

Lukas R. Weith & Luciano Rezzolla  
Goethe University Frankfurt

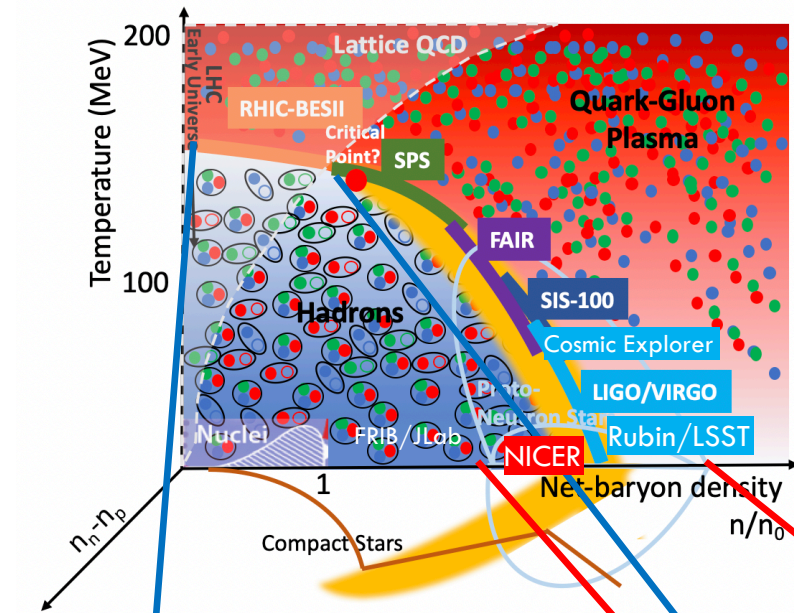
# STATUS OF THE MUSES COLLABORATION

Claudia Ratti  
University of Houston

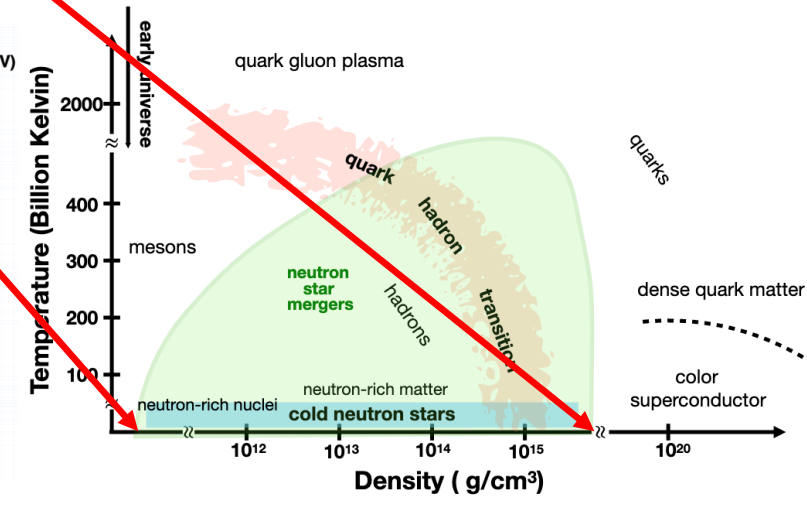
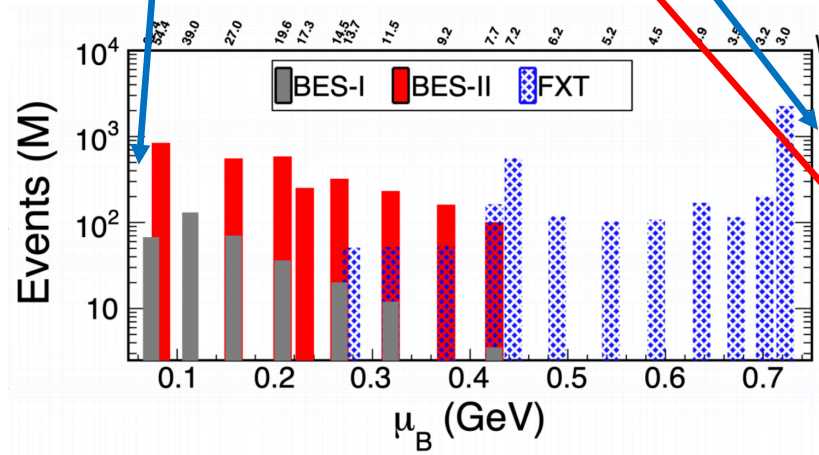


# MOTIVATING SCIENCE GOALS

- Is there a critical point in the QCD phase diagram?
- What are the degrees of freedom in the vicinity of the phase transition?
- Where is the transition line at high density?
- What are the phases of QCD at high density?
- What is the nature of matter in the core of neutron stars?



- Run 2019:
  - Collider:  $\sqrt{s_{NN}} = 14.6, 19.6, 200$  GeV
  - Fixed target:  $\sqrt{s_{NN}} = 3.2$  GeV
- Run 2020:
  - Collider:  $\sqrt{s_{NN}} = 9.2, 11.5$  GeV
  - Fixed target:  $\sqrt{s_{NN}} = 3.5, 3.9, 4.5, 5.2, 6.2, 7.2, 7.7$  GeV
- Run 2021:
  - Collider:  $\sqrt{s_{NN}} = 7.7, 17.3$  GeV
  - Fixed target:  $\sqrt{s_{NN}} = 3.0, 9.2, 11.5, 13.7$  GeV



# TERRESTRIAL FACILITIES FOR FINITE-DENSITY QCD

Compilation by D. Cebra

CP=Critical Point

OD= Onset of  
Deconfinement

DHM=Dense  
Hadronic Matter

Facility	RHIC BESII	SPS	SIS-100 SIS-300	J-PARC HI
Exp.:	STAR +FXT	NA61	CBM	JHITS
Start:	2019-2021	2009	2025	2025
Energy:	7.7– 19.6	4.9-17.3	2.7-8.2	2.0-6.2
$\sqrt{s_{NN}}$ (GeV)	2.5-7.7			
Rate:	100 HZ	100 HZ	<10 MHZ	100 MHZ
At 8 GeV	2000 Hz			
Physics:	CP&OD	CP&OD	OD&DHM	OD&DHM

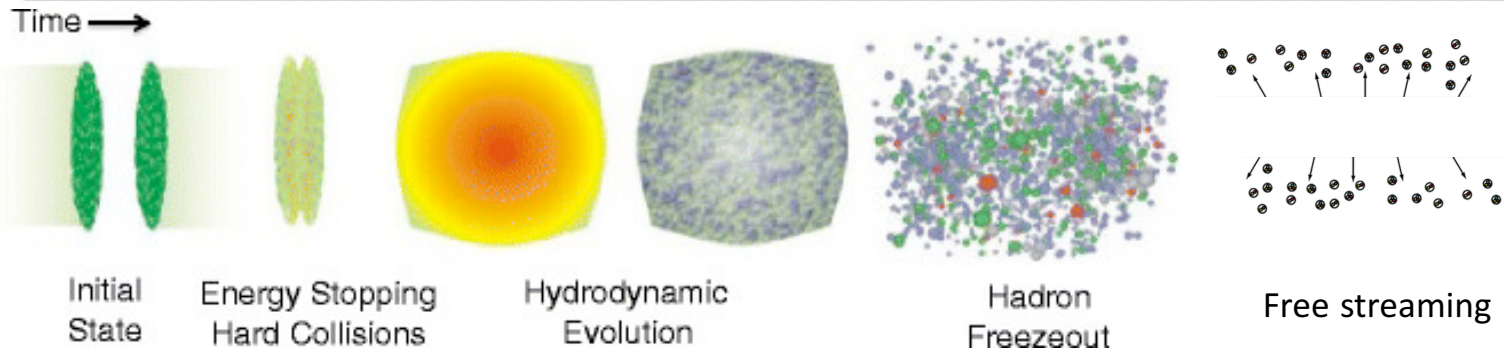
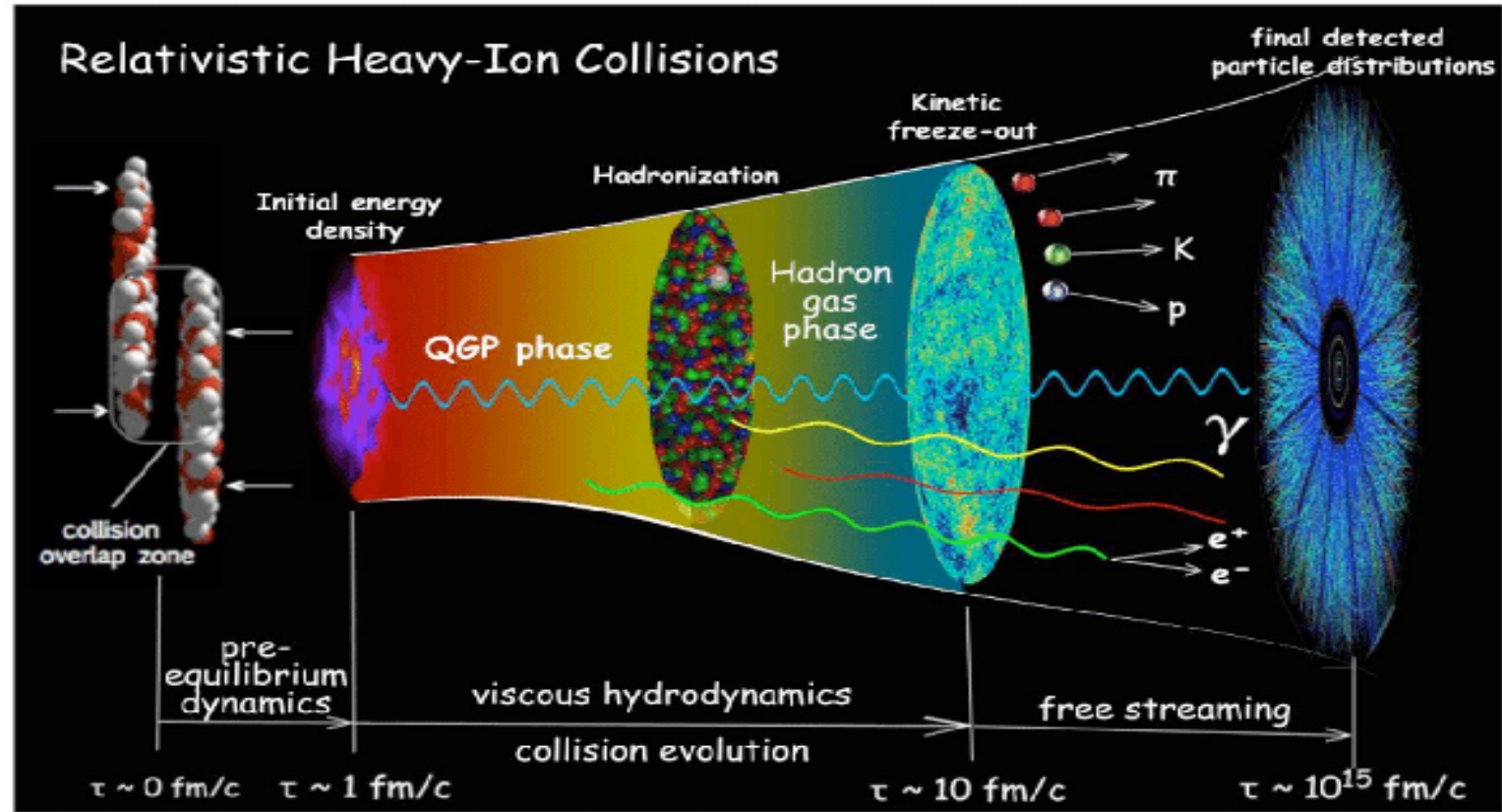
Collider  
Fixed target

Fixed target  
Lighter ion  
collisions

Fixed target

Fixed target

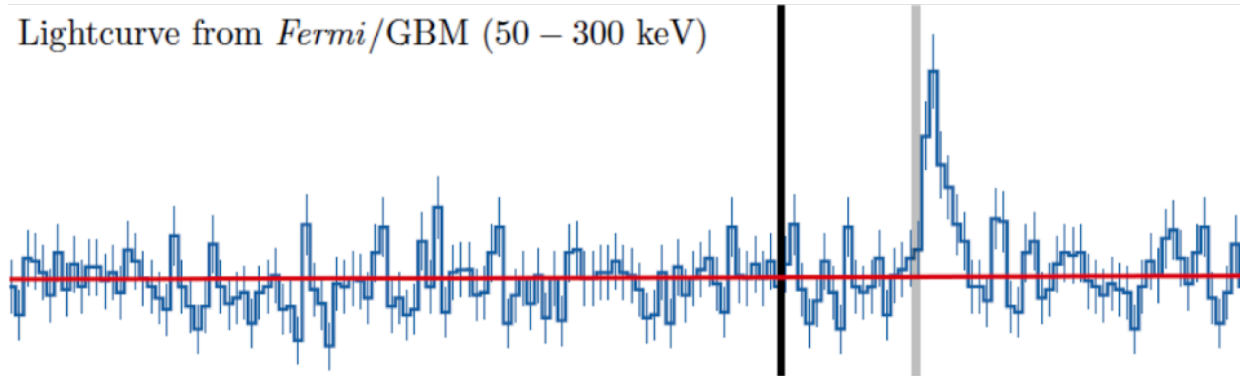
# ANATOMY OF A HEAVY-ION COLLISION



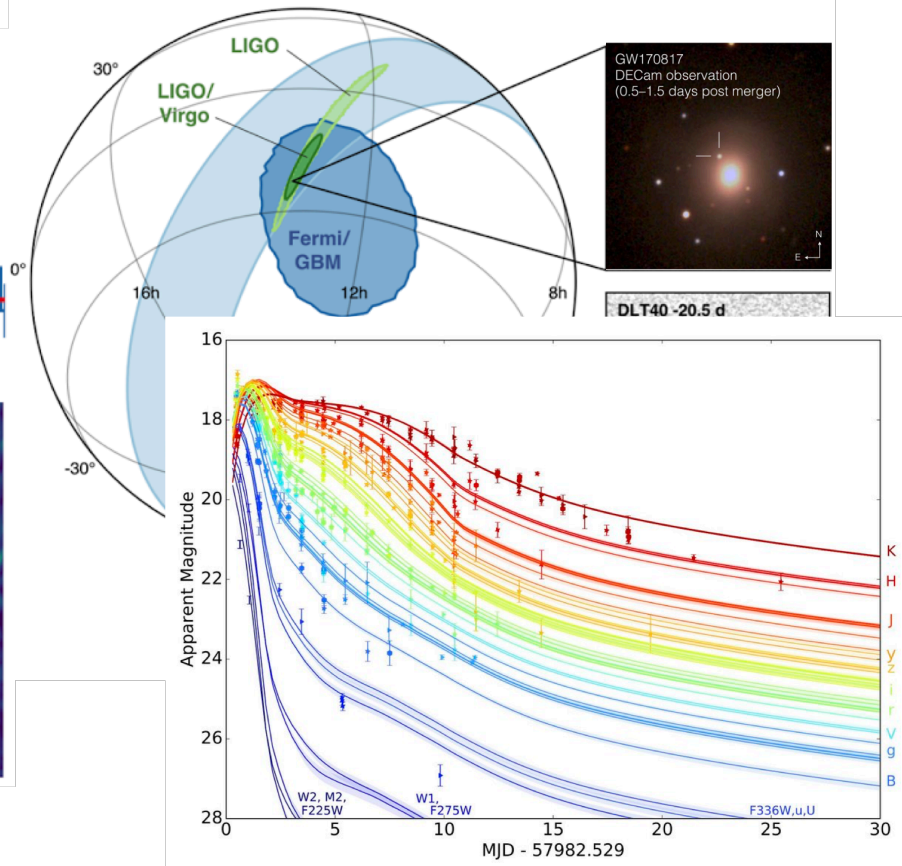
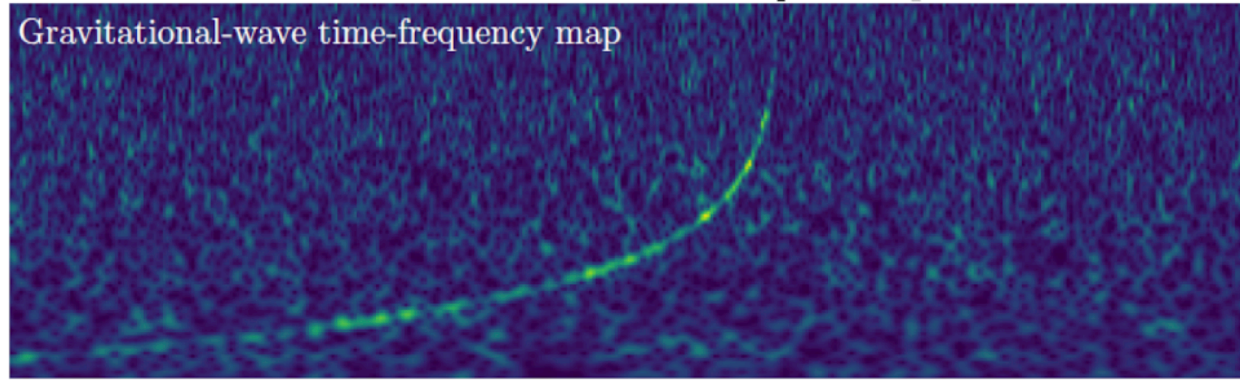
# GW170817

Demonstrated the ability of mergers to advance nuclear physics

Lightcurve from *Fermi*/GBM (50 – 300 keV)



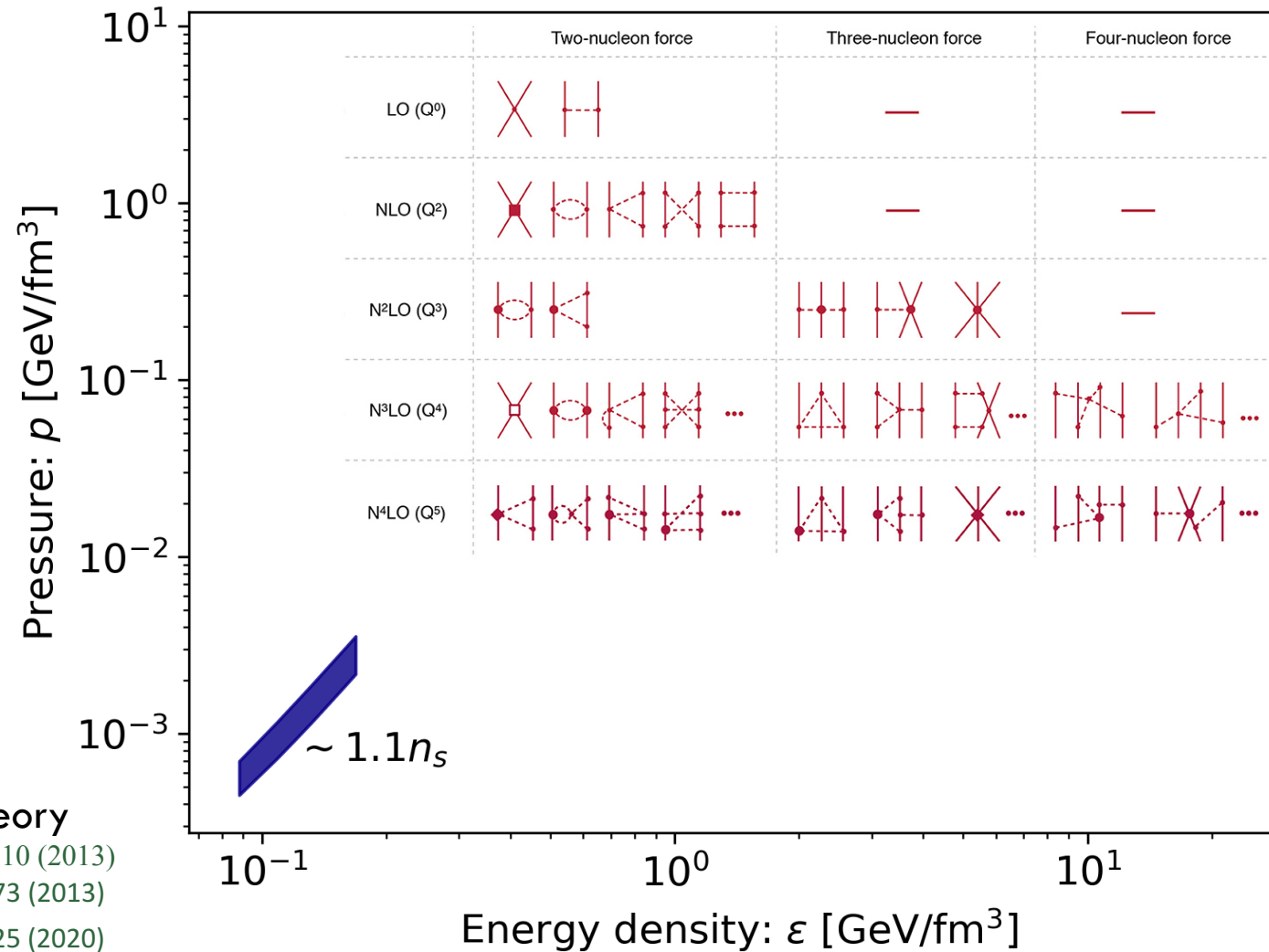
Gravitational-wave time-frequency map



LIGO/Virgo PRL (2017)

P.S. Cowperthwaite et al., *Astrophys. J. Lett.* (2017)

# NEUTRON STARS AND MERGERS



Chiral effective theory

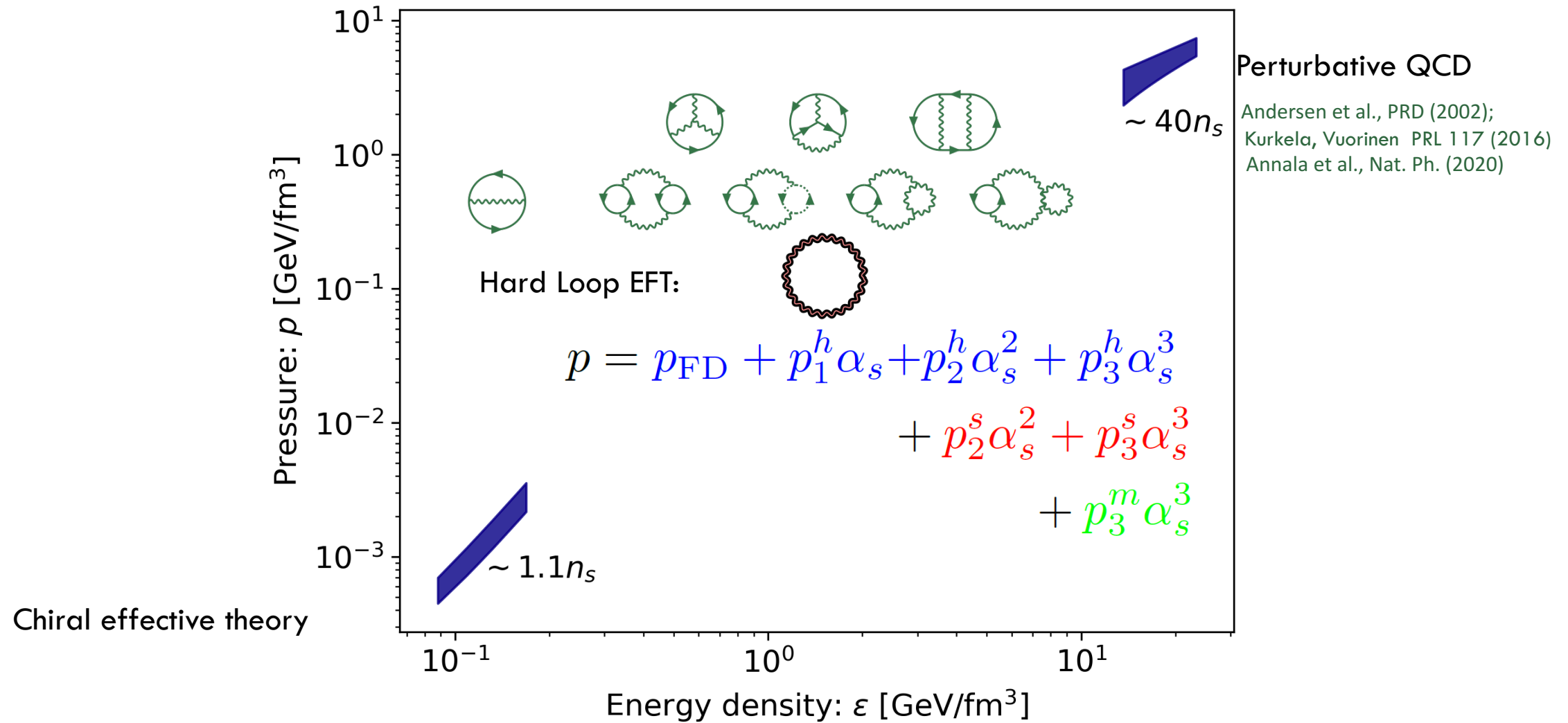
Tews et al. PRL 110 (2013)

Hebeler, Lattimer et.al. APJ 773 (2013)

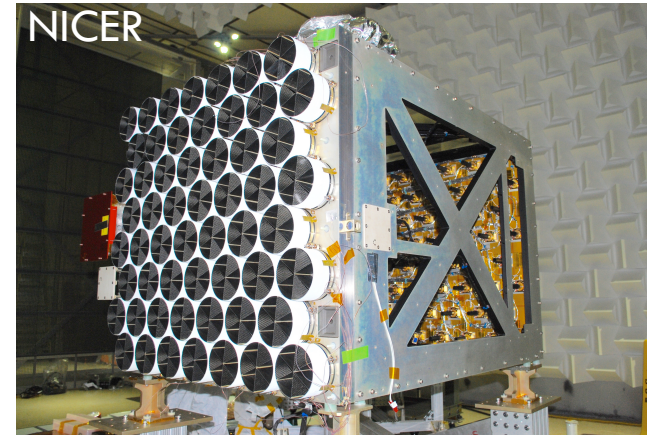
Drischler, Furnstahl et.al. PRL 125 (2020)



