

# Beam-beam effects overview

## and their impact on collider design and performance

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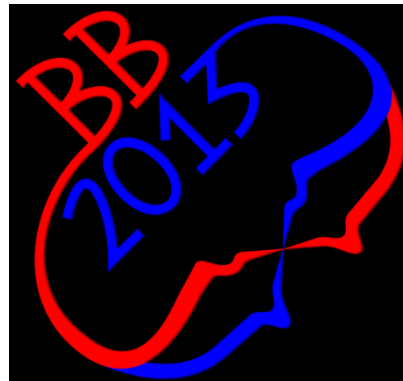


# Workshops on beam-beam effects in circular colliders

- 1999 (CERN)

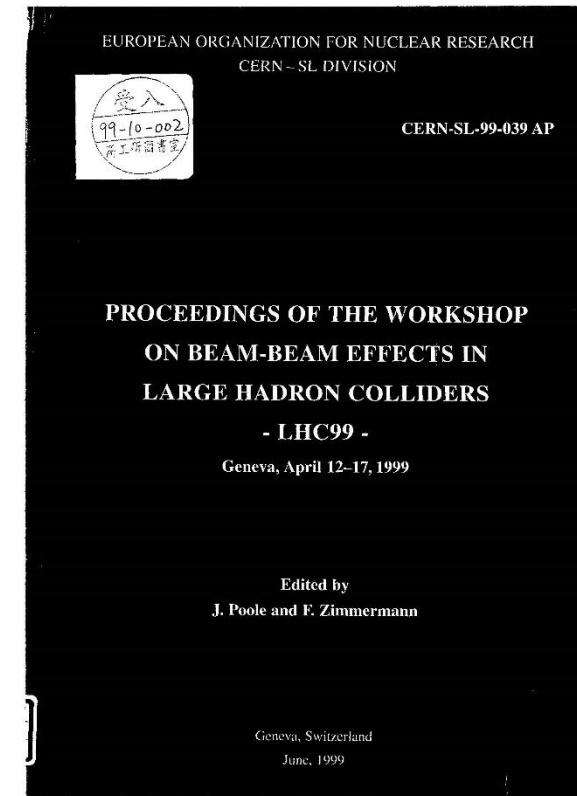
- 2001 (Fermilab)

- 2013 (CERN)

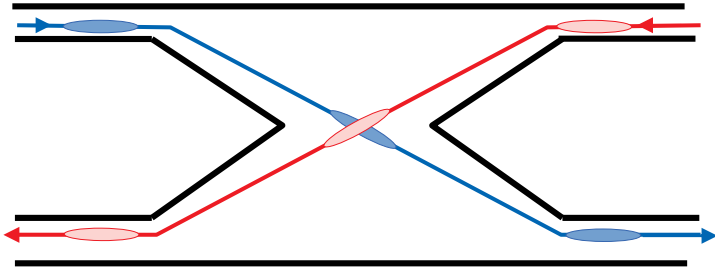


- 2018 (LBNL)

- 2024 (EPFL)



# Electron-positron collider evolution



- Two separate beam pipes “Factories”
  - Allows for many bunches (reaching total currents of few A) without parasitic encounters
  - Imposes a large crossing angle

Crab cavities  
(KEKB)

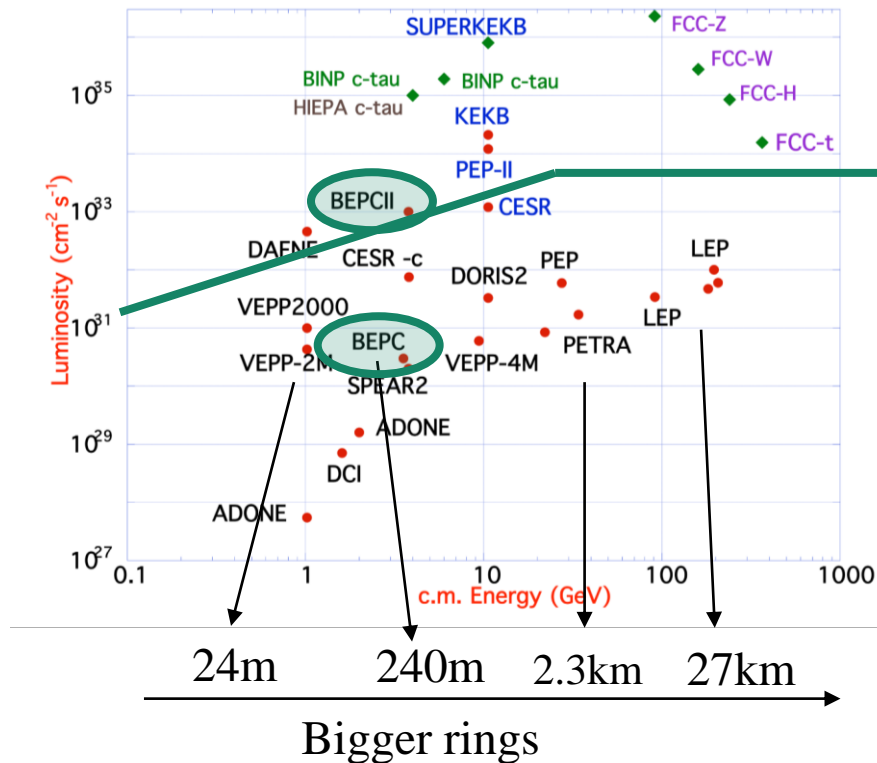
[Funakoshi13]

