



Search for Spinning Black Hole Binaries in Advanced LIGO: Parameter tuning of HACR

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Overview

**Goal: Detection of SBHB's in Time
Frequency representation of Advanced
LIGO data**

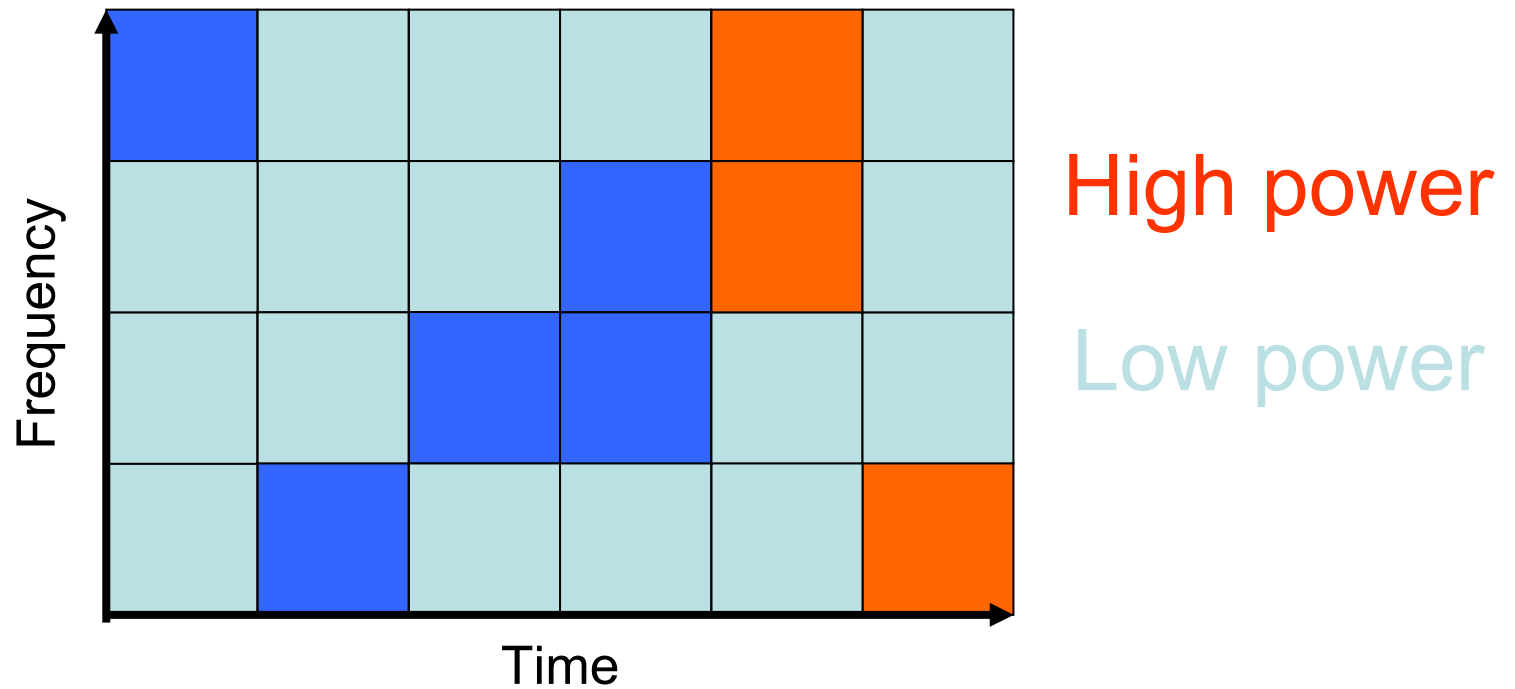
- What is HACR?
- Spinning Black Hole Binaries
- Tuning HACR in 2 steps
- Results
- Conclusions and Future Work

What is HACR?

- **Hierarchical Algorithm for Clusters and Ridges** written by R. Balasubramanian
- Time-frequency search
- Short bursts of excess power
- More robust than matched-filtering
- Implemented in GEO++ as HACRMon

