

Probing Hadronization Through Jet Substructure Analysis

ArXiv: [arXiv:2212.11846v2](https://arxiv.org/abs/2212.11846v2)

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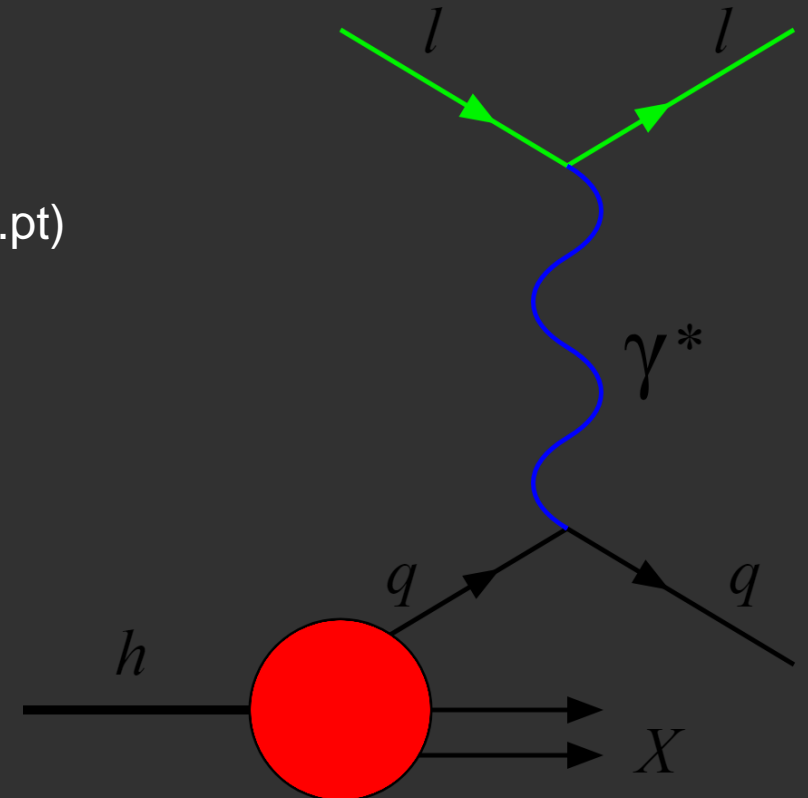
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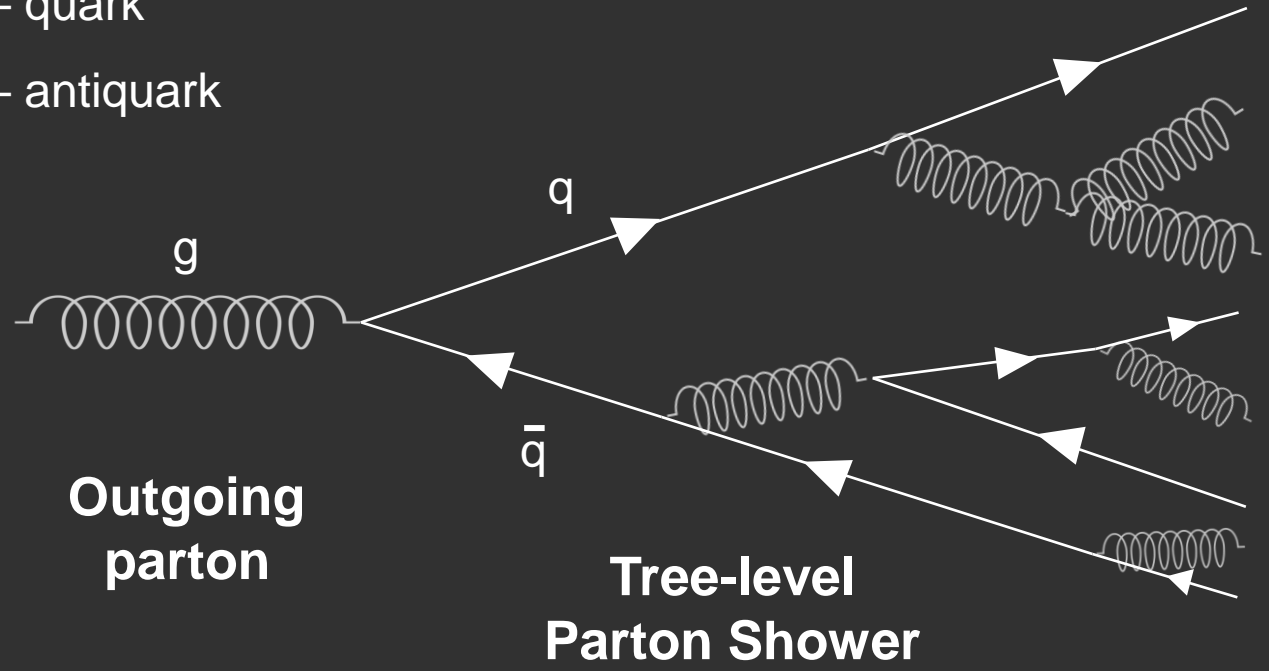


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Collision Physics

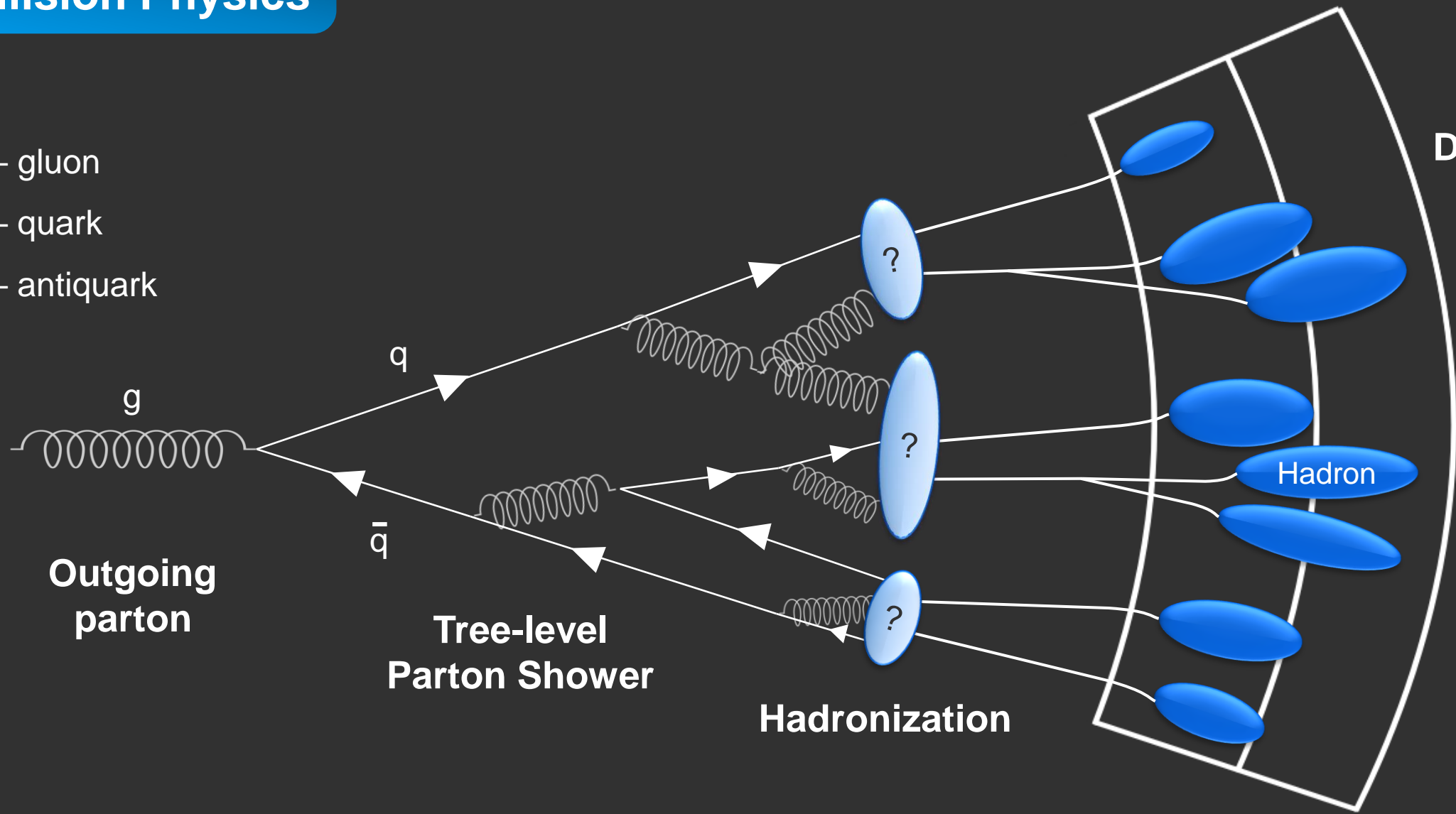
g – gluon
 q – quark
 \bar{q} – antiquark



Perturbative QCD

Collision Physics

g – gluon
 q – quark
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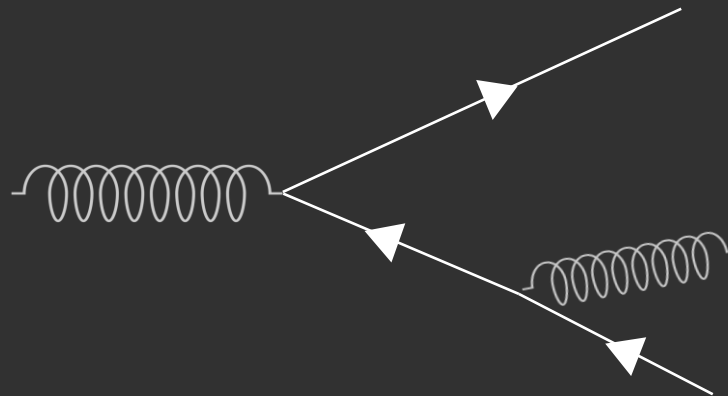
Perturbative QCD

Non-perturbative QCD

Hadronization Models

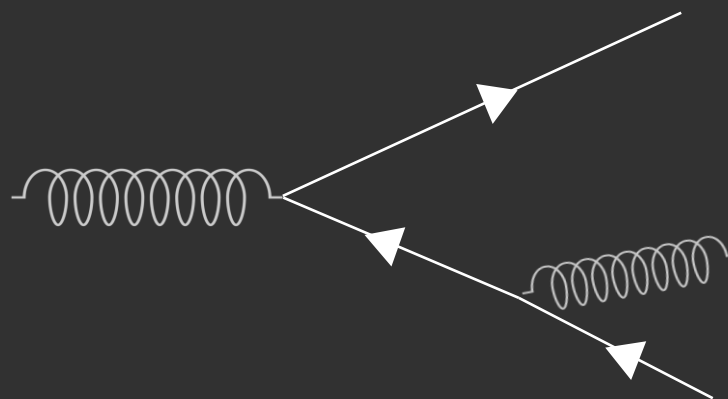
Lund String (Pythia, Jetset)

[B. Andersson, G. Gustafson, and B. Soderberg, Z. Phys.C 20, 317 (1983)]



Cluster Fragmentation (Herwig, Sherpa)

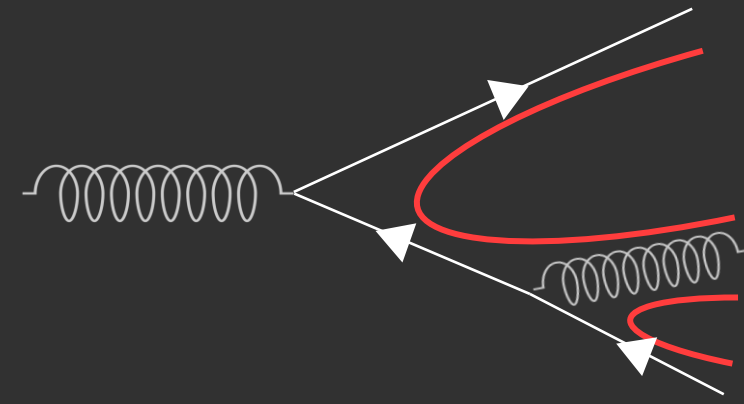
[D. Amati and G. Veneziano, Phys. Lett. B 83, 87 (1979)]



Hadronization Models

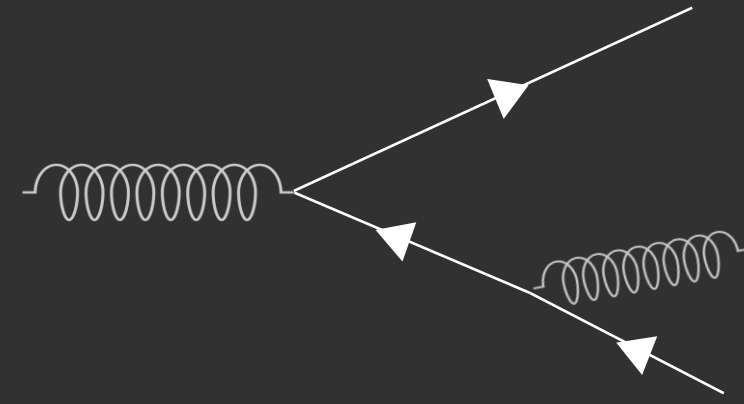
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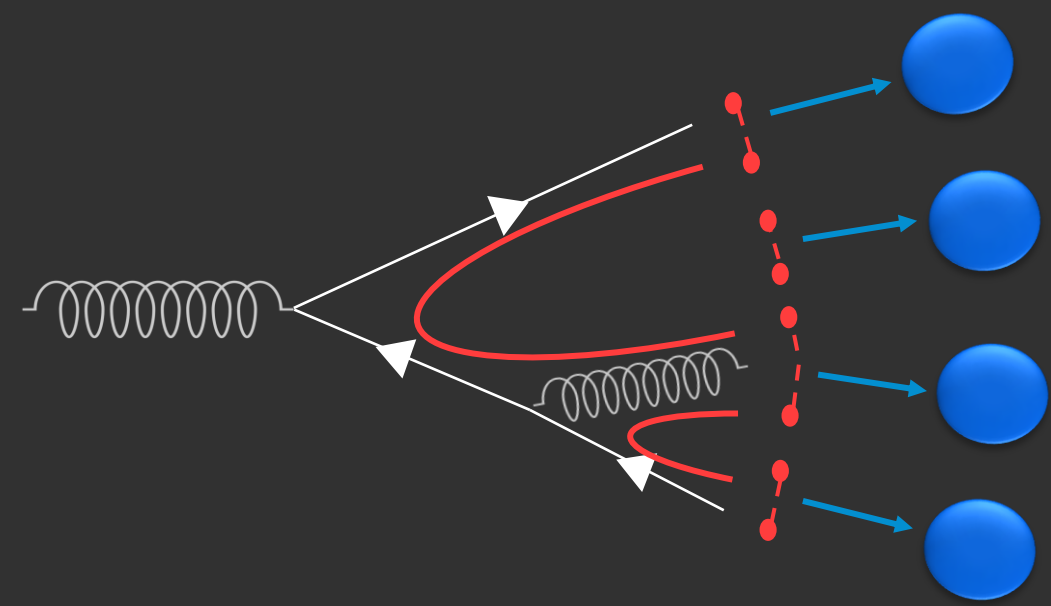
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Hadronization Models