Crab waist

(DAPHNE, SuperKEKB)

[Raimondi06, Zobov10]

- Single bunch current remains limited by the beam-beam tune shift



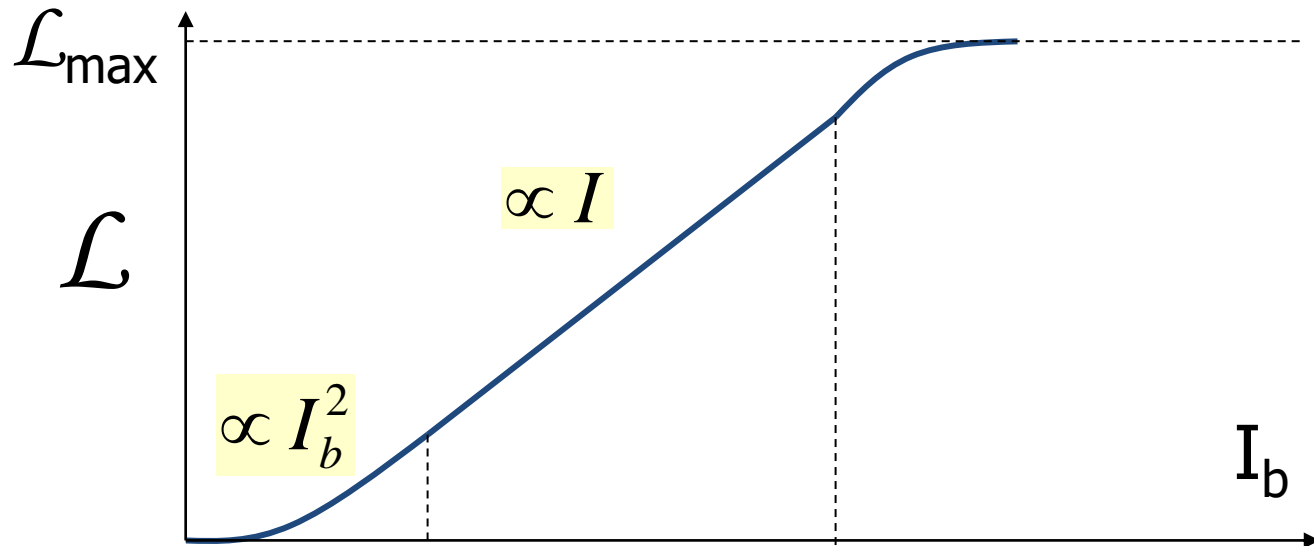
- Single beam pipe

- Number of bunches limited by parasitic encounters
- Single bunch current limited by the beam-beam tune shift (“beam-beam limit”)

