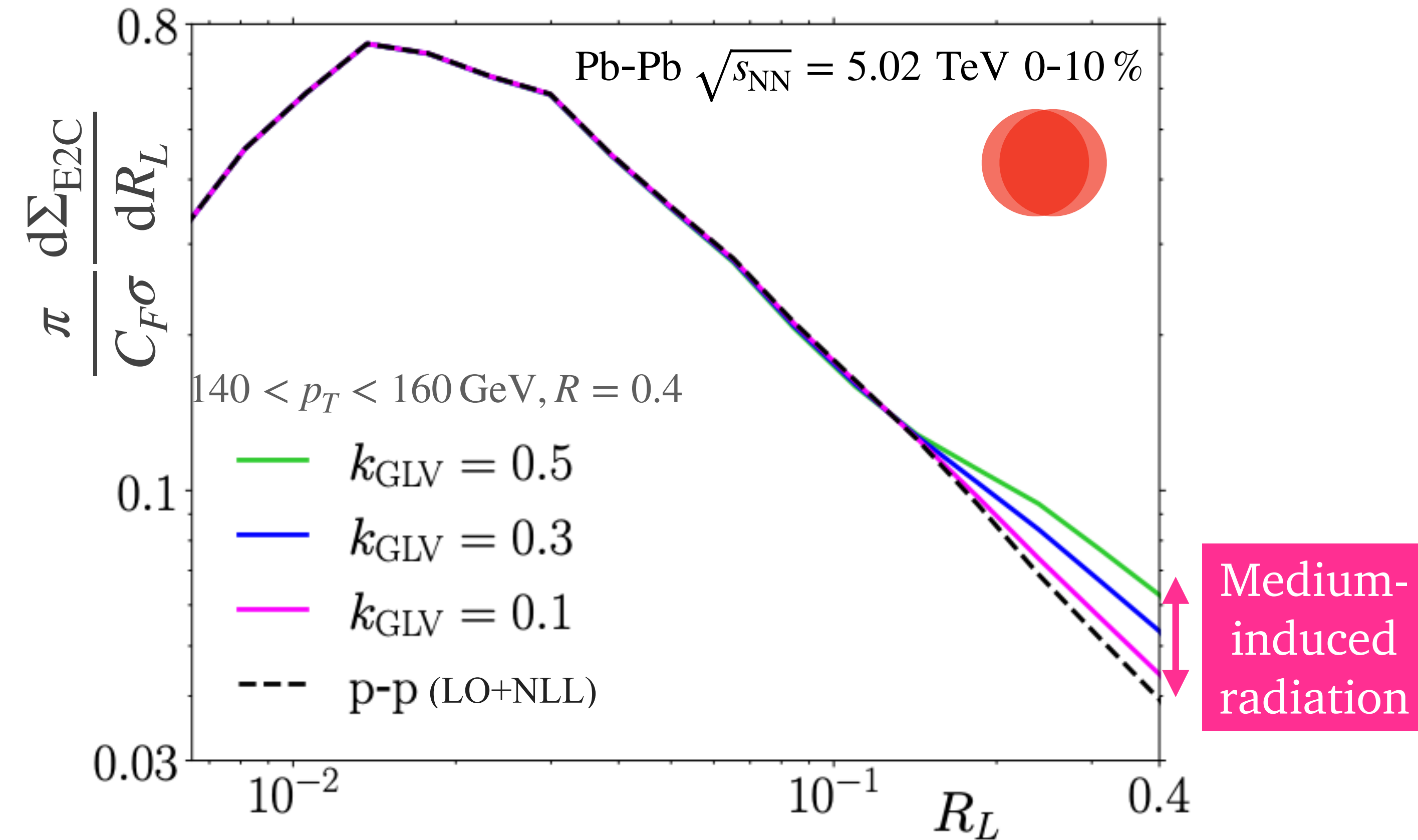
CA, Dominguez, Holguin, Marquet, Moul, [2407.07936](#)

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k_{GLV} and normalization are free parameters!

E2C in heavy-ions

E2C γ -tagged jets



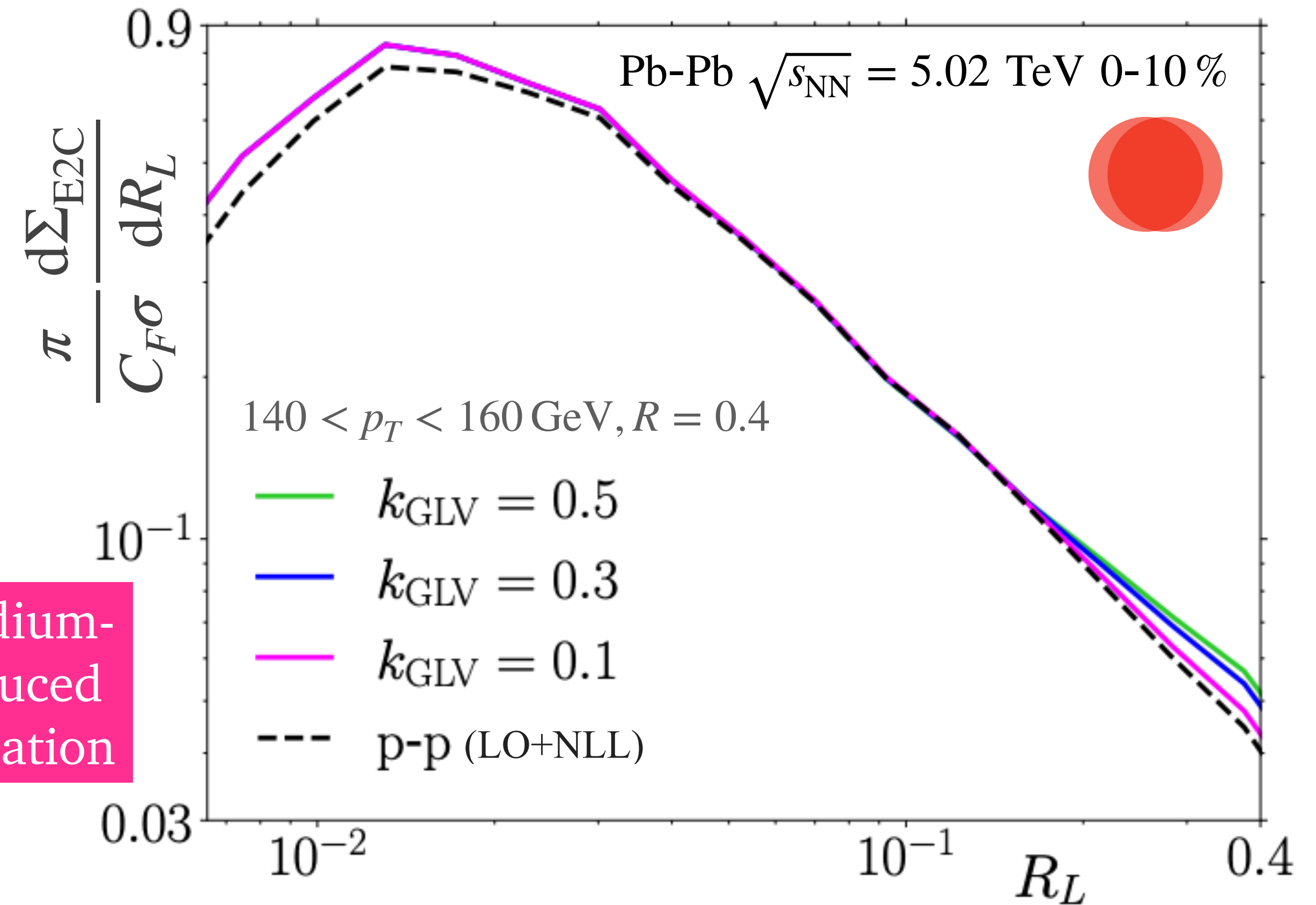
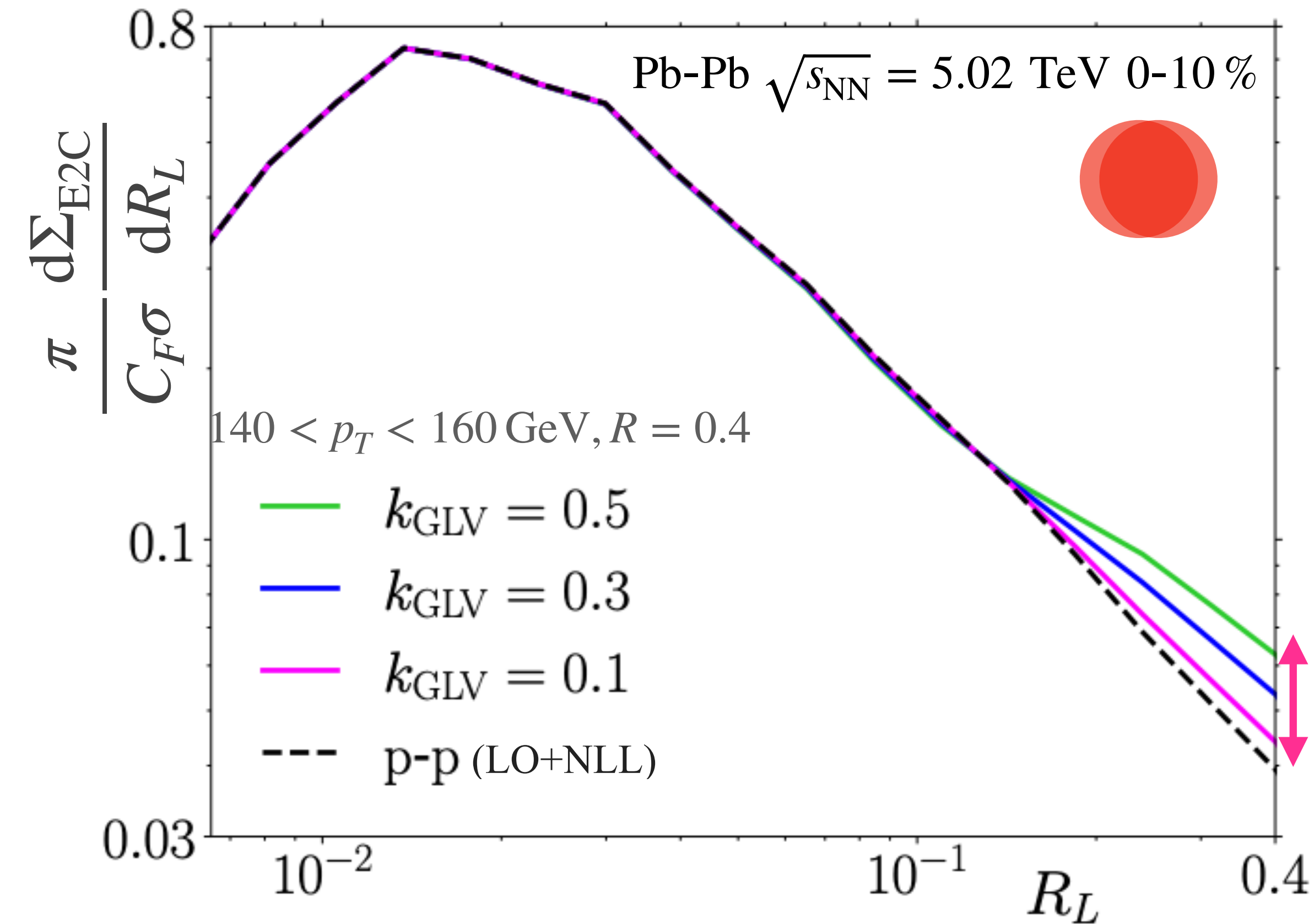
Medium response: can also appear at large angles!

