

# The Flavour of BSM: from LHC to Future Experiments

Joe Davighi, CERN

Zurich Phenomenology Workshop, 9<sup>th</sup> January 2024, University of Zurich

Key message:

1. “Deconstructing” SM gauge interactions [ $G_{12} \times G_3 \rightarrow G$ ] offers well-motivated solutions to flavour puzzle; current measurements allow significant natural\* parameter space
2. Future experiments, especially EW precision programme of **FCC-ee** but also HL-LHC, Belle II, Mu3e..., will cover this natural parameter space

\* Natural means:

1. Electroweak stability:  $\delta M_h^2 \lesssim (\text{TeV})^2$
2. Order-1 marginal couplings in UV model

# This Talk

1. SM & BSM Flavour Puzzles  $\rightarrow$  accidental  $U(2)$  flavour symmetries
2. Natural gauge explanations by deconstructing the SM near the TeV
  - $G_{12}^{EW} \times G_3^{EW} \rightarrow G^{EW}$ , Higgs charged under  $G_3^{EW}$
  - Generic consequences: large  $\delta m_h^2$  (naturalness?), large deviations in EWPO
3. Sketches of the UV
4. Phenomenological Case Studies
  - Deconstructed  $U(1)_Y$ ,  $m_{Z'} \gtrsim 4.5$  TeV; deconstructed  $SU(2)_L$ ,  $m_{W',Z'} \gtrsim 9.5$  TeV
  - Flavour + high pT + EW precision all provide complementary constraints
  - FCC-ee will push back scales by a (significant!) order of magnitude: natural  $\rightarrow$  unnatural

# 1. Flavour and accidental symmetries

# The Flavour Puzzle(s)

Fermion sector of SM contains many mysteries:

1. Why those (chiral) representations / hypercharges?
2. Why 3 generations?
3. Why huge (technically natural) hierarchies in SM Yukawa couplings  $y \bar{\Psi}_L H \Psi_R$ ?

Masses:  $1 \approx y_t \gg y_c \gg y_u \sim 10^{-5}, y_e \sim 10^{-6}$

Mixings:  $V_{us} \gg V_{cb} \gg V_{ub}$

# The Flavour Puzzle(s)

See Claudia's talk

SM Lagrangian exhibits approximate  $U(2)_L \times U(2)_R$  flavour symmetry

SM flavour puzzle

Barbieri et al [1105.2296](#), Isidori, Straub [1202.0464](#), Fuentes-Martin et al, [1909.02519](#)

$$Y_u \sim \begin{pmatrix} & & \\ < 0.01 & 0.04 & \\ & & 1 \end{pmatrix}; \quad \text{origin of } U(2)\text{s and } U(2)\text{-breaking spurions?}$$

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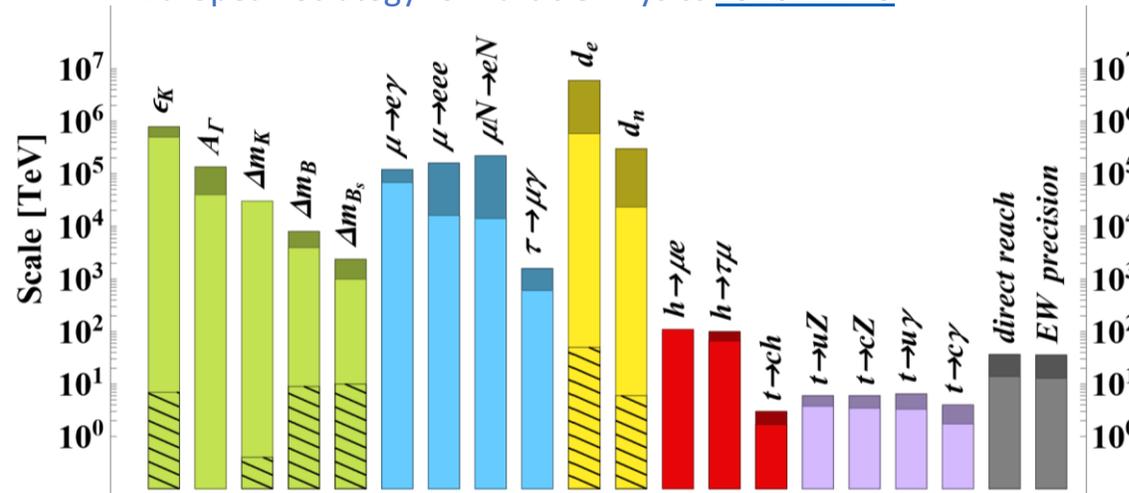
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If New Physics is light ( $\Lambda < 10$  TeV), it also exhibits  $U(2)$  flavour symmetries

BSM flavour puzzle

Need to suppress e.g. **kaon mixing**, which probes effective scale  $\sim 10^{5-6}$  TeV

European Strategy for Particle Physics [1910.11775](#)



## Aside: $U(2)$ or $U(3)$ ?

D'Ambrosio, Giudice, Isidori, Strumia, [hep-ph/0207036](#) ...

Traditional MFV: New Physics has approximate  $U(3)$  i.e. flavour-universal, broken only by  $Y_{u,d,e}$

- $U(3)$  and  $U(2)$  equally good for evading flavour bounds (BSM flavour puzzle);
- $U(3)$  more predictive (fixed spurions)

### Reasons to prefer $U(2)$

- $U(2)$  can **also explain SM flavour puzzle**;  $U(3)$  cannot!
- $U(3)$  unnecessarily aggressive; ties 3<sup>rd</sup> family couplings (most important for **naturalness**) to valence quark couplings, which are strongly bound by LHC
- With  $U(2)$ , NP can couple most to 3<sup>rd</sup> generation; it can be lighter, and so more natural



For 33 vs 11 quark indices in  $\mathcal{L} \sim \frac{C_{ij}}{\Lambda^2} Q^i Q^j L^a L^b$ , bounds on  $C_{ij}/\Lambda^2$  from LHC Drell—Yan weaker by factor  $\sim 10$ , see e.g. [Allwicher et al [2207.10714](#); Allwicher et al [2207.10756](#) ]

## 2. Explaining the accidents: Deconstructing the SM forces

Hypothesis:  $U(2)$ s manifest in Yukawas and NP couplings have *common dynamical origin!*

Emerge as **accidental symmetries** from spontaneously-broken **non-universal** gauge symmetry that acts differently on 3<sup>rd</sup> family, same on 1<sup>st</sup> and 2<sup>nd</sup>

# Flavour non-universality

- Want  $U(2)^n$  to emerge as **accidental** from a flavour **non-universal gauge symmetry**

## Horizontal approach

- One approach is to “factorize the flavour problem” by gauging a horizontal symmetry

$$G = G_{\text{SM}} \times G_{\text{hor}} \rightarrow G_{\text{SM}}$$

Froggatt, Nielsen, [Nucl Phys B \(1979\)](#)

- All heavy gauge bosons are SM singlet  $Z'$ s. Examples:

➤ Gauge  $G_{\text{hor}} = U(2)^n$  symmetries directly

➤ Gauge a particular  $G_{\text{hor}} = U(1)_X$  a la Froggatt—Nielsen

Recent examples:

Greljo, Thomsen, [2309.11547](#)

Antusch, Greljo, Stefanek, Thomsen, [2311.09288](#)

... Cornella et al [2306.08026](#)

# Flavour non-universality, non-horizontally

- Want  $U(2)^n$  to emerge as accidental from a flavour non-universal gauge symmetry

## Deconstruction approach:

- A more intricate approach is to split apart (or “deconstruct”) SM gauge symmetry by flavour:

$$G = G_{\text{SM},12} \times G_{\text{SM},3} \rightarrow G_{\text{SM}}$$

Arkani-Hamed, Cohen, Georgi [hep-th/0104005](#); ... Craig, Green, Katz [1103.3708](#); ... Bordone, Cornella, Fuentes-Martin, Isidori, [1712.01368](#) ...

- Heavy gauge bosons in adjoint of  $G_{\text{SM}}$ , e.g. if  $G_{\text{SM}} = SU(2)_L$  we get a heavy electroweak triplet, coupled to a flavour-non-universal fermion current

### Gauge Model of Generation Nonuniversality

Xiao-yuan Li<sup>(a)</sup> and Ernest Ma

*Department of Physics and Astronomy, University of Hawaii at Manoa, Honolulu, Hawaii 96822*

(Received 13 October 1981)

An electroweak gauge model is discussed, where generations are associated with separate gauge groups with different couplings. The observed  $\mu$ - $e$  universality is the result of a mass-scale inequality,  $\nu_{03} \ll \nu_{12}$ , in much the same way as strong isospin is the result of  $m_u, m_d \ll 1$  GeV. However, in contrast to the standard model, it is now possible to have (1) a longer  $\tau$  lifetime, (2) an observable  $B^0$ - $\bar{B}^0$  mixing, and (3) many gauge bosons  $W_i, Z_i$  in place of  $W, Z$  with  $M_{W_i} > M_W$  and  $M_{Z_i} > M_Z$ .

