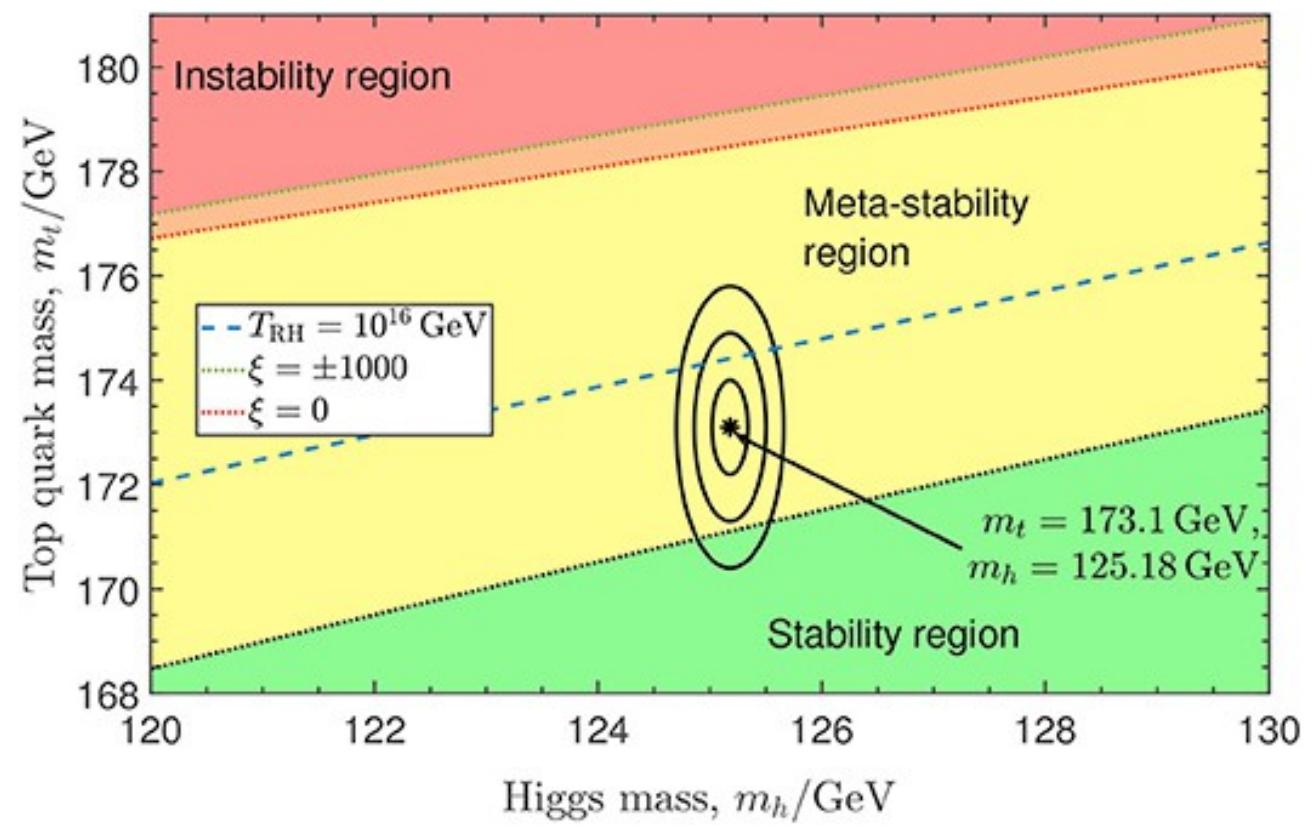


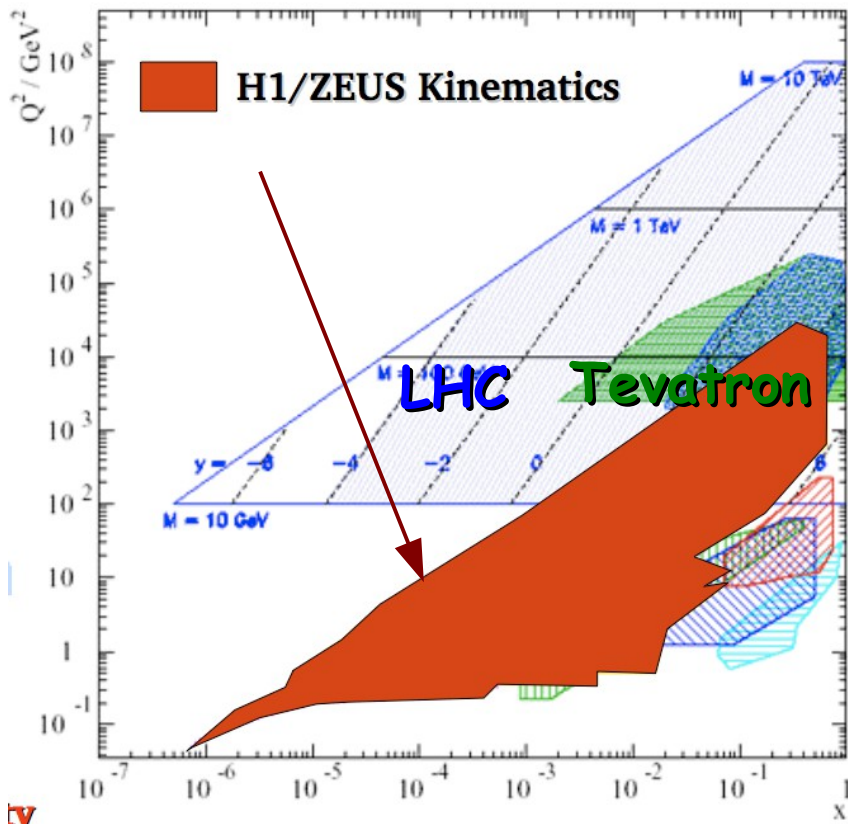
Proton structure and HERA data ...

... or rather: will we tunnel?



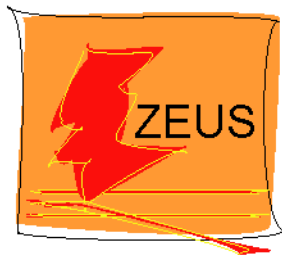
Proton structure

- PDFs used in interactions with proton: **LHC**, **Tevatron**, **HERA**
- Precision of many measurements often limited by PDF uncertainty
 - Higgs/top properties**



Inclusive measurements from HERA are core of every parton density extraction

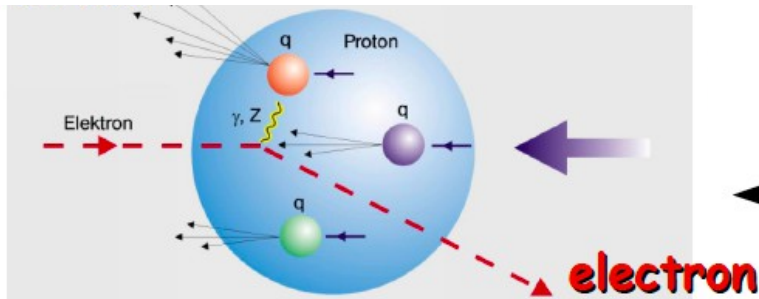
HERA accelerator



Two colliding experiments

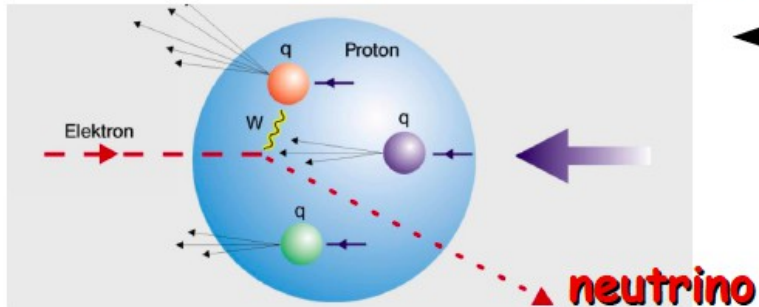


Deep Inelastic Scattering @ HERA



Neutral Current (NC)

γ, Z^0 exchange



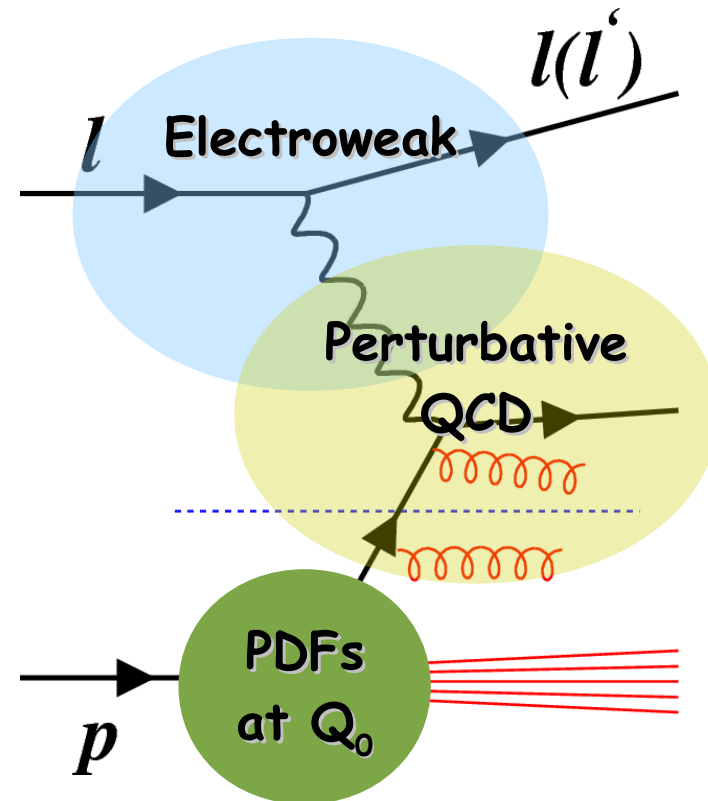
Charged Current (CC)

W^\pm exchange

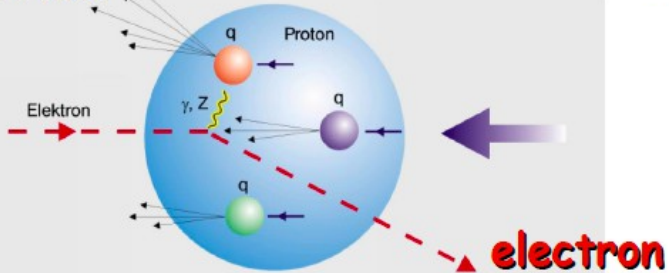
$$Q^2 = -q^2 = -(k - k')^2$$

$$x = \frac{Q^2}{2p \cdot q} \quad y = \frac{p \cdot q}{p \cdot k}$$

$$s = (p + k)^2 \quad Q^2 = x \cdot y \cdot s$$



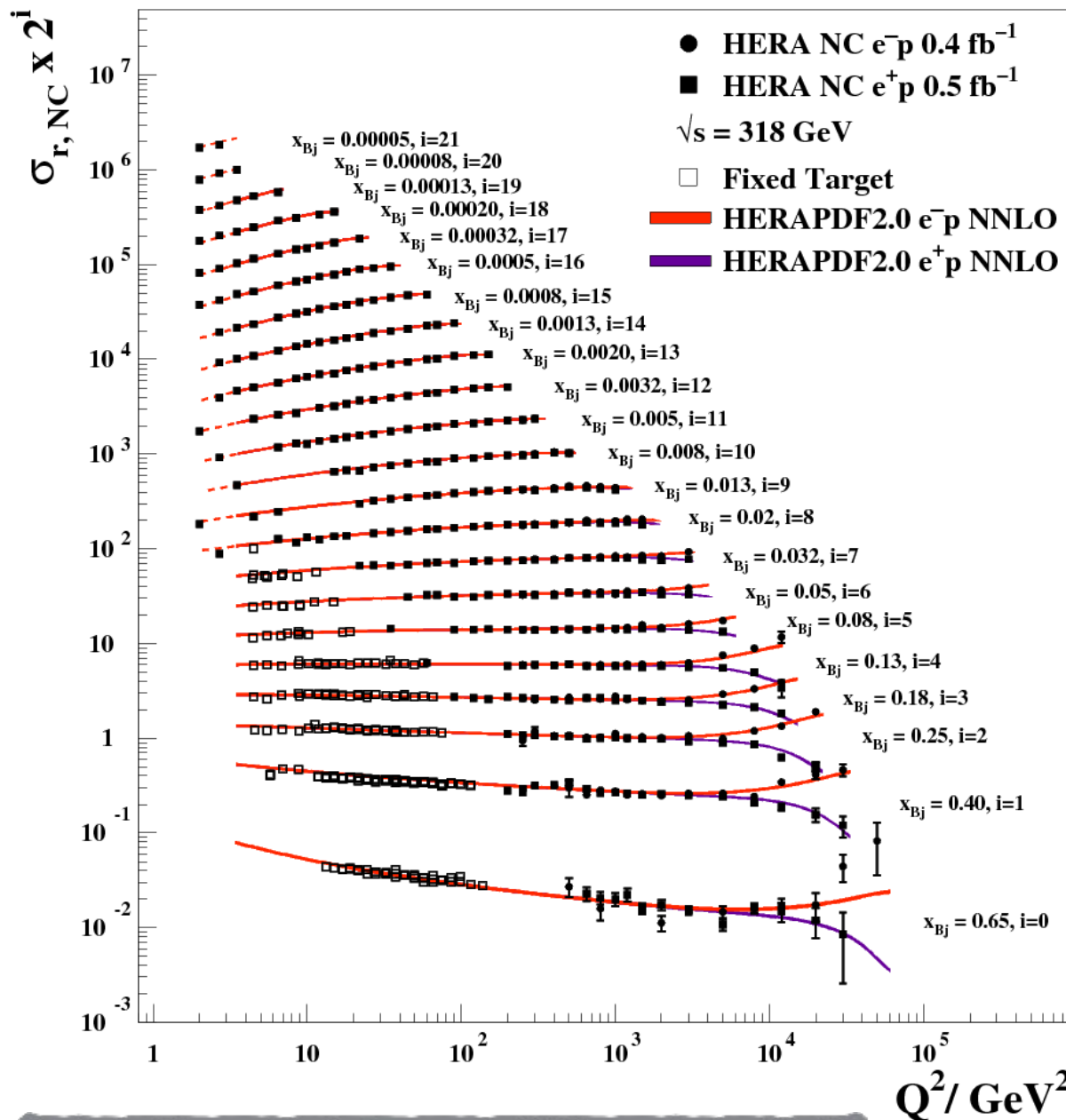
HERA combined inclusive DIS



H1 and ZEUS

HERA combined DIS data are core of every modern PDF extraction

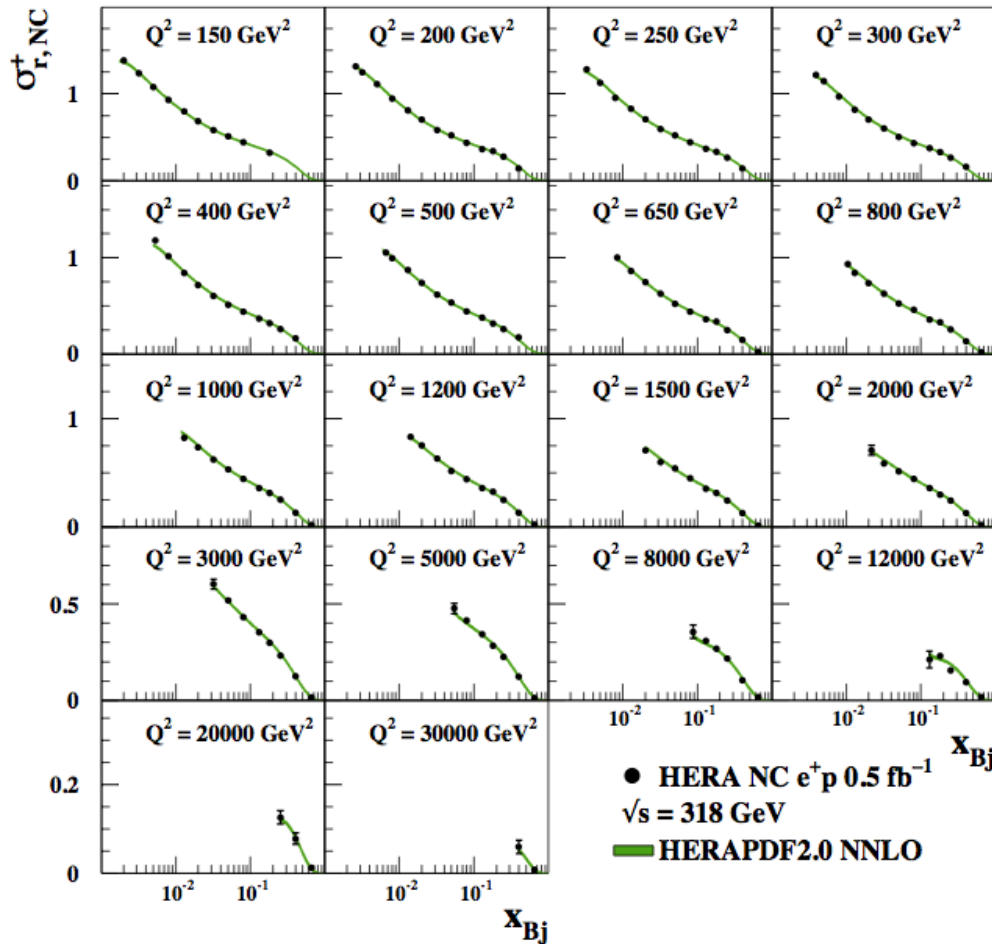
- 2927 data points combined to 1307
- Impressive precision
- Beautiful QCD and EW effects clearly seen



Neutral Current

$$\frac{d^2\sigma_{NC}^{\pm}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[Y_+ F_2 \mp Y_- xF_3 - y^2 F_L \right]$$

H1 and ZEUS



Proton structure functions

$$F_2 = x \sum e_q^2 [q(x) + \bar{q}(x)]$$

- Sensitive to quarks

$$xF_3 = x \sum 2e_q a_q [q(x) - \bar{q}(x)]$$

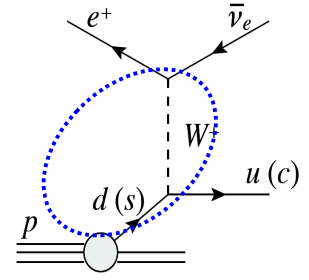
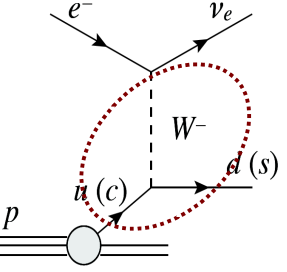
- Sensitive to valence distributions

$$F_L \sim \alpha_s x g$$

- Sensitive to gluon

- Gluon also from scaling violation and charm+jet data

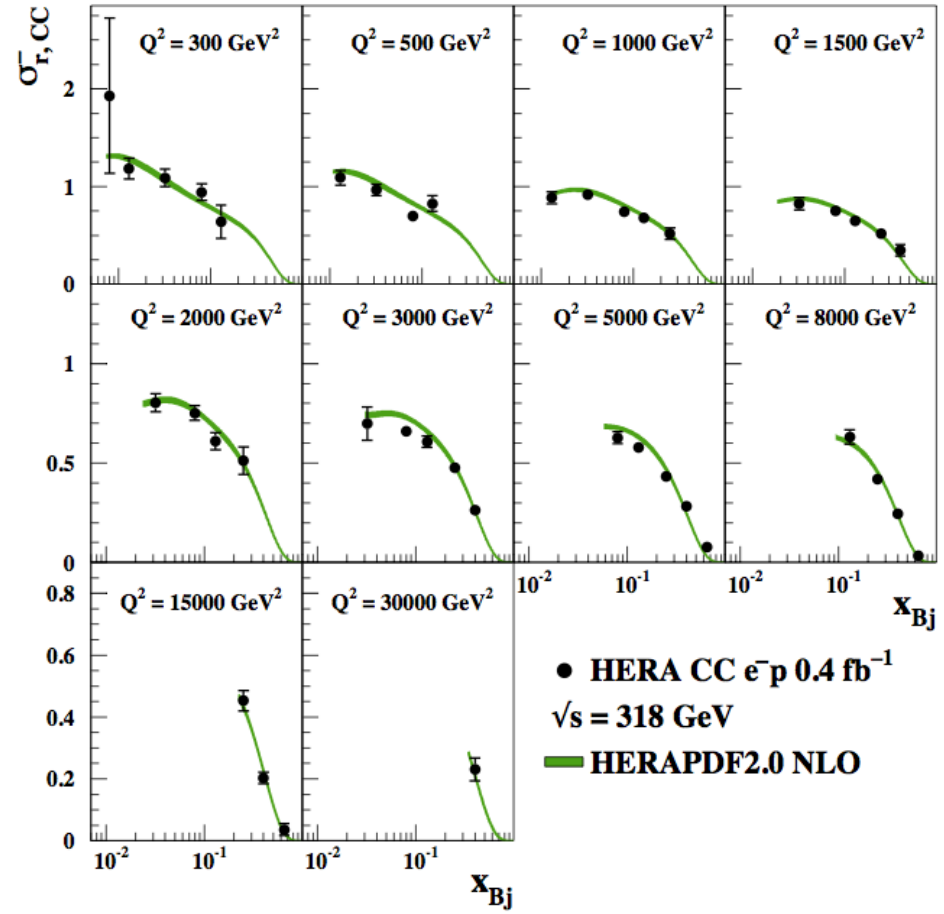
Charge Current: flavor decomposition



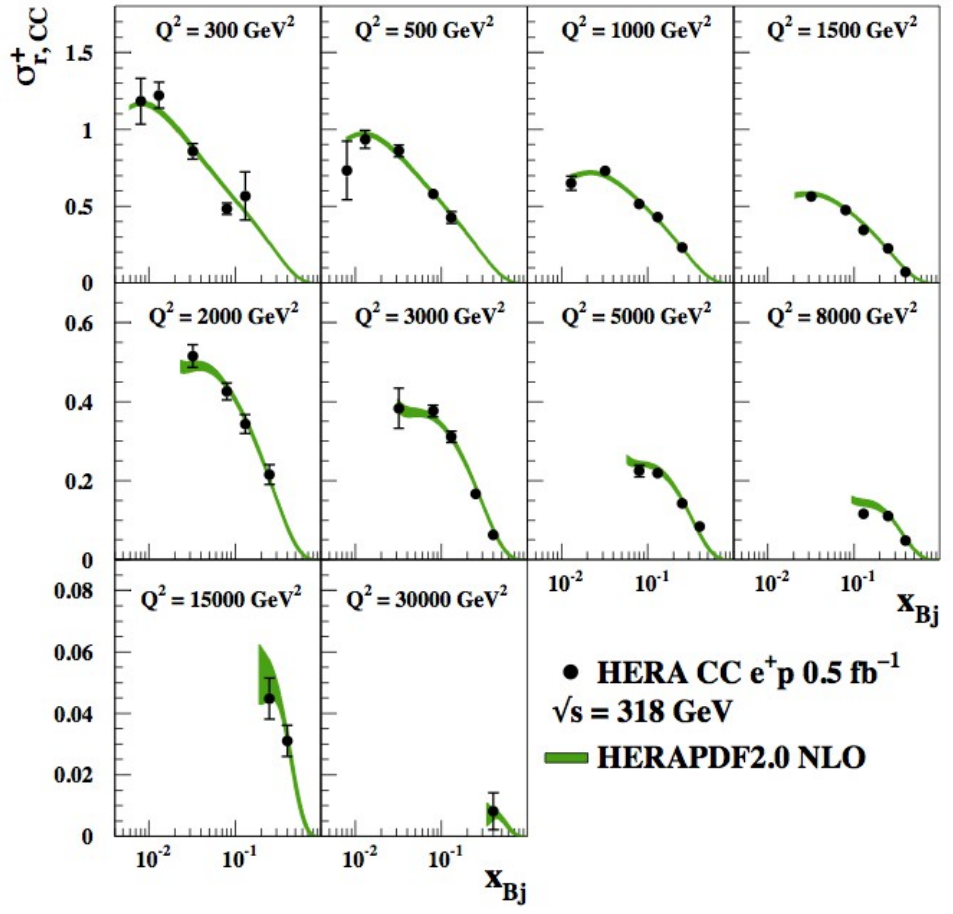
$$\sigma_{CC}^- \sim x[u + c] + x(1 - y)^2[\bar{d} + \bar{s}]$$

$$\sigma_{CC}^+ \sim x[\bar{u} + \bar{c}] + x(1 - y)^2[d + s]$$

H1 and ZEUS



H1 and ZEUS



Global analysis of parton distributions

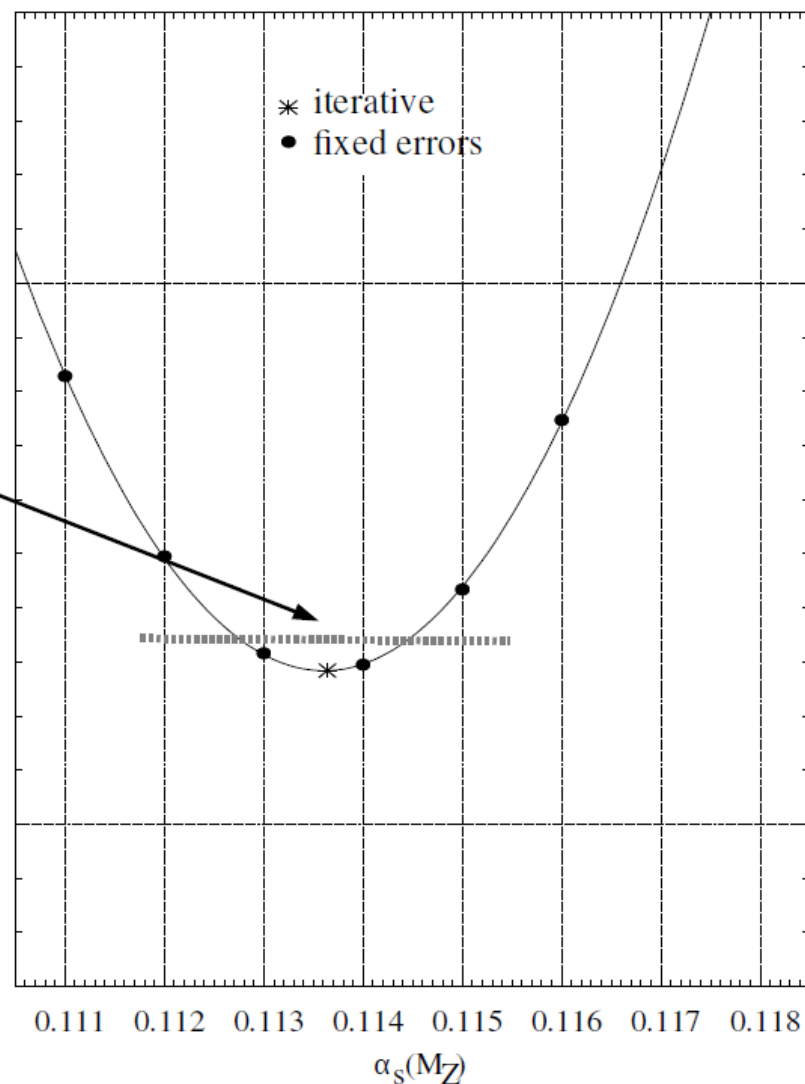
Goal: determination of the *input distributions* (for light quarks and gluons):

Method: Parametrizations $xf(x, Q_0^2) = Nx^a(1-x)^b$ function(x)
and usual *statistical estimation* (fits):

$$\chi^2(p) = \sum_{i=1}^N \left(\frac{\text{data}(i) - \text{theory}(i, p)}{\text{error}(i)} \right)^2$$

Position of minimum gives the value
and curvature gives the error (region
within a certain “tolerance” $\Delta\chi^2 = 1$)
(Monte Carlo methods can also be used)

Usually the chi-square definition is
more sophisticated, experimental
correlations are also treated, etc.



HERAPDF philosophy

HERAPDF approach uses only
HERA data in global QCD fit

HERAPDF2.0 parameterisation

$$xf(x) = Ax^B(1-x)^C(1+Dx+Ex^2)$$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

- Additional constrains

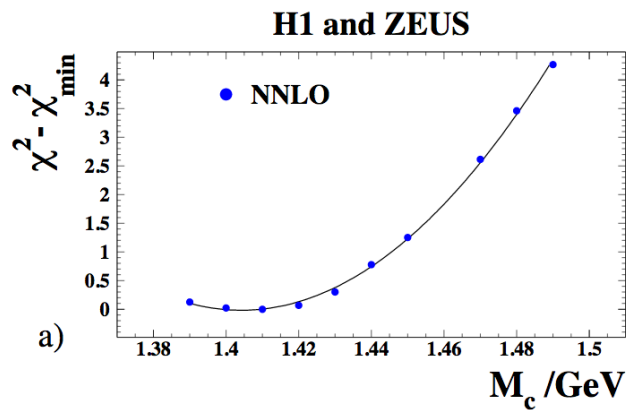
- A_{u_v}, A_{d_v}, A_g : constrained by the quark-number sum rules and momentum sum rule

- $B_{\bar{U}} = B_{\bar{D}}$:

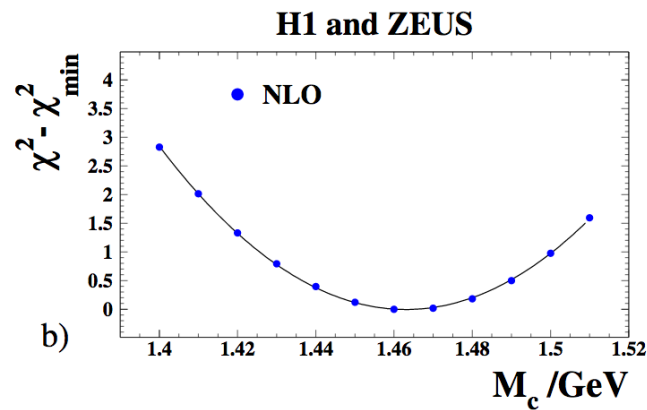
- $x\bar{s} = f_s x\bar{D}$ at starting scale, $f_s = 0.4$

Estimation of charm & beauty masses

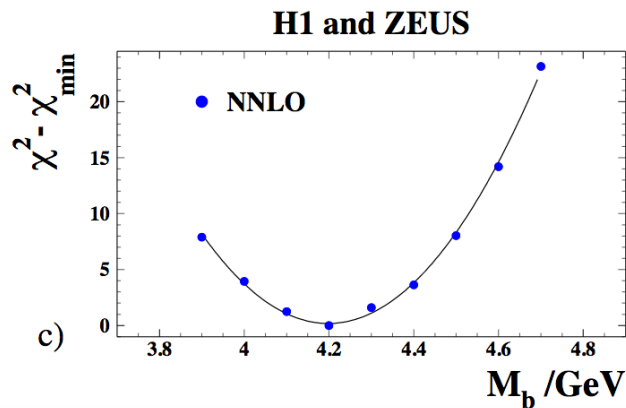
- new HERA combined charm and beauty data: EPJ C78 (2018), 473
 - updated estimation of M_c and M_b
 - Heavy Quark (HQ) coefficient functions evaluated using Thorne-Roberts Optimised Variable Flavour Number Scheme