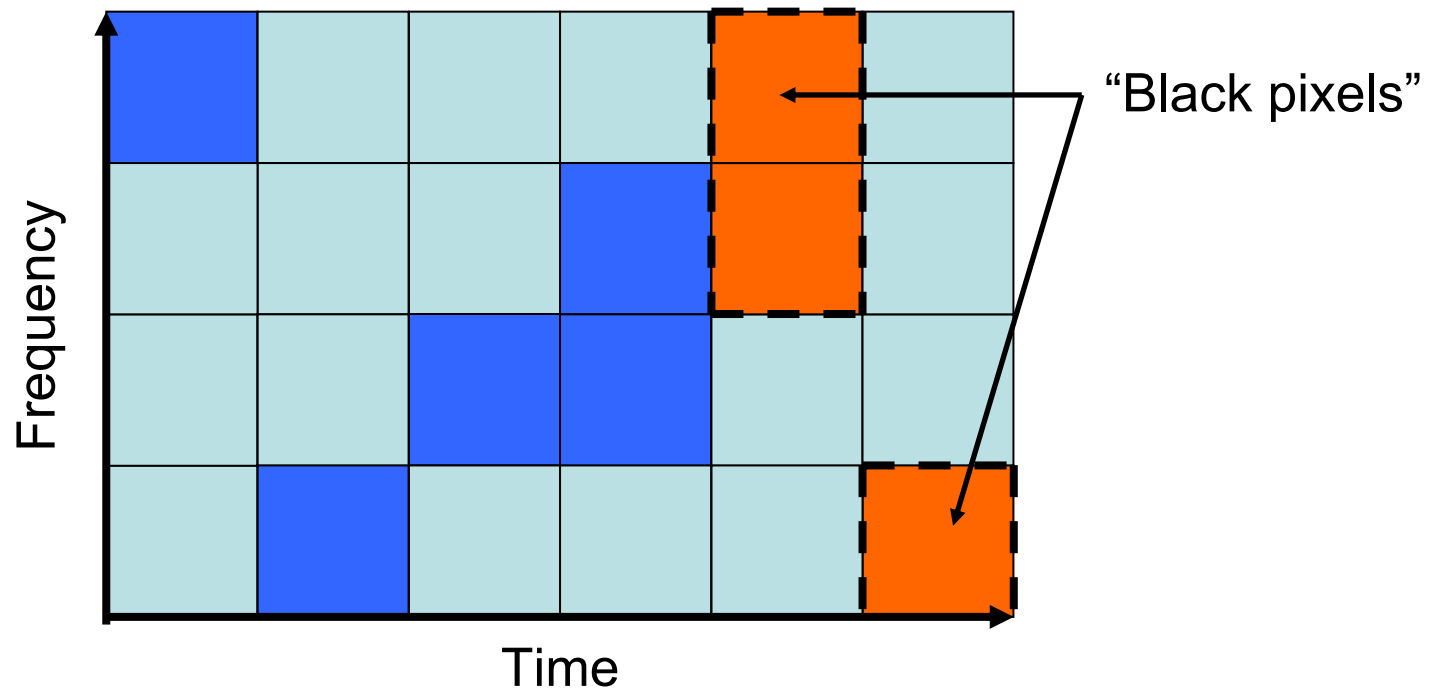
How HACR works

1. Identify pixels with $P > \eta_{\text{upper}}$



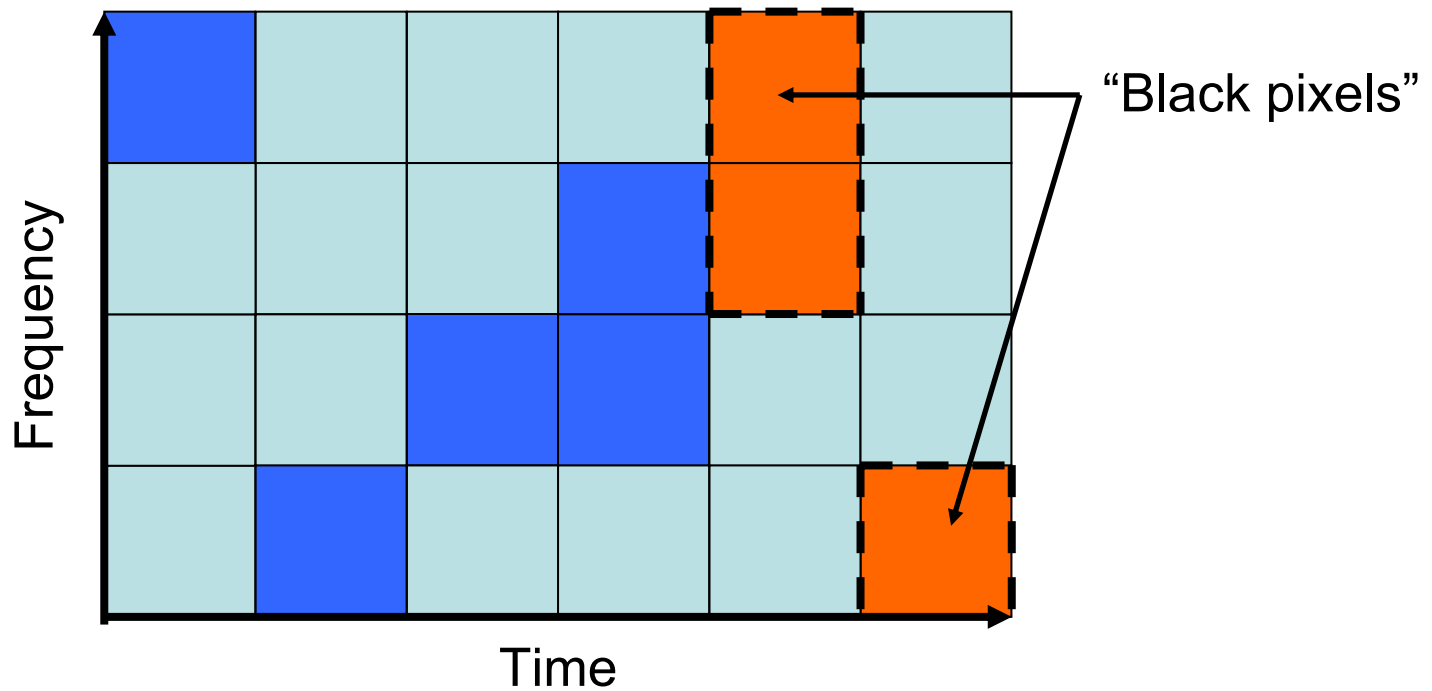
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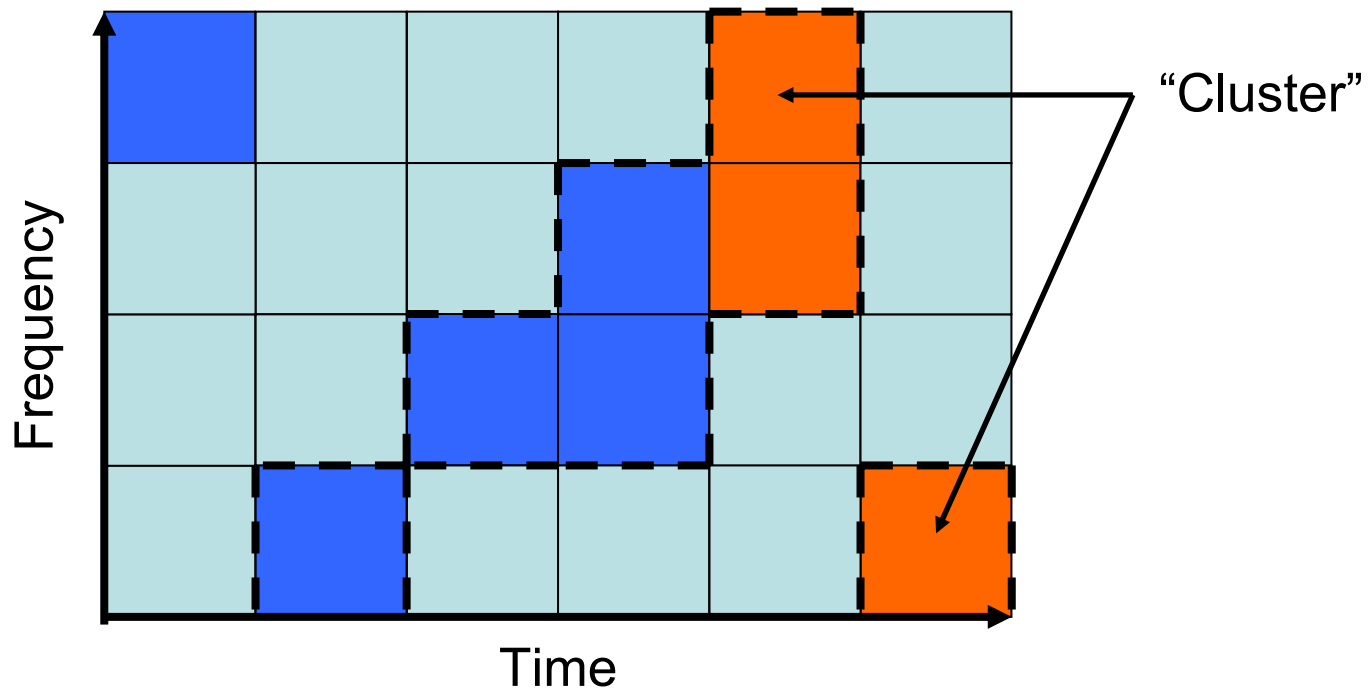
How HACR works

