

Phase-sensitive modified cyclotron Frequency Measurements with a single trapped Antiproton



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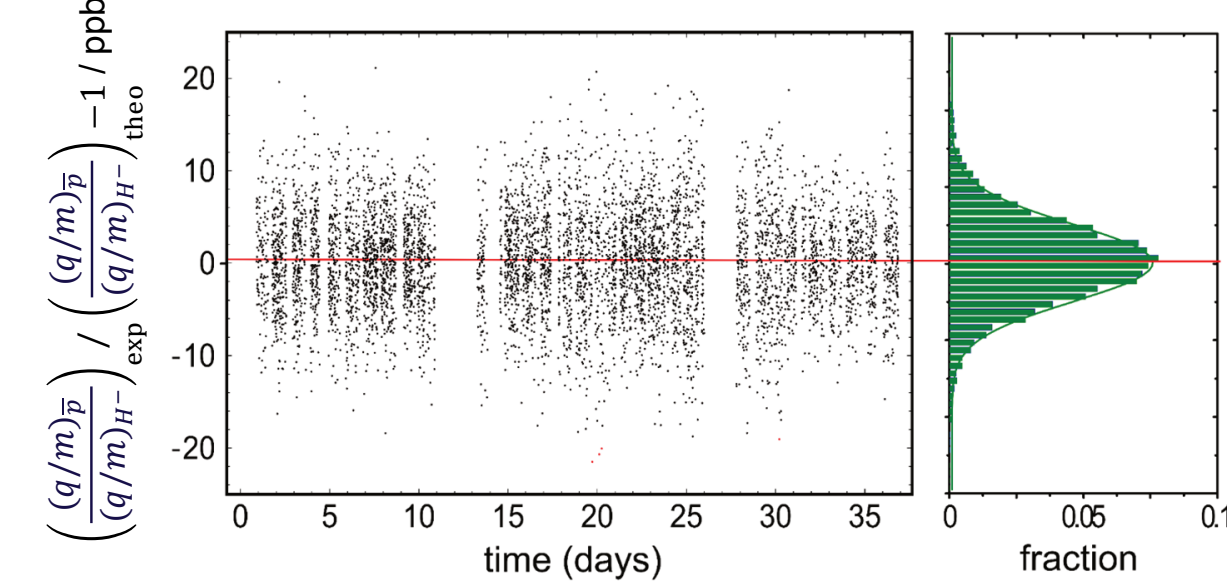
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Motivation

Measurements at BASE CERN [1]

- p and \bar{p} charge-to-mass ratio relative to each other to remove B dependence (H^- used instead of p due to opposite charge)

$$\omega_{c,\bar{p}} = \frac{q\bar{p}}{m\bar{p}} B \Rightarrow \frac{q\bar{p}/m\bar{p}}{q_p/m_p} = \frac{\omega_{c,\bar{p}}}{\omega_{c,p}}$$



$$\frac{(q/m)_{\bar{p}}}{(q/m)_p} + 1 = -3(16) \times 10^{-12} \text{ 16ppt [2]}$$