In conclusion, we have put forward in this paper a radical, if not heretical, point of view that both the observed  $\mu$ - $e$  universality and the known suppression of flavor-changing neutral-current kaon processes are in fact accidents, in much the same way that strong isospin is an accident. We thus predict a hierarchy of generations, in analogy with strong SU(2), SU(3), SU(4), etc., in which each succeeding generation breaks the universality of weak interactions more and more

Li, Ma, [1981](#)

# Flavour non-universality, non-horizontally

$$G = G_{\text{SM},12} \times G_{\text{SM},3} \rightarrow G_{\text{SM}}$$

Deconstruction of SM gauge interactions is a theoretically appealing approach:

1. Charge assignment and anomaly-freedom inherited from SM (no *ad hoc* choices)
2. Breaking pattern, assuming scalar condensate  $\phi$ , is **generic** for simple  $G$ 
  - for any choice of gauge couplings, and any scalar rep  $\phi \sim (\mathbf{R}_{12} \neq 1, \mathbf{R}_3 \neq 1)$ , you *always* break to the diagonal (ergo flavour-universal) subgroup
  - ... because there is no other non-trivial subgroup embedding, by *Goursat's lemma*
  - i.e. flavour universality of SM emerges almost **inevitably** from deconstructed  $G_{\text{SM}}$
3. Easy to find semi-simple UV completions with deconstruction approach
  - e.g. Pati—Salam cubed [[Bordone et al 1712.01368](#)],  $SU(5)$  cubed [[Fernandez-Navarro, King, 2311.05683](#)]
  - In contrast most  $G_{\text{SM}} \times U(1)_X$ , even anomaly-free, have no semi-simple completion

Goursat, 1889  
Craig, Garcia-Garcia,  
Sutherland, [1704.07831](#)

Davighi, Tooby-Smith,  
[2206.11271](#)

# Flavour non-universality, non-horizontally

Davighi, Isidori [2303.01520](#)

With Higgs charged under  $G_{SM,3}$ , deconstruction can explain Yukawa hierarchies via accidental  $U(2)^n$ :

$$SU(3)^{[12]} \times SU(3)^{[3]}$$

$$Y \sim \begin{pmatrix} \times & \times & \\ \times & \times & \\ & & \times \end{pmatrix}$$

Allows 2 x 2 matrix of light Yukawas  
(Higgs colourless)

Explains  $V_{cb} \ll 1$

Doesn't explain  $m_2 \ll m_3$

$$SU(2)_L^{[12]} \times SU(2)_L^{[3]}$$

$$Y \sim \begin{pmatrix} & & \\ & & \\ \times & \times & \times \end{pmatrix}$$

Rank-1 matrix, can be  
diagonalised by a RH-rotation  
that is unphysical (as in SM)

Explains  $V_{cb} \ll 1$

Explains  $m_2 \ll m_3$

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Explains  $m_2 \ll m_3$

Need to deconstruct EW gauge  
symmetry to explain  $m_2 \ll m_3$



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## \* What of Naturalness?

Unavoidable finite corrections to Higgs mass squared:

See also Allwicher, Isidori, Thomsen [2011.01946](#)

c.f. Farina, Strumia, Pappadopulo, [1303.7244](#)

$$\delta m_h^2 \sim \left(\frac{1}{16\pi^2}\right)^2 g_S^2 y_t^2 N_c M_X^2$$

$$\delta m_h^2 \sim \frac{1}{16\pi^2} g_L^2 M_X^2$$

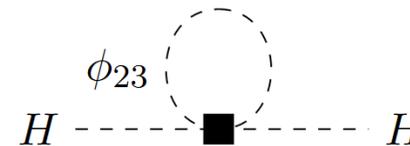
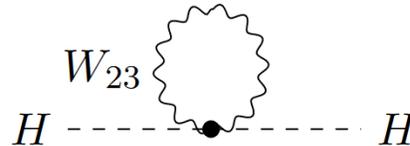
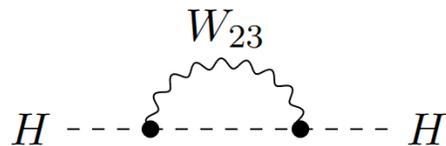
$$\delta m_h^2 \sim \frac{1}{16\pi^2} g_Y^2 M_X^2$$

Requiring  $\delta M_h^2 \lesssim (125 \text{ GeV})^2$  (aggressive),  $\delta M_h^2 \lesssim (\text{TeV})^2$  (little hierarchy) gives naturalness 'bounds':

$$M_{G'} \lesssim 10 (80) \text{ TeV}$$

$$M_{W'_L} \lesssim 2.5 (20) \text{ TeV}$$

$$M_{Z'_Y} \lesssim 5 (40) \text{ TeV}$$



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## \* Electroweak Precision

Deconstructing  $SU(2)_L$  and/or  $U(1)_Y$  gives tree-level effects in EWPOs: strong constraints  $\sim 5 \text{ TeV}$  or so

For deconstructed colour (e.g. '4-3-2-1'), EWPO much milder [[Allwicher, Isidori, Lizana, Selimovic, Stefanek 2302.11584](#)]

See also Allwicher, Isidori, Thomsen [2011.01946](#)

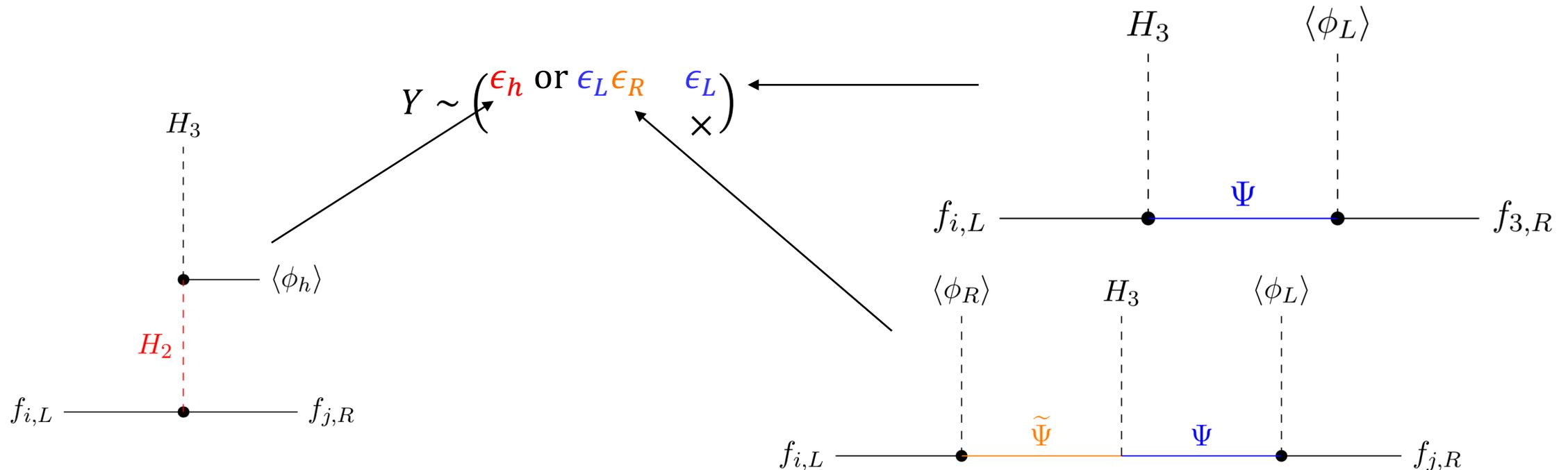
c.f. Farina, Strumia, Pappadopulo, [1303.7244](#)

### 3. UV completion?

# General Ingredients

Integrate out vector-like fermions  $\Psi$  or heavy Higgs-like scalars  $H_i$  to generate effective higher-dimensional Yukawa interactions, suppressed by ratios of scales  $\epsilon \sim \langle \phi \rangle / M_{\Psi/H}$

Link fields  $\phi$  typically in bi-fundamental of  $G_{12} \times G_3$ ; condensate breaks to diagonal



These ingredients give extra Higgs mass contributions (and phenomenological effects); but these are more model-dependent than the gauge sector contributions

See e.g. Davighi, Isidori [2303.01520](#)  
for naturalness implications

# Resolving the 1-2 sector

- $G_{\text{SM},12} \times G_{\text{SM},3} \rightarrow G_{\text{SM}}$  could be last step in a **multi-scale** breaking from fully deconstructed  $G_1 \times G_2 \times G_3$
- Scale hierarchy  $\Lambda_{12} > \Lambda_{23}$ ; the higher breaking step  $G_1 \times G_2 \rightarrow G_{12}$  resolves 1-2 substructure i.e. explains the  $y_1/y_2$  hierarchy
  - $\Lambda_{12}$  *must* be higher (100s TeV), because it will induce 1-2 flavour violation e.g. kaon mixing
  - But this remains natural from Higgs perspective, because Higgs not charged under  $G_1 \times G_2$