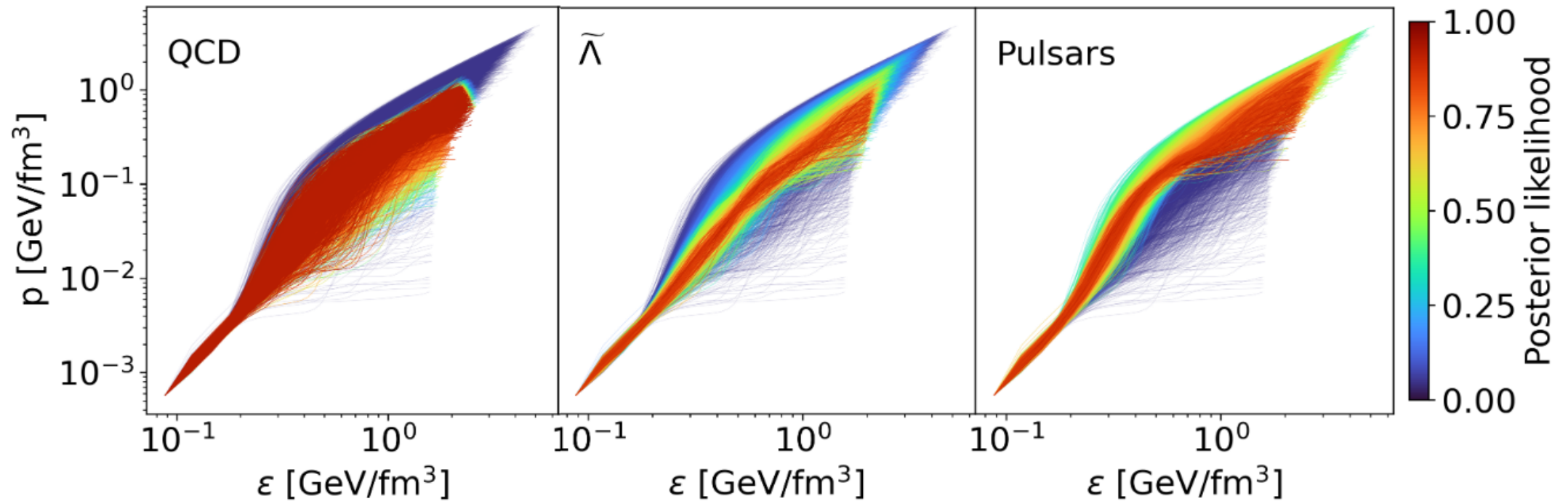
# NEUTRON STARS AND MERGERS



# NEUTRON STARS AND MERGERS



QCD input and NS observations can constrain the interpolation

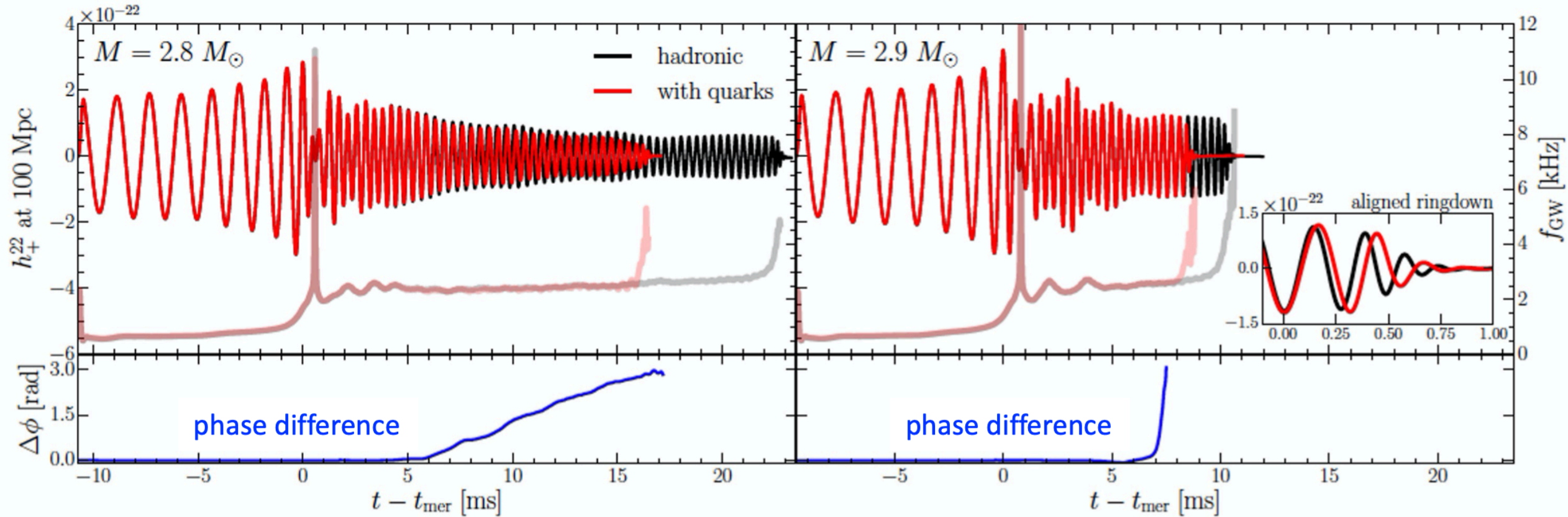
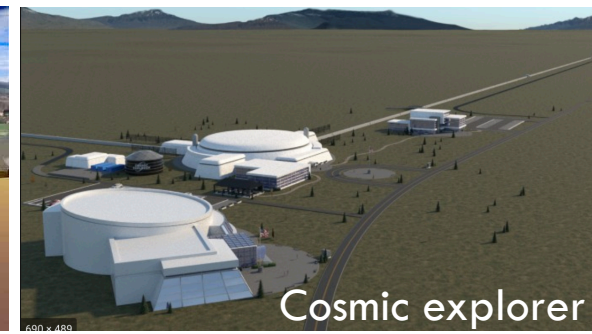
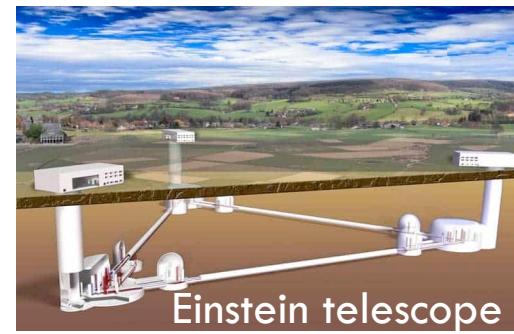


Slide adapted from talk by A. Kurkela



# NEUTRON STARS AND MERGERS

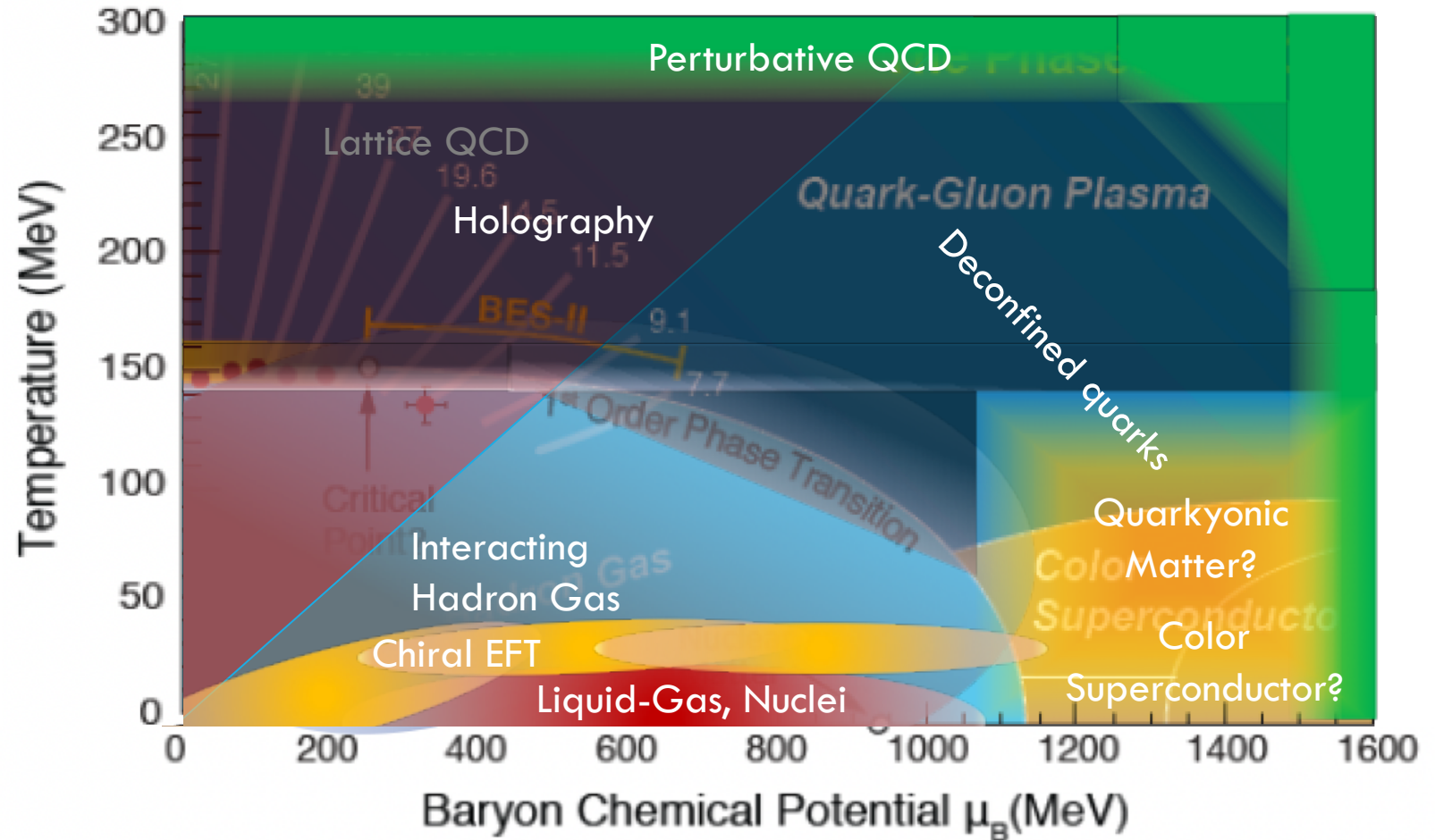
- Post-merger signal sensitive to order of the phase transition
- Next generation observatories will be able to detect it!
- Need to combine the nuclear physics input and simulations



E. Most et al., PRL (2019)

# WHAT HAPPENS AT LARGE DENSITIES?

- We need to merge the lattice QCD equation of state with other effective theories
- Careful study of their respective range of validity
- Constrain the parameters to reproduce known limits
- Test different possibilities and validate/exclude them



Lattice QCD: S. Borsanyi, C. R. et al, PRL (2021)  
 Interacting HRG: V. Vovchenko et al., PRL (2017)  
 Liquid-gas, Nuclei: see e.g. Du et al. PRC (2019)  
 Chiral EFT: see e.g. Holt, Kaiser, PRD (2017)  
 Holography: R. Critelli, C. R. et al., PRD (2017)

pQCD: Andersen et al., PRD (2002); Annala et al., Nat. Ph. (2020)  
 quarks: C. R. et al., PRD (2006), Dexheimer et al., PRC (2009);  
 Baym et al., Astr. J. (2019)  
 quarkyonic: McLerran, Pisarski NPA (2007)  
 CSC: Alford et al., PLB (1998); Rapp et al., PRL (1998), S. Rossner,  
 C. R. et al, PRD (2007), .



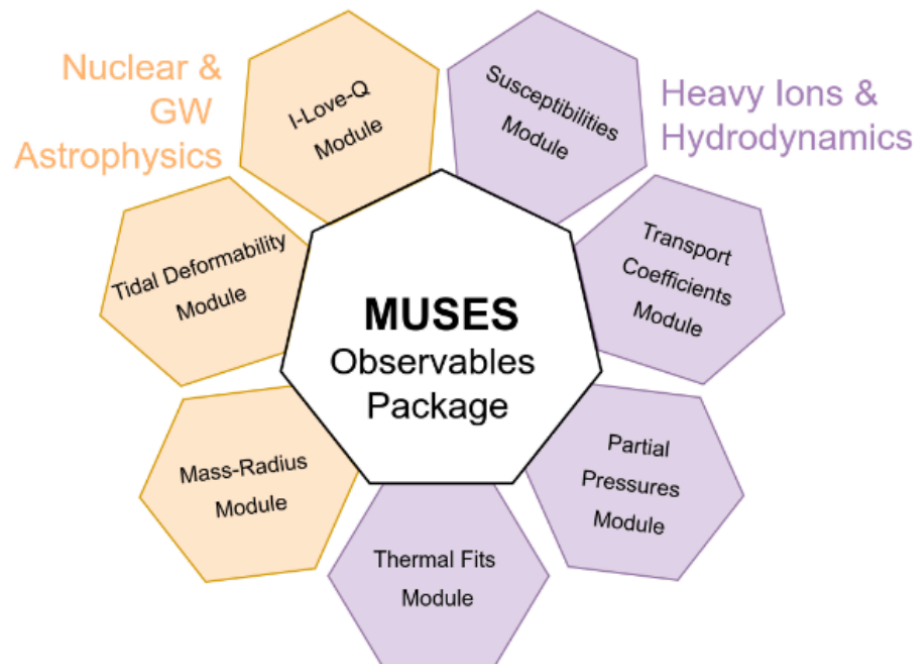
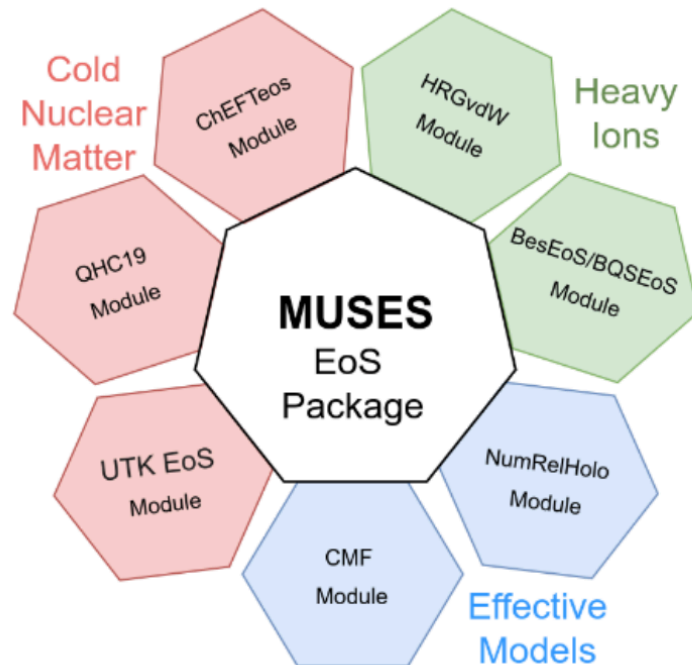
# MUSES – MODULAR UNIFIED SOLVER OF THE EQUATION OF STATE

*“An open-source **cyberinfrastructure** fostering a **community-driven** ecosystem that provides key **computational tools** to promote, transform and support groundbreaking research in nuclear physics and astrophysics, computational relativistic fluid dynamics, gravitational-wave and computational astrophysics.”*

- **Modular:** while at low densities the equation of state is known from 1<sup>st</sup> principles, at high  $\mu_B$  we will implement different models (“modules”) that the user will be able to pick
- **Unified:** the different modules will be smoothly merged together to ensure maximal coverage of the phase diagram, while respecting established limiting cases (lattice, perturbative QCD, ChPT...)

# MUSES GOALS AND MILESTONES

- CyberInfrastructure of interoperating tools and services within a replicable and flexible deployment system
  - Upgrade of existing calculation tools to modern programming languages
  - **Equation of State (EoS) package** that combines all the EoS modules using smooth transition functions
  - **Web-based tools and services** that provide interactive interfaces to the calculation engine
  - **Job management system** that executes client-requested calculations using the best available processing system
  - Scalable, high-availability **deployment system** that can be reproduced in other computing environments



# DEVELOPERS & USERS

- The team which we put together consists of
  - **Developers:** physicists + computer scientists will work together to develop the software that generates the equations of state over a range of temperature and chemical potentials to cover the whole phase diagram
  - **Users:** a variety of scientists from different communities, who have expressed an interest in the output of the framework



# PARTICIPANTS

## PI and co-PIs

1. Nicolas Yunes; University of Illinois at Urbana-Champaign; **PI**
2. Jacquelyn Noronha-Hostler; University of Illinois at Urbana-Champaign; co-PI
3. Jorge Noronha; University of Illinois at Urbana-Champaign; co-PI
4. Claudia Ratti; University of Houston; co-PI and **spokesperson**
5. Veronica Dexheimer; Kent State University; co-PI

## Senior investigators

1. Matias Carrasco Kind; National Center for Supercomputing Applications
2. Roland Haas; National Center for Supercomputing Applications
3. Timothy Andrew Manning; National Center for Supercomputing Applications
4. Andrew Steiner; University of Tennessee, Knoxville
5. Jeremy Holt; Texas A&M University
6. Gordon Baym; University of Illinois at Urbana-Champaign
7. Mark Alford; Washington University in Saint Louis
8. Elias Most; Princeton University

## External collaborators

1. Helvi Witek; University of Illinois at Urbana-Champaign
2. Stuart Shapiro; University of Illinois at Urbana-Champaign


This is the list that appeared in the proposal  
BUT: Muses collaboration paper was signed by 58 authors  
→ We are growing!

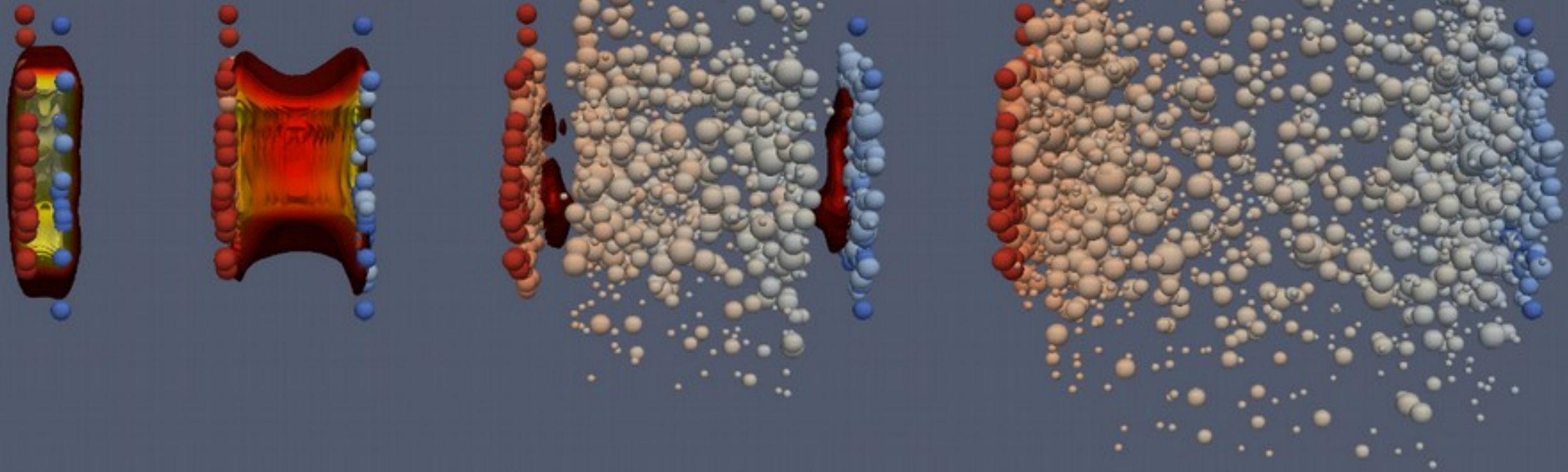
3. Katerina Chatziioannou; California Institute of Technology
4. Phillip Landry; California State University Fullerton
5. Reed Essick; Perimeter Institute
6. Rene Bellwied; University of Houston
7. David Curtin; University of Toronto
8. Michael Strickland; Kent State University
9. Matthew Luzum; University of Sao Paulo
10. Hajime Togashi; Kyushu University
11. Toru Kojo; Central China Normal University
12. Hannah Elfner; GSI/Goethe University Frankfurt



# ALPHA-RELEASE: MAY 1<sup>ST</sup> 2024

## DETAILS

- ❖ A first set of modules will be released on this date
- ❖ They will be open-source, but still preliminary
- ❖ We invite interested people to test these modules and give us their feedback
- ❖ The modules to be released will be marked as  during my talk



# EOS FOR HEAVY IONS

- EoS from first principles
- EoS with 3D Ising critical point
- HRG model
- EoS from Holography



# HEAVY ION COLLISIONS: DETAILS AND NEEDS

## DETAILS

- ❖ System is described in terms of hydrodynamic simulations
- ❖ Strangeness neutrality  $\langle \rho_S \rangle = 0$
- ❖ Short lifetime, strangeness conserved
- ❖ Charge: p vs. n in ions:  $\langle \rho_Q \rangle = 0.4 \langle \rho_B \rangle$
- ❖ System is not in equilibrium

## NEEDS

- ❖ To take into account local fluctuations, 4D Equation of State is needed
- ❖ Free parameters:  $T, \mu_B, \mu_S, \mu_Q$
- ❖ Thermodynamic variables ( $p, s, \epsilon, \rho_B, c_s^2$ )
- ❖ 1<sup>st</sup> and 2<sup>nd</sup> order derivatives of pressure with respect to chemical potentials
- ❖ Inclusion of critical point
- ❖ Transport coefficients

**α-RELEASE**

See talk by Johannes Jahan

# EQUATION OF STATE FROM FIRST PRINCIPLES (BQSEOS)

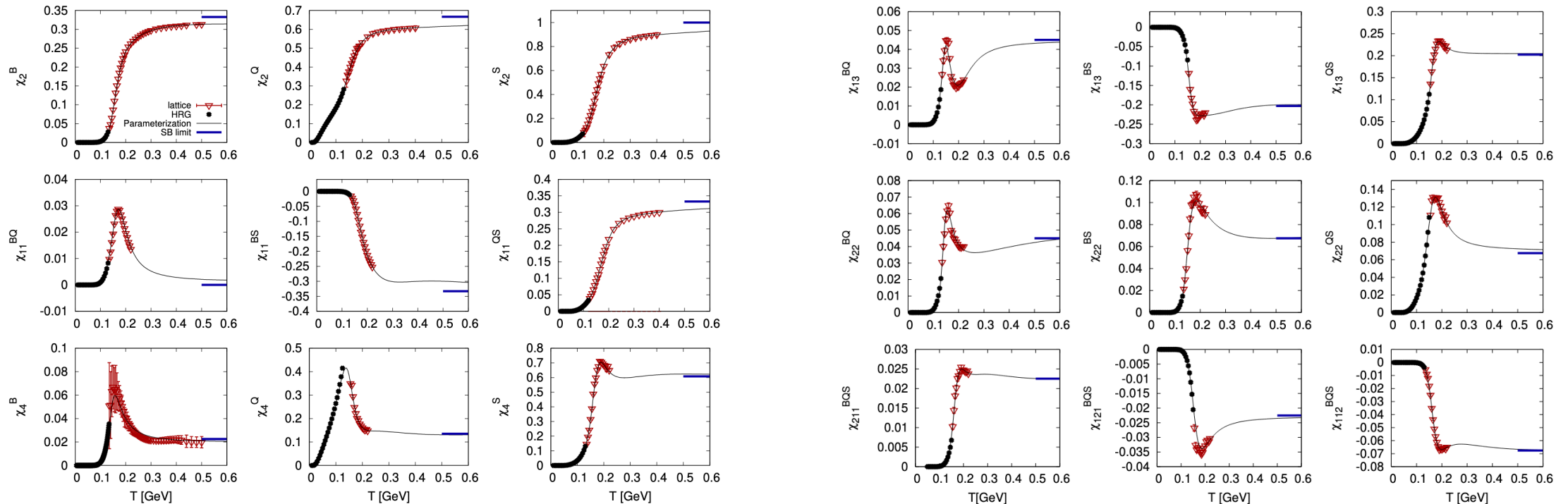
Range:  $0 < T < 600 \text{ MeV}$ ;  $\mu_B < 450 \text{ MeV}$

- Full Taylor expansion needed to study different  $\mu_S$  and  $\mu_Q$  scenarios

$$\frac{p(T, \mu_B, \mu_Q, \mu_S)}{T^4} = \sum_{i,j,k} \frac{1}{i!j!k!} \chi_{ijk}^{BQS} \left(\frac{\mu_B}{T}\right)^i \left(\frac{\mu_Q}{T}\right)^j \left(\frac{\mu_S}{T}\right)^k$$

- Coefficients are available up to global order 4 ( $\mu/T < 2$ )

S. Borsanyi, C. R. et al., JHEP (2018)  
 J. Noronha-Hostler, C. R. et al., PRC (2019)  
 A. Monnai et al., PRC (2019)



# UPDATE: NEW EXPANSION SCHEME (4D-TEXS)

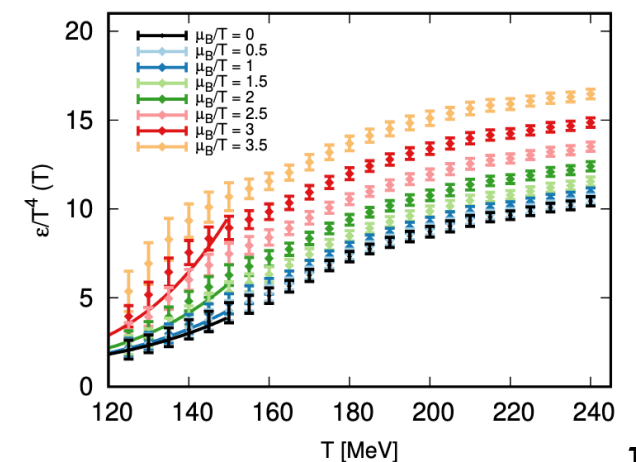
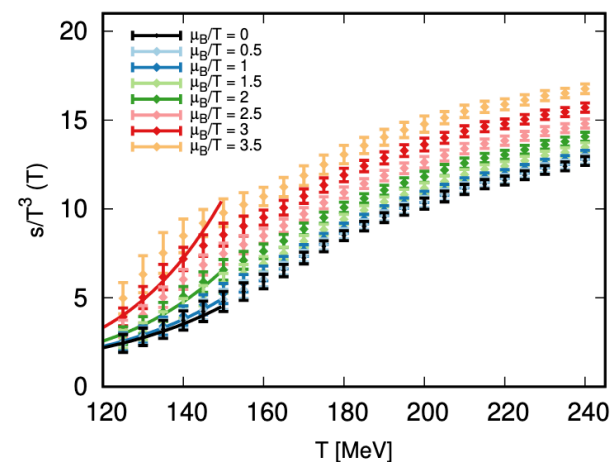
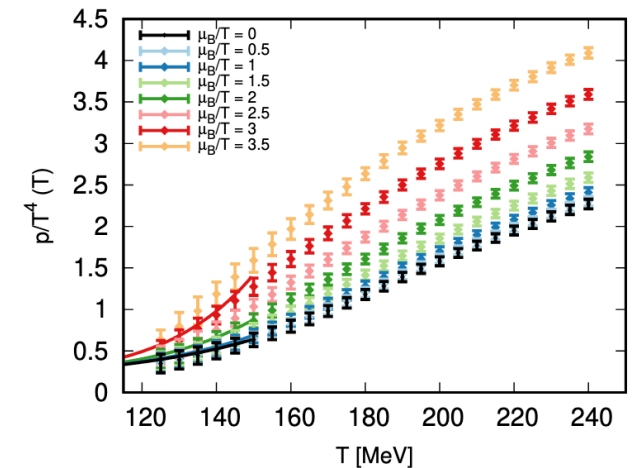
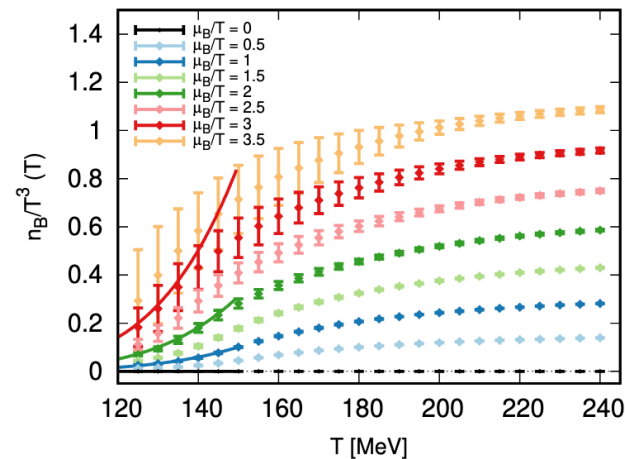
- Novel expansion scheme allows to extend to  $\mu_B/T \sim 3.5$
- EoS available at  $\mu_S = \mu_Q = 0$
- It was recently extended to the case  $\langle n_S \rangle = 0$ ,  $\langle n_Q \rangle = 0.4 \langle n_B \rangle$  of relevance for heavy-ion collisions