- p and \bar{p} magnetic moment relative to the (anti-)nuclear magneton

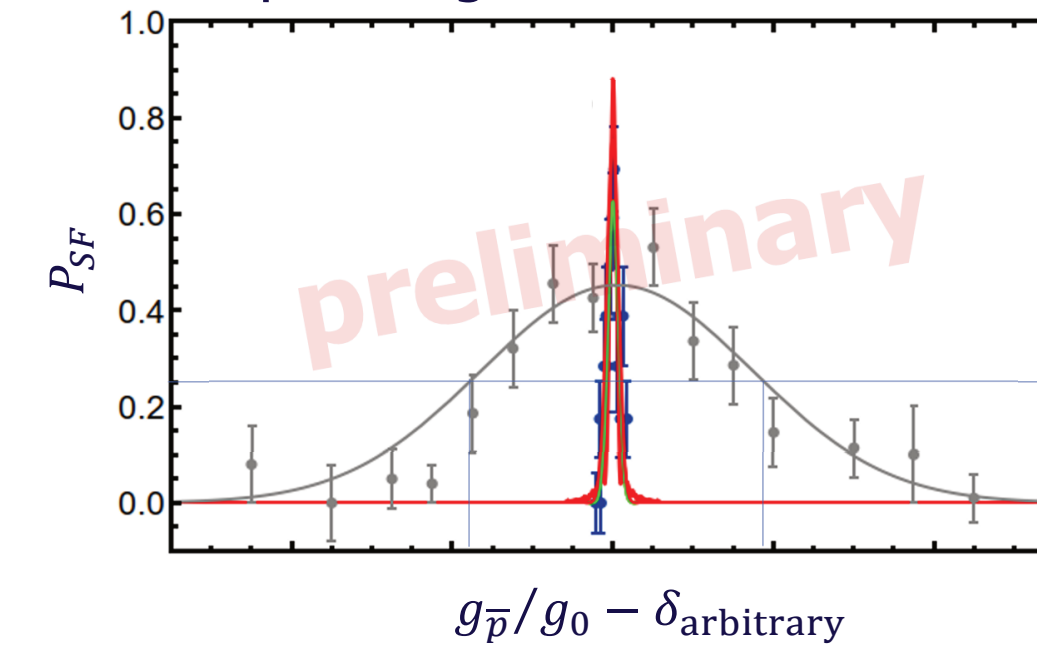
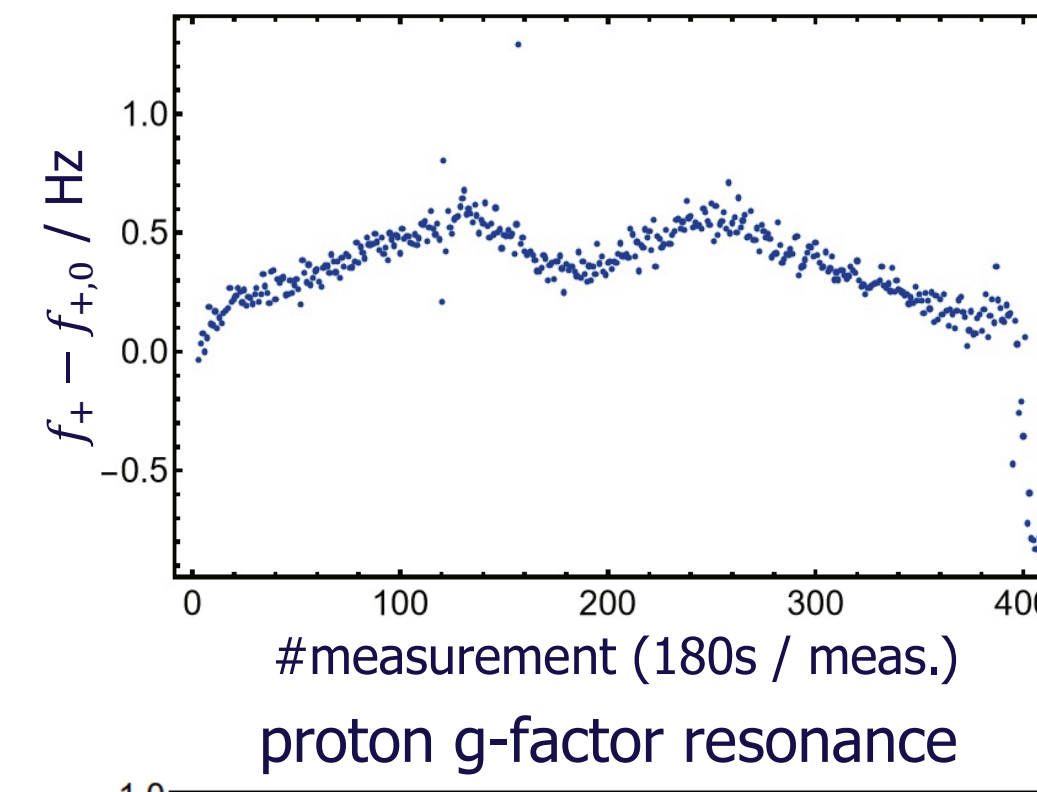
$$\frac{q\bar{p}}{m\bar{p}} B = \omega_{c,\bar{p}} = \frac{2\mu_N B}{\hbar} \Rightarrow \frac{g}{2} = \frac{\omega_{L,\bar{p}}}{\omega_{c,\bar{p}}} = \frac{\mu_{\bar{p}}}{\mu_N}$$

