

INVESTIGATION OF THE TWO- PARTICLE SOURCE FUNCTION AT $\sqrt{s_{NN}} = 2.76$ TEV WITH EPOS

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DAY OF FEMTOSCOPY

2023, GYÖNGYÖS

[arXiv:2212.02980](https://arxiv.org/abs/2212.02980) Phys. Lett. B (2023)

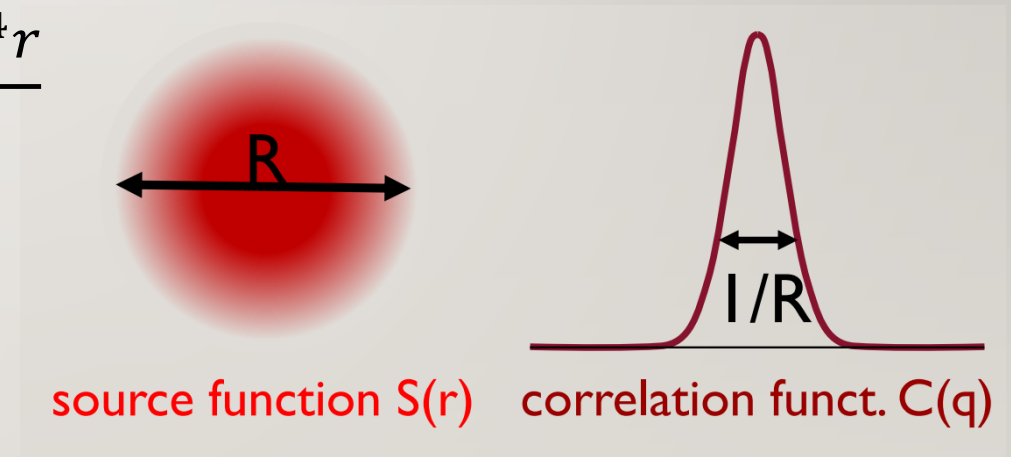


2 / 16 FEMTOSCOPY – THE TWO-PARTICLE SOURCE

- Two-particle (pair) source: $D(r, K) = \int S\left(\rho + \frac{r}{2}, K\right) S\left(\rho - \frac{r}{2}, K\right) d^4\rho$

relative coordinate \leftarrow average momentum \uparrow single-particle \uparrow phase-space density \uparrow
- Correlation function: $C(q, K) = \frac{\int D(r, K) |\Psi_q(r)|^2 d^4r}{\int D(r, K) d^4r}$

relative momentum \uparrow pair wave function \uparrow
- Experiments – no direct access to pair-source
 - Assume given source shape and wave function
 - Calculate the correlation function
 - Test the assumptions on the measured correlation
- Event generator models (like EPOS) – direct access to pair-source!



3 / 16 LÉVY DISTRIBUTIONS IN HEAVY ION PHYSICS

- Measurements suggest phenomena beyond Gaussian distribution

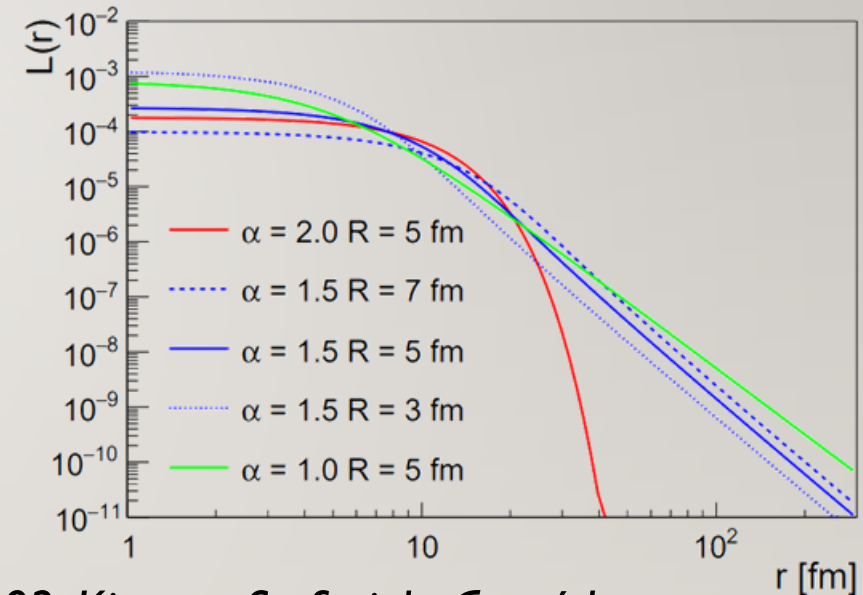
- Lévy-stable distribution: $L(\mathbf{r}; \alpha, R) = (2\pi)^{-3} \int d^3 \mathbf{q} e^{i\mathbf{q}\mathbf{r}} e^{-\frac{1}{2}|\mathbf{q}R|^\alpha}$

- α : Lévy stability index
- R : Lévy scale parameter

- 1-D projection: $L(r; \alpha, R) = (2\pi^2 r)^{-1} \int dq e^{-\frac{1}{2}(qr)^\alpha} \sin(qr) q$

- Some possible causes:

- **Event averaging** (Cimerman et al., *Phys.Part.Nucl.* 51 (2020) 282)
- **Resonance decays** (Csanád, Csörgő, Nagy, *Braz.J.Phys.* 37 (2007) 1002; Kincses, Stefaniak, Csanád, *Entropy* 24 (2022) 308)
- **Hadronic rescattering, anomalous diffusion** (*Braz.J.Phys.* 37 (2007) 1002; *Entropy* 24 (2022) 308)



4 / 16 THE EPOS MODEL

- EPOS = **E**nergy conserving quantum mechanical multiple scattering approach, based on **P**artons (parton ladders), **O**ff-shell remnants, and **S**aturation of parton ladders *K.Werner et al., PRC82 (2010) 044904, PRC89 (2014) 064903*
- Monte-Carlo based phenomenological model
- Stages of the evolution:
 - Initial stage – parton based Gribov-Regge theory
 - Core-corona separation
 - 3+1D viscous hydrodynamic evolution
 - Hadronic rescattering – UrQMD
- Dataset: EPOS3 2.76 TeV PbPb, 800k events