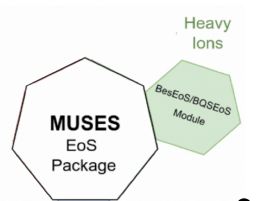
## Goals:

- Extension to  $\mu_S$  &  $\mu_Q \neq 0$  (4D)
- Implementation into the MUSES engine

S. Borsanyi, C. R. et al., PRL (2021)

S. Borsanyi, C. R. et al., PRD (2022)





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# ISING-TEXS EOS

To put 3DIsing model Critical behavior into Lattice QCD Alternative Expansion EoS for  $\mu_B \in [0,700]MeV$  and  $T \in [10,800]MeV$

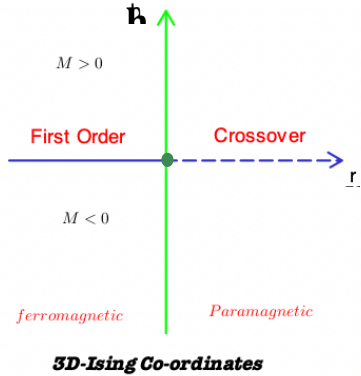
**Purpose:**

**Physics:**

$$n_B(T, \mu_B) = \frac{\mu_B}{T} \chi_2^B(T', 0)$$

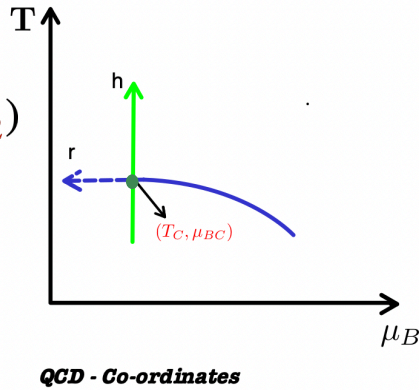
$$T'[T, \mu_B] = T \left[ 1 + \kappa_2^{BB}(T) \left(\frac{\mu_B}{T}\right)^2 + \kappa_4^{BB}(T) \left(\frac{\mu_B}{T}\right)^4 + \mathcal{O}\left(\frac{\mu_B}{T}\right)^6 \right]$$

See talk by Micheal Kahangirwe  
arXiv: 2402.08636

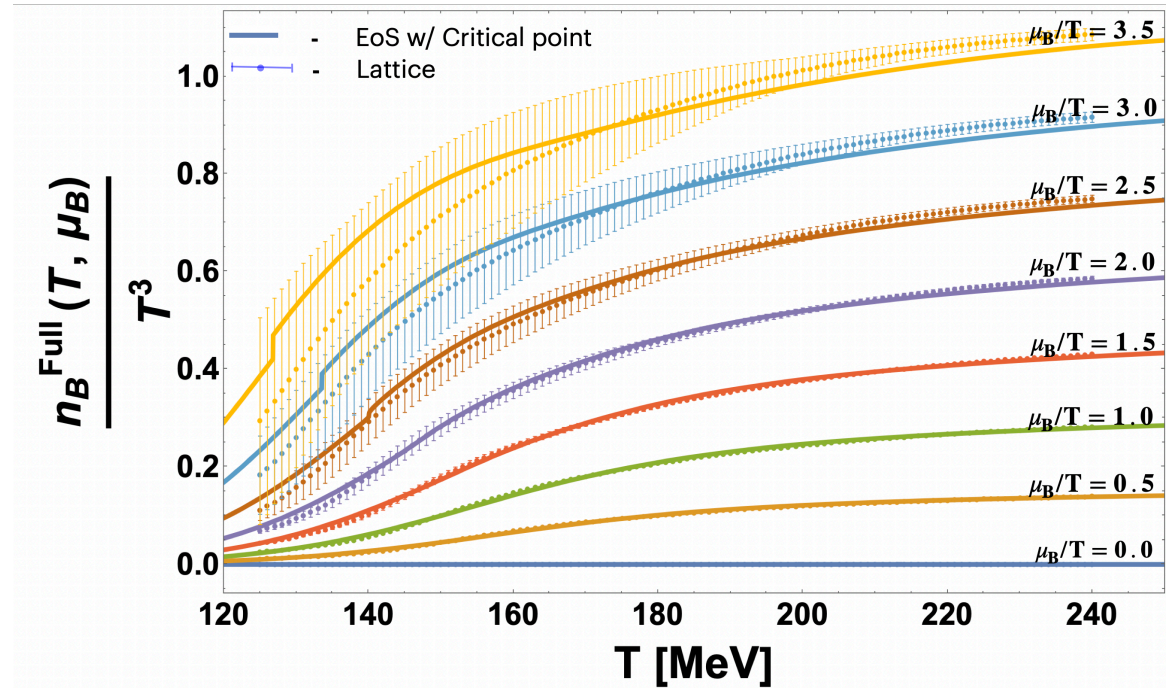


$$\frac{T' - T_0}{T_0} = w h \sin \alpha_{12}$$

$$\frac{\mu_B^2 - \mu_{BC}^2}{T_0^2} = w(-r\rho - h \cos \alpha_{12})$$



**User Input**  $\mu_{BC}, w, \rho, \alpha_{12}$



**Status:**



Available on GitHub

**Remaining Work:**

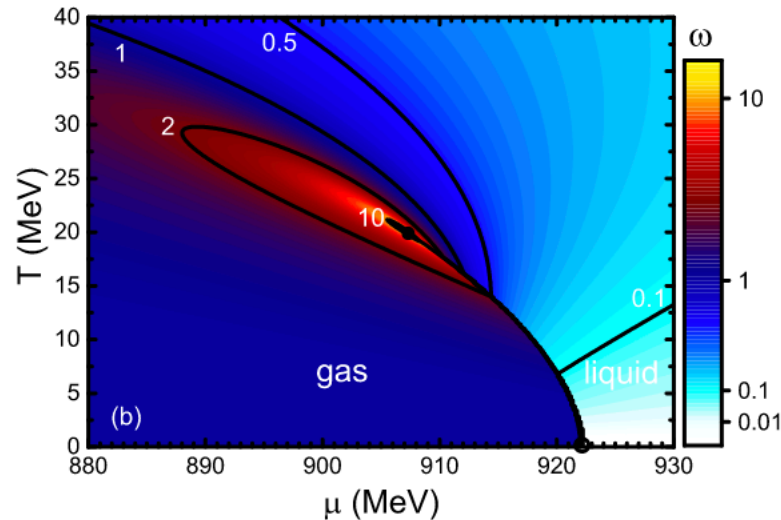
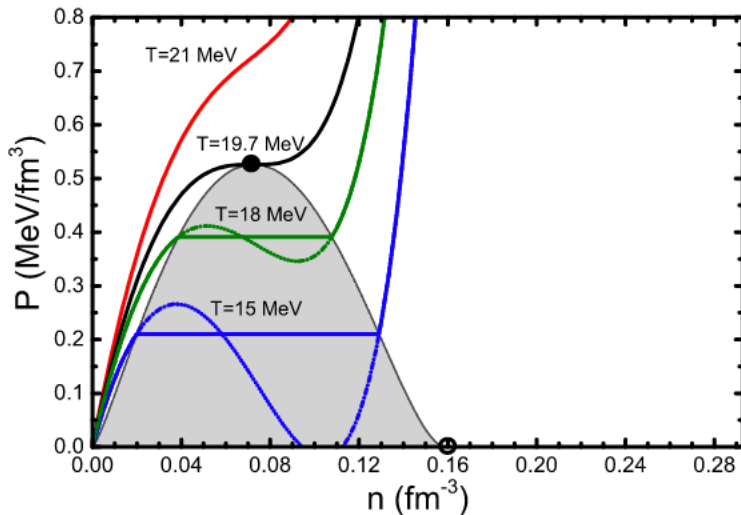
- Defining the YAML specifications & manifest + Python wrappers to ensure input/output compatibility requirements
- Create the Docker container



# HADRON RESONANCE GAS (HRG) MODEL

Range:  $0 < T < 160 \text{ MeV}$ ;  $\mu_B < 1 \text{ GeV}$

- The HRG model provides a well-established and realistic Equation of State at low temperatures
- Its ideal version is based on the assumption that an **interacting gas of hadrons** in the ground state can be well-approximated by an **ideal gas of resonances**
- At large density we need to incorporate additional interactions such as van Der Waals
- It describes the liquid-gas phase transition



- Goals:**
- Fix the parameters to describe the liquid-gas critical point
  - Thermal FIST already does this
  - Incorporation into MUSES
  - Extend hadronic spectrum to the most updated PDG list

# EQUATION OF STATE FROM HOLOGRAPHY (NUMRELHOLO)

J. Grefa, C. R. et al., PRD (2021), PRD (2022)

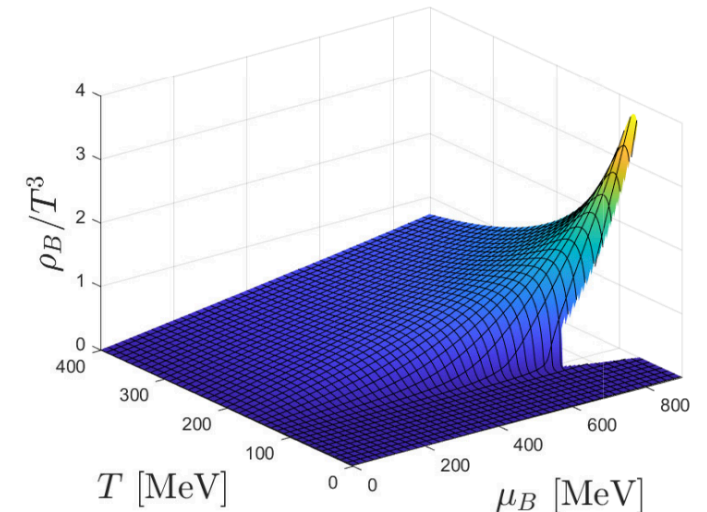
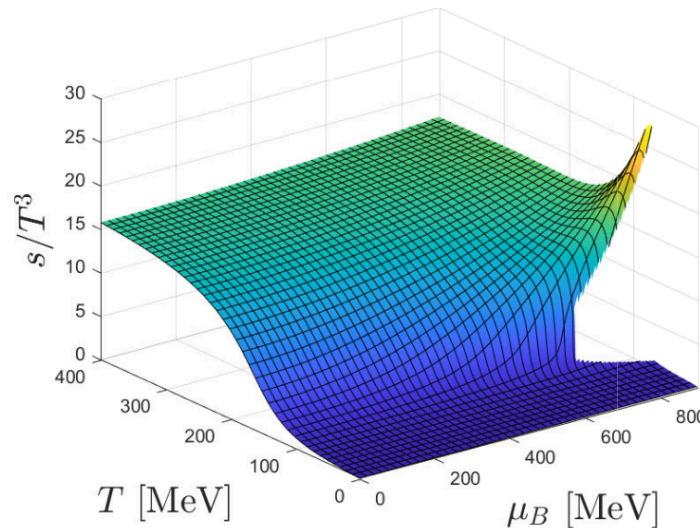
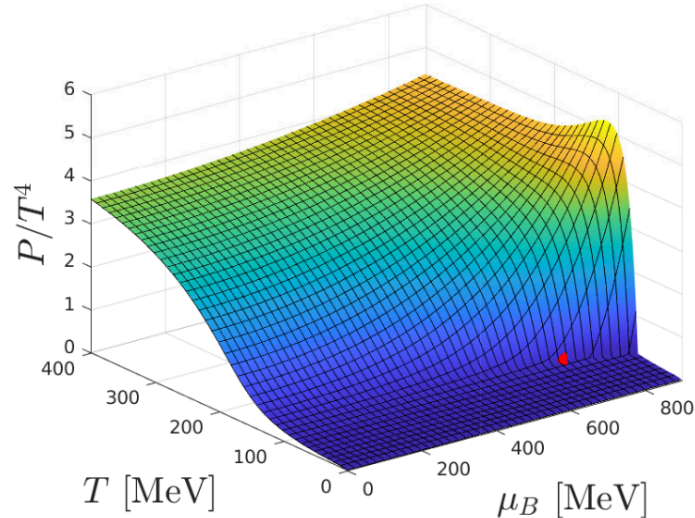
Range:  $30 \text{ MeV} < T < 400 \text{ MeV}$ ;  $\mu_B < 1100 \text{ MeV}$

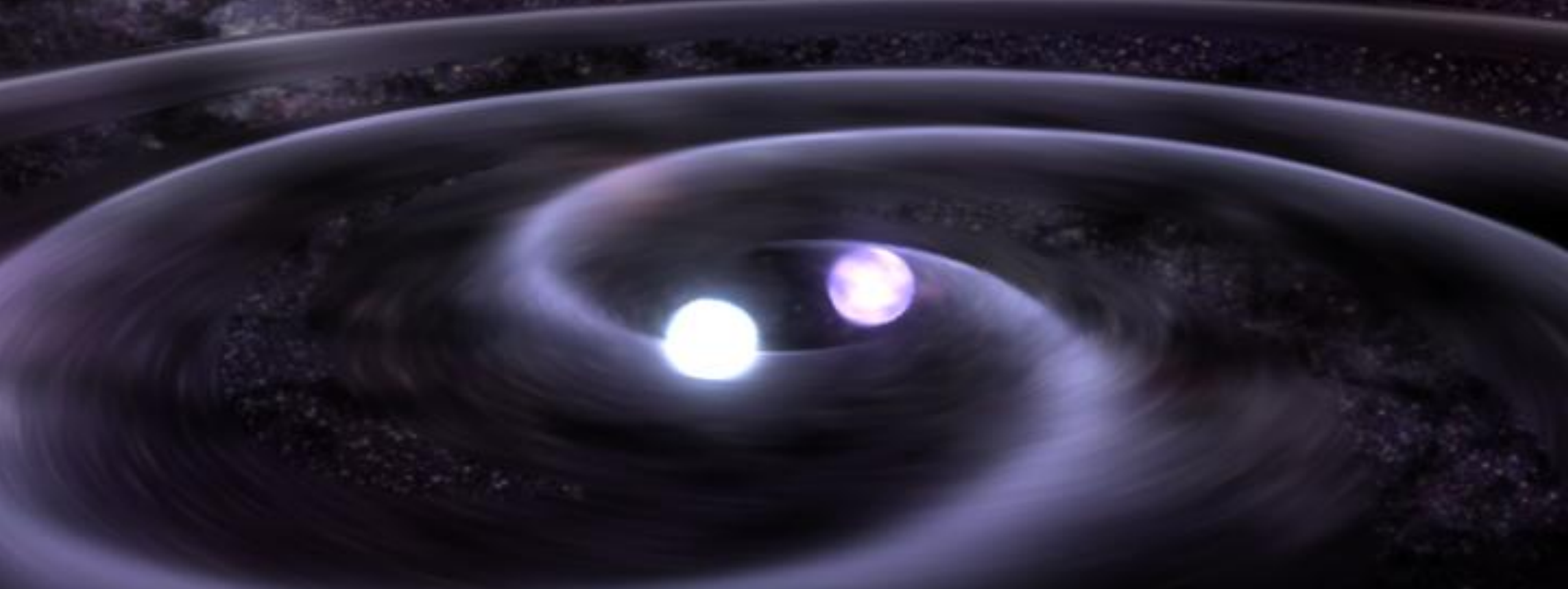
See talk by Joaquin Grefa

- Use AdS/CFT correspondence
- Fix the parameters to reproduce everything we know from the lattice
- Calculate equation of state at finite density
- Model currently has only baryon number
- Model has a critical point

### Outlooks:

- Extension to multiple conserved charges





# EOS FOR NEUTRON STARS

- Chiral Mean Field Model
- QHC19
- UTK EOS
- Chiral effective theory

# NEUTRON STARS & MERGERS: DETAILS AND NEEDS

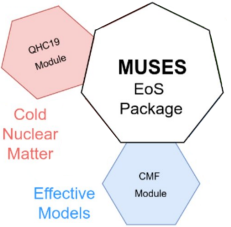
## DETAILS

- ❖ Long lifetime
- ❖ Weak decay:  $s \rightarrow u + W^-$
- ❖ Strangeness most likely \*not\* in equilibrium
- ❖ Electrically neutral for stability  
 $\langle \rho_Q \rangle = 0$

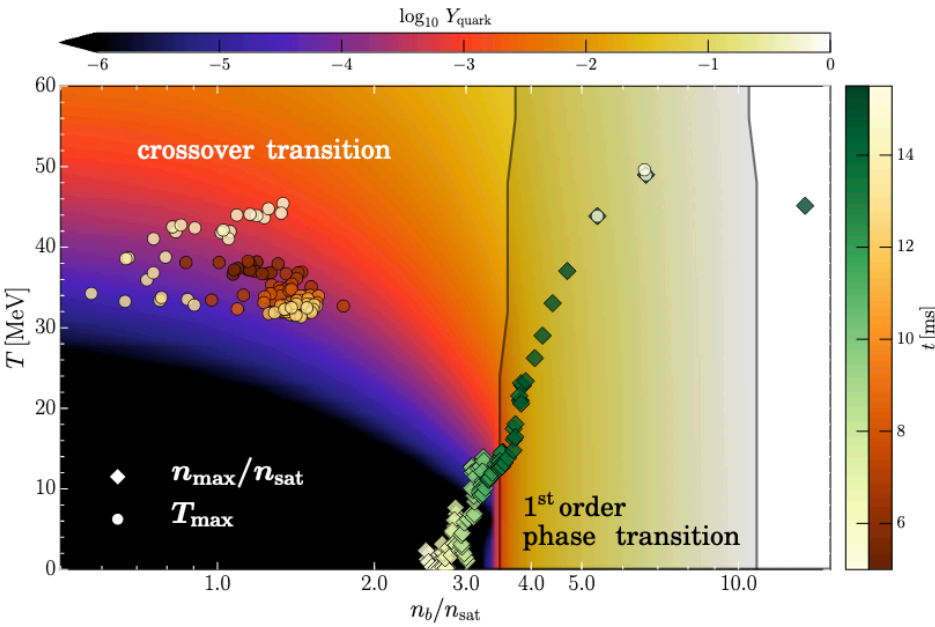
## NEEDS

- ❖ Standard EOS:  $(p, s, \varepsilon, \rho_B, c_s^2, \mu_i, Y_i)$
- ❖ Finite-T EOS for mergers
- ❖ Ranges:  $0 < \rho_B < (4-5)\rho_0, 0 < T < 100 \text{ MeV}$
- ❖ T=0 EOS for mergers and neutron stars
- ❖ Lepton EOS
- ❖ Variable proton fraction





# MULTI-PHASE EQUATIONS OF STATE FOR NEUTRON STARS



## ○ Chiral Mean Field (CMF) model

- Crossover at low density and first-order phase transition at high density
- Based on non-linear sigma model with the addition of deconfined quarks
- Reproduces nuclear & astrophysics constraints, and matches pQCD in relevant regimes

V. Dexheimer, S. Schramm, PRC (2009)  
E. Most, V. Dexheimer et al., PRL (2019)

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## ○ Quark-Hadron Crossover (QHC19)

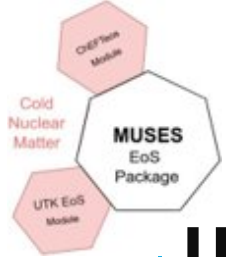
- EoS with smooth crossover between hadrons and quarks
- Hadronic EoS is based on the Togashi model, which describes non-uniform and uniform matter, and beta-equilibrium
- Quark matter is described in the NJL model with vector interaction

G. Baym et al., Astrophys. J (2019)

Goals:

- Optimization of the code
- Incorporation into MUSES (NJL part only at 1<sup>st</sup>)





# HADRONIC EQUATIONS OF STATE FOR NEUTRON STARS

## ○ Chiral effective field theory (ChiEFT)

- Interacting nucleons and pions within chiral effective field theory
- Describes matter in the range  $T < 30 \text{ MeV}$  ;  $800 \text{ MeV} < \mu_B < 1100 \text{ MeV}$
- Proton fraction:  $0 < Y_p < 0.6$

[J. Holt & N. Kaiser, PRC \(2017\)](#)



## ○ University of Tennessee in Knoxville (UTK) EoS

- Includes nucleonic degrees of freedom based on a phenomenological fit to nuclear experiments & astronomical observations
- Covers densities from  $10^{-12}$  to  $2 \text{ fm}^{-3}$ , and  $T \rightarrow 100 \text{ MeV}$

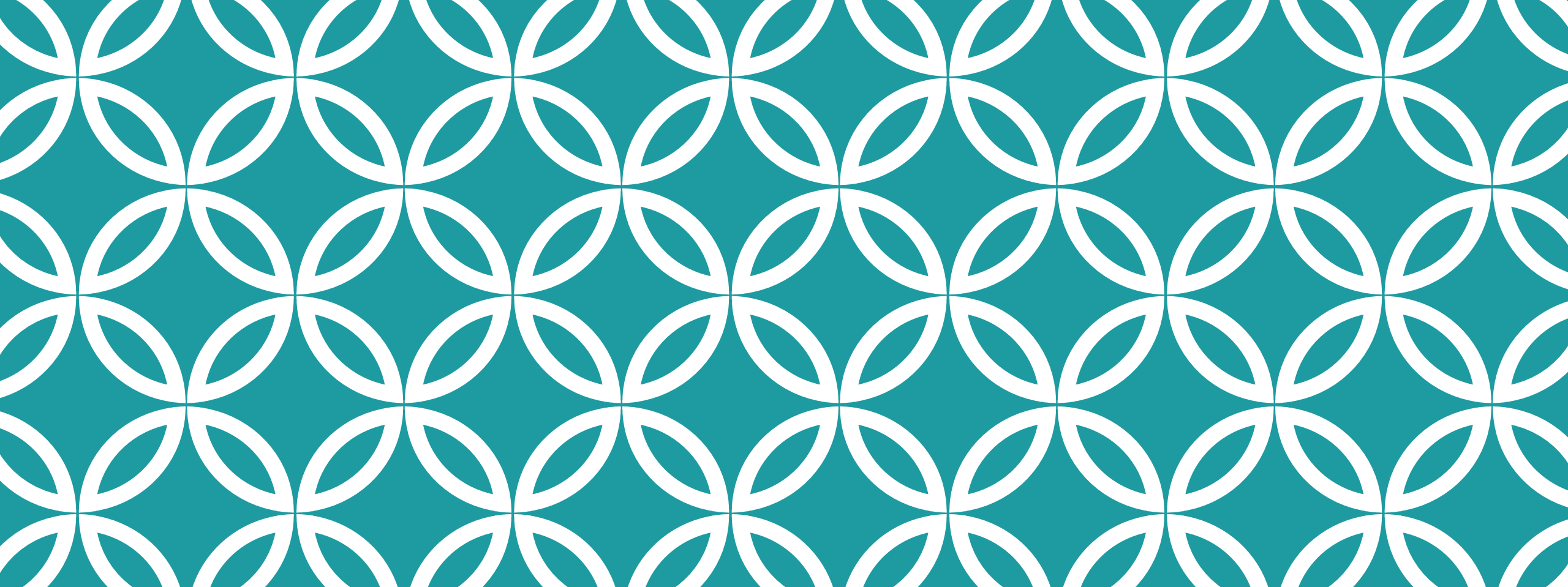
[X. Du, A. Steiner, J. Holt, PRC \(2019\)](#)



Outlooks:

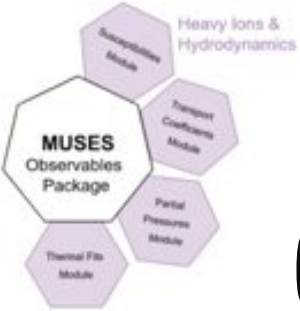
- Extension to strangeness degrees of freedom





# USERS

- Observables for heavy-ions
- Observables for neutron stars
- Flavor Equilibration
- Compatibility with existing codes/repositories



# OBSERVABLES FOR HEAVY-IONS

## ○ Susceptibilities & hadronic species contributions

- Susceptibilities from lattice QCD will be computable
- using HRG, one can study the breakdown of different hadron families:
  - we will provide combinations for hadronic contributions to total pressure
  - we will provide analogous relations for susceptibilities

## ○ Transport coefficients from Holographic module

- Thermal conductivity
- Baryon conductivity & diffusion
- Shear & bulk viscosities
- HQ drag force & Langevin diffusion coefficients
- Jet quenching parameter

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## ○ Freeze-out physics

- T and  $\mu_b$  at chemical freeze-out can be fitted from experimental data with HRG
- will be incorporated with Thermal-FIST

