



# Jets: Hard-Soft Correlation

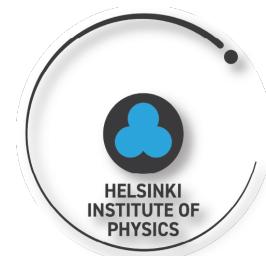
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Ismail Soudi

University of Jyväskylä  
Helsinki Institute of Physics



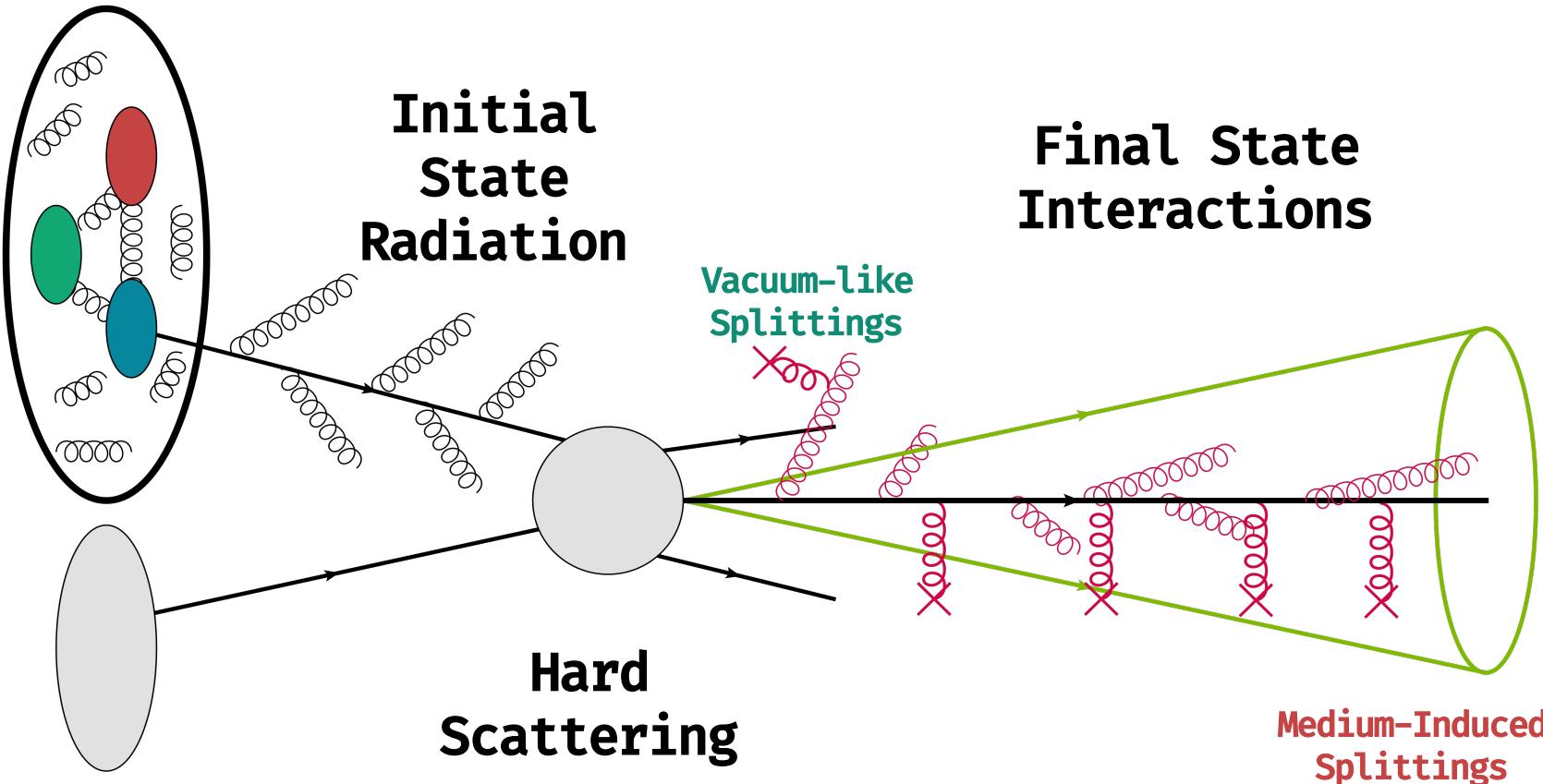
UNIVERSITY OF JYVÄSKYLÄ



CoE QM

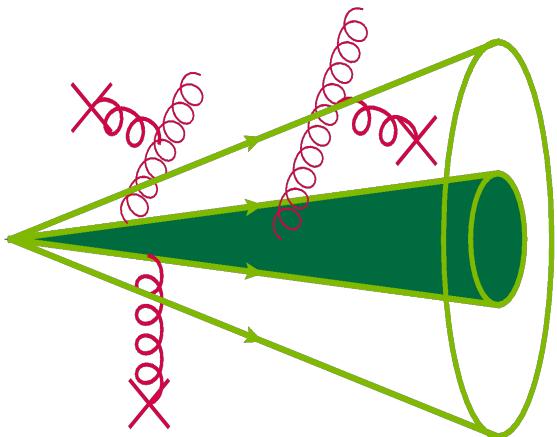


# Hard-Soft Correlations



# Vacuum-Like Physics

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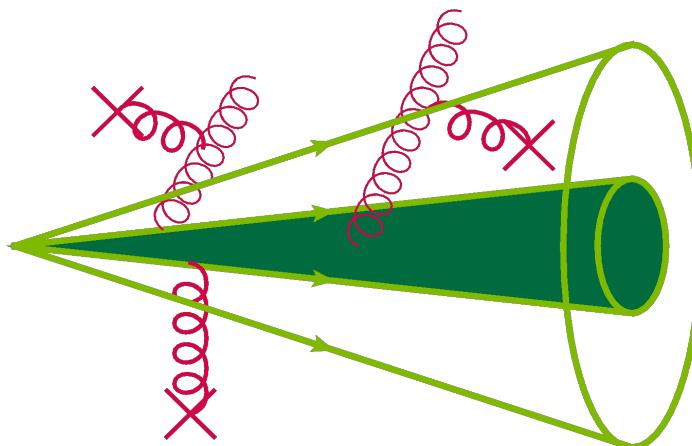
- Initial Coherent Scatterings
  - » Factorization: Coherent Radiation Not Resolved By QGP [Caucal, Iancu, Mueller, Soyez PRL(2018)]
  - » Delayed Energy Loss ( $\tau=0.6 \text{ fm}/c$ ) [Andres, Armesto, Niemi, Paatelainen, Salgado PLB(2020)]
  - » Modified Vacuum Shower [Kumar, Majumder, Shen(2020)]
  - » Coherent Energy Loss  $\Rightarrow$  Jet  $v_2$  and  $R_{AA}$  [Mehtar-Tani, Pablos, Tywoniuk PRD(2024)]
  - » ...

See also: A. Takacs Mon 15:00

# Decoherence

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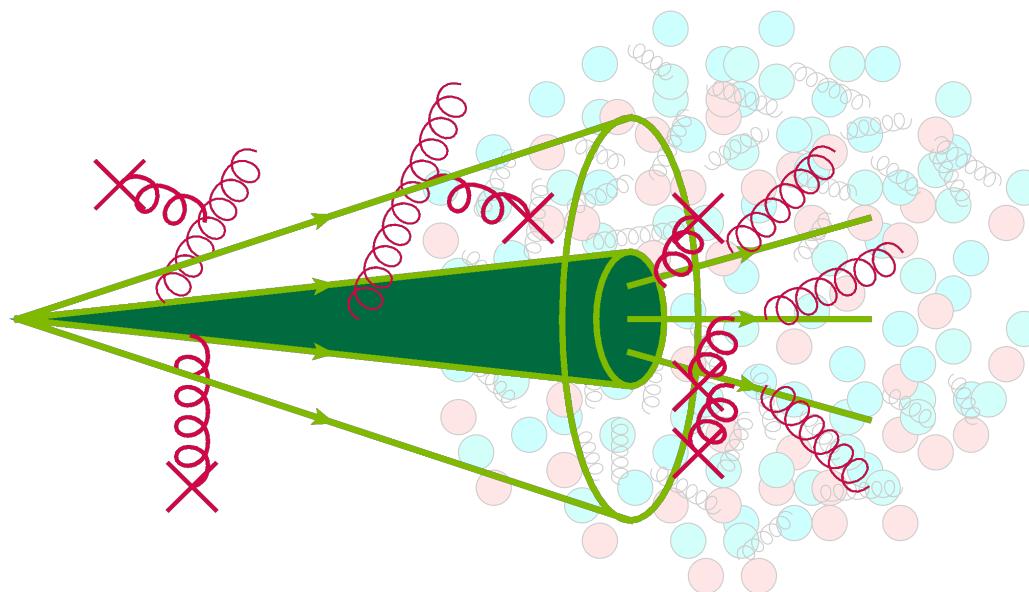
- Individual Antennas Resolved By QGP



# Decoherence

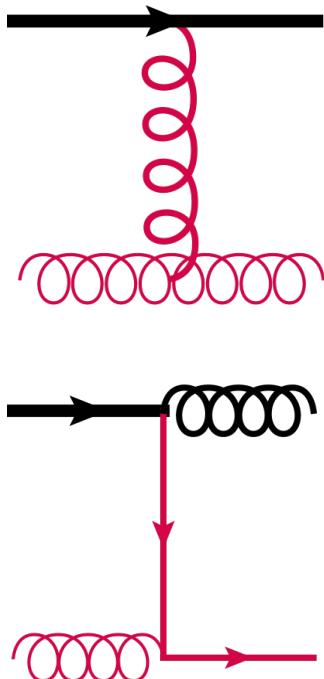
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- Individual Antennas Resolved By QGP



