

# Collectivity in $e^+e^-$ Collisions

**Yen-Jie Lee (MIT)**

The 4th International Workshop on QCD Collectivity at the Smallest Scales  
25 June, 2024

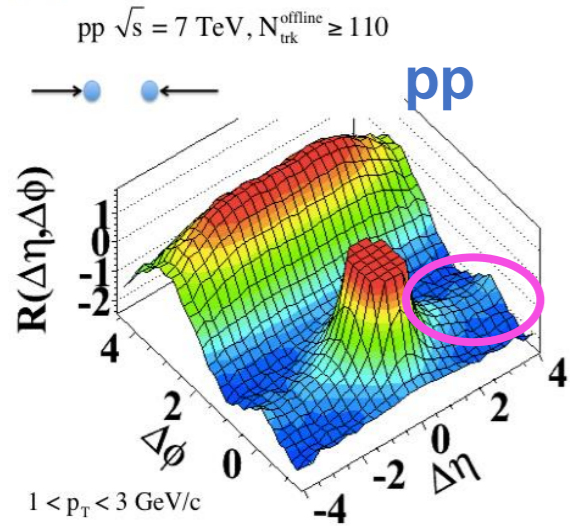
In Collaboration with Yu-Chen “Janice” Chen (MIT), Yi Chen (Vanderbilt U.), Anthony Badea (U. Chicago), Austin Baty (UIC), Gian Michele Innocenti (MIT), Marcello Maggi (INFN Bari), Christopher McGinn (MIT), Michael Peters (MIT), Tzu-An Sheng (MIT), Jesse Thaler (MIT)



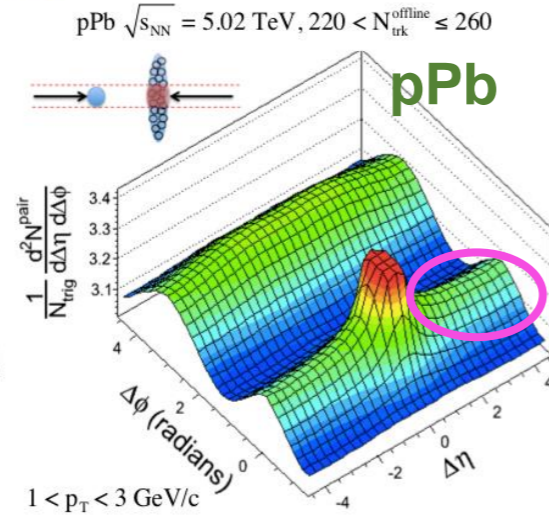
MIT HIG group's work was supported by US DOE-NP



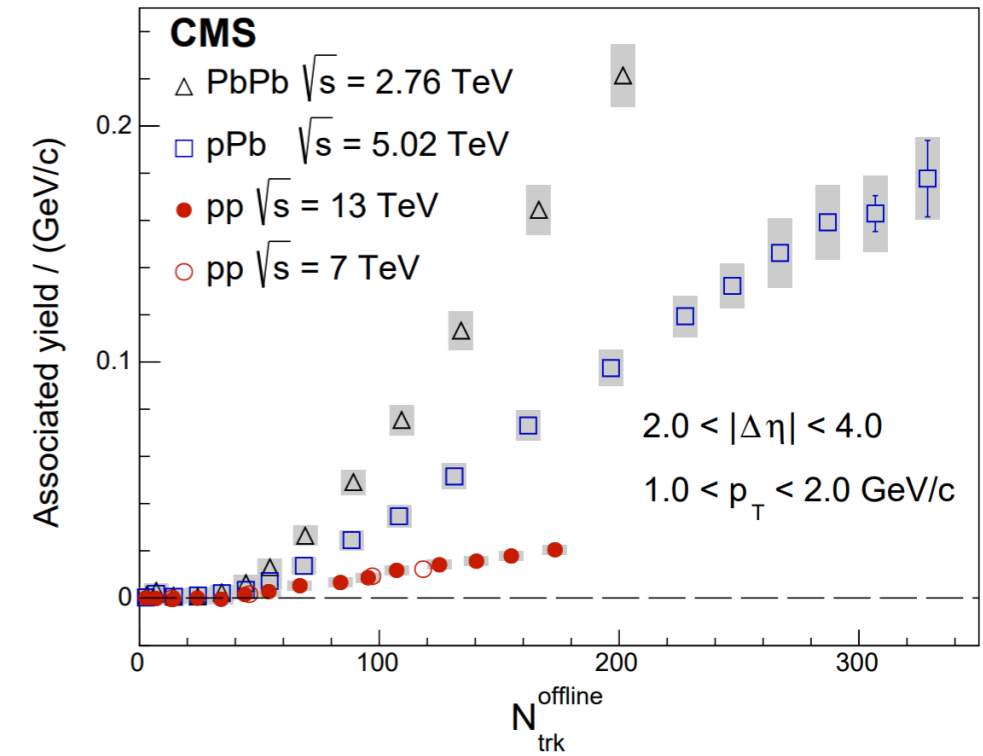
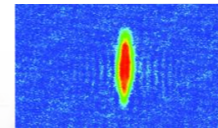
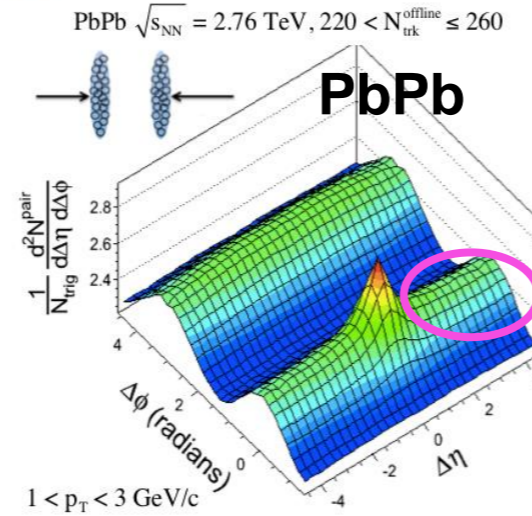
# Motivation



2010



2012



- The first unexpected discovery at LHC: **Ridge** in high multiplicity pp from CMS
- The origin may not necessary hydrodynamics, possible explanations includes:
  - Initial state effect (e.g. CGC)
  - Escape mechanism / Single or few scatterings (AMPT, PYTHIA with Rope Mechanism, Multi-parton rescattering...)
  - Final state effect due to mini-QGP
  - ...

CMS JHEP 09 (2010) 091  
 CMS pPb PLB 718 (2013) 795-814

# Physics Questions to be Addressed

- What are the minimum conditions for ridge signal in a small system?
- Can detectable collectivity arise from final state effects unrelated to the initial state?
- How does collectivity vary in different physics processes?
- Is the underlying physics the same in small and large systems?
- ...



# Physics Questions to be Addressed

- What are the minimum conditions for ridge signal in a small system?

Vary the transverse size and multiplicity of the collision system

- Can detectable collectivity arise from final state effects unrelated to the initial state?

Use electron beams that doesn't have initial hadron structure

- How does collectivity vary in different physics processes?

Select and study specific physics processes

- Is the underlying physics the same in small and large systems?

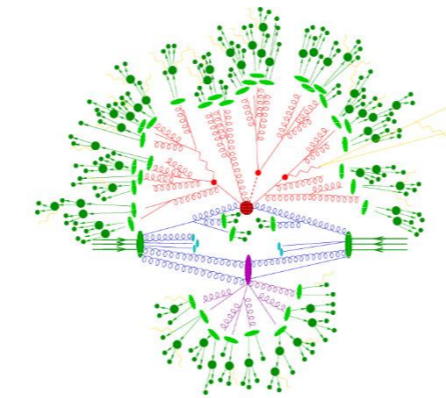
By collection of all the experimental data and compare

- ...

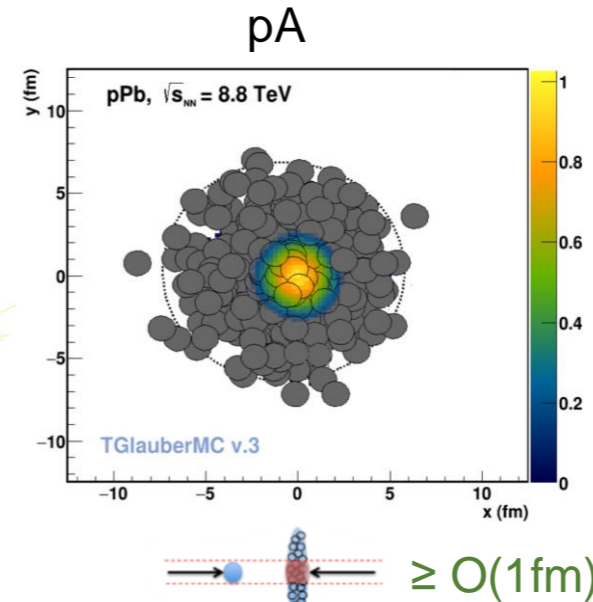


# System Size

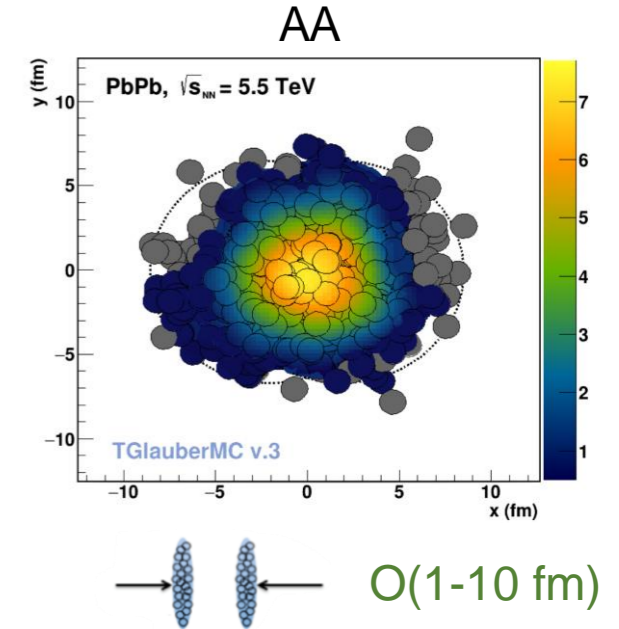
“Transverse Size” / MPI



$\sim O(1\text{fm})$



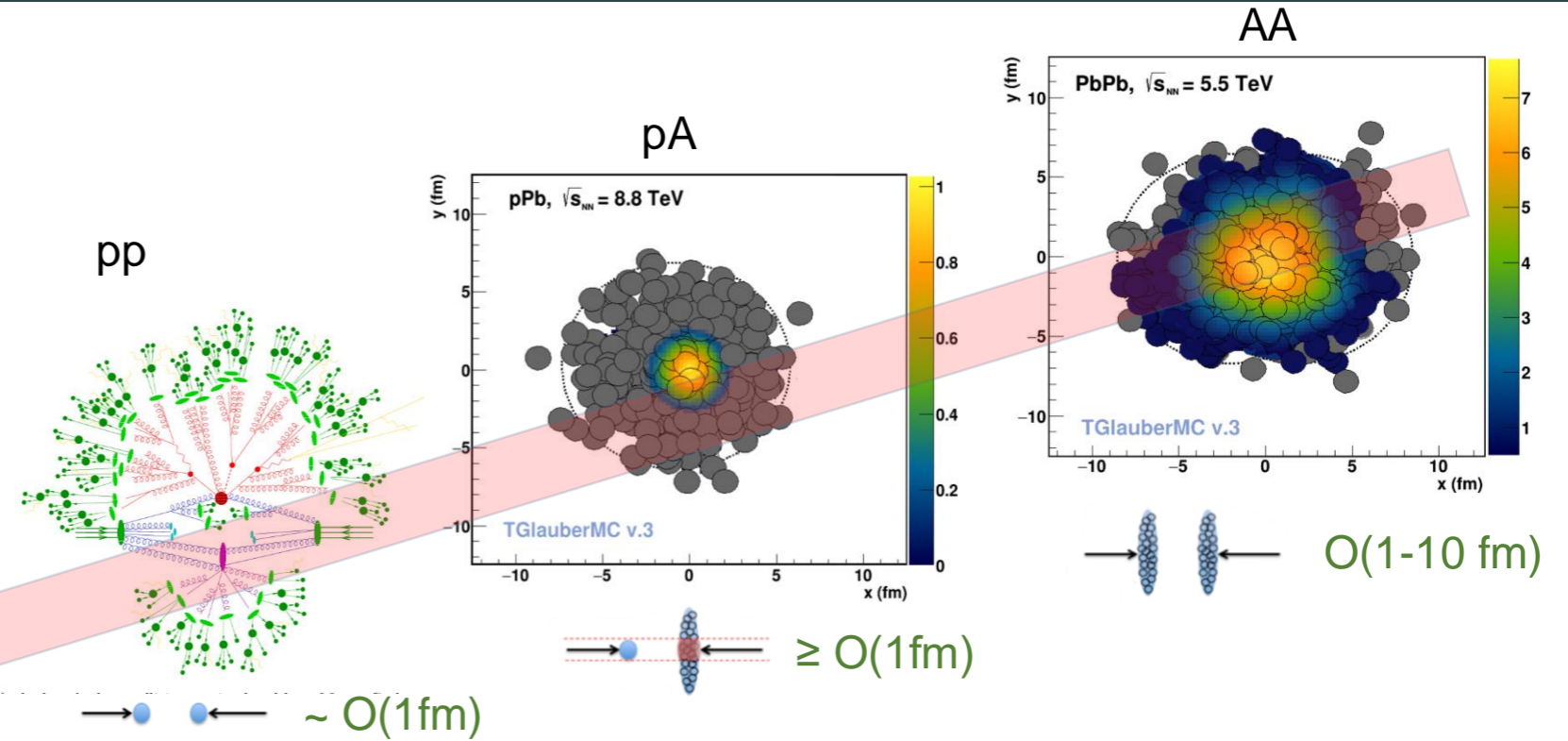
$\geq O(1\text{fm})$



Multiplicity

# System Size

“Transverse Size” / MPI

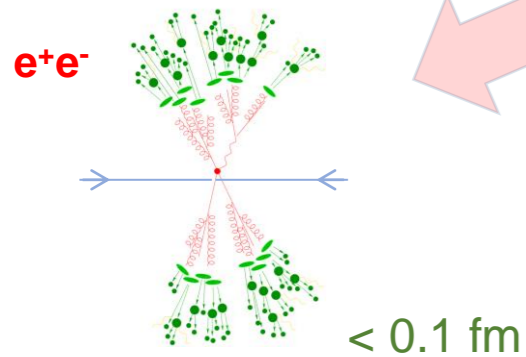


**In the small system limit**, it is crucial to emphasize the space and time dependence of parton shower development.

Multiplicity

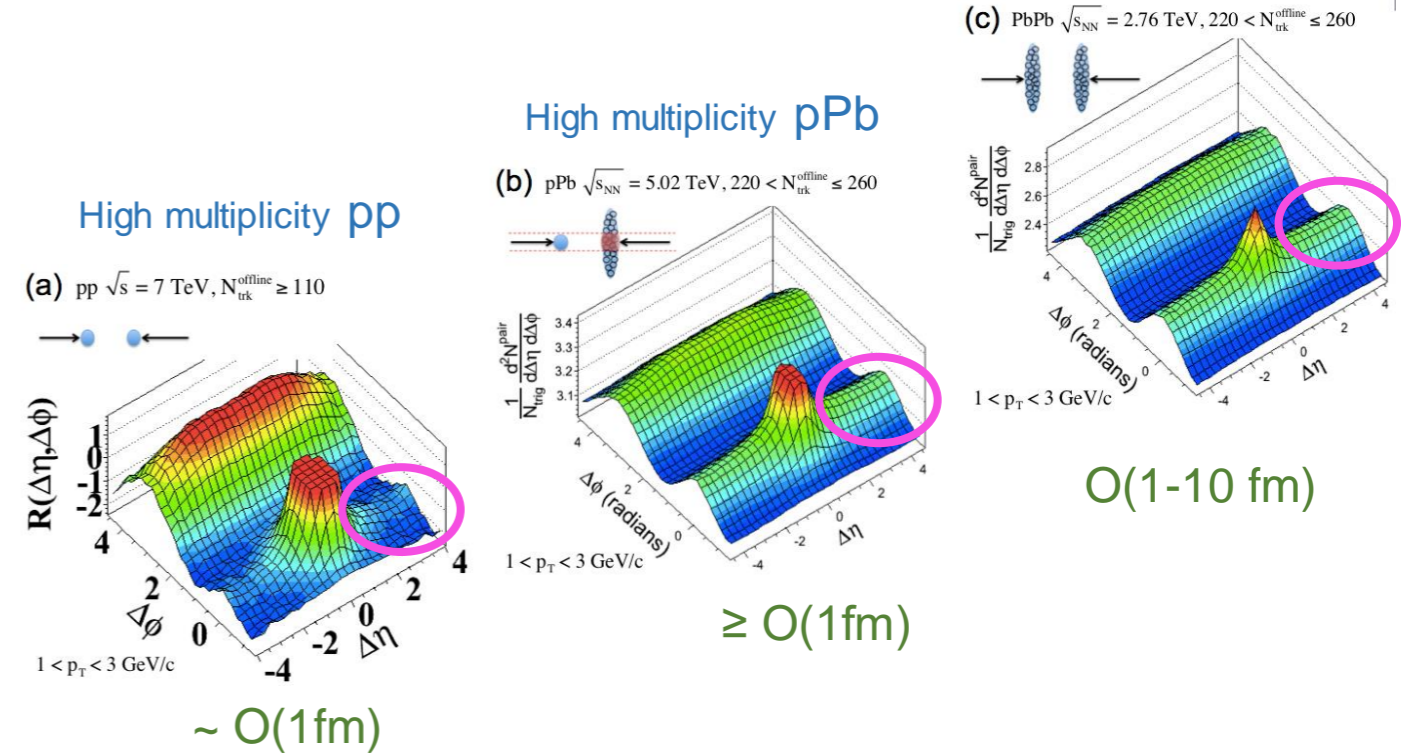
# Smallest System: $e^+e^-$

“Transverse Size” / MPI



•  $e^+e^-$  events: collisions with **well-defined initial conditions**

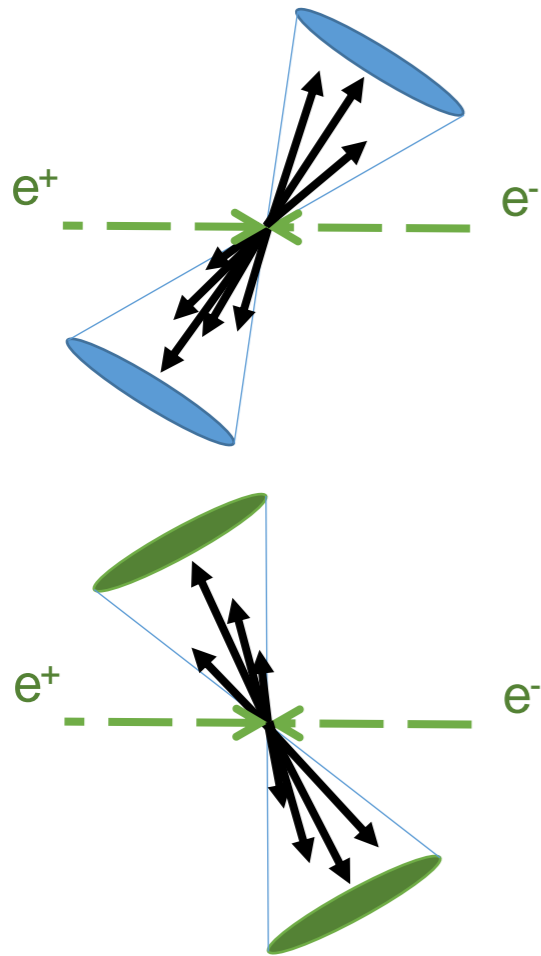
- No complication from hadron structure
- No multi-parton interaction
- No gluonic initial state radiation



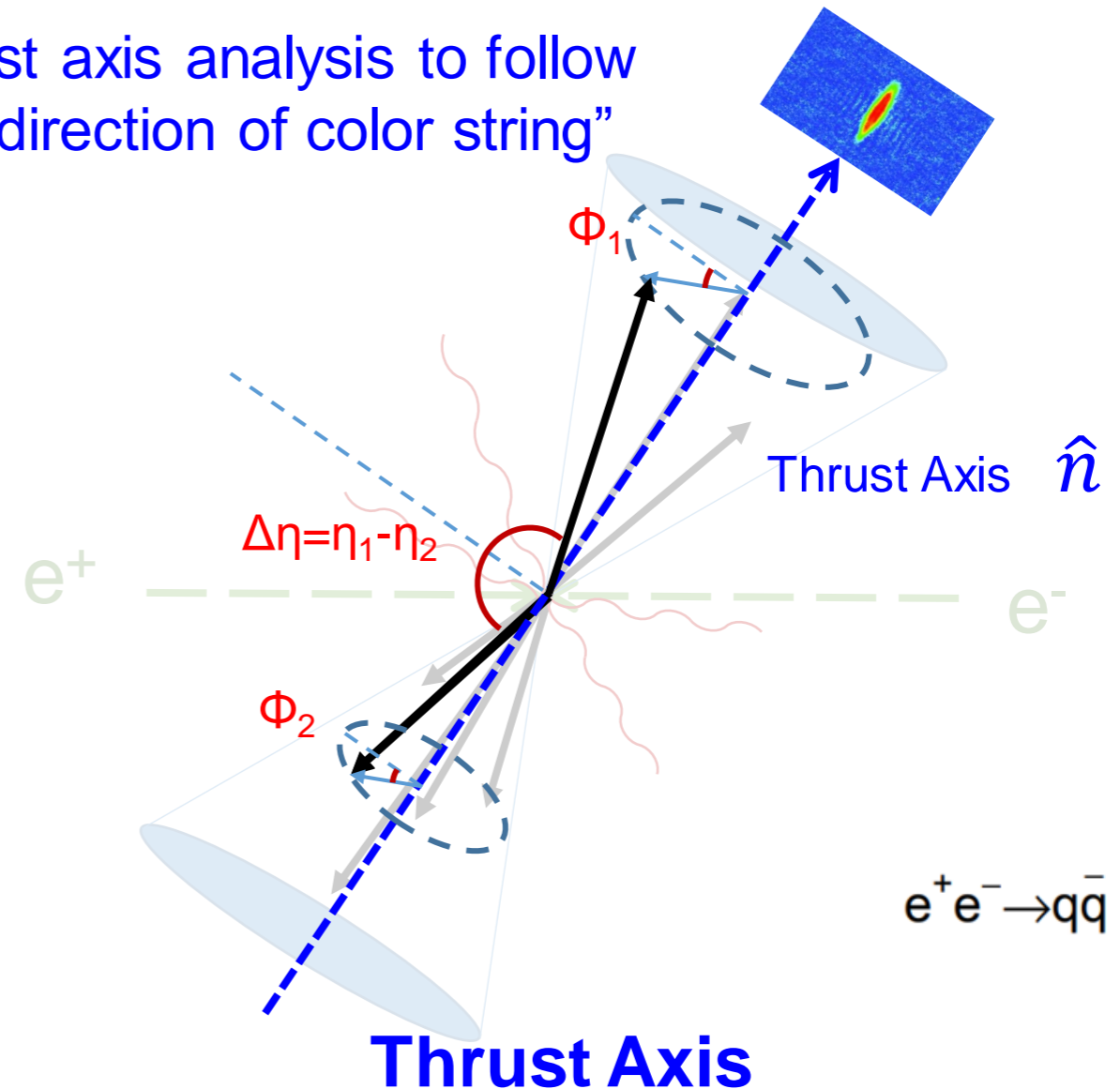
Multiplicity

# Reference Axis for $e^+e^-$

Random orientation of the jets



Thrust axis analysis to follow the “direction of color string”

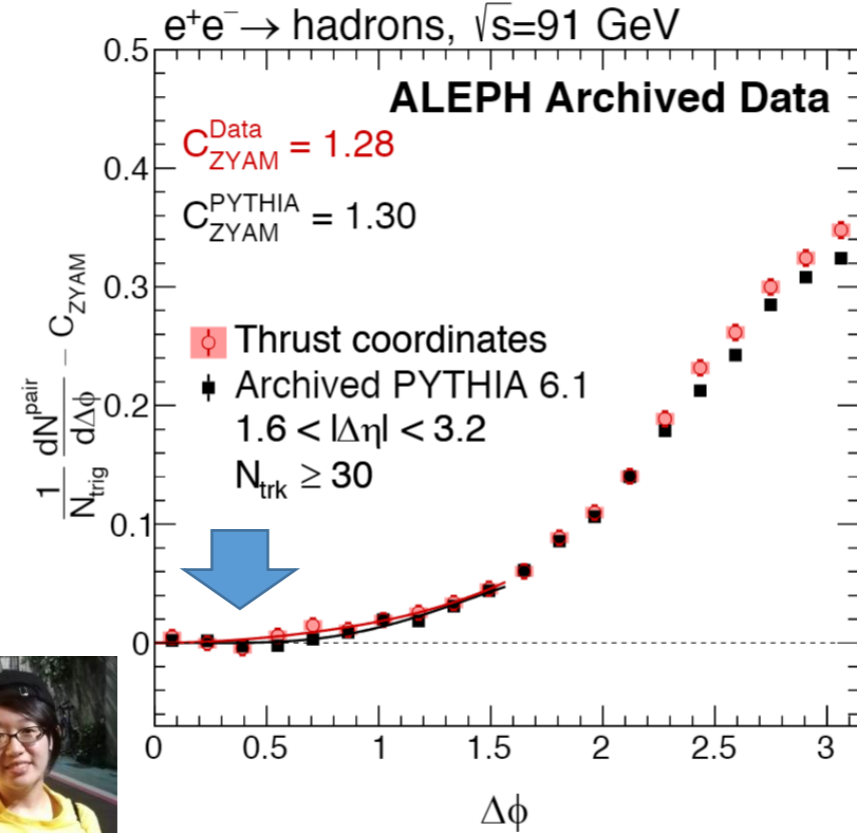
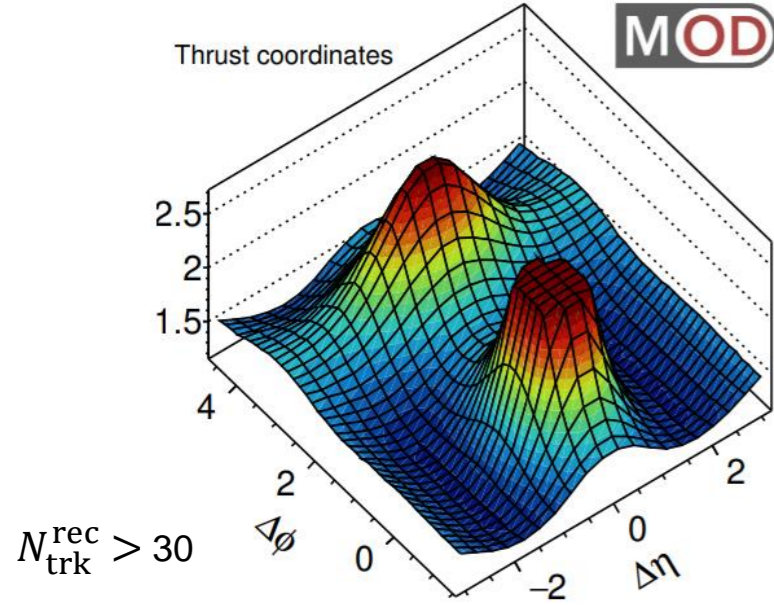


Sensitive to “medium expansion” perpendicular to the **Thrust axis**  
(**Not necessary QGP**, it could be a few rescatterings of partons)

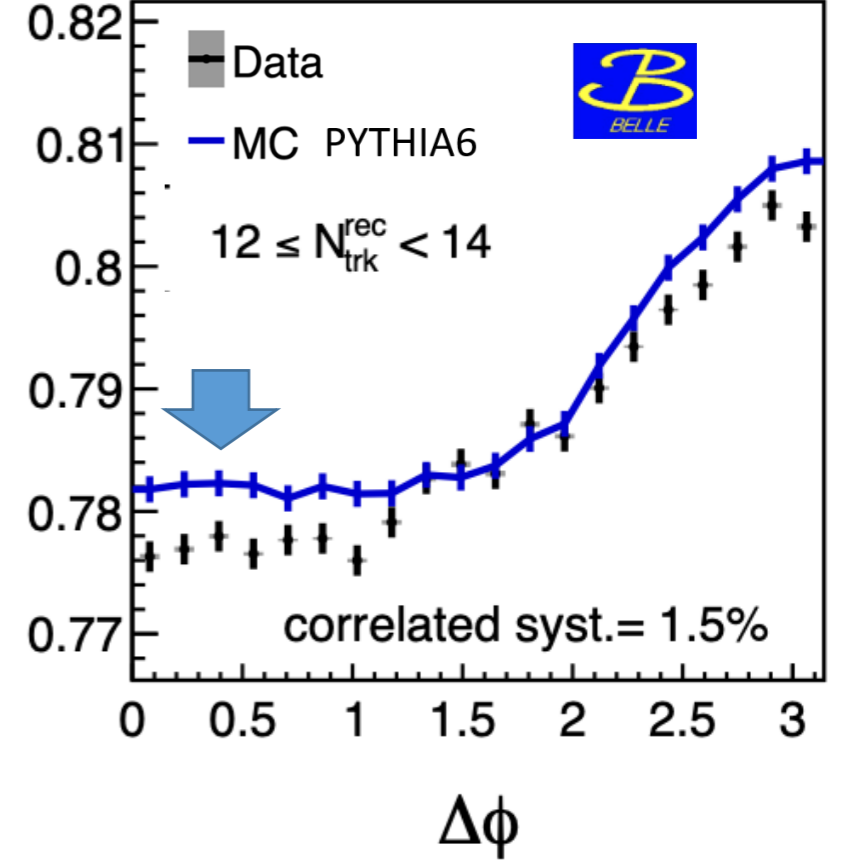


# $e^+e^-$ at 10.52 (Belle) and 91 GeV (ALEPH)

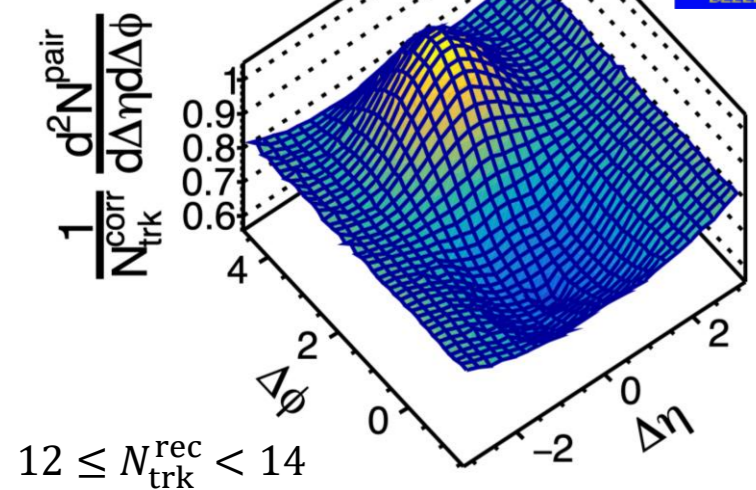
91 GeV



Belle  $e^+e^-$ ,  $\sqrt{s}=10.52$  GeV



10.52 GeV



Thrust  
Belle



Janice Chen

- No sign of ridge signal in high multiplicity electron-positron collisions up to  $\sim 35$  charged particles per event
- New reference to the collective behavior in small systems!

