



Matteo Cadeddu matteo.cadeddu@ca.infn.it



In collaboration with M. Atzori Corona, N. Cargioli, F. Dordei, C. Giunti

A bird's eye view: global analysis of nuclear and electroweak properties and the role of CEvNS



For a recent review see Europhysics Letters, Volume 143, Number 3, 2023 (EPL 143 34001), <u>arXiv:2307.08842v2</u>

Coherent elastic neutrino nucleus scattering (aka CEνNS)

+A pure weak neutral current process

$$\frac{d\sigma_{\nu_{\ell}-\mathcal{N}}}{dT_{\mathrm{nr}}}(E,T_{\mathrm{nr}}) = \frac{G_{\mathrm{F}}^2 M}{\pi} \left(1 - \frac{MT_{\mathrm{nr}}}{2E^2}\right) (Q_{\ell,\mathrm{SM}}^V)^2$$

+Weak charge of the nucleus

$$Q_{\ell,SM}^{V} = \begin{bmatrix} g_{V}^{p}(\nu_{\ell}) ZF_{Z}(|\vec{q}|^{2}) + g_{V}^{n}NF_{N}(|\vec{q}|^{2}) \end{bmatrix}$$

protons

In general, in a weak neutral current process which involves nuclei, one deals with **nuclear form factors** that are different for protons and neutrons and cannot be disentangled from the neutrino-nucleon couplings!



J. Erler and S. Su. *Prog. Part. Nucl. Phys.* 71 (2013). arXiv:1303.5522 & PDG2023 and **M. Atzori Corona et al. arXiv:2402.16709**

+ Neutrino-nucleon tree-level couplings $g_V^p = \frac{1}{2} - 2 \sin^2(\vartheta_W) \cong 0.02274$ $g_V^n = -\frac{1}{2} = -0.5$ See F. Dordei's talk on radiative corrections

+ Radiative corrections are expressed in terms of WW, ZZ boxes and the <u>neutrino</u> <u>charge radius</u> diagram → <u>Flavour dependence</u>

$$g_V^p(\nu_e) \simeq 0.0381, \, g_V^p(\nu_\mu) \simeq 0.0299 \quad g_V^n \simeq -0.5117$$

Nuclear physics, but since $g_V^n \approx -0.51 \gg g_V^p(v_\ell) \approx 0.03$ neutrons contribute the most



What we can learn from $CE\nu NS$



Interplay between nuclear and electroweak physics

- +This feature is always present when dealing with electroweak processes.
- Atomic Parity Violation (APV): atomic electrons interacting with nuclei- Cesium (Cs) and lead (Pb) available.
- Parity Violation Electron Scattering (PVES): polarized electron scattering on nuclei- PREX(Pb) & CREX(Ca)
- Coherent elastic neutrino-nucleus scattering (CEvNS)-Cesium-iodide (CsI), argon (Ar) and germanium (Ge) available.





Where did we leave off at the last MG7 edition?



The CsI neutron skin fixing $\sin^2(\vartheta_W)$

If we fix the value of $\sin^2 \vartheta_W$ at the SM prediction (0.23863(5)) then we obtain (1D fit):

M. Atzori Corona et al., EPJC 83 (2023) 7, 683
 arXiv:2303.09360

 R_n (CsI) = 5.47 ± 0.38 fm

 \sim 7% precision

Neutron skin: R_n (CsI)- R_p (CsI)

 $\Delta R_{np}(CsI) = 0.69 \pm 0.38 \, \text{fm}$

Theoretical values of the neutron skin of Cs and I obtained with nuclear mean field models. The value is compatible with all the models...

 127τ

 $0.12 < \Delta R_{np}^{CsI} < 0.24 \text{ fm}$

1330-

tron Sk	$\frac{N}{S}$
u	S
e ke	S
NI TO KR	$\tilde{\mathbf{S}}$
	S
	S
	S
	\mathbf{S}