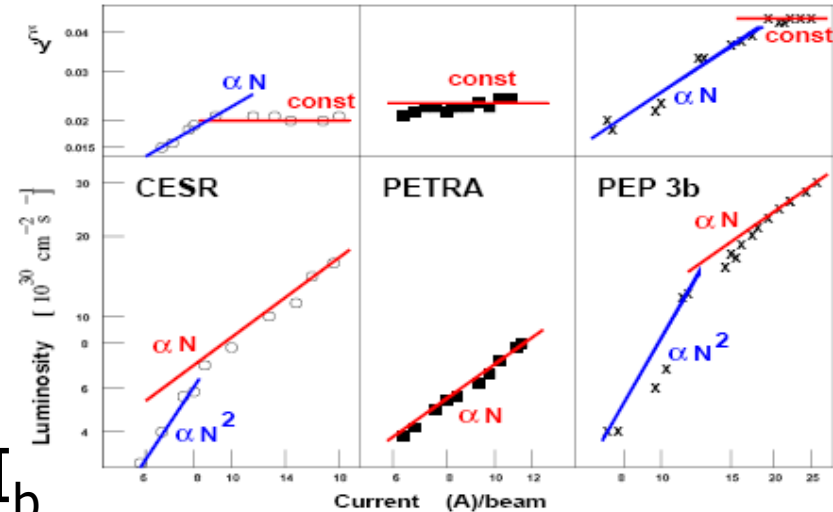
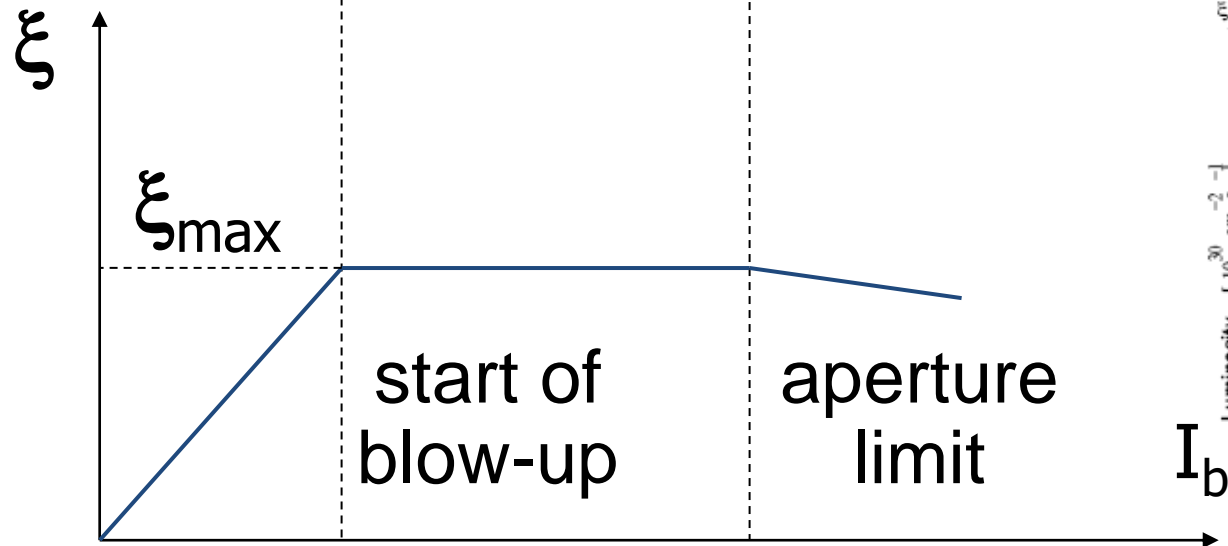
4-beam compensation  
(DCI) [Derbenev73]

Round beams (VEPP-2000)  
[Danilov96, Shwartz16]

# Beam - beam limit



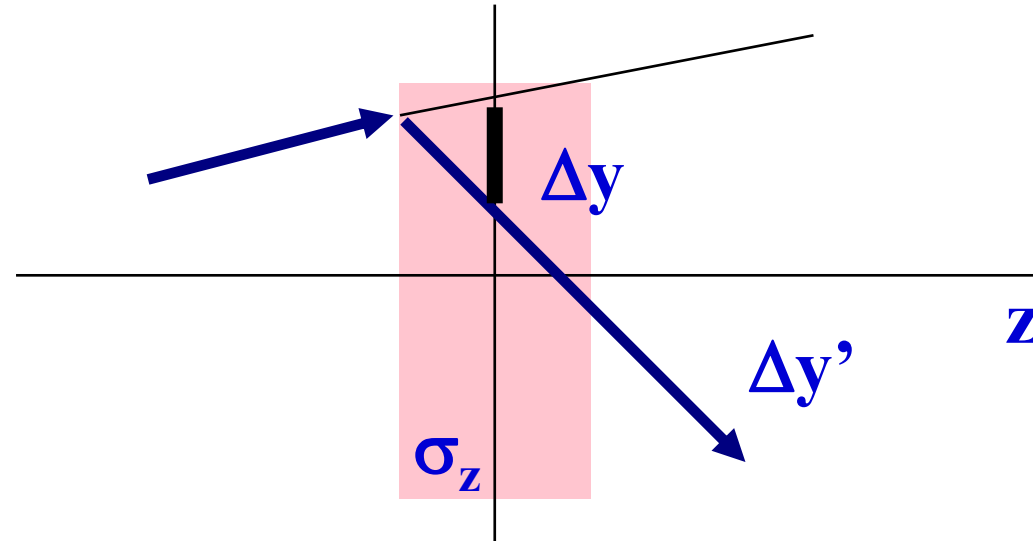
$$\mathcal{L} \propto \frac{I_b^2}{A^*}$$



# Beam – beam effects in linear and circular colliders

- Near the axis the other bunch is equivalent to a focusing lens

$$\frac{1}{f_{x,y}} = \frac{2Nr_e}{\gamma\sigma_{x,y}(\sigma_x + \sigma_y)}$$



- Disruption is defined as:

$$D_{x,y} \equiv \frac{2Nr_e}{\gamma} \frac{\sigma_z}{\sigma_{x,y}(\sigma_x + \sigma_y)} \quad \left( = \frac{\sigma_z}{f_{x,y}} \text{ for a Gaussian} \right)$$

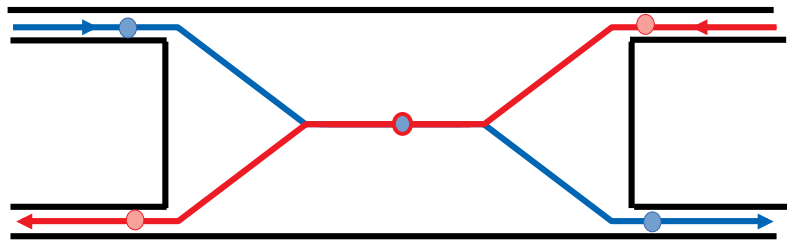
- and it can be viewed as:

- to connect it to the storage ring jargon

$$\frac{\Delta y}{\sigma_y} = -\frac{\sigma_z}{f_y} = -4\pi\xi_y \frac{\sigma_z}{\beta_y^*}$$

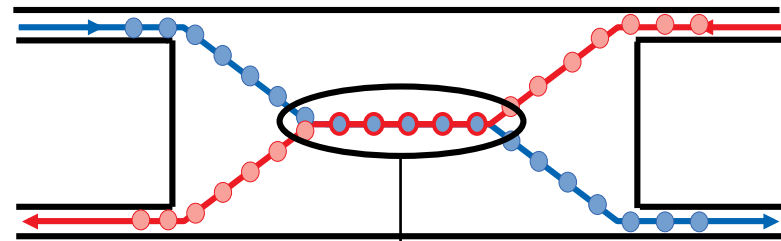
$$\frac{\Delta y'}{\sigma_{y'}} = -\frac{\beta_y^*}{f_y} = -4\pi\xi_y$$

# Hadron collider evolution



- Limited by beam-beam tune shift

→ Electron lens 'non-linear' compensation [Fischer17]

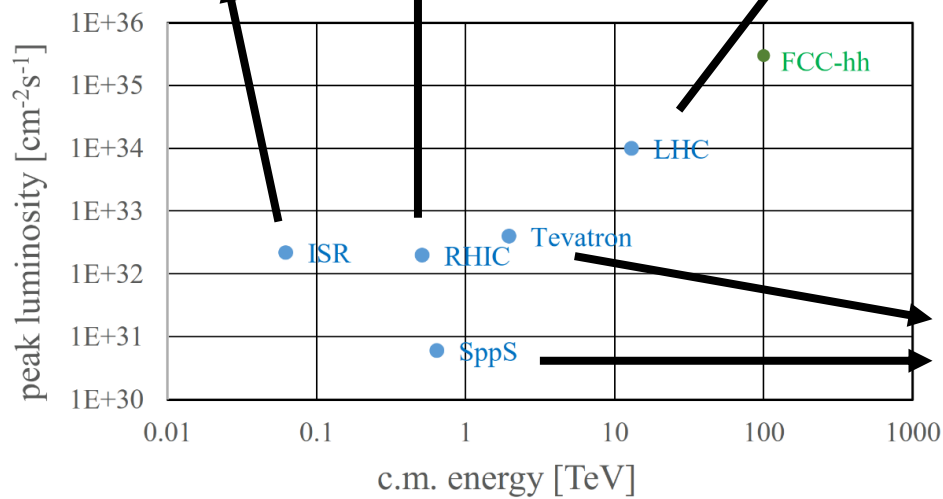


- Limited by parasitic encounters

→ Current carrying wire [Sterbini24]

→ Crab cavity [HL-LHC]

Not limited by beam-beam [Huebner74]



→ Bigger rings + stronger magnets

- Single pipe p-pbar colliders

- Number of bunches limited by parasitic encounters →
- Challenging p-bar production

Number!

Not same for each bunch!  
"Pacman"

Electron lens 'tune shift' compensation [Shiltsev07]

# Finite bunch length effect

- Important development for the understanding of parasitic encounters for both  $e^+e^-$  and  $pp$  (self-consistent orbit / optics, non-linear dynamics)
  - → The current trend for either designs (and also e-p) is to increase the number of bunches and minimize number of parasitic encounters by having two separate beam pipes
  - → **Finite bunch length effect (crossing angle, hourglass)**

$$\mathcal{L} \approx \frac{I_{tot} \gamma \xi}{r_0 \beta^*} R_{HG}$$

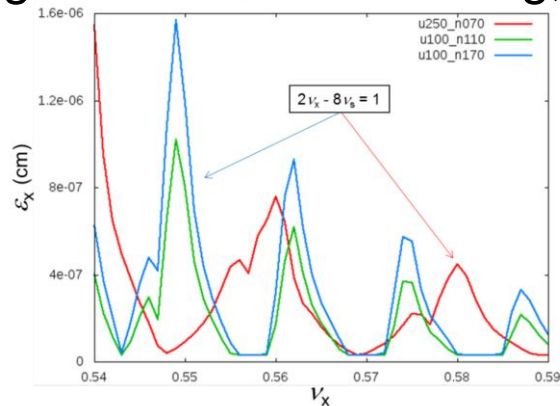
$(\sigma_y = \sigma_x)$

$$\mathcal{L} \approx \frac{\gamma}{2er_e} \frac{I_{tot} \xi_y}{\beta_y^*} R_{HG}$$