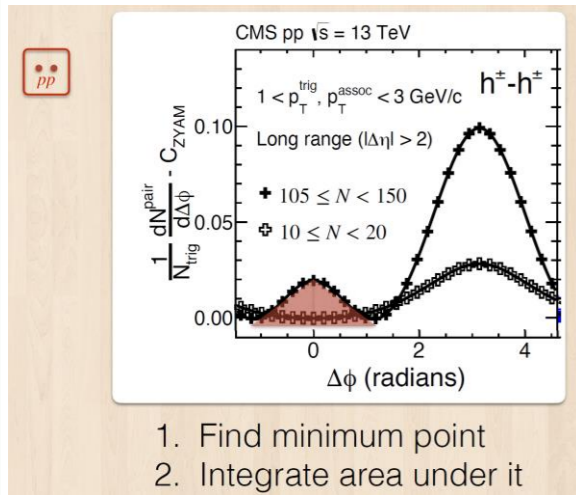
ALEPH archived data PRL 123, 212002 (2019)

Off Y(4S) resonance, Belle PRL 128 (2022) 14, 142005  
On Y(4S) resonance, Belle JHEP 03 (2023) 171



# Compilation of Ridge Yield Limit in $e^+e^-$ collisions

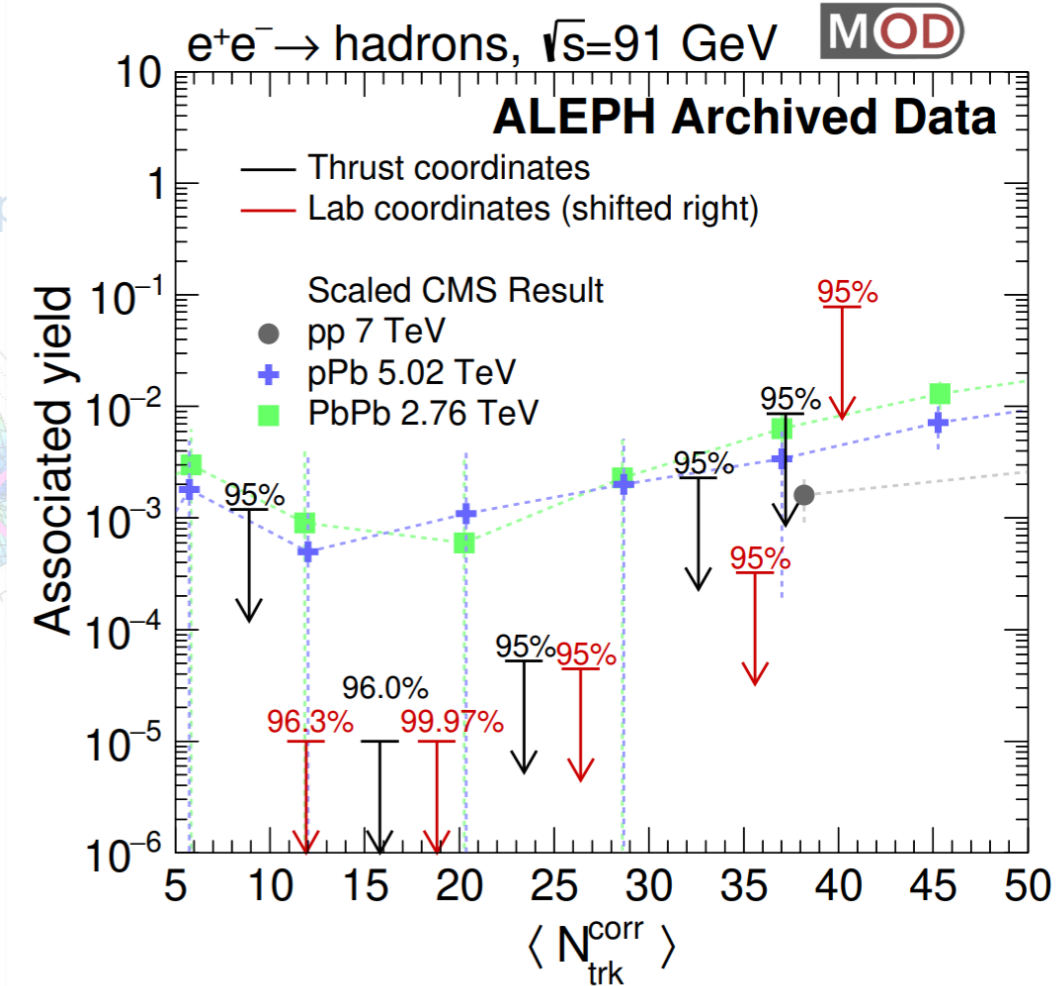
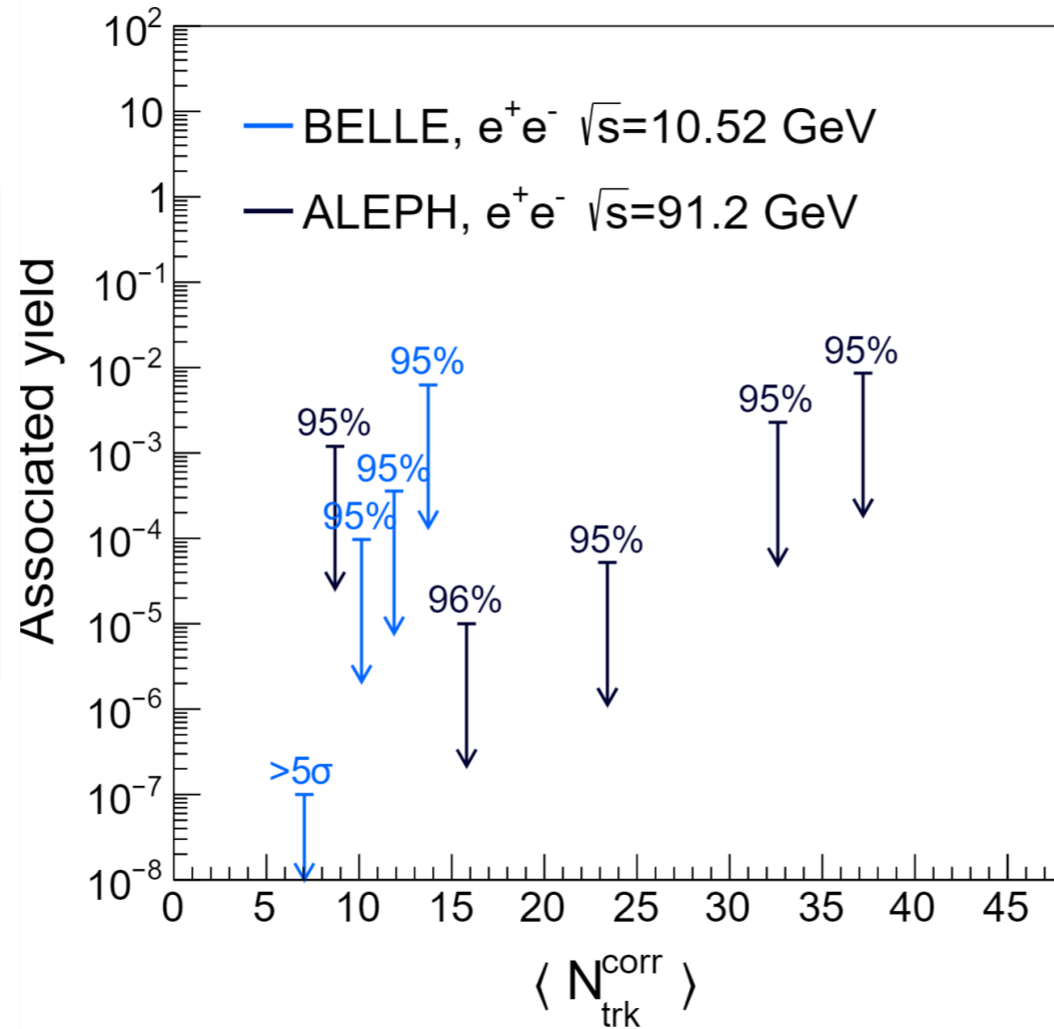
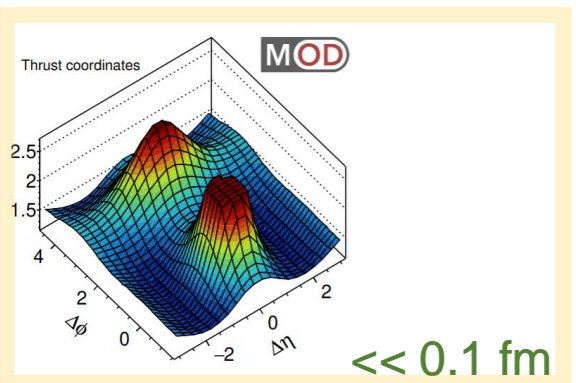
“Transverse Size”



1. Find minimum point
2. Integrate area under it

Yi Chen's slide

$e^+e^-$

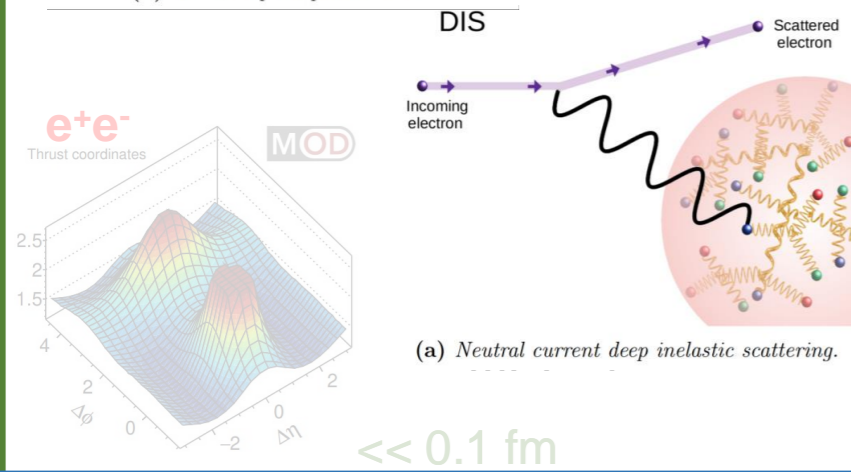
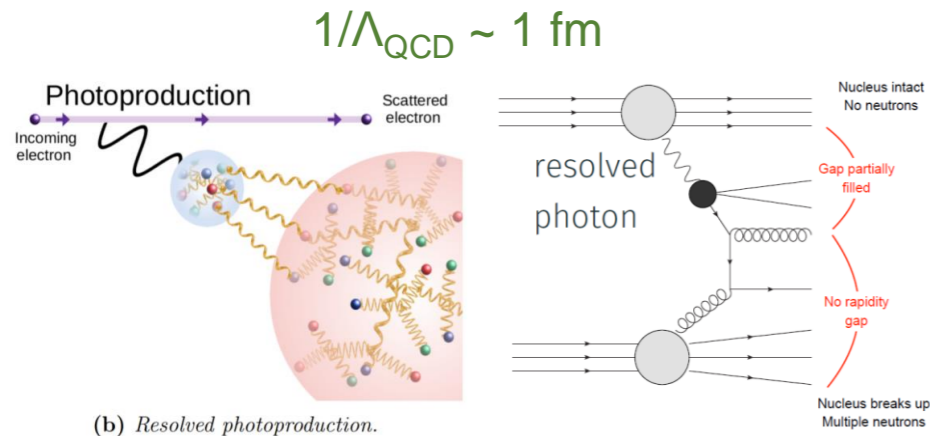


No significant ridge signal in  $e^+e^- \rightarrow q\bar{q}$   
from low to high multiplicity (up to  $\sim 35$  particles)

Multiplicity

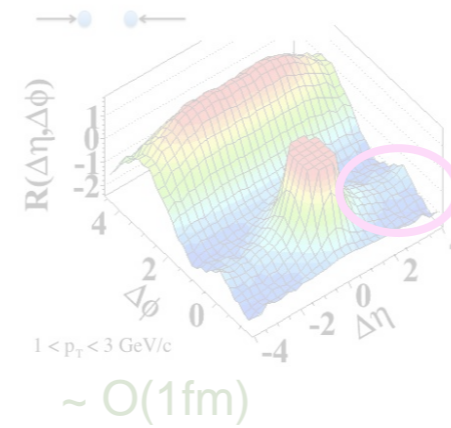
# Searches with ZEUS, H1 and CMS $\gamma p$

“Transverse Size” / MPI



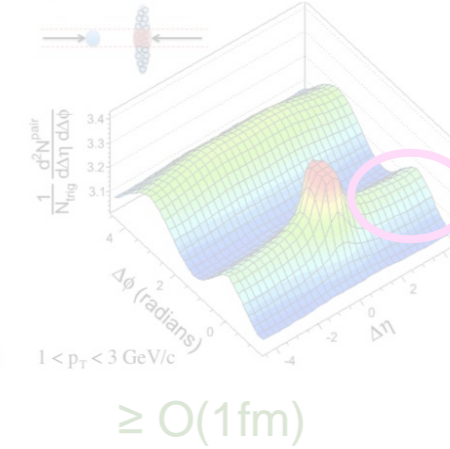
High multiplicity pp

(a) pp  $\sqrt{s} = 7 \text{ TeV}$ ,  $N_{\text{ch}}^{\text{offline}} \geq 110$

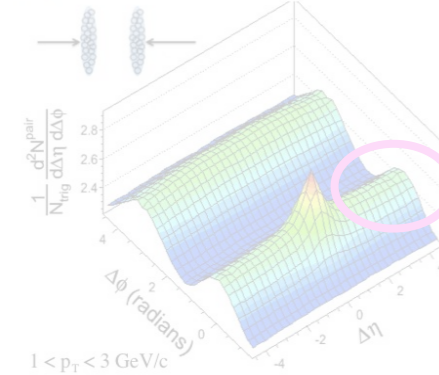


High multiplicity pPb

(b) pPb  $\sqrt{s_{\text{NN}}} = 5.02 \text{ TeV}$ ,  $220 < N_{\text{ch}}^{\text{offline}} \leq 260$



(c) PbPb  $\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV}$ ,  $220 < N_{\text{ch}}^{\text{offline}} \leq 260$

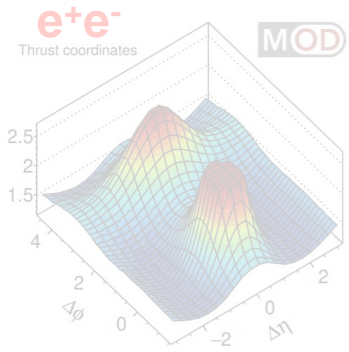
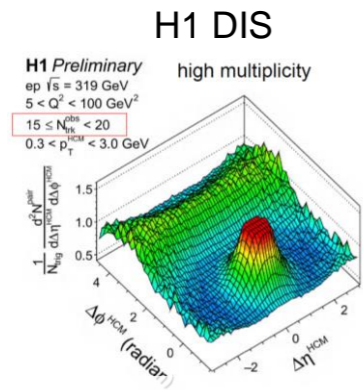
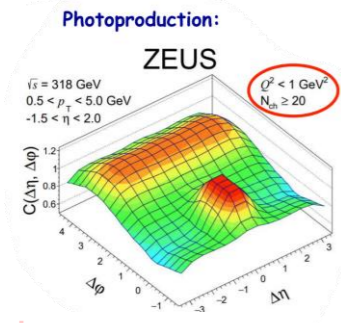


Multiplicity

# Searches with ZEUS, H1 and CMS $\gamma p$

“Transverse Size” / MPI

See Nicole Lewis’s talk in the workshop

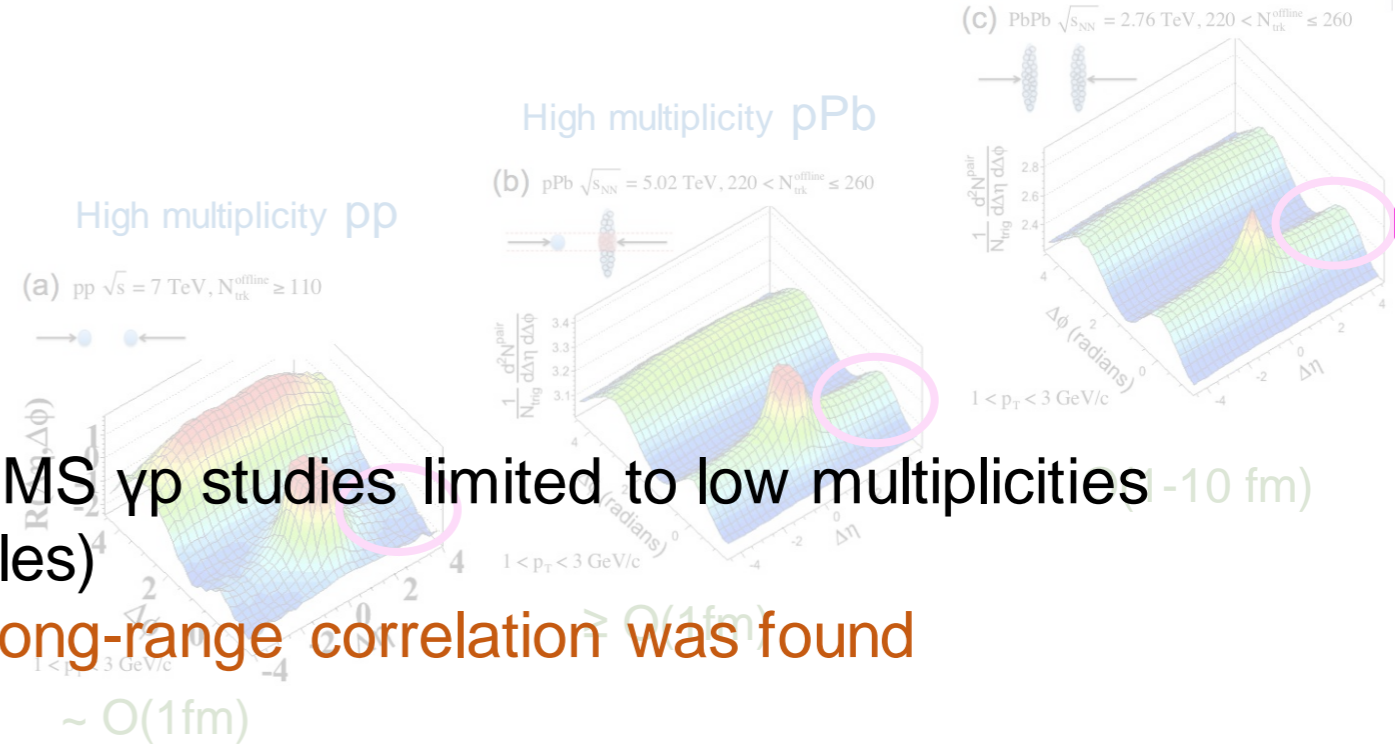


MPI ≥ 1  
“MPI”=1  
≪ 0.1 fm

ZEUS, H1 and CMS  $\gamma p$  studies limited to low multiplicities (Up to ~20 particles)

No indication of long-range correlation was found

ATLAS  $\gamma Pb$  shows no sign of ridge before subtraction



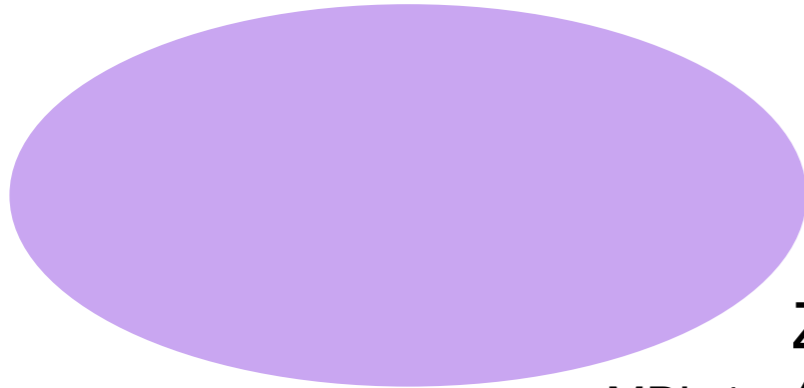
ZEUS ep neutral current DIS: [JHEP 04 \(2020\) 070](#)  
 ZEUS ep photonuclear: [JHEP 12 \(2021\) 102](#)  
 H1 ep neutral current DIS: (preliminary) [H1prelim-20-033](#)  
 CMS pPb photonuclear: [PLB 844 \(2023\) 137905](#)  
 ATLAS PbPb photonuclear: [PRC 104 \(2021\) 1, 014903](#)

Multiplicity

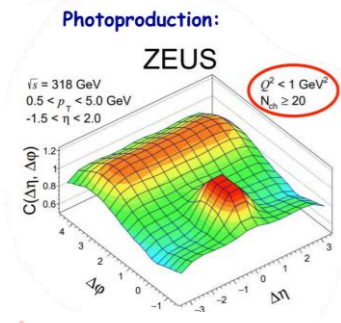


# System Size

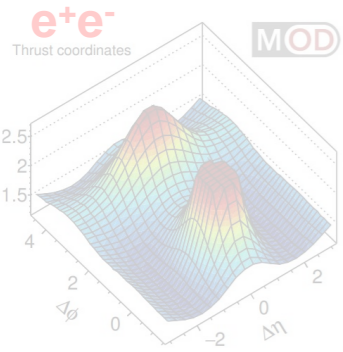
“Transverse Size” / MPI



MPI > 1



MPI ≥ 1



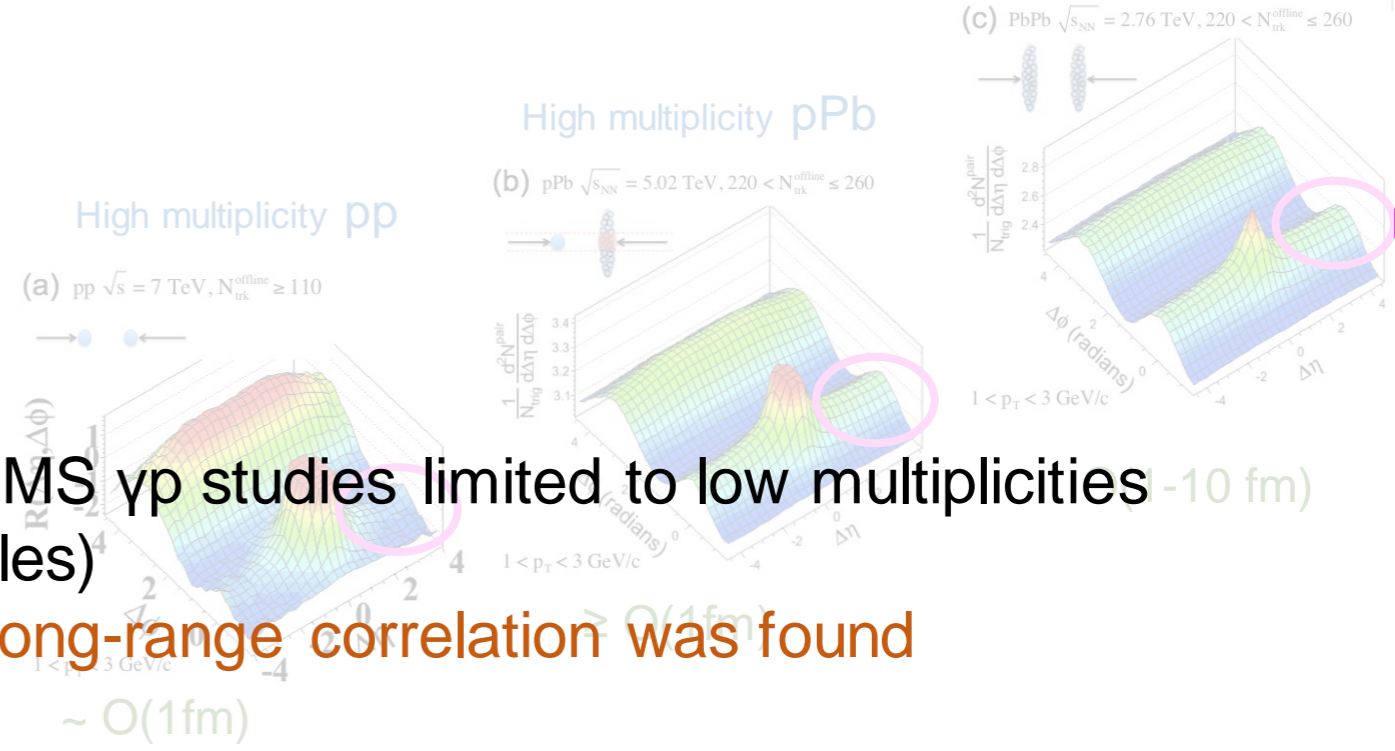
“MPI”=1

<< 0.1 fm

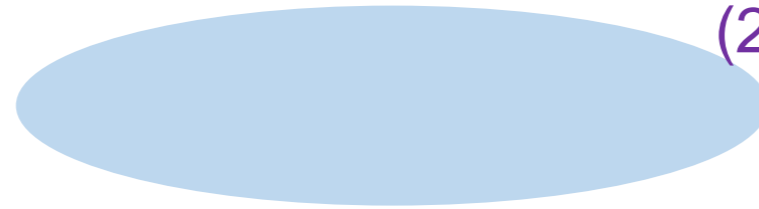
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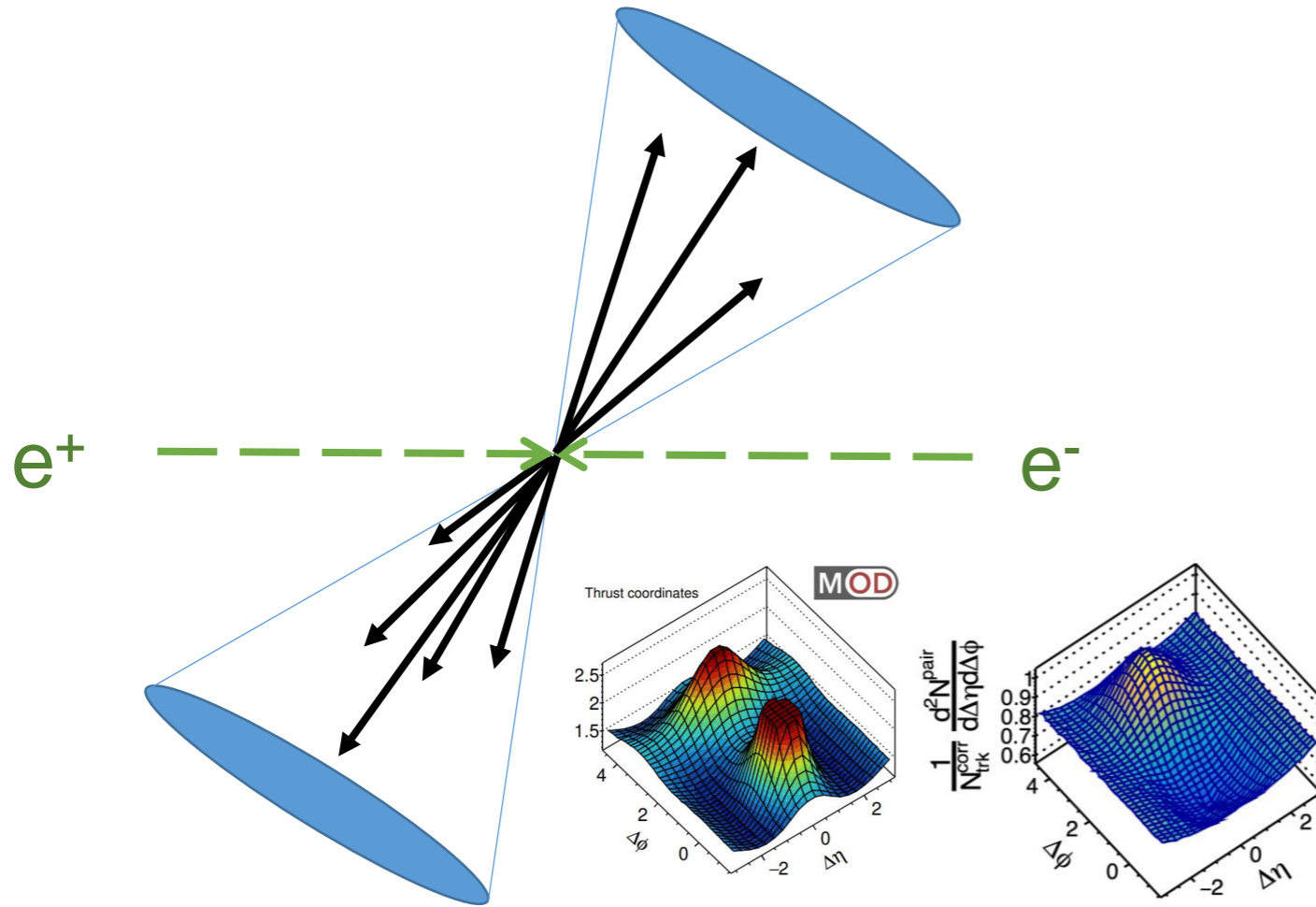
- Next steps:
- (1) Increase multiplicity
  - (2) Increase  $\langle \text{MPI} \rangle$



Multiplicity

# Can We Overlap Two Color Strings?

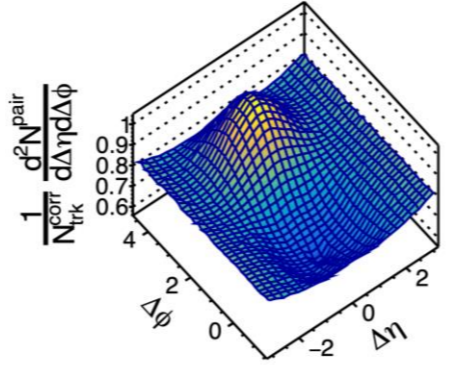
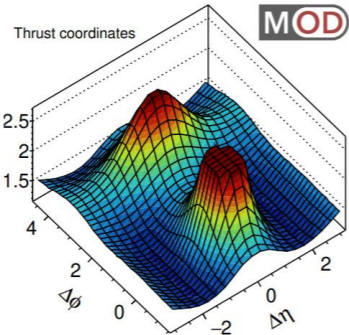
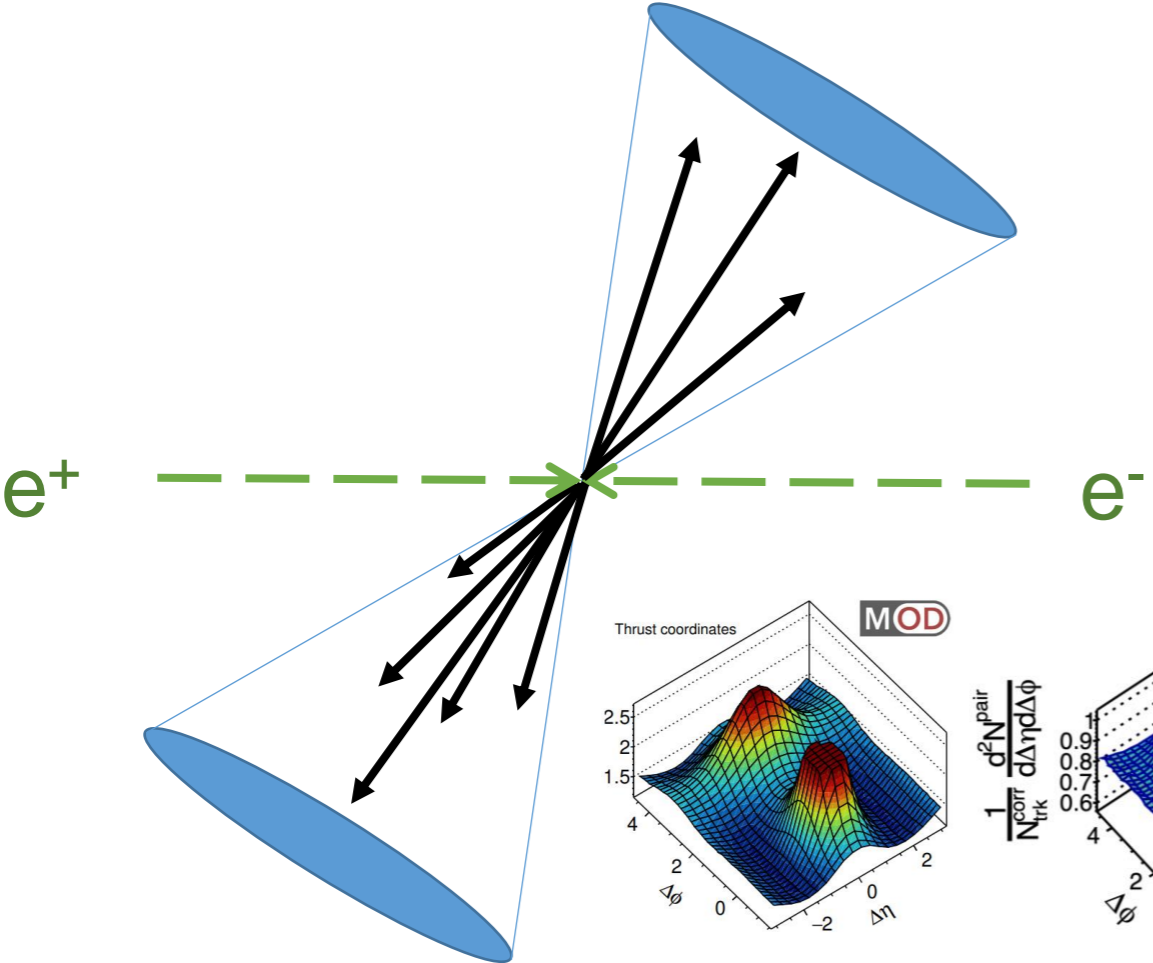
$$e^+ e^- \rightarrow q \bar{q}$$