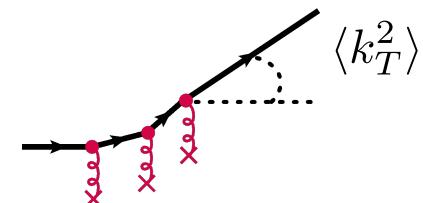
# Jet-Medium Scattering

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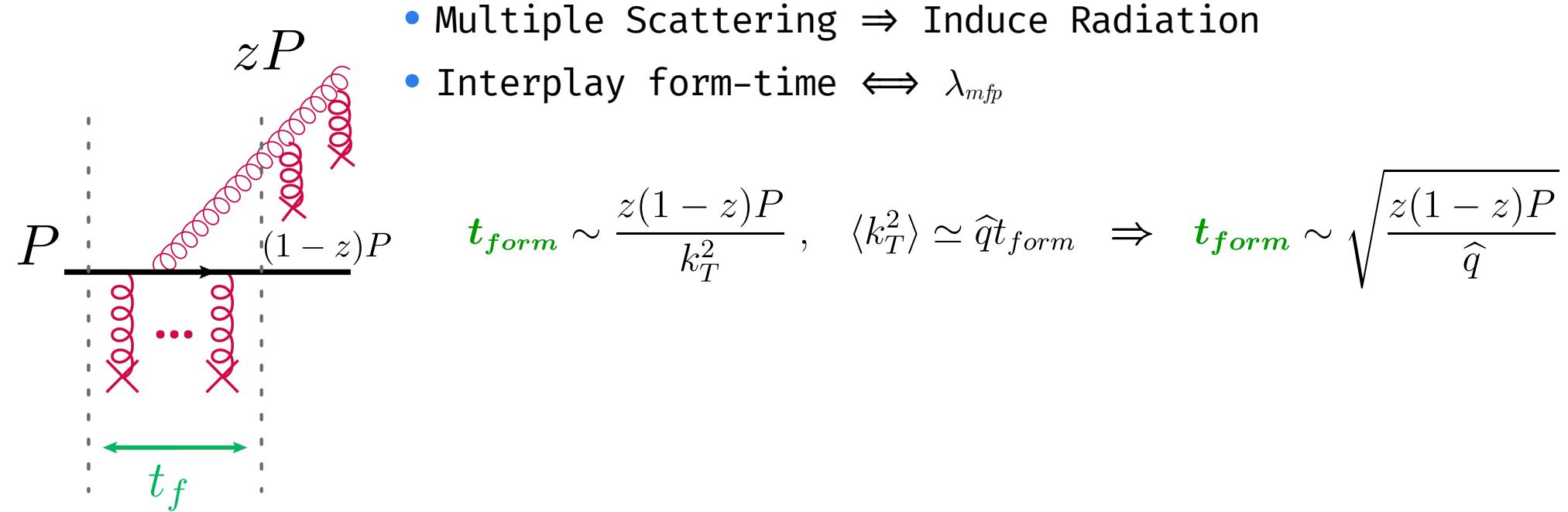


- Multiple Scattering:

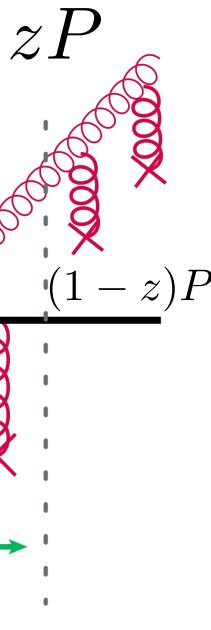
- » Momentum Broadening
  - » Drag
  - » Conversion
- $\left. \right\} \propto \hat{q} = \frac{\langle k_T^2 \rangle}{L}$



# Medium-Induced Radiation



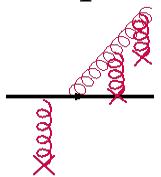
# Medium-Induced Radiation



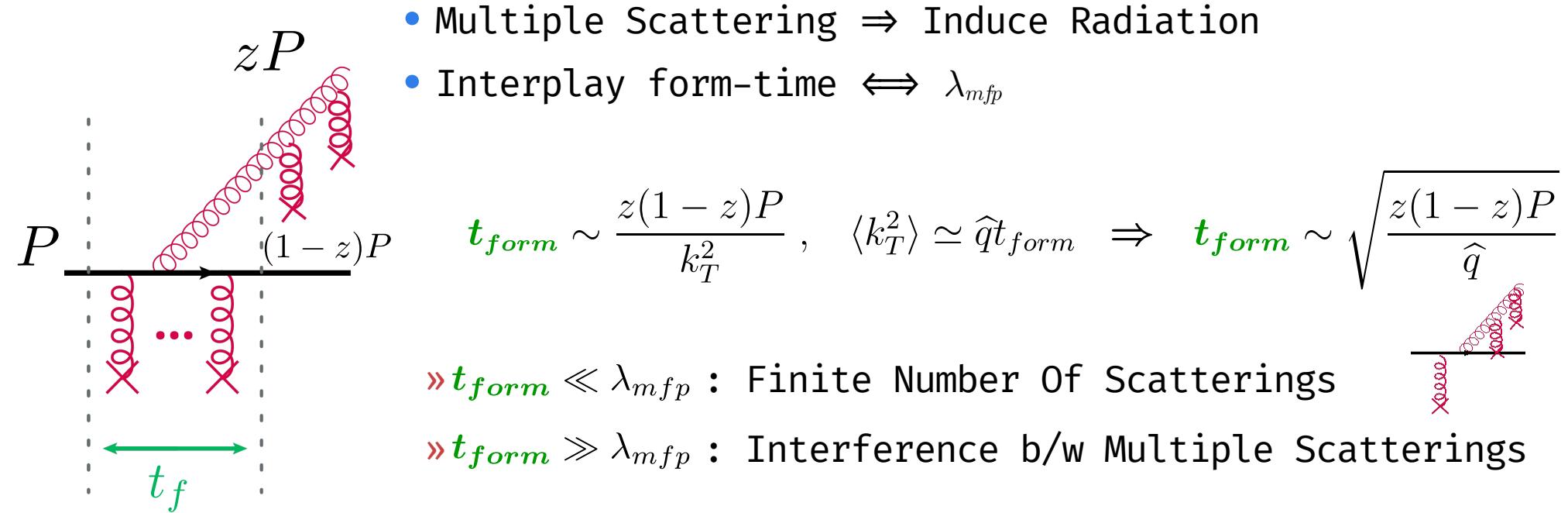
- Multiple Scattering  $\Rightarrow$  Induce Radiation
- Interplay form-time  $\Leftrightarrow \lambda_{mfp}$

$$t_{\text{form}} \sim \frac{z(1-z)P}{k_T^2}, \quad \langle k_T^2 \rangle \simeq \hat{q} t_{\text{form}} \quad \Rightarrow \quad t_{\text{form}} \sim \sqrt{\frac{z(1-z)P}{\hat{q}}}$$

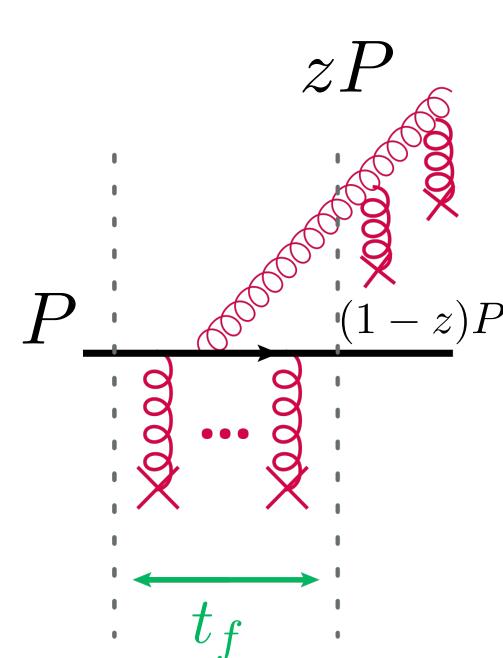
»  $t_{\text{form}} \ll \lambda_{mfp}$  : Finite Number Of Scatterings



# Medium-Induced Radiation



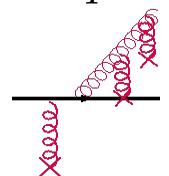
# Medium-Induced Radiation



- Multiple Scattering  $\Rightarrow$  Induce Radiation
- Interplay form-time  $\Leftrightarrow \lambda_{mfp}$

$$t_{\text{form}} \sim \frac{z(1-z)P}{k_T^2}, \quad \langle k_T^2 \rangle \simeq \hat{q} t_{\text{form}} \Rightarrow t_{\text{form}} \sim \sqrt{\frac{z(1-z)P}{\hat{q}}}$$

»  $t_{\text{form}} \ll \lambda_{mfp}$  : Finite Number Of Scatterings



»  $t_{\text{form}} \gg \lambda_{mfp}$  : Interference b/w Multiple Scatterings

- Interference Effects  $\Rightarrow$  LPM Suppression for  $zP \gg T$

# Medium-Induced Radiation

» BDMPS-Z Formalism: Resum Multiple-Scattering diagram

The diagram illustrates the BDMPS-Z formalism. A black line with a green circular source emits red wavy lines representing radiation. The rate of emission is given by the derivative of the total cross-section with respect to the energy transfer  $z$ , which is also the spectrum of the emitted radiation.

$$\underbrace{\frac{d\Gamma_{bc}^a}{dz}(P, z, t)}_{\text{Rate}} = \underbrace{\frac{d}{dt} \frac{dI_{bc}^a}{dz}(P, z, t)}_{\text{Spectrum}} = \frac{g^2 P_{bc}^a(z)}{4\pi P^2 z^2 (1-z)^2} \text{Re} \int_0^t dt_1 \int_{\mathbf{p}, \mathbf{q}} \frac{i\mathbf{q} \cdot \mathbf{p}}{\delta E(\mathbf{q})} \underbrace{\Gamma_3(t)}_{\text{Medium}} \circ G(t, \mathbf{q}; t_1, \mathbf{p}).$$