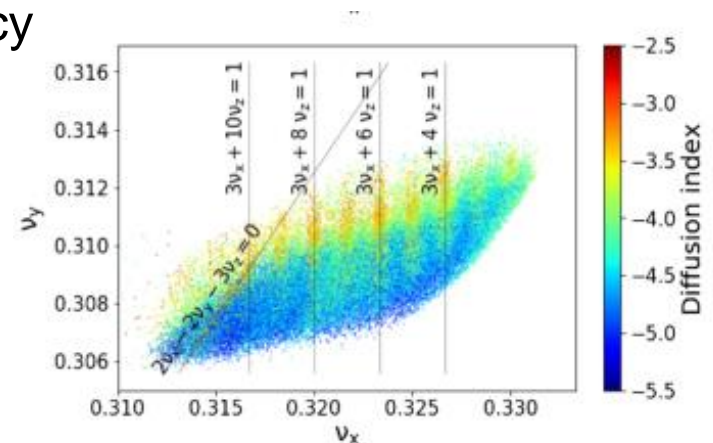
$(\sigma_y \ll \sigma_x)$

- Large efforts to understand and increase the maximum beam-beam tune shift including synchrotron effects [Piwinski87, ..., Hirata92, ..., Xu21]
  - → Constraints on transverse/longitudinal tunes, Piwinski angle, hourglass parameter, lattice driven resonances
  - → (Partial) mitigation: crab waist tuning, Crab cavity frequency

FCC-ee Z horizontal tune scan including crab waist [Shatilov17]



EIC with crab cavity, including RF curvature [Xu21]



# Classic “Mini – $\beta$ ” schemes

- Luminosity

$$\mathcal{L} \propto \frac{N^2}{A^*} \quad A^* = 4\pi\sigma_x\sigma_y$$

- Tune shift

$$\xi_y \propto \frac{N}{A^*} < \xi_{\max} \quad \Rightarrow \quad N \propto A^*$$

We want large current,  
fill large collision area!

- Required large emittance: “fill the aperture”

$$\mathcal{L} \propto A^*$$

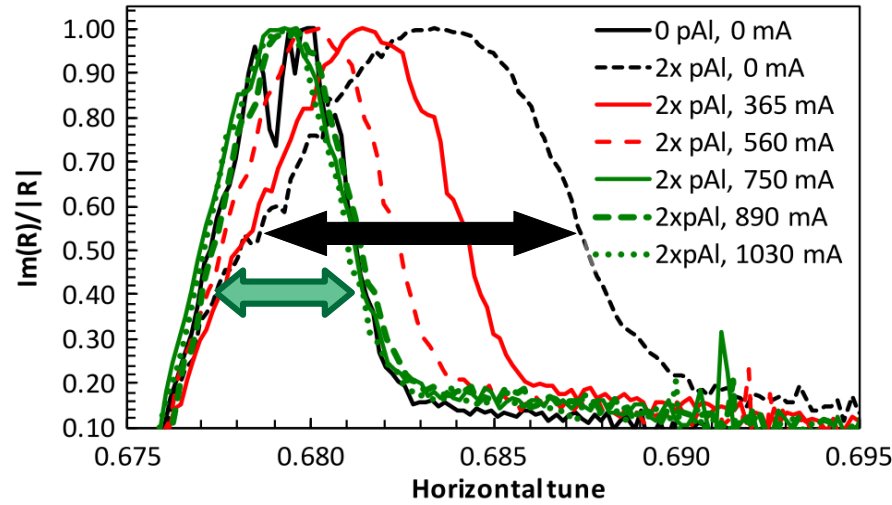
- With the advent of small emittance collider rings

Luminosity per unit power!  
Fill dynamic aperture  
to the limit of transverse density



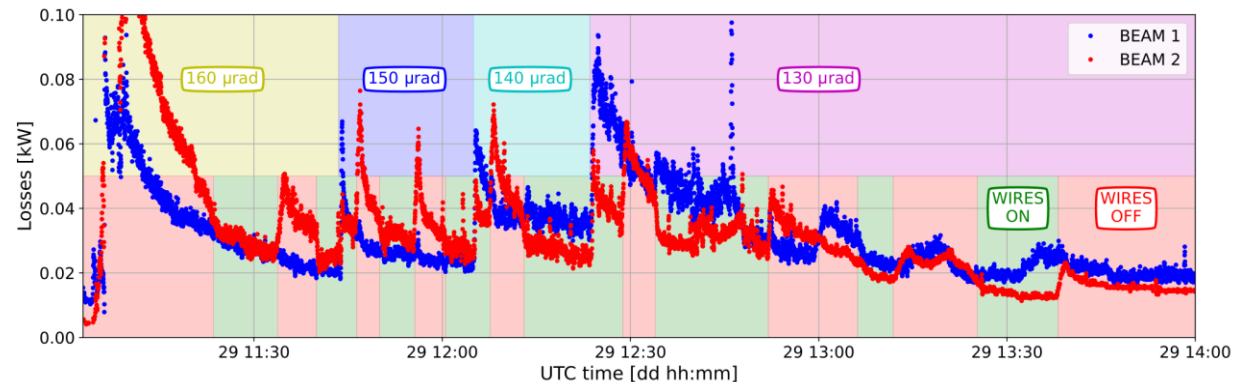
# Rise of beam-beam compensation

- In the last 20 years, we observe a rise in successful compensation scheme, based on detailed understanding of side effects such as noise (e-lens), feed-down and non-linear optics control (wire, crab waist, resonance compensation)