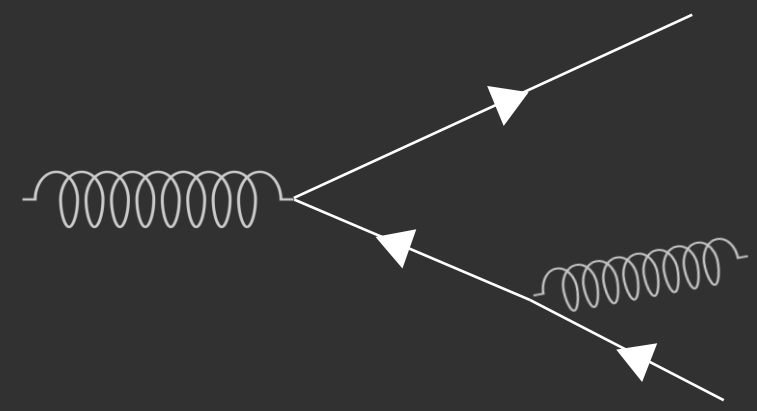
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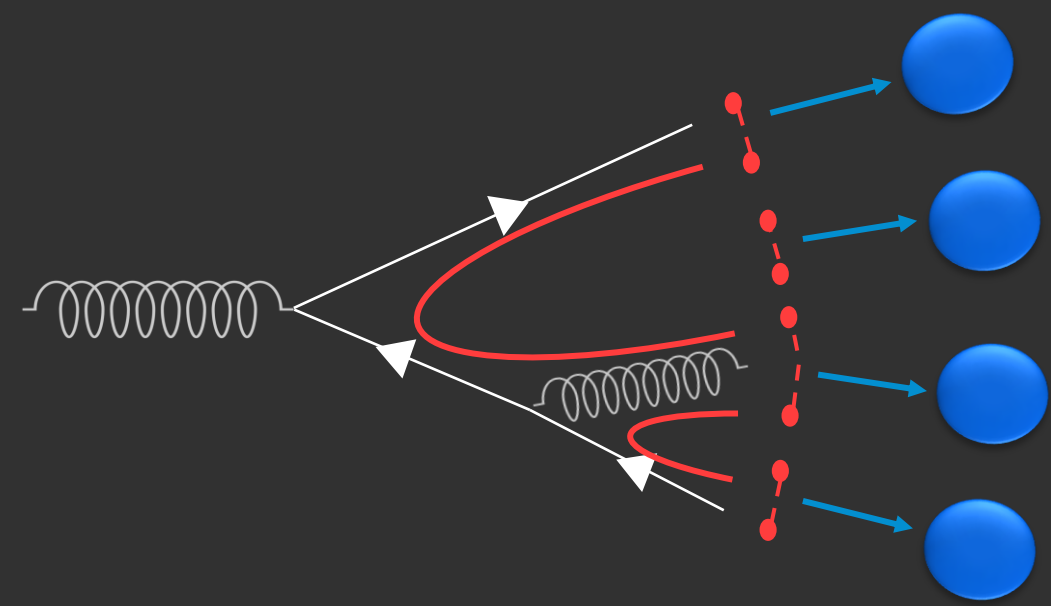
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Hadronization Models

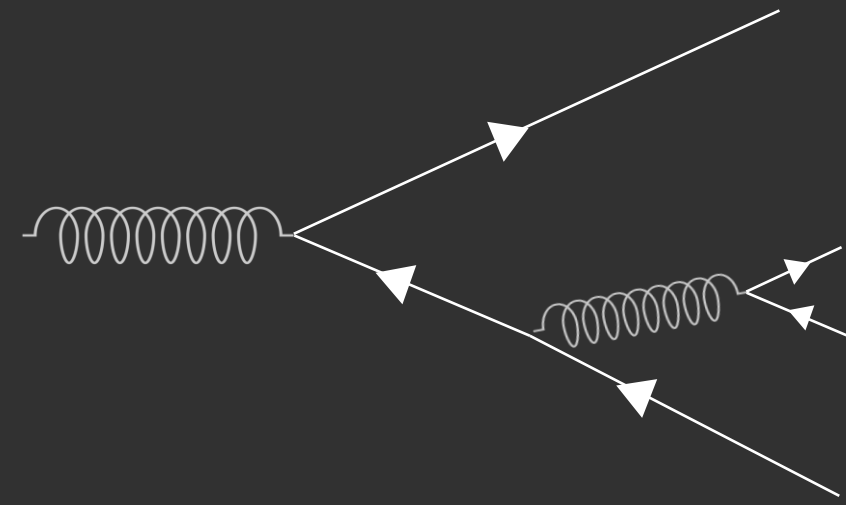
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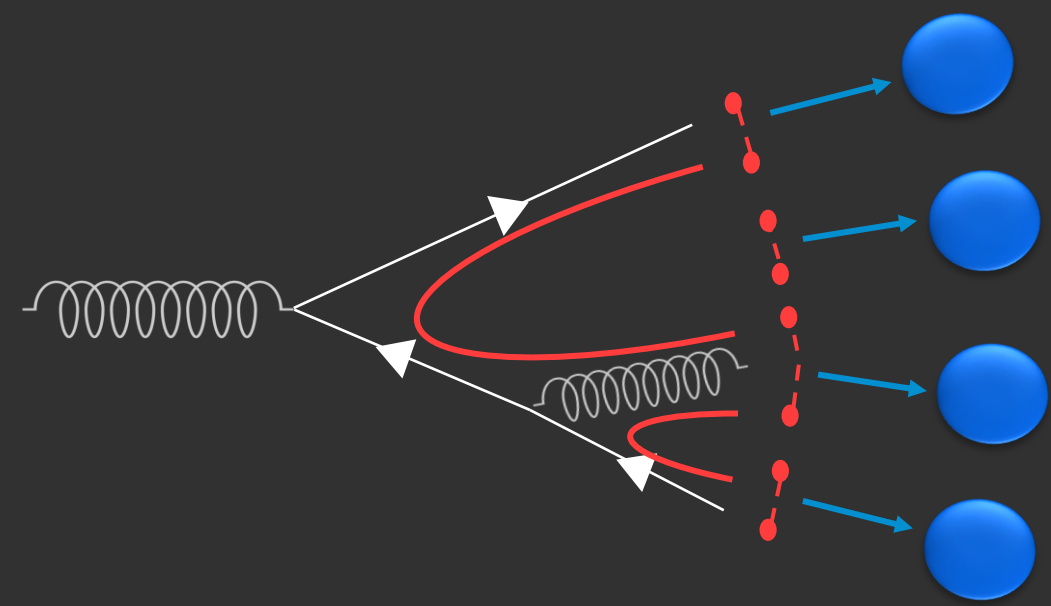
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Hadronization Models

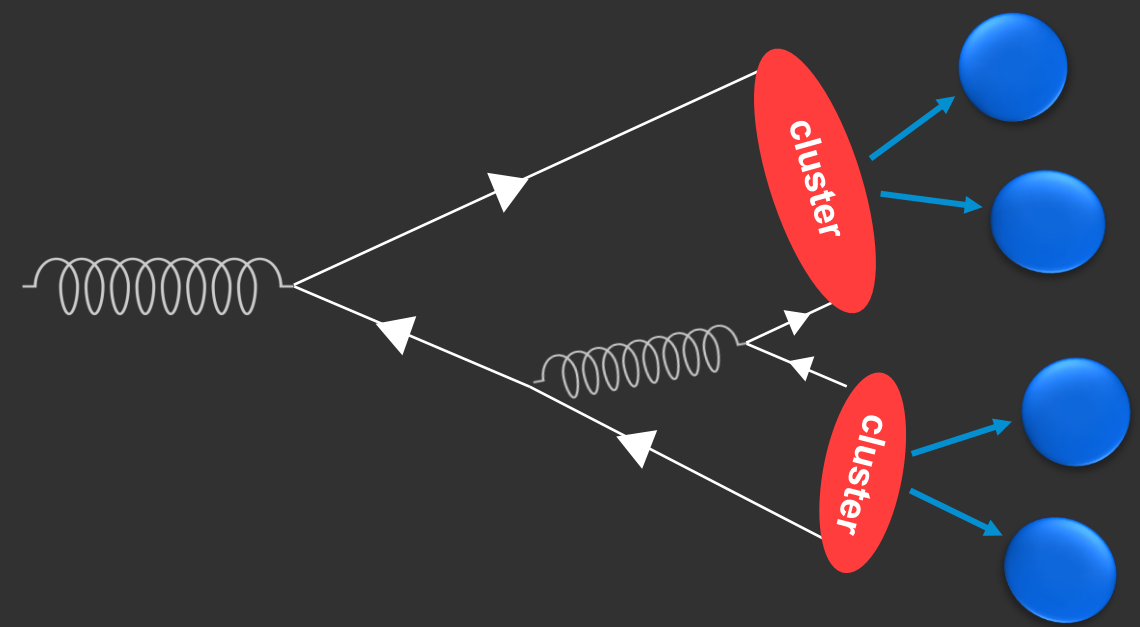
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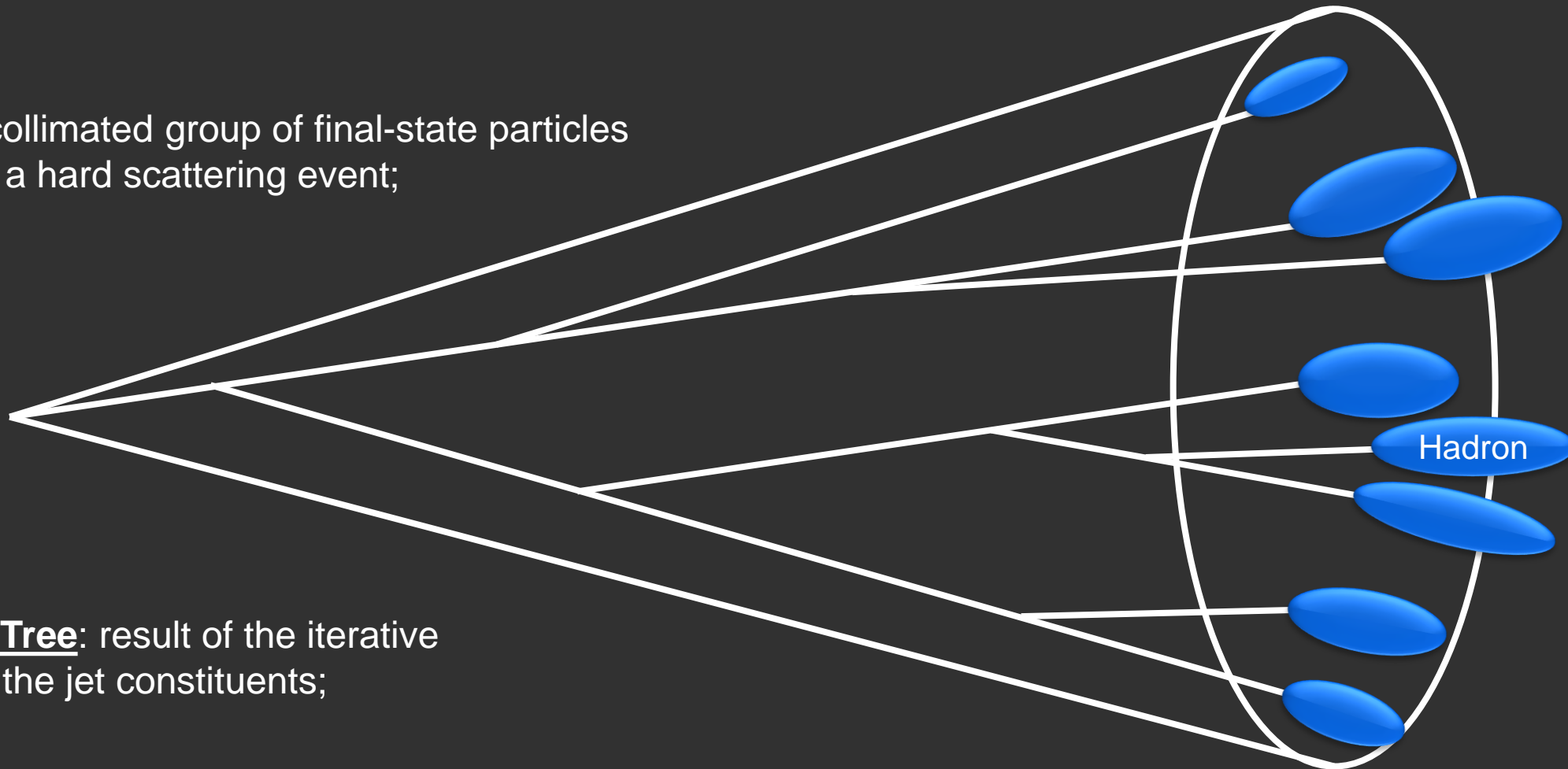
[D. Amati and G. Veneziano, Phys. Lett. B 83, 87 (1979)]



Jets

Jet: highly-collimated group of final-state particles produced in a hard scattering event;

Clustering Tree: result of the iterative grouping of the jet constituents;



- **Objective:** find substructure observables with increased sensitivity to hadronization effects!

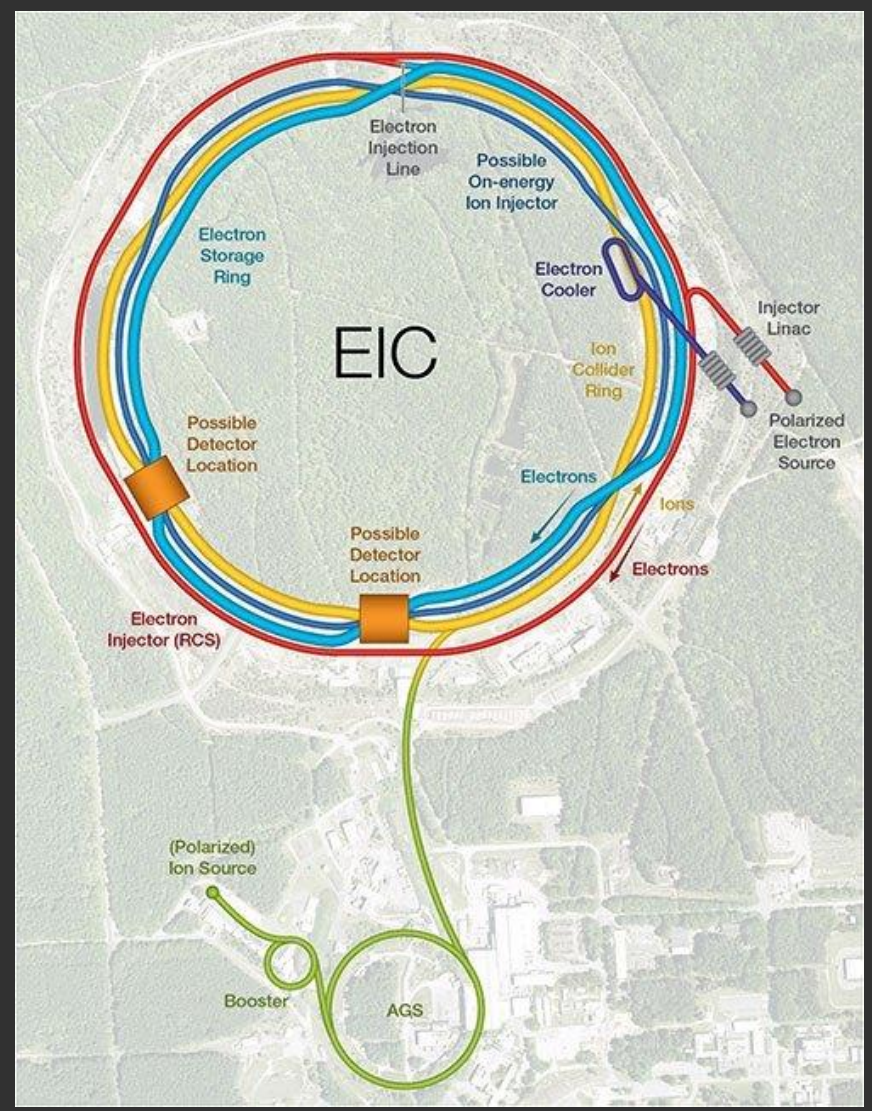
Simulation and Jet Analysis

➤ Monte Carlo event generators: **PYTHIA 8.306** and **HERWIG 7**;

Settings	Values
E_e	18 GeV
E_p	275 GeV
Q^2	$> 50 \text{ GeV}^2$
$p_{T,part}$	$> 0.2 \text{ GeV}/c$

➤ Jets are found using the anti- k_T jet clustering algorithm and re-clustered using the τ algorithm with SoftDrop grooming.

