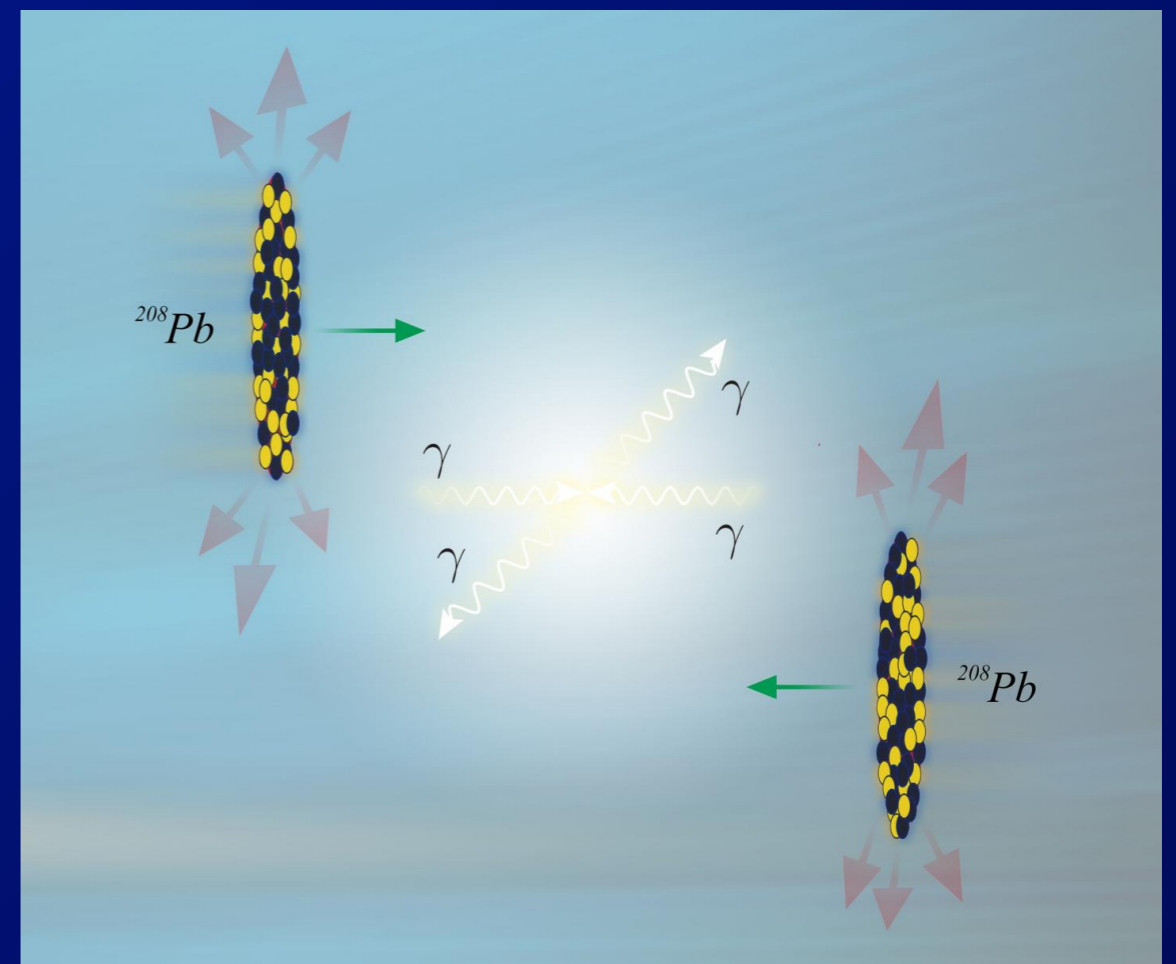


Photon-photon physics in heavy ion collisions

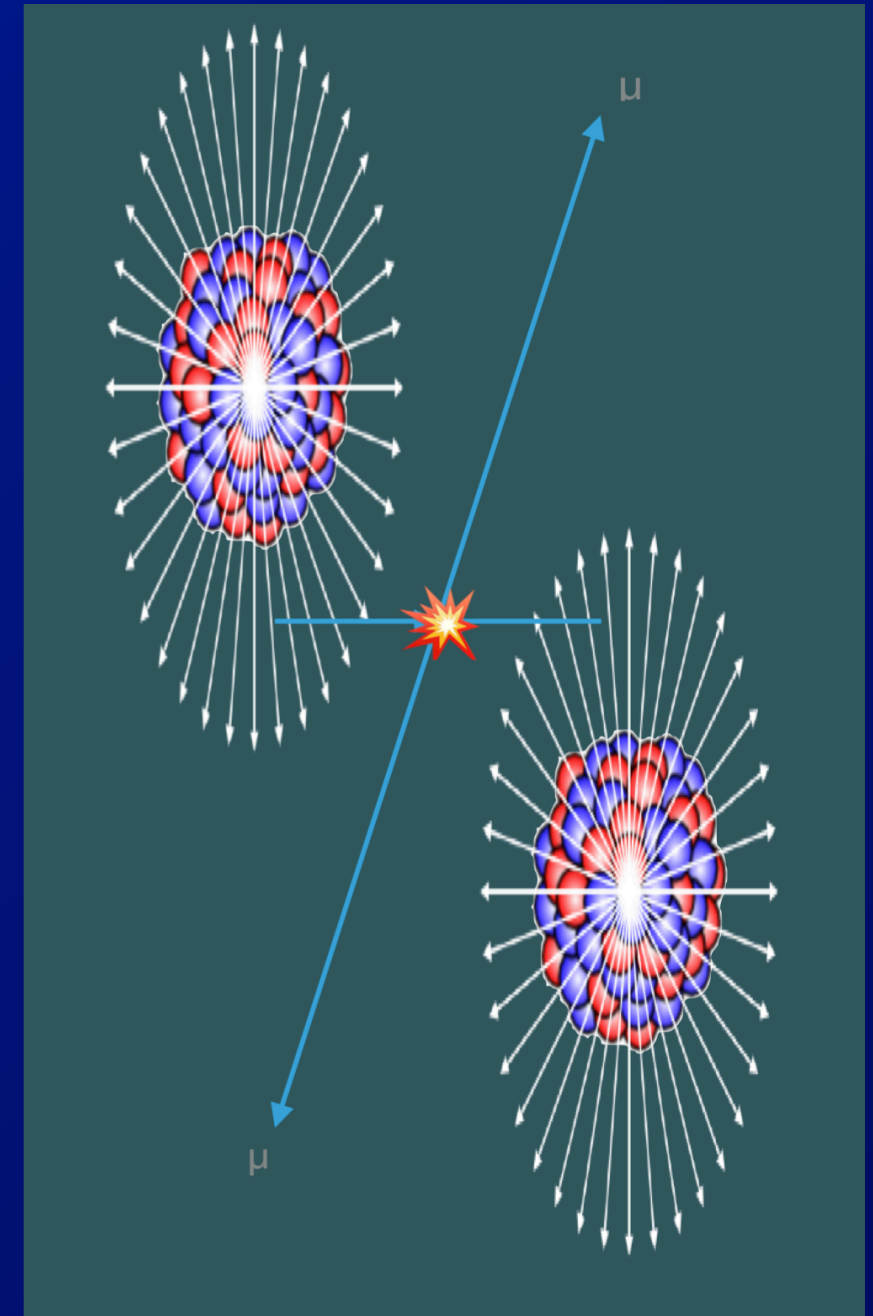
Prof. Brian Cole, Columbia University
October 26, 2023

WILHELM UND ELSE
HERAEUS-STIFTUNG



- **Introduction**
 - Nuclei as sources of quasi-real photons
- **Control measurements: exclusive dilepton**
 - ATLAS and STAR e^+e^-
- **Light-by-light scattering**
 - Measurements, Limits on ALP production
- **$\tau^+\tau^-$ and τ $g-2$ measurement**
 - ATLAS & CMS results
- **Photon k_T distributions**
 - CMS: $\mu^+\mu^-$ acoplanarity vs # forward neutrons
 - ATLAS: $\gamma+\gamma \rightarrow \mu\mu$ in hadronic A+A collisions
- **$\gamma+A \rightarrow$ jets advertisement**
- **Summary**

- **Weizsacker & Williams + Jackson + ... :**
 - Highly relativistic particles act as sources of \sim real photons
- **Finger physics:**
 - When $\lambda > R/\gamma$, or equivalently $E \lesssim \hbar c \gamma/R$, the photons are emitted coherently
 - At LHC, Pb+Pb @ 5.02 TeV, coherence condition is $E \lesssim 80$ GeV
 - **(Coherent) Photon flux** $\propto Z^2$
 - $\gamma+\gamma$ luminosity $\propto Z^4$
- **During heavy ion operation, the LHC is also a Large Photon Collider**
 - $\Rightarrow \sqrt{s} > 100$ GeV



EPA, STARlight, geometry

- Until recently, calculations of the photon flux in UPC collisions started with textbook formula
 - photon flux density for given energy, k at a perpendicular distance, r_{\perp}

$$\Rightarrow N(k, b) = \frac{Z^2 \alpha}{\pi^2} \frac{k}{(\hbar c)^2} \frac{1}{\gamma^2} \left[K_1^2(x) + \frac{1}{\gamma^2} K_0^2(x) \right] \quad x \equiv \frac{k r_{\perp}}{\gamma \hbar c}$$

\Rightarrow correlation between r_{\perp} and energy

EPA, STARlight, geometry

- Until recently, calculations of the photon flux in UPC collisions started with textbook formula

– photon flux density for given energy, k at a perp. distance, r_{\perp}

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\Rightarrow correlation between r_{\perp} and energy

- geometric convolution w/ no-hadronic interaction factor

– e.g. STARlight formula for $\gamma+\gamma$:

$$\Rightarrow \frac{d^2 N_{\gamma\gamma}(k_1, k_2)}{dk_1 dk_2} = \int \int d^2 b_1 d^2 b_2 P_{\text{NOHAD}}(|\vec{b}_1 - \vec{b}_2|) N(k_1, \vec{b}_1) N(k_2, \vec{b}_2)$$

- But, in textbook or literature, handling of $r_{\perp} < R$, unsettled

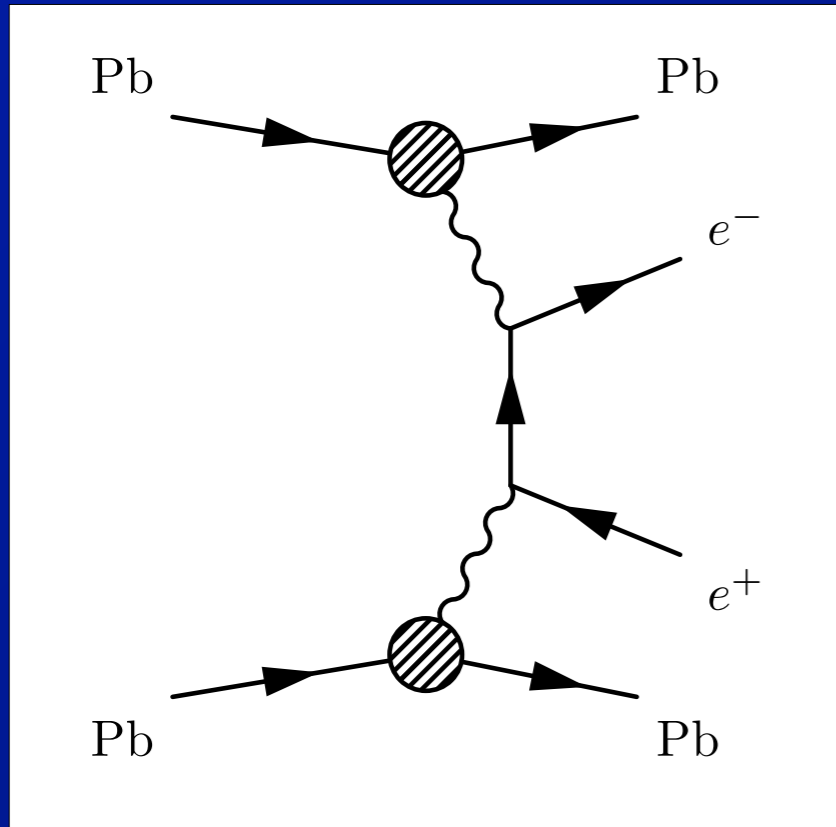
\Rightarrow For example, STARlight neglects photons w/ $r_{\perp} < R$

\Rightarrow SuperChic does not

$\gamma+\gamma$ production of
dileptons

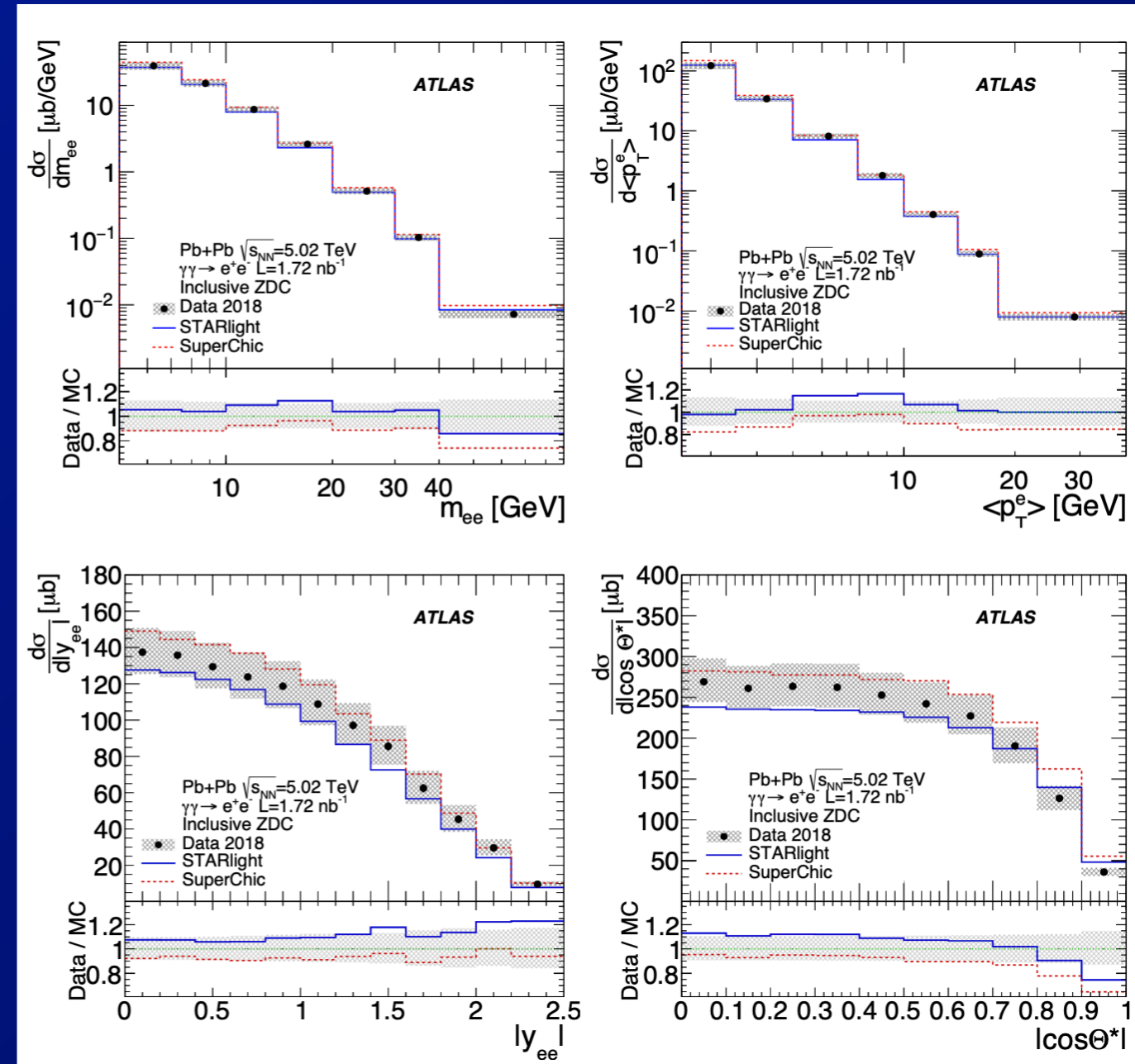
Dilepton production in $\gamma+\gamma$ collisions

- At leading order in QED the $\gamma+\gamma \rightarrow l^+l^-$ process is simple



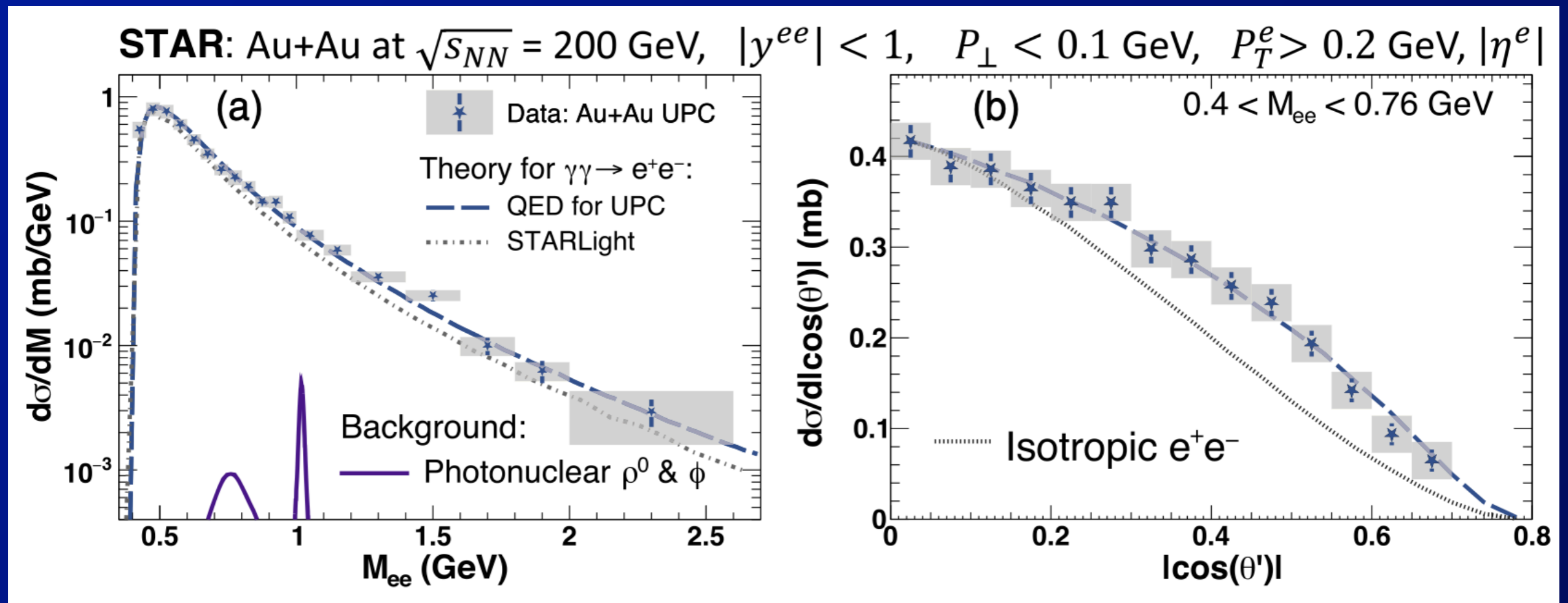
- Well-established calculations
- High-statistics measurements
- Good agreement with theory**

⇒ Declare success



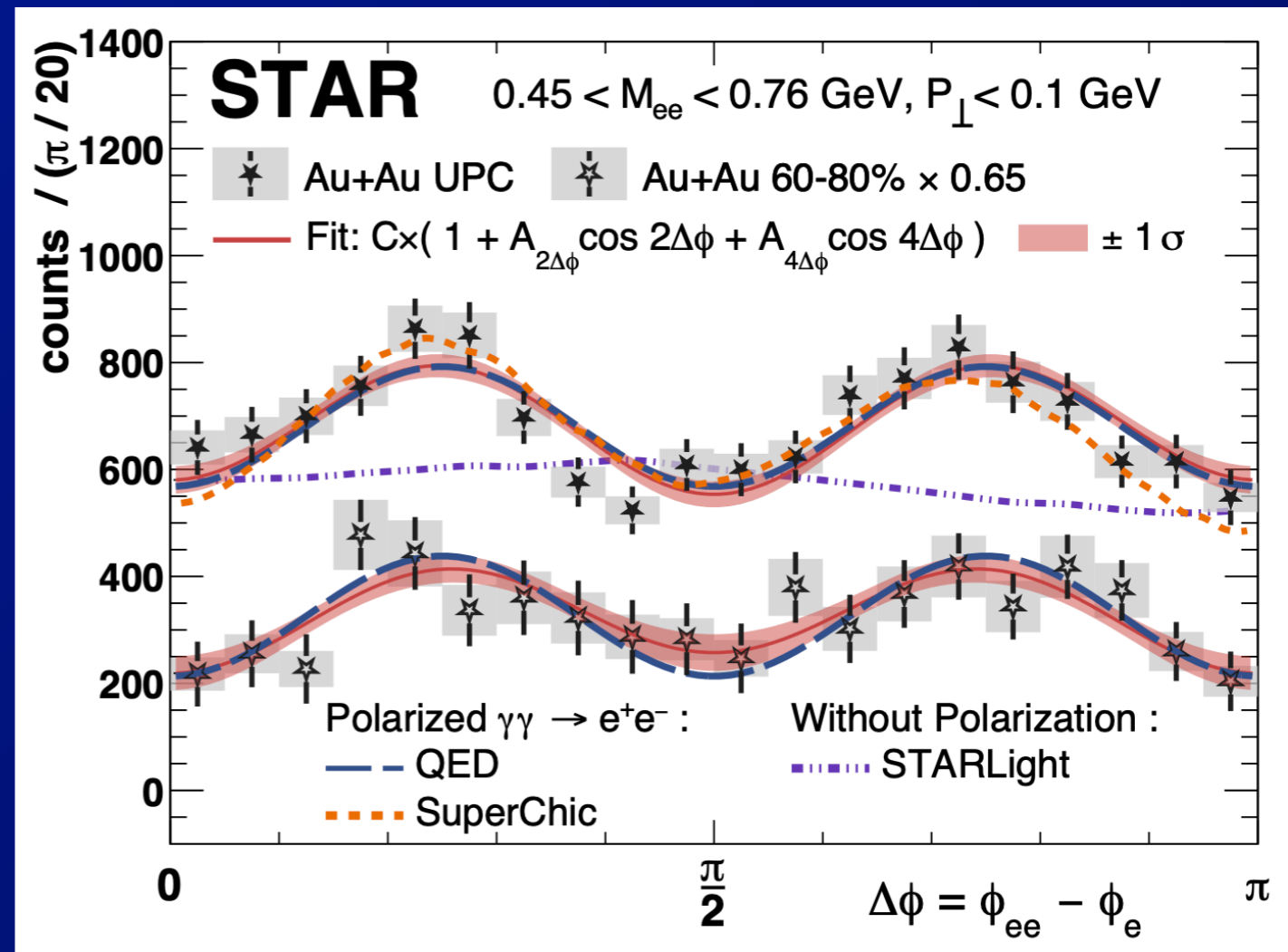
ATLAS UPC e^+e^-
JHEP 06 (2023) 182

- STAR UPC $\gamma+\gamma\rightarrow e^+e^-$ in 200 GeV Au+Au ($L_{\text{int}} = 70 \mu\text{b}^{-1}$)
 $-0.4 < M_{ee} < 2.6 \text{ GeV}$, $p_{Tee} < 0.1 \text{ GeV}$, $|y_{ee}| < 1$
- Compared to STARLight and “QED” calculation
 \Rightarrow STARLight slightly underpredicts data
 \Rightarrow QED calculation agrees well with data



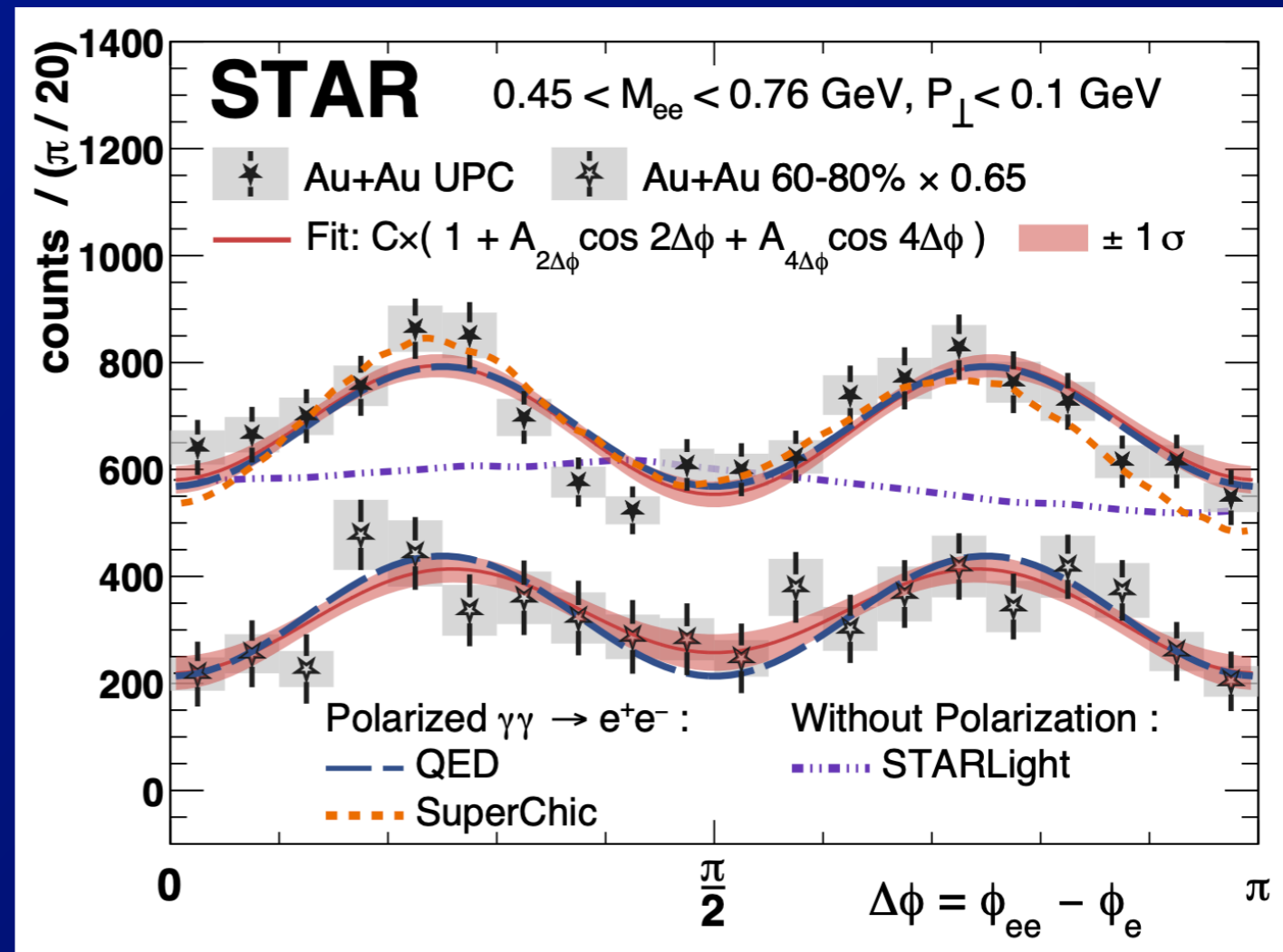
STAR exclusive e^+e^-

- First measurement of the angular correlation between lepton pair p_T vector and lepton ϕ angles
 - possible due to the low electron p_T values and \ll material