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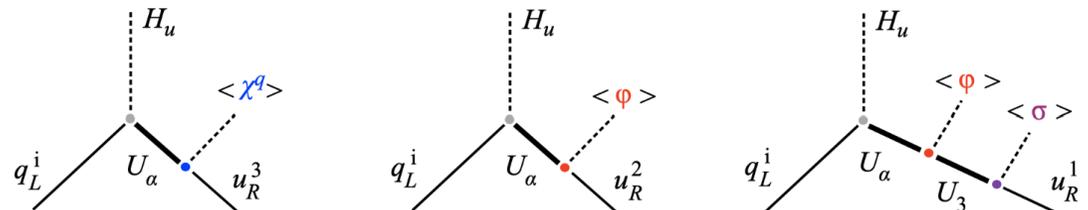
## Abelian Example: ‘Minimal Flavour Deconstruction’

Barbieri, Isidori, [2312.14004](#)

vev scale	Field	$U(1)_Y^{[3]}$	$U(1)_{B-L}^{[12]}$	$U(2)_{T_{3R}}^{[2]}$	$U(1)_{T_{3R}}^{[1]}$	$SU(3) \times SU(2)$
$v$	$H_{u,d}$	-1/2	0	0	0	( <b>1, 2</b> )
$O(10^{-1}) \times \Lambda_{[23]}$	$\chi^q$	-1/6	1/3	0	0	( <b>1, 1</b> )
	$\chi^l$	1/2	-1	0	0	( <b>1, 1</b> )
	$\phi$	1/2	0	-1/2	0	( <b>1, 1</b> )
$O(10^{-1}) \times \Lambda_{[12]}$	$\sigma$	0	0	1/2	-1/2	( <b>1, 1</b> )

$$Y \sim \left( \begin{array}{ccc|c} & U(1)_{B-L}^{[12]} & & \\ & U(1)_{T_{3R}}^{[1]} & U(1)_{T_{3R}}^{[2]} & \\ \hline O(\epsilon_\sigma \epsilon_\phi) & O(\epsilon_\phi) & O(\epsilon_\chi) & U(1)_{B-L}^{[12]} \\ \hline O(\epsilon_\sigma \epsilon_\phi \epsilon_\chi) & O(\epsilon_\phi \epsilon_\chi) & O(1) & \end{array} \right)$$

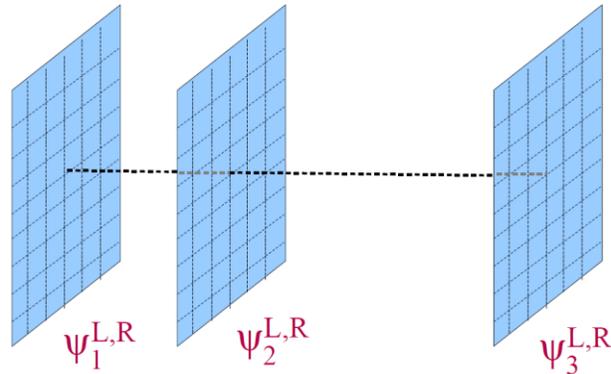
Example generation of light Yukawa EFT operators:



# What is the origin of the flavour deconstruction?

*Example origin 1: Fifth dimension*

Realise multiple flavour sites via **multiple stable branes** in 5d bulk



Fuentes-Martin, Isidori, Lizana, Selimovic, Stefaneck, [2203.01952](#)

One bulk electroweak  $SO(5) \supset SU(2)_L \times SU(2)_R$  gauge symmetry

- Holographic Higgs as light pNGB
- Fermions localised on **3 branes**  $\rightarrow \prod_{i=1}^3 SU(2)_{L,i} \times SU(2)_{R,i}$  in effective 4d description
- $SU(2)_R$  more sharply localised on branes ( $SU(2)_L$  is “more universal”)

# What is the origin of the flavour deconstruction?

## Example origin 2: 4d gauge flavour unification

Allanach, Gripaos, Tooby-Smith, [2104.14555](#)

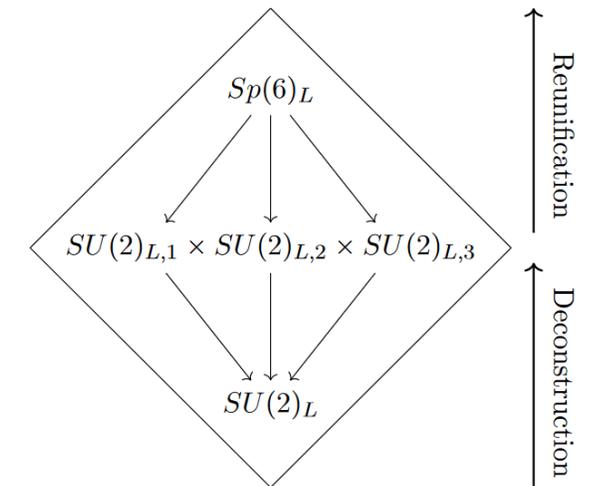
Complete UV unification of matter into two Weyls  $\psi_L \oplus \psi_R$ ; implies one of only 3 gauge groups

E.g.  $SU(4) \times \prod_{i=1}^3 (SU(2)_{L,i} \times SU(2)_{R,i}) \hookrightarrow SU(4) \times Sp(6)_L \times Sp(6)_R$

- $2^{\oplus 3} \hookrightarrow \mathbf{6}$ : all SM fermions in just one pair of chiral fields  $\Psi_{L/R}$
- Offers a “gauge answer” to “why 3 generations?”
- Higgs  $\hookrightarrow (\mathbf{6}, \mathbf{6})$ ; EW-breaking vev also breaks flavour symmetry
- The “extra ingredients” here come for free, as the extra Higgs-like scalars!

Davighi, Tooby-Smith, [2201.07245](#)

Davighi, [2206.04482](#)



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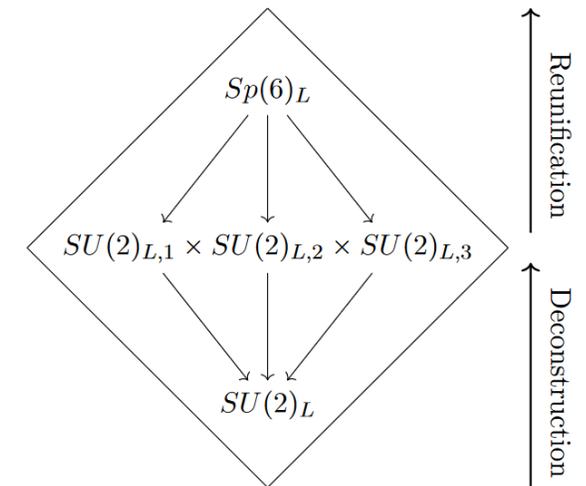
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Davighi, Tooby-Smith, [2201.07245](#)

Davighi, [2206.04482](#)

BUT: flavour-universal  $SU(4)$  breaking must be  $\gtrsim 200$  TeV due to  $K_L \rightarrow e^+ \mu^-$   
vs. natural scale for  $SU(4)$  breaking is 10 (80) TeV

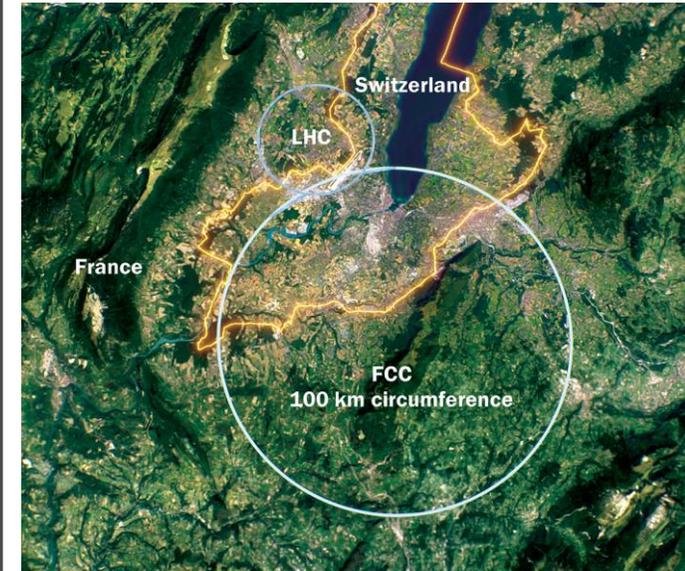
A natural realisation could require e.g. SUSY < 80 TeV





# 4. Phenomenology: Present & Future

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# Flavoured SM gauge bosons

- High-scale breaking  $G_{SM,1} \times G_{SM,2} \rightarrow G_{SM,12}$  gives  $U(2)$ -violation; typically there is **one dominant meson mixing constraint** e.g. kaon,  $D$ -meson mixing
- **Low-energy** pheno of all these models dominated by the low-scale breaking  $G_{SM,12} \times G_{SM,3} \rightarrow G_{SM}$
- Gives heavy gauge bosons in adjoint, coupled to flavour-non-universal fermion current:

$$J^\mu \sim g_{12}^2 (J_1^\mu + J_2^\mu) - 2g_3^2 J_3^\mu, \quad J_3^\mu \supset D_{SM}^\mu H$$

