

THEORY INTRODUCTION TO EXTENDED HIGGS MODELS

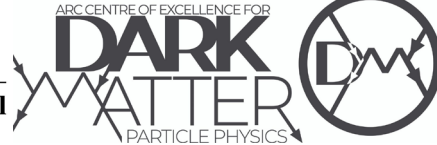
A dark matter phenomenology perspective

LCH DM 24 @ CERN

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Australian Research Council



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01 MOTIVATIONS AND ASSUMPTIONS

- Many fermions but only 1 scalar discovered so far
- DM could be connected to SM through spin-0 or spin-1 particles
- New spin-1 resonances highly constrained
- Spin-1 with non-purely vector couplings requires new scalars
- Extended higgs sectors well motivated (MSSM/NMSSM, EW Baryogenesis, Neutrino masses)

- S-channel mediator
- Spin-0
- DM is SM singlet Fermion (scalar?)



- DM can only couple to scalar that is SM singlet S
- SM fermions can only couple to SM higgs-like doublet ϕ



- Need $S - \phi$ mixing!



02 MINIMAL MODELS: 2HDM+S/A

- One more assumption: CP-preserving → Cannot mix CP-even with C-odd
- Minimal: only one mixing

$$\mathcal{L} = -yS\bar{\chi}\chi$$

CP-Even

- Mix S with SM doublet ϕ ?



Yes



No

- DM search turns into higgs precision

- Need one additional doublet for freedom on SM fermions-new scalar(s) couplings

$$\mathcal{L} = -iyP\bar{\chi}\gamma^5\chi$$

CP-Odd

- No pseudoscalar in the SM



- Need one additional doublet



02 MINIMAL MODELS: 2HDM+S/A

2HDM+s

1612.03475

CP-Even

- Mixing term $H_1^\dagger H_2 S$
- 3-scalar mixing $\rho_{1,2,3} \rightarrow h, H, s$
- 1 Pseudoscalar A
- 1 charged scalar H^\pm
- Only h, H, s can couple to both DM and SM fermions
- Rotation matrix for $\rho_{1,2,3} \rightarrow h, H, s$ constrained by higgs-strength

2HMD+a

1404.3716

CP-Odd

- Mixing term $H_1^\dagger H_2 P$
- 2-pseudoscalar mixing $\eta_{1,2} \rightarrow a, A$
- 2 Scalars h, H
- 1 charged scalar H^\pm
- Only a, A can couple to both DM and SM fermions
- Rotation matrix for $\rho_{1,2} \rightarrow |\cos(\alpha - \beta)| \ll 1$



02 MINIMAL MODELS: 2HDM+S/A

- 2HDM+a parameter space

$$\begin{aligned} V = & m_{11}H_1^\dagger H_1 + m_{22}H_2^\dagger H_2 + m_{12}(H_1^\dagger H_2 + H_2^\dagger H_1) + \\ & + \frac{\lambda_1}{2}(H_1^\dagger H_1)^2 + \frac{\lambda_2}{2}(H_2^\dagger H_2)^2 + \lambda_3(H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4(H_1^\dagger H_2)(H_2^\dagger H_1) \\ & + \lambda_5 \left((H_1^\dagger H_2)^2 + (H_2^\dagger H_1)^2 \right) \\ & + \frac{1}{2}m_{PP}P^2 + \lambda_P P^4 + \frac{1}{2}\lambda_{P1}P^2 H_1^\dagger H_1 + \frac{1}{2}\lambda_{P2}P^2 H_2^\dagger H_2 + i\mu P(H_1^\dagger H_2 - H_2^\dagger H_1) \end{aligned}$$

- 13 parameters (CP-conserving, all real) +2 (DM yukawa and mass) – 2 constraints $(v, m_h) = 13$ free parameters
- Most DM phenomenology insensitive to λ_P ➡ Usually 12 parameters considered



02 MINIMAL MODELS: 2HDM+S/A

- 2HDM+a parameter space

$$m_{11}, m_{22}, m_{12}, \lambda_{1,2,3,4,5}, m_{PP}, \lambda_{P1}, \lambda_{P2}, \mu, y_\chi, m_\chi$$

Can be exchanged for

$$v, \mathbf{m}_h, m_H, m_A, m_{H^\pm}, m_a, m_\chi, \tan\beta, \cos(\alpha - \beta), \sin\theta, y_\chi, \lambda_3, \lambda_{P1}, \lambda_{P2}$$