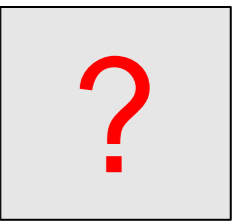
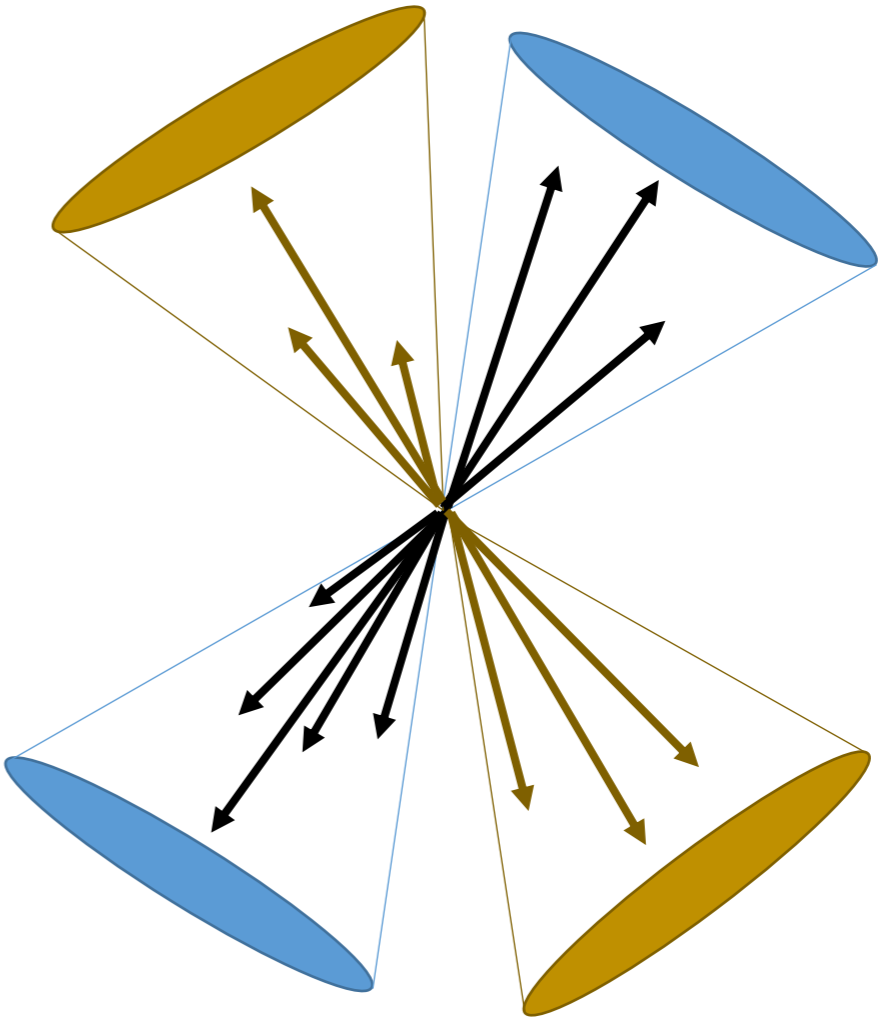
No ridge-like structure

# Can We Overlap Two Color Strings?

$$e^+ e^- \rightarrow q \bar{q}$$



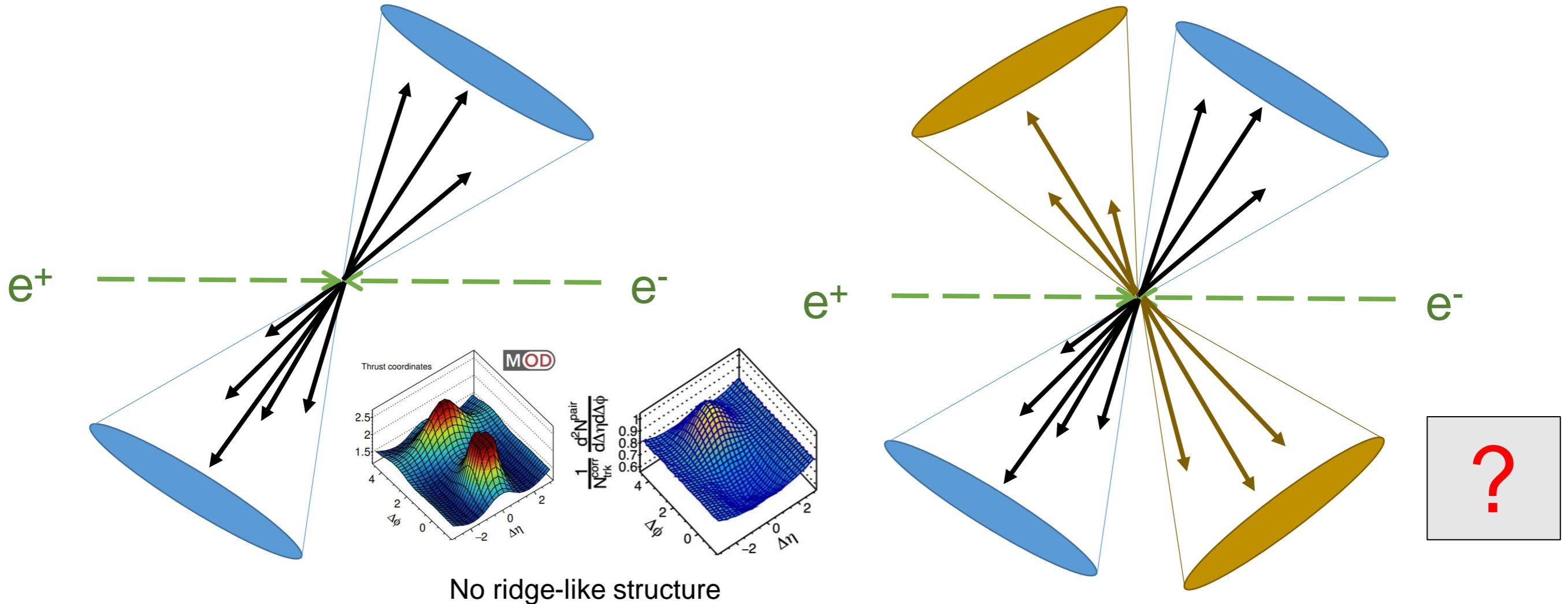
No ridge-like structure



# High Multiplicity $e^+e^-$ Event at LEP 2 !!

$$e^+e^- \rightarrow q\bar{q}$$

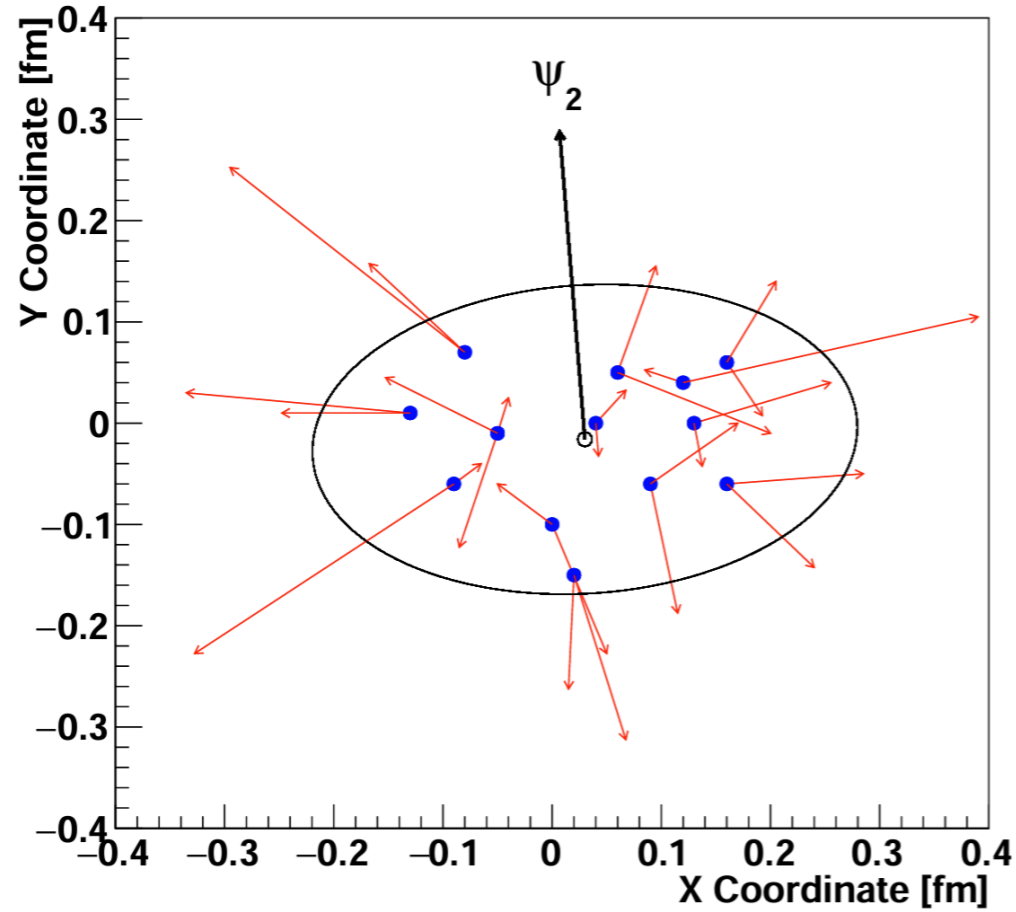
$$e^+e^- \rightarrow W^+W^- \rightarrow q\bar{q}q\bar{q}$$



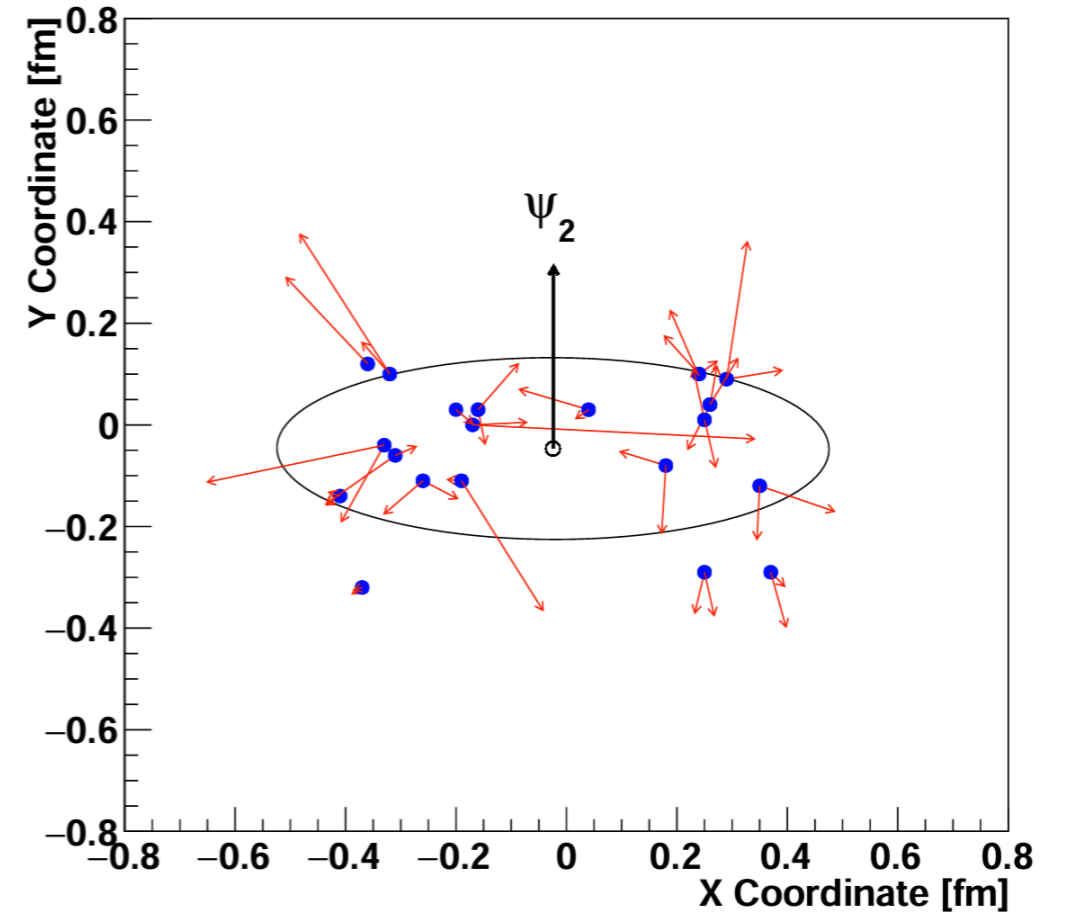


# Example Study with AMPT

## Single-String Configuration

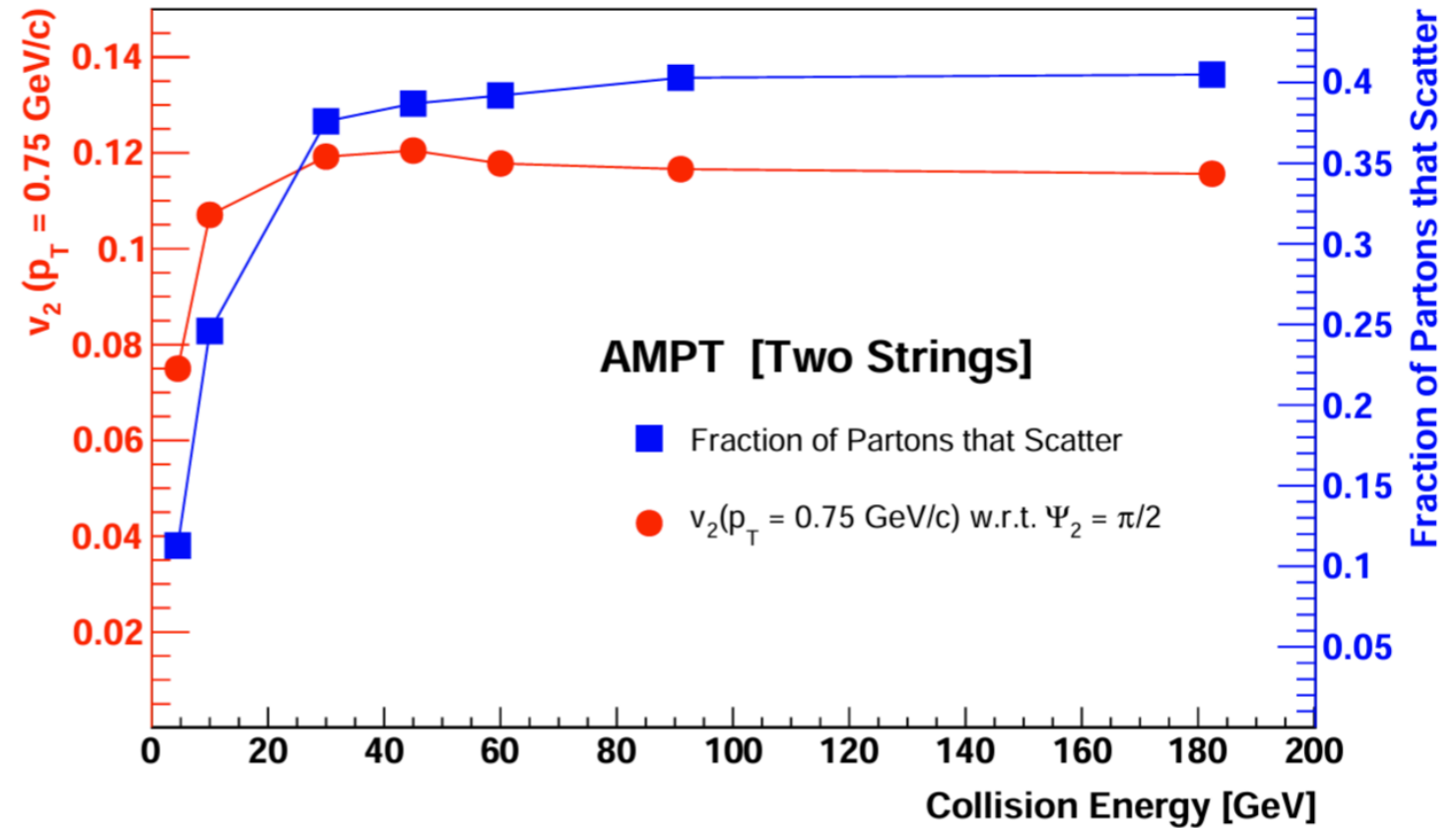
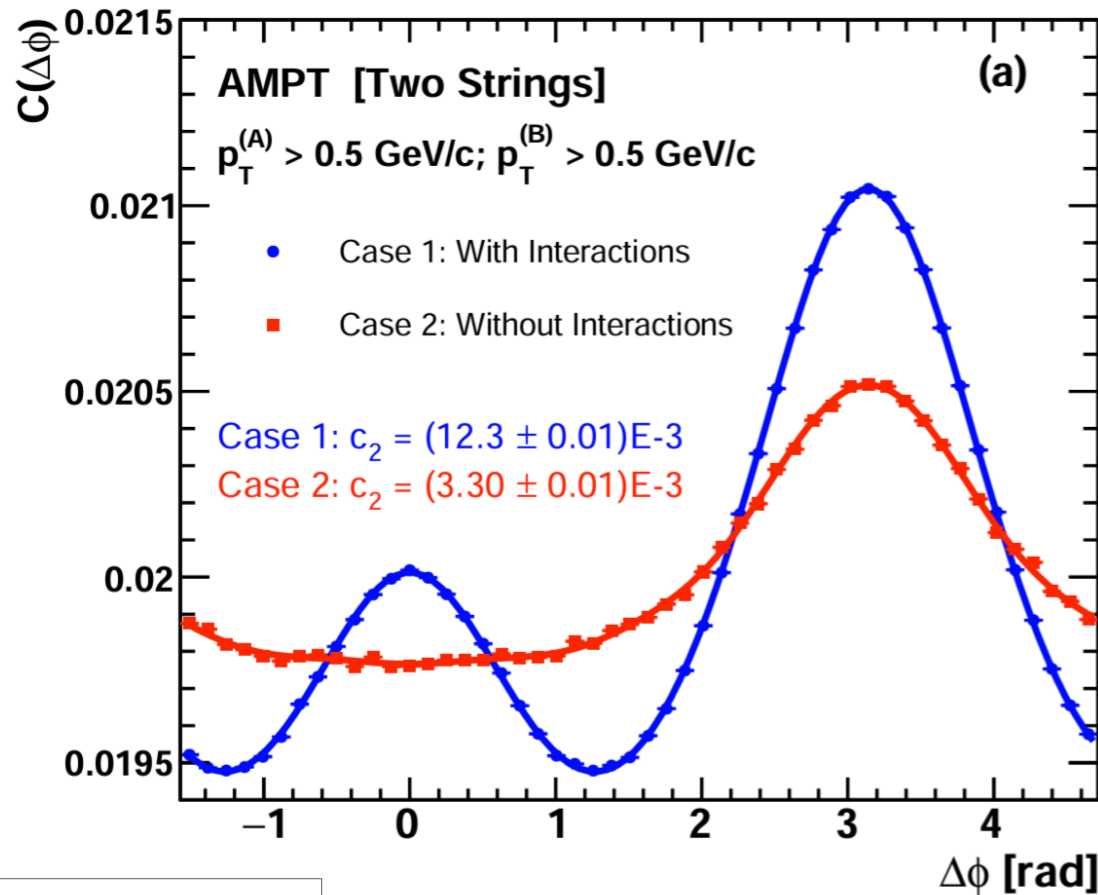


## Two-String Configuration

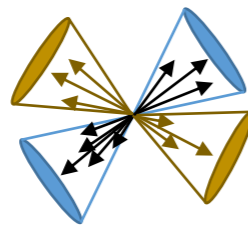
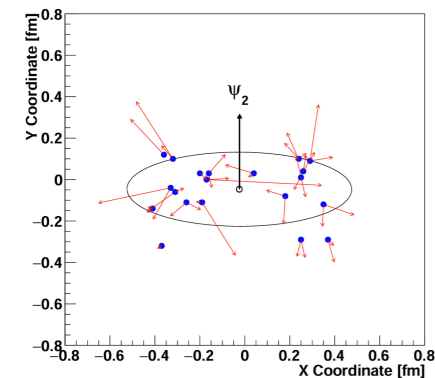


J. Nagle et al, PRC 97 (2018) 2, 024909

# Example: Two Strings Configuration Study with AMPT



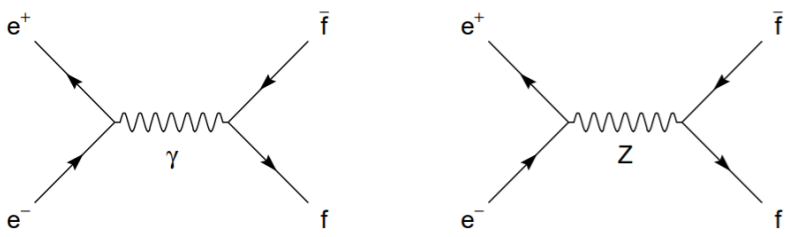
- With Interaction: A significant enhancement of  $v_2$
- Little change in terms of  $v_3$  magnitude (from a Fourier decomposition fit to the data in the figure)



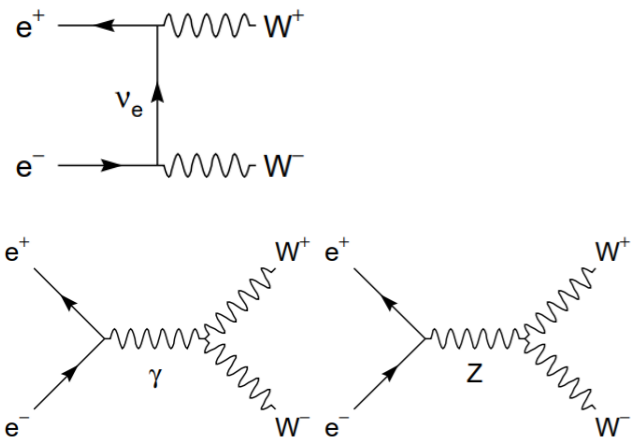
J. Nagle et al, PRC 97 (2018) 2, 024909

# Charged Particle Multiplicity Distributions in LEP2 Data

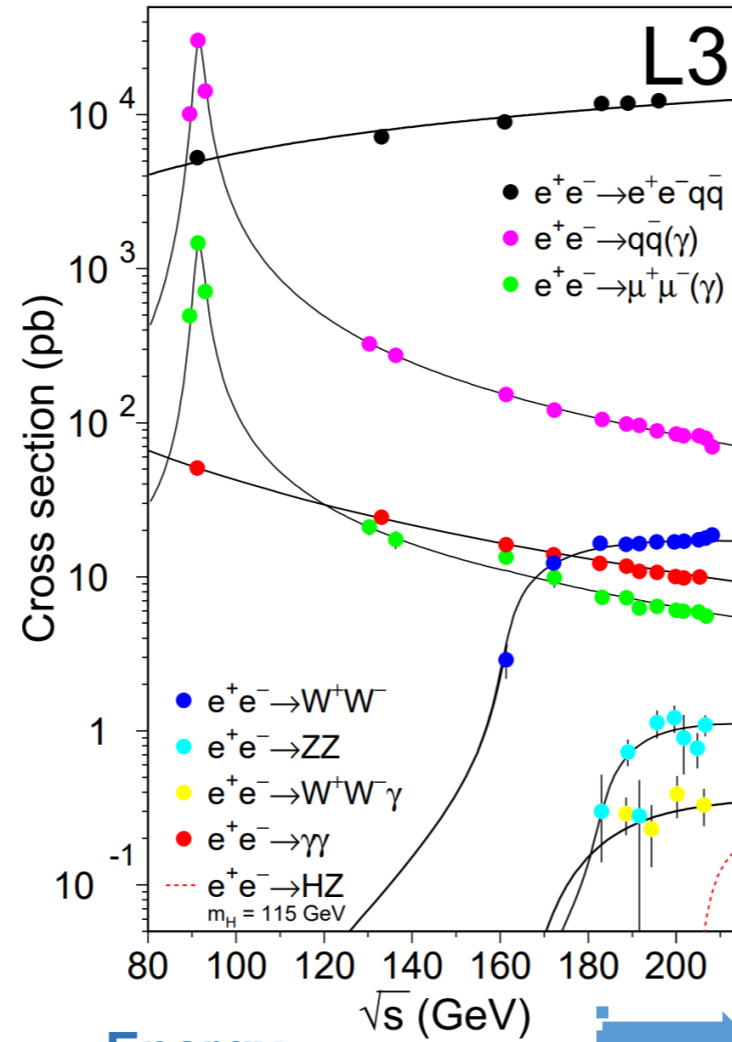
●  $e^+e^- \rightarrow qq(\gamma)$



●  $e^+e^- \rightarrow W^+W^-$



Phys. Rept. 532 (2013) 119-244

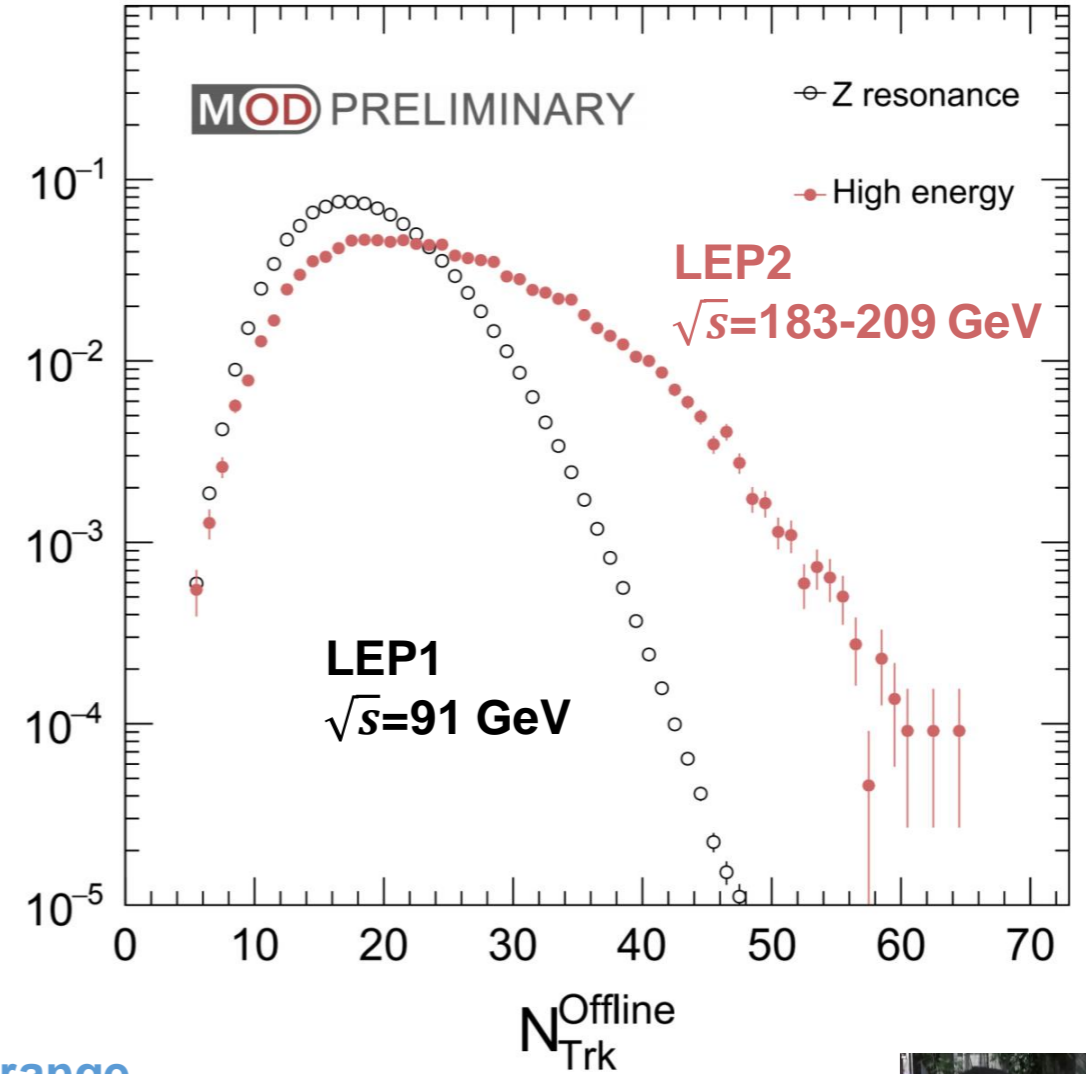


Energy

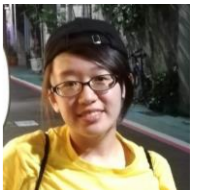
EPJC 63 611 (2009)

Reported range

Fraction of Total Events



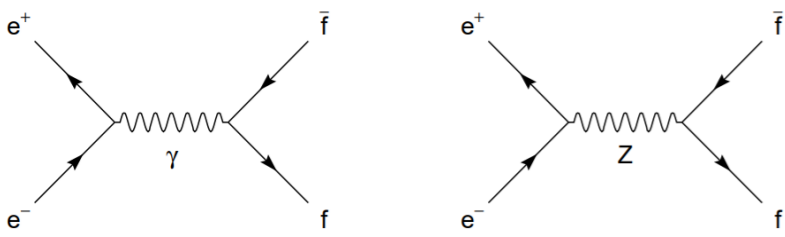
- **LEP2 energies** also give access to different physics processes



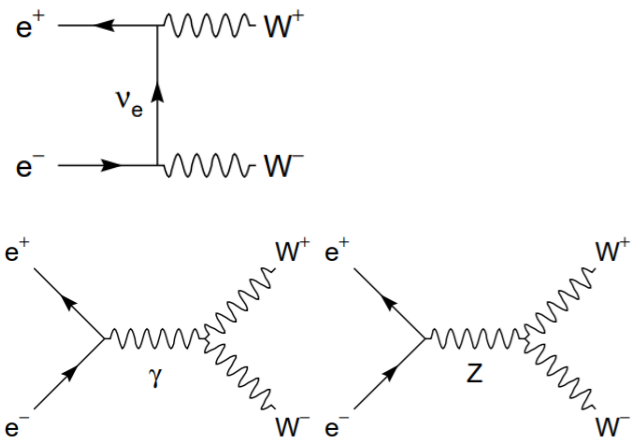
Yu-Chen "Janice" Chen (MIT)

# Charged Particle Multiplicity Distributions in LEP2 Data

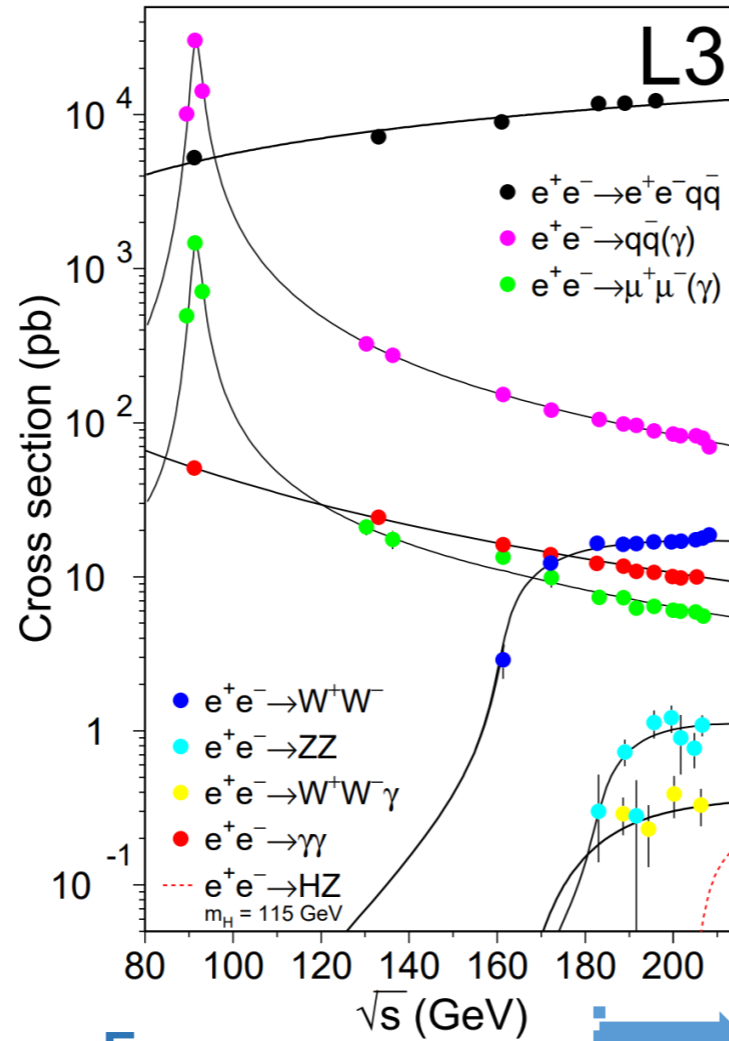
●  $e^+e^- \rightarrow q\bar{q}(\gamma)$