2. Identify neighbouring pixels with $P > \eta_{\text{lower}}$



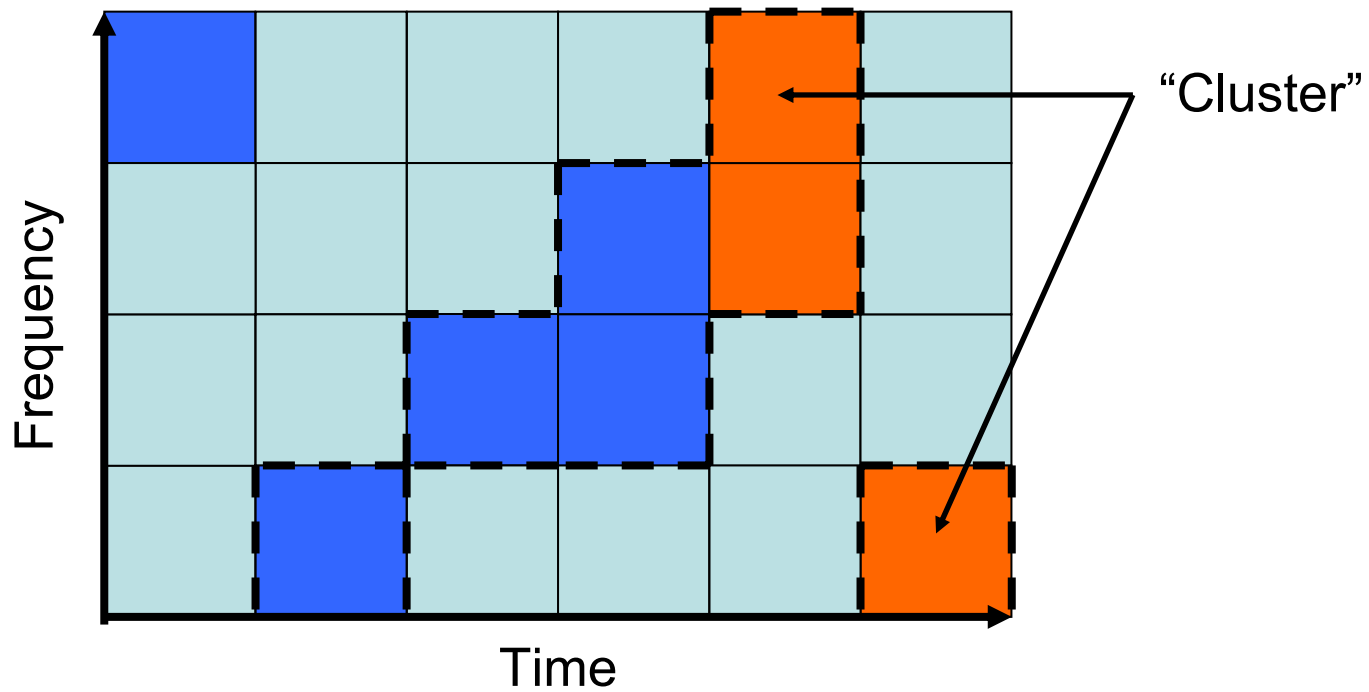
How HACR works

2. Identify neighbouring pixels with $P > \eta_{\text{lower}}$



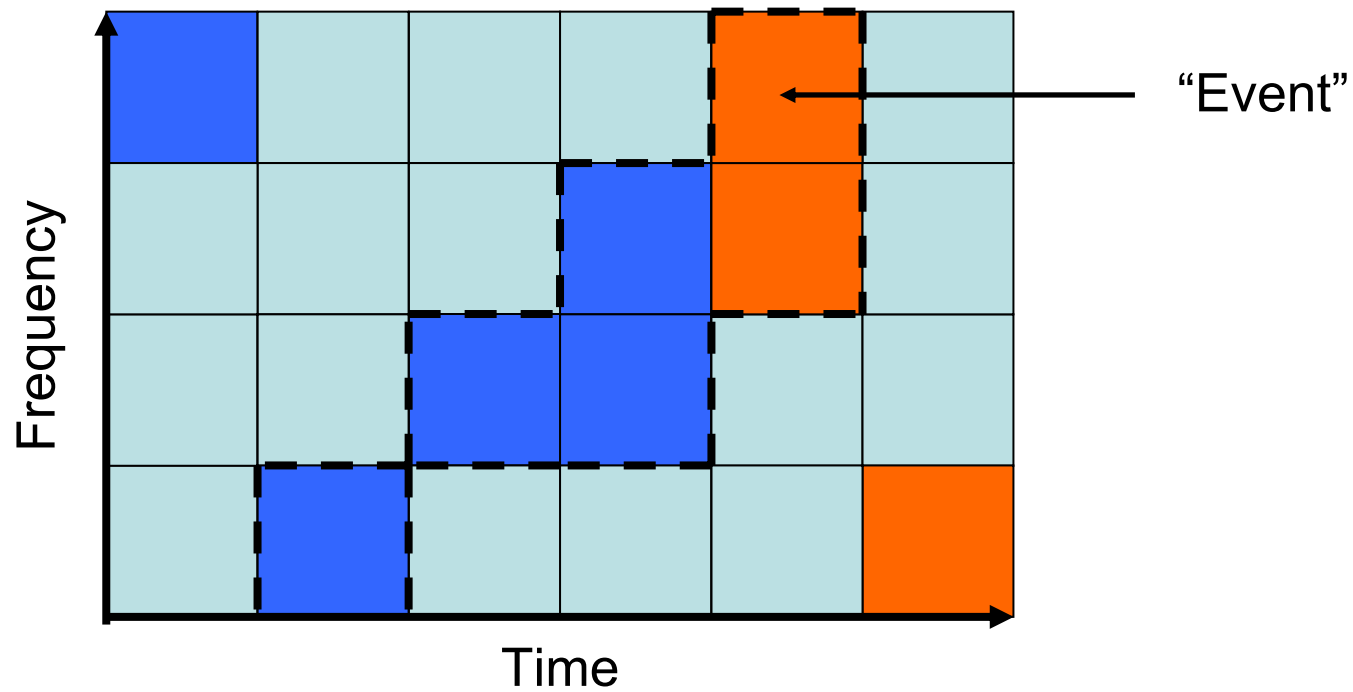
How HACR works

3. Identify clusters with $N_{\text{pixels}} > N_{\text{threshold}}$



