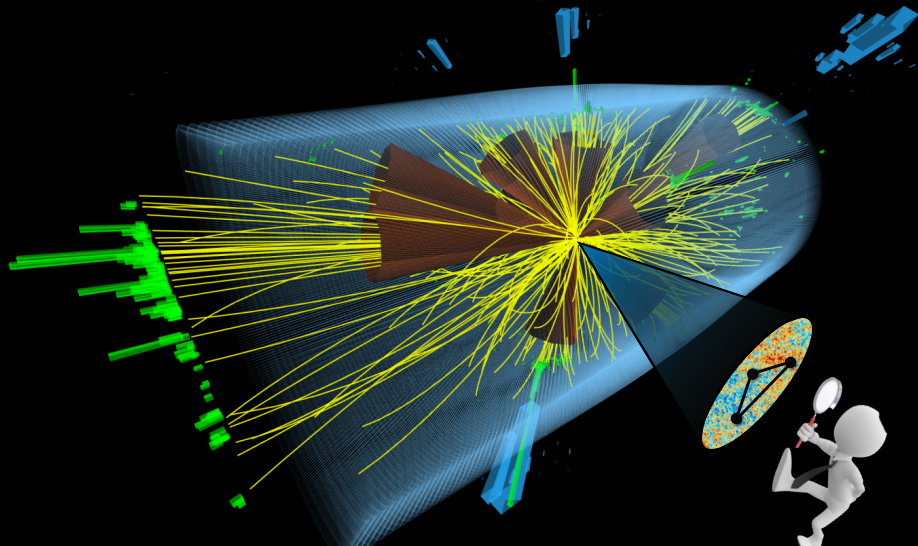


# Imaging Intrinsic and Emergent Scales of the QGP

Ian Moutt  
Yale



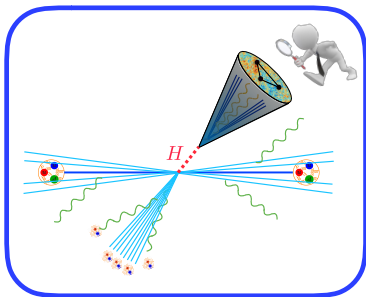
# Jet Substructure!



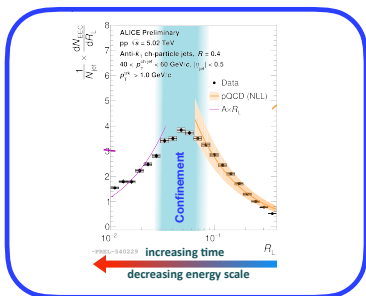
# Jet Substructure

- Jet substructure has emerged as a central new technique at colliders:

## Innovative Search Techniques



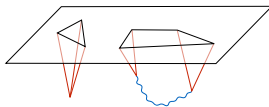
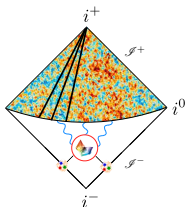
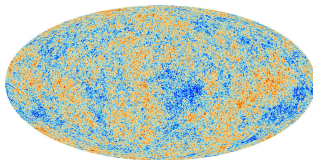
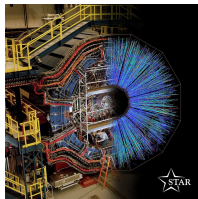
## Novel Probes of QCD Dynamics



- Has evolved well beyond its origin to have a large impact on BSM, SM, high energy QCD and nuclear physics.

# Decoding Energy Flux: QGP

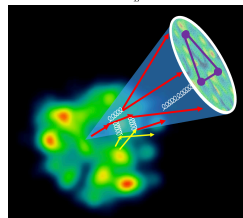
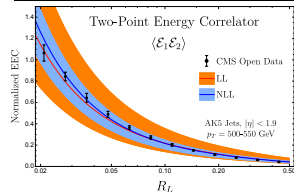
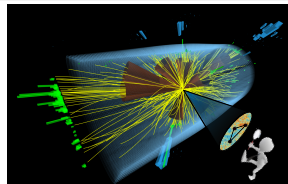
- Subtle questions about the QGP are imprinted in collider energy flux:



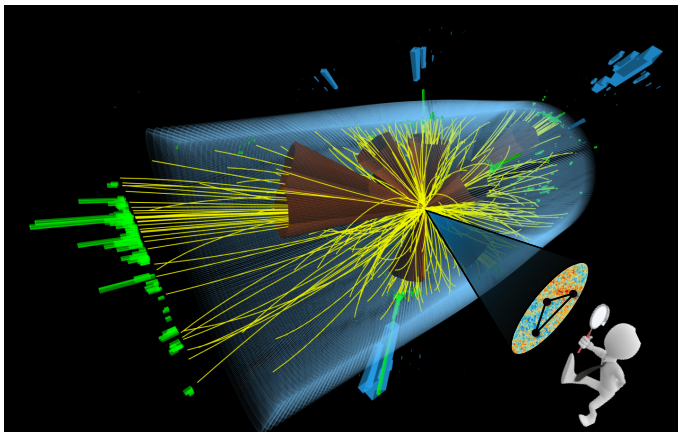
- Requires development of field theoretic techniques to interpret correlations in terms of the dynamics of the underlying field theory.