Yang, He, Moulton, Wang, [2310.01500](#) Bossi, Kudinoor, Moulton, Pablos, Rai, Rajagopal, [2407.13818](#)

E2C in heavy-ions

E2C γ -tagged jets

E2C Inclusive jets

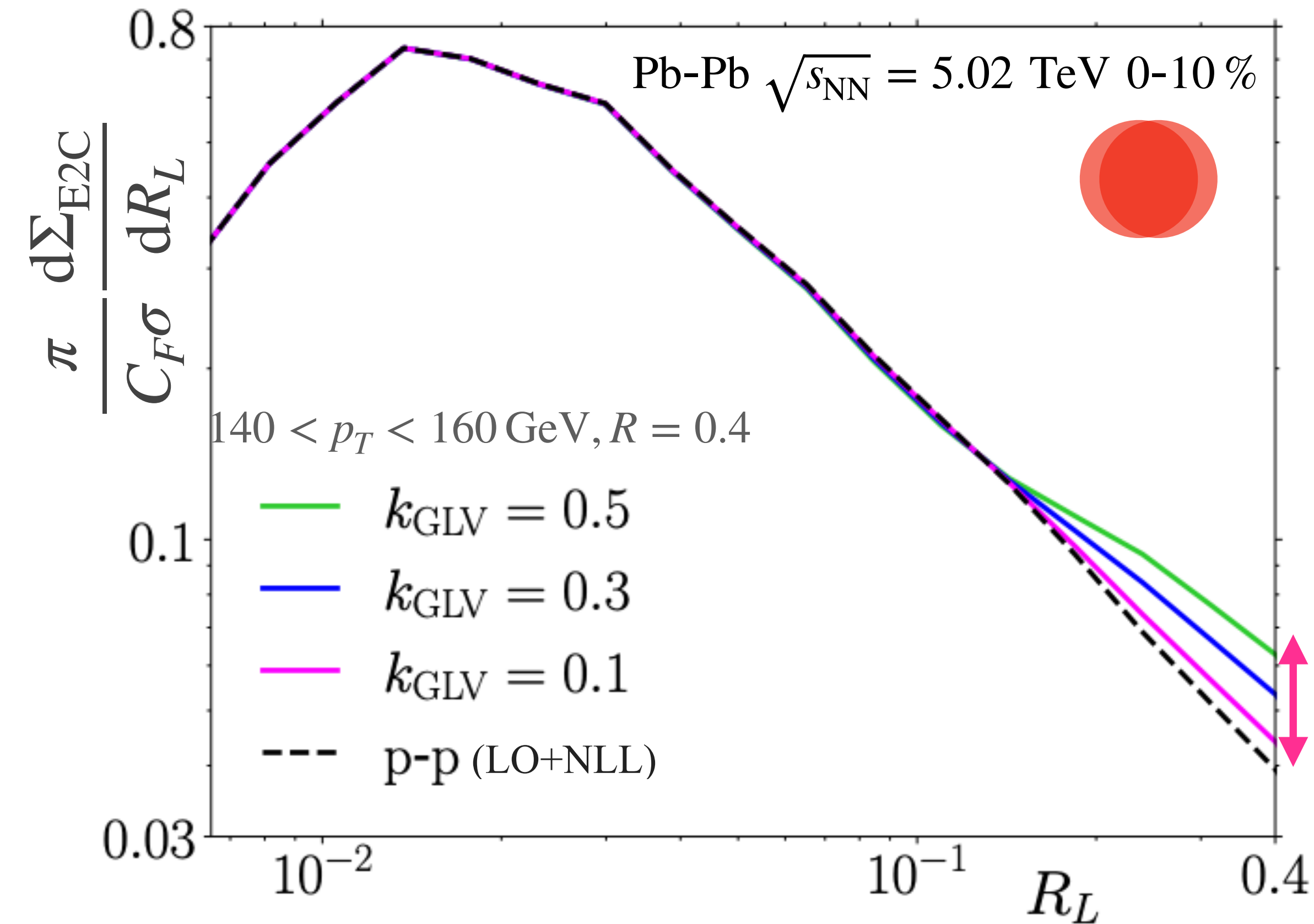


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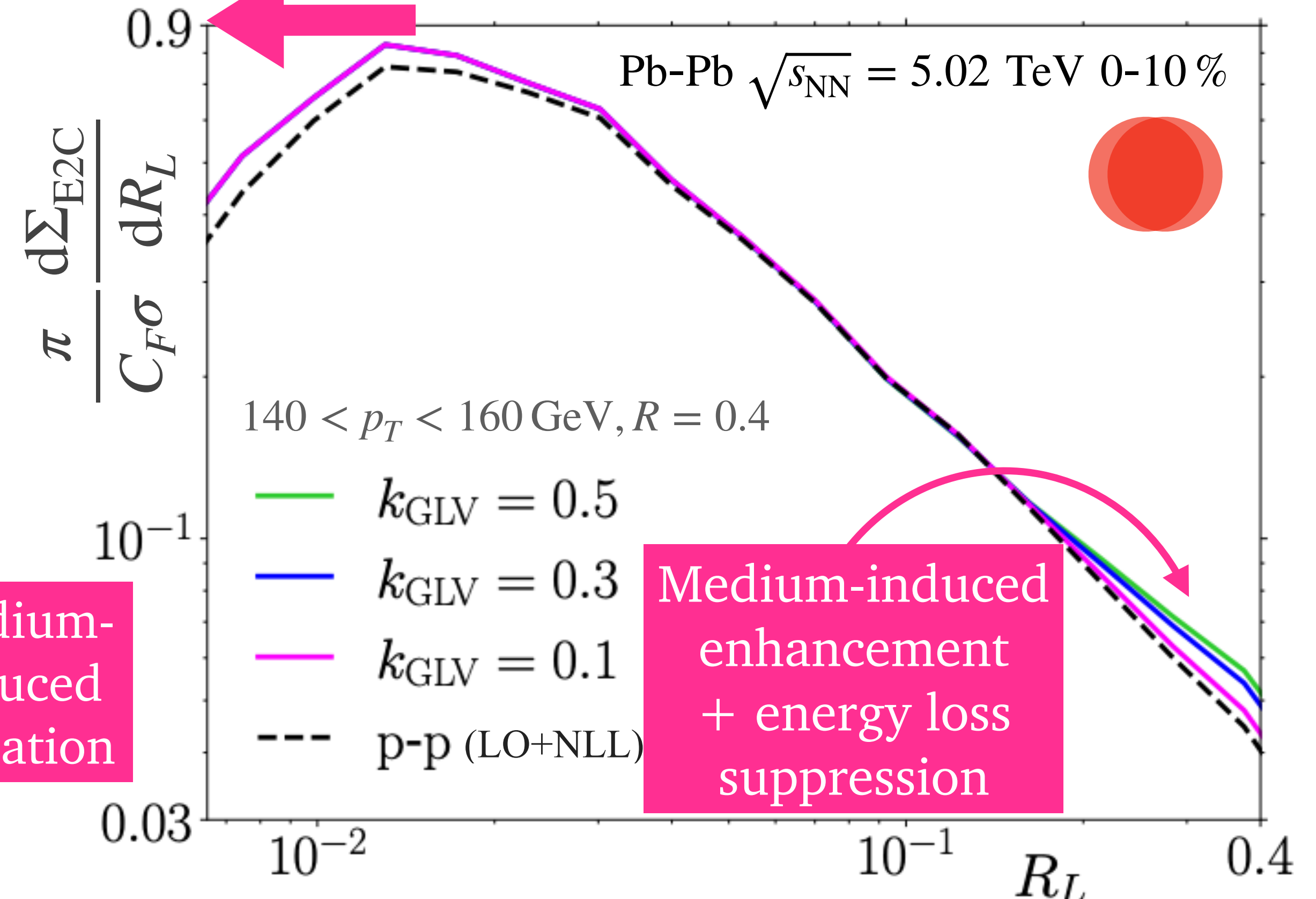
Yang, He, Mout, Wang, [2310.01500](#) Bossi, Kudinoor, Mout, Pablos, Rai, Rajagopal, [2407.13818](#)

E2C in heavy-ions

E2C γ -tagged jets



E2C Inclusive jets



See also: Barata et al. [2312.12527](#)

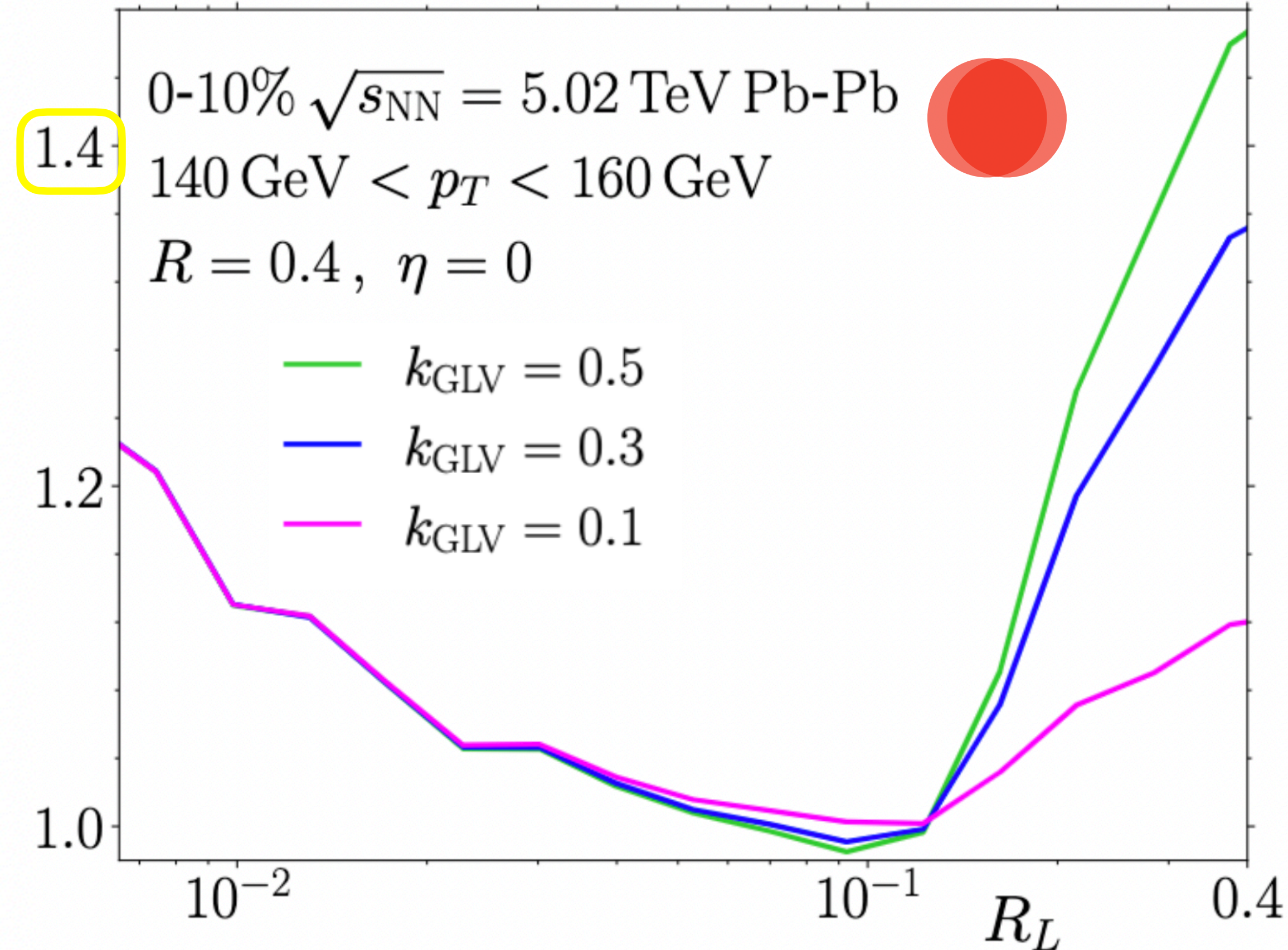
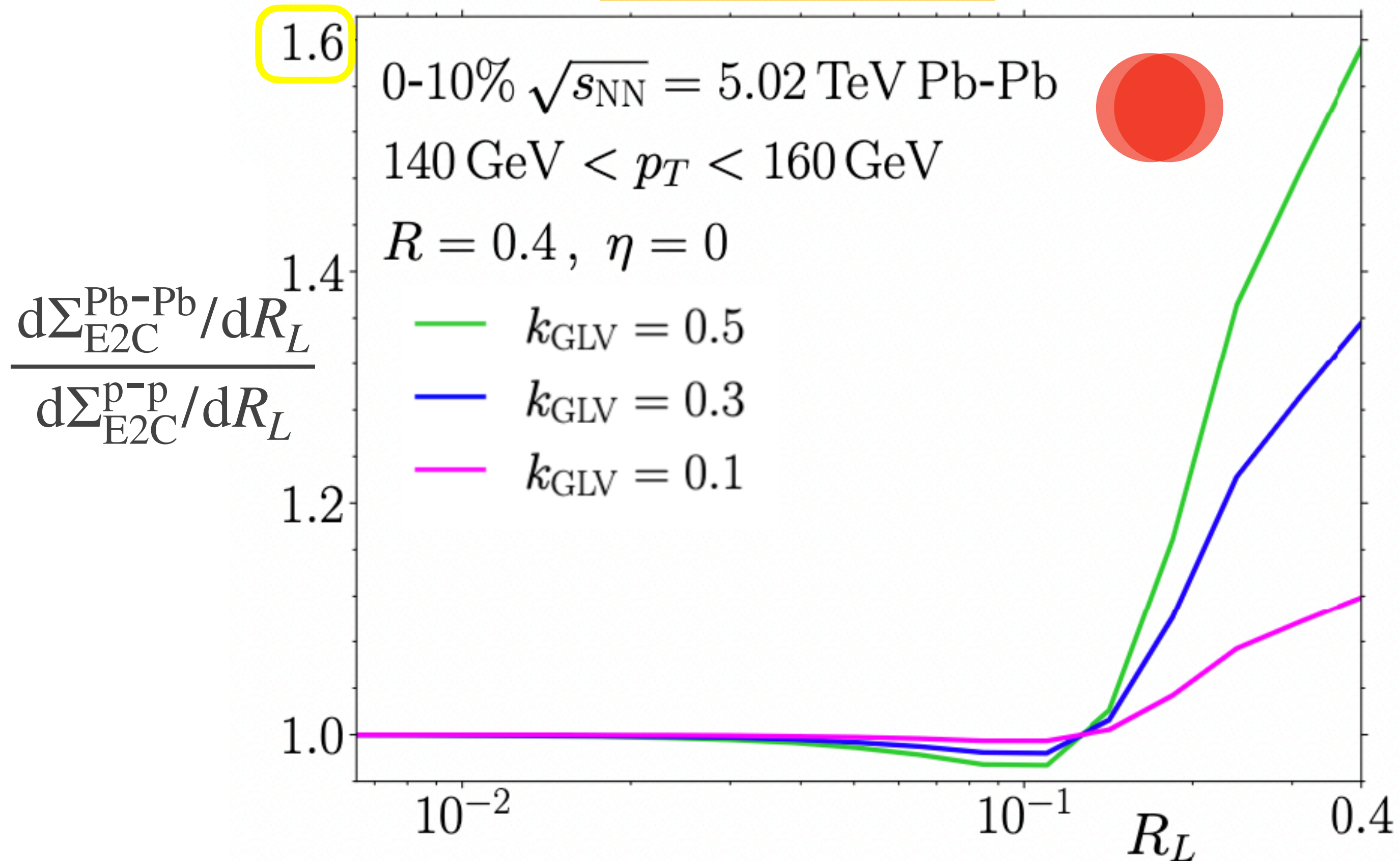
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Yang, He, Mout, Wang, [2310.01500](#)