How HACR works

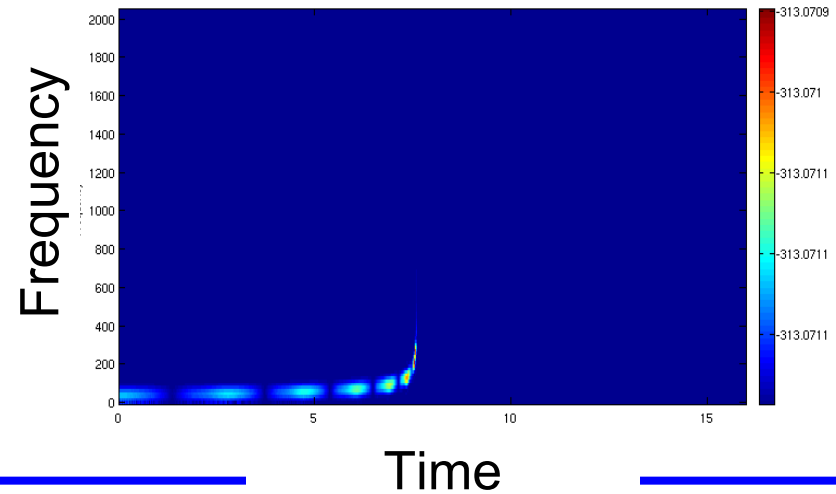
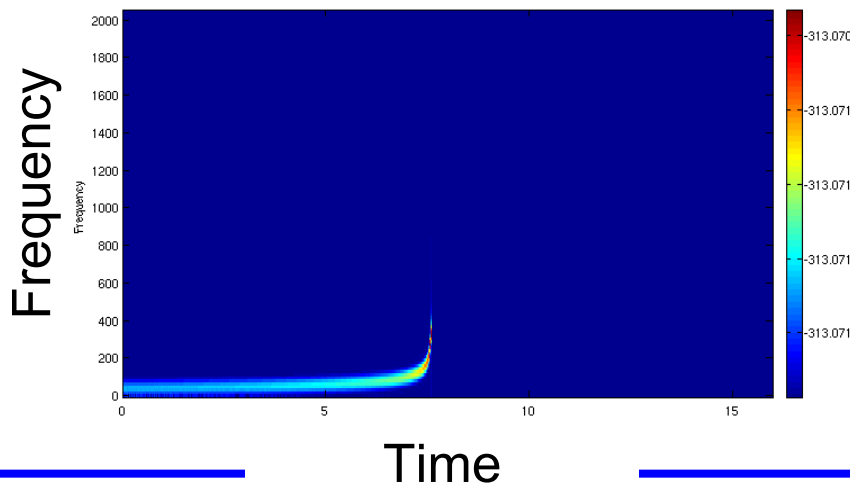
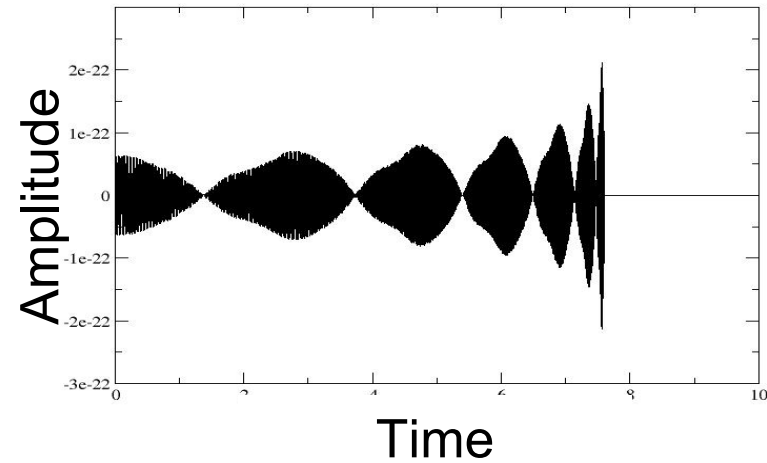
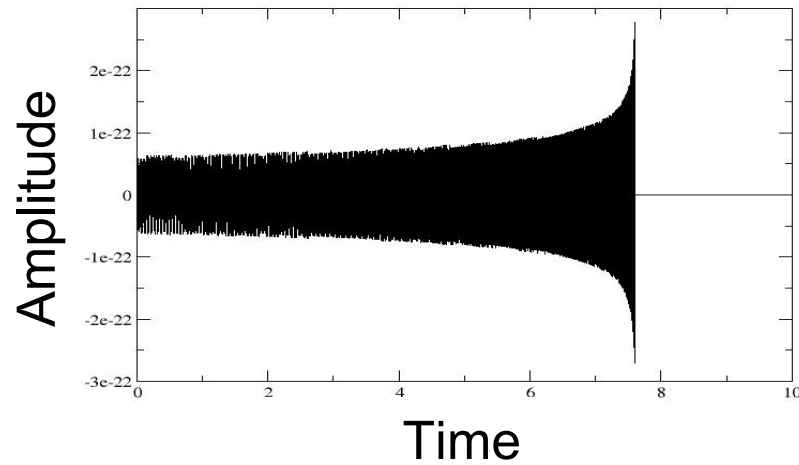
3. Identify clusters with $N_{\text{pixels}} > N_{\text{threshold}}$