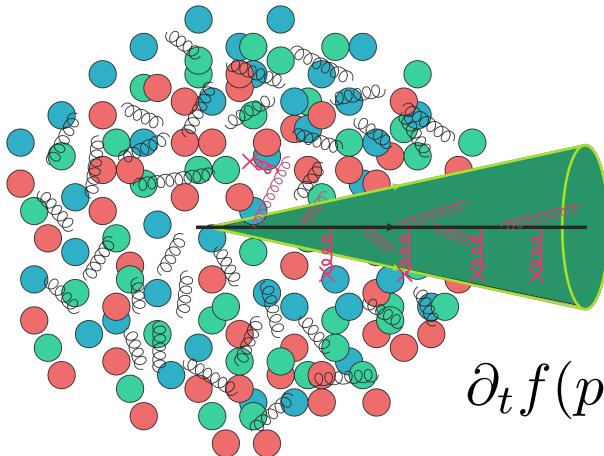
Below, several specific forms for the medium-induced rate  $\Gamma(t)$  are listed:

- $\Gamma(t) \propto \frac{1}{q^2(q^2 + m_D^2)}$  » HTL Potential
- $\Gamma(t) \propto \frac{1}{(q^2 + m_D^2)^2}$  » Static Screening
- $\Gamma(t) \propto \hat{q} b^2$  » Harmonic Oscillator (HO)
- $\Gamma(t) \propto C_{NP-QCD}(q)$  » Non-perturbative [Moore, Schlusser, Schlichting IS JHEP(2020)]
- $\Gamma(t) \propto C_{Non-Eq}(q)$  » Non-Eq Extracted

A plot shows the distribution  $\hat{q}(t) = \int d^2 k_T k_T^2 \Gamma(t)$  as a function of  $k_T^2$ . The distribution is shown to rise with  $k_T^2$ , with a dashed line indicating a power-law behavior.

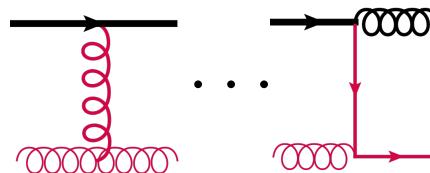
S. Shi Mon. 15:40      F. Lindenbauer Mon 17:30

# Effective Kinetic Theory



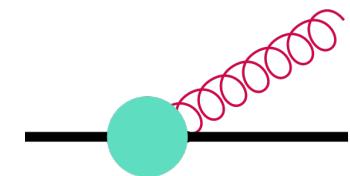
$$\partial_t f(p) =$$

» Elastic Scattering



$$C^{2 \leftrightarrow 2}[f]$$

» Effective  $1 \leftrightarrow 2$  Rate



$$C^{1 \leftrightarrow 2}[f]$$

Static/Evolving

$$f(p) = f^{QGP}(p) + \delta f^{jet}(p)$$

Includes Medium Recoil/Response

$$\delta f^{jet}(p) = f(p) - f^{QGP}(p) \leq 0$$

Energy Distribution

$$D(x) = \delta(xE_0 - p)p^3 \delta f^{jet}(p)$$

# AMY Kinetic Theory

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» Integrate Out Time-Dependence  $t_{form} \sim \sqrt{\frac{z(1-z)P}{\hat{q}}} \ll L$

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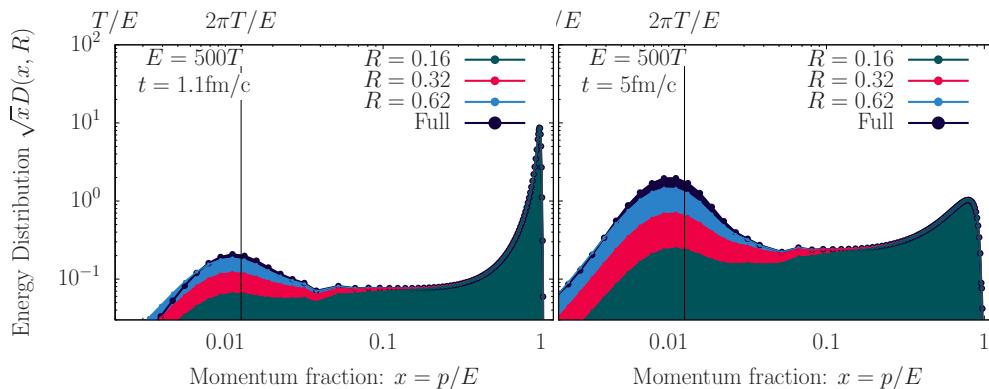
$$\frac{d\Gamma_{bc}^a}{dz}(P, z, \infty) = \frac{g^2 P_{bc}^a(z)}{4\pi P^2 z^2 (1-z)^2} \text{Re} \int_0^\infty dt_1 \int_{\mathbf{p}, \mathbf{q}} \frac{i \mathbf{q} \cdot \mathbf{p}}{\delta E(\mathbf{q})} \Gamma_3(t) \circ G(\infty, \mathbf{q}; t_1, \mathbf{p}) .$$

# AMY Kinetic Theory

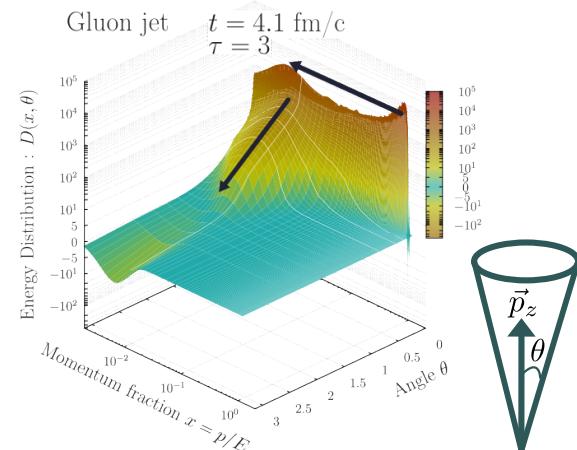
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[Mehtar-Tani Schlichting IS JHEP(2023)]



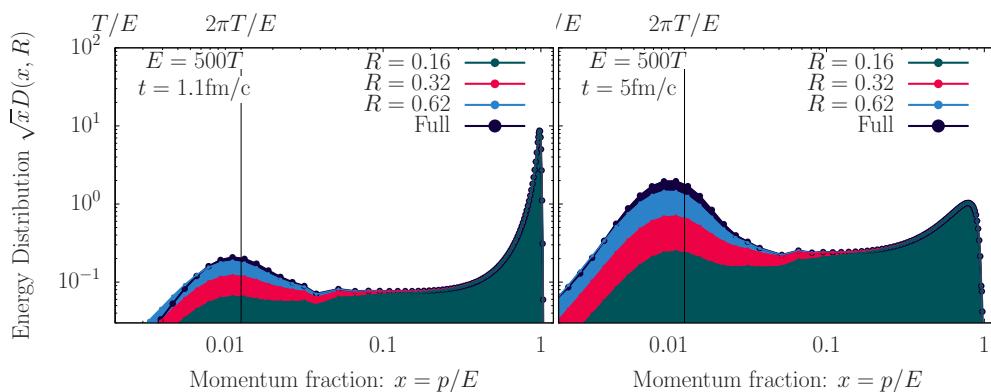
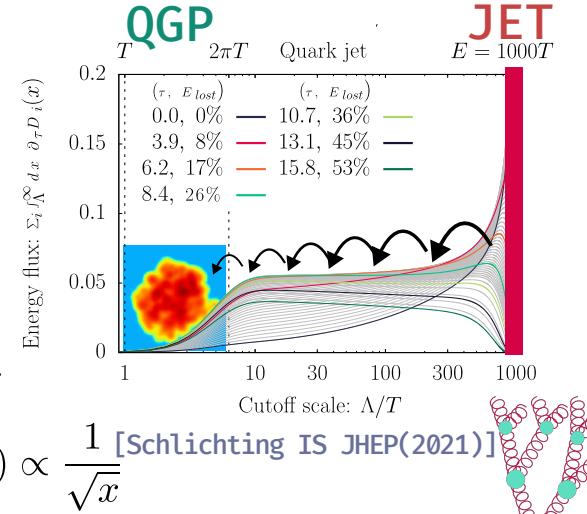
# AMY Kinetic Theory

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» K-Z Turbulent Cascade  $\Rightarrow$  Stationary Solution  $D(x) \propto \frac{1}{\sqrt{x}}$