- First measurement of the angular correlation between lepton pair p_T vector and lepton ϕ angles
 - possible due to the low electron p_T values and \ll material

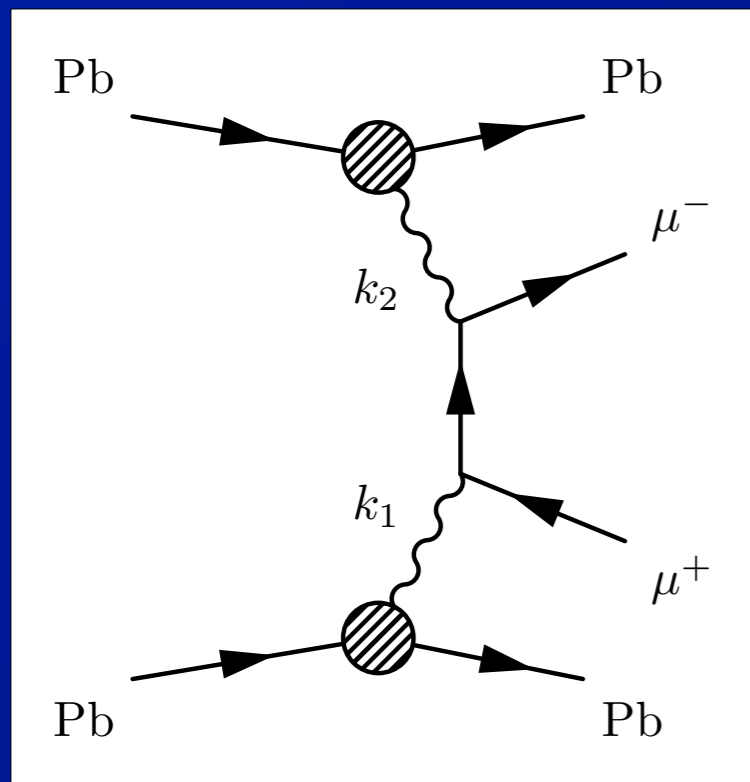
- Compare to calculations:
 - Reasonable agreement with QED and SuperChic
 - \Rightarrow QED: $\cos(4\Delta\phi)$ modulation from linear polarization of the photons



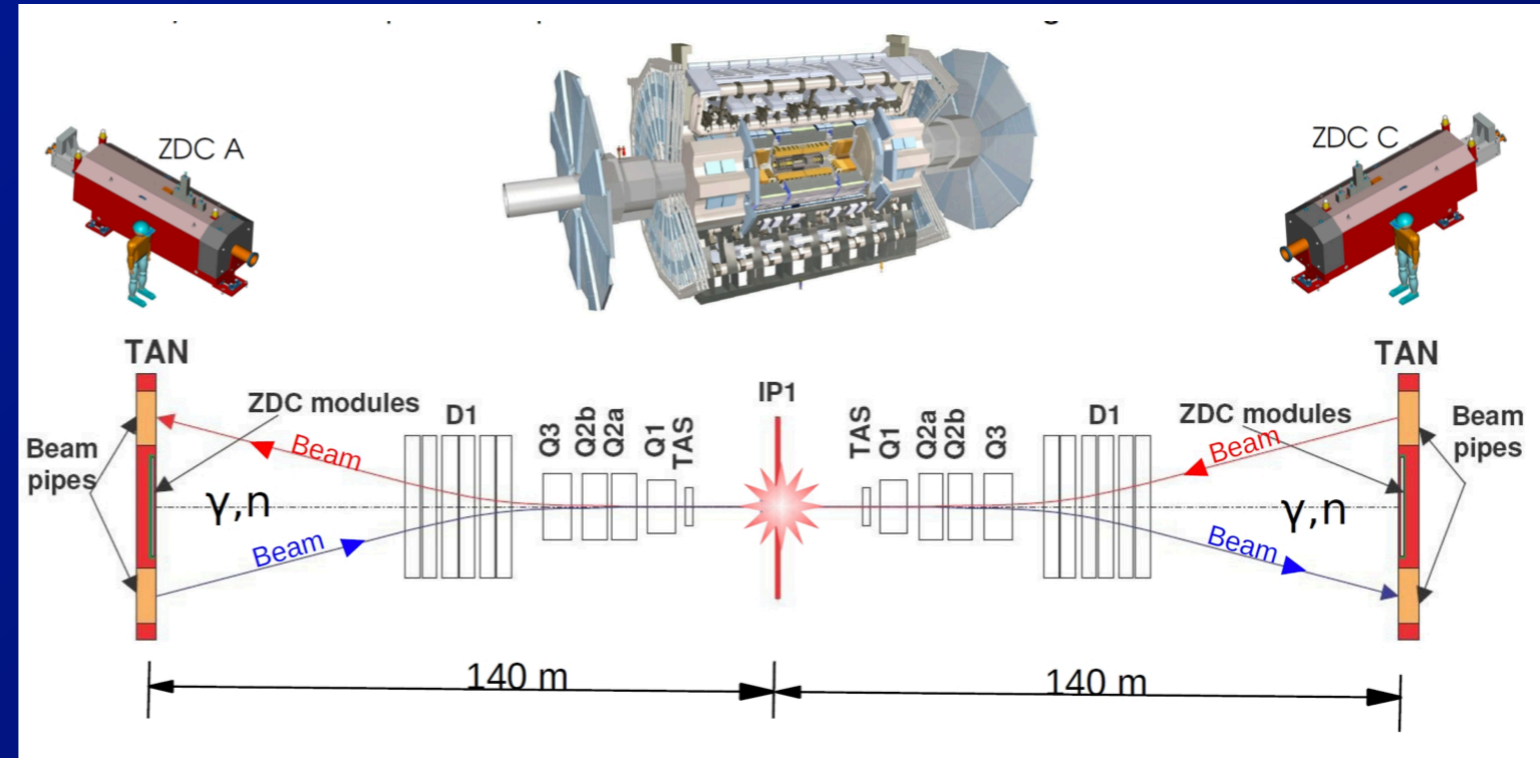
$\gamma+\gamma$ scattering and
forward neutrons

Nuclear breakup via Coulomb Excitation 12

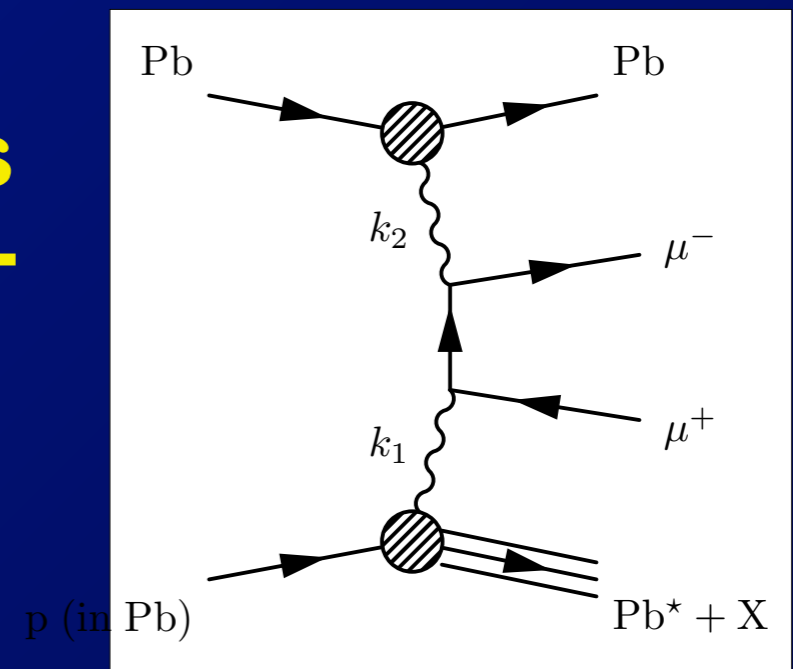
- In Pb+Pb $\gamma+\gamma$, coherent photons dominate
 \Rightarrow Nominally: no forward neutrons in 0 degree calorimeters



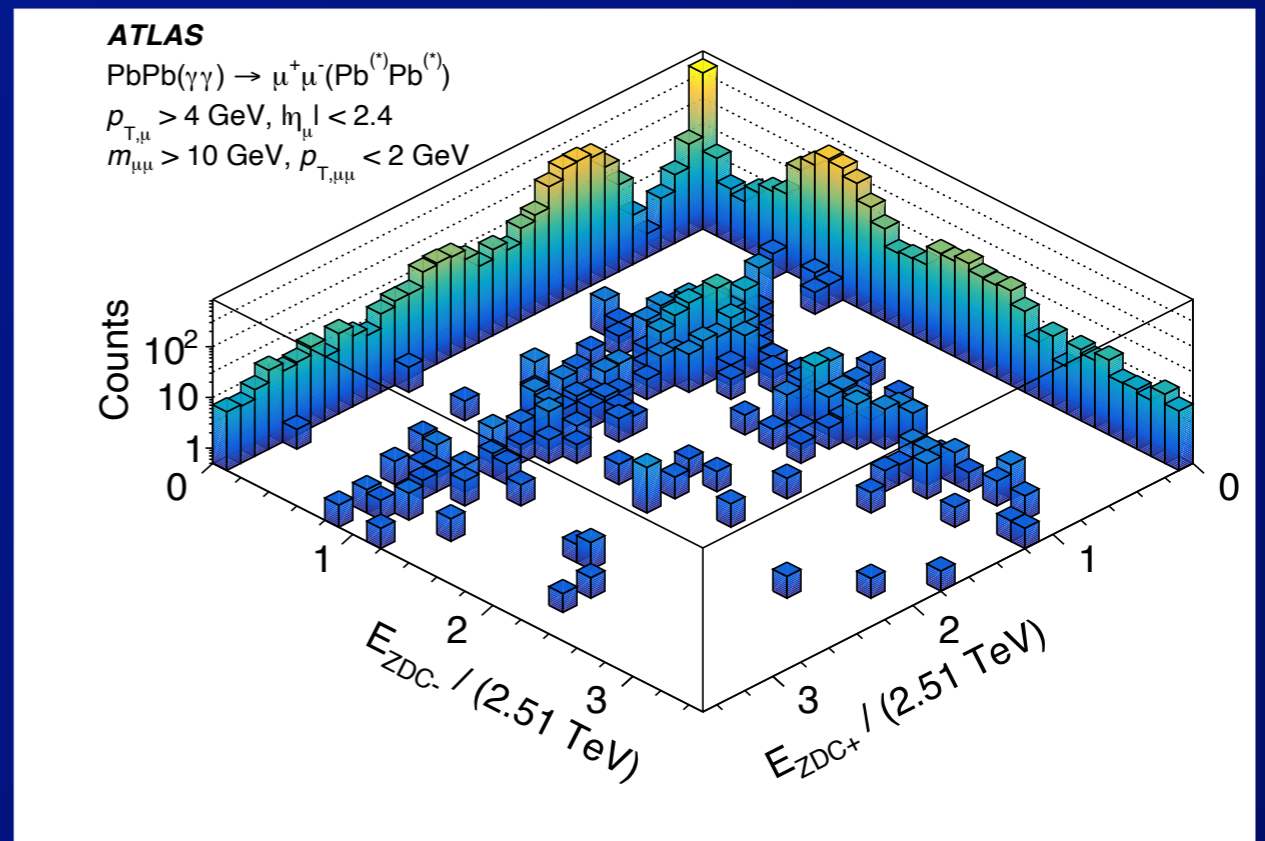
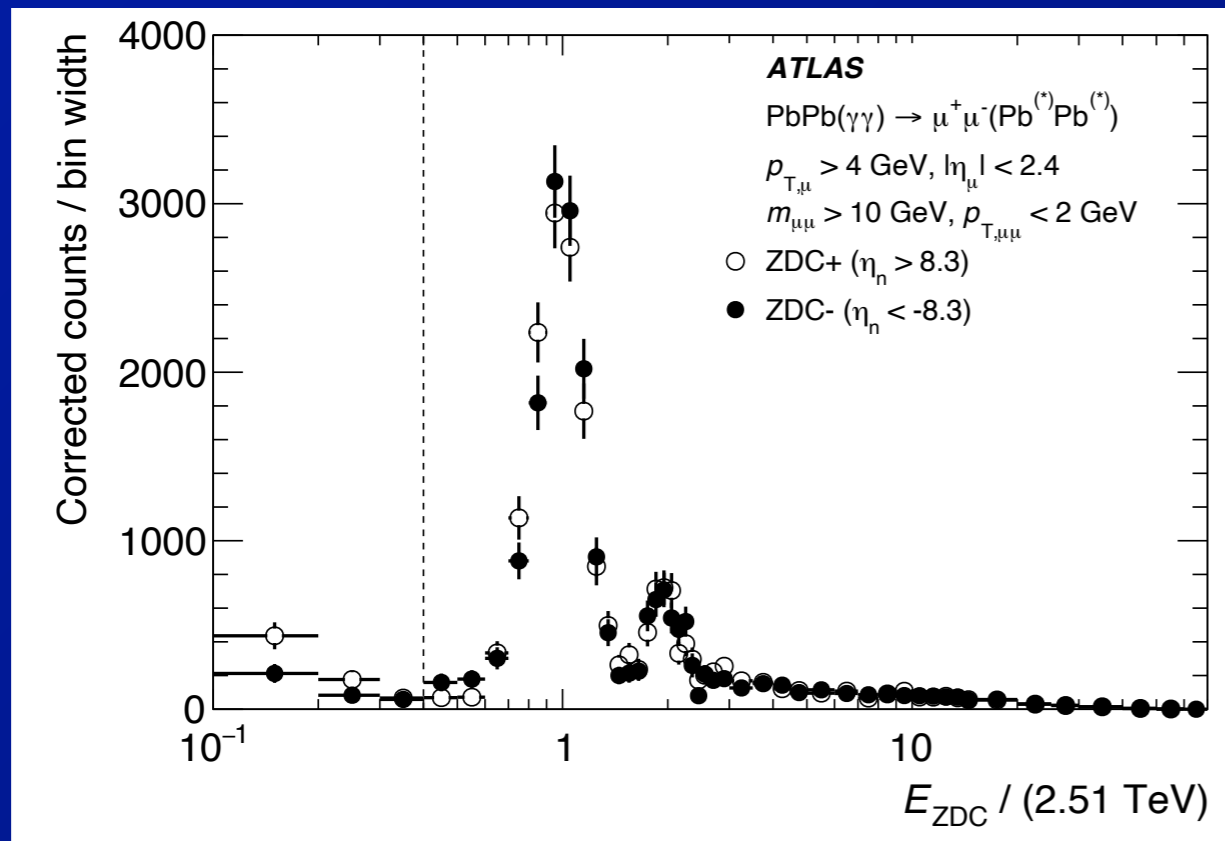
“0n0n”



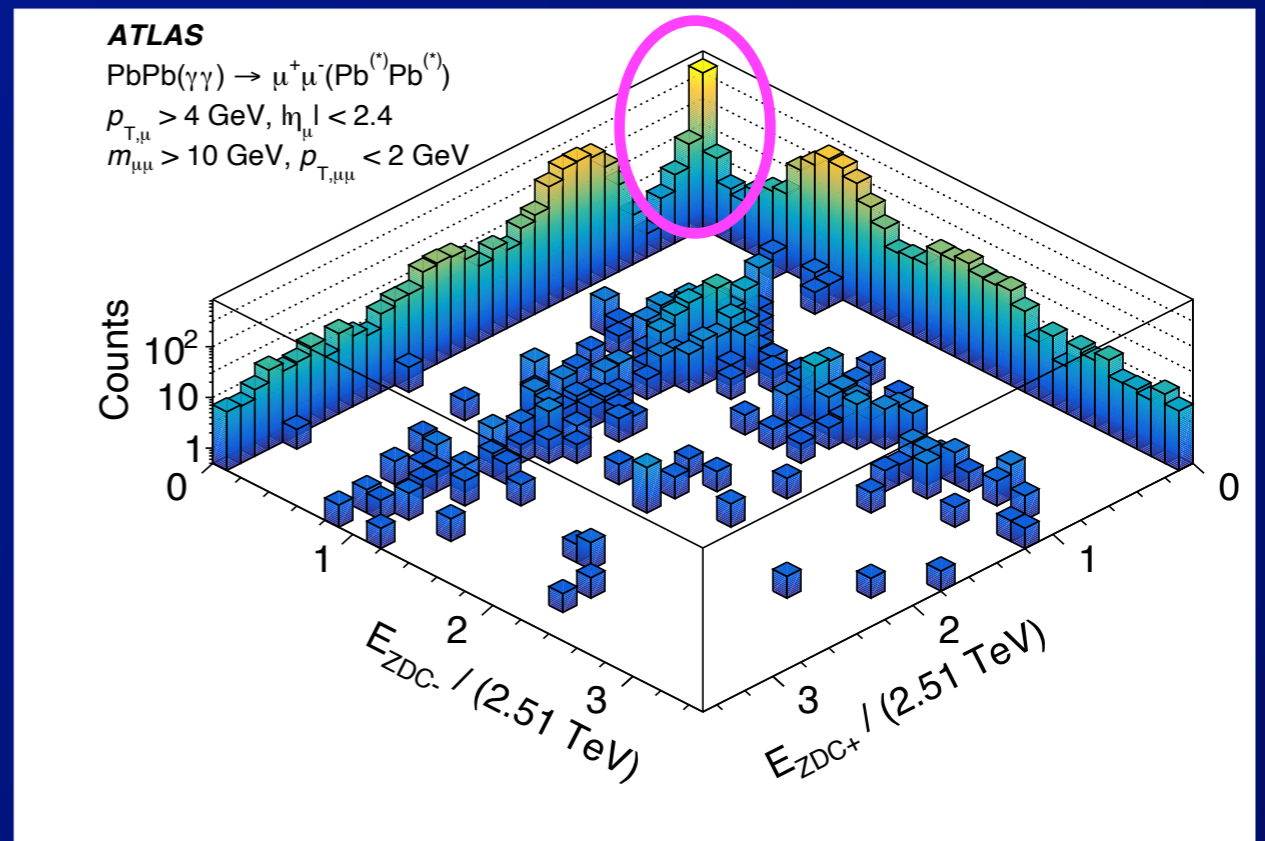
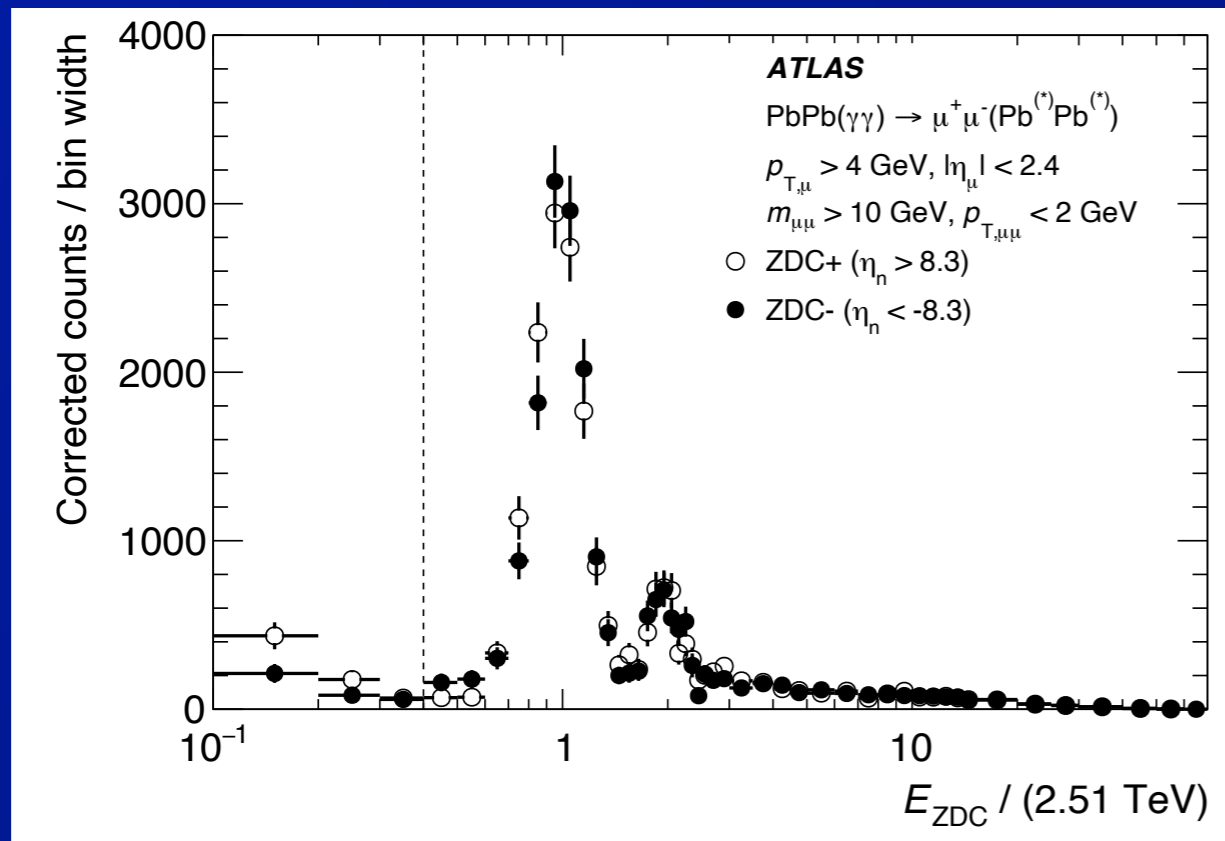
- However, long-range EM interactions can induce giant dipole resonance++
 \Rightarrow Emission of 1 or more neutrons by one or both nuclei
 \Rightarrow Explore with ATLAS $\gamma+\gamma \rightarrow \mu+\mu^-$



- Event topology as seen in the two ZDCs

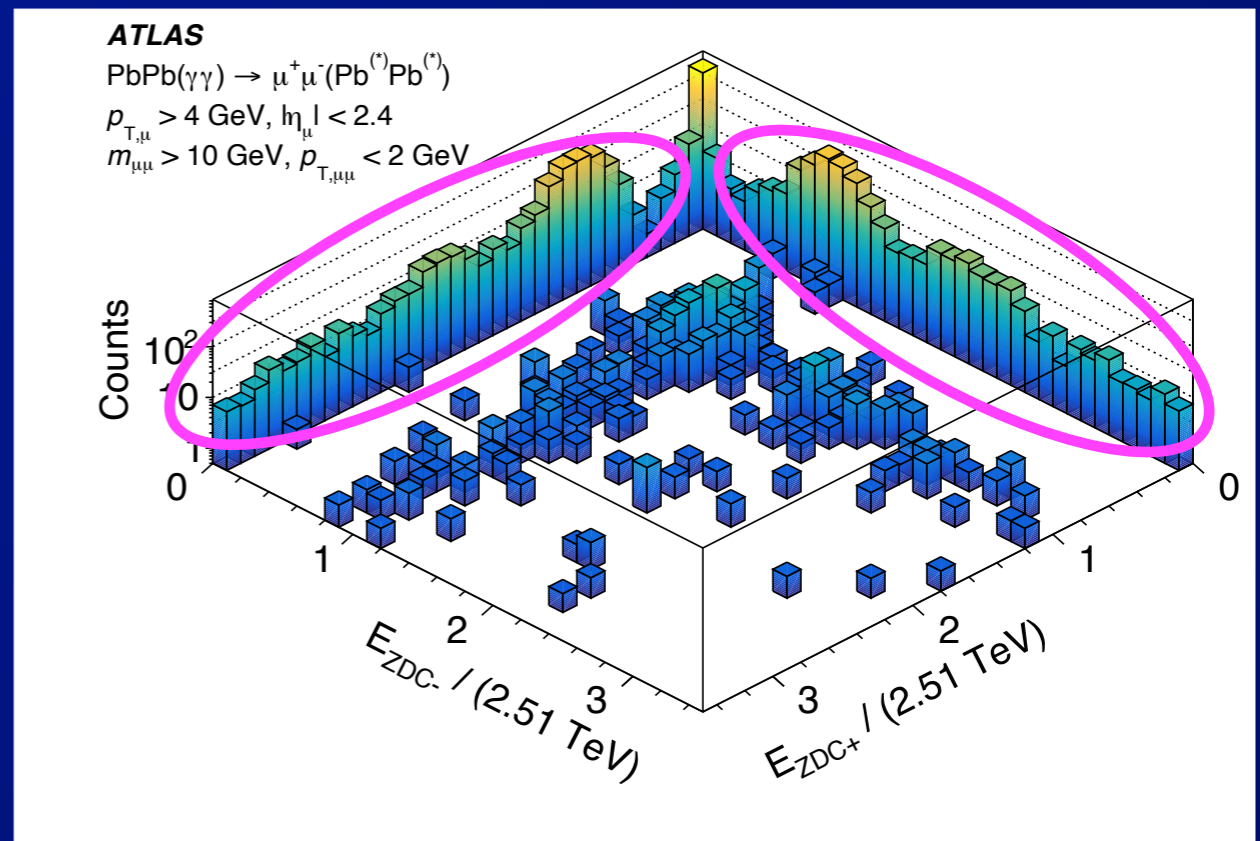
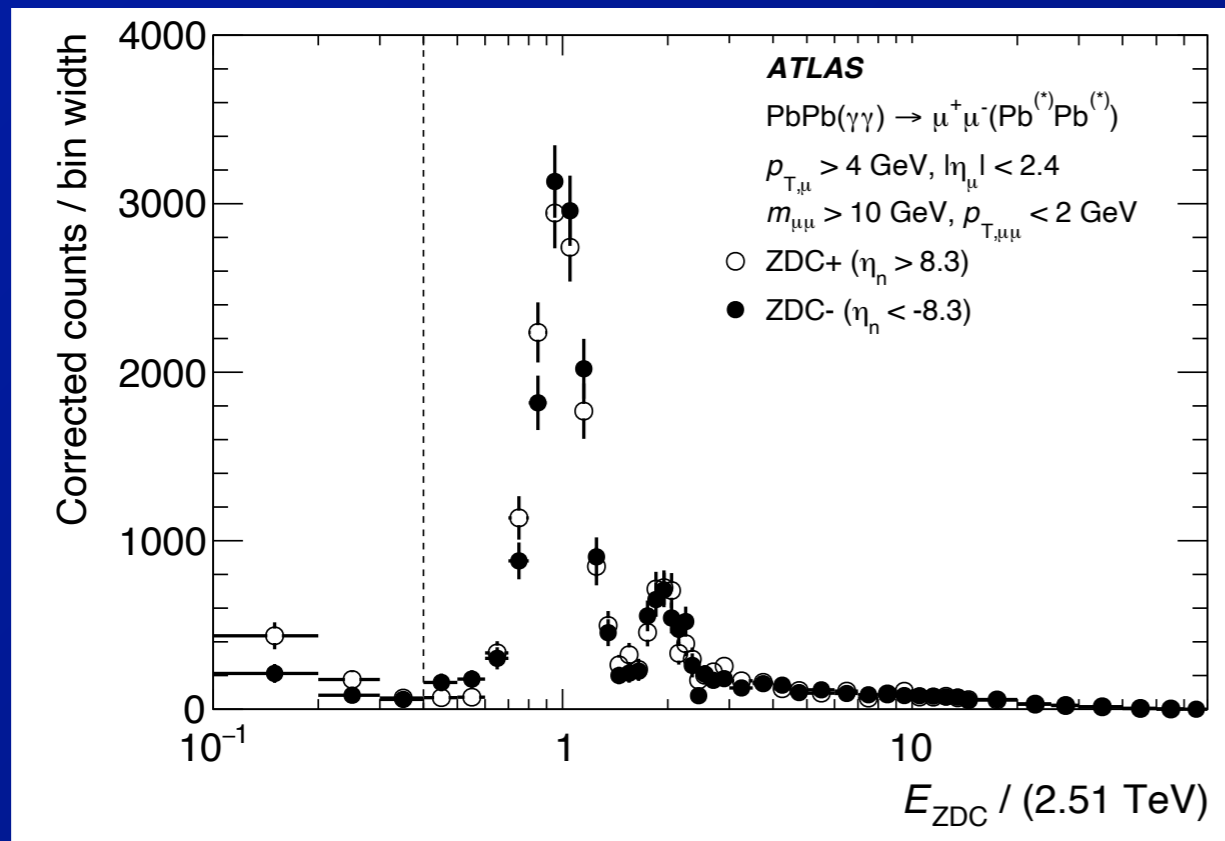