RECONSTRUCTING THE TWO-PARTICLE SOURCE

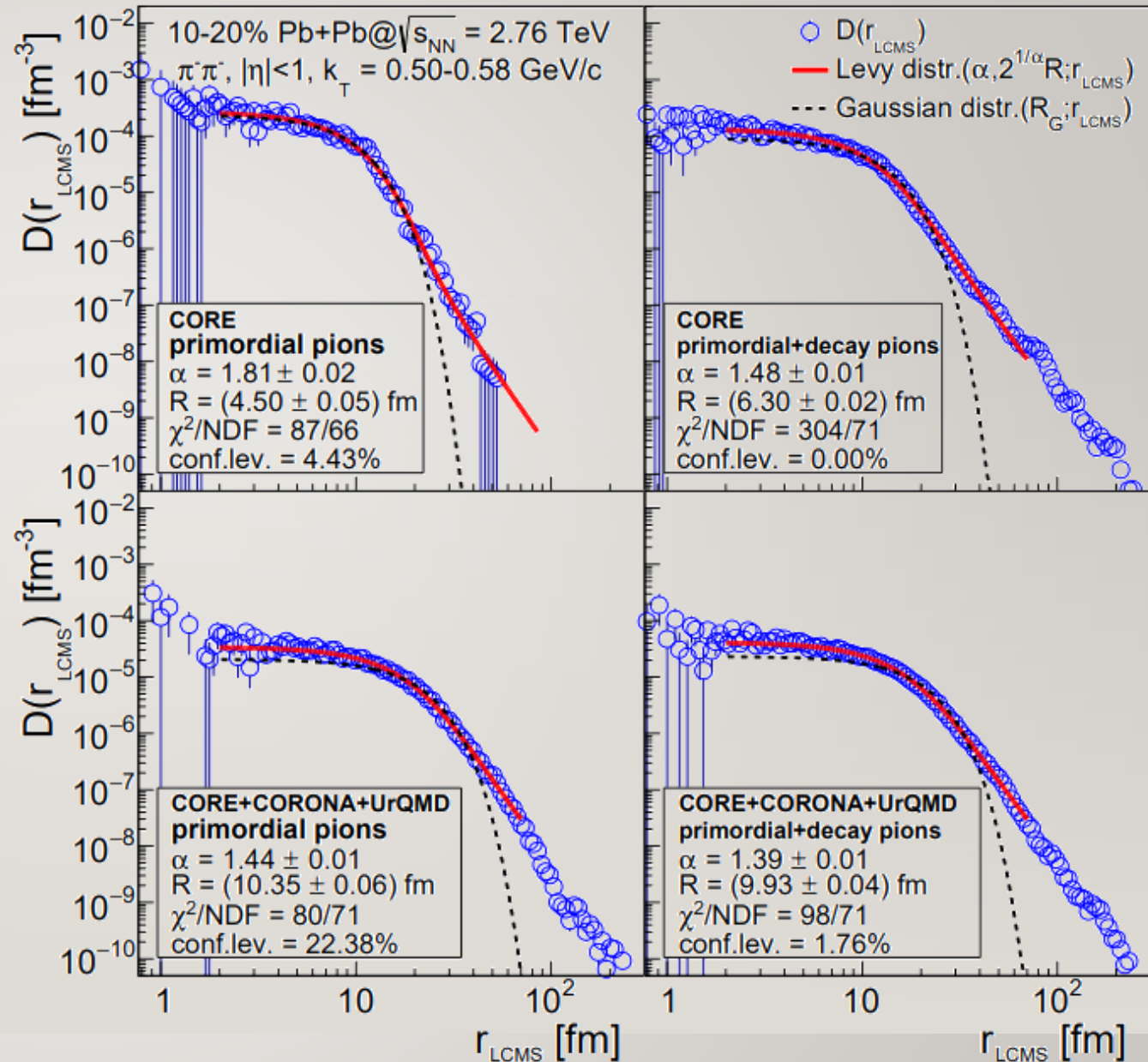
- Source spherically symmetric in the LCMS (*PHENIX coll., Phys. Rev. Lett. 93 (2004), 152302*)
- $\mathbf{r}_{LCMS} = \left(x_1 - x_2, y_1 - y_2, \frac{z_1 - z_2 - \beta(t_1 - t_2)}{\sqrt{1 - \beta^2}} \right), \beta = \frac{p_{z,1} + p_{z,2}}{E_1 + E_2}$
- Calculate $D(r_{LCMS})$ event-by-event!
- Average transverse momentum (k_T) classes
- Investigated cases:
 - Pions:
 - CORE, primordial
 - CORE, primordial+decay
 - CORE+CORONA+UrQMD, primordial
 - CORE+CORONA+UrQMD, primordial+decay
 - Kaons: CORE+CORONA+UrQMD, primordial+decay
 - Protons: CORE+CORONA+UrQMD, primordial+decay

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LÉVY FITS TO THE TWO-PARTICLE SOURCE

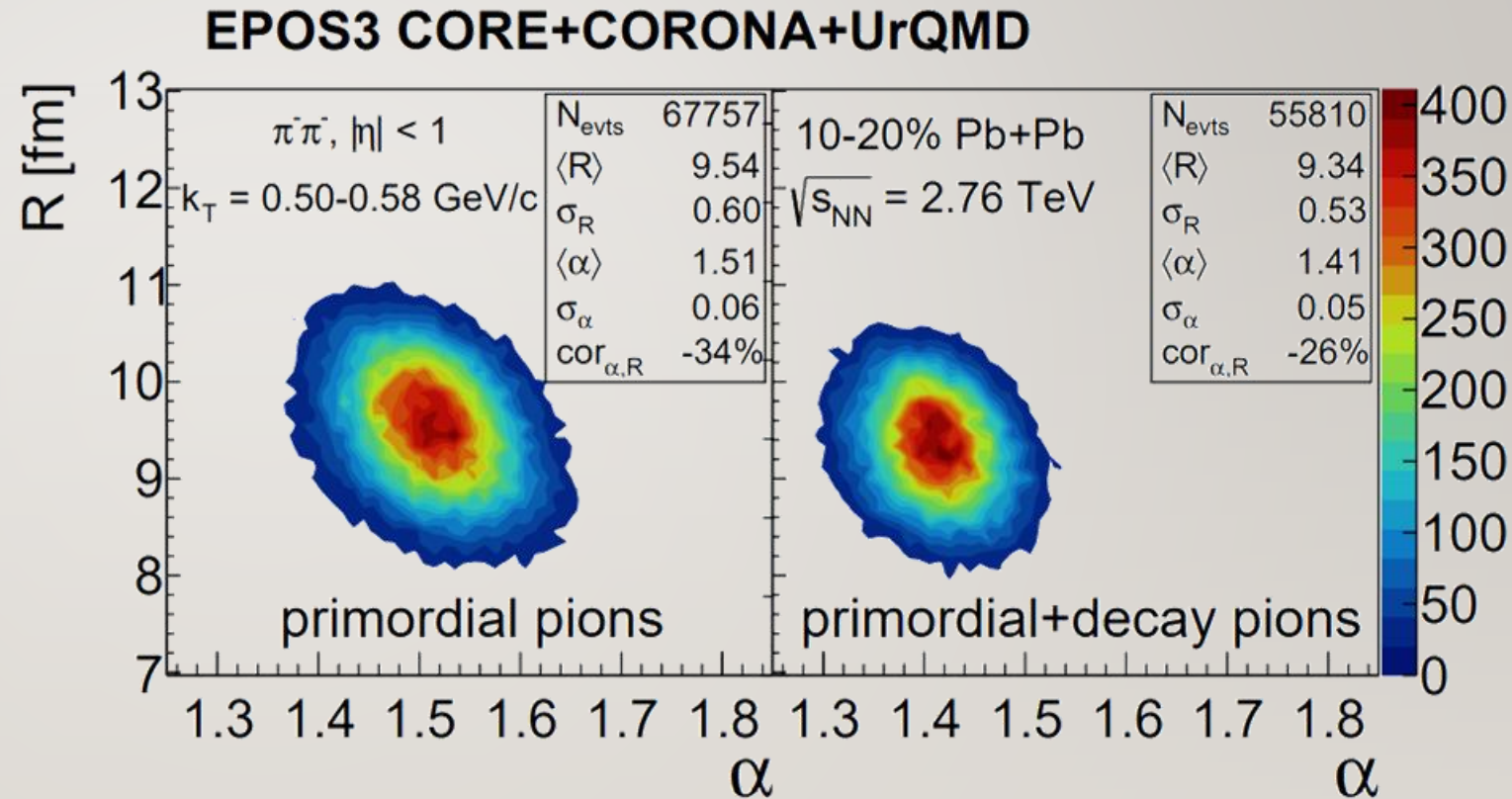
- Event-by-event Lévy fits
- Without decays and UrQMD \rightarrow close to Gaussian
- After decays or UrQMD \rightarrow far from Gaussian
- Lévy shape appears in single events!
- Similar fits for kaons and protons
- Only keep fits with $CL > 0.1\%$