					1						\mathbf{Cs}		
	Model	R_p^{point}	R_p	R_n^{point}	R_n	$\Delta R_{np}^{\text{point}}$	ΔR_{np}	R_p^{point}	R_p	R_n^{point}	R_n	$\Delta R_{np}^{\text{point}}$	ΔR_{np}
	SHF SkI3 81	4.68	4.75	4.85	4.92	0.17	0.17	4.74	4.81	4.91	4.98	0.18	0.18
	SHF SkI4 81	4.67	4.74	4.81	4.88	0.14	0.14	4.73	4.80	4.88	4.95	0.15	0.14
1	SHF Sly4 82	4.71	4.78	4.84	4.91	0.13	0.13	4.78	4.85	4.90	4.98	0.13	0.13
1	SHF Sly5 82	4.70	4.77	4.83	4.90	0.13	0.13	4.77	4.84	4.90	4.97	0.13	0.13
	SHF Sly6 82	4.70	4.77	4.83	4.90	0.13	0.13	4.77	4.84	4.89	4.97	0.13	0.13
	SHF Sly4d 83	4.71	4.79	4.84	4.91	0.13	0.12	4.78	4.85	4.90	4.97	0.12	0.12
1	SHF SV-bas 84	4.68	4.76	4.80	4.88	0.12	0.12	4.74	4.82	4.87	4.94	0.13	0.12
1	SHF UNEDF0 85	4.69	4.76	4.83	4.91	0.14	0.14	4.76	4.83	4.92	4.99	0.16	0.15
	SHF UNEDF1 86	4.68	4.76	4.83	4.91	0.15	0.15	4.76	4.83	4.90	4.98	0.15	0.15
	SHF SkM* 87	4.71	4.78	4.84	4.91	0.13	0.13	4.76	4.84	4.90	4.97	0.13	0.13
	SHF SkP 88	4.72	4.80	4.84	4.91	0.12	0.12	4.79	4.86	4.91	4.98	0.12	0.12
	RMF DD-ME2 89	4.67	4.75	4.82	4.89	0.15	0.15	4.74	4.81	4.89	4.96	0.15	0.15
	RMF DD-PC1 90	4.68	4.75	4.83	4.90	0.15	0.15	4.74	4.82	4.90	4.97	0.16	0.15
	RMF NL1 91	4.70	4.78	4.94	5.01	0.23	0.23	4.76	4.84	5.01	5.08	0.25	0.24
	RMF NL3 92	4.69	4.77	4.89	4.96	0.20	0.19	4.75	4.82	4.95	5.03	0.21	0.20
	RMF NL-Z2 93	4.73	4.80	4.94	5.01	0.21	0.21	4.79	4.86	5.01	5.08	0.22	0.22
	RMF NL-SH 94	4.68	4.75	4.86	4.94	0.19	0.18	4.74	4.81	4.93	5.00	0.19	0.19





The strategy **APV (Cs)**

+ Sensitive to the weak mixing angle + Similarly sensitive to the neutron skin

COHERENT (Csl)

- $+ CE_{\nu}NS$ is sensitive to the neutron skin
- + But less sensitive to the weak mixing angle

0.250 $\sin^2 \vartheta_{\rm W}({\rm COH-CsI}) = 0.231^{+0.027}_{-0.024}(1\sigma)^{+0.046}_{-0.039}(90\%{\rm CL})^{+0.058}_{-0.047}(2\sigma)$ APV only 68.27% CL 90.00% CL 0.26F95.45% CL 99.00% CL 0.245 99.73% CL 0.25 $^{SM}(m)$ **COHERENT CsI** E158 APV(Cs) (fixed skin) 0.240 $\sin^2 \theta_W$ 0.24 Free-neutron skin (ee) $\sin^2 \vartheta_W$ (LEP Q_{weak} APV(Cs) LHC APV (ep) 0.23 SLC PDG **PVDIS** 0.235 PDG2020 Tevatron⁻⁻ $\Delta R_{np}^{Cs} = 0.13 \text{ fm}$ APV(Cs) PDG $(e^{2}\mathrm{H})$ Free neutron 0.22 corresponds to 0.230 $\Delta R_{np}^{Cs}(Extr.) = 0.13 \text{ fm}$ 0.21 skin Extrapolated from 0.001 0.010 0.100 10 100 1000 0.225 antiprotonic atoms... 0.0 0.2 0.6 0.4 μ [GeV] ΔR_{np} [fm] Why not combining them

Combined fit of COHERENT and APV(Cs)

 $R_n(\text{CsI})=5.5^{+0.4}_{-0.4} \text{ fm } \sin^2 \vartheta_W = 0.2423^{+0.0032}_{-0.0029} \chi^2_{\text{min}} = 85.1$



Where are we now?

M. Atzori Corona et al. Refined determination of the weak mixing angle at low energy, <u>arXiv:2405.09416</u> (2024)

Cs neutron skin from proton-elastic scattering

New measurement from **proton-cesium elastic scattering at low momentum transfer** using an in-ring reaction technique at the **Cooler Storage Ring** (**CSRe**) at the Heavy lon Research Facility in Lanzhou, which can be included in the derivation of $\sin^2 \vartheta_W$. The authors employed this value to re-extract the COHERENT $\sin^2 \vartheta_W$ value by fitting the CEvNS Csl dataset, finding $\sin^2 \vartheta_W = 0.227 \pm 0.028$.

New direct measurement of the cesium-133 neutron skin, $\Delta R_{np}(Cs) = 0.12 \pm 0.21$ fm available!

+ Experiments with hadronic probes are more precise BUT result interpretation of hadronic probe experiments is difficult due to the complexity of strong-force interactions.



Hovewer, this is the first **DIRECT** determination of R_n(Cs)!



"Cesium neutron radius determination with hadronic probes has been historically experimentally challenging due to the low melting point and spontaneous ignition in air."

First results: fit using R_n(Cs) from CSRe

ES

 + We combine APV(Cs) and COHERENT CsI adding a prior on R_n(Cs)= 4.94 ± 0.21 fm coming from the Cooler Storage Ring (CSRe)

$\sin^2 \vartheta_W$	$R_n(^{133}Cs)[fm]$
$0.2396\substack{+0.0020\\-0.0019}$	5.04 ± 0.19

Big improvement with respect to our previous result (arXiv:2303:09360):

 $\sin^2 \vartheta_W = 0.2423^{+0.0032}_{-0.0029}, \ R_n(\text{CsI}) = 5.5^{+0.4}_{-0.4} \text{ fm}$

 ✓ Pros: For the first time a direct measurement on R_n(Cs) is used

Cons: CSRe R_n(Cs) still comes from hadronic probes...

