ROADMAP OF DARK MATTER MODELS FOR RUN3 CERN WORKSHOP, 13-17 MAY 2024



Cosmological perspectives and constraints on t-channel models

CHIARA ARINA, 16/05/2024





CP3, UCLOUVAIN

Cosmology of t-channel models

- The work presented here is based on several contributions
 - T-channel white paper (cosmo section effort), together with M. Becker, E. Copello, M. Garny, J. Harz, J. Heisig, A. Ibarra, S. Khalil, M. Kirtiman, Y. Koay, L. Lopez Honorez, T. Murphy, L. Panizzi, D. Sengupta and S. Tentori
 - CA, B. Fuks, J. Heisig, M. Kraemer, L. Mantani, L. Panizzi, Phys. Rev. D 108 (2023) [arXiv:2307.10367 [hep-ph]]
 - CA, B. Fuks, L. Mantani, H. Meis, L. Panizzi, J. Salko, Phys. Lett. B 813 (2021) [arXiv:2010.136038 [hep-ph]]
 - CA, B. Fuks, L. Mantani, Eur. Phys J. C 80 (2020) [arXiv:2001.05024 [hepph]]

Cosmology of t-channel models

- Brief overview of the minimal simplified t-channel models
- Early universe physics and constraints on such models
- Today's probes from astroparticle and dark matter experiments
- Complementarity with collider searches for few selected benchmarks

HERE CONSIDERED ONLY COLORED MEDIATORS COUPLING TO QUARKS

UNDERLINE THE DIFFERENCES WHEN RELEVANT THAT DEPEND ON THE QUARK GENERATION

HOWEVER T-CHANNEL CAN APPEAR UNDER MANY FORMS (SEE TALKS THIS MORNING) AND CAN BE LEPTOPHILIC AS WELL





- Y is charged under the dark symmetry
- Y decays into 1 DM and 1 SM particle
- Y can be coloured if it couples to quarks as well as gluons
- X is a SM gauge singlet
- The model can be leptophilic

 $\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{kin} + \mathcal{L}_F(\chi) + \mathcal{L}_F(\tilde{\chi}) + \mathcal{L}_S(S) + \mathcal{L}_S(\tilde{S}) + \mathcal{L}_V(V) + \mathcal{L}_V(\tilde{V})$

VERY GENERIC MODEL WITH 6 DARK MATTER CANDIDATES AND 24 MEDIATORS OF DIFFERENT SPIN



$$\mathcal{L}_{F}(X) = \begin{bmatrix} \lambda_{\mathbf{Q}} \bar{X} Q \varphi_{Q}^{\dagger} + \lambda_{\mathbf{u}} \bar{X} u \varphi_{u}^{\dagger} + \lambda_{\mathbf{d}} \bar{X} d \varphi_{d}^{\dagger} + \text{h.c.} \end{bmatrix}$$
$$\mathcal{L}_{S}(X) = \begin{bmatrix} \hat{\lambda}_{\mathbf{Q}} \bar{\psi}_{Q} Q X + \hat{\lambda}_{\mathbf{u}} \bar{\psi}_{u} u X + \hat{\lambda}_{\mathbf{d}} \bar{\psi}_{d} d X + \text{h.c.} \end{bmatrix}$$
$$\mathcal{L}_{V}(X) = \begin{bmatrix} \hat{\lambda}_{\mathbf{Q}} \bar{\psi}_{Q} X Q + \hat{\lambda}_{\mathbf{u}} \bar{\psi}_{u} X u + \hat{\lambda}_{\mathbf{d}} \bar{\psi}_{d} X d + \text{h.c.} \end{bmatrix}$$

UNIQUE IMPLEMENTATION FOR COLLIDER AND DM STUDIES

MODEL FILES AND DOCUMENTATION ARE AVAILABLE HERE: <u>HTTP://FEYNRULES.IRMP.UCL.AC.BE/WIKI/DMSIMPT</u>

 $\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{kin} + \mathcal{L}_F(\chi) + \mathcal{L}_F(\tilde{\chi}) + \mathcal{L}_S(S) + \mathcal{L}_S(\tilde{S}) + \mathcal{L}_V(V) + \mathcal{L}_V(\tilde{V})$