EPOS3 single event



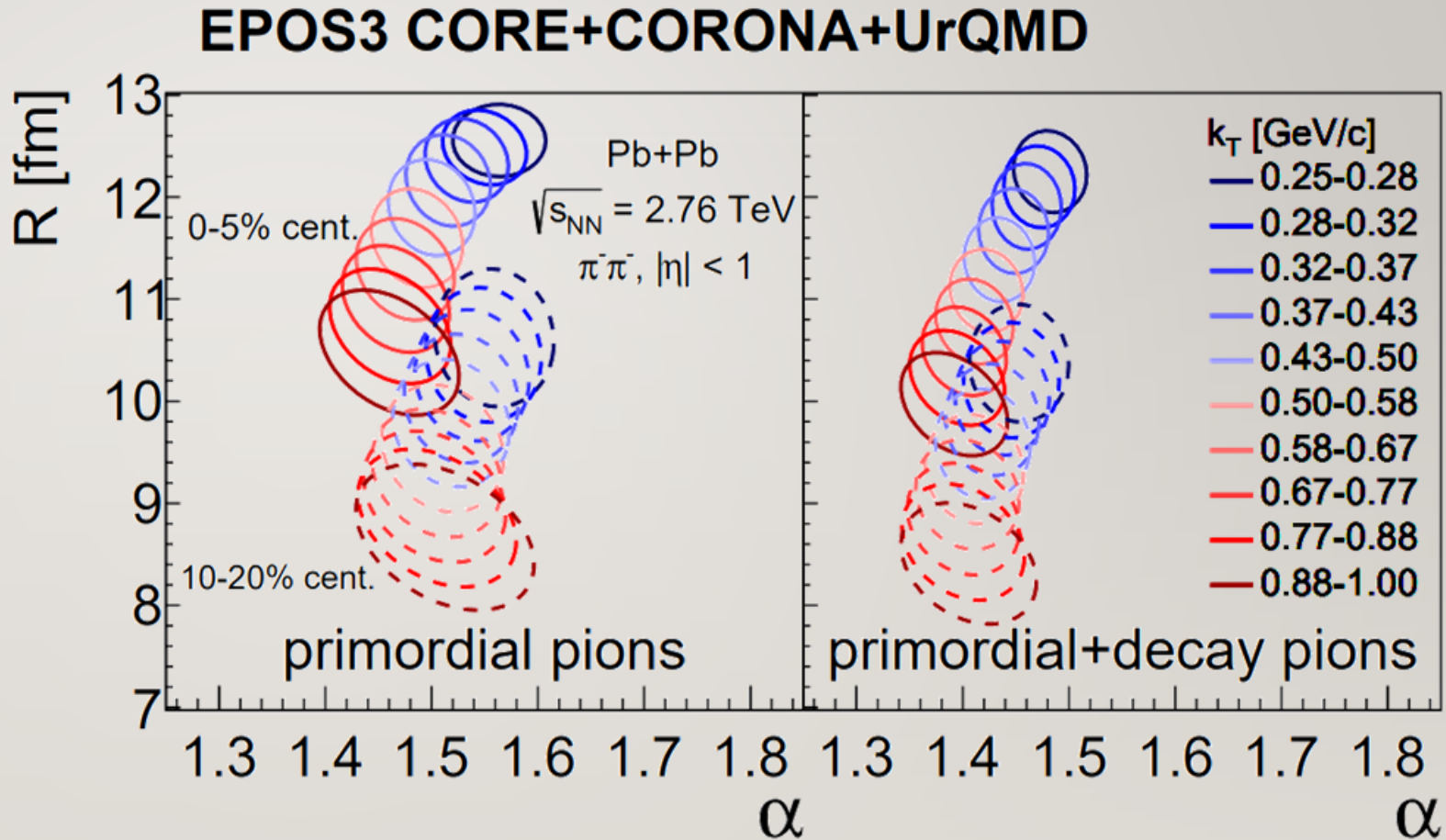
7/16 DISTRIBUTION OF THE SOURCE PARAMETERS

- Collect all fit results in R vs α histograms
- Similar figures for each centrality, k_T and for kaons or protons
- Extract average values $\langle R \rangle$ and $\langle \alpha \rangle$
- Extract standard deviations
- Investigate centrality and k_T dependence