Settings	Values
R	1
$p_{T,jet}$	$> 5 \text{ GeV}/c$
η_{jet}	$-1.5 < \eta_{jet} < 3.5$
z_{cut}	0.1
β	0

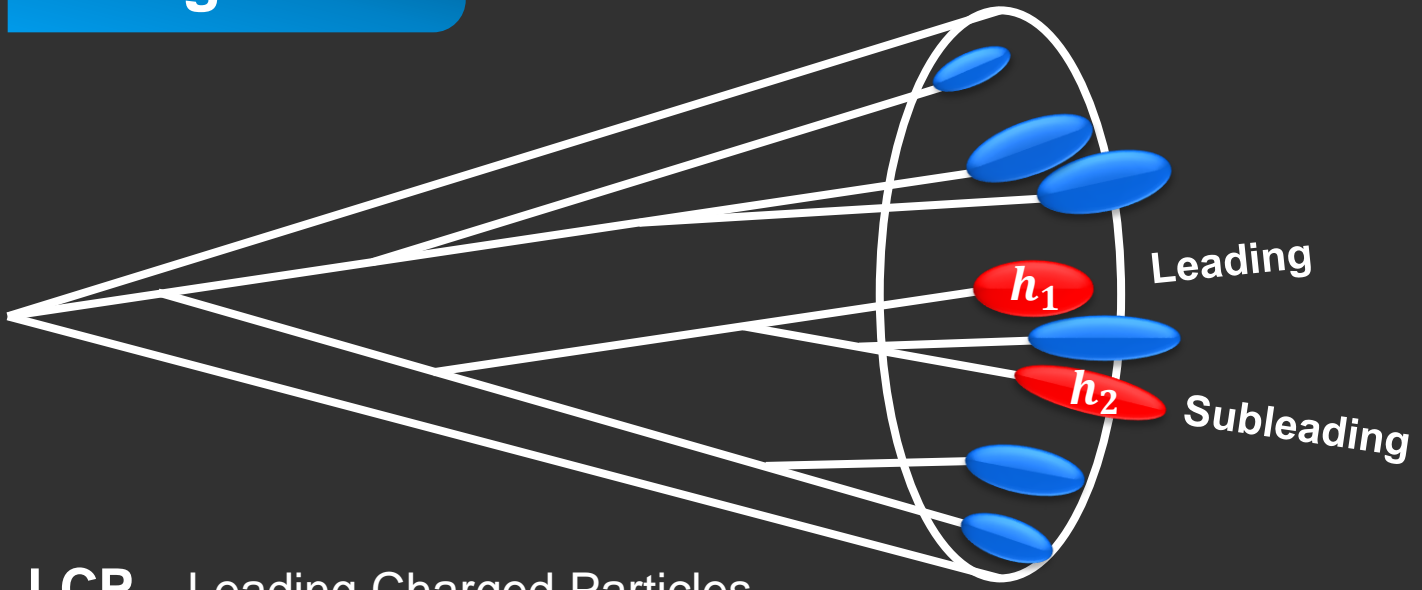


[A. J. Larkoski et al., arXiv:1402.2657v2]

SD criterion:
$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} > z_{cut} \left(\frac{\Delta R_{12}}{R} \right)^\beta$$

Charge Ratio

[Y.-T. Chien et al, arXiv:2109.15318]



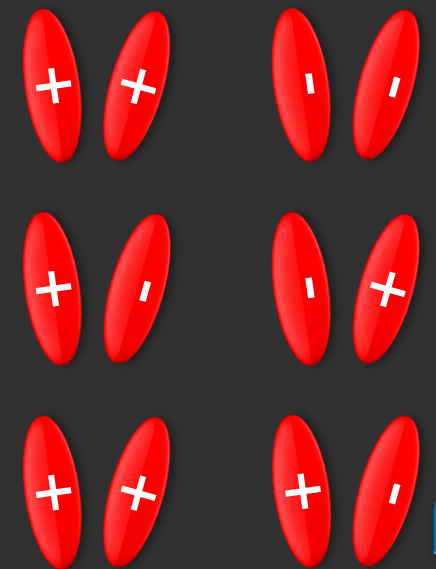
LCP – Leading Charged Particles

Charge Correlation Ratio:

$$r_c = \frac{\frac{d\sigma_{h_1 h_2}}{dX} - \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}{\frac{d\sigma_{h_1 h_2}}{dX} + \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}$$

h_1, h_2 – pion (π), kaon (K), proton (p)
 X – jet substructure variable of choice

- $r_c > 0$: higher probability of producing jets with equally-charged LCP;
- $r_c < 0$: higher probability of producing jets with oppositely-charged LCP;
- $r_c = 0$: jets produced randomly with equally- or oppositely-charged LCP.



Formation Time

[L. Apolinário et al, arXiv:2012.021999]

[L. Apolinário et al, arXiv:2401.14229]

Formation Time

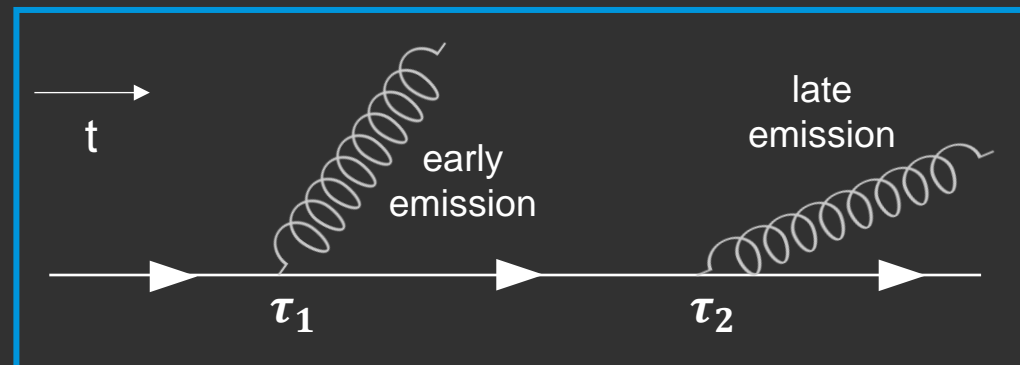
$$\tau_{form} = \frac{1}{2 E z (1 - z) (1 - \cos \theta_{12})}$$

Estimate of the timescales involved in a particle splitting into 2 other particles that act as independent sources of additional radiation

E source energy

θ_{12} angle between the 2 emitted prongs

$z = \frac{\min(E_1, E_2)}{E_1 + E_2}$ energy fraction



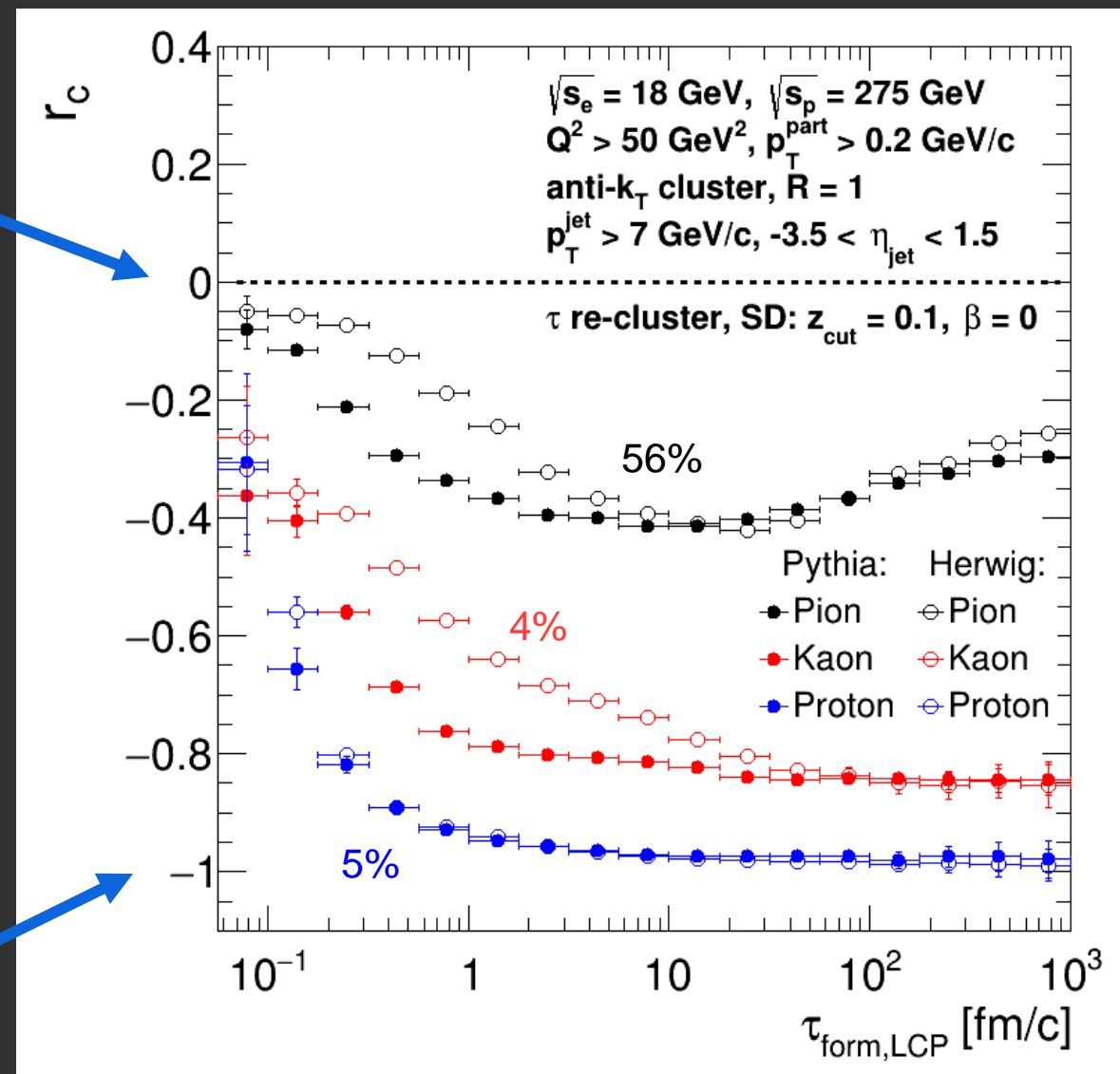
$$\tau_1 < \tau_2$$

Charge Ratio

$$r_c = \frac{\frac{d\sigma_{h_1 h_2}}{dX} - \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}{\frac{d\sigma_{h_1 h_2}}{dX} + \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}, \quad X = \tau_{form}$$

50% same-sign, 50% opposite-sign jets

0% same-sign, 100% opposite-sign jets



[Similar to study in Y.-T. Chien et al, arXiv:2109.15318]

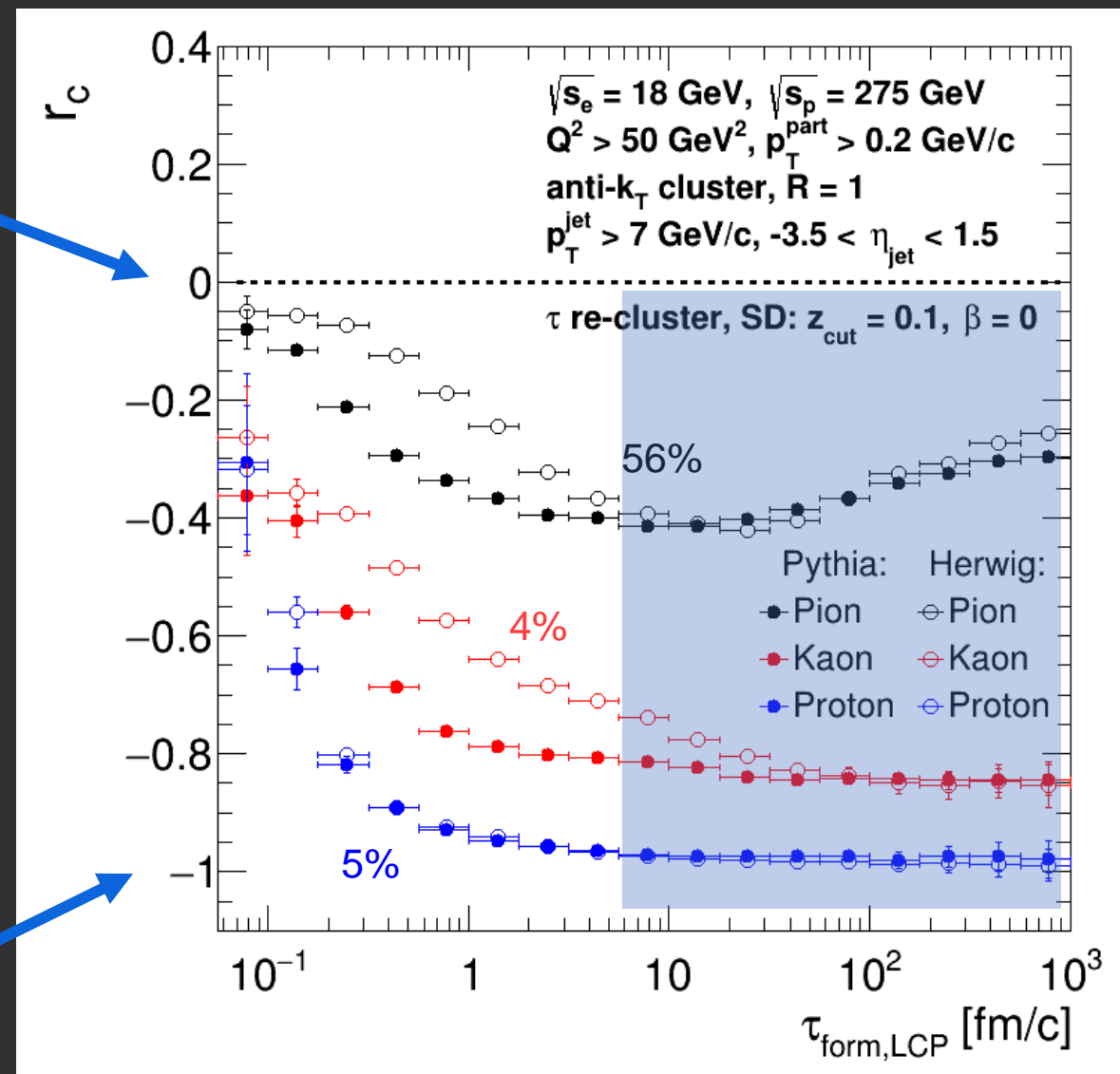
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50% same-sign, 50% opposite-sign jets