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$$\mathcal{L}_{F}(X) = \begin{bmatrix} \lambda_{\mathbf{Q}} \bar{X} Q \varphi_{Q}^{\dagger} + \lambda_{\mathbf{u}} \bar{X} u \varphi_{u}^{\dagger} + \lambda_{\mathbf{d}} \bar{X} d \varphi_{d}^{\dagger} + \text{h.c.} \end{bmatrix}$$
$$\mathcal{L}_{S}(X) = \begin{bmatrix} \hat{\lambda}_{\mathbf{Q}} \bar{\psi}_{Q} Q X + \hat{\lambda}_{\mathbf{u}} \bar{\psi}_{u} u X + \hat{\lambda}_{\mathbf{d}} \bar{\psi}_{d} d X + \text{h.c.} \end{bmatrix}$$
$$\mathcal{L}_{V}(X) = \begin{bmatrix} \hat{\lambda}_{\mathbf{Q}} \bar{\psi}_{Q} X Q + \hat{\lambda}_{\mathbf{u}} \bar{\psi}_{u} X u + \hat{\lambda}_{\mathbf{d}} \bar{\psi}_{d} X d + \text{h.c.} \end{bmatrix}$$

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VERY GENERIC MODEL WITH 6 DARK MATTER CANDIDATES AND 24 MEDIATORS OF DIFFERENT SPIN



$$\mathcal{L}_{F}(X) = \begin{bmatrix} \lambda_{\mathbf{Q}} \bar{X} Q \varphi_{Q}^{\dagger} + \lambda_{\mathbf{u}} \bar{X} u \varphi_{u}^{\dagger} + \lambda_{\mathbf{d}} \bar{X} d \varphi_{d}^{\dagger} + \text{h.c.} \end{bmatrix}$$
$$\mathcal{L}_{S}(X) = \begin{bmatrix} \hat{\lambda}_{\mathbf{Q}} \bar{\psi}_{Q} Q X + \hat{\lambda}_{\mathbf{u}} \bar{\psi}_{u} u X + \hat{\lambda}_{\mathbf{d}} \bar{\psi}_{d} d X + \text{h.c.} \end{bmatrix}$$
$$\mathcal{L}_{V}(X) = \begin{bmatrix} \hat{\lambda}_{\mathbf{Q}} \bar{\psi}_{Q} X Q + \hat{\lambda}_{\mathbf{u}} \bar{\psi}_{u} X u + \hat{\lambda}_{\mathbf{d}} \bar{\psi}_{d} X d + \text{h.c.} \end{bmatrix}$$

New couplings 3x3 matrices in flavour space real and flavour diagonal

UNIQUE IMPLEMENTATION FOR COLLIDER AND DM STUDIES

MODEL FILES AND DOCUMENTATION ARE AVAILABLE HERE: HTTP://FEYNRULES.IRMP.UCL.AC.BE/WIKI/DMSIMPT

Name	DM	Mediators	Parameters
S3M_uni	$ ilde{\chi}$		
S3D_uni	X	$arphi Q_f, arphi u_f, arphi d_f$	$M_{arphi},M_{\chi},\lambda_{arphi}$
S3M_3rd	$ ilde{\chi}$		
S3D_3rd	<u>X</u>	$arphi Q_3, arphi u_3, arphi d_3 = $	
S3M_uR	$ ilde{\chi}$	(0)	
S3D_uR	χ	$arphi u_1$	
F3S_uni	$ ilde{S}$	a/a a/a a/a	
F3C_uni	$_S$	$\psi Q_f, \ \psi u_f, \ \psi a_f$	$M_{\pi} = M_{\pi} = \hat{\lambda}$
F3S_3rd	\tilde{S}	$a_{12} = a_{12} = a_{12} = a_{12} = a_{12}$	
F3C_3rd	S	$\psi_{Q_3}, \psi_{u_3}, \psi_{d_3}$	$\chi_{1}S, \chi_{\psi}, \chi_{\psi}$
F3S_uR	\tilde{S}		
F3C_uR	S	$arphi u_1$	
F3V_uni	$ ilde{V}_{\mu}$	$a _{\lambda}$ $a _{\lambda}$ $a _{\lambda}$	- $M_V, M_\psi, \hat{\lambda}_\psi$ -
F3W_uni	V_{μ}	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$	
F3V_3rd	\tilde{V}_{μ}	$a_{12} = a_{12} = a_{12} = a_{12} = a_{12}$	
F3W_3rd	V_{μ}	$\psi_{Q_3}, \psi_{u_3}, \psi_{d_3}$	
F3V_uR	\tilde{V}_{μ}		
F3W_uR	V_{μ}	$arphi u_1$	