$$\frac{g\bar{p}}{2} \frac{q\bar{p}}{m\bar{p}} B = \omega_{L,\bar{p}} = \frac{\mu_{\bar{p}} B}{\hbar}$$

- $\Delta g_{\bar{p}} \gtrsim \Delta\omega_{c,\bar{p}} \gg \Delta\omega_{L,\bar{p}}$
- $\Delta\omega_{L,\bar{p}} \approx ???$ (coherence limited)
- $\Delta\omega_{c,\bar{p}} \approx ???$

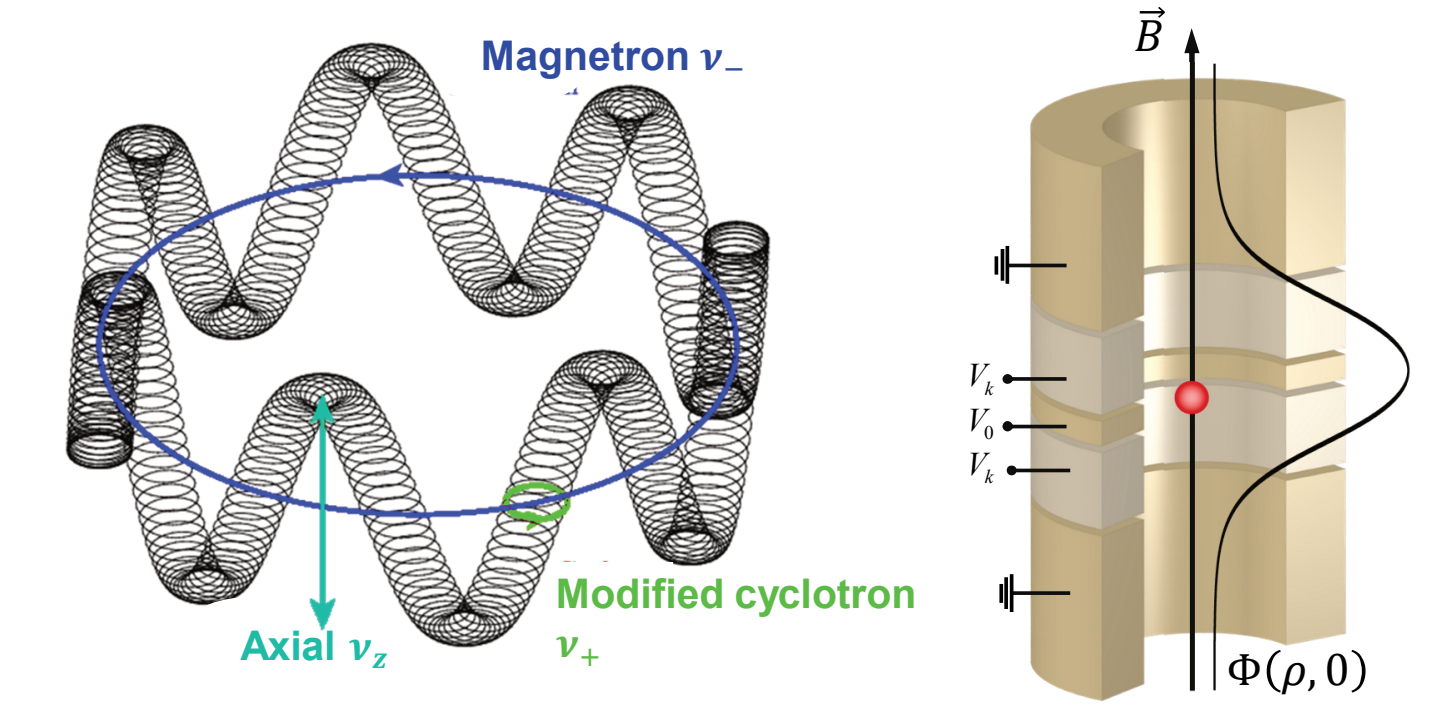
$$\frac{g\bar{p}}{2} = 2.792\,847\,344\,62(82) \text{ 0.3ppb [3]}$$