●  $e^+e^- \rightarrow W^+W^-$



Phys. Rept. 532 (2013) 119-244



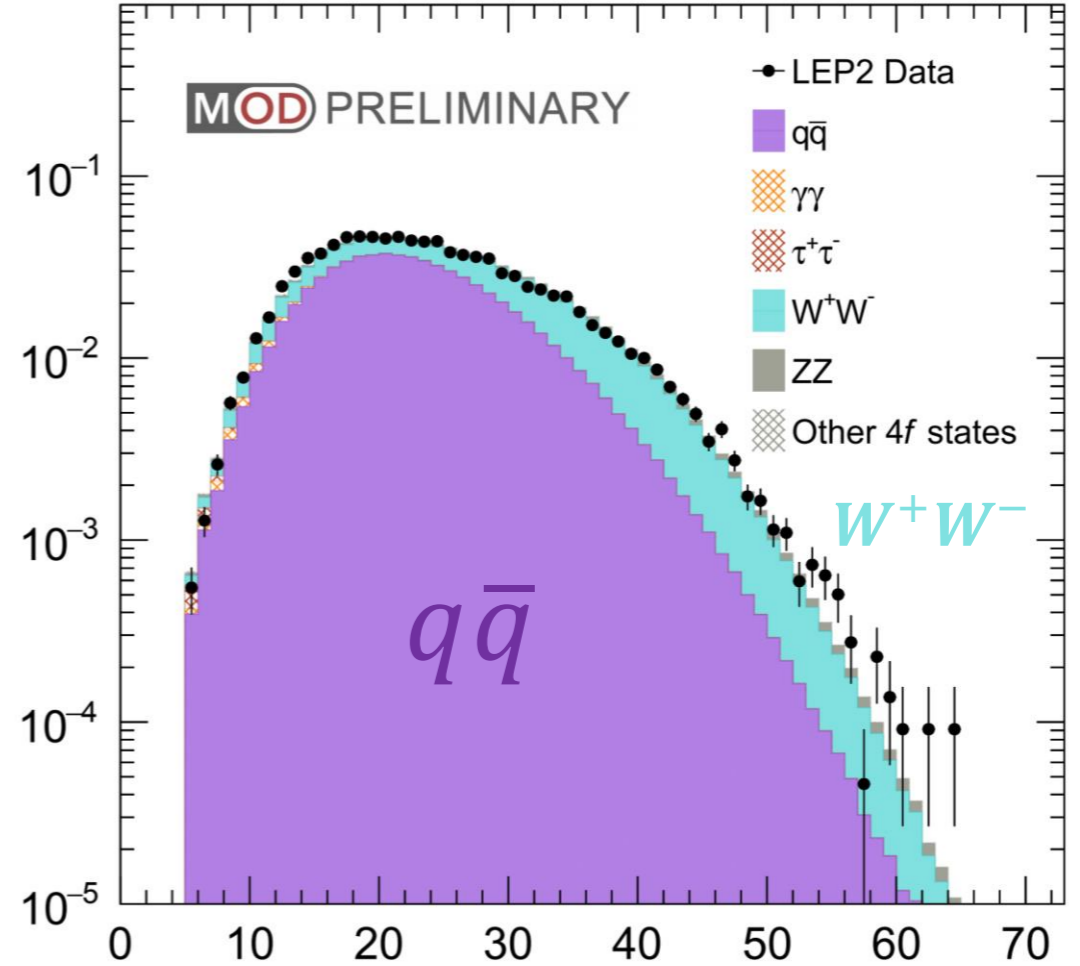
Energy

EPJC 63 611 (2009)

Reported range

$e^+e^- \rightarrow \text{hadrons}, \sqrt{s}=183-209$  GeV

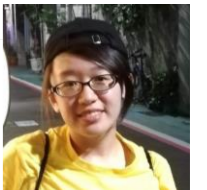
Fraction of Total Events



\*MC contributions are stacked

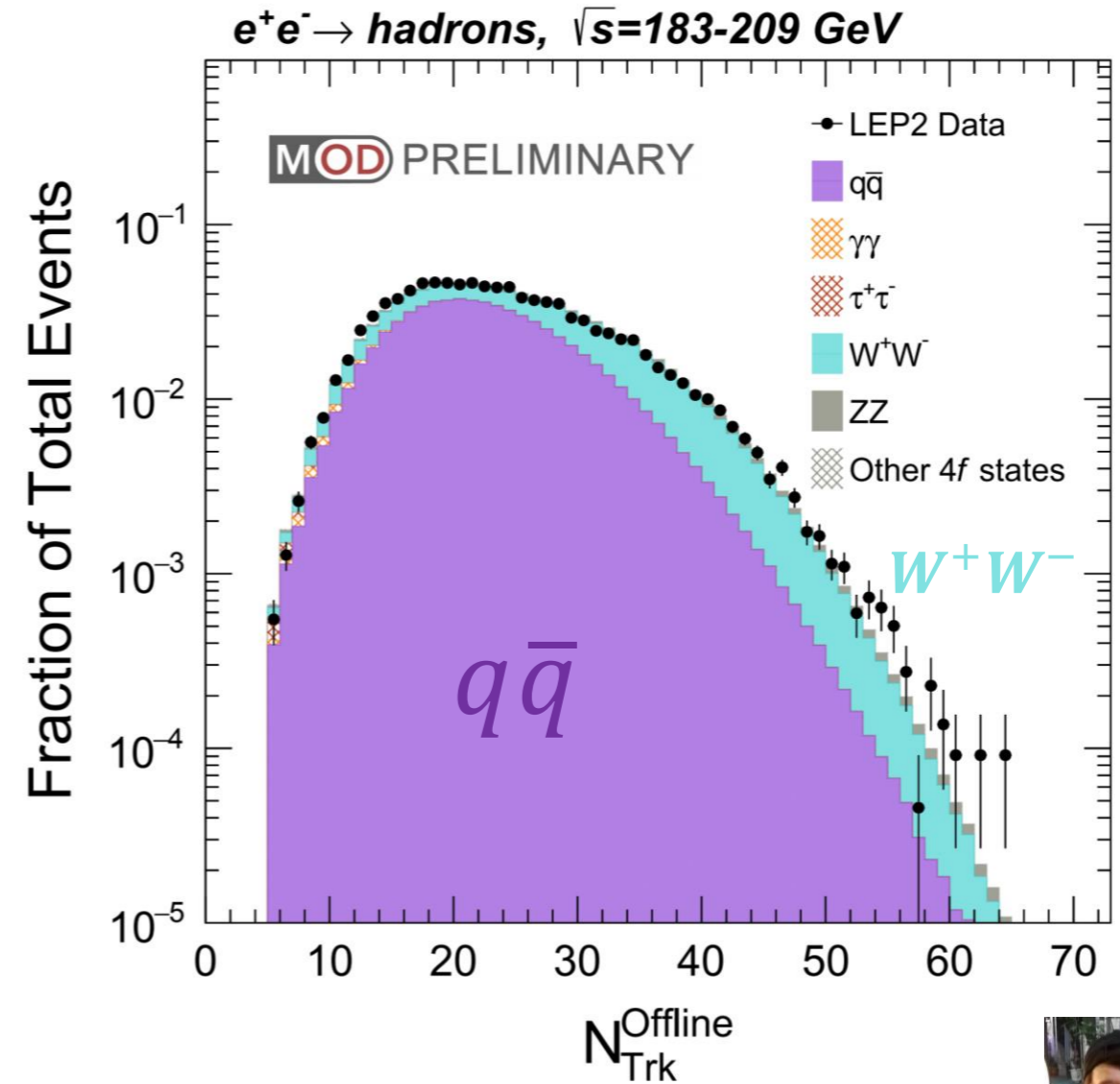
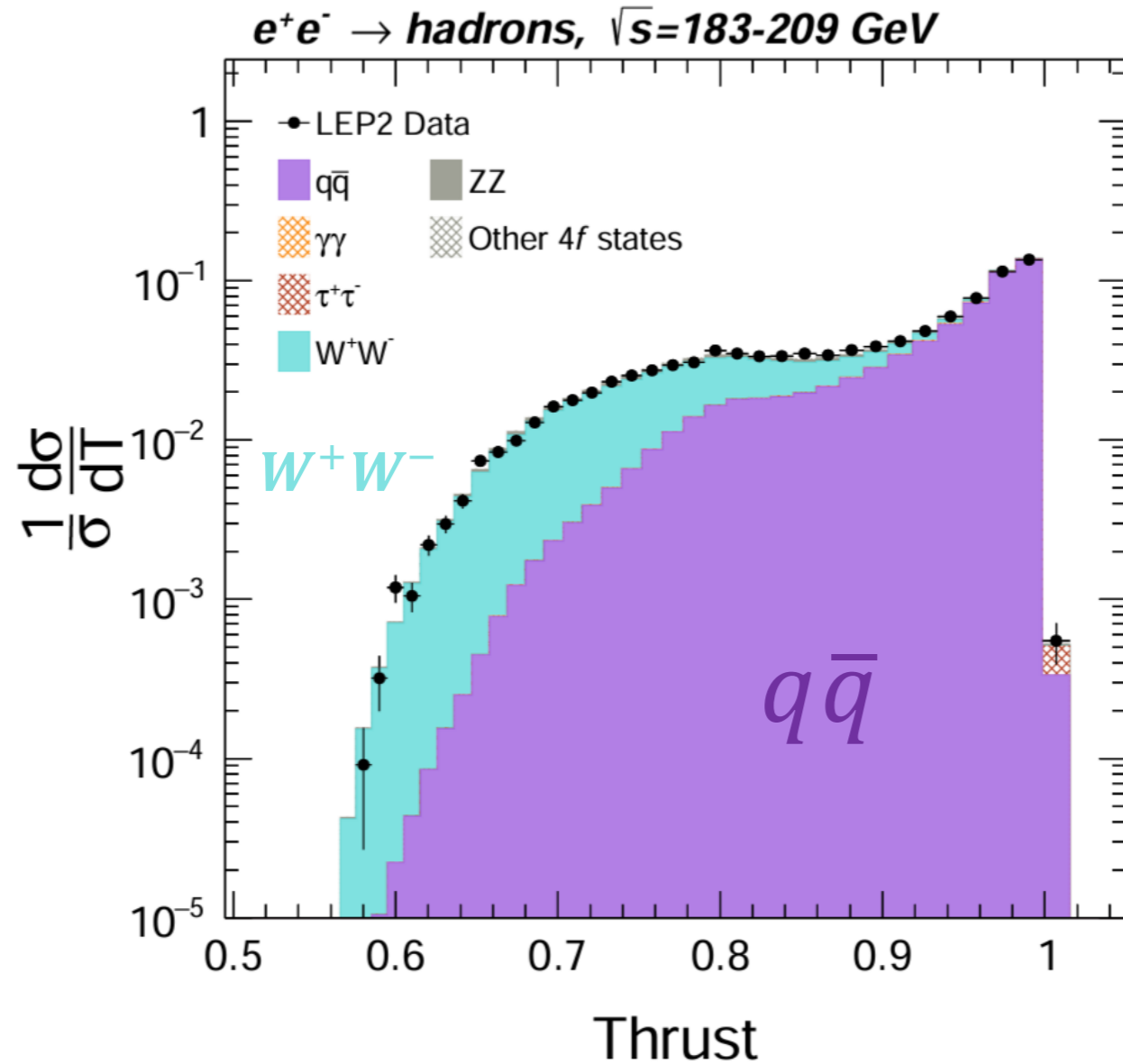
$N_{\text{Trk}}^{\text{Offline}}$

- LEP2 energies also give access to different physics processes
- At high multiplicity,  $W^+W^-$  contribution becomes significant

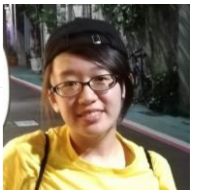


Yu-Chen "Janice" Chen (MIT)

# Example validation study of archived data and MC

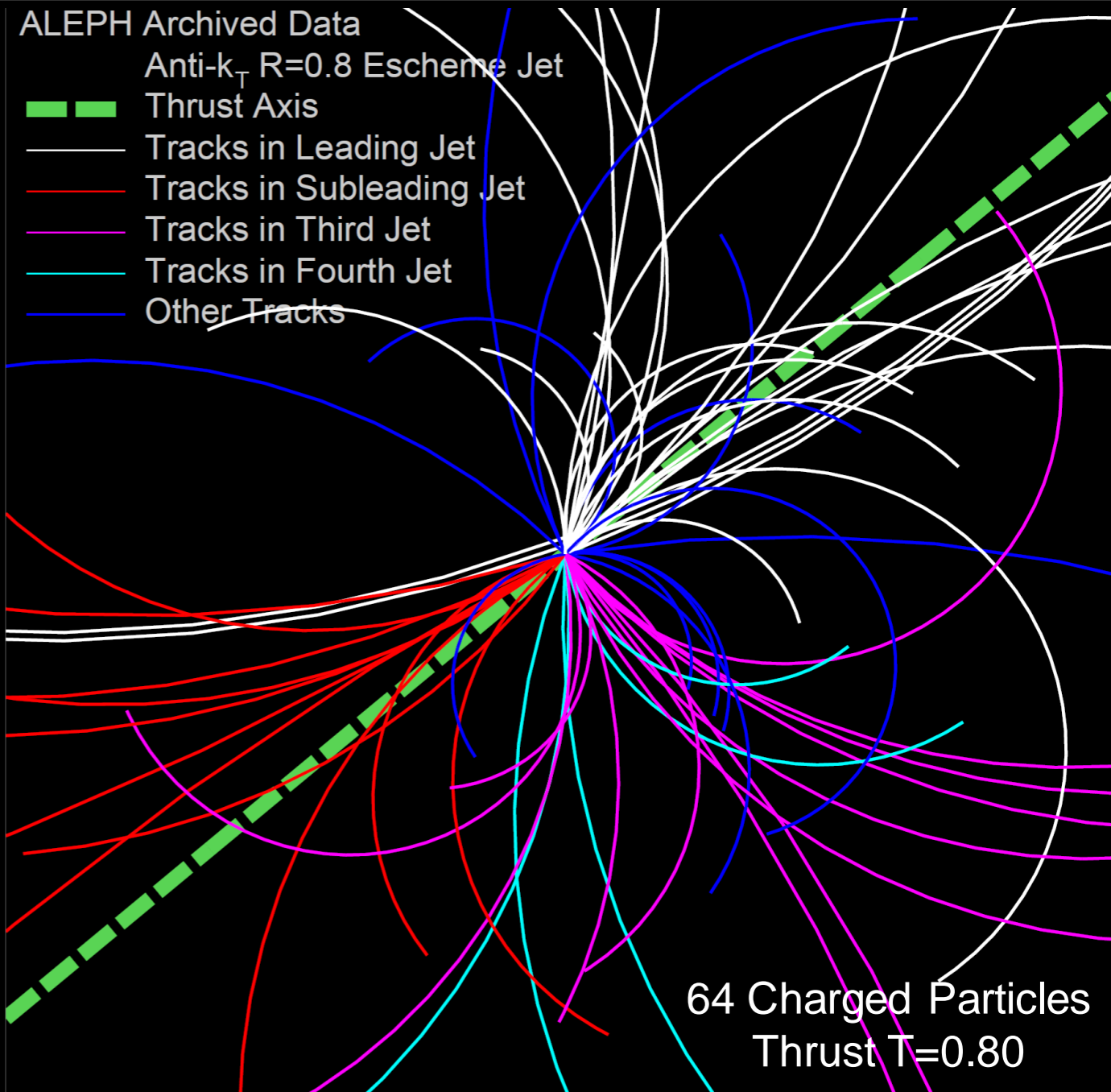
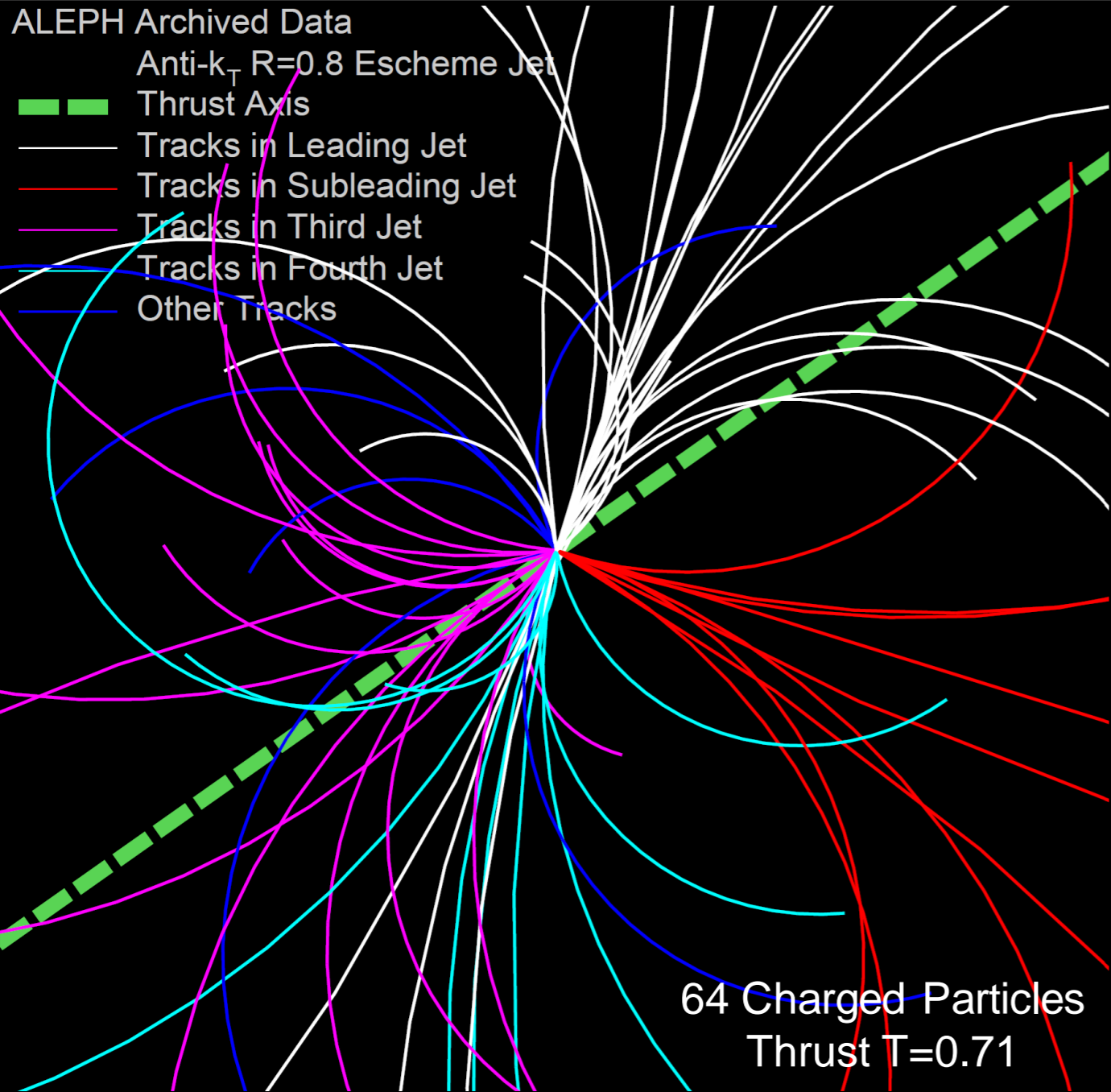


- Inspected thrust distributions (shown) and many other control plots (visible energies) year-by-year.
- Reasonable agreement between data and archived MC.

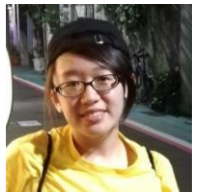
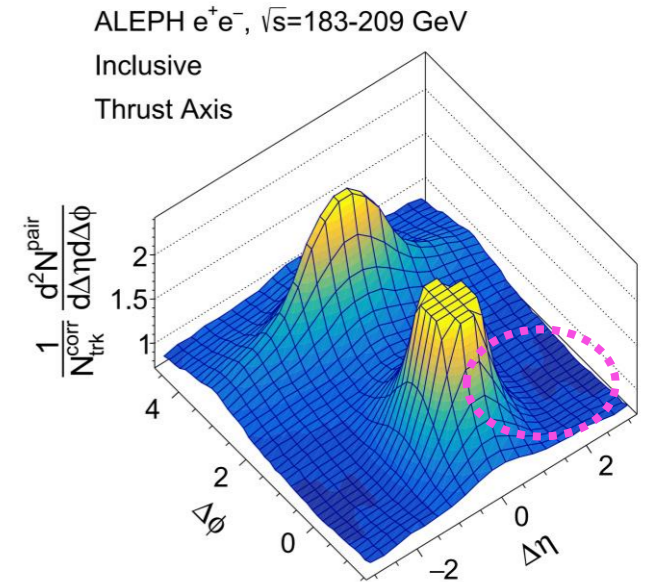
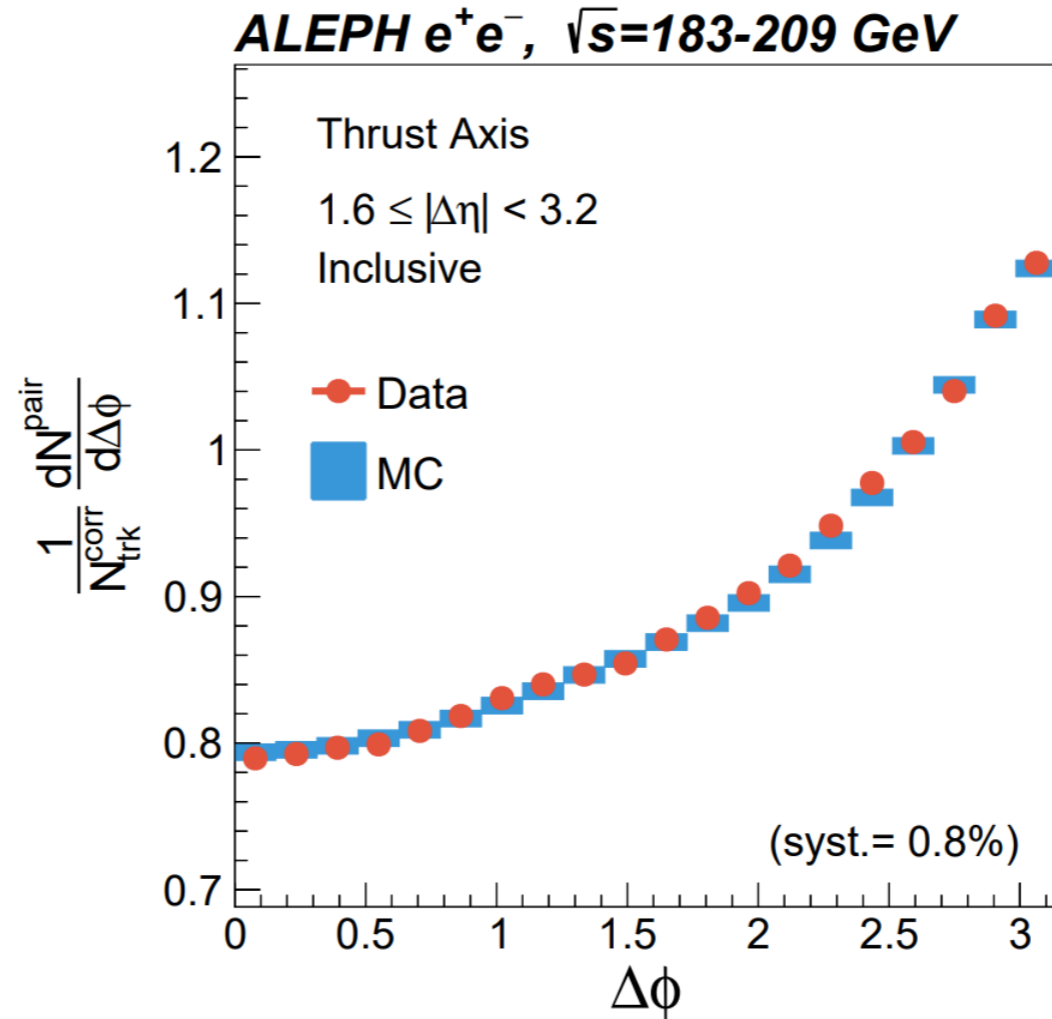
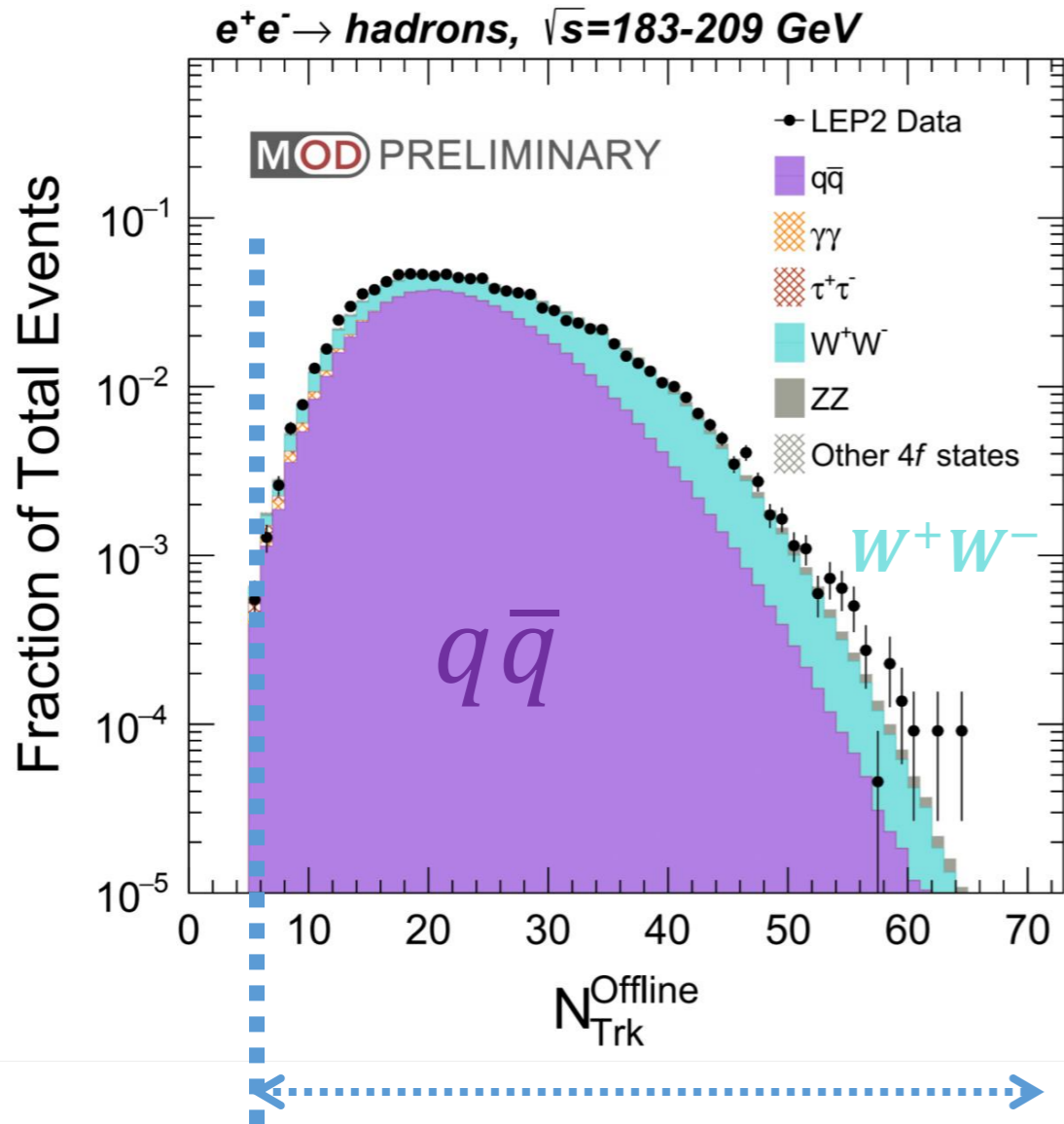


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# The Highest Multiplicity Events in Archived LEP2 Data



# Inclusive Hadronic $e^+e^-$ Events at LEP 2 ( $N_{ch} \geq 5$ )

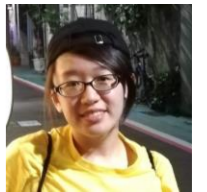
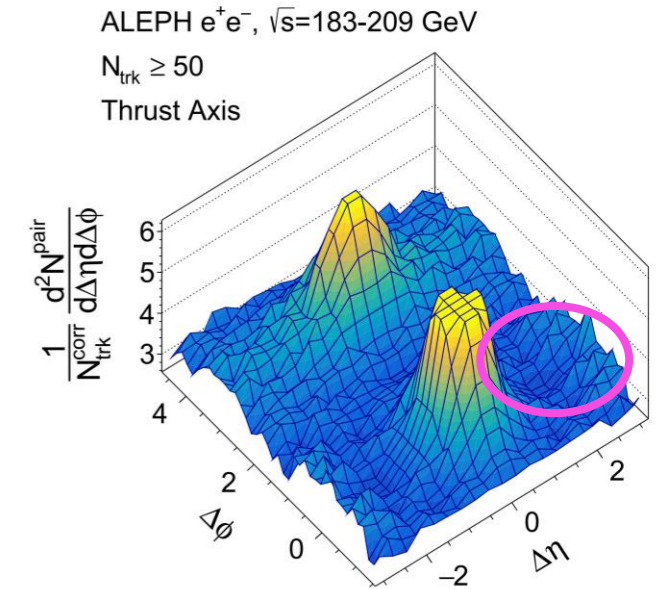
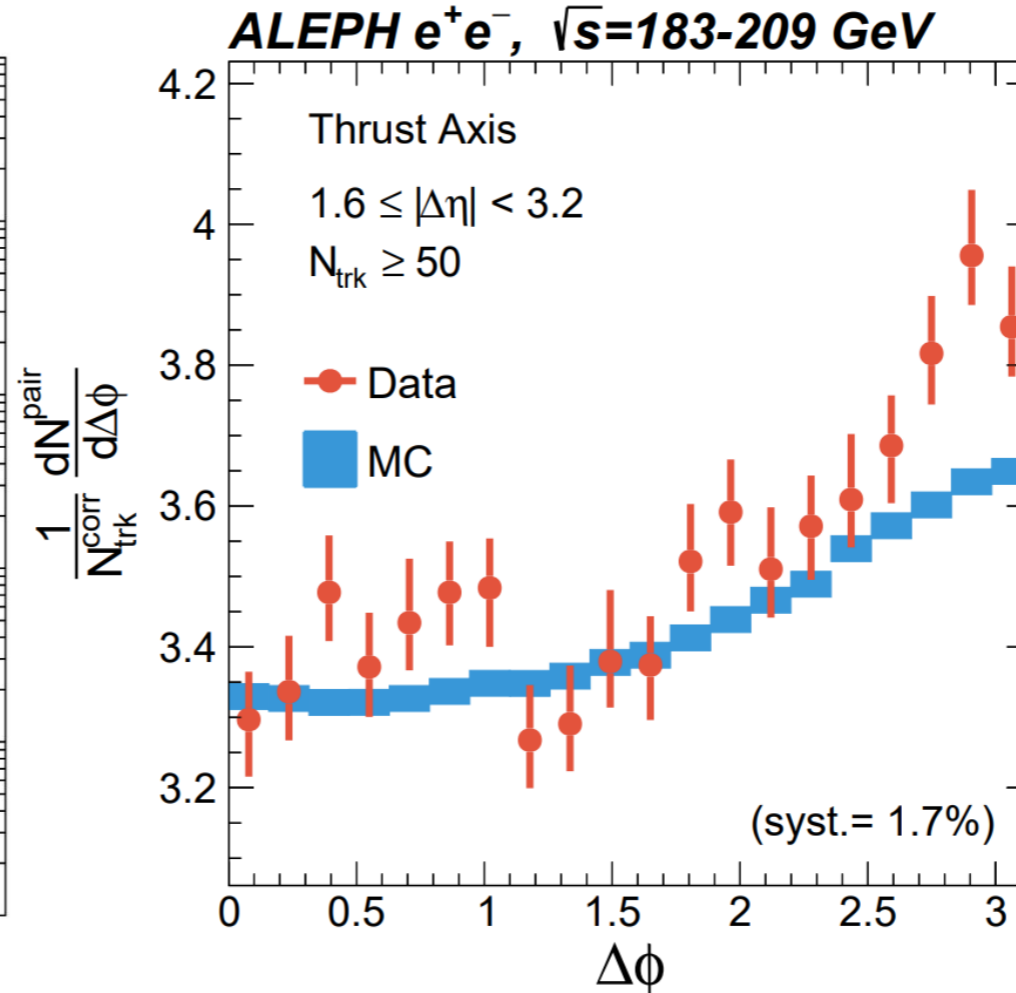
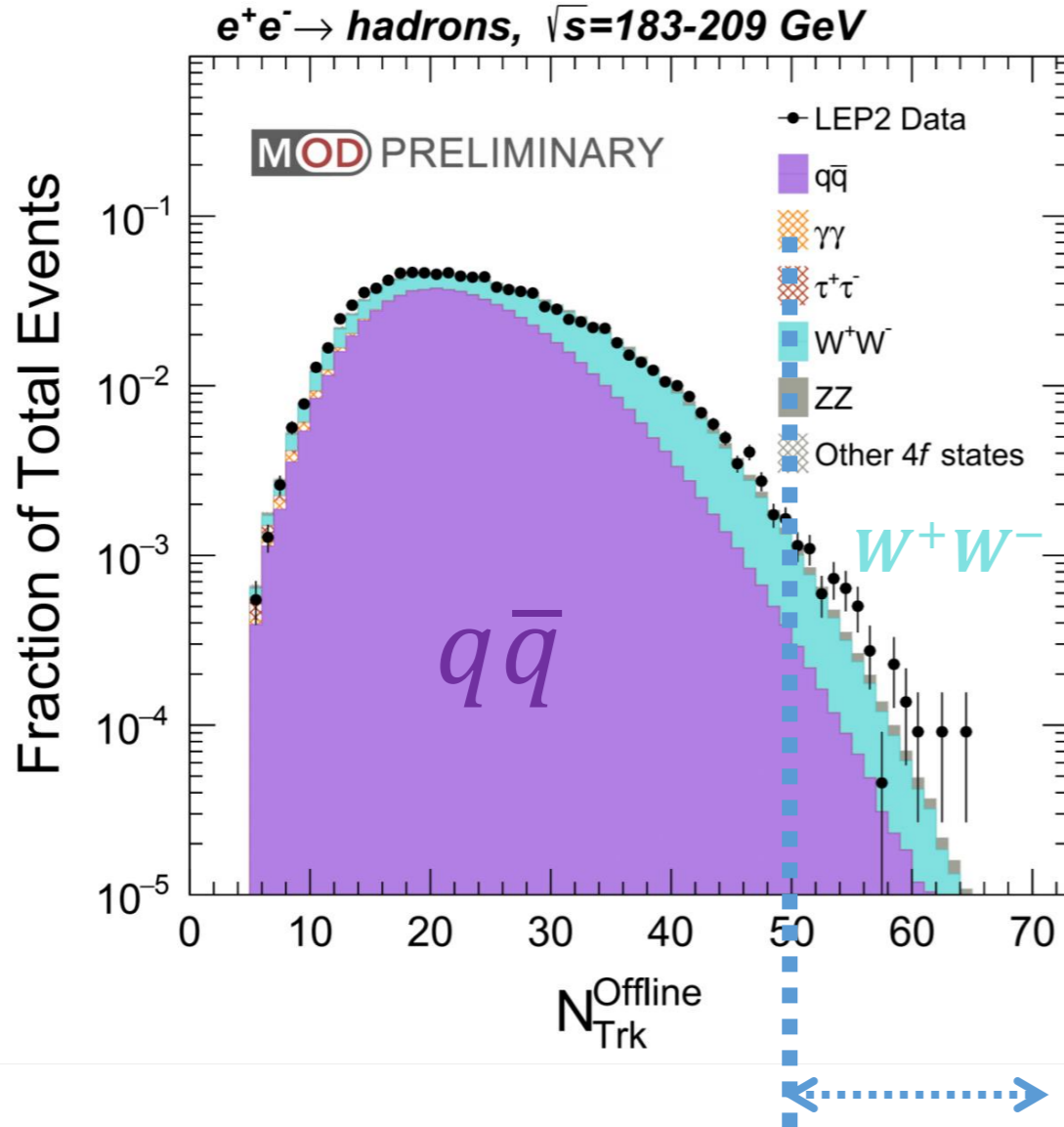