Fixed

- Benchmark point for run 2:
- $\cos(\alpha - \beta) = 0$ (several reasons)
- $\tan\beta, \sin\theta$ free parameters
- $m_H = m_{H^\pm}$ (custodial symmetry)
- $m_H = m_A (= m_{H^\pm})$ also adopted in some cases
- λ_3 satisfying BFB condition
- $\lambda_{P1} = \lambda_{P2} = \lambda_3$ to keep $\Gamma(H \rightarrow aa), \Gamma(A \rightarrow ha)$ small
- y_χ large enough to allow $BR(a \rightarrow \chi\chi) \sim 100\%$ for $m_a < 2m_t$
- $m_\chi = 10\text{GeV}$ small enough to allow $BR(a \rightarrow \chi\chi) \sim 100\%$ for $m_a > 100\text{GeV}$



03

THEORY CONSTRAINTS

- Unitarity: will set upper bounds on λ_i
- Perturbativity: possibly, you want to stay away from the unitarity limit
- Bounded from Below: set of inequalities to guarantee that the potential has global minimum. Will give minimum and maximum values of λ_i
- Stable vacuum: the chosen minima is the global one: condition involving parameters of the potential



- In the limit of large masses for the heavy scalars, mass splittings will be forced to be small due to the upper bounds on the couplings.



04 EWPT, FLAVOUR

- EWPT: S, T, U Peskin-Takeuchi parameters, with $T \propto \Delta\rho$

Assumption $m_H = m_{H^\pm}$

- For $\cos(\alpha - \beta) = 0$, $\Delta\rho = \frac{1}{(4\pi)^2 v^2} \left(\cos^2\theta f(m_{H^\pm}^2, m_A^2, m_H^2) + \sin^2\theta f(m_{H^\pm}^2, m_a^2, m_H^2) \right)$
- $f(x, y, x) = 0 \Rightarrow m_H = m_{H^\pm}$ is sufficient to have $\Delta\rho = 0$
- Deviations from $m_H = m_{H^\pm}$ allowed as long as $\Delta\rho \in [-1.6 \cdot 10^{-3}, 2 \cdot 10^{-3}]$
- Some mass hierarchies can only give a certain sign of $\Delta\rho$

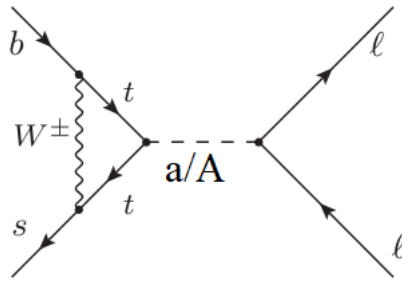
Assumption $\cos(\alpha - \beta) = 0$

- For $m_H = m_{H^\pm}$ and $\cos(\alpha - \beta) \neq 0$, $\Delta\rho \propto \cos^2(\alpha - \beta)$
- Small deviations from $\cos(\alpha - \beta) = 0$ allowed



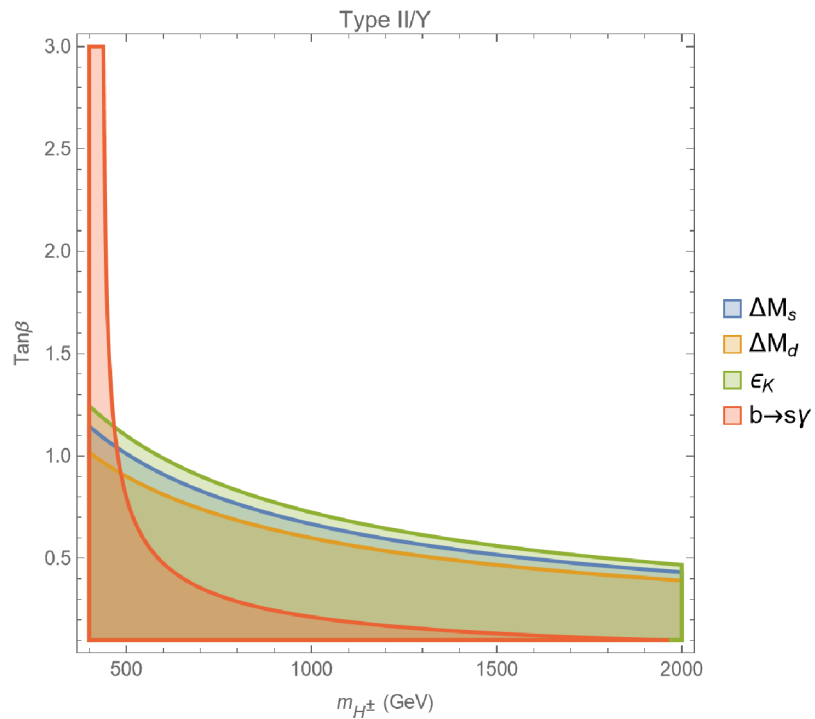
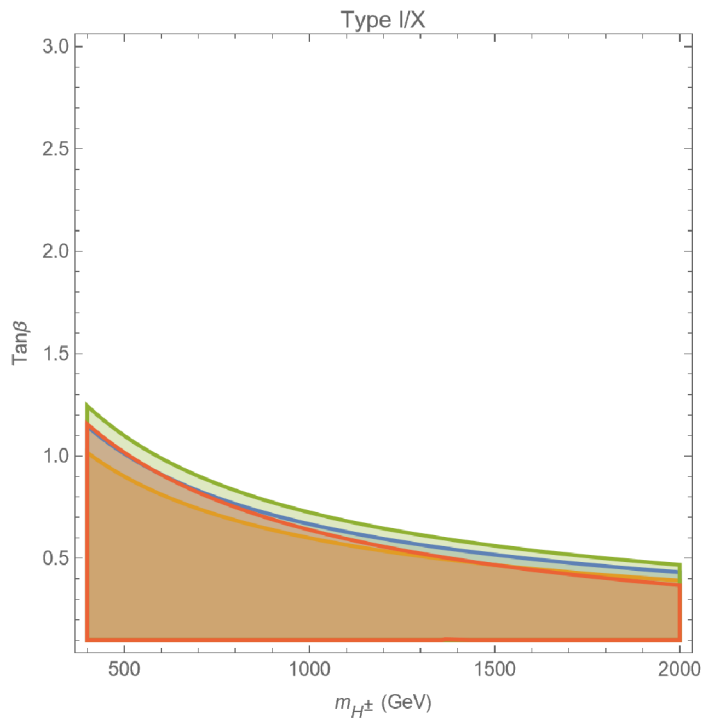
04 EWPT, FLAVOUR