# Outline

- Decoding Energy Flux
- Scaling Behavior of Quarks and Gluons
- Imaging Intrinsic and Emergent Scales of the QGP

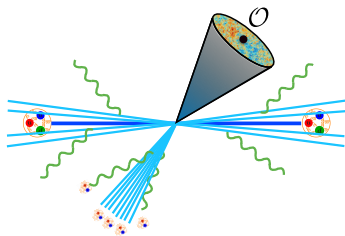


# Decoding Energy Flux



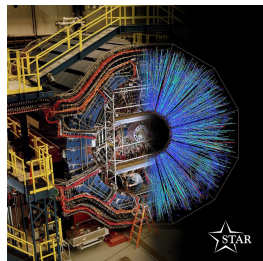
# Observables

- Observables are the link between theory and experiment:  
We want to make this link as direct as possible.



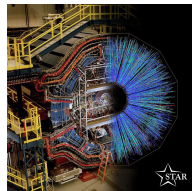
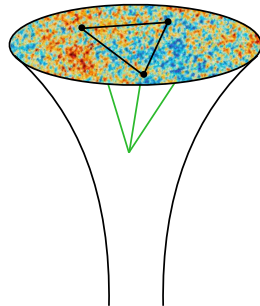
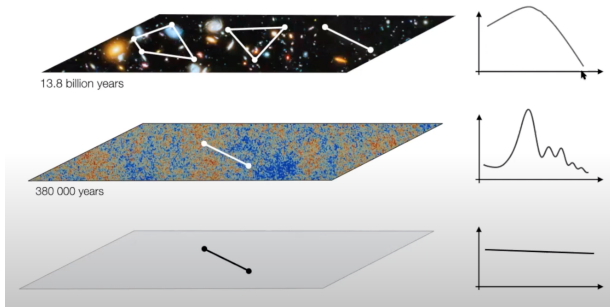
$$\langle \mathcal{O} \rangle = \langle \Psi | \mathcal{O} | \Psi \rangle$$

- As we move to studying more subtle features, we need to sharpen this link.
- Correctly choosing observables facilitates the experiment  $\leftrightarrow$  theory link.



# Decoding Energy Flux

- In condensed matter physics or cosmology we decode the underlying dynamics using correlation functions.



- What is the analog for collider physics?



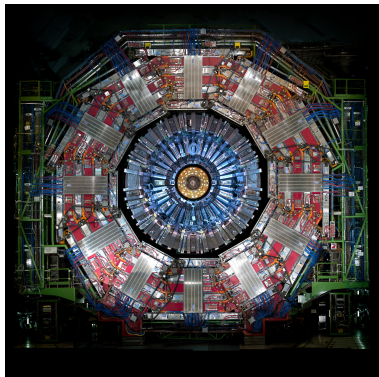
# Defining the Problem

- What is a detector?



$$\begin{aligned} \text{Hammer} &= \sum_i h_i \mathcal{O}_i \\ \text{Camera} &= \sum_j c_j \mathcal{D}_j \end{aligned}$$

[Caron Huot, Kologlu, Kravchuk, Meltzer, Simmons Duffin]

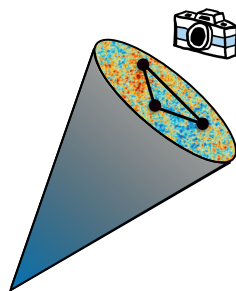


- To be able to understand subtle signals in energy flux, we must understand what a detector is in Quantum Field Theory.

# Calorimeter Cells in Field Theory

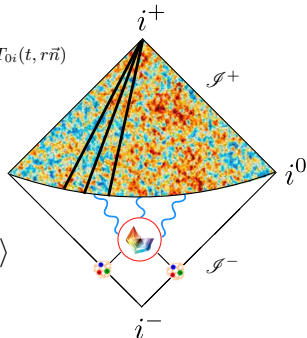
- Calorimeter cells can be given a field theoretic definition in terms of light-ray operators.