$$t_{\text{form}} \sim \sqrt{\frac{z(1-z)P}{\hat{q}}} \ll L$$



# AMY Kinetic Theory

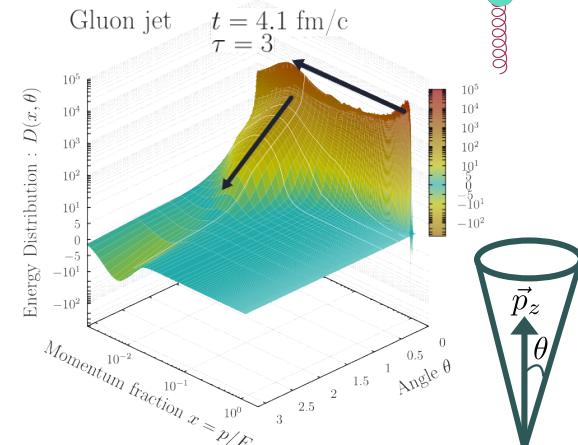
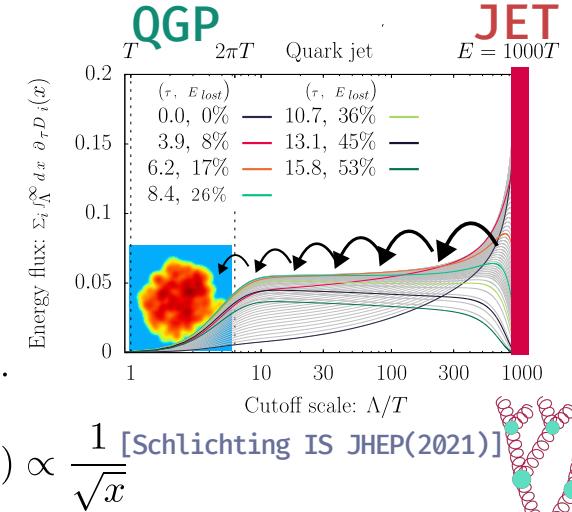
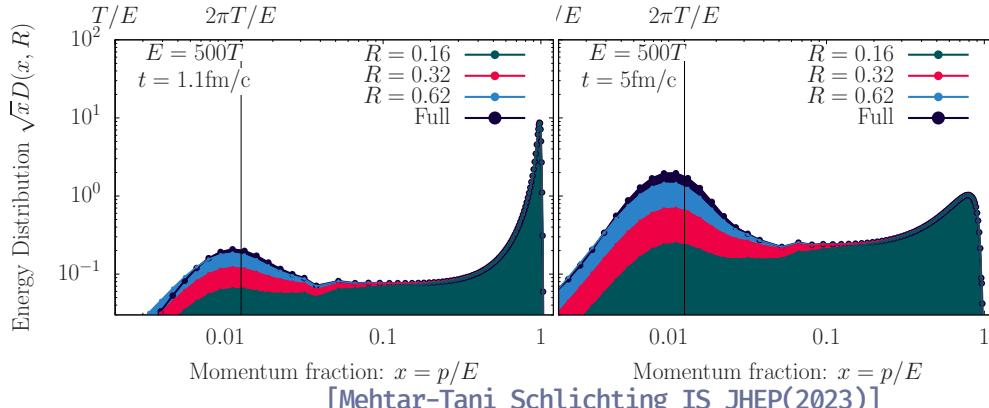
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» K-Z Turbulent Cascade  $\Rightarrow$  Stationary Solution  $D(x) \propto \frac{1}{\sqrt{x}}$  [Schlichting IS JHEP(2021)]

» Due to the Rate Momentum Dependence

$$\partial_t D(x) = \int_0^1 dz \mathcal{K}(z) \frac{1}{\sqrt{x}} \left[ \sqrt{z} D\left(\frac{x}{z}\right) - z D(x) \right]$$



c.f. [Blaizot, Iancu, Mehtar-Tani PRL(2013)]  
 [Blaizot, Mehtar-Tani AOP(2016)]

# Evolving Background

L. F. Zhou Poster  
S. B. Cabodevila Mon 18:10

[Zhou, Brewer, Mazeliauskas  
JHEP(2024)]

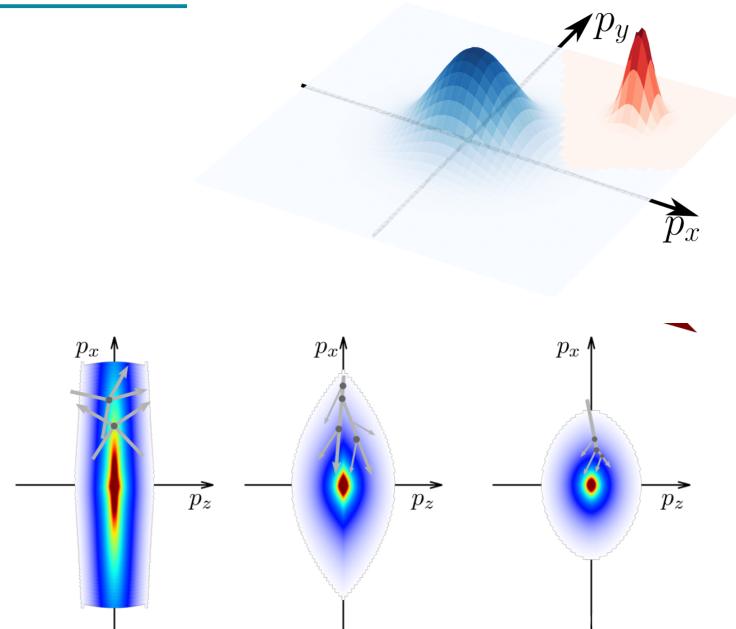
- Evolving Medium

$$\left(\partial_\tau + \frac{p_z}{\tau} \partial_{p_z}\right) f^{QGP}(p, t) = C[f^{QGP}]$$

$$\left(\partial_\tau + \frac{p_z}{\tau} \partial_{p_z}\right) \delta f^{jet}(p, t) = C[f^{QGP}, \delta f^{jet}]$$

- CGC Initial Condition:

$$f^{QGP}(p, t=0) = \frac{2A}{\lambda} \frac{Q_0 \exp[-\frac{2}{3}(p_T^2 + \xi^2 p_z^2)/Q_0^2]}{\sqrt{p_T^2 + \xi^2 p_z^2}}$$

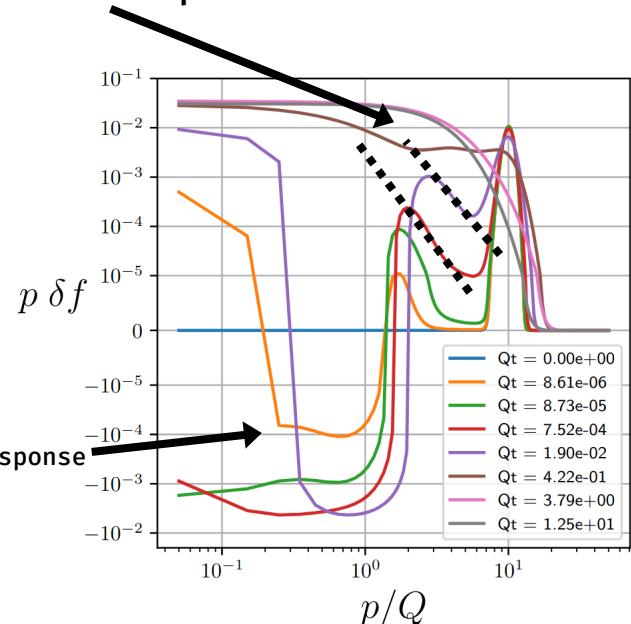


Evolving

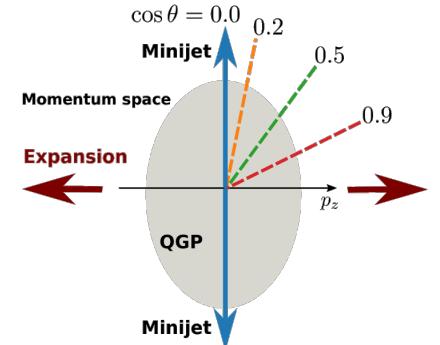
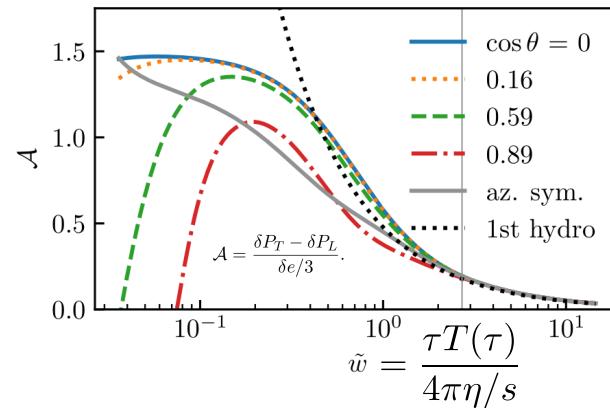
$$f(p, t) = f^{QGP}(p, t) + \delta f^{jet}(p, t)$$

# AMY Kinetic Theory

» K-Z Spectrum Recovered



» “Hydrodynamisation” Of Jets:  
Indistinguishable From Soft  
Background Perturbations  $\tilde{\omega}_{mjh} = 2.7$



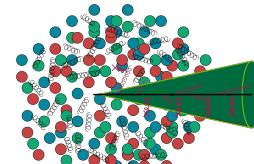
[Zhou, Brewer, Mazeliauskas JHEP(2024)]

# Medium Response

- Thermalized Jet Distribution

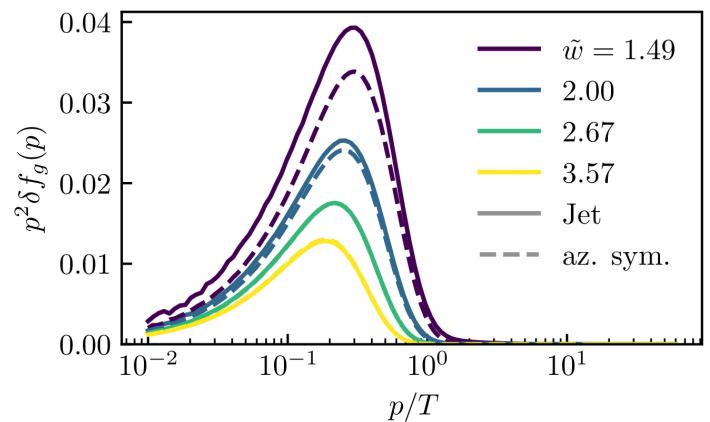
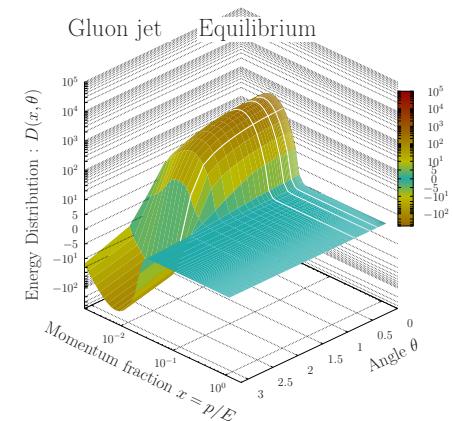
» Static Medium:

$$\delta \bar{f}_a^{(eq)}(\mathbf{p}) = V \left[ \boldsymbol{\delta T} \partial_T + \boldsymbol{\delta u^z} \partial_{u^z} + \boldsymbol{\delta \mu_f} \partial_{\mu_f} \right] n_a(\mathbf{p})$$