- Event topology as seen in the two ZDCs



– 0n0n - no neutrons in either ZDC

- Event topology as seen in the two ZDCs

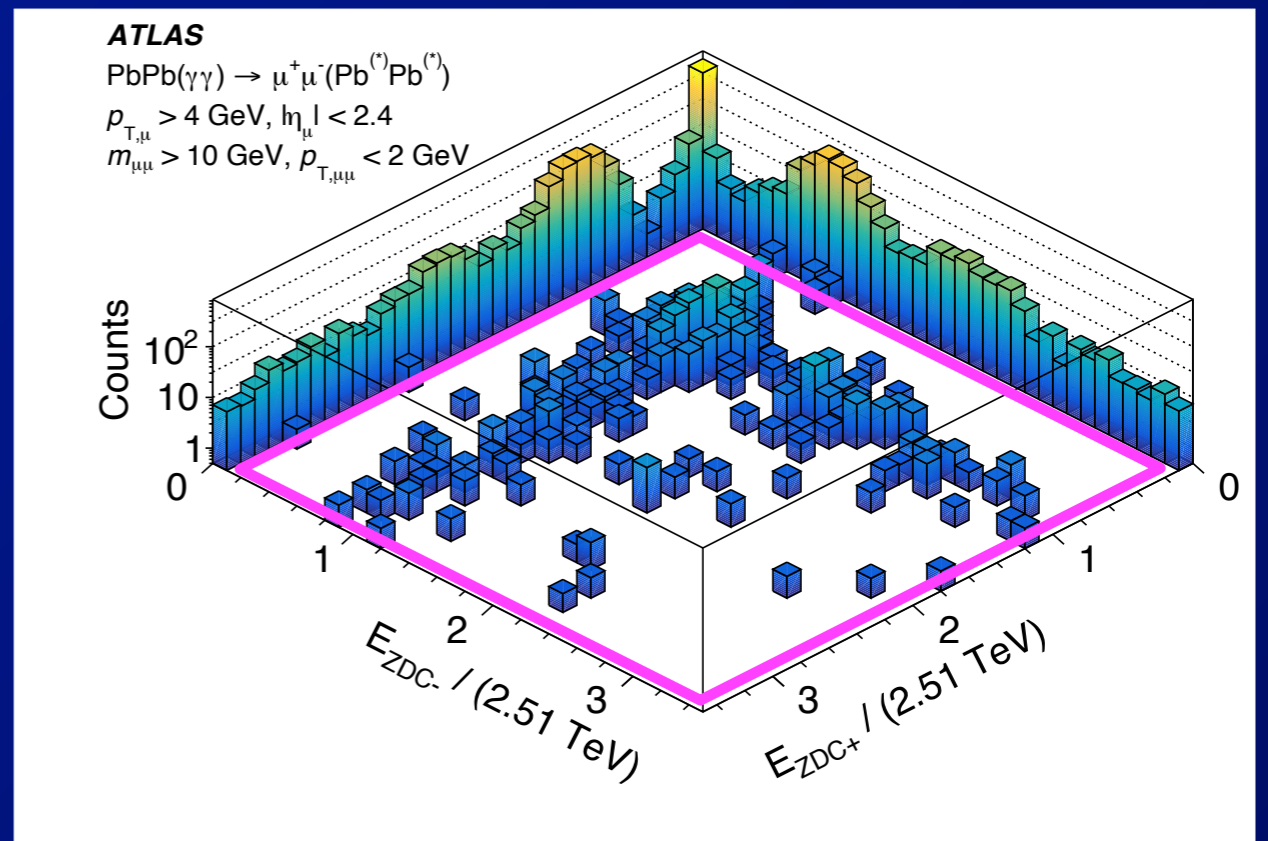
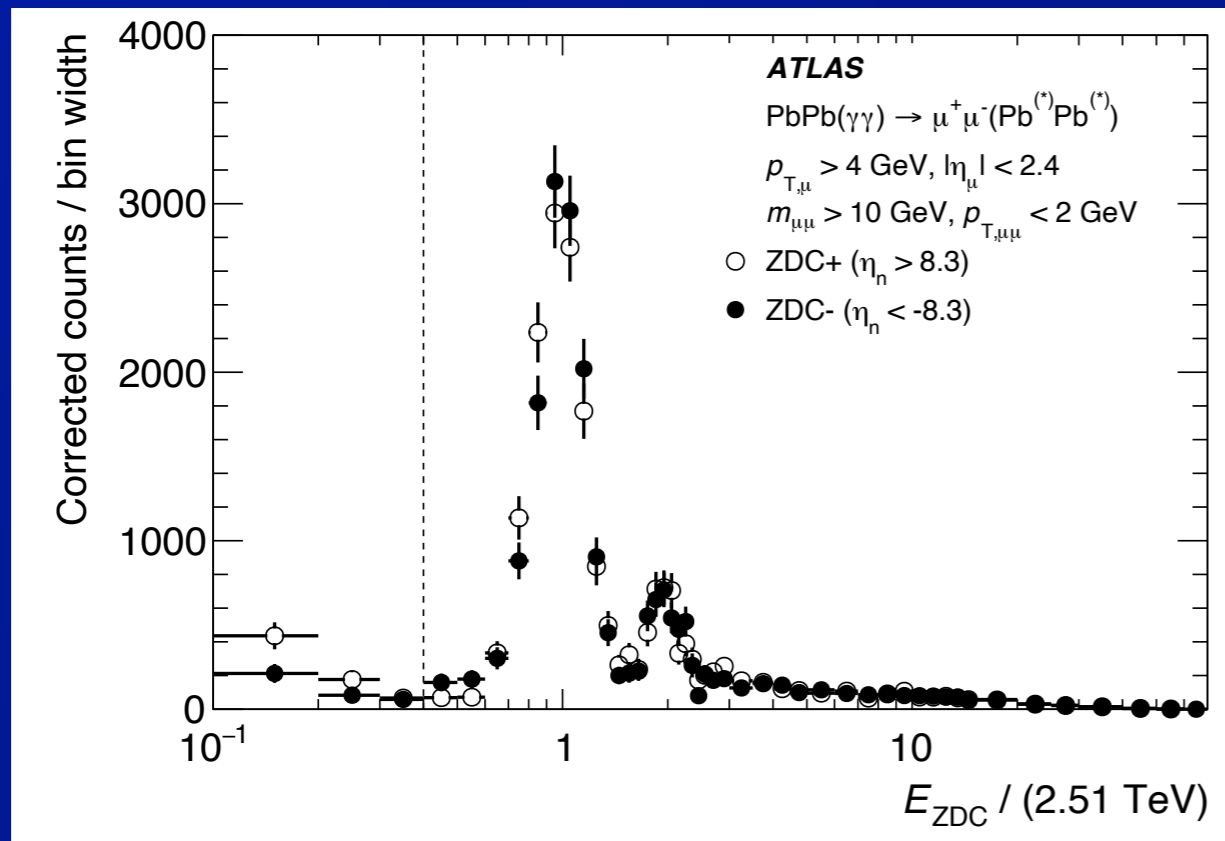


– $0nXn$

\Rightarrow 0 neutrons in one

$\Rightarrow \geq 1$ in the other

- Event topology as seen in the two ZDCs



– XnXn

$\Rightarrow \geq 1$ neutrons in both

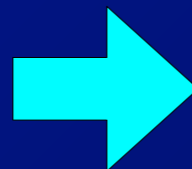
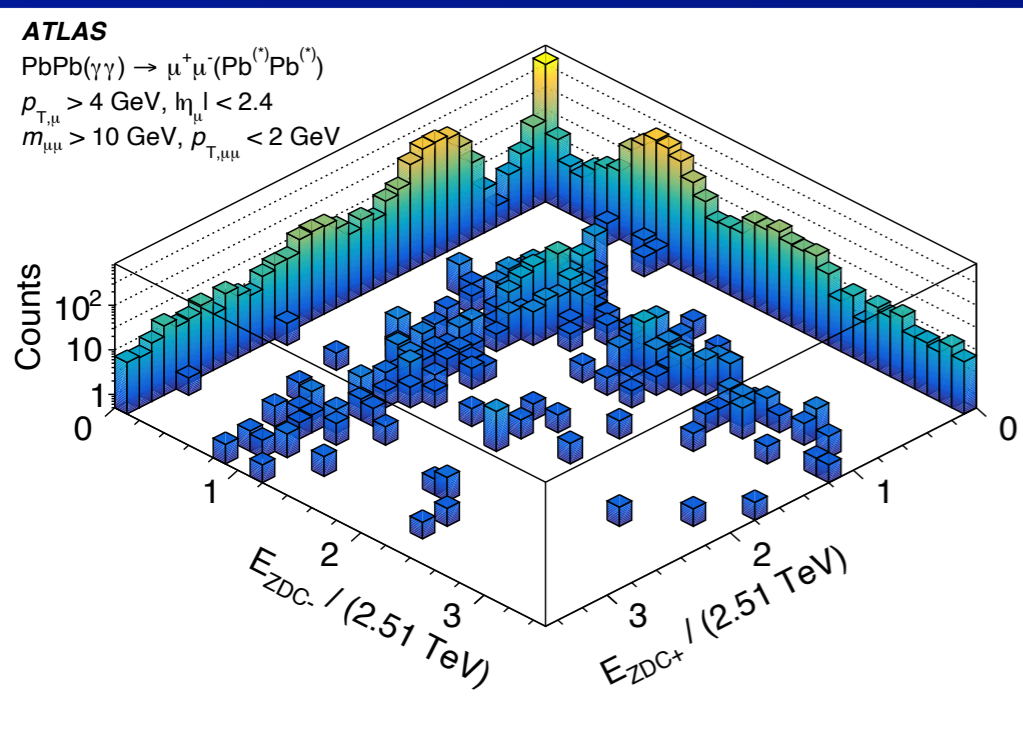
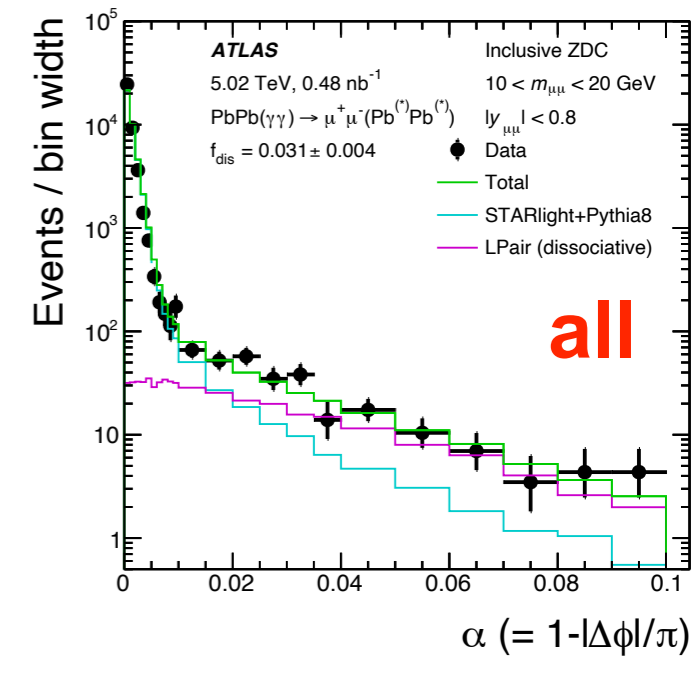
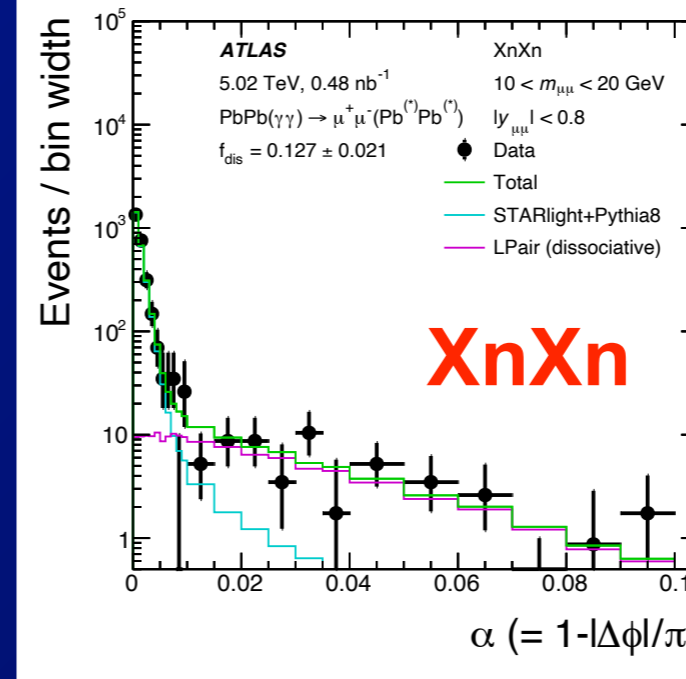
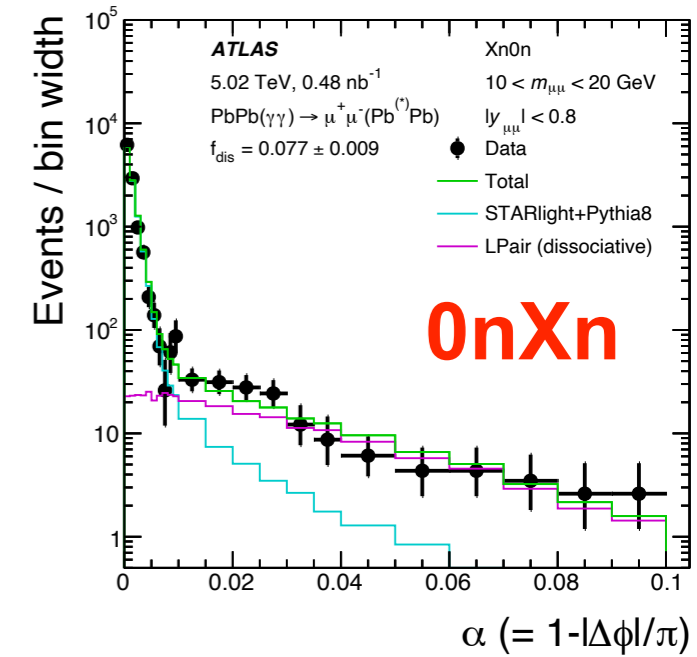
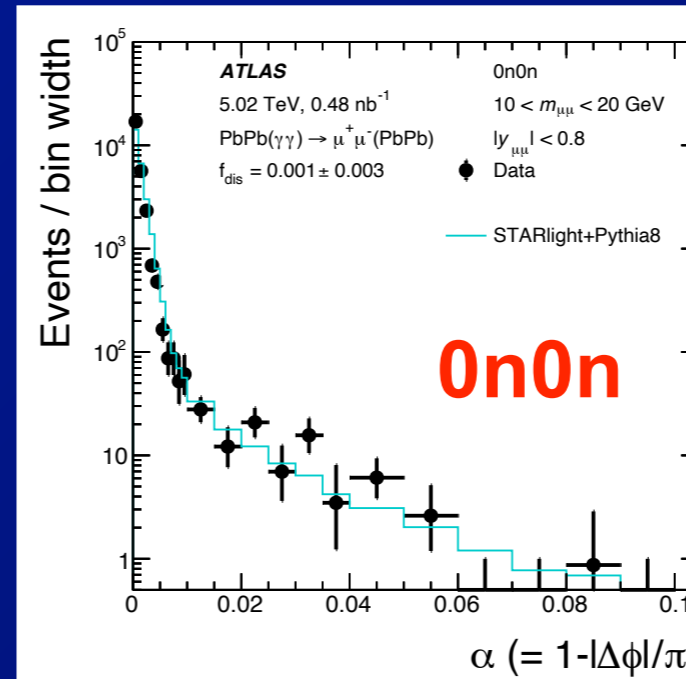
$\gamma+\gamma \rightarrow \mu^+\mu^-$, nuclear breakup

• Dimuon acoplanarity distributions

– for different topologies

⇒ Large-acoplanarity tails change shape for different neutron topologies

$$\alpha = 1 - \frac{\Delta\phi}{\pi}$$



- Dimuon acoplanarity distributions

$$\alpha = 1 - \frac{\Delta\phi}{\pi}$$

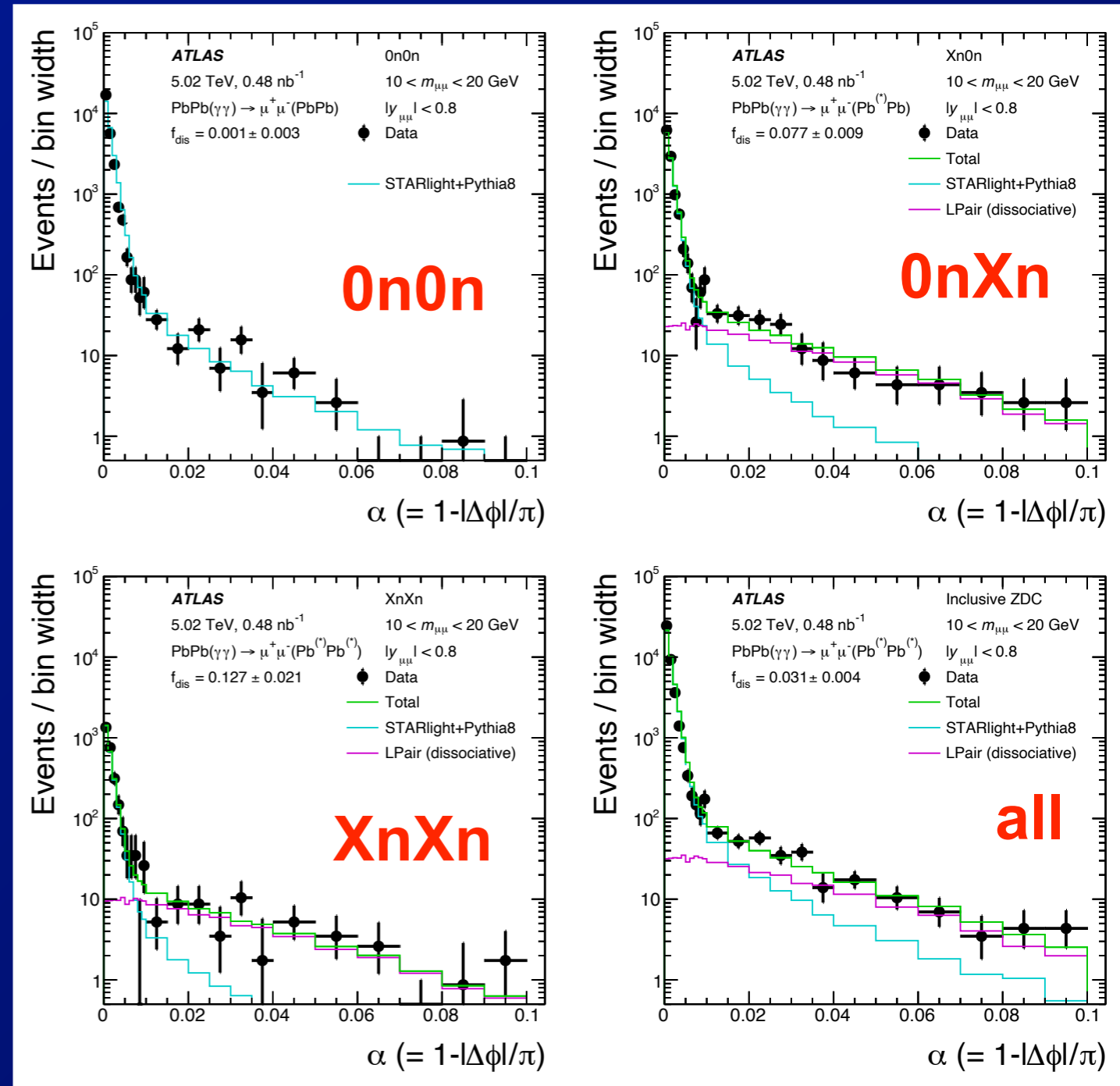
- for different topologies

⇒ Large-acoplanarity tails change shape for different neutron topologies

- Dominant effect:

- Dissociative emission of photons *a la* pp

⇒ Described by LPair



$\gamma+\gamma \rightarrow \mu^+\mu^-$, nuclear breakup

• Dimuon acoplanarity distributions

– for different topologies

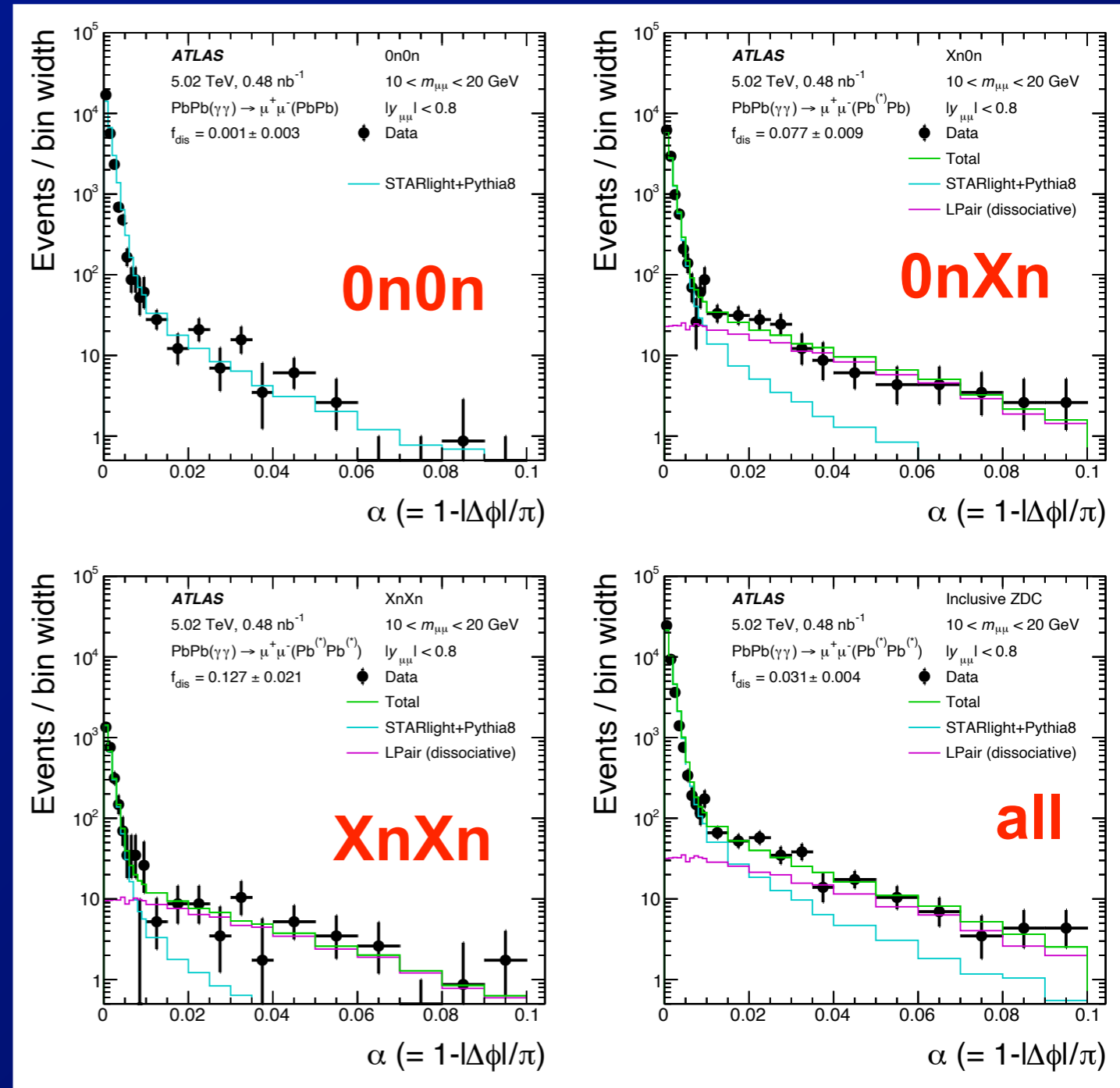
⇒ Large-acoplanarity tails change shape for different neutron topologies

• More generally

– Forward neutron rejection (i.e. 0n0n requirement) reduces $\gamma\gamma$ backgrounds