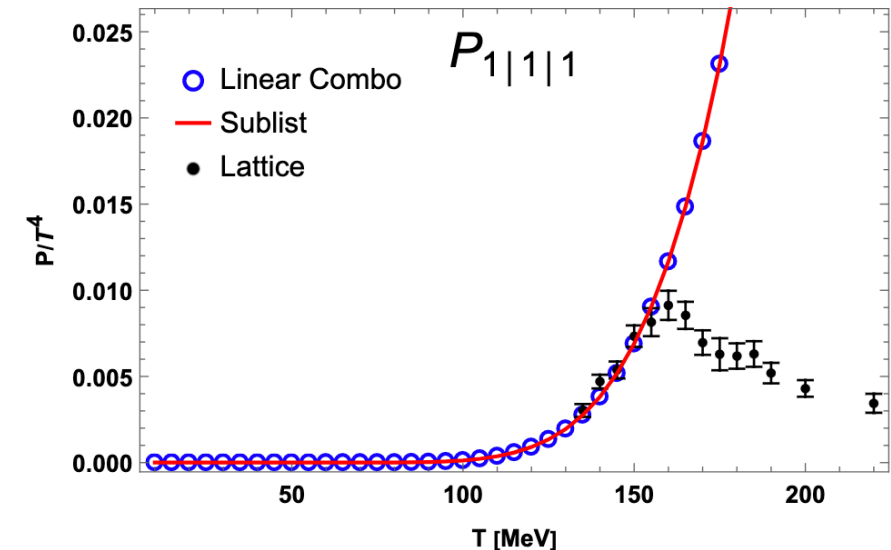


Figure 5.11:  $P_{1|1|1} = -\frac{1}{4}\chi_{13}^{SQ} + \frac{1}{4}\chi_{22}^{SQ} - \frac{1}{4}\chi_{112}^{BSQ} + \frac{1}{4}\chi_{121}^{BSQ}$



# OBSERVABLES FOR NEUTRONS STARS & MERGERS

## ○ QLIMR module

- Given an EoS, solves the Tolmann-Oppenheimer-Volkoff (TOV) equations and computes:
  - Q: quadrupole moment Q of NS
  - L: tidal Love number (tidal force deformability)
  - I: moment of inertia
  - M: mass of NS
  - R: radius of NS

α-RELEASE

## ○ Flavor equilibration

- $\beta$ -equilibrium:  $\mu_n - \mu_p - \mu_e = 0$
- Given an EoS, computes:
  - Urca rates  
( $n \rightarrow p + e + \bar{\nu}_e$  /  $p + e \rightarrow n + \nu_e$ )
  - Equilibrium charge fractions
  - Relaxation rates
  - Damping time
  - Susceptibilities
  - Bulk viscosity

α-RELEASE

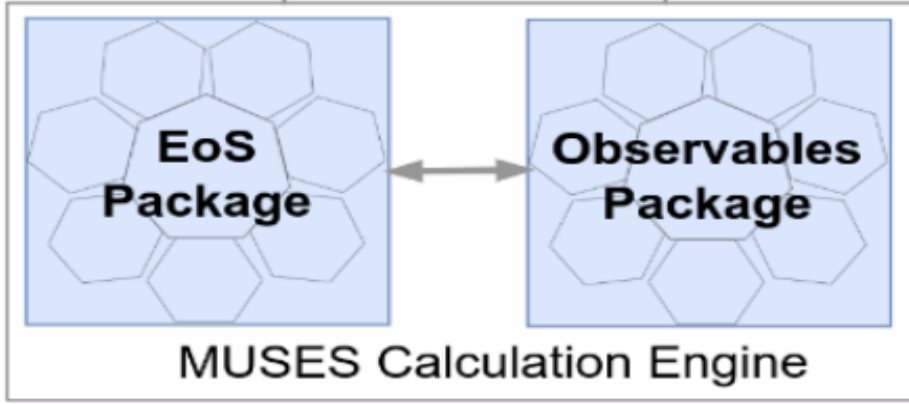
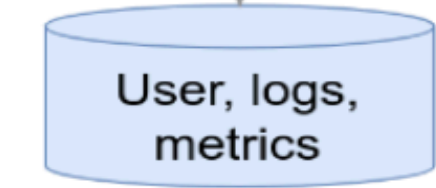
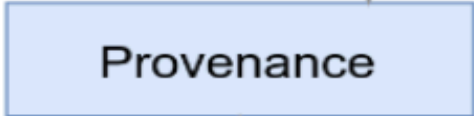
## ○ Adapter modules for NS & mergers simulation tools

- Ensuring compatibility with CompStar Online Supernovae Equations of State ([CompOSE](#)), a standard format, with the aim to provide thousands of 1D/2D/3D EoS tables for NS
- Ensuring compatibility with merger simulations

**Top Level**  
Containerized  
Web-based  
Tools & Services



**Low Level**  
Containerized  
Web-based  
Tools & Services



Computationally Intensive Tasks

Batch Processing  
*Campus Clusters, Delta, XSEDE*



**I ILLINOIS** NCSA

Storage

# CYBERINFRASTRUCTURE



# CYBERINFRASTRUCTURE BINDS US ALL

- Connect computer scientists and physicists to provide solutions to numerical method challenges
- We need multidimensional EoS interpolators, root-finders, etc.
- Make sure code is compatible with heavy-ion and neutron-star simulations
- We need to learn how to merge different equations of state
  
- Another important part of the work is to ensure user-friendly interface and usability

We expect soon the first few modules to be deployed!

# FIRST MUSES-WIDE PUBLICATION!

## Theoretical and Experimental Constraints for the Equation of State of Dense and Hot Matter

Rajesh Kumar,<sup>1,\*</sup> Veronica Dexheimer,<sup>1,†</sup> Johannes Jahan,<sup>2</sup> Jorge Noronha,<sup>3</sup> Jacquelyn Noronha-Hostler,<sup>3</sup> Claudia Ratti,<sup>2</sup> Nico Yunes,<sup>3</sup> Angel Rodrigo Nava Acuna,<sup>2</sup> Mark Alford,<sup>4</sup> Mahmudul Hasan Anik,<sup>5</sup> Katerina Chatziioannou,<sup>6,7</sup> Hsin-Yu Chen,<sup>8,9</sup> Alexander Clevinger,<sup>1</sup> Carlos Conde,<sup>3</sup> Nikolas Cruz Camacho,<sup>3</sup> Travis Dore,<sup>10</sup> Christian Drischler,<sup>11</sup> Hannah Elfner,<sup>12</sup> Reed Essick,<sup>13</sup> David Friedenber, <sup>14</sup> Suprovo Ghosh,<sup>15</sup> Joaquin Grefa,<sup>2</sup> Roland Haas,<sup>3</sup> Jan Hammelmann,<sup>16</sup> Steven Harris,<sup>17</sup> Carl-Johan Haster,<sup>18,19</sup> Tetsuo Hatsuda,<sup>20</sup> Mauricio Hippert,<sup>3</sup> Renan Hirayama,<sup>16</sup> Jeremy W. Holt,<sup>14</sup> Micheal Kahangirwe,<sup>2</sup> Jamie Karthein,<sup>21</sup> Toru Kojo,<sup>22</sup> Philippe Landry,<sup>23</sup> Zidu Lin,<sup>5</sup> Matthew Luzum,<sup>24</sup> T. Andrew Manning,<sup>3</sup> Jordi Salinas San Martin,<sup>3</sup> Cole Miller,<sup>25</sup> Elias Roland Most,<sup>26,27,28</sup> Debora Mroczek,<sup>3</sup> Azwinndini Muronga,<sup>29</sup> Nicolas Patino,<sup>3</sup> Jeffrey Peterson,<sup>1</sup> Christopher Plumberg,<sup>30</sup> Damien Price,<sup>2</sup> Constanca Providencia,<sup>31</sup> Romulo Rougemont,<sup>32</sup> Satyajit Roy,<sup>5</sup> Hitansh Shah,<sup>2</sup> Stuart Shapiro,<sup>3</sup> Andrew W. Steiner,<sup>5,33</sup> Michael Strickland,<sup>1</sup> Hung Tan,<sup>3</sup> Hajime Togashi,<sup>22</sup> Israel Portillo Vazquez,<sup>2</sup> Pengsheng Wen,<sup>14</sup> and Ziyuan Zhang<sup>4</sup>





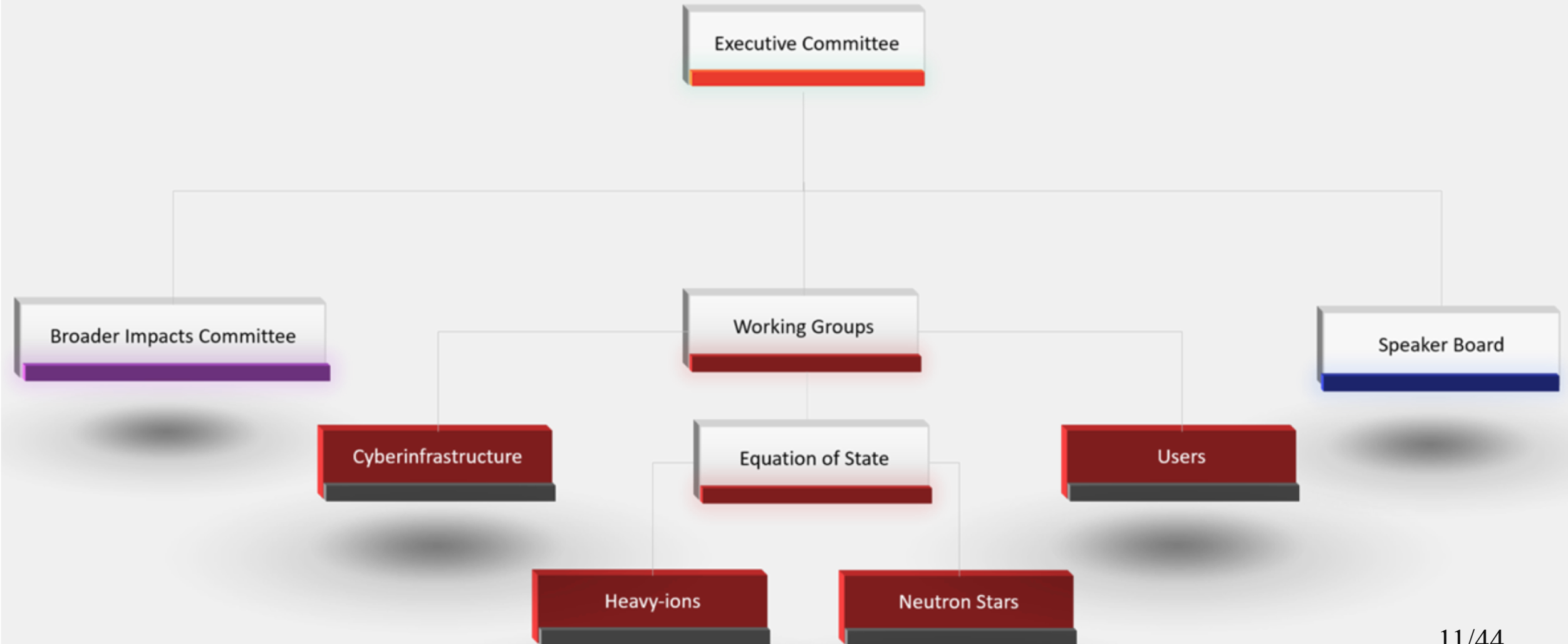
# CONCLUSIONS

- MUSES will provide a modular unified solver for the equation of state and calculate observables of relevance for the heavy-ion and astrophysics communities
- We are currently in our third year
- Watch out for the alpha release
- Check out our webpage at <https://muses.physics.illinois.edu/>
- We welcome new users any time



**Backup slides**

# MUSES ORGANIZATION



# NSF CSSI

- Cyberinfrastructure for Sustained Scientific Innovation

*“The Cyberinfrastructure for Sustained Scientific Innovation (CSSI) umbrella program seeks to enable funding opportunities that are flexible and responsive to the evolving and emerging needs in cyberinfrastructure.”*

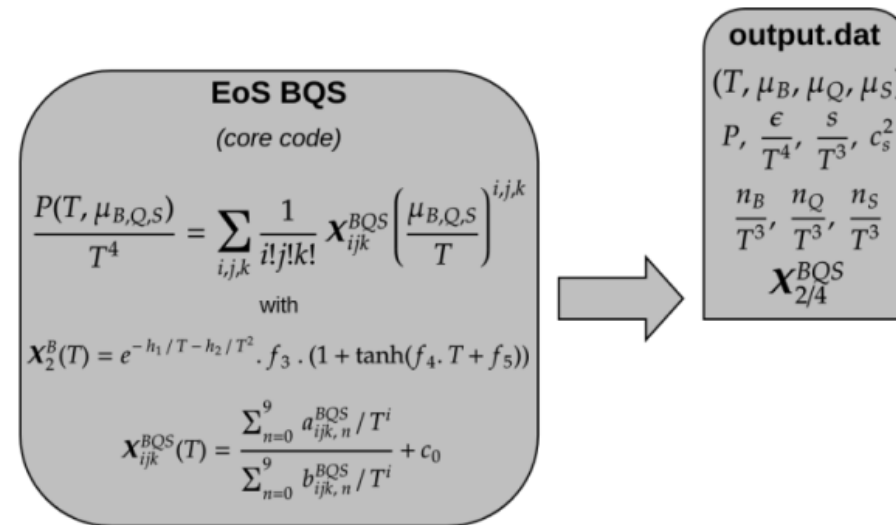
*“**Framework Implementations:** These awards target larger, interdisciplinary teams organized around the development and application of services aimed at solving **common research problems** faced by NSF researchers in one or more areas of science and engineering, and resulting in a sustainable community framework providing CI services to a diverse community or communities.”*

# MODULE - BQS EOS

**Developers:** Hitansh S. + Johannes J. + Claudia R. (UH)

**Purpose :** provide calculation of a Taylor expanded EoS in 4D ( $T, \mu_B, \mu_S, \mu_Q$ ) in the ranges  $T \in [30,800]$  MeV and  $\mu_i \in [0,450]$  MeV

Ratti group:  
 See talk by Johannes Jahan



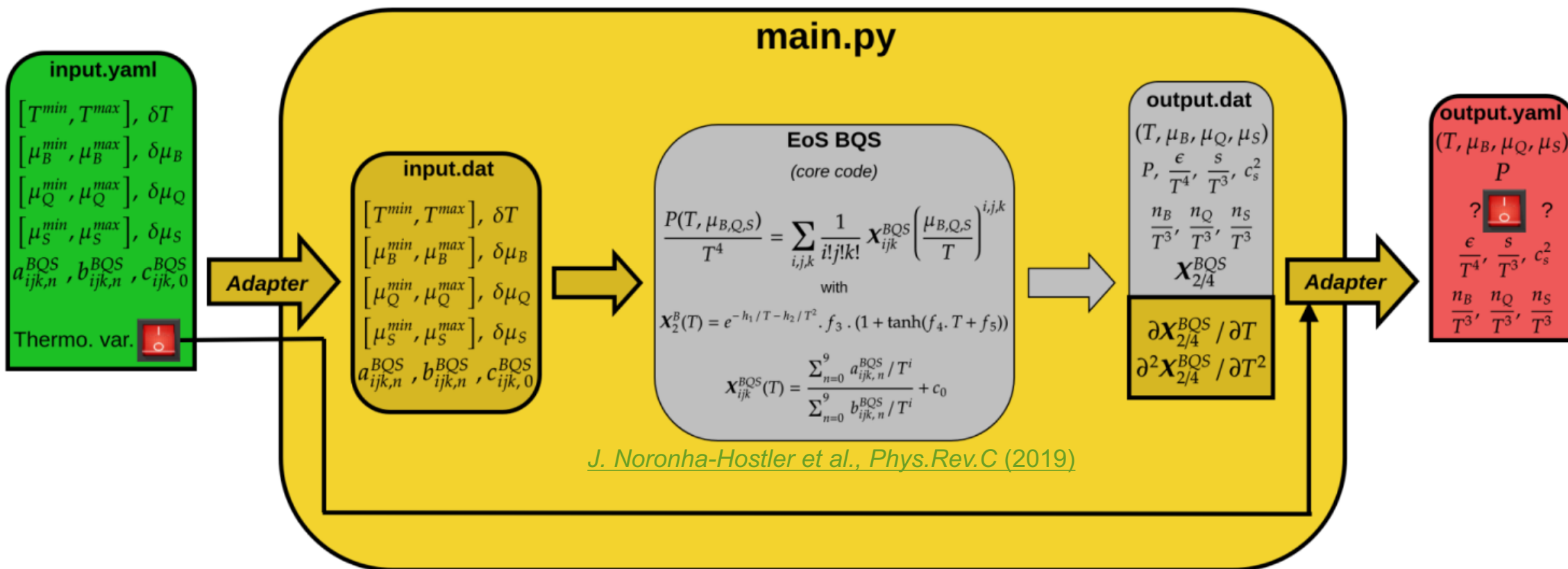
*J. Noronha-Hostler et al., Phys.Rev.C (2019)*

# MODULE - BQS EOS

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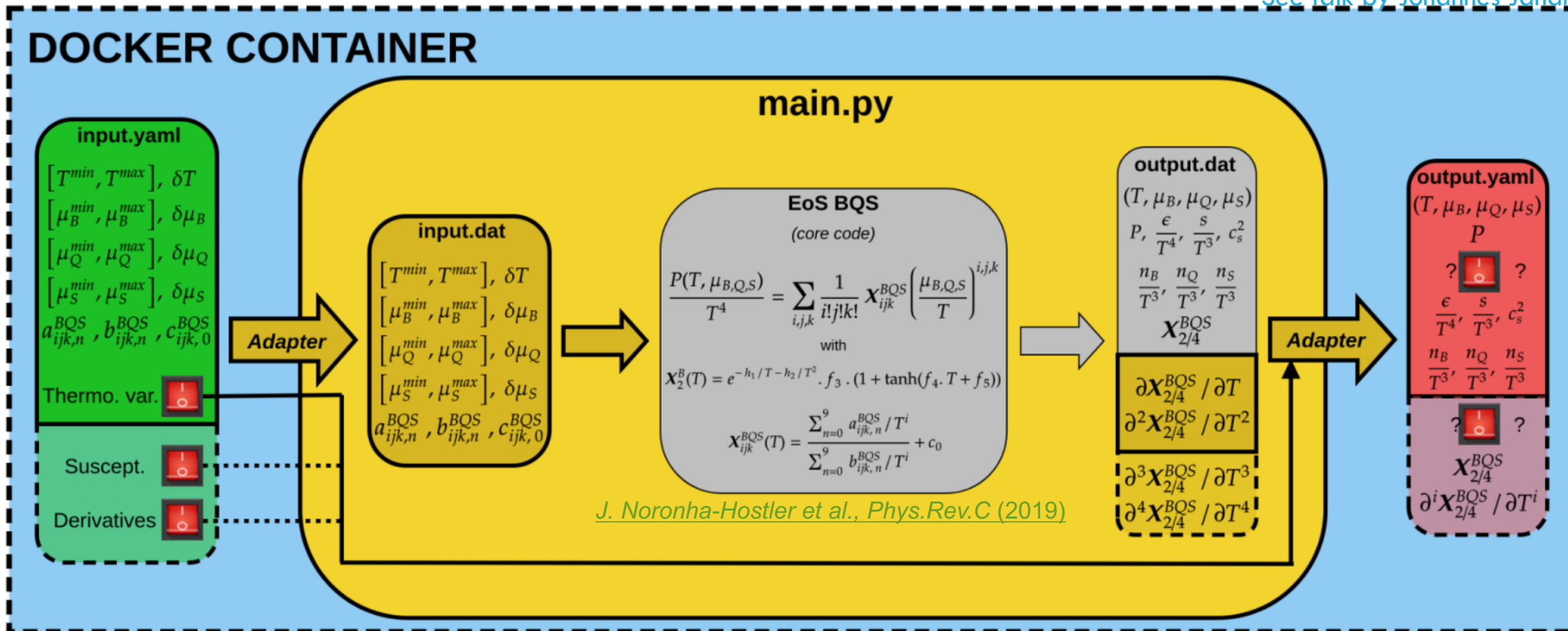
Ratti group:  
 See talk by Johannes Jahan



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Ratti group:

See talk by Johannes Jahan



# EQUATION OF STATE WITH 3D-ISING CRITICAL POINT (BESEOS)

Range:  $0 < T < 800 \text{ MeV}$ ;  $\mu_B < 450 \text{ MeV}$

Ratti group:

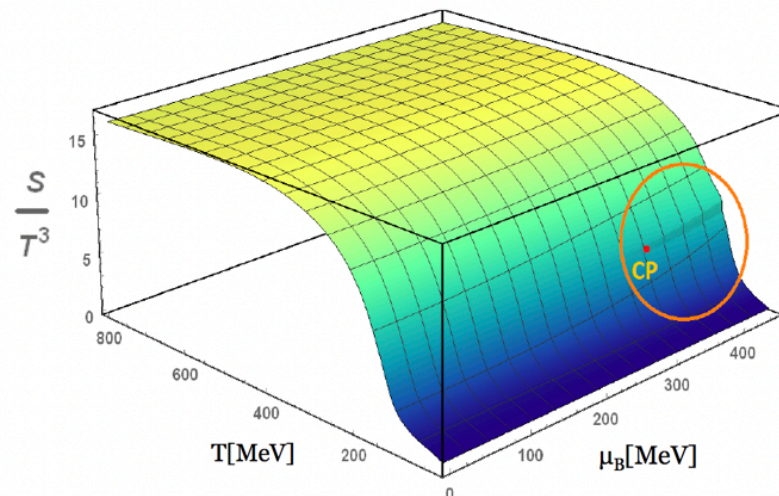
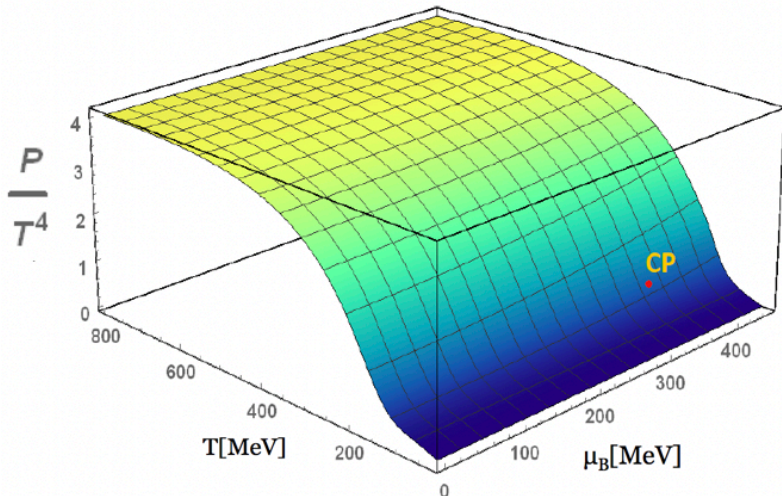
See talk by Micheal Kahangirwe  
 P. Parotto, C. R. et al., PRC (2020)

J. Karthein, C. R. et al., EPJ Plus (2021)

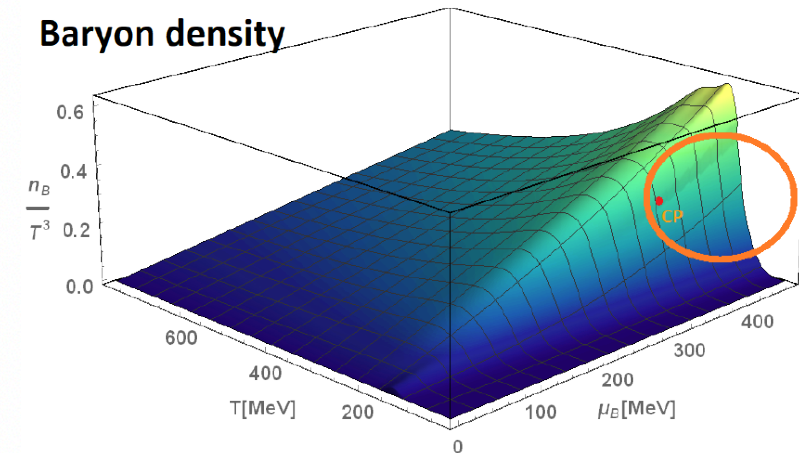
- Implement scaling behavior of 3D-Ising model EoS
- Define map from 3D-Ising model to QCD
- Estimate contribution to Taylor coefficients from 3D-Ising model critical point
- Reconstruct full pressure
- Currently available at  $\mu_S = \mu_Q = 0$  and for  $\langle n_S \rangle = 0$ ,  $\langle n_Q \rangle = 0.4 \langle n_B \rangle$

**Goals:**

- Extension of range in  $\mu_B$
- Extension to three conserved charges
- Incorporation into MUSES



**Baryon density**





# EQUATION OF STATE FROM HOLOGRAPHY (NUMRELHOLO)

J. Grefa, C. R. et al., PRD (2021)

Range:  $30 \text{ MeV} < T < 400 \text{ MeV}$ ;  $\mu_b < 1100 \text{ MeV}$

Noronha-Ratti groups:

See talk by Mauricio Hippert

## Before MUSES

- Slow Matlab code
- Noisy results
- Filters needed
- No documentation
- Artisanal fit

## Current status

- Fast, stable C++ EoS
- Bayesian analysis almost done
- Partial documentation
- Transport coefs. (Matlab)

## Purpose

- Optimized C++ code for Holographic EoS
- Transport coefs.
- Inclusion of strangeness and electric charge

## To do

- Standardized tests
- Final version of EoS
- CE integration
- C++ transport coefs.
- Strangeness and electric charge