Spinning Black Hole Binaries

- Require 17 physical parameters to accurately describe waveform
- Spin-induced precession of orbital plane causes modulation of amplitude and phase
- Amplitude modulation causes of GW “archipelago” of clusters in TF map

Spinning Black Hole Binaries



Tuning HACR

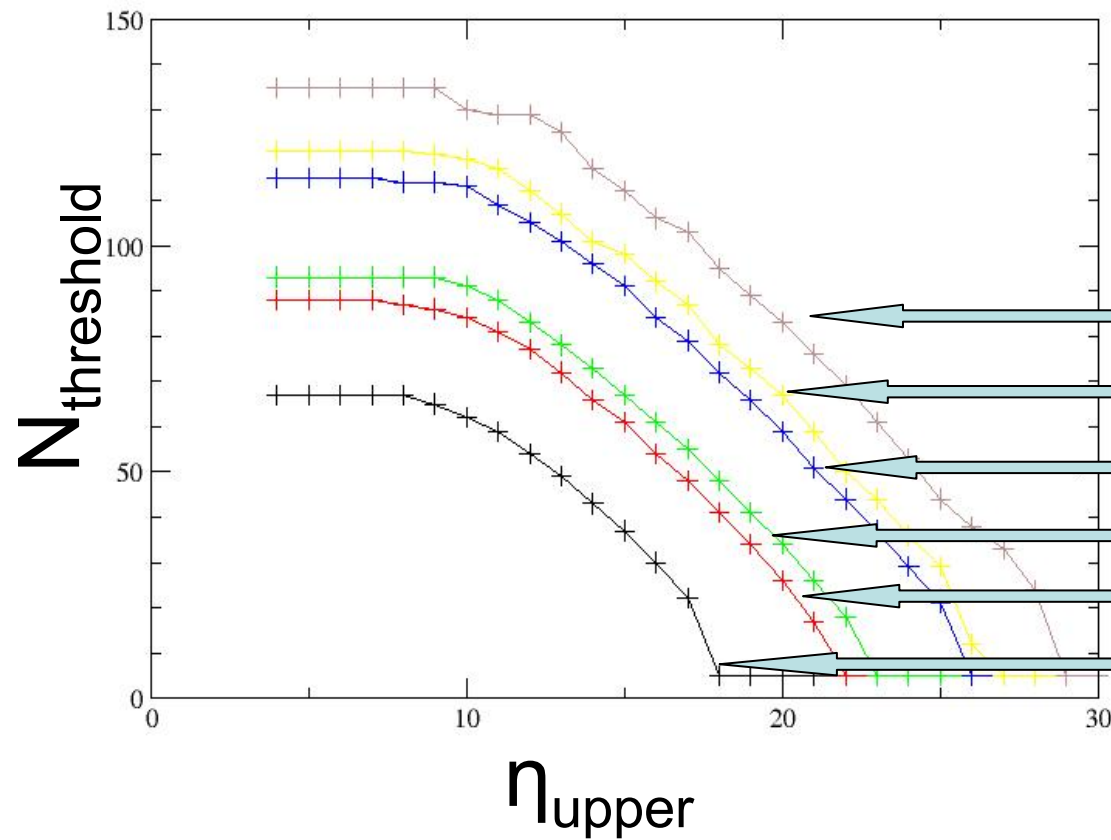
**For a given false alarm rate maximise
probability of detection**

- 3 parameters: η_{upper} , η_{lower} , $N_{\text{threshold}}$
- Identify combinations of threshold parameters (η_{upper} , $N_{\text{threshold}}$) that produce a constant false alarm rate...
- ... then for each combination of parameters measure probability of detection

False Alarm Analysis

- 100,000s of simulated Adv. LIGO data
 - Gaussian white noise convolved with Adv. LIGO PSD
- Analyse once with low values of thresholds
 - $\eta_{\text{upper}} = 4$
 - $N_{\text{threshold}} = 5$
- Store maximum-power and number of pixels for each found “event”
- For range of η_{upper} choose values of $N_{\text{threshold}}$ that give specific False Alarm rates
- Python scripts that search through a mysql database

False Alarm Analysis



Contours of constant
false alarm rate

1 False alarm per...

...hour (27.8 events)

...1000s (100 events)

...**10 mins (166.7 events)**

...100s (1000 events)

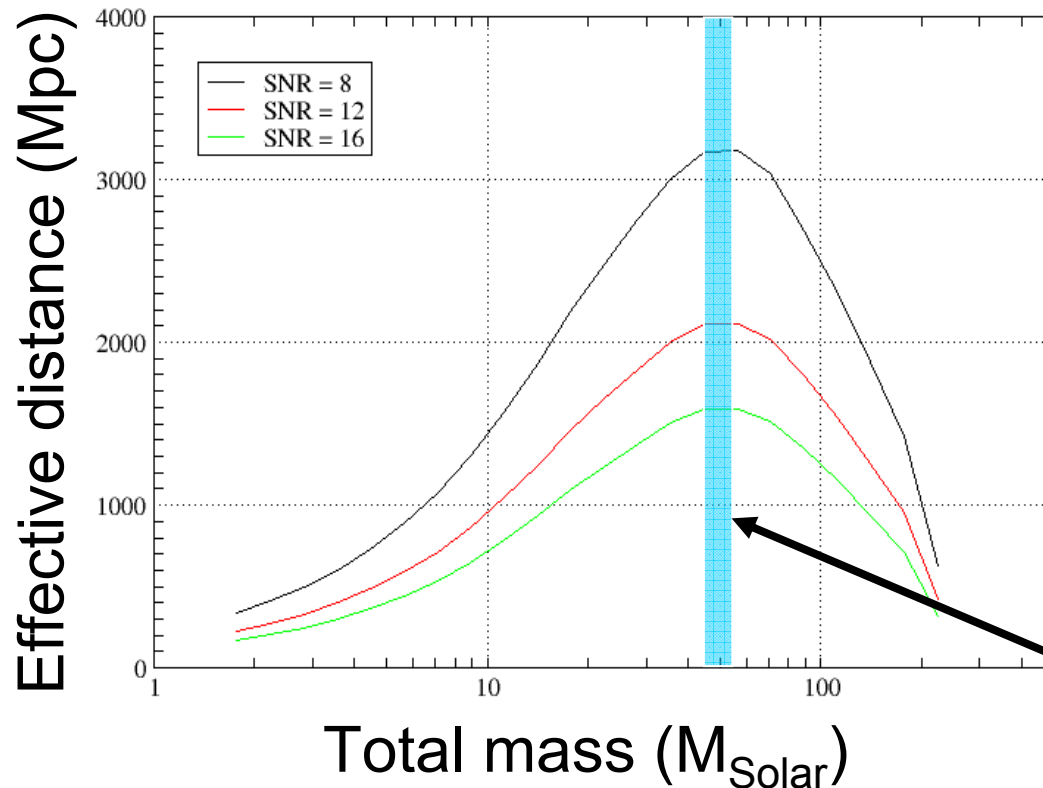
...min (1666.7 events)