Yu-Chen "Janice" Chen (MIT)

- Excellent agreement between **data** and **simulation (Archived MC)**

arXiv:2312.05084

# High Multiplicity $e^+e^-$ Events at LEP 2 ( $N_{\text{trk}} \geq 50$ )



Yu-Chen "Janice" Chen (MIT)

- A long-range near-side correlation signal shows up at high multiplicity!
- Data also feature a narrower away-side spectrum at  $\Delta\phi \sim \pi$

arXiv:2312.05084



# High Multiplicity $e^+e^-$ Events at LEP1 vs LEP 2

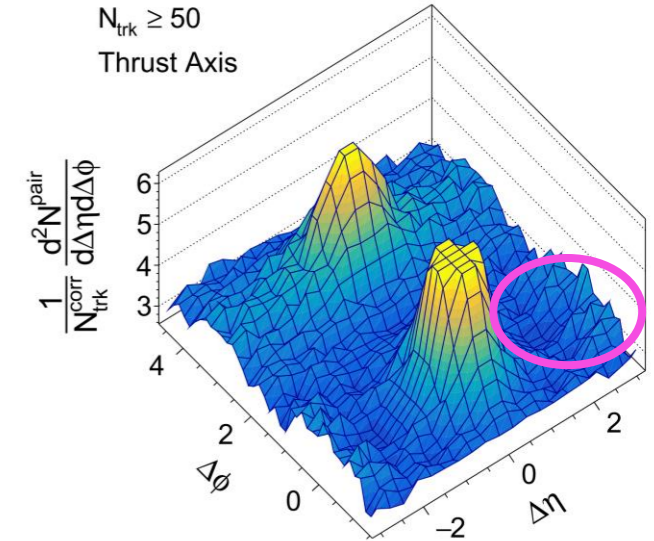
LEP1  $N_{\text{trk}} > 35$

LEP2  $N_{\text{trk}} > 50$

ALEPH  $e^+e^-$ ,  $\sqrt{s}=183\text{-}209$  GeV

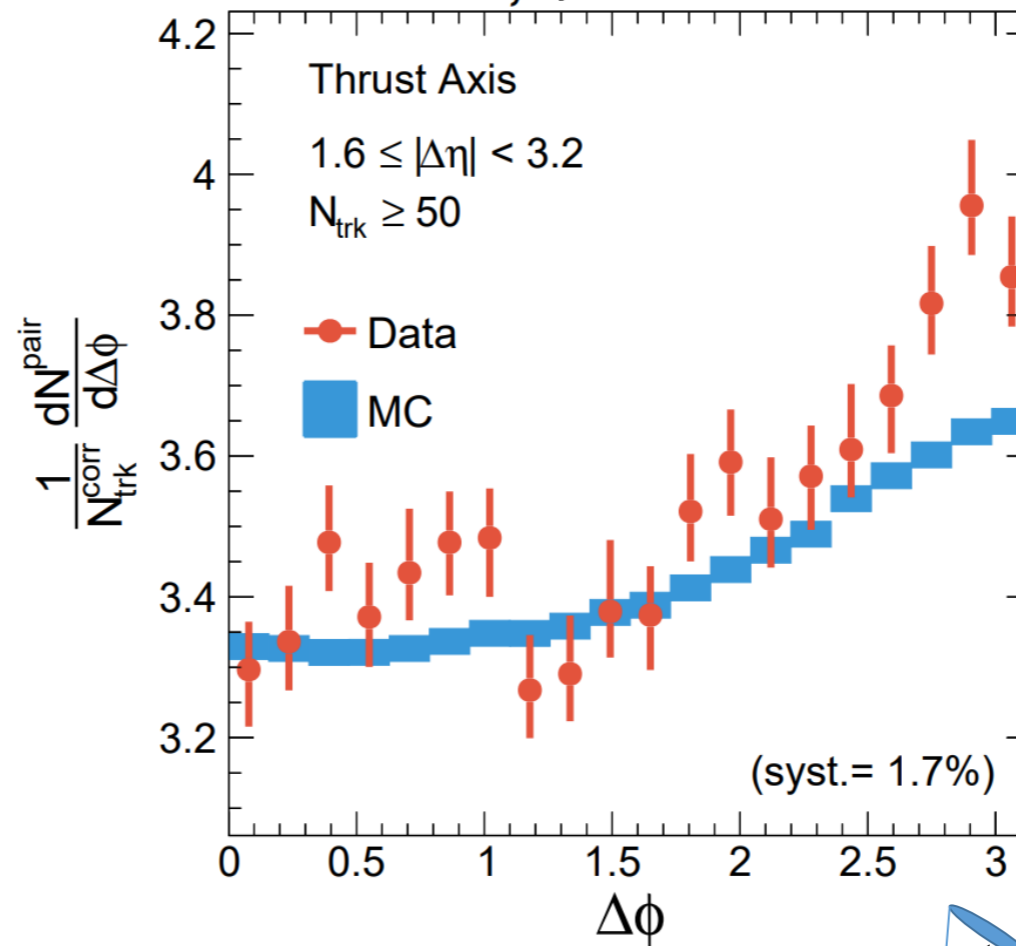
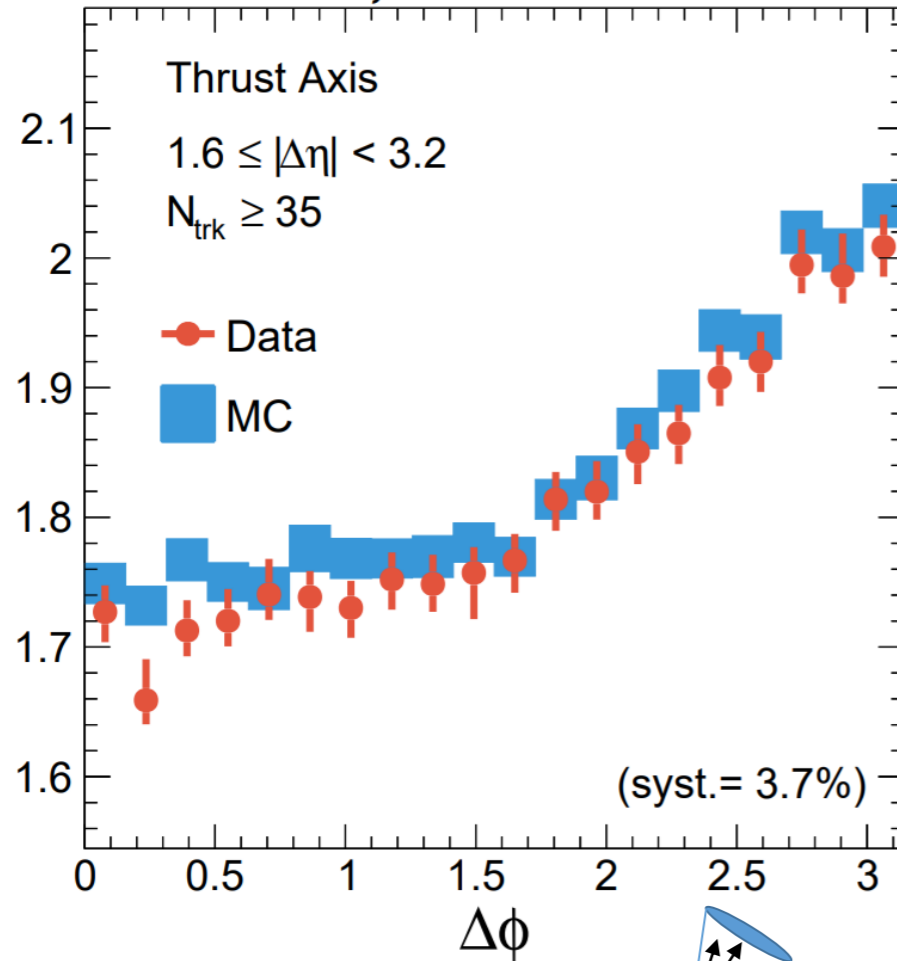
$N_{\text{trk}} \geq 50$

Thrust Axis

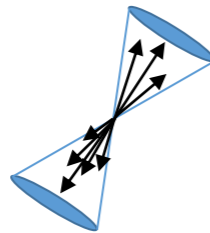


ALEPH  $e^+e^-$ ,  $\sqrt{s}=91.2$  GeV

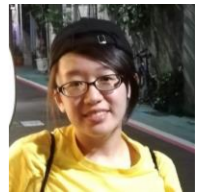
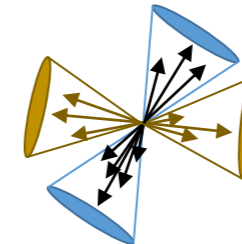
ALEPH  $e^+e^-$ ,  $\sqrt{s}=183\text{-}209$  GeV



$e^+e^- \rightarrow q\bar{q}(\gamma)$



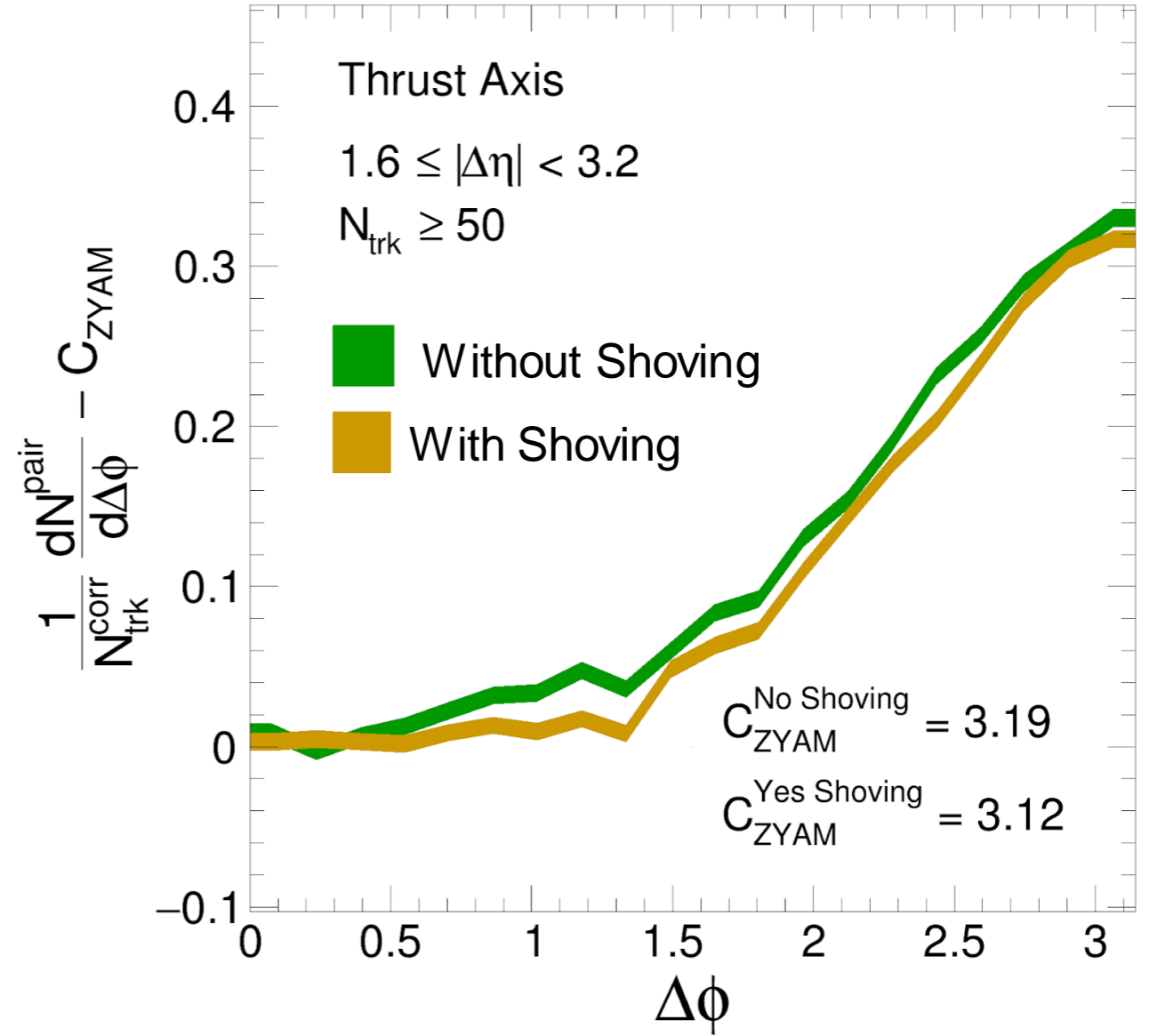
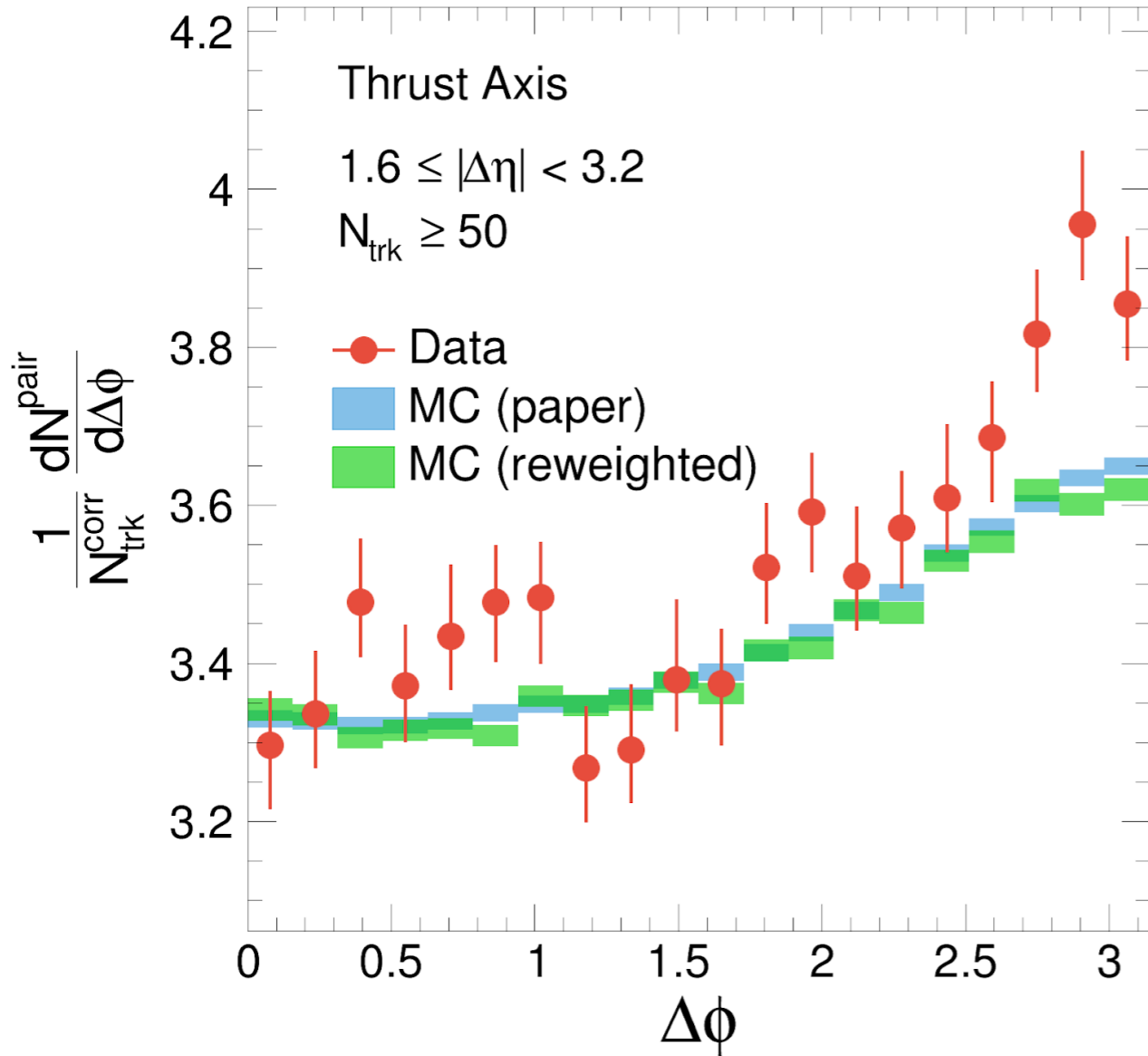
$e^+e^- \rightarrow W^+W^-$  enriched



Yu-Chen "Janice" Chen (MIT)

arXiv:2312.05084

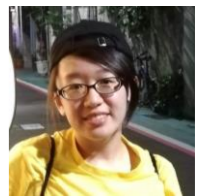
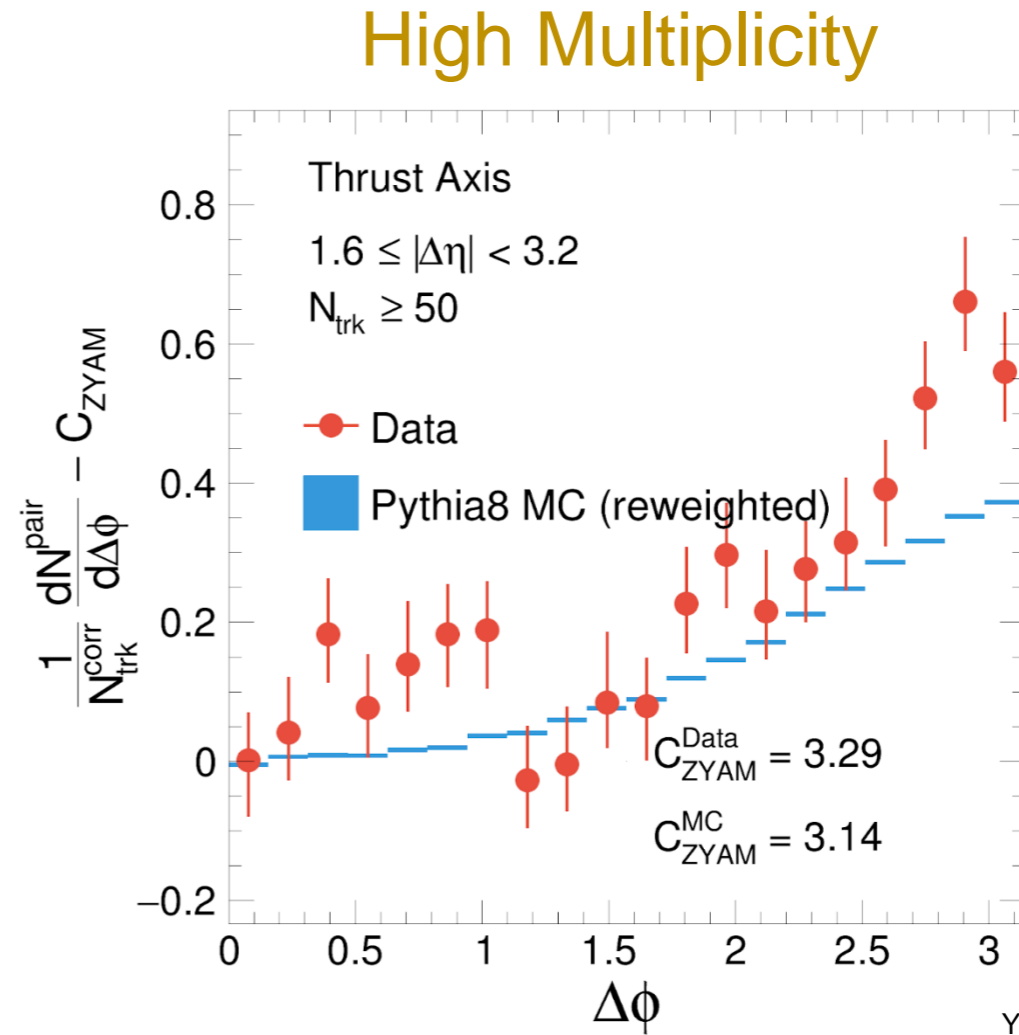
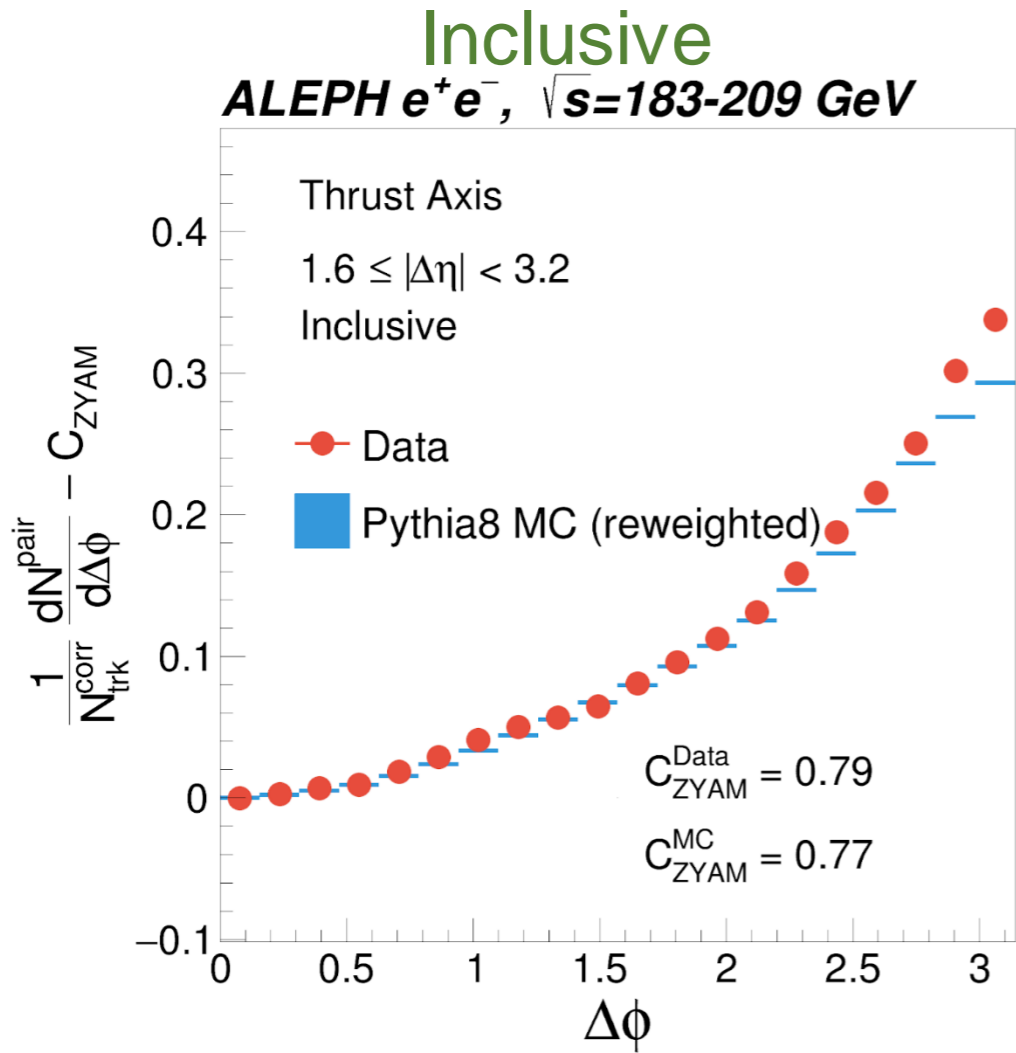
# Additional Cross-checks at High Multiplicity



- Reweight the MC to match the data multiplicity spectrum
- Effect of reweighting is small
- **PYTHIA8 with shoving** changes the correlation function
- Doesn't produce a near-side excess

arXiv:2312.05084

# Comparison to Prediction from PYTHIA8



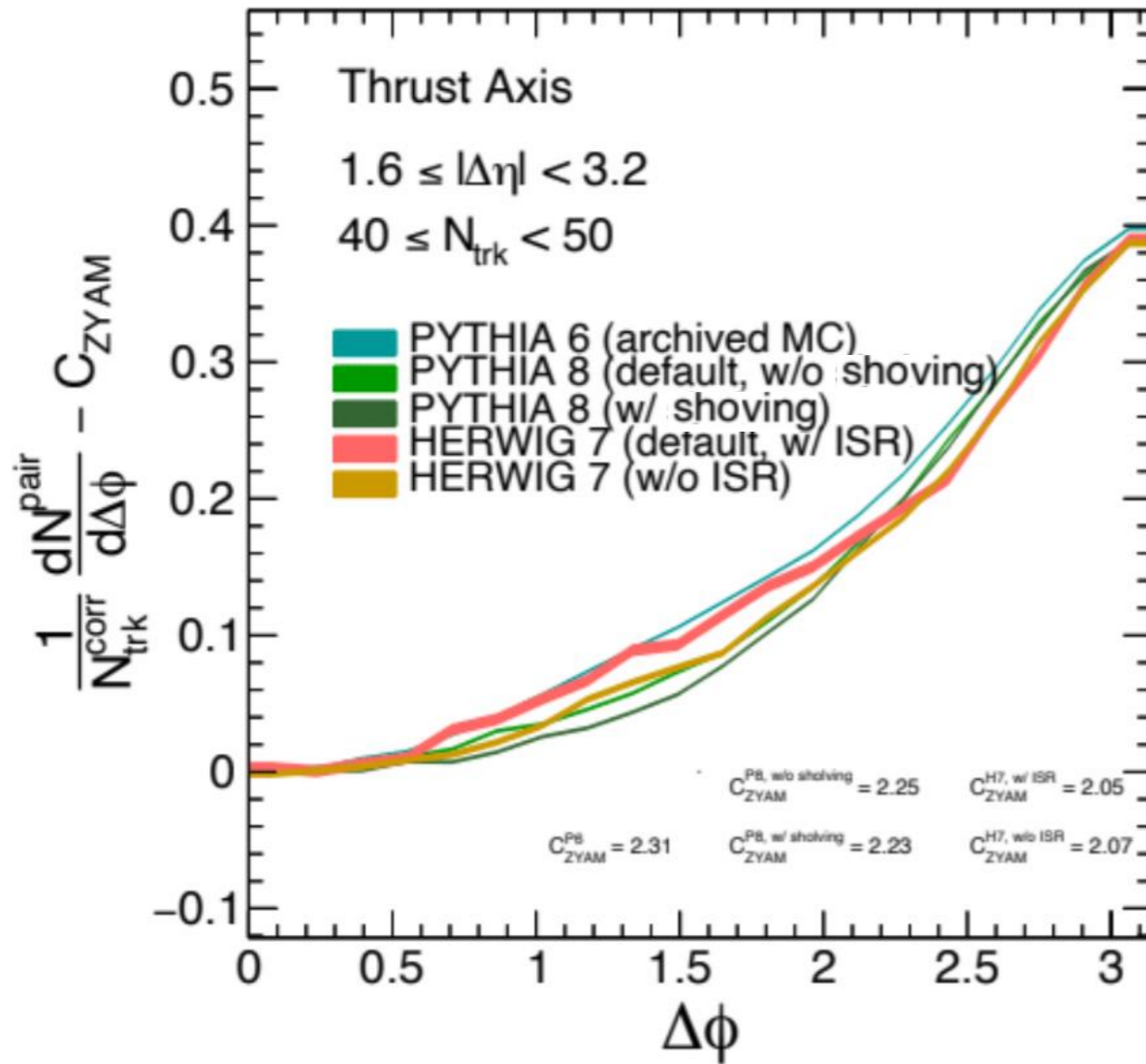
Yu-Chen "Janice" Chen (MIT)

- Smear PYTHIA8 with detector tracking efficiency from archived MC
- Reweight multiplicity to match with data
- **Worse description of the inclusive sample than archived MC**
- No peak structure at  $\Delta\phi \sim 0$