Can we use electroweak only inputs?



ElectroWeak only fit

- + We perform a fit using Electroweak (EW) only information removing the R_n(Cs) input from CSRe
- + APV(Cs) 21
- + COHERENT CsI

+ APV(Pb)+PREX-II

- M. Atzori Corona et al. PRC 105, 055503 (2022), Arxiv: 2112.09717,
- APV has been measured also using lead.
- Moreover PREX-II has measured the Pb neutron skin with Parity Violation Electron Scattering (PVES).

0.30

We can profit from a 0.25 [پ very nice correlation (¹³³Cs) between $R_{n}(Cs)$ and 0.20 R_n(Pb) within many ∆Rpoint ARpoint 0.15 theoretical nuclear models to translate $R_n(Pb)$ to $R_n(Cs)$ non-EW on Pb 0.10 0.15 0.20 0.25 0.30 0.10 - M. Cadeddu et al. ΔR_{np}^{point} (²⁰⁸Pb) [fm]

[」] PRD **104**, 011701 (2021), arXiv:2104.03280



 $R_n(Pb)$ to $R_n(Cs)$





Conclusions for $\sin^2 \vartheta_W$





Thanks for your attention!

BACKUP



Global 1 sigma with APV(21)



Using ImE_{PNC} PDG





Using ImE_{PNC} PDG





Global using ImE_{PNC} PDG



Atomic Parity Violation in cesium APV(Cs)



Interaction mediated by the photon and so mostly sensitive to the charge (proton) distribution Interaction mediated by the Z boson and so mostly sensitive to the weak (neutron) distribution. [–] M. Cadeddu and F. Dordei, PRD 99, 033010 (2019), arXiv:1808.10202

- Parity violation in an atomic system can be observed as an electric dipole transition amplitude between two atomic states with the same parity, such as the 6*S* and 7*S* states in cesium.
 - Indeed, a transition between two atomic states with same parity is forbidden by the parity selection rule and cannot happen with the exchange of a photon.
 - ✓ However, an electric dipole transition amplitude can be induced by a Z boson exchange between atomic electrons and nucleons → Atomic Parity Violation (APV) or Parity Non Conserving (PNC).

+ The quantity that is measured is the usual **weak charge**

$$Q_W^{SM} \approx Z (1 - 4 \sin^2 \theta_W^{SM}) - N$$

Extracting the weak charge from APV $Q_W = N \left(\frac{\operatorname{Im} E_{\text{PNC}}}{\beta} \right)_{\text{exp.}} \left(\frac{Q_W}{N \operatorname{Im} E_{\text{PNC}}} \right)_{\text{th.}} \beta_{\text{exp.+th.}}$

+ Experimental value of electric dipole transition amplitude between 6S and 7S states in Cs

C. S. Wood et al., Science **275**, 1759 (1997)

J. Guena, et al., PRA **71**,
 042108 (2005)

PDG2020 average

$$Im\left(\frac{E_{PNC}}{\beta}\right) = -1.5924(55)$$
mV/cm

✓ Theoretical amplitude of the <u>electric dipole transition</u> $E_{\text{PNC}} = \sum_{n} \left[\frac{\langle 6s | H_{\text{PNC}} | np_{1/2} \rangle \langle np_{1/2} | d | 7s \rangle}{E_{6s} - E_{np_{1/2}}} + \frac{\langle 6s | d | np_{1/2} \rangle \langle np_{1/2} | H_{\text{PNC}} | 7s \rangle}{E_{7s} - E_{np_{1/2}}} \right],$

> where **d** is the electric dipole operator, and

$$H_{\rm PNC} = -\frac{G_F}{2\sqrt{2}}Q_W\gamma_5\rho(\mathbf{r})$$

Value of Im*E_{PNC}* used by PDG (V. Dzuba *et al.*, PRL 109, 203003 (2012))

Im $E_{\rm PNC} = (0.8977 \pm 0.0040) \times 10^{-11} |e| a_B Q_W / N$ see also

nuclear Hamiltonian describing the **electron-nucleus weak interaction** $\rho(\mathbf{r}) = \rho_p(\mathbf{r}) = \rho_n(\mathbf{r}) \rightarrow \text{neutron skin correction}$ needed β : tensor transition polarizability It characterizes the size of the Stark mixing induced electric dipole amplitude (external electric field)

Bennet & Wieman, PRL 82, 2484 (1999) Dzuba & Flambaum, PRA 62 052101 (2000)

PDG2020 average $\beta = 27.064 (33) a_B^3$

NEW result on Im*E*_{PNC} !