...10s (10,000 events)

Injection of SBHB waveforms

- Physical waveforms
- (1-49), (10-40) and (25-25) M_{solar}
- Mass that Adv. LIGO can see furthest
- 1000 injections each with SNR = 8, 12, 16
- Measure number of injections recovered for each combination of $(\eta_{\text{upper}}, N_{\text{threshold}})$

Span of Adv. LIGO



- Effective distance:

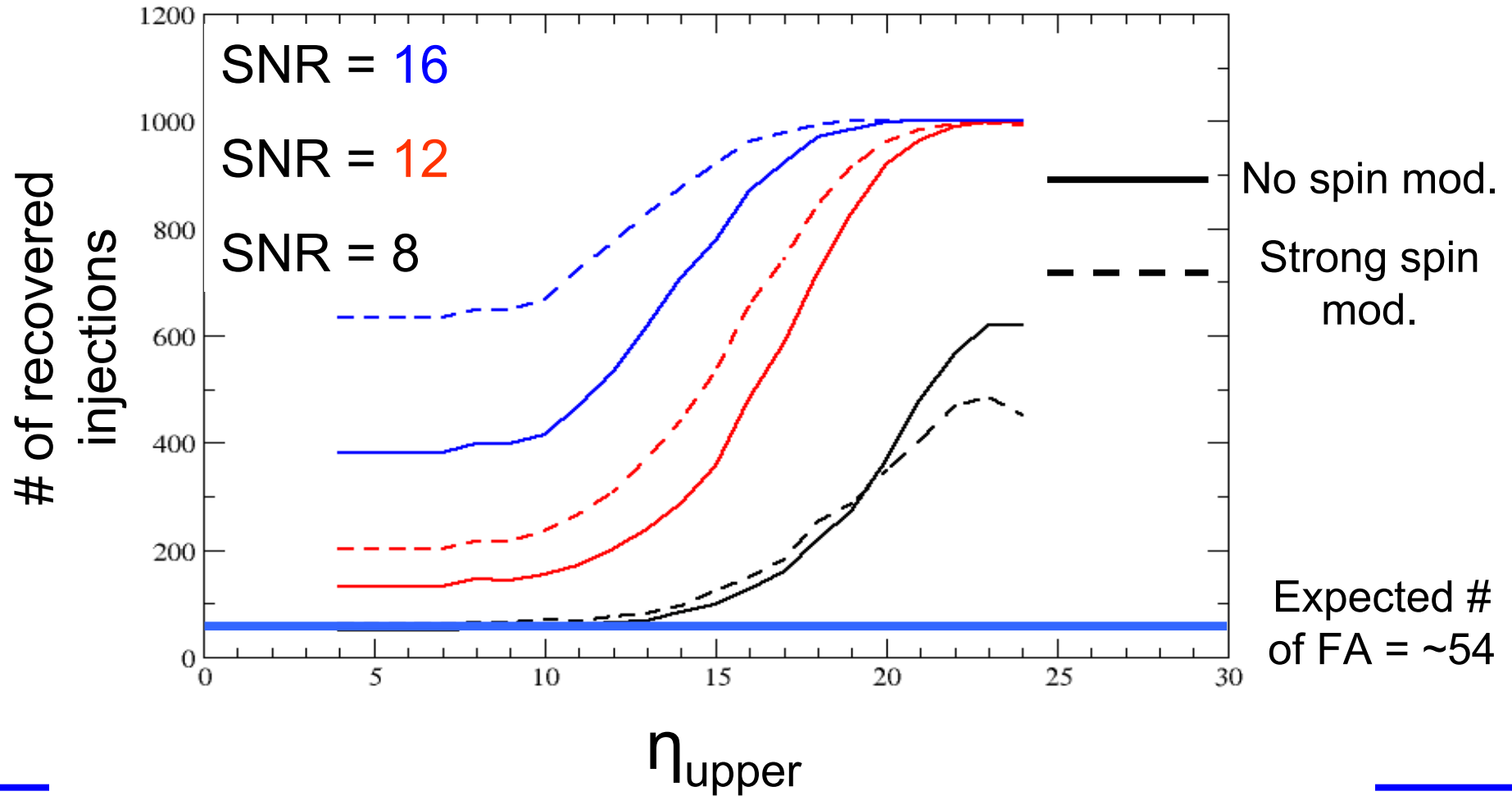
$$d = \frac{M^{5/6}}{\rho \pi^{3/2}} \left(\frac{5\eta}{6} \right)^{1/2} \left[\int_{f_{low}}^{f_{LSO}} df \frac{f^{-7/3}}{S_h(f)} \right]^{1/2}$$