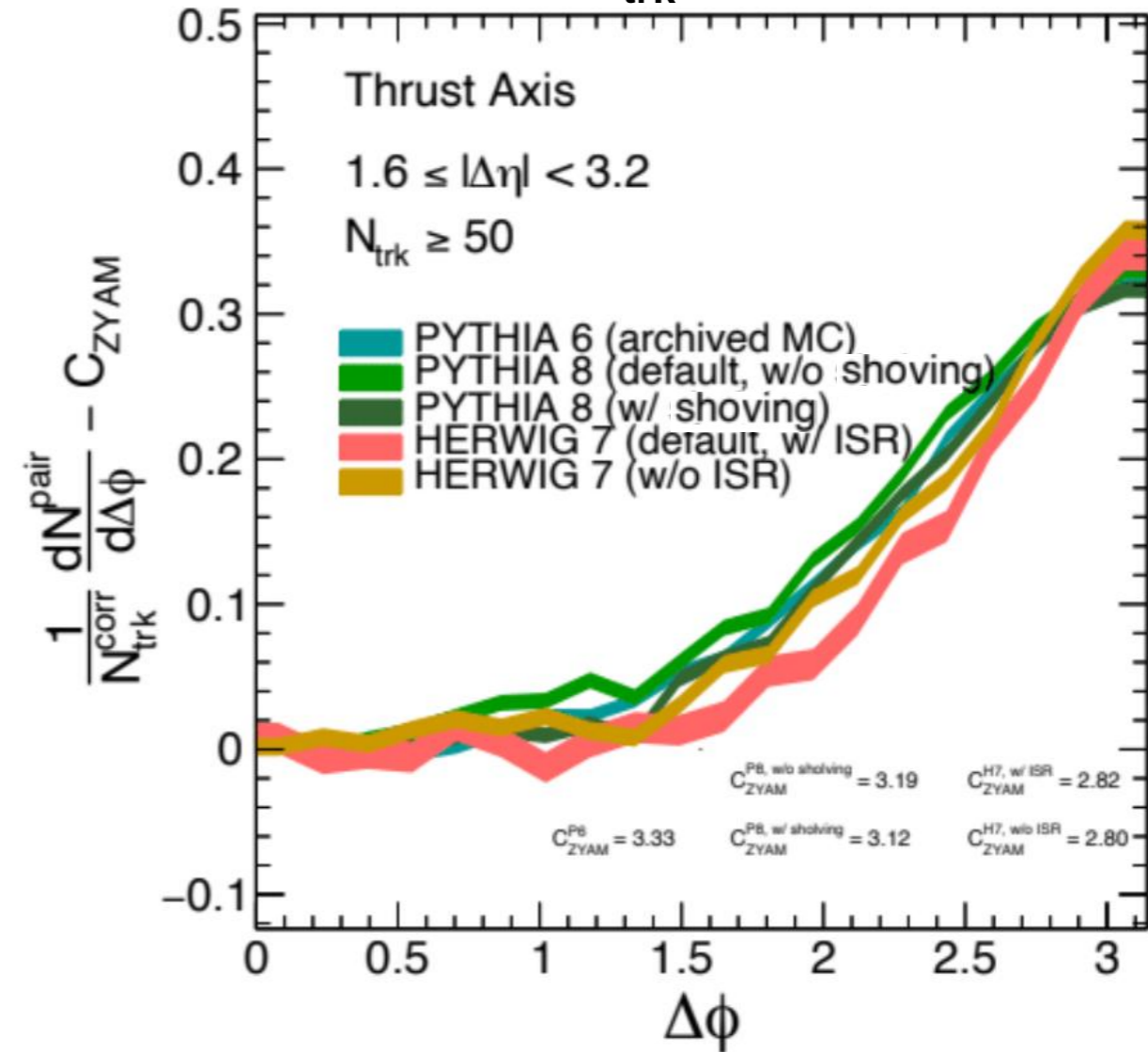
arXiv:2312.05084

# PYTHIA and HERWIG Generator Studies

$40 < N_{\text{trk}} < 50$



$N_{\text{trk}} > 50$



- **HERWIG7** (with or without ISR) and **PYTHIA8** (with or without shoving)
- No near-side enhancement observed

# Associated Yield as a Function of Multiplicity

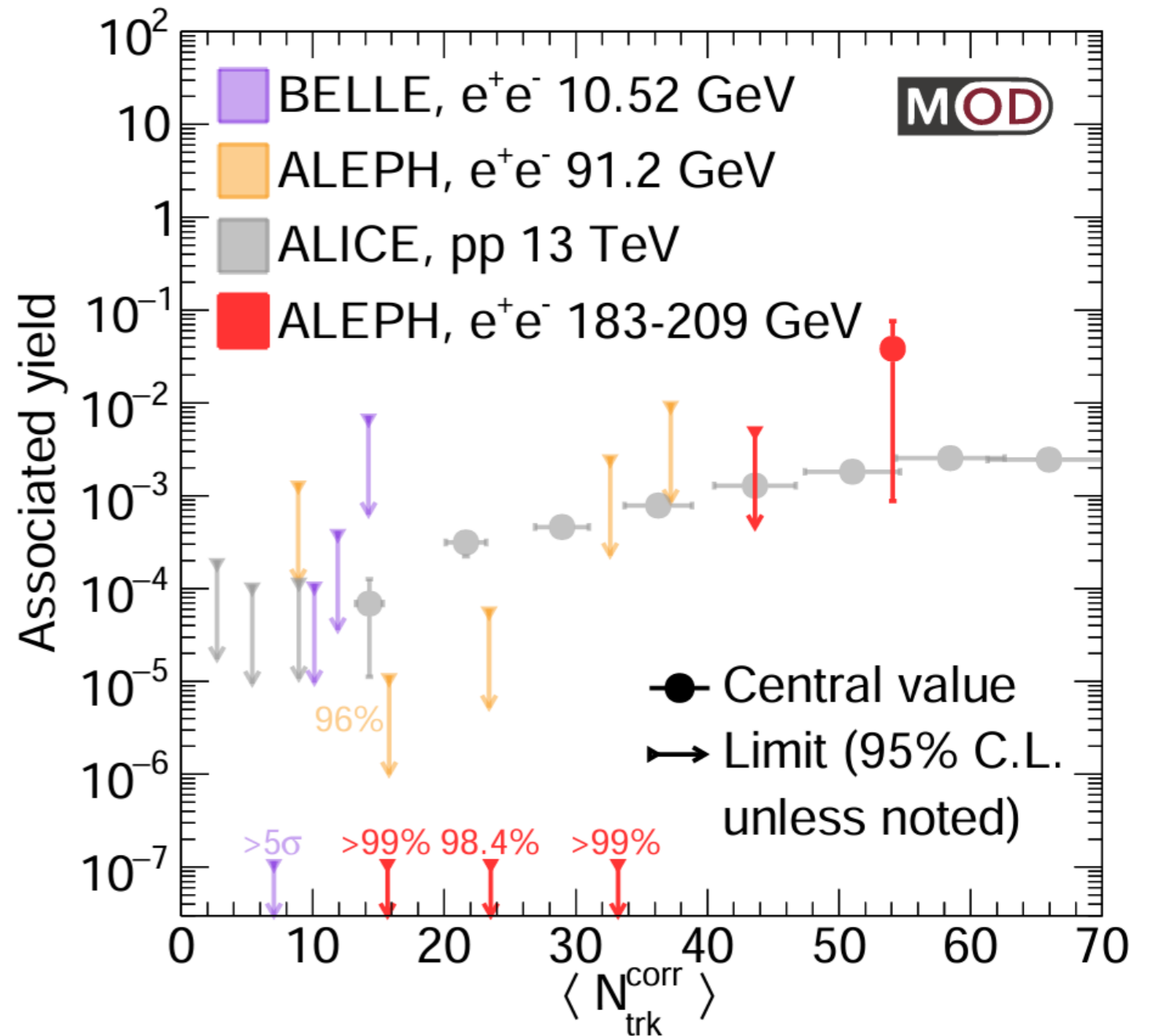
- Very tight upper limit set with **Belle**, **LEP1** and **LEP2** data set at low multiplicity (<40), lower than **ALICE** pp results

See You Zhou's talk

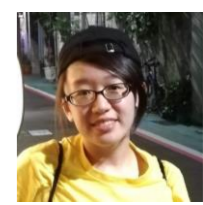
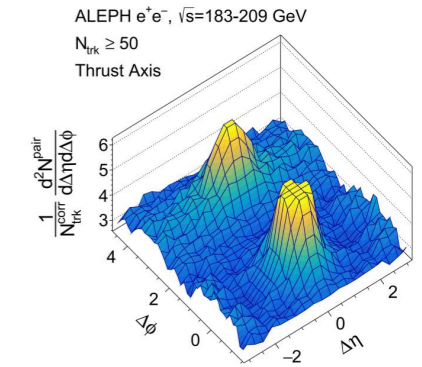
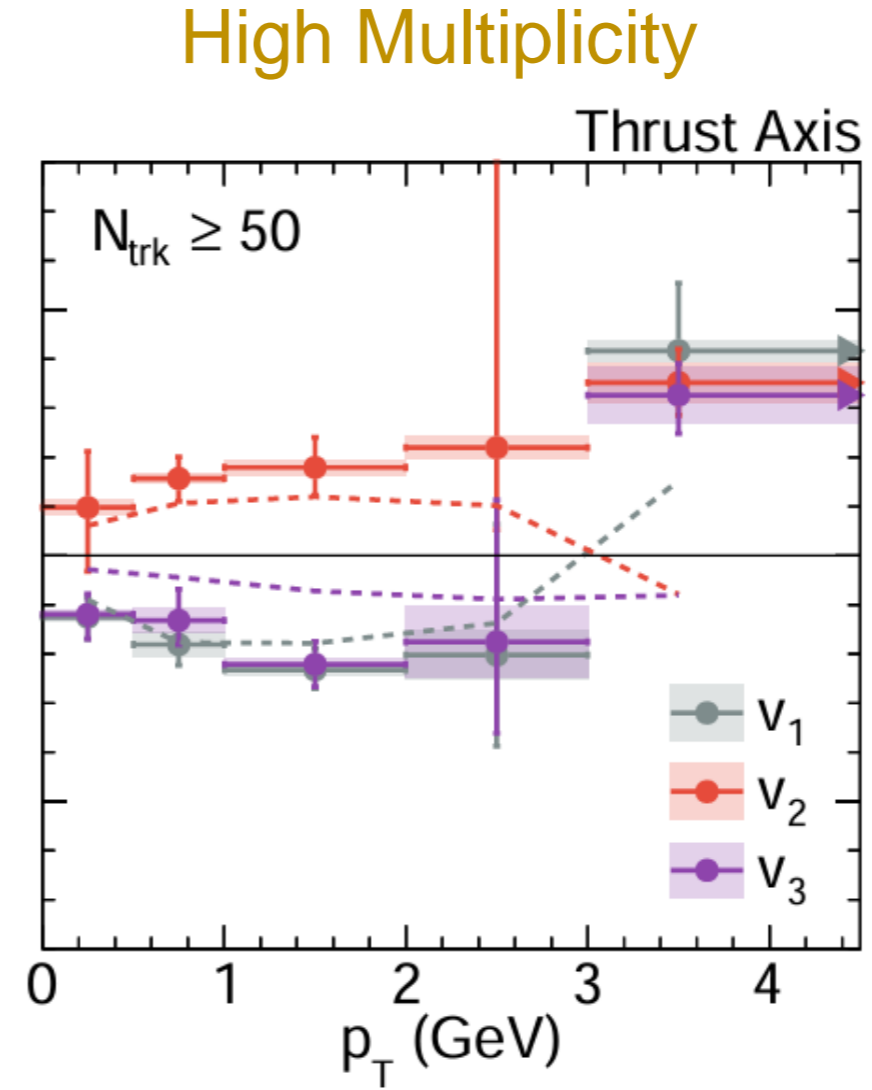
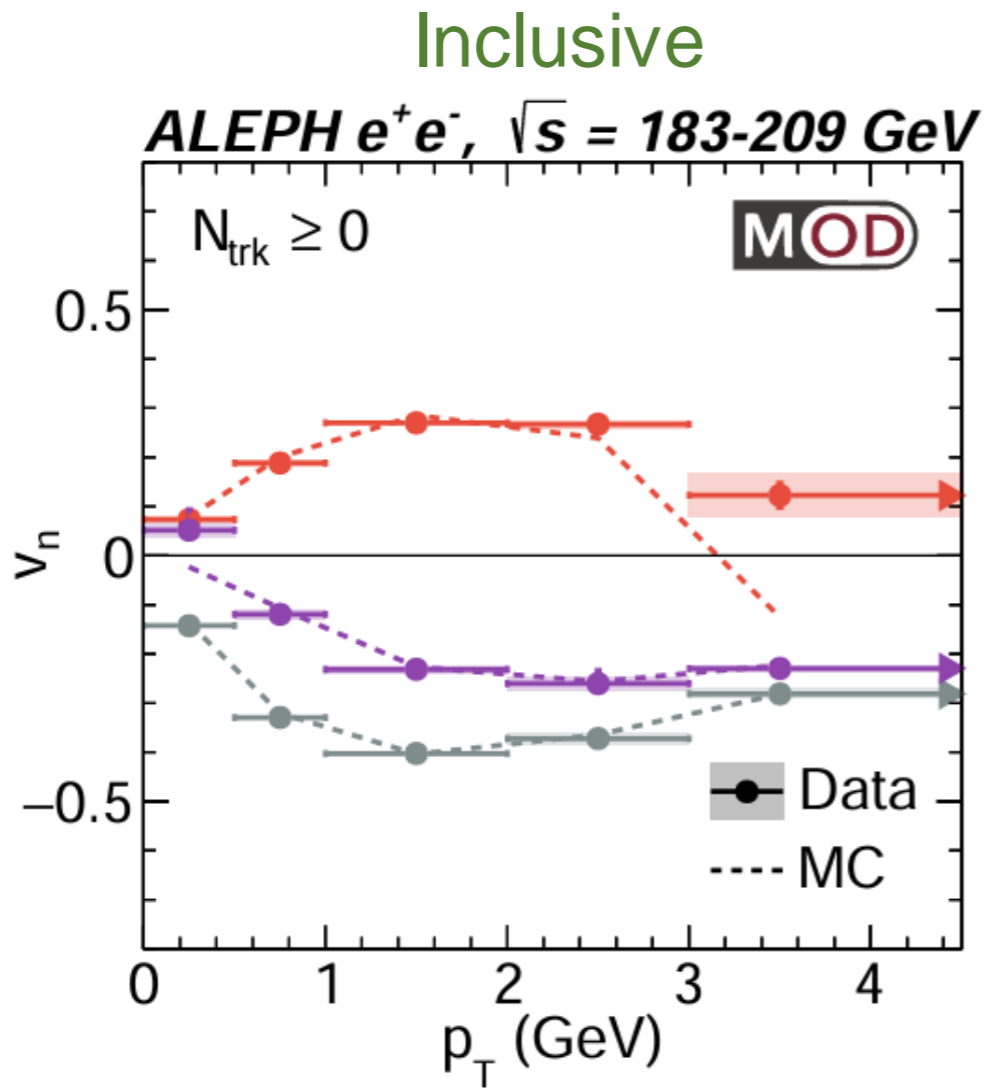
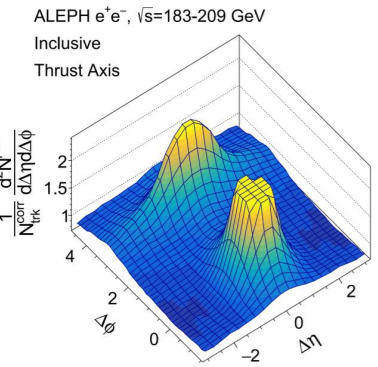
- Indication of an increasing trend at high multiplicity in LEP2 data
- Non-zero central value reported at the highest multiplicity bin with large statistical uncertainty

arXiv:2312.05084

Analysis note: MITHIG-MOD-NOTE-23-011 (arXiv:2309.09874)



# Extracted $v_n$ vs. Charged Particle $p_T$



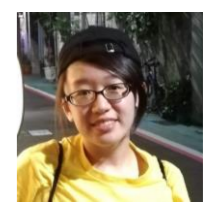
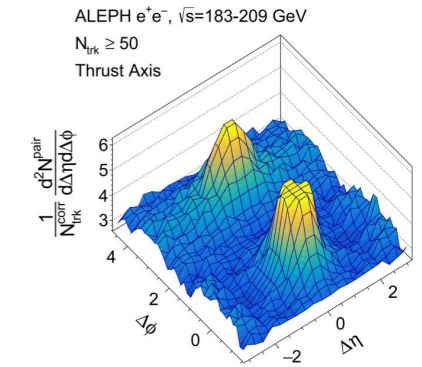
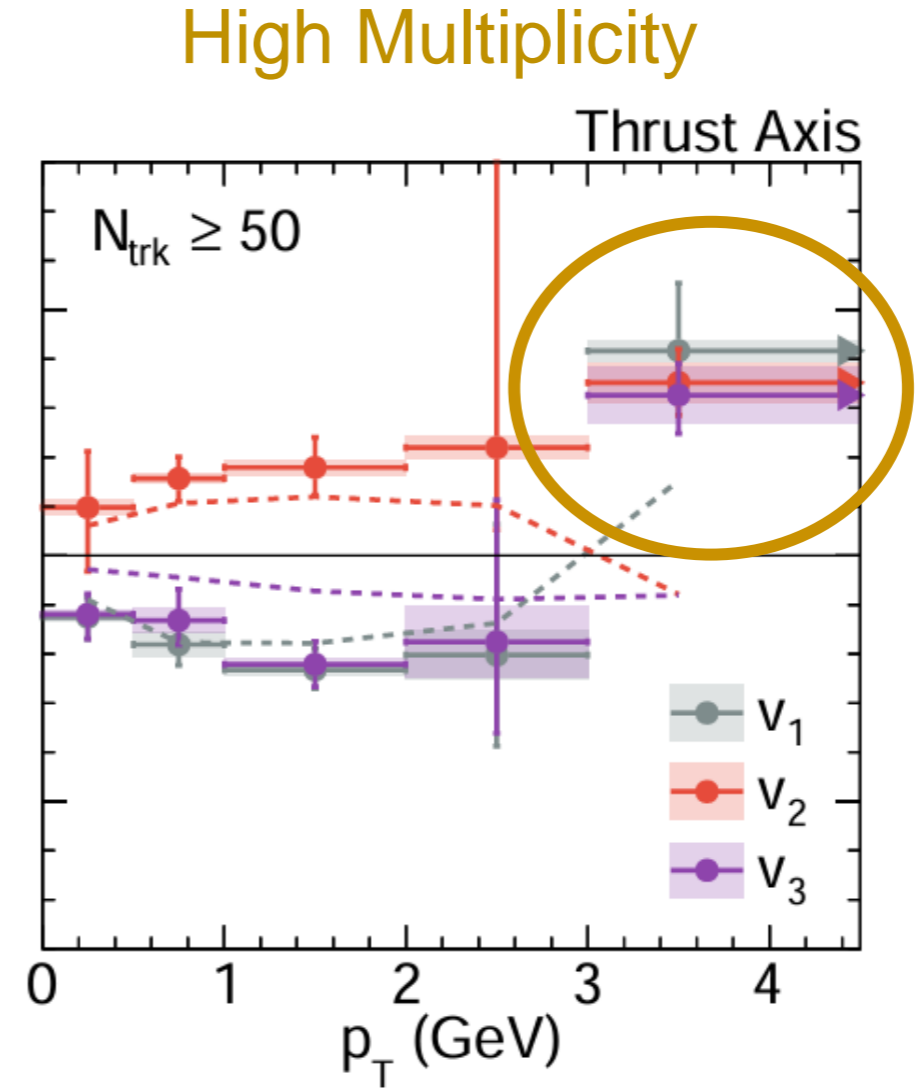
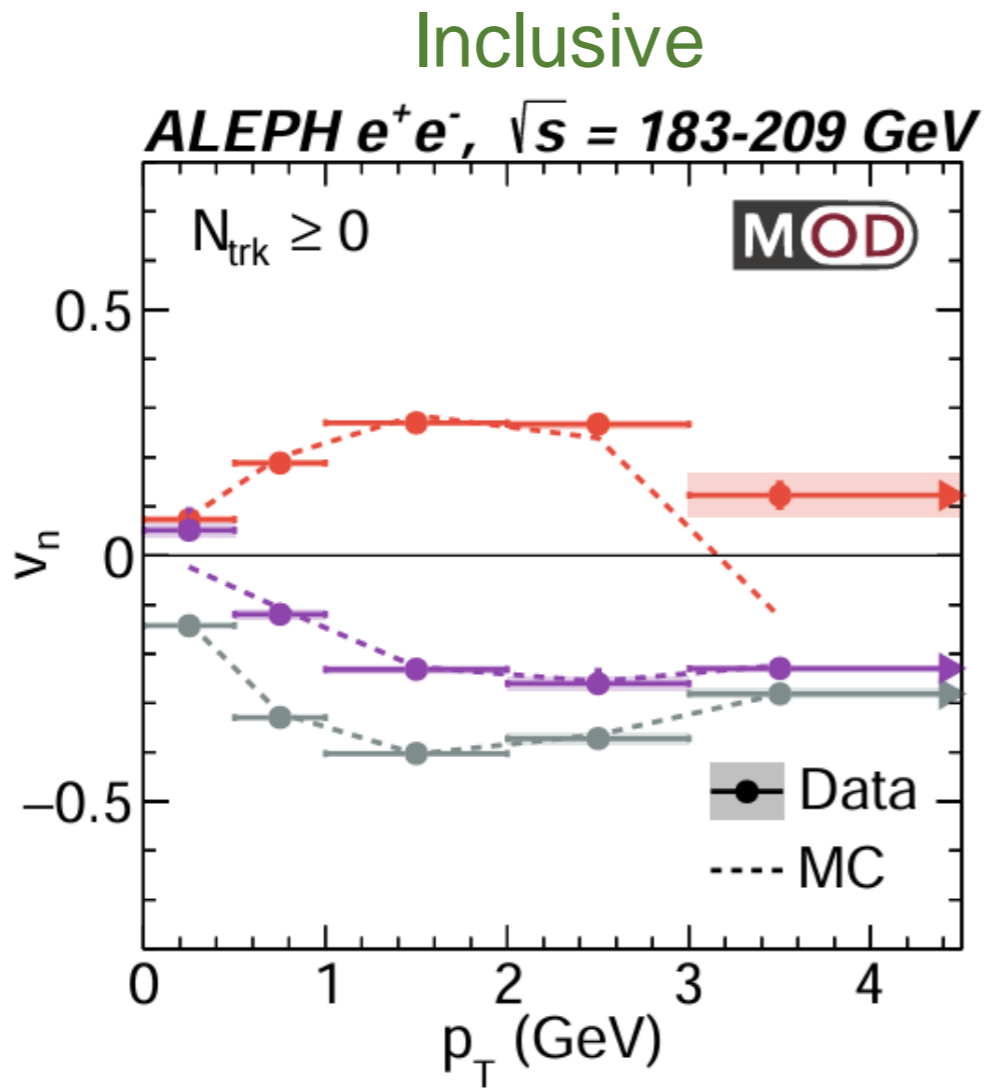
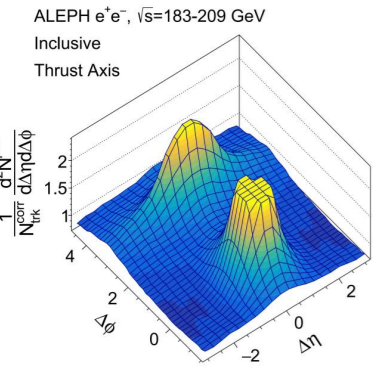
Yu-Chen "Janice" Chen (MIT)

- Reasonable agreement between **Inclusive data** and MC (Left)
- At **High Multiplicity** (Right): Larger  $v_2$  and  $v_3$  magnitudes than MC (dash lines)

arXiv:2312.05084



# Extracted $v_n$ vs. Charged Particle $p_T$



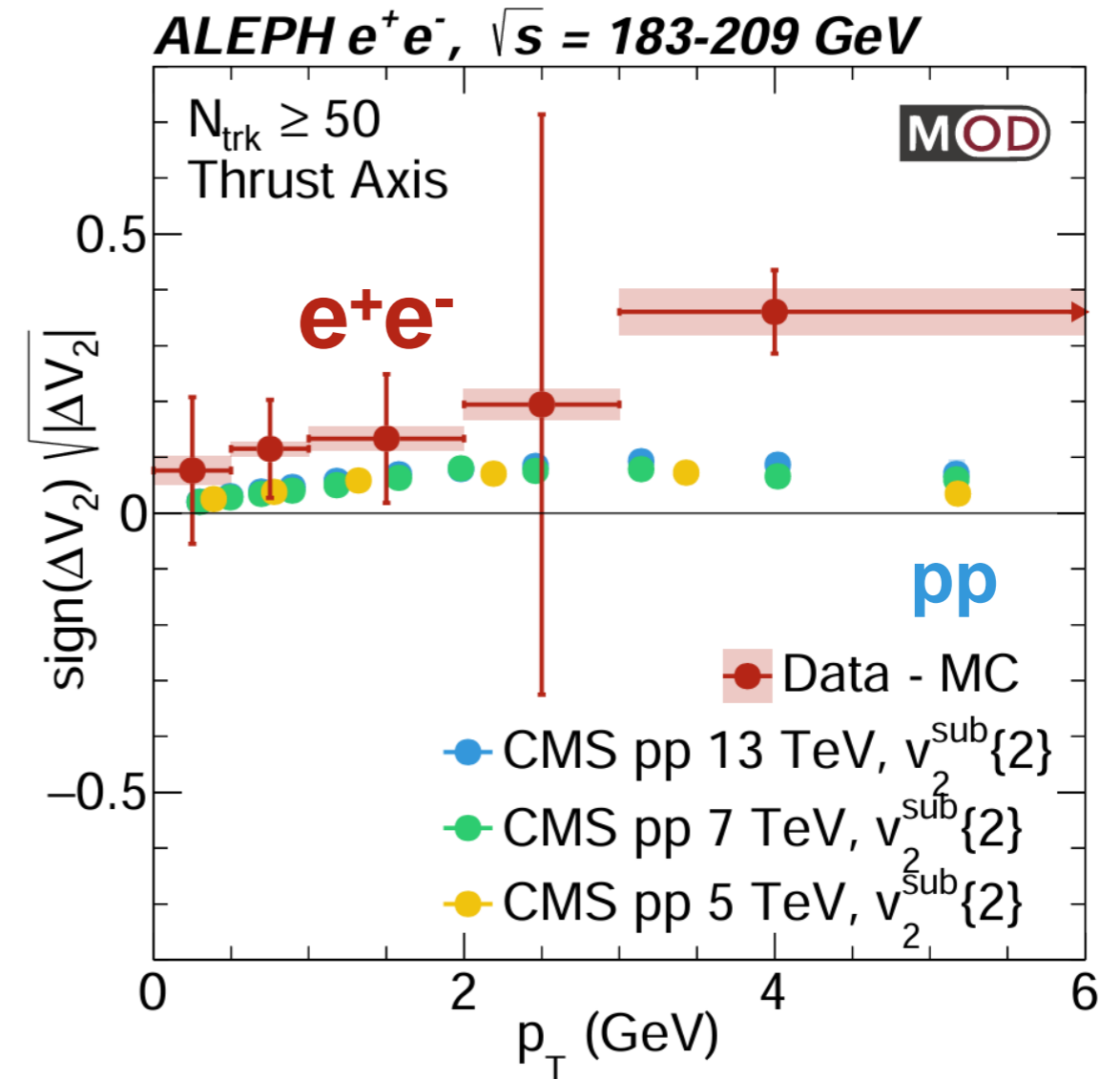
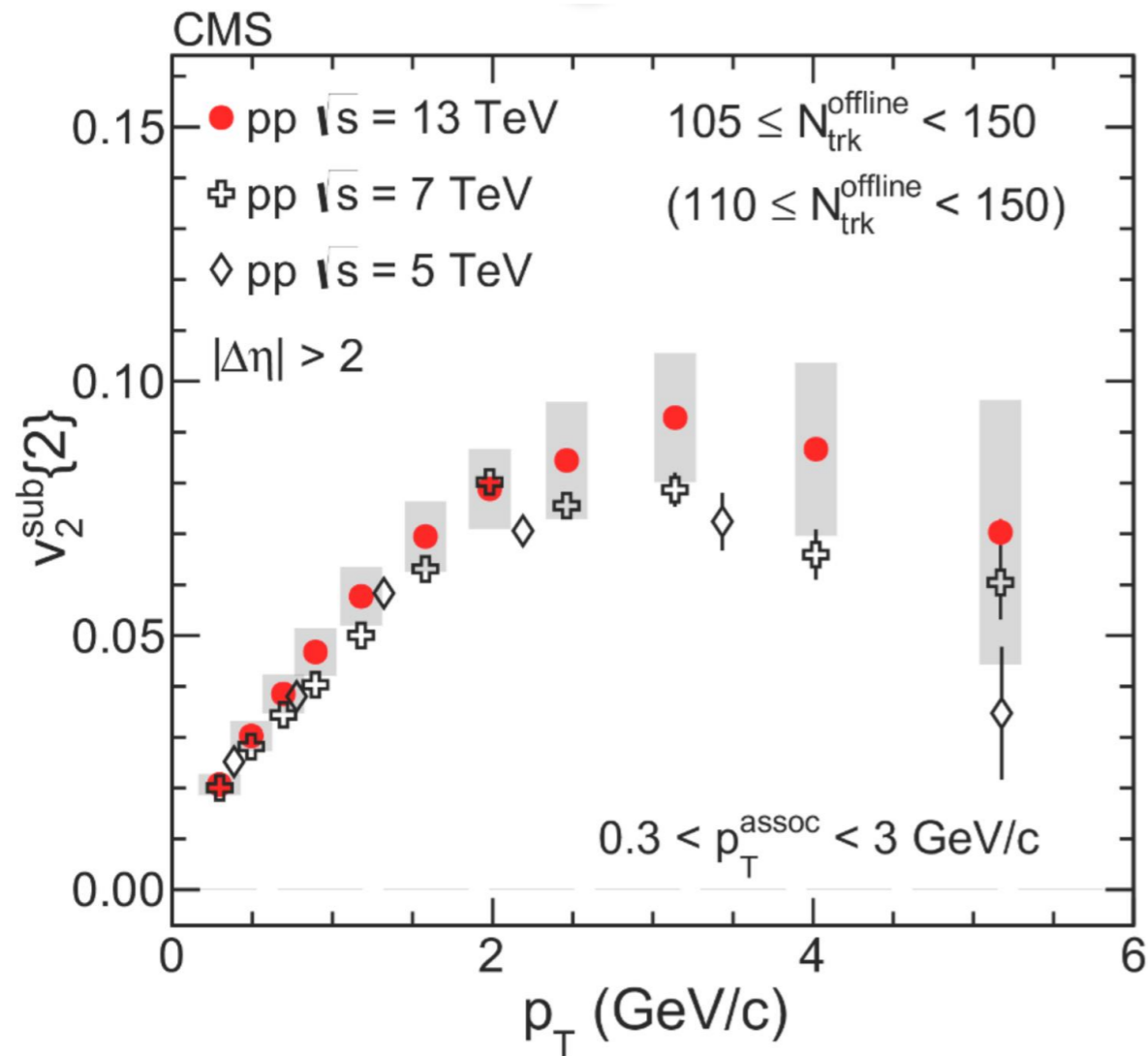
Yu-Chen "Janice" Chen (MIT)