- One can pump up the (relative) coupling to the heavy or light families by varying  $g_{12}/g_3$ .
- BUT we **cannot decouple either** completely, because there is a matching condition

$$\frac{1}{g^2} = \frac{1}{g_{12}^2} + \frac{1}{g_3^2} \Rightarrow g_{12}, g_3 > g$$

Parametrization:  $g_{SM} = g_3 \cos \theta = g_2 \sin \theta \cos \phi = g_1 \sin \theta \sin \phi$

Contrast these explicit models with simplified  $U(2)$ -based SMEFT analysis, in which the light generations can be decoupled – see Claudia's talk

# Flavoured SM gauge bosons

$$J^\mu \sim g_{12}^2 (J_1^\mu + J_2^\mu) - 2g_3^2 J_3^\mu, \quad J_3^\mu \supset D_{\text{SM}}^\mu H, \quad g_{12}, g_3 > g$$

Focus on deconstructed EW bosons,  $SU(2)_{L,12} \times SU(2)_{L,3}$  and  $U(1)_{Y,12} \times U(1)_{Y,3}$

[The  $SU(4)_3 \times SU(3)_{12}$  phenomenology is well-explored in B-anomaly context]

Important SMEFT operators:

	Flavour (mixing, $bs\mu\mu$ )	LHC Drell-Yan $pp \rightarrow ll$ ( $lv$ )	Electroweak Precision
$SU(2)_{L,12} \times SU(2)_{L,3}$	$O_{qq}^{(3)}, O_{lq}^{(3)}$	$O_{lq}^{(3)}$ ( $ll$ and $lv$ )	$O_{Hq}^{(3)}, O_{Hl}^{(3)}$
$U(1)_{Y,12} \times U(1)_{Y,3}$	$O_{qq}^{(1)}, O_{dd} \dots, O_{lq}^{(1)}, O_{qe}, \dots$	$O_{lq}^{(1)}, O_{qe}, O_{eu}, O_{ed}, \dots$	$O_{Hq}^{(1)}, O_{Hl}^{(1)}, O_{He}, \dots, O_{HD}$

**Current bounds:** all 3 observable classes give very complementary constraints!

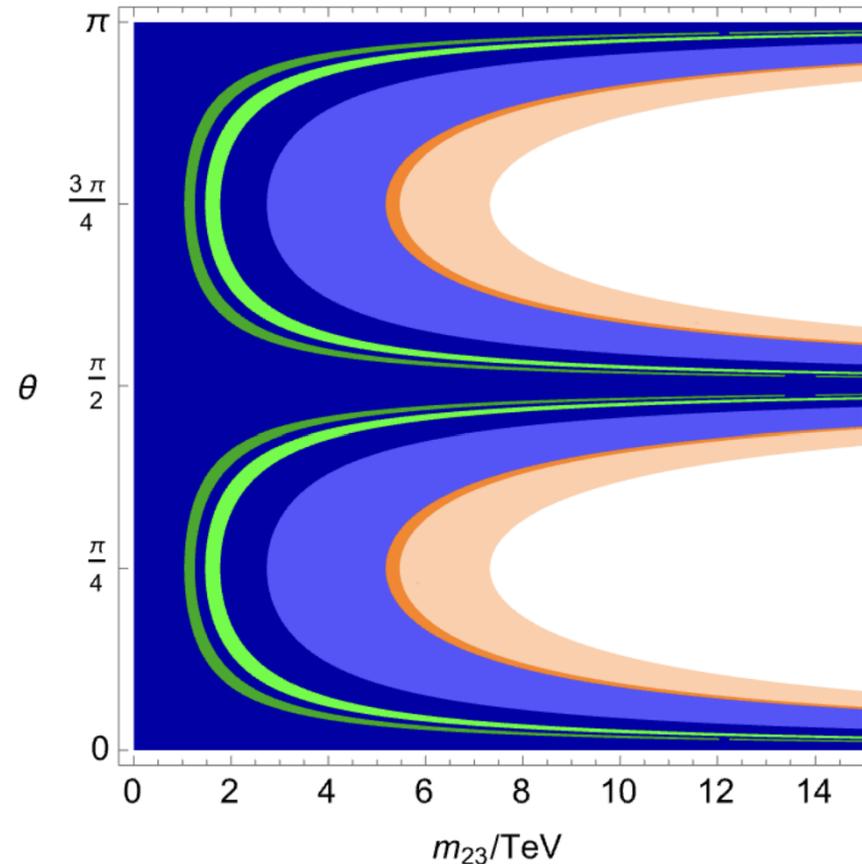
# Deconstructed $SU(2)_L$

Davighi, Gosnay, Miller, Renner [2312.13346](#)

See also Capdevila, Crivellin, Lizana, Pokorski [2401.00848](#)

	Quark Flavour bounds (meson mixing, $bs\mu\mu$ )	LHC Drell-Yan $pp \rightarrow ll (lv)$	Electroweak Precision, LFUV in $\tau$ decays
$SU(2)_{L,12} \times SU(2)_{L,3}$	$O_{qq}^{(3)}, O_{lq}^{(3)}$	$O_{lq}^{(3)}$ ( $ll$ and $lv$ )	$O_{Hq}^{(3)}, O_{Hl}^{(3)}$

Quark Flavour



[Charged current unimportant]

- $B_s \rightarrow \mu\mu$  (up-alignment)
- $B_s \rightarrow \mu\mu$  ( $[V_d]_{32}^* = V_{cb}/2$ )
- $B_s$  mixing (up-alignment)
- $B_s$  mixing ( $[V_d]_{32}^* = V_{cb}/2$ )
- $B \rightarrow K^{(*)} \nu\nu$  favoured region (up-alignment)
- $B \rightarrow K^{(*)} \nu\nu$  favoured region ( $[V_d]_{32}^* = V_{cb}/2$ )

The model predicts  $C_L = 0$  for  $bs$  coupling to 3<sup>rd</sup> generation neutrinos; so cannot enhance  $b \rightarrow s\nu\nu$  w.r.t  $b \rightarrow s\mu\mu$

# Deconstructed $SU(2)_L$

Davighi, Gosnay, Miller, Renner [2312.13346](#)

See also Capdevila, Crivellin, Lizana, Pokorski [2401.00848](#)

	Quark Flavour bounds (meson mixing, $bs\mu\mu$ )	LHC Drell-Yan $pp \rightarrow ll$ ( $lv$ )	Electroweak Precision, LFUV in $\tau$ decays
$SU(2)_{L,12} \times SU(2)_{L,3}$	$O_{qq}^{(3)}, O_{lq}^{(3)}$	$O_{lq}^{(3)}$ ( $ll$ and $lv$ )	$O_{Hq}^{(3)}, O_{Hl}^{(3)}, O_{ll}$