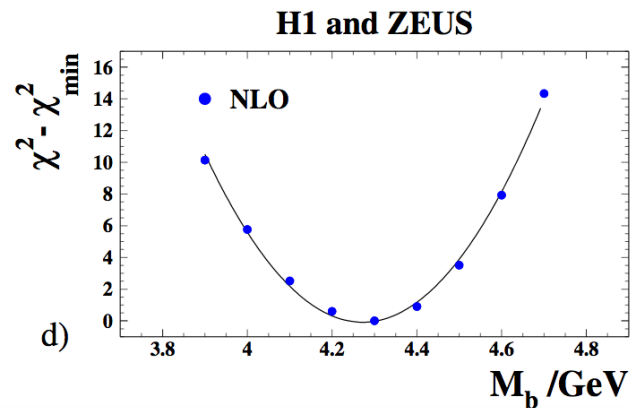
$$M_c = 1.41 \pm 0.04$$



$$M_c = 1.46 \pm 0.04$$



$$M_b = 4.2 \pm 0.1$$



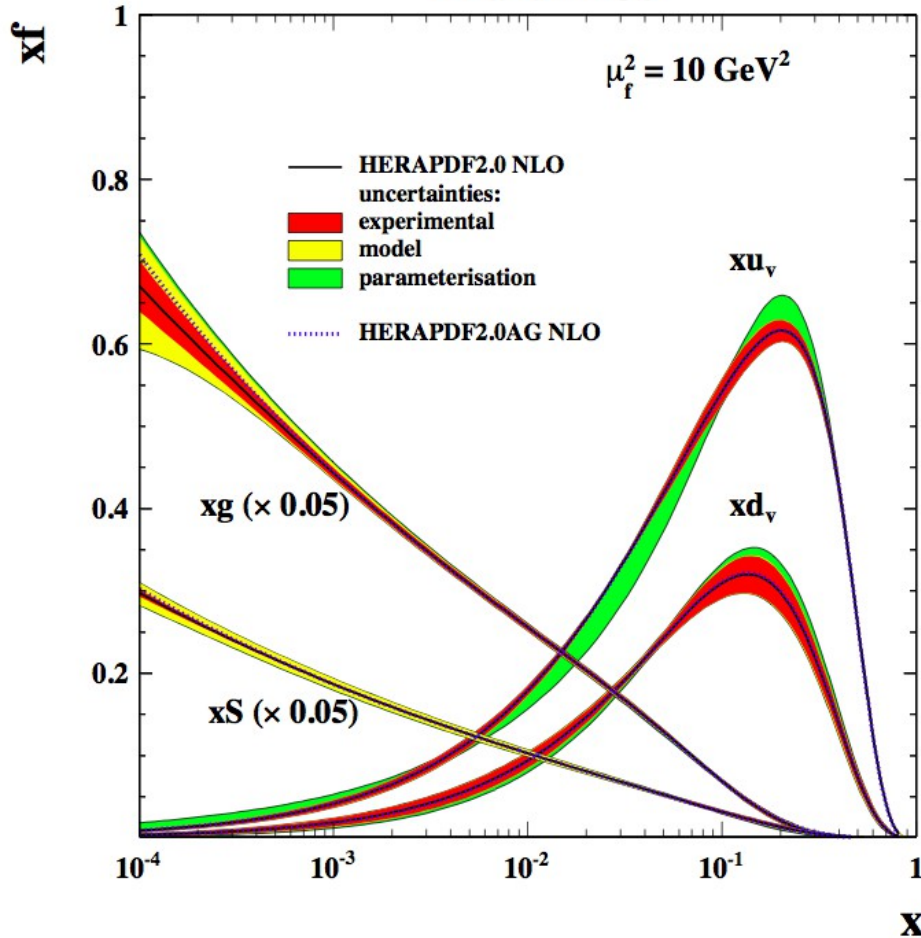
$$M_b = 4.3 \pm 0.1$$

HERAPDF2 NLO & NNLO parton densities

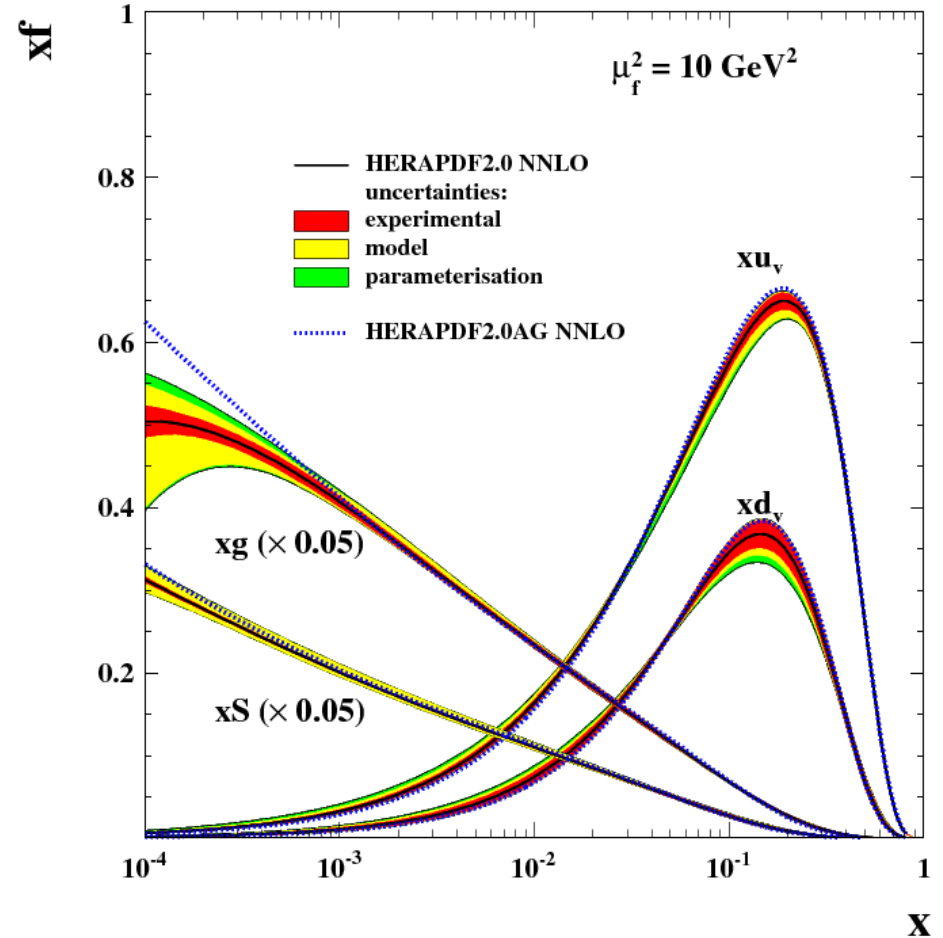
NLO

NNLO

H1 and ZEUS



H1 and ZEUS



HERAPDF2.0 extracted

with experimental, model and parametrization uncertainties

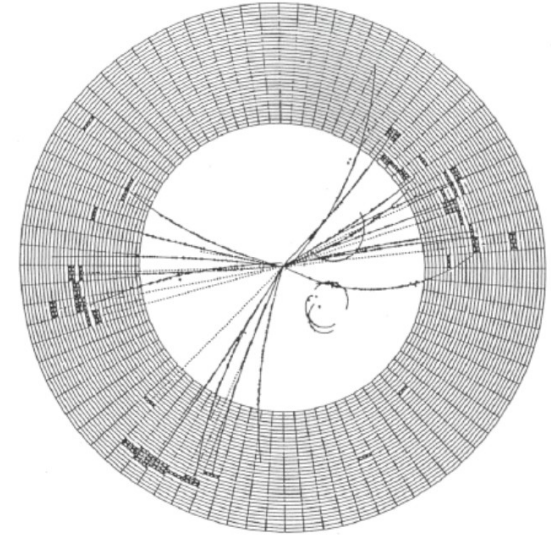
Including HERA jet data

Jets produced @ DESY for almost 45 years

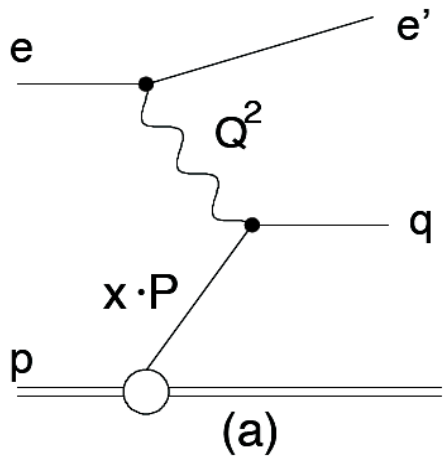
At HERA direct information on gluon and $\alpha_s(M_Z)$ comes from jet production

→ Possible simultaneous determination of parton densities and $\alpha_s(M_Z)$

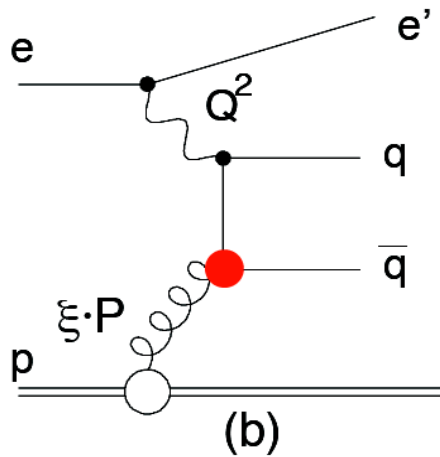
Jets at PETRA, 1979



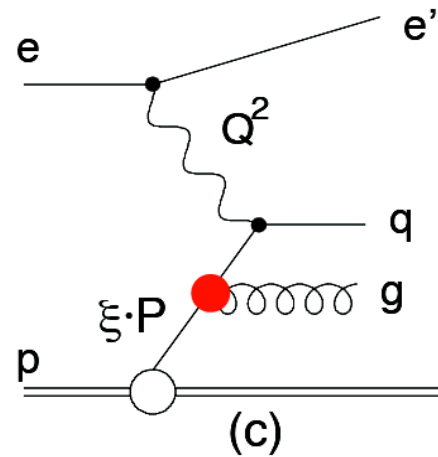
Jets at HERA



elweak coupling

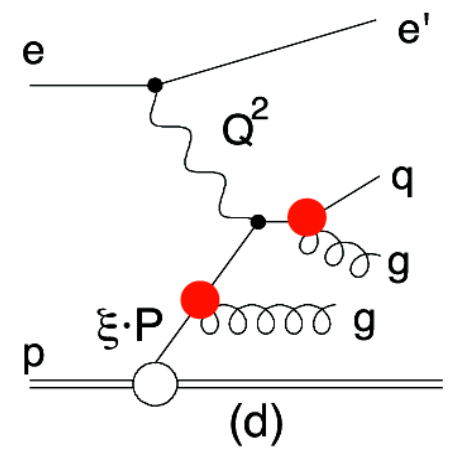


$\propto \alpha_s$



$\propto \alpha_s$

dijets

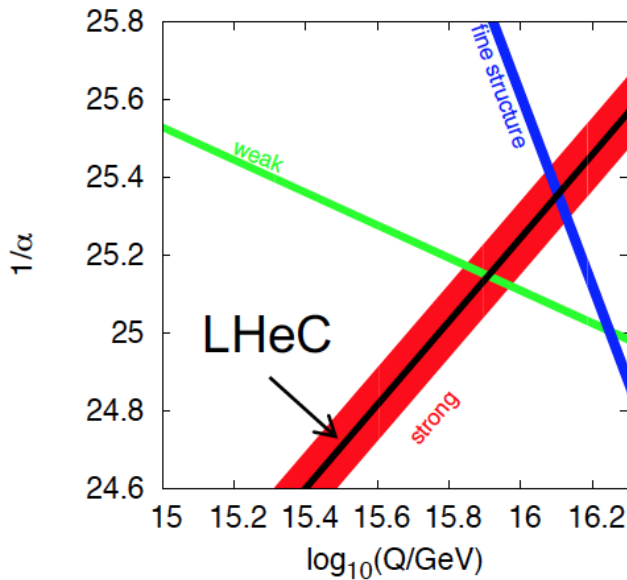


$\propto \alpha_s^2$

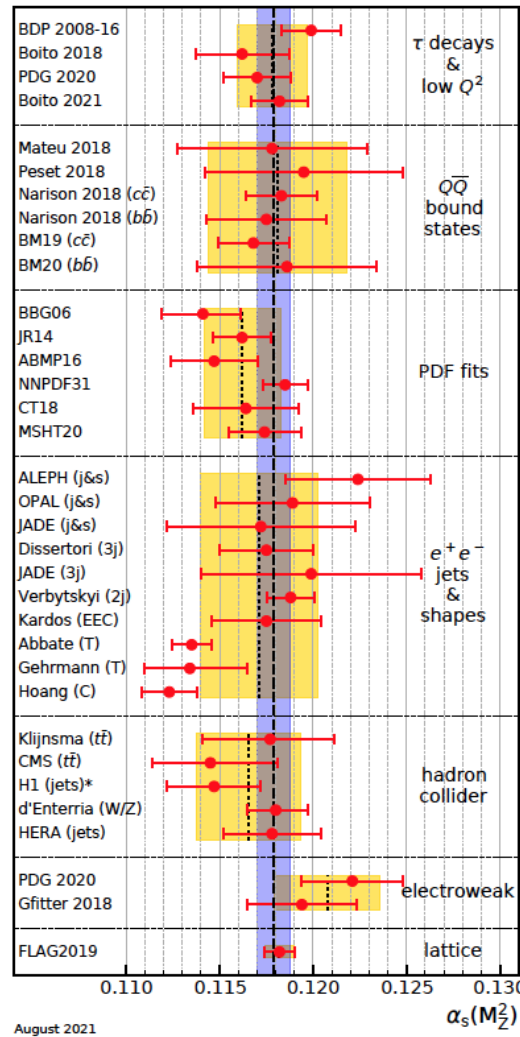
trijets

*** SUMS (GeV) *** PTOT 35.788 PTRANS 29.964 PLONG 15.788 CHARGE -2
TOTAL CLUSTER ENERGY 15.169 PHOTON ENERGY 4.693 NR OF PHOTONS 11

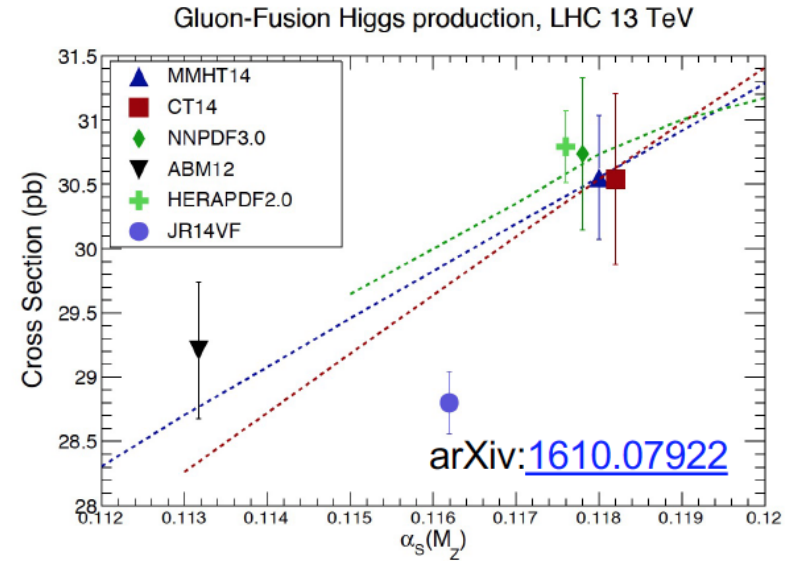
Why look at α_s ?



- α_s is least known coupling constant;
- needed to constrain GUT scenarios; cross section predictions, including Higgs;
- ...



PDG21: $\alpha_s = 0.1175 \pm 0.0010$ (w/o lattice)

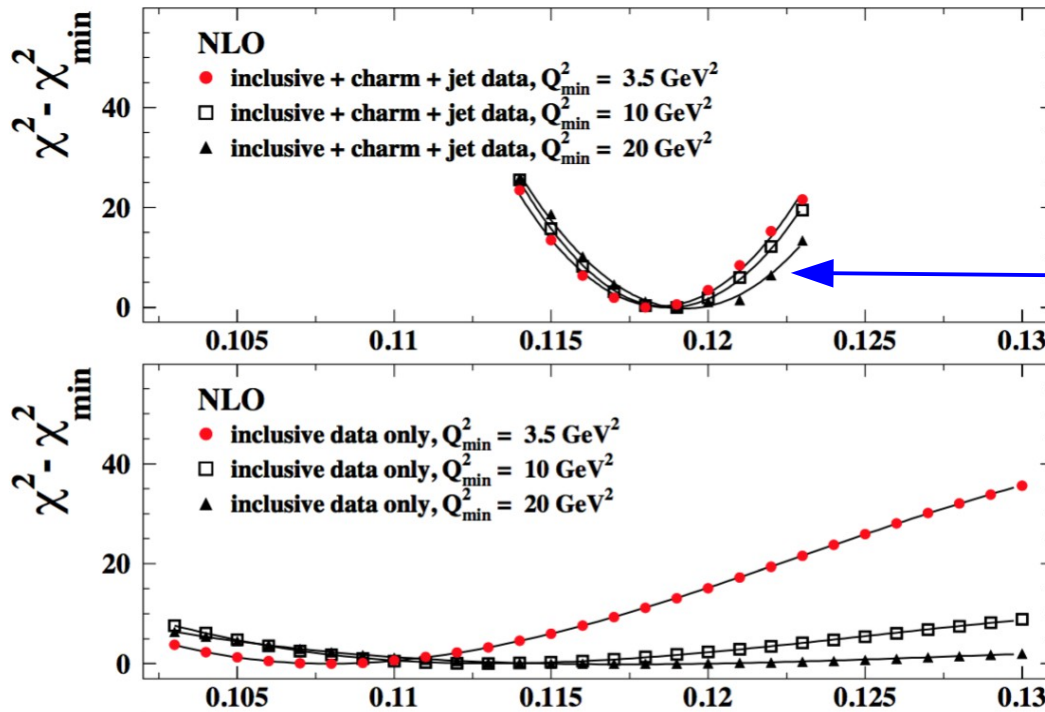


- **PDFs** and/or α_s limit: precision SM and Higgs measurements, BSM searches, ...

what is true α_s central value and uncertainty?
 new precise determinations have important role to play

Why study jets @ HERA? And anywhere else

H1 and ZEUS



- HERA inclusive data carry little information on $\alpha_s(M_Z)$
- Jet data sensitive to $\alpha_s(M_Z)$



New NNLO calculations for HERA ep jet production available now

- Implemented in FastNLO and APPELGRID → fast cross section calculation possible
- EPJ C 82, 243 (2022) arXiv:2112.01120

→ Possible simultaneous determination of PDFs and $\alpha_s(M_Z)$ at NNLO

HERA jet data used in NNLO PDF fit

EPJC C82 (2022) 243

- Inclusive jets and dijets included
- Trijets from HERAPDF2Jets NLO excluded → no NNLO predictions
- H1 low Q^2 data added - particularly sensitive to $\alpha_s(M_Z)$
- Some data points excluded due theory limitations
 - Data at low scale $\mu = (p_{t2} + Q_2) < 10 \text{ GeV}$ → scale variations are large (~25% NLO and ~10% NNLO)
 - 6 ZEUS dijet data points at low pt for which predictions are not truly NNLO

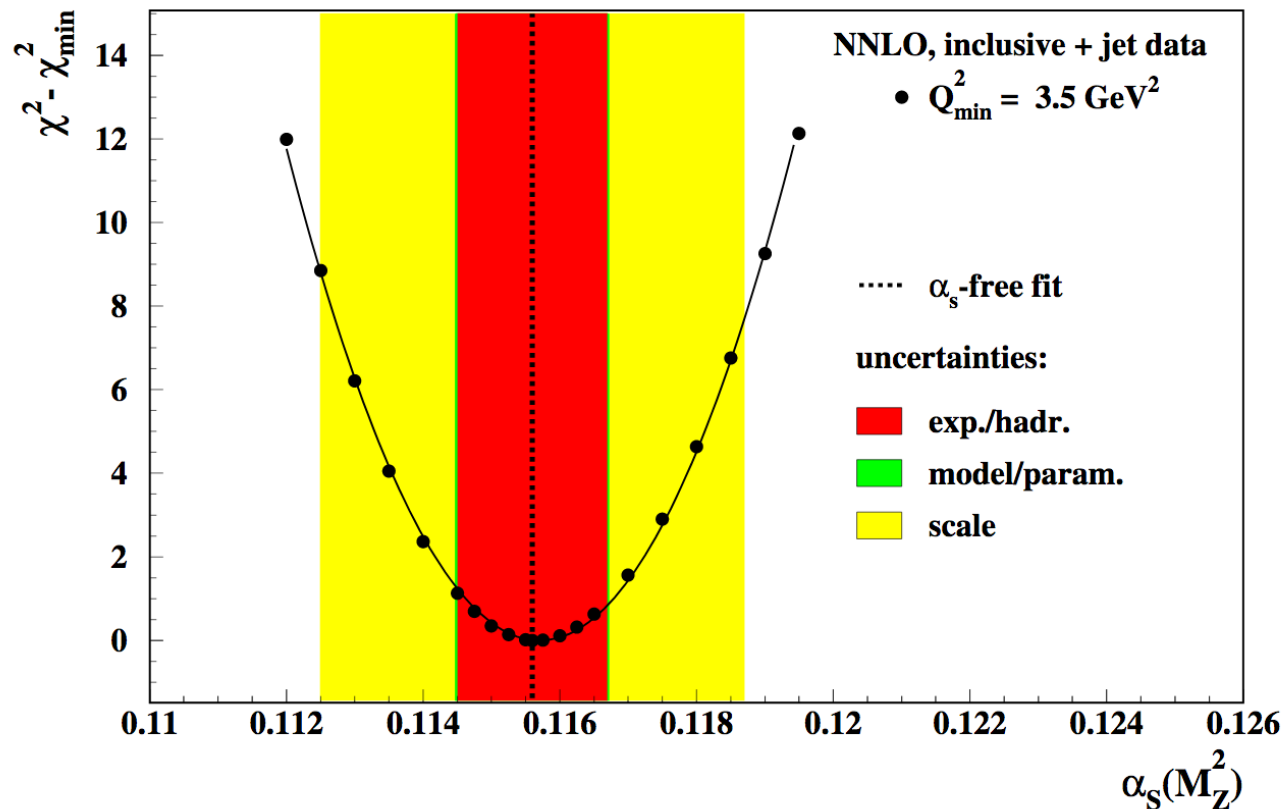
Data set	taken		$Q^2[\text{GeV}^2]$ range		\mathcal{L} pb ⁻¹	e^+/e^-	\sqrt{s} GeV	Norma- lised	All points	Used points
	from	to	from	to						
H1 HERA I normalised jets	1999	2000	150	15000	65.4	e^+p	319	yes	24	24
H1 HERA I jets at low Q^2	1999	2000	5	100	43.5	e^+p	319	no	28	20
H1 normalised inclusive jets at high Q^2	2003	2007	150	15000	351	e^+p/e^-p	319	yes	30	30
H1 normalised dijets at high Q^2	2003	2007	150	15000	351	e^+p/e^-p	319	yes	24	24
H1 normalised inclusive jets at low Q^2	2005	2007	5.5	80	290	e^+p/e^-p	319	yes	48	37
H1 normalised dijets at low Q^2	2005	2007	5.5	80	290	e^+p/e^-p	319	yes	48	37
ZEUS inclusive jets	1996	1997	125	10000	38.6	e^+p	301	no	30	30
ZEUS dijets	1998	2000 & 2004	2004	20000	374	e^+p/e^-p	318	no	22	16

- QCD PDF fit with jet data
 - With fixed $\alpha_s(M_Z)$
 - With free $\alpha_s(M_Z)$ or doing $\alpha_s(M_Z)$ scan → $\alpha_s(M_Z)$ value

α_s @ NNLO from HERA jets

- $\alpha_s(M_Z)$ determined with experimental, model, param. and hadr. uncertainties
- In fits with free $\alpha_s(M_Z)$ **scale uncertainty** important \rightarrow calculated as 100% correlated between bins and data sets

H1 and ZEUS



$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \quad {}^{+0.0001}_{-0.0002} \text{ (model + parameterisation)}$$

$$\pm 0.0029 \text{ (scale)}$$

Comparison to other HERAPDF2.0 fits

- For previous NLO results scale uncertainty applied as 50% correlated and 50% uncorrelated between bins and data sets (due to inclusion of HQ and trijet data)
- Using the previous procedure at NNLO:

NNLO

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \begin{matrix} +0.0001 \\ -0.0002 \end{matrix} \text{ (model + parameterisation)}$$

$$\pm 0.0022$$

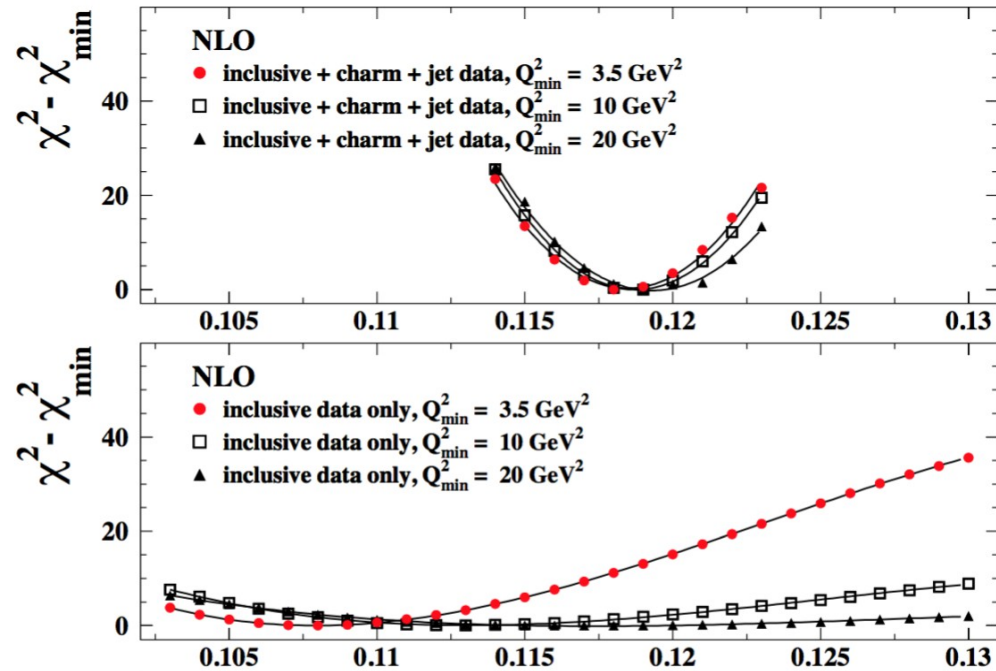
HERAPDF2.0Jets NLO

$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 \text{ (exp)} \pm 0.0005 \text{ (model/parameterisation)} \\ \pm 0.0012 \text{ (hadronisation)} \begin{matrix} +0.0037 \\ -0.0030 \end{matrix} \text{ (scale)} .$$

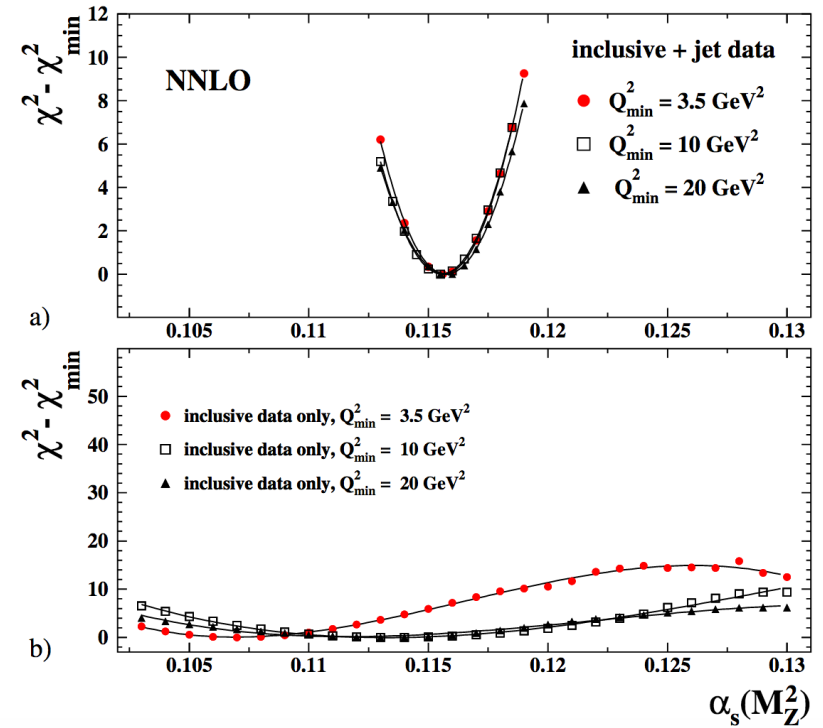
Scale uncertainties reduced
 → as expected for NNLO calculations

Completing NLO picture

H1 and ZEUS



H1 and ZEUS



- Similar behavior and level of precision at NLO and NNLO
- However direct comparison of 2015 and 2022 results not possible
→ different scale choice and slightly different jet data sets
- After unifying (details in backup)

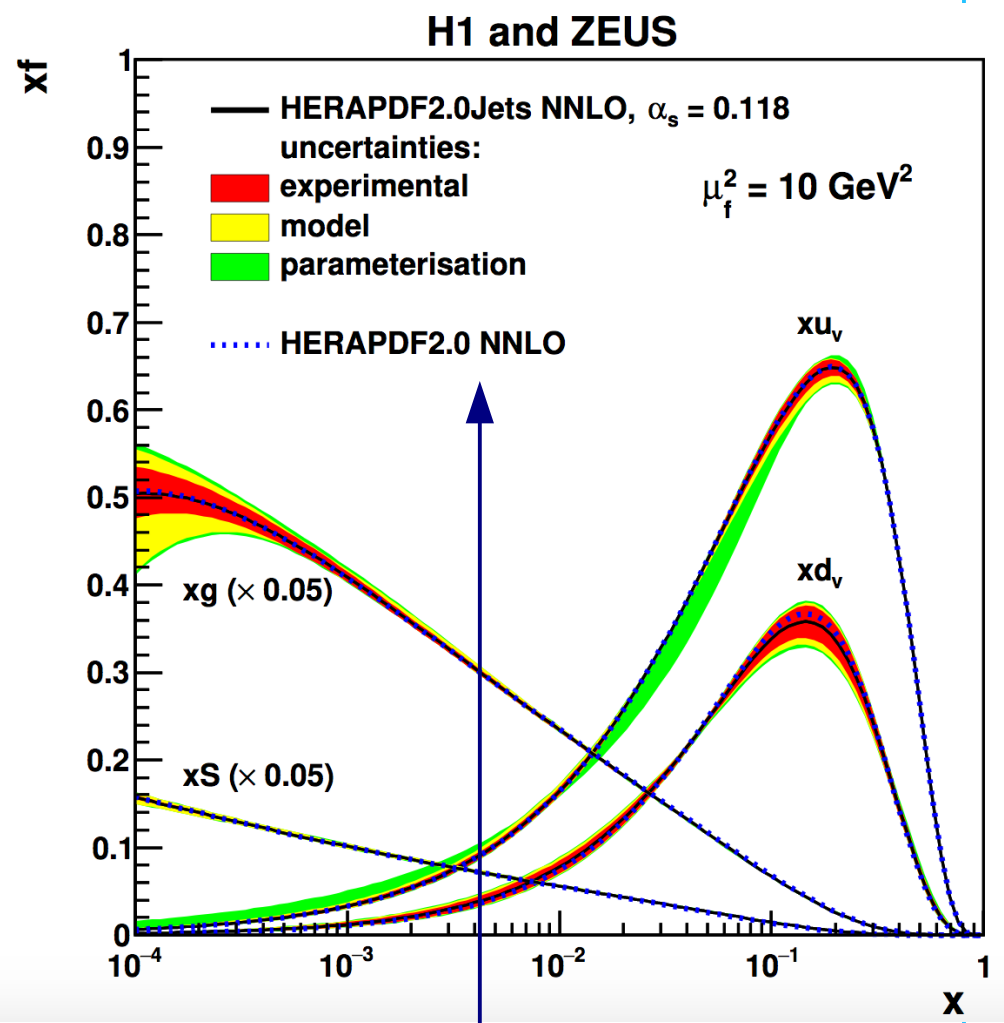
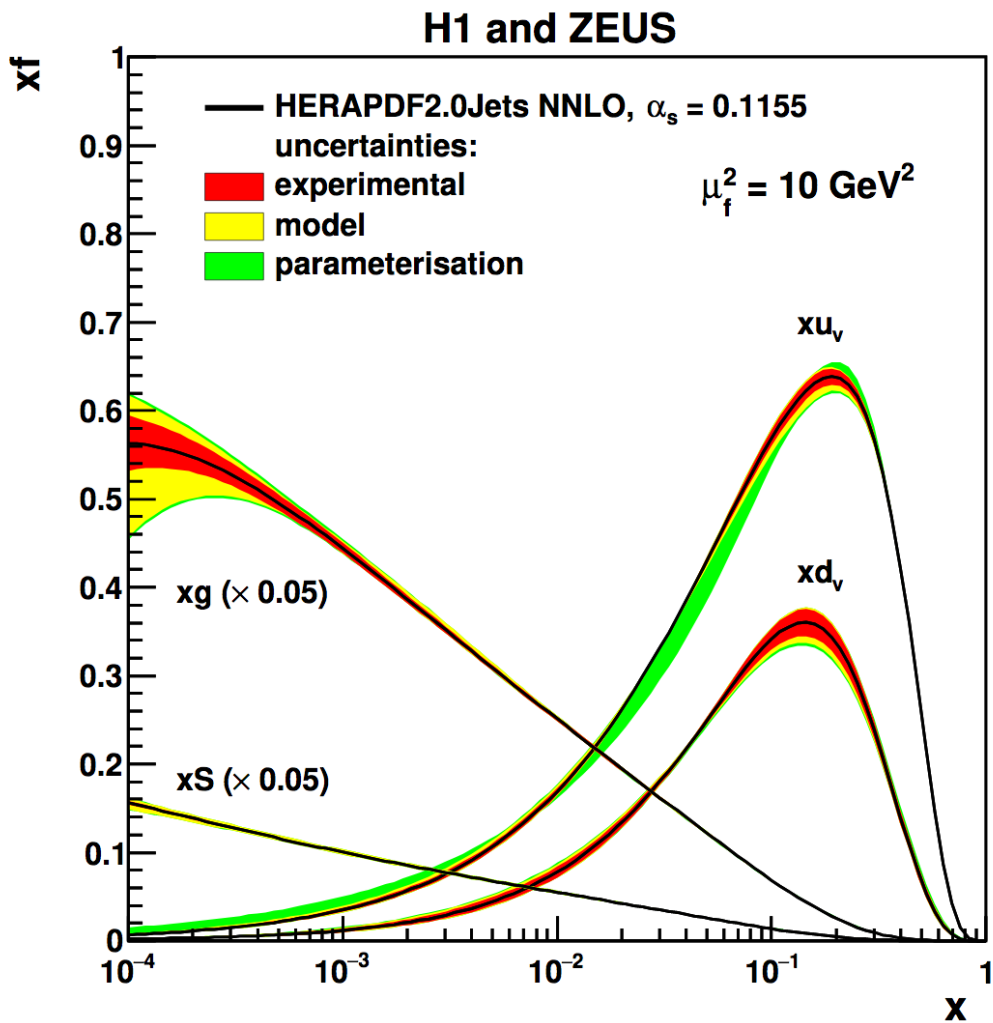
$$\alpha_s(M_Z) = 0.1186 \pm 0.0014 \text{ (exp) NLO}$$