I will refer with APV2021 when usign Im E_{PNC} from B. K. Sahoo et al. PRD 103, L111303 (2021)

Atomic Parity Violation for weak mixing angle measurements Using SM prediction at low energy ✓ Weak charge in the SM including radiative corrections $\sin^2 \hat{\theta}_W(0) = 0.23857(5)$ $Q_W^{SM+r.c.} \equiv -2\left[Z\left(g_{AV}^{ep} + 0.00005\right) + N\left(g_{AV}^{en} + 0.00006\right)\right] \left(1 - \frac{\alpha}{2\pi}\right) \approx Z\left(1 - 4\sin^2\theta_W^{SM}\right) - N$ Theoretically Experimentally 1σ difference $Q_{W}^{\text{exp.}}({}^{133}_{55}Cs) = -72.82(42)$ $Q_W^{SM \text{ th}} \left({}^{133}_{55}Cs \right) = -73.23(1)$ 083C01 (2022) 0.245 **RGE Running** Particle Threshold Measurements SLAC E158 0.24 2022, **Q**_{weak} $(n)^{\mathbf{M}} \theta_{\mathbf{r}}^{\mathbf{0.235}}$ $\sin^2 \hat{\theta}_W$ (2.4 MeV)=0.2367±0.0018 APV eDIS LEP 1 SLC LHC Tevatron But which Cs neutron 0.23 skin correction is used? 0.225 10^{-3} 10^{-2} 10³ 10^{-1} 10² 10^{-4} 10 10⁴ 27 μ[GeV]

Group)





2nd advantage: extract both $R_n(Csl) \& \sin^2 \vartheta_W$ from data





2nd advantage: extract both $R_n(CsI)$ and $\sin^2 \vartheta_W$ from data $R_n(CsI)=5.4^{+0.5}_{-0.4} \text{ fm } \sin^2 \vartheta_W=0.2397^{+0.0032}_{-0.0032} \chi^2_{\min}=85.2$





Combined 2D fit with COHERENT and APV(Cs)



Weak mixing angle

The Weinberg angle, θ_W is a fundamental parameter of the EW theory of the SM. It determines the relative strength of the weak NC vs. the electromagnetic interaction. There are many ways to define it, one of those is the **minimal subtraction scheme** (\overline{MS}).

 $ightarrow \sin^2 \hat{\theta}_W(M_Z) \equiv \hat{s}_Z^2 = 0.23122 \pm 0.00004 \, (\overline{MS})$

the energy scale. For low energies it assumes the value

 $0.2399\substack{+0.0016+0.0026+0.0032\\-0.0016-0.0026-0.0032}$ APV PDG + CsI $| 0.2374^{+0.0020+0.0032+0.0039}_{-0.0018-0.0031-0.0037} |$ The value of $\sin^2 \hat{\theta}_W$ runs as a function of the momentum transfer or $APV 2021 + CsI 0.2398^{+0.0016+0.0026+0.0032}_{-0.0015-0.0026-0.0031}$ $\hat{s}_0^2(0) = 0.23863 \pm 0.00005 \,(\overline{MS})$ 0.245 RGE Running -PD(Particle Threshold However $R_n(Cs)$ (or $\sin^2 \vartheta$ Measurements 1202-VAN the neutron skin) SLAC E158 0.24 has been taken 99% C from **indirect Q**_{weak} $sin^2\hat{\theta}_W(\mu)$ measurements ON eDIS 0.235 using antiprotonic 🔏 0.234 0.236 0.238 0.240 0.242 $\sin^2 \vartheta_W$ atoms, which are known to be LEP 1 Historically APV(Cs) has LHC Tevatron SLC affected by 90% CL ^{0.23} been used to estract the considerable model lowest energy dependencies determination of $\sin^2 \hat{\theta}_W$. 0.225 10^{3} 10^{-1} 10^{-4} 10 10^{2} 10⁴ μ[GeV] 0.18 0.20 0.22 0.24 0.26 0.28 0.16 0.30

M. Atzori Corona et al., EPJC 83 (2023) 7, 683, arXiv:2303:09360

 $\sin^2 \vartheta_W$

COH-CsI

APV PDG

APV 2021

 $\sin^2 \vartheta_W$

 $\chi^2_{\rm min}$

86.0

86.0

86.0

3σ

2σ

 1σ

best-fit $^{+1\sigma+90\%}$ CL $^{+2\sigma}$

 $0.231^{+0.027+0.046+0.058}_{-0.024-0.039-0.047}$

 $0.2375^{+0.0019+0.0031+0.0038}_{-0.0019-0.0031-0.0038}$

The Csl neutron skin

First result Cadeddu et al. Phys. Rev. Lett. 120, 072501 (2018), arXiv:1710.02730

0.18



 $R_n(\text{COH} - \text{CsI}) = 5.47^{+0.38}_{-0.38}(1\sigma)^{+0.63}_{-0.72}(90\%\text{CL})^{+0.76}_{-0.89}(2\sigma) \text{ fm},$



The past, present and future of R_n measurements with CE ν NS and PVES See details in D. Akimov et al., arXiv:2204.04575 (2022)

- **COH-CryoCsI-I**: 10 kg, cryogenic temperature (~40*K*), twice the light yield of present CsI crystal at 300K
- **COH-CryoCsI-II**: 700 kg undoped CsI detector. Both lower energy threshold of 1.4 keVnr while keeping the shape of the energy efficiency of the present COHERENT CsI.