# CHIRAL MEAN FIELD MODEL (CMF)

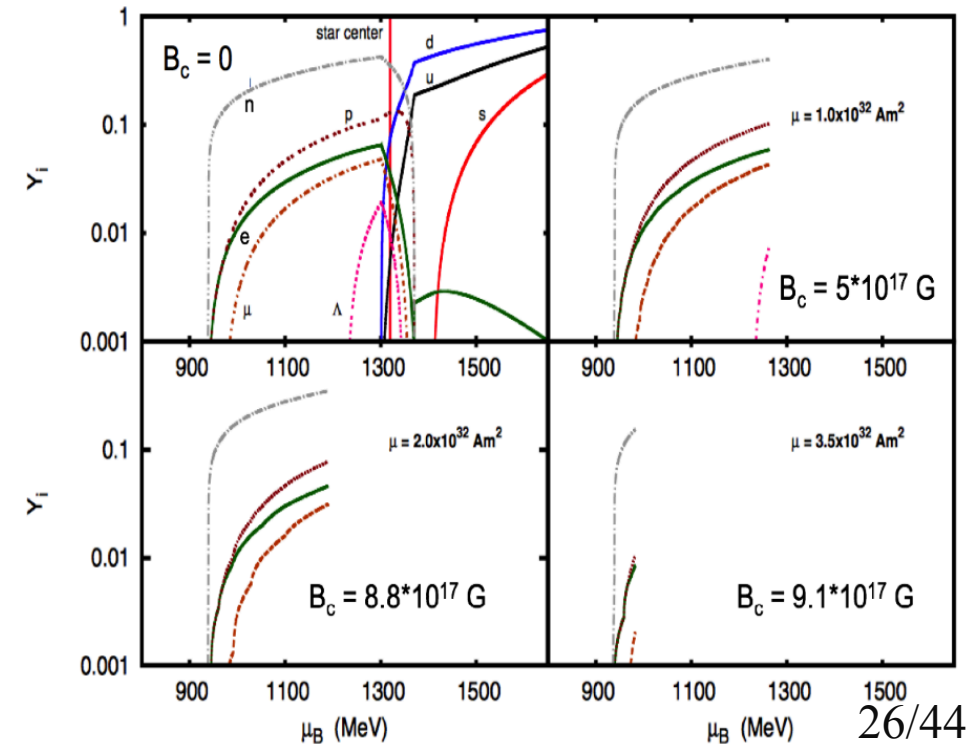
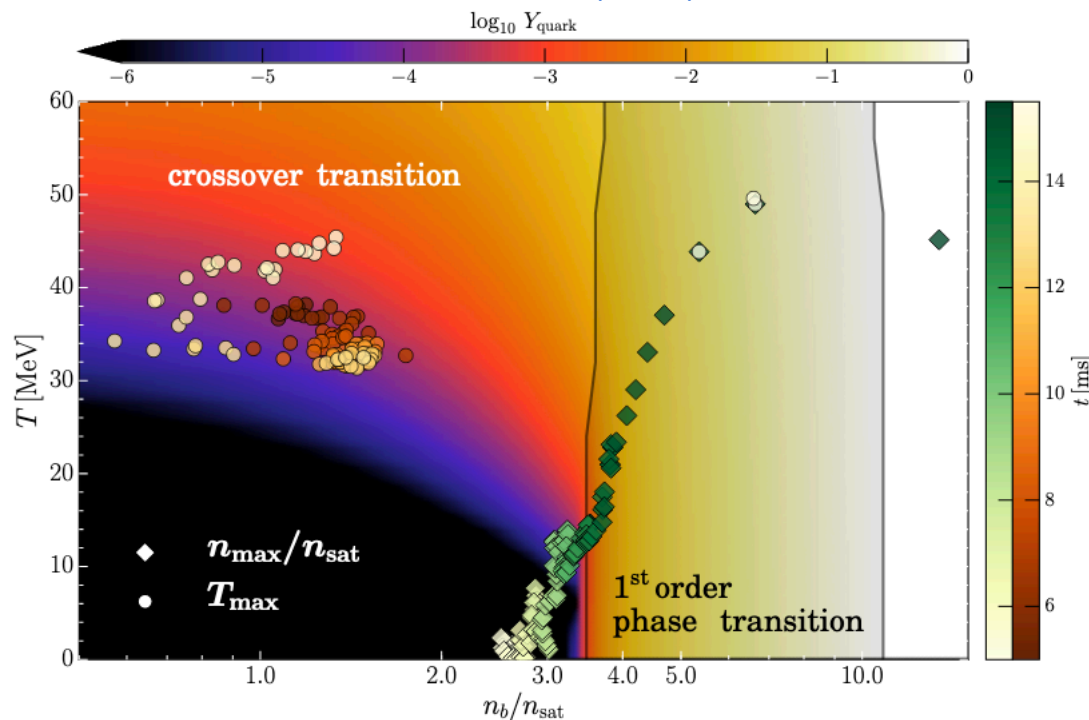
V. Dexheimer, S. Schramm PRC (2009)

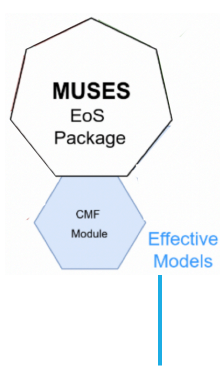
- Crossover at low density and first-order phase transition at high density
- Based on non-linear sigma model with the addition of deconfined quarks
- Reproduces nuclear and astrophysical constraints
- Matches perturbative QCD in the relevant regime

### Goals:

- Optimization of the code
- Parameter fit to new lattice data
- Incorporate into MUSES

E. Most, V. Dexheimer et al., PRL (2019)





Dexheimer/Noronha-Hostler groups:  
See talk by Nicholas Cruz Camacho

## Purpose

- Create an open-source optimized modular modern C++ code within the MUSES calculation engine to compute multidimensional EoS tables using the CMF model.

## Status before MUSES

- Fortran 77 proprietary code
- Spaghetti code between non- and magnetic cases, not properly documented
- Antique root solving and integration routines

## Current status

- High resolution zero temperature nonmagnetic case that agrees with the previous code for all particles ✓
- Dockerfile available and registered into the calculation engine 0.10.0 ✓
- Offline coupled to QLIMR ✓

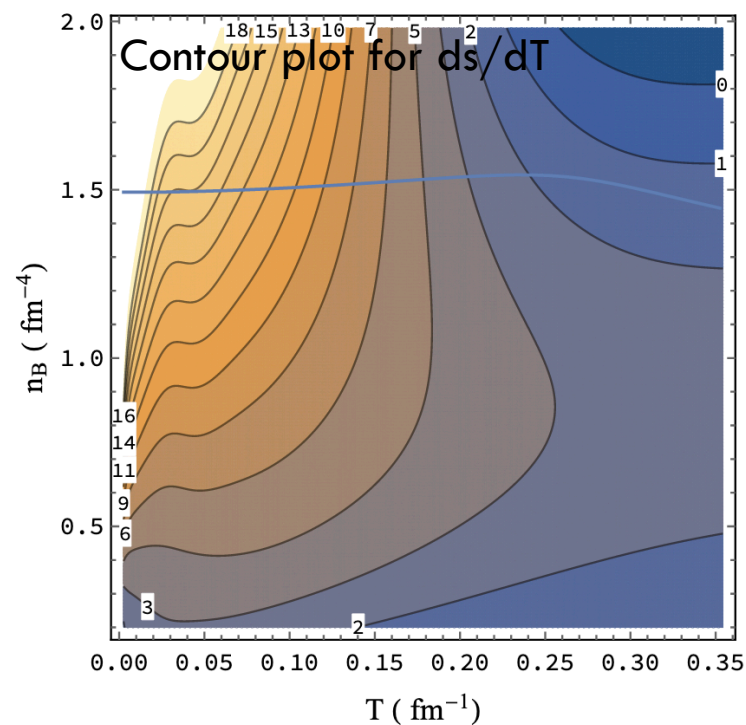
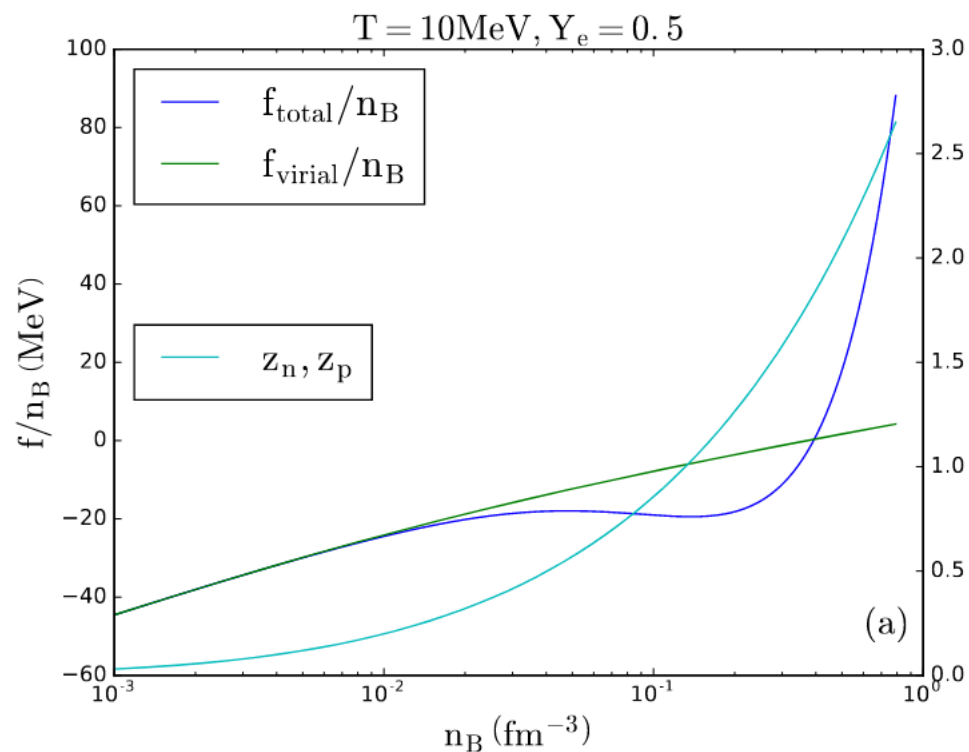
## Outlook

- Couple to flavor equilibration module [Ziyuan Zhang](#)
- Zero temperature magnetic case
- Finite temperature non- and magnetic case
- Add thermal meson interactions
- Introduce normalization that breaks the mass degeneracy between vector mesons [Rajesh Kumar](#)

# UNIVERSITY OF TENNESSEE KNOXVILLE EOS(UTK EOS)

- Includes nucleonic degrees of freedom based on a phenomenological fit to nuclear experiment and astronomical observations
- Covers densities from  $10^{-12}$  to  $2 \text{ fm}^{-3}$  and temperatures up to 100 MeV

X. Du, A. Steiner, J. Holt, PRC (2019)



## Goals:

- Optimization of the code
- Extension to strangeness degrees of freedom
- Incorporate into MUSES



A. Steiner group: See talk by Satyajit Roy

# UNIVERSITY OF TENNESSEE KNOXVILLE EOS(UTK EOS)

X. Du, A. Steiner, J. Holt, PRC (2019)

## Purpose:

- ❖ Include strangeness
- ❖ Use machine learning to improve the EOS calculation

## Status:

- ❖ Built code infrastructure
- ❖ Three density regimes: non-degenerate, near saturation (with nuclei), high-density matter
- ❖ Non-degenerate strangeness being implemented with hadronic resonances
- ❖ Strangeness with nuclei? Some ideas

## Outlook:

- ❖ Finalize testing of non-degenerate strangeness
- ❖ Include pion-nucleon interactions
- ❖ Improve EOS for crust
- ❖ Implement CMF or NJL for high density
- ❖ Slow code: plan to also create tables
- ❖ Neutrino opacities

## MACHINE LEARNING

- ❖ Working on neural network and Gaussian process interpolators

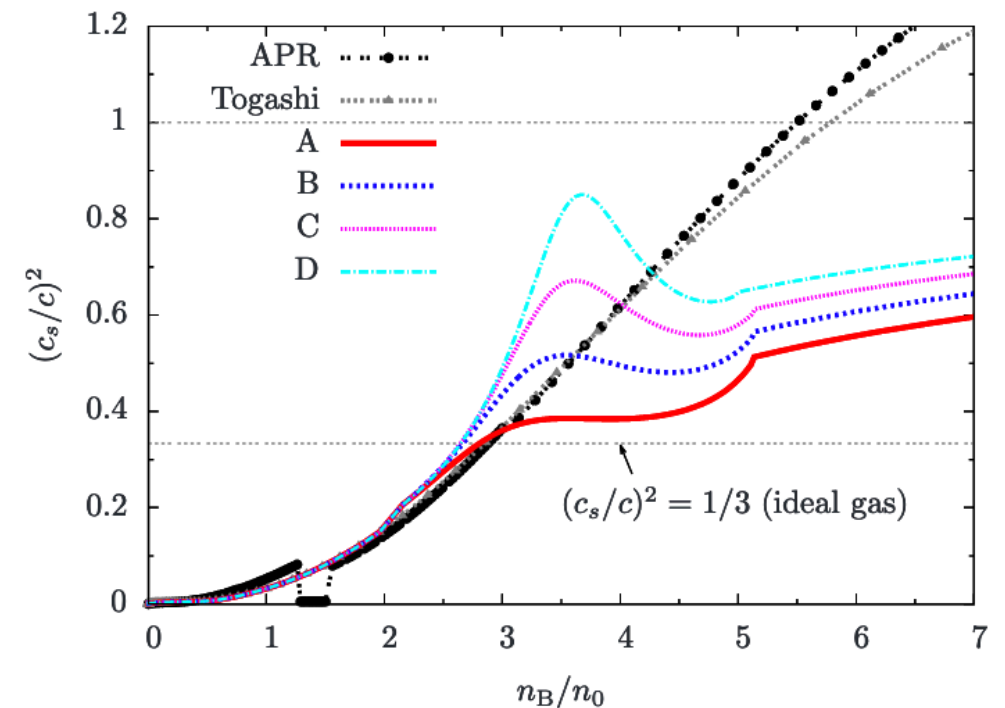
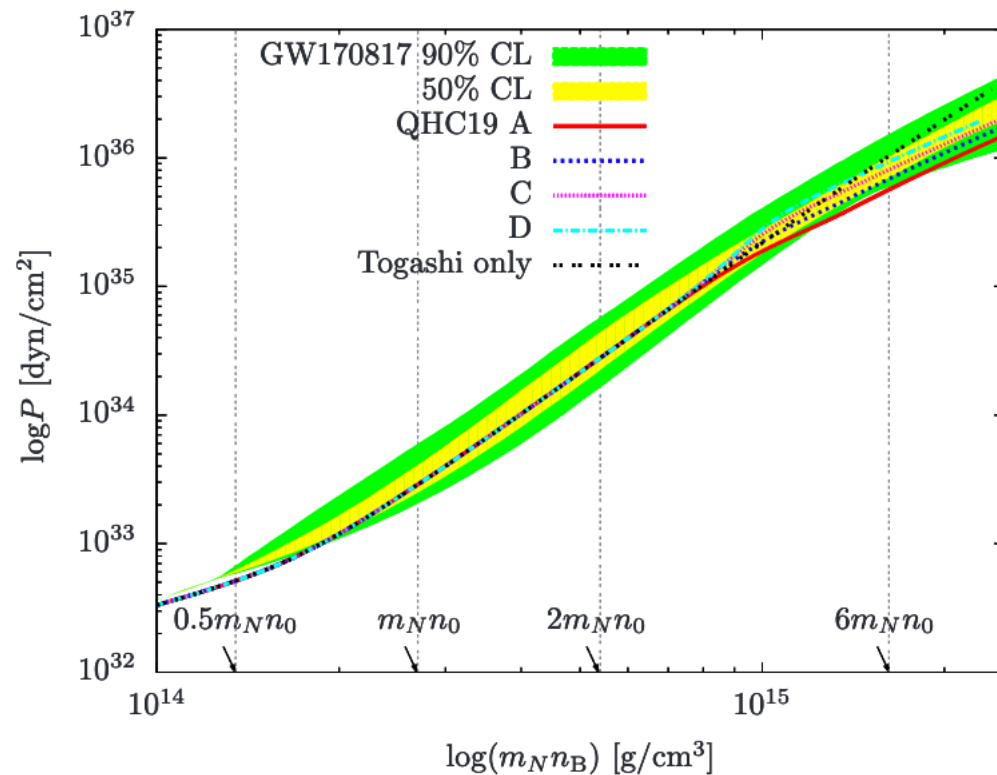
# QUARK-HADRON CROSSOVER (QHC19)

G. Baym et al., *Astrophys. J* (2019)

- Equation of state with smooth crossover between hadrons and quarks
- Hadronic EoS is based on the Togashi model, which describes non-uniform and uniform matter, and beta-equilibrium
- Quark matter is described in the NJL model with vector interaction

## Goals:

- Optimization of the code
- Incorporation into MUSES
- Current goal: NJL only



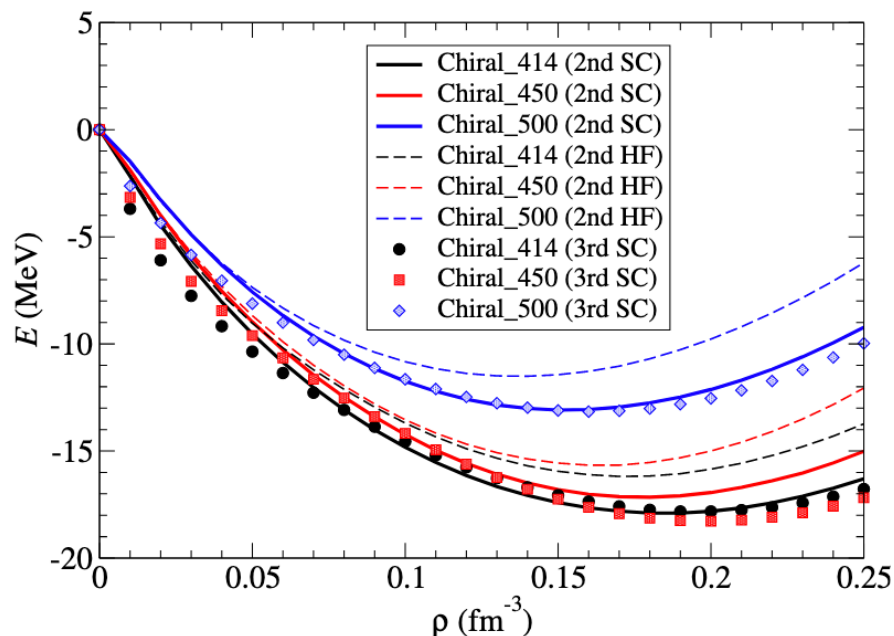
# CHIRAL EFFECTIVE FIELD THEORY (CHEFTEOS)

J. Holt & N. Kaiser, PRD (2017)

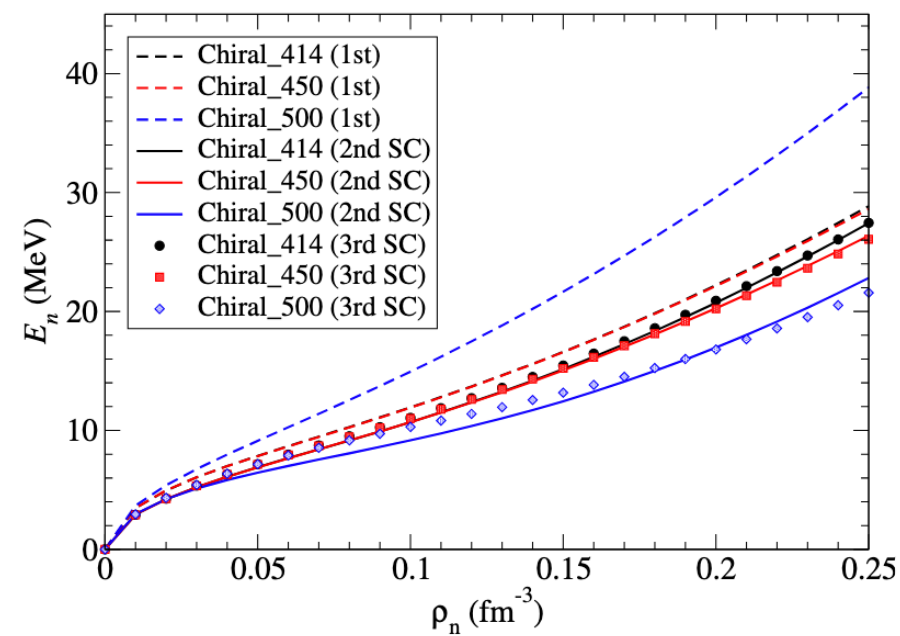
- Describes matter in the range  $T < 30$  MeV,  $800 \text{ MeV} < \mu_B < 1100$  MeV
- Proton fraction:  $0 < Y_p < 0.6$
- Interacting nucleons and pions within chiral effective field theory
- Constrains do not exist for asymmetric matter

## Goals:

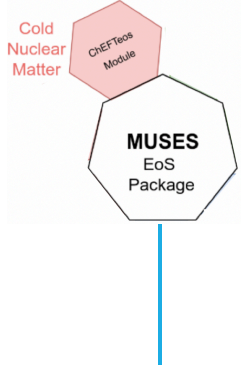
- Optimization of the code
- Optimization of root-finding techniques
- Incorporate into MUSES



EoS for symmetric nuclear matter



EoS for neutron matter



J. Holt group: See talk by David Friedenber

# CHIRAL EFFECTIVE FIELD THEORY (CHEFTEOS)

J. Holt & N. Kaiser, PRD (2017)

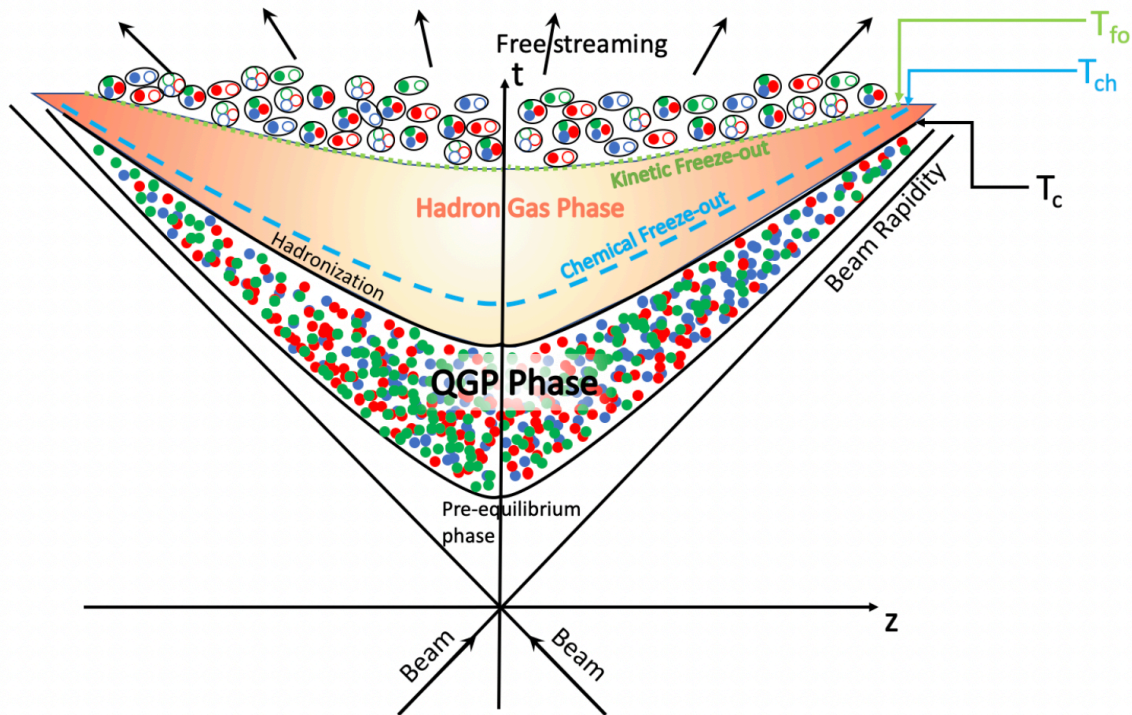
**Purpose:** ❖ Calculate first and second order contributions to the free energy at arbitrary density and temperature

**Status:** ❖ First order and second order codes  
❖ Calculate free energy and Grand Canonical potential

**Outlook:** ❖ Interface with MUSES cyberinfrastructure  
❖ Docker container  
❖ Extend phase space into third dimension  
❖ Self-energy corrections to second order



# FREEZE-OUT PHYSICS: FLUCTUATIONS & THERMAL FITS



- **Chemical freeze-out:** inelastic reactions cease: the chemical composition of the system is fixed (particle yields and fluctuations)
- Experimental results are available for these observables
- By fitting them with the HRG model, we can obtain the temperature and chemical potential of the chemical freeze-out
- Thermal FIST already does this
- Goal: incorporate it into MUSES engine

# PARTIAL PRESSURES

- Lattice QCD calculates full pressure
- There is no way of identifying the degrees of freedom that produced it
- We want to find a way of isolating the contribution of family of hadrons, grouped according to their quantum numbers
- Exploit the functional form of the HRG model EOS
- Build the partial pressures as linear combinations of susceptibilities
- There are 13 such partial pressures
- Goal: needs to be discussed

C. Ratti group: See talk by Angel Nava

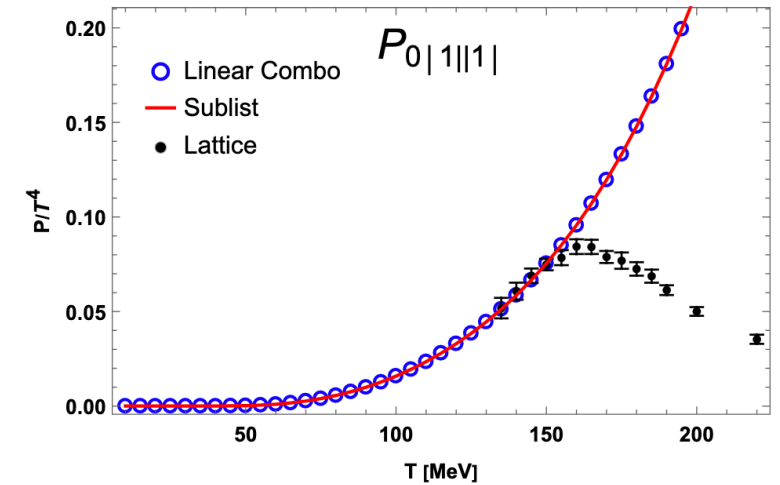


Figure 5.6:  $P_{0|1||1|} = \frac{1}{8}\chi_2^Q - \frac{1}{8}\chi_4^Q + \frac{1}{3}\chi_{13}^{SQ} - \frac{1}{12}\chi_2^S + \chi_{22}^{SQ} - \frac{1}{3}\chi_{31}^{SQ} + \frac{1}{12}\chi_4^S + \frac{1}{4}\chi_{13}^{BQ} + \chi_{112}^{BSQ} + \frac{1}{6}\chi_{13}^{BS} - \frac{1}{4}\chi_{31}^{BQ} - \frac{1}{6}\chi_{31}^{BS}$