[Hofman, Maldacena]  
[Korchemsky, Sterman]  
[Ore, Sterman]  
[Basham, Brown, Ellis, Love]



$$\mathcal{E}(\vec{n}) = \lim_{r \rightarrow \infty} r^2 \int_0^\infty dt n^i T_{0i}(t, r\vec{n})$$

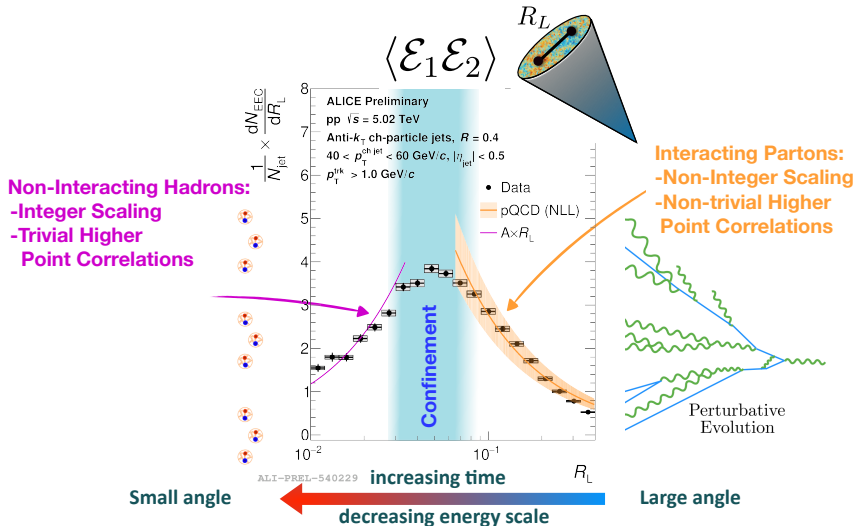
$$\langle \Psi | \mathcal{E}(\hat{n}_1) \cdots \mathcal{E}(\hat{n}_k) | \Psi \rangle$$



- Provides a sharp link between experimentally measurable observables and the underlying QFT.

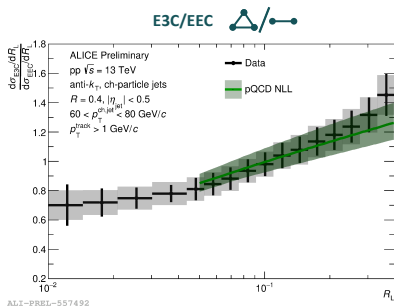
# Energy Correlators: Reality

Figure: Wenqing Fan



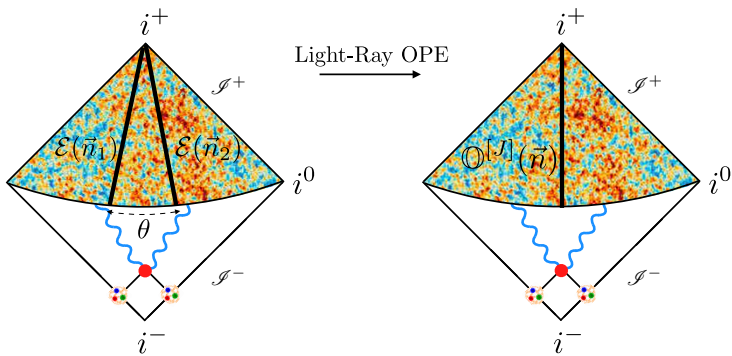
# Energy Correlators: Reality

- See talk by Ananya Rai on realities of vacuum measurement.



- See talk by Jussi Viinikainen on realities of heavy ion measurement.

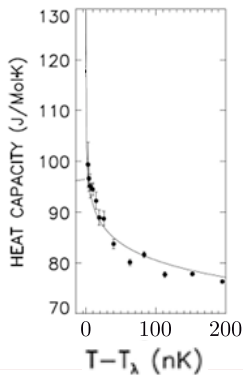
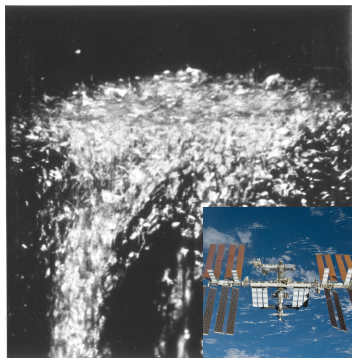
# Scaling Behavior of Quarks and Gluons



# Scaling Behavior in QFT

- Scaling behavior in Euclidean regime well understood.