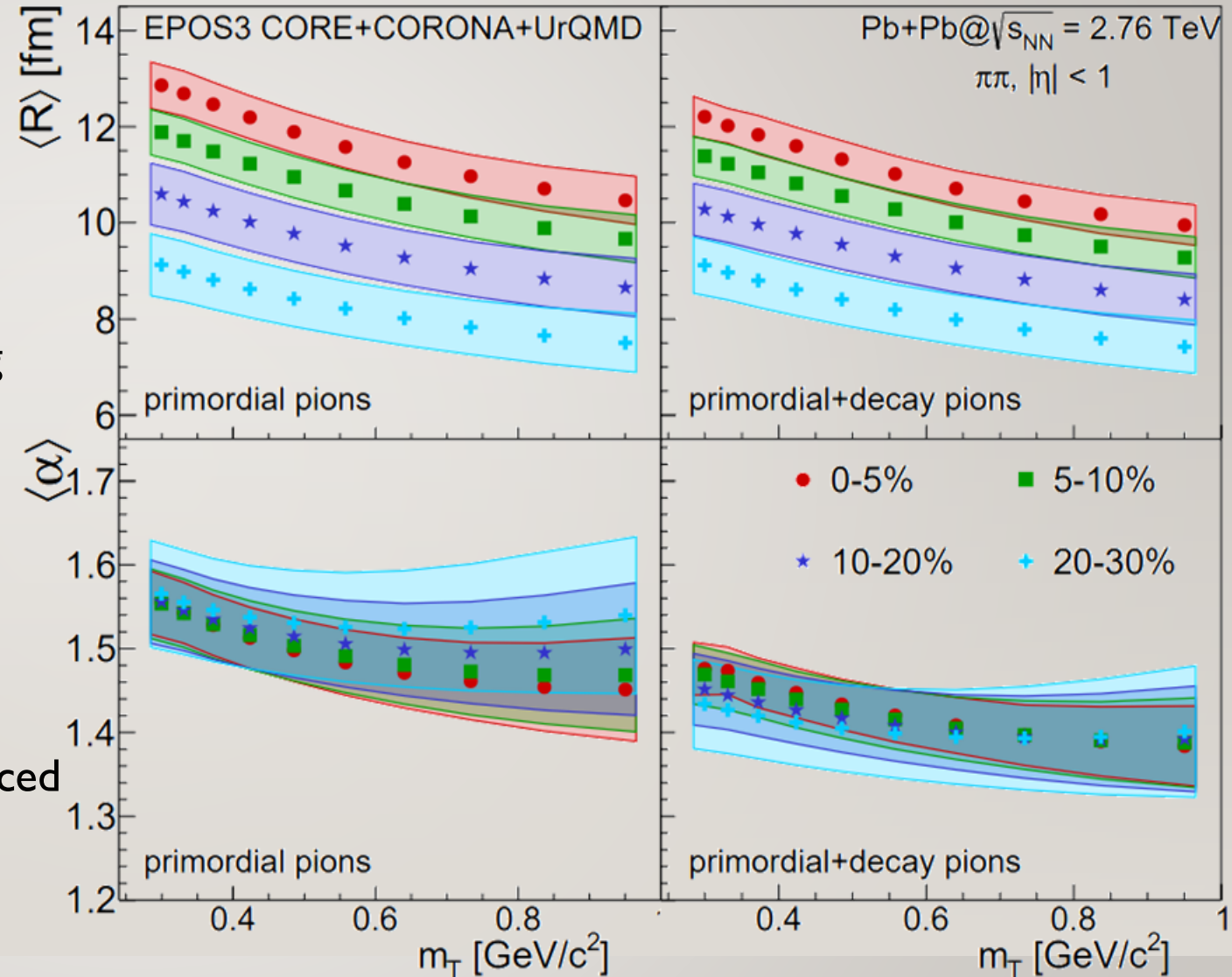
8/16 CONTOURS OF THE R VS α DISTRIBUTIONS

- 1σ contours for all k_T classes
 - Ellipses from σ_α, σ_R and $COR_{\alpha,R}$
 - Only 2 centralities in one figure for clarity
- $\alpha - R$ anti-correlation
- Illustrates centrality and k_T dependence