COHERENT future argon: "COH-LAr-750" LAr based detector for precision CEvNS

TRADEFIC



The past, present and future of $\sin^2 \vartheta_W$ with CEvNS and APV



Neutron nuclear radius in argon



Combined fit in (time, energy, PSP) space suggest $>3\sigma$ CEvNS detection significance

Recoil Energy (keVnr) 150 200 250

Dominant backgrounds: 1. ³⁹Ar beta decay 2. Beam related neutrons

Akimov et al, COHERENT Coll. PRL 126, 01002 (2021)

```
COHERENT future argon: "COH-Ar-750"
LAr based detector for precision CE\nu NS
```

82kg TOTAL 0.561m*3

Single phase, scintillation only, 750 kg total (610 kg fiducial)

3000 CEvNS/year

Improvements with the latest CsI dataset

+ New quenching factor

 $E_{ee} = f(E_{nr}) = aE_{nr} + bE_{nr}^2 + cE_{nr}^3 + dE_{nr}^4.$ a=0.05546, b=4.307, c= -111.7, d=840.4

Akimov et al. (COHERENT Coll), arXiv:2111.02477, JINST 17 P10034 (2022)

+ 2D fit, arrival time information included $N_{ij}^{\text{CE}\nu\text{NS}} = (N_i^{\text{CE}\nu\text{NS}})_{\nu_{\mu}} P_j^{(\nu_{\mu})} + (N_i^{\text{CE}\nu\text{NS}})_{\nu_e,\bar{\nu}_{\mu}} P_j^{(\nu_e,\bar{\nu}_{\mu})}$



+ Doubled the statistics and reduced syst. uncertainties

$$\sigma_{\rm CE\nu NS} = 13\%, \sigma_{\rm BRN} = 0.9\%,$$

and $\sigma_{\rm SS} = 3\%$

Theoretical number of CEvNS events



arXiv:2303.09360

40

$$\chi_{\rm C}^2 = \sum_{i=2}^9 \sum_{j=1}^{11} \left(\frac{N_{ij}^{\rm exp} - \sum_{z=1}^3 (1+\eta_z) N_{ij}^z}{\sigma_{ij}} \right)^2 + \sum_{z=1}^3 \left(\frac{\eta_z}{\sigma_z} \right)^2,$$

[–] Cadeddu et al., PRC 104, 065502 (2021), arXiv:2102.06153







COHERENT CsI χ^2

+Poissonian least-square function:

+ Since in some energy-time bins the number of events is zero, we used the Poissonian least-squares function

$$\chi_{\rm CsI}^2 = 2\sum_{i=1}^9 \sum_{j=1}^{11} \left[\sum_{z=1}^4 (1+\eta_z) N_{ij}^z - N_{ij}^{\rm exp} + N_{ij}^{\rm exp} \ln\left(\frac{N_{ij}^{\rm exp}}{\sum_{z=1}^4 (1+\eta_z) N_{ij}^z}\right) \right] + \sum_{z=1}^4 \left(\frac{\eta_z}{\sigma_z}\right)^2, \quad (10)$$

where the indices i, j represent the nuclear-recoil energy and arrival time bin, respectively, while the indices z = 1, 2, 3, 4 for N_{ij}^z stand, respectively, for CE ν NS, $(N_{ij}^1 = N_{ij}^{\text{CE}\nu\text{NS}})$, beam-related neutron $(N_{ij}^2 = N_{ij}^{\text{BRN}})$, neutrino-induced neutron $(N_{ij}^3 = N_{ij}^{\text{NIN}})$ and steady-state $(N_{ij}^4 = N_{ij}^{\text{SS}})$ backgrounds obtained from the anti-coincidence data. In our notation, N_{ij}^{exp} is the experimental event number obtained from coincidence data and $N_{ij}^{\text{CE}\nu\text{NS}}$ is the predicted number of CE ν NS events that depends on the physics model under consideration, according to the cross-section in Eq. (1), as well as on the neutrino flux, energy resolution, detector efficiency, number of target atoms and the CsI quenching factor [16]. We take into account the systematic uncertainties with the nuisance parameters η_z and the corresponding uncertainties $\sigma_{\text{CE}\nu\text{NS}} = 0.12$, $\sigma_{\text{BRN}} = 0.25$, $\sigma_{\text{NIN}} = 0.35$ and $\sigma_{\text{SS}} = 0.021$ as explained in Refs. [6, 16].