- Tune spread reduction measured by beam transfer function with and without electron lens [Fischer17]
- Compensation of **half** the tune shift in order to maintain Landau damping
- **Two fold increase of luminosity**

- Loss reduction with wires at the LHC (partial system deployed in operation, cf. Guido's talk)



# High intensity regime

- The failure of the 4-beam compensation scheme highlights the importance of understanding collective instabilities [Derbenev73]
  - Important work to understand stability (Landau damping) of beam-beam modes [Yokoya90, Perevdenstsev01, Chao05, Alexahin02] → Several measurements of the  $\sigma/\pi$  modes + flip-flop effect

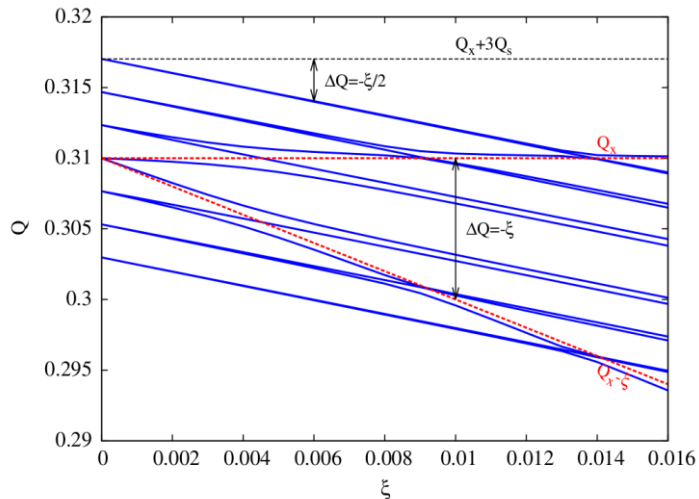
$$\mathcal{L} \approx \frac{I_{tot} \gamma \xi}{r_0 \beta^*} R_{HG}$$

$(\sigma_y = \sigma_x)$

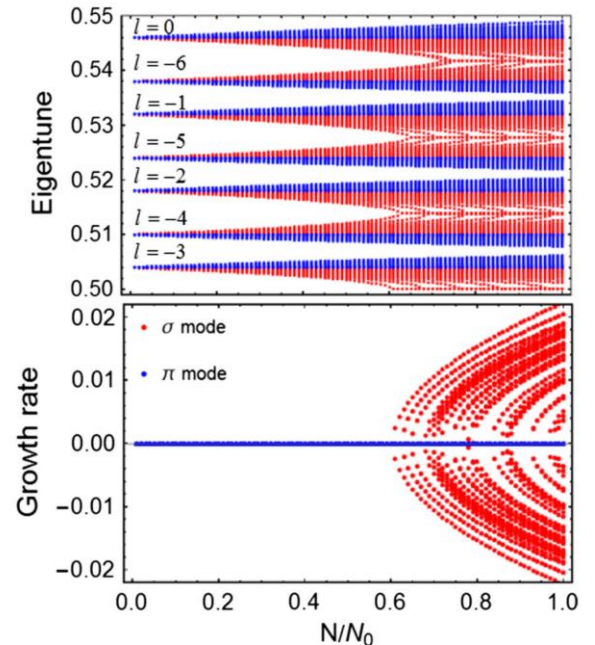
$$\mathcal{L} \approx \frac{\gamma}{2e r_e} \frac{I_{tot} \xi_y}{\beta_y^*} R_{HG}$$

$(\sigma_y \ll \sigma_x)$

- The high intensity regime pushes the beam stability
  - The need for tight collimation and a large number of cavities leads to **strong wake fields**
  - Feedback (noise) for the coupled bunch instability



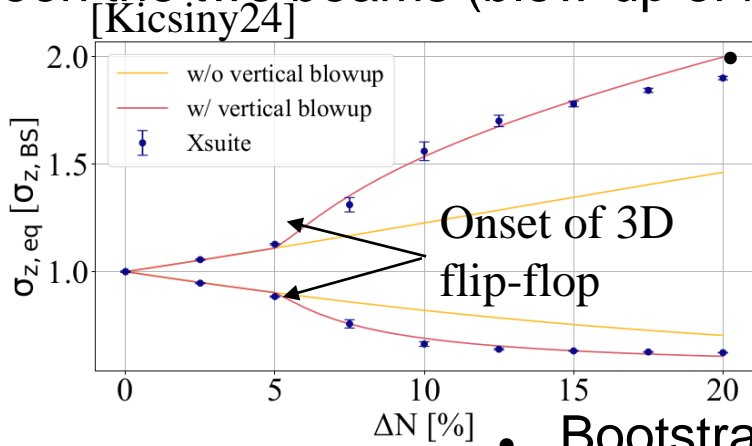
- Coupling instability of beam-beam modes caused by transverse impedance [White14, Zhang23]
- Loss of Landau damping for weak head-tail modes [Buffat14]