- Equal mass binaries:

$$\eta = 0.25$$

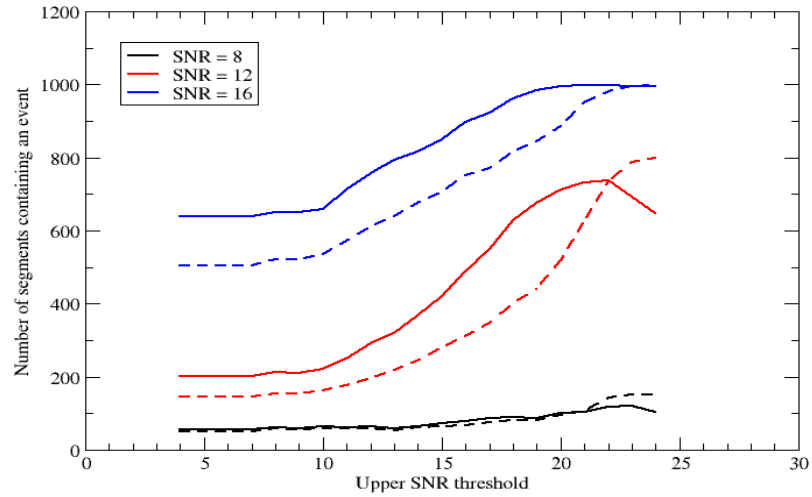
M = 50M_{Solar}

(25-25) M_{Solar} Results

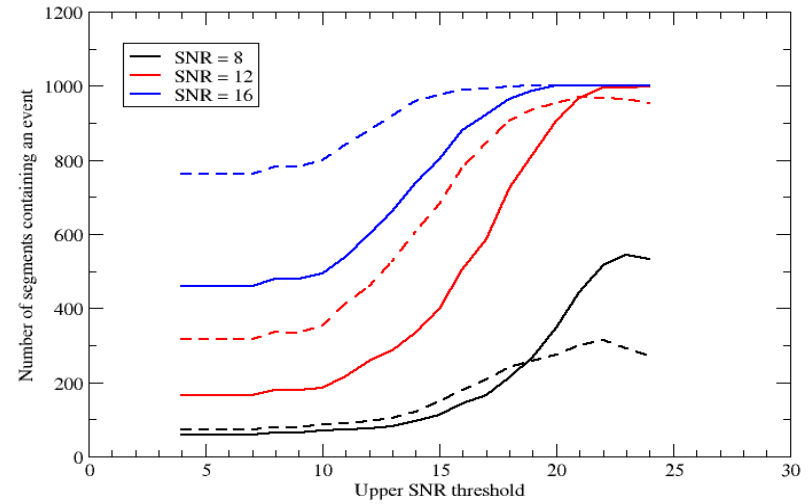


(encodes corresponding $N_{\text{threshold}}$)