Dresden-II weak mixing angle results

- M. Atzori Corona et al., JHEP **09**, 164 (2022), arXiv:2205.09484

+Very sensitive to the Ge quenching factor parametrization





THE NUCLEAR FORM FACTOR

• The nuclear form factor, F(q), is taken to be the Fourier transform of a spherically symmetric ground state mass distribution (both proton and neutrons) normalized so that F(0) = 1:

For a weak interaction like for CEvNS you deal with the **weak form factor**: the Fourier transform of the weak charge distribution (neutron + proton distribution weighted by the weak mixing angle)

It is convenient to have an analytic expression like the Helm form factor $F_N^{\text{Helm}}(q^2) = 3 \, \frac{j_1(qR_0)}{qR_0} \, e^{-q^2 s^2/2}$

$$\frac{d\sigma}{dE_{r}} \cong \frac{G_{F}^{2} m_{N}}{4\pi} \left(1 - \frac{m_{N}E_{r}}{2E_{v}^{2}}\right) Q_{w}^{2} \times |F_{weak}(E_{r})|^{2} \xrightarrow{0.1}_{U} 0.01$$
Weak charge × weak form factor
$$\begin{bmatrix}g_{V}^{p} ZF_{Z}(E_{r}, R_{p}) + g_{V}^{n} NF_{N}(E_{r}, R_{n})\end{bmatrix}^{2} \xrightarrow{0.1}_{U} 0.01$$
Weak charge × weak form factor
$$\begin{bmatrix}g_{V}^{p} ZF_{Z}(E_{r}, R_{p}) + g_{V}^{n} NF_{N}(E_{r}, R_{n})\end{bmatrix}^{2} \xrightarrow{0.1}_{U} 0.01$$

$$\xrightarrow{0.1}_{U} 0.01$$

$$\xrightarrow{0.1}_$$



= Helm R. Phys. Rev. **104**, 1466 (1956)

FITTING THE COHERENT CSI DATA FOR THE NEUTRON RADIUS

G. Fricke et al., Atom. Data Nucl. Data Tabl. 60, 177 (1995)

From muonic X-rays data we have
 (For fixed t = 2.3 fm)

 $R_{ch}^{Cs} = 4.804 \text{ fm}$ (Cesium charge rms radius) $R_{ch}^{I} = 4.749 \text{ fm}$ (Iodine charge rms radius)

$$R_p^{\rm rms} = \sqrt{R_{ch}^2 - \left(\frac{N}{Z} \langle r_n^2 \rangle + \frac{3}{4M^2} + \langle r^2 \rangle_{SO}\right)}$$

 $\frac{R_p^{Cs} = 4.821 \pm 0.005 \text{ fm (Cesium rms proton radius)}}{R_p^I = 4.766 \pm 0.008 \text{ fm (Iodine rms-proton radius)}}$ $\frac{d\sigma}{dE_r} \cong \frac{G_F^2 m_N}{4\pi} \left(1 - \frac{m_N E_r}{2E_v^2}\right) \left[g_V^p Z F_Z \left(E_r, R_p^{Cs/I}\right) + g_V^n N F_N (E_r, R_n^{CsI})\right]^2$

 $R_n^{Cs} \& R_n^I$ very well known so we fitted COHERENT CsI data looking for R_n^{CsI} ...

2 Boson

FROM THE CHARGE TO THE PROTON RADIUS

One need to take into account finite size of both protons and neutrons plus other corrections





The proton form factor n2 1 1

$$\frac{d\sigma_{\nu-CSI}}{dT} = \frac{G_F^2 M}{4\pi} \left(1 - \frac{MT}{2E_{\nu}^2} \right) \left[N F_N(T, R_n) - \varepsilon Z F_Z(T, R_p) \right]^2$$

The proton structures of ${}^{133}_{55}Cs$ (N = 78) and ${}^{127}_{53}I$ (N = 74) have been studied with muonic spectroscopy and the data were fitted with **two**parameter Fermi density distributions of the form

 $\rho_F(r) = \frac{\rho_0}{1 + \rho(r-c)/a}$

Where, the **half-density radius** *c* is related to the **rms radius** and the *a* parameter quantifies the **surface** thickness $t = 4 a \ln 3$ (in the analysis fixed to 2.30 fm).

Fitting the data they obtained

 $R_{ch}^{Cs} = 4.804 \, \text{fm}$ (Caesium proton rms radius) $R_{ch}^{I} = 4.749 \, \text{fm}$ (lodine proton rms radius)

[G. Fricke et al., Atom. Data Nucl. Data Tabl. 60, 177 (1995)]



 $\rho(\mathbf{r})/\rho_0$





Weak mixing angle (WMA)

+ The Weinberg angle, θ_W is a fundamental parameter of the **electroweak** (EW) theory of the Standard Model (SM), usually expressed as $\sin^2 \theta_W$ + WMA determines the relative strength of the weak neutral $\sqrt{g^2 + {g'}^2}$ current (NC) vs. electromagnetic interaction

> Tree-level
$$\sin^2 \theta_W = 1 - \frac{M_W^2}{M_Z^2} = \frac{g'^2}{g^2 + g'^2}$$

+ The **on-shell scheme** promotes the tree-level formula to a definition of the renormalized $\sin^2 \theta_W$ to all orders in perturbation theory (quite sensitive to the top mass)

→
$$sin^2 θ_W → s_W^2 \equiv 1 - \frac{M_W^2}{M_Z^2} = 0.22343 \pm 0.00007$$
 (on-shell)

- + **Minimal subtraction scheme** (\overline{MS}) $\sin^2 \hat{\theta}_W(\mu) = \frac{\hat{g}'^2(\mu)}{\hat{g}^2(\mu) + \hat{g}'^2(\mu)}$ where the couplings are defined in the \overline{MS} and the energy scale μ is conveniently chosen to be M_Z for many EW processes (less sensitive to the top mass)
 - > $\sin^2 \hat{\theta}_W(M_Z) \equiv \hat{s}_Z^2 = 0.23122 \pm 0.00003 \,(\overline{\text{MS}})$