$$\frac{g\bar{p}}{2} = 2.792\,847\,344\,1(42) \text{ 1.5ppb [4]}$$



Determining $\omega_{c,\bar{p}}$

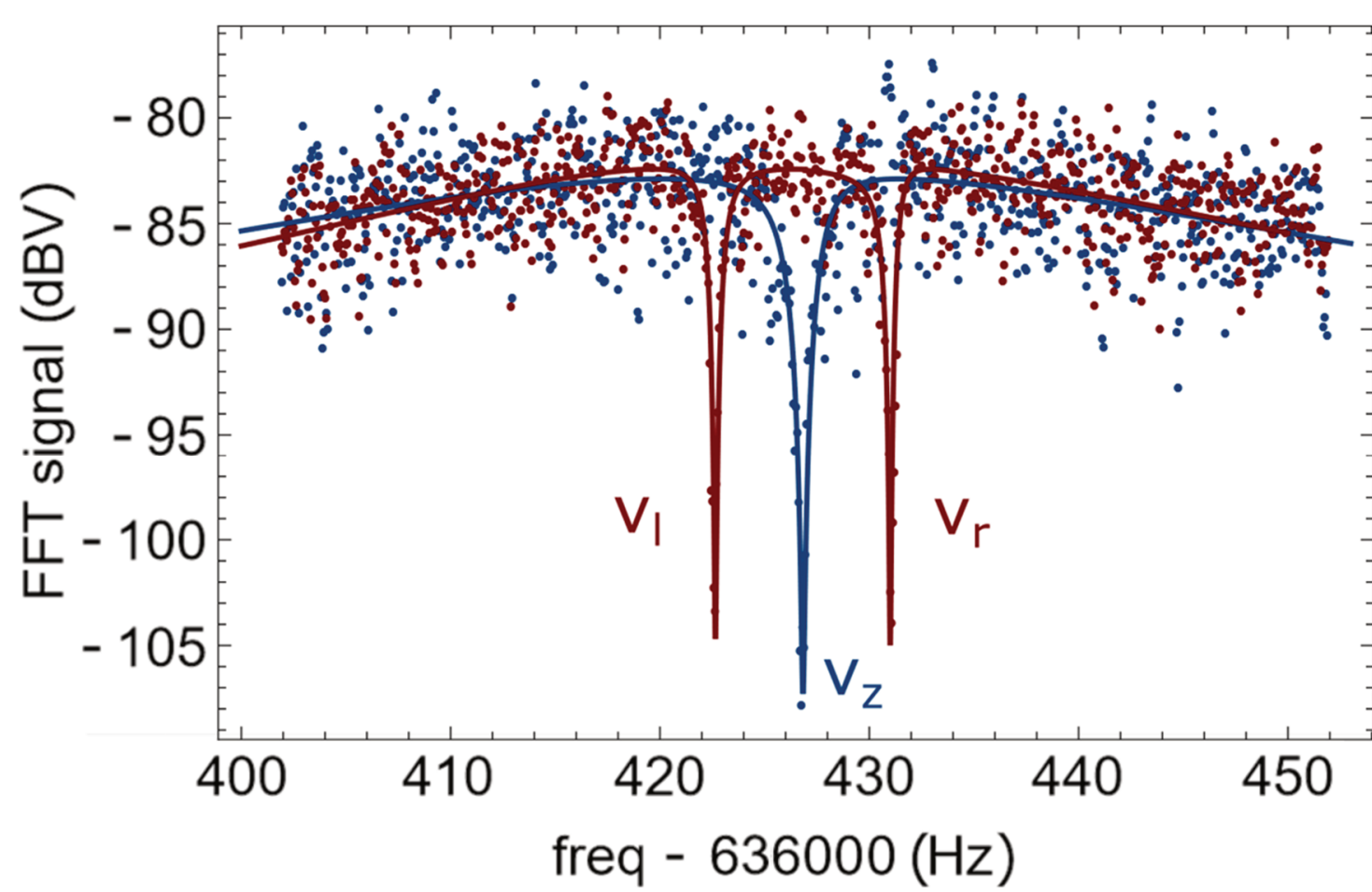
- BASE uses Penning traps to confine particles [5]