➤ **Late time LCP:** $r_c \sim$ constant and close to -1, meaning jets more likely to have opposite-sign LCP;

0% same-sign, 100% opposite-sign jets



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Charge Ratio

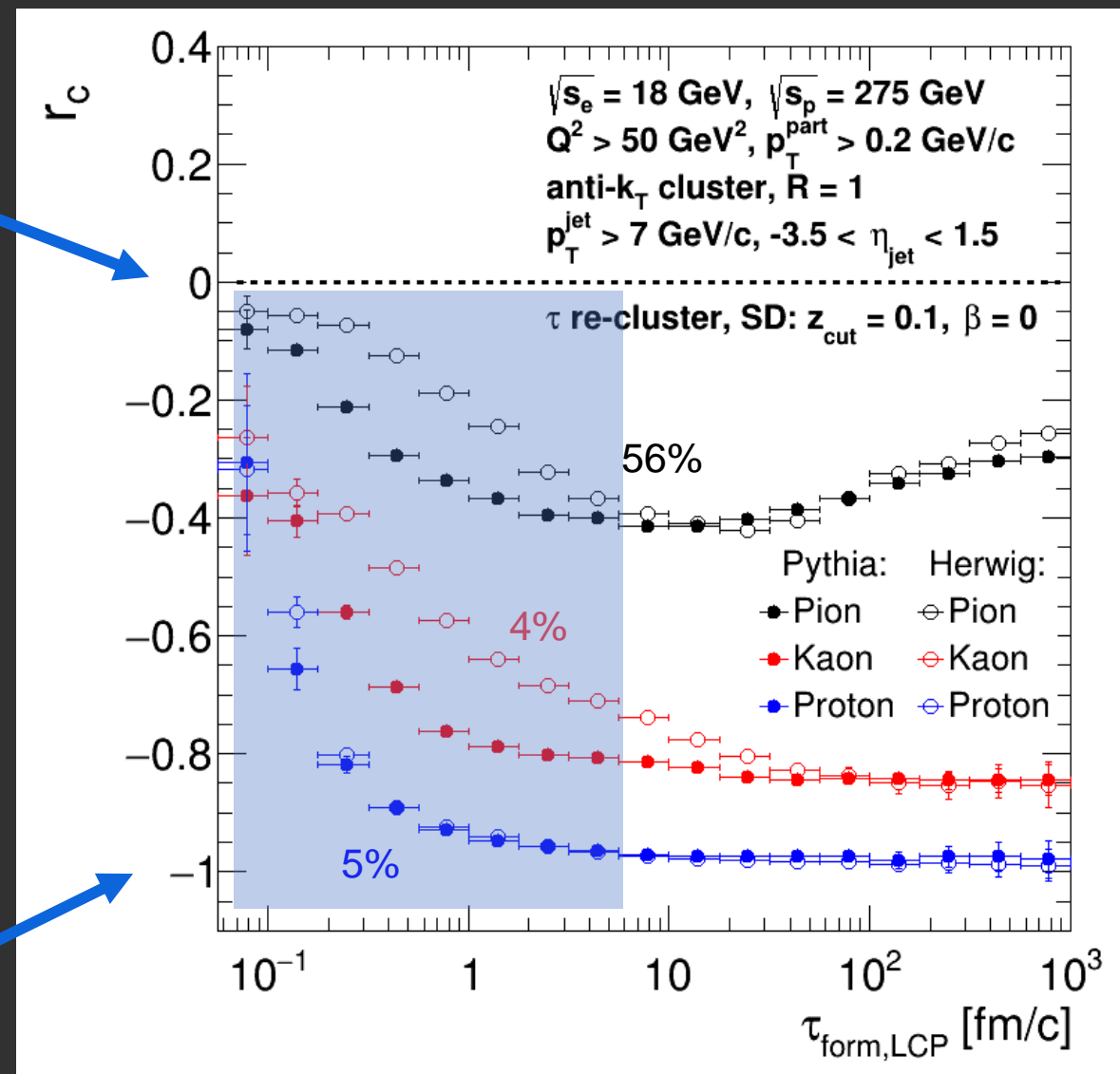
$$r_c = \frac{\frac{d\sigma_{h_1 h_2}}{dX} - \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}{\frac{d\sigma_{h_1 h_2}}{dX} + \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}, \quad X = \tau_{form}$$

50% same-sign, 50% opposite-sign jets

➤ **Late time LCP:** $r_c \sim$ constant and close to -1, meaning jets more likely to have opposite-sign LCP;

➤ **Early time LCP:** r_c closer to 0, meaning larger charge randomization of the leading particles;

0% same-sign, 100% opposite-sign jets



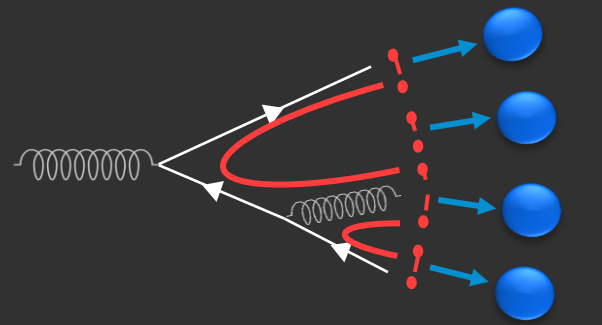
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Charge Ratio

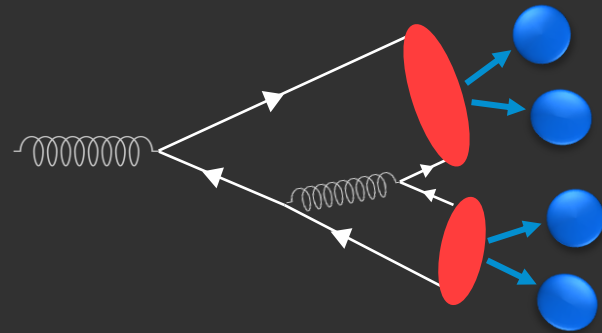
$$r_c = \frac{\frac{d\sigma_{h_1 h_2}}{dX} - \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}{\frac{d\sigma_{h_1 h_2}}{dX} + \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}, \quad X = \tau_{form}$$

50% same-sign, 50% opposite-sign jets

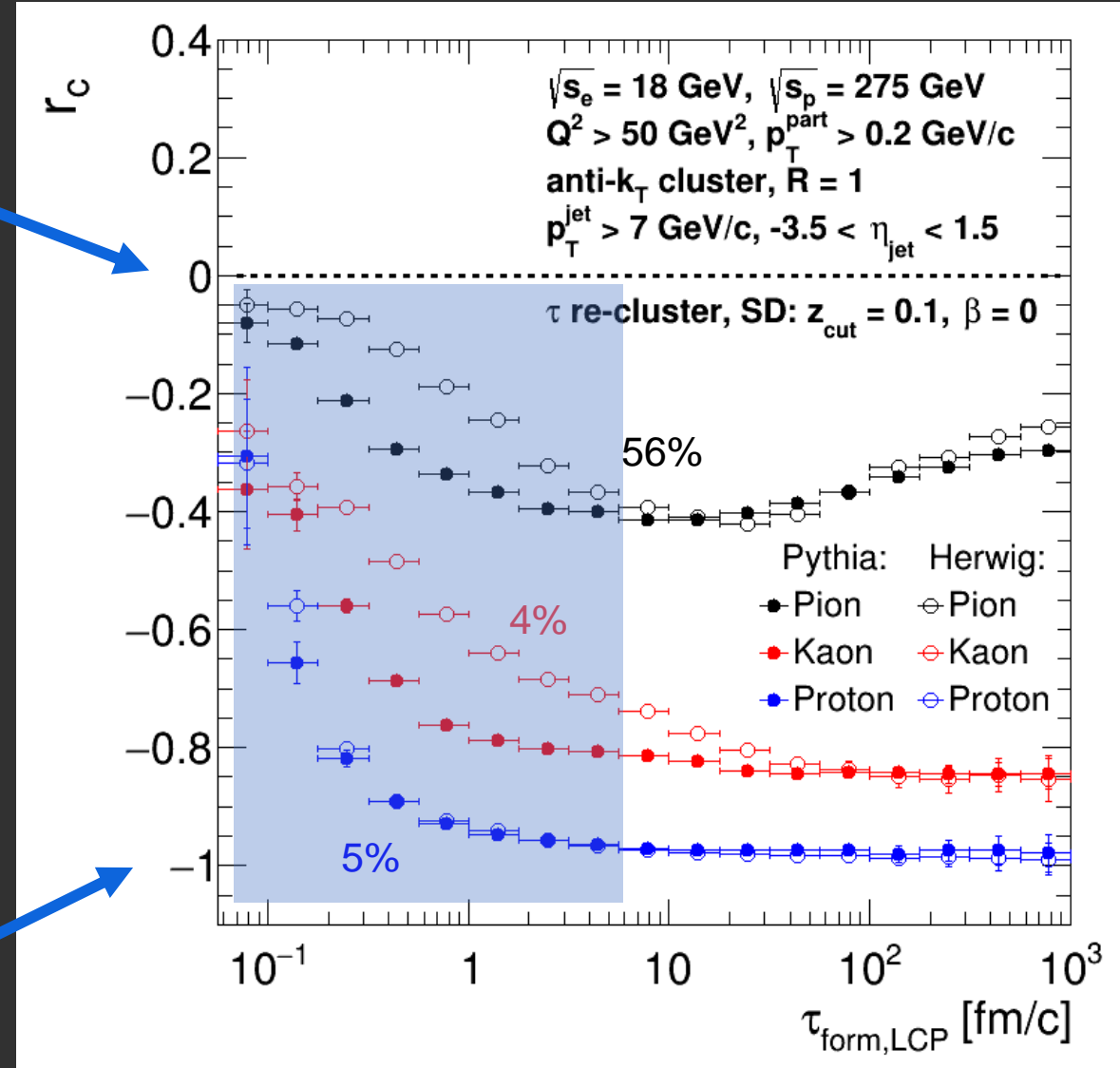
Lund String



Cluster Fragmentation



0% same-sign, 100% opposite-sign jets



[Similar to study in Y.-T. Chien et al, arXiv:2109.15318]

Charge Ratio

$$r_c = \frac{\frac{d\sigma_{h_1 h_2}}{dX} - \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}{\frac{d\sigma_{h_1 h_2}}{dX} + \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}, \quad X = \tau_{form}$$

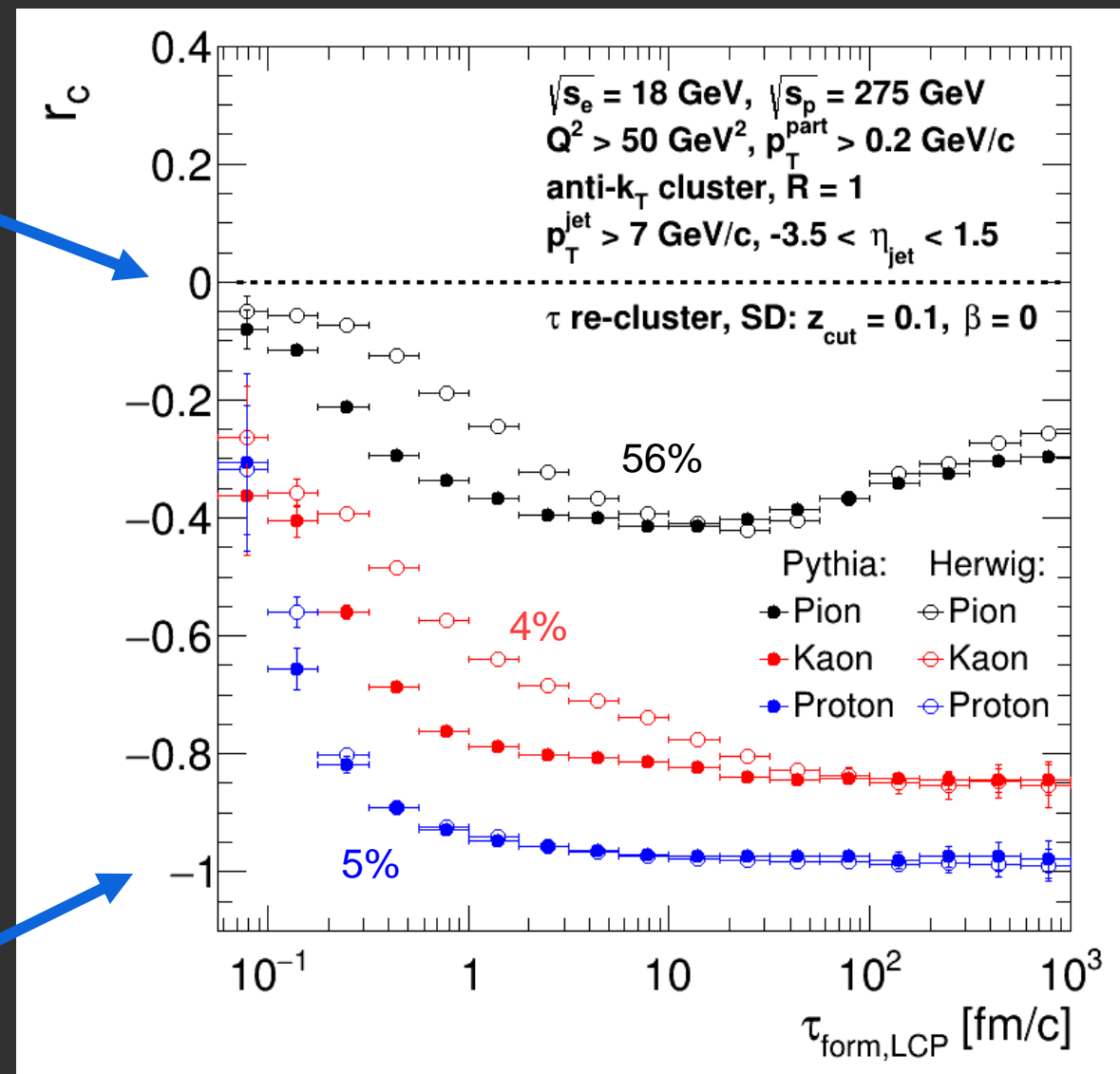
50% same-sign, 50% opposite-sign jets

$$z_{LCP} \sim 0.5$$

$$\tau_{form,LCP} = \frac{1}{2 E z (1-z) (1 - \cos \theta_{12})} \sim \frac{1}{E \theta^2}$$

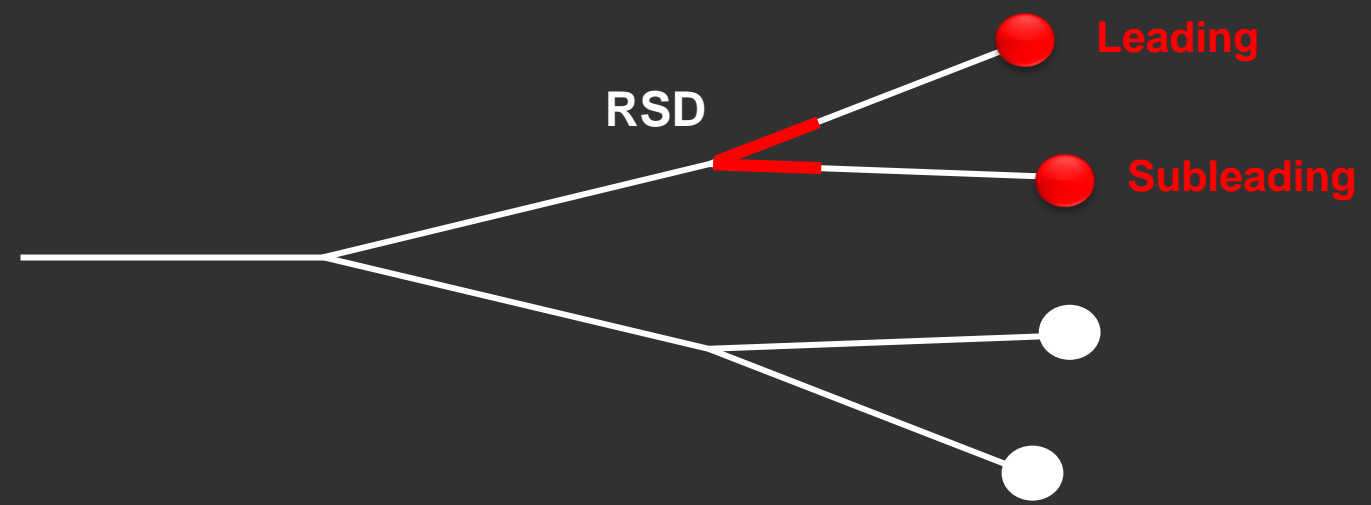
- Where in the clustering tree are the leading charged particles coming from?
- What is the r_c dependence on jet substructure?