- Flavour: $B_s \rightarrow \mu\mu$, $b \rightarrow s\gamma$, $\Delta M_{s,d}$, ϵ_K
- $b \rightarrow s\gamma$, $\Delta M_{s,d}$, ϵ_K driven by $H^\pm \rightarrow$ only depend on m_{H^\pm} , $\tan\beta$
- $B_s \rightarrow \mu\mu$ gets contributions from neutral scalars \rightarrow depends on all masses, $\tan\beta$, $\cos(\alpha - \beta)$, $\sin\theta$
- $b \rightarrow s\gamma$ provides low limit on m_{H^\pm} for Type II/Y
- $B_s \rightarrow \mu\mu$ provides a lower (Type II: also upper) limit on $\tan\beta$ for fixed m_a



04

EWPT, FLAVOUR



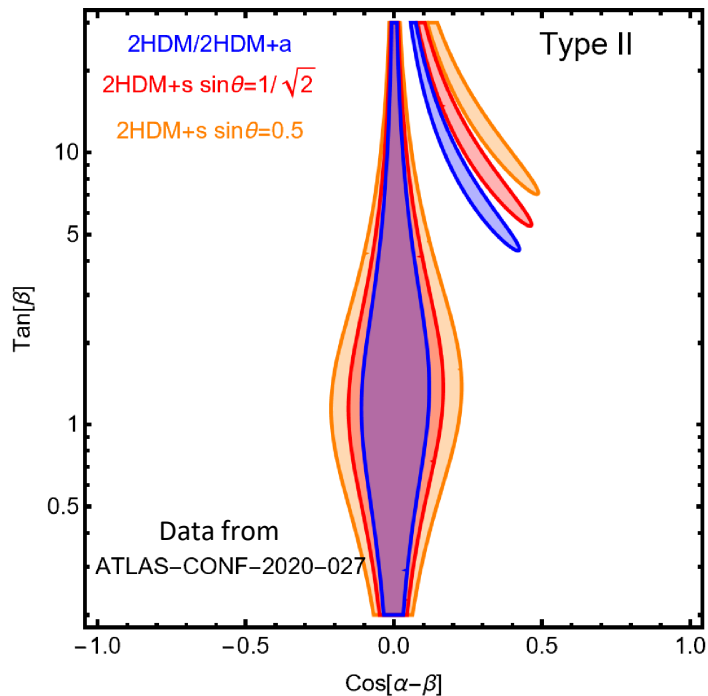
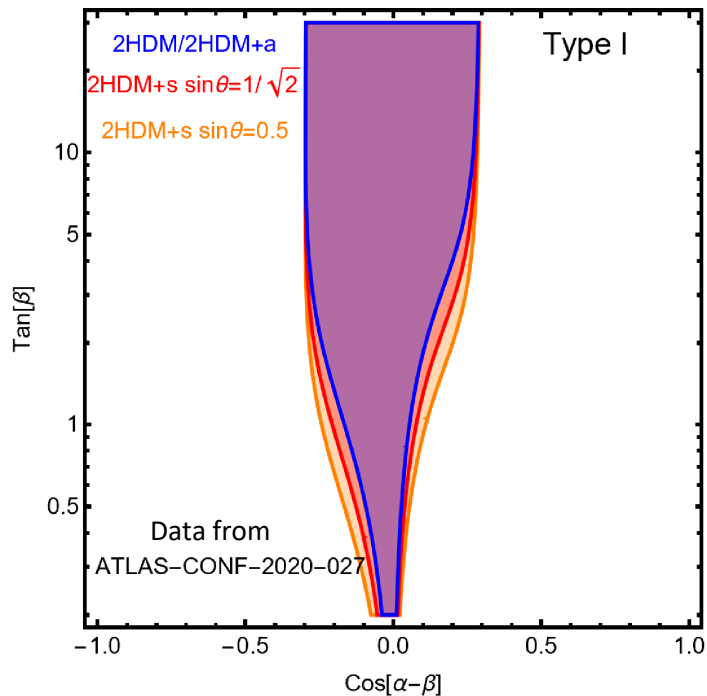
05 ALIGNMENT