- $\omega_c = \sqrt{\omega_+^2 + \omega_z^2 + \omega_-^2}$, $\omega_+ \gg \omega_z \gg \omega_-$
 - Custom built high-Q resonators allow precise determination of ω_z and sidebands of ω_- and ω_+
 - resonators at ω_+ only at much lower Q
 - ω_- sufficiently precisely measured with SB method
- $\sigma(\omega_c) \approx \sigma(\omega_+)$!

Sideband Method ω_+

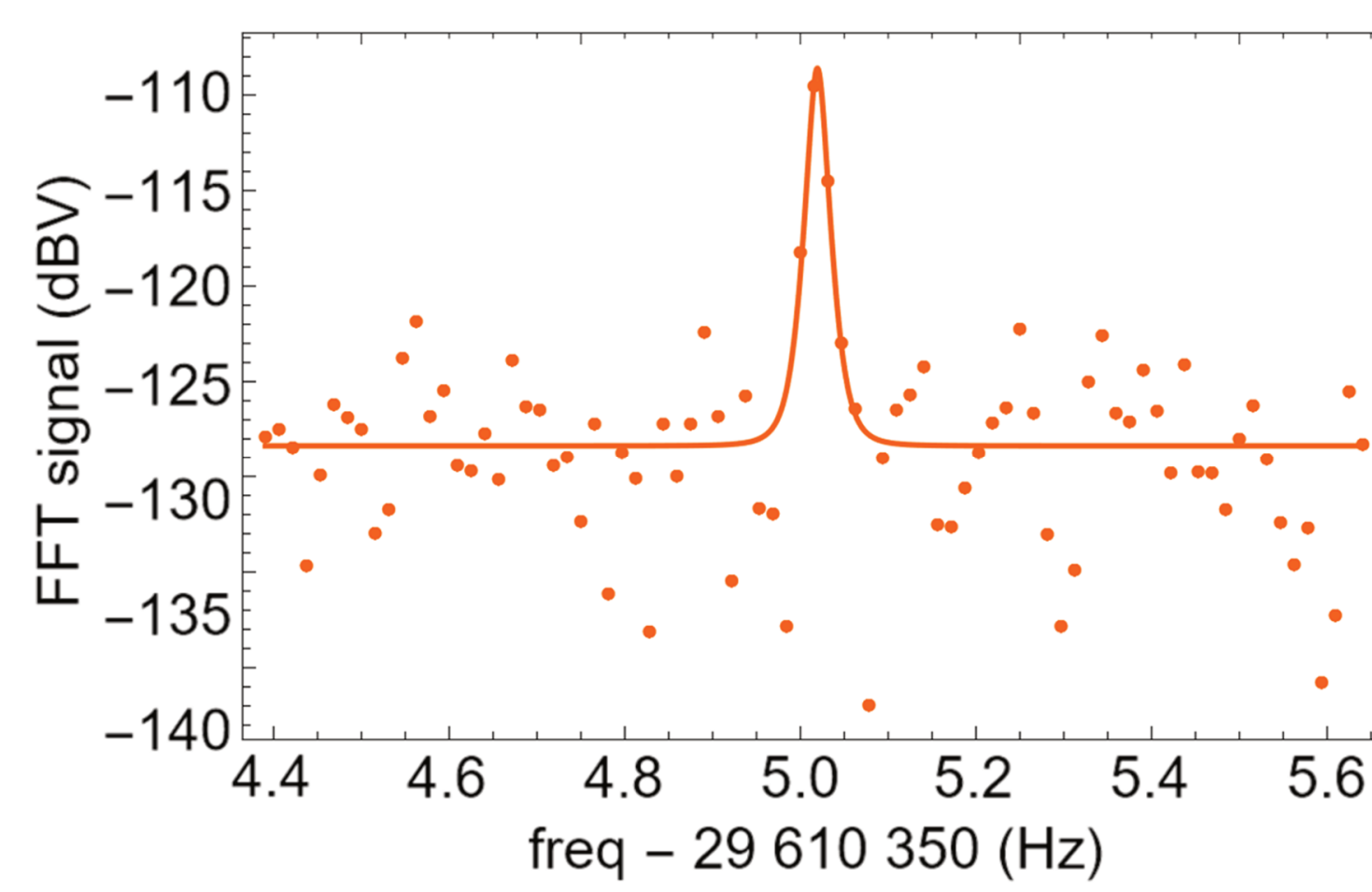
- Single Dip
 - low energy particle thermally coupled to a parallel RCL resonator
 - Johnson noise in resonator causes LSD $\sim \sqrt{4k_B T \text{Re}[Z(\omega)]}$ noise
 - around the particles axial resonance frequency ω_z , the particle shorts the noise, acting as a serial RCL resonator with a greater Q
 - no energy transfer due to random phase, but thermalization
- Double Dip
 - using prior knowledge of $\omega_{+/-}$, radiating $\omega_{RF} \approx \omega_{+/-} \mp \omega_z$
 - Rabi-couples axial with other mode
 - then $\omega_{+/-}$ can be determined via $\omega_{+/-} = \omega_{RF} \pm \omega_l \pm \omega_r \mp \omega_z$