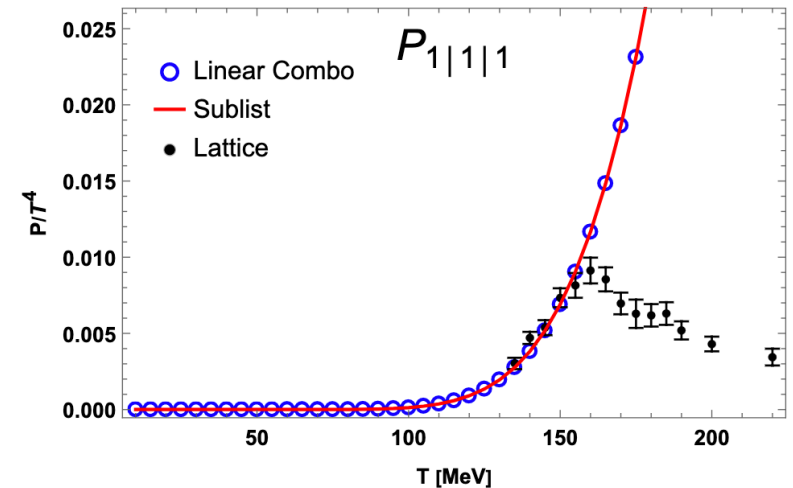
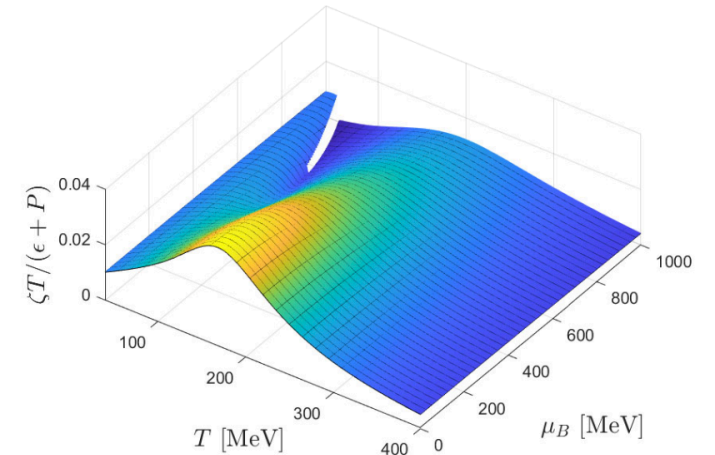
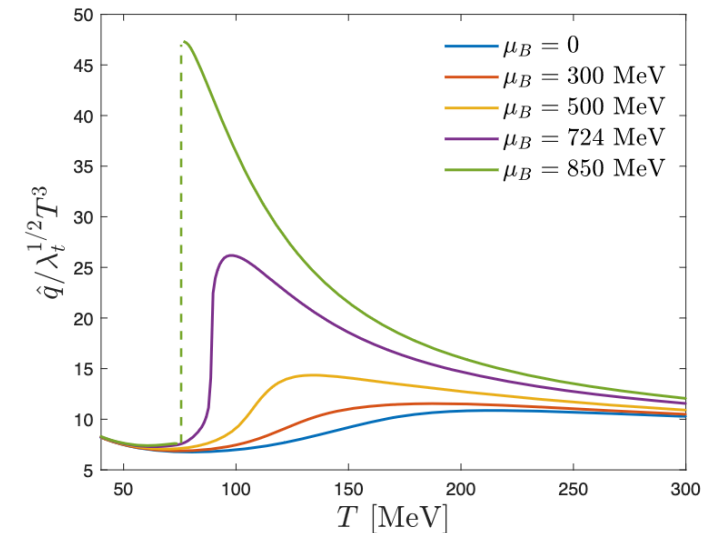


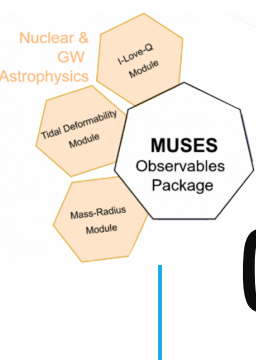
Figure 5.11:  $P_{1|1||1|} = -\frac{1}{4}\chi_{13}^{SQ} + \frac{1}{4}\chi_{22}^{SQ} - \frac{1}{4}\chi_{112}^{BSQ} + \frac{1}{4}\chi_{121}^{BSQ}$

# TRANSPORT COEFFICIENTS

- Calculated in the holographic model
- Provide the following:
  - Baryon conductivity & diffusion
  - Thermal conductivity
  - Heavy quark drag force & Langevin diffusion coefficients
  - Jet quenching parameter
  - Shear viscosity
  - Bulk viscosity
- Status: we published the coefficients
- Need to start working on the code

Ratti/Noronha groups: J. Grefa et al., PRD (2022)





# QLIMR MODULE

## Purpose

Given a barotropic EoS table, the main purpose of this module is to compute the radius  $R_*$ , the mass  $M_*$ , the moment of inertia  $I$ , the tidal Love number  $\lambda$  and the quadrupole moment  $Q$  of a NS for a given set of central energy densities  $\varepsilon_c$ .

## Status before MUSES

A Mathematica code was developed by Hung Tan which achieves the main purpose of this module. It also contains additional functions to compute binary love relations.

## Current status

- Computes  $R_*$ ,  $M_*$ ,  $I$  and  $\lambda$  using `.yaml` files and python adaptors for I/O data.
- Works effectively in docker.
- Locally running using CMF module EoSs.

## What remains to be done

- Finish code parallelization.
- Solve  $l = 0$  equations at  $\mathcal{O}(\Omega^2)$ .
- Output all local functions as `.CSV` files.
- Integrate into calculation engine.
- Compute  $Q$  and binary Love relations.

# FLAVOR EQUILIBRATION

**Purpose:** ❖ Provide code to calculate Urca rates and related dense matter properties

**Status:**

- ❖ Completed Python code that can calculate Urca rates, equilibrium charge fraction, relaxation rates, susceptibilities, bulk viscosity, damping time.
- ❖ Containerized the module using Docker. Working on integration to the calculation engine.
- ❖ Writing a paper on flavor equilibration using the module code.
- ❖ Investigated Gaussian process regression as a better interpolator.

**Outlook:**

- ❖ Possible expansions of the functionality. ( $n_{pe\mu}$  matter, neutrino-trapped regime, Urca rates with arbitrary neutrino distribution function, etc.)
- ❖ Possible usage of Gaussian process interpolation for MUSES

# COMPATIBILITY WITH COMPOSE

- ❖ CompStar Online Supernovae Equations of State  
<https://compose.obspm.fr>
- ❖ Provides hundreds of 1D, 2D and 3D EoS tables in a common format for astrophysical applications
- ❖ The goal is to make MUSES compatible with CompOSE standard files
- ❖ Work on this will begin summer 2023, starting with the CMF and lepton modules.

# COUPLING TO NUMERICAL RELATIVITY

❖ Start date: Late 2023 – 2024

❖ Goals:

- Ensure MUSES can be used in neutron star merger simulations
- Various formats and table sampling
- Ensure sufficient performance (interpolation!)
- Initial exploration of impact of nuclear parameters

❖ Related work:

- First simulation of effective bulk viscosity in mergers  
(with Alford, Haber, Harris, Noronha, Zhang)
- Exploration of nuclear symmetry energy  
(with Raithel / not MUSES)

# COMMUNITY-DRIVEN

- We held a workshop “From heavy-ion collisions to neutron stars” in August 2020

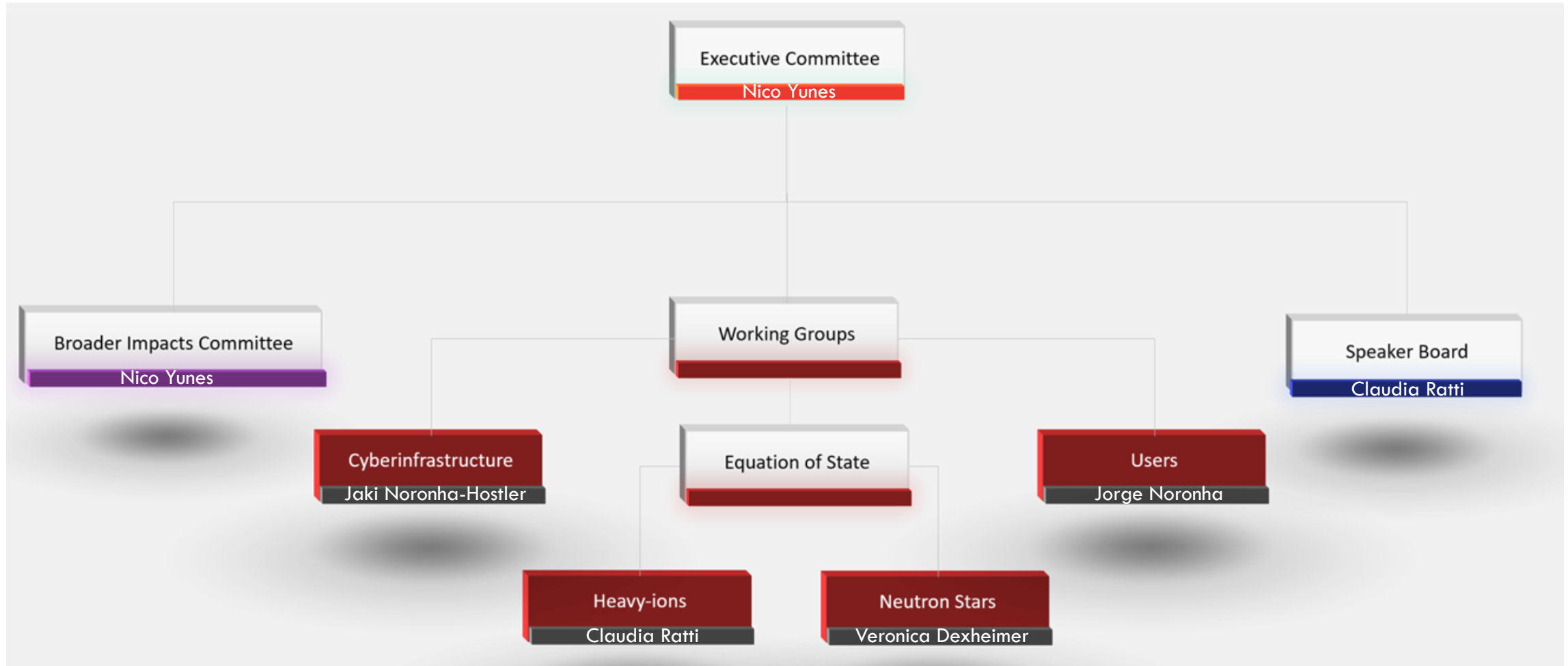


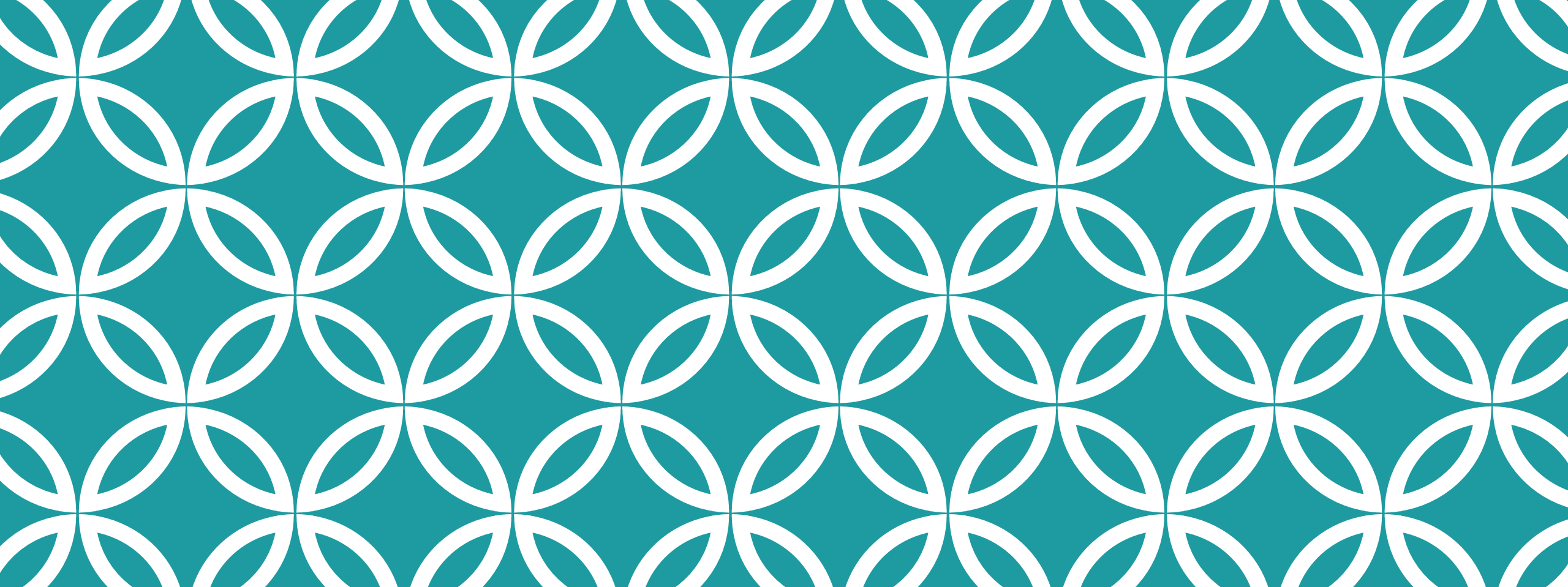


# COMMUNITY-DRIVEN

- *We held a workshop “From heavy-ion collisions to neutron stars” in August 2020*
- *~100 registered participants from heavy-ion and neutron-star communities*
- *Talks + panel discussions on what is really needed to move forward*
  - *Realistic, flexible equation of state in which the users can pick and choose different options (degrees of freedom, first-order vs smooth crossover, exotic quark flavors, values of electric charge and strangeness chemical potentials...)*

# ORGANIZATION





# BROADER IMPACT COMMITTEE

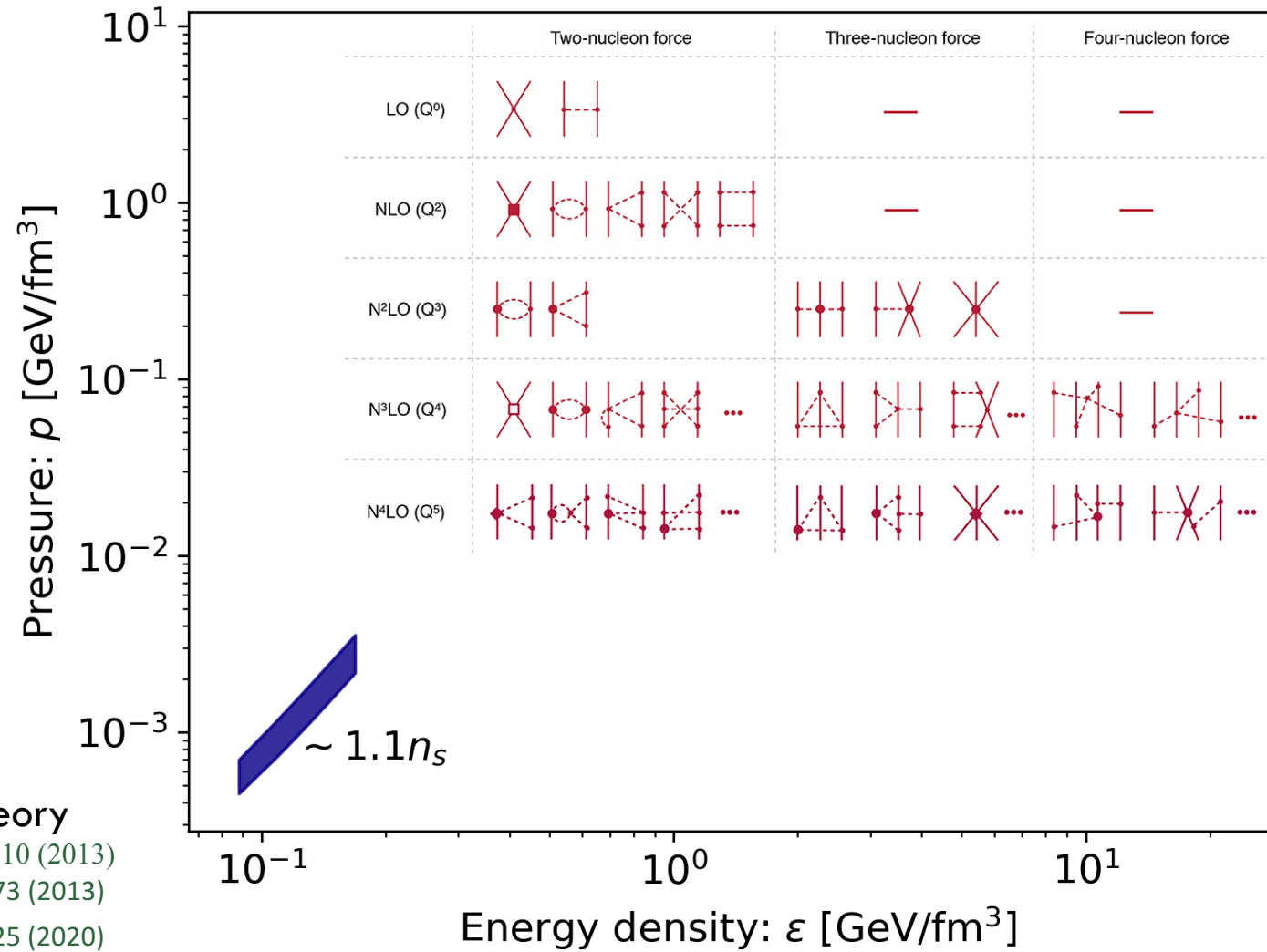
- Seminar series
- Schools
- Hybrid workshops
- Tutorial system
- Diversity



# BROADER IMPACT

- **Annual workshop** that combines a training camp and a professional think tank
  - Students and postdocs have the possibility to establish collaborations with more senior scientists
- Bi-weekly **seminar series** on MUSES-related topics (suggest speakers to Mauricio Hippert, Jamie Karthein, Joaquin Grefa, Hung Tan, Peter Jeffery)
- **Tutorial**: Web-based teaching system to provide the community with a self-learning tool
- **Diversity**: recruitment, support, training of underrepresented students and postdocs (REU, CuWiP, UH); creation of a multi-lingual “for the public” section on the webpage

# NEUTRON STARS AND MERGERS



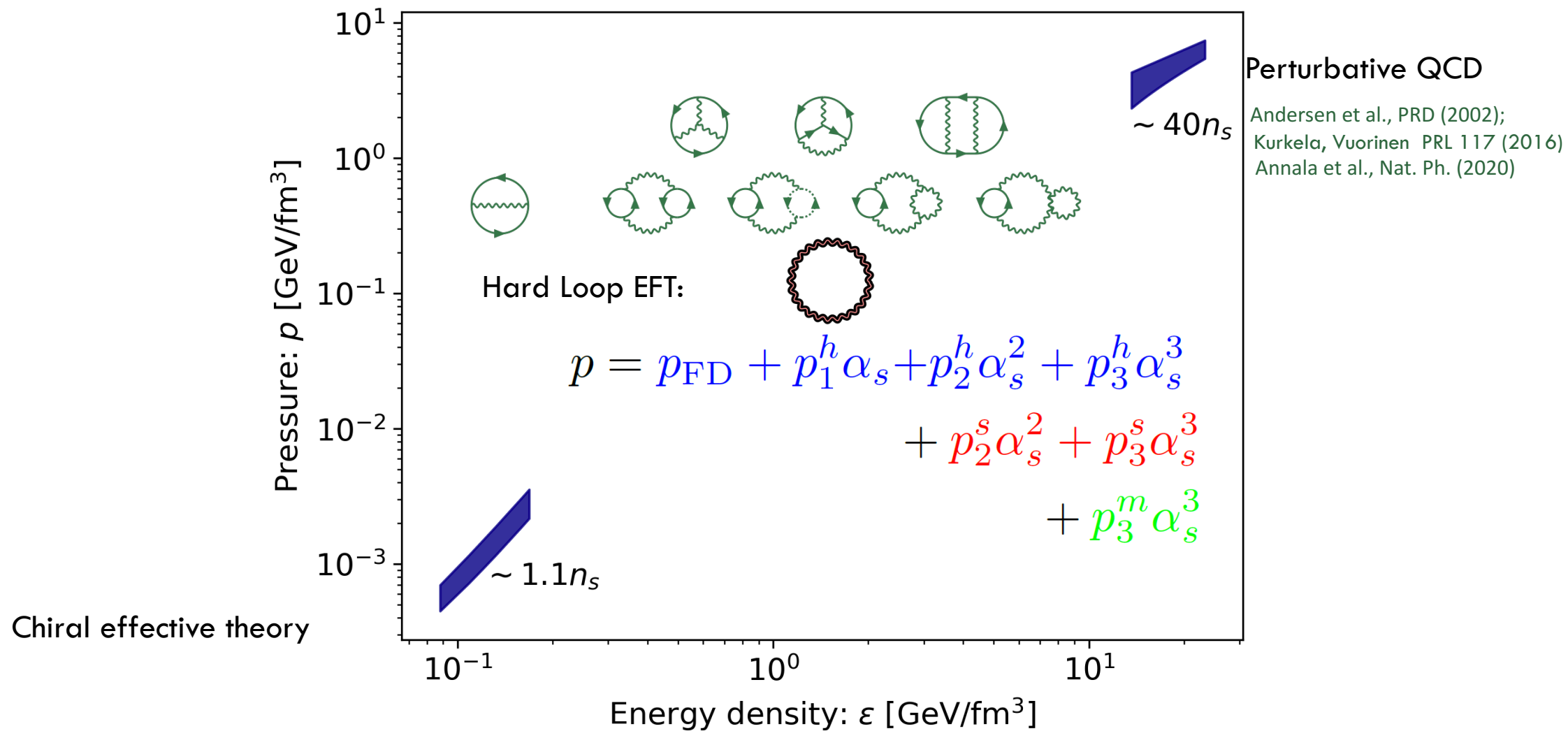
Chiral effective theory

Tews et al. PRL 110 (2013)

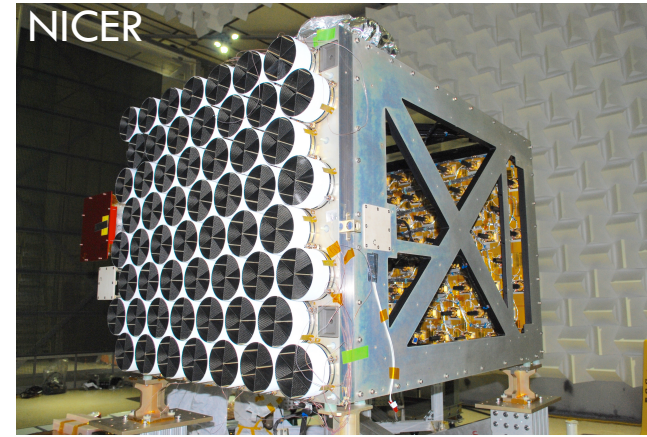
Hebeler, Lattimer et.al. APJ 773 (2013)

Drischler, Furnstahl et.al. PRL 125 (2020)

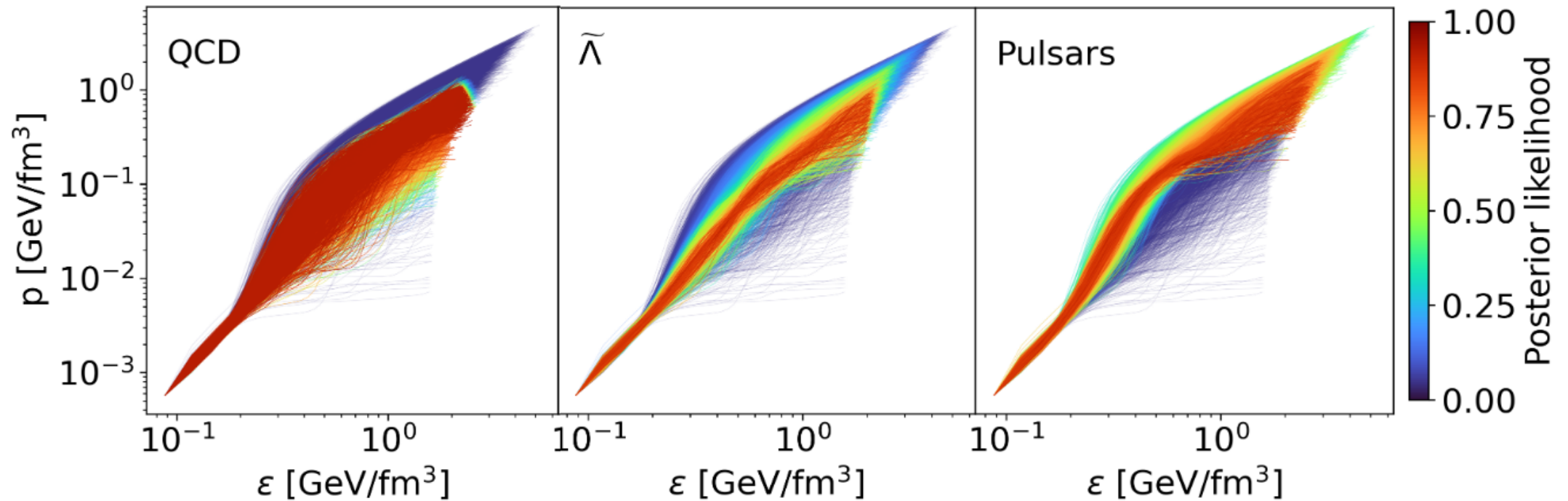
# NEUTRON STARS AND MERGERS



# NEUTRON STARS AND MERGERS



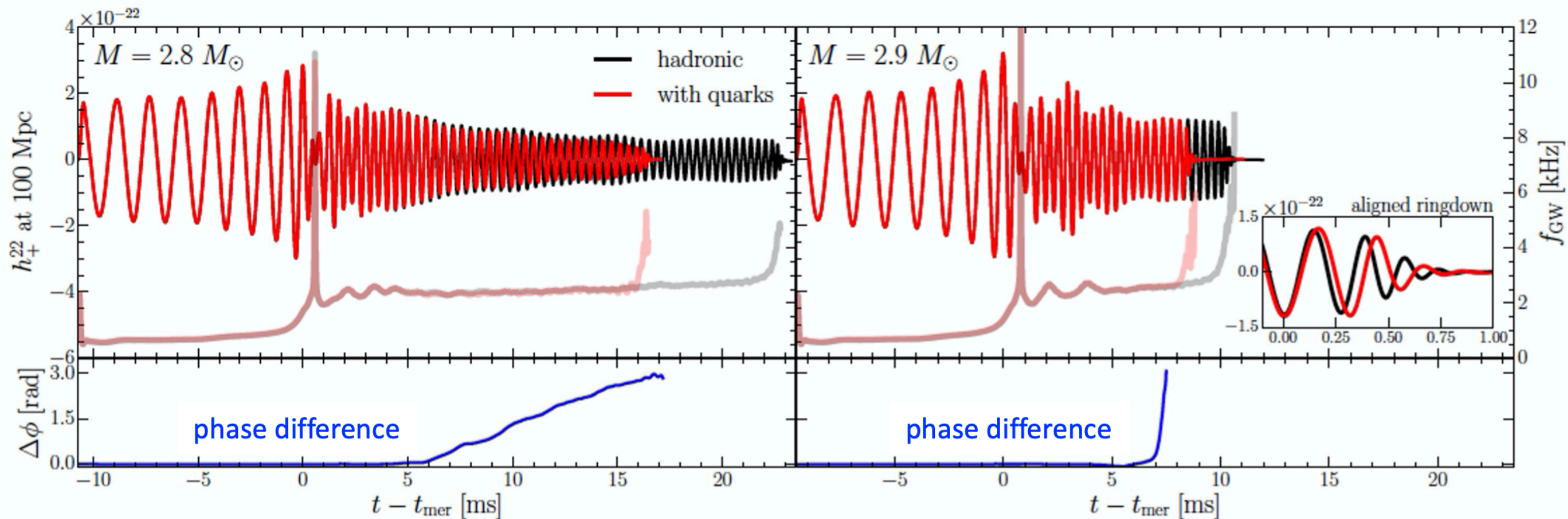
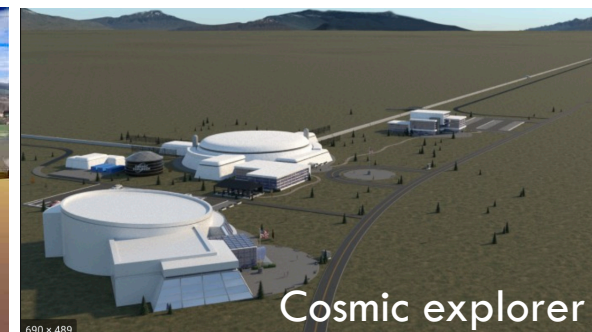
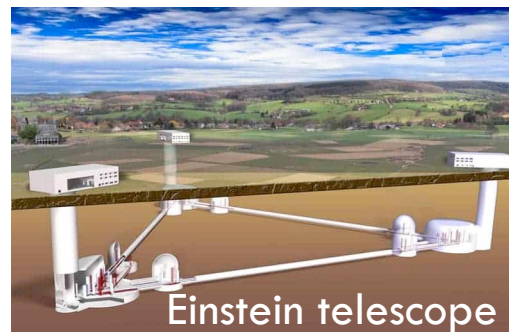
QCD input and NS observations can constrain the interpolation