THE GENERIC MODEL HAS SEVERAL RESTRICTIONS WHERE THE UNDESIRED FIELDS ARE DECOUPLED AND INTERACTIONS ARE SET TO ZERO

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Name	DM	Mediators	Parameters	THE GENERIC MODEL HAS SEVERAL	
S3M_uni	$ ilde{\chi}$	$(0, 0, \dots, 0)$	$M_{\varphi}, M_{\chi}, \lambda_{\varphi}$	RESTRICTIONS WHERE THE UNDESIRED FIELDS ARE DECOUPLED AND INTERACTIONS ARE SET TO ZERO	
	<u>x</u>	$\varphi \otimes_f, \varphi u_f, \varphi u_f$			
S3M_3rd	$ ilde{\chi}$				
	<u>x</u>	$arphi Q_3, arphi u_3, arphi d_3$		Any restriction has 3 free model parameters: DM and mediator masses + coupling (M_X, M_Y, λ)	
S3M_uR	$ ilde{\chi}$	(0			
S3D_uR	χ	$arphi u_1$			
F3S_uni	$ ilde{S}$		$M_S, M_{\psi}, \hat{\lambda}_{\psi}$		
F3C_uni	S	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$			
F3S_3rd	\tilde{S}				
F3C_3rd	S	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$			
F3S_uR	\tilde{S}	ψ_{u_1}			
F3C_uR	S				
F3V_uni	$ ilde{V}_{\mu}$	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$	$M_V,M_\psi,\hat\lambda_\psi$		
F3W_uni	V_{μ}				
F3V_3rd	\tilde{V}_{μ}	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$			
F3W_3rd	V_{μ}				
F3V_uR	\tilde{V}_{μ}	ψ_{u_1}	-	6	
F3W_uR	V_{μ}				

Name	DM	Mediators	Parameters	THE GENERIC MODEL HAS SEVERAL
S3M_uni	$ ilde{\chi}$	(0.0		RESTRICTIONS WHERE THE UNDESIRED
S3D_uni	_χ		_	FIELDS ARE DECOUPLED AND INTERACTIONS ARE SET TO ZERO
S3M_3rd	$\tilde{\chi}$		$M_{\varphi}, M_{\chi}, \lambda_{\varphi}$	
	<u>X</u>	$arphi_{Q_3},arphi_{u_3},arphi_{d_3}$		
S3M_uR	$ ilde{\chi}$	(0		
S3D_uR	χ	φu_1		
F3S_uni	$ ilde{S}$	$\frac{1}{2}$		
F3C_uni	$_S$	$\varphi Q_f, \varphi u_f, \varphi u_f$	$M_S, M_{\psi}, \hat{\lambda}_{\psi}$	Any restriction has 3 free model parameters:
F3S_3rd	$ ilde{S}$	a_{12} a_{12} a_{12} a_{12}		
F3C_3rd	S	$\varphi_{Q_3}, \varphi_{u_3}, \varphi_{u_3}$		DM and mediator masses + coupling
F3S_uR	$ ilde{S}$	ψ_{u_1}		(M_{X},M_{Y},λ)
F3C_uR	S			
F3V_uni	$ ilde{V}_{\mu}$	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$		
F3W_uni	V_{μ}		\hat{M}_{f} \hat{M}_{3} $M_{V}, M_{\psi}, \hat{\lambda}_{\psi}$	
F3V_3rd	$ ilde{V}_{\mu}$	$\psi_{Q_3}, \psi_{u_3}, \psi_{d_3}$		
F3W_3rd	V_{μ}			
F3V_uR -	$- ilde{V}_{\mu}$	ψ_{u_1}		coupling only to quark up-right
F3W_uR	V_{μ}			