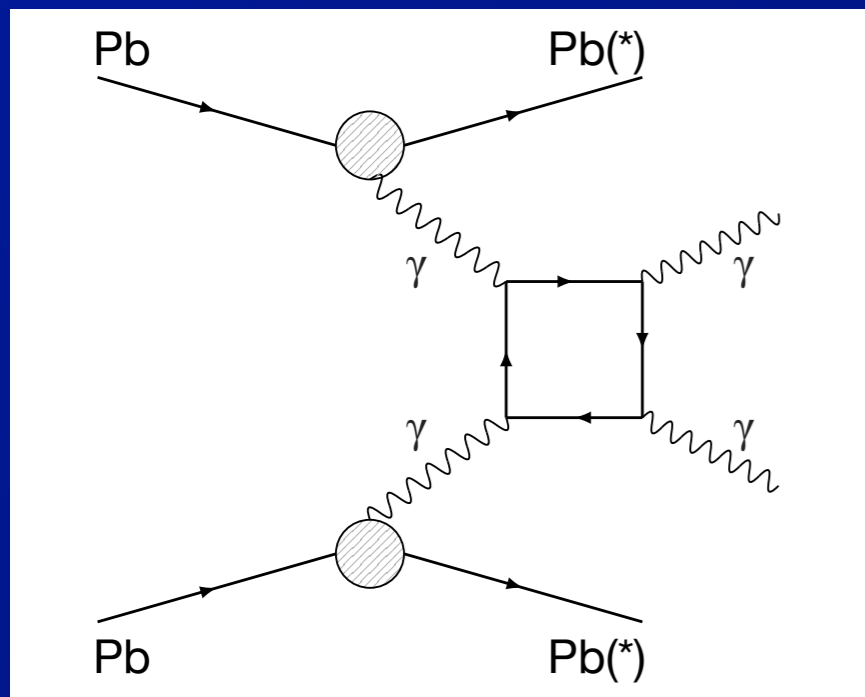
⇒ $\gamma+A$, diffractive, dissociative γ

$$\alpha = 1 - \frac{\Delta\phi}{\pi}$$

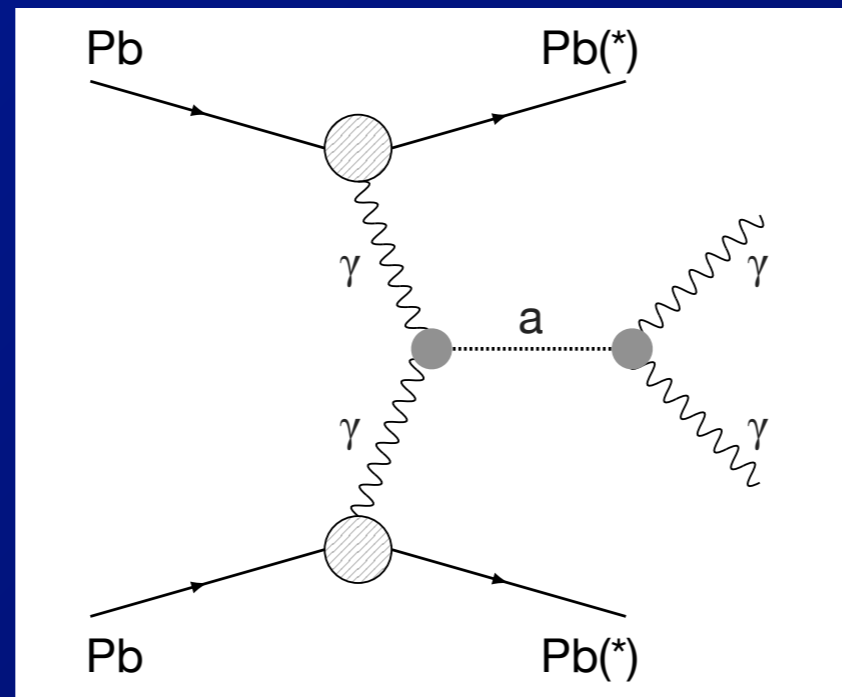


Light-by-light scattering

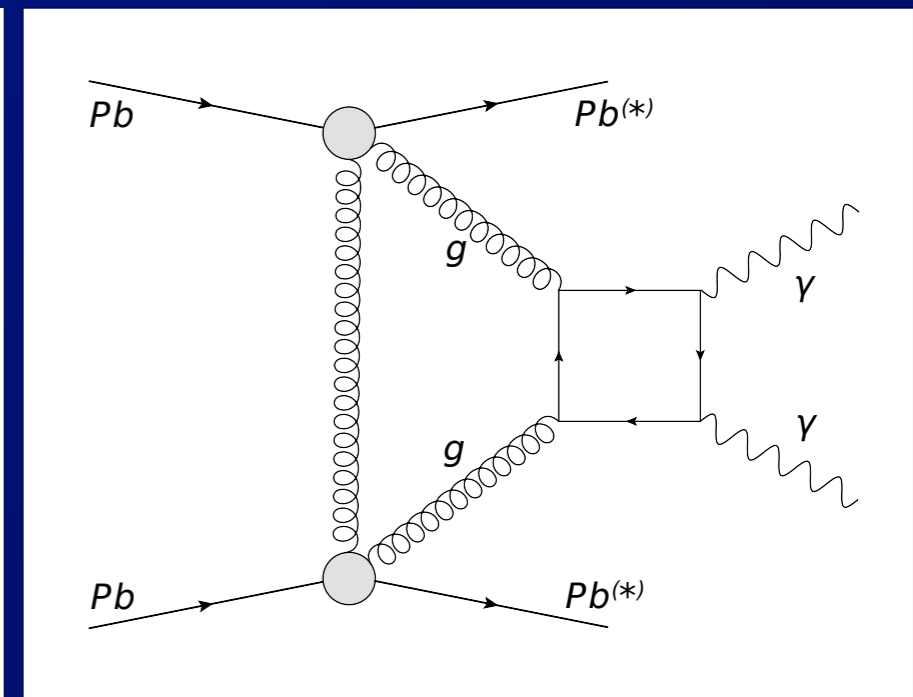
- Light-by-light scattering of (\approx) real photons was discovered @ LHC
 - by both ATLAS and CMS
 - now being used to search from BSM physics
 - \Rightarrow e.g. axion-like particles (ALP)
- Diagrams for three processes:



SM L-by-L



L-by-L ALP



CEP $g+g \rightarrow \gamma\gamma$
(Background)

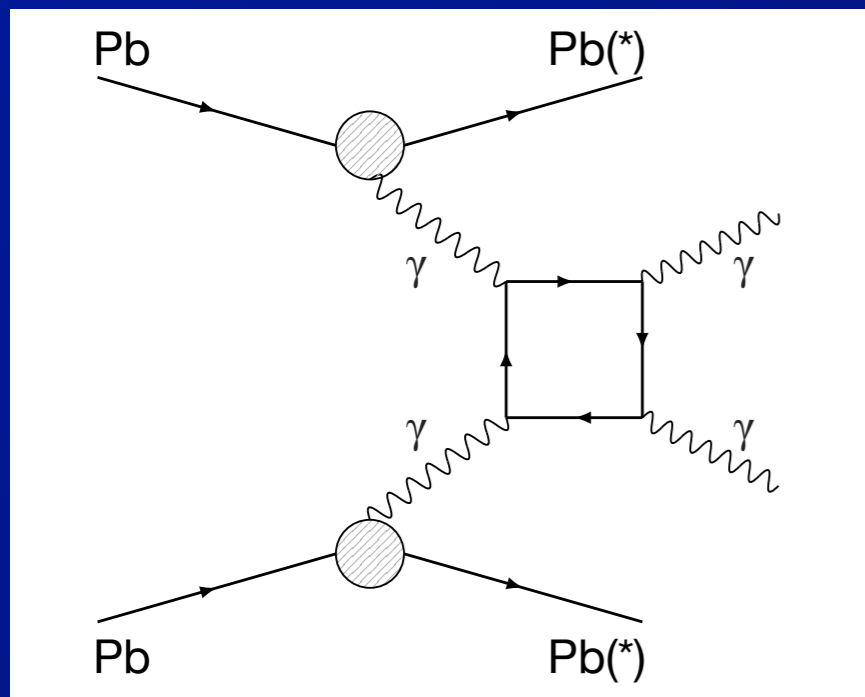
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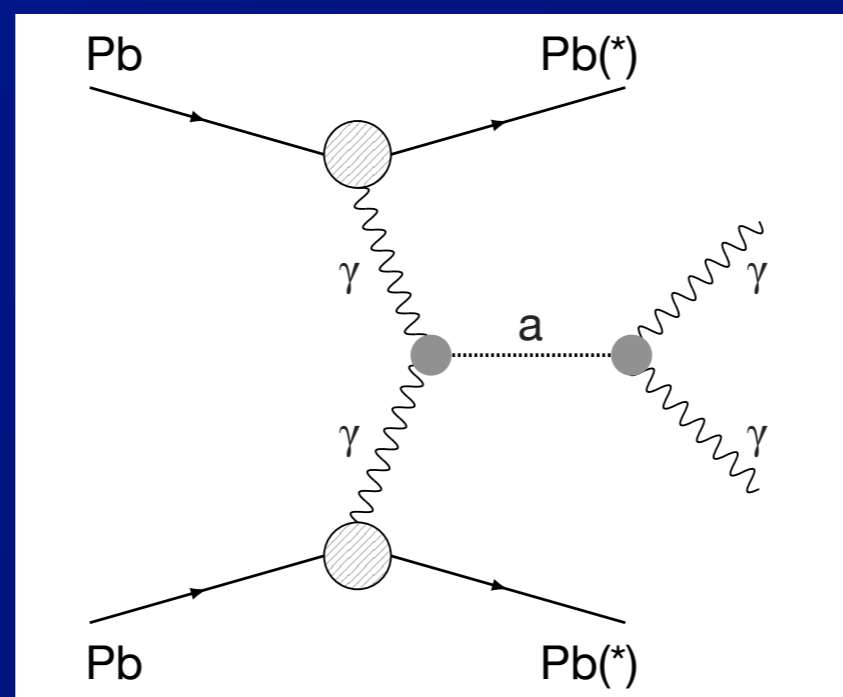
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⇒ e.g. axion-like particles (ALP)

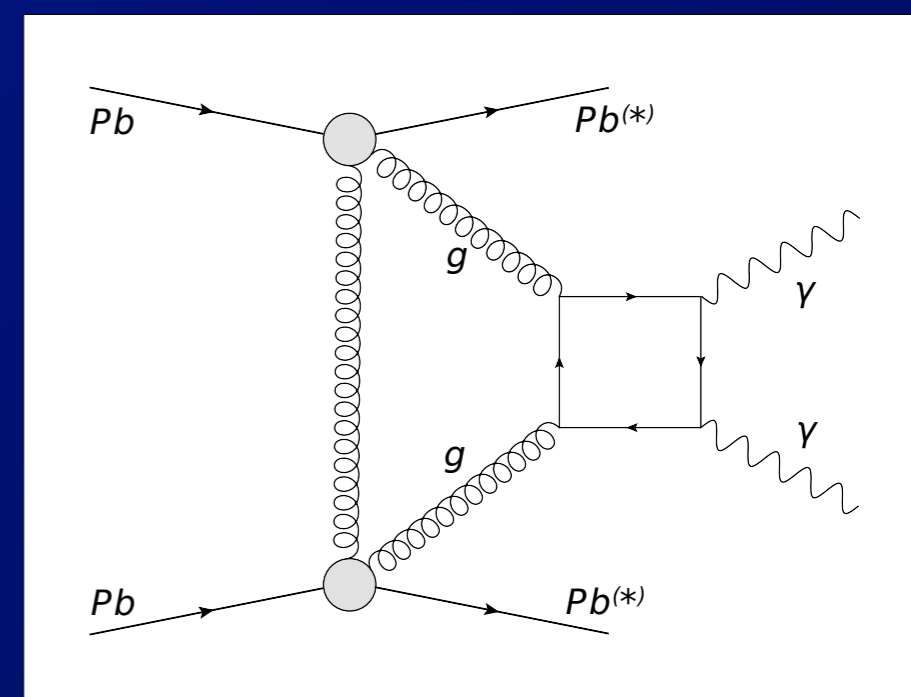
- Diagrams for three processes:



SM L-by-L



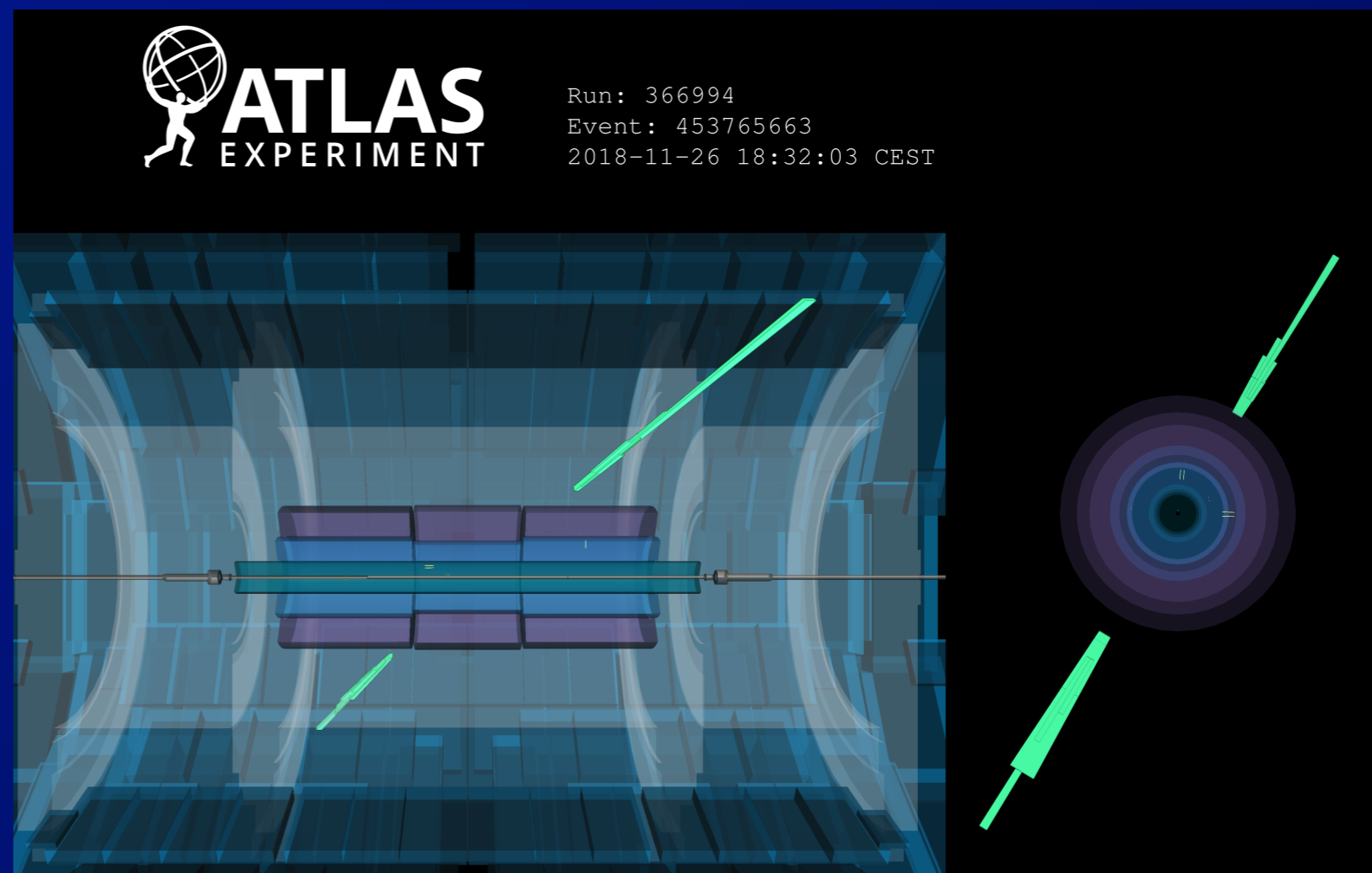
L-by-L ALP



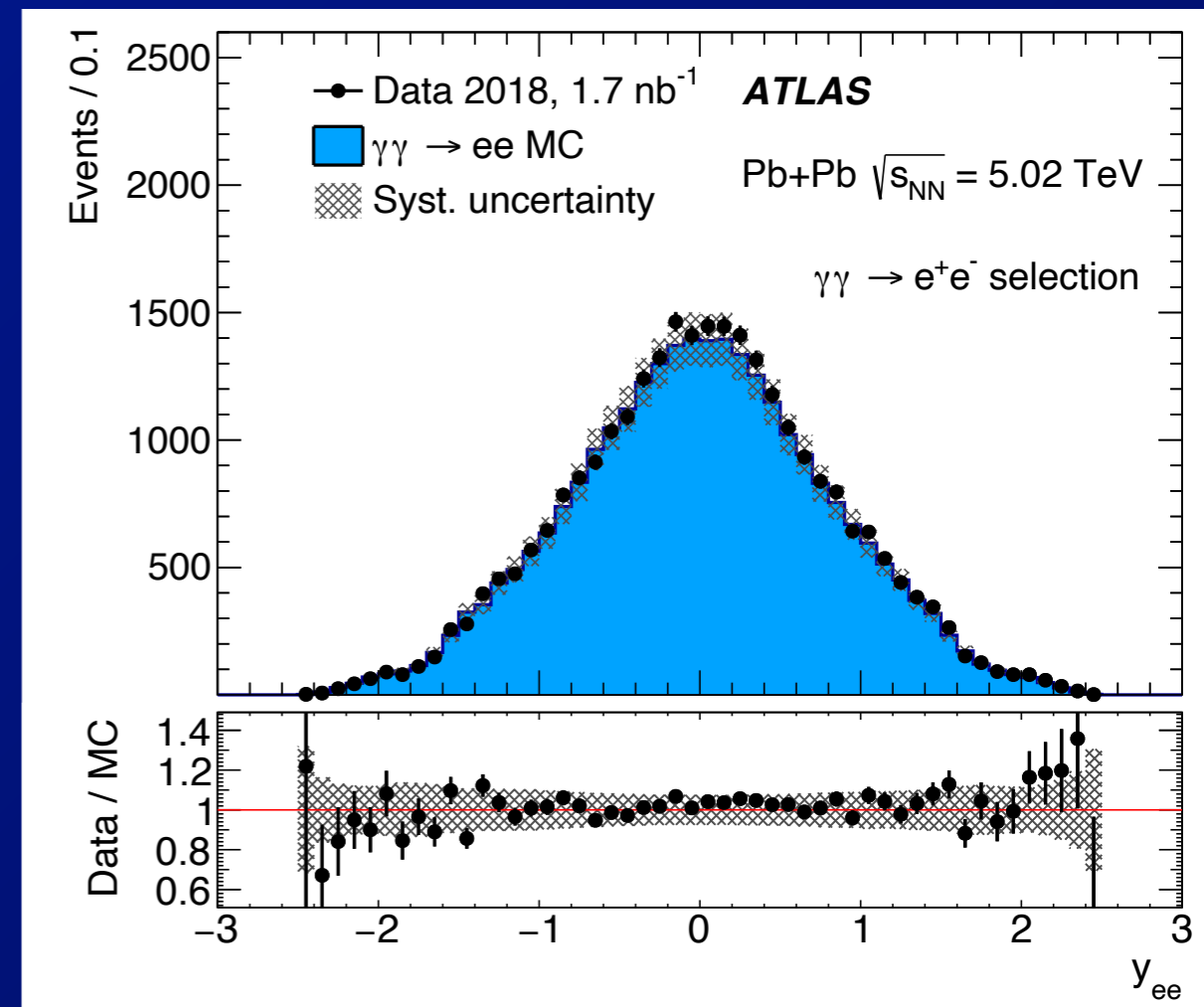
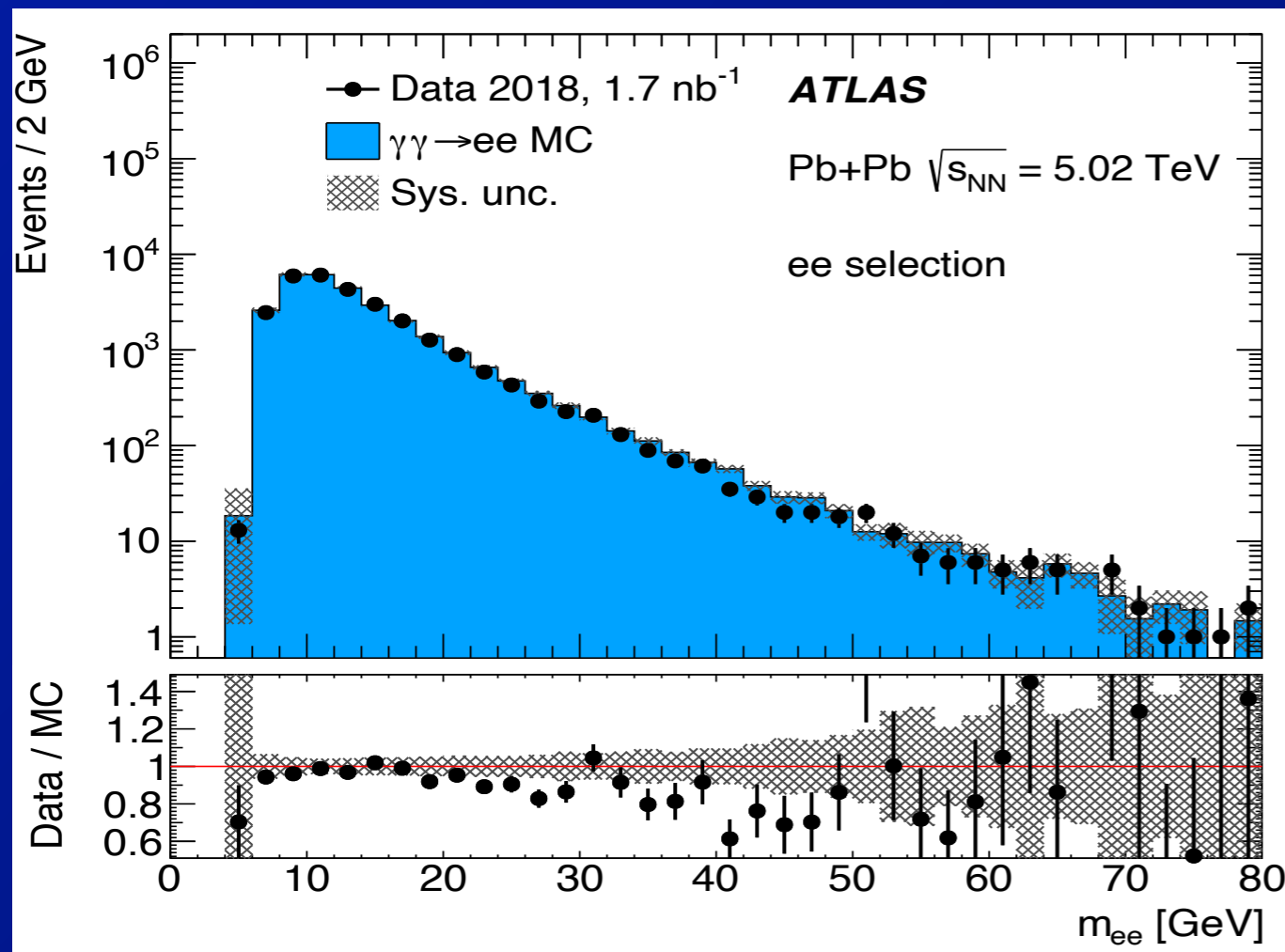
CEP $g+g \rightarrow \gamma\gamma$
nuclear breakup likely

- Using 2018 data, Pb+Pb @ 5.02 TeV (1.7 nb^{-1})
- Exclusive $\gamma\gamma$ events (no tracks):
 - $E_{T\gamma} > 2.5 \text{ GeV}$, $|\eta|_{\gamma} < 2.37$ (excl 1.37-1.52)
 - $m_{\gamma\gamma} > 5 \text{ GeV}$
 - $p_{T\gamma\gamma} < 1(2) \text{ GeV}$, $A_{\phi} < 0.01$

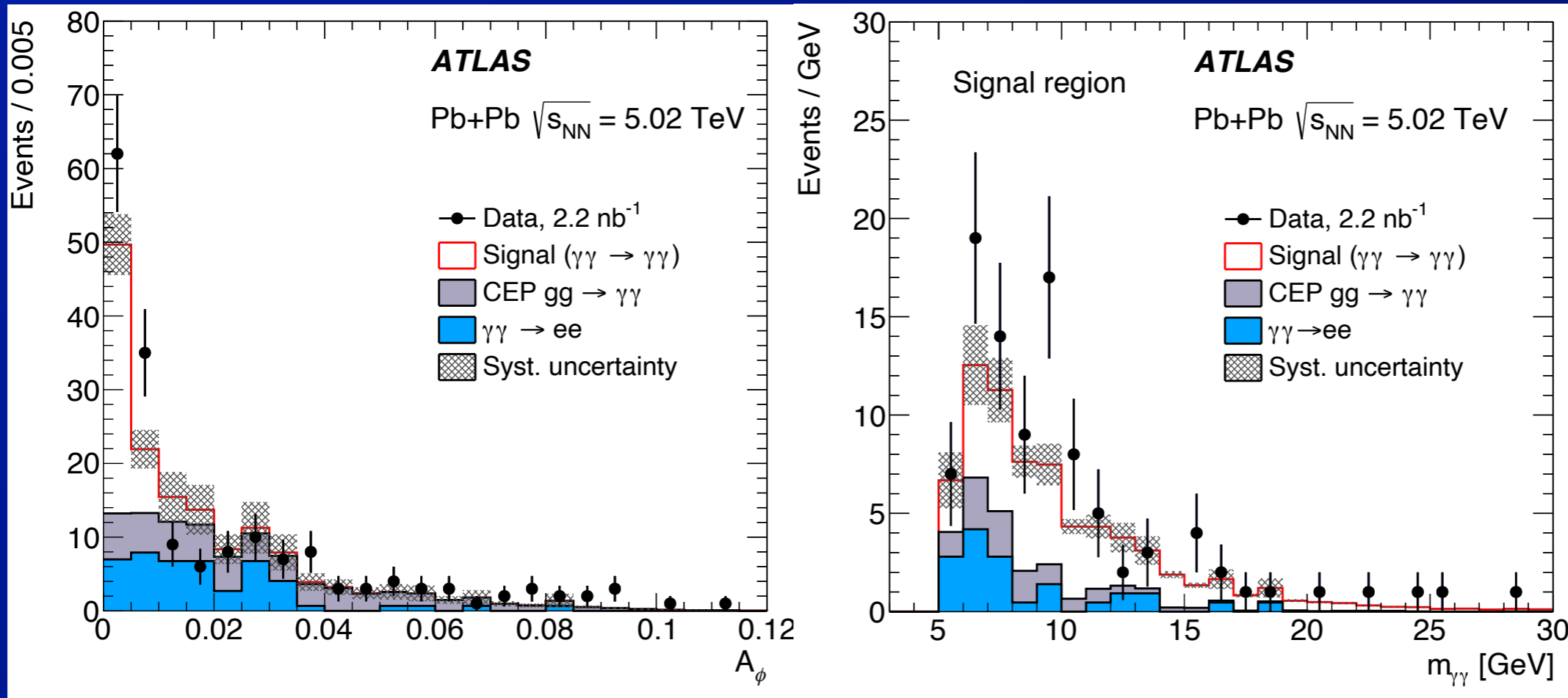
Phys. Rev. Lett. 123 (2019) 052001



- exclusive e^+e^- used to validate EM energy scale, trigger & reco. efficiencies

