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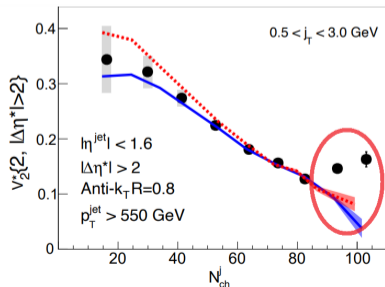
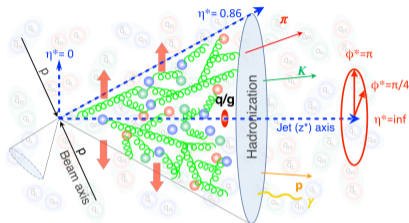
Unraveling the Final-State Interactions and Correlations Inside High-Multiplicity Jets at LHC

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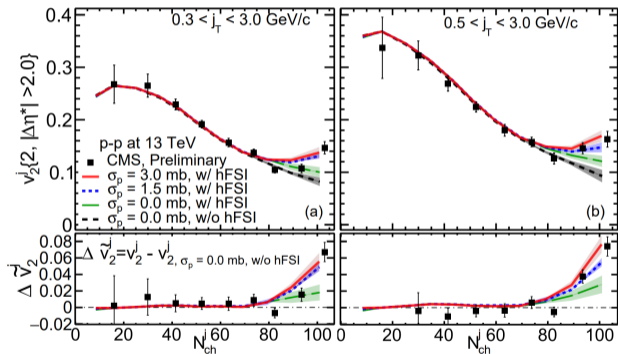
Non-Trivial Two-Particle Correlations in High-Multiplicity Jets



- A jet reference coordinate
- Redefine the constituents' momentum as: $\vec{p}^* = (j_T, \eta^*, \phi^*)$.
- For jets with $\langle N_{ch}^j \rangle \sim 100$, a **near-side enhancement** is observed, as seen in v_2 of two-particle correlations, which is absent in PYTHIA8 or SHERPA.

A. Hayrapetyan et al. [CMS], arXiv:2312.17103.

A Recent Work Suggests Importance of Final-State Interactions



- Final-state partonic and hadronic interactions
- Partonic rescatterings are crucial for reproducing such behavior, while hadronic rescatterings alone are insufficient.

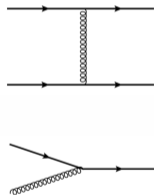
W. Zhao, Z. W. Lin and X. N. Wang, *arXiv:2401.13137*.

Our Work: Systematic Study of Various Sources of FS Correlations

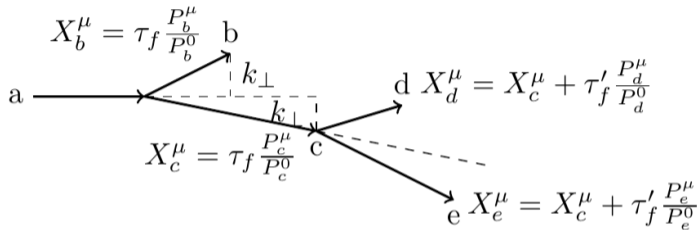
- ① Examine effects of parton shower components in PYTHIA:
 - Multiple Parton Interactions (MPI)
 - Initial-State Radiation (ISR)
 - Final-State Radiation (FSR)

After parton shower, we apply the following processes:

- ② Build a relatively consistent spacetime picture.
- ③ 2→2 partonic rescattering process
- ④ 2→1 partonic fusion process
- ⑤ Trace color flow and keep color neutral
- ⑥ Hadronic rescattering process



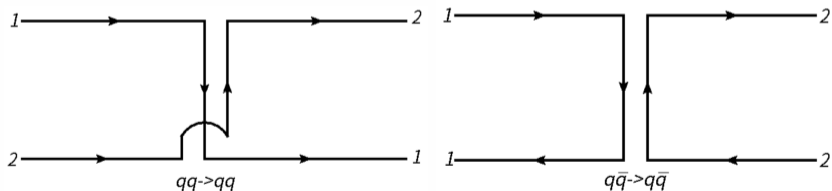
Build a Relatively Consistent Spacetime Picture