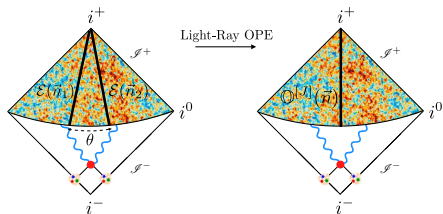
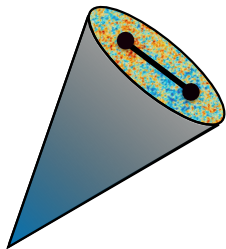
## $\lambda$ -point of Helium



$$\mathcal{O}(x)\mathcal{O}(0) = \sum x^{\gamma_i} c_i \mathcal{O}_i$$

# The OPE Limit of Lightray Operators

- Energy flow operators admit a Lorentzian OPE: “the lightray OPE”



$$\mathcal{E}(\hat{n}_1)\mathcal{E}(\hat{n}_2) \sim \sum \theta^{\tau_i-4} \mathbb{O}_i(\hat{n}_1)$$

[Hofman, Maldacena]

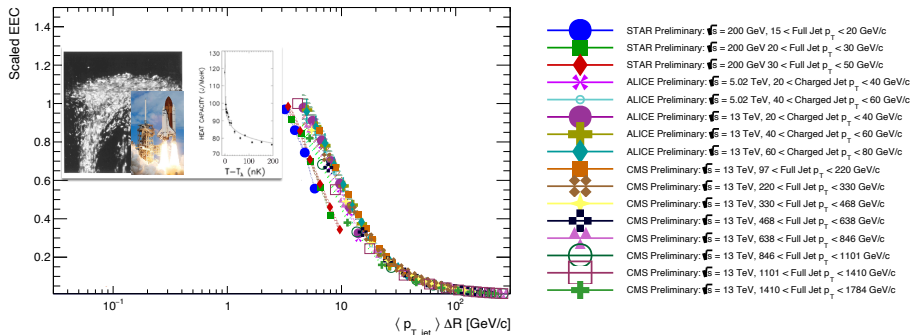
[Chang, Kologlu, Kravchuk, Simmons Duffin, Zhiboedov]

- Predicts universal scaling behavior in correlations of energy flux at energies  $E \gg \Lambda_{\text{QCD}}$ .

# Scaling Behavior in Jets

Thanks to Helen Caines, Meng Xiao, ChenFeng Lu,  
Andrew Tamis, Ananya Rai.

- The  $\mathcal{E}(\hat{n}_1)\mathcal{E}(\hat{n}_2)$  OPE inside high-energy jets!

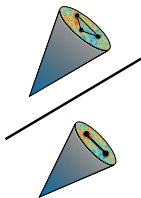


- Dominated by classical scaling. Can we accurately measure anomalous scaling?

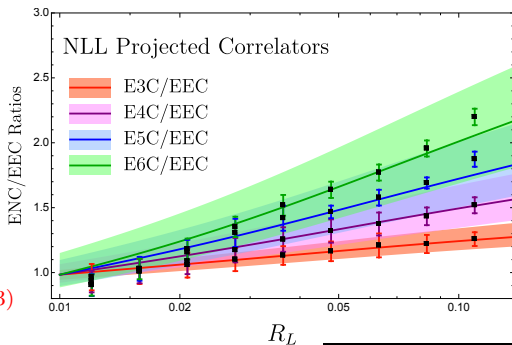


# The Spectrum of a Jet

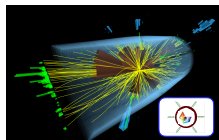
- The light-ray OPE predicts that the  $N$ -point correlators develop an anomalous scaling that depends on  $N$ .



$$\frac{\langle \mathcal{E}_1 \mathcal{E}_2 \dots \mathcal{E}_{J-1} \rangle}{\langle \mathcal{E}_1 \mathcal{E}_2 \rangle} \sim \frac{\langle \mathcal{O}^{[J]} \rangle}{\langle \mathcal{O}^{[3]} \rangle} \sim R_L^{\gamma(J) - \gamma(3)}$$



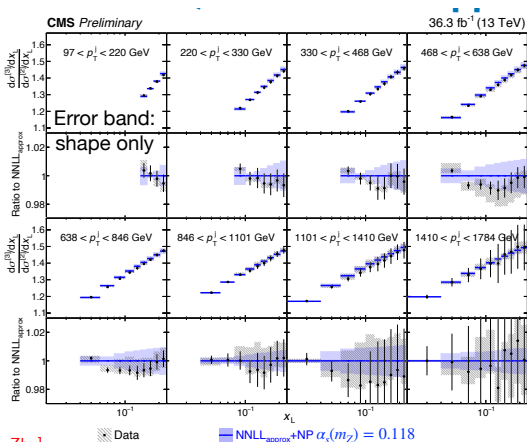
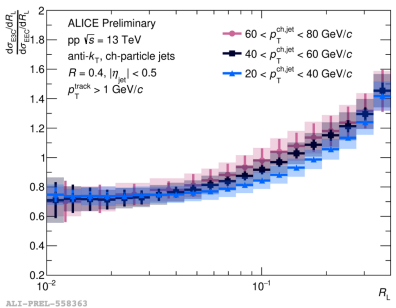
- Directly probes the spectrum of (twist-2) light-ray operators from asymptotic energy flux.