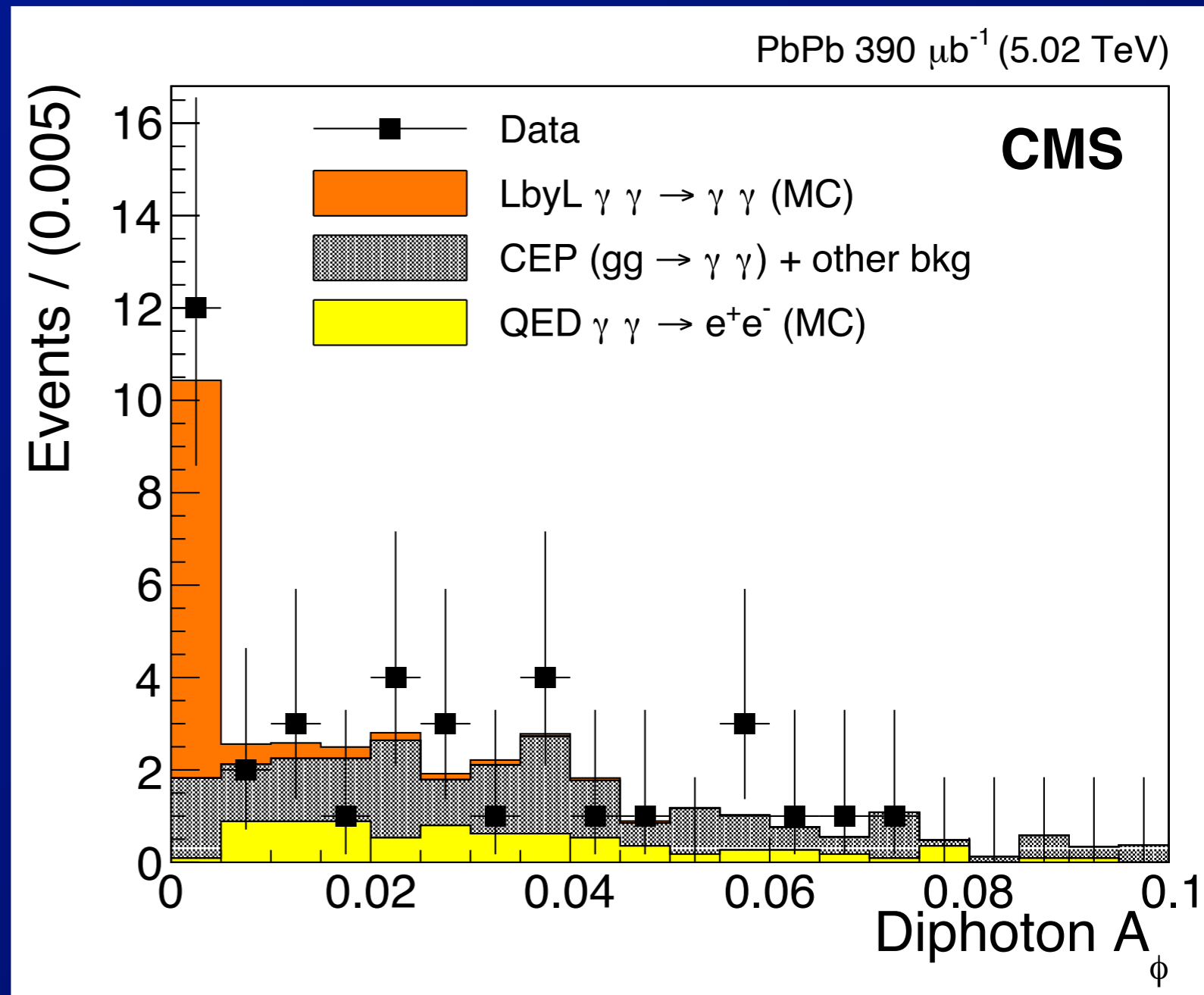


- CEP bkgd from MC, normalized w/ data, $A_\phi > 0.01$



- 97 events observed, background: 27 ± 5
 $\Rightarrow \sigma_{fid} = 120 \text{ nb} \pm 17 \text{ (stat.)} \pm 13 \text{ (syst.)} \pm 4 \text{ (lumi.)}$
- Ratio to theory(ies):
 $\Rightarrow \text{(combining)} 1.5 \pm 0.3$

- Using 2015 data set (0.39 nb^{-1})
- Exclusive $\gamma\gamma$ events
 - $E_{T\gamma} > 2 \text{ GeV}$, $|\eta|_{\gamma} < 2.4$
 - $p_{T\gamma\gamma} < 1 \text{ GeV}$, $A_{\phi} < 0.01$
- Estimate CEP background using $A_{\phi} > 0.02$



- Using 2015 data set (0.39 nb^{-1})

- Exclusive $\gamma\gamma$ events

- $E_{T\gamma} > 2 \text{ GeV}, |\eta|_{\gamma} < 2.4$

- $p_{T\gamma\gamma} < 1 \text{ GeV}, A_{\phi} < 0.01$

- Result: 14 L-by-L candidates

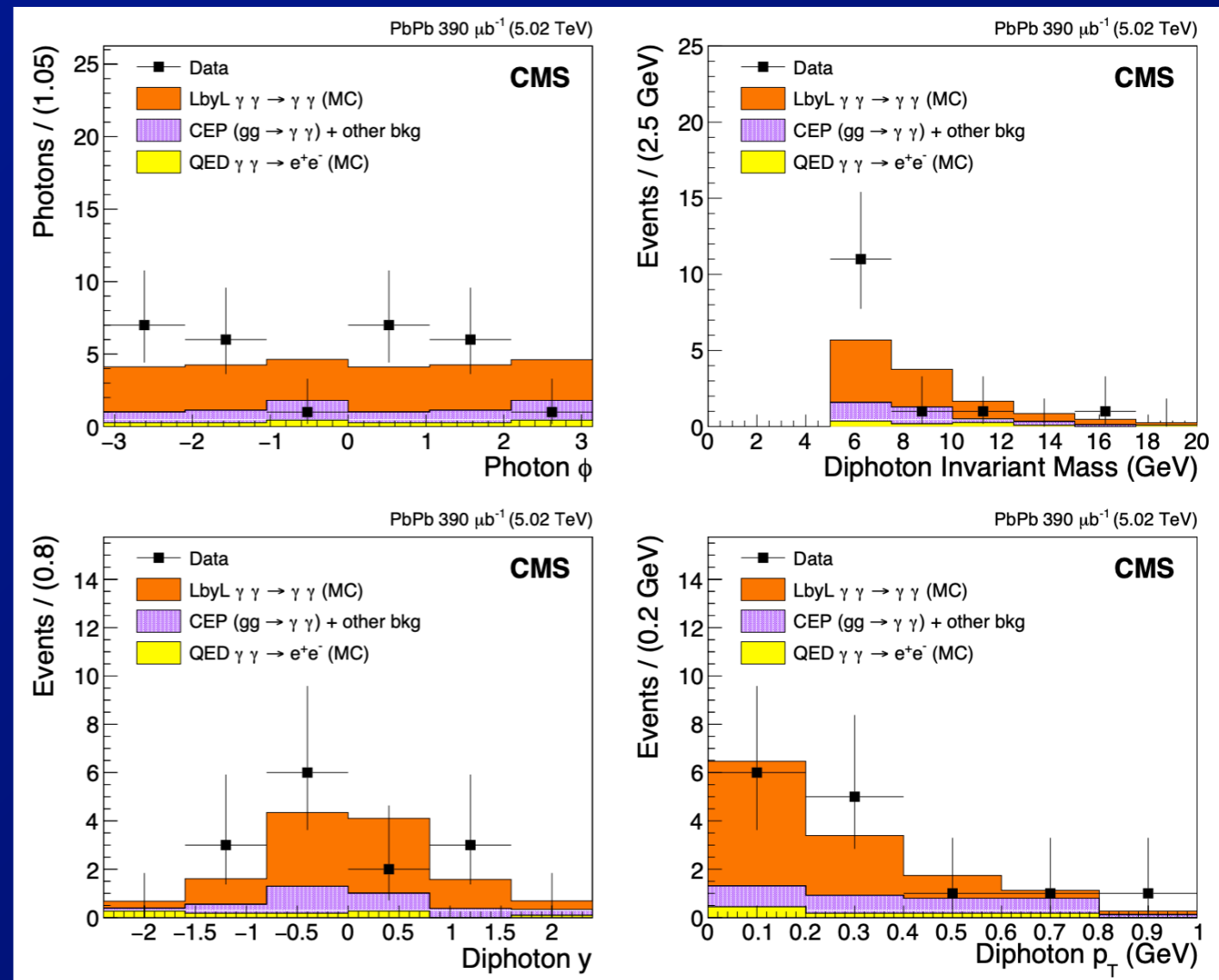
- 9 ± 0.1 expected

- 3.0 ± 1.1 CEP bkgd

- 1.0 ± 0.3 e^+e^- bkgd

$\Rightarrow \sigma_{\text{fid}} = 120 \pm 46 \text{ (stat)} \pm 28 \text{ (syst)} \pm 12 \text{ (theo)} \text{ nb}$

\Rightarrow Theoretical: $\sigma_{\text{fid}}(\gamma\gamma \rightarrow \gamma\gamma) = 116 \pm 12 \text{ nb}$.

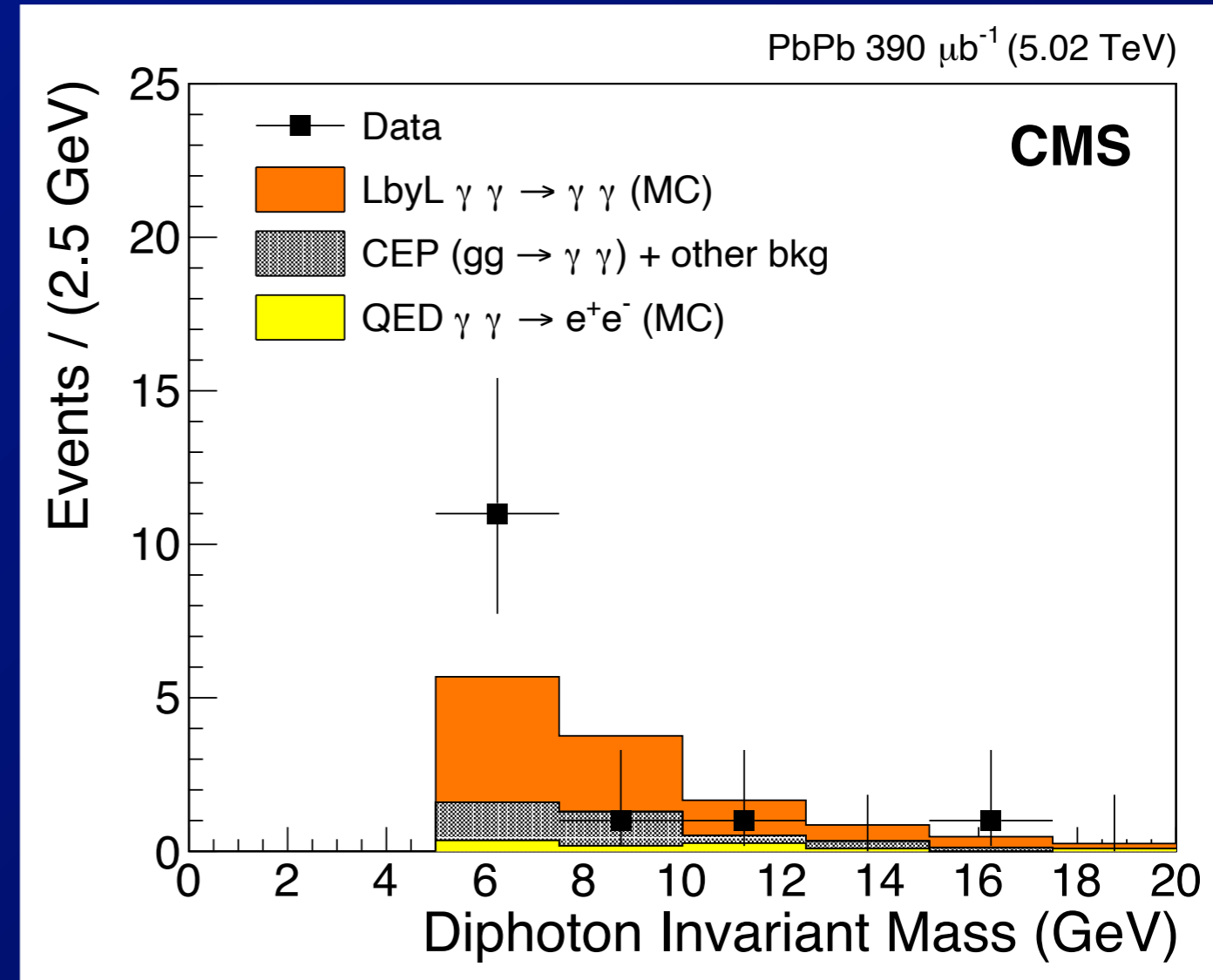
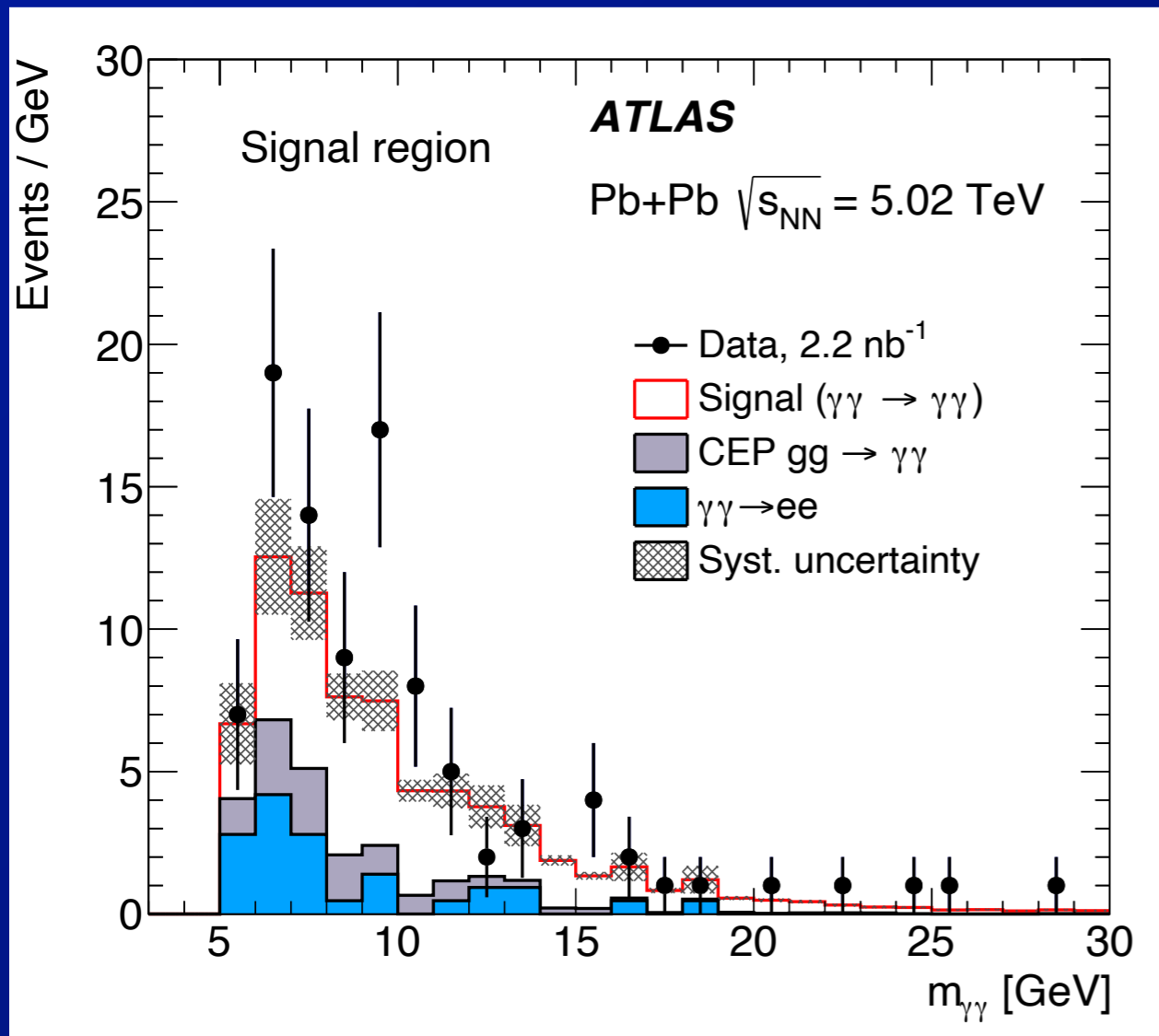


Phys. Lett. B 797 (2019) 134826

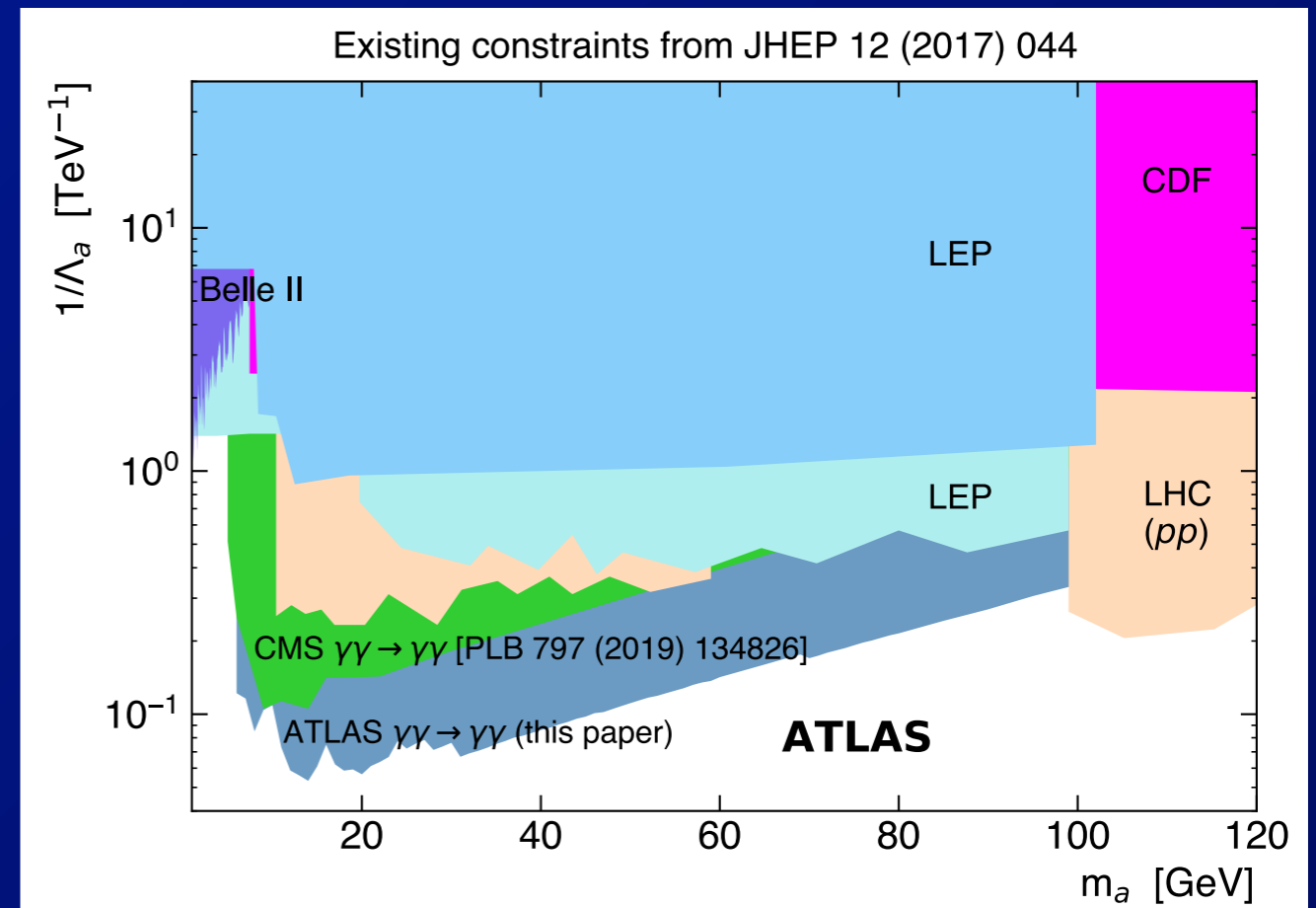
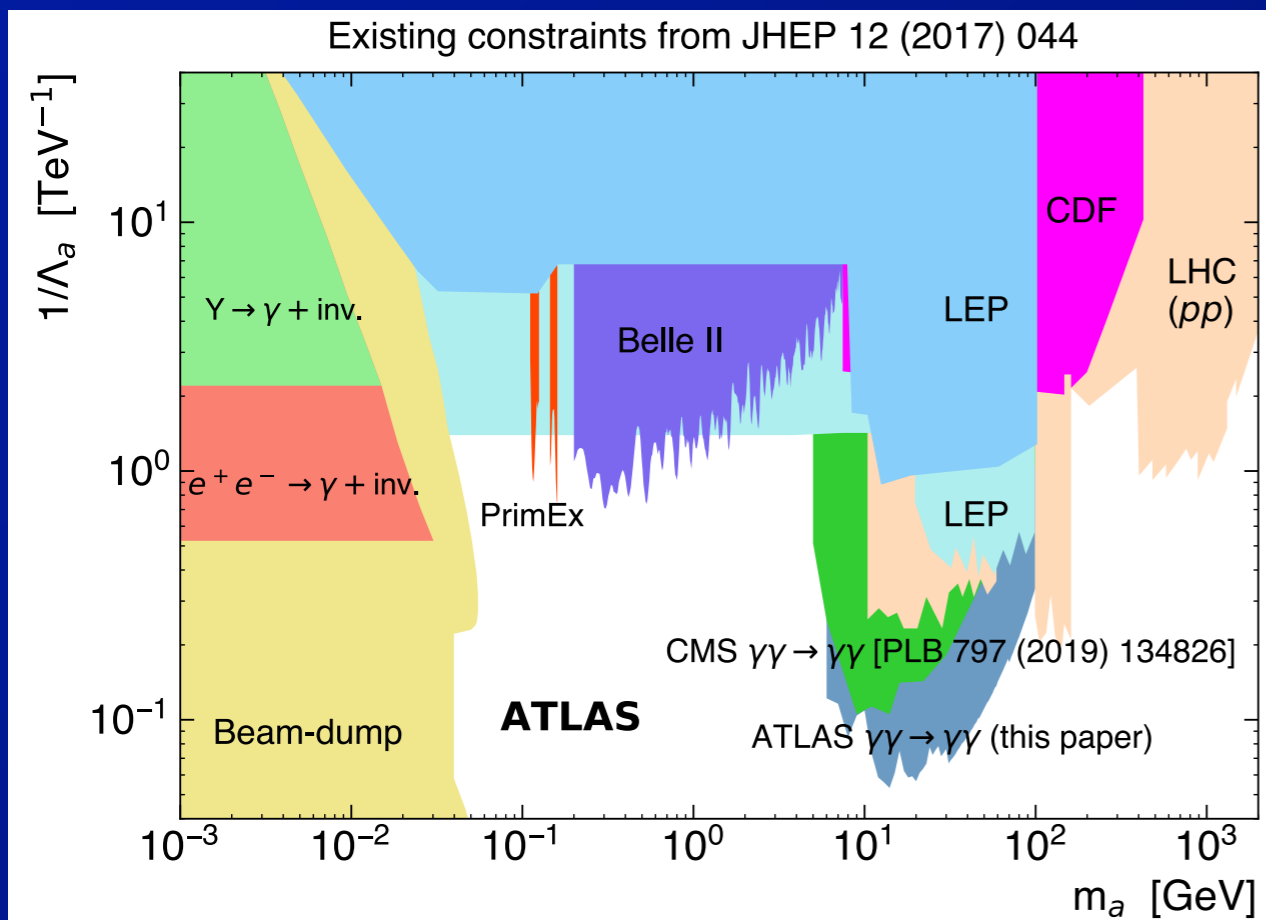
- **ALP searches:**

- Look for narrow resonances in $m_{\gamma\gamma}$ distribution

⇒ Both ATLAS and CMS data consistent with background-only hypothesis



- LHC measurements in UPC light-by-light:
 - CMS and ATLAS constraints on $\gamma\gamma \rightarrow \text{ALP}$



- ⇒ LHC light-by-light data provide improved constraints on ALP production in mass range 5-100 GeV
- Note: no combination (yet) of ATLAS and CMS data

$\tau^+ \tau^-$ and $\tau g-2$

- Studying tau properties in ultra-peripheral collisions is an old idea



CERN-TH. 6205/91

The Possibility of Using a Large Heavy-Ion Collider for Measuring the Electromagnetic Properties of the Tau Lepton *