$$\alpha_s(M_Z) = 0.1144 \pm 0.0013 \text{ (exp) NNLO}$$

Fits with fixed α_s

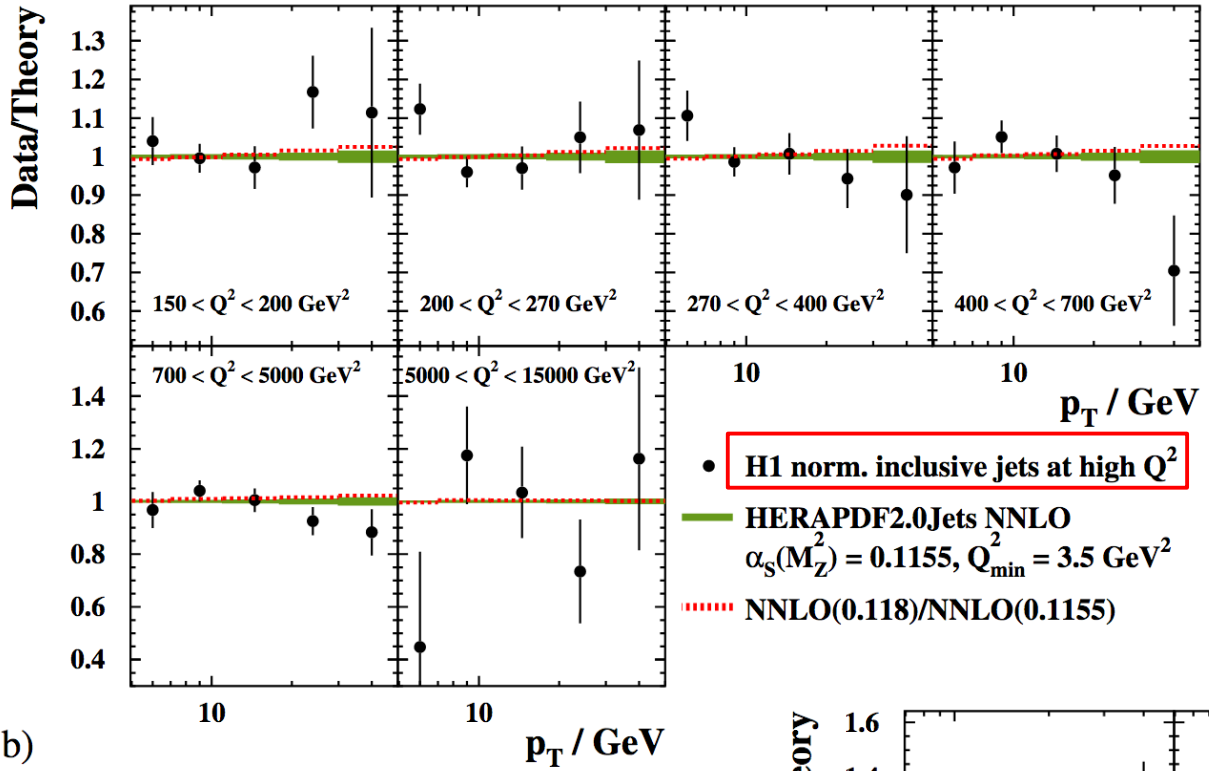
0.1155

0.118



compatible with HERAPDF2 NNLO

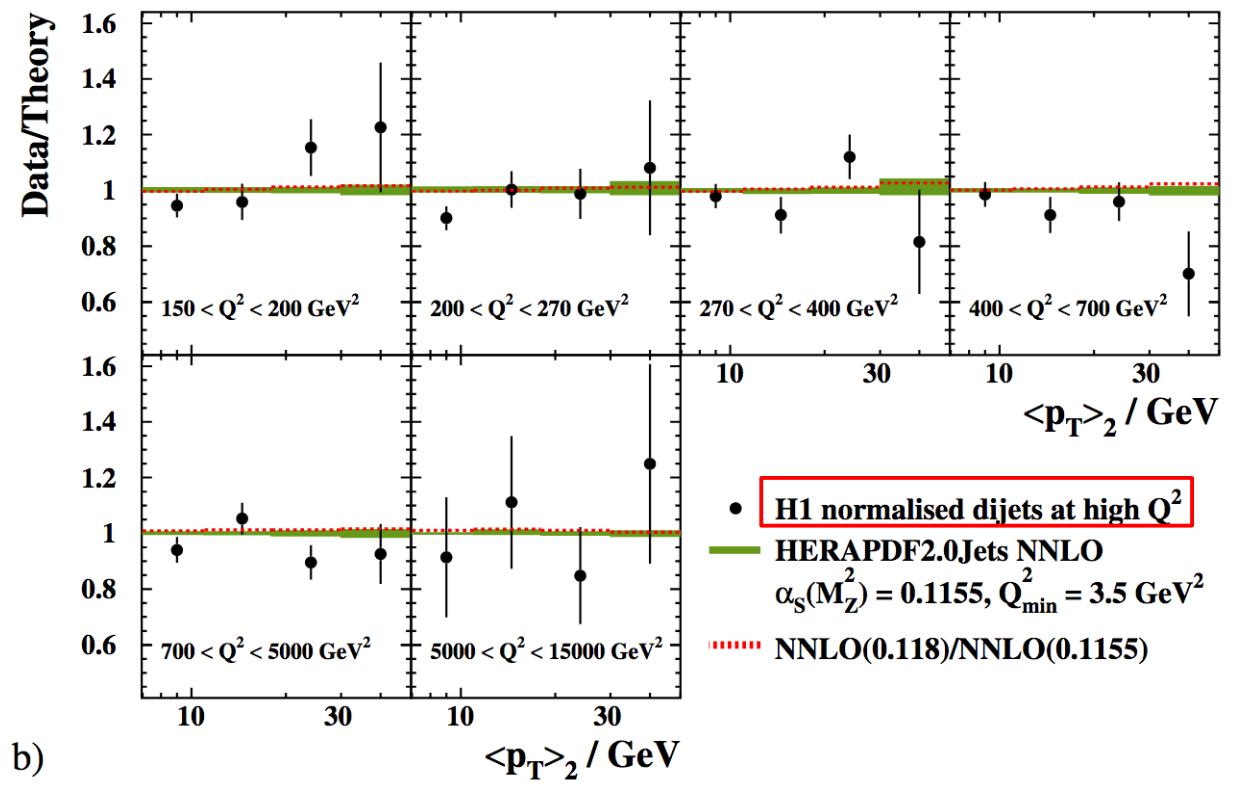
H1 and ZEUS



Comparison of theory predictions to H1 HERA II normalised jets @ high Q^2
 → good agreement for all data used in PDF fits

b)

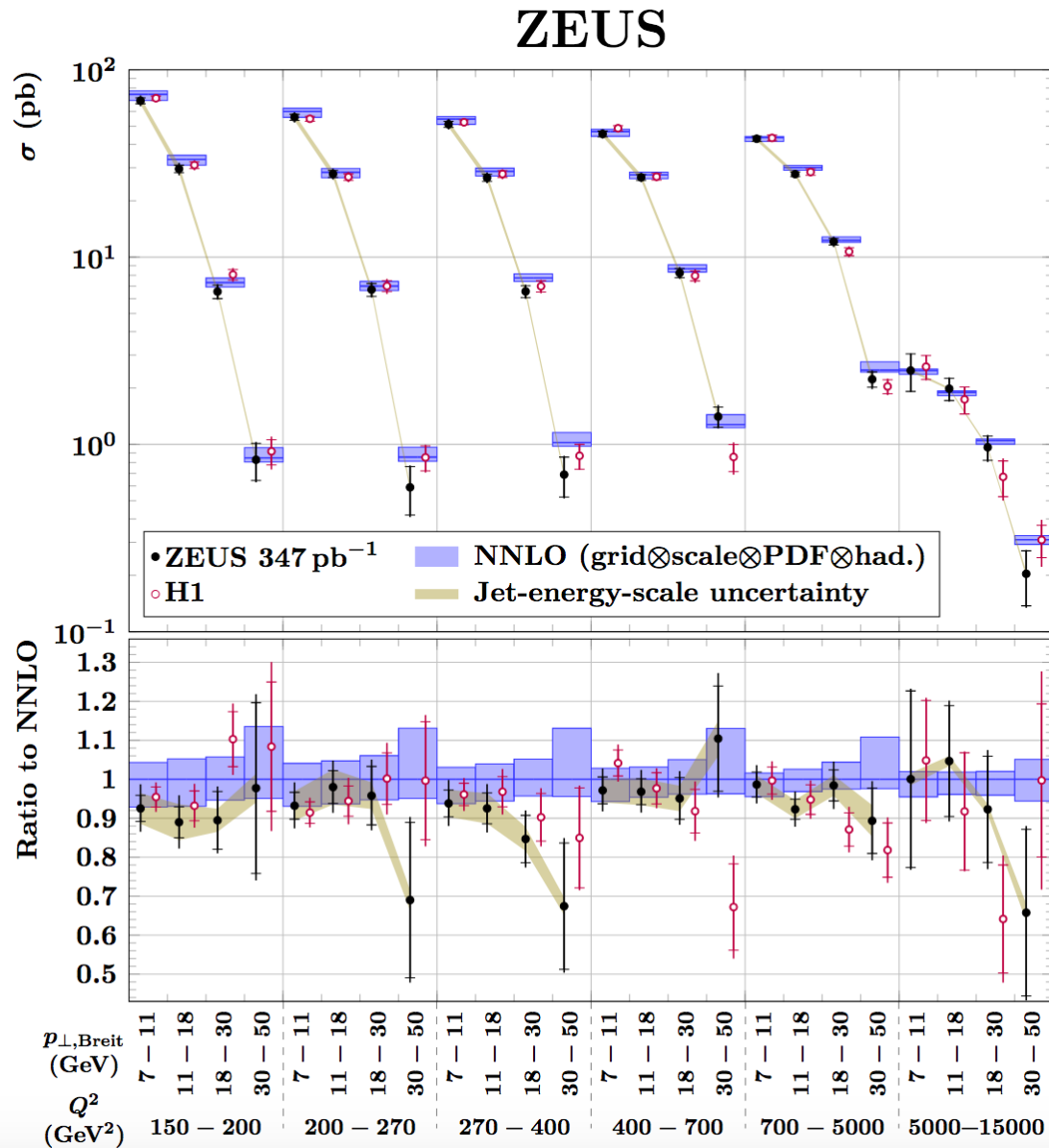
H1 and ZEUS



b)

New ZEUS jet measurement

arxiv:2309.02889, submitted to EPJC



- New HERAII high- Q^2 inclusive jets results from ZEUS (16 years after shutdown)
- Phase-space and cuts identical to H1 high- Q^2 result → direct comparison possible

- Good agreement with H1 and with theory predictions → used in simultaneous PDF and α_s fit


ZEUS-jets QCD fit @ NNLO



- Used jet data sets
 - HERAI ZEUS inclusive jets at high Q^2
 - HERAI+II ZEUS di-jets at high Q^2
 - *New HERAII ZEUS inclusive jets at high Q^2*
- Statistical correlations between ZEUS HERAII jet data sets taken into account via correlation matrix
- Fit method and settings follow exactly HERAPDF2 strategy

Results

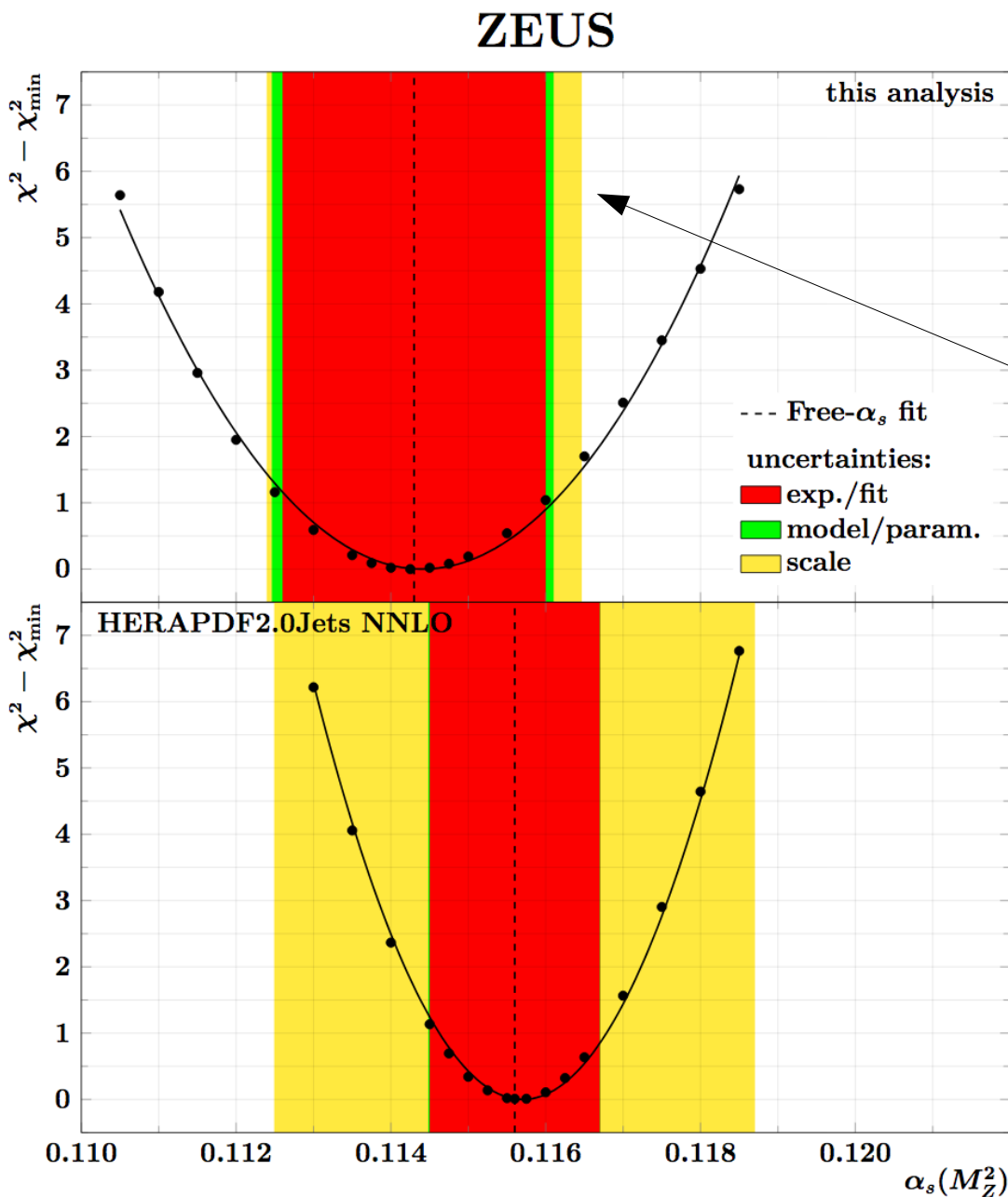
$$\alpha_s(M_Z^2) = 0.1142 \pm 0.0017 \text{ (exp./fit)} \begin{matrix} +0.0006 \\ -0.0007 \end{matrix} \text{ (model/parameterisation)} \begin{matrix} +0.0006 \\ -0.0004 \end{matrix} \text{ (scale)}$$

- *Note scale uncertainty!* 
- Calculated as 50%-correlated and 50%-uncorrelated

$$\text{NNLO: } \alpha_s(M_Z^2) = 0.1142 \pm 0.0017 \text{ (exp./fit)} \begin{matrix} +0.0006 \\ -0.0007 \end{matrix} \text{ (model/param.)} \begin{matrix} +0.0006 \\ -0.0004 \end{matrix} \text{ (scale)}$$

$$\text{NLO: } \alpha_s(M_Z^2) = 0.1159 \pm 0.0017 \text{ (exp./fit)} \begin{matrix} +0.0007 \\ -0.0009 \end{matrix} \text{ (model/param.)} \begin{matrix} +0.0012 \\ -0.0009 \end{matrix} \text{ (scale)}$$

Comparison to HERAPDF2Jets NNLO



- Central value compatible with HERAPDF and world average
- Increased experimental uncertainty ← fewer jet datasets used
- Scale uncertainty here calculated as 100% correlated

$$\begin{aligned} &+0.0012 \\ &-0.0005 \end{aligned} \text{ (scale)}$$

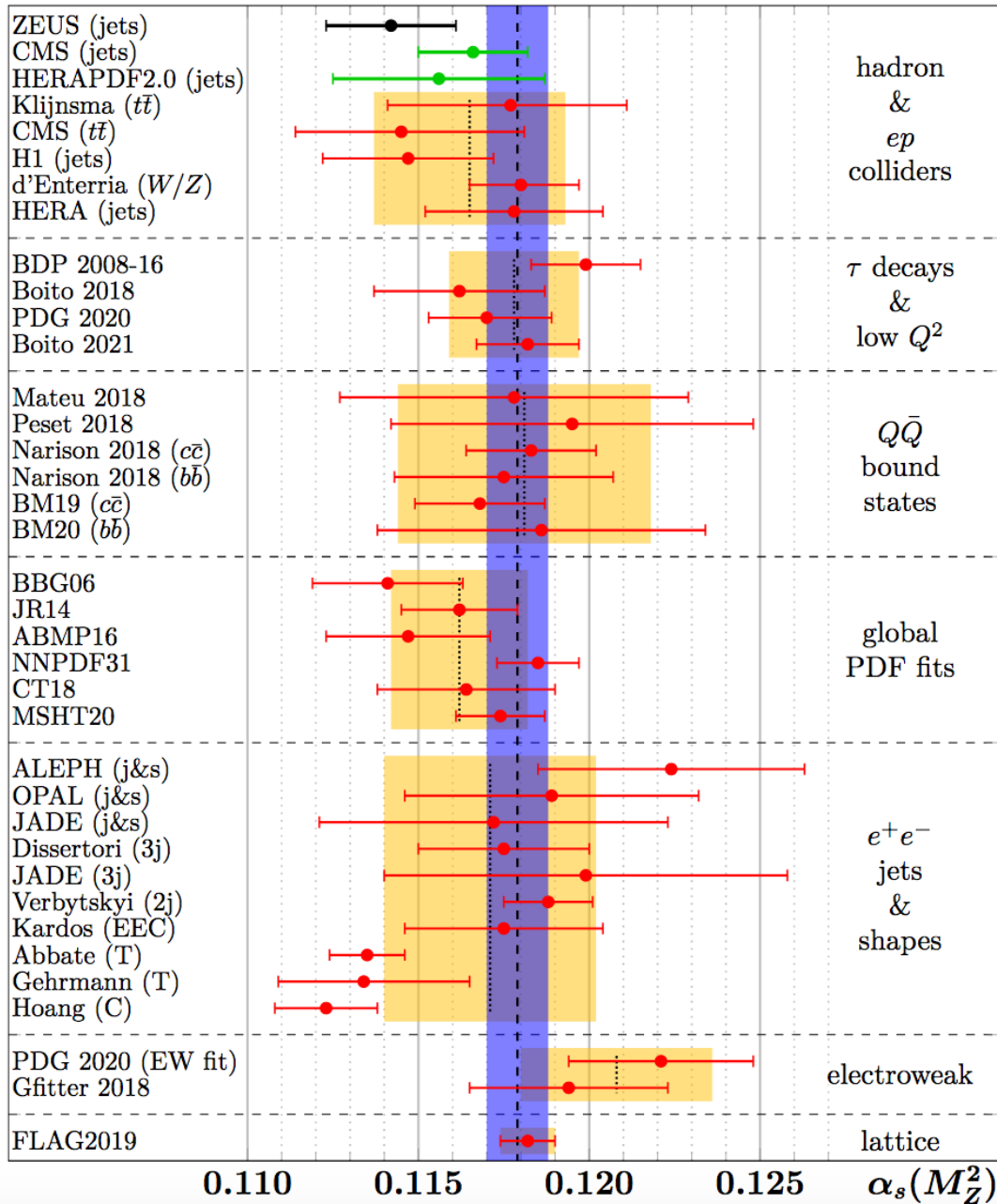
to compare to HERAPDF2Jets

Significantly decreased scale uncertainty

- absence of low Q^2 jet data
- 50%-correlated and 50%-uncorrelated uncert.

Comparison to other α_s estimations

ZEUS



Reduced scale uncertainty

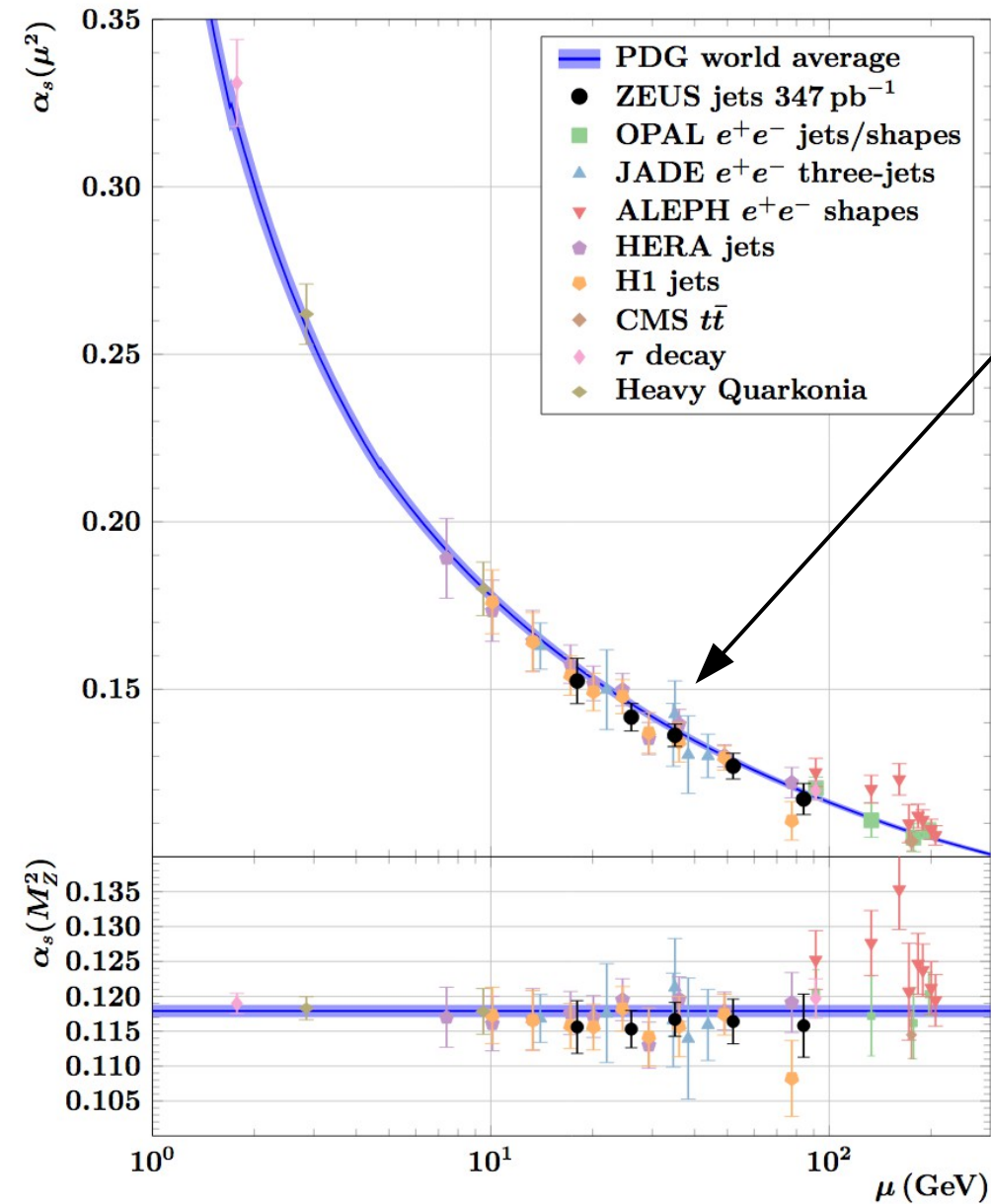


present analysis is one of the most precise measurements of $\alpha_s(M_Z^2)$ at hadron colliders so far[†]

[†]PTEP 2020, 8, 083C01 (2020)

Running of strong coupling

ZEUS



- Running of strong coupling expected from theory and confirmed by various measurements
- ZEUS measured α_s in 5 energy bins
 - All values very well compatible with result of global determination
- Measurements consistent with each other and with theory expectations

Dependence of strong coupling on energy scale consistent with previous measurements and perturbative QCD expectation

New DIS data for PDFs:

EIC

An aerial photograph showing a large circular facility, likely the Electron-Ion Collider (EIC), surrounded by a dense forest. The facility includes several buildings and a large circular structure. The text 'EIC' is overlaid in the center of the image.

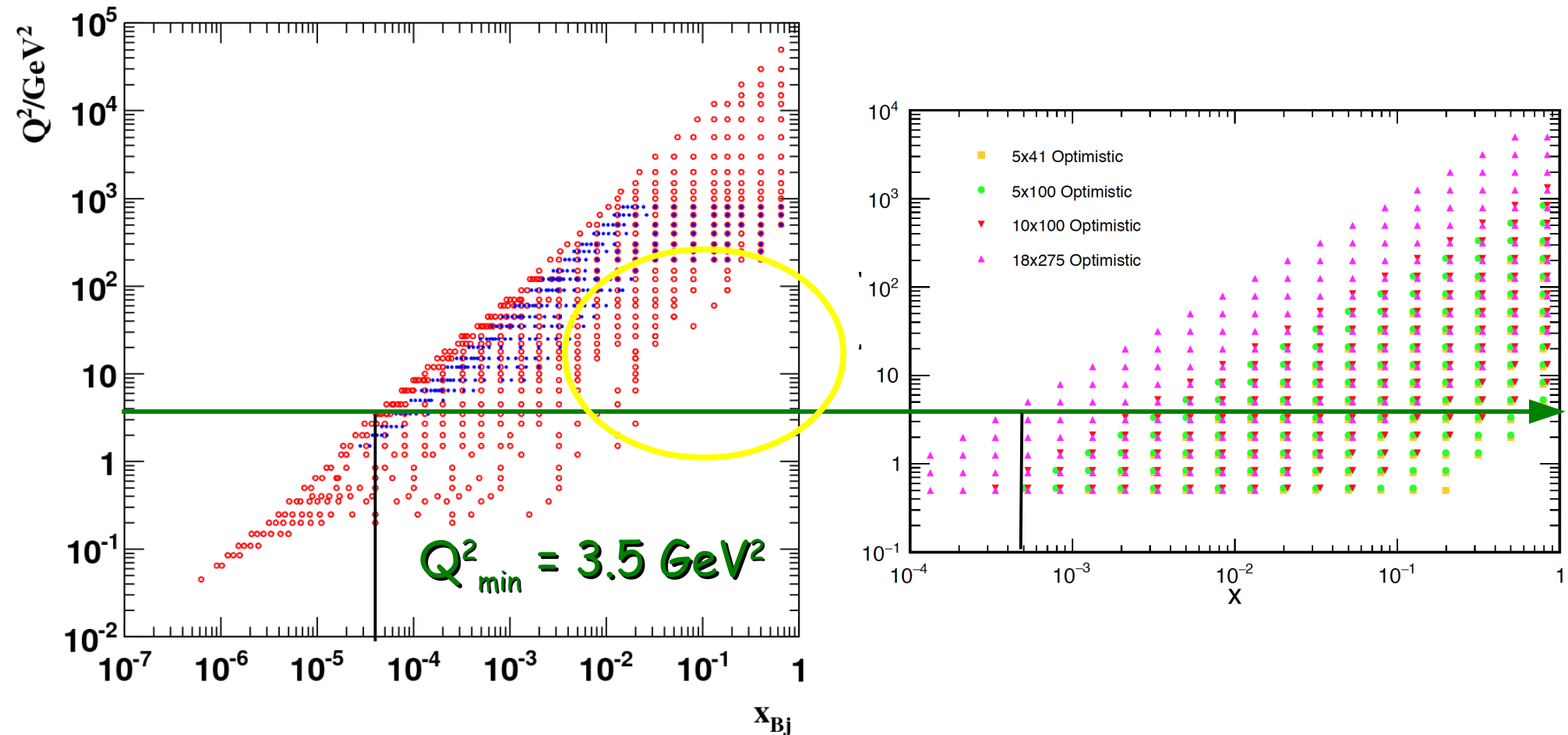
EIC & Collinear PDFs

→ sneak preview, more in F. Giuli's talk & poster on Tuesday

arXiv:2309.11269, submitted to EPJC

HERA & ATHENA phase-space

H1 and ZEUS

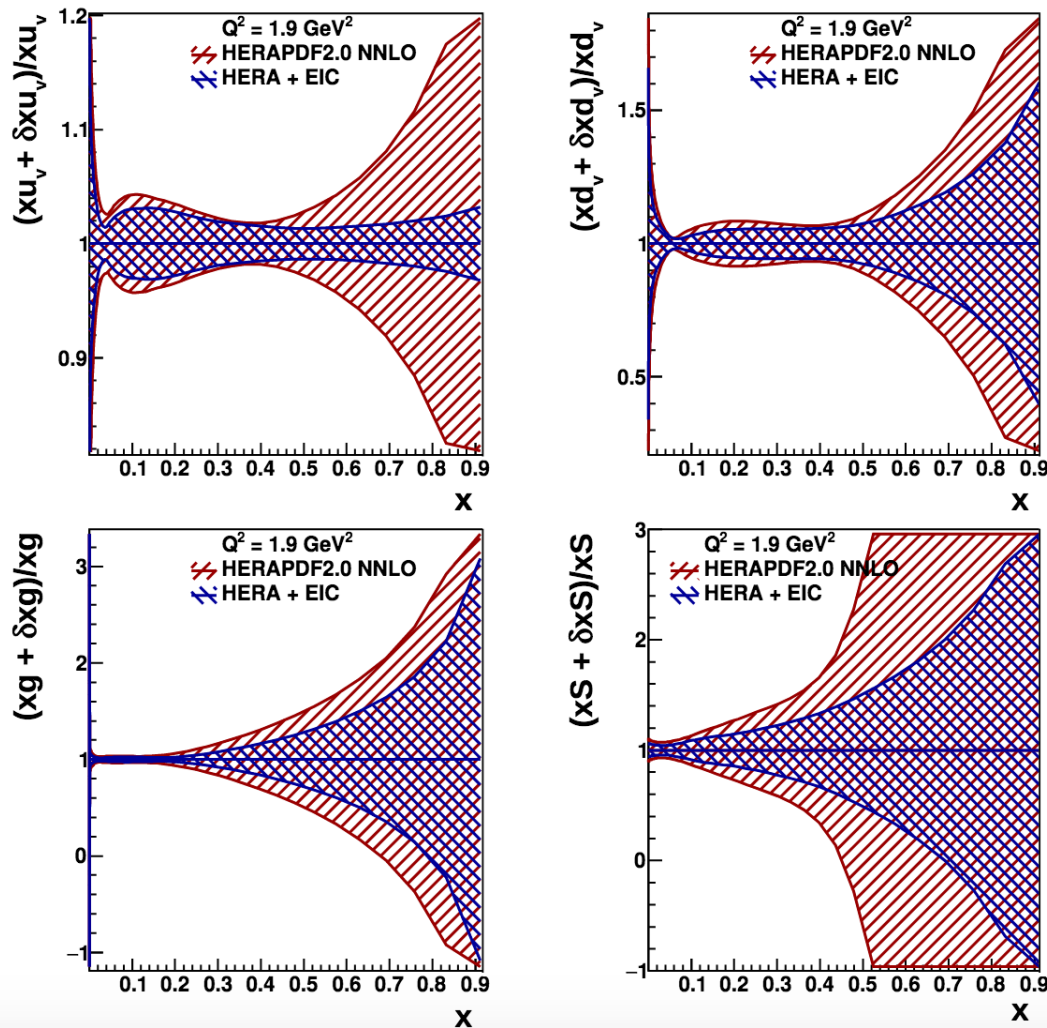


High- x region not covered by HERA → impact on high- x PDFs expected

HERAPDF philosophy: get PDFs with HERA data only

Fits with ATHENA pseudo-data

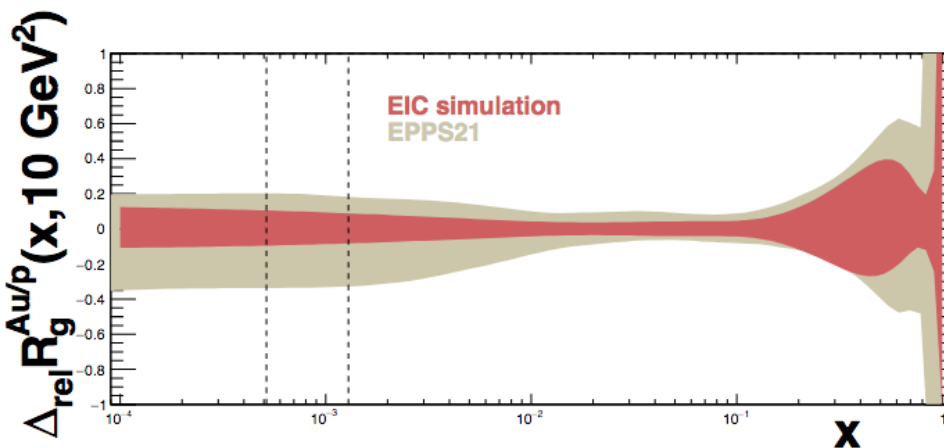
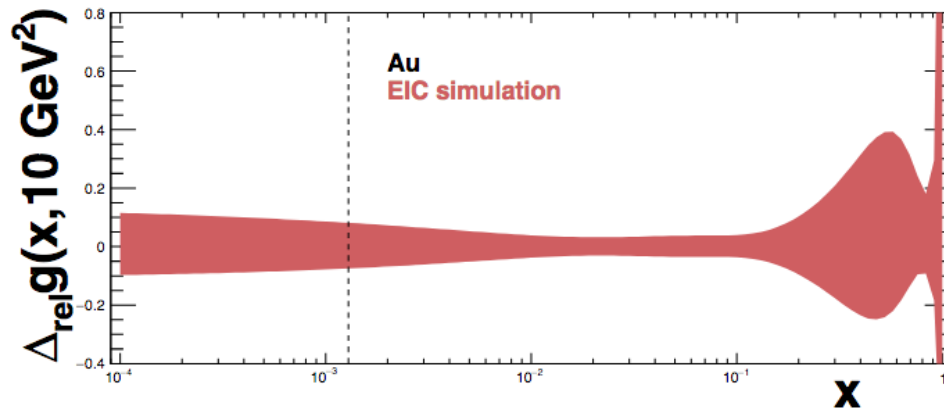
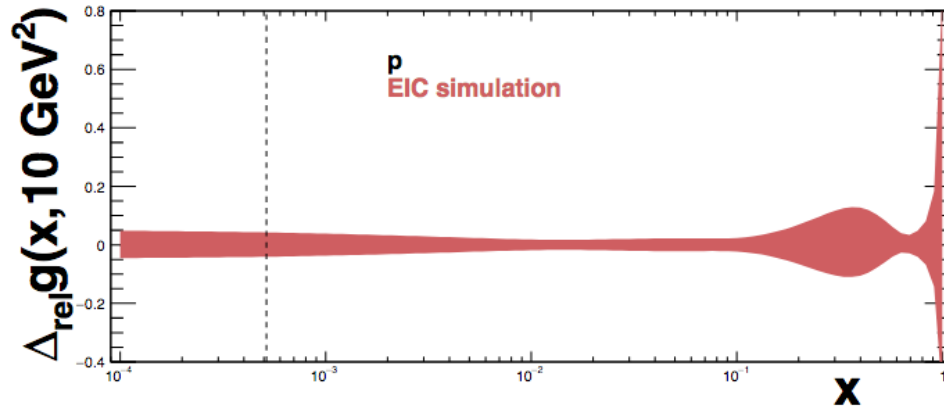
- ATHENA pseudo-data created using HERAPDF2 NNLO
 - NC: 5 centre-of-mass energies
 - CC: only highest energy so far
 - "realistic" uncertainties estimation
- PDF fits "HERAPDF2-style" with DIS and DIS+EIC data