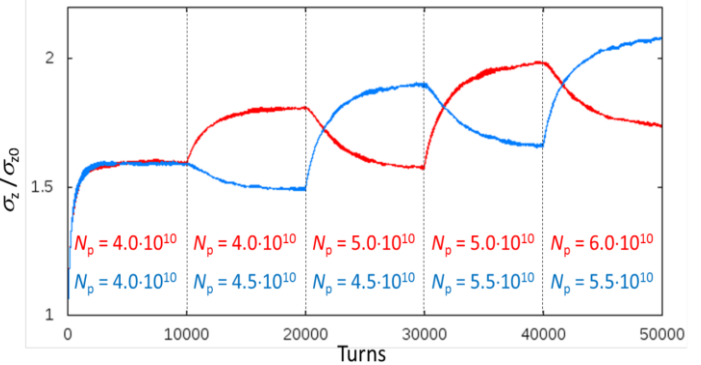
- Coupling instability of beam-beam modes caused by longitudinal impedance [Lin22]

# Beamstrahlung

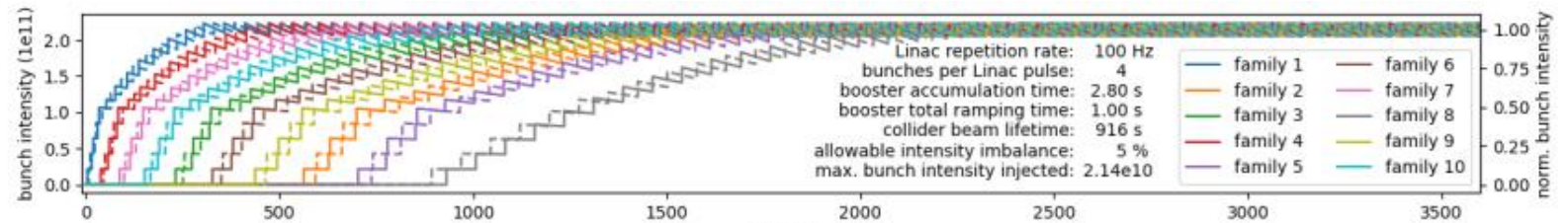
- Beamstrahlung is no longer exclusive to linear colliders
- → The energy spread is no longer defined by the lattice but rather the result from an **equilibrium** between the two beams (blow-up of bunch length decreases beamstrahlung)



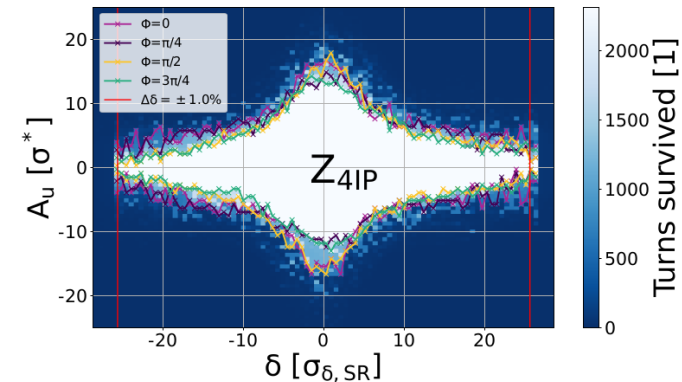
Bootstrap injection to gradually reach the equilibrium bunch length and maintain good enough symmetry between the beams [Shatilov17]



- Bootstrap injection that also mitigate e-cloud instabilities [Bartosik24]



- → The strength of the beam-beam interaction becomes limited by the lattice momentum acceptance (beamstrahlung lifetime)



# Muon colliders

- Multibunch operation is disfavored (The luminosity goes linearly with the number of bunches but quadratically with the bunch population)
- With a 'single pipe' acceleration chain, there will be beam-beam interactions in the re-circulating LINACs and rapid cycling synchrotrons, not only in the collider ring.
- Due to the short lifetime, the beam-beam force is strong only for few turns ( $\sim 100$ ), much larger beam-beam tune shift might be tolerable.

To be studied...