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J.I. Illana

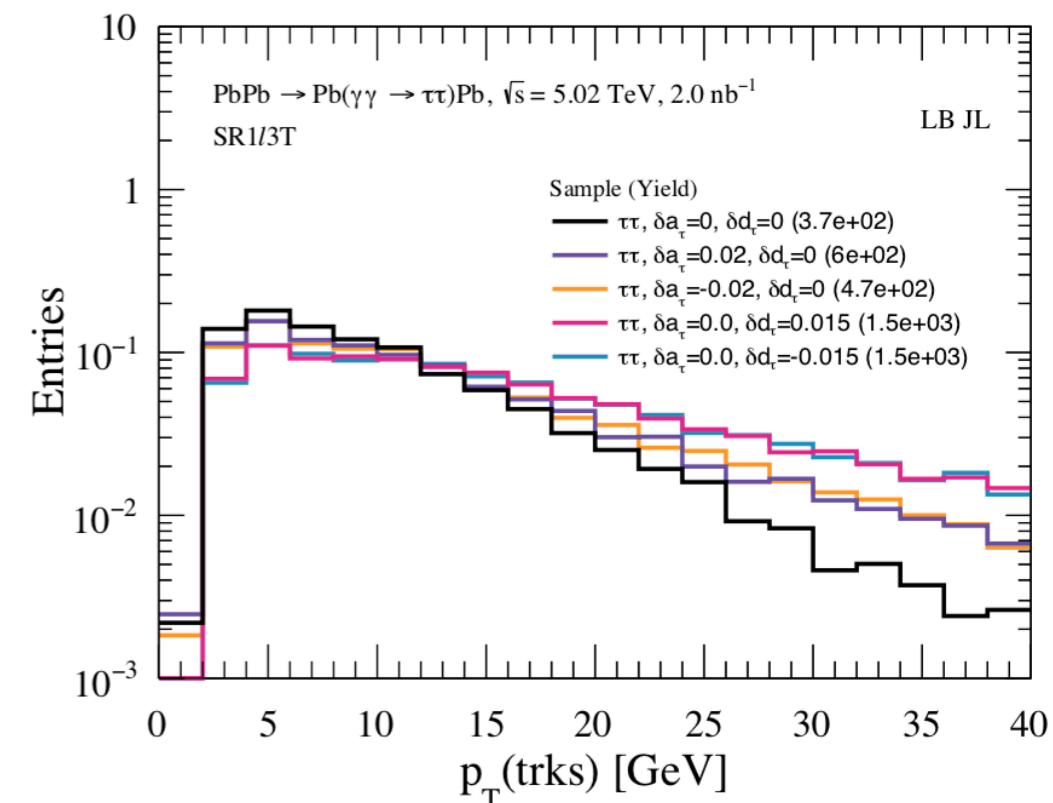
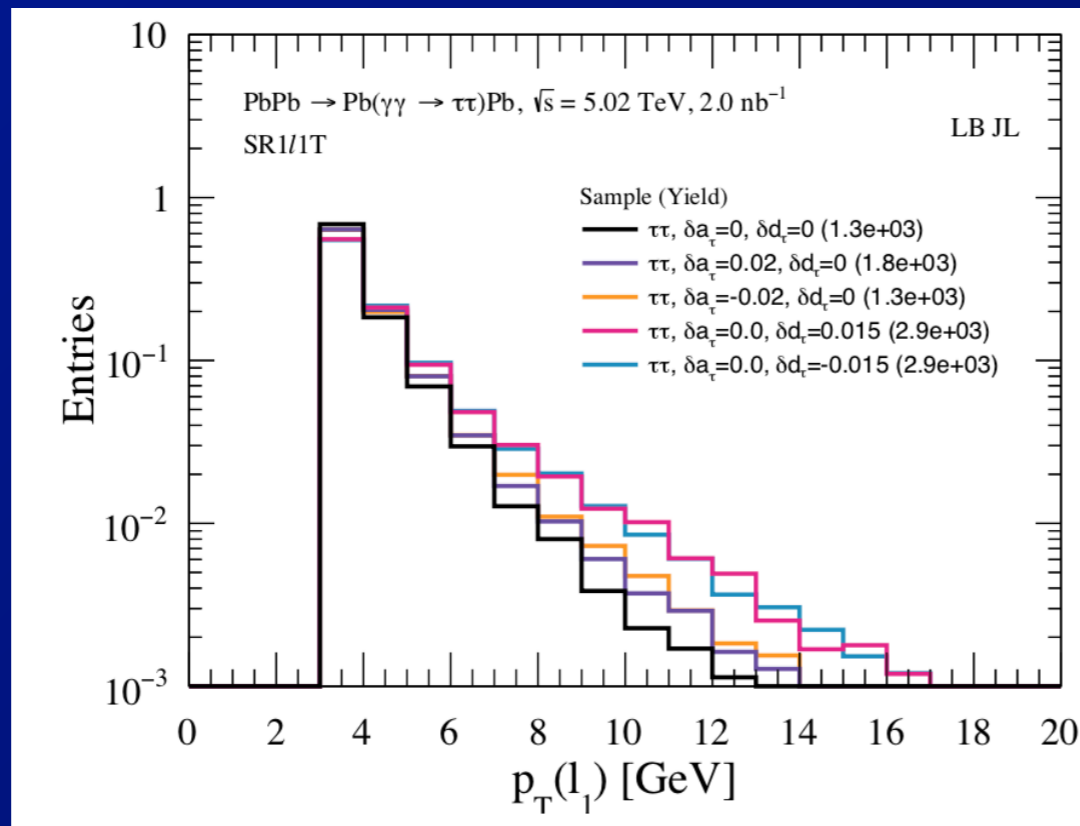
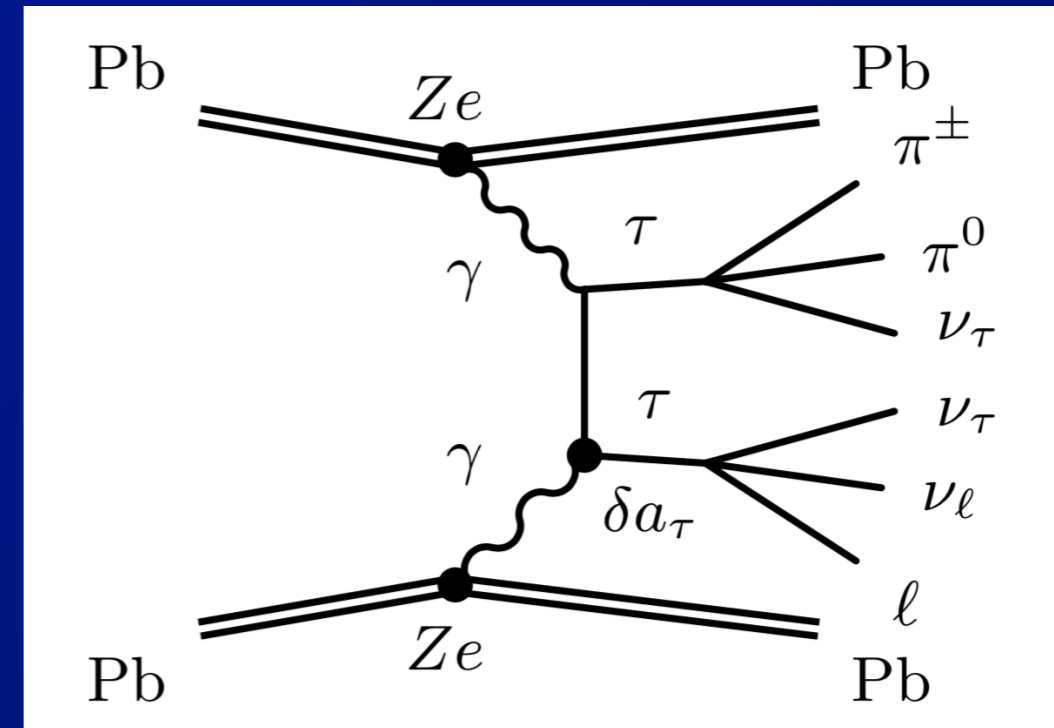
*Departamento de Física Teórica y del Cosmos,
Universidad de Granada, E-18071 Granada, Spain*

Abstract

We study the potential of a large heavy-ion collider for the measurement of the electromagnetic properties of the tau lepton. Measuring the anomalous magnetic and the electric dipole moments of the tau at $q^2 \sim 0$ with a precision of $\sim 4 \times 10^{-5}$ and $\sim 4 \times 10^{-3}$, respectively, at the LHC and/or SSC should be no problem. Whereas the precision at RHIC should be a few per cent, comparable to present limits and to the expected precision at LEP.

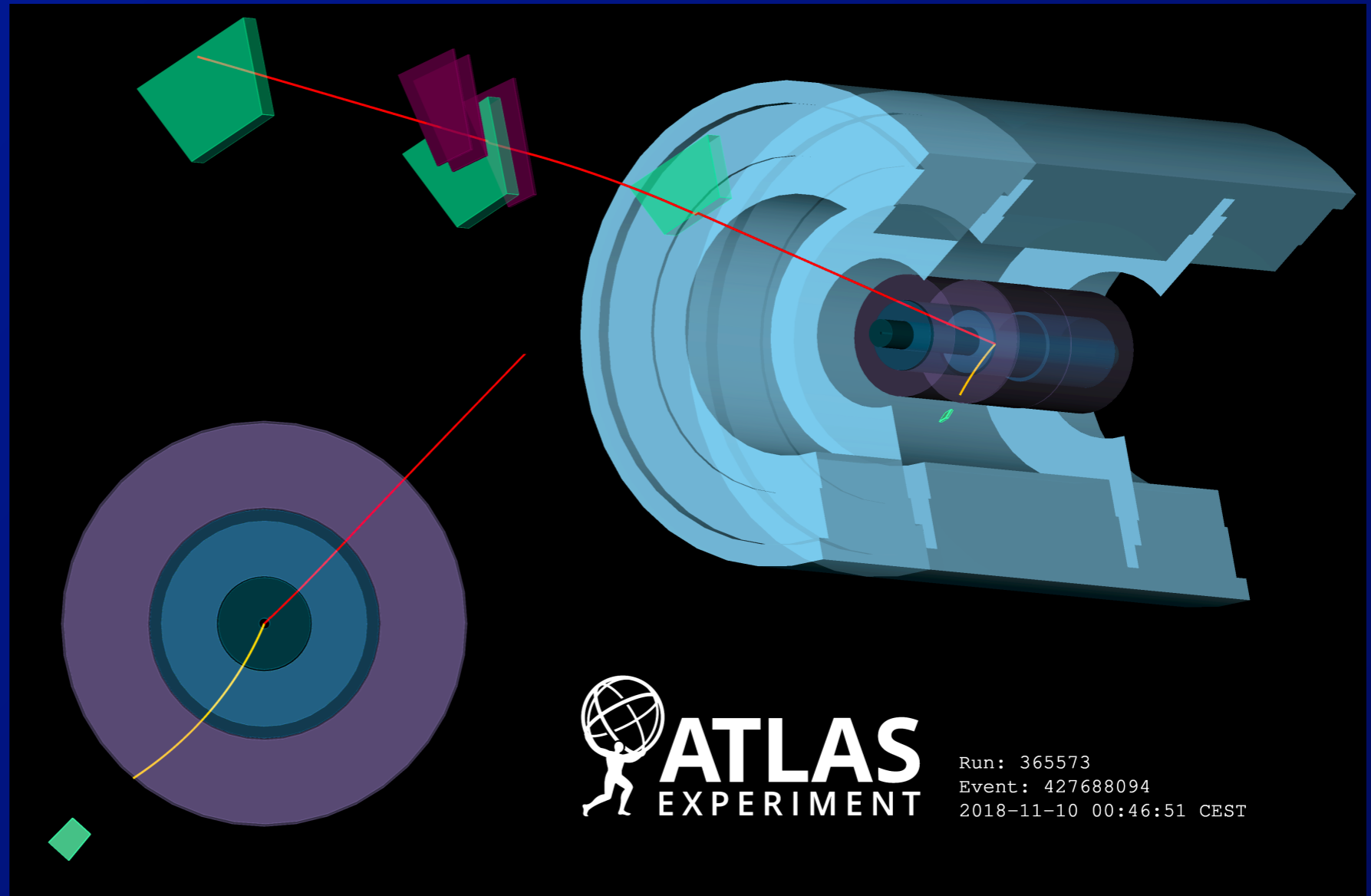
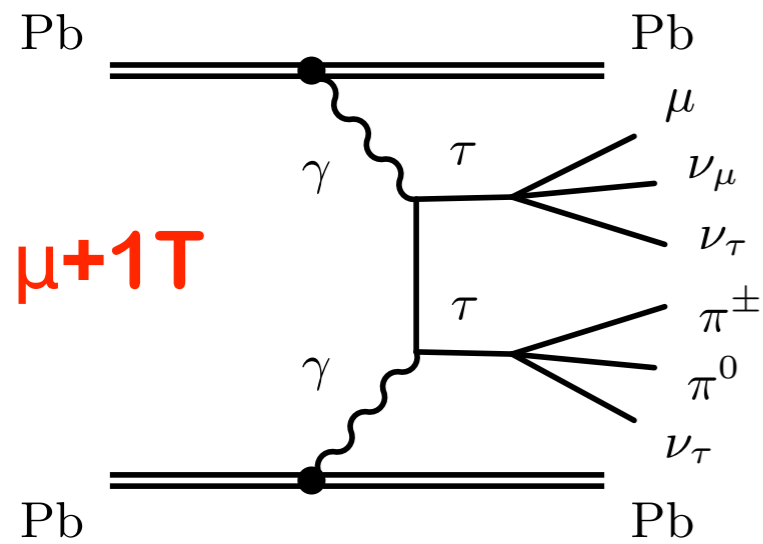
• **Beresford and Liu:**

- tau g-2 measurements could be made using UPC $\gamma+\gamma \rightarrow \tau^+ \tau^-$
- mass increases sensitivity to BSM physics
- ⇒ the kinematics of the taus & decay products are sensitive to BSM physics

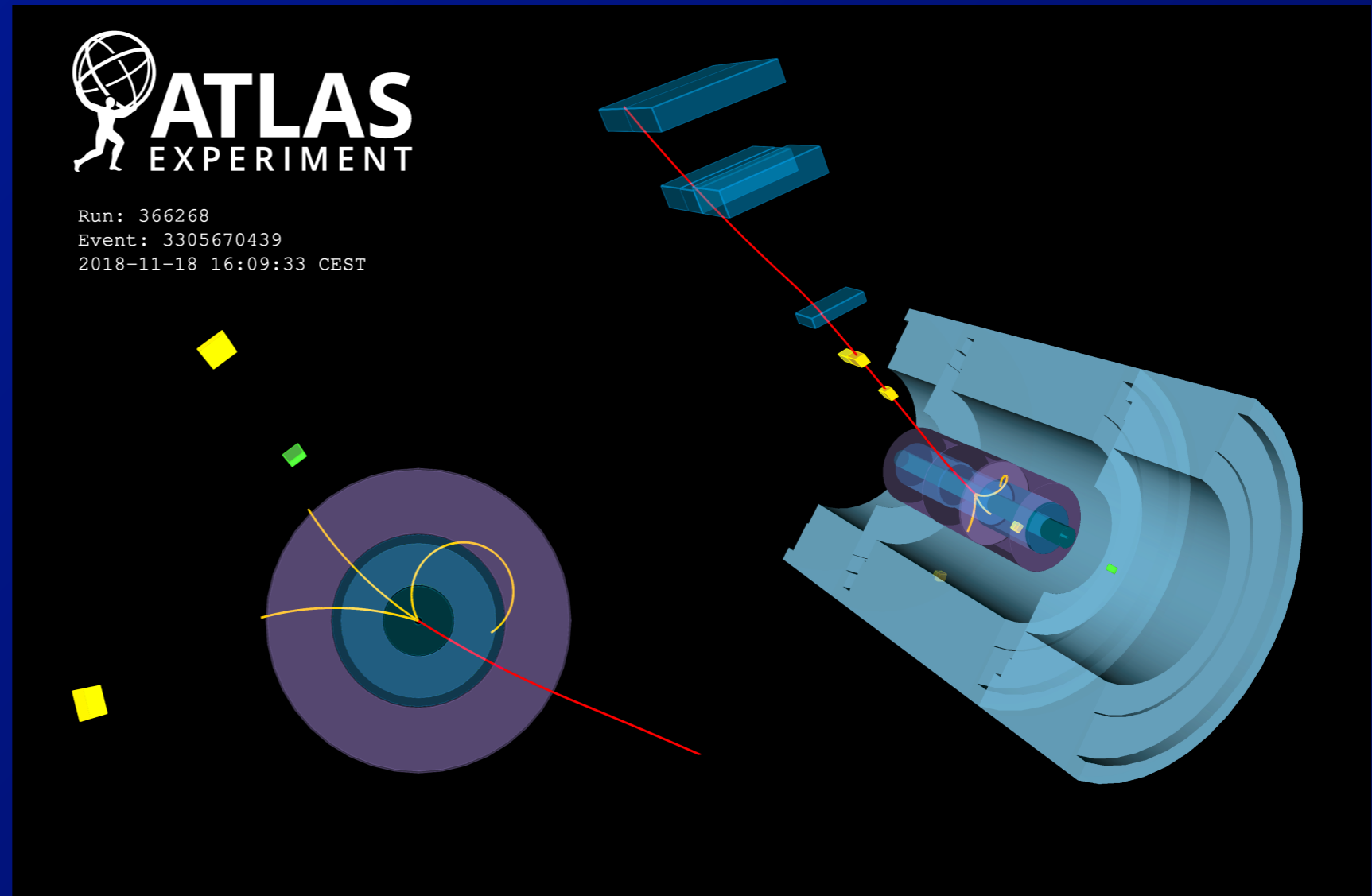
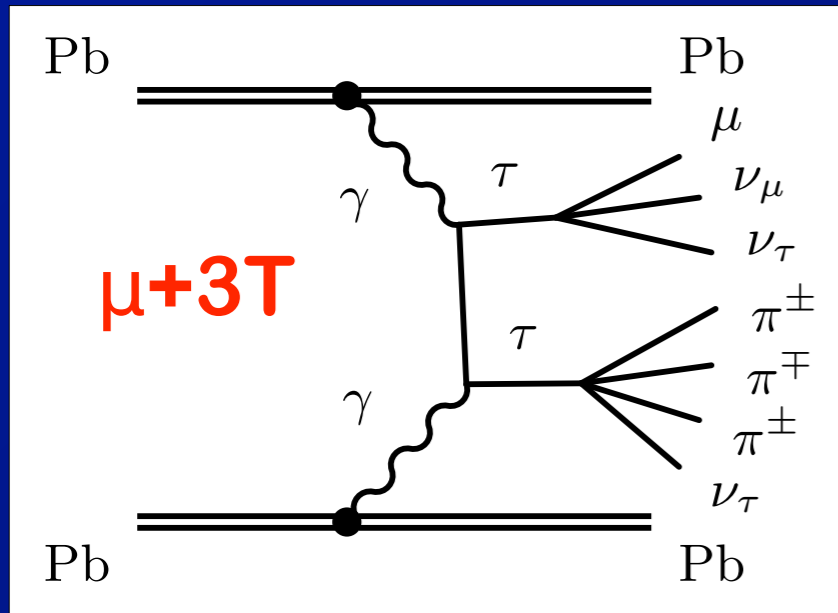


- ATLAS used three signal CRs to select events with 2 τ decays

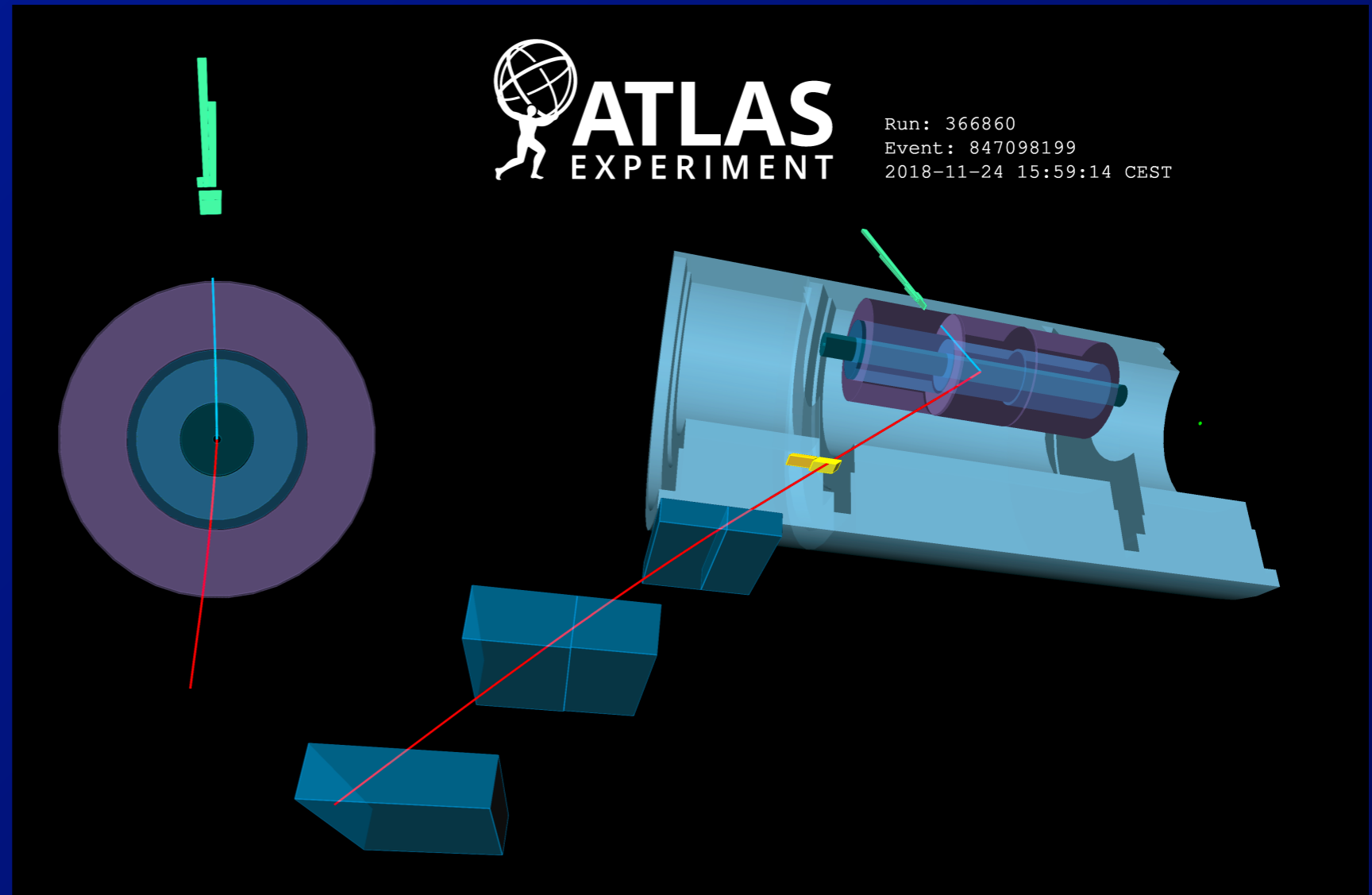
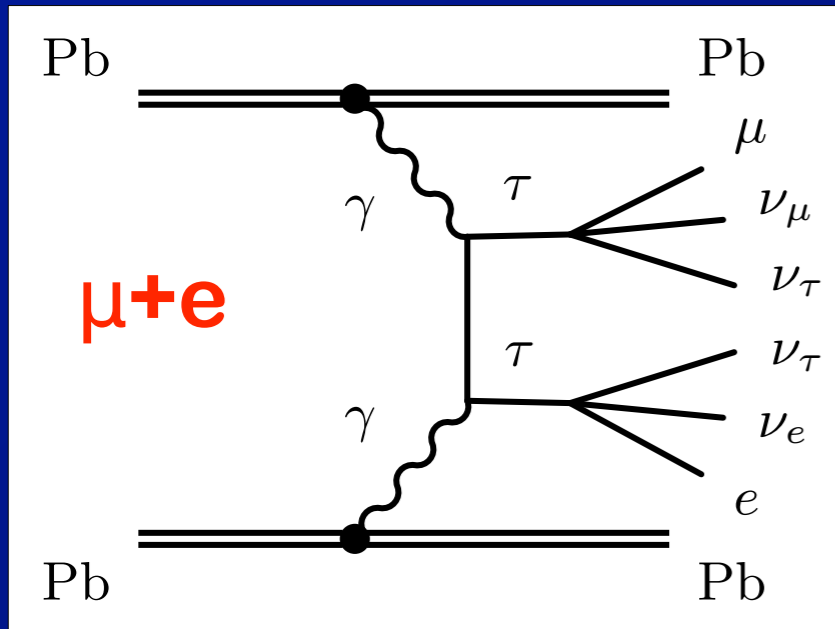
- ATLAS used three signal channels/regions to select events with 2 τ decays
 - Muon + 1 track



- ATLAS used three signal channels/regions to select events with 2 τ decays
 - Muon + 3 tracks



- ATLAS used three signal channels/regions to select events with 2 τ decays
 - Muon + electron