- Measured strength of higgs couplings to fermions and gauge bosons requires to be close to alignment
- 2HDM+a: same constraints as in 2HDM, as hff , hVV are the same as in 2HDM
- 2HDM+s: 3×3 mixing gives more freedom, 3 mixing angles instead of 1
- 2HDM+s: hff measurements can be less constraining on $\cos(\alpha - \beta)$



05 ALIGNMENT

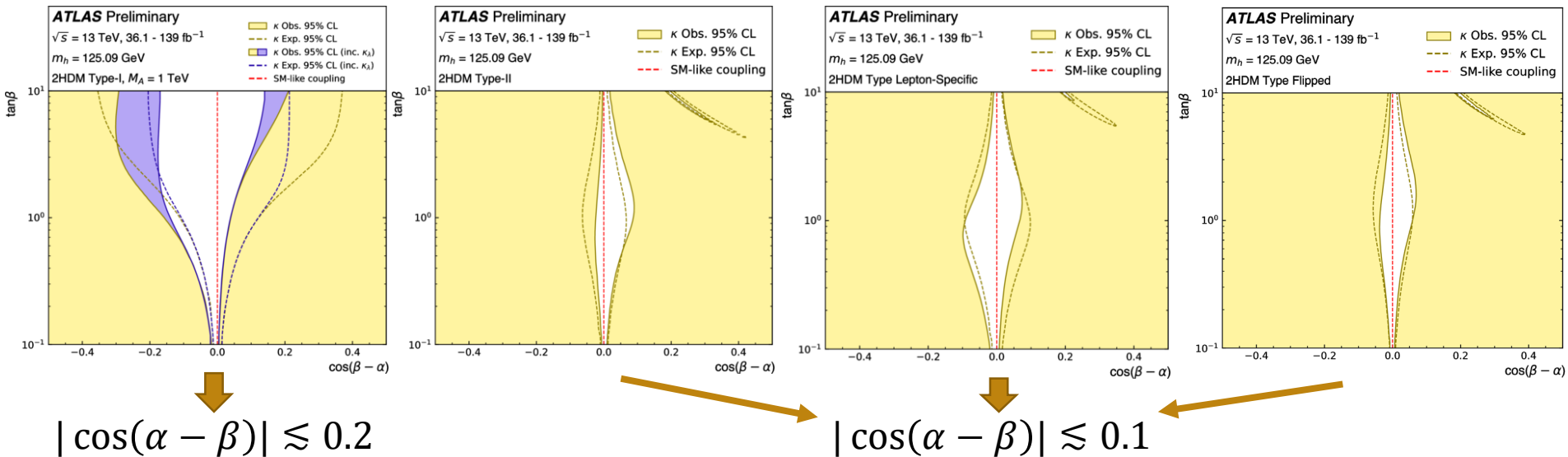
2HDM+s vs 2HDM+a comparison



05 ALIGNMENT

2HDM/2HDM+a constraints

ATLAS-CONF-2023-052



05 THEORY+EWPT+FLAVOUR+ALIGNMENT

Dropping Assumption $m_H = m_{H^\pm} = m_A$

- Allows for more freedom on λ_3 , allowing it to be $\mathcal{O}(1)$
- One might still need to be forced to consider particular hierarchies arising from the BFB and global minima conditions