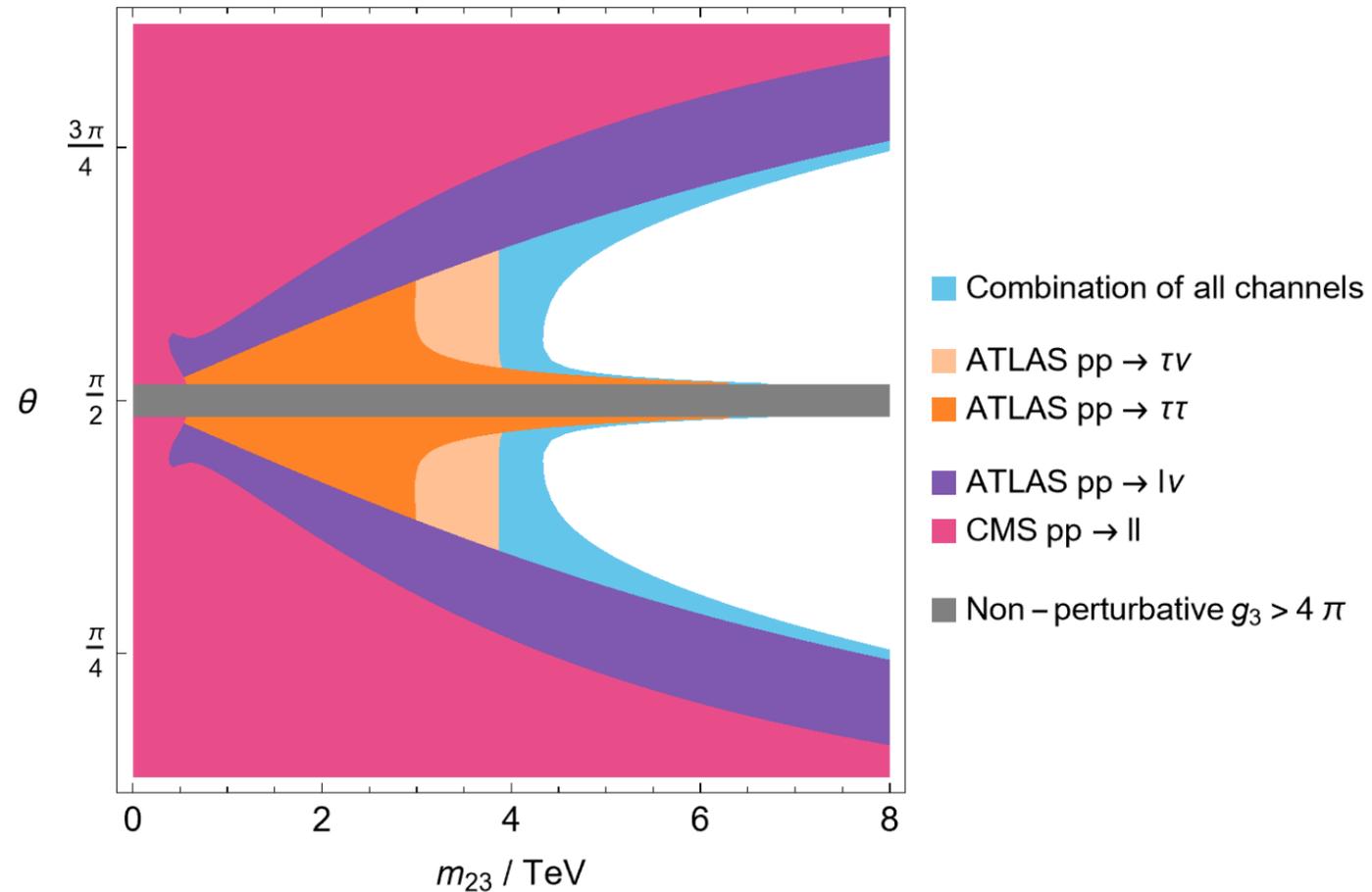
## LHC Drell—Yan

Computed using **HighPT**

Allwicher et al, [2207.10756](#)

LHC searches all using  $139 \text{ fb}^{-1}$ :

[2002.12223](#), [ATLAS-CONF-2021-025](#), [CMS, 2103.02708](#), [ATLAS, 1906.05609](#)



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## Electroweak

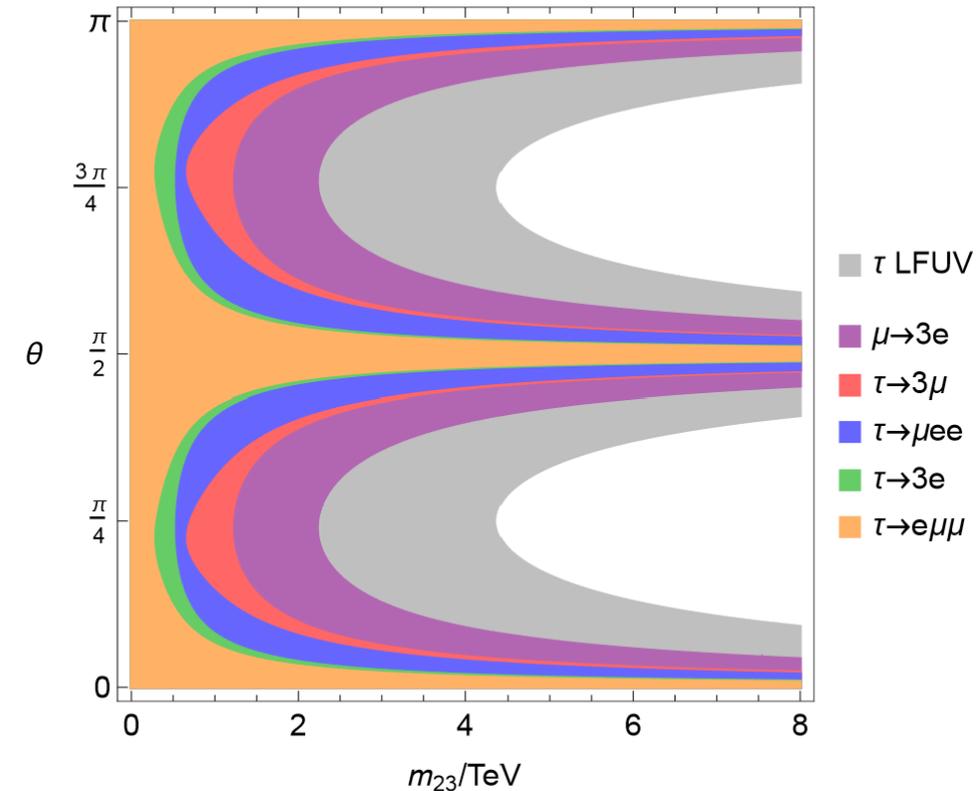
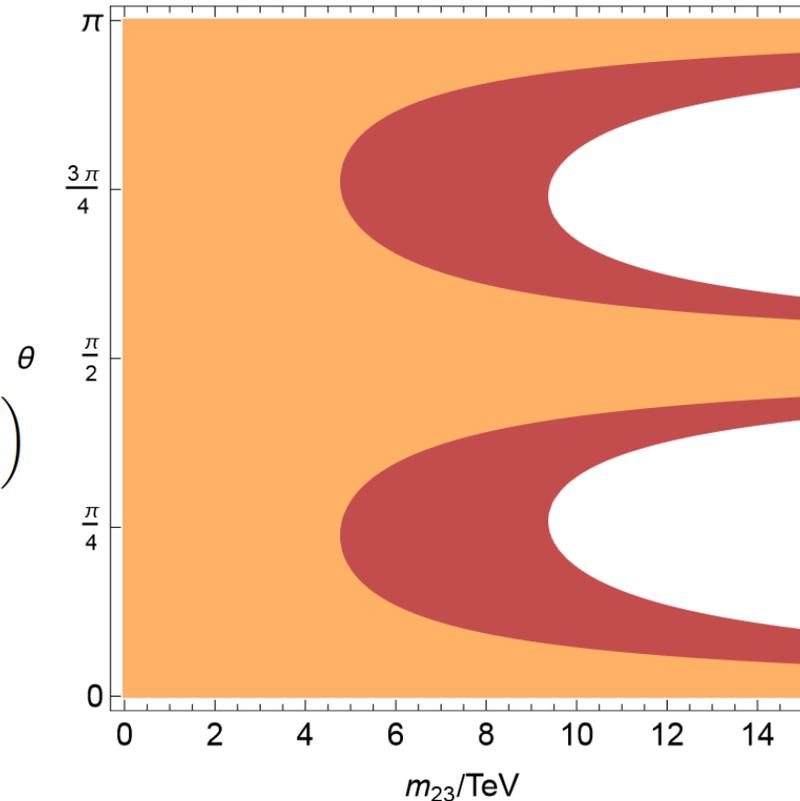
- EW fit (with  $m_W$  (2017))
- EW fit (without  $m_W$ )

Model predicts negative shift in  $m_W$

$$\delta m_W^2 = (m_W^2)_{\text{SM}} \Delta \frac{s_W}{c_W} g_{\text{SM}}^2 \left( \frac{2 + \cot^2 \theta}{2m_{23}^2} \right)$$

$$\Delta = 2\sqrt{2}G_{FCW}s_W/(c_W^2 - s_W^2)$$

Due to observed positive shift (excluding CDF'2022),  $m_W$  has huge effect on EW fit