Scale dependent→ running of WMA

U

е

S

FERMION

Quarks

Leptons

Gauge Boson

Higgs Boson

BOSONS

Scale dependence of the weak mixing angle

- The value of $\sin^2 \hat{\theta}_W$ varies as a function of the momentum transfer or energy scale («running»). +
- Working in the $\overline{\text{MS}}$, the main idea is to relate the case of the WMA to that of the electromagnetic coupling $\hat{\alpha}$
- The vacuum polarization contributions are crucial +



Neutron radius determination of 133 Cs and its impact on the interpretation of CE ν NS-CsI measurement

Y. Huang^{a,b}, S. Y. Xia^{c,d}, Y. F. Li^{c,d}, X. L. Tu^{a,*}, J. T. Zhang^a, C. J. Shao^a, K. Yue^a, P. Ma^a, Y. F. Niu^e, Z. P. Li^f, Y. Kuang^f, X. Q. Liu^b, J. F. Han^b, P. Egelhof^g, Yu. A. Litvinov^g, M. Wang^a, Y. H. Zhang^a, X. H. Zhou^a, Z. Y. Sun^a

^aInstitute of Modern Physics, Chinese Academy of Sciences, Lanzhou 730000, China ^bKey Laboratory of Radiation Physics and Technology of the Ministry of Education, Institute of Nuclear Science and Technology, Sichuan University, Chengdu 610064, China ^cInstitute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China ^dSchool of Physical Sciences, University of Chinese Academy of Sciences, Beijing

100049, China

^eSchool of Nuclear Science and Technology, Lanzhou University, Lanzhou 730000, China ^fSchool of Physical Science and Technology, Southwest University, Chongqing 400715, China

^gGSI Helmholtzzentrum für Schwerionenforschung GmbH, D-64291 Darmstadt, Germany

Abstract

Proton-¹³³Cs elastic scattering at low momentum transfer is performed using an in-ring reaction technique at the Cooler Storage Ring at the Heavy Ion Research Facility in Lanzhou. Recoil protons from the elastic collisions between the internal H₂-gas target and the circulating ¹³³Cs ions at 199.4 MeV/u are detected by a silicon-strip detector. The matter radius of ¹³³Cs is deduced by describing the measured differential cross sections using the Glauber model. Employing the adopted proton distribution radius, a point-neutron radius of 4.86(21) fm for ¹³³Cs is obtained. With the newly determined neutron radius, the weak mixing angle $\sin^2\theta_W$ is independently extracted to be 0.227(28) by fitting the coherent elastic neutrino-nucleus scattering data. Our work limits the $\sin^2\theta_W$ value in a range smaller than the ones proposed by the previous independent approaches, and would play an important role in searching new physics via the high precision CE ν NS-CsI cross section data in the near

*Corresponding author.



Figure 1: Scatter plot of the recoil proton energy versus the strip number of DSSD. The solid (red), dashed (green), and dash-dotted (pink) lines denote the calculated proton energies for elastic and two inelastic scattering channels, respectively. For more details see text.

Small-angle p-nucleus elastic distributions are sensitive to matter distribution radius.

present work, a well established procedure [44, 49, 50] based on the Glauber multiple-scattering theory [51] is employed to extract the matter radius of ¹³³Cs through describing the measured $\frac{d\sigma}{d\Omega}(\theta)$. The $\frac{d\sigma}{d\Omega}(\theta)$ values are expressed in the Glauber model as a function of the matter density distribution $\rho(r)$ and the proton-nucleon scattering amplitude $f_{pi}(q)$ with i = n or p, see Ref. [50] for details. To reduce the model-dependent errors of matter radius, the scattering amplitude parameters were calibrated at 200 MeV [48] to be $\sigma_{pp} =$ 1.788(20) fm², $\sigma_{pn} = 3.099(27)$ fm², $\alpha_{pp} = 0.893(17)$, $\alpha_{pn} = 0.325(23)$, and $\beta_{pp} = \beta_{pn} = 0.528(41)$ fm², which are adopted here to calculate the $f_{pi}(q)$. These values have been adopted to fit the differential cross sections of p-¹⁶O elastic scattering at 200 MeV and reproduce the well-known matter radius of ¹⁶O [48].

Email address: tuxiaolin@impcas.ac.cn (X. L. Tu)

As shown in Fig. 2, the measured ddo $\Omega(\theta)$ are well described with the Glauber model by adjusting R and L0. With the obtained R and fixed a, a root-mean-square (rms) point-matter radius Rpm for 133Cs is determined to be

$$R_{\rm pm} = \left(\frac{\int \rho(r) r^4 dr}{\int \rho(r) r^2 dr}\right)^{\frac{1}{2}} = 4.811 \pm 0.127 \,\,{\rm fm}\,,\tag{3}$$

where uncertainties from statistics, input parameters, and Glauber model are about 0.12 fm, 0.03 fm, and 0.03 fm, respectively. The radius uncertainties caused by statistics and input parameters are estimated by using the randomly sampled experimental $\frac{d\sigma}{d\Omega}(\theta)$ and input parameters within 2σ band [50], respectively. The model-dependent error at 200 MeV is estimated by comparing the well-known proton radii with the matter radii of ¹²C, ¹⁶O, and ²⁸Si determined with the similar method, where similar proton and matter radii are expected for the N = Z nuclei. To check the effects of background, only recoil protons with energies > 1 MeV were analyzed, and a consistent radius of 4.825 fm is obtained. Details and reliability considerations about radius determinations can be found in Refs. [30, 50].