- The less restrictive $m_H = m_{H^\pm}$ assumption can allow for (some of) these decays:
 - $A \rightarrow Ha$
 - $A \rightarrow HZ$
 - $H \rightarrow Aa$
 - $H \rightarrow AZ$
 - $H \rightarrow AA$ (this one requires large mass splitting \rightarrow not too large $m_{H,A}$)



05 THEORY+EWPT+FLAVOUR+ALIGNMENT

Dropping Assumption $m_H = m_{H^\pm}$

- Allows for more decay channels to open (depending on mass hierarchy):
- $A \rightarrow H^\pm W^\mp$
- $H \rightarrow H^\pm W^\mp$
- $H \rightarrow H^\pm H^\mp$ (requires low m_{H^\pm} → Type I/X)
- $H^\pm \rightarrow HW^\pm$
- $H^\pm \rightarrow AW^\pm$

Dropping Assumption $\cos(\alpha - \beta) = 0$

- Allows several couplings to be non-zero, opening decay channels:
- $HW^+W^-, H \rightarrow W^\pm W^\mp$
- $HZZ, H \rightarrow ZZ$
- $hH^\pm W^\mp, H^\pm \rightarrow hW^\pm$
- $hAZ, A \rightarrow hZ$
- $haZ, a \rightarrow hZ$
- $Hhh, H \rightarrow hh$
- $HhW^+W^-, H \rightarrow hW^+W^-$
- $HhZZ, H \rightarrow hZZ$
-



05

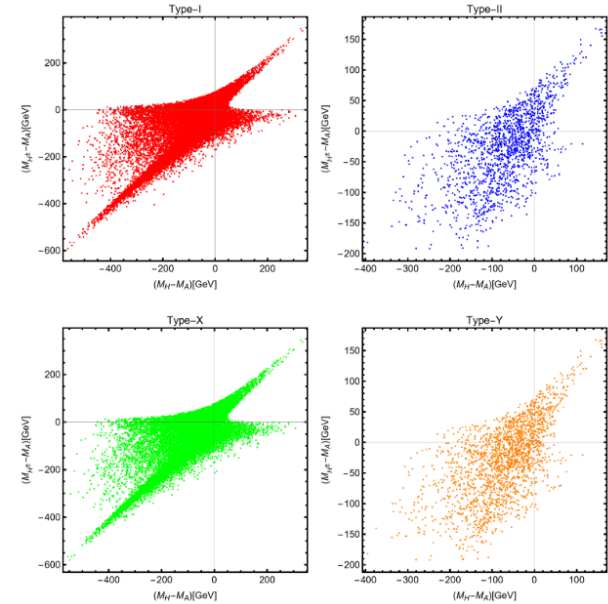
THEORY+EWPT+FLAVOUR+ALIGNMENT

Possible Mass splitting for M_A, M_H, M_{H^\pm} ?

EWPT: at least one mass splitting needs to be small

- $M_H \sim M_{H^\pm}$
- Any of the other 2 together with an upper bound on $\sin\theta$
- Unitarity/perturbativity: hard upper bound on any mass splitting
- Ballpark upper bound from perturbativity (M_A, M_H, M_{H^\pm}):

$$\frac{\Delta M}{100\text{GeV}} \lesssim \frac{\text{TeV}}{M}$$



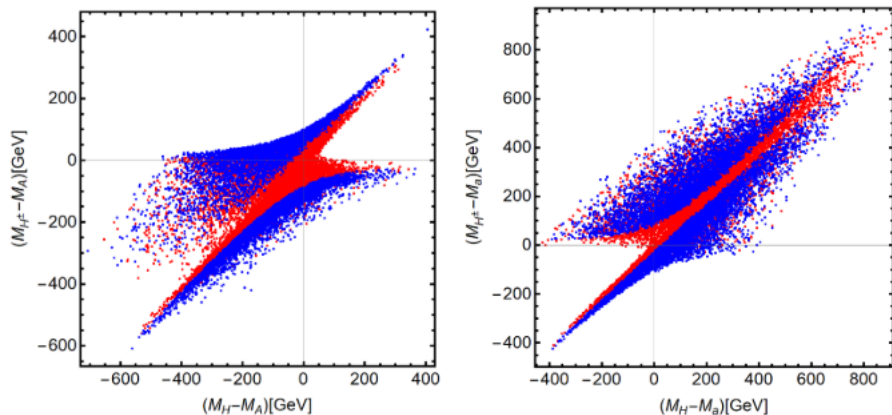
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05

THEORY+EWPT+FLAVOUR+ALIGNMENT

New CDF II measurement?