Bossi, Kudinoor, Mout, Pablos, Rai, Rajagopal, [2407.13818](#)

E2C: Pb-Pb/p-p ratio

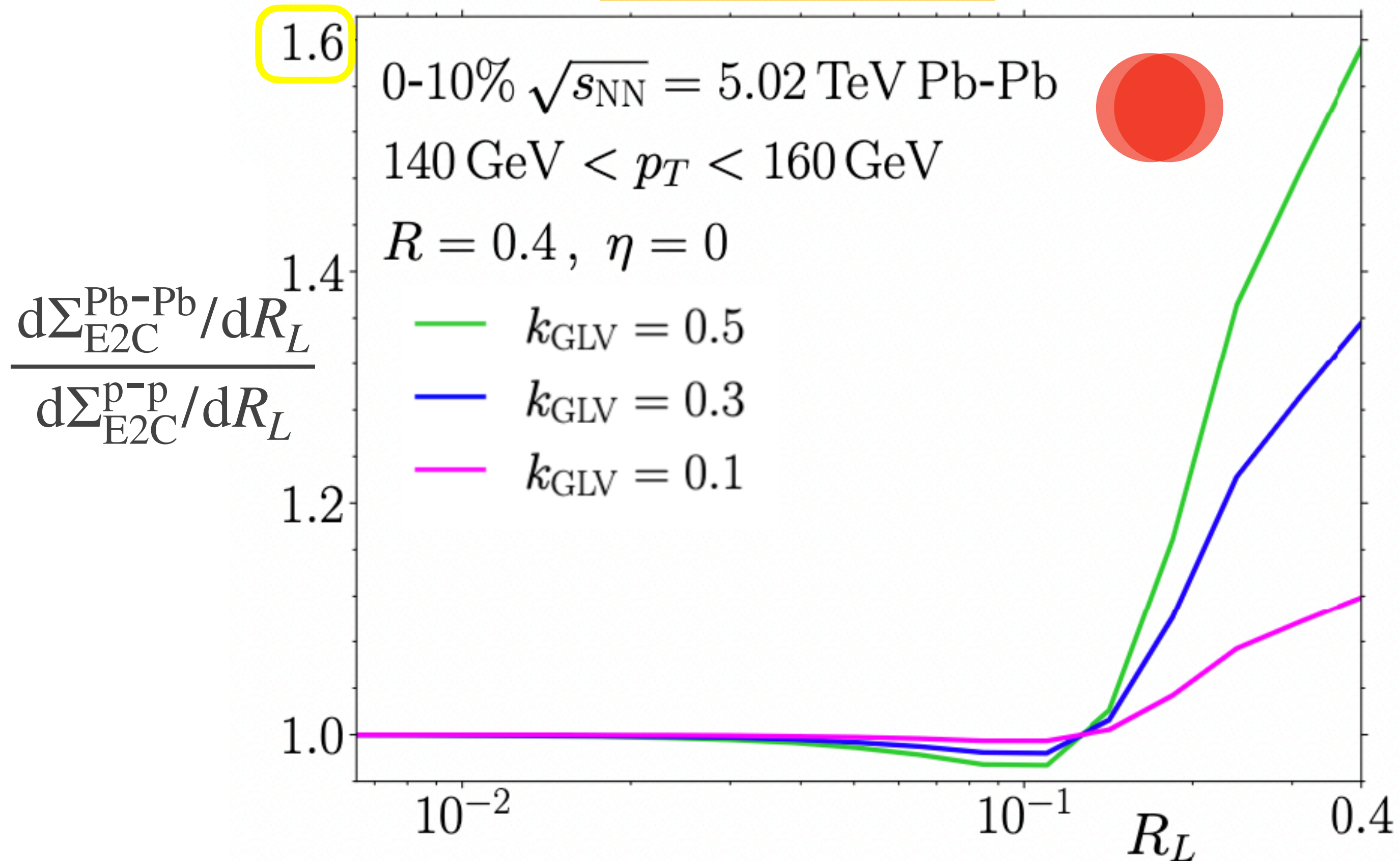
γ -tagged jets



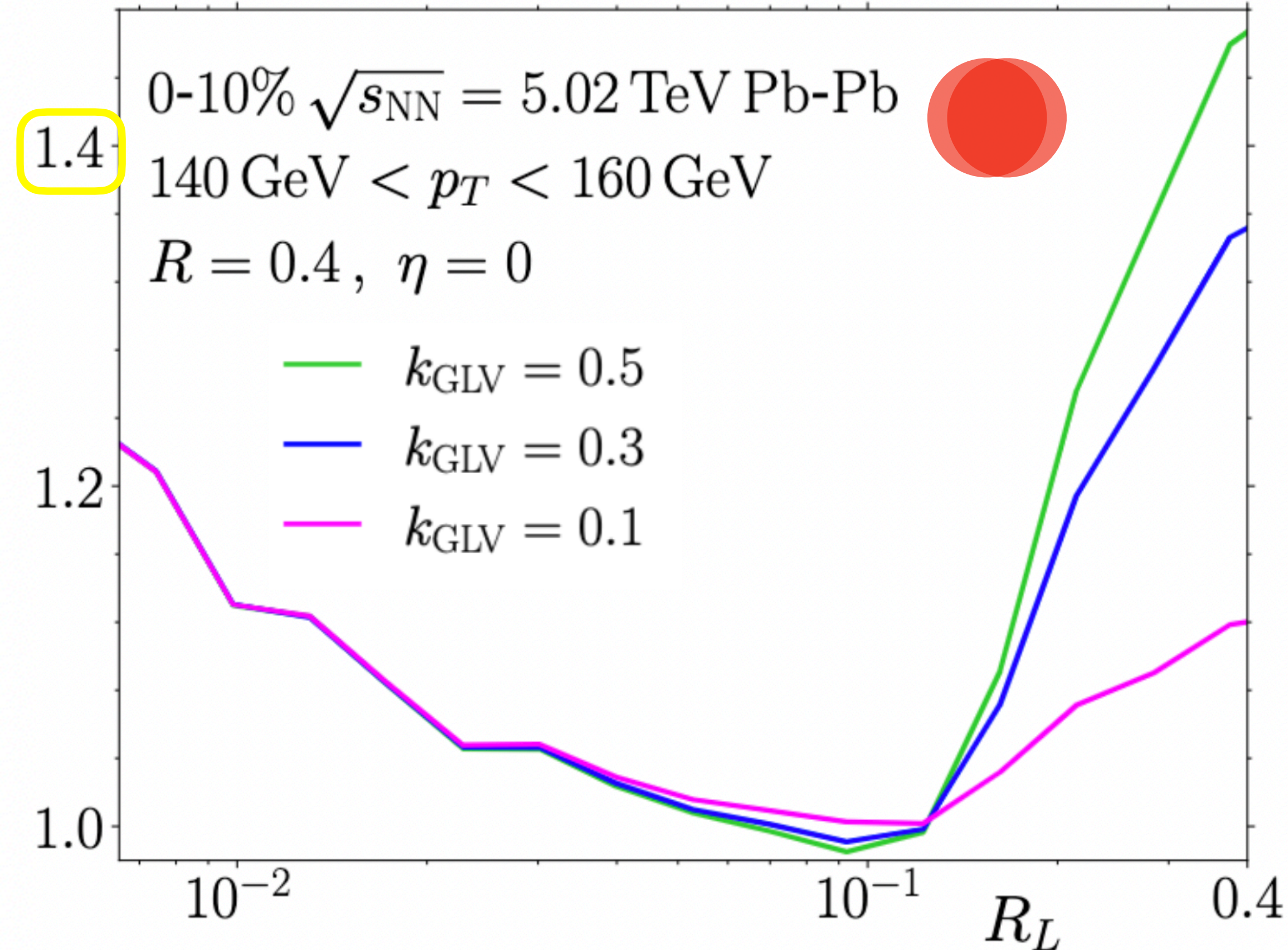
Selection bias: non-trivial angular structure at small angles and some reduction of the enhancement at large angles

E2C: Pb-Pb/p-p ratio

γ -tagged jets



Inclusive jets



Selection bias: non-trivial angular structure at small angles and some reduction of the enhancement at large angles

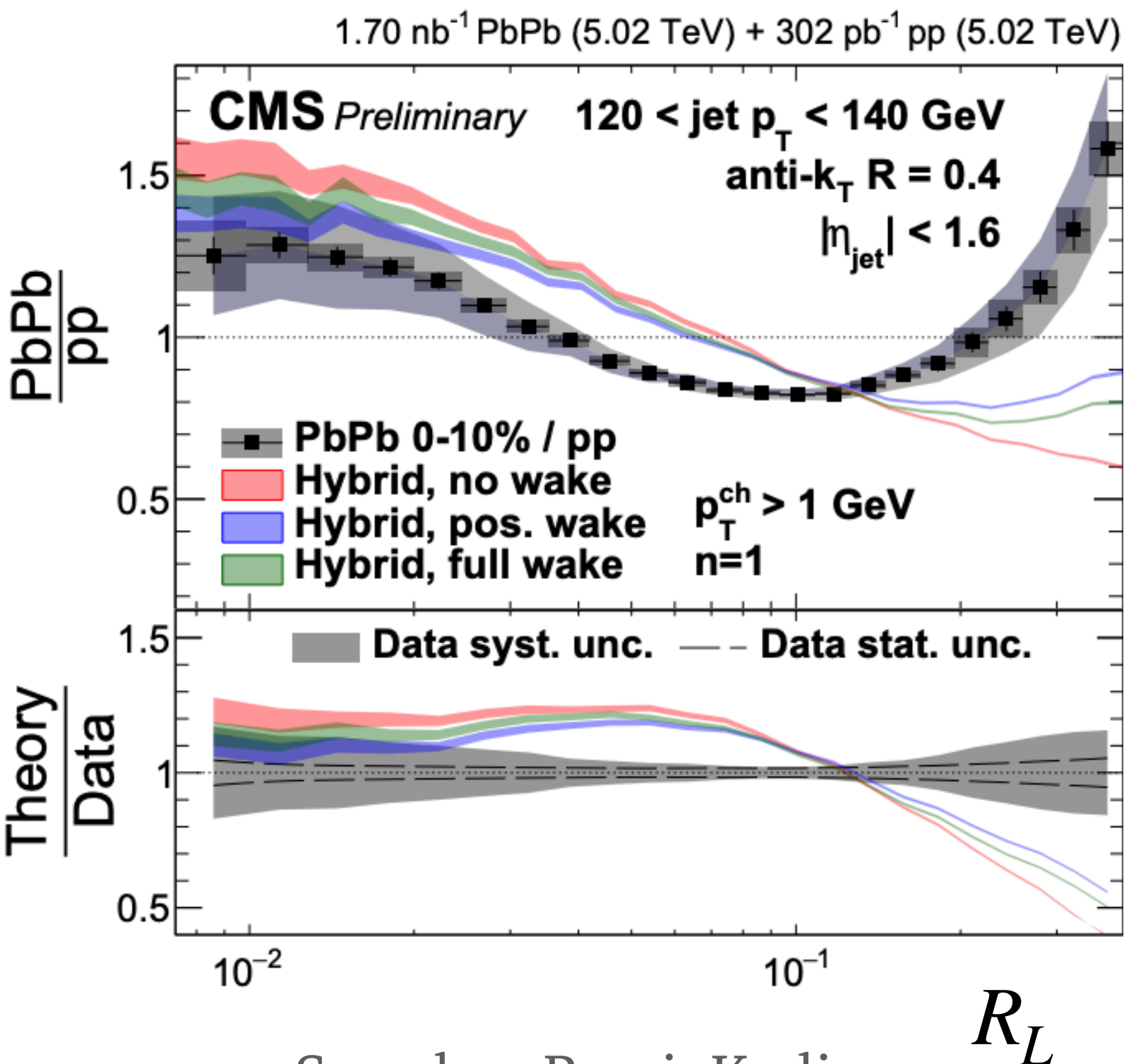
E2C: A-A/p-p ratio predictions

CMS-PAS-HIN-23-004

From [Jussi Viinikainen's talk at the Energy Correlators at the Collider Frontier workshop](#)