As expected for DIS-only fits:

- Dramatic improvement of valence quarks at large x
- Improvement also for gluons/sea

Impact of EIC data on nuclear PDF @NLO



- Nuclear modification factors for gluon (for u valence and u sea quarks similar picture)

→ comparison with EPPS21
(representative current global fit)

- Fixed target DIS and DY data
- p+A at LHC
- π^0 from PHENIX

Precision largely improved with EIC data only
→ factor of two @ $x \sim 0.1$

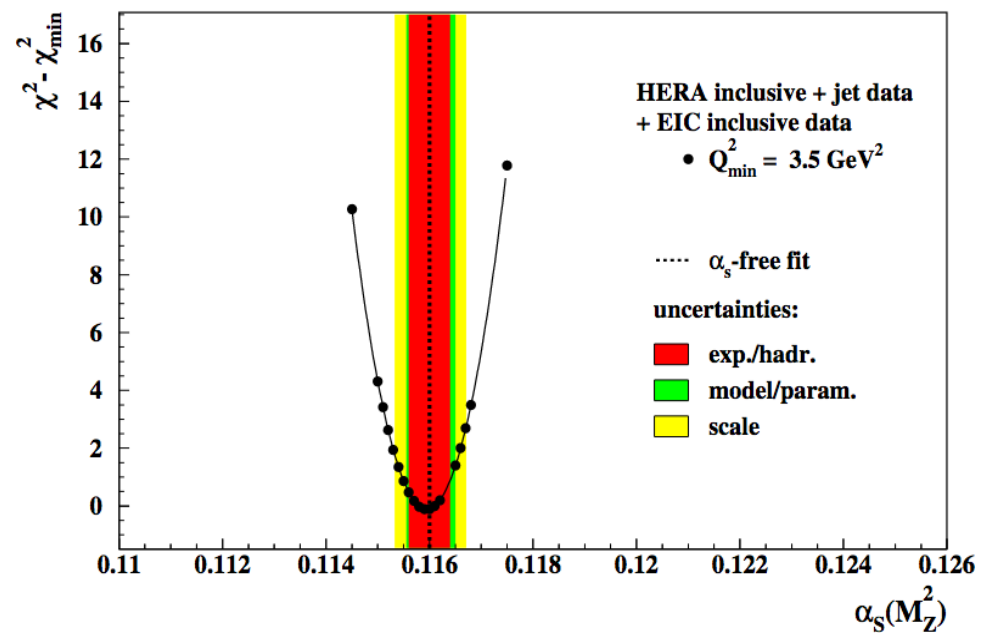
EIC & strong coupling

→ sneak preview, more in Z. Demiroglu's talk & poster on Tuesday

arXiv:2309.11269, accepted by EPJC

Simultaneous PDF and α_s fits with HERA DIS + jets and EIC DIS

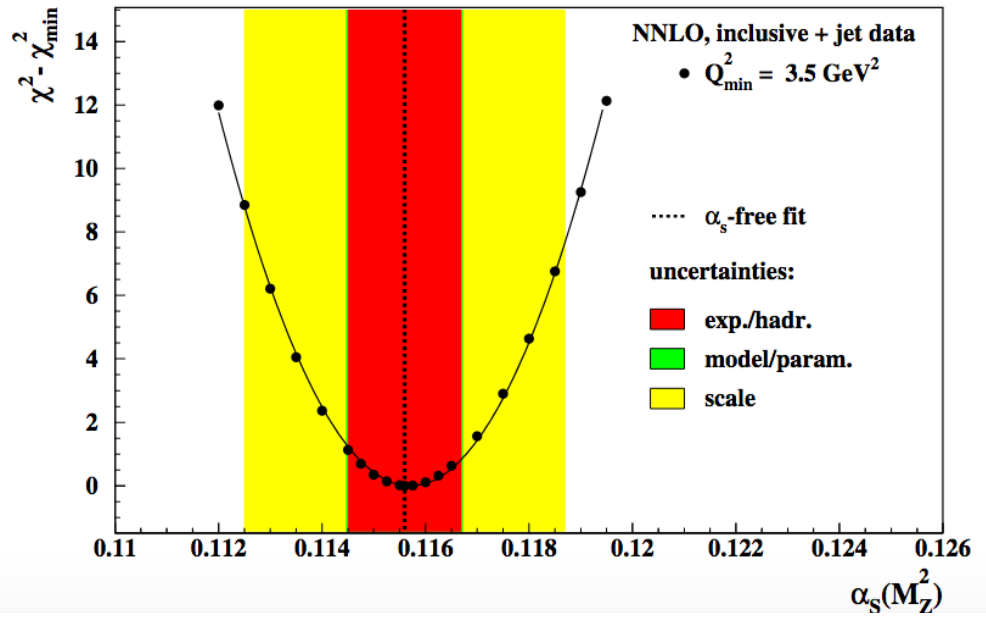
HERA inclusive and jets + EIC inclusive



$$\alpha_s(M_Z^2) = 0.1160 \pm 0.0004 \text{ (exp)} \begin{matrix} +0.0003 \\ -0.0002 \end{matrix} \text{ (model + parameterisation)} \pm 0.0005 \text{ (scale)}$$

→ stunning improvement in uncertainties, also in scale uncertainty!

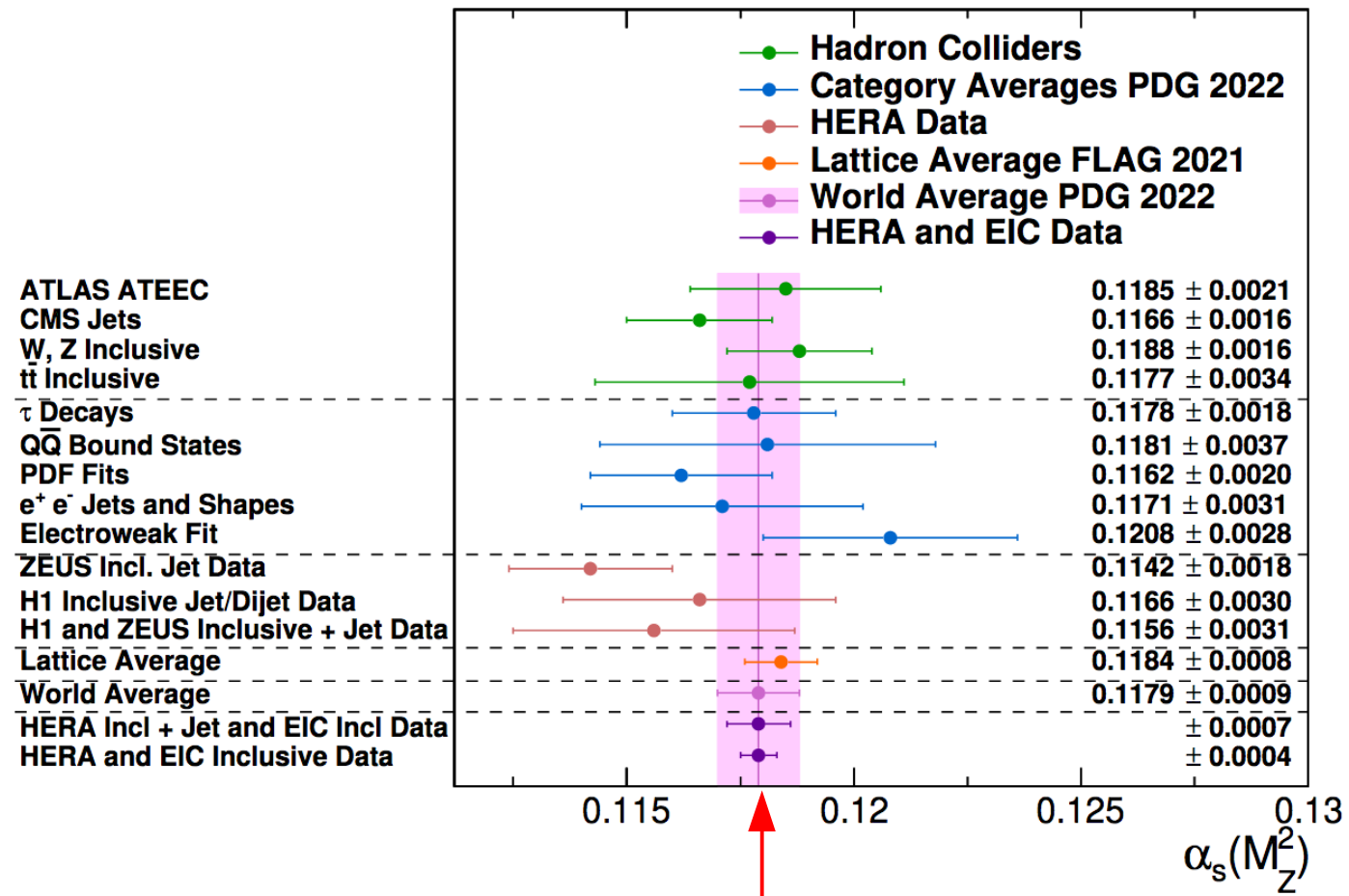
H1 and ZEUS



$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \begin{matrix} +0.0001 \\ -0.0002 \end{matrix} \text{ (model + parameterisation)} \pm 0.0029 \text{ (scale)}$$

Simultaneous PDF and α_s fits with only inclusive data from HERA and EIC

→ stunning improvement possible due to kinematic phase-space and high-x quark evolution



below 0.4%!

$$\alpha_s(M_Z^2) = 0.1159 \pm 0.0004 \text{ (exp)} \begin{matrix} +0.0002 \\ -0.0001 \end{matrix} \text{ (model + parameterisation)}$$

Message to take away: completely subjective



I'm still standing

Message to take away: completely subjective

- HERA still has something to say!

→ ZEUS new jet measurement + $\alpha_s(M_Z)$ fit

$$\alpha_s(M_Z^2) = 0.1138 \pm 0.0014 \text{ (exp/fit)} \begin{matrix} +0.0004 \\ -0.0008 \end{matrix} \text{ (model/parameterisation)} \begin{matrix} +0.0012 \\ -0.0005 \end{matrix} \text{ (scale)}$$

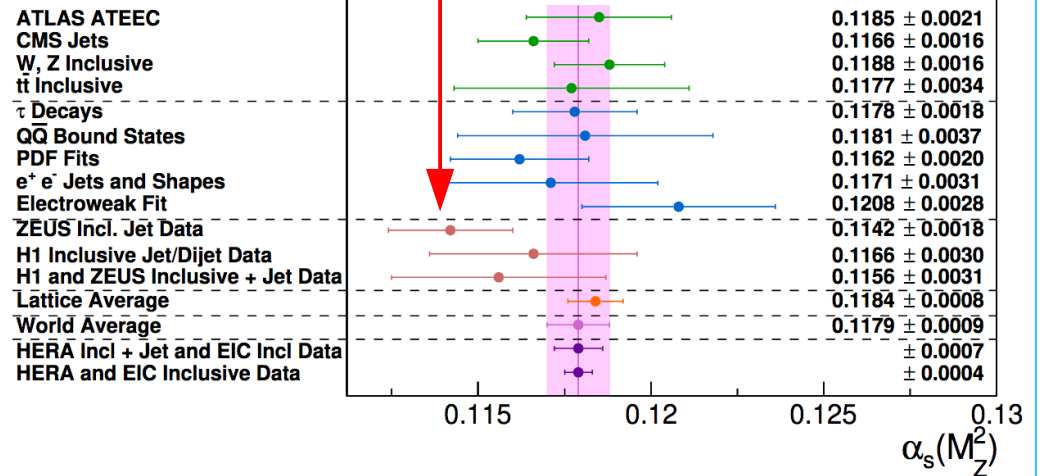
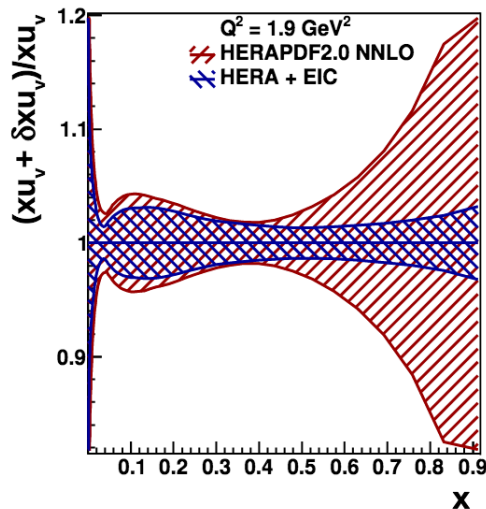
→ one of the most precise measurements of $\alpha_s(M_Z^2)$ at hadron colliders

- Using EIC data will make tremendous difference

→ proton PDFs, especially at high x

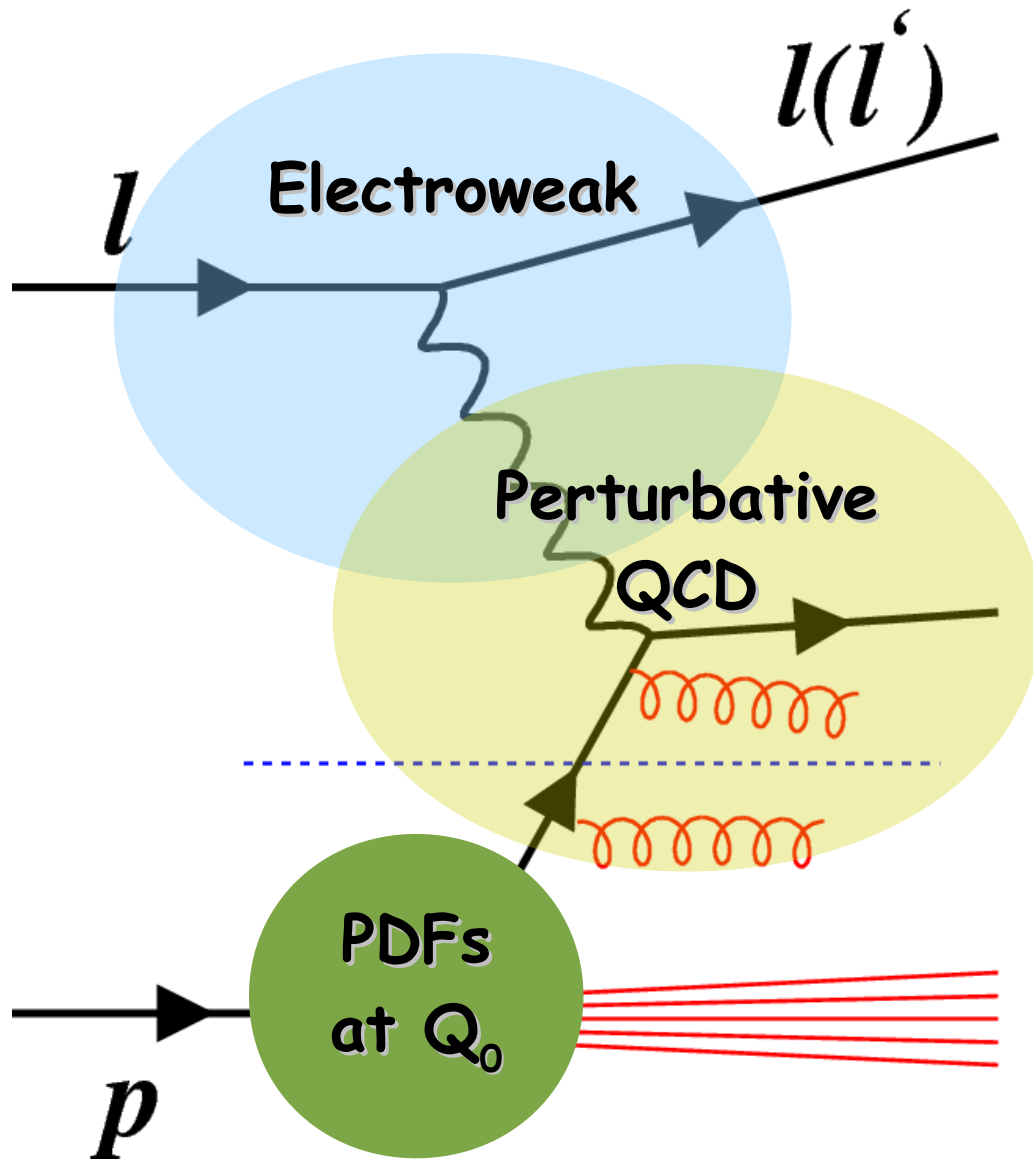
→ nPDFs constrained with 10% precision

→ $\alpha_s(M_Z)$ determination



Additional slides

Deep Inelastic Scattering @ HERA



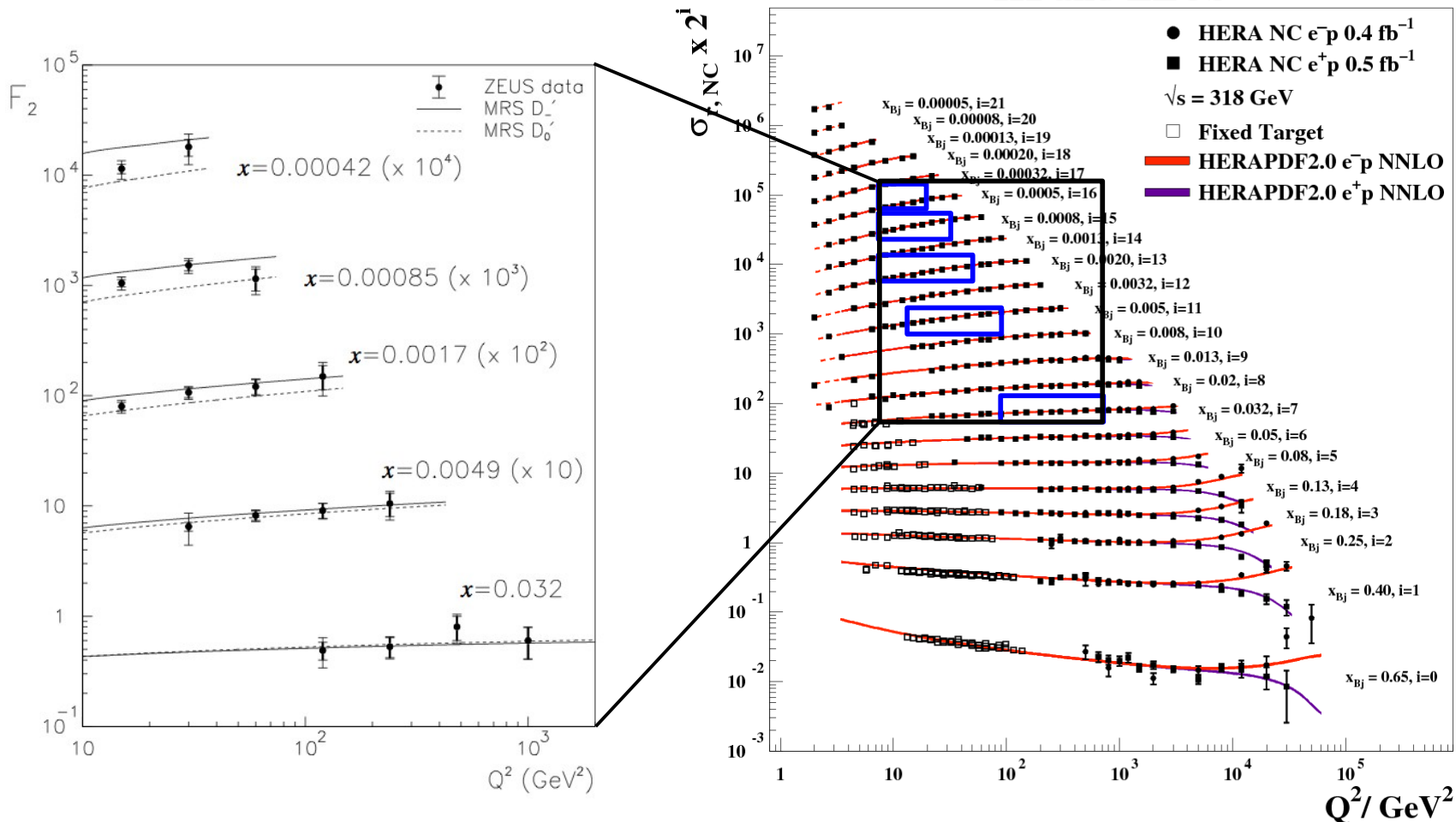
- Fix pQCD & PDFs
! Test Electroweak
- Fix Electroweak
! Test pQCD & PDFs

- Fix Electroweak & pQCD
! Determine PDFs

DIS @ HERA

First: 1993 → Final: 2015

H1 and ZEUS

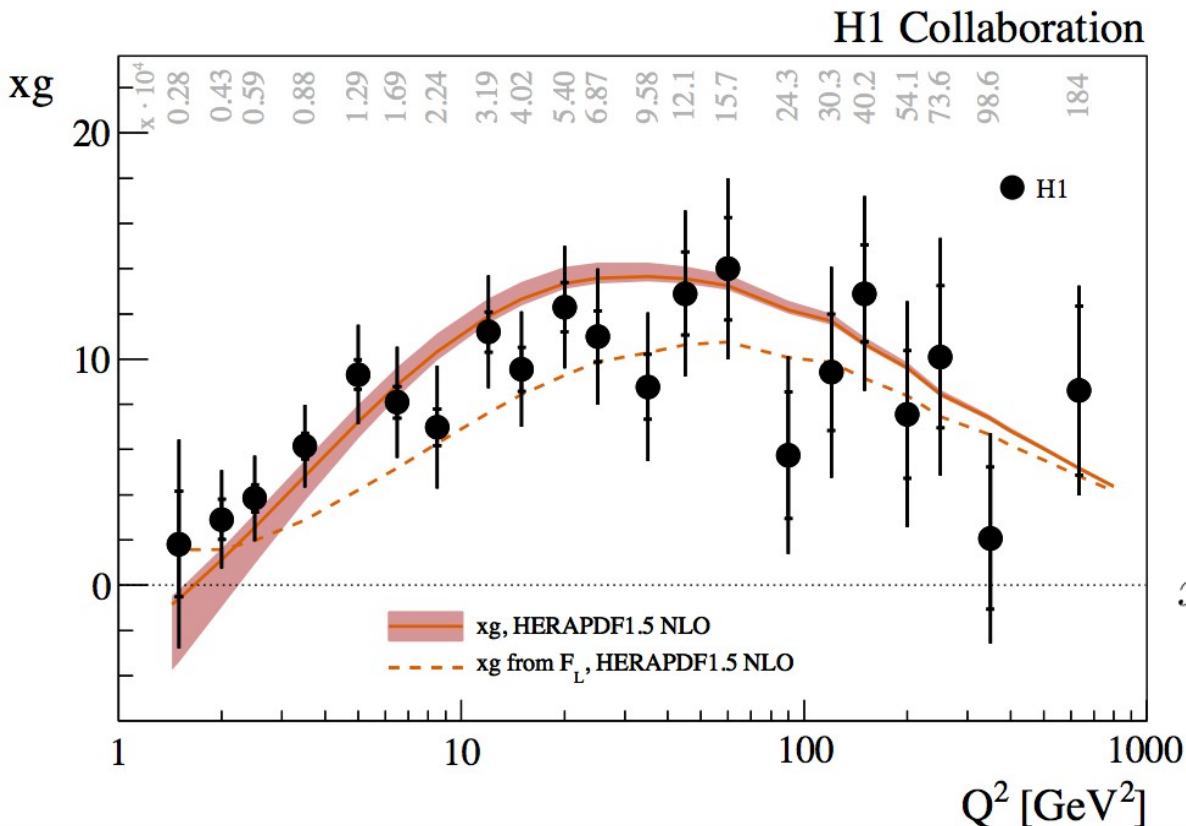


2007: HERA shutdown

→ 16th anniversary of end, 31st anniversary of start

Gluon from F_L

- H1 performed direct extraction of gluon density from F_L measurement @NLO

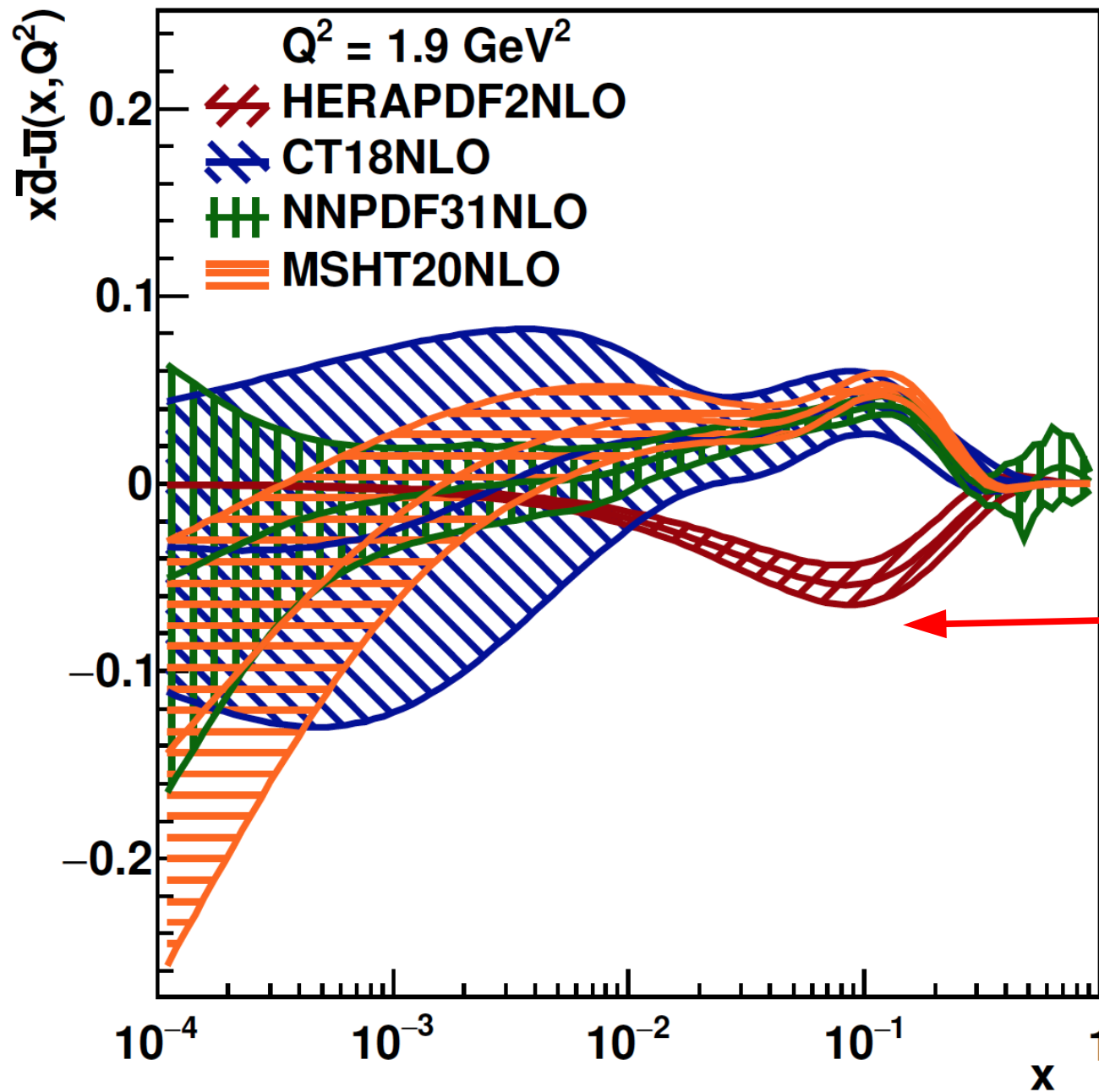


- Direct extraction of gluon density from F_L using approximation

$$xg(x, Q^2) \approx 1.77 \frac{3\pi}{2\alpha_S(Q^2)} F_L(ax, Q^2)$$

Gluon approximated from F_L agrees with gluon determined from scaling violations

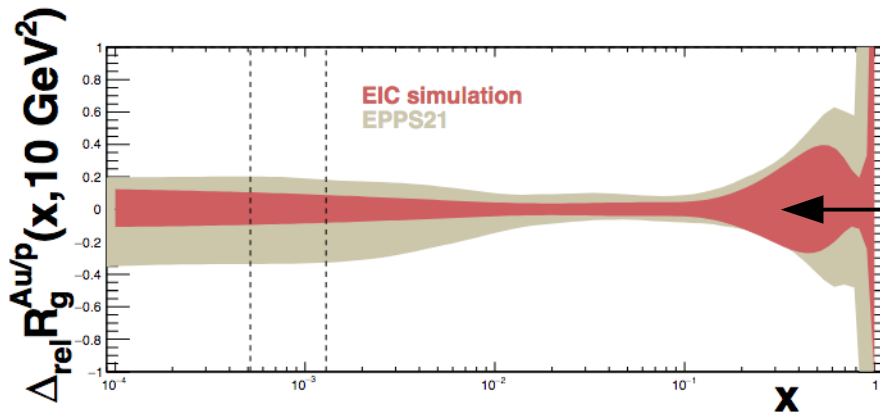
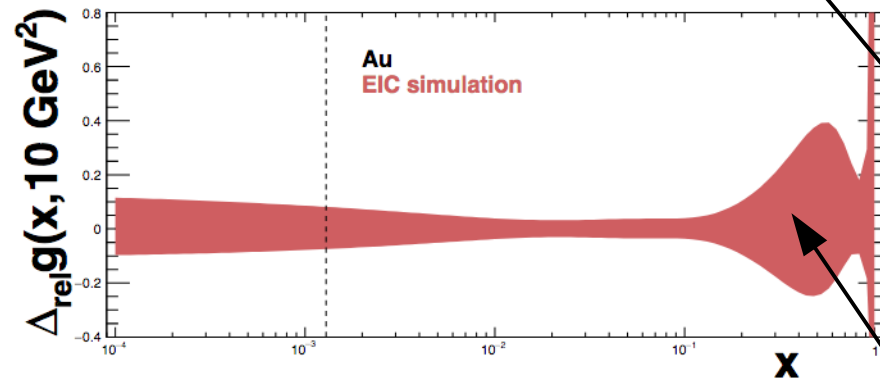
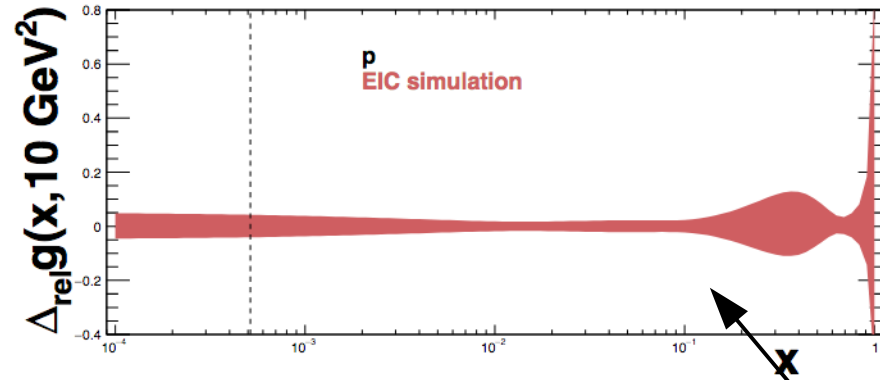
My private EIC wish list ...