- A proper spacetime evolution is key to uncovering the correlations.
- For a $1 \rightarrow 2$ parton splitting, estimate the **formation time** $\tau_f = \frac{2E}{Q^2}$ based on the virtuality.
- Test the impact of parton's vertex of MPI:
 - 1 same as hard process
 - 2 finite \vec{x}_\perp displacement

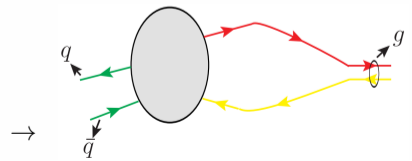
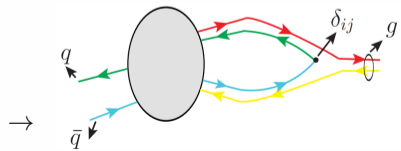
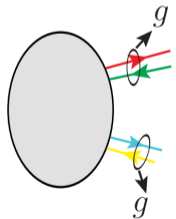
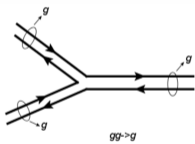
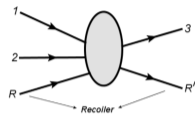
2→2 Partonic Rescattering Process

- Assume t -channel dominates: $\frac{d\sigma}{dt} \propto \frac{\alpha_s^2}{(t-\Lambda^2)^2}$.
- Apply a geometrical collision scheme: scattering occurs if $d_{ij} < \sqrt{\sigma/\pi}$.
- Exchange color in each collision in the large- N_c limit.



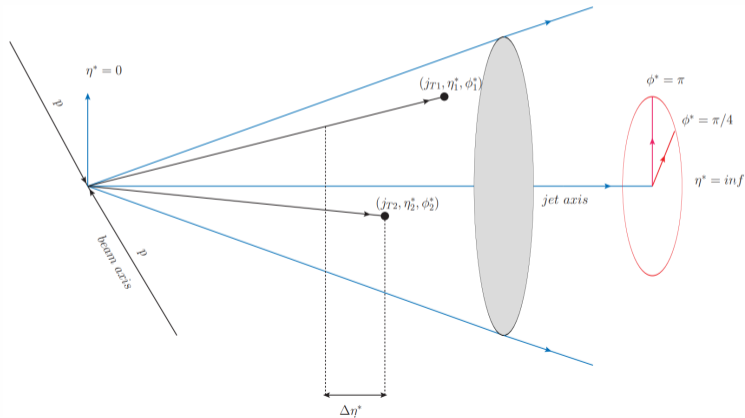
2→1 Partonic Fusion Process

- Keep momentum conservation.
- Fusion happens if $(P_1 + P_2)^2 < m_{\text{fusion}}^2$ and $d_{ij} < d_{\text{fusion}}$.
- Trace color flow to ensure neutrality.



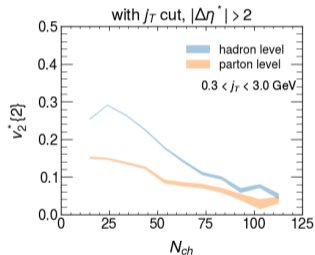
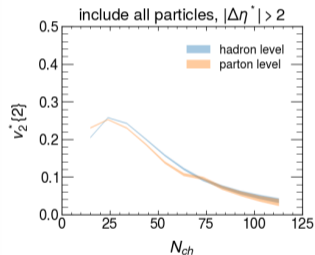
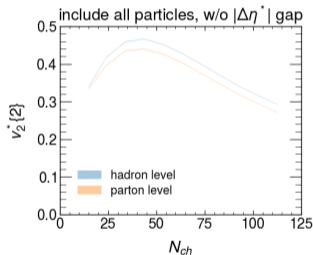
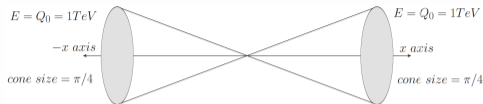
Hadronization, Hadronic Rescattering and v_2

- PYTHIA8 assigns spacetime production vertices to all primary hadrons from string breakups and includes a hadronic rescattering framework as well.
- Calculate v_2 in ϕ^* with the Q-cumulant method include a $|\Delta\eta^*|$ gap.