0% same-sign, 100% opposite-sign jets



[Similar to study in Y.-T. Chien et al, arXiv:2109.15318]

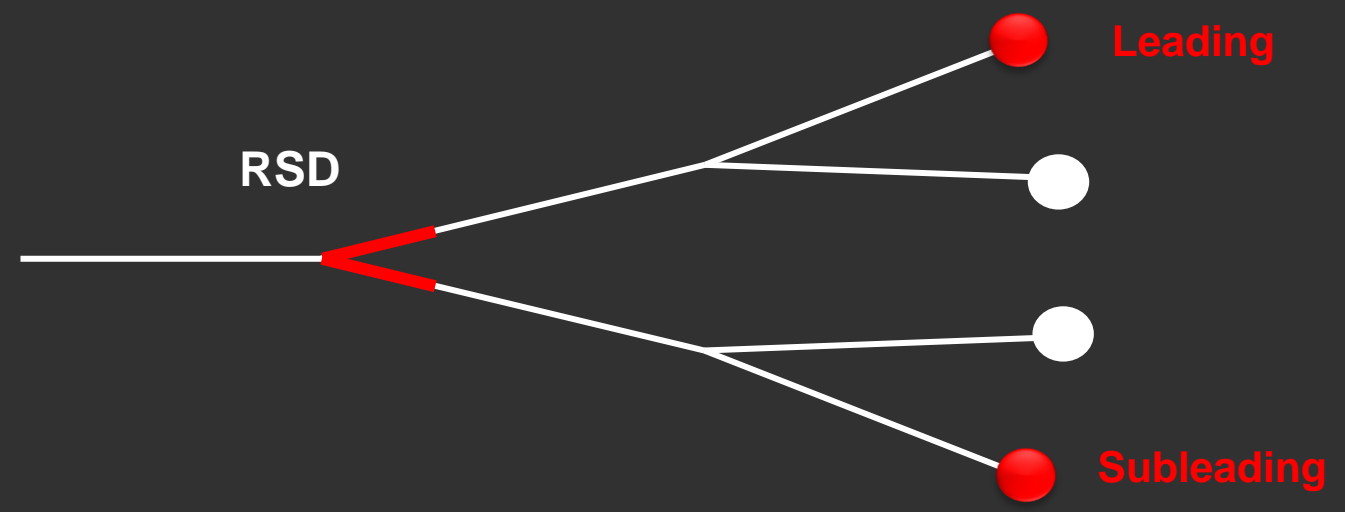
Resolved SoftDrop Splitting – RSD



➤ The **RSD** is the SoftDrop splitting in the clustering tree where the leading charged particles get separated into 2 different subjects;

➤ **Top** clustering tree:

- $N_{SD} = 2$
- $N_{RSD} = 2$
- RSD depth = $N_{RSD}/N_{SD} = 2/2$



➤ **Bottom** clustering tree:

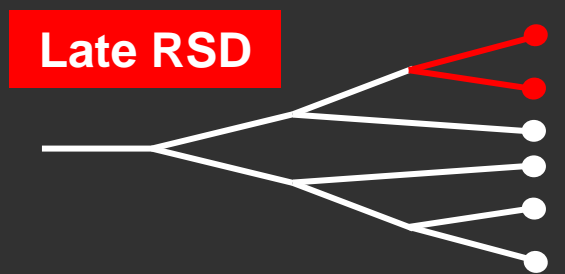
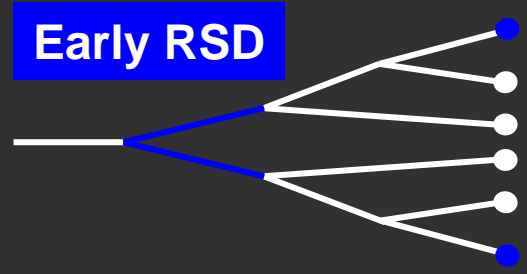
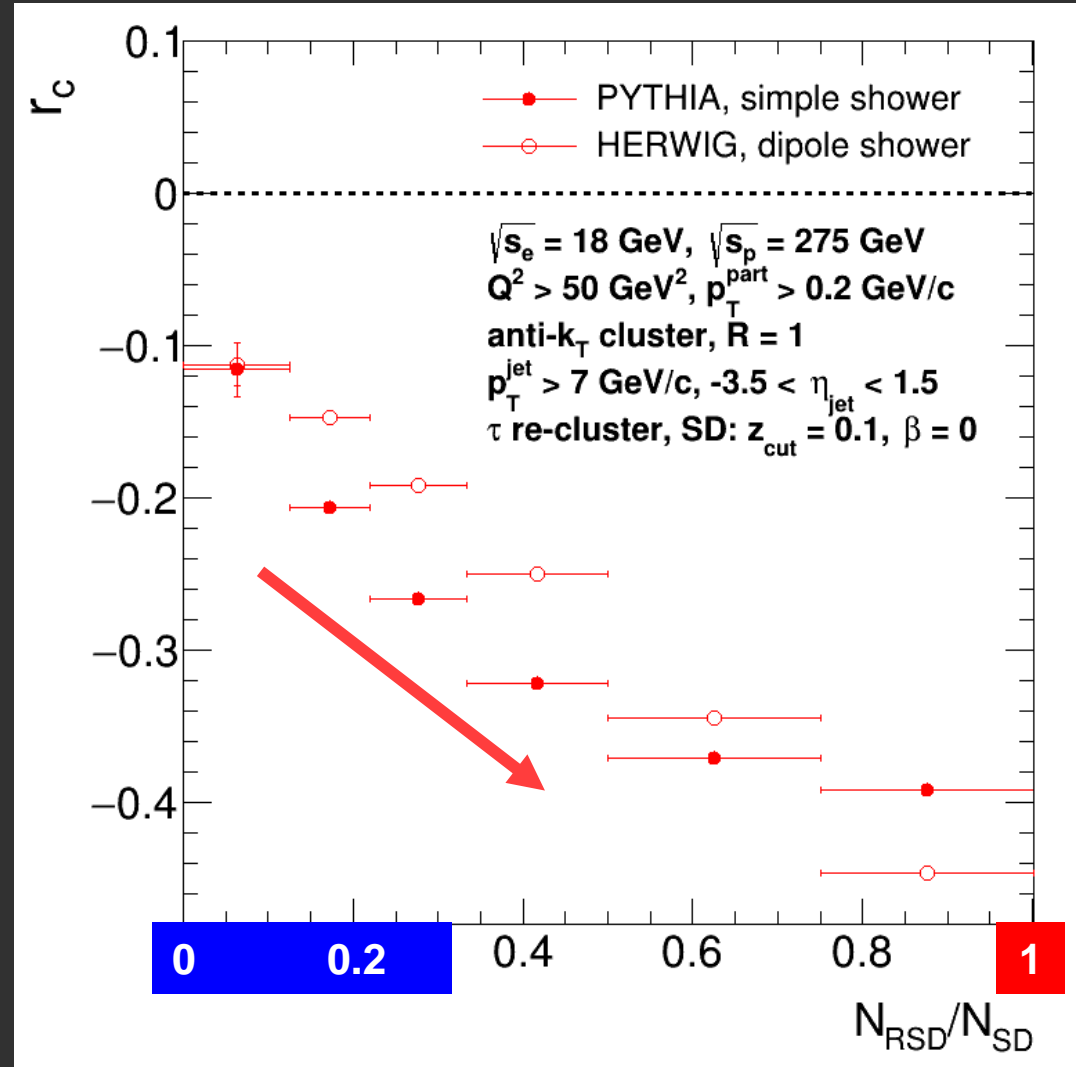
- $N_{SD} = 2$
- $N_{RSD} = 1$
- RSD depth = $N_{RSD}/N_{SD} = 1/2$

Charge Ratio vs RSD Depth

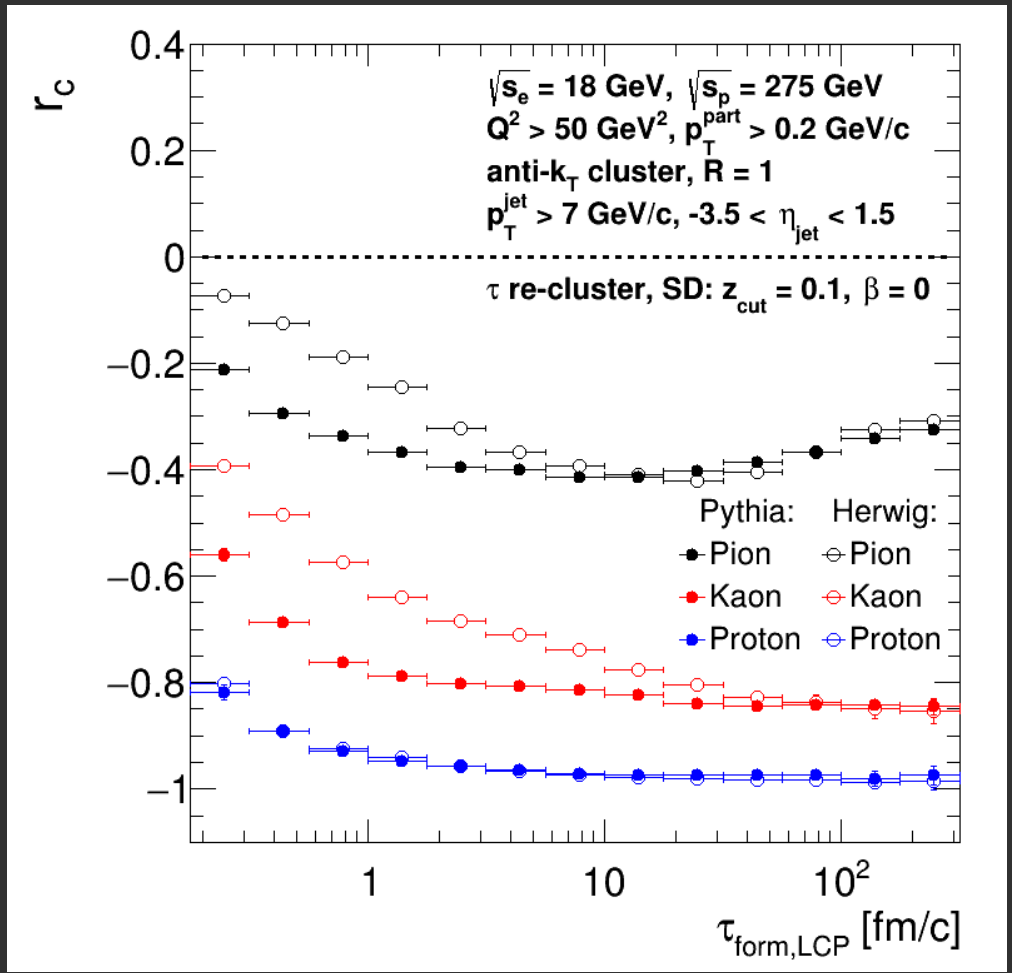
$$r_c = \frac{\frac{d\sigma_{h_1 h_2}}{dX} - \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}{\frac{d\sigma_{h_1 h_2}}{dX} + \frac{d\sigma_{h_1 \bar{h}_2}}{dX}}, \quad X = \frac{N_{RSD}}{N_{SD}}$$

- **Large RSD depths:** few subsequent branchings, “remembers” charge correlation of leading particles;
- **Small RSD depths:** several subsequent branchings, “forgets” charge correlation of leading particles

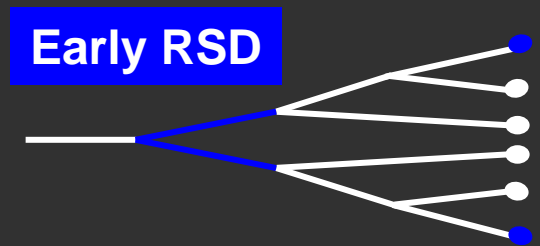
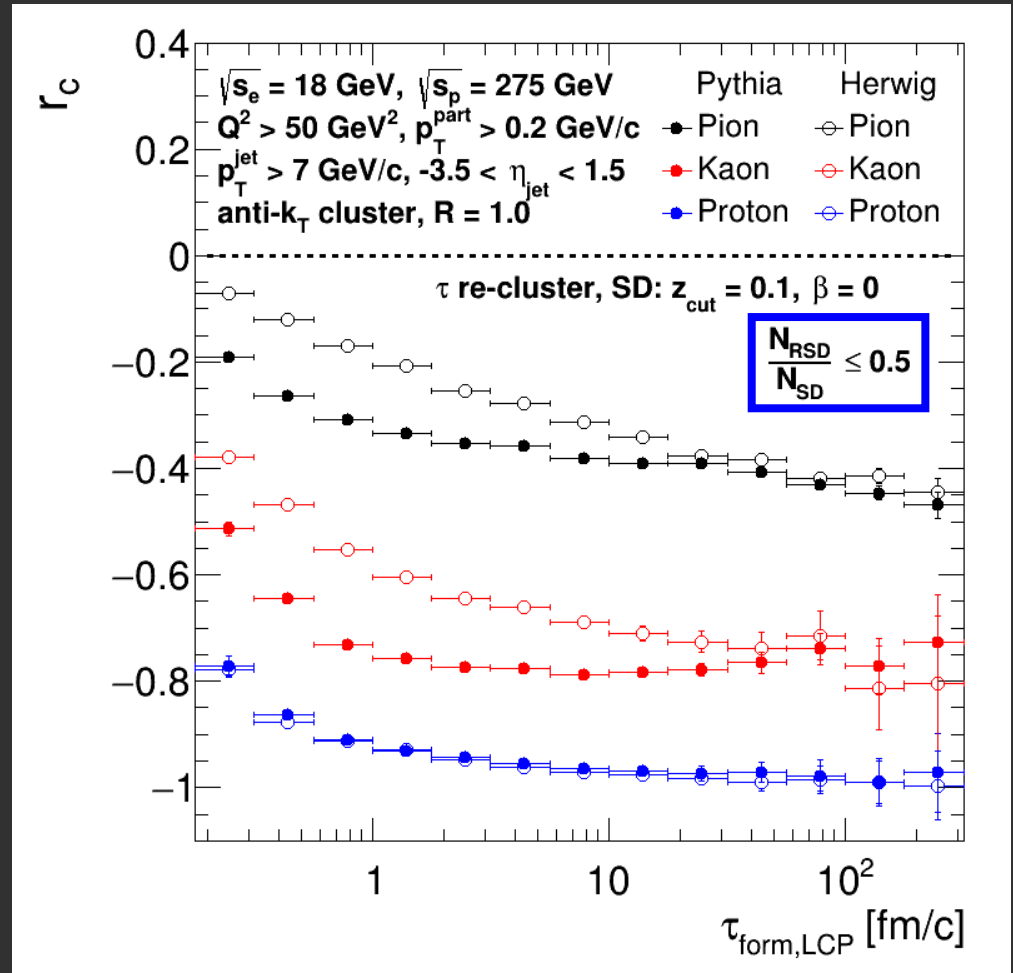
Conclusion: r_c depends strongly on jet substructure topology!