HERA: only available high energy ep DIS data
 → all other fits include fixed target DIS data or DY data

Is that a real effect?

EIC, world's first e+A collider → will explore nuclear structure at unprecedented level, up to heaviest nuclei



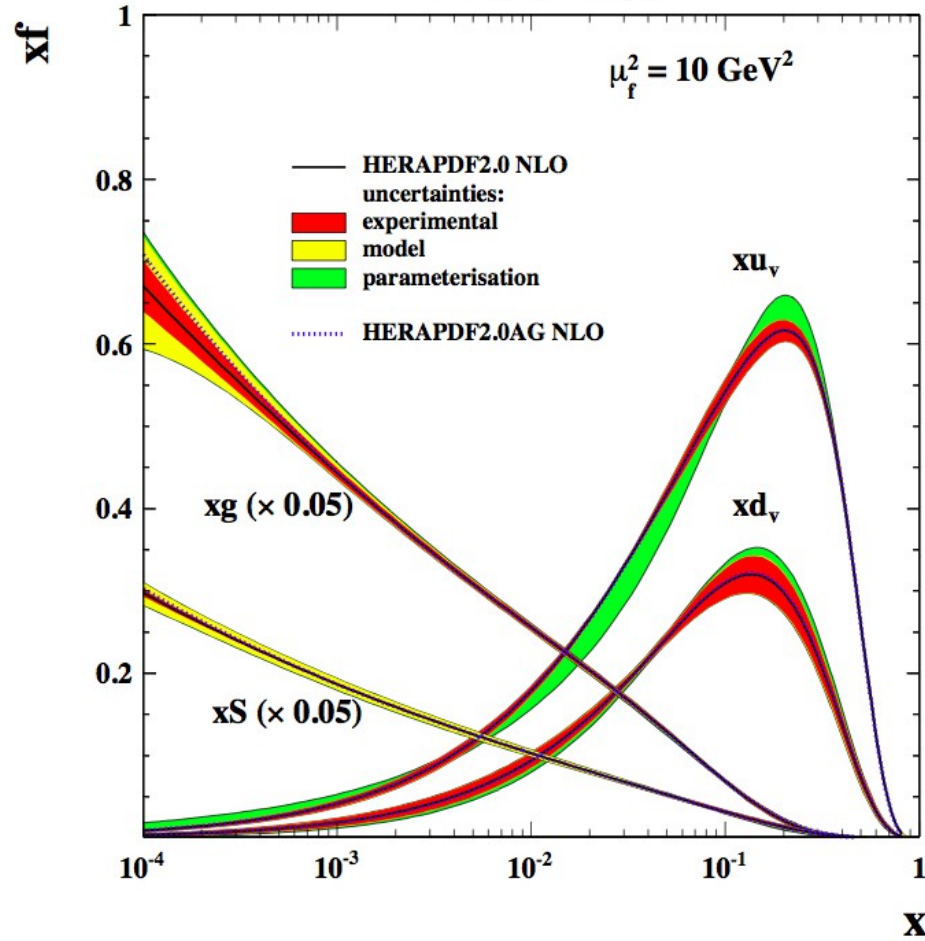
- Nuclear PDFs studied in terms of nuclear modification factor R:

It encodes deviations of nPDFs from simple scaling of free nucleon PDFs with atomic mass A after accounting for varying proton-to-neutron ratios using isospin symmetry

- Relative uncertainty of gluon in proton ATHENA-only fits
- Uncertainty of gluon in gold nucleus
- Nuclear modification factor formed from ratio of gluon in gold and proton

Color decomposition of uncertainties

H1 and ZEUS



Experimental uncertainties:

- Hessian method
- Conventional $\Delta\chi^2 = 1 \Rightarrow 68\% \text{ CL}$

Variation	Standard Value	Lower Limit	Upper Limit
Q_{\min}^2 [GeV ²]	3.5	2.5	5.0
Q_{\min}^2 [GeV ²] HiQ2	10.0	7.5	12.5
M_c (NLO) [GeV]	1.47	1.41	1.53
M_c (NNLO) [GeV]	1.43	1.37	1.49
M_b [GeV]	4.5	4.25	4.75
f_s	0.4	0.3	0.5
μ_{f_0} [GeV]	1.9	1.6	2.2

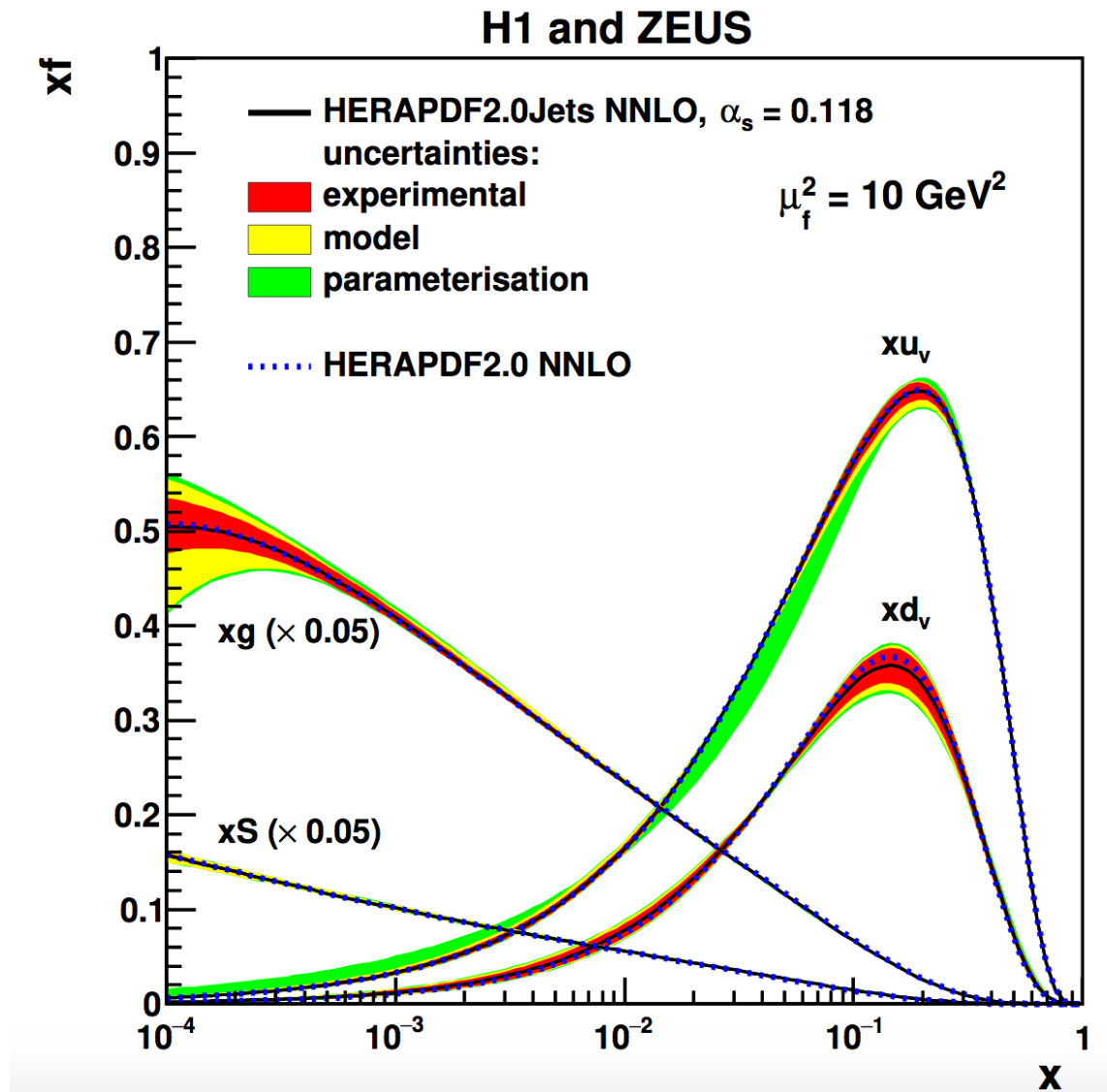
Adding D and E parameters to each PDF

Parametrisation uncertainties
- largest deviation

Model uncertainties
- all variations added in quadrature

Fit with fixed $\alpha_s = 0.118$

How does it compare to HERAPDF2.0? **Well!**



comparison to other HERA DIS results

1. **H1** NNLO jet study using fixed PDFs, includes H1 inclusive-jet and di-jet:

$$\text{H1 jets } \mu > 2m_b \quad 0.1170 \quad (9)_{\text{exp}} \quad (7)_{\text{had}} \quad (5)_{\text{PDF}} \quad (4)_{\text{PDF}\alpha_s} \quad (2)_{\text{PDFset}} \quad (38)_{\text{scale}}$$

with similar breakup of uncertainties and similar μ , new HERA result:

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 (\text{exp+had+PDF}) \begin{matrix} +0.0001 \\ -0.0002 \end{matrix} (\text{model + parameterisation}) \pm 0.0029 (\text{scale})$$

H1 also provided a **PDF+ α_s** fit to H1 inclusive and jet data

$$0.1147 \quad (11)_{\text{exp,NP,PDF}} \quad (2)_{\text{mod}} \quad (3)_{\text{par}} \quad (23)_{\text{scale}}$$

analysis required $Q^2 > 10\text{GeV}^2$; NEW HERA result re-evaluated with this cut (rather than $>3.5\text{GeV}^2$), is:

$$\alpha_s(M_Z^2) = \boxed{0.1156} \pm 0.0011 (\text{exp}) \pm 0.0002 (\text{model + parameterisation}) \pm \boxed{0.0021} (\text{scale})$$

2. **NNLOJet+APPLfast** using fixed PDFs, includes H1+ZEUS inclusive-jet:

$$\text{HERA inclusive jets } \mu > 2m_b \quad 0.1171 \quad (9)_{\text{exp}} \quad (5)_{\text{had}} \quad (4)_{\text{PDF}} \quad (3)_{\text{PDF}\alpha_s} \quad (2)_{\text{PDFset}} \quad (33)_{\text{scale}}$$

Updates in the procedure

- scale choice changes:
- factorisation: $\mu_F^2 = (Q^2 + p_t^2)$
- cf. $\mu_F^2 = Q^2$ in previous NLO analysis; updated since not a good choice for low Q^2 jet data; change makes almost no difference for high Q^2 jets
- renormalisation: $\mu_R^2 = (Q^2 + p_t^2)$
- cf. $\mu_R^2 = (Q^2 + p_t^2)/2$ in previous NLO analysis
- NNLO fit with $\mu_R^2 = (Q^2 + p_t^2)$ gives $\Delta X^2 = -15$ cf. $\mu_R^2 = (Q^2 + p_t^2)/2$ and vice versa for NLO fit
- scale uncertainties treated as completely correlated between bins and datasets

† p_t denotes p_t^{jet} in the case of inclusive jet cross sections and $\langle p_t \rangle$ for dijets

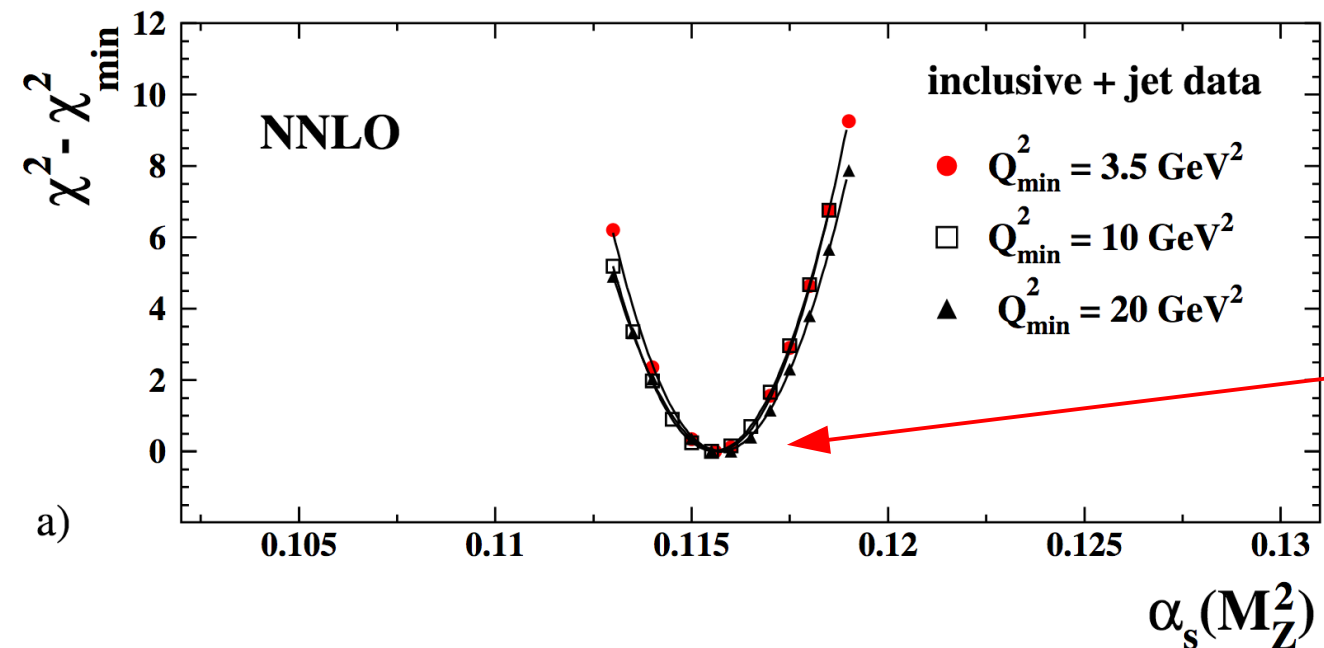
- improved treatment of hadronisation uncertainties; NOW included together with exp. systematics; treated as $1/2$ correlated, $1/2$ uncorrelated between bins and datasets
- (small) uncertainties on theory predictions included

Checking robustness of results

- HERA data at low x and Q^2 may be subject to need for $\ln(1/x)$ resummation or higher twist effects (eg arXiv:1506.06042, 1710.05935)

→ χ^2 scans performed with harder Q^2 cuts

H1 and ZEUS



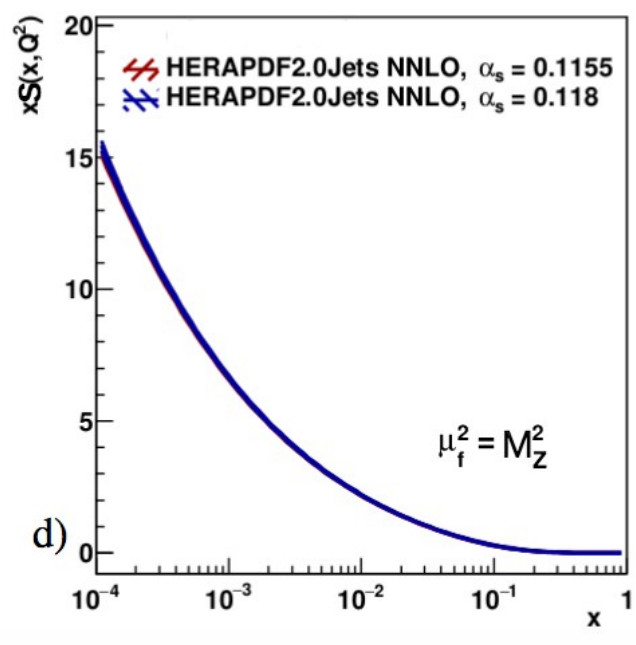
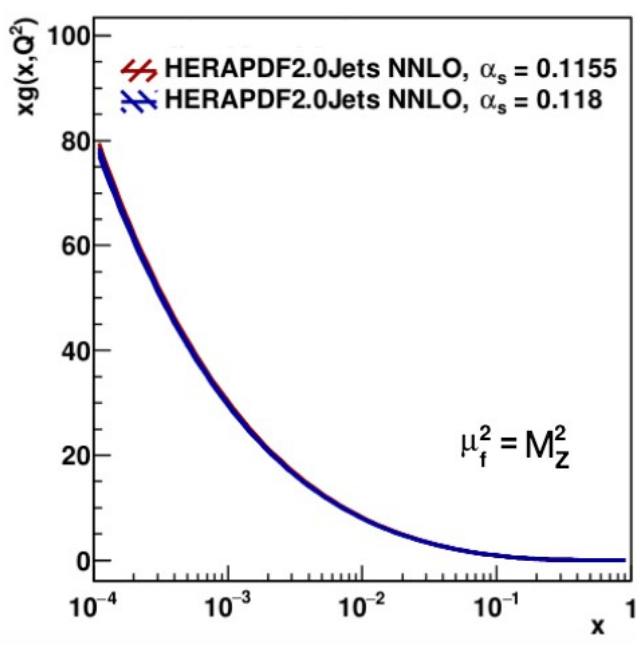
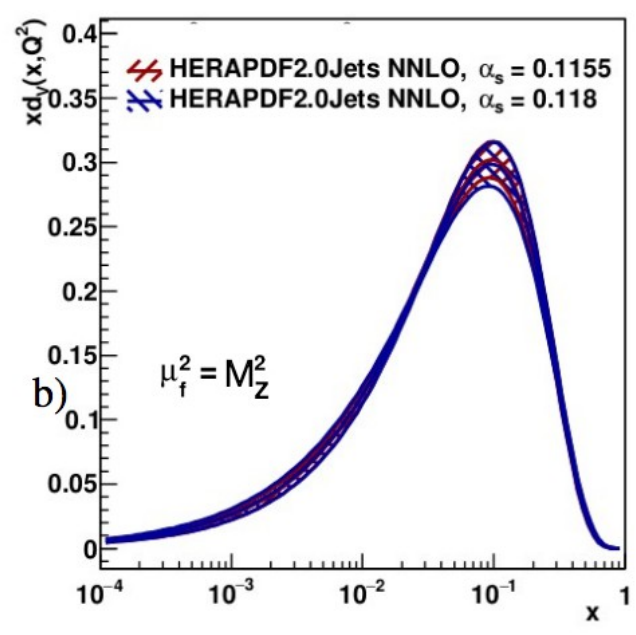
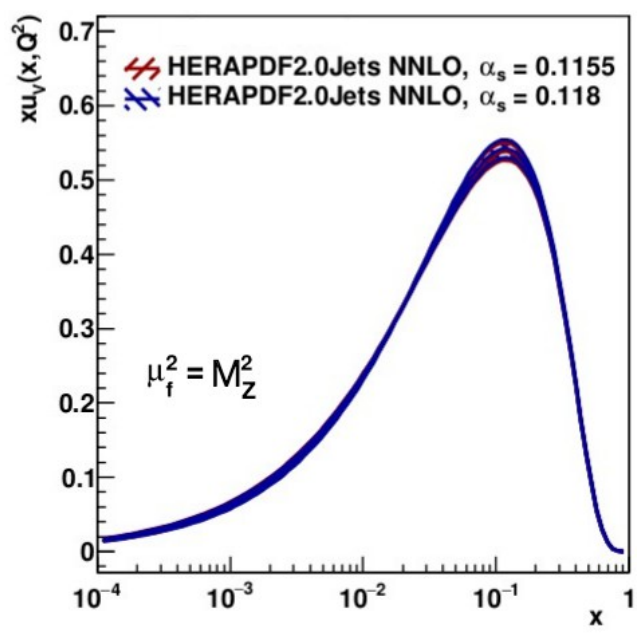
Q^2 cuts do not result in any significant change to the value of $\alpha_s(M_Z)$

- Alternative parameterisations checked
 - No negative gluon term and no NG but additional Dg parameter
 - both give the same result
 - consistent with nominal

$$\alpha_s(M_Z^2) = 0.1151 \pm 0.0010 \text{ (exp)}$$

... and how it compares to $\alpha_s = 0.1155$

H1 and ZEUS



Some remarks on NLO to NNLO comparison- (not in the paper)

Our present NNLO result using $\frac{1}{2}$ correlated and $\frac{1}{2}$ uncorrelated scale uncertainty

$$\alpha_s(M_Z) = 0.1156 \pm 0.0011(\text{exp})^{+0.0001}_{-0.0002}(\text{model+parametrisation}) \pm 0.0022(\text{scale})$$

where “exp” denotes the experimental uncertainty which is taken as the fit uncertainty, including the contribution from hadronisation uncertainties.

Maybe compared with the NLO result

$$\alpha_s(M_Z) = 0.1183 \pm 0.0008(\text{exp}) \pm 0.0012(\text{had})^{+0.0003}_{-0.0005}(\text{mod/param})^{+0.0037}_{-0.003}(\text{scale})$$

BUT

- the choice of scale was different;
- the NLO result did not include the recently published H1 low- Q^2 inclusive and dijet data [28];
- the NLO result did not include the newly published low p_T points from the H1 high- Q^2 inclusive data;
- the NNLO result does not include trijet data;
- the NNLO result does not include the low p_T points from the ZEUS dijet data;
- the NNLO analysis imposes a stronger kinematic cut $\mu > 10 \text{ GeV}$
- the treatment of hadronisation uncertainty differs.

All these changes with respect to the NLO analysis had to be made to create a consistent environment for a fit at NNLO. at the same time, an NLO fit cannot be done under exactly the same conditions as the NNLO fit since the H1 low Q^2 data cannot be well fitted at NLO. However, an NLO and an NNLO fit can be done under the common conditions:

(from A. Cooper-Sarkar, alpha-s 2022 workshop)

An NLO and an NNLO fit can be done under the common conditions:

- choice of scale, $\mu_f^2 = \mu_r^2 = Q^2 + p_T^2$;
- exclusion of the H1 low- Q^2 inclusive and dijet data;
- exclusion of the low- p_T points from the H1 high- Q^2 inclusive jet data;
- exclusion of trijet data;
- exclusion of low- p_T points from the ZEUS dijet data;
- exclusion of data with $\mu < 10$ GeV
- hadronisation uncertainties treated as correlated systematic uncertainties as done in the NNLO analysis.

The values of $\alpha_s(M_Z)$ obtained for these conditions are:

$0.1186 \pm 0.0014(\text{exp})$ NLO and $0.1144 \pm 0.0013(\text{exp})$ NNLO.

The change of the NNLO value from the preferred value of 0.1156 is mostly due to the exclusion of the H1 low Q^2 data and the low- p_T points at high Q^2

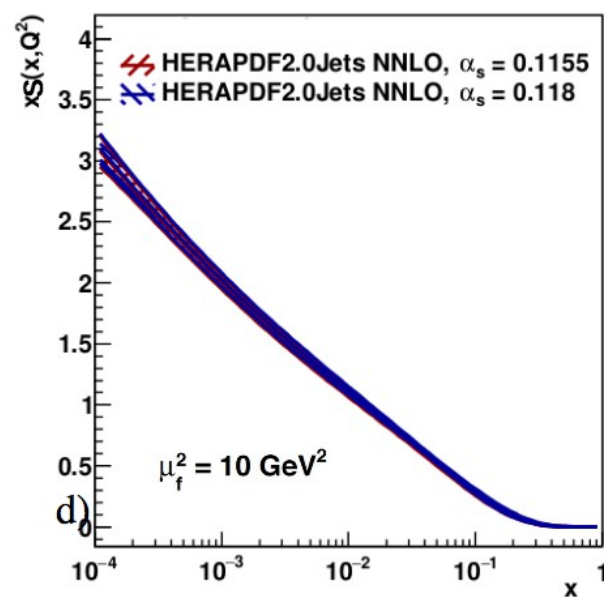
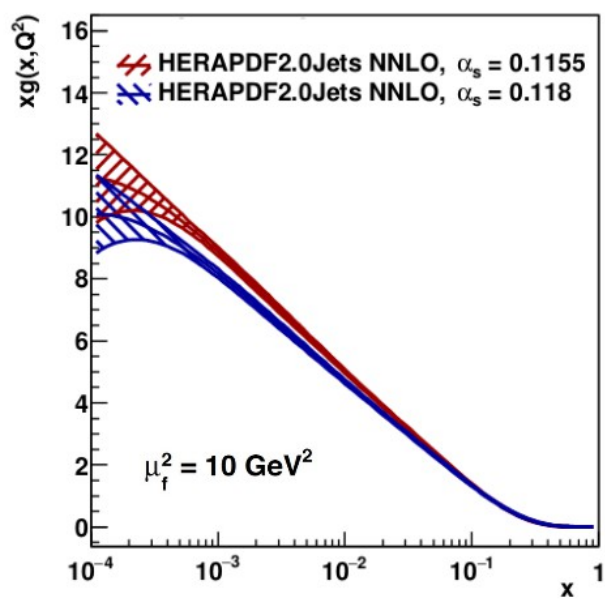
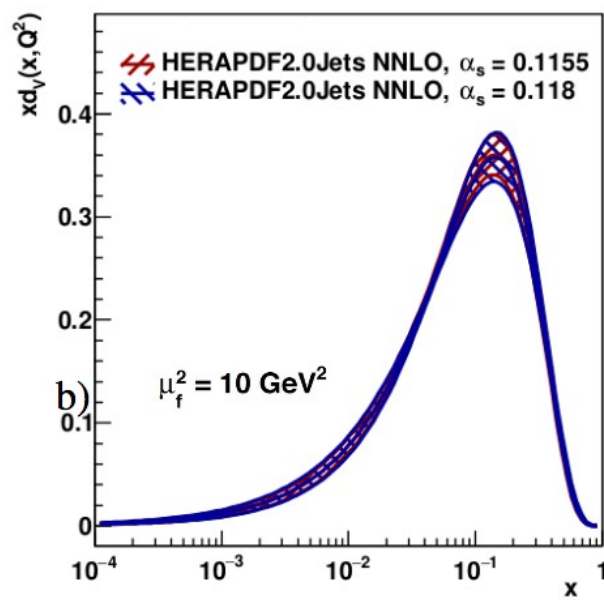
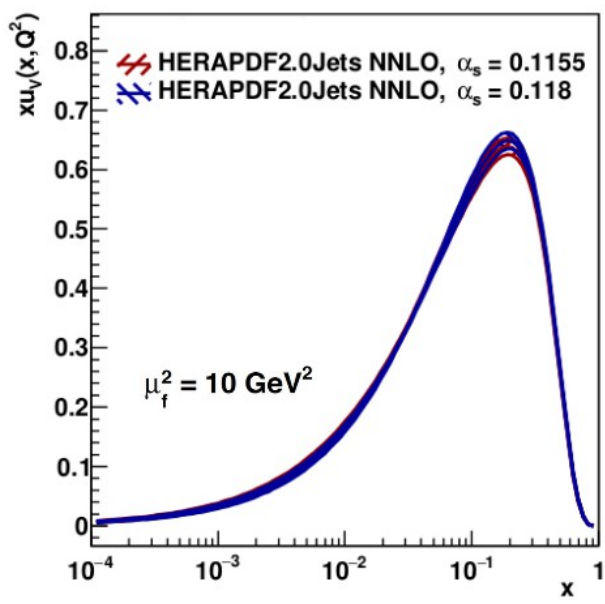
What do we mean when we say the H1 low Q^2 jets cannot be well fitted at NLO?

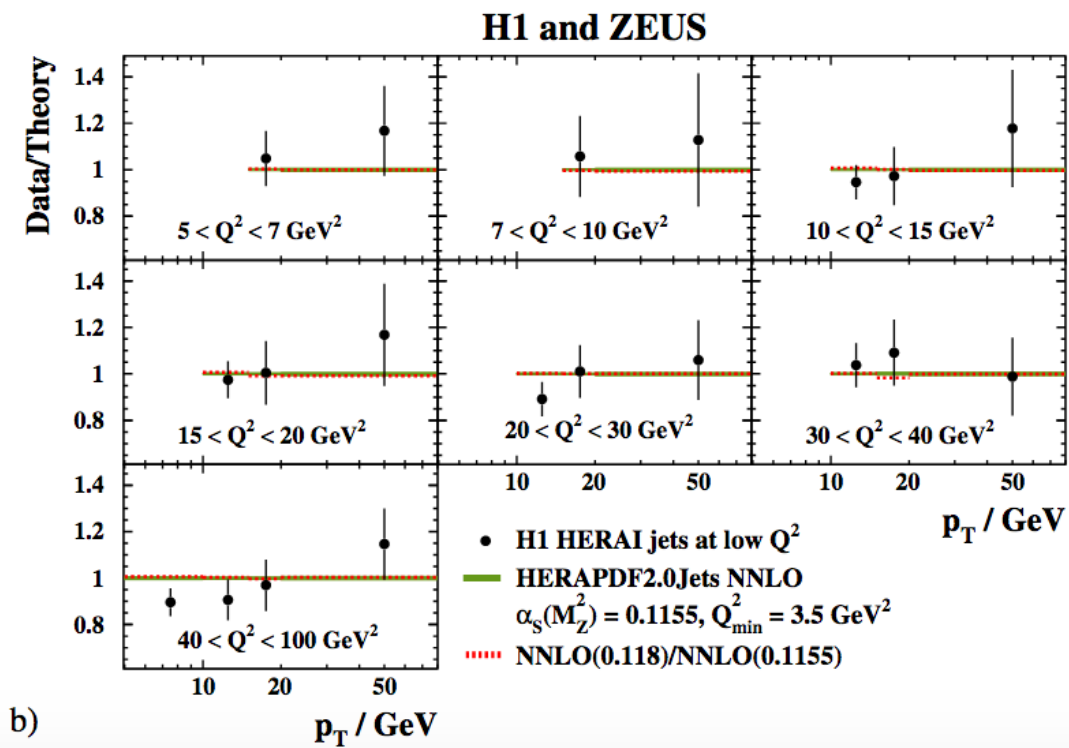
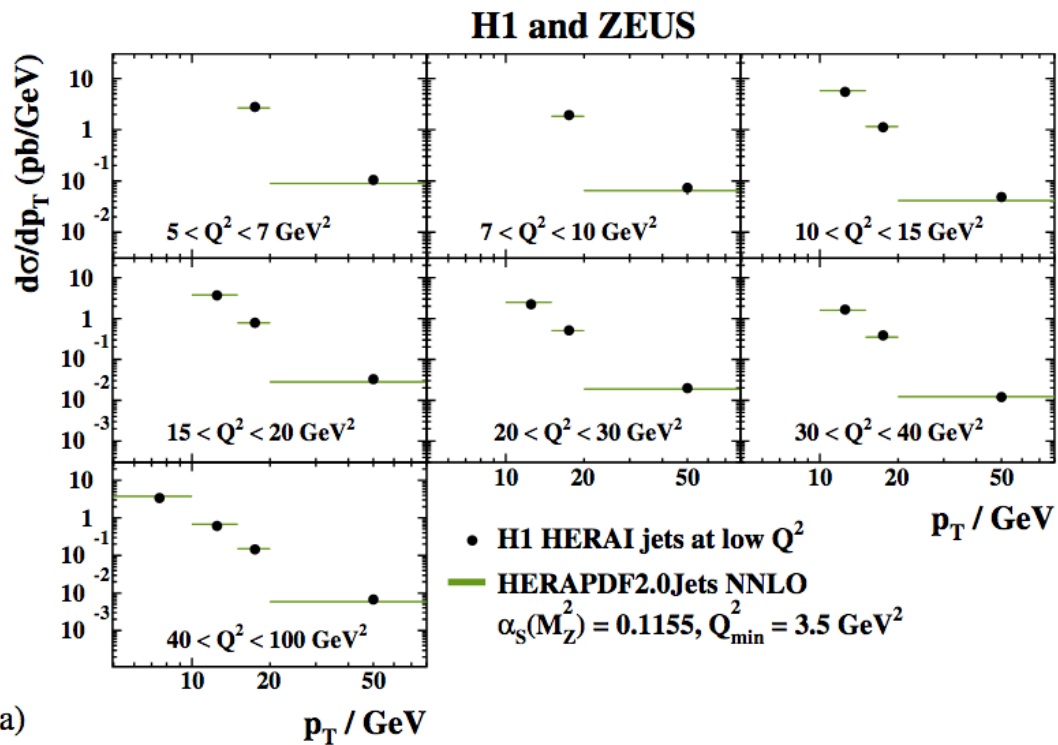
Simply this, that at NNLO the increase in overall χ^2 of the fit when the 74 data pts of these data are added is ~ 80 (exact value depends on $\alpha_s(M_Z)$ and on scale choice)