# Anomalous Scaling of 3/2 Ratio

- Anomalous scaling measured from 15 GeV to 1784 GeV!

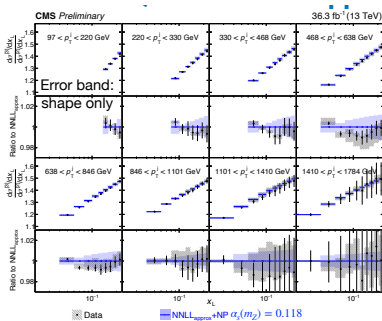
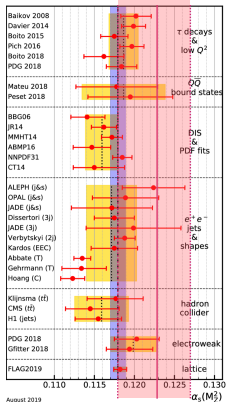
$$\frac{\langle \mathcal{E}_1 \mathcal{E}_2 \mathcal{E}_3 \rangle}{\langle \mathcal{E}_1 \mathcal{E}_2 \rangle} \sim \frac{\langle \mathcal{O}^{[3]} \rangle}{\langle \mathcal{O}^{[3]} \rangle} \sim R_L^{\gamma(4) - \gamma(3)}$$



Using [Lee, Mecaj, Moul], [Chen, Gao, Li, Xu, Zhang, Zhu]

# The Strong Coupling

- Proof of principle  $\alpha_s$  can be extracted from jet substructure in complicated hadron collider environment: 4% accuracy.
- Hope to use high energies of the LHC to resolve previous tensions in  $\alpha_s$  extractions.

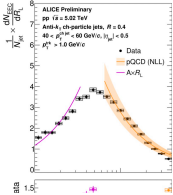
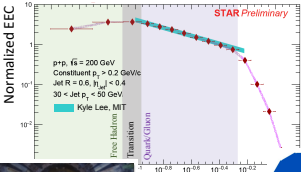
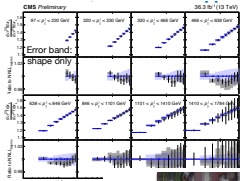


$$\alpha_s(m_Z) = 0.1229^{+0.0040}_{-0.0050}$$

$$= 0.1229^{+0.0014(stat.)+0.0030(theo.)+0.0023(exp.)}_{-0.0012(stat.)-0.0033(theo.)-0.0036(exp.)}$$

# Energy Correlators in Data

- A milestone in connecting jet substructure with QFT!



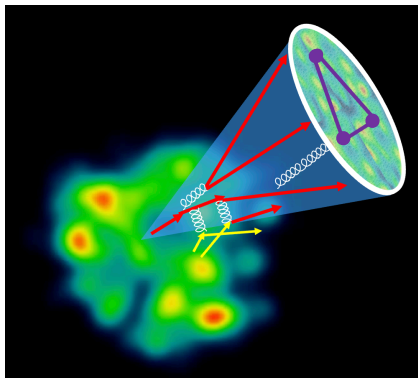
JETS ELUCIDATE HOW PARTONS EVOLVE INTO HADRONS



STRONG INTERACTIONS NEWS  
**Measuring energy correlators inside jets**  
 3 November 2023

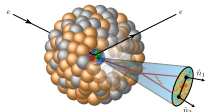
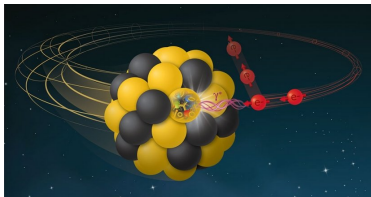
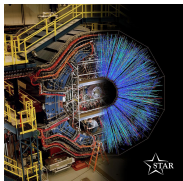
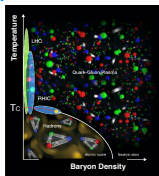
- Can we image how the QGP modifies the correlators?

# Resolving the Scales of the QGP

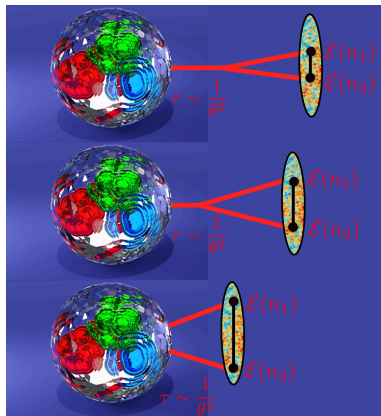


# Imaging Emergent and Intrinsic Scales of QCD

- Upshot: Massless QCD above the confinement scale exhibits powerlaw scaling in energy flux  $\implies$  any new scale introduced into the system will imprint itself at a characteristic scale.
- Understanding of jets in vacuum allows them to be used as well calibrated probes in more complicated systems: hot and cold nuclear matter.