- Reasonable agreement between **Inclusive data** and MC (Left)
- At **High Multiplicity** (Right): Larger  $v_2$  and  $v_3$  magnitudes than MC (dash lines)
- $v_1$ ,  $v_3$  change sign at high  $p_T$

arXiv:2312.05084



# $\Delta v_2$ in $e^+e^-$ Compared to $v_2^{\text{sub}}$ in pp Collisions

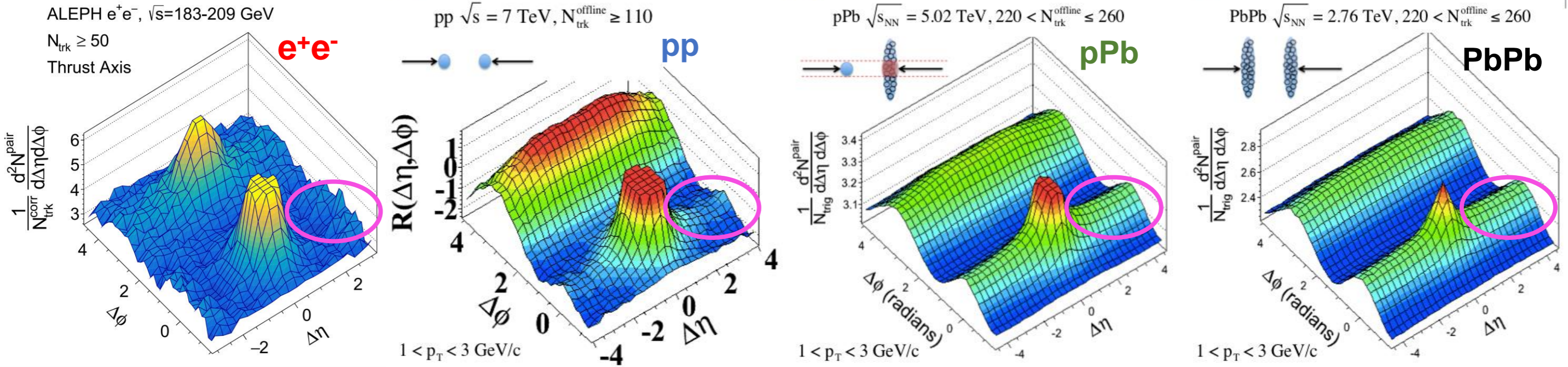


- MC based “Non-flow subtraction”:  $\Delta v_2 = v_2^{\text{Data}} - v_2^{\text{MC}}$
- Similar increasing trend in  $e^+e^-$  and pp data as a function of  $p_T$

arXiv:2312.05084



# Emerging Picture



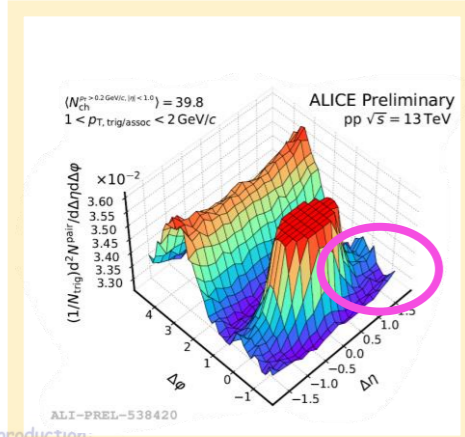
# Emerging Picture

## “Transverse Size” / “MPI”

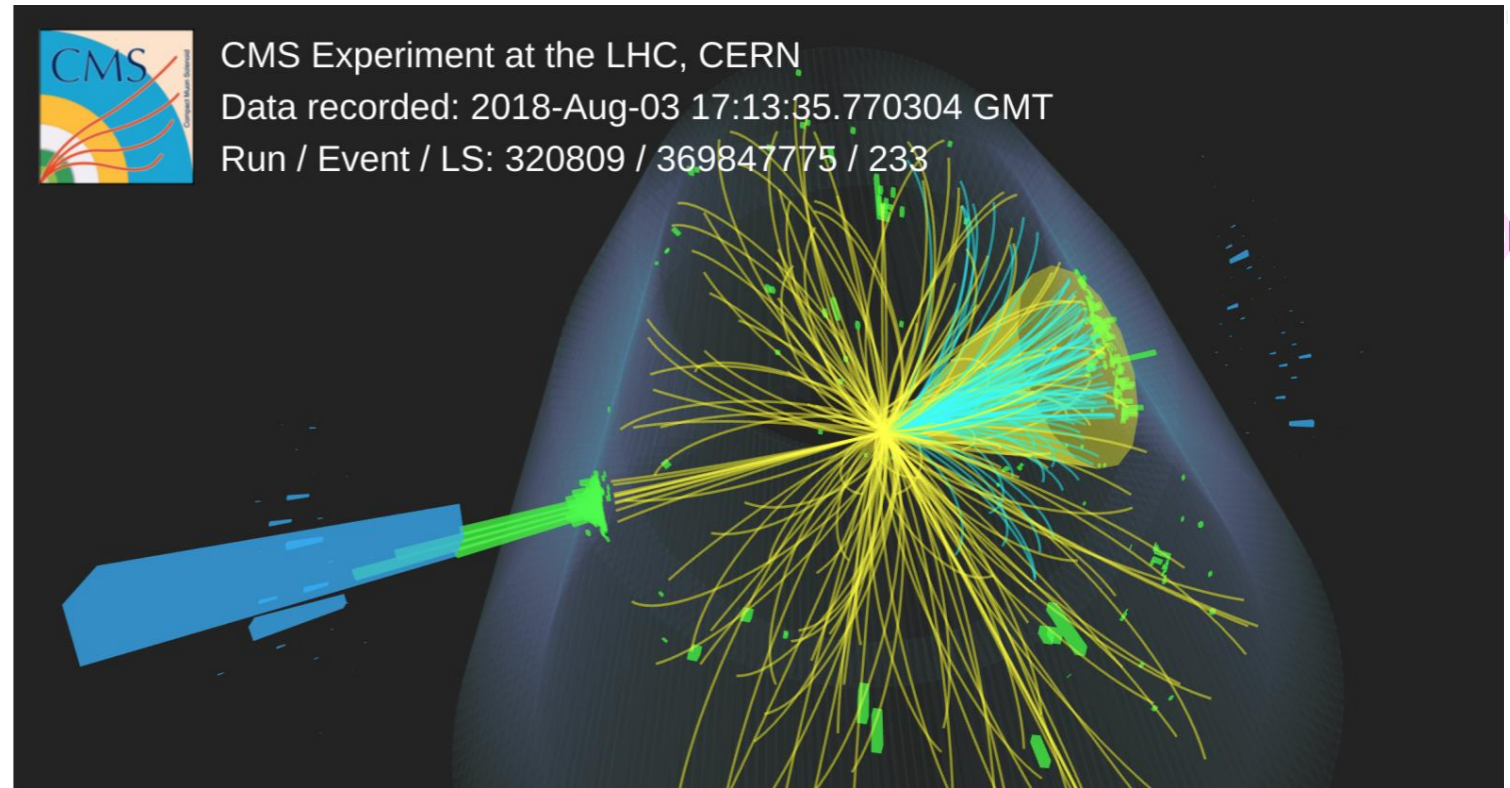
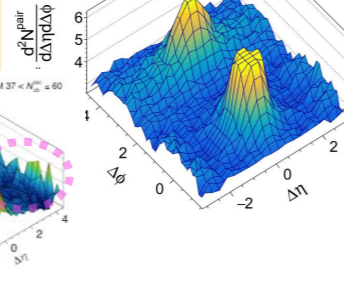
ALICE Low multiplicity pp signal

See You Zhou’s talk

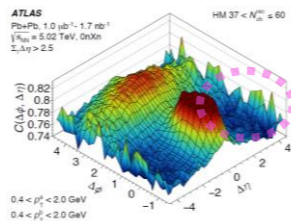
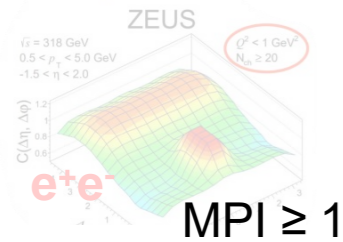
MPI > 1



ALEPH  $e^+e^-$ ,  $\sqrt{s}=183\text{-}209$  GeV  
 $N_{trk} \geq 50$   
Thrust Axis  
 $e^+e^- \rightarrow W+W^-$

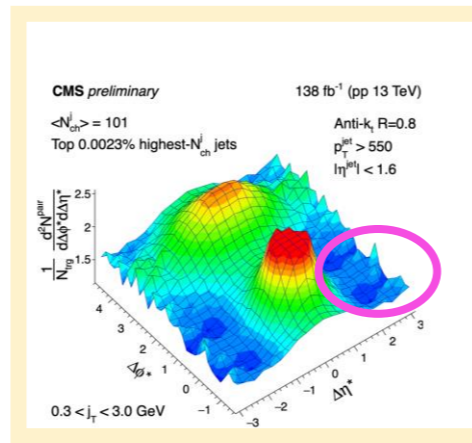
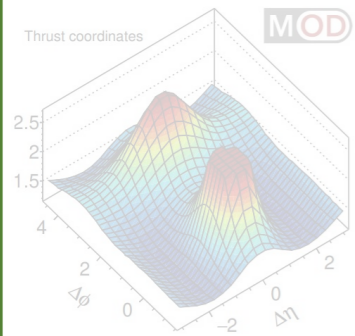


Photoproduction:



Larger MPI than  $\gamma\gamma$

“MPI”=1

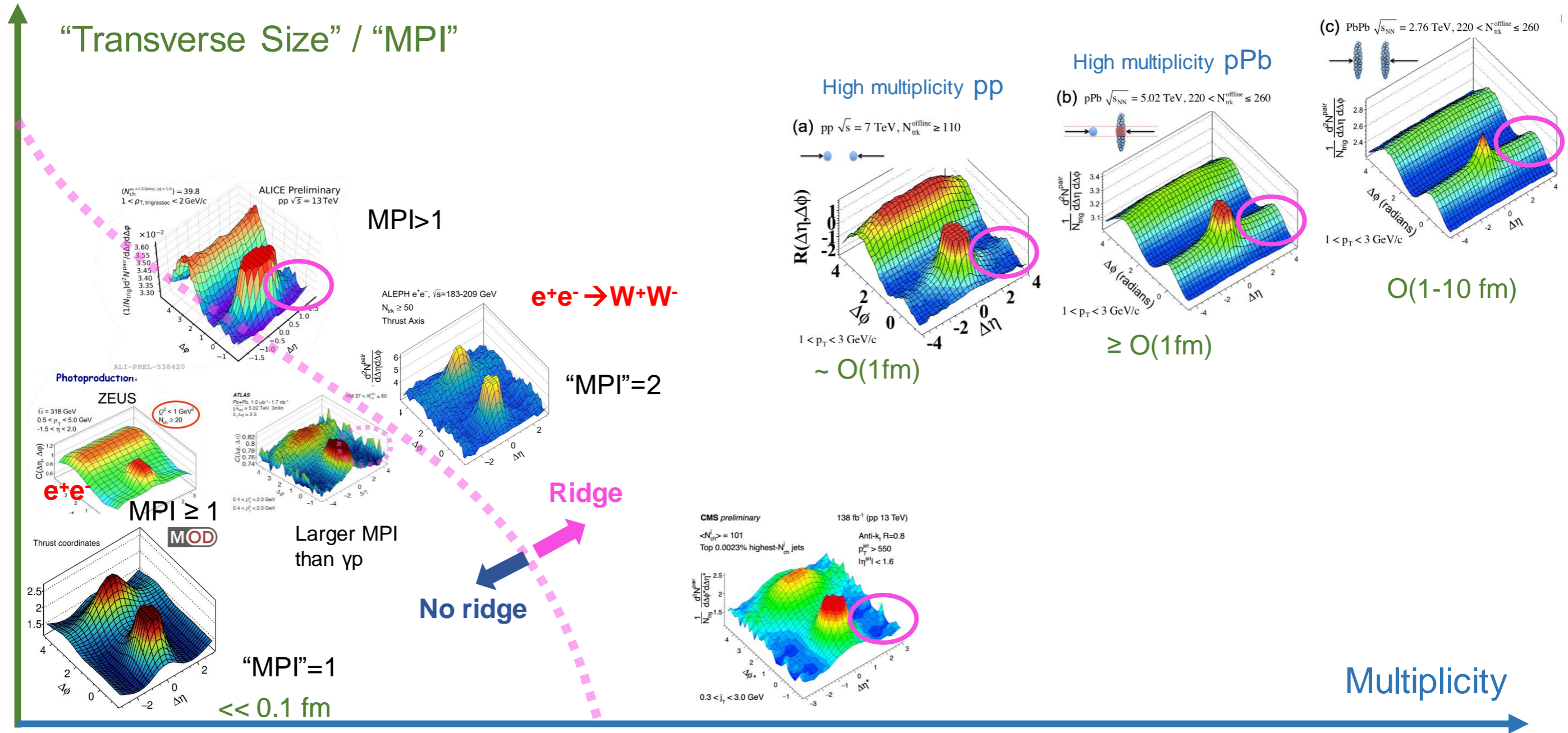


CMS High Multiplicity Jet

See Austin Baty’s talk

Multiplicity

# Emerging Picture (Artist's impression)



# Lessons Learned from Collectivity Searches

- What are the minimum conditions for ridge signal in a small system?

Large MPI and/or multiplicity events help reducing the  $V_{1\Delta}$  and directly reveal the ridge

- Can detectable collectivity arise from final state effects unrelated to the initial state?

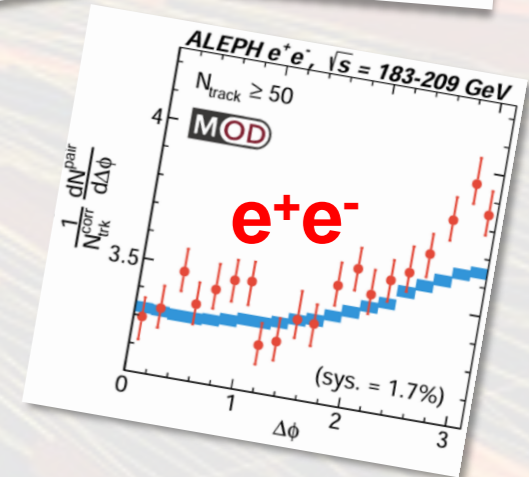
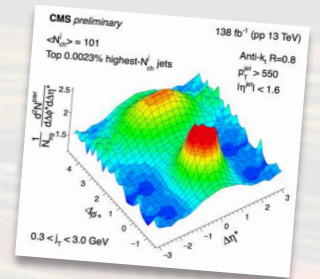
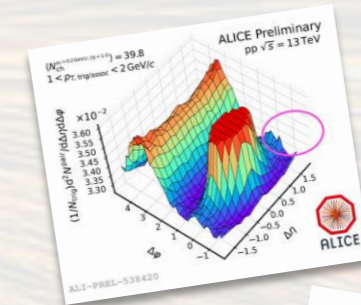
Indication of final state effects from CMS high multiplicity single jet and ALEPH LEP2 data

- How does collectivity vary in different physics processes?

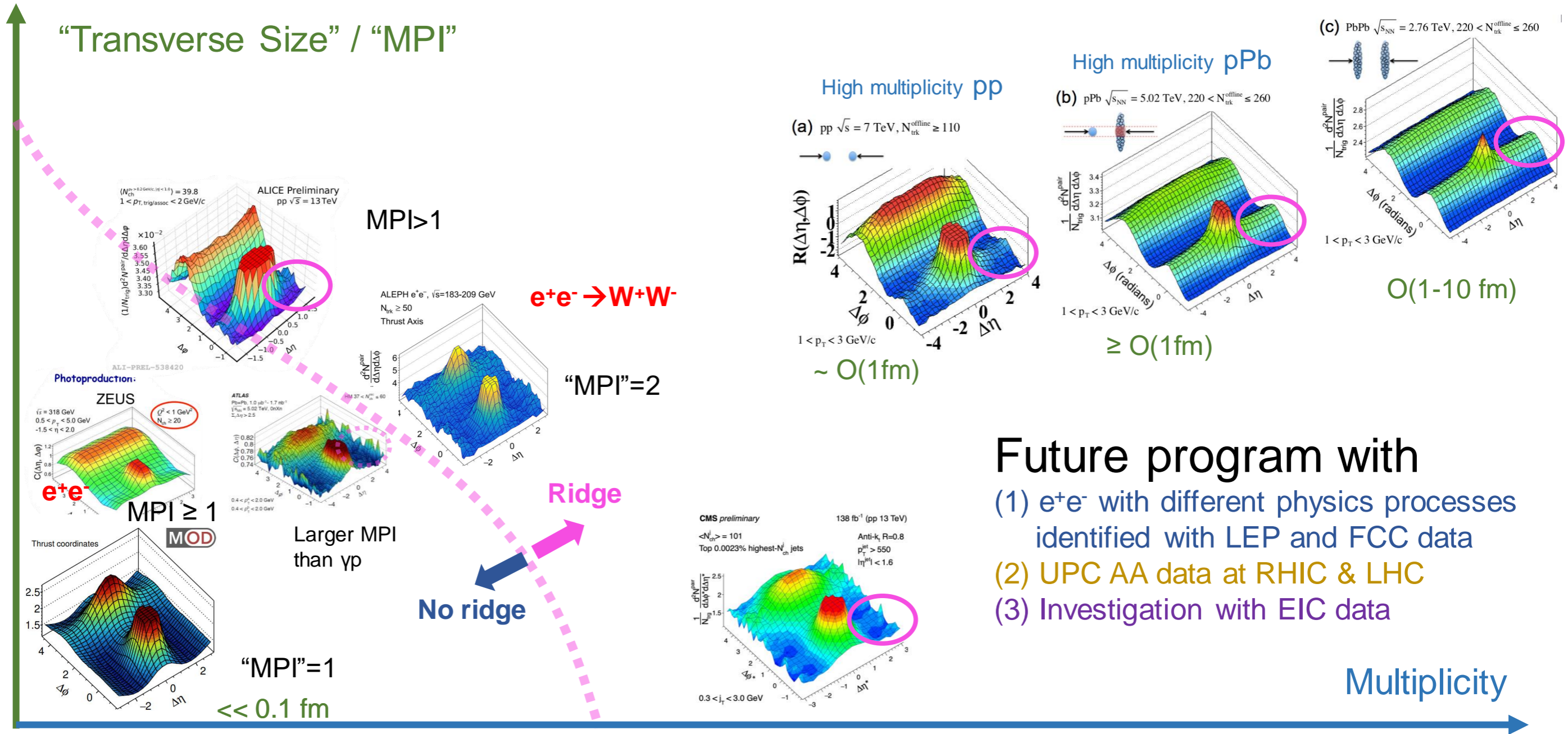
Long-range near-side correlations vary in different physics processes in LEP data

- Is the underlying physics the same in small and large systems?

Data suggest that small systems lacking hadronic initial state effects could still yield a ridge-like signal. Nature of the correlation to be understood.



# Emerging Picture (Artist's impression)

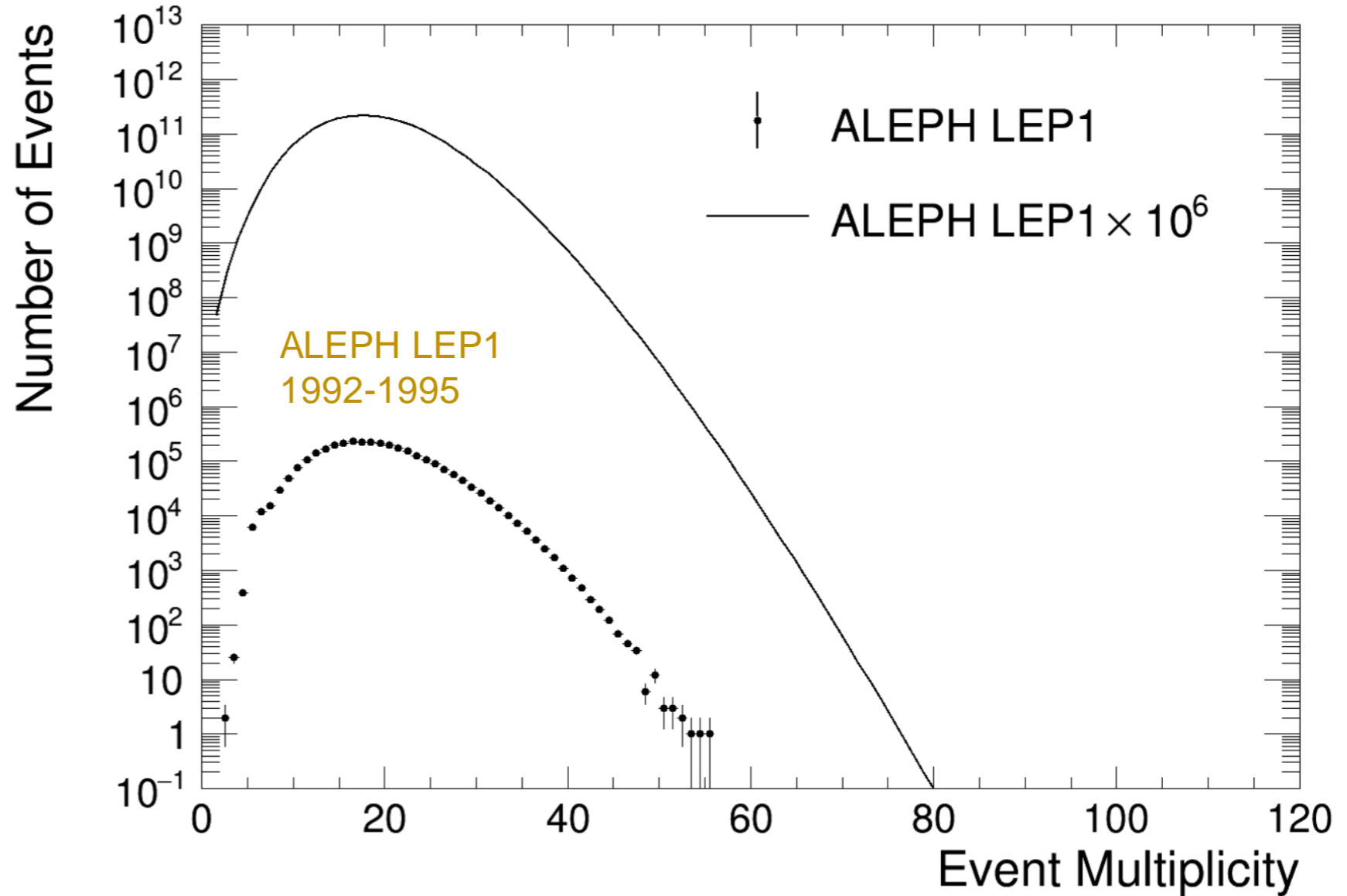
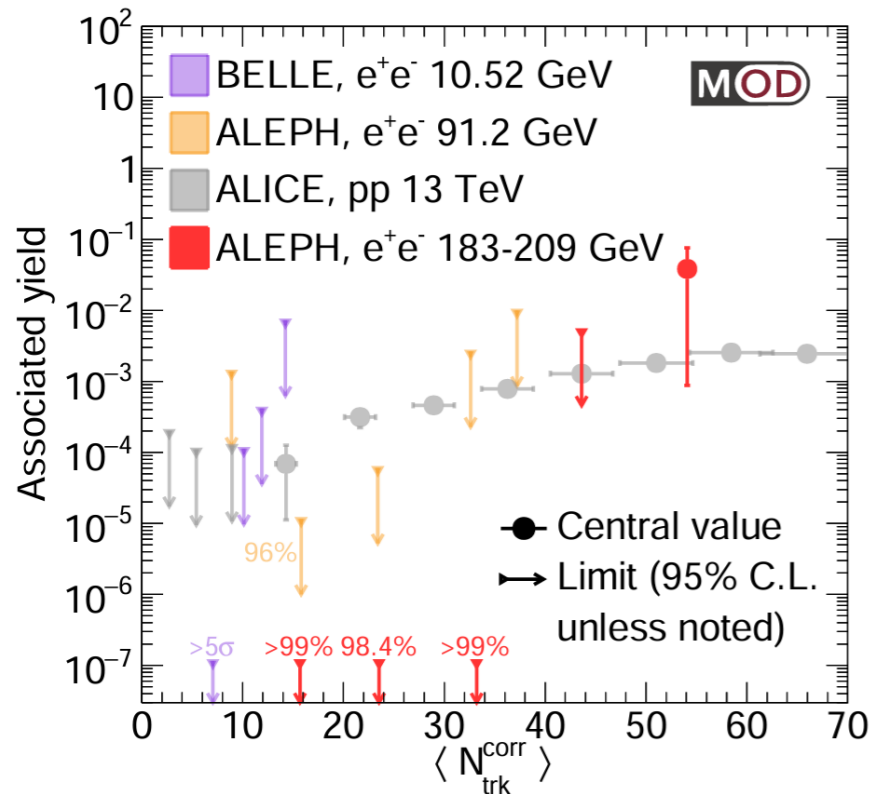


- Future program with**
- (1)  $e^+e^-$  with different physics processes identified with LEP and FCC data
  - (2) UPC AA data at RHIC & LHC
  - (3) Investigation with EIC data



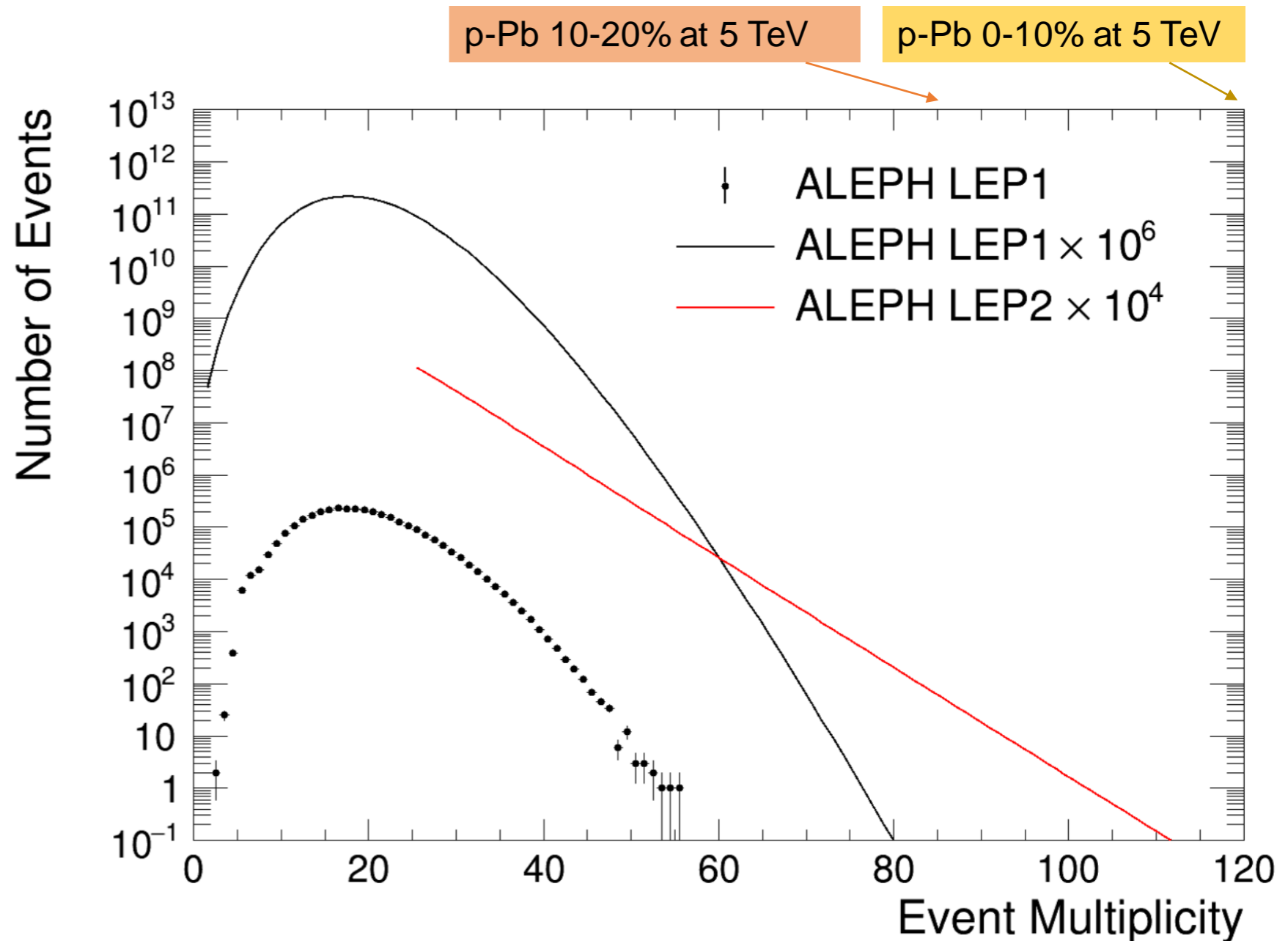
# Projection to FCC-ee

- Estimation with ALEPH archived data
- Extrapolation with NBD fit to the archived data
- Significantly higher reach up to event multiplicity of around 75 particles



# Projection to FCC-ee

- Extrapolation with archived LEP2 data
- Significant increase in multiplicity reach:  
~ **central proton-lead collisions**
- Large statistics will enable new analyses which are not yet accessible:
  - 3-particle and multi-particle correlation analyses
  - Strangeness enhancement
  - Charm baryon to meson ratio enhancement
  - Studies of its process dependence
  - High multiplicity jet substructure
  - High multiplicity event energy-energy-correlators
- ... many other ideas to come!



# Selected List of Analyses

## • $e^+e^-$

- ALEPH LEP1 (91 GeV) [PRL 123 \(2019\) 21, 212002](#)
- ALEPH LEP2 (183-209 GeV): <https://arxiv.org/pdf/2312.05084>
- Belle Off-resonance (10.52 GeV) : [PRL 128 \(2022\) 14, 142005](#)
- Belle On-resonance (Y(4S)): [JHEP 03 \(2023\) 171](#)

## • $\gamma p$

- CMS pPb photonuclear: [PLB 844 \(2023\) 137905](#)
- ZEUS ep neutral current DIS: [JHEP 04 \(2020\) 070](#)
- ZEUS ep photonuclear: [JHEP 12 \(2021\) 102](#)
- H1 ep neutral current DIS: (preliminary) [H1prelim-20-033](#)

## • $\gamma Pb$

- ATLAS PbPb photonuclear: [PRC 104 \(2021\) 1, 014903](#)

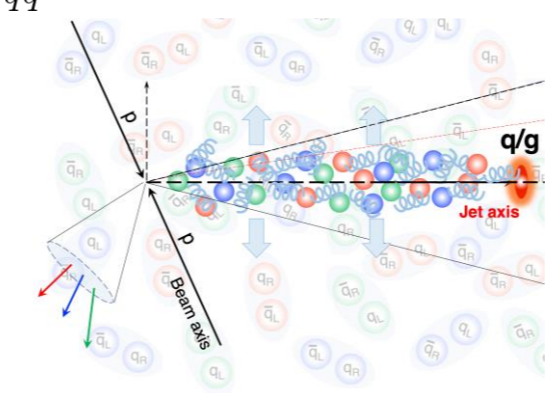
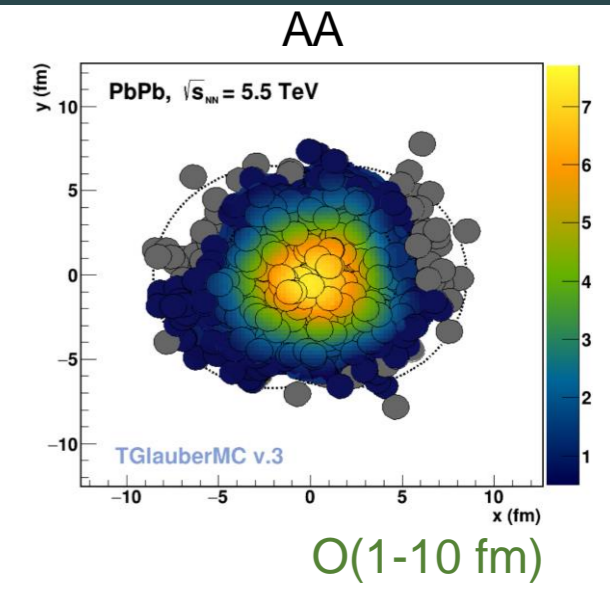
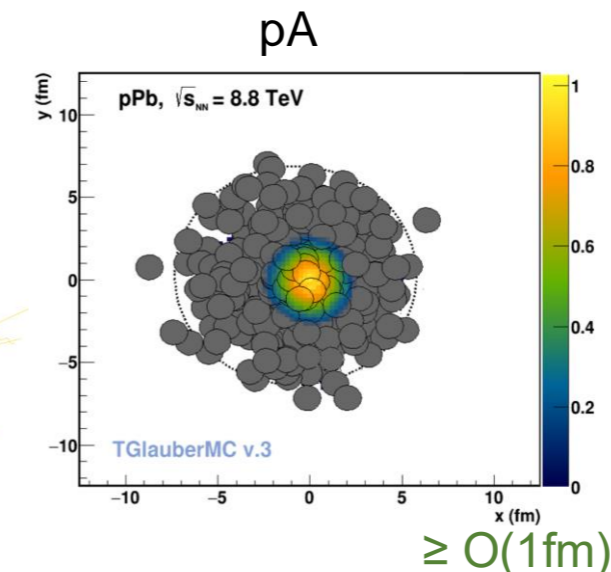
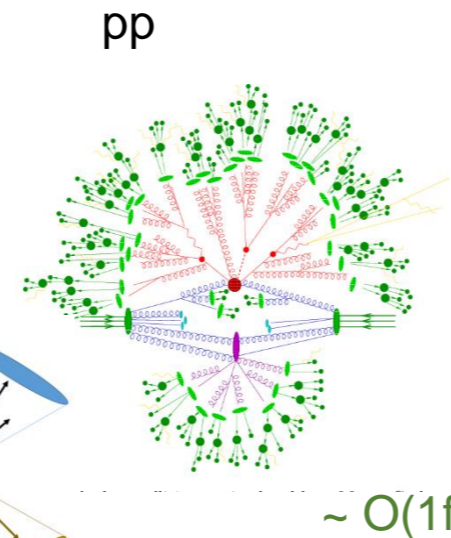
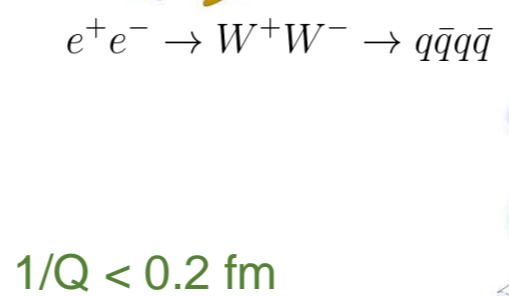
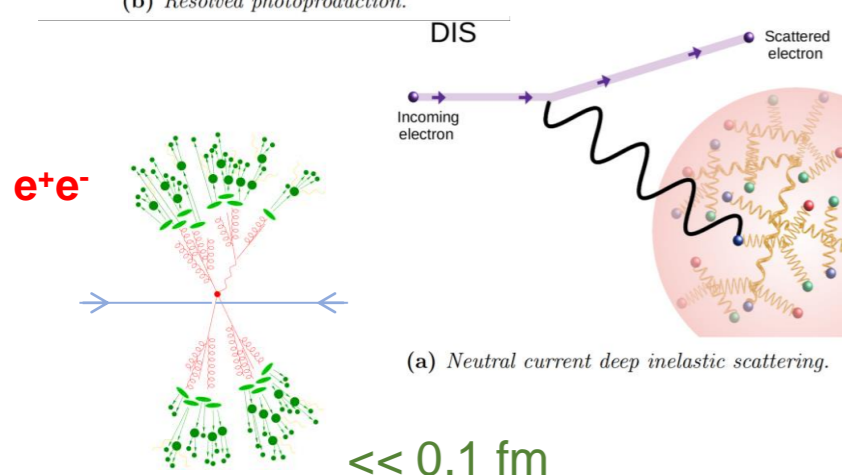
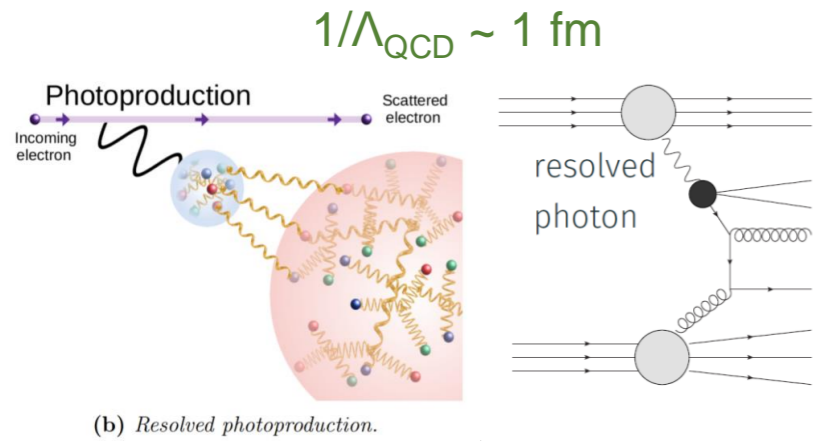
## • pp