Name	DM	Mediators	Parameters	THE GENEDIC MODEL HAS SEVEDAL
S3M_uni	$ ilde{\chi}$		- $M_{\varphi}, M_{\chi}, \lambda_{\varphi}$ -	RESTRICTIONS WHERE THE UNDESIRED FIELDS ARE DECOUPLED AND INTERACTIONS ARE SET TO ZERO
S3D_uni	χ	$\varphi_{Q_f}, \varphi_{u_f}, \varphi_{a_f}$		
S3M_3rd	$ ilde{\chi}$	(0,0) $(0,1)$ $(0,1)$		
	<u>X</u>	$\varphi_{Q_3}, \varphi_{u_3}, \varphi_{a_3}$		
S3M_uR	$ ilde{\chi}$	(0		
S3D_uR	χ	$arphi u_1$		
F3S_uni	$ ilde{S}$	a/a = a/a = a/a		
F3C_uni	$_S$	$\varphi Q_f, \varphi u_f, \varphi a_f$	$M_S, M_{\psi}, \hat{\lambda}_{\psi}$	Any restriction has 3 free model parameters: DM and mediator masses + coupling (M_X, M_Y, λ)
F3S_3rd	$ ilde{S}$	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$		
F3C_3rd	$_S$			
F3S_uR	$ ilde{S}$	ψ_{u_1}		
F3C_uR	S			
F3V_uni	$ ilde{V}_{\mu}$	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$	$M_V,M_\psi,\hat\lambda_\psi$	
F3W_uni	V_{μ}			
F3V_3rd	$ ilde{V_{\mu}}$	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$		coupling only to b and t quarks
F3W_3rd	V_{μ}			
F3V_uR	$ ilde{V}_{\mu}$	ψ_{u_1}		coupling only to quark up-right
F3W_uR	V_{μ}			

Name	DM	Mediators	Parameters	THE GENERIC MODEL HAS SEVERAL
S3M_uni	$ ilde{\chi}$			RESTRICTIONS WHERE THE UNDESIRED FIELDS ARE DECOUPLED AND INTERACTIONS ARE SET TO ZERO
	X	$\varphi_{Q_f}, \varphi_{u_f}, \varphi_{d_f}$	_	
S3M_3rd	$ ilde{\chi}$	$arphi_{Q_3},arphi_{u_3},arphi_{d_3}$	$M_{\varphi}, M_{\chi}, \lambda_{\varphi}$	
S3D_3rd	X			
S3M_uR	$ ilde{\chi}$	(0		
S3D_uR	χ	$arphi u_1$		
F3S_uni	$ ilde{S}$			
F3C_uni	S	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$	$M_S, M_{\psi}, \hat{\lambda}_{\psi}$	Any restriction has 3 free model parameters: DM and mediator masses + coupling (M_X, M_Y, λ)
F3S_3rd	\tilde{S}	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$		
F3C_3rd	S			
F3S_uR	\tilde{S}	ψ_{u_1}		
F3C_uR	S			
F3Vuni	$ ilde V_{\mu}$	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$		coupling to all guarks
F3W_uni	V_{μ}		$M_V, M_\psi, \hat{\lambda}_\psi$	
F3V_3rd_	\tilde{V}_{μ}	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$		coupling only to b and t quarks
F3W_3rd	V_{μ}			
F3V_uR –	\tilde{V}_{μ}	ψ_{u_1}	-	coupling only to quark up-right
F3W_uR	V_{μ}			



Early universe: freeze-out



LARGE COUPLING = WIMP DETECTABLE SIGNATURES IN DIRECT, INDIRECT SEARCH EXPERIMENT FOR DARK MATTER AND AT COLLIDERS

TYPICALLY LO PROCESSES ARE DOMINANT



- Sommerfeld enhancement and bounds state formation can be relevant when mediators are light (YY —> qq, YY —> gg)
- For d-wave suppressed annihilation cross-sections NLO corrections are relevant
- Pheno is the basically the same for all quark flavours (threshold effects for heavy quarks)







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Annihilation XX, YX, YY —> AB becomes inefficient
Conversions such as Y -> XA, YA -> XB (A,B=SM) lead the freeze-out process

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Much more in J. Heisig talk





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Annihilation XX, YX, YY —> AB becomes inefficient
Conversions such as Y -> XA, YA -> XB (A,B=SM) lead the freeze-out process

SMALL COUPLINGS

- CHALLENGING TO SEE IN DARK MATTER
 SEARCHES
- PROVIDE LLP SIGNALS AT LHC
- CAN HAVE VERY COMPRESSED SPECTRUM • CONSTRAINTS FROM EARLY UNIVERSE (E.G. LYMAN- α , CMB, BBN)