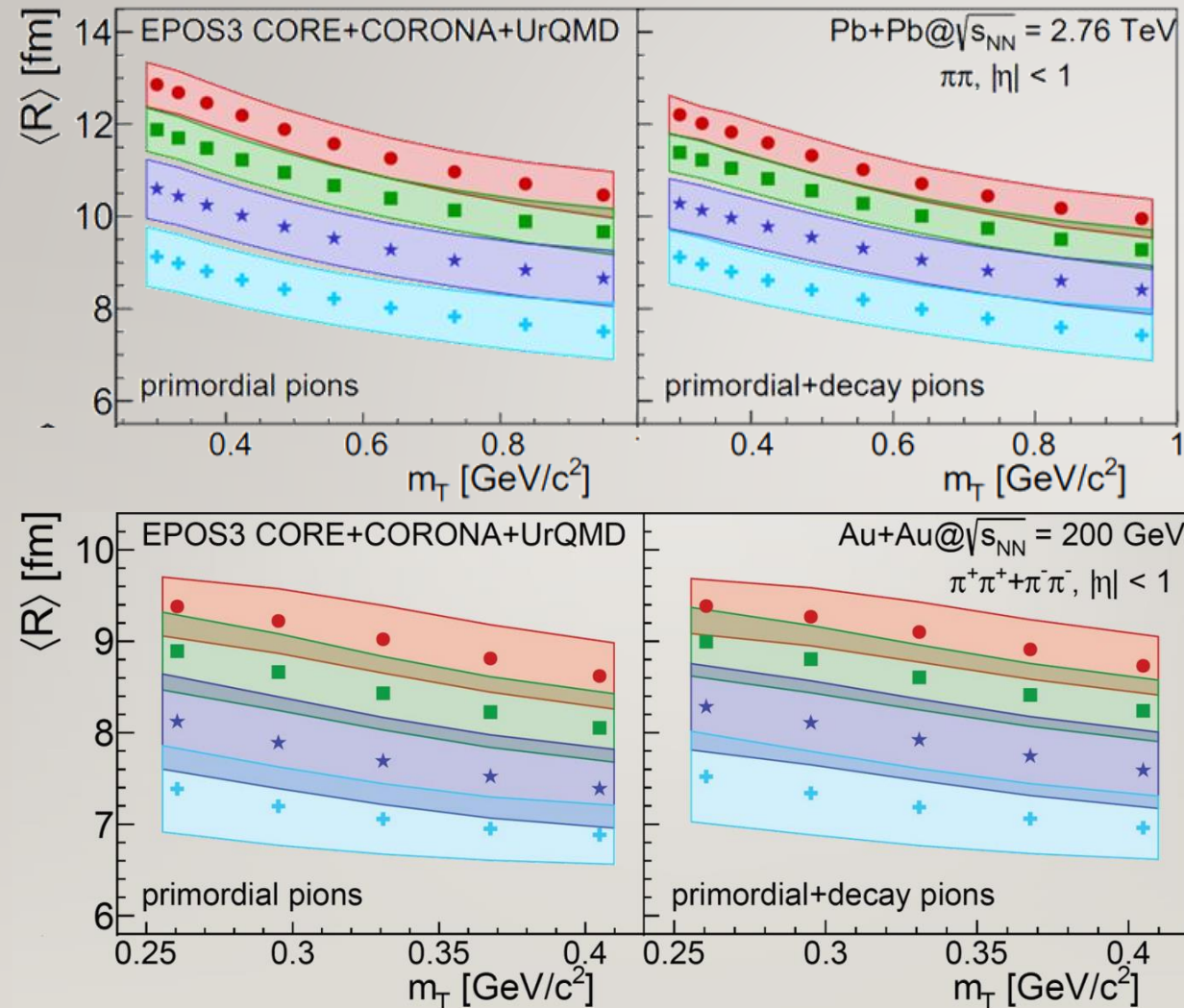


9/16 PION SOURCE PARAMETERS

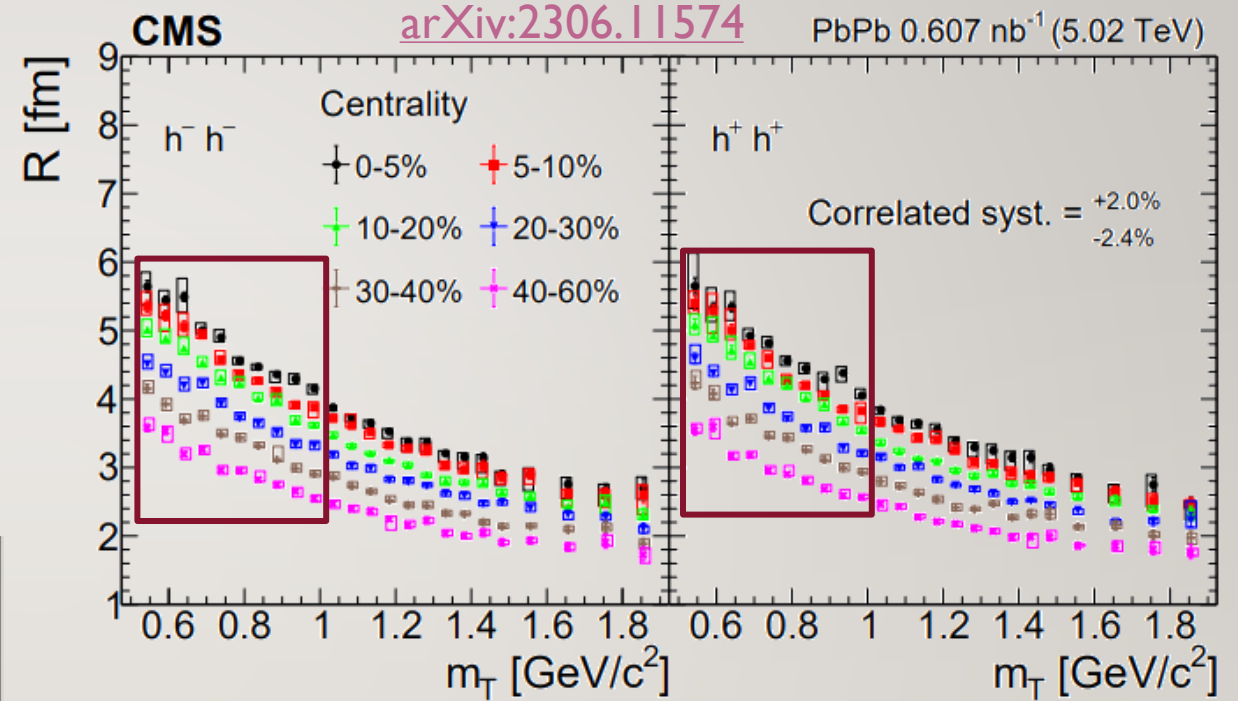
- Transverse mass: $m_T = \sqrt{k_T^2 + m^2}$
- Lévy scale parameter (R):
 - Larger in central collisions \rightarrow spatial scale
 - Decreases with $m_T \rightarrow$ hydrodynamic scaling
 - Small effect of decay products
- Lévy stability index (α):
 - Weak centrality dependence
 - Small decrease with m_T
 - Smaller after decays \rightarrow source shape influenced
- Error bands = standard deviation of $R/\alpha \neq$ statistical uncertainty of $\langle R \rangle / \langle \alpha \rangle$



10/16 COMPARISON TO DATA AND LOWER ENERGY EPOS

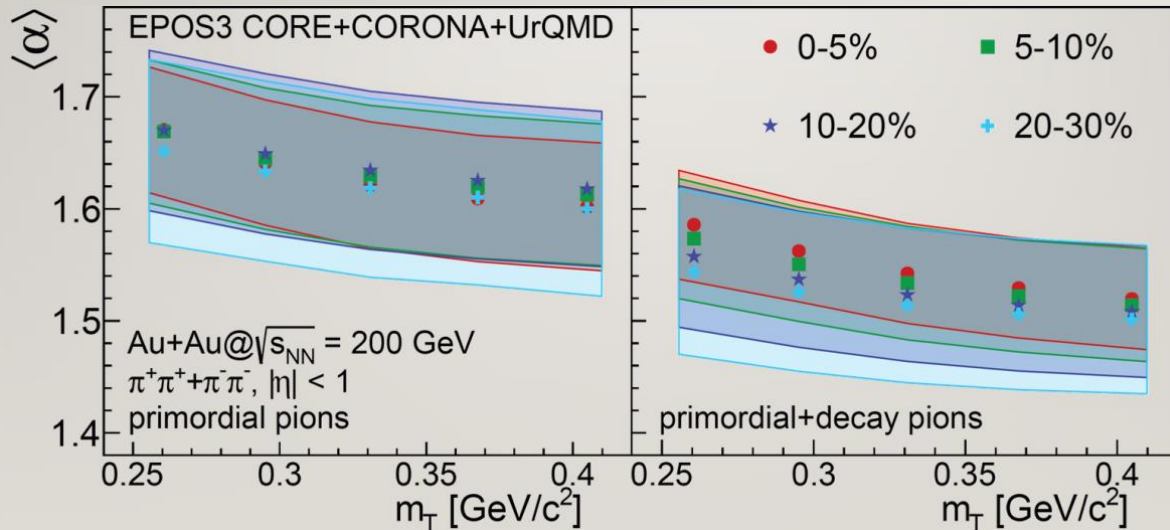
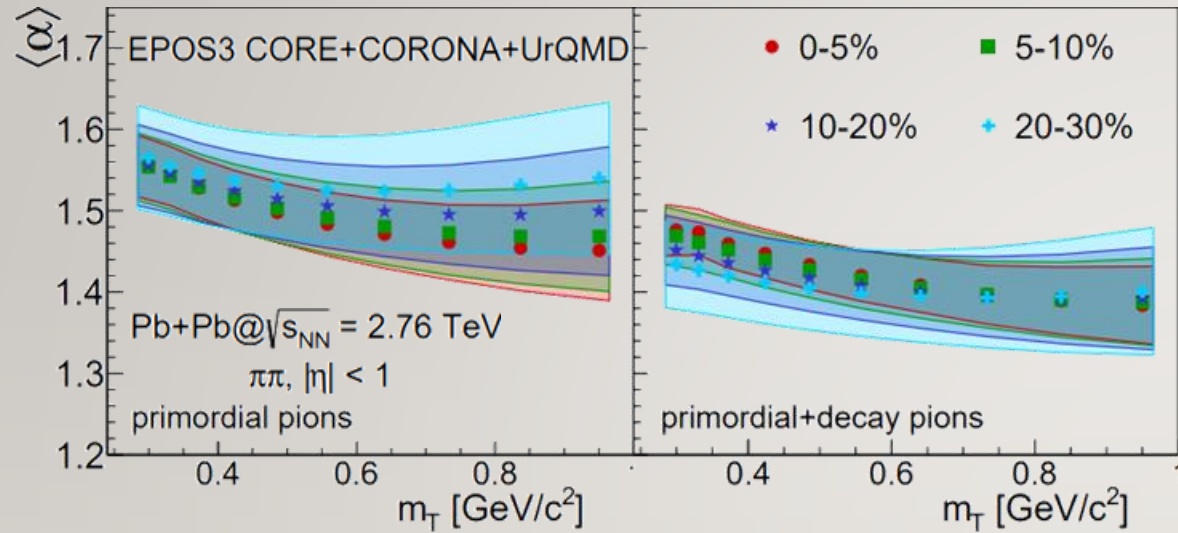