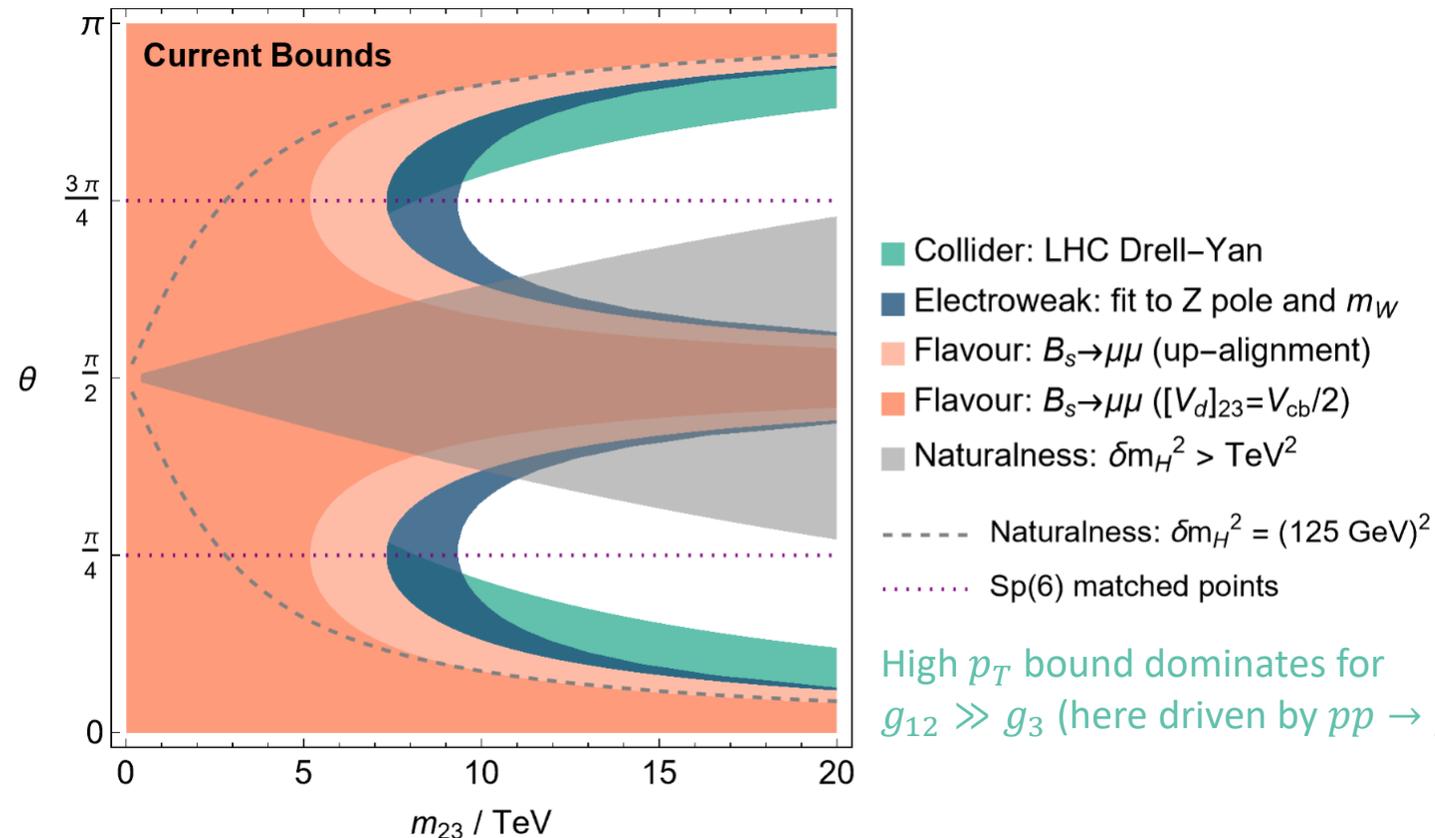
# Deconstructed $SU(2)_L$

Davighi, Gosnay, Miller, Renner [2312.13346](#)

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Kaon mixing can be satisfied for  $m_{12}$  as light as 160 TeV, for  $g_1 = g_2$ . For the  $W_{23}$  triplet:



$$M_{W'_L, Z'_L} > 9.5 \text{ TeV}$$

Driven by EWPOs (LEP II + W mass), with flavour and LHC highly complementary

Plenty of **natural** parameter space remains!

# Deconstructed $U(1)_Y$

Davighi, Stefanek [2305.16280](#)

Expect to provide the **most natural** model; double benefit from  $g_Y \sim g_L/2$

1. Roughly x2 smaller Higgs mass correction
2. Roughly x2 smaller NP effects

See also

Fernández Navarro, King [2305.07690](#)

Allanach, Davighi [1809.01158](#)

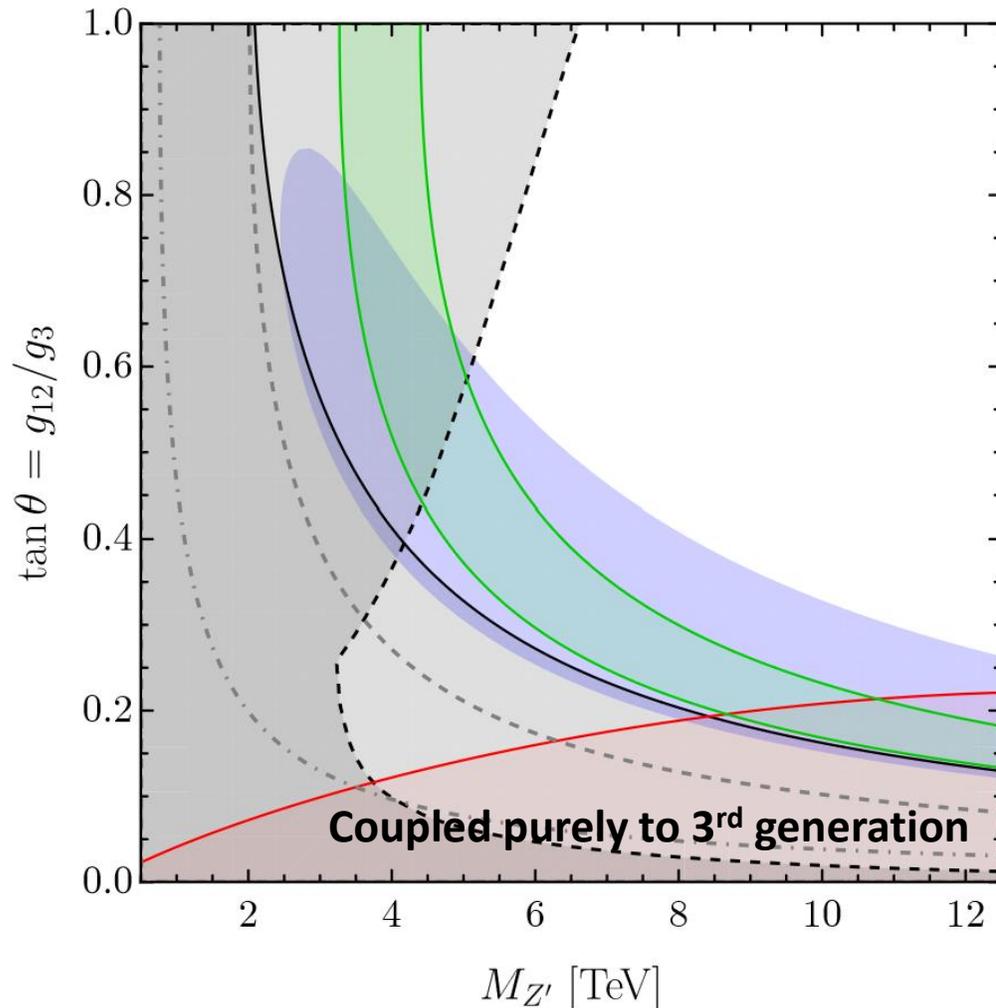
	Flavour (mixing, $bs\mu\mu$ )	LHC Drell-Yan $pp \rightarrow ll$	Electroweak Precision
$U(1)_{Y,12} \times U(1)_{Y,3}$	$O_{qq}^{(1)}, O_{dd}, \dots, O_{lq}^{(1)}, O_{qe}, \dots$	$O_{lq}^{(1)}, O_{qe}, O_{ew}, O_{ed}, \dots$	$O_{Hq}^{(1)}, O_{Hl}^{(1)}, O_{He}, \dots, O_{HD}$

LL 4-quark operators especially small thanks to  $Y_Q g_Y \sim 1/18$

+ve shift in  $M_W$  currently preferred by EW fit (even ignoring CDF II measurement)

# Deconstructed $U(1)_Y$

Davighi, Stefaneke [2305.16280](#)



- $B_s$  mixing (with up-alignment! Suppressed by  $Y_Q g_Y$ )
- $B_s \rightarrow \mu\mu$  exclusion (strong-ish because our  $bs\mu\mu$  is  $\approx C_{10}$ )
- Electroweak fit (1 sigma) using a new  $M_W$  average
- Electroweak fit (2 sigma exclusion) excluding CDF II  $M_W$
- High  $p_T$  exclusion (recast of  $pp \rightarrow ee, \mu\mu, \tau\tau$  searches)
- Percent tuning in  $M_h^2$
- A “natural” explanation of fermion mass hierarchies

$$M_{Z'_Y} \gtrsim 4 \text{ TeV}$$

- As for deconstructed  $SU(2)_L$ , lowest allowed mass from intersection of high  $p_T$  + EWPO
- Lighter mass (more natural) allowed, as anticipated

## Looking to the Future

We have seen that flavour-deconstructing electroweak gauge interactions, to explain the flavour puzzle, gives big effects in EWPOs.

**FCC-ee is an amazing opportunity** to probe these models, and cover the parameter space in which they remain natural.

But there are also shorter-term prospects to be excited about...