Hybrid model

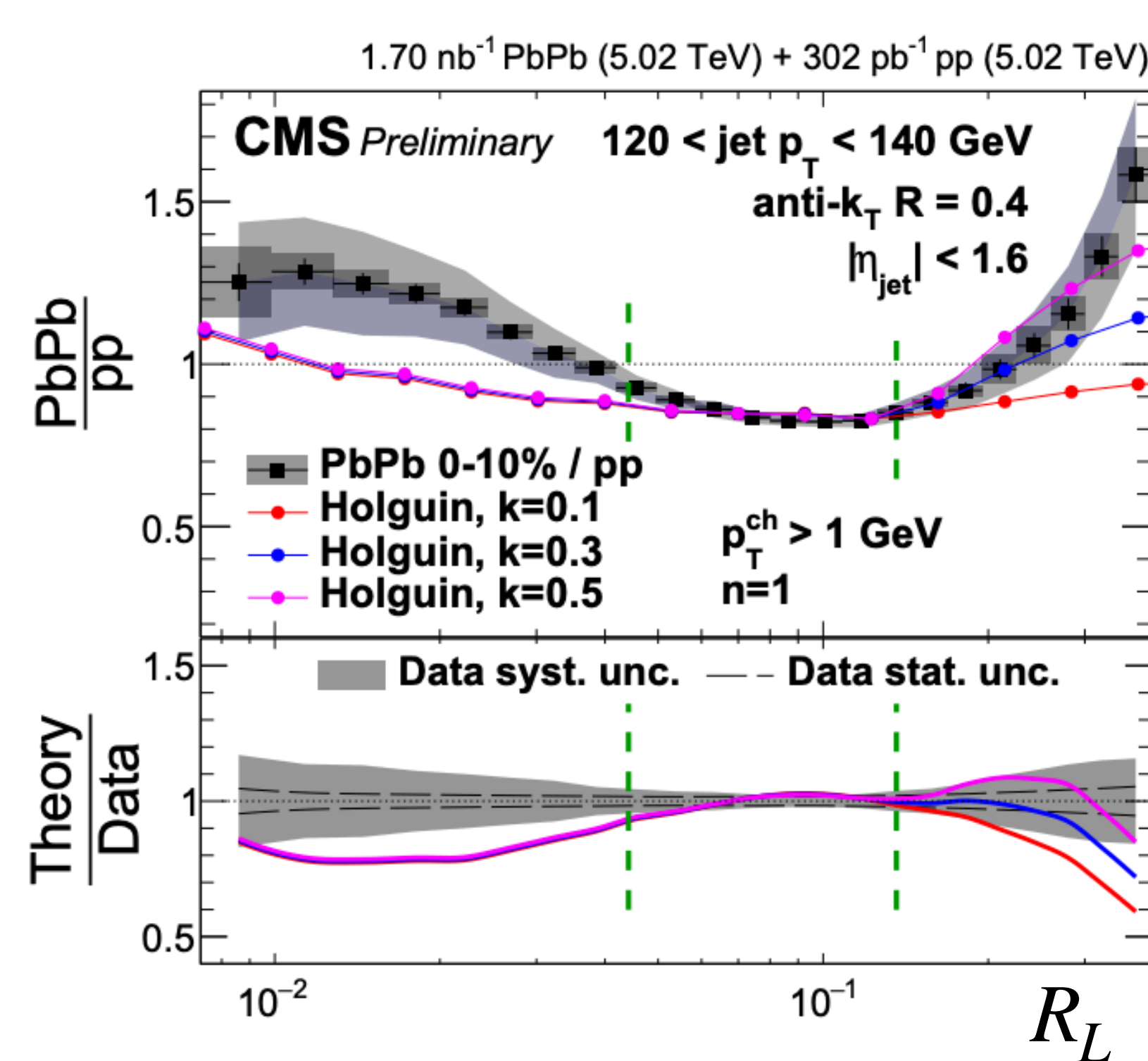
Pablos, Kudinoor, Rajagopal



See also: Bossi, Kudinoor, Moul, Pablos, Rai, Rajagopal, [2407.13818](#)

CA, Dominguez, Holguin, Marquet, Moul

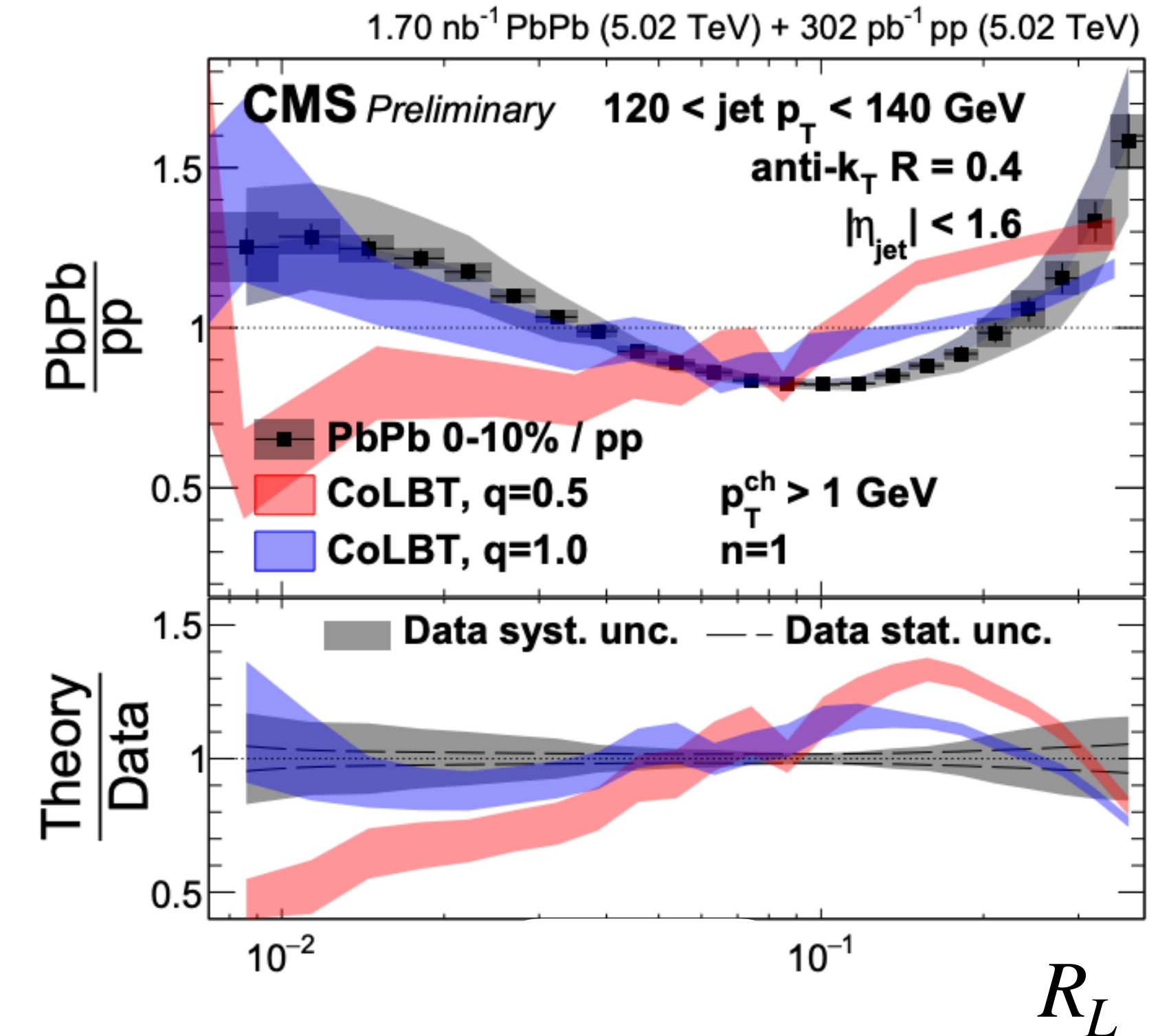
CA, Dominguez, Holguin, Marquet, Moul



CA, Dominguez, Holguin, Marquet, Moul, [2407.07936](#)

CoLBT

Yang, He, Wang

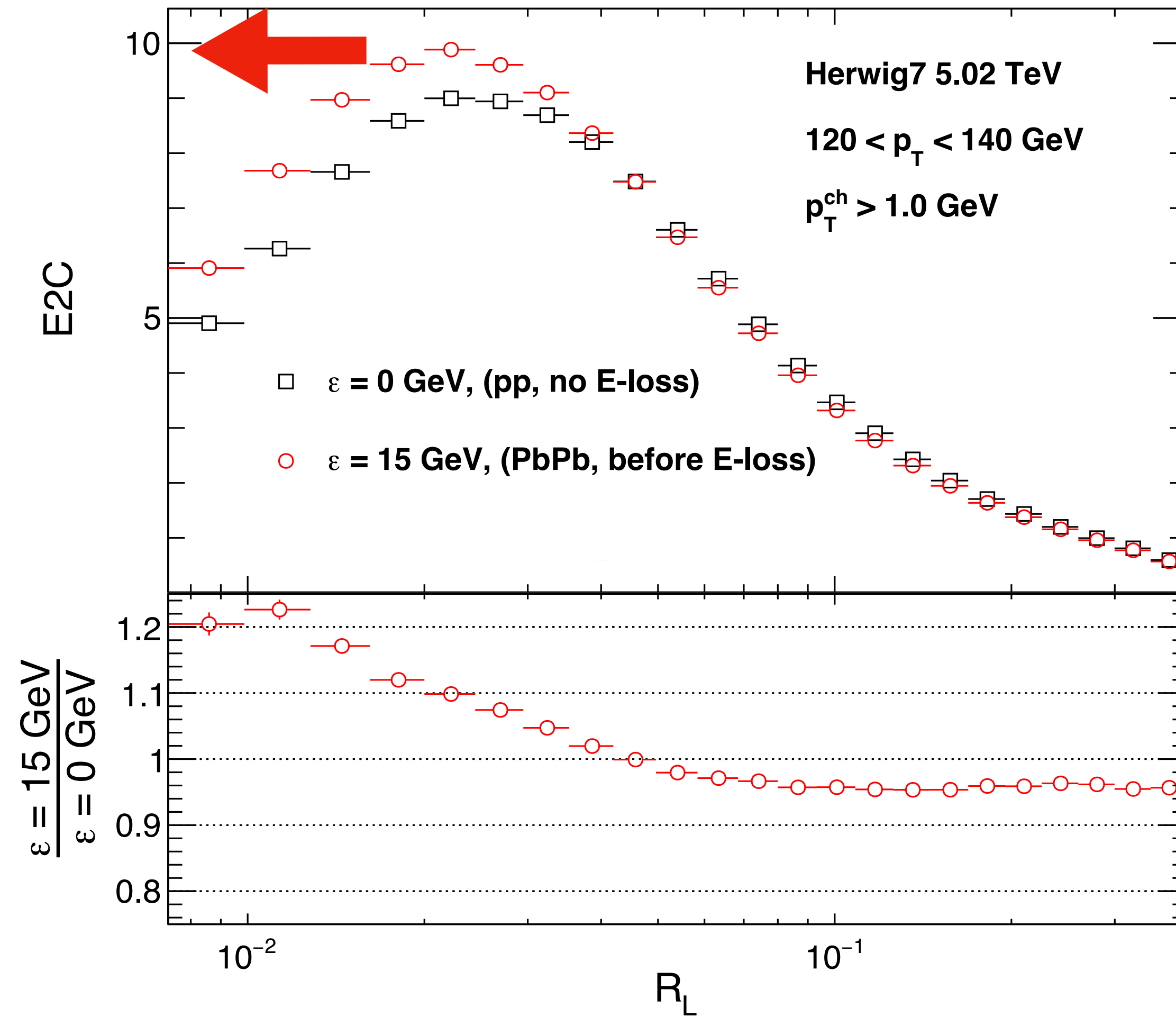


See also: Yang, He, Moul, Wang, [2310.01500](#)