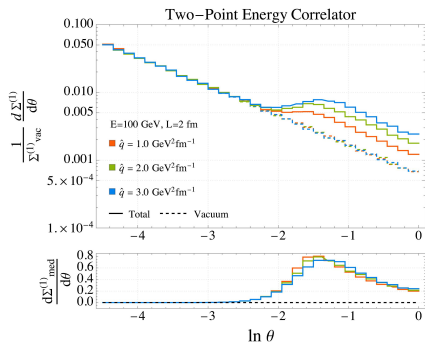
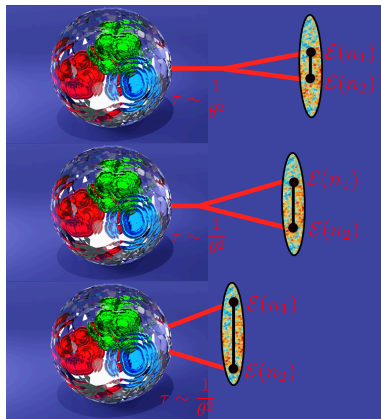
# Resolving the Scales of the QGP: Static Medium



- The QGP introduces a number of new scales into the problem.
- Consider first a static medium.
- We will focus on one scale,  $\theta_L \sim \frac{1}{\sqrt{LE}}$ , which determines the angle at which splittings resolve the medium

# Resolving the Scales of the QGP: Static Medium

- QGP scales cleanly imprinted in two-point correlation.

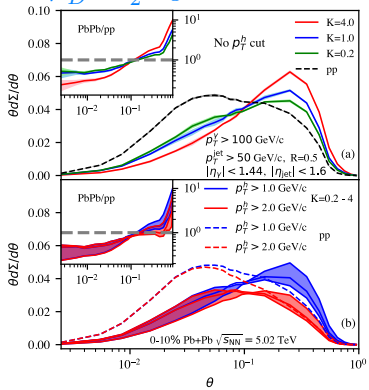
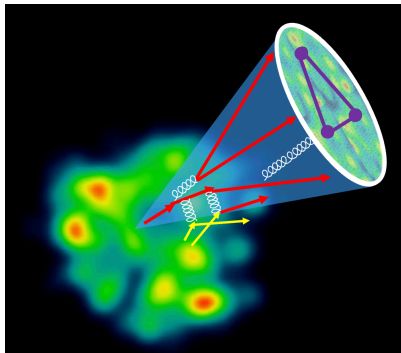


[Andres, Dominguez, Holguin, Kunnawalkam Elayavalli, Marquet, Moul] →

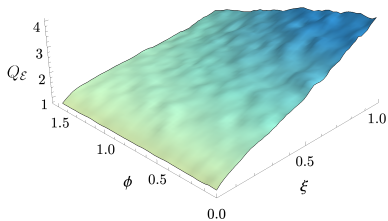
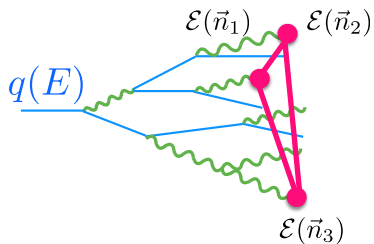


# Resolving the Scales of the QGP: Full Simulation

- Perform full simulation in CoLBT. [X.N. Wang et al.]
- Enhanced at large angles from both medium response and bremsstrahlung. Suppressed at small angles by energy loss and momentum broadening. [Yang, He, Moulton, Wang]
- Sensitivity to the Debye screening mass  $\mu_D^2 = \frac{3}{2}K g^2 T^2$ : Probe short distance structure of the QGP.

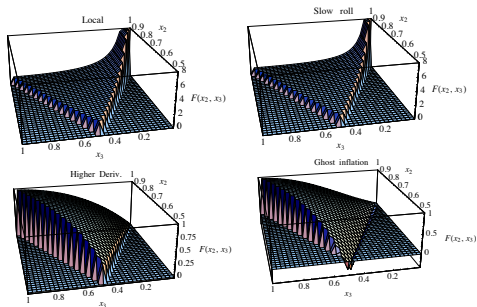
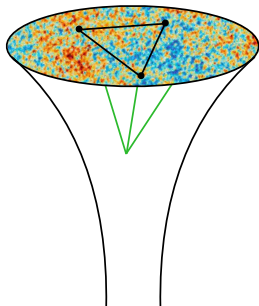