Slide adapted from talk by A. Kurkela

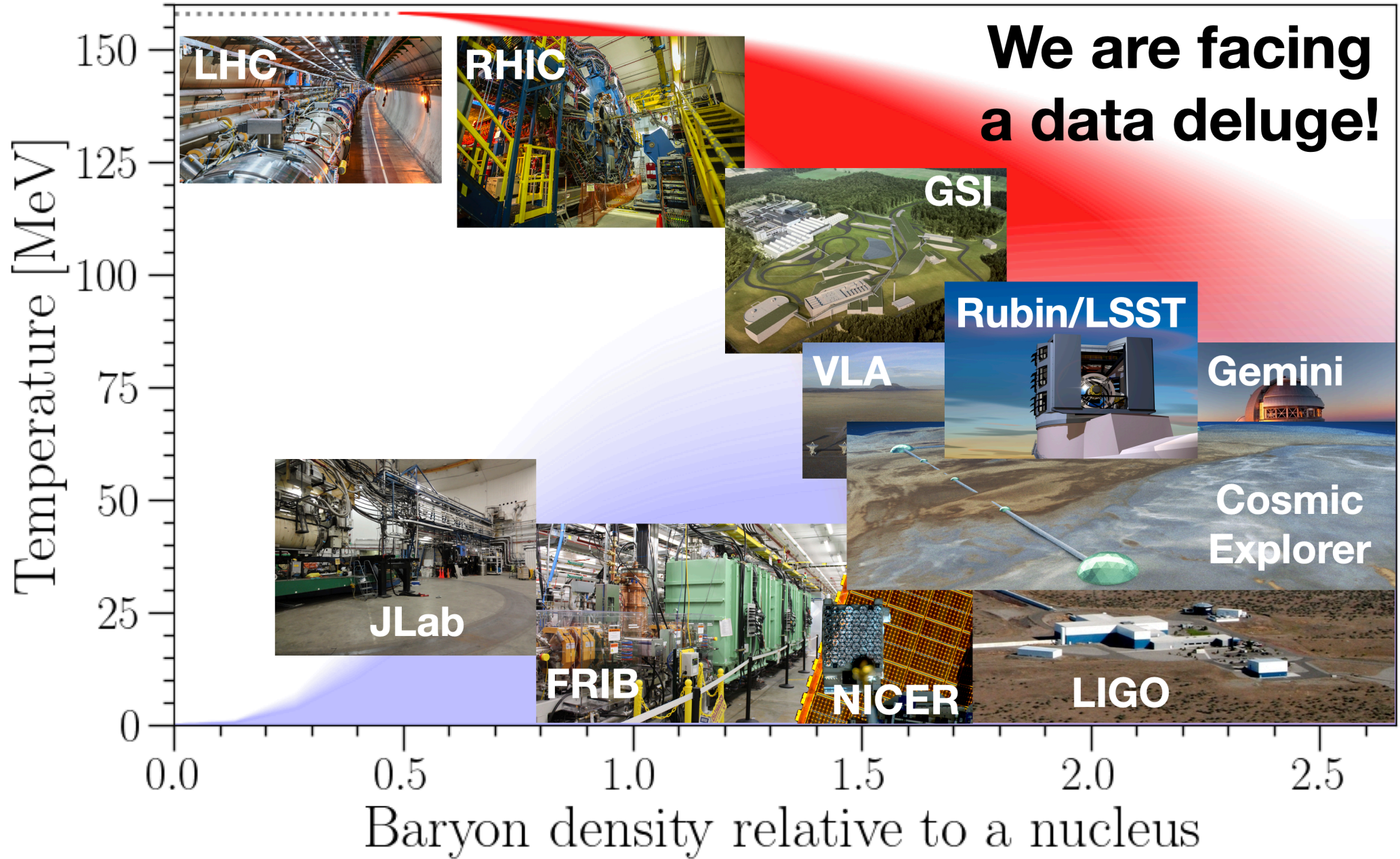
# NEUTRON STARS AND MERGERS

- Post-merger signal sensitive to order of the phase transition
- Next generation observatories will be able to detect it!
- Need to combine the nuclear physics input and simulations



E. Most et al., PRL (2019)







# EQUATIONS OF STATE

V. Dexheimer, S. Schramm PRC (2009)

G. Baym et al., Astrophys. J (2019)

X. Du, A. Steiner, J. Holt, PRC (2019)

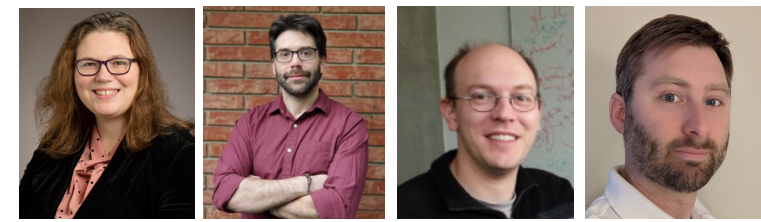
J. Holt & N. Kaiser, PRD (2017)

- Chiral mean field model
  - Crossover at low density and first-order phase transition at high density
  - Based on non-linear sigma model with the addition of deconfined quarks
- Quark-Hadron Crossover (QHC19)
  - Smooth crossover between hadrons and quarks
- UTK Equation of state
  - Includes nucleonic degrees of freedom based on a phenomenological fit to nuclear experiment and astronomical observations
- Chiral effective field theory
  - Interacting nucleons and pions within chiral effective field theory

# WEBPAGES

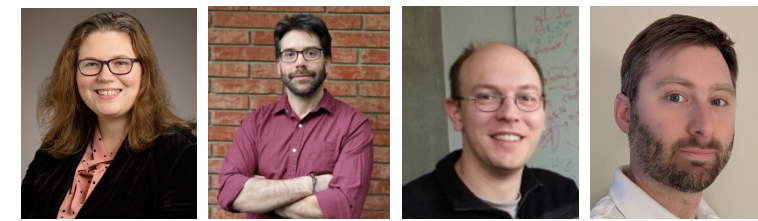
- Static webpage
- Computational tools
- Forum
- More resources (JupyterHub, Community chat, Collaborative documents, Collaboration Cloud storage)





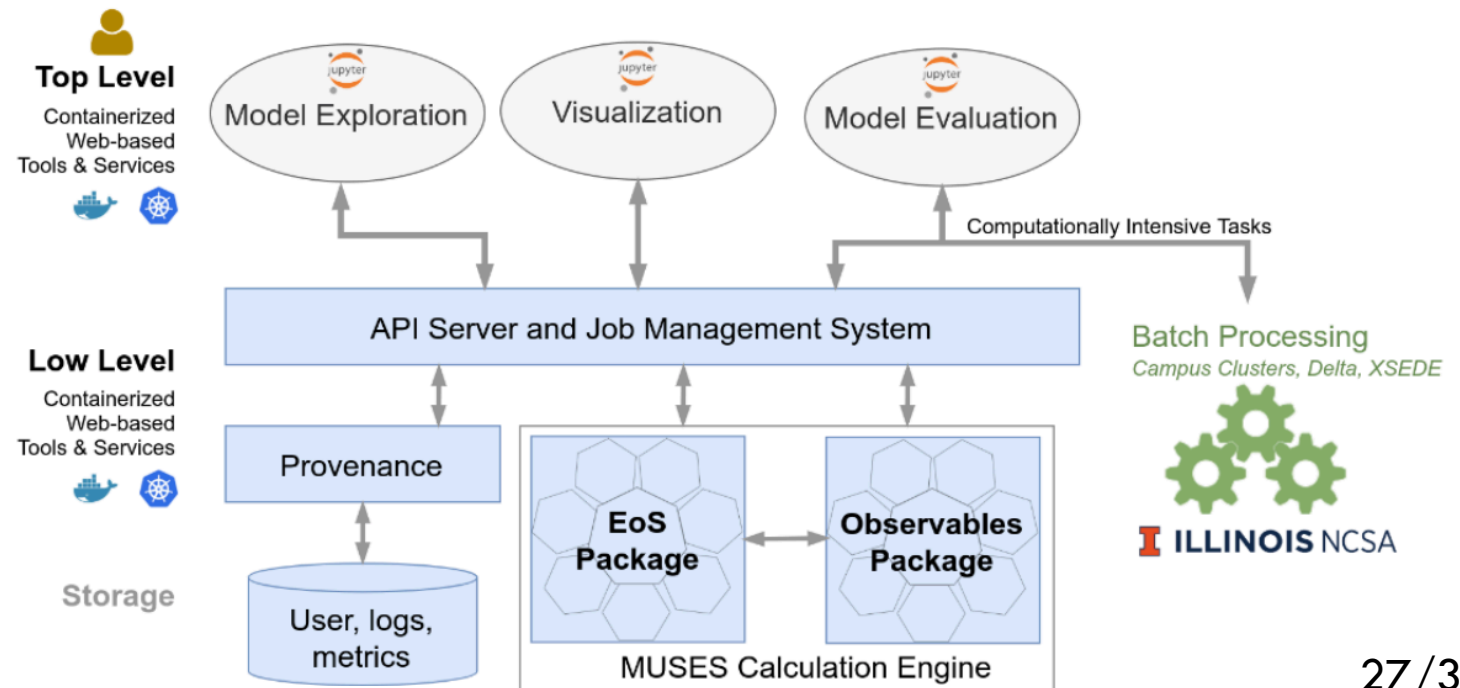
# WEB TOOLS

- Web interface allows access, interaction with the parameters, models, packages, and the computing nodes to perform the calculations
- Users can register and get access to documentation, manage their submitted jobs, download all input/output of their calculation
- New users can access a model exploration component, that allows them to understand MUSES as a whole
- The model evaluation component will be used for interactive, real-time evaluation of models
- The visualization component will provide tools to visualize the parameter space and the model in an intuitive way
- Computationally-intensive tasks will be submitted using a bash processing system and results will be retrieved when ready



# LOW-LEVEL SERVICES

- The client-facing API will handle communication with client applications
- Direct communication with the Batch and Provenance for storage
- Provenance will record all useful information: user activity, workflows executed, models evaluated, inputs/outputs, details of computational jobs (all only accessible internally)
- Storage will consist of a collection of services that store and serve data





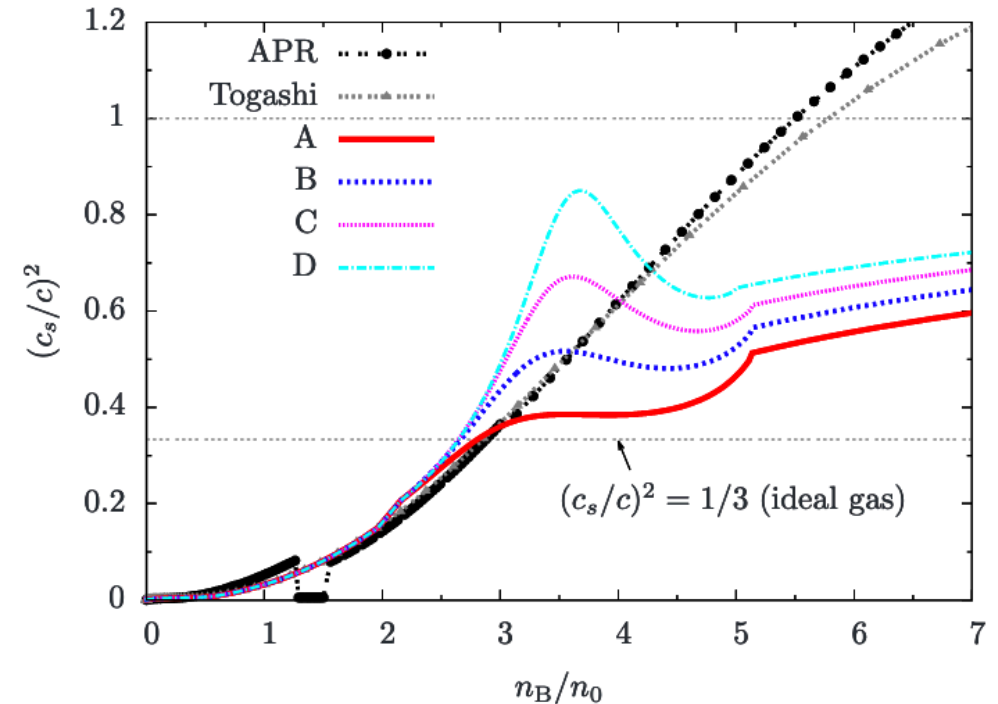
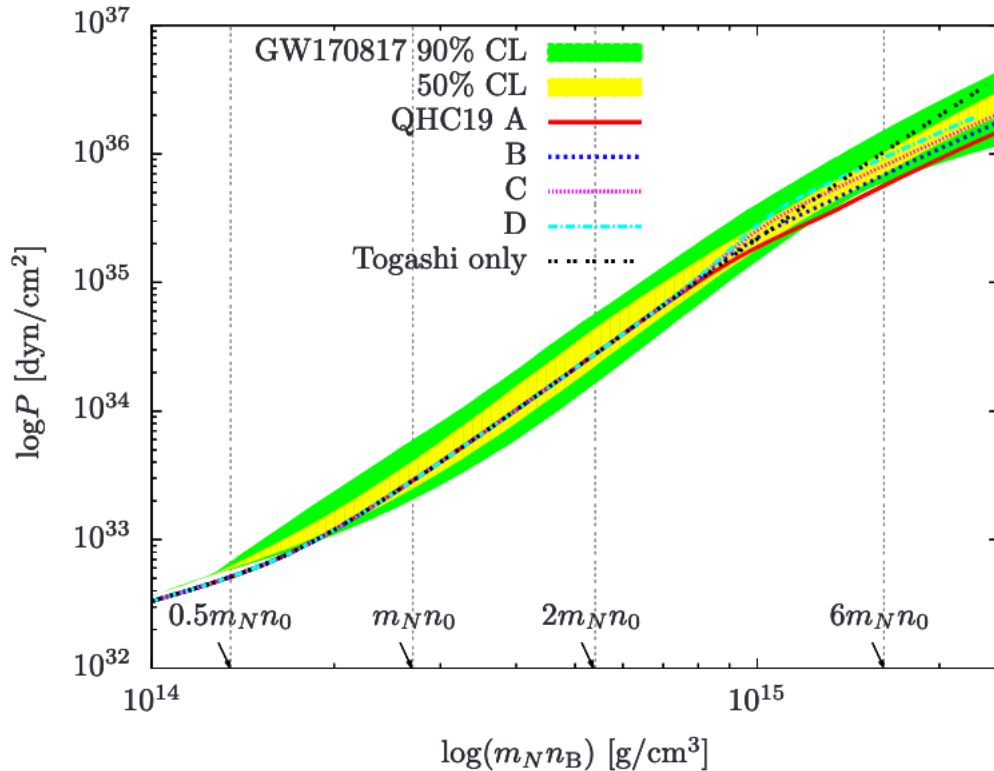
# QUARK-HADRON CROSSOVER (QHC19)

G. Baym et al., *Astrophys. J* (2019)

Goals:

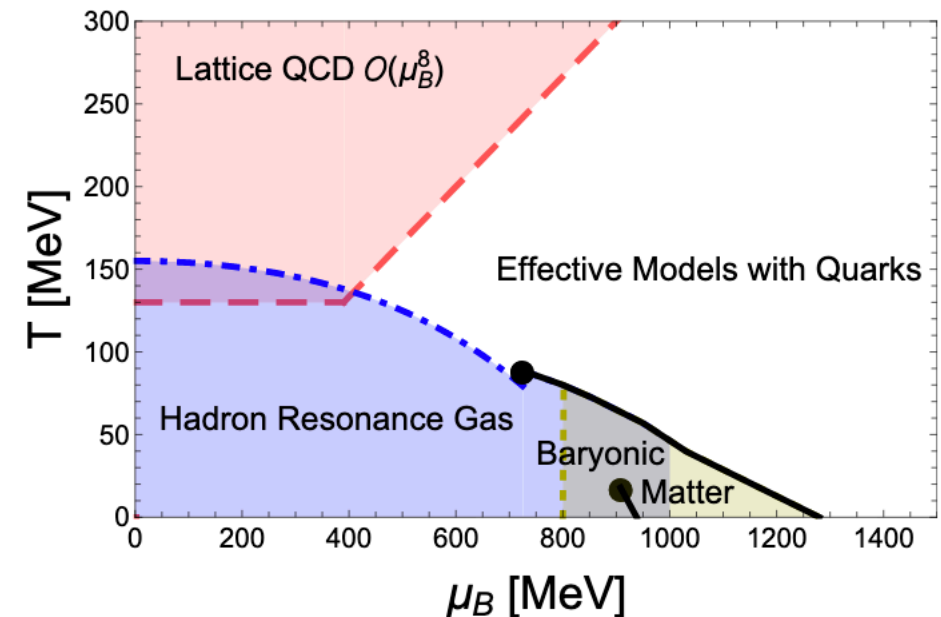
- Optimization of the code
- Incorporation into MUSES

- Equation of state with smooth crossover between hadrons and quarks
- Hadronic EoS is based on the Togashi model, which describes non-uniform and uniform matter, and beta-equilibrium
- Quark matter is described in the NJL model with vector interaction



# FERMIONIC SIGN PROBLEM

- QCD can only be solved numerically in the range of temperature and density relevant to study the phase transition
- This numerical technique is lattice QCD and it is based on Monte Carlo importance sampling
- Importance sampling cannot be applied at finite density, because the weight becomes complex
- For this reason, we do not know the equation of state and phase diagram at all temperatures and densities from first principles
- We need to rely on models to explore the regions which lattice QCD cannot reach



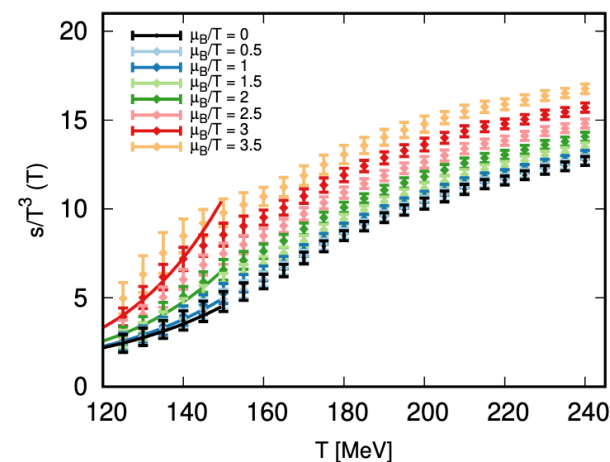
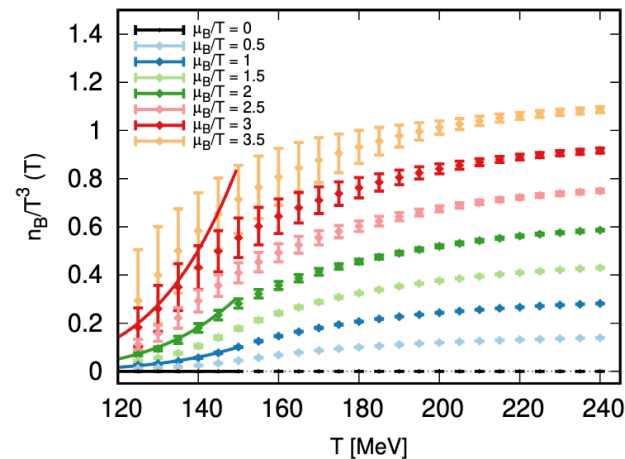


# EQUATION OF STATE FROM FIRST PRINCIPLES

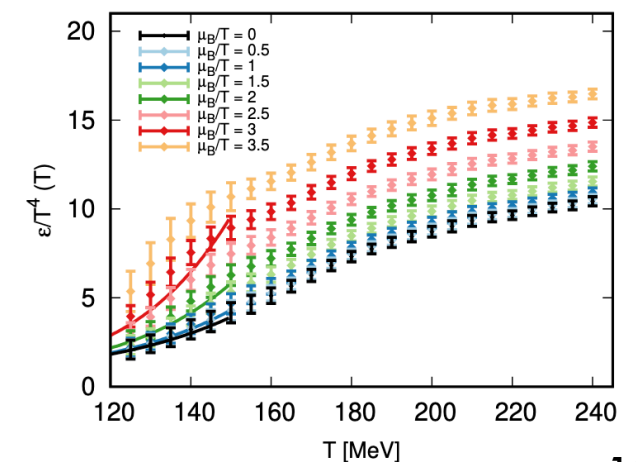
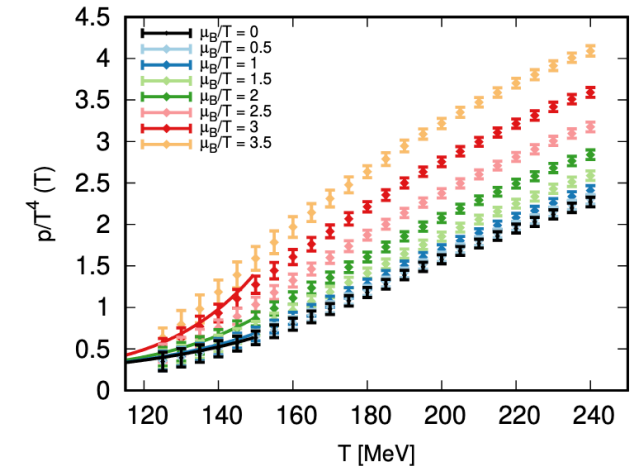
- Novel expansion scheme allows to extend to  $\mu_B/T \sim 3.5$
- EoS available so far at  $\mu_S = \mu_Q = 0$
- Working on the extension to the case  $\langle n_S \rangle = 0, \langle n_Q \rangle = 0.4 \langle n_B \rangle$  of relevance for heavy-ion collisions

## Goals:

- Extension to highest possible  $\mu_B$
- Extension to  $\mu_S$  &  $\mu_Q \neq 0$
- Implementation into the MUSES engine



S. Borsanyi, C. R. et al., PRL (2021)



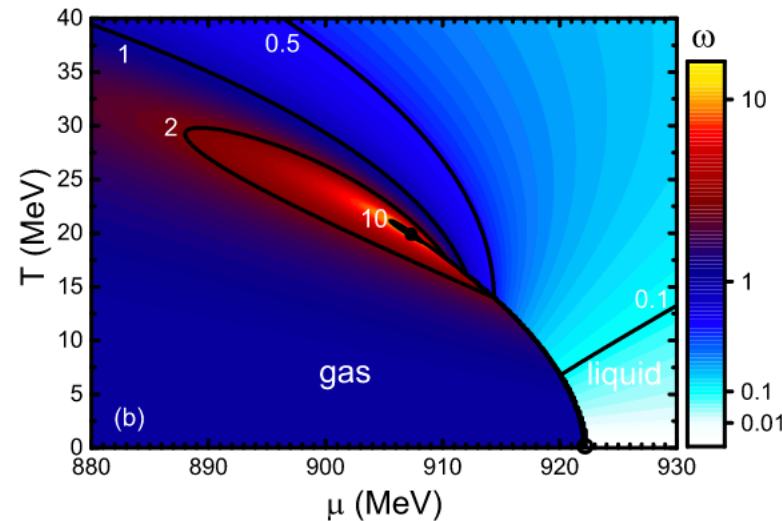
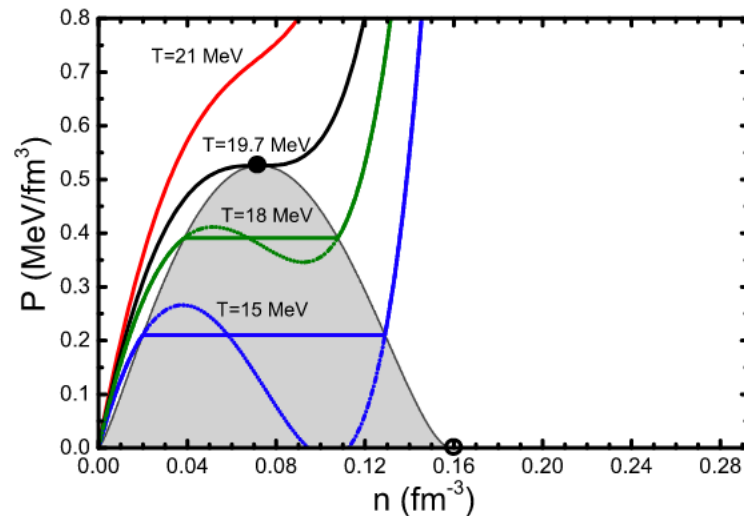