SM FIT
CDF II

2212.14788



05

THEORY+EWPT+FLAVOUR+ALIGNMENT

Mass splitting: $M_A - M_a$

There is no hard limit, but will be limited by EWPT

$$\sin 2\theta = \frac{2\mu v}{M_A^2 - M_a^2}$$

As this relation holds, having a large $M_A^2 - M_a^2$ without a small mixing angle pushed the new coupling μ to large values




μ becomes a “new physics scale”



05

THEORY+EWPT+FLAVOUR+ALIGNMENT

Masses: how large/small can they be?

- 2HDM has decoupling limit, no hard upper limit
- 
- Upper limit driven by other considerations, like ggF production cross sections
 - Lower limit on M_a driven by invisible higgs:
 - $M_a > \frac{M_h}{2}$ from 2-body decay $h \rightarrow aa$
 - $M_a \gtrsim 75\text{GeV}$ from 3 body decay $h \rightarrow aa^*$



06 (IN)DIRECT DETECTION

Direct Detection

- Very sensitive to y_χ, m_χ  Complementary to collider

- 2HDM+S: has SI cross section at tree level



Evading constraints usually requires:

- A fine-tunes cancellation of couplings and/or
- A fine-tuned cancellation of diagrams and/or
- Small DM yukawa y_χ and/or
- A light DM mass

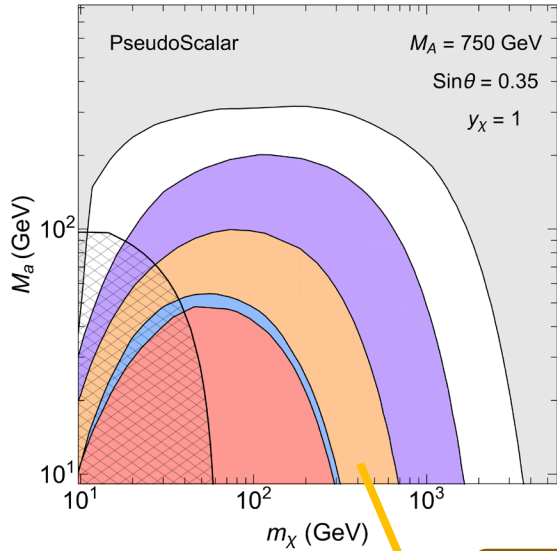
- 2HDM+a: has a q^4 suppressed SD cross section at tree level
- Dominant DD contribution is loop level SI cross section
- Couplings $\lambda_{P1}, \lambda_{P2}$ substantially enhance σ at small $\sin\theta$
- σ becomes smaller for small values of $\lambda_{P1}, \lambda_{P2}, \sin\theta$, or small y_χ or $m_\chi \ll M_a$ or $m_\chi \gg M_a$