- **Simultaneous analysis of 3 signal channels**

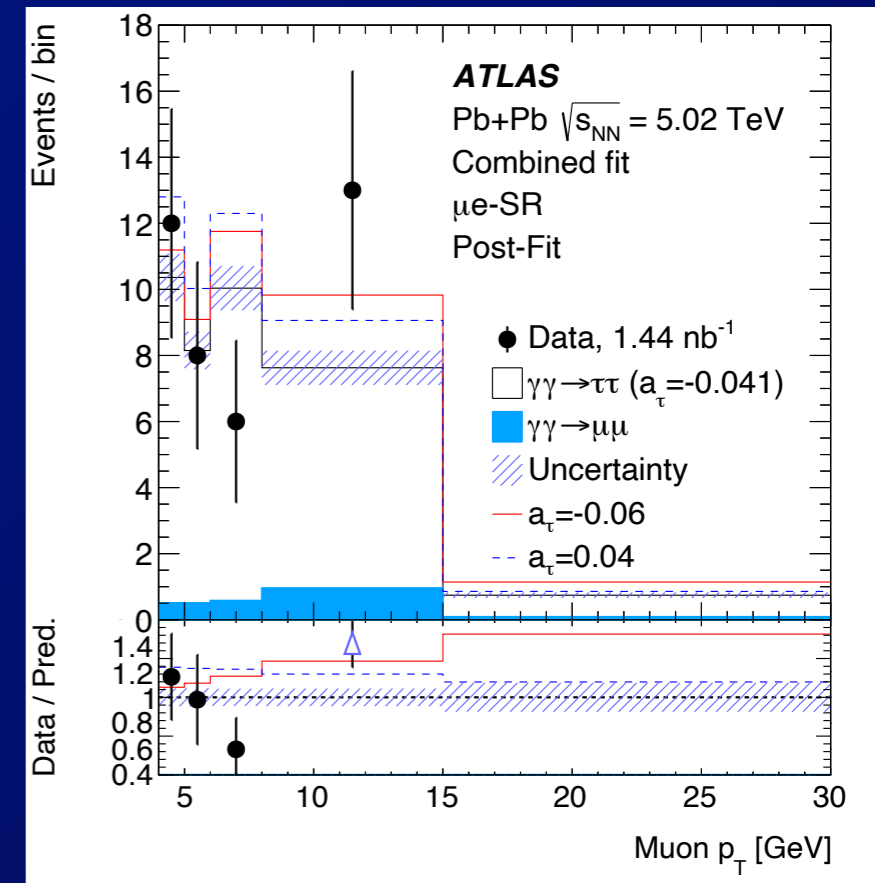
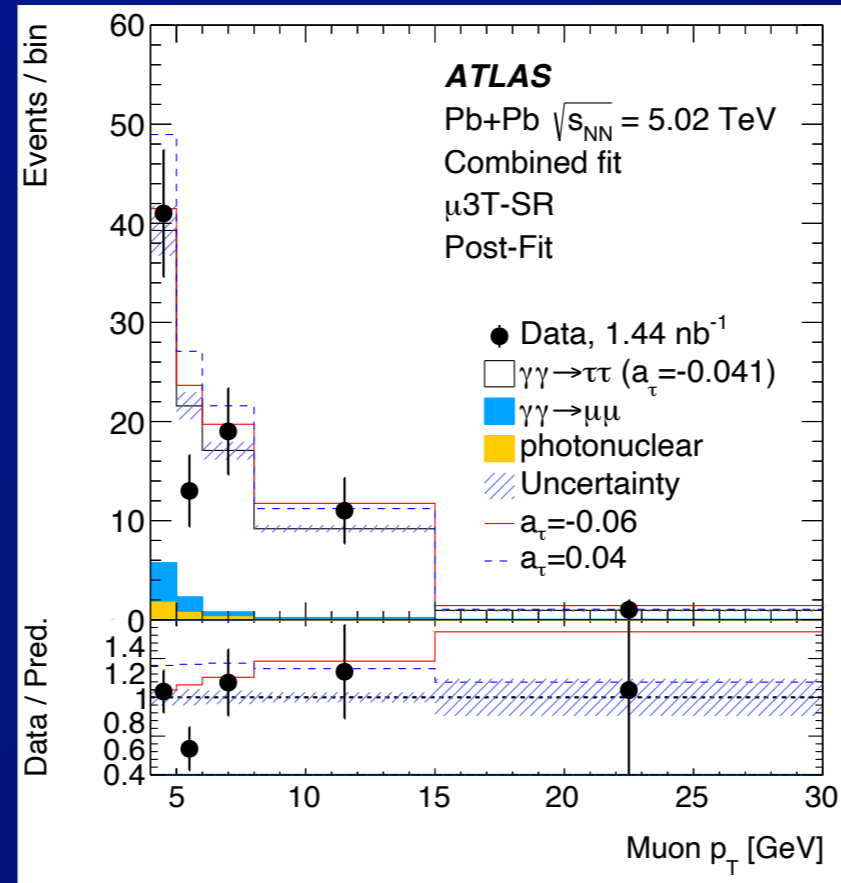
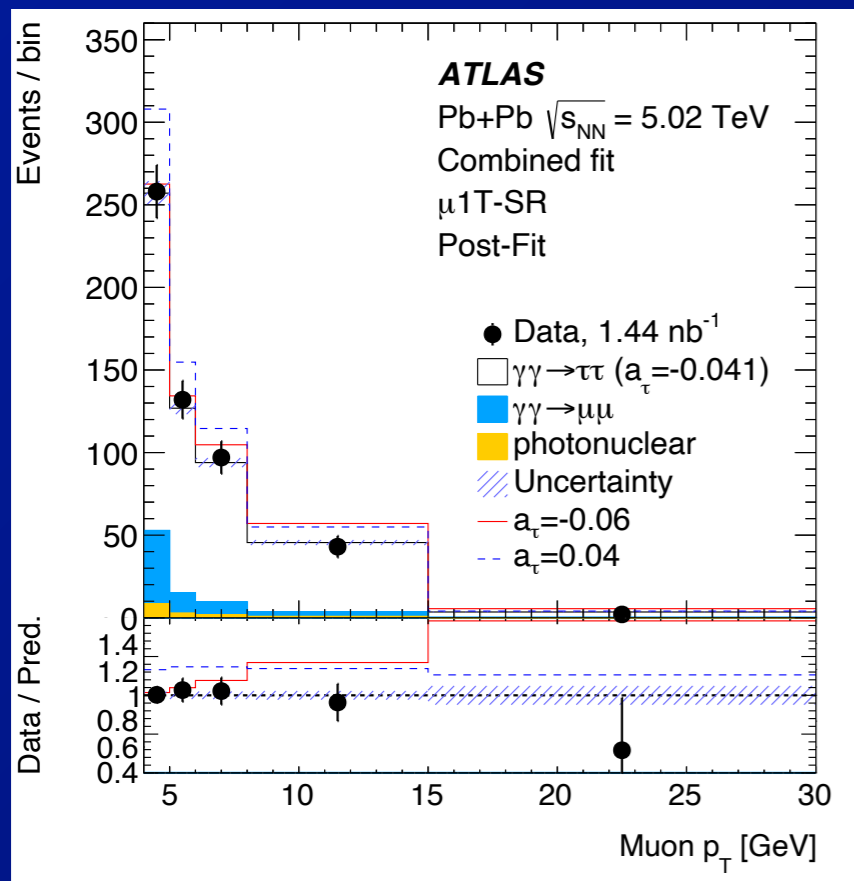
- 3 control regions to constrain backgrounds

⇒ Expected backgrounds < 15% in all three channels

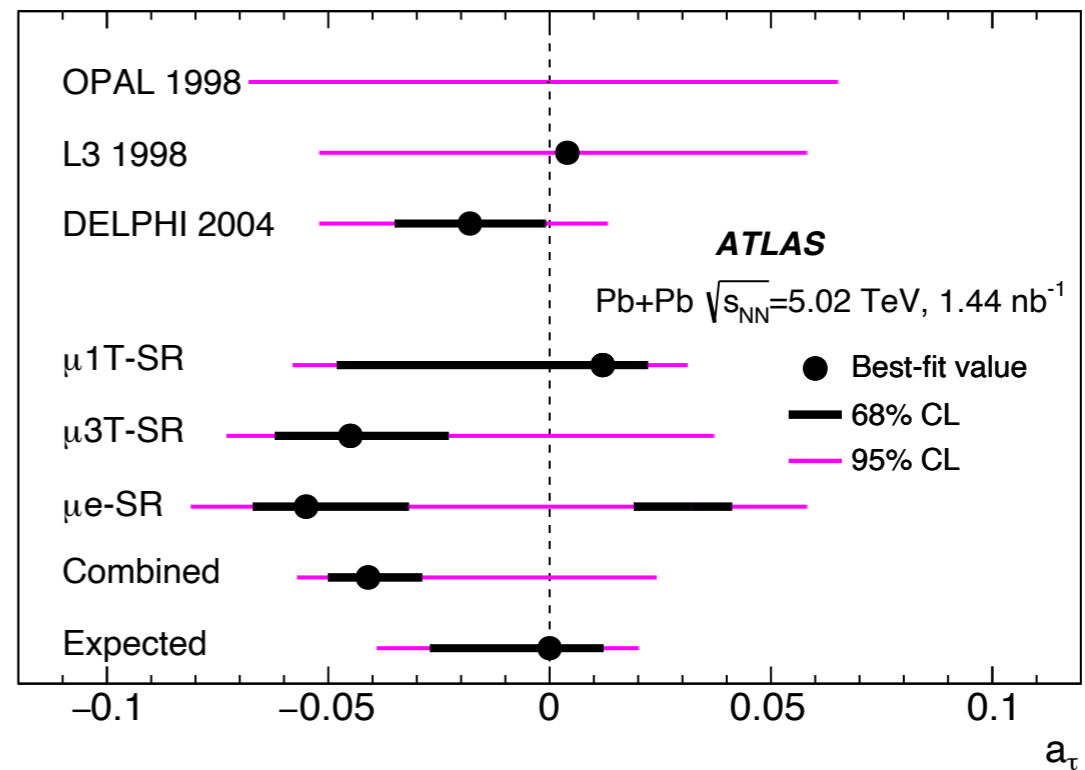
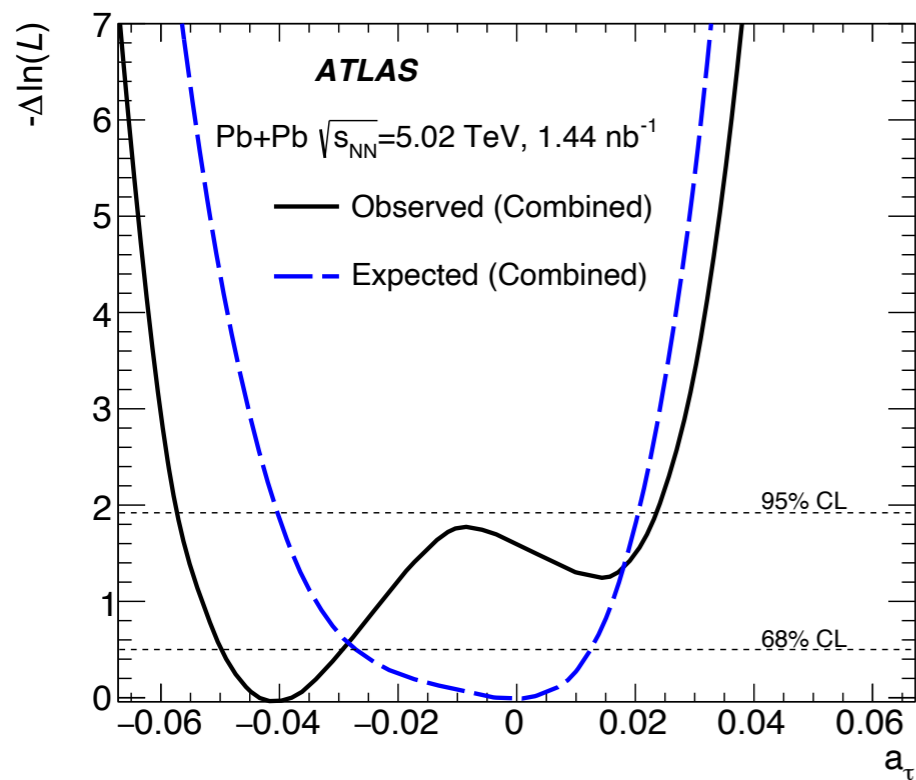
- **LL Fit to a_τ assuming $\gamma\tau\tau$ coupling** $F_1(q^2)\gamma^\mu + F_2(q^2)\frac{i}{2m_\tau}\sigma^{\mu\nu}q_\nu$

- Similar parameterization to LEP analyses

⇒ $a_\tau \equiv (g_\tau - 2)/2 = -0.041, a_\tau^{\text{SM}} = 0.0012$

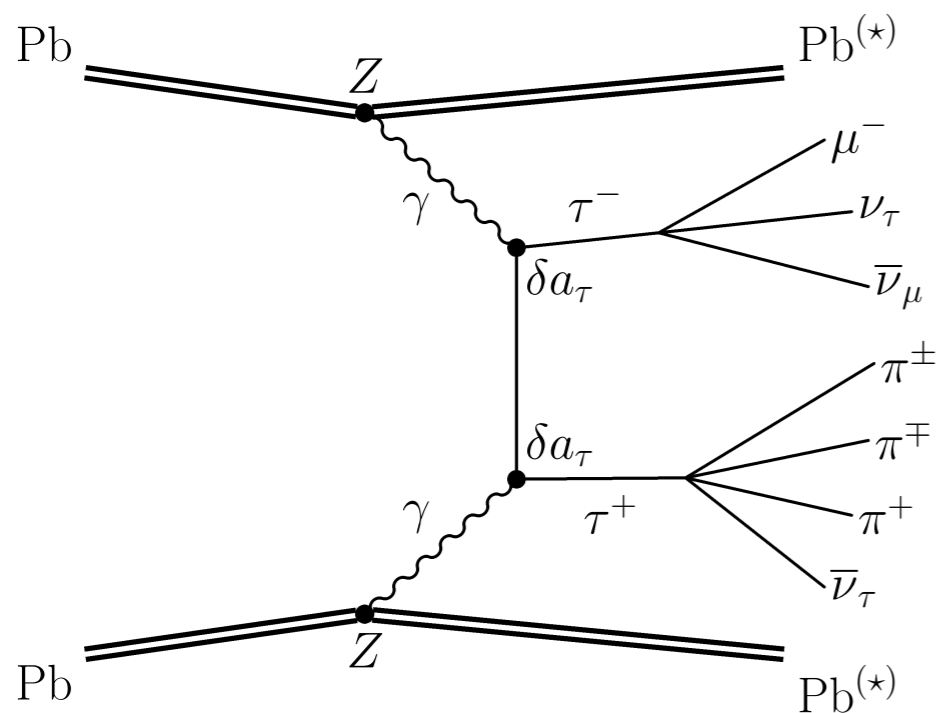


- LL Fit to a_τ assuming $\gamma\tau\tau$ coupling $F_1(q^2)\gamma^\mu + F_2(q^2)\frac{i}{2m_\tau}\sigma^{\mu\nu}q_\nu$
- “Standard” evaluation of 68% and 95% CLs
 - But interference between SM and BSM processes make the 95% CLs “unusual”
 - ⇒ Allow non-zero positive and negative a_τ



⇒ Use of muon p_τ distributions makes result less sensitive to uncertainties in photon flux

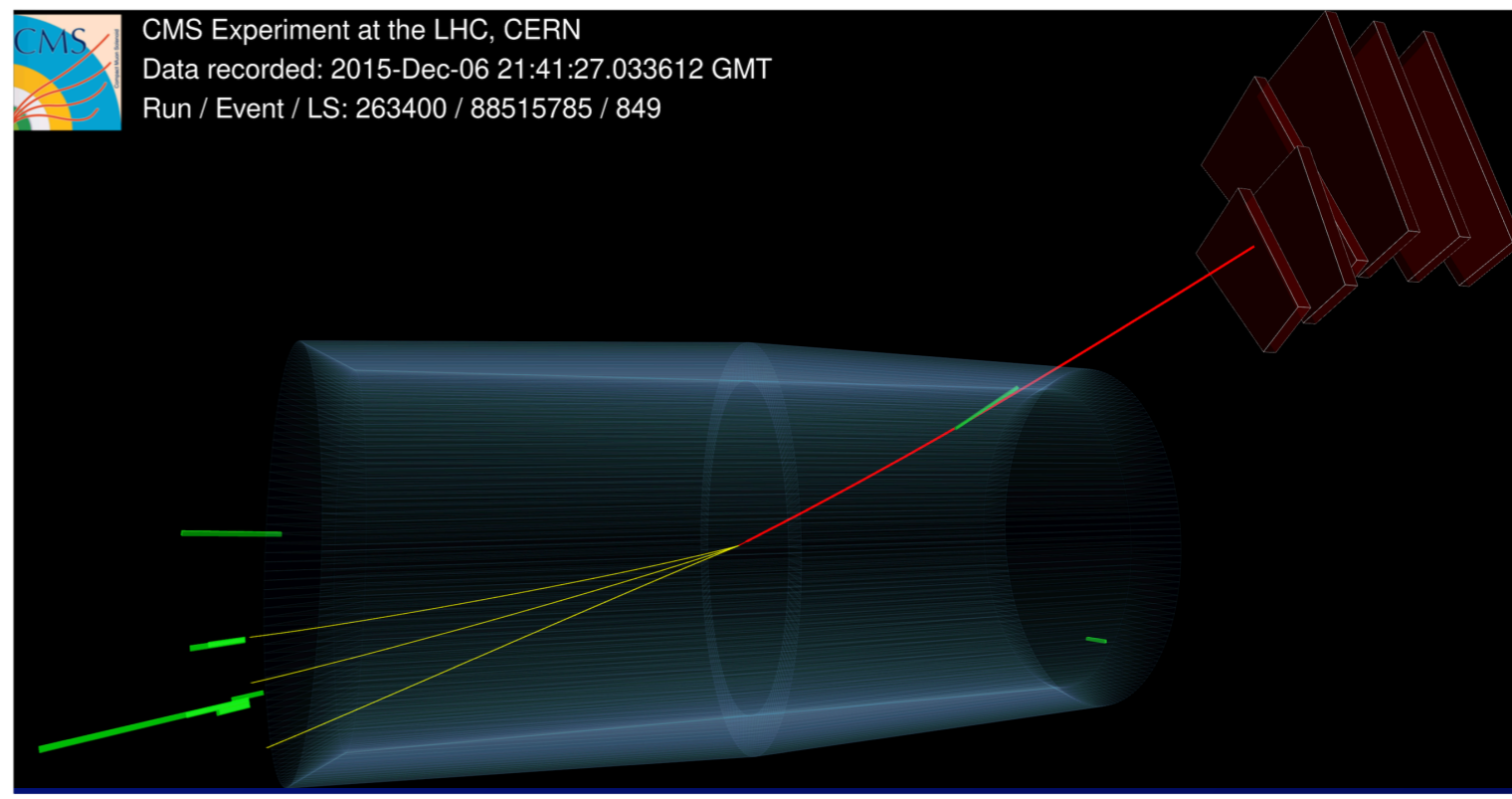
- CMS measurement focused on the $\mu+3$ track channel
 - ⇒ Directly constrain one of the tau decays
- Less luminosity (0.4 nb^{-1}), but lower p_{τ} threshold on muon:
 - $p_{\tau\mu} > 3.5 \text{ GeV}$ for $|\eta_{\mu}| < 1.2$,
 - $p_{\tau\mu} > 2.5 \text{ GeV}$ for $1.2 < |\eta_{\mu}| < 2.4$
- ⇒ Similar statistical precision on σ_{fid} as the ATLAS measurement
- ⇒ But by fitting σ_{fit} , sensitive to photon flux



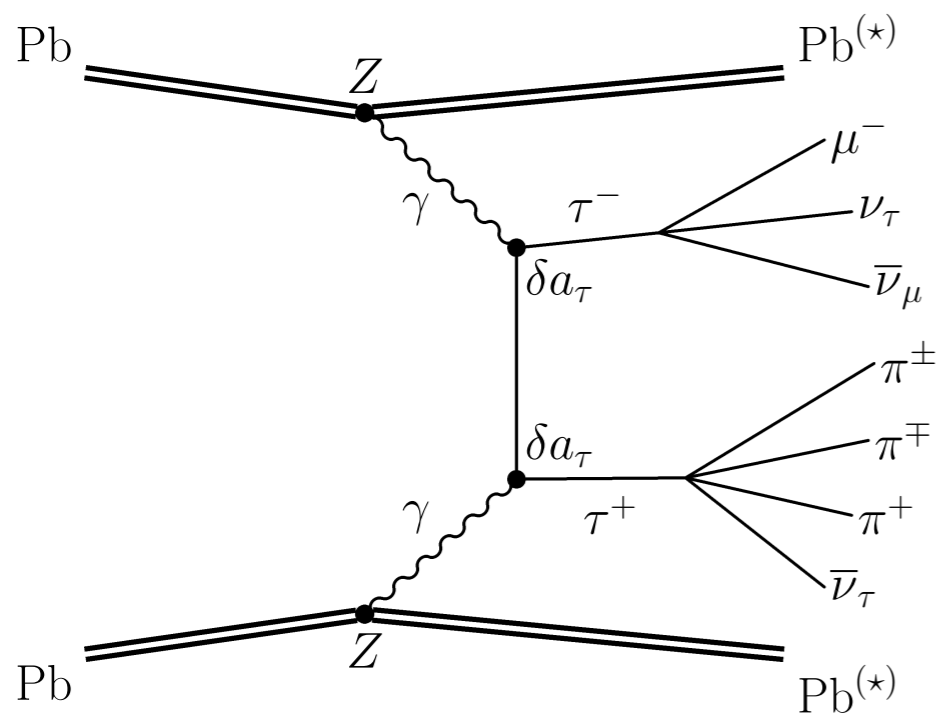
CMS Experiment at the LHC, CERN

Data recorded: 2015-Dec-06 21:41:27.033612 GMT

Run / Event / LS: 263400 / 88515785 / 849

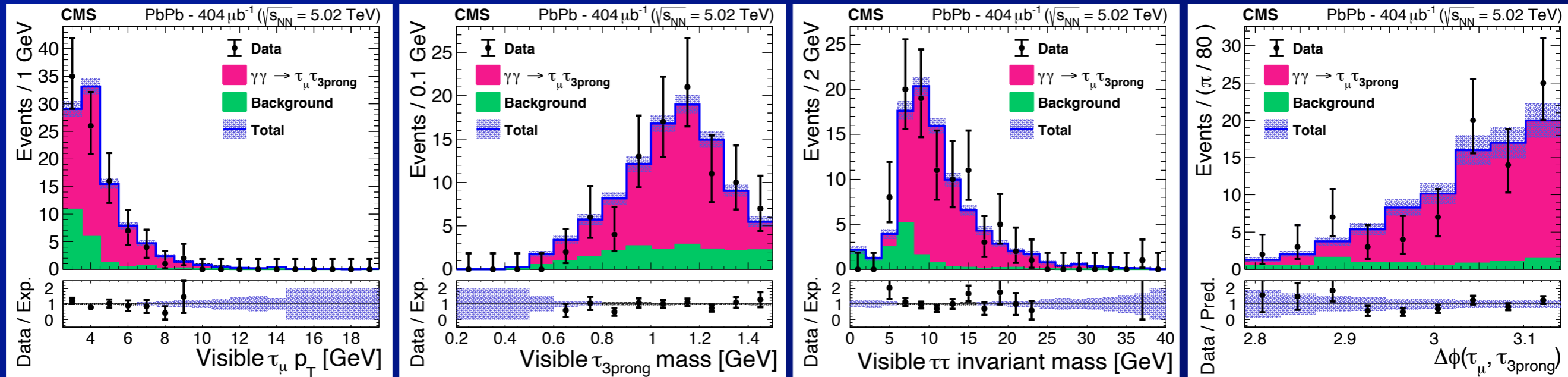


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Muon selection	$p_T > 3.5 \text{ GeV}$ for $ \eta < 1.2$ $p_T > 2.5 \text{ GeV}$ for $1.2 < \eta < 2.4$
Pion selection	$p_T > 0.5 \text{ GeV}$ for the leading $p_T > 0.3 \text{ GeV}$ for the (sub-)subleading $ \eta < 2.5$
$\tau_{3\text{prong}}$ selection	$p_T^{\text{vis}} > 2 \text{ GeV}$ and $0.2 < m_\tau^{\text{vis}} < 1.5 \text{ GeV}$

- Clean $\gamma\gamma \rightarrow \tau^+\tau^-$ signal with low bkgd (@ small $m_{\tau\tau}$)
- 3 CR regions at higher track multiplicity, and/or higher E_{HF}^{lead} used to constrain background

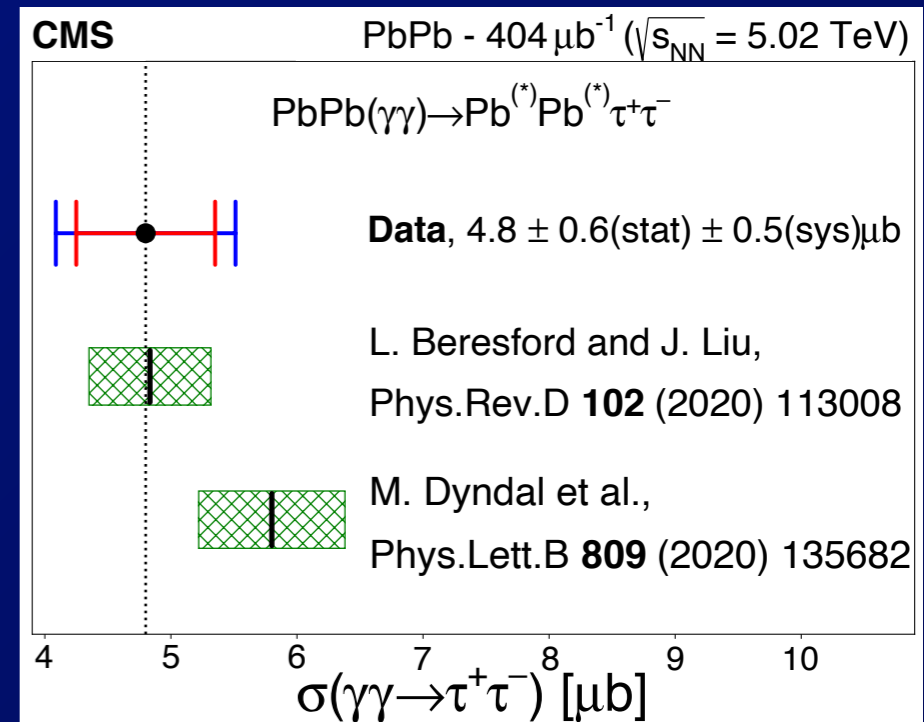


- From fit to μ -3T $\Delta\phi$ distribution

$\Rightarrow N_{sig} = 77 \pm 12$

\Rightarrow SM ratio: $r = 0.99 (+0.16) (-0.14)$

$\Rightarrow A_\tau = 0.001 (+0.055) (-0.089)$ 68% CL



**$\gamma+\gamma$ production of dileptons:
A closer look**

- The photon k_T distribution has only recently been a subject of significant focus & effort.
 - Typically related to nuclear Form factor

⇒ e.g. in STARlight:

$$\frac{dN(k, p_T)}{dp_T} = \frac{2F^2(Q^2 = p_T^2)p_T^3}{(2\pi)^2((k/\gamma)^2 + p_T^2)^2}$$

- But this formula (not unique to STARlight) loses correlation between the photon k_T and r_\perp
 - ⇒ required by physics (see [arXiv 2207.05595.pdf](https://arxiv.org/abs/2207.05595))
- r_\perp and/or b-dependence of photon k_T distribution the subject of much recent work by multiple groups

- Recent calculation by Zha, Brandenburg, Tang, Xu
 - Using formalism from Hencken, Trautmann, Baur
- Start from EM potential of the two nuclei

$$A_1^\mu(k_1, b) = -2\pi(Z_1 e) e^{ik_1^\tau b_\tau} \delta(k_1^\nu u_{1\nu}) \frac{F_1(-k_1^\rho k_{1\rho})}{k_1^\sigma k_{1\sigma}} u_1^\mu$$
$$A_2^\mu(k_2, 0) = -2\pi(Z_2 e) e^{ik_2^\tau b_\tau} \delta(k_2^\nu u_{2\nu}) \frac{F_2(-k_2^\rho k_{2\rho})}{k_2^\sigma k_{2\sigma}} u_2^\mu$$

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 - Using formalism from Hencken, Trautmann, Baur
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 - Then, using S-matrix analysis (not QED) obtain “gEPA”

$$A_1^\mu(k_1, b) = -2\pi(Z_1 e) e^{ik_1^\tau b_\tau} \delta(k_1^\nu u_{1\nu}) \frac{F_1(-k_1^\rho k_{1\rho})}{k_1^\sigma k_{1\sigma}} u_1^\mu$$

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$$\sigma = 16 \frac{Z^4 e^4}{(4\pi)^2} \int d^2 b \int \frac{dw_1}{w_1} \frac{dw_2}{w_2} \frac{d^2 k_{1\perp}}{(2\pi)^2} \frac{d^2 k_{2\perp}}{(2\pi)^2} \frac{d^2 q_\perp}{(2\pi)^2}$$

$$\times \frac{F(-k_1^2)}{k_1^2} \frac{F(-k_2^2)}{k_2^2} \frac{F^*(-k_1'^2)}{k_1'^2} \frac{F^*(-k_2'^2)}{k_2'^2} e^{-i\vec{b} \cdot \vec{q}_\perp}$$

$$\times [(\vec{k}_{1\perp} \cdot \vec{k}_{2\perp})(\vec{k}'_{1\perp} \cdot \vec{k}'_{2\perp}) \sigma_s(w_1, w_2)$$

$$+ (\vec{k}_{1\perp} \times \vec{k}_{2\perp})(\vec{k}'_{1\perp} \times \vec{k}'_{2\perp}) \sigma_{ps}(w_1, w_2)]$$

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- Using formalism from Hencken, Trautmann, Baur