# Non-Gaussianities in Energy Flux



# Non-Gaussianities

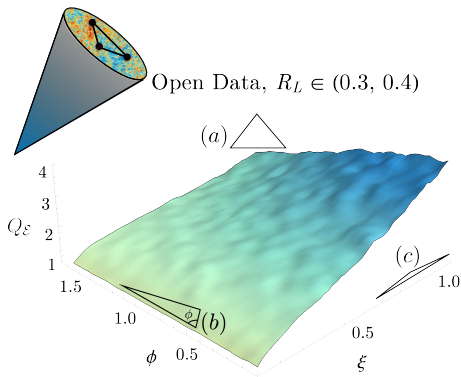
- Higher-point correlators probe more detailed aspects of interactions.
- e.g. Non-Gaussianities allow one to distinguish models of inflation.



- What is the structure of higher-point functions of energy flux?

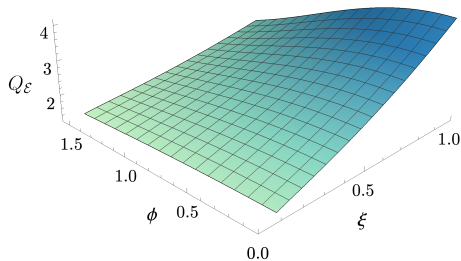
# Shape Dependence of Non-Gaussianities: Vacuum

- Can directly study non-gaussianities inside high energy jets.



$$G_{N,\xi}(z) = \frac{1+u+v}{2uv}(1+z) - \frac{1+u}{2uv}\log(u) - \frac{1+v}{2uv}\log(v) - (1+u+v)(0,+0,)\Phi(z) + \frac{(1+u^2+z^2)}{2uv}\Phi(z) + \frac{(z-z^2)(u+v+u^2+z^2+u^2v+uv^2)}{4u^2v^2}\Phi(z) + \frac{(u-1)(u+1)}{2uv^2}D_2^2(z) + \frac{(v-1)(v+1)}{2u^2v}D_2^2(1-z) + \frac{(u-v)(u+v)}{2uv}D_2^2\left(\frac{z}{z-1}\right)$$

LL + LO prediction,  $R_L = 0.35$



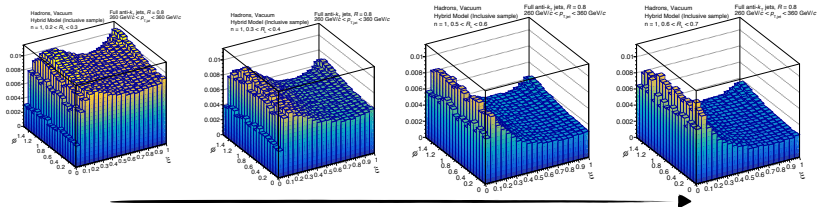
[Chen, Moutl, Thaler, Zhu]

- Illustrates theoretical control over multi-point correlations!

# Resolving the Scales of the QGP

- Higher point correlators allow us to probe the “shape” of modifications from the QGP: unravel different physical effects
- Illustrate by imaging the wake in the hybrid model.

## Vacuum



Increasing  $R_L$

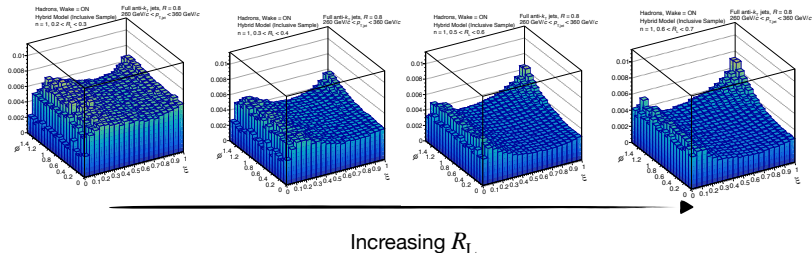
[Bossi, He, Kudinoor, Moul, Pablos, Rai, Rajagopal]



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## Wake

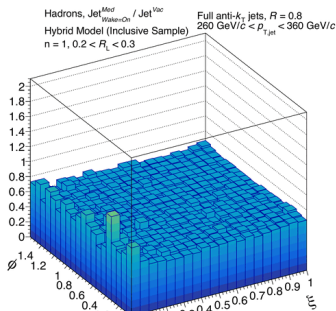
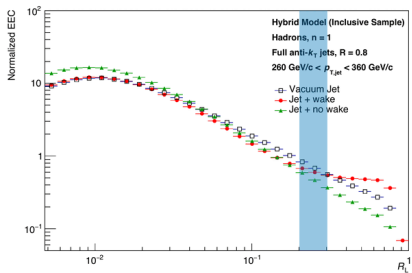