With the obtained $R_{\rm pm}$, a point-neutron distribution radius $R_{\rm pn}$ of ¹³³Cs is determined to be

$$R_{\rm pn} = \sqrt{\frac{A}{N}R_{\rm pm}^2 - \frac{Z}{N}R_{\rm pp}^2} = 4.86 \pm 0.21 \,\,{\rm fm},\tag{4}$$

where N, Z, and A are the neutron, proton, and mass number, respectively. The adopted point-proton radius $R_{\rm pp}$ of 4.740(5) fm for ¹³³Cs is deduced from charge radius [30, 54].

We extract the neutron skin of ¹³³Cs to be $R_{\rm pn} - R_{\rm pp} = 0.12(21)$ fm.





Figure 4: (a) The χ^2_{all} contours in the plane of R_{fn} versus $\sin^2\theta_W$. The blue curves and point represent results when both R_{fn} and $\sin^2\theta_W$ are free variables in the CE ν NS-CsI data fitting. The black curves and point add the constraint imposed by the presently deduced radius. (b) The distribution of reported neutron radii of ¹³³Cs [15, 17, 18, 20, 21, 22, 23, 24, 25, 26, 27] deduced from the CE ν NS-CsI data [10, 11].



Parity Violation Electron Scattering (PVES) and APV on Lead



Lead neutron skin from non-EW probes...

	Experimental Δr_{np}^{\exp} (fm)	Method	Evaluated Δr_{np}^{eva} (fm)	$\frac{\Delta r_{np}^{eva} - \Delta r_{np}^{exp}}{\text{error}}$
²⁰⁸ Pb	0.150(20) [21,36]	AA	0.167(11)	0.9
	0.250(90) [49]	(α, α)		-0.9
	0.080(50) [56]	(p, p)		1.7
	0.160(50) [57]	(p, p)		0.1
	0.060(100) [59]	(p, p)		1.1
	0.360(200) [64]	(p, p)		-1.0
	0.180(70) [67]	(p, p)		-0.2
	0.190(90) [72]	GDR		-0.3
	0.300(70) [74]	(α, α)		-1.9
	0.211(63) [75]	(p, p)		-0.7
	0.197(42) [76]	(p, p)		-0.7
	0.260(130) [77]	(α, α)		-0.7
	0.420(200) [77]	(α, α)		-1.3
	0.273(90) [78]	(α, α)		-1.2
	0.182(70) [79]	(p, p)		-0.2
	0.140(40) [80]	(p, p)		0.7
	0.180(35) [81]	PDR		-0.4
	0.120(70) [82]	GDR		0.7
	0.160(45) [83]	AA		0.2
	0.200(64) [32]	AA		-0.5



Table 4. 208 Pb neutron skin measurements and theoretical predictions with 1 σ uncertainties

²⁰⁸ Pb Experiment	Reference	r_{np}^{208} (fm)
Coherent $\pi^0 \gamma$ production	[77]	$0.15^{+0.03}_{-0.04}$
Pionic atoms	[73]	0.15 ± 0.08
Pion scattering	[73]	0.11 ± 0.06
p annihilation	[78,79]	0.18 ± 0.06
Elastic polarized p scattering	[70]	0.16 ± 0.05
Elastic polarized p scattering	[80]	$0.211^{+0.054}_{-0.063}$
Elastic p scattering	[81]	0.197 ± 0.042
Elastic p scattering	[72]	0.119 ± 0.045
Parity-violating e ⁻ scattering (PREX I+II)	[17]	0.283 ± 0.071
²⁰⁸ Pb experimental weighted mean		0.166 ± 0.017
Pygmy dipole resonances	[82]	0.180 ± 0.035
r_{np}^{Sn}	[83]	0.175 ± 0.020
Anti-analog giant dipole resonance	[84]	0.216 ± 0.048
Symmetry energy ²⁰⁸ Pb	[85]	0.158 ± 0.014
Dispersive optical model	[86]	$0.18^{+0.25}_{-0.12}$
Dispersive optical model	[67]	0.25 ± 0.05
Coupled cluster expansion	[66]	0.17 ± 0.03
r_{np}^{48}	[63,64], this paper	0.128 ± 0.040
α ²⁰⁸	[62], this paper	0.154 ± 0.019
a ²⁰⁸	[20,64], this paper	0.188 ± 0.017
²⁰⁸ Pb theoretical weighted mean		0.170 ± 0.008

Lattimer arXiv:2301.03666v1

PRC 104, 034303 (2021)