» Evolving Medium:

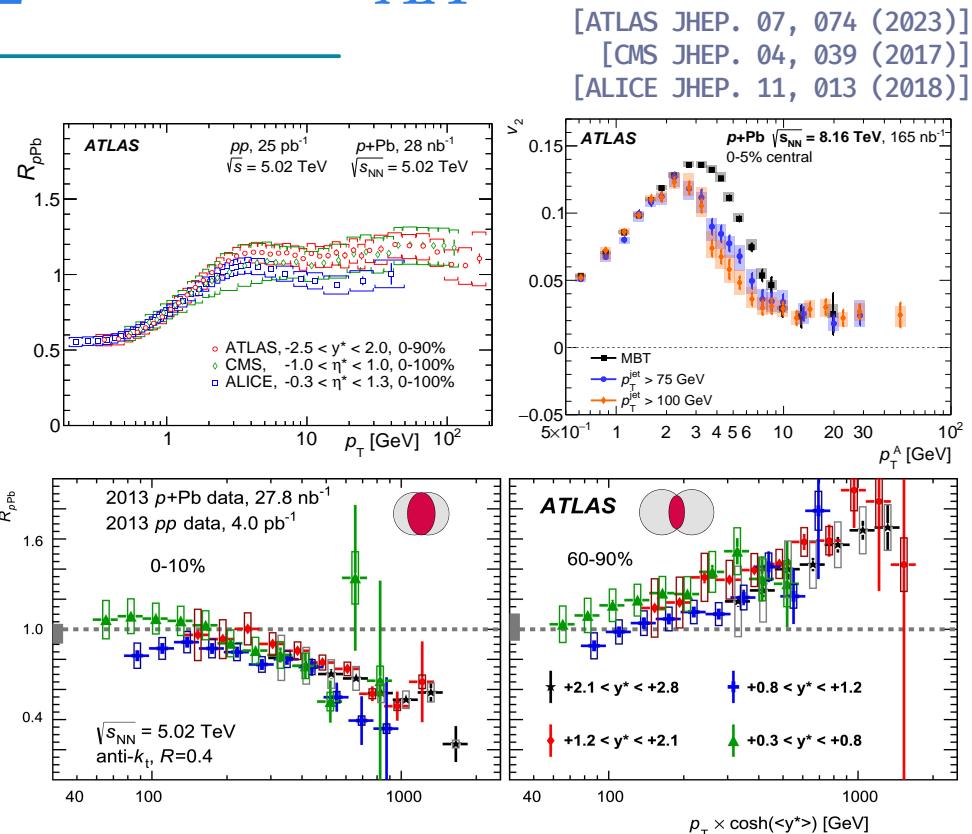
$$\delta f_{\text{visc}} = \frac{\eta/s}{\tau \bar{T}(\tau)} (1 - 3 \cos^2 \theta) F \left( p/\bar{T}(\tau) \right)$$



[Zhou, Brewer, Mazeliauskas JHEP(2024)]

# Small Systems: $v_2$ vs $R_{AA}$

- High- $p_T$   $v_2$  in  $pp$  and  $pPb$
- Centrality Dependence  $R_{pPb}$ 
  - » Initial State Correlations?
  - » Initial State Energy loss?
- Exciting Lab For Hard/Soft Correlations



[ATLAS Phys. Lett. B. 748, 392–413 (2015)]

[ATLAS JHEP. 07, 074 (2023)]  
 [CMS JHEP. 04, 039 (2017)]  
 [ALICE JHEP. 11, 013 (2018)]

# Jet No Longer A Perturbation

- Jets No Longer A Perturbation On Top Of Bulk

- » Jet Carry Substantial Amount Of Energy

- » Jet Modifies The Bulk

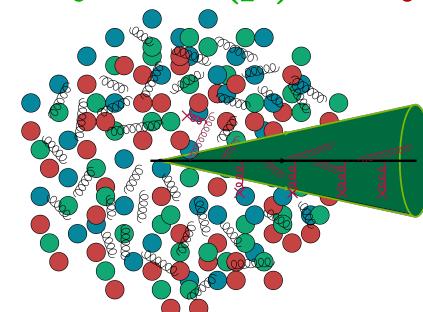
- » Bulk Extent is Small  $\Rightarrow$  Finite Size Effects Important

- » Energy Loss Negligible?

- » Vacuum-like Physics Important:  
Higher-Twist, GLV...

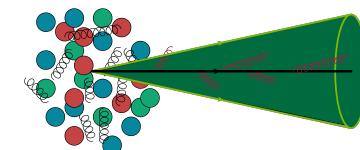
Heavy-Ion

$$f(p) = f^{QGP}(p) + \delta f^{jet}(p)$$



Small Systems

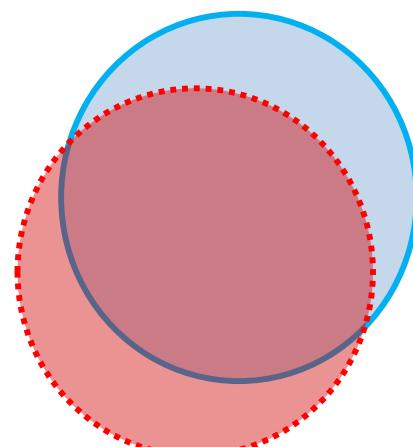
$$f(p) = f^{jet}(p) + \delta f^{Bulk}(p)$$



# Transverse Correlation

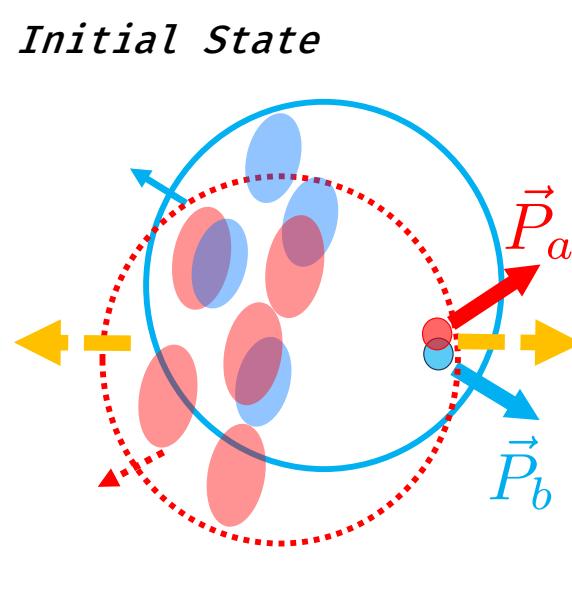
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*Initial State*

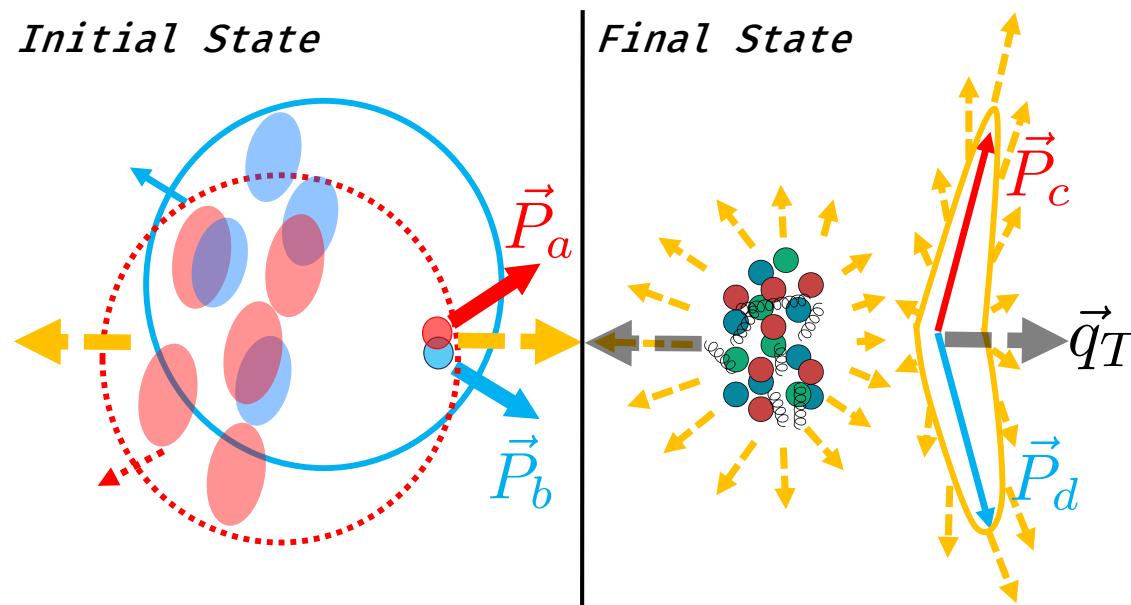


# Transverse Correlation

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# Transverse Correlation



» Balanced Transverse Momentum  $\vec{q}_T = \vec{p}_{aT} + \vec{p}_{bT}$  b/w Hard/Soft Particles