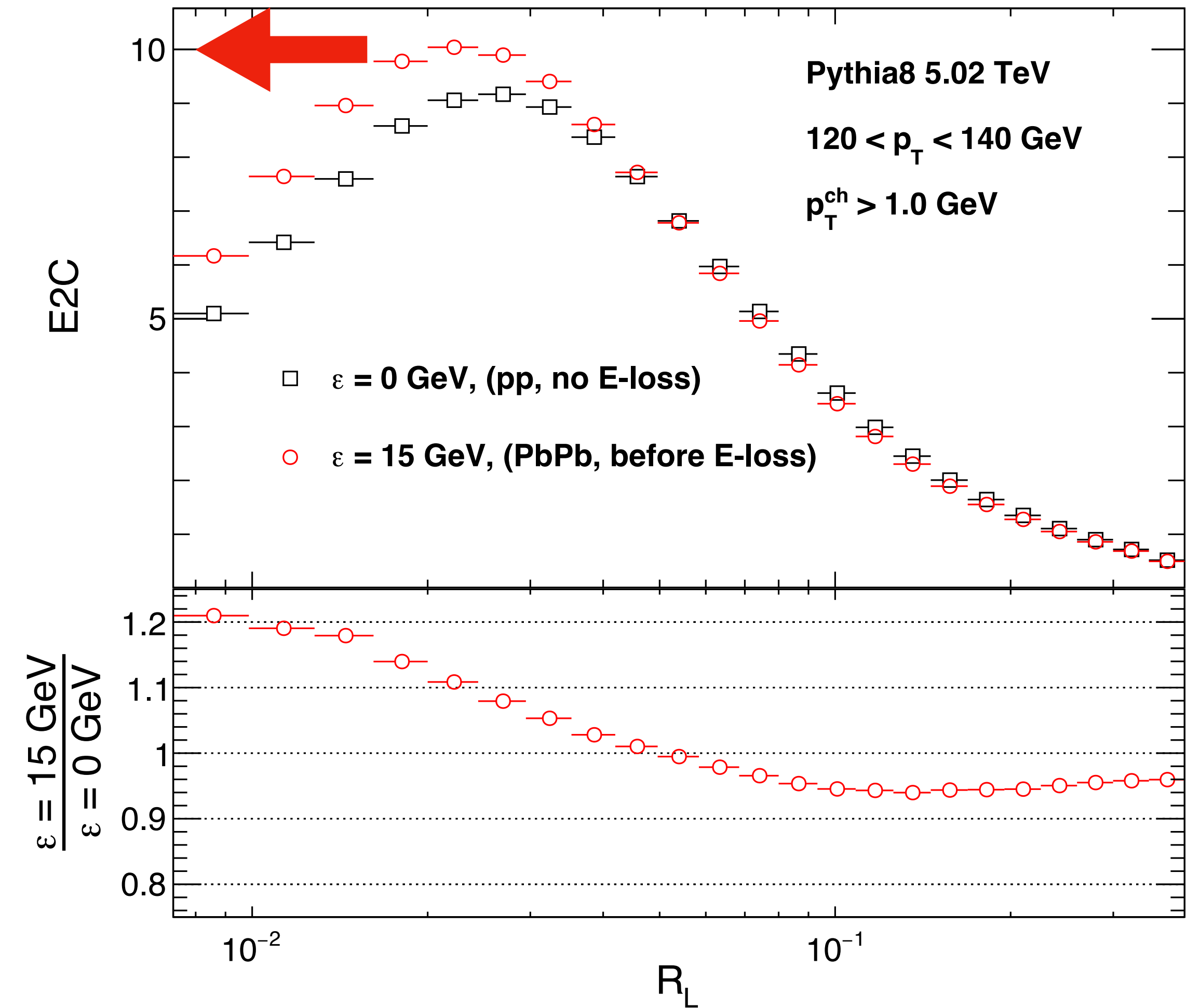
Mitigating energy loss

CA, Holguin, Kunnawalkam Elayavalli,
Viinikainen, [2409.07514](#)

15 GeV shift



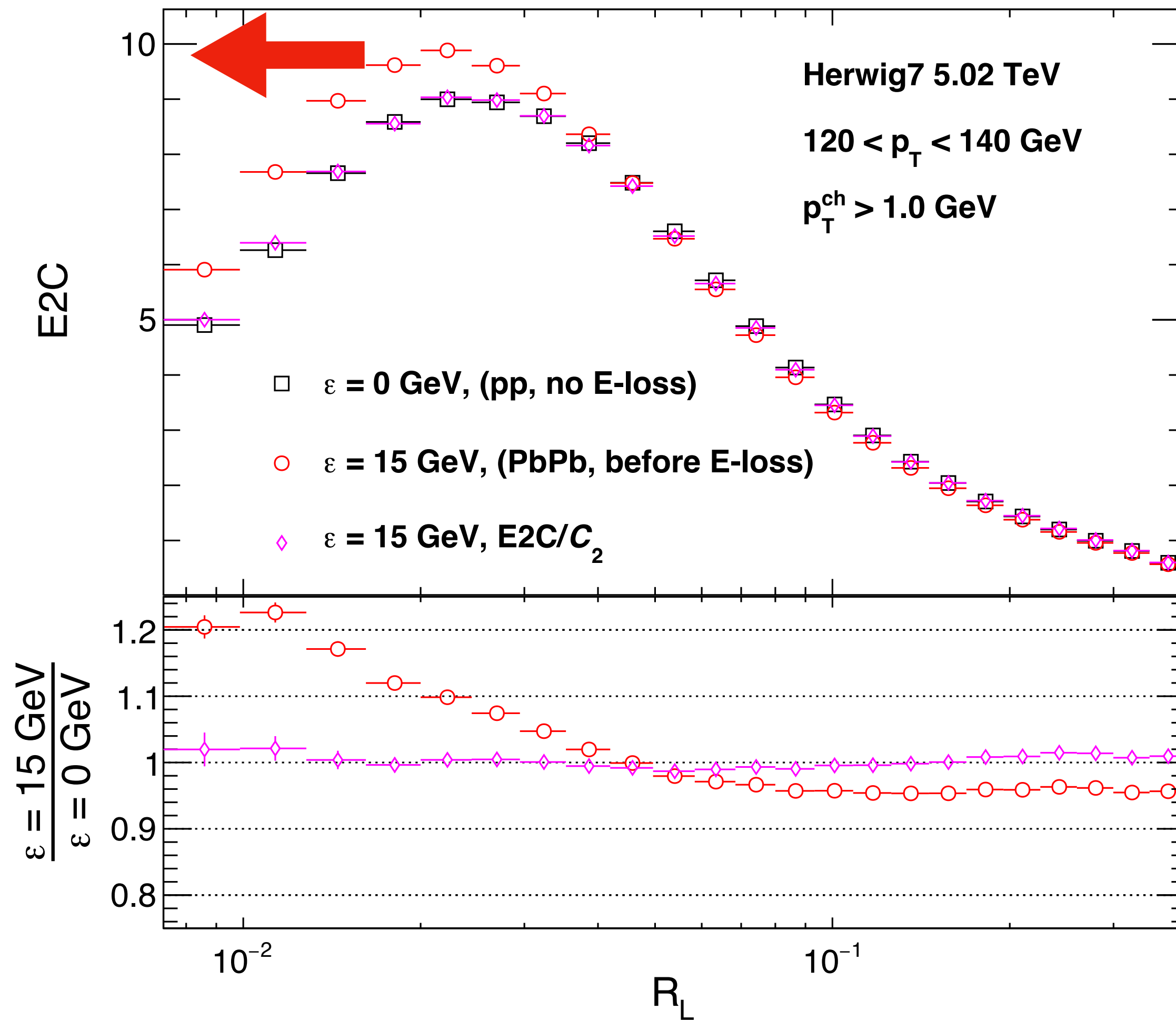
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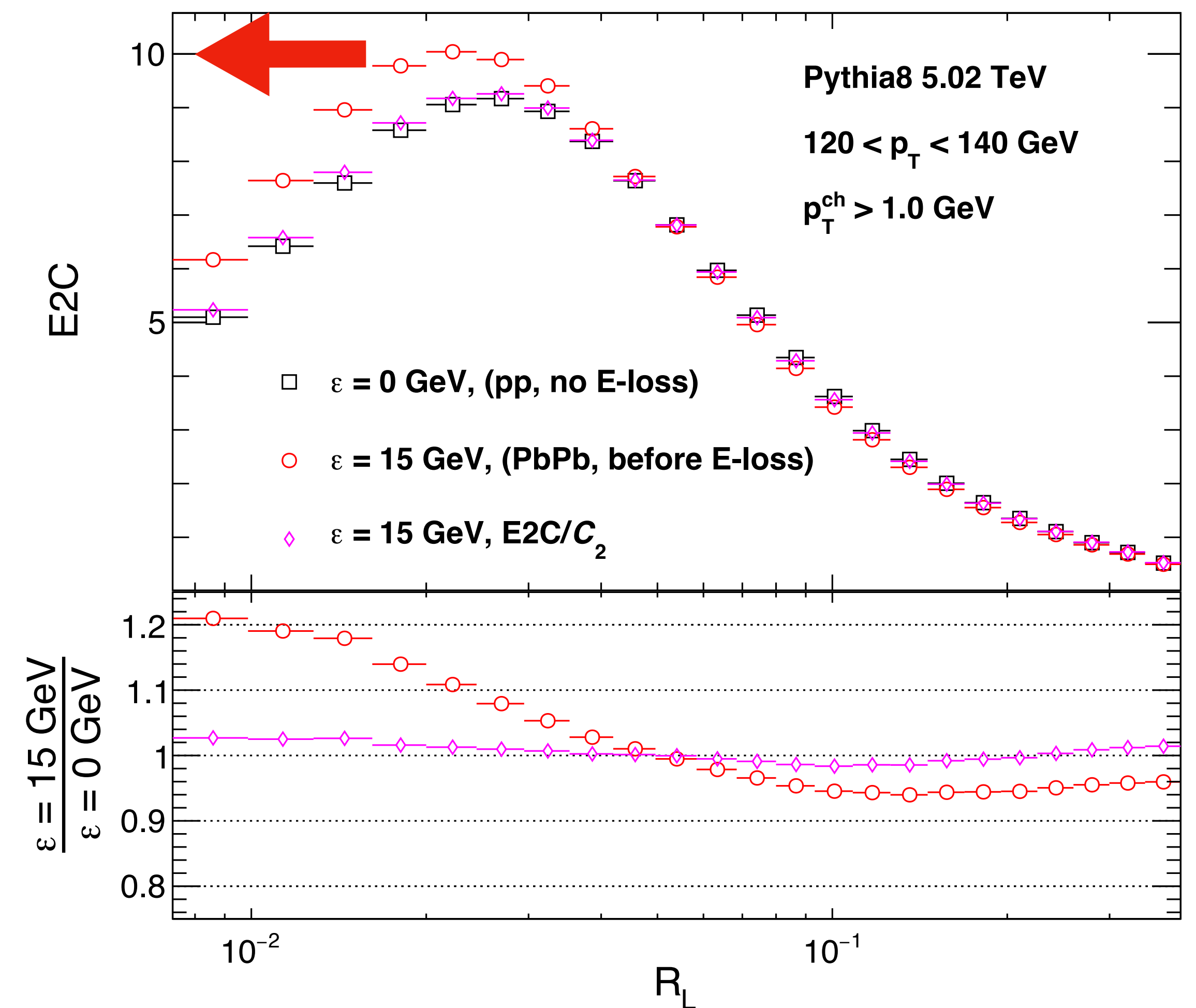
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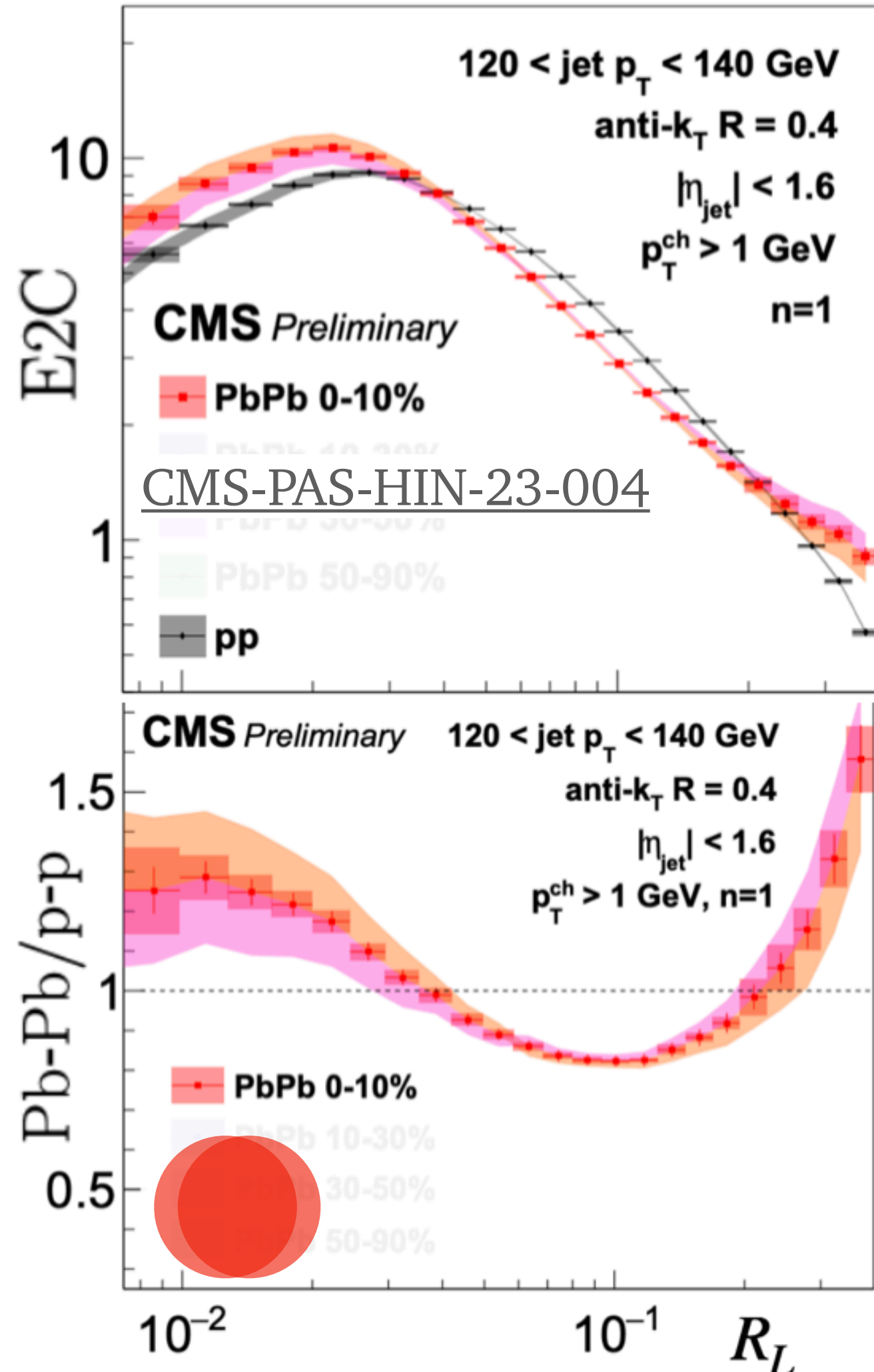
E2C/ C_2 : almost no selection bias effect!