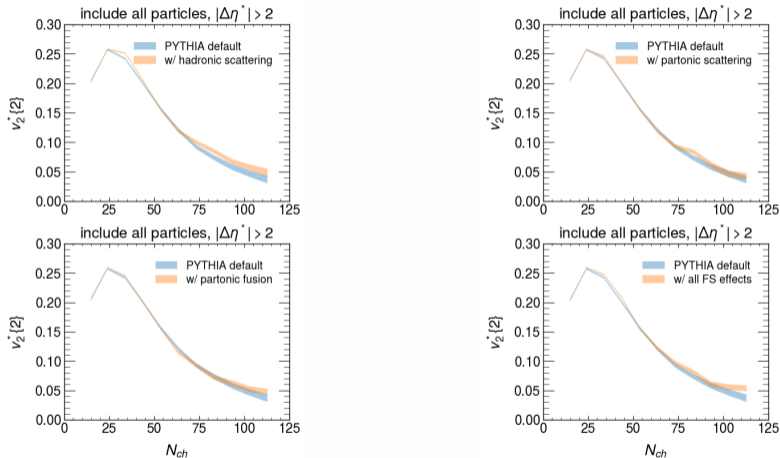
- ① α_s (0.35)
- ② Λ (0.5GeV)
- ③ m_{fusion} (0.5GeV)
- ④ d_{fusion} (0.5fm)

Case 1: A $q\bar{q}$ -initiated Shower, No Underlying Event



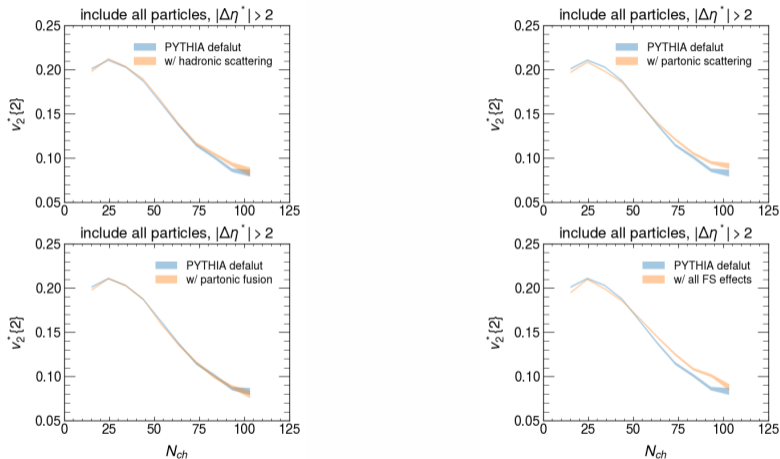
- Hadronization mainly contributes to short-range correlations and has a slight impact on long-range correlations.
- v_2 at partonic and hadronic levels are similar for long-range correlation but changes with j_T cuts due to different j_T distributions.

Case 1: A $q\bar{q}$ -initiated Shower, No Underlying Event



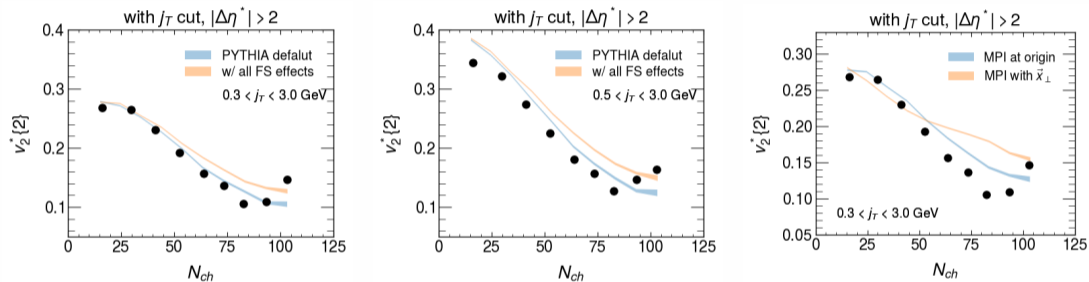
- Hadronic rescattering increase v_2 at high-multiplicity, and partonic interactions have a smaller but still notable influence.

Case 2: Jets in p-p Collision With Underlying Event



- Partonic rescattering appears to have a larger effect than hadronic rescattering, while the impact of partonic fusion is negligible in this complex environment.