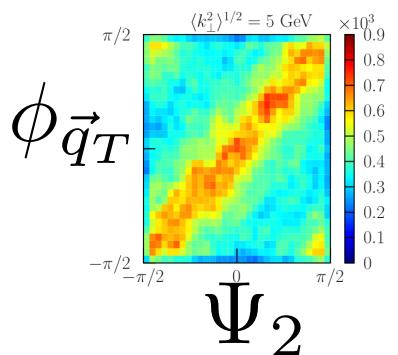
# Transverse Correlation

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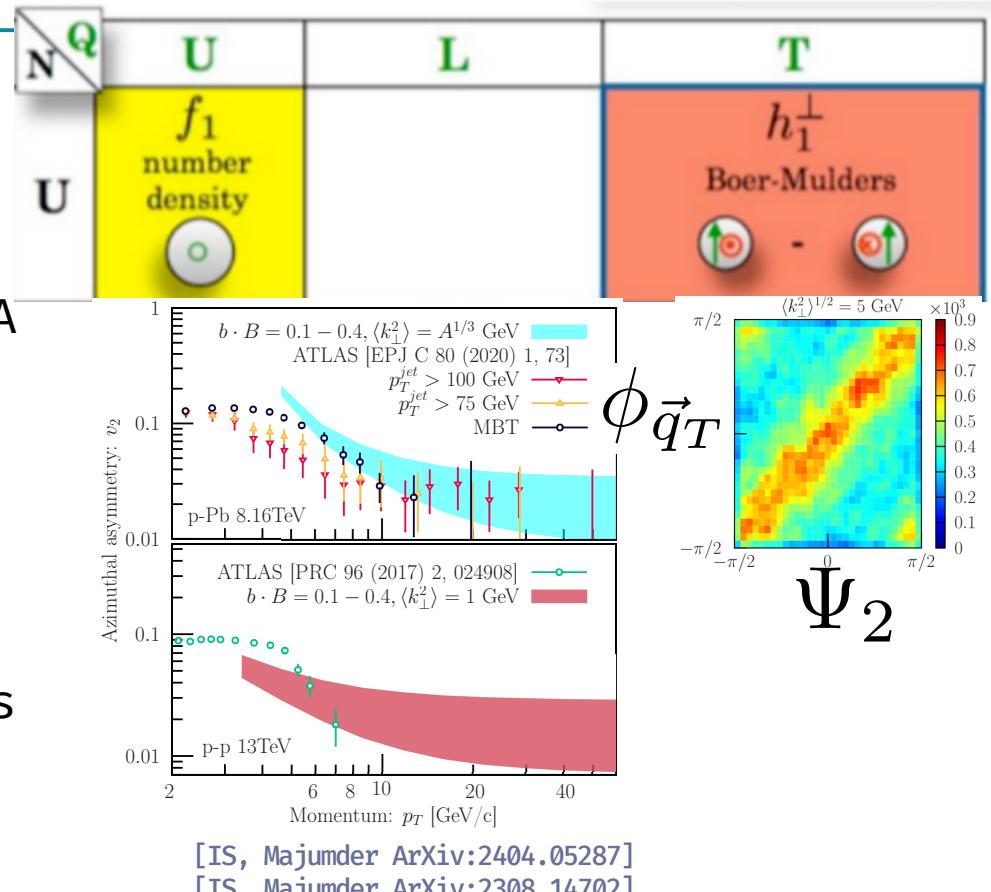
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- Conservation Of Momentum  $\Rightarrow$  Hard/Soft Correlation
  - » Corroborated By Simple PYTHIA simulation



# Transverse Correlation

- Conservation Of Momentum  $\Rightarrow$  Hard/Soft Correlation
  - » Corroborated By Simple PYTHIA simulation
- TMD-PDFs and FFs:
  - » Azimuthal Correlations Due Initial  $k_T$
  - » Boer-Mulders'/Collins Effects

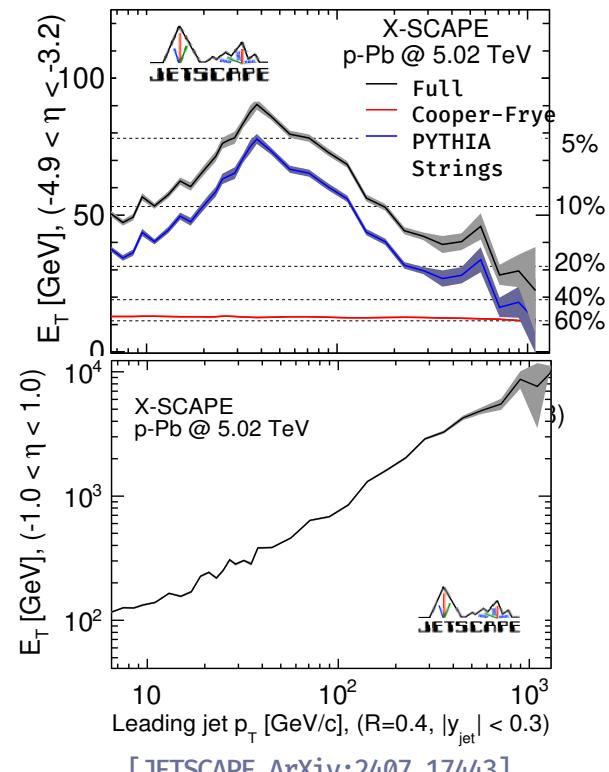


[IS, Majumder ArXiv:2404.05287]  
[IS, Majumder ArXiv:2308.14702]

# Energy Conservation

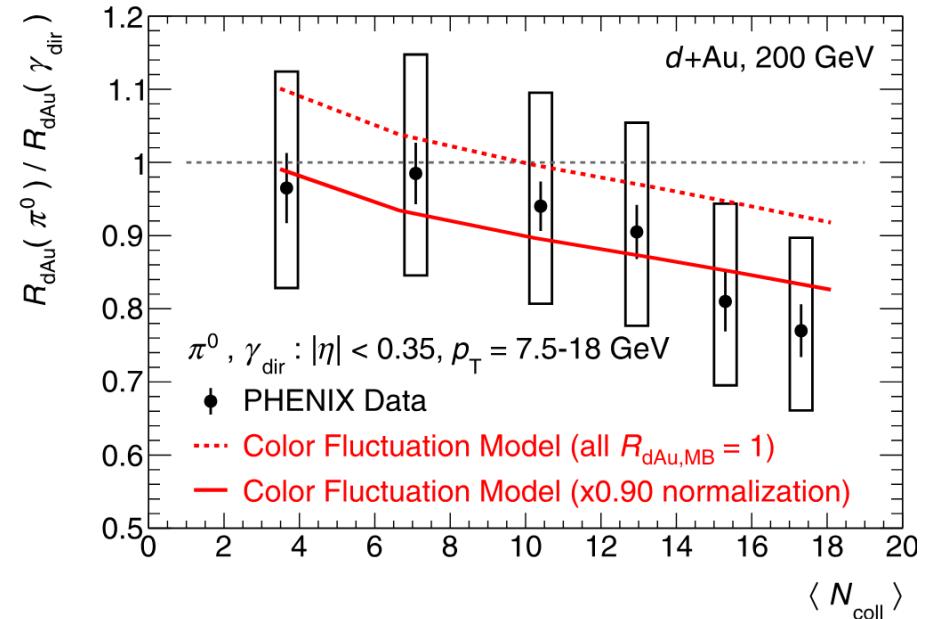
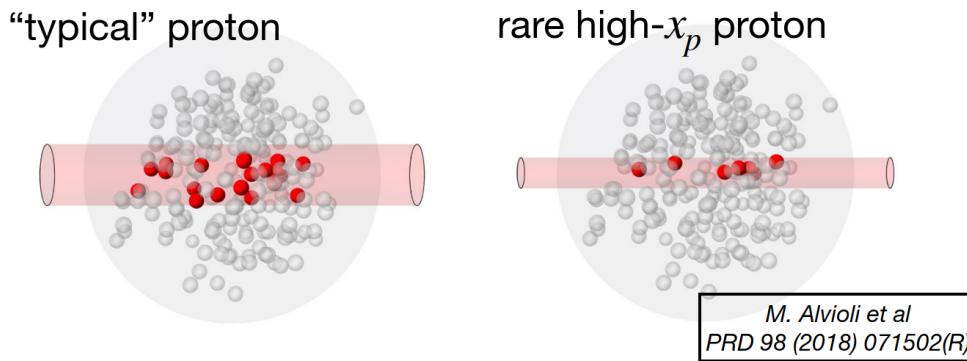
S. Jeon Tue. 16:15

- Multi-stage Framework For Small Systems
  - » Correlations b/w Soft/Hard Particle Production
  - » Competition b/w Jet  $p_T$  and Partonic remnants
  - » Hard Scattering Increasing  $E_T$  until Momentum Conservation Limits