Much more in J. Heisig talk

Direct detection of WIMPs



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Direct detection of WIMPs

SPIN-INDEPENDENT INTERACTION: DARK MATTER COUPLES TO ALL NUCLEONS (SENSITIVE TO A²)



DIRECT DETECTION SENSITIVE UP TO TENS OF TEV IN DARK MATTER MASS ($\propto m_X^{-2}$)

Direct detection of WIMPs



UFO AT LO AND NLO CAN BE USED DIRECTLY INTO DARK MATTER TOOLS







Dark matter annihilation in galactic halos at present time

LO ANNIHILATION (DIRAC AND VECTORIAL DARK MATTER)

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BOUNDS FROM FERMI-LAT DWARF SPHEROIDAL GALAXIES GA BE COMPUTED AUTOMATICALLY WITHIN MADDM

Dark matter annihilation in galactic halos at present time

 LO ANNIHILATION IS P-WAVE OR D-WAVE SUPPRESSED (MAJORANA OR SCALAR DARK MATTER)
 NLO PROCESSES UPLIFT THE SUPPRESSION AND PRODUCE A SHARP FEATURE IN THE GAMMA-RAY ENERGY SPECTRUM

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GAMMA LINE SEARCHES ARE THE MOST STRINGENT BOUNDS

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Benchmark 1: coupling to UR

=	Name	DM	Mediators	Parameters	We consider all models coupling to u _R quark = 6 in total
	S3M_uni	$ ilde{\chi}$			$(M_{\times}, M_{\times}, \lambda)$
	S3D_uni	χ	${arphi}_Q_f,{arphi}_u_f,{arphi}_d_f$		
-	 S3M_3rd	$\tilde{\chi}$			
	S3D_3rd	χ	$arphi_{Q_3},arphi_{u_3},arphi_{d_3}$	$M_{arphi}, M_{\chi}, \lambda_{arphi}$	Fermionic DM (Majorana
-	S3M_uR	$\tilde{\chi}$			and Dirac) and scalar
	S3D_uR	χ	$arphi u_1$		mediator
	F3S_uni	$ ilde{S}$		$M_S,M_\psi,\hat\lambda_\psi$	
	F3C_uni	S	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$		
-	F3S_3rd	\tilde{S}			
	F3C_3rd	S	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$		
	F3S_uR	$\tilde{\tilde{S}}$			Scalar DM (real and
	F3C_uR	S			complex) and fermionic
	F3V_uni	$ ilde{V}_{\mu}$	alı alı alı	- $M_V,M_\psi,\hat\lambda_\psi$	- mediator
	F3W_uni	V_{μ}	$\psi_{Q_f},\psi_{u_f},\psi_{d_f}$		
-	F3V_3rd	\tilde{V}_{μ}			
	F3W_3rd	V_{μ}	$\psi_{Q_3},\psi_{u_3},\psi_{d_3}$		Vector DM (real and
-	F3V_uR	\tilde{V}_{μ}			complex) and fermionic 16
	F3W_uR	V_{μ}	ψu_1		mediator

Benchmark 1: coupling to u_R complex case

Benchmark 1: coupling to u_R real case

ASSUMING WIMP SCENARIO AND CORRECT RELIC DENSITY VIA FO COSMOLOGY EXCLUDES A LOT BUT STILL VIABLE BENCHMARKS

FREEZE-IN REGION AND COMPRESSED SPECTRA TO BE INVESTIGATED STILL...

From arXiv:2307.10367

Benchmark 2: coupling to t_R

Benchmark 2: coupling to t_R for freeze-in and superWIMP

Majorana particle as X and scalar particle as Y (M_X, M_Y, λ)

- WIDE RANGE OF DM MASSES CAN BE CONSIDERED
- LOW MASSES ARE CONSTRAINED BY COSMOLOGY
- COMPRESSED SPECTRA CONSTRAINED BY DISPLACED VERTICES AND R-HADRONS
- NICE COMPLEMENTARITY
- WIDE VIABLE REGION (NO DD OR ID BOUND)

Summary

DARK MATTER CANDIDATES ARISING FROM SIMPLIFIED AND MINIMAL T-CHANNEL MODELS ARE PARTICULAR ATTRACTIVE BECAUSE OF THEIR PREDICTIVITY:

- IF CONSIDERED AS WIMPS THEY ARE PRETTY CONSTRAINED BY INDIRECT AND DIRECT SEARCHES OF DARK MATTER;
- MODELS COUPLING TO U AND D ARE MORE CONSTRAINED (COMPLEX CANDIDATES ARE BASICALLY EXCLUDED)
- MODELS COUPLING TO 2ND AND 3RD GEN ARE LESS CONSTRAINED BY DIRECT DETECTION
- PHENO OF RELIC AND INDIRECT DETECTION DO NOT STRONGLY DEPEND ON THE QUARK FLAVOR (BESIDES MASS EFFECTS)
- Models beyond the minimal version and/or theoretical complete models feature enlarged parameter space, specific signatures, ...;
- Freeze-in, superWIMP, conversion driven freeze-out are other mechanisms that shape LLP regions and/or very compressed spectra: different regions and masses to explore yet;
- A non-standard cosmological history can change the model parameter space and open up new regions;
- Much more in the white paper to appear, stay tuned!

Back up slides

Bound states and Sommerfeld enhancement (from arXiv:2203.04326)

SOMMERFELD ENHANCEMENT

$$\begin{split} \sigma_{\mathrm{SE},[\mathbf{R}]} v_{\mathrm{rel}} &= c_{[\mathbf{R}]} S_{0,[\mathbf{R}]} \, \sigma_{0}, \\ \sigma_{\mathbf{3} \otimes \bar{\mathbf{3}} \to gg} v_{\mathrm{rel}} &= \sigma_{\mathbf{3} \otimes \bar{\mathbf{3}} \to gg, 0} \left(\frac{2}{7} S_{0,[\mathbf{1}]} + \frac{5}{7} S_{0,[\mathbf{8}]} \right), \\ \sigma_{\mathbf{3} \otimes \bar{\mathbf{3}} \to q\bar{q}} v_{\mathrm{rel}} &= \sigma_{\mathbf{3} \otimes \bar{\mathbf{3}}, 0} \left(f_{[\mathbf{1}]}(g_{s}, g_{\mathrm{DM}}) S_{0,[\mathbf{1}]} + f_{[\mathbf{8}]}(g_{s}, g_{\mathrm{DM}}) S_{0,[\mathbf{8}]} \right), \\ \sigma_{\mathbf{3} \otimes \mathbf{3} \to qq} v_{\mathrm{rel}} &= \sigma_{\mathbf{3} \otimes \mathbf{3} \to qq, 0} S_{0,[\mathbf{6}]}, \\ \sigma_{\mathbf{3}_{i} \otimes \mathbf{3}_{j} \to q_{i}q_{j}} &= \sigma_{\mathbf{3}_{i} \otimes \mathbf{3}_{j} \to q_{i}q_{j}, 0} \left(\frac{1}{3} S_{0,[\bar{\mathbf{3}}]} + \frac{2}{3} S_{0,[\mathbf{6}]} \right). \end{split}$$

$$V(r)_{\mathbf{3}\otimes\bar{\mathbf{3}}} = \begin{cases} -\frac{4}{3}\frac{\alpha_s}{r} & [\mathbf{1}] \\ +\frac{1}{6}\frac{\alpha_s}{r} & [\mathbf{8}] \end{cases} ; \quad V(r)_{\mathbf{3}\otimes\mathbf{3}} = \begin{cases} -\frac{2}{3}\frac{\alpha_s}{r} & [\mathbf{\bar{3}}] \\ +\frac{1}{3}\frac{\alpha_s}{r} & [\mathbf{6}] \end{cases}$$

Lyman-alpha bounds

FI AND SW (NON-THERMAL) CAN BE PRODUCED WITH A CERTAIN BOOST AND AFFECT STRUCTURE FORMATION BOUNDS FROM WARM DARK MATTER (THERMAL) CAN BE TRANSLATED INTO FI AND SW TERMS

$$m_X \gtrsim \begin{cases} 15 \,\text{keV} \times \left(\frac{106.75}{g_*(T_{\text{FI}})}\right)^{1/3} & \text{for FI through decays,} \\ \\ 3.8 \,\text{GeV} \times \left(\frac{R_{\Gamma}^{\text{SW}}}{10^{-12}}\right)^{-1/2} \times \left(\frac{106.75}{g_*(T_{\text{SW}})}\right)^{1/3} & \text{for SW,} \end{cases}$$