Case 2: Jets in p-p Collision With Underlying Event



- Including all final-state interactions increases v_2 , but the very strong enhancement of v_2 at high multiplicity observed in CMS data is still not reproduced.
- Introducing a finite transverse displacement in MPI coordinates sharply increases v_2 at high multiplicity due to more collisions at partonic level.

Summary

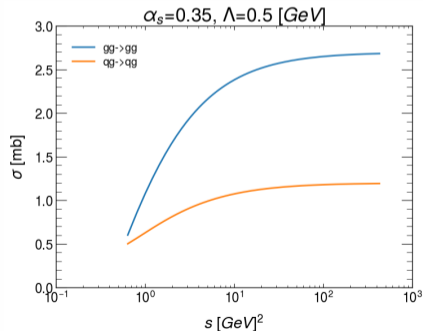
- Spacetime is important for studying correlations inside high-multiplicity jets.
- Partonic rescattering, partonic fusion, and hadronic rescattering all contribute to correlations in high-multiplicity jets, but their relative importance varies based on the underlying event.
- The strength of the correlations changes depending on the j_T of the particles.
- The current setup does not exhibit the v_2 enhancement seen at high multiplicity, as shown in CMS data. We aim to advance our study with a focus on:
 - To Refine the spacetime picture
 - To increase the strength of scattering
 - To optimize fusion strategies to enhance fusion probability

Back Up

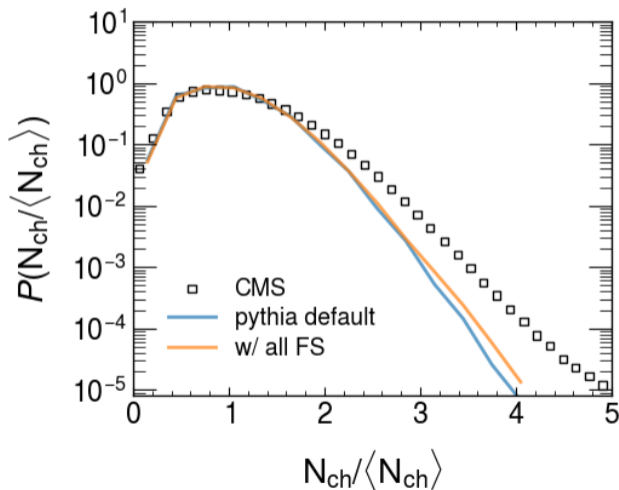
Model Parameters

The key model parameters are:

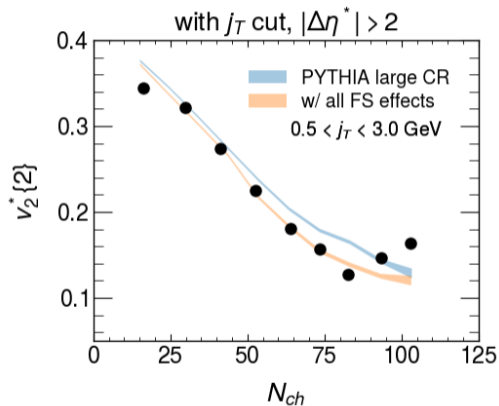
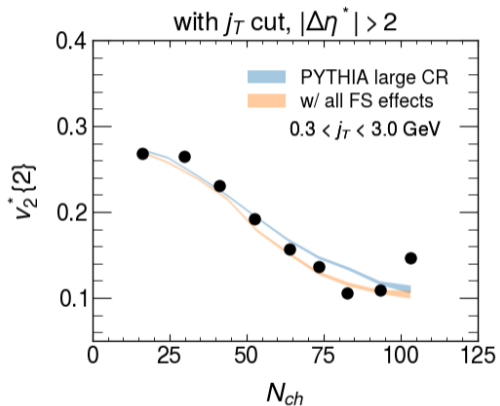
- ① α_s (0.35): strong coupling constant for the collision process
- ② Λ (0.5GeV): regularization scale for the differential cross section
- ③ m_{fusion} (0.5GeV): invariant mass boundary for fusion pairs
- ④ d_{fusion} (0.5fm): distance threshold for fusion to occur