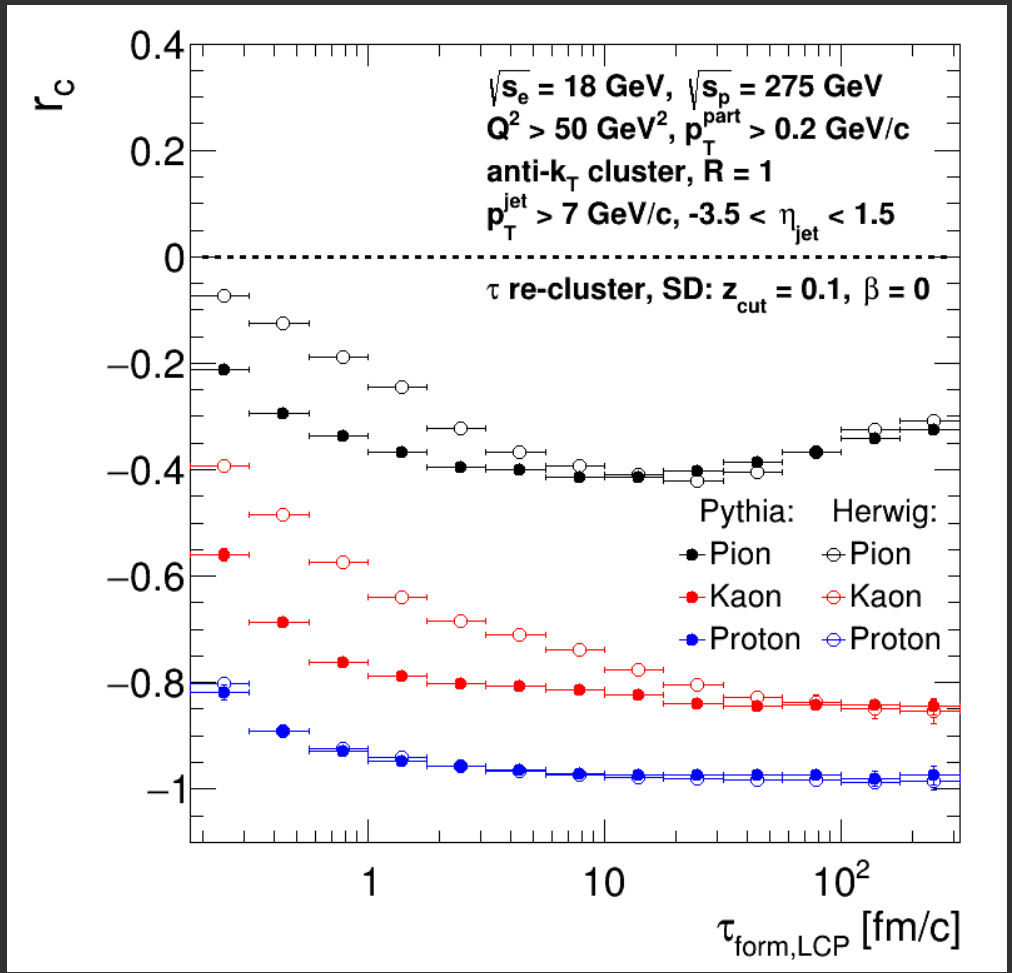
Charge Ratio with Selections



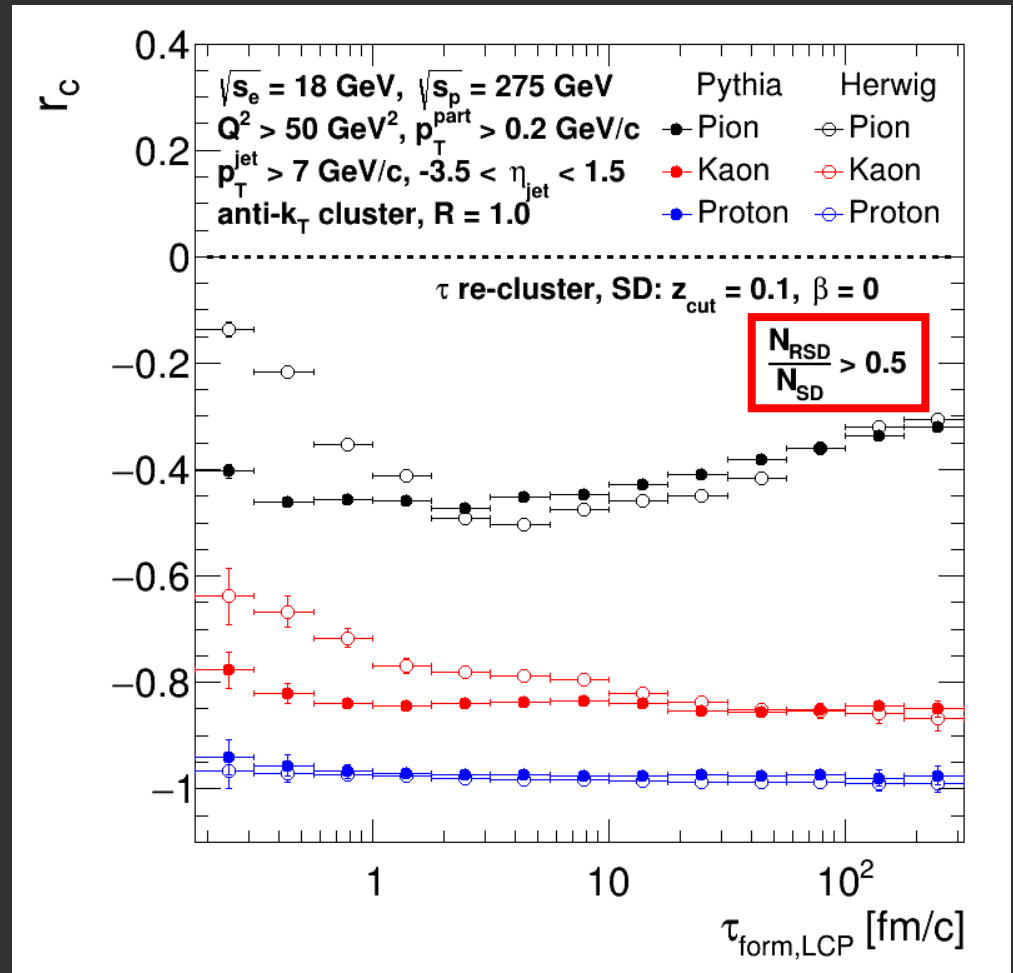
Inclusive Plot



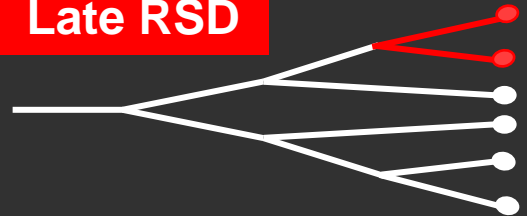
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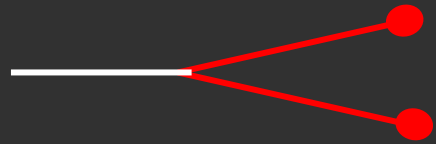