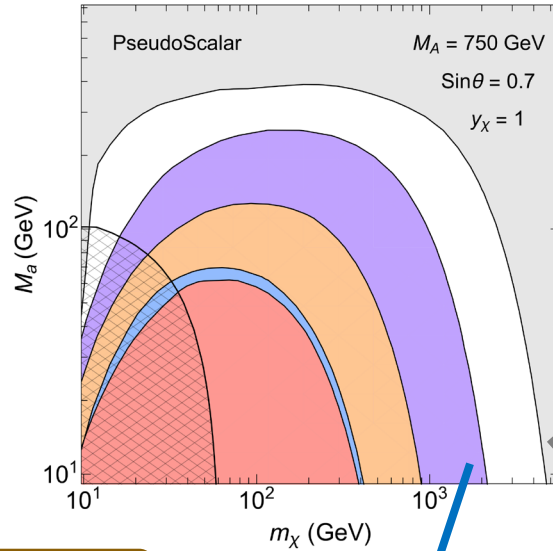
06

(IN)DIRECT DETECTION

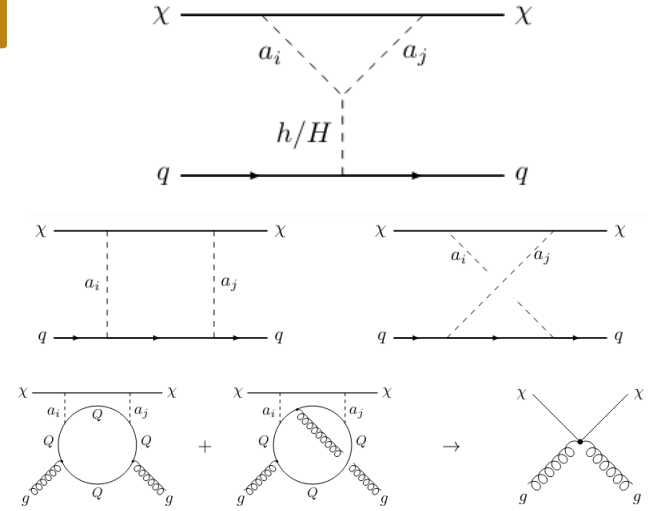
Direct Detection



1803.01574
XENON1T 2ty



1810.01039
XENONnT 20ty



Improved expressions
1810.01039

Neutrino Floor



06 (IN)DIRECT DETECTION

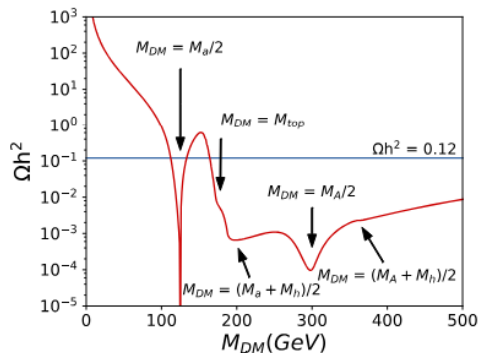
Indirect Detection

- Very sensitive to y_χ, m_χ \rightarrow Complementary to collider
- 2HDM+S: has p-wave suppressed annihilations
 \downarrow
- Annihilations for ID are highly suppressed
- Still possible to reproduce relic density if annihilation to boson is allowed 1710.10764
- Annihilation cross section can become very large once $t\bar{t}$ or scalar/vector boson annihilation channels open up \rightarrow
- 2HDM+a: has s wave annihilations
 \downarrow
- Annihilation cross section can become very large once $t\bar{t}$ or scalar/vector boson annihilation channels open up
 \downarrow
- Evading ID constraints easy if y_χ, m_χ are small enough, but
- Achieving the right relic density usually requires either fine-tuning m_χ or choosing very large/small values or y_χ

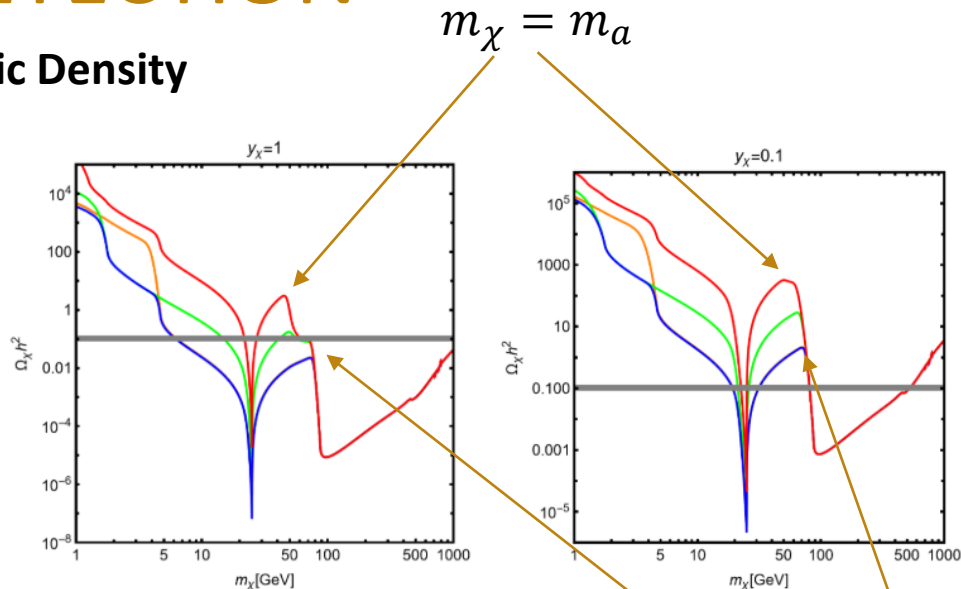


06 (IN)DIRECT DETECTION

ID/Relic Density



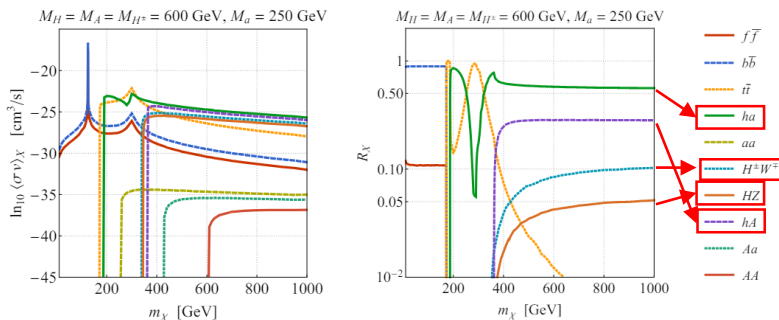
1810.09420



$m_\chi = m_a$

2212.14788 $m_\chi = (m_a + m_h)/2$

$\tan\beta = 5, \cos(\alpha - \beta) = 0, \theta = \pi/4$
 $m_a = 50\text{GeV}, M_{H,A,H^\pm} = 800\text{GeV}$