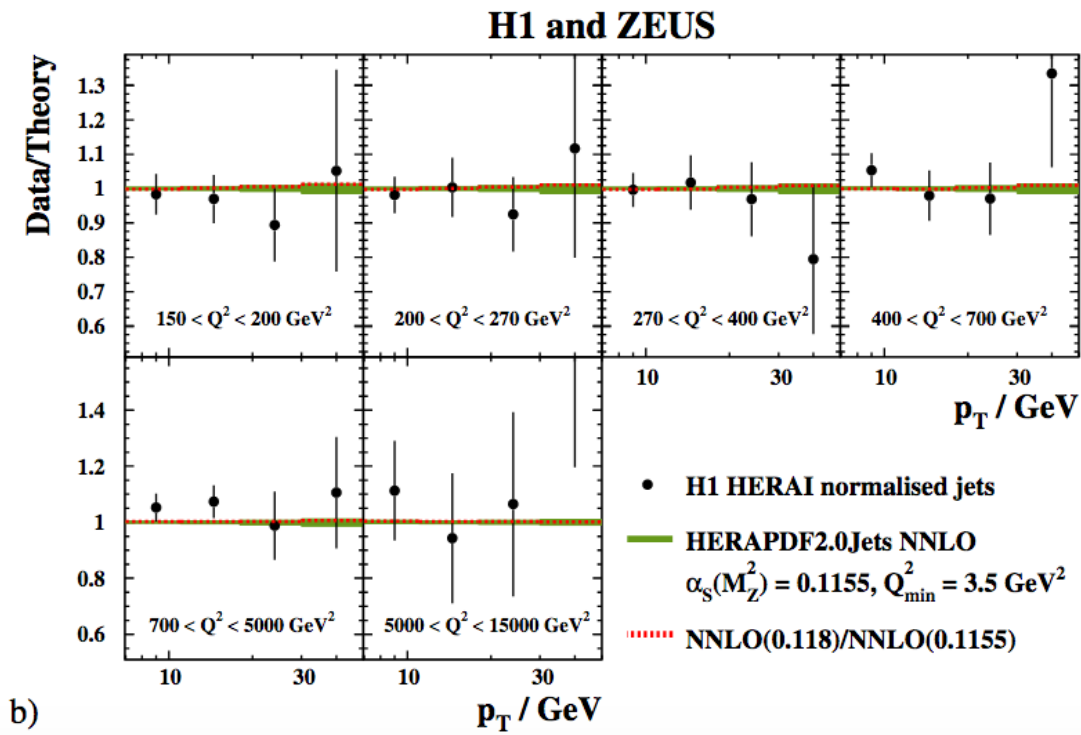
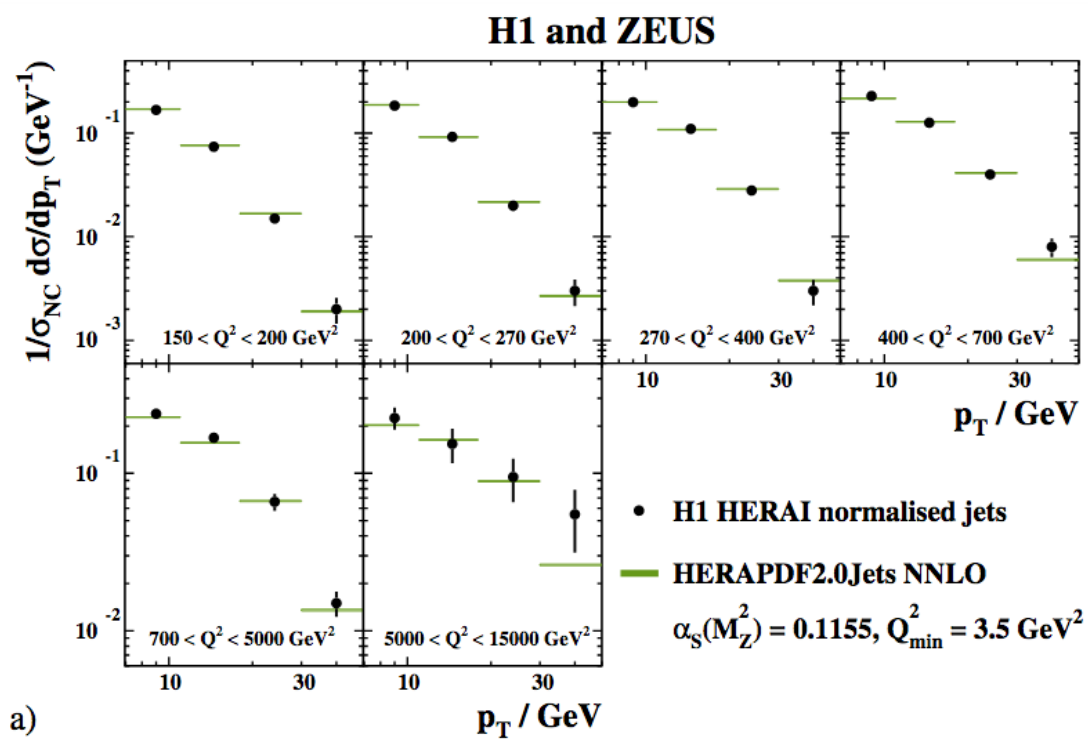
Whereas at NLO the increase in overall χ^2 of the fit when the 74 data pts of these data are added is ~ 180 .

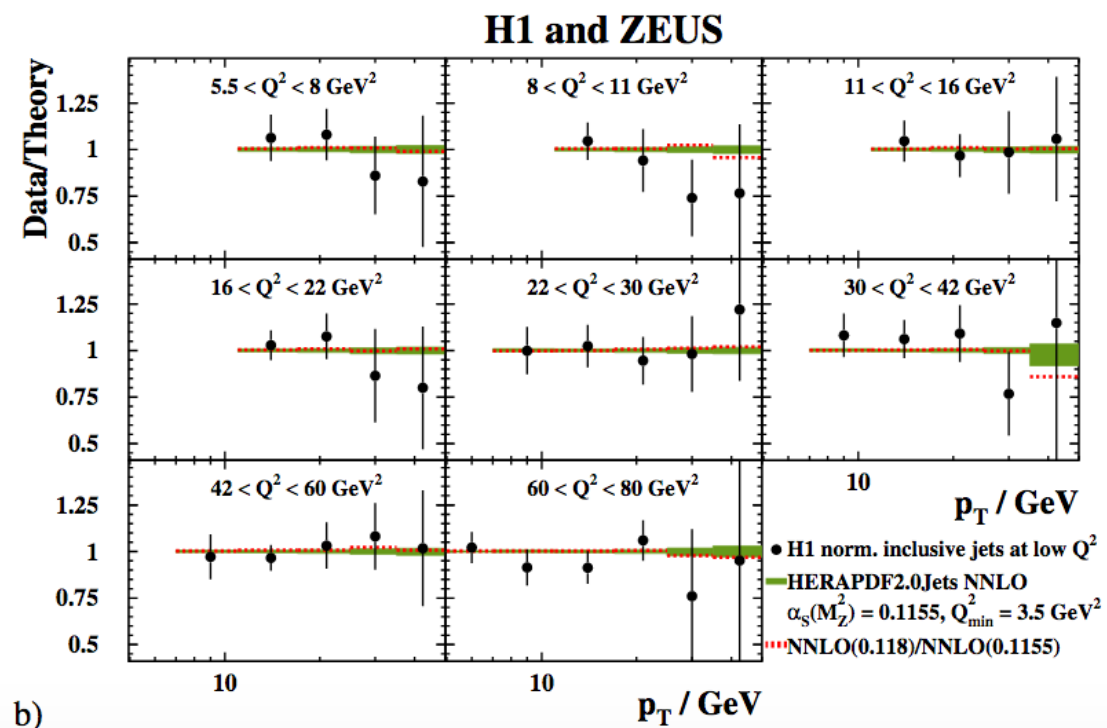
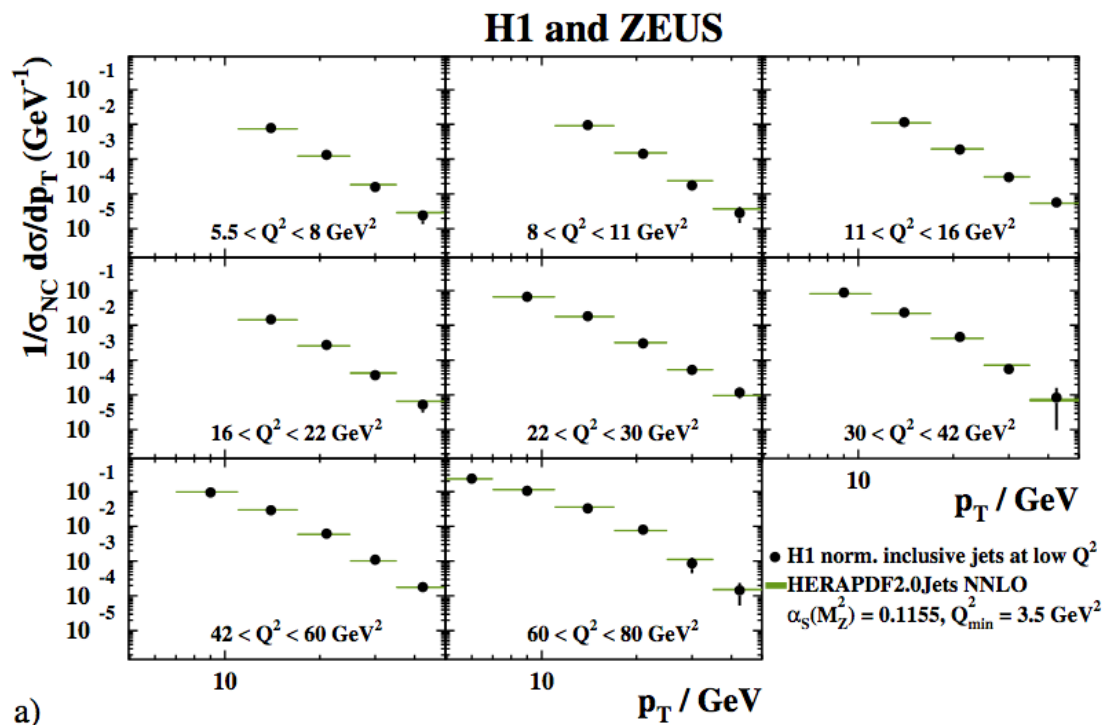
... and how it compares to $\alpha_s = 0.1155$

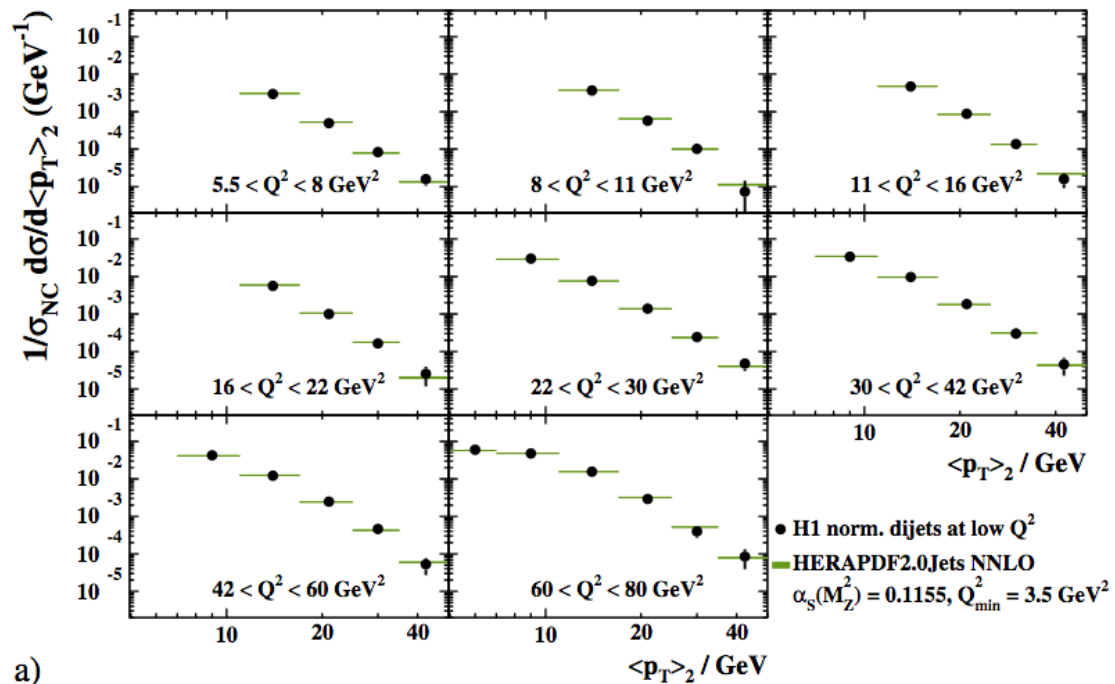
H1 and ZEUS



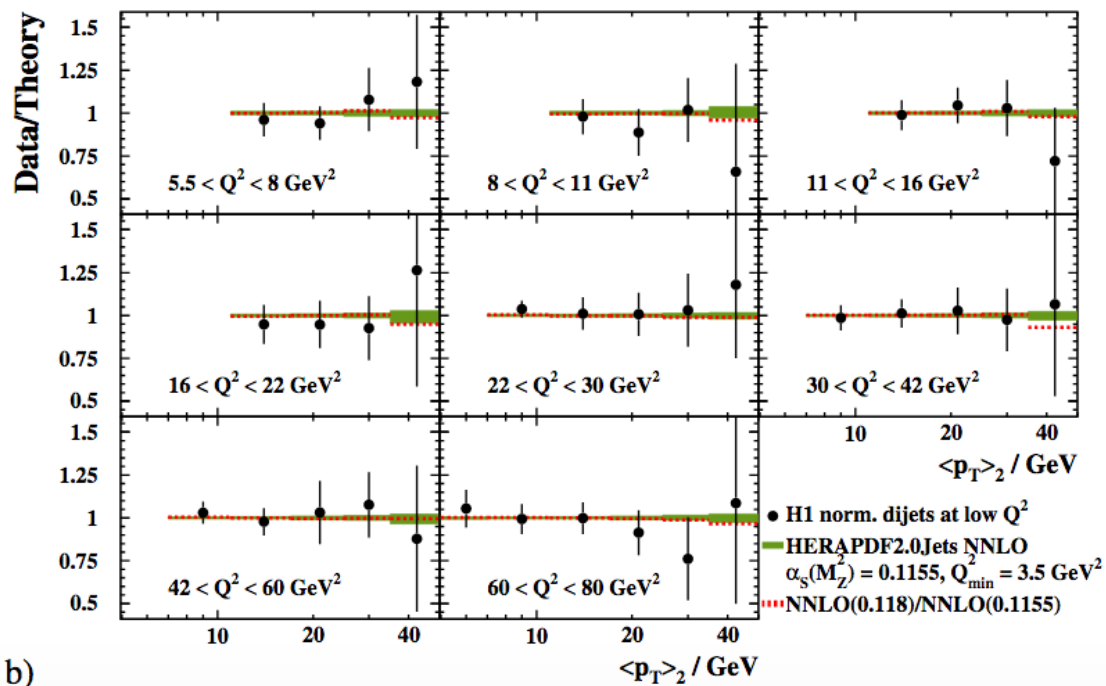




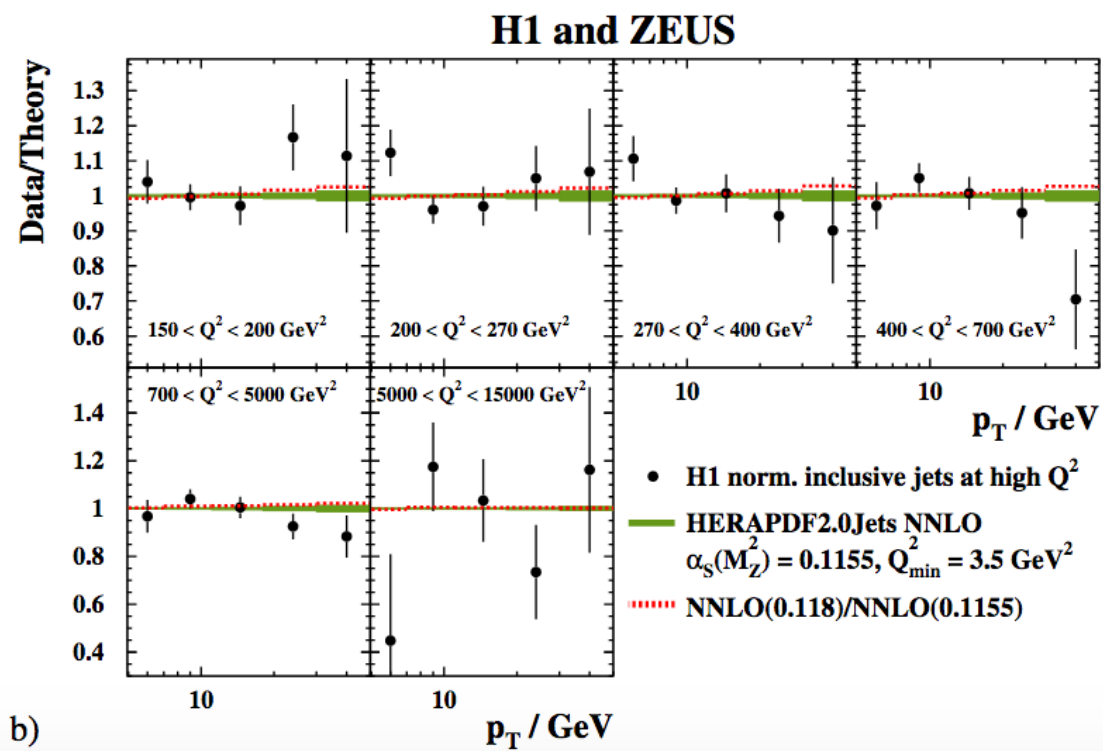
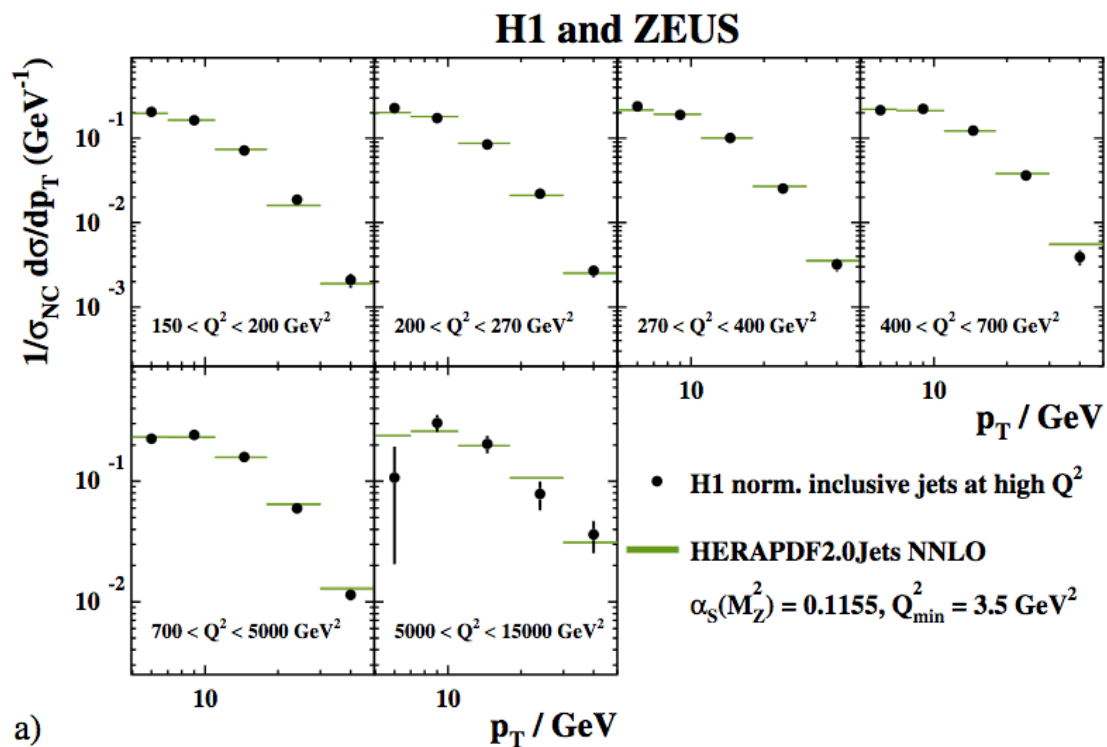


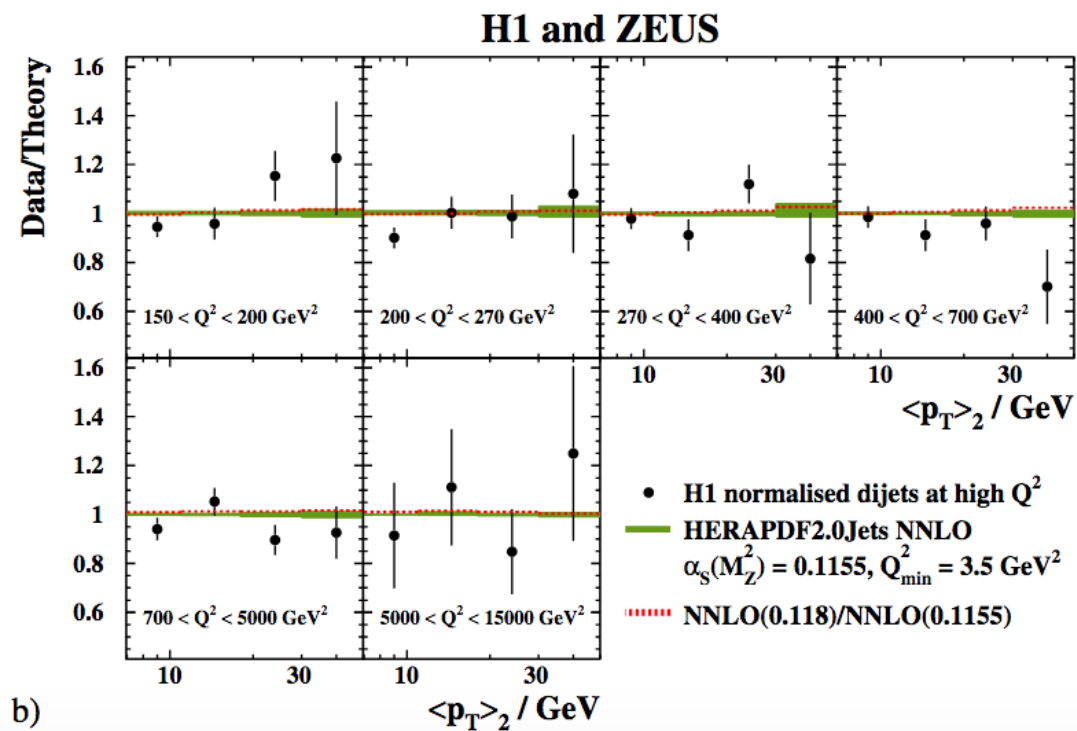
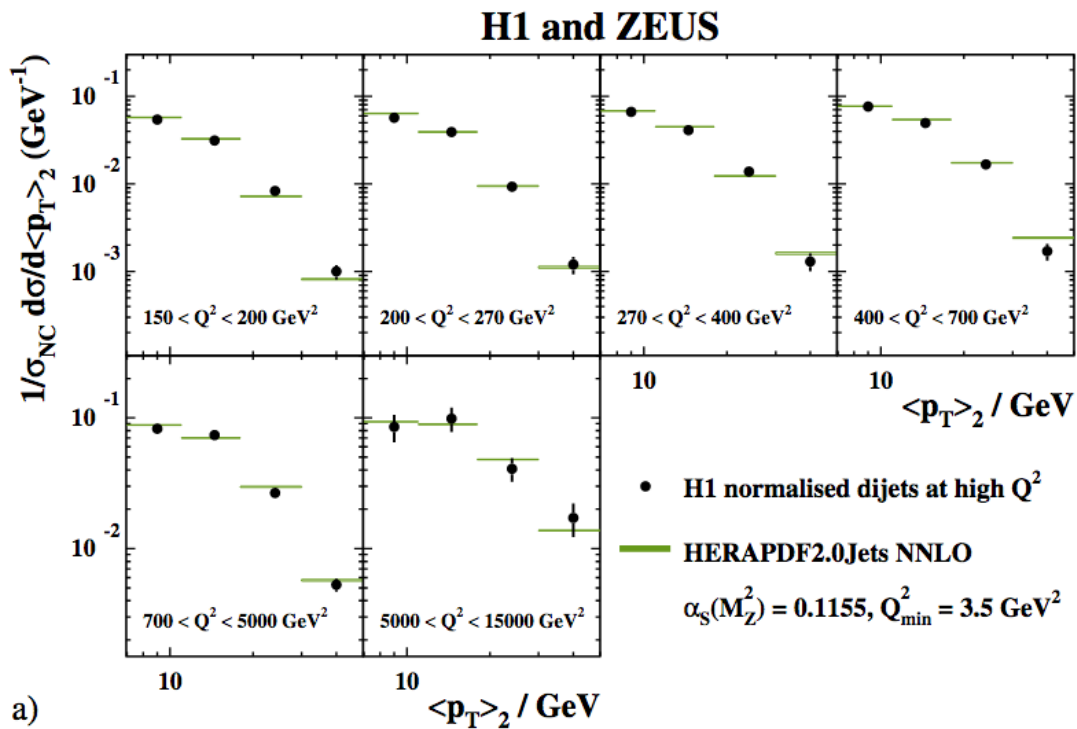
H1 and ZEUS


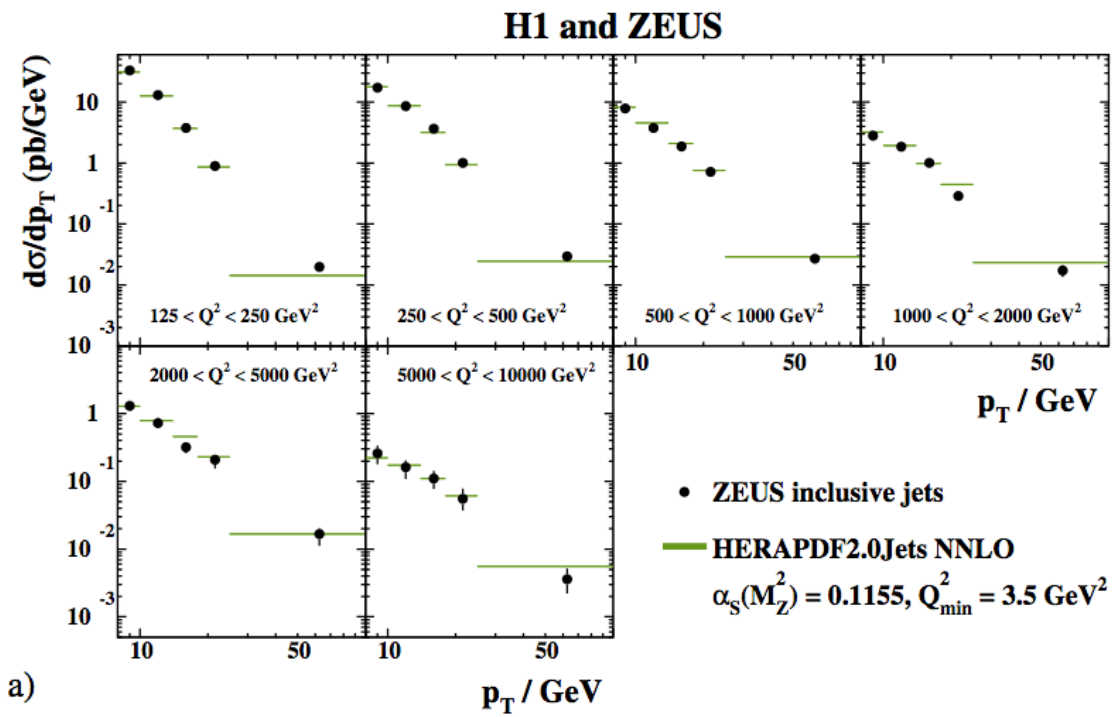
a)

H1 and ZEUS


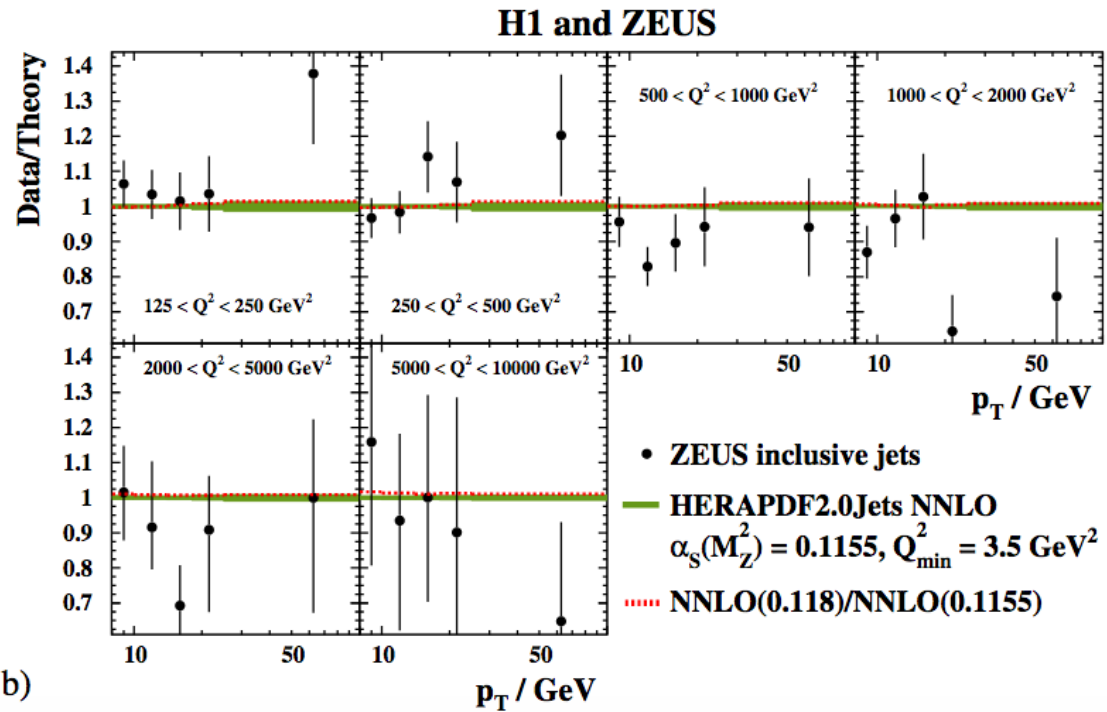
b)



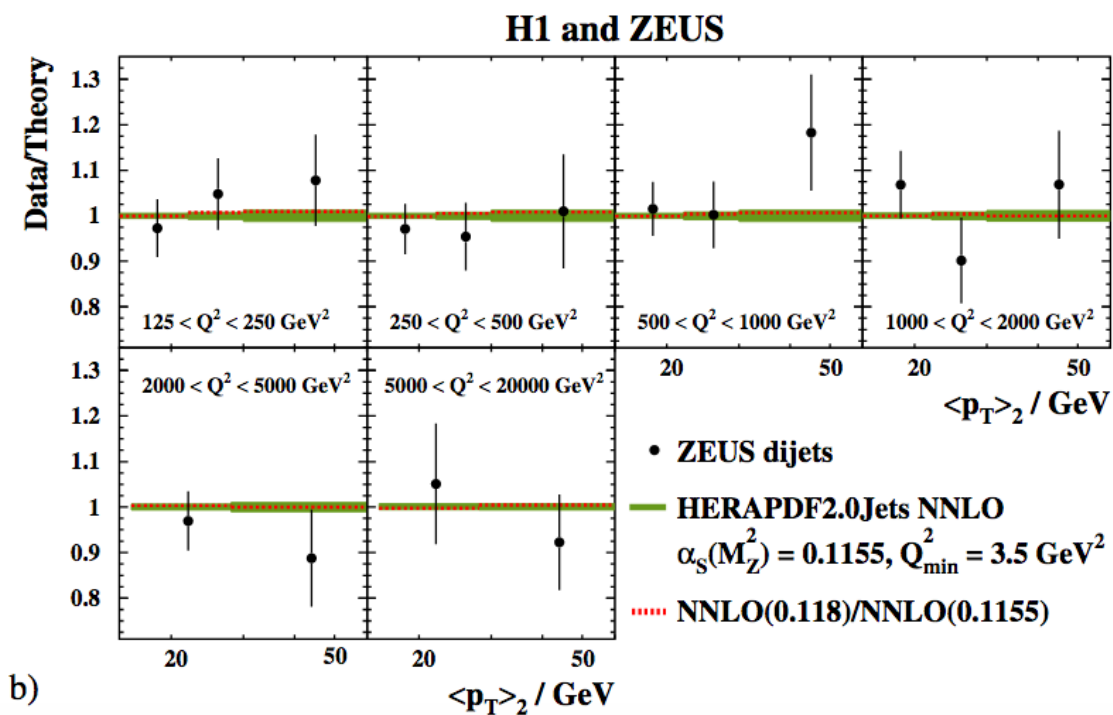
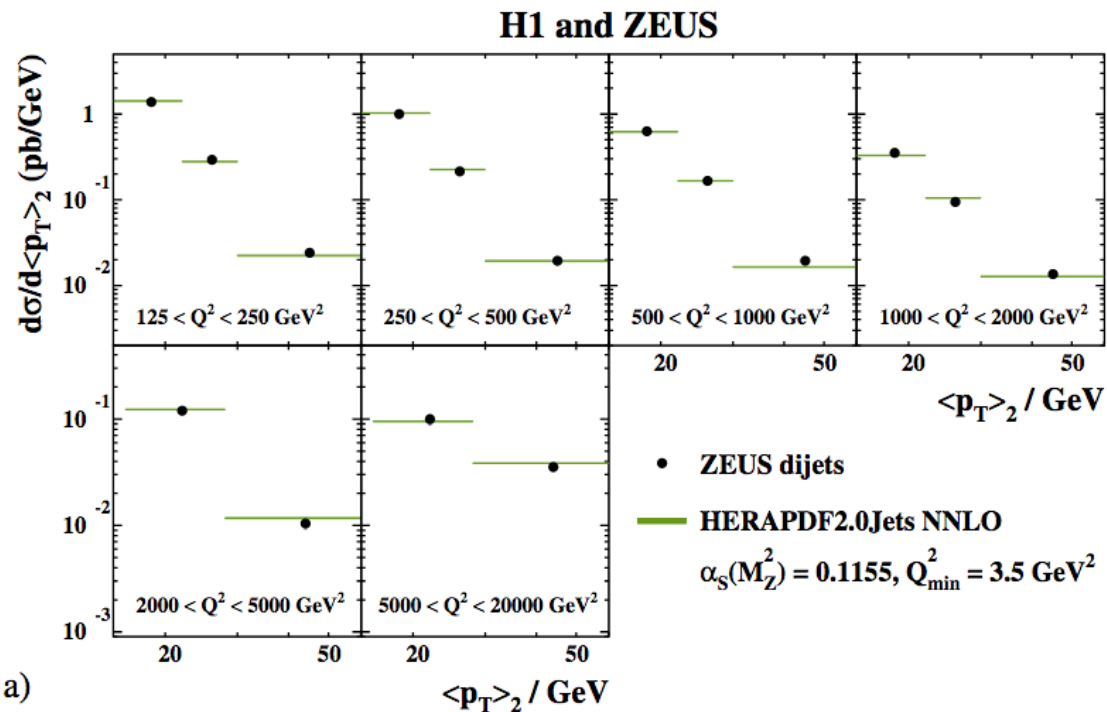




a)