Late RSD



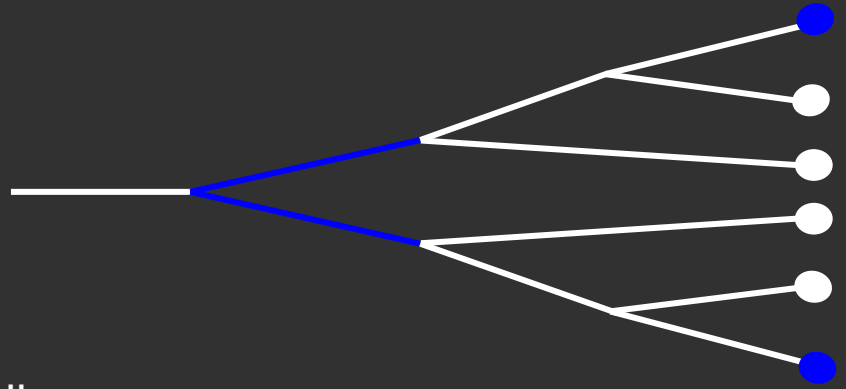
Charge Ratio with Selections

Example 1 of jet topology

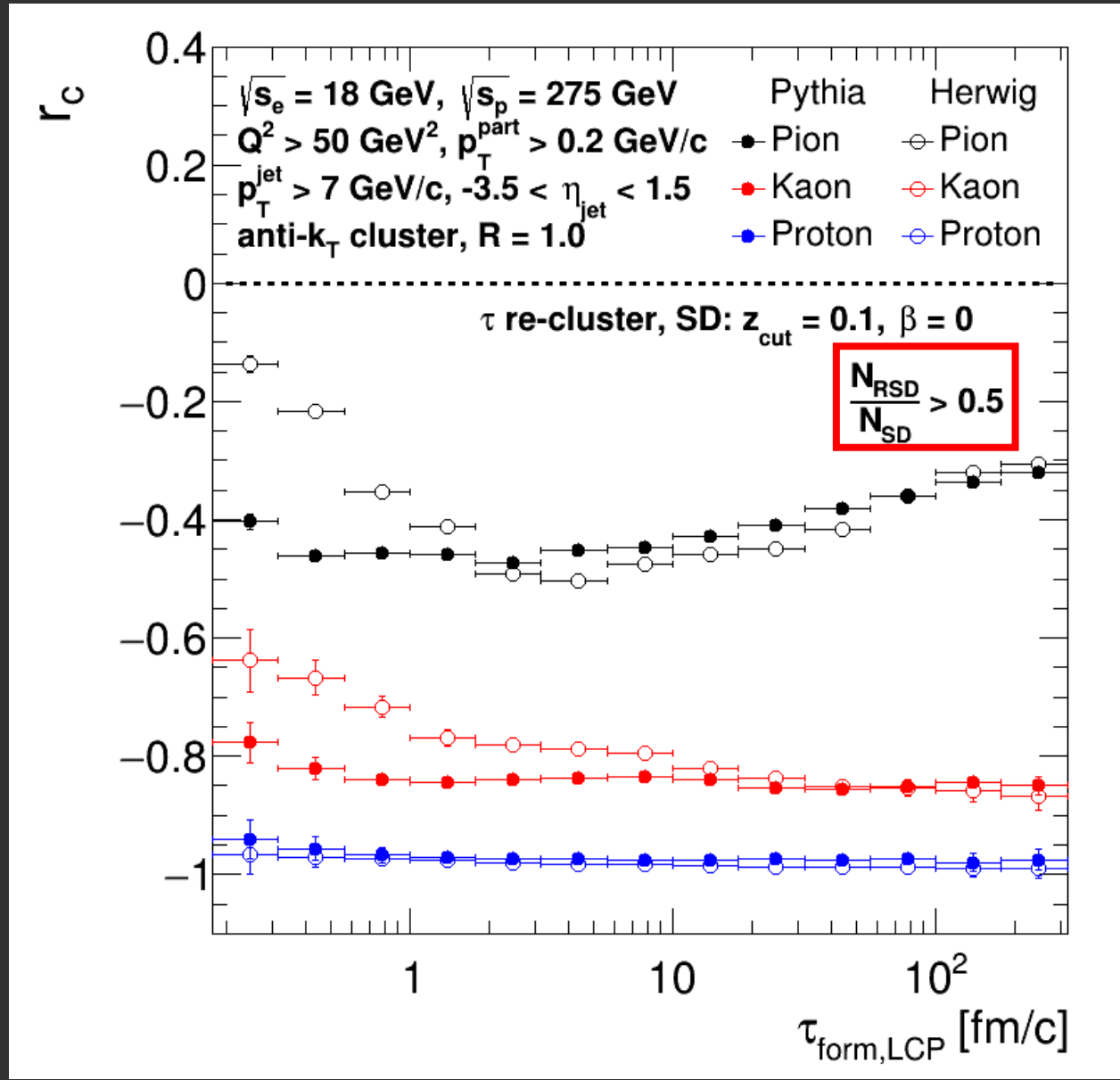


- Small $\tau_{form,LCP}$
- Large RSD depth

Example 2 of jet topology

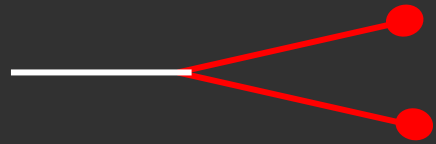


- Small $\tau_{form,LCP}$
- Small RSD depth



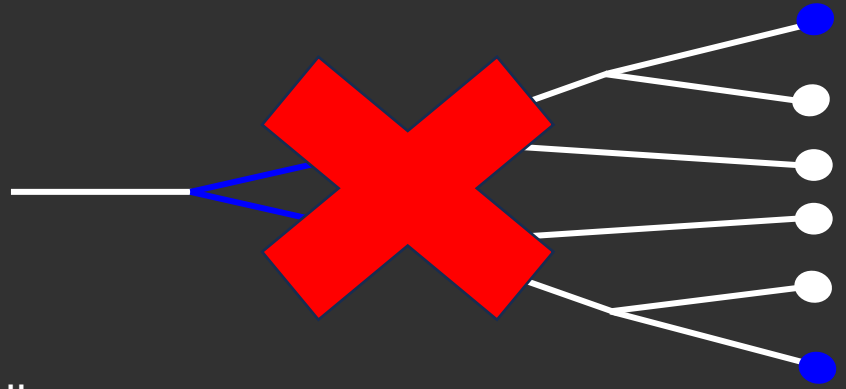
Charge Ratio with Selections

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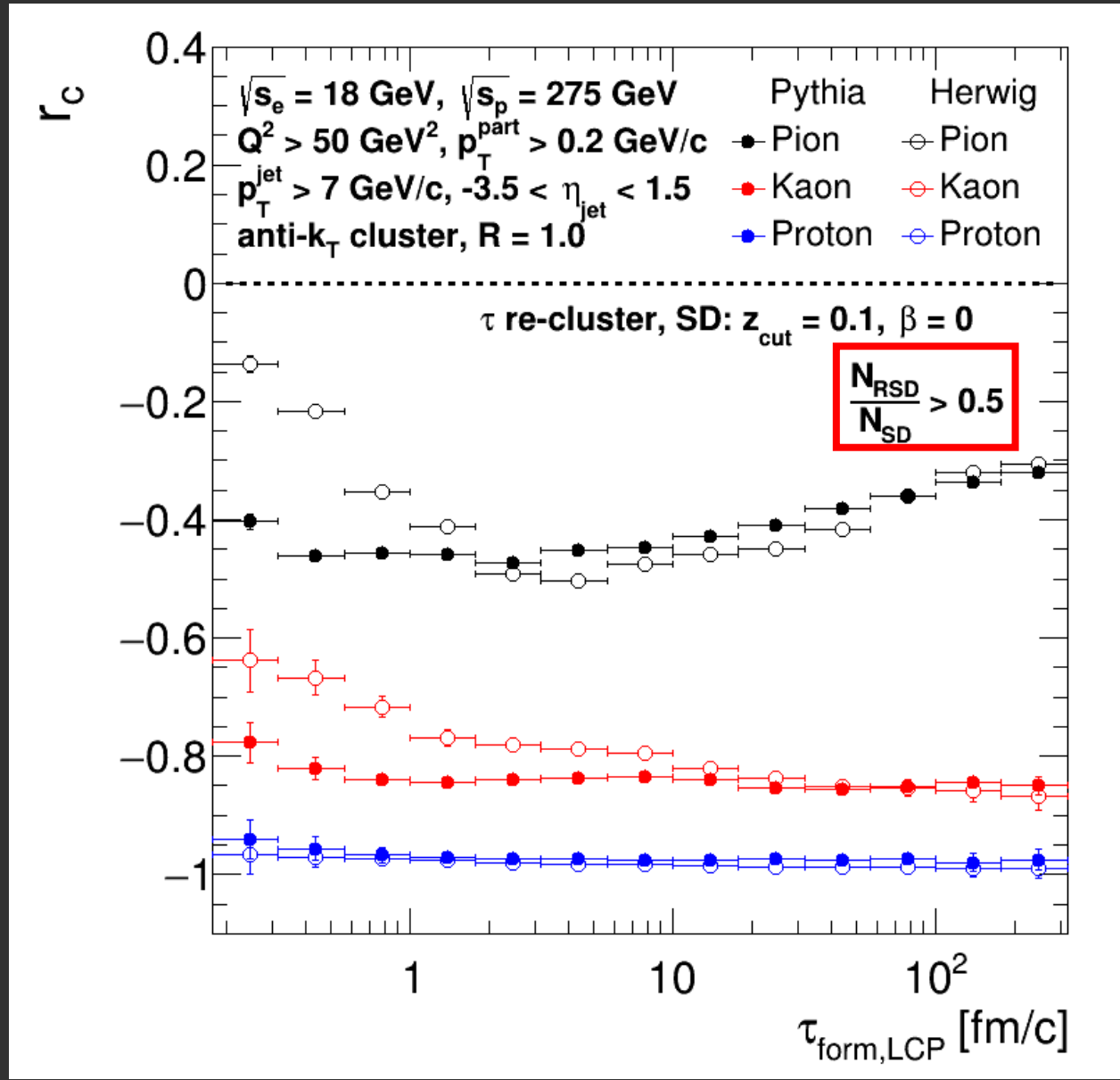


- Small $\tau_{form,LCP}$
- Large RSD depth

Example 2 of jet topology

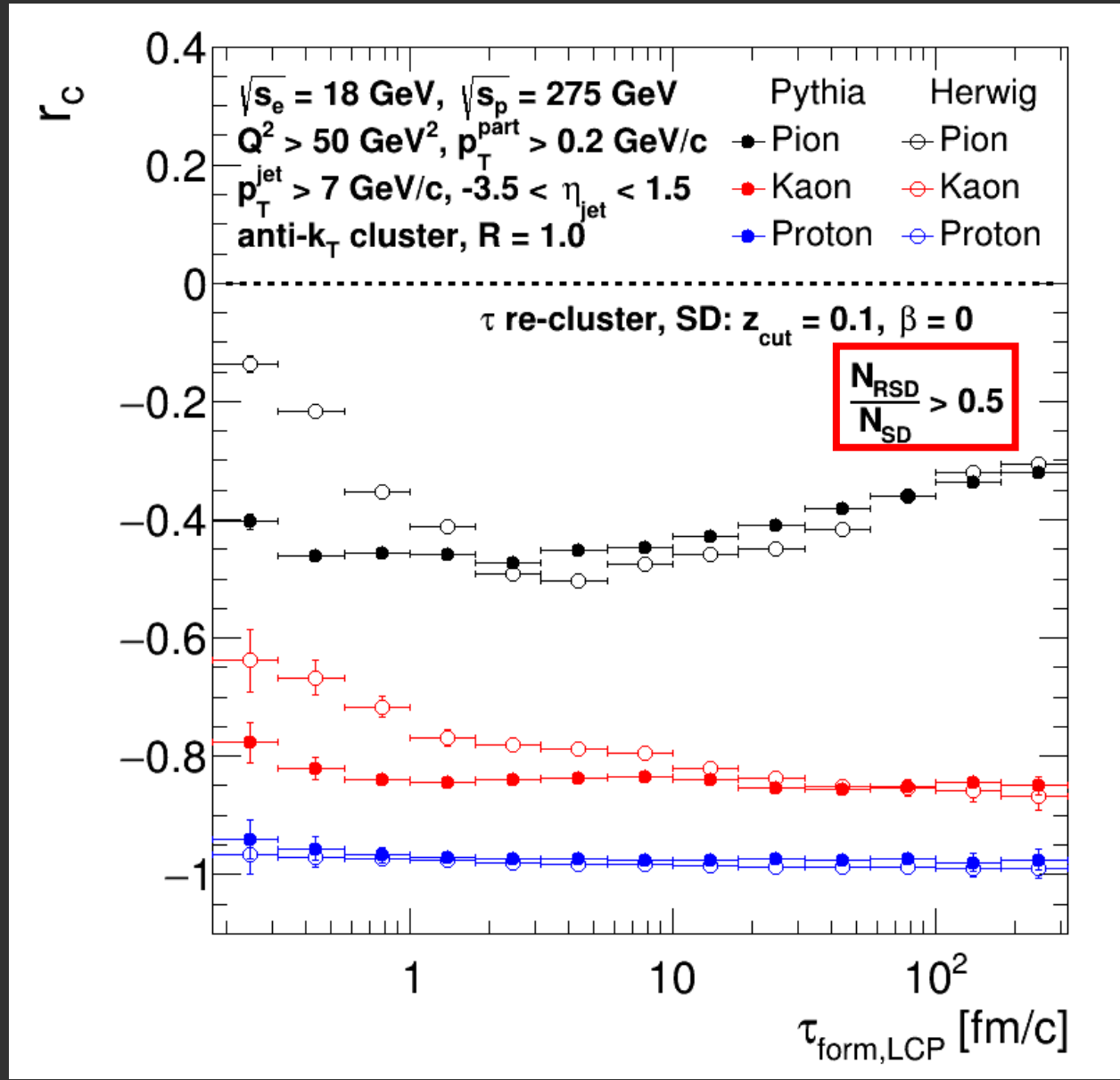


- Small $\tau_{form,LCP}$
- Small RSD depth



Conclusions

- RSD distinguishes different jet topologies, showing r_c is strongly dependent on substructure;
- Selection on late RSD reveals a qualitatively different behaviours of r_c from Pythia (Lund string) and Herwig (cluster fragmentation).



Thank you for your attention!

Questions?

Aknowledgements



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Backup Slides

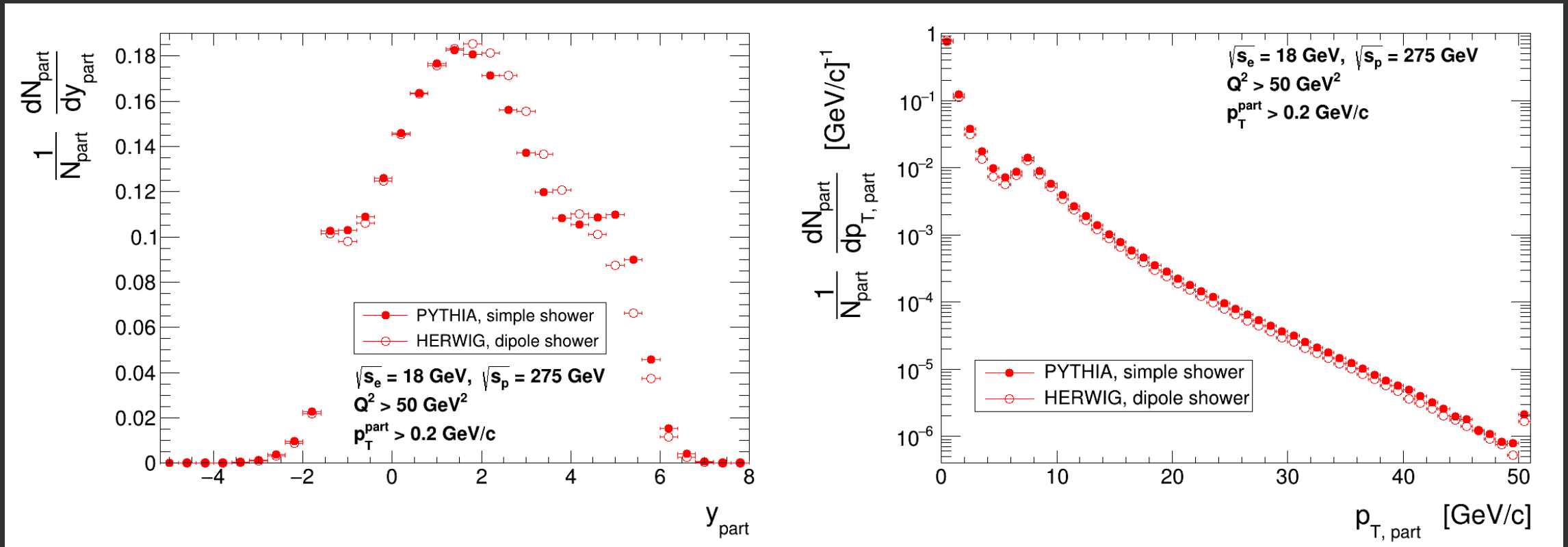


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Parton Description Matching

- PYTHIA's simple shower and HERWIG's dipole shower are the parton shower descriptions that allow for the best case scenario matching between event-level variables on both Monte Carlos, such as particle rapidity, transverse momentum and azimuthal angle.



Implementation

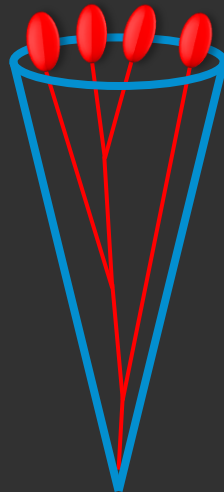
["Soft drop" (2014);
"Time reclustering for jet
quenching studies" (2021)]

- Jet analysis is performed with **FastJet**
- **Distance measure** used to cluster pairs of particles together:

$$d_{ij} = \min(p_{T1}^{2p}, p_{T2}^{2p}) \frac{\Delta R_{ij}^2}{R^2}$$

p_T – particle transverse momentum
 R – jet radius
 ΔR_{ij} – measure of the angular distance

- **Anti- k_t** algorithm:
 - Sensitive to hard objects
 - Unphysical clustering trees
- **C/A** algorithm: Angular-ordered trees
- τ algorithm: Reverse time-ordered trees



Parameter p defines the clustering algorithm

$p = -1$

$p = 0$

$p = 0.5$

⇓

⇓

⇓

Anti- k_t
algorithm

Cambridge/Aachen
(C/A) algorithm

τ
algorithm

⇓

⇓

⇓

Jet finding

Jet substructure studies

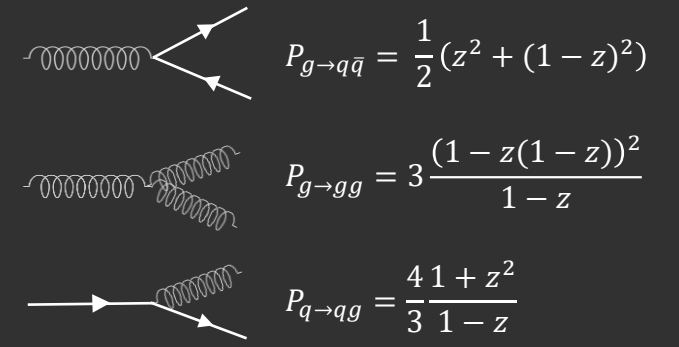
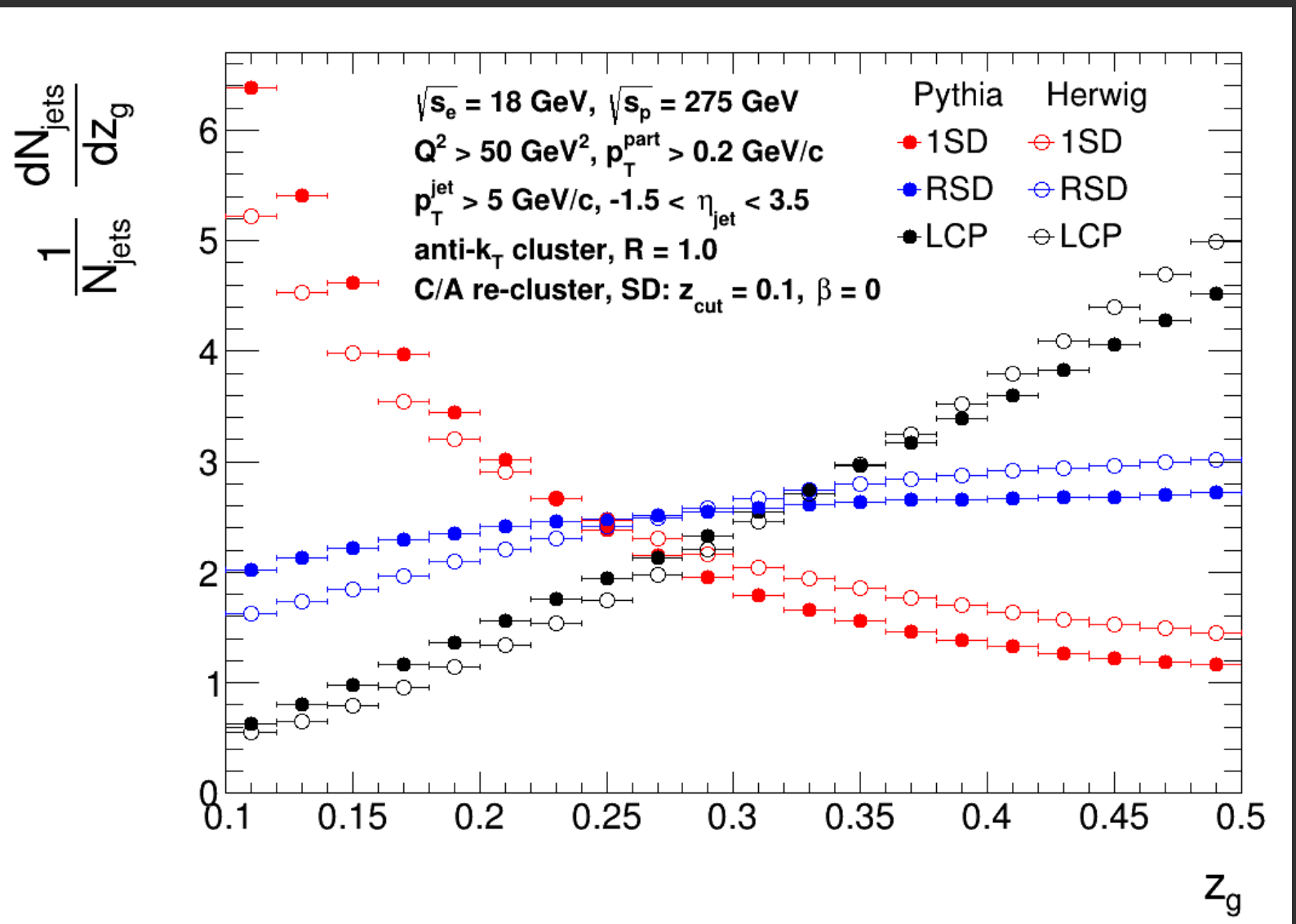
τ algorithm

$$d_{ij}^{p=0.5} = \min(p_{T1}, p_{T2}) \frac{\Delta R_{ij}^2}{R^2} \sim E z \theta^2 \approx \frac{1}{\tau_{form}}$$

in the high-energy, soft and collinear limits!