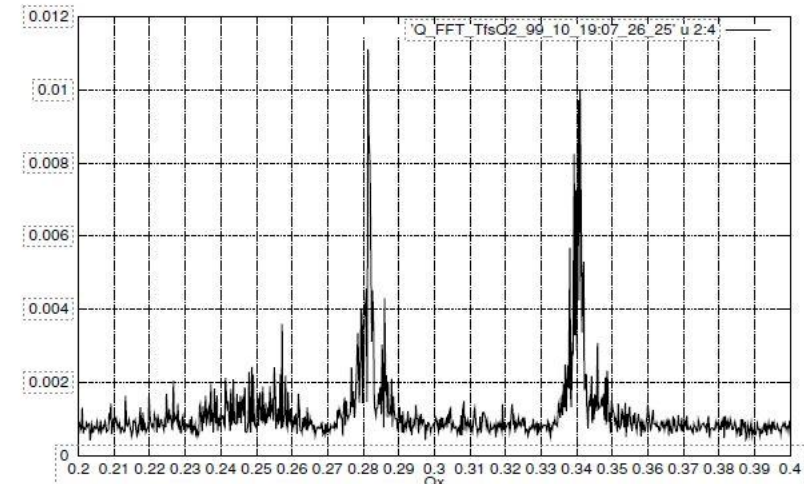
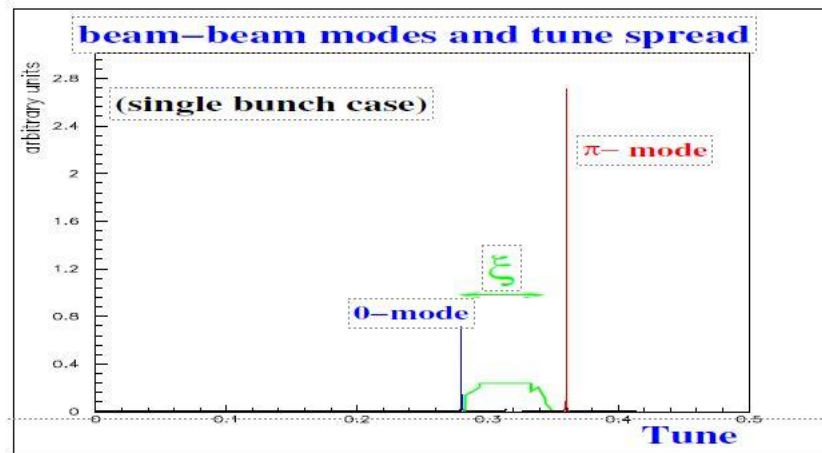
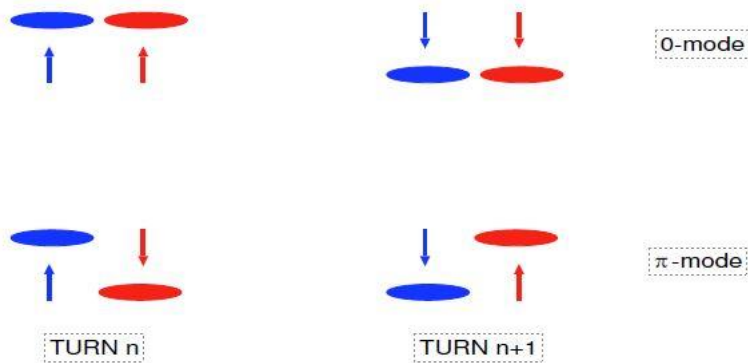
# Beam beam limit at LHC: why so much higher?

	LEP ( $e^+e^-$ )	LHC (pp)
Beam sizes	$160 - 200\mu\text{m} \cdot 2 - 4\mu\text{m}$	$16.6\mu\text{m} \cdot 16.6\mu\text{m}$
Intensity N	$4.0 \cdot 10^{11}/\text{bunch}$	$1.15 \cdot 10^{11}/\text{bunch}$
Energy	100 GeV	7000 GeV
$\beta_x^* \cdot \beta_y^*$	1.25 m $\cdot$ 0.05 m	0.55 m $\cdot$ 0.55 m
Crossing angle	0.0	285 $\mu\text{rad}$
Beam-beam parameter( $\xi$ )	(+) 0.0700	(-) 0.0034

X 2-3?

# Diagnostics and observables

- Beam-beam tune shift: is it a good measure of beam-beam interaction?
  - But! Close to integer resonances dynamic beta inflation!
  - Why is it larger than expected in the new/higher energy machines???
- Coherent modes ( $\sigma$  and  $\pi$  modes): beautiful observations



Need tools to measure the nonlinear aspects! Usable and be used!

# Rise of interplays

“Although beam-beam simulations have advanced in the past **25 years** or so, more ingredients need to be incorporated to make them more realistic, such as non-linear lattice maps, **field calculations** with bunch length effects, current-dependent effects [...] and errors such as jitter and off-center collisions.”

(after *M.A. Furman @ eeFACT97*)

**Most of these aspects will be discussed this week !**

# Challenges to design better colliders

## Maximum Integrated vs. peak luminosity

Hadrons: leveling schemes, radiation damping

Leptons: top-up injection

## Machine Detector Interface (MDI)

Hadrons: pile-up:  $10^9 - 10^{11}$  interactions/s, x100 particles/s

Hadrons & Leptons: Backgrounds in the detectors!

## Improved simulation tools and

... their **benchmarking** (LHC, SUPERKEKB, etc.)

**Relevant observables!**



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# Thank You

Wishing you a good workshop  
and  
lots of new ideas