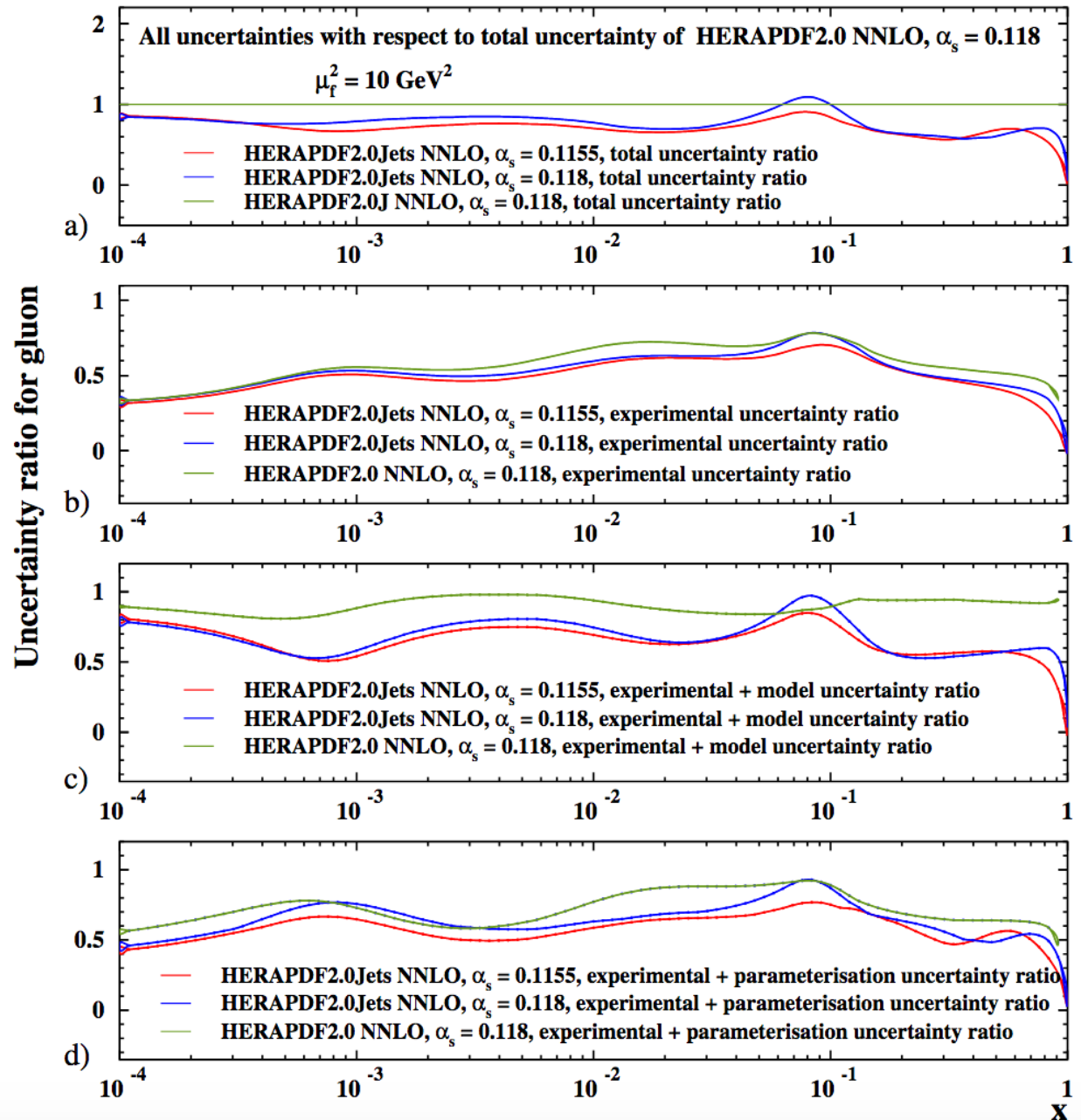
b)



Uncertainties

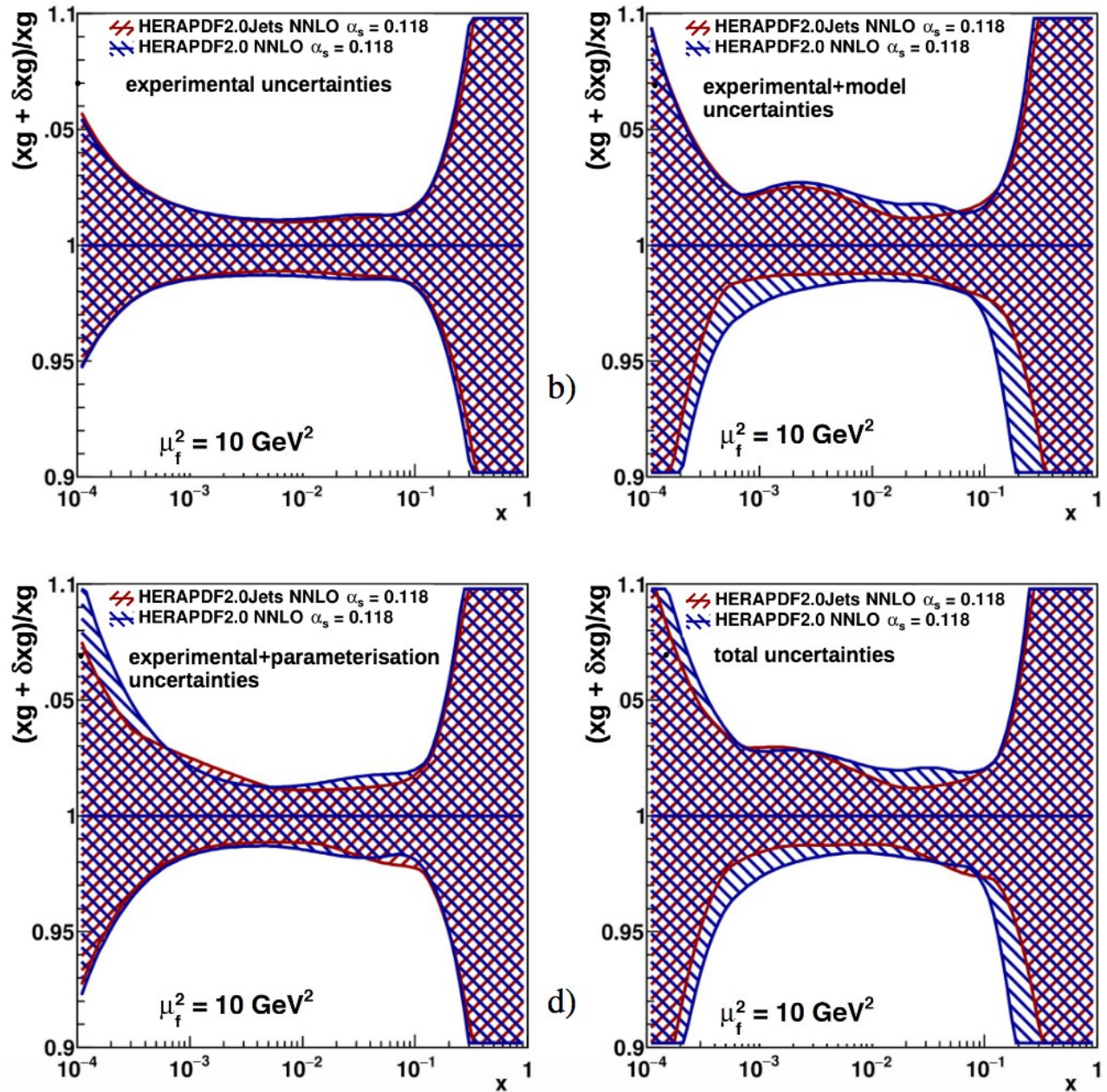
- Reduction of low- x gluon ($x < 10^{-3}$) uncertainties due to reduced model/param uncertainties in variations of M_c and μ_f^2
- Reduction of high- x gluon ($x > 10^{-3}$) uncertainties due to reduced model/param/exp uncertainties
- The same for other scales

H1 and ZEUS



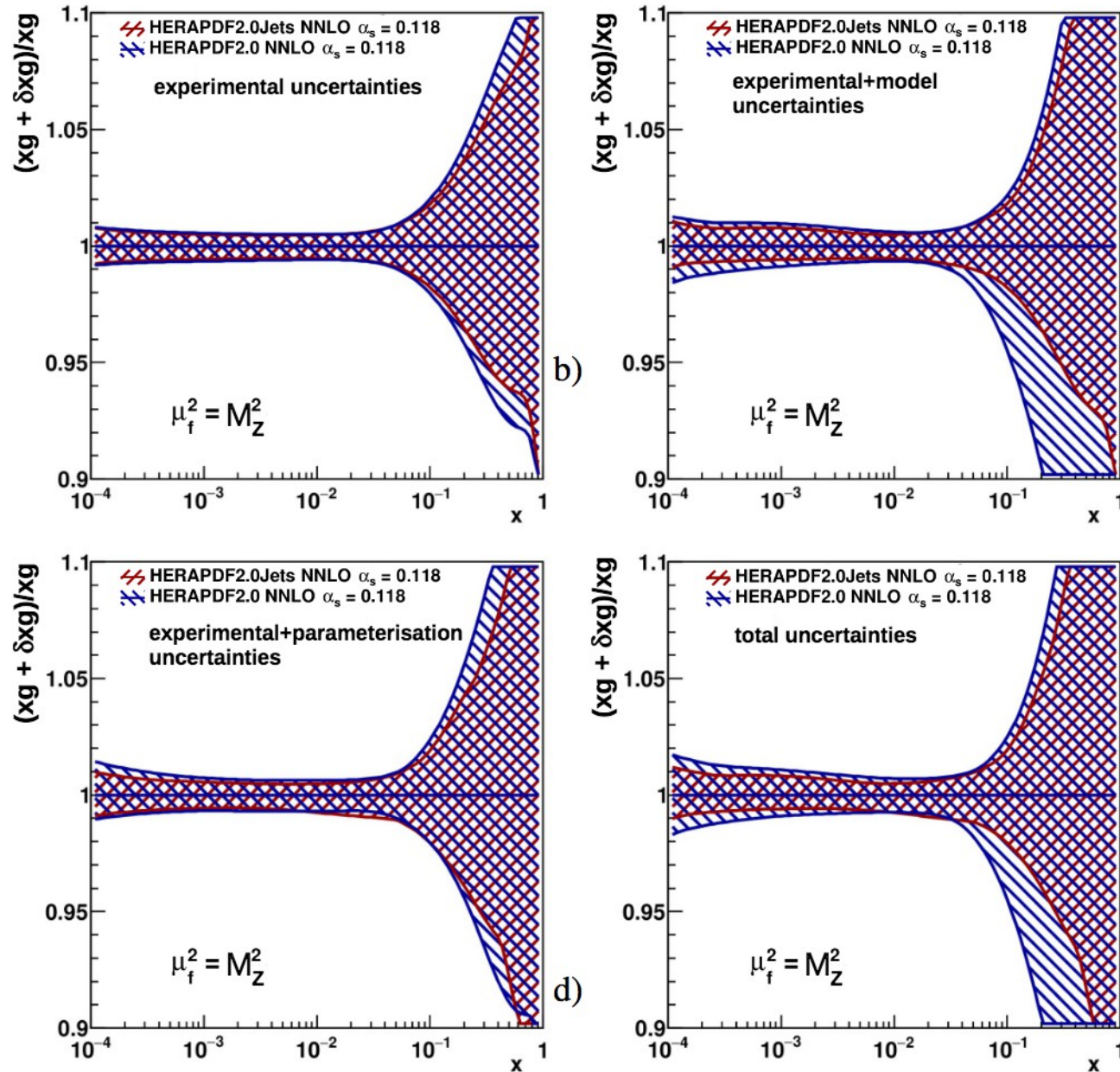
Uncertainties

H1 and ZEUS



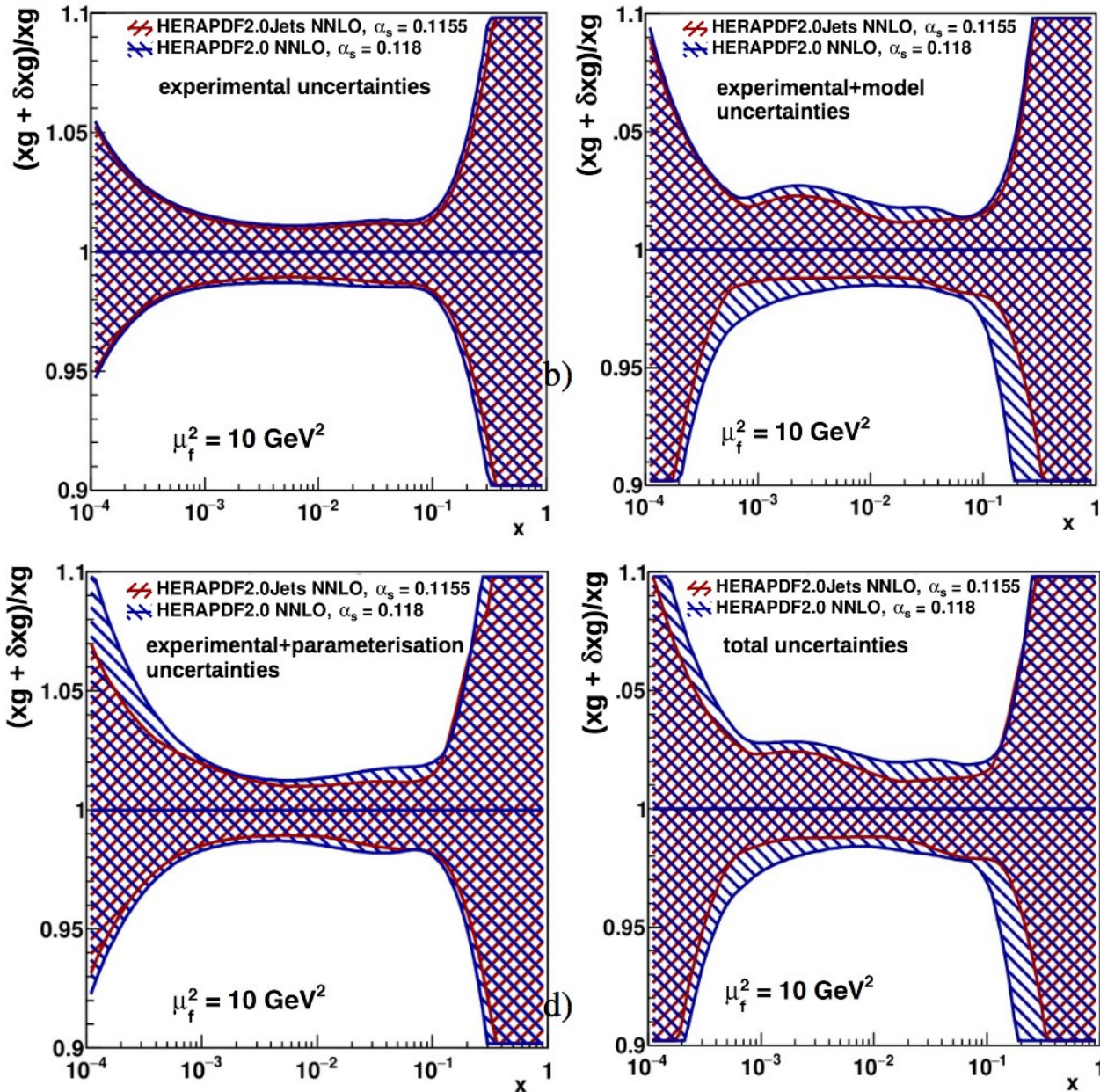
Uncertainties

H1 and ZEUS



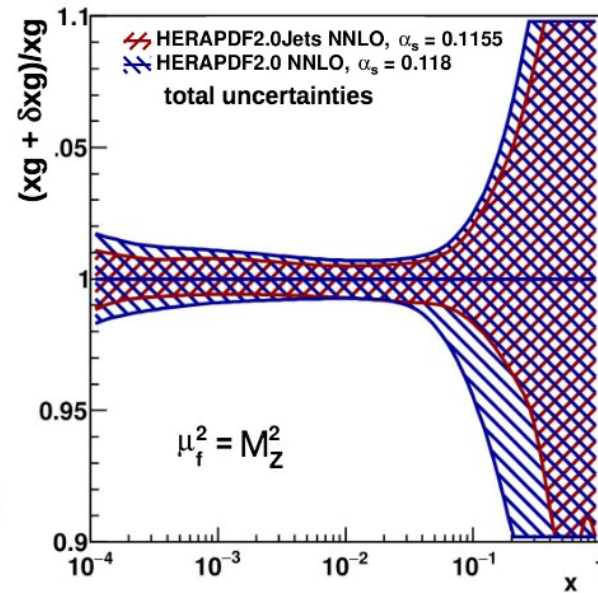
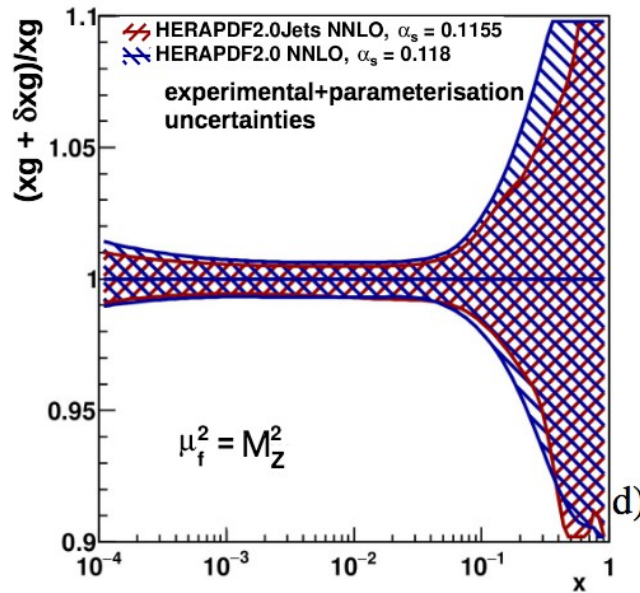
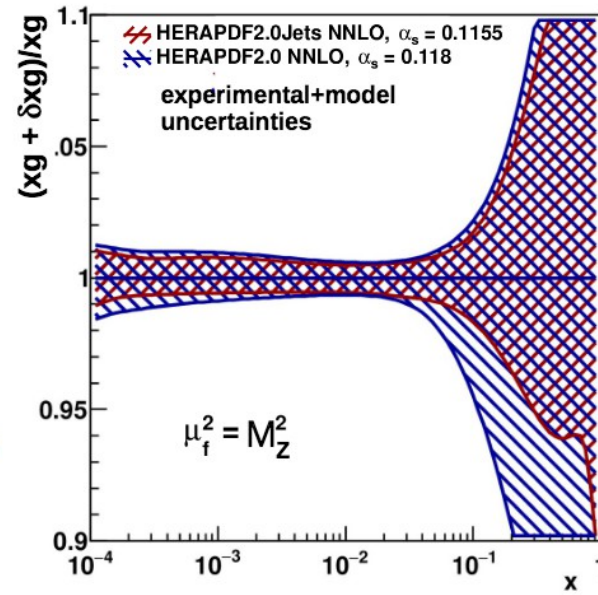
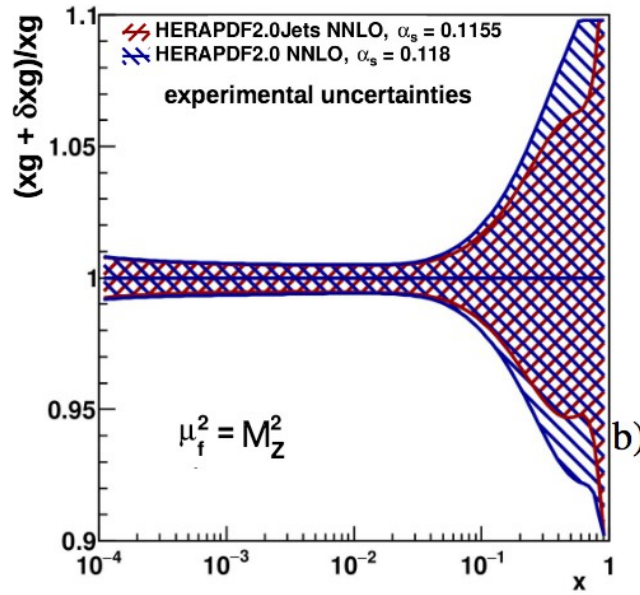
Uncertainties