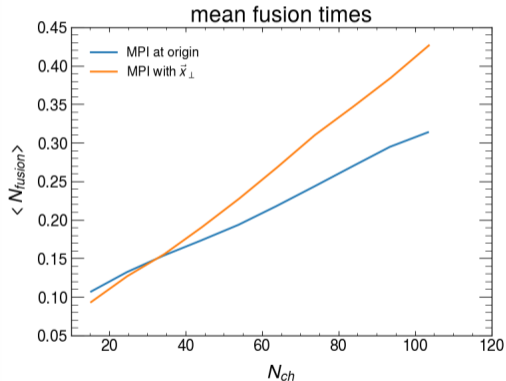
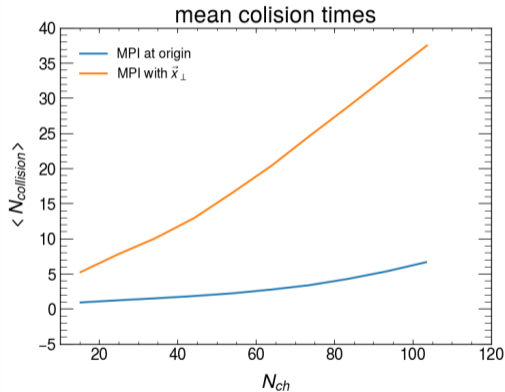
Multiplicity distribution



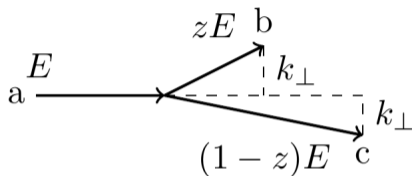
PYTHIA MPI-based Color Reconnection & Larger range



Mean Collision or Fusion Times



Formation Time



- For FSR, "a" get the virtuality:

$$Q^2 = \frac{k_T^2}{z(1-z)E}, \quad \tau_f = \frac{2E}{Q^2} = \frac{2z(1-z)E}{k_T^2}$$

- For ISR, "b" get the virtuality:

$$Q^2 = \frac{k_T^2}{(1-z)E}, \quad \tau_f = \frac{2zE}{Q^2} = \frac{2z(1-z)E}{k_T^2}$$

Large N_c Limit

- In this picture, the Fierz identity:

$$(T_{ij}^a)(T_{kl}^b) = \frac{1}{2}(\delta_{il}\delta_{kj} - \frac{1}{N_c}\delta_{ij}\delta_{kl})$$

will be considered as:

$$(T_{ij}^a)(T_{kl}^b) = \frac{1}{2}\delta_{il}\delta_{kj}$$

- The 3-gluon vertex:

$$gf^{abc}T_{ij}^a T_{kl}^b T_{mn}^c$$

will be considered as:

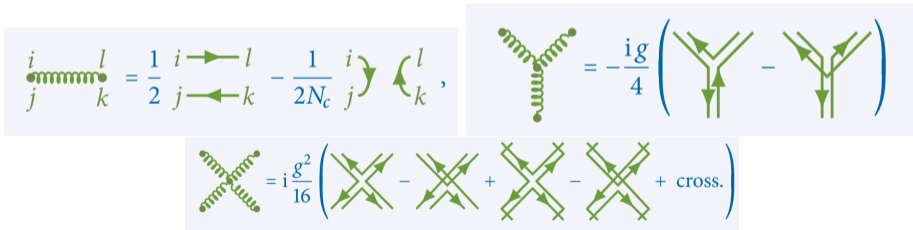
$$gf^{abc}T_{ij}^a T_{kl}^b T_{mn}^c = -\frac{i}{4}g(\delta_{il}\delta_{jm}\delta_{nk} - \delta_{in}\delta_{jk}\delta_{lm})$$

Large N_c Limit

- The 4-gluon vertex will be:

$$-ig^2 f^{abx} f^{xcd} T_{ij}^a T_{kl}^b T_{mn}^c T_{op}^d = i \frac{g^2}{16} (\delta_{il} \delta_{jo} \delta_{kn} \delta_{mp} - \delta_{in} \delta_{jk} \delta_{lo} \delta_{mp} - \delta_{il} \delta_{jm} \delta_{kp} \delta_{on} + \delta_{ip} \delta_{jk} \delta_{lm} \delta_{on})$$