- Start from EM potential of the two nuclei

- then, using S-matrix analysis (not QED) obtain “gEPA”

- has explicit Fourier term involving the A+A impact parameter, \mathbf{b}

$$A_1^\mu(k_1, b) = -2\pi(Z_1 e) e^{ik_1^\tau b_\tau} \delta(k_1^\nu u_{1\nu}) \frac{F_1(-k_1^\rho k_{1\rho})}{k_1^\sigma k_{1\sigma}} u_1^\mu$$

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- Recent calculation by Zha, Brandenburg, Tang, Xu

– Using formalism from Hencken, Trautmann, Baur

- Start from EM potential of the two nuclei

– Alternatively, perform the actual QED computation:

$$A_1^\mu(k_1, b) = -2\pi(Z_1 e) e^{ik_1^\tau b_\tau} \delta(k_1^\nu u_{1\nu}) \frac{F_1(-k_1^\rho k_{1\rho})}{k_1^\sigma k_{1\sigma}} u_1^\mu,$$

$$A_2^\mu(k_2, 0) = -2\pi(Z_2 e) e^{ik_2^\tau b_\tau} \delta(k_2^\nu u_{2\nu}) \frac{F_2(-k_2^\rho k_{2\rho})}{k_2^\sigma k_{2\sigma}} u_2^\mu$$

$$\sigma = \int d^2b \frac{d^6 P(\vec{b})}{d^3p_+ d^3p_-} = \int d^2q \frac{d^6 P(\vec{q})}{d^3p_+ d^3p_-} \int d^2b e^{i\vec{q}\cdot\vec{b}},$$

$$\frac{d^6 P(\vec{q})}{d^3p_+ d^3p_-} = (Z\alpha)^4 \frac{4}{\beta^2} \frac{1}{(2\pi)^6 2\epsilon_+ 2\epsilon_-} \int d^2q_1$$

$$F(N_0)F(N_1)F(N_3)F(N_4)[N_0 N_1 N_3 N_4]^{-1}$$

$$\times \text{Tr}\{(\not{p}_- + m)[N_{2D}^{-1}\psi_1(\not{p}_- - \not{q}_1 + m)\psi_2 +$$

$$N_{2X}^{-1}\psi_2(\not{q}_1 - \not{p}_+ + m)\psi_1](\not{p}_+ - m)[N_{5D}^{-1}\psi_2$$

$$(\not{p}_- - \not{q}_1 - \not{q} + m)\psi_1 + N_{5X}^{-1}\psi_1(\not{q}_1 + \not{q} - \not{p}_+$$

$$+ m)\psi_2]\},$$

with

$$N_0 = -q_1^2, N_1 = -[q_1 - (p_+ + p_-)]^2,$$

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- Which also has the explicit Fourier term involving the impact parameter, \mathbf{b}

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$$A_2^\mu(k_2, 0) = -2\pi(Z_2 e) e^{ik_2^\tau b_\tau} \delta(k_2^\nu u_{2\nu}) \frac{F_2(-k_2^\rho k_{2\rho})}{k_2^\sigma k_{2\sigma}} u_2^\mu$$

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– both gEPA and QED calculations have **b-dependent** “broadening” of the dilepton p_T distributions

⇒ more on this later

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- An alternative calculation has been performed by Klein *et al*, and Klusek-Gawenda *et al*:
- Starting from the photon Wigner distribution
 - describe the correlation between photon k_T and r_\perp
 - using formalism developed for PDFs (Belitsky, Ji, Yuan)

$$xf_\gamma(x, k_T; b_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} e^{i\Delta_\perp \cdot b_\perp} xf_\gamma(x, k_T; \Delta_\perp).$$

$$\begin{aligned} xf_\gamma(x, k_T; \Delta_\perp) &= xh_\gamma(x, k_T; \Delta_\perp) \\ &= \frac{4Z^2\alpha}{(2\pi)^2} \frac{q_\perp \cdot q'_\perp}{q^2 q'^2} F_A(q^2) F_A(q'^2) \end{aligned}$$

$$q_\perp = k_T - \Delta_\perp/2, \quad q'_\perp = k_T + \Delta_\perp/2$$

$$q^2 = q_\perp^2 + x^2 m_p^2.$$

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- ⇒ Also see Fourier term, but now for single nucleus

$$x f_\gamma(x, k_T; b_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{i\Delta_\perp \cdot b_\perp} x f_\gamma(x, k_T; \Delta_\perp).$$

$$\begin{aligned} x f_\gamma(x, k_T; \Delta_\perp) &= x h_\gamma(x, k_T; \Delta_\perp) \\ &= \frac{4Z^2 \alpha}{(2\pi)^2} \frac{q_\perp \cdot q'_\perp}{q^2 q'^2} F_A(q^2) F_A(q'^2) \end{aligned}$$

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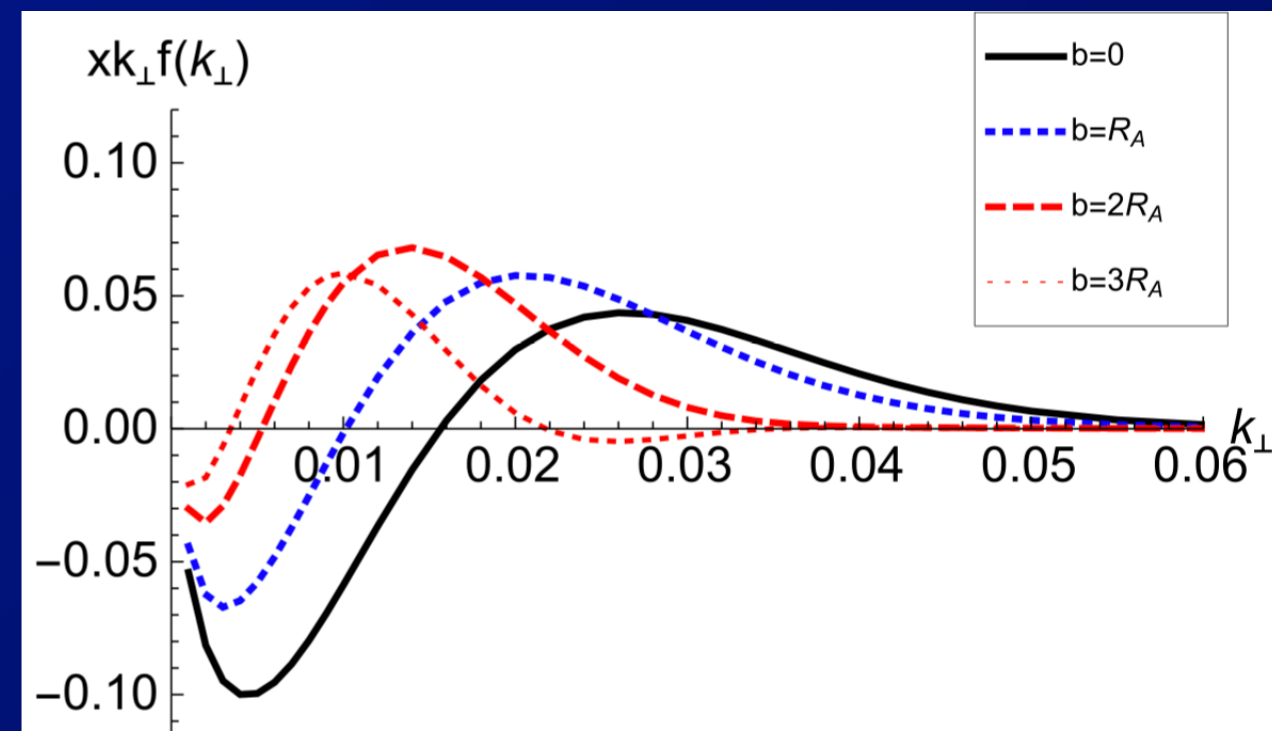
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⇒ Non-trivial dependence of photon WF on b , k_T

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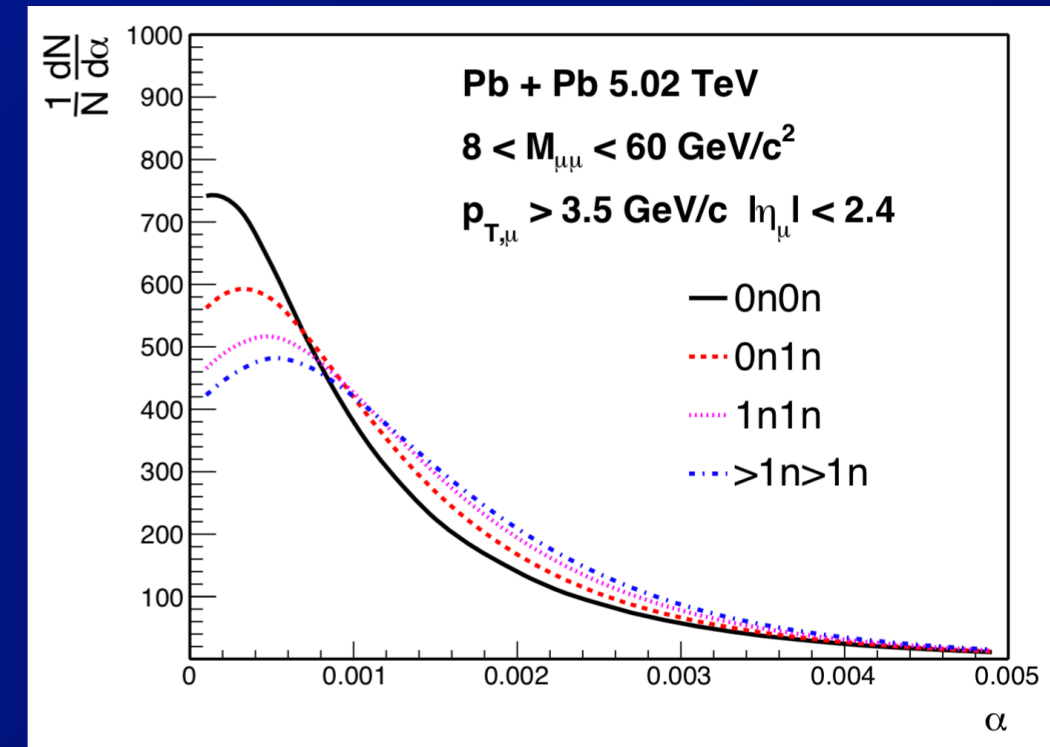
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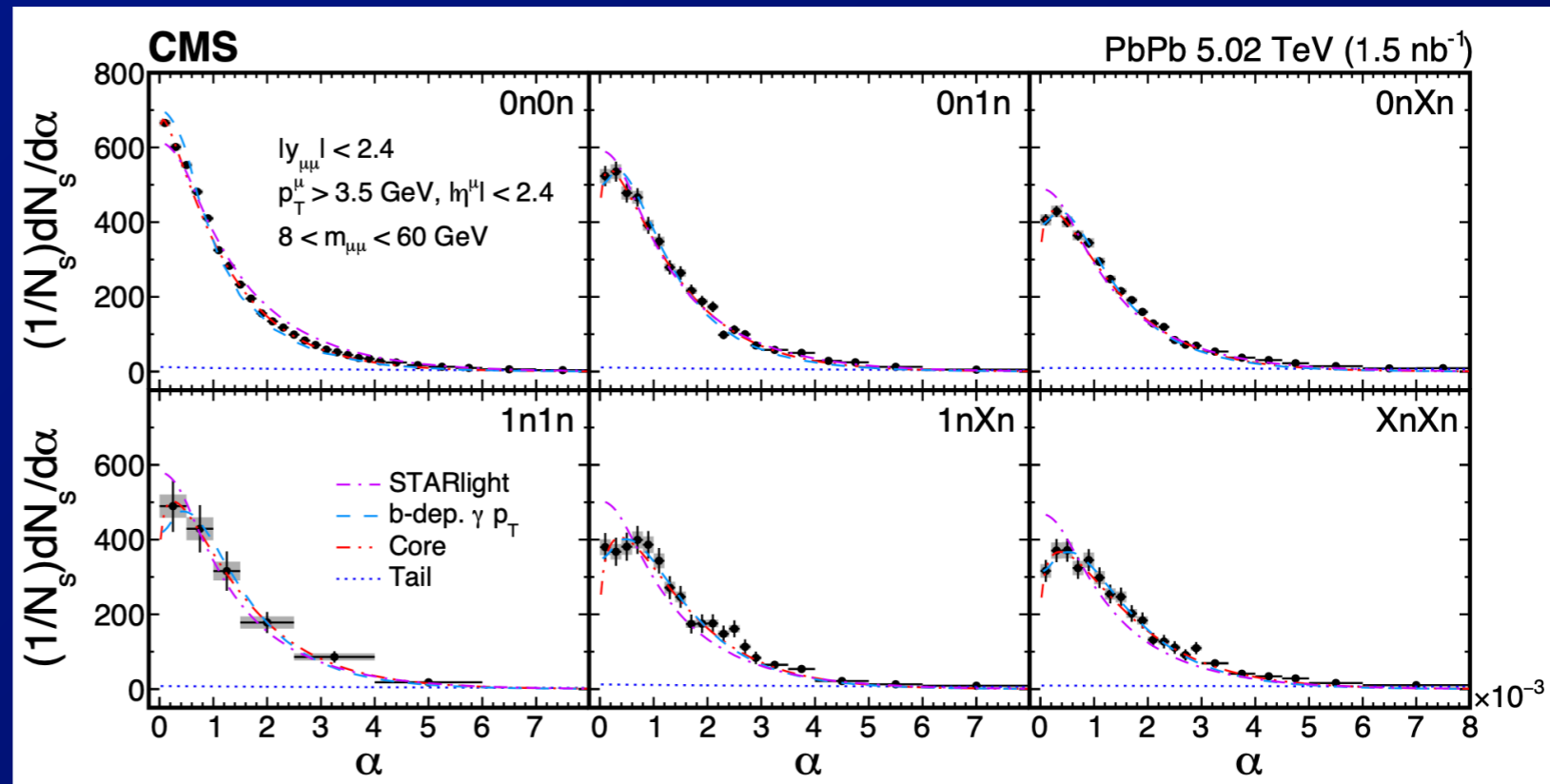


Brandenburg et al, arXiv:2006.07365

- **b-dependence of Coulomb excitation, forward neutrons**
- **+ b dependence of photon k_T**
 \Rightarrow Broadening of dilepton acoplanarity with increasing nuclear breakup (# neutrons)



- **Observed by CMS**

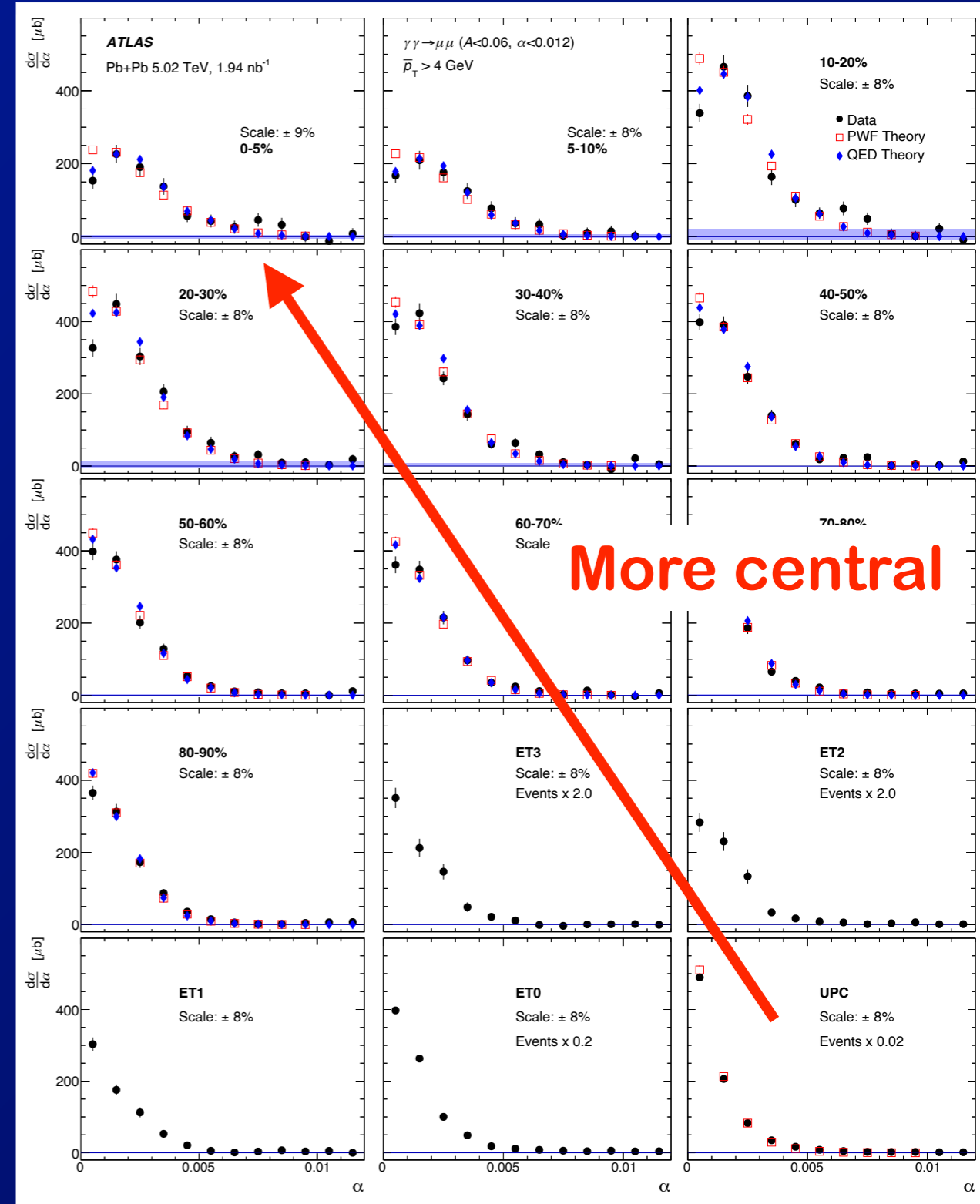


• ATLAS studied $\gamma+\gamma \rightarrow \mu^+\mu^-$ in hadronic Pb+Pb collisions

– Goal: use tight $\Delta\phi$ correlation of muons as EM probe of the quark gluon plasma

⇒ See a centrality-dependence of $\mu^+\mu^-$ acoplanarity distribution

⇒ Magnetic field? Collisional?



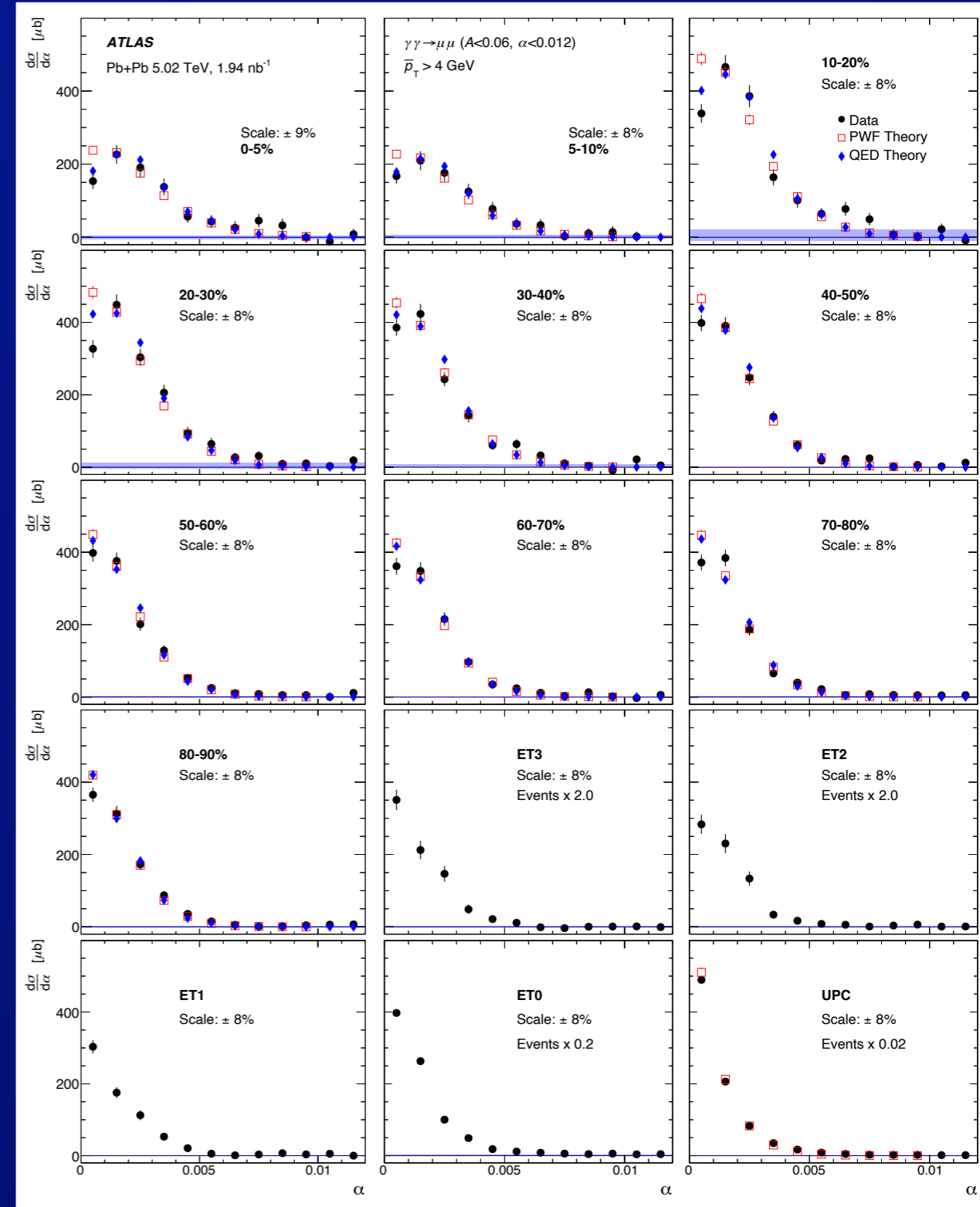
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$\gamma+\gamma$ dilepton production in hadronic Pb+Pb 56

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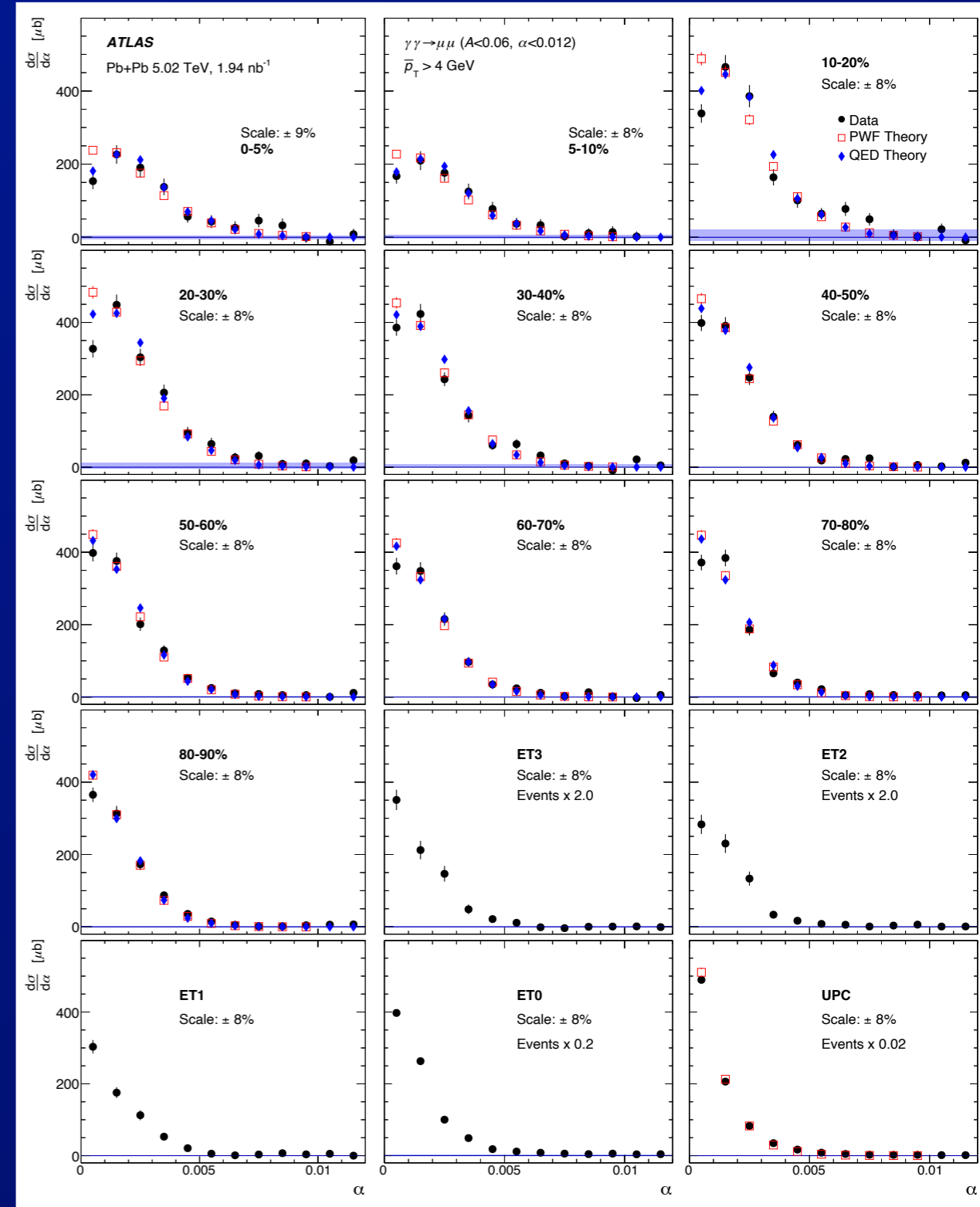
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⇒ May provide new/competitive method to probe the electromagnetic structure of nuclei.



- **LHC (and RHIC) are high-luminosity photon colliders**
 - Can study $\gamma+\gamma$ scattering with $\sqrt{s} > 100$ GeV
 - Photon fluxes can be calculated ab initio
 - But important details still under study
 - ⇒ Especially photon k_T and correlation with r_\perp and b
- **$\gamma+\gamma \rightarrow$ dilepton data provide important tests of theory**
 - But there are complications/interesting physics
 - ⇒ Photon k_T and impact parameter dependence
 - ⇒ Dissociative γ emission
 - ⇒ Higher-order processes (didn't discuss)
 - $\gamma+\gamma \rightarrow$ dileptons in hadronic Pb+Pb collisions a new topic
- **$\gamma+\gamma$ processes are being used for SM and BSM tests**
 - Light-by-light, ALP limits
 - $\tau g-2$
 - ⇒ more will come: e.g. WW, $b\bar{b}$, exotics, ...