# HADRON RESONANCE GAS (HRG) MODEL

V. Vovchenko et al., PRC (2015)

- The HRG model provides a well-established and realistic Equation of State at low temperatures
- Its ideal version is based on the assumption that an **interacting gas of hadrons** in the ground state can be well-approximated by an **ideal gas of resonances**
- At large density we need to incorporate additional interactions such as van Der Waals
- It describes the liquid-gas phase transition



## Goals:

- Optimization of the code
- Fix the parameters to describe the liquid-gas critical point
- Incorporation into MUSES



# EQUATIONS OF STATE

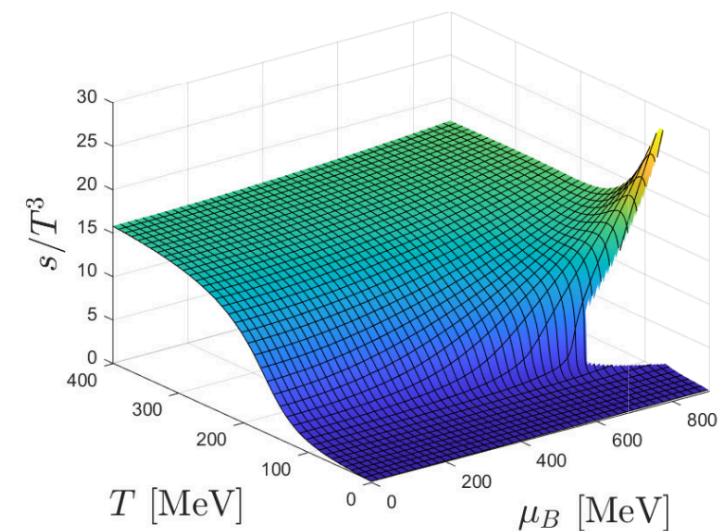
- Taylor expansion from lattice QCD at finite  $T$ ,  $\mu_B$ ,  $\mu_S$ ,  $\mu_Q$ 
  - Coverage:  $120 < T < 800$  MeV,  $0 < \mu_B / T < 2.5$
- HRG model with van der Waals interactions
  - Coverage:  $0 < T < 150$  MeV,  $0 < \mu_B < 1000$  MeV
- EoS with 3D Ising model critical point
  - Coverage:  $0 < T < 800$  MeV,  $0 < \mu_B < 450$  MeV
- Equation of state from holography
  - Coverage:  $100 < T < 800$  MeV,  $0 < \mu_B < 1100$  MeV

[J. Grefa, C. R. et al., PRD \(2021\)](#)

[S. Borsanyi, C. R. et al., JHEP \(2018\)](#)  
[J. Noronha-Hostler, C. R. et al., PRC \(2019\)](#)  
[A. Monnai et al., PRC \(2019\)](#)

[V. Vovchenko et al., PRC \(2015\)](#)

[P. Parotto, C. R. et al., PRC \(2020\)](#)  
[J. Karthein, C. R. et al., EPJ Plus \(2021\)](#)





# EQUATION OF STATE WITH 3D-ISING CRITICAL POINT (BESEOS)

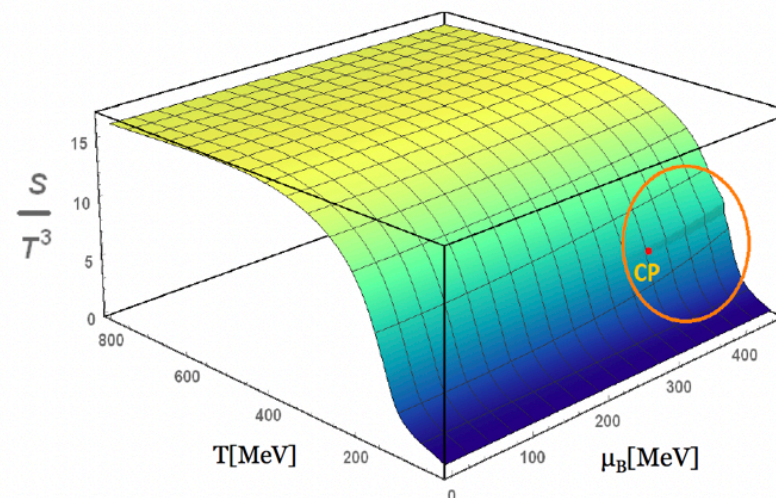
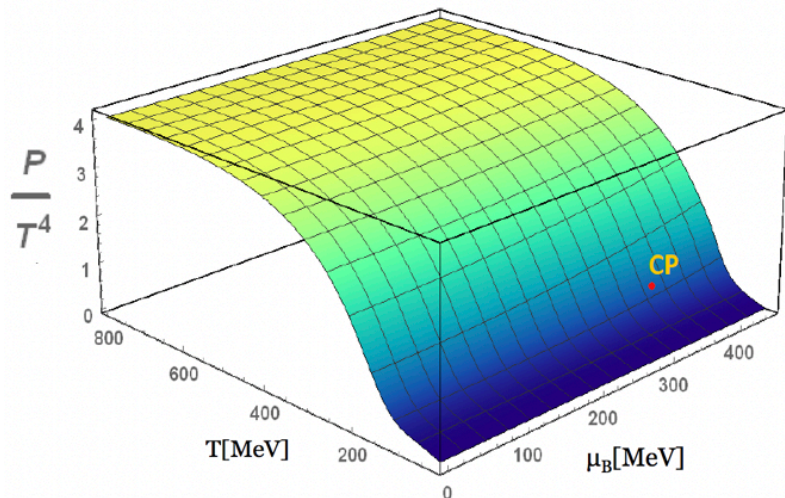
- Implement scaling behavior of 3D-Ising model EoS
- Define map from 3D-Ising model to QCD
- Estimate contribution to Taylor coefficients from 3D-Ising model critical point
- Reconstruct full pressure
- Currently available at  $\mu_S = \mu_Q = 0$  and for  $\langle n_S \rangle = 0$ ,  $\langle n_Q \rangle = 0.4 \langle n_B \rangle$

P. Parotto, C. R. et al., PRC (2020)

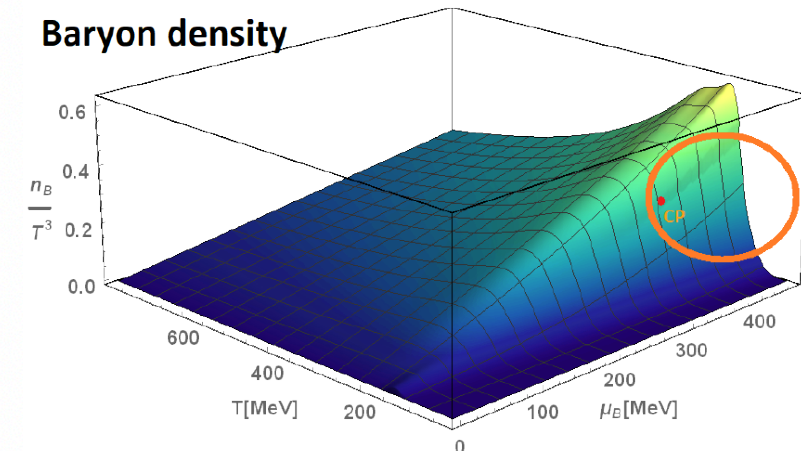
J. Karthein, C. R. et al., EPJ Plus (2021)

## Goals:

- Extension of range in  $\mu_B$
- Extension to three conserved charges
- Incorporation into MUSES



## Baryon density





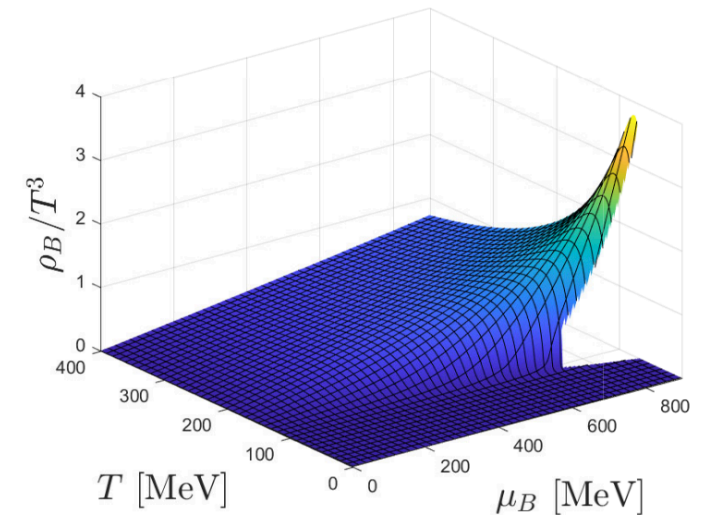
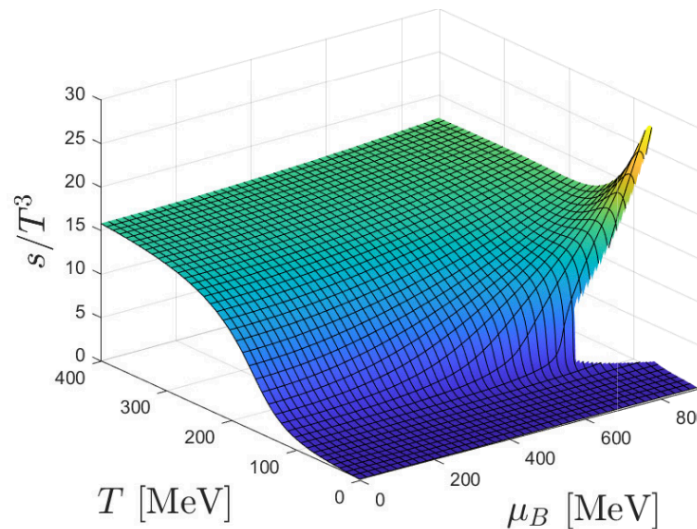
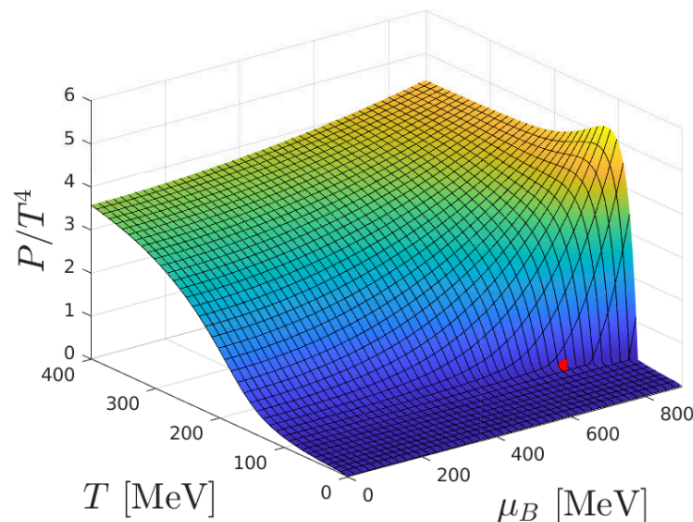
# EQUATION OF STATE FROM HOLOGRAPHY (NUMRELHOLO)

J. Grefa, C. R. et al., PRD (2021)

- Use AdS/CFT correspondence
- Fix the parameters to reproduce everything we know from the lattice
- Calculate equation of state at finite density
- Model currently has only baryon number
- Prediction of critical point:  $T_C = 89 \text{ MeV}$   $\mu_{BC} = 723 \text{ MeV}$

## Goals:

- Optimization of the code
- Inclusion of more than one conserved charge
- Incorporation into MUSES

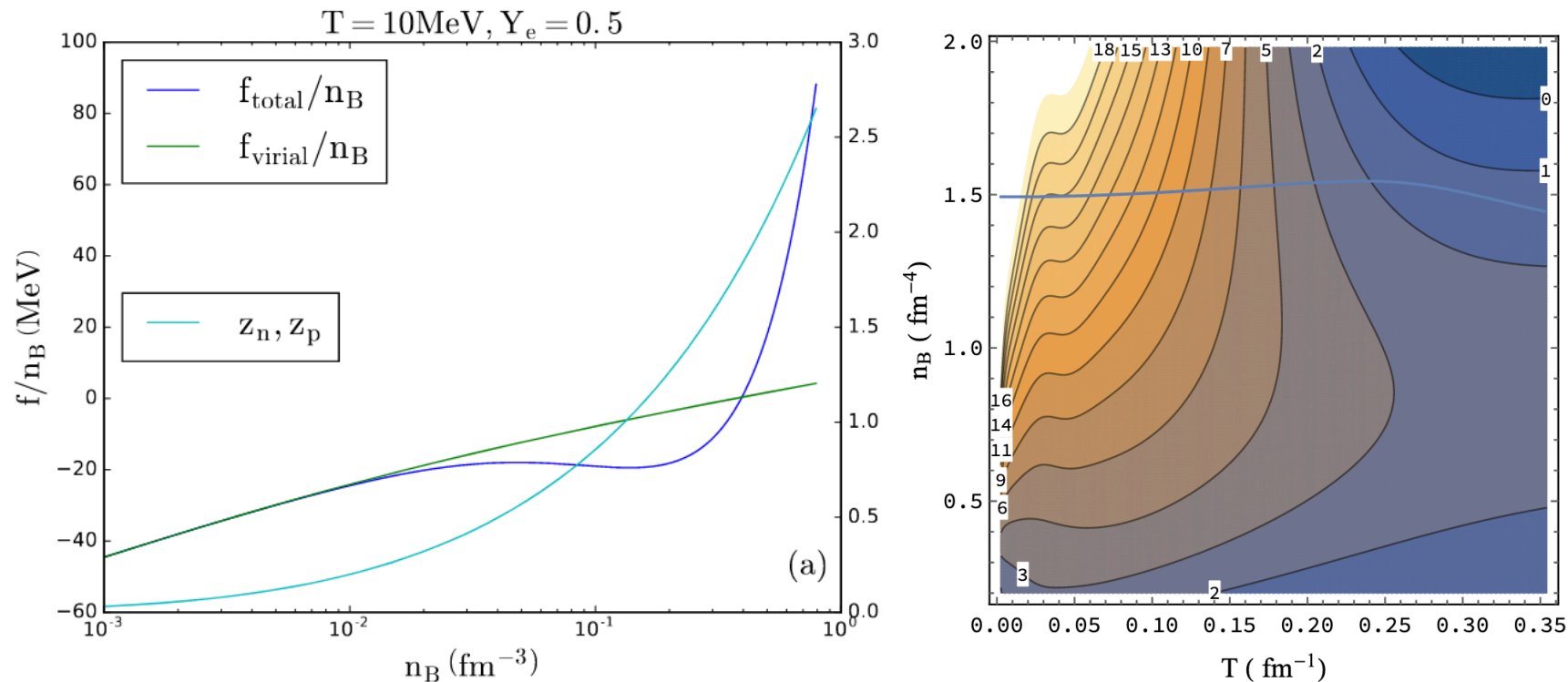




# UNIVERSITY OF TENNESSEE KNOXVILLE EOS(UTK EOS)

X. Du, A. Steiner, J. Holt, PRC (2019)

- Includes nucleonic degrees of freedom based on a phenomenological fit to nuclear experiment and astronomical observations
- Covers densities from  $10^{-12}$  to  $2 \text{ fm}^{-3}$  and temperatures up to 100 MeV



- Goals:**
- Optimization of the code
  - Extension to strangeness degrees of freedom
  - Incorporate into MUSES



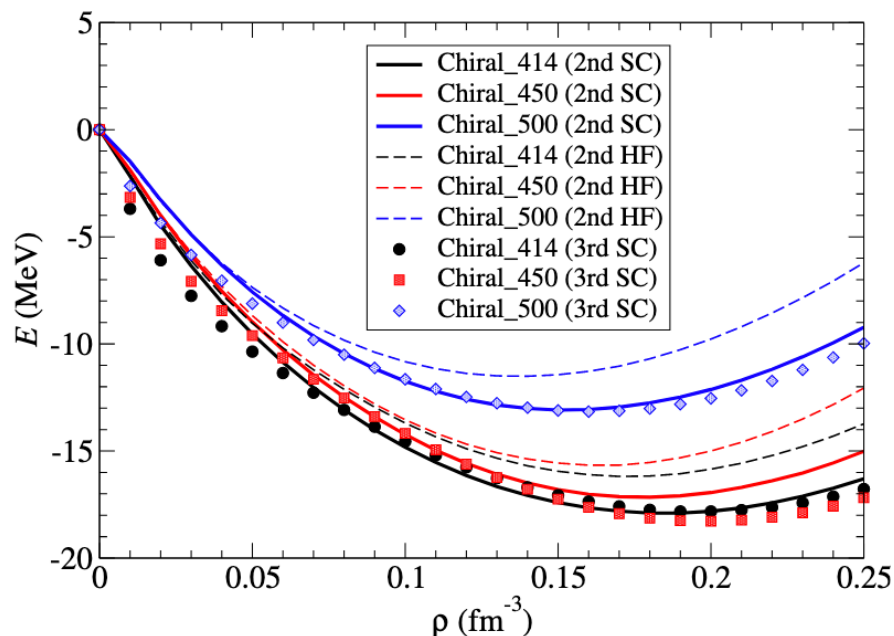
# CHIRAL EFFECTIVE FIELD THEORY (CHEFTEOS)

J. Holt & N. Kaiser, PRD (2017)

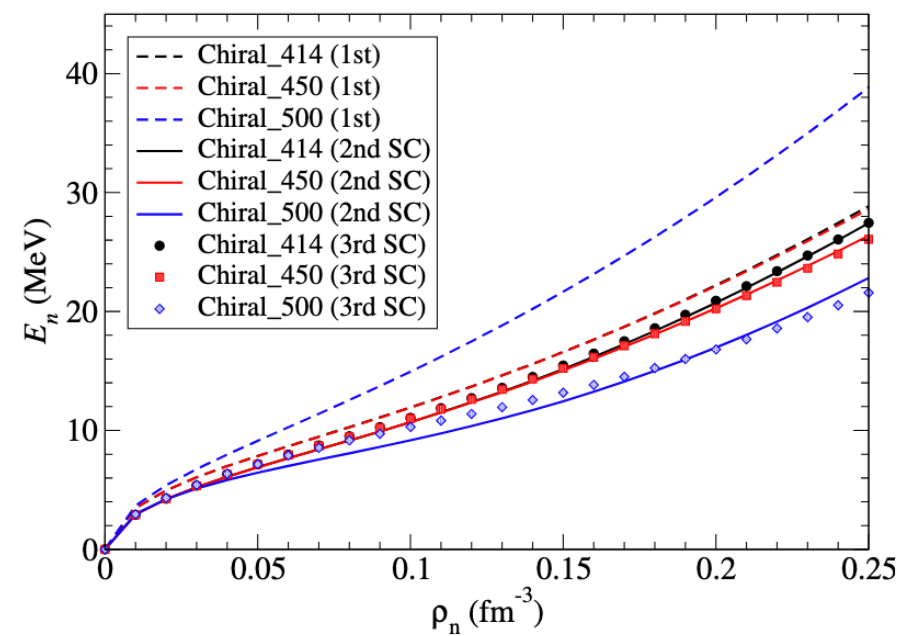
- Describes matter in the range  $T < 25$  MeV,  $800$  MeV  $< \mu_B < 1100$  MeV
- Interacting nucleons and pions within chiral effective field theory
- Constrains do not exist for asymmetric matter

## Goals:

- Optimization of the code
- Optimization of root-finding techniques
- Incorporate into MUSES



EoS for symmetric nuclear matter



EoS for neutron matter

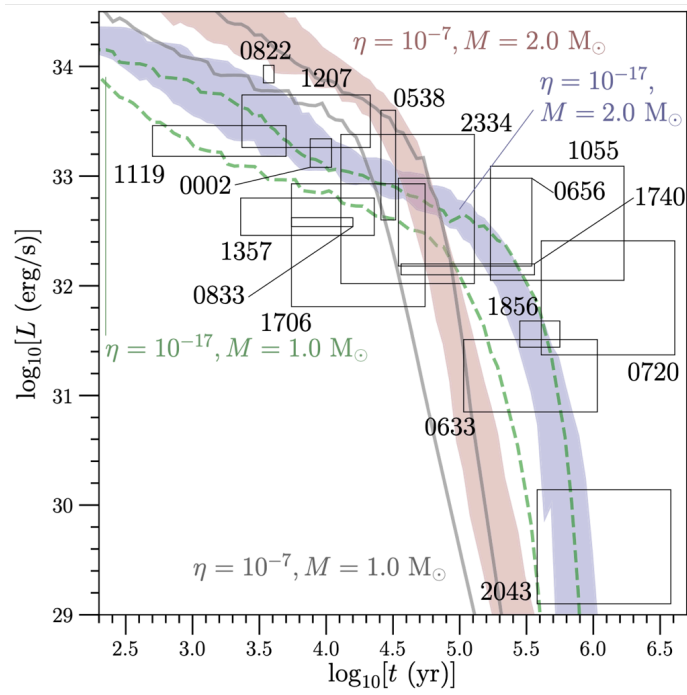
# From Observables to Nuclear Physics

## Nucleon-nucleon interactions from neutron star mergers

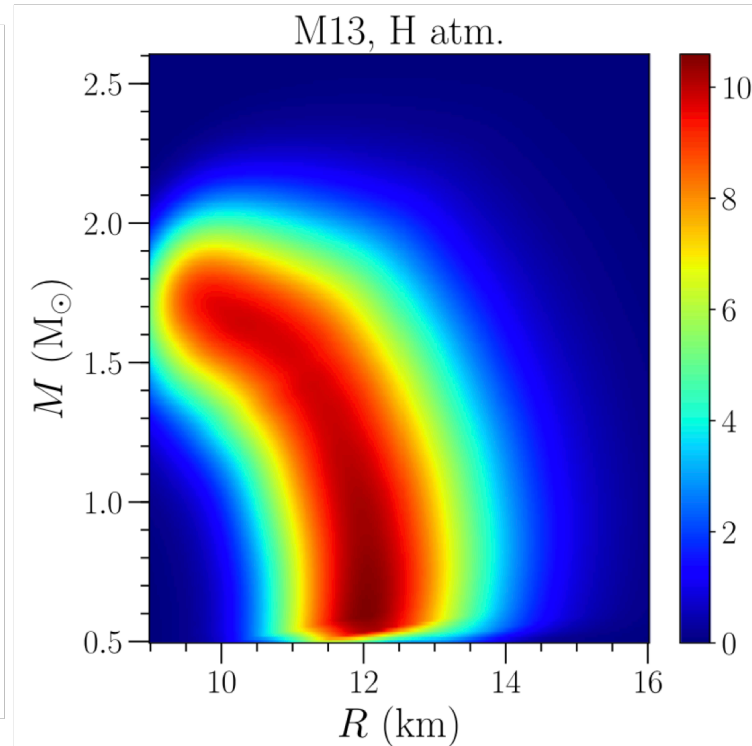
- Goal of the hub is to go beyond the “obvious” observable parameters and understand nuclear physics, but...
- We will not understand mergers work until we understand the nuclear theory
- We cannot constrain nuclear theories without understanding mergers
- Develop models that constrain the underlying nuclear theory using multi-messenger observables
- Start with reasonable prior choices, use observations to tune nuclear theory, improve models, revisit observations, make predictions

# Multi-Messenger Inference

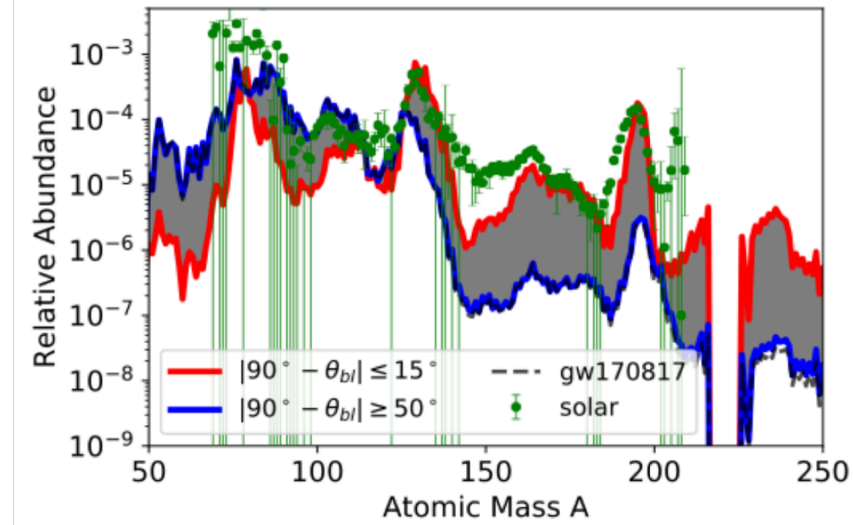
## Connecting to observables



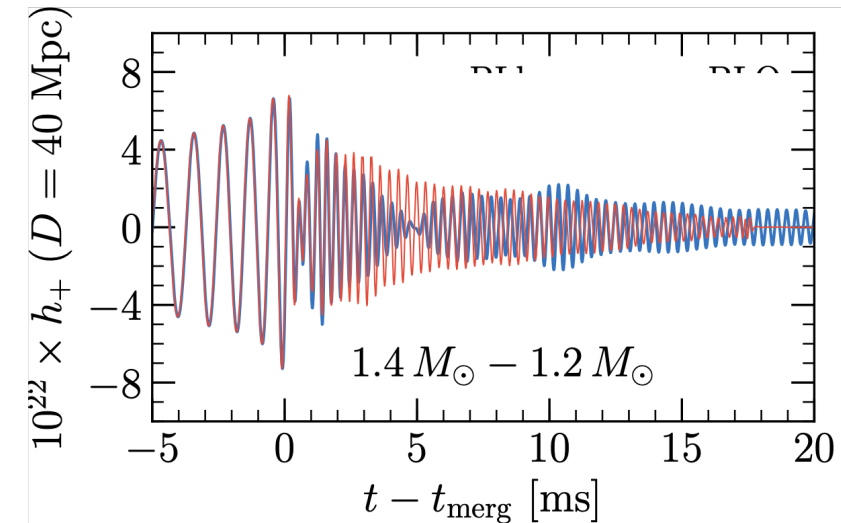
Age-luminosity relations for isolated neutron stars (UTK)



X-ray spectra of Quiescent low-mass X-ray binaries (UTK)



r-process abundances (PSU, UNH and UTK)



Predictions for multi-messenger observations (SU, CSUF, PSU)