07 COLLIDER SIGNATURES

New possible Decays/couplings

Drop degenerate mass assumption

- $A \rightarrow Ha$
- $A \rightarrow HZ$
- $H \rightarrow Aa$
- $H \rightarrow AZ$
- $H \rightarrow AA$
- $A \rightarrow H^\pm W^\mp$
- $H \rightarrow H^\pm W^\mp$
- $H \rightarrow H^\pm H^\mp$
- $H^\pm \rightarrow HW^\pm$
- $H^\pm \rightarrow AW^\pm$

Drop alignment assumption

- $H \rightarrow W^\pm W^\mp$
- $H \rightarrow ZZ$
- $H^\pm \rightarrow hW^\pm$
- $A \rightarrow hZ$
- $a \rightarrow hZ$
- $H \rightarrow hh$
- $H \rightarrow hW^+W^-$
- $H \rightarrow hZZ$



07

COLLIDER SIGNATURES

Signature	Run 2	No degen. mass	No alignment
$h + E_T$	✓	+	
$Z + E_T$	✓	+	
$tW^- + E_T$	✓		
$t\bar{t} + E_T$	✓	+	?
$b\bar{b} + E_T$	✓	+	
$j + E_T$	✓	+	
$b\bar{b}Z$	✗	✓	
$ZZ + E_T$	✗	✓	
$hh + E_T$	✗	✓	

2404.05704



07 COLLIDER SIGNATURES

A few collider anomalies...

2309.03870

Final state	Characteristics	SM backgrounds	Significance
$\ell^+\ell^-(b\text{-jets})$ ^{243, 246, 247}	$m_{\ell\ell} < 100 \text{ GeV}$	$t\bar{t}, Wt$	$> 5\sigma$
$\ell^+\ell^-(\text{no jet})$ ^{242, 248}	$m_{\ell\ell} < 100 \text{ GeV}$	W^+W^-	$\approx 3\sigma$
$\ell^\pm\ell^\pm, 3\ell + (b\text{-jets})$ ^{245, 249, 250}	Moderate H_T	$t\bar{t}W^\pm, t\bar{t}t\bar{t}$	$\approx 3\sigma$
$\ell^\pm\ell^\pm, 3\ell, (\text{no } b\text{-jet})$ ^{244, 251, 252}	In association with h	$W^\pm h(125), WWW$	$\gtrsim 4\sigma$
$Z(\rightarrow \ell\ell)\ell, (\text{no } b\text{-jet})$ ^{243, 253}	$p_T^Z < 100 \text{ GeV}$	ZW^\pm	$> 3\sigma$

Suggesting

$$gg \rightarrow t\bar{t}\phi_1, \phi_1 \rightarrow \phi_2\phi_3, \phi_2 \rightarrow WW, \phi_3 \rightarrow b\bar{b}$$

ϕ_2 needs to be a scalar to have WW coupling and $m_2 \sim 150 \text{ GeV}$

WW coupling requires non-alignment in 2HDM and usually implies mixing also in a generic scalar sector

2HDM+a interpretation: $\phi_1 = A, \phi_2 = H, \phi_3 = a$ (requires non-alignment!)

However, no ZZ signal is observed \rightarrow prefers models without $ZZ\phi_2$ coupling




07

COLLIDER SIGNATURES

A few collider anomalies...

2309.03870

- Hints of $\gamma\gamma$ at 95GeV , 152GeV , 680GeV
- $\gamma\gamma$ at 95GeV supported by $\tau\tau$ and $b\bar{b}$ (LEP)  Many papers!
- $\gamma\gamma, ZZ$ hints at 680GeV
- $b\bar{b}\gamma\gamma$ hint at 680GeV , with $\gamma\gamma$ compatible with 95GeV

All pointing towards extended scalar sector!



07 COLLIDER SIGNATURES

Some thoughts/questions for discussion time:

- Consider signatures coming from non-alignment?
- $WW, ZZ, VV + X$ signatures? VBF?
- Other Yukawa types? Non-alignment prefers Type I
- Going down to $m_a \sim 95 \text{ GeV}$ or even $m_a \sim 80 \text{ GeV}$?
- Lower and upper limits for M_A ?
- What if $2m_\chi > m_a$? All $+E_T$ signatures would turn into $+b\bar{b}$
- Origin and workaround of large Γ problem?
- Higher order corrections available for scalars, not pseudoscalars!



THANK YOU



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