# Deconstructed $SU(2)_L$ : Future Prospects

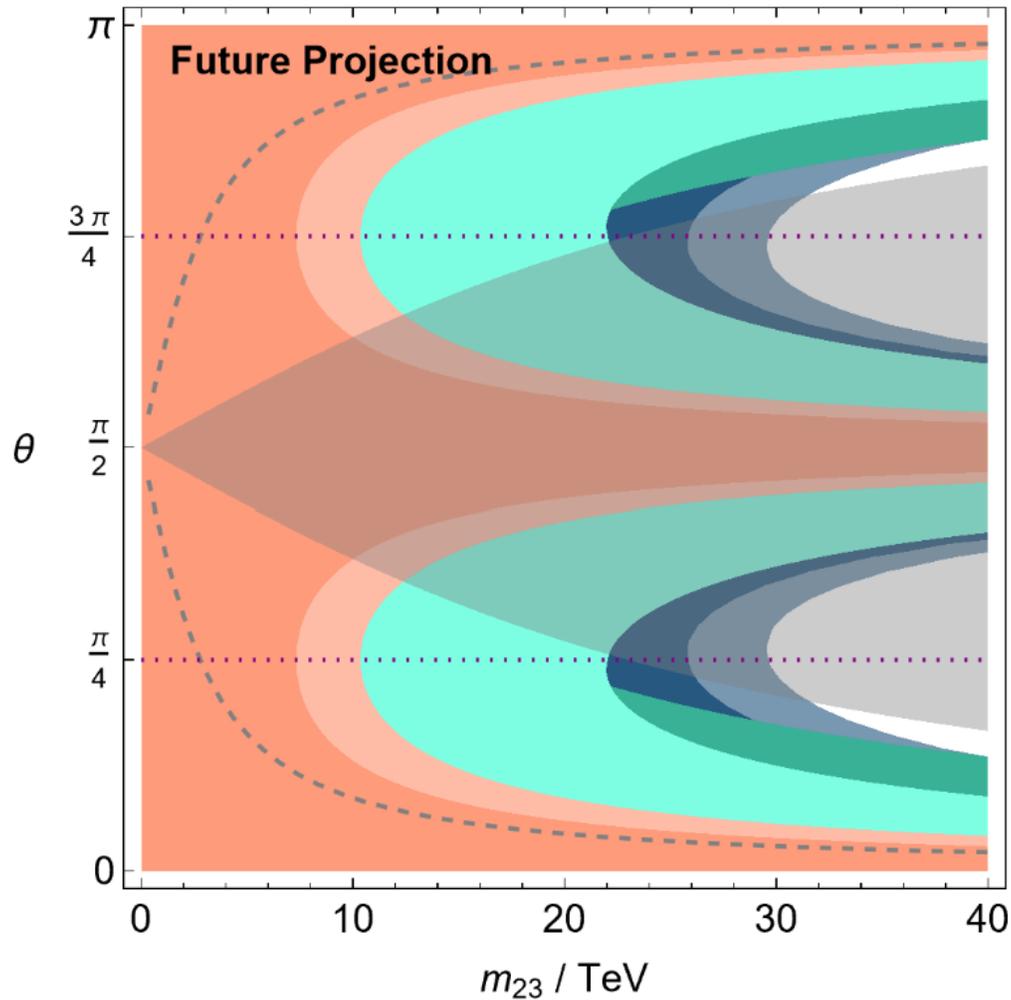
Davighi, Gosnay, Miller, Renner [2312.13346](#)

We perform the following studies of future sensitivities to the  $W_{23}$  gauge bosons

- HL-LHC projections for Drell—Yan, assuming  $3 \text{ ab}^{-1}$  integrated lumi and SM bkg rate in all bins, implemented in *HighPT*
- HL-LHC projection for  $BR(B_s \rightarrow \mu\mu)$ , the most important flavour constraint on the model; use LHCb expected precision of 4.4% [HL-LHC Working Group 4 1812.07638](#)
- EWPOs from FCC-ee Z pole run, taking projections from [de Blas et al [2206.08326](#)], plus  $m_W$  plus “off-peak” constraints on 4-lepton operators (assuming SM central values)
- Conservative estimate of FCC-ee improvements in  $\tau$ LFUV ratios
- LFV tests from Belle II (tau decays), and huge leap in sensitivity from Mu3e

# Deconstructed $SU(2)_L$ : Future Prospects

Davighi, Gosnay, Miller, Renner [2312.13346](#)



- Electroweak: projected FCC-ee including off-Z-peak
- Electroweak: projected FCC-ee, Z-pole observables only
- Collider: projected Drell-Yan at HL-LHC
- cLFV: projected  $\mu \rightarrow 3e$  at Mu3e (CKM-like leptons)
- Flavour: projected  $B_s \rightarrow \mu\mu$  at HL-LHC (up-alignment)
- Flavour: projected  $B_s \rightarrow \mu\mu$  at HL-LHC ( $[V_d]_{23} = V_{cb}/2$ )
- Naturalness:  $\delta m_H^2 > \text{TeV}^2$

--- Naturalness:  $\delta m_H^2 = (125 \text{ GeV})^2$

⋯ Sp(6) matched points

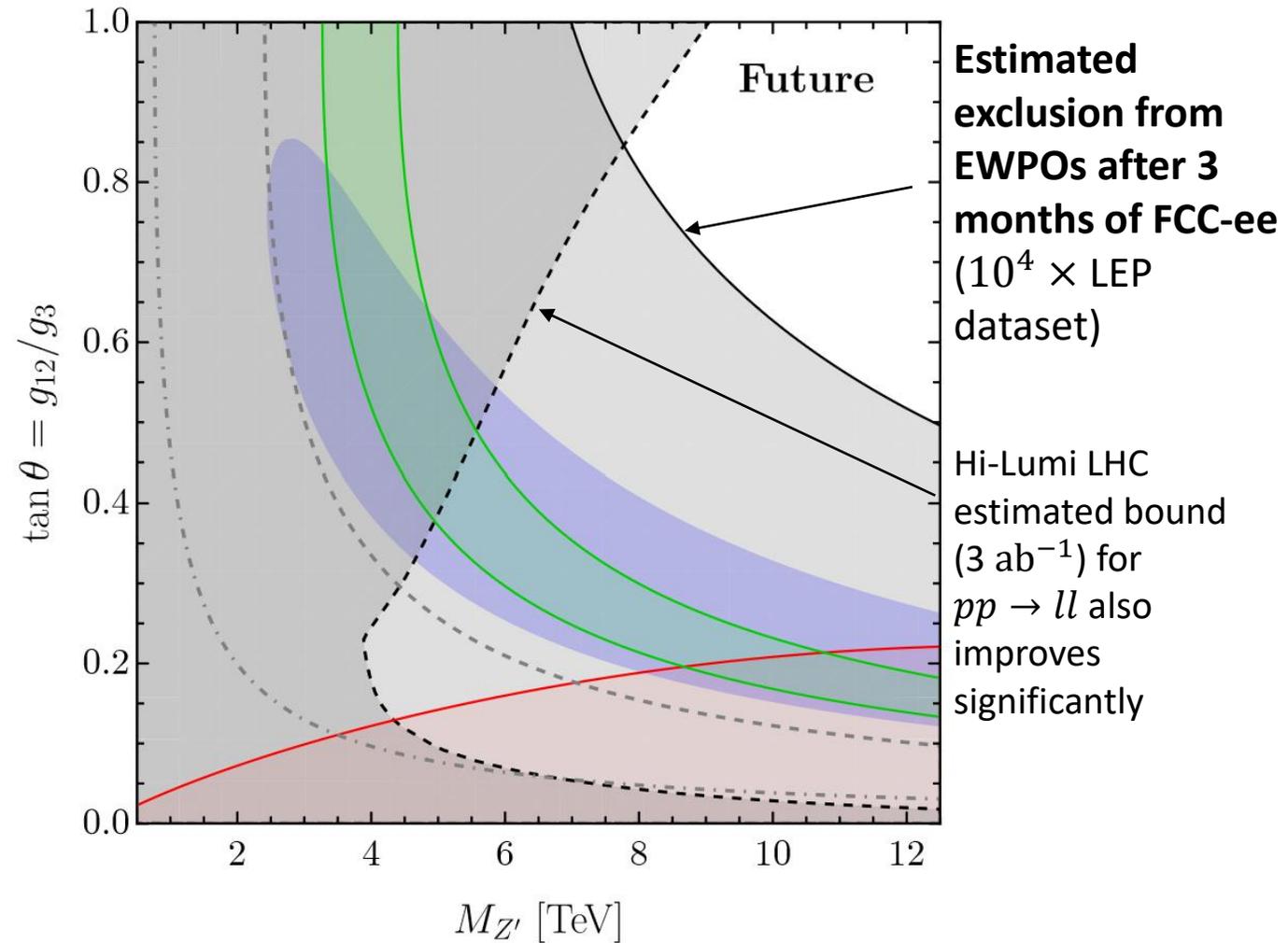
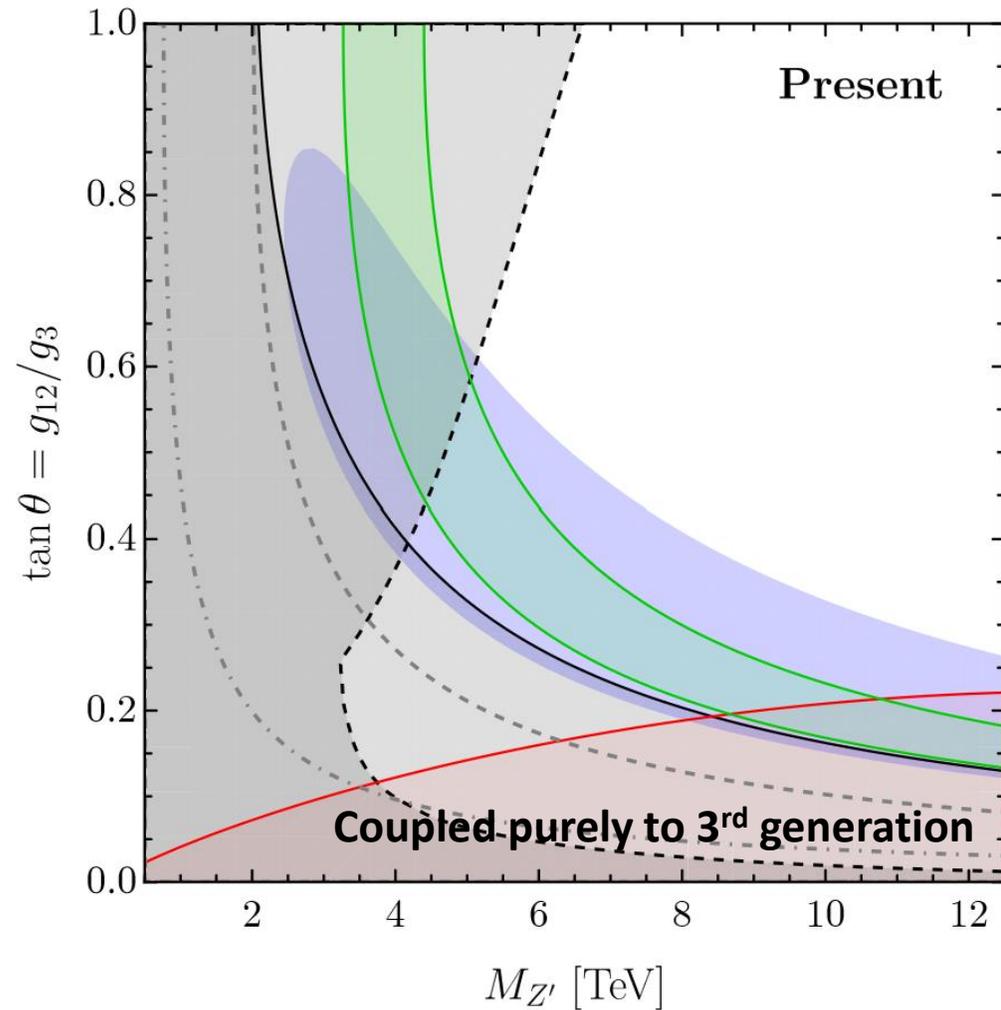
HL-LHC Drell-Yan and Mu3e rule out impressive parameter space in the medium term before FCC-ee