[Bossi, He, Kudinoor, Moul, Pablos, Rai, Rajagopal]



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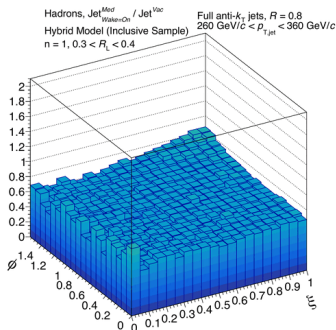
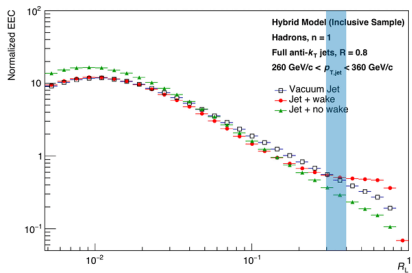


[Bossi, He, Kudinoor, Moul, Pablos, Rai, Rajagopal]



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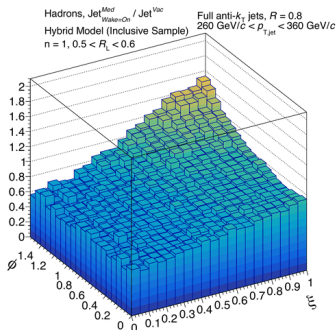
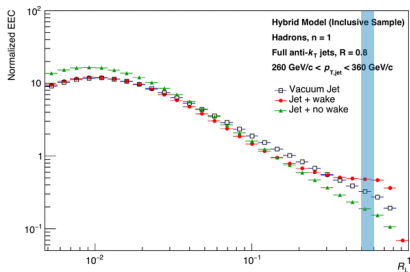


[Bossi, He, Kudinoor, Moul, Pablos, Rai, Rajagopal]



# Resolving the Scales of the QGP

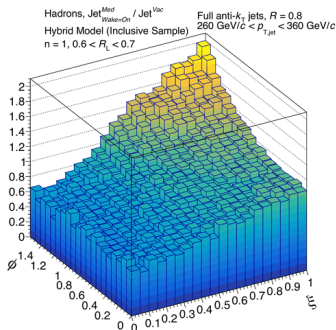
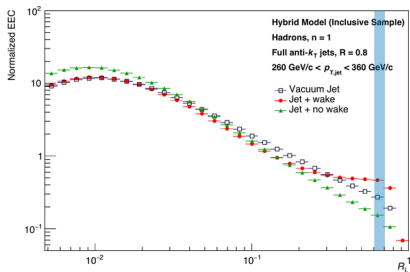
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[Bossi, He, Kudinoor, Moul, Pablos, Rai, Rajagopal]

# Resolving the Scales of the QGP

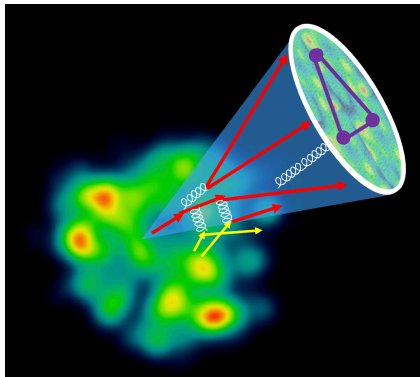
- Higher point correlators allow us to probe the “shape” of modifications from the QGP: unravel different physical effects
- Illustrate by imaging the wake in the hybrid model.



[Bossi, He, Kudinoor, Moul, Pablos, Rai, Rajagopal]

# Energy Correlators in Data

- Measurement of energy correlators in heavy ion will be a milestone in bridging collider measurements with the underlying QFT description of the QGP!

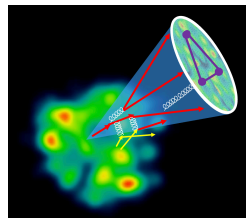
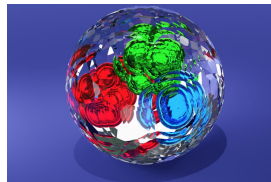
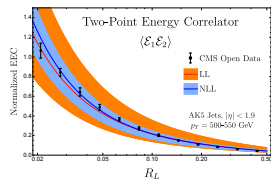


DATA?

- Will provide a direct measurement of this fundamental quantity in a finite temperature non-abelian gauge theory!

# Summary

- Correlation functions,  $\langle \mathcal{E}(n_1) \cdots \mathcal{E}(n_k) \rangle$ , provide a sharp link between theory and experiment. And can now be directly measured.
- Intrinsic and emergent scales imprint themselves in correlation functions at characteristic scales.
- Energy correlators provide a unique new tool to unravel the microscopic structure of the QGP.



Thanks!