Results – Groomed Momentum Fraction

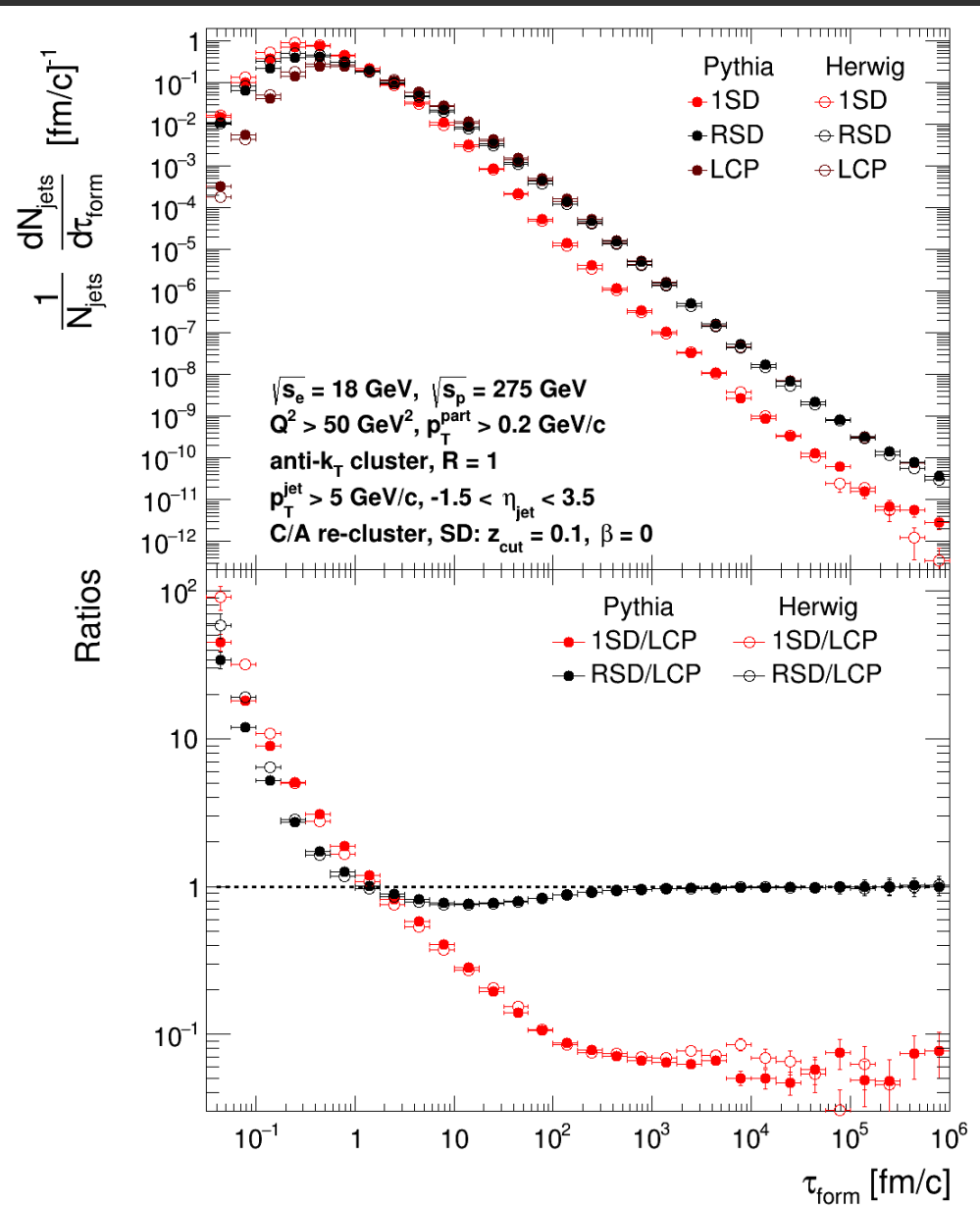
$$z_g = \frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}}$$



- **1SD** is highly **asymmetrical**; distributions extremely peaked for small z_g
- **LCP** is highly **symmetrical**; distributions extremely peaked for large z_g
- **RSD** is more symmetrical than 1SD and more asymmetrical than LCP; more to the likes of the LCP splitting

Results – Formation Time

$$\tau_{form} = \frac{1}{2 E z (1 - z) (1 - \cos \theta_{12})}$$

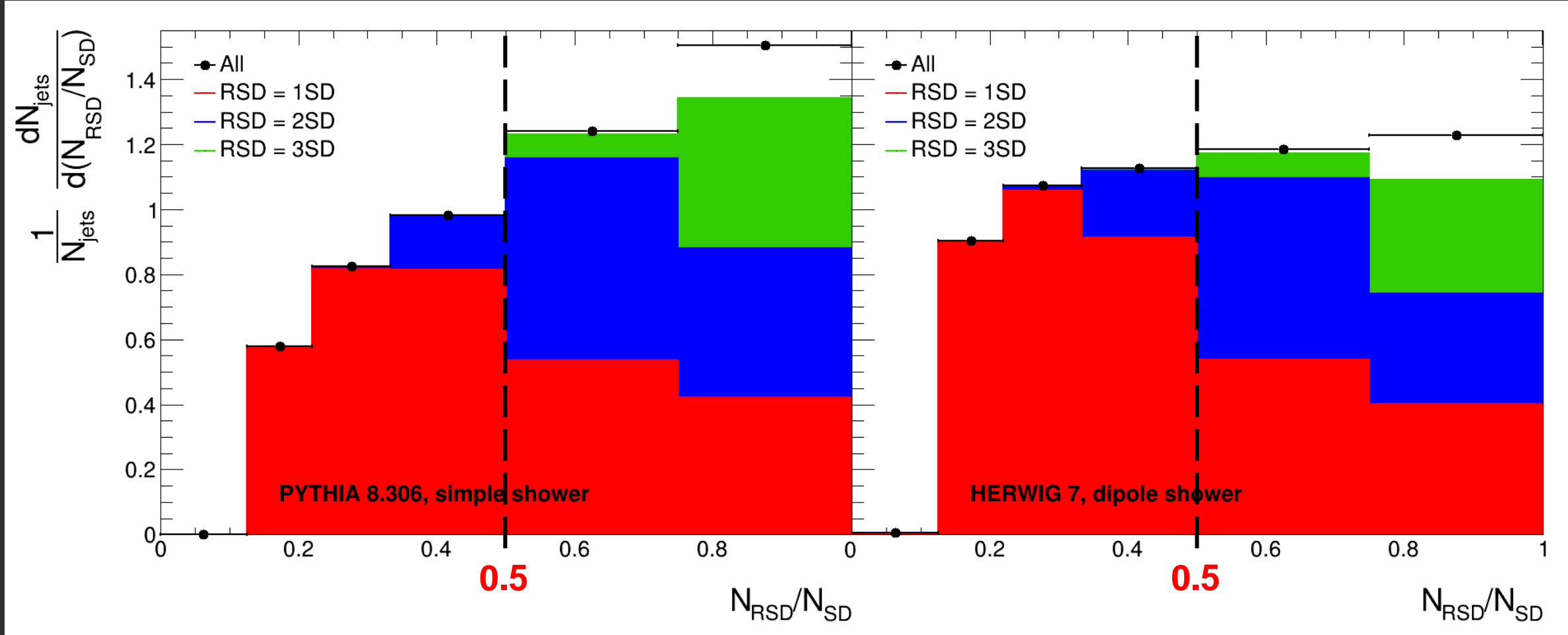


- 1SD tends to have smaller τ_{form}
- LCP tends to have larger τ_{form}
- RSD sits between the 1SD and the LCP
- $\tau_{form,1SD} \neq \tau_{form,LCP}$
- $\tau_{form,RSD} \approx \tau_{form,LCP}$

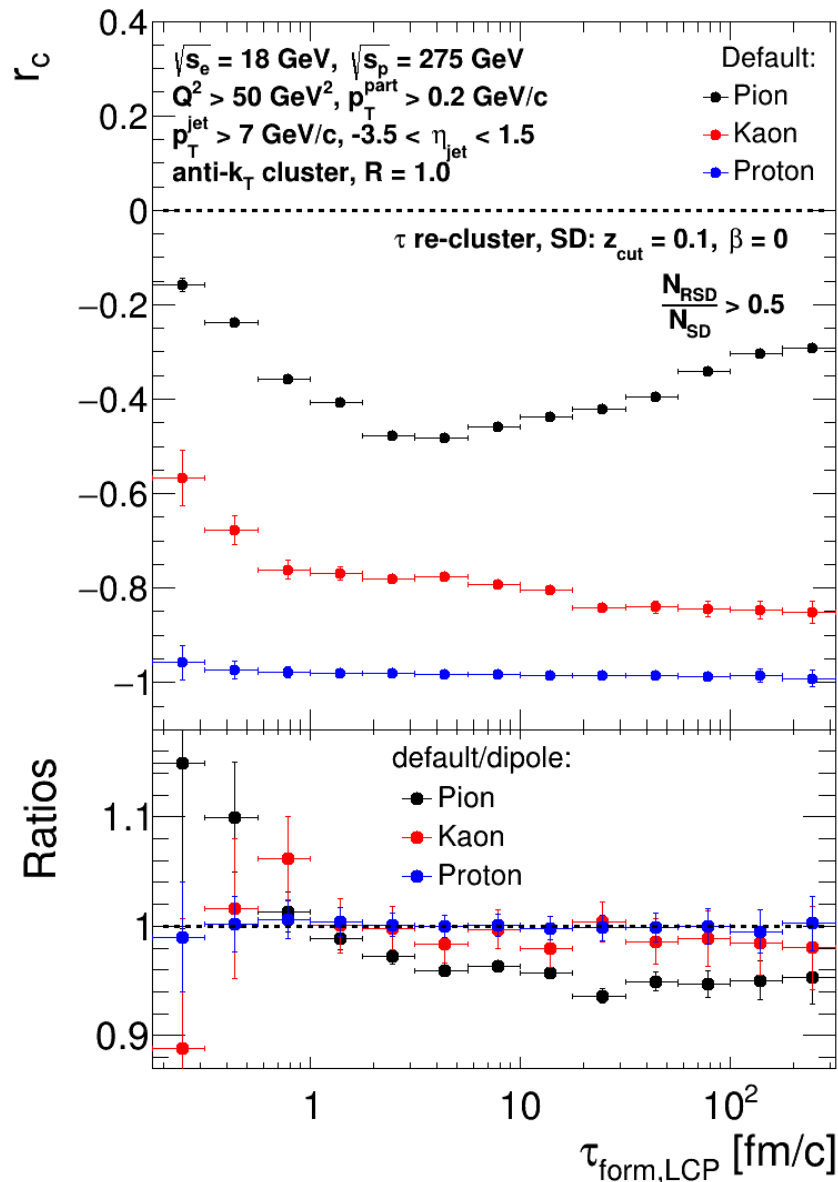
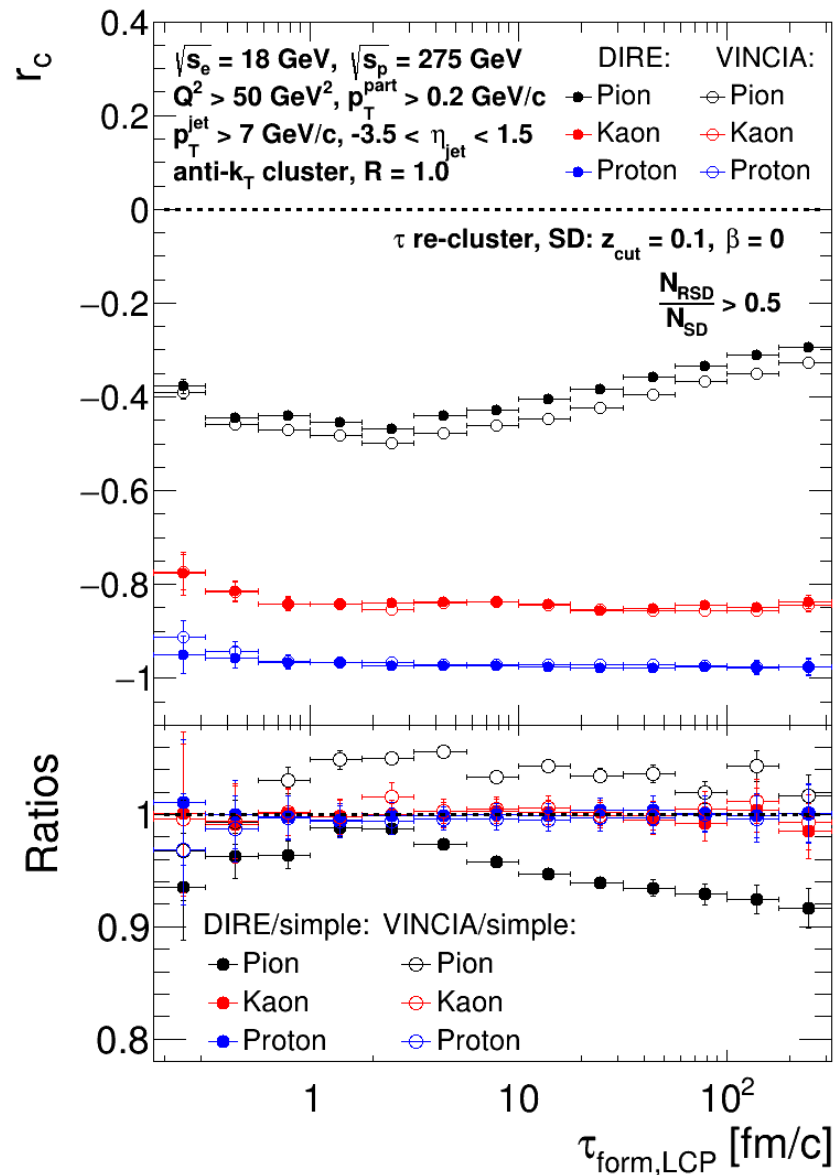
Conclusion: RSD splitting, an actual splitting from the clustering tree, is a good proxy for the LCP

RSD Depth

$$N_{RSD}/N_{SD}$$



Charge Ratio – Parton Shower Dependence



➤ The behaviour observed for these jet selections is robust against parton shower descriptions;

➤ Since the r_c is meant to be sensitive to hadronization physics, this is good news!