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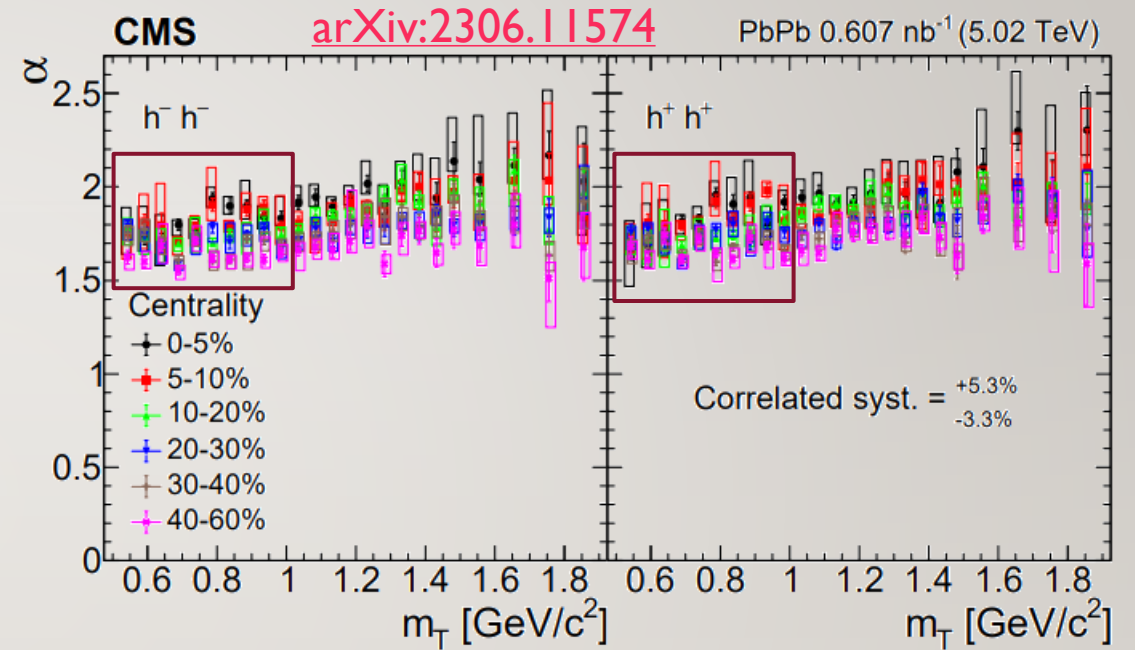


- Similar centrality and m_T dependence
- $\langle R \rangle(2.76 \text{ TeV EPOS}) > \langle R \rangle(200 \text{ GeV EPOS})$
- $\langle R \rangle(2.76 \text{ TeV EPOS}) > R(5.02 \text{ TeV data}) ?$

COMPARISON TO DATA AND LOWER ENERGY EPOS



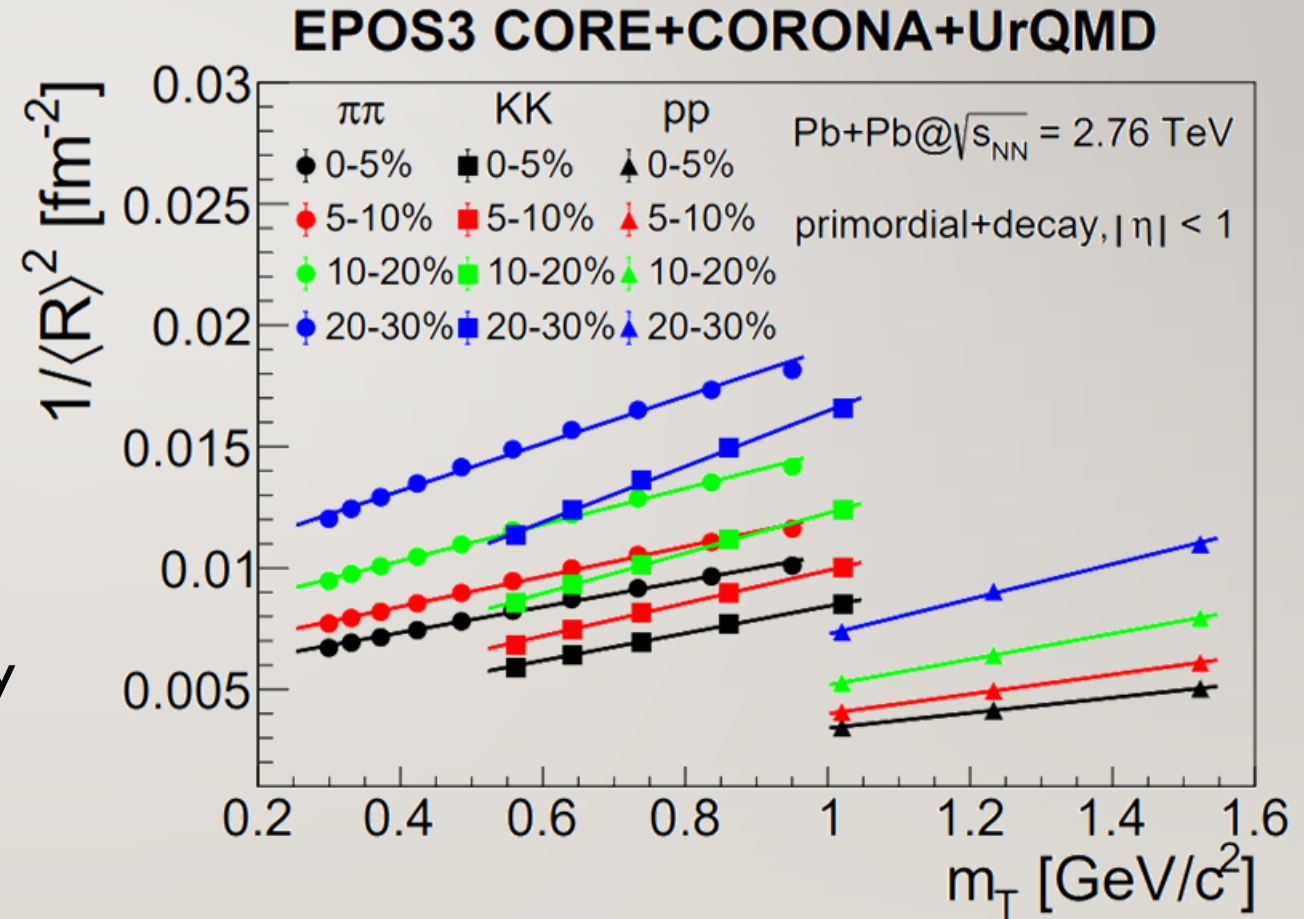
Kincses, Stefaniak, Csanád, *Entropy* 24 (2022) 308



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12/16 PION, KAON, PROTON LÉVY SCALE PARAMETER