# Bjorken-x

D. Perepelitsa Mon 14:40



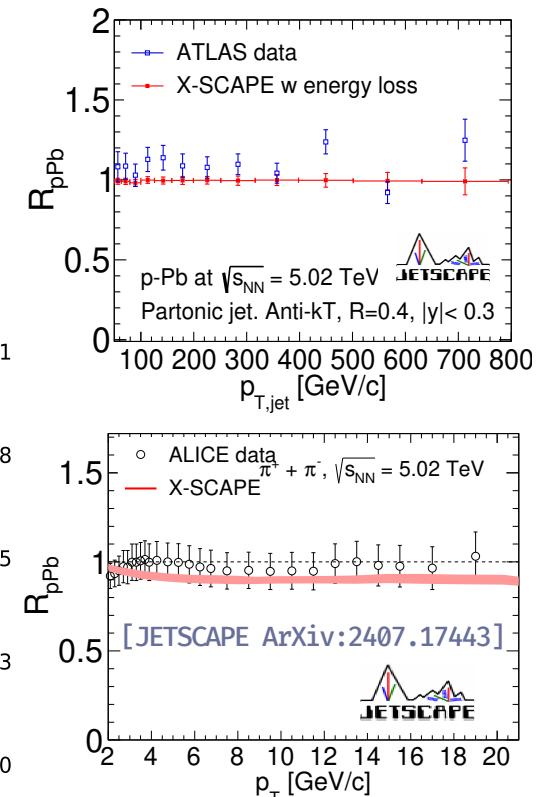
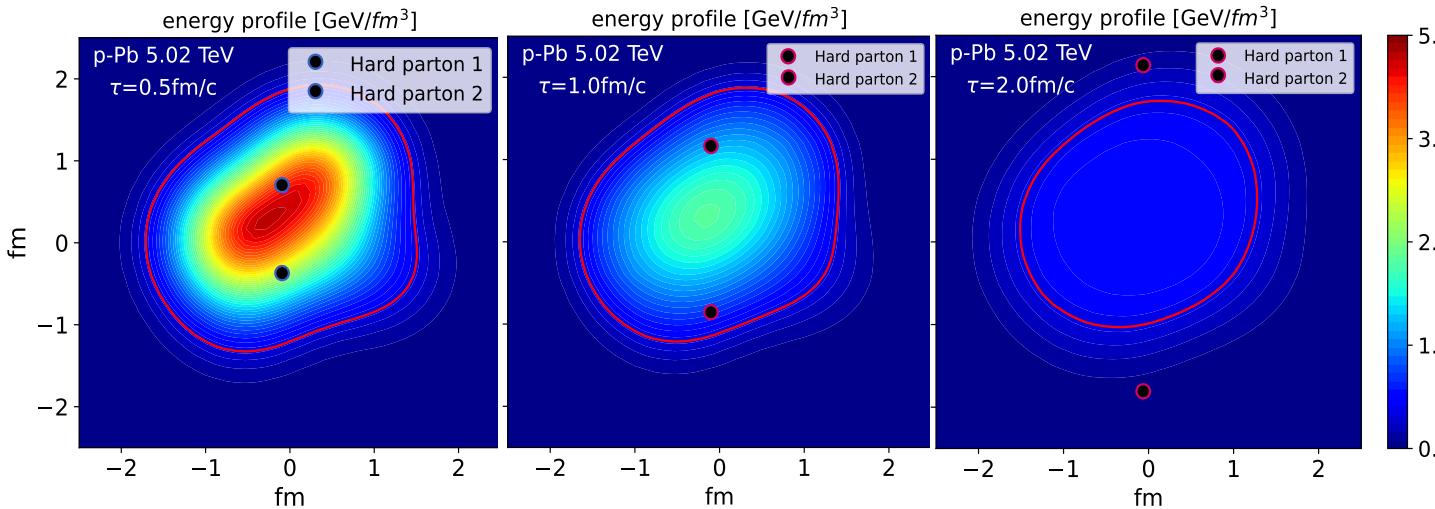
- Presence of Hard Partons  $\Rightarrow$  Significant Difference Bjorken-x Distribution Than Average Protons

[Perepelitsa PRC(2024)]

# Energy Loss?

S. Jeon Tue. 16:15

- Short Bulk Extent
  - » Energy Loss Negligible



# Formation Time

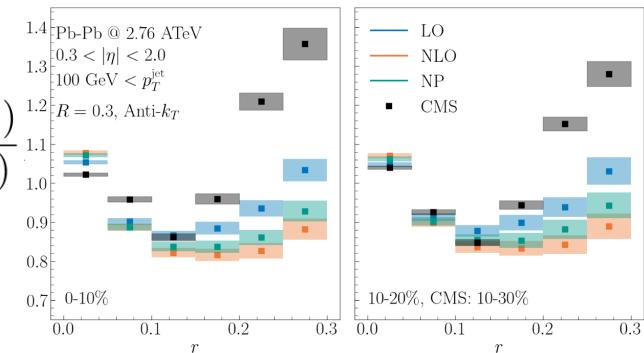
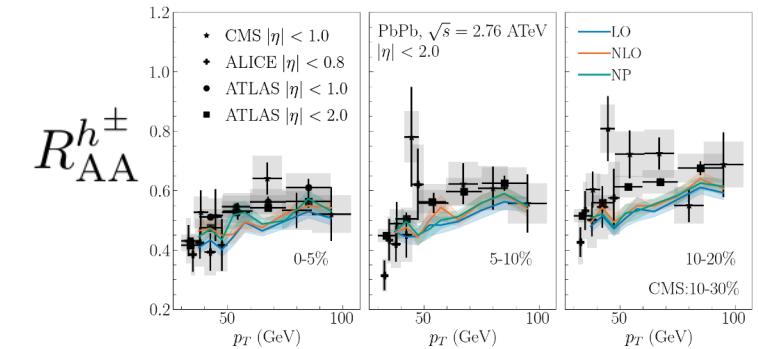
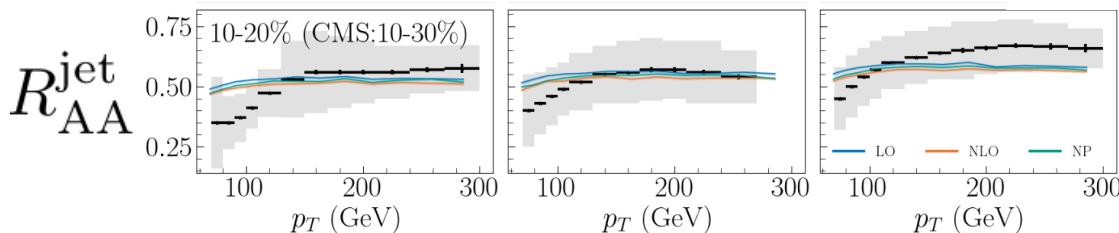
Shuzhe Mon. 15:40

» Formation Time  $\Rightarrow$  Simultaneous Desc.

Charged Hadron And Jet  $R_{AA}$

» Limitation: Jet Substructure  
Observables

» LO/NLO/NP Potential  $\Rightarrow$  Similar Ratios,  
 $\neq$  Substructure

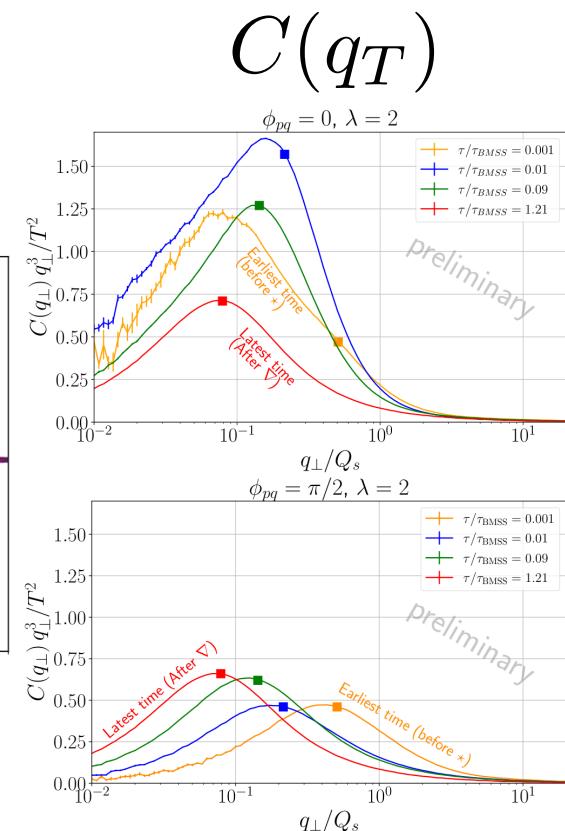
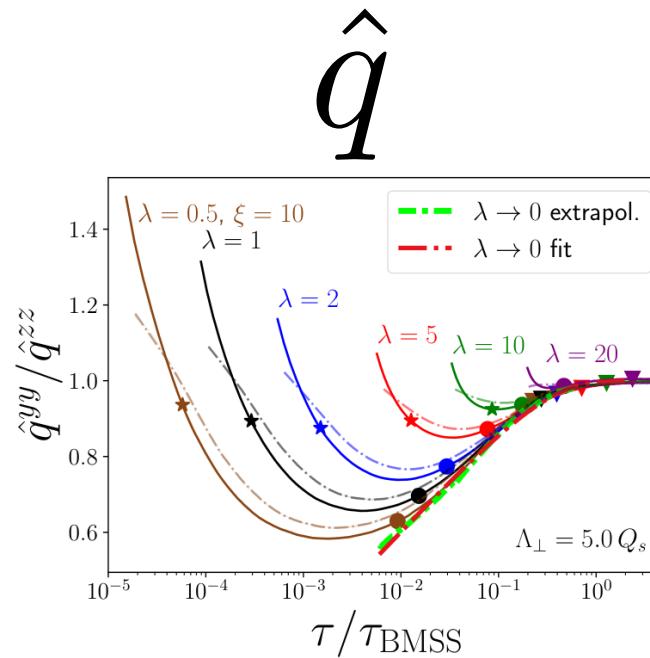


[ Modarresi-Yazdi, Shi, Gale, Jeon ArXiv:24  
07.19966 ]

# Early Stages

F. Lindenbauer Mon. 17:30

- Broadening In Non-Eq EKT
  - » Momentum Broadening Affected By Anisotropy  $\Rightarrow$  Scaling Behavior
  - » Broadening Kernel Extraction  $\Rightarrow$  Markedly Different Throughout The Equilibration

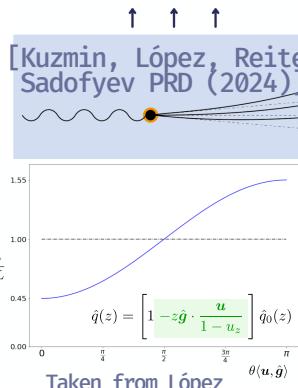


[K. Boguslavski, A. Kurkela, T. Lappi, F. Lindenbauer, J. Peuron PLB (2024) PhysRevD (2024)]

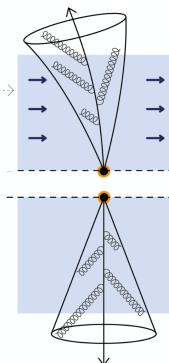
# Gradient effects

## Medium Gradients

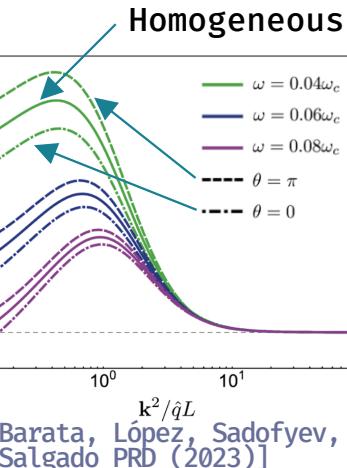
### Broadening



X. Lopez Wed. 11:10



### Radiation



## Jet Drift

$$\langle \vec{q}_{drift} \rangle = \hat{e}_\perp \int d\tau \frac{3}{E(\tau)} \frac{\mu^2(\tau)}{\lambda(\tau)} \ln \frac{E(\tau)}{\mu(\tau)} \frac{u_\perp(\tau)}{1 - u_\parallel(\tau)}$$