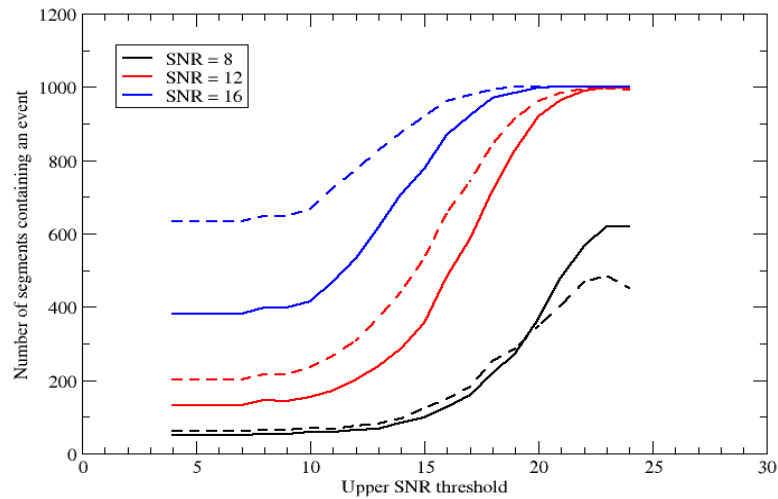
(1-49) M_{Solar}



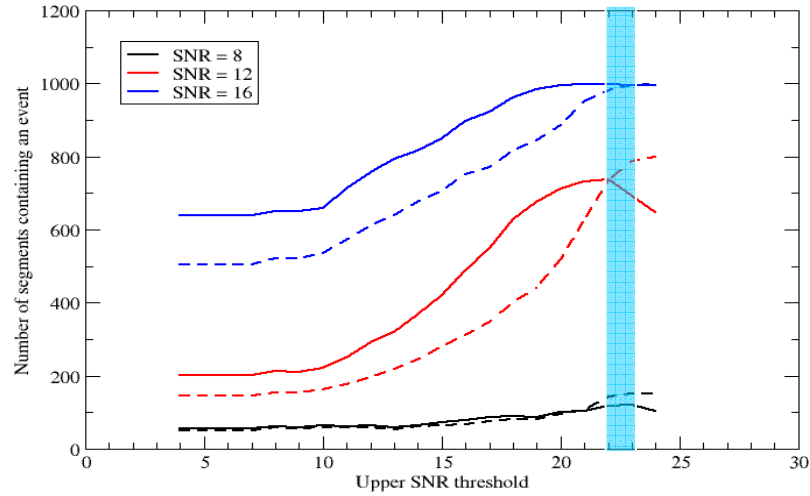
(10-40) M_{Solar}



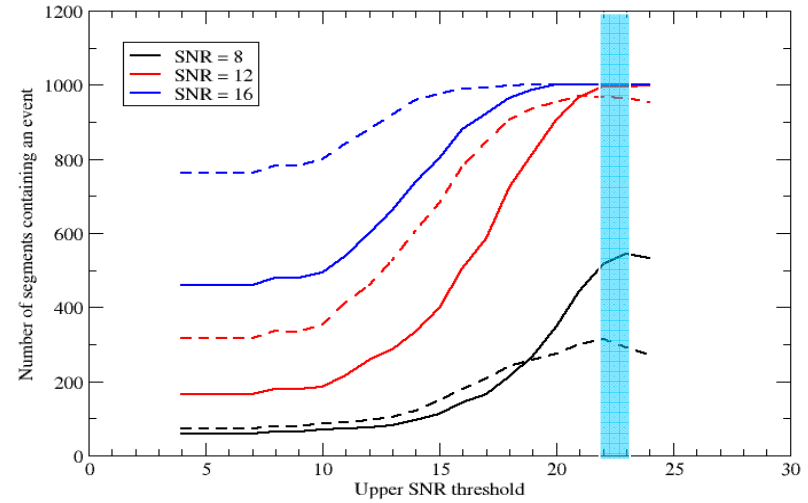
(25-25) M_{Solar}



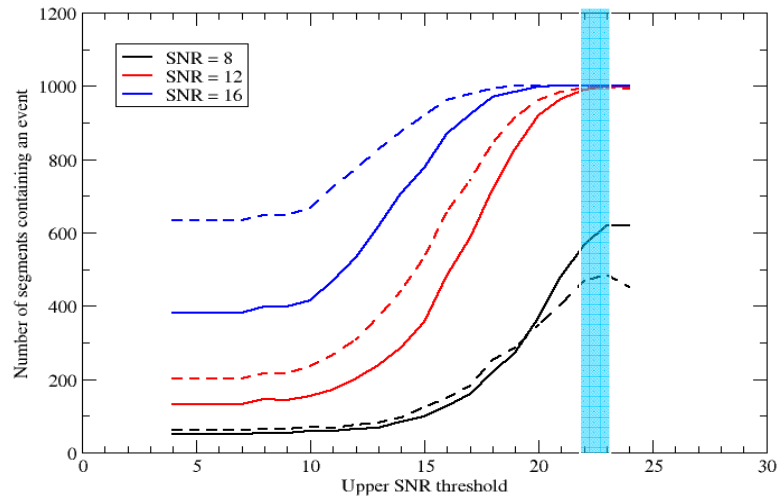
(1-49) M_{Solar}



(10-40) M_{Solar}



(25-25) M_{Solar}



$$\eta_{\text{upper}} = 23$$

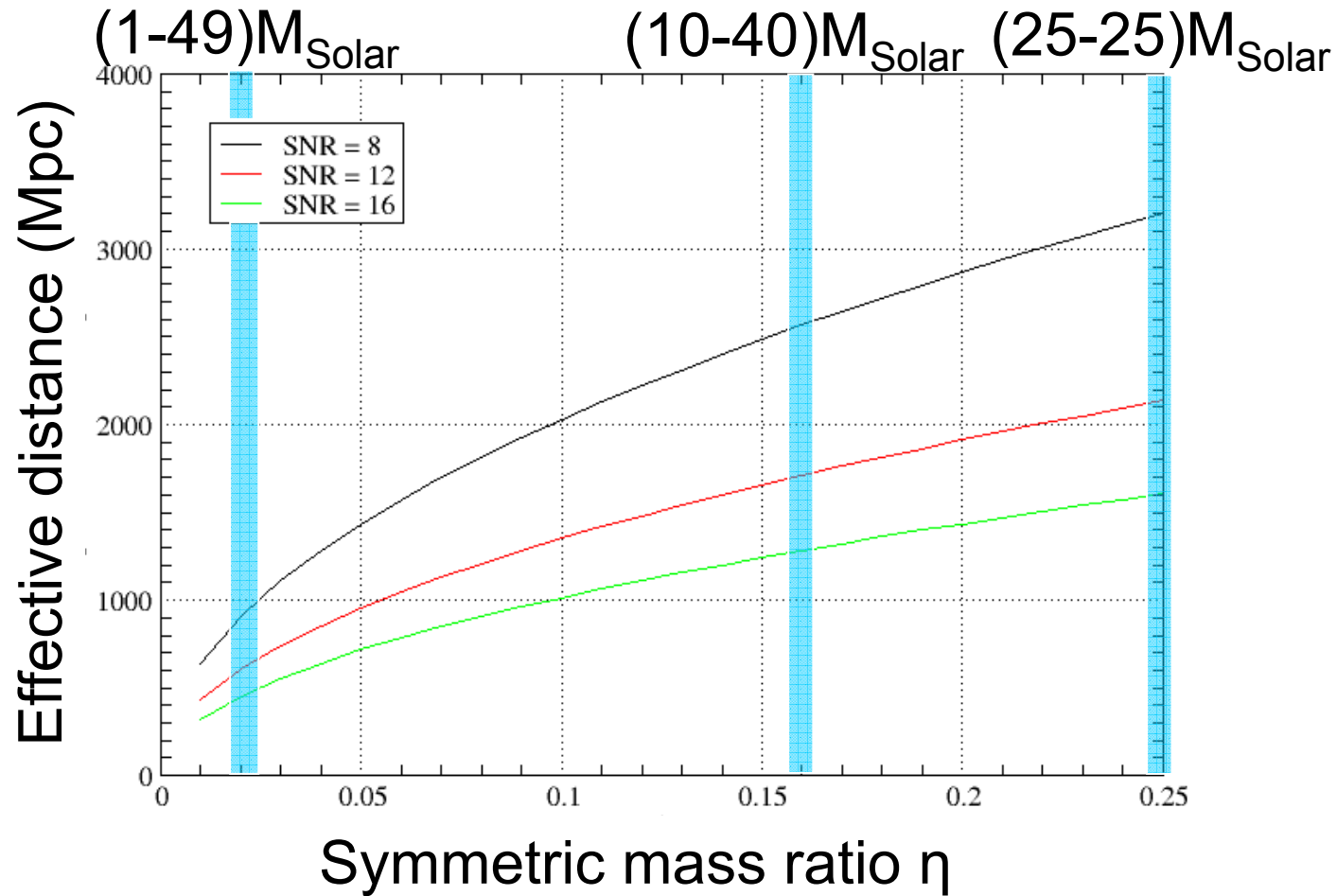
$$N_{\text{threshold}} = 50$$

Results and Conclusions

System	Effective distance (Mpc)		
	$\rho = 8$	$\rho = 12$	$\rho = 16$
(1-49)	898	599	449
(10-40)	2565	1710	1283
(25-25)	3207	2138	1603

- Near certain detection of all studied systems to eff. dist. ~ 449 Mpc
- Near certain detection of $(25-25)M_{\text{Solar}}$ binaries to eff. dist. ~ 2 Gpc

Span of Adv. LIGO



Future Work

- Write up for PRD
- Power law pattern matching for potential event clusters
- Tune HACR for EMRI signals in LISA (with Jonathan Gair)
- Written AddSpectrogramMon for LISA++
 - Combining LISA channels