$$M_{W'_L, Z'_L} > 30 \text{ TeV}$$

Entire natural parameter space almost covered

# Deconstructed $U(1)_Y$ $Z'$ boson

Davighi, Stefaneck [2305.16280](#)



Key message:

1. “Deconstructing” SM gauge interactions offers well-motivated solutions to flavour puzzle; current measurements allow significant natural\* parameter space
2. Future experiments, especially an EW precision machine like **FCC-ee** but also HL-LHC, Belle II, Mu3e, ..., will cover this natural parameter space

Thank you!

# Backup

# Semi-simple UV completions

Nice UV requirement:  $\exists$  embedding  $G \hookrightarrow$  semi-simple i.e. no fundamental gauged  $U(1)$ s:

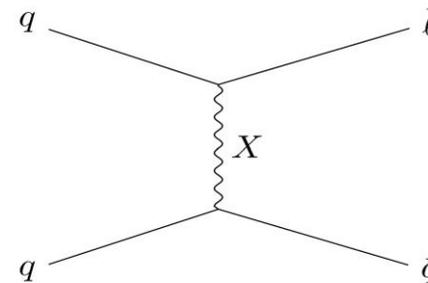
- “Explain” hypercharge quantisation and origin of SM fermion reps
- has a shot at asymptotic freedom (couplings become weaker in UV)

Combined with finite naturalness + assuming no extra fermions, this greatly restricts space of UV models

- All semi-simple extensions of 3-generation SM are classified; [Allanach, Gripaos, Tooby-Smith, 2104.14555](#)
- All feature one of the basic “vertical” unification patterns of Pati—Salam  $SU(4) \times SU(2)_L \times SU(2)_R$ , or  $SU(5)$  or  $SO(10)$  [Pati, Salam, 1974](#), [Georgi, Glashow, 1974](#), [Georgi, 1975](#), [Fritzsch, Minkowski, 1975](#)



$SU(5)$  &  $SO(10)$  feature LQs that give tree-level proton decay!  $\Rightarrow M_X \gtrsim$  GUT scale  
So  $SU(5)$  &  $SO(10)$ -based options cannot appear in low-scale natural models



$\therefore$  vertical unification structure requires  $SU(4)$ s and  $SU(2)_R$ s

# Semi-simple UV completions

From our bottom-up  $G_U \times H_{12} \times G_3$ , we have 4 options (up to choices of  $H_{12}$ )

Davighi, Isidori [2303.01520](#)

	$G_U$	$G_3$	$H_{12}$	Flavour structure
Model 1	$SU(2)_L$	$SU(4)^{[3]} \times SU(2)_R^{[3]}$	$\times$	$\begin{pmatrix} \epsilon_R & \epsilon_\Omega \\ \epsilon_R \epsilon_\Omega & 1 \end{pmatrix}$ <input checked="" type="checkbox"/> <input checked="" type="checkbox"/>
Model 2	$SU(2)_R$	$SU(4)^{[3]} \times SU(2)_L^{[3]}$	$\times$	$\begin{pmatrix} \epsilon_L & \epsilon_\Omega \epsilon_L \\ \epsilon_\Omega & 1 \end{pmatrix}$ <input type="checkbox"/>
Model 3	$SU(4)$	$SU(2)_L^{[3]} \times SU(2)_R^{[3]}$	$\times$	$\begin{pmatrix} \epsilon_L \epsilon_R & \epsilon_L \\ \epsilon_R & 1 \end{pmatrix}$ <input checked="" type="checkbox"/>
Model 4	$\emptyset$	$SU(4)^{[3]} \times SU(2)_L^{[3]} \times SU(2)_R^{[3]}$	$\times$	$\begin{pmatrix} \epsilon_L \epsilon_R & \epsilon_\Omega \epsilon_L \\ \epsilon_R \epsilon_\Omega & 1 \end{pmatrix}$ <input checked="" type="checkbox"/>



Higgs and  $\psi_3$ ,  
dominate  $M_h^2$

$\psi_{1,2}$ , small impact on  $M_h^2$ ,  
can UV complete at higher  $E$

## Minimal Flavour Deconstruction:

An Abelian model that fits inside model 1 was recently explored in [[Barbieri, Isidori, 2312.14004](#)]

# What is the origin of the flavour deconstruction?

$G_{SM,12} \times G_{SM,3} \rightarrow G_{SM}$  could be last step in a **multi-scale** breaking from fully deconstructed  $G_1 \times G_2 \times G_3$ ; scale hierarchy  $\Lambda_{12} > \Lambda_3$ ;  $G_1 \times G_2 \rightarrow G_{12}$  breaking resolves 1-2 substructure

*Example origin 3:*

“Hybrid” approach prioritizing flavour and naturalness:

$$G = SU(2)_L \times \underbrace{SU(4)^3}_{V_{cb}} \times \underbrace{SU(4)^{12}}_{m_2/m_3} \times \underbrace{SU(2)_R^3}_{m_1/m_2} \times Sp(4)_R^{12}$$

Davighi, Isidori [2303.01520](#)

- ✓ Realises “Model 1” with nicest flavour structure
- ✓ Keeping  $SU(2)_L$  **universal** helps “seclude”  $\delta M_h^2$  from large corrections
- ✓ Complete model has all 1-loop gauge beta functions negative

# Deconstructed $U(1)_Y Z'$ boson: model details

Expect to provide the **most natural** model; double benefit from  $g_Y \sim g_L/2$

1. Roughly x2 smaller Higgs mass correction Davighi, Stefaneke [2305.16280](#)
2. Roughly x2 smaller NP effects

	Flavour (mixing, $bs\mu\mu$ )	LHC Drell-Yan $pp \rightarrow ll$	Electroweak Precision
$U(1)_{Y,12} \times U(1)_{Y,3}$	$O_{qq}^{(1)}, O_{dd}, \dots, O_{lq}^{(1)}, O_{qe}, \dots$	$O_{lq}^{(1)}, O_{qe}, O_{eu}, O_{ed}, \dots$	$O_{Hq}^{(1)}, O_{Hl}^{(1)}, O_{He}, \dots, O_{HD}$

Explicit model:

- TeV:  $U(1)_{Y_{12}} \times U(1)_{Y_3} \rightarrow U(1)_Y$  by two scalars  $\Phi_{q,H}$  (realises “model 1” flavour structure)
- Light Yukawas generated by UV states at  $\sim 10$  TeV (safe choice of  $U(2)$ -breaking spurions):

Field	$SU(3)_c$	$SU(2)_L$	$U(1)_3$	$U(1)_{12}$	Generates:
$H_{12}$	<b>1</b>	<b>2</b>	0	1/2	$y_{c,s,\mu,u,d,e}, V_{us}$
$Q_{L,R}$	<b>3</b>	<b>2</b>	1/6	0	$V_{cb}, V_{ub}$

$$\frac{y_c}{y_t} \approx \frac{y_u^2}{y_u^3} \frac{f\langle\Phi_H\rangle}{m_{12}^2}$$

- RH mixing is zero at tree-level
- Semi-simple UV completion? Assume layer of SUSY / compositeness first kicks in around 10 TeV (for “best possible” solution to the *large* hierarchy problem)