Mitigating energy loss

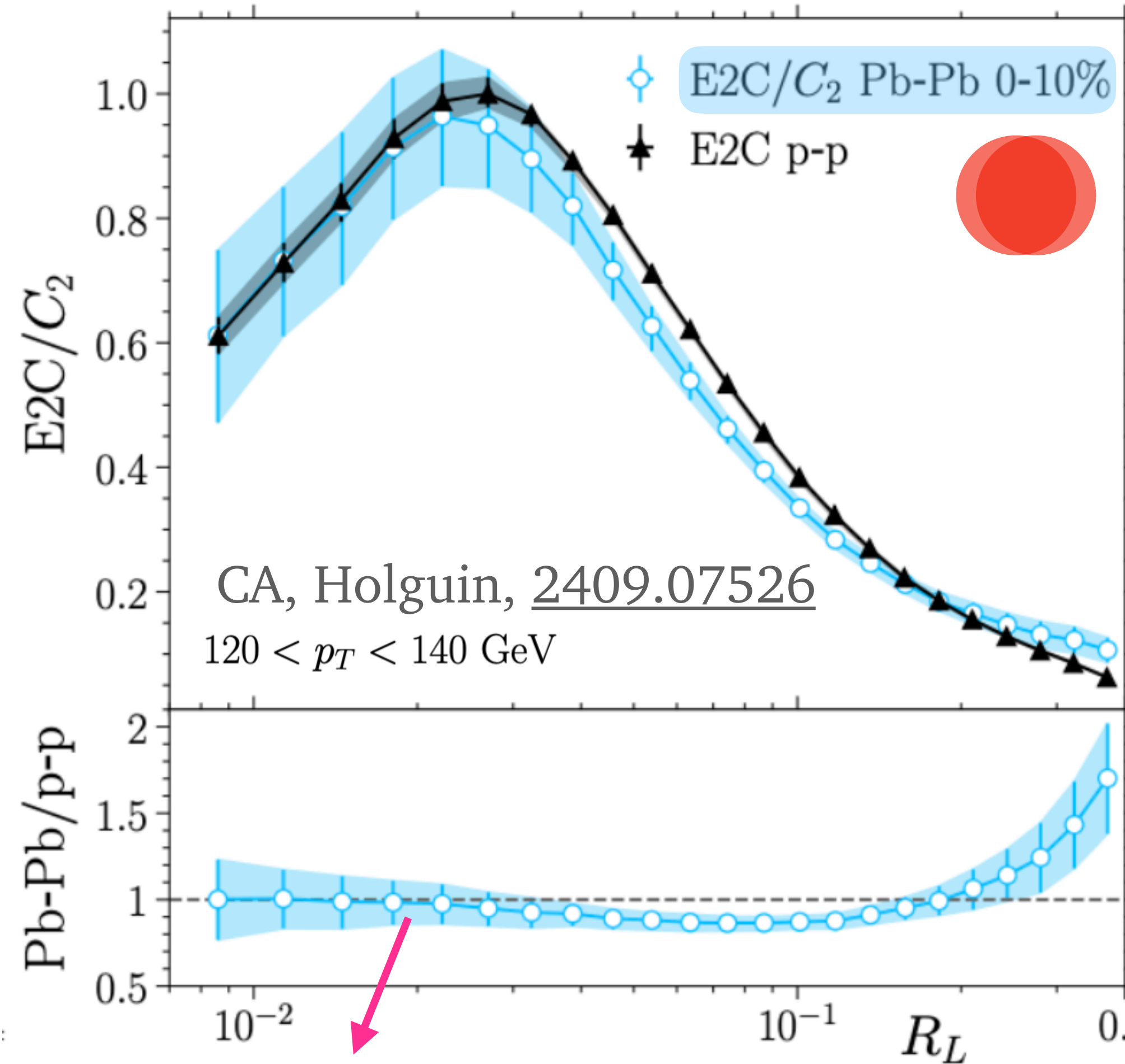
$$C_2(R_L) \equiv \left(\frac{F_{E2C}^{AA}(R_L, 2)}{F_{E2C}^{PP}(R_L, 2)} \right)^{\frac{2}{3}} - \left(\frac{F_{E2C}^{AA}(R_{\text{peak}}, 2)}{F_{E2C}^{PP}(R_{\text{peak}}, 2)} \right)^{\frac{2}{3}} + 1$$

E2C in inclusive jets

1.70 nb⁻¹ PbPb (5.02 TeV) + 302 pb⁻¹ pp (5.02 TeV)



Unbiased E2C in inclusive jets



C₂ can be directly obtained from the E2C!

Larger enhancement

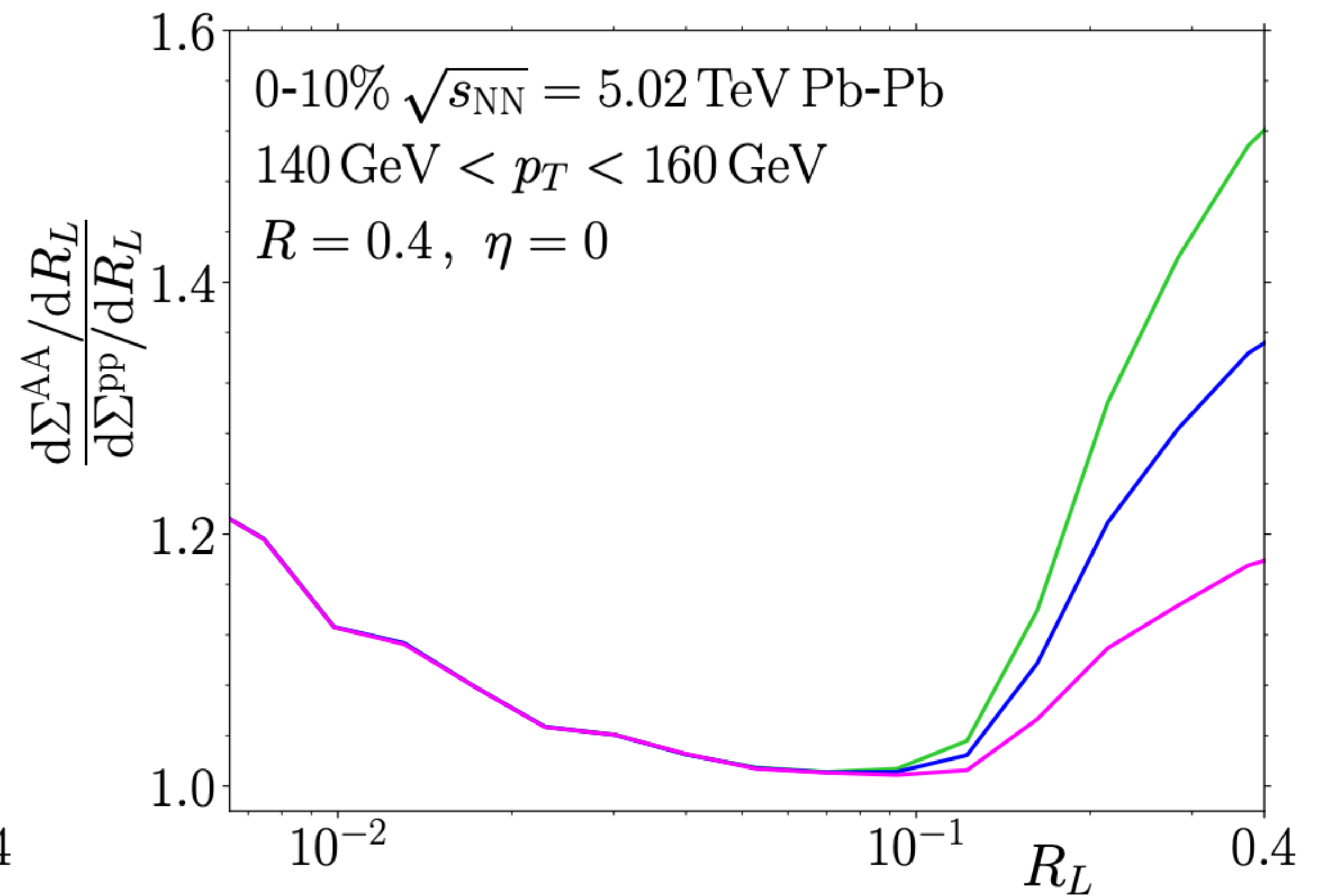
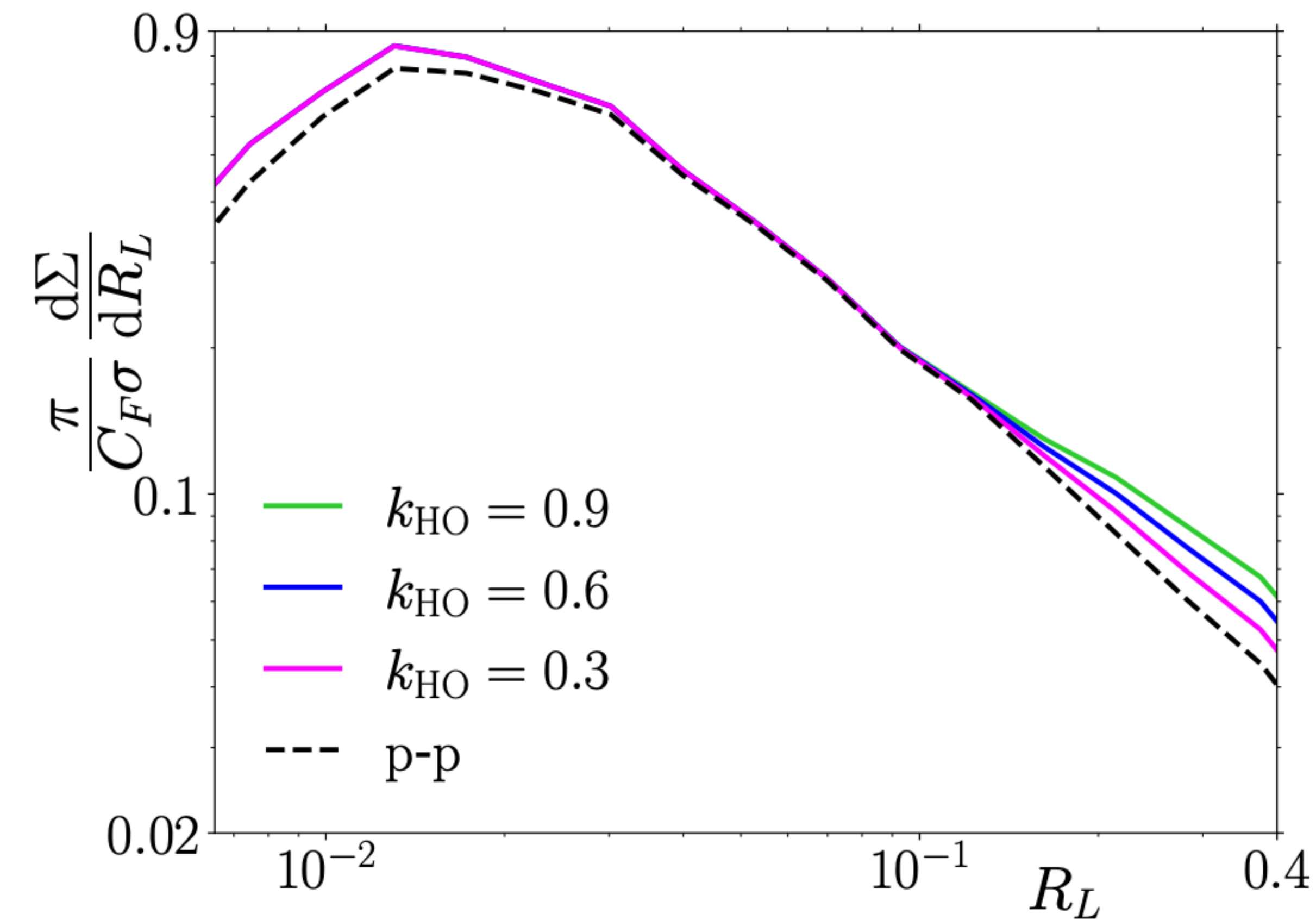
Within current uncertainties: the free hadron region is flat