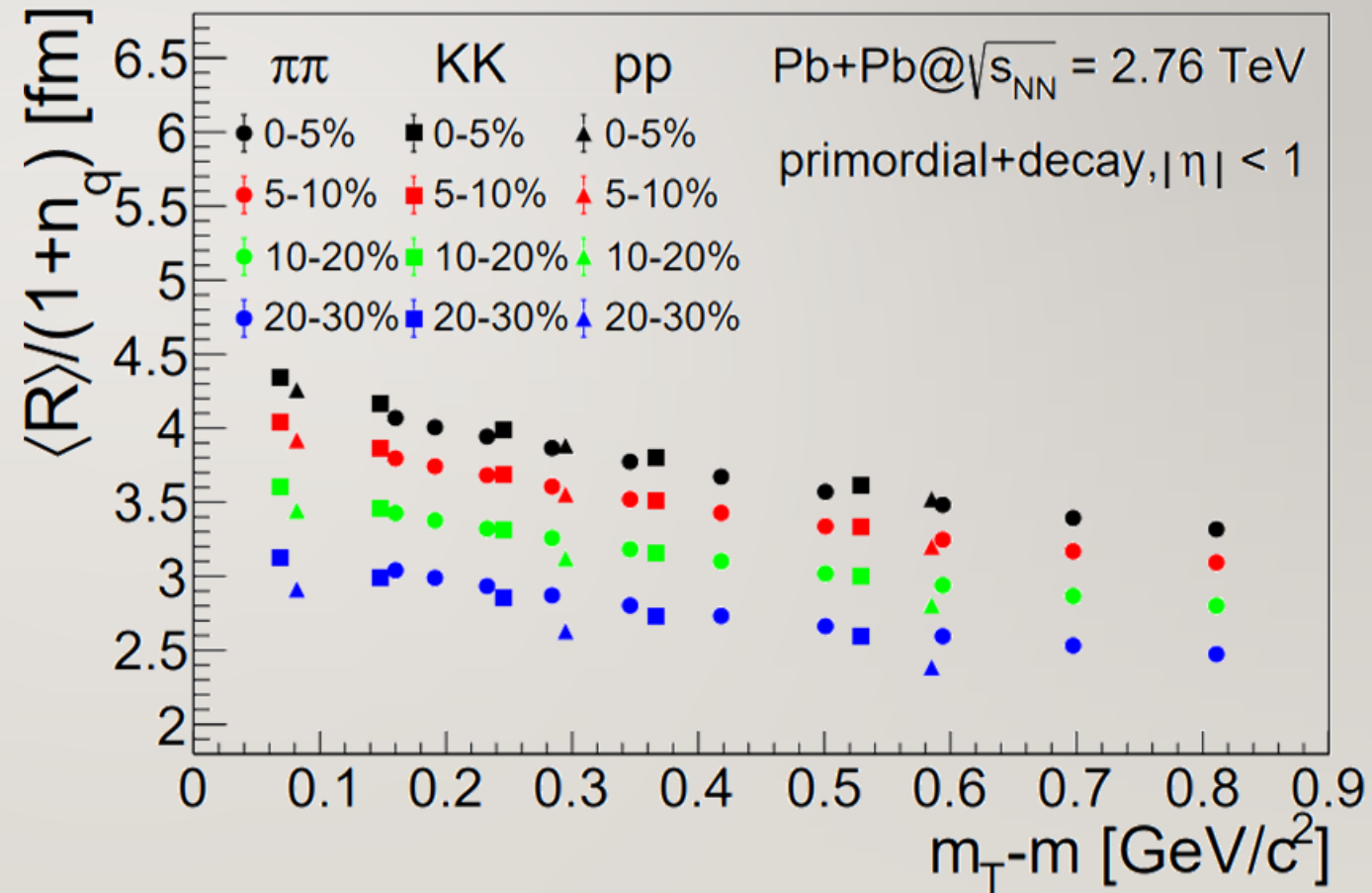
- Similar trends
- Hydrodynamics + Gaussian source \rightarrow
 $\frac{1}{R^2} \sim m_T$ particle independent scaling
- EPOS $\rightarrow R$ depends on the particle type
- No universal m_T scaling in EPOS
- For given species scaling is approximately fulfilled
- Stat. uncertainties smaller than markers



13/16 INTERESTING SPECIES INDEPENDENT SCALING OF R

- R vs. $(m_T - m)$ → same curve for pions and kaons
- Divide R with one plus the number of valence quarks → same curve for protons
- Unknown reasons and interpretation