H1 and ZEUS

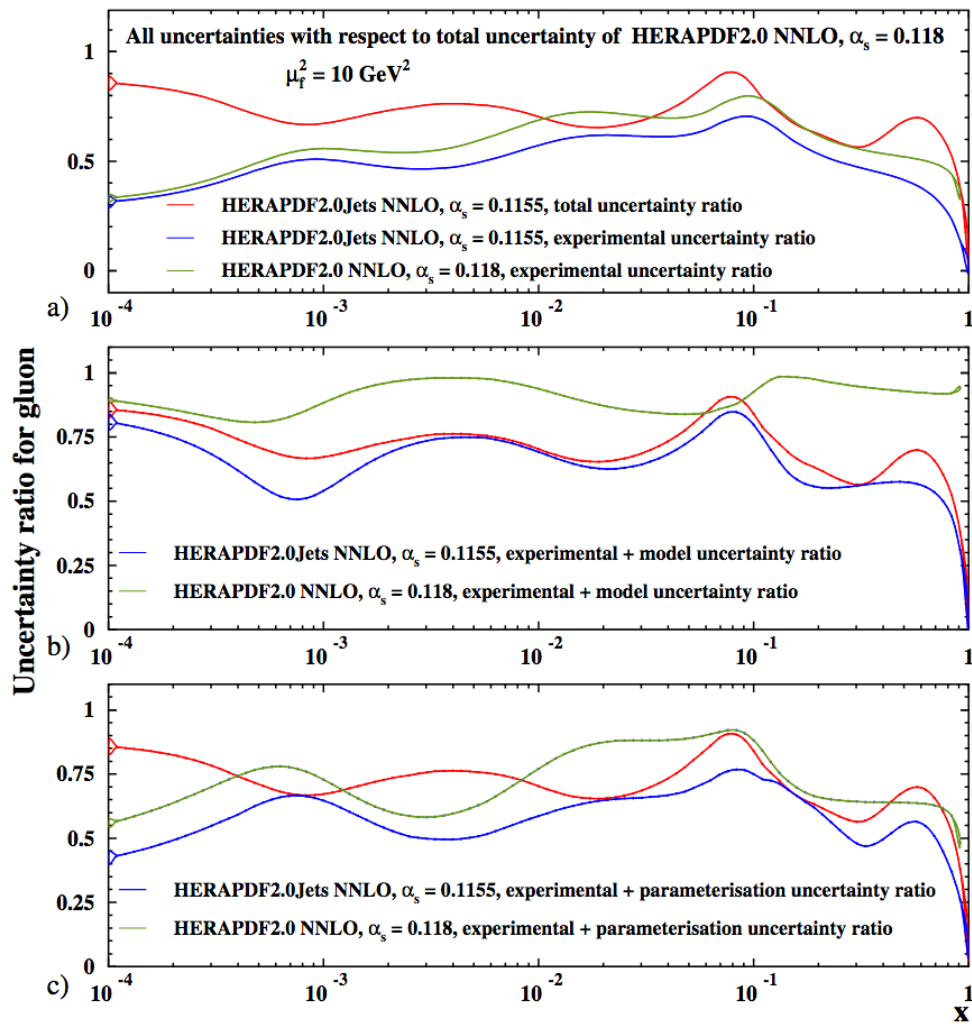


Uncertainties

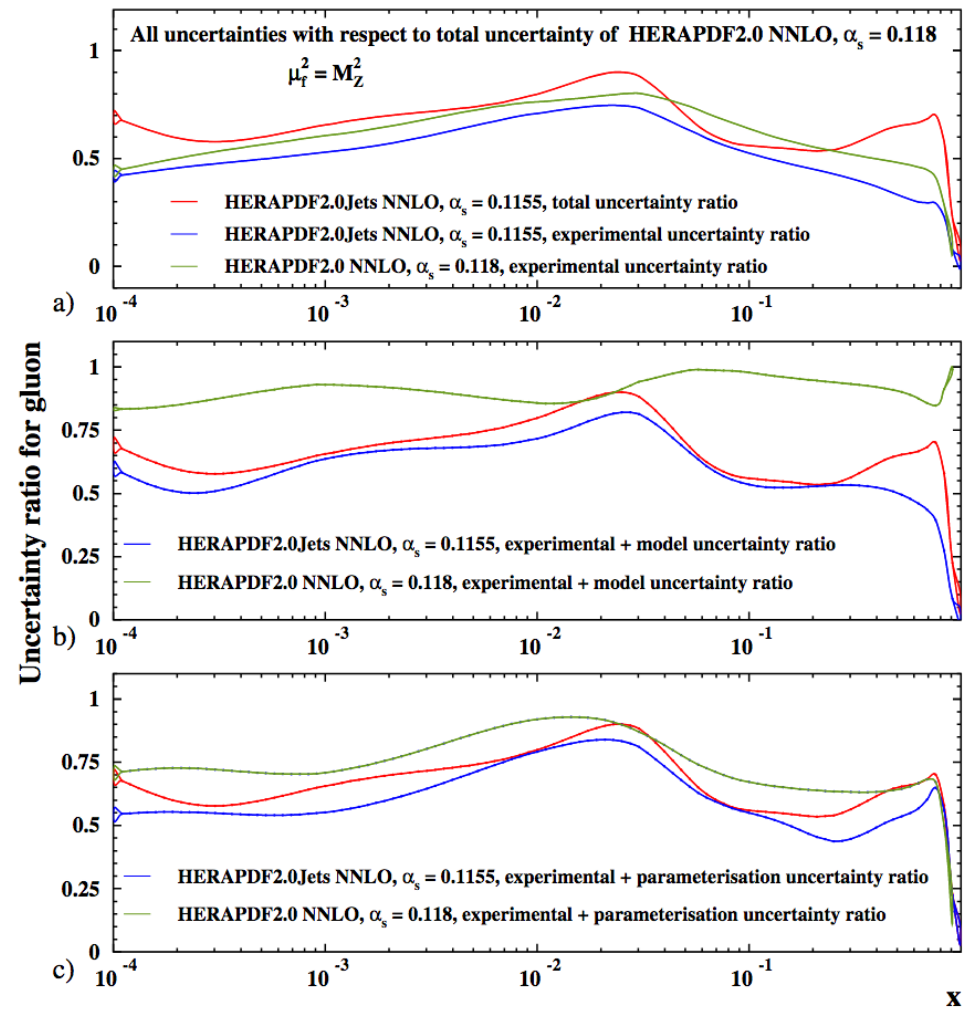
H1 and ZEUS



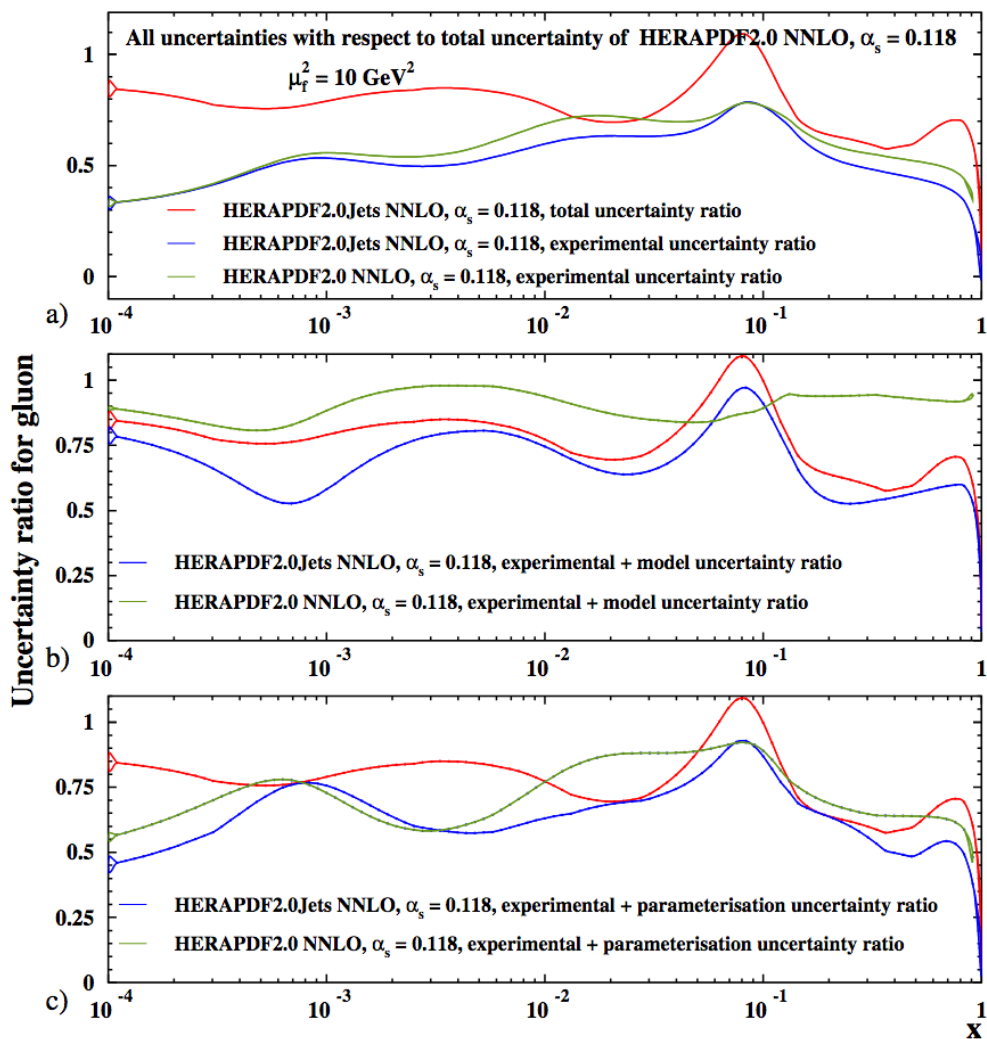
H1 and ZEUS



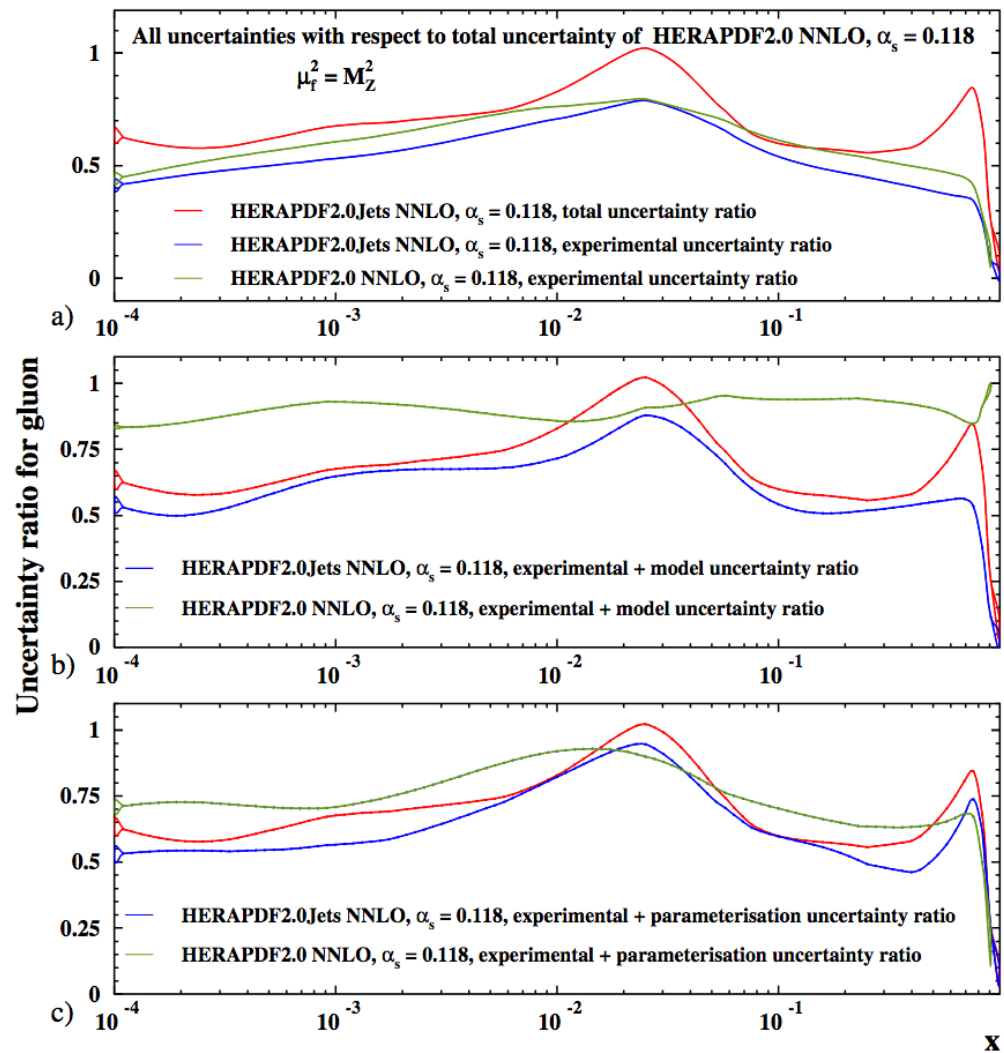
H1 and ZEUS

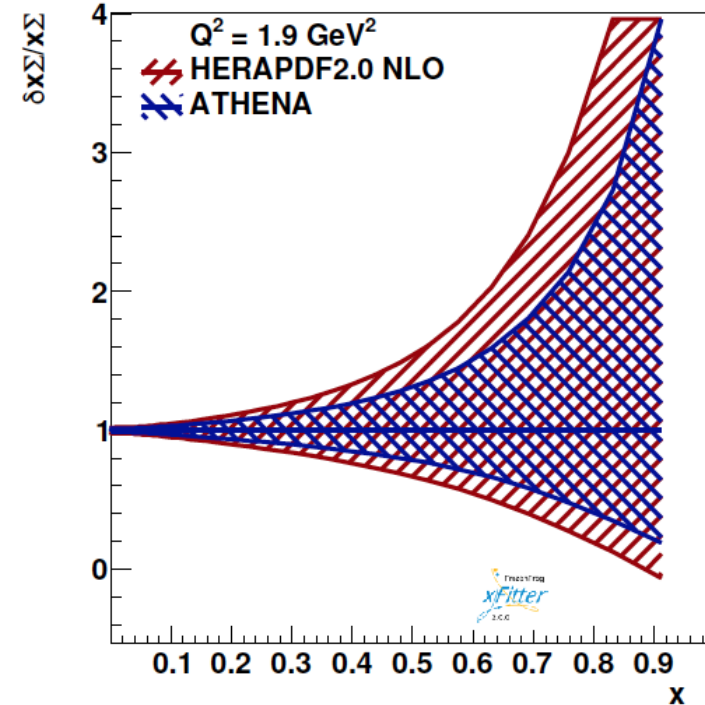
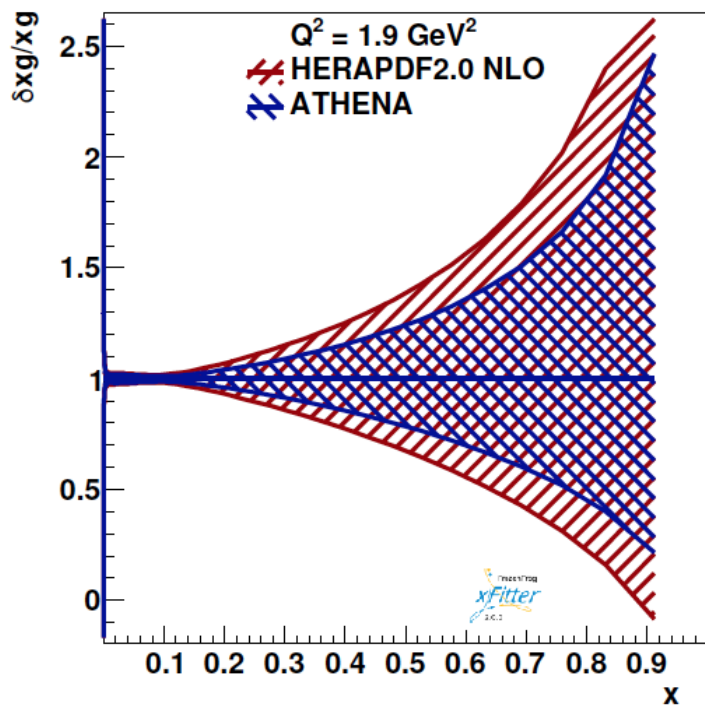
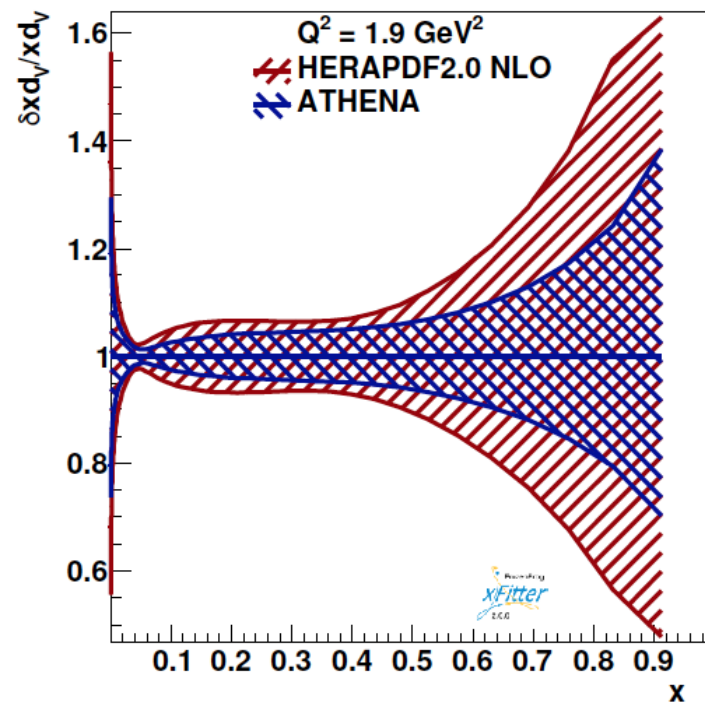
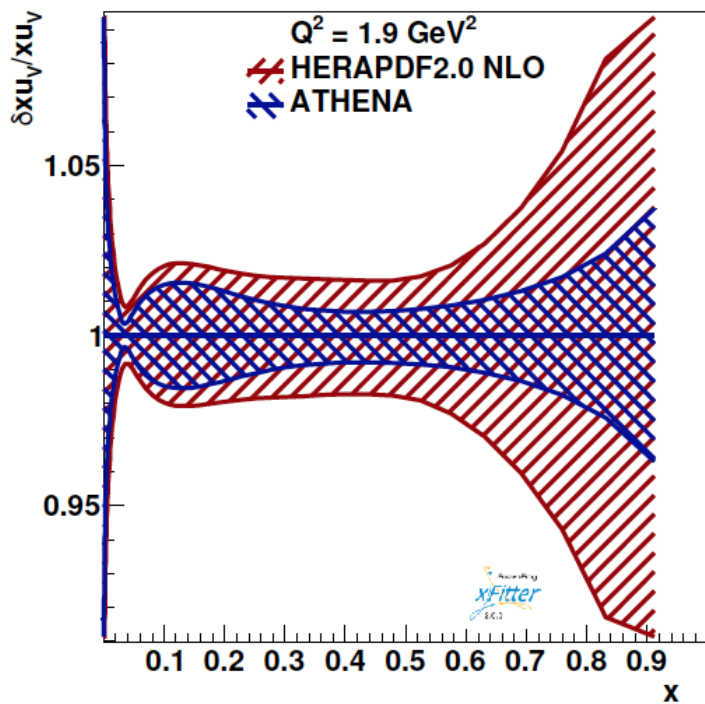


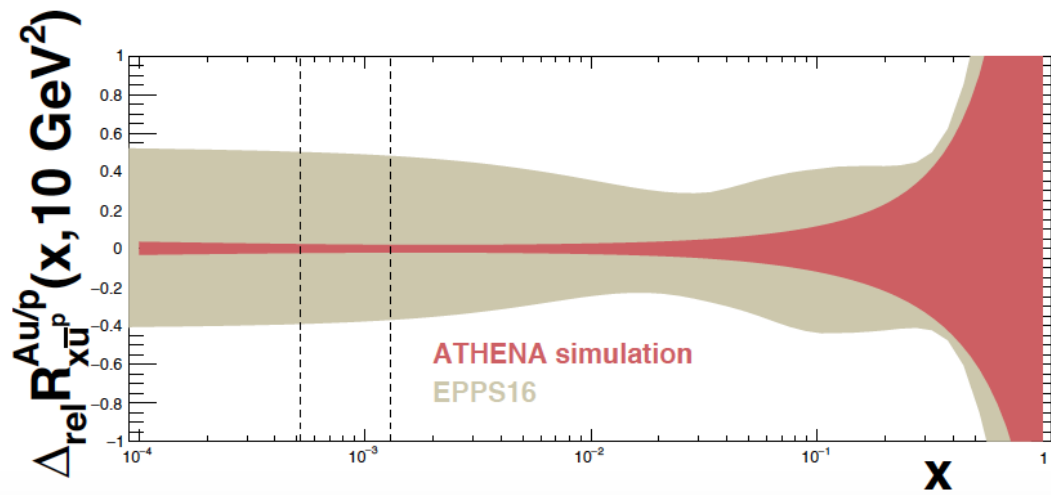
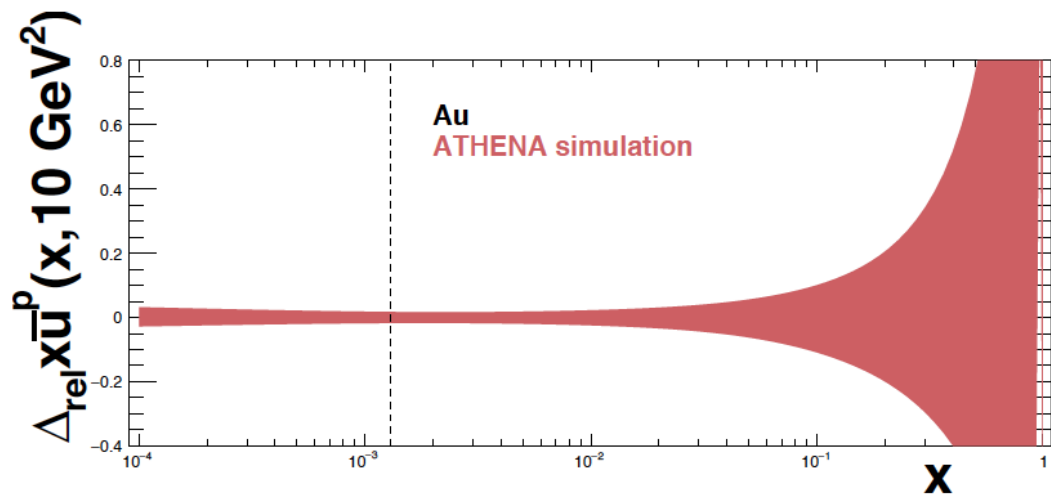
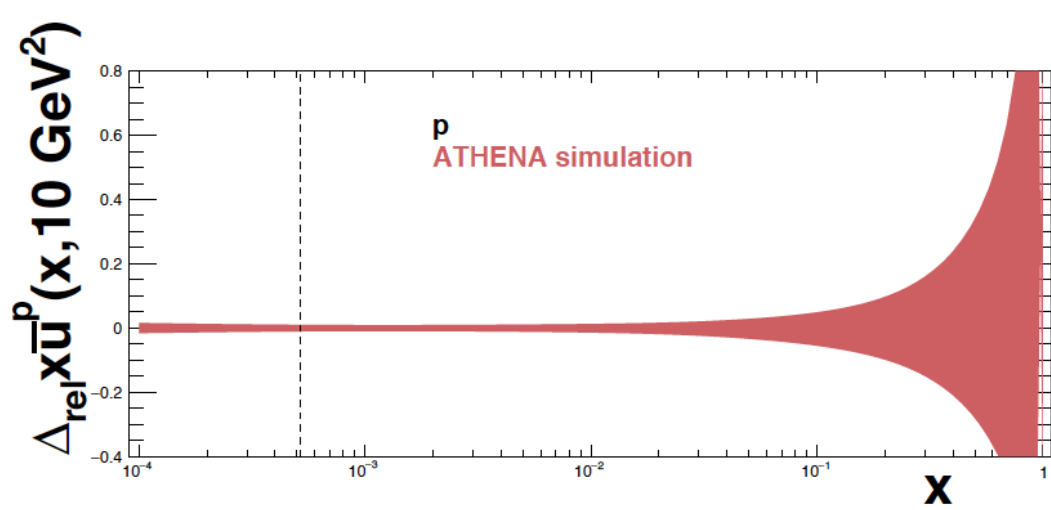
H1 and ZEUS

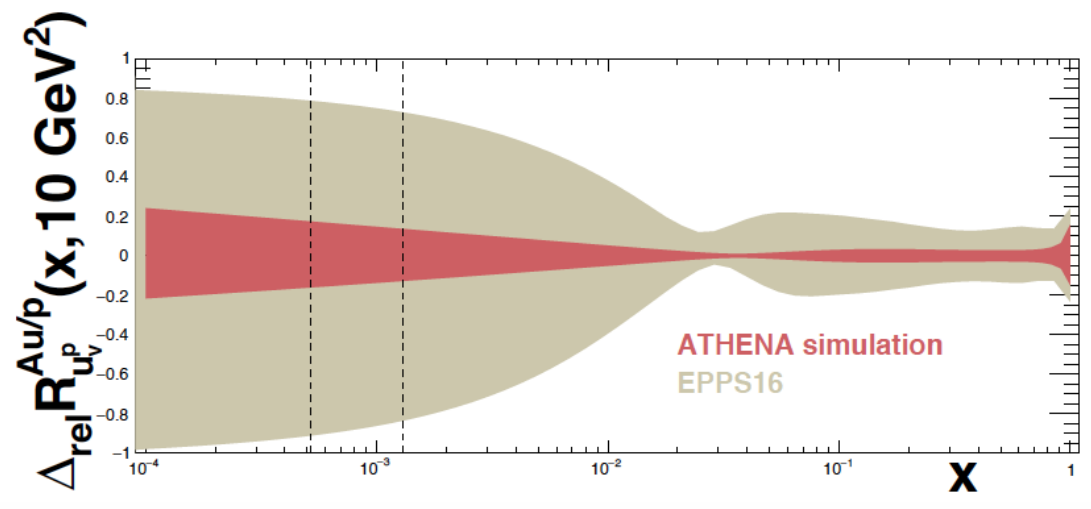
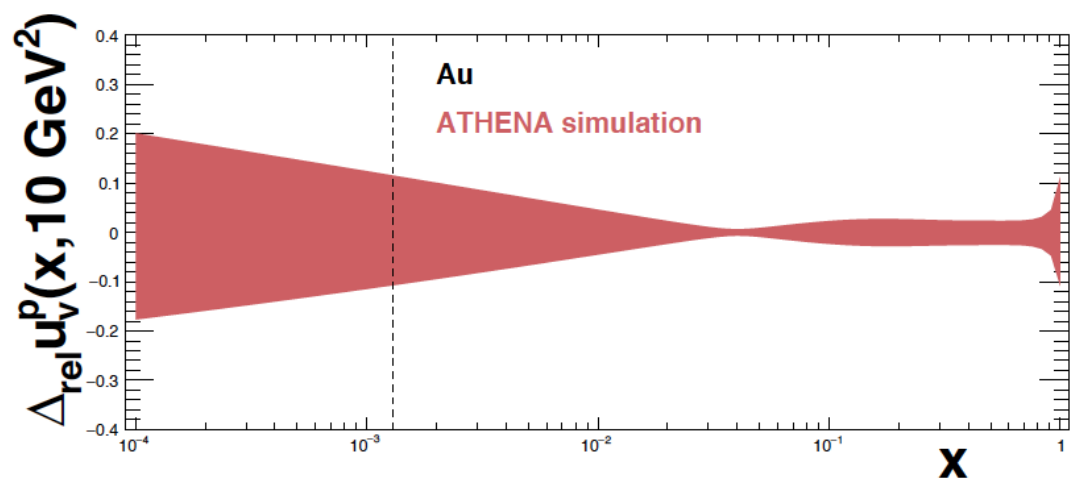
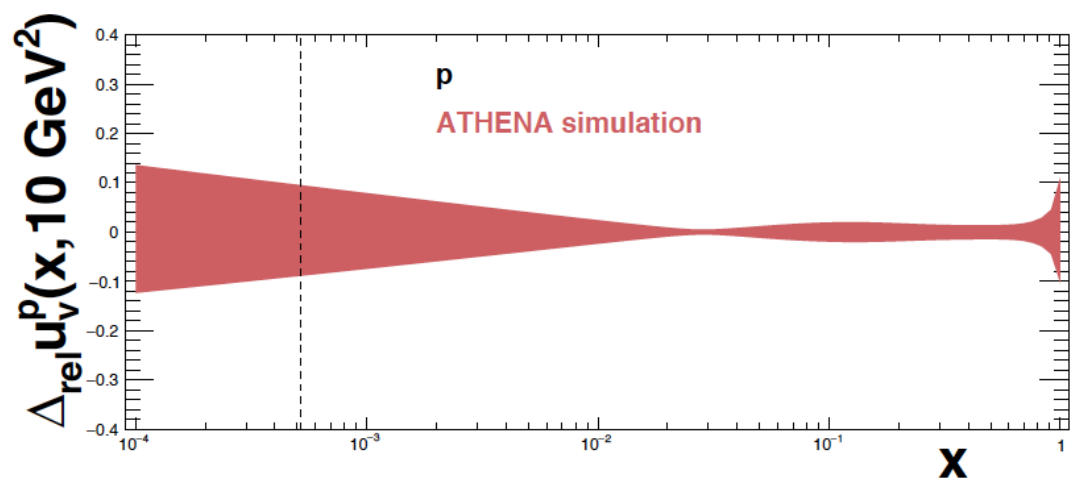


H1 and ZEUS











Fitting procedure in a nutshell:

- parameterize collinear PDF at μ_0^2
- produce PB kernels for collinear & TMD distributions to evolve them to $\mu^2 > \mu_0^2$
[*Eur. Phys. J. C* **74**, 3082 (2014)]
- perform fits to measurements using xFitter frame to extract the initial parametrization (with collinear coefficient functions at NLO)
- store the TMDs in a grid for later use in CASCADE3 [*Eur. Phys. J. C* **81**, no.5, 425 (2021)]
- plot collinear and TMD pdfs within TMDPLOTTER [[arXiv:2103.09741](https://arxiv.org/abs/2103.09741)]

5 FLNS:

- full coupled evolution with all flavors & $\alpha_s(M_Z^{n_f=5}) = 0.118$
- HERAPDF parametrization form
- using full HERA I+II inclusive DIS data ($3.5 < Q^2 < 50000 \text{ GeV}^2$ & $4.10^{-5} < x < 0.65$)
- $\chi^2/dof=1.21$

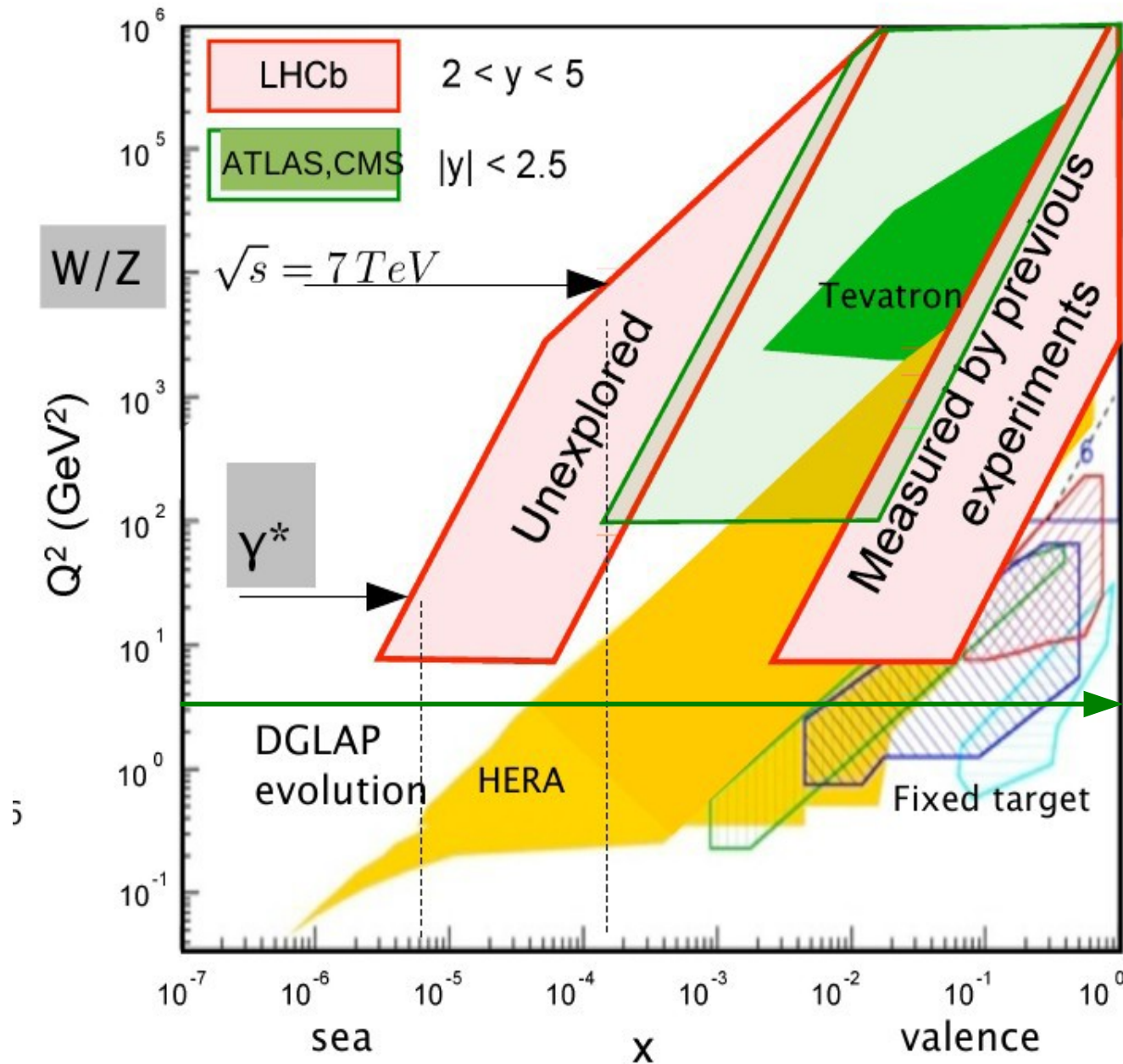
[*Phys. Rev. D* **99** (2019) no. 7, 074008]

4 FLNS:

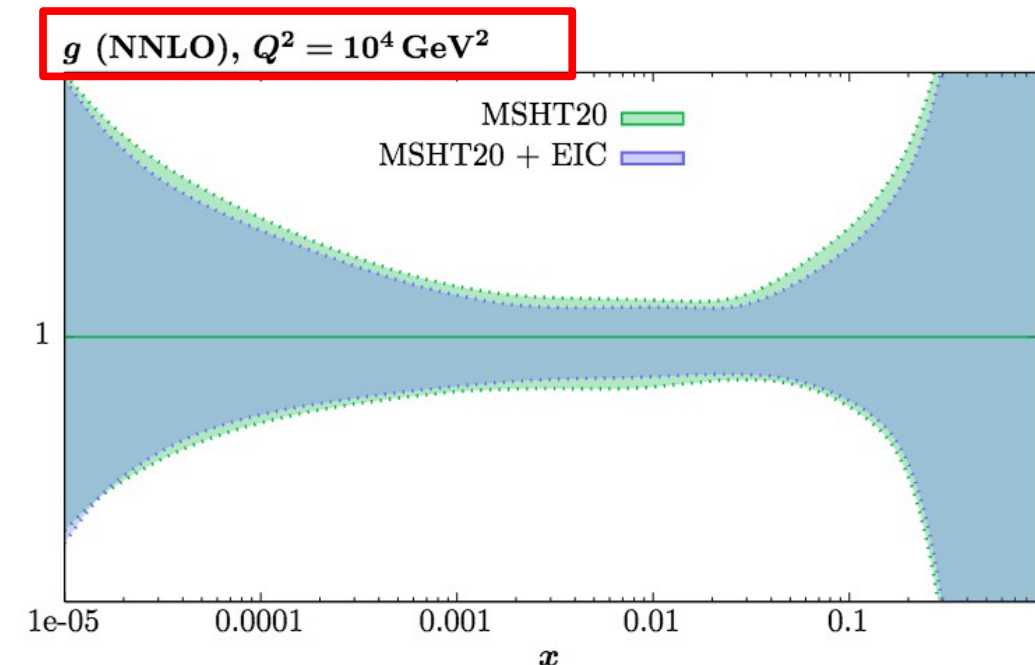
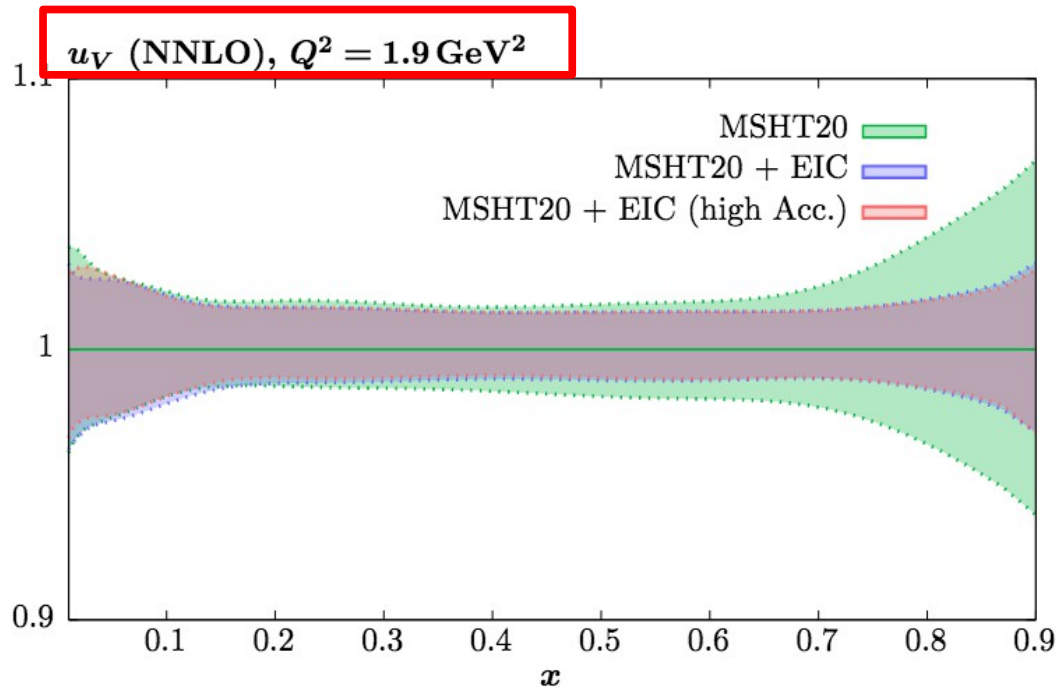
- the same functional form & data as 5FL - parameters are re-fitted
- $m_b \rightarrow \infty$ & $\alpha_s(M_Z^{n_f=4}) = 0.1128$
- $\chi^2/dof = 1.25$

[[arXiv:2106.09791](https://arxiv.org/abs/2106.09791)]

Various data in other PDF sets

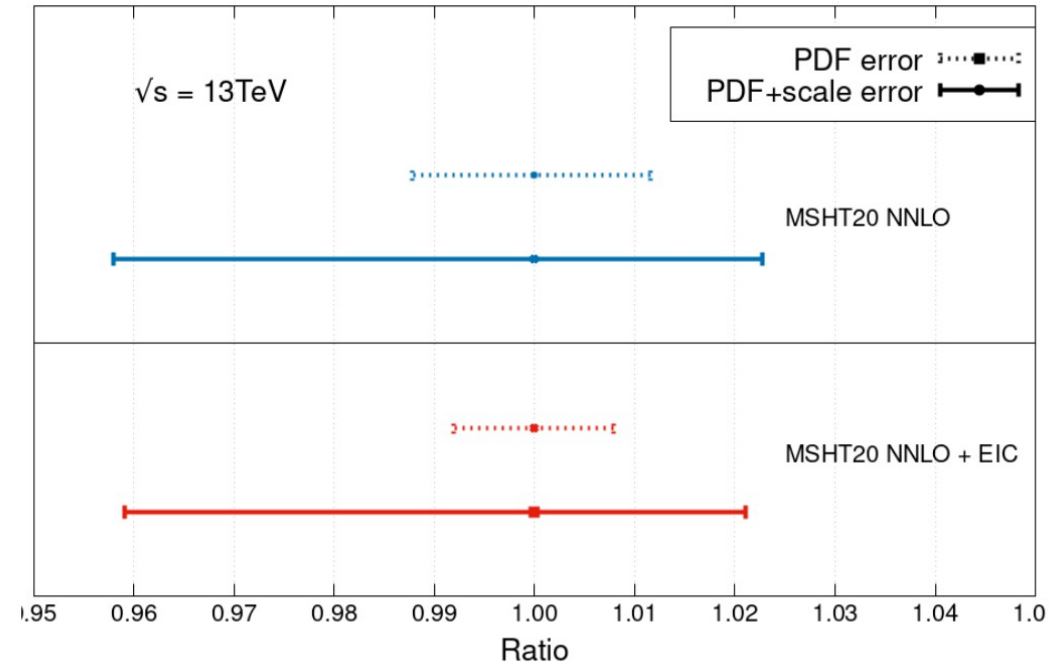
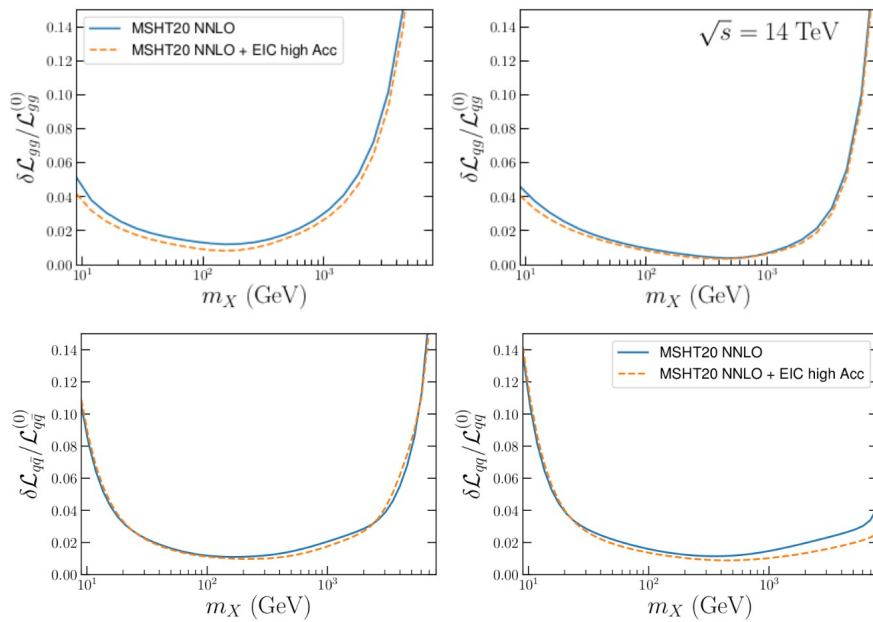


Impact of EIC data on global fits @NNLO



- Full fits with MSHT20 pseud-data
- Improvement significantly reduced compared with HERAPDF2.0
- Still significant effects present
 - biggest impact on up-valence distribution
 - small but valuable improvement on all parton species visible at all x and Q^2 values

Impact of EIC data on global fits @NNLO



- relatively mild improvement for luminosities
→ consistent with changes seen in PDF uncertainties.