Conclusions

- **Qualitative good description** of the CMS E2C data in **inclusive jets** for the 0-10% centrality and all p_T bins
- **Medium-induced splittings** create an **enhancement at large angles**
- **Energy loss: shifts** the E2C in Pb-Pb **towards small angles** w.r.t. the p-p result
reduces the enhancement at large angles
- **E2C/ C_2 : new E2C-based** observable that **removes leading order energy loss effects!**

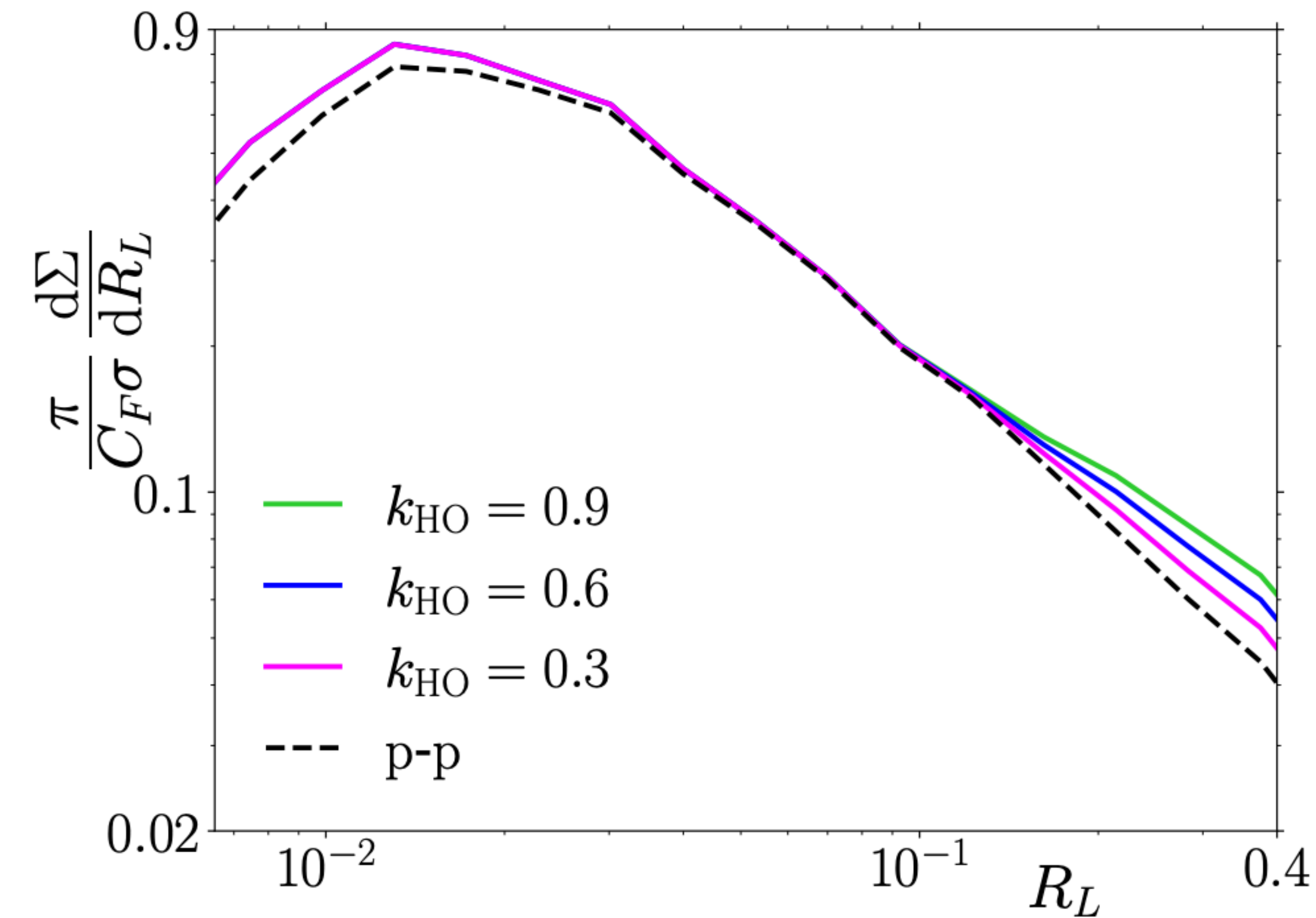
Thank you!