- ALICE MB: <https://arxiv.org/pdf/2311.14357.pdf>
- CMS Single Jet in pp: [CMS-HIN-21-013 arXiv:2312.17103](#)



# System Size

“Transverse Size” / “MPI”

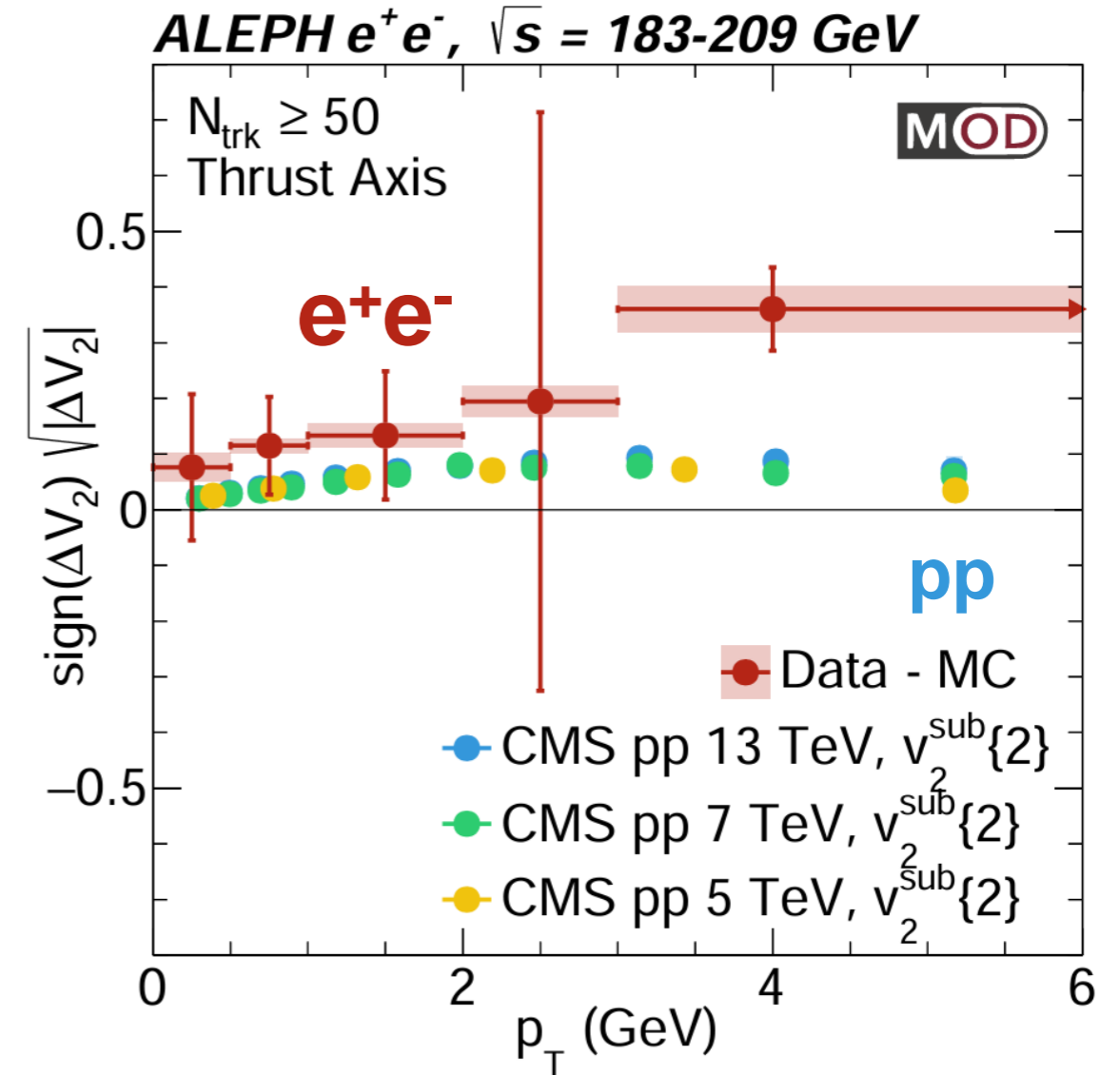
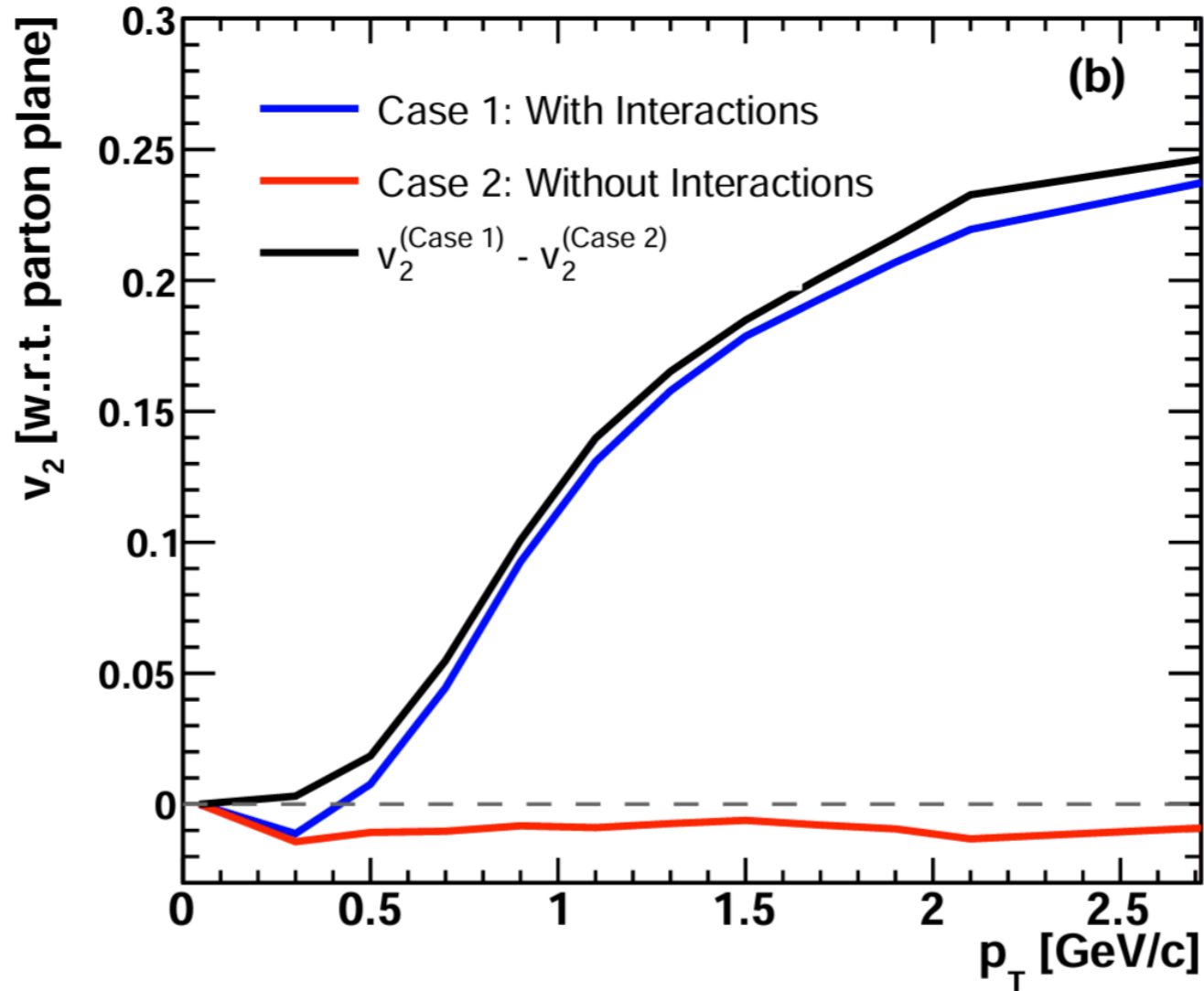


Multiplicity

# Backup Slides



# $\Delta v_2$ in $e^+e^-$



- MC based “Non-flow subtraction”:  $\Delta v_2 = v_2^{\text{Data}} - v_2^{\text{MC}}$

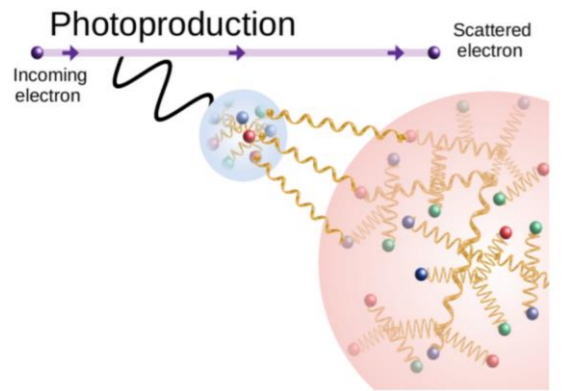
J. Nagle et al, PRC 97 (2018) 2, 024909

arXiv:2312.05084

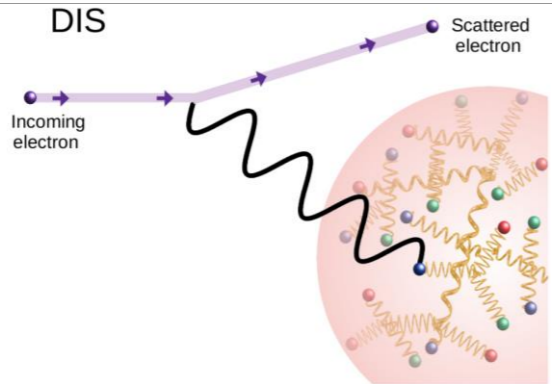
# System Size

“Transverse Size” / MPI

$$1/\Lambda_{\text{QCD}} \sim 1 \text{ fm}$$



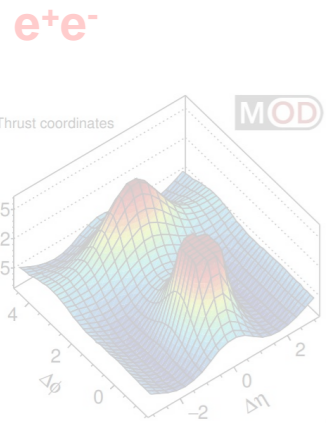
(b) Resolved photoproduction.



(a) Neutral current deep inelastic scattering.

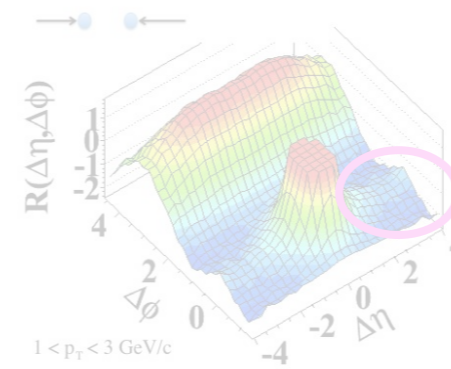
$$1/Q < 0.2 \text{ fm}$$

$\ll 0.1 \text{ fm}$



High multiplicity pp

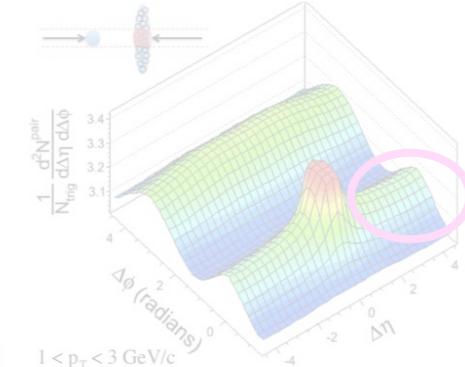
(a) pp  $\sqrt{s} = 7 \text{ TeV}$ ,  $N_{\text{ch}}^{\text{offline}} \geq 110$



$\sim O(1 \text{ fm})$

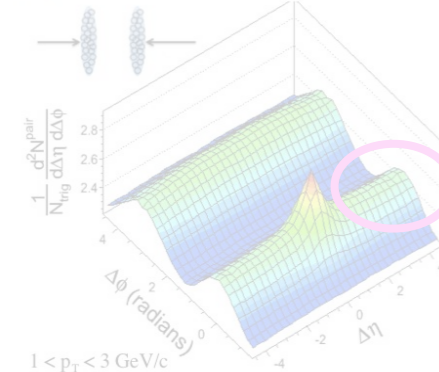
High multiplicity pPb

(b) pPb  $\sqrt{s_{\text{NN}}} = 5.02 \text{ TeV}$ ,  $220 < N_{\text{ch}}^{\text{offline}} \leq 260$



$\geq O(1 \text{ fm})$

(c) PbPb  $\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV}$ ,  $220 < N_{\text{ch}}^{\text{offline}} \leq 260$

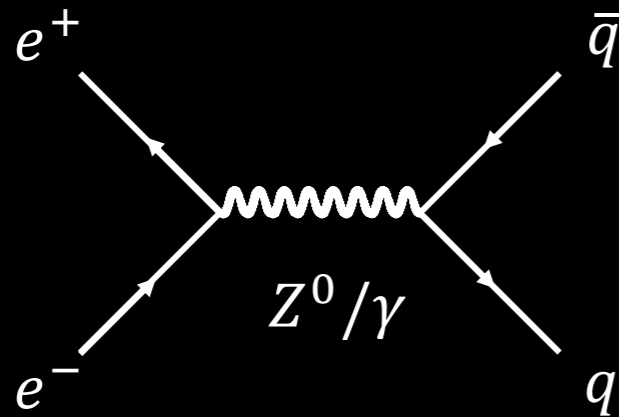


$O(1-10 \text{ fm})$

Multiplicity

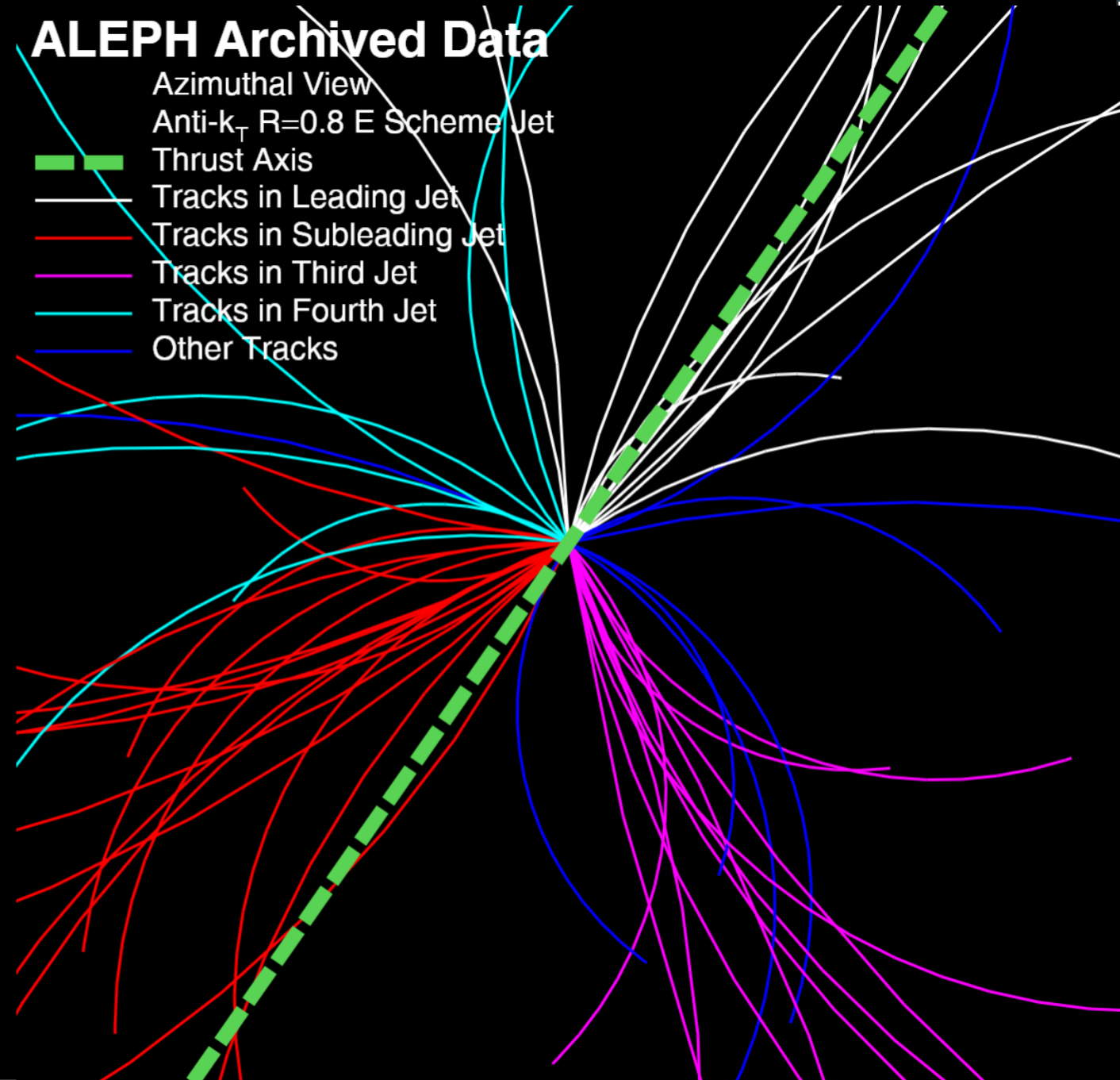
# High Multiplicity Event in $e^+e^-$ Collisions in LEP1

Highest multiplicity event in ALEPH LEP1 data  
Collision Energy = 91 GeV



## ALEPH Archived Data

- Azimuthal View
- Anti- $k_T$   $R=0.8$  E Scheme Jet
- Thrust Axis
- Tracks in Leading Jet
- Tracks in Subleading Jet
- Tracks in Third Jet
- Tracks in Fourth Jet
- Other Tracks



Anthony Badea Austin Baty Chris McGinn Michael Peters Jesse Thaler Gian Michele Innocenti Paoti Chang Tzu-An Sheng

+ YJL

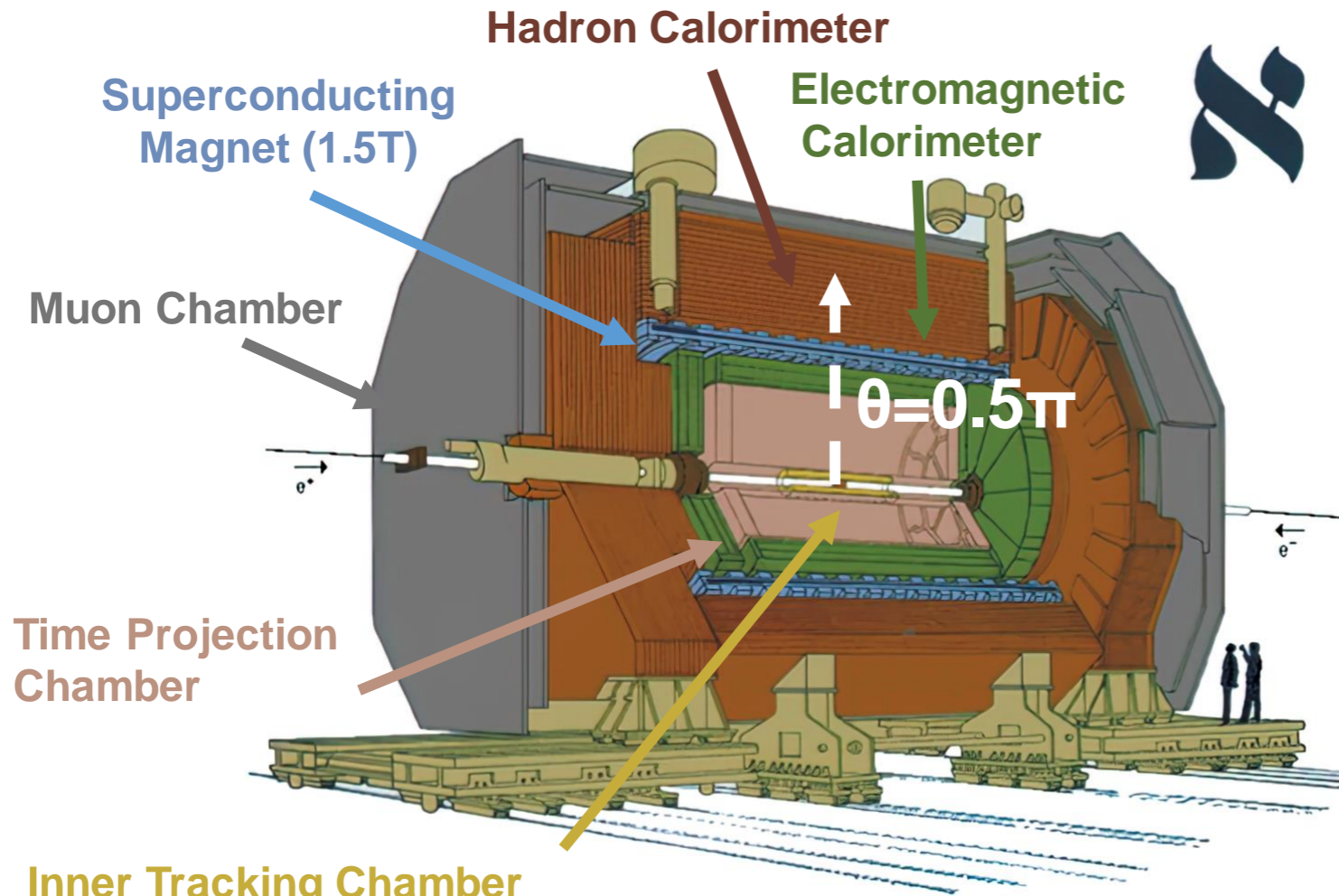
arXiv: 1906.00489  
PRL 123, 212002 (2019)

55 Charged Particles  
Thrust  $T=0.71$

# Hadronic Event Selection

- **Track Selection:**
  - Particle Flow Candidate 0, 1, 2
  - Number of TPC hits for a charged tracks  $\geq 4$
  - $|d_0| < 2$  cm
  - $|z_0| < 10$  cm
  - $|\cos\theta| < 0.94$
  - $p_T > 0.2$  GeV (transverse momentum with respect to beam axis)
  - $N_{\text{TPC}} \geq 4$
  - $\chi^2/\text{ndf} < 1000$ .
- **Neutral Hadron Selection:**
  - Particle Flow Candidate 4, 5 (ECAL / HCAL object)
  - $E > 0.4$  GeV
  - $|\cos\theta| < 0.98$
- **Event Selection:**
  - Number of good charged particles  $\geq 5$  (including charged hadrons and leptons)
  - Number of good ch+neu. Particles  $\geq 13$
  - $E_{\text{charged}} > 15$  GeV
  - $|\cos(\theta_{\text{sphericity}})| < 0.82$

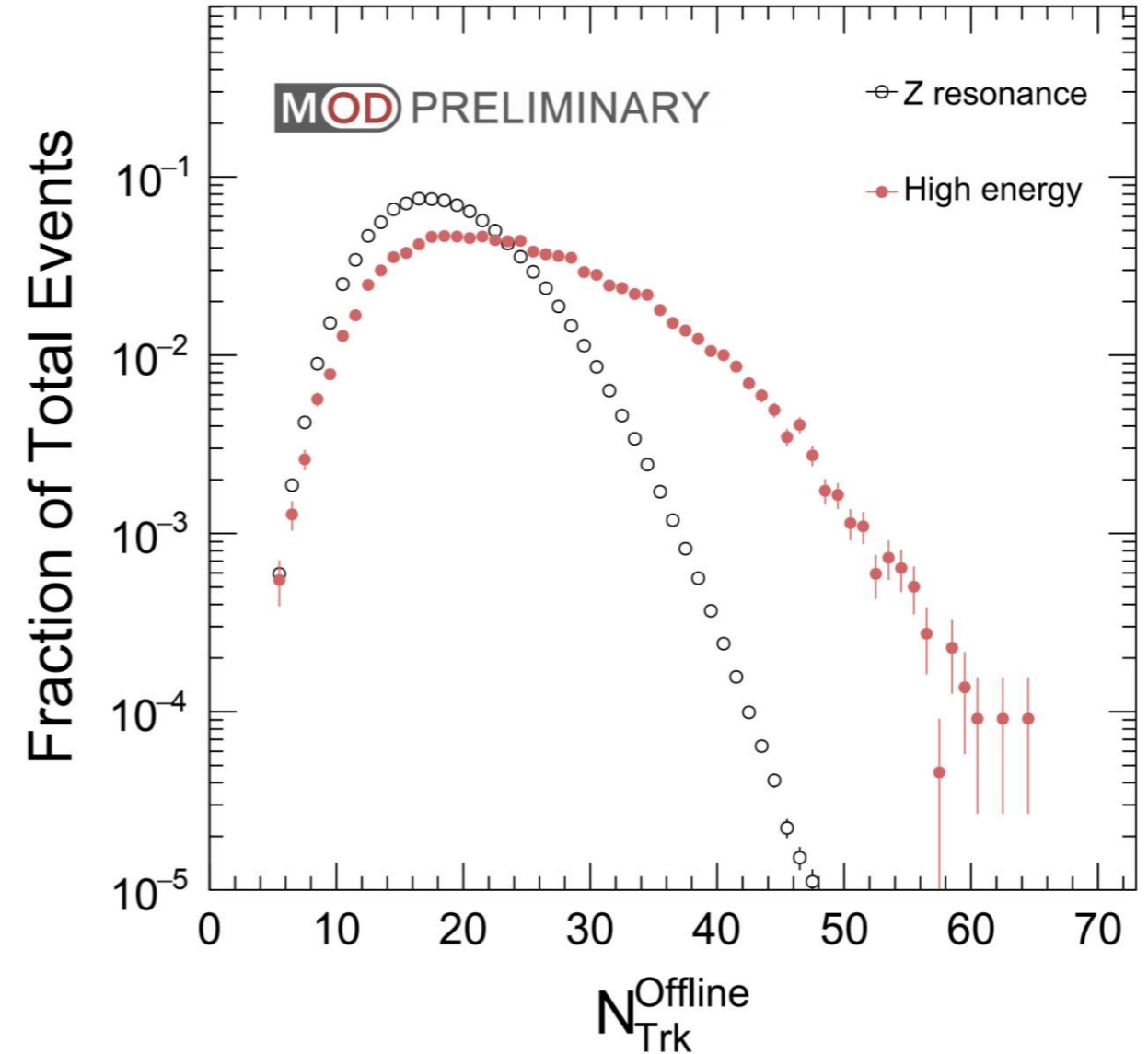
# The ALEPH Detector



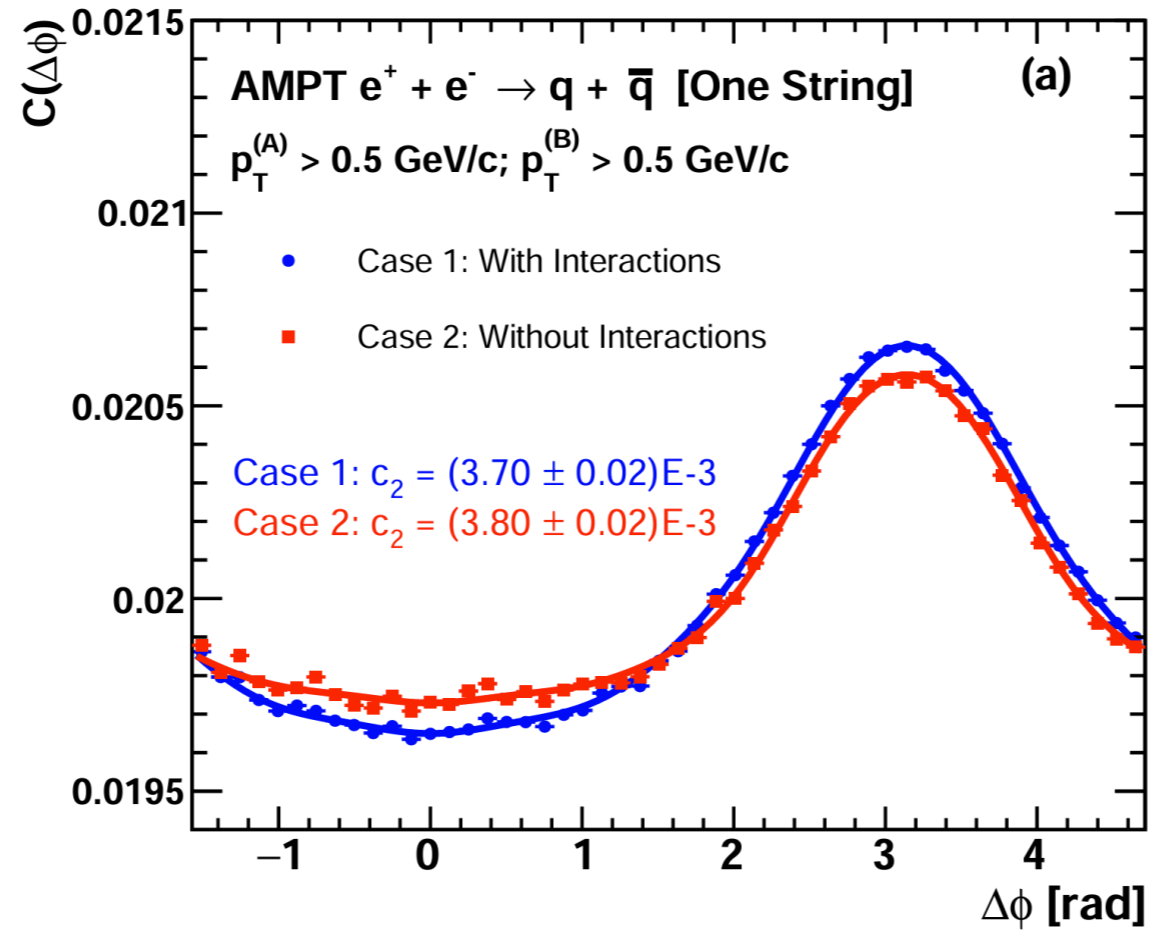
## Inner Tracking Chamber

- LEP1  $e^+e^-$  data at Z pole (91 GeV) taken between 1992-1995
- **LEP2  $e^+e^-$  data above Z pole up 209 GeV**
  - ~ **RHIC** energy

## Charged Particle Multiplicity



# Example: One-String Configuration Study with AMPT



J. Nagle et al, PRC 97 (2018) 2, 024909