Flow enhanced and flow direction controlled

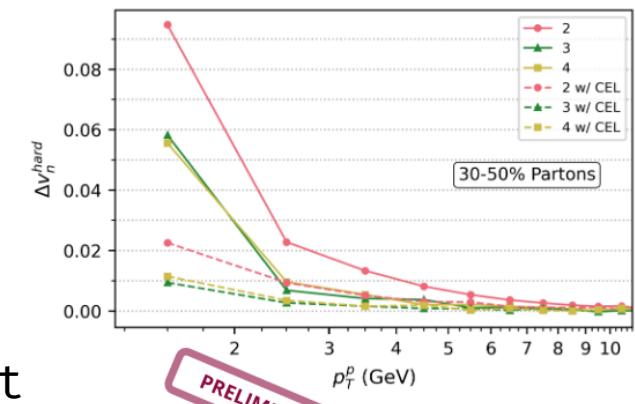
$\frac{1}{\lambda} = \sigma \rho$

$\rho \propto T^3$

$\mu \propto T$

Energy suppressed

Temperature/Density Enhanced



J. Bahder Tue 11:50

» Suppressed Broadening/Radiation Along Gradient

» Enhanced Broadening/Radiation Opposite To Gradient

» Jet- $v_2$  correlations due to drifts

**Derivation**  
A. V. Sadofyev, I. Vitev,  
& M. D. Sievert  
Phys.Rev.D 104 (2021)  
(arXiv:2104.09513)

**Analytic Phen.**  
L. Antiporda, J. Bahder, H.  
Rahman  
& M. D. Sievert  
Phys.Rev.D 105 (2022)  
(arXiv:2110.03590)

# Conclusion

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- Heavy-Ion  $\Rightarrow$  Jet Perturbation On Top Of The QGP
  - Small Systems  $\Rightarrow$  Bulk Dynamics Altered By Jets
- »Observables  $\Rightarrow$  Jet  $v_2$  vs  $R_{AA}$  , Jet-Substructure See Daniel Talk Before
- »Small Systems  $\Rightarrow$  A Laboratory to Understand Int. St. Correlations? Int. St. Energy Loss? See Isobel Talk Next

# Backup

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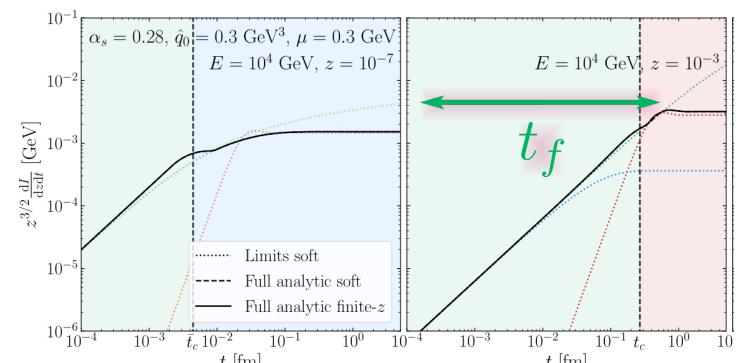
# Beyond AMY

## » Time Dependent Splitting Rates

$$\partial_t D(x) = \int_0^1 dz \left[ \frac{d\Gamma_{bc}^a}{dz} \left( \frac{x}{z}, z, \textcolor{red}{t} \right) z D \left( \frac{x}{z} \right) - \frac{d\Gamma_{bc}^a}{dz}(x, z, \textcolor{red}{t}) z D(x) \right]$$

## » Static Medium

[Isaksen, Takacs, Tywoniuk JHEP(2023)]



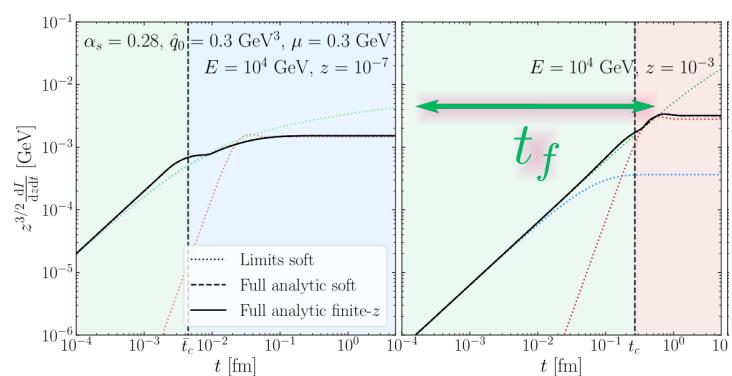
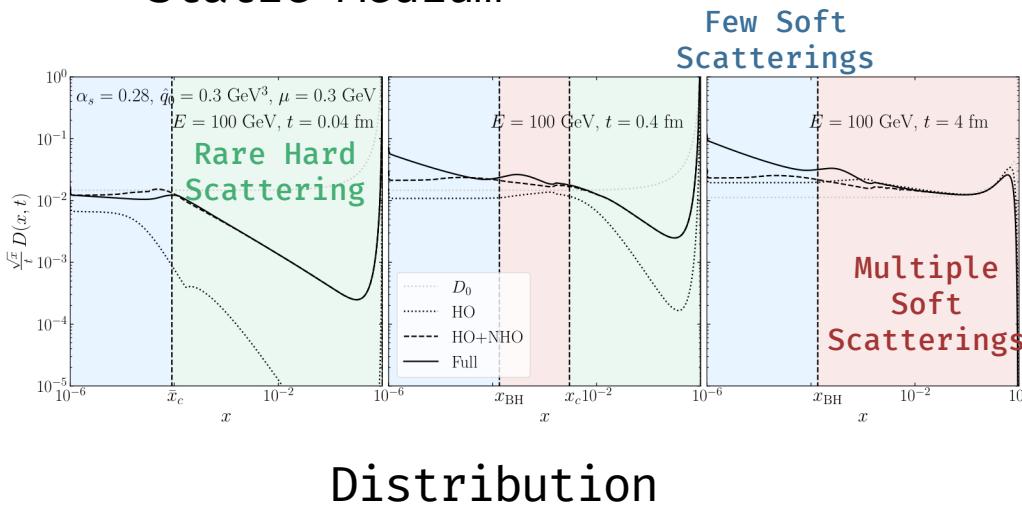
Rate

# Beyond AMY

## » Time Dependent Splitting Rates

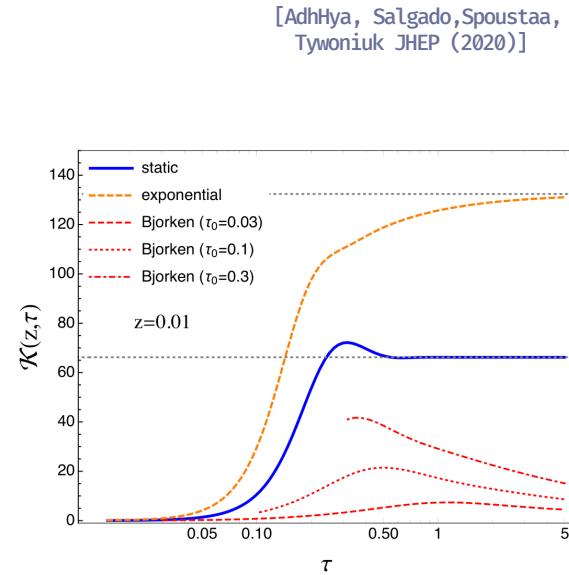
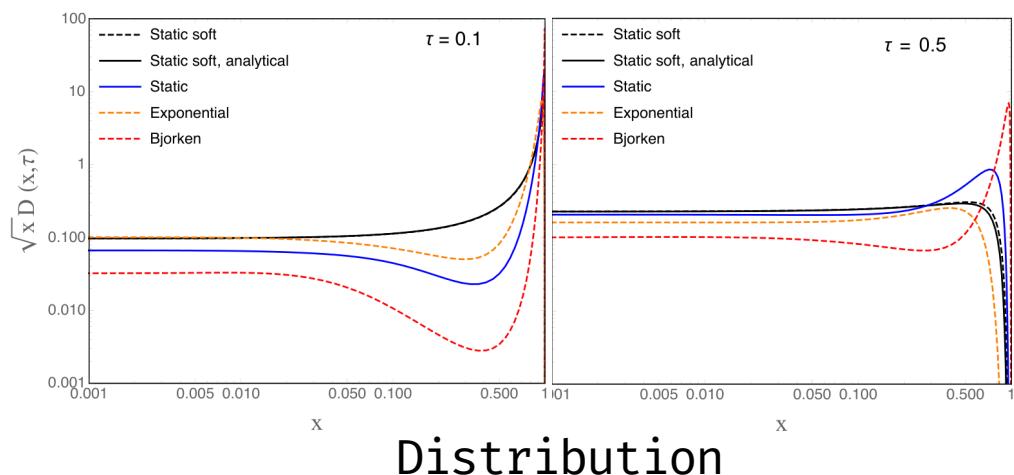
$$\partial_t D(x) = \int_0^1 dz \left[ \frac{d\Gamma_{bc}^a}{dz} \left( \frac{x}{z}, z, \textcolor{red}{t} \right) z D \left( \frac{x}{z} \right) - \frac{d\Gamma_{bc}^a}{dz}(x, z, \textcolor{red}{t}) z D(x) \right]$$

## » Static Medium



# Harmonic Oscillator

- » Rates in Expanding Medium w/ HO Approx.
- » Analytical expressions [BDMPS, Arnold]
- » Temperature decreases  $T \ll P \Rightarrow$  Multiple Soft Scattering



Rate