Multiple scatterings

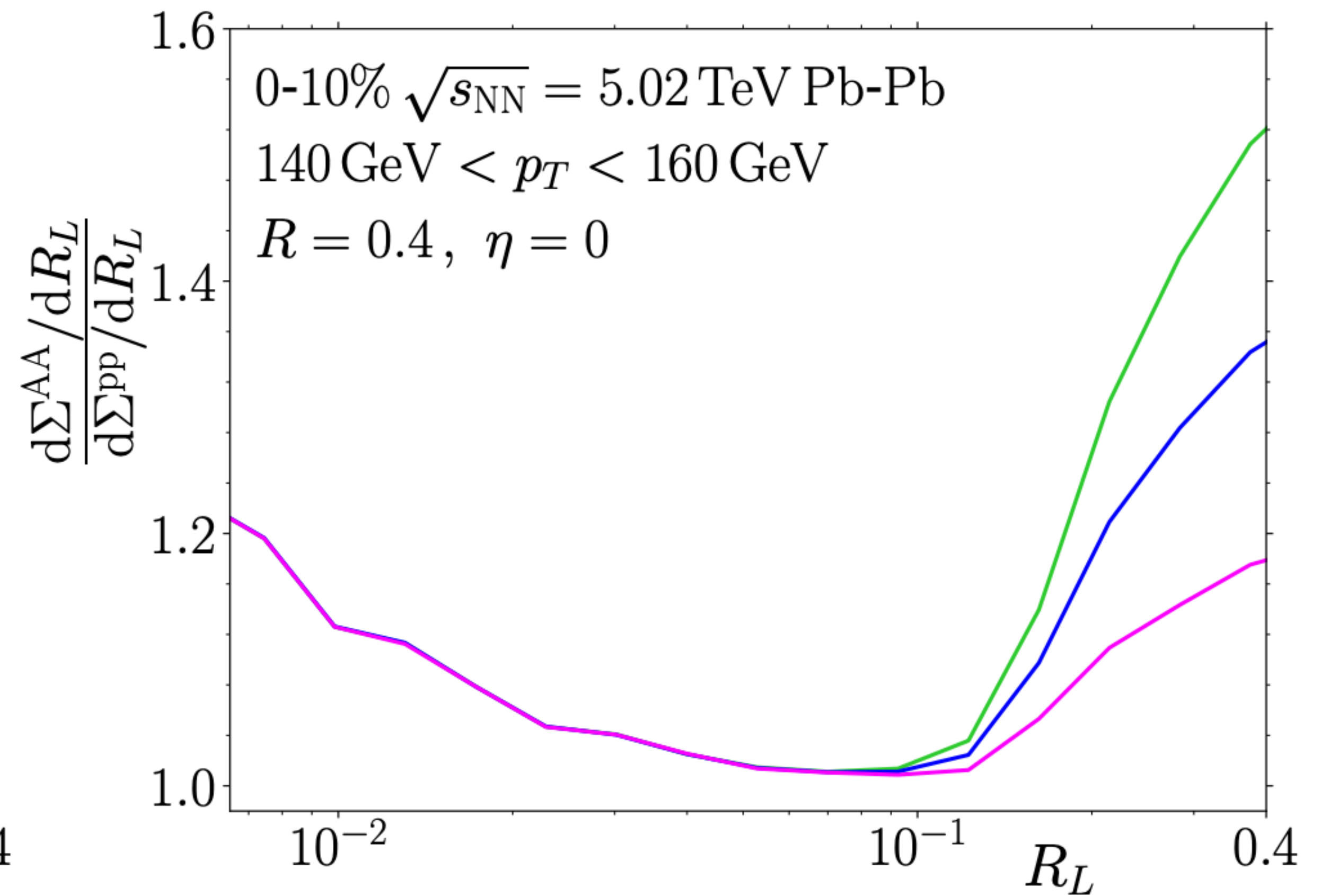


Multiple scatterings

Inclusive jets

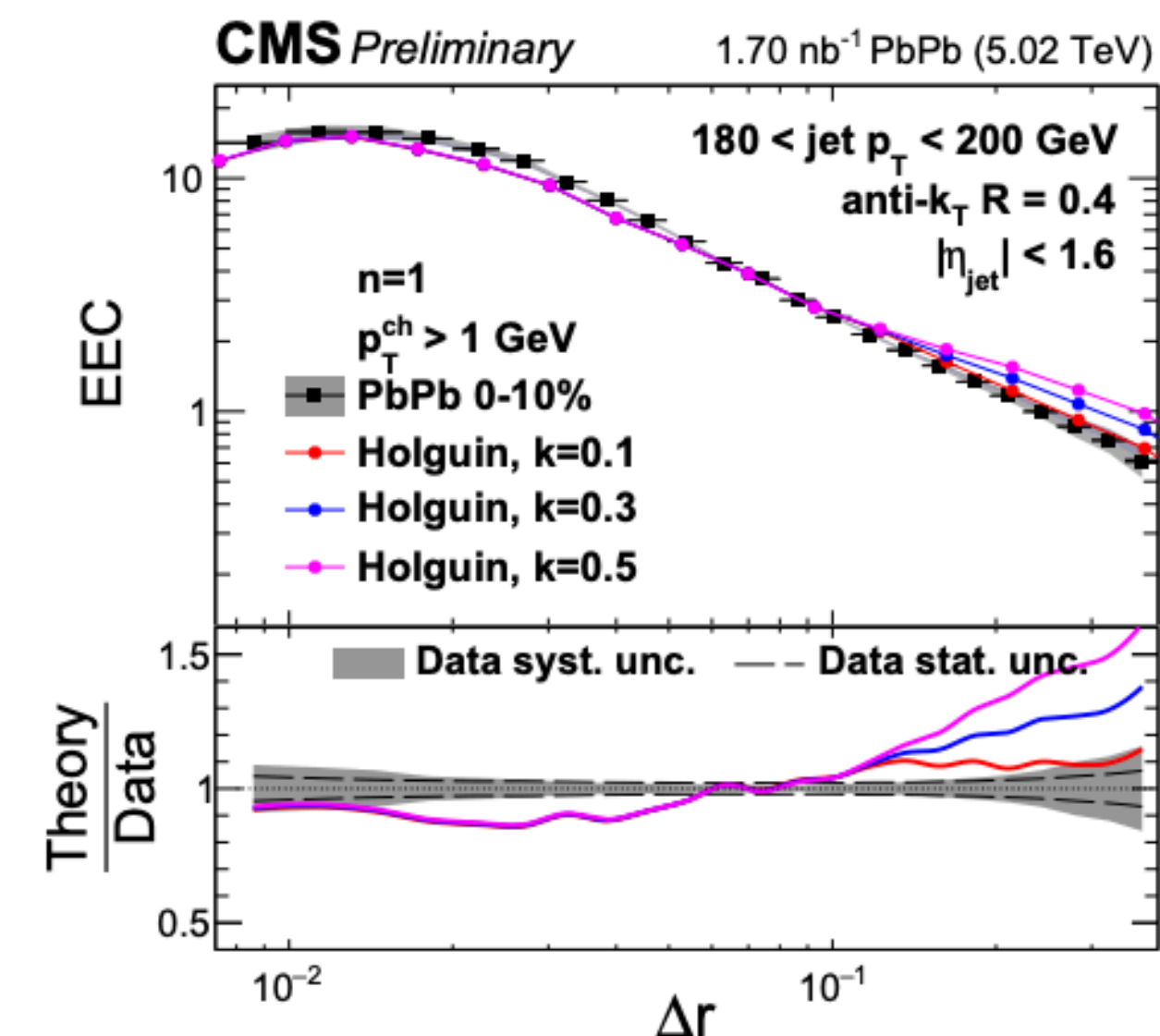
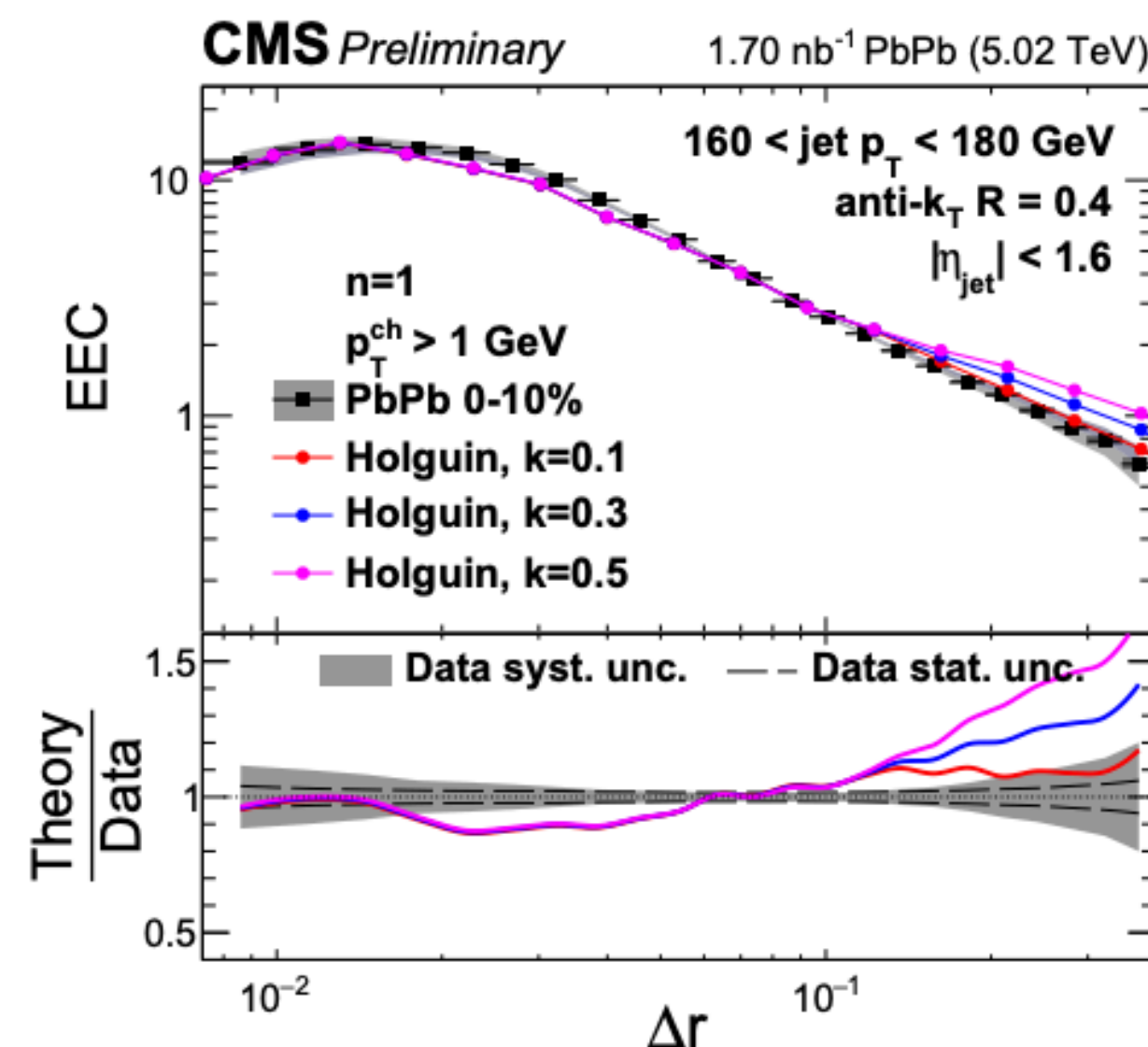
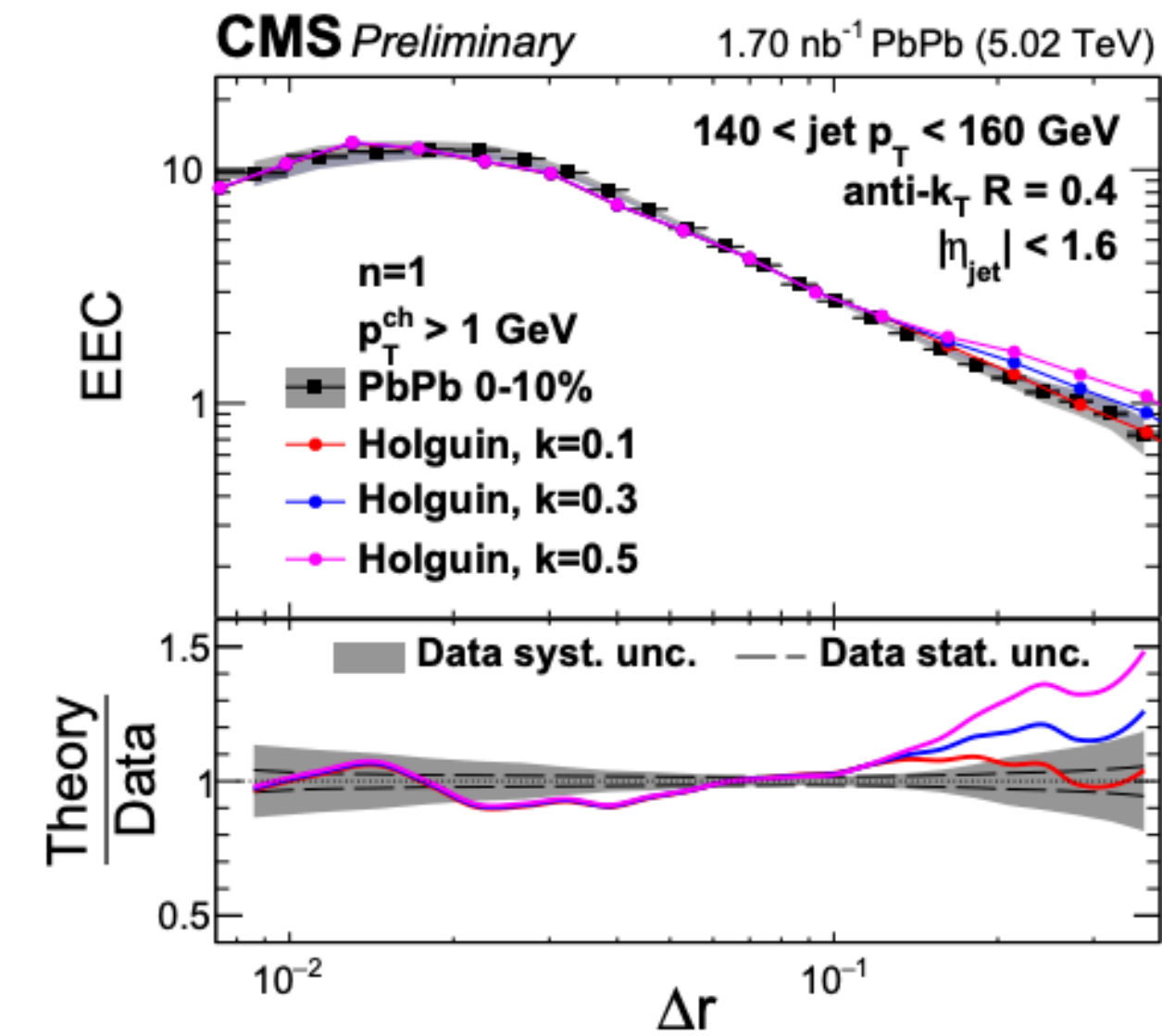
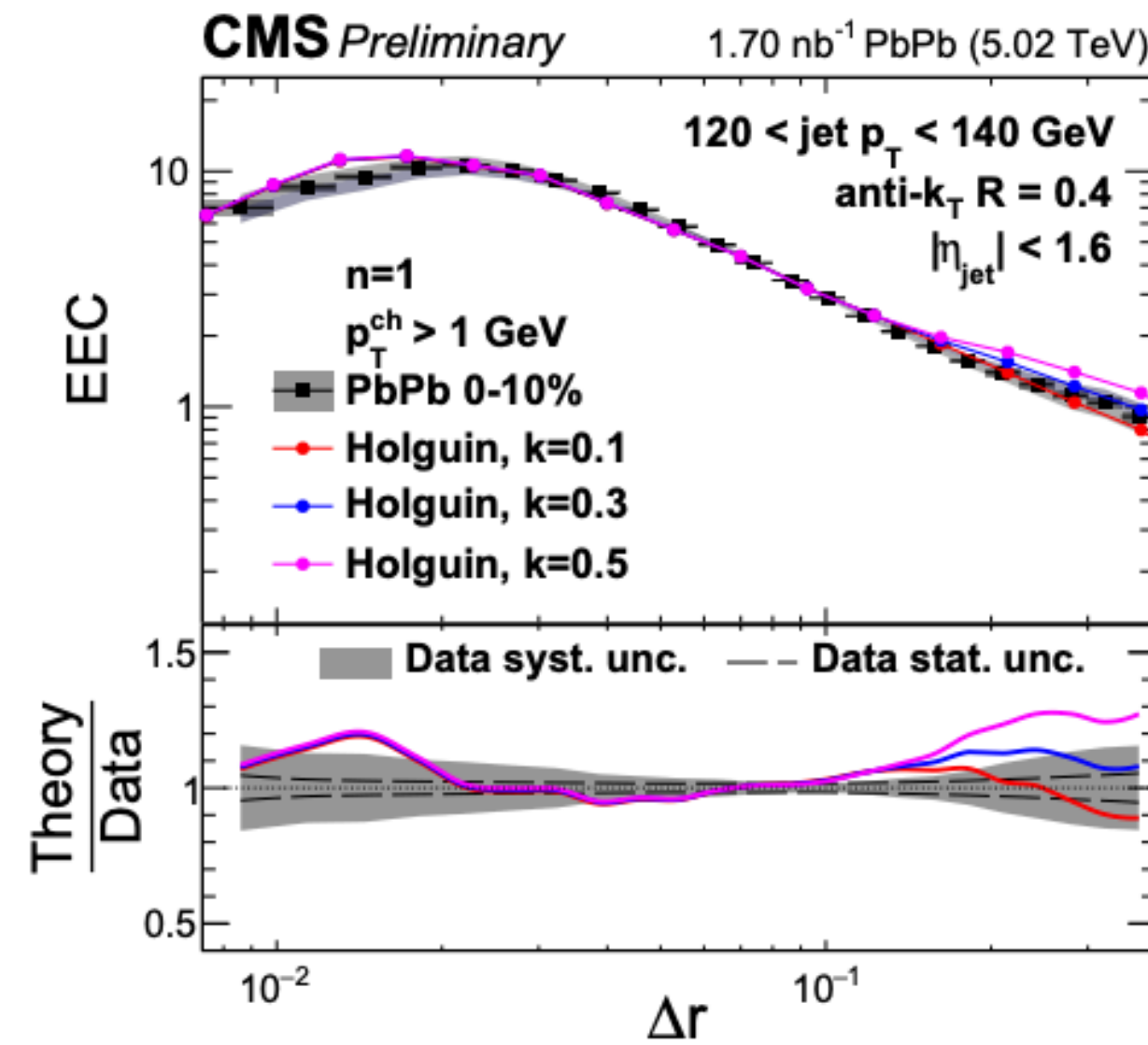


Inclusive jets

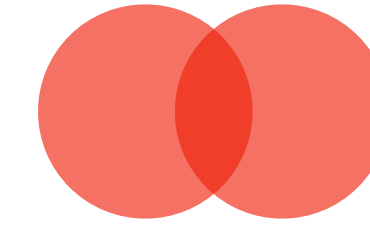
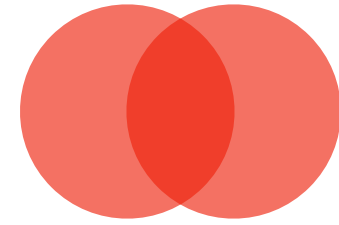
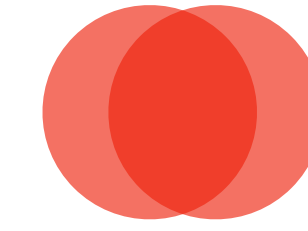
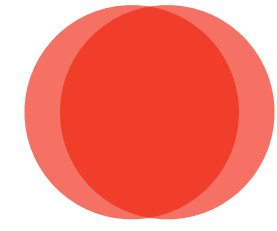


p_T dependence

From [Jussi Viinikainen's talk](#) unveiling the measurement at the [Energy Correlators at the Collider Frontier workshop](#)



Mitigating energy loss



Mitigating energy loss

$120 < p_T < 140$ GeV, Centrality dependence