- Show with image



The image shows the decomposition of the 4-gluon vertex into two parts. The first part is a box containing the equation:

$$i \begin{array}{c} i \\ \text{gluon} \\ j \end{array} \begin{array}{c} l \\ \text{gluon} \\ k \end{array} = \frac{1}{2} \begin{array}{c} i \rightarrow l \\ j \leftarrow k \end{array} - \frac{1}{2N_c} \begin{array}{c} i \rightarrow \\ j \rightarrow \end{array} \begin{array}{c} \leftarrow l \\ \leftarrow k \end{array},$$

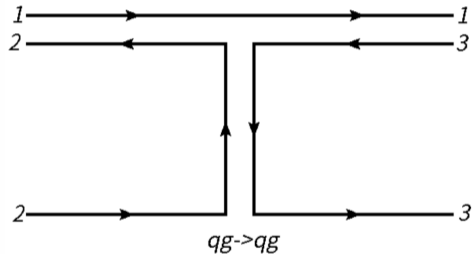
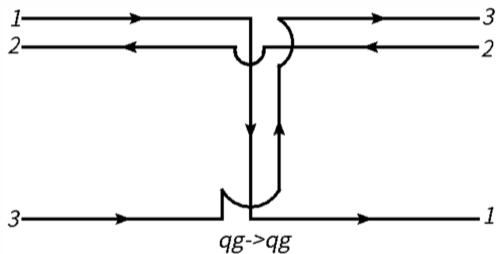
The second part is a box containing the equation:

$$\begin{array}{c} \text{gluon} \\ \text{gluon} \\ \text{gluon} \\ \text{gluon} \end{array} = -\frac{ig}{4} \left(\begin{array}{c} \text{Y} \\ \text{Y} \end{array} - \begin{array}{c} \text{Y} \\ \text{Y} \end{array} \right)$$

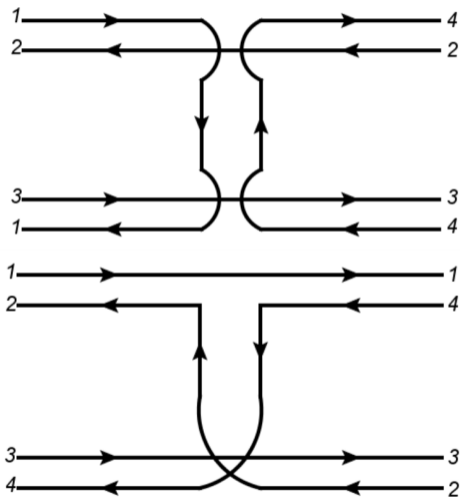
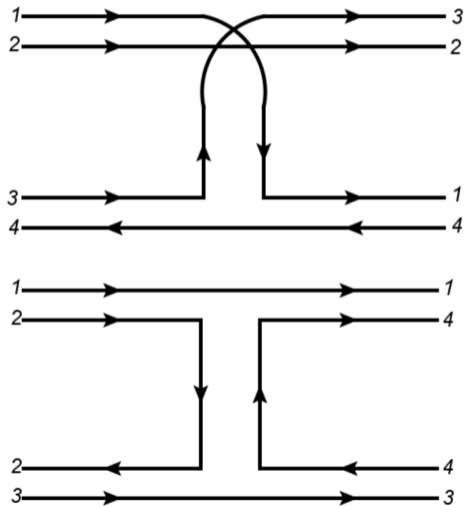
The third part is a box containing the equation:

$$\begin{array}{c} \text{gluon} \\ \text{gluon} \\ \text{gluon} \\ \text{gluon} \end{array} = i \frac{g^2}{16} \left(\begin{array}{c} \text{X} \\ \text{X} \\ \text{X} \\ \text{X} \end{array} - \begin{array}{c} \text{X} \\ \text{X} \\ \text{X} \\ \text{X} \end{array} + \begin{array}{c} \text{X} \\ \text{X} \\ \text{X} \\ \text{X} \end{array} - \begin{array}{c} \text{X} \\ \text{X} \\ \text{X} \\ \text{X} \end{array} + \text{cross.} \right)$$

Color Information for $qg \rightarrow qg$ Scattering



Color Information for $gg \rightarrow gg$ Scattering



Color Information for Fusion