EPOS3 CORE+CORONA+UrQMD

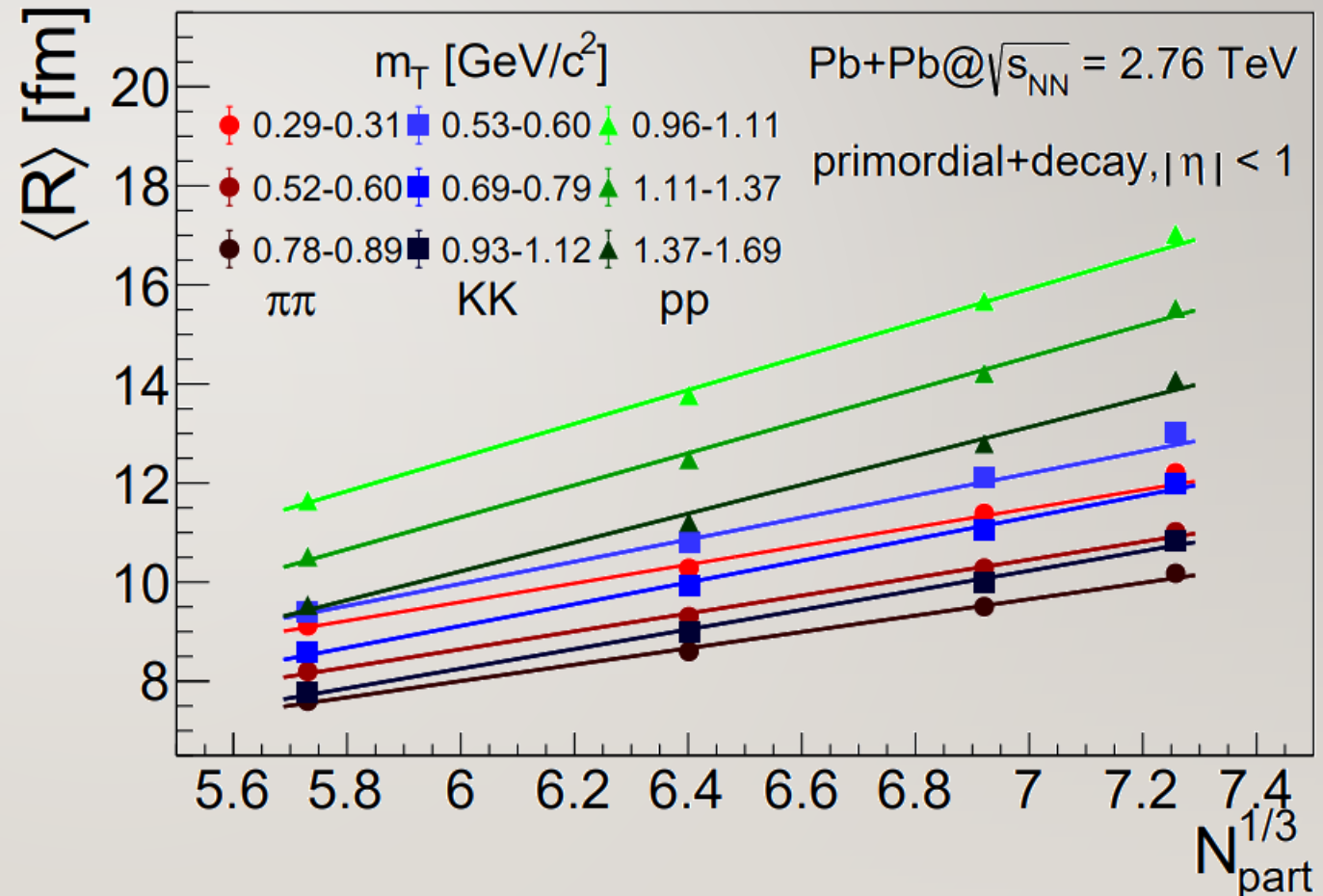


4/16 LÉVY SCALE PARAMETER VS N_{part}

- N_{part} : average number of participating nucleons
- $N_{part}^{1/3} \sim$ one-dimensional initial size
- Approximately linear scaling \rightarrow geometric interpretation
- Super small statistical uncertainties:

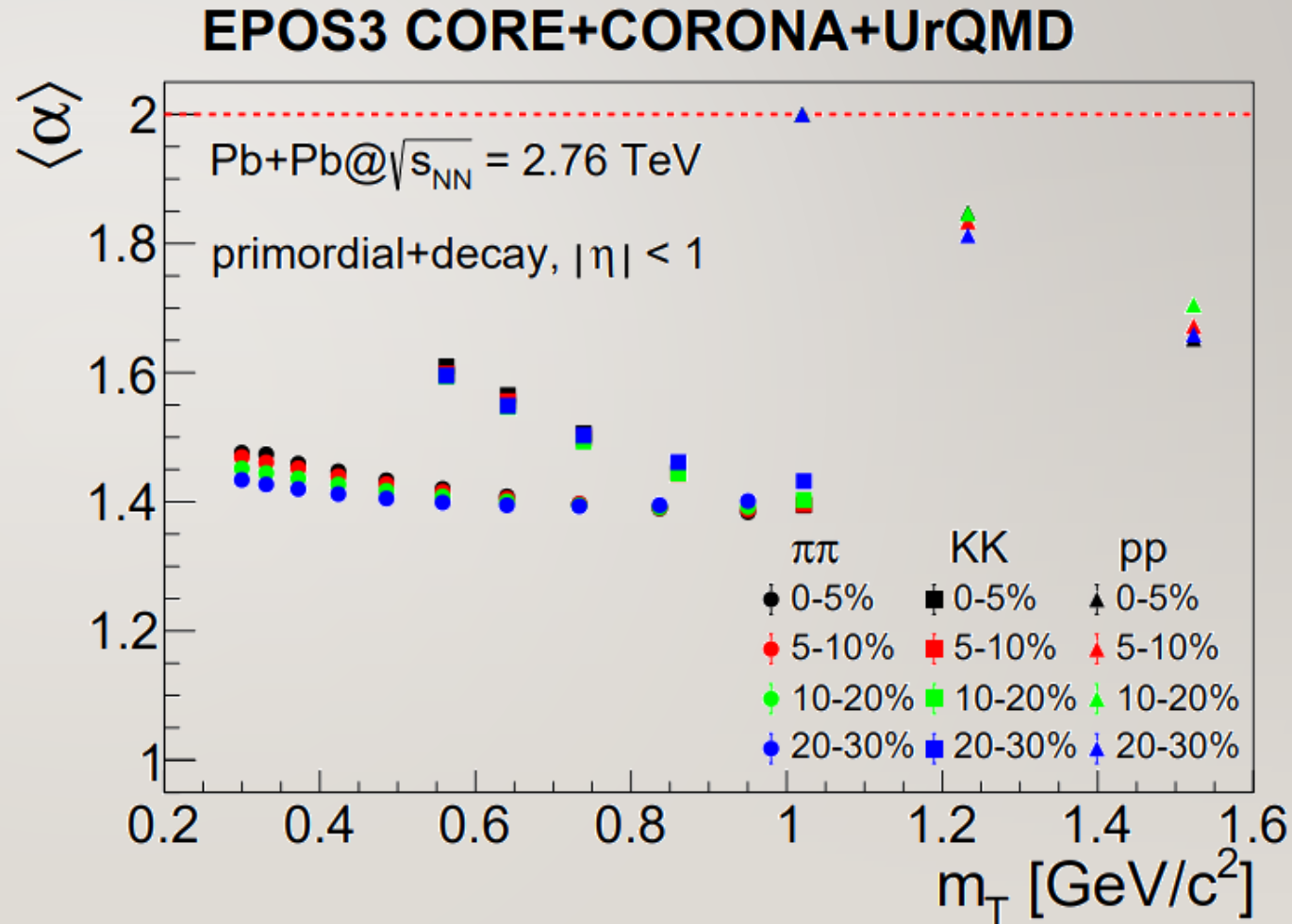
$$\frac{\sigma_R}{\sqrt{N_{evts}}} \approx 0.01\%$$

EPOS3 CORE+CORONA+UrQMD



15/16 PION, KAON, PROTON LÉVY STABILITY INDEX

- Source deviation from Gaussian ($\alpha = 2$)
- In case of anomalous diffusion:
 - Smaller cross-section \rightarrow larger mean free path \rightarrow longer power-law tail \rightarrow smaller α
- Prediction: $\alpha_K < \alpha_\pi < \alpha_p$
- Only partially fulfilled!
- Anomalous diffusion cannot be the only reason for the Lévy shape



6/16 SUMMARY

- **Analysis steps:**

- Event-by-event reconstruction of the two-particle source in EPOS 2.76 TeV PbPb
- Single event Lévy fits – **event-by-event Lévy shape**
- Extract mean Lévy parameters $\langle R \rangle$ and $\langle \alpha \rangle$

- **Results:**

- Hydrodynamic-like and geometric scaling of $\langle R \rangle$
- $\langle \alpha \rangle$ affected by decays
- Similar trends to experiment, but different magnitudes
- Particle species dependent $\langle R \rangle$
- Partially fulfilled predictions of anomalous diffusion
- Preprint: [arXiv:2212.02980](https://arxiv.org/abs/2212.02980) (accepted at Phys. Lett. B)

} pions

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**THANK YOU FOR
YOUR ATTENTION!**



BACKUP SLIDES



19 KAON AND PROTON EXAMPLE FIT

EPOS3 single event