(optimal conditions) $\sigma_{+,SB} \approx 1.46 \text{ ppb} \sim 1/\sqrt{T}$ (avg) @ 180 s

Peak Method ω_+

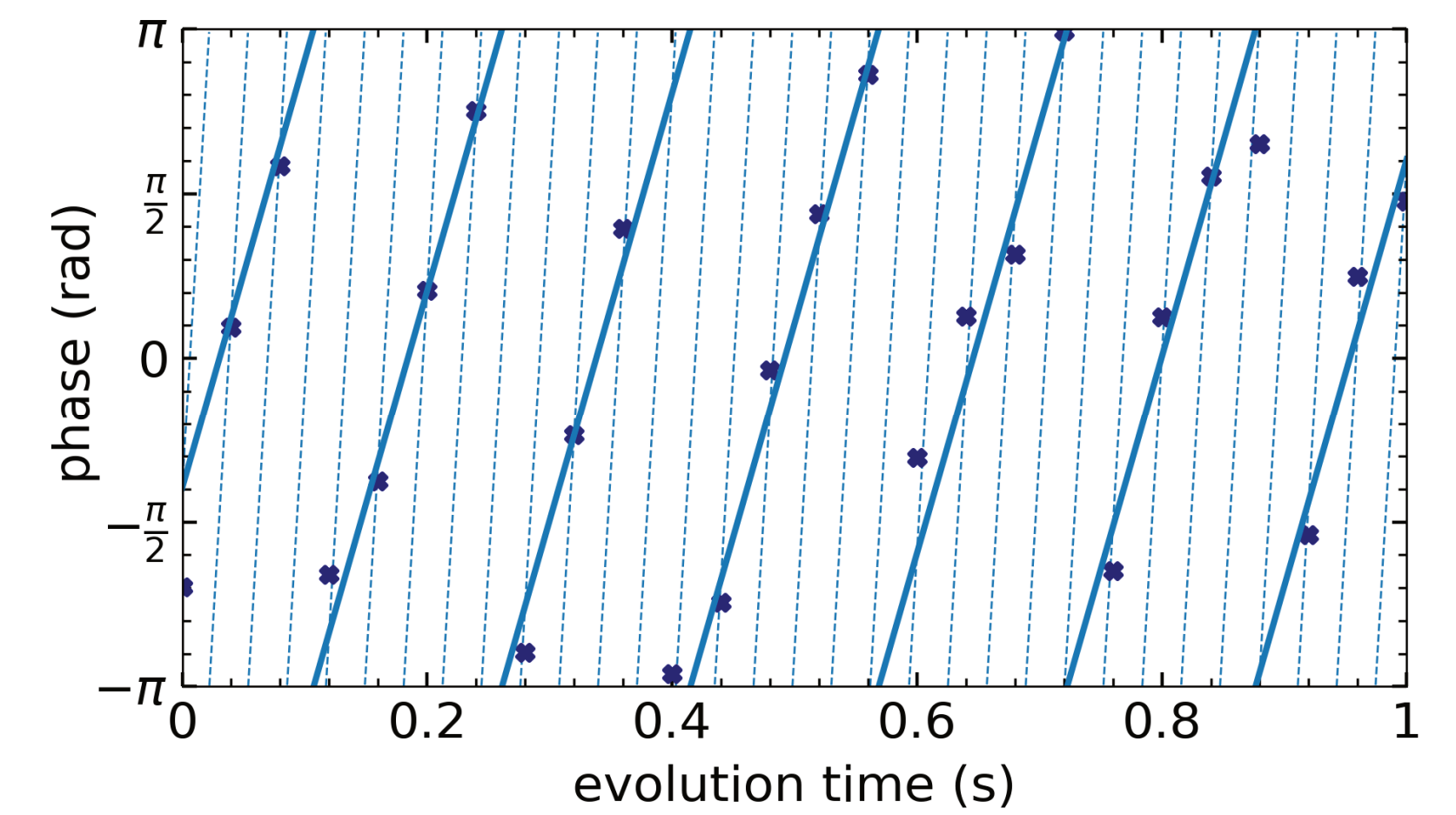
- Cyclotron resonator limited in Q-value, potential dip too thin to detect at $\Delta\omega_{+,dip} \sim 20 \text{ mHz}$, and SNR lower (10 dB) than axial (20 dB)
- Induce peak in LSD by exciting particle on ω_+ resonator
 - $U_{Res} = RI_{\bar{p}} \rightarrow$ stronger signal at resonator resonance frequency
 - advantage: direct measurement
 - problem: inhomogeneous $\vec{B}(\vec{r})$
 - high E_+ \rightarrow high r_+ \rightarrow systematic shifts in ω_+
 - high E_+ \rightarrow high $\sigma(E_+) \rightarrow$ high $\sigma(r_+) \rightarrow$ increased scatter in ω_+
 - recording requires particle energy loss (energy decay exponential)
 - upper limit in single shot FFT timespan



(optimal conditions) $\sigma_{+,PK} \approx 0.5 \text{ ppb} \sim 1/\sqrt{T}$ (avg.) @ 60 s

Phase Method [8] ω_+

- $\Delta\phi = \omega_+ \Delta t$, allowing frequency fit of ω_+ from $\Delta\phi$ information
- Excite particle with from ω_+ detuned resonator, knowing initial phase
- Rabi coupling for $\frac{1}{2}T_{Rabi} \sim \sqrt{P_{RF}}$ imprints ω_+ phase onto ω_z phase
- Axial phases are able to be determined via FFT of decaying axial peak
- Advantages: method allows long particle evolution at constant E_+
- Problems / limits:
 - initial phase scatter from cyclotron excitation procedure
 - systematic frequency shifts from high energy cyclotron mode
 - frequency drifts due to magnetic field drift
 - frequency aliasing due to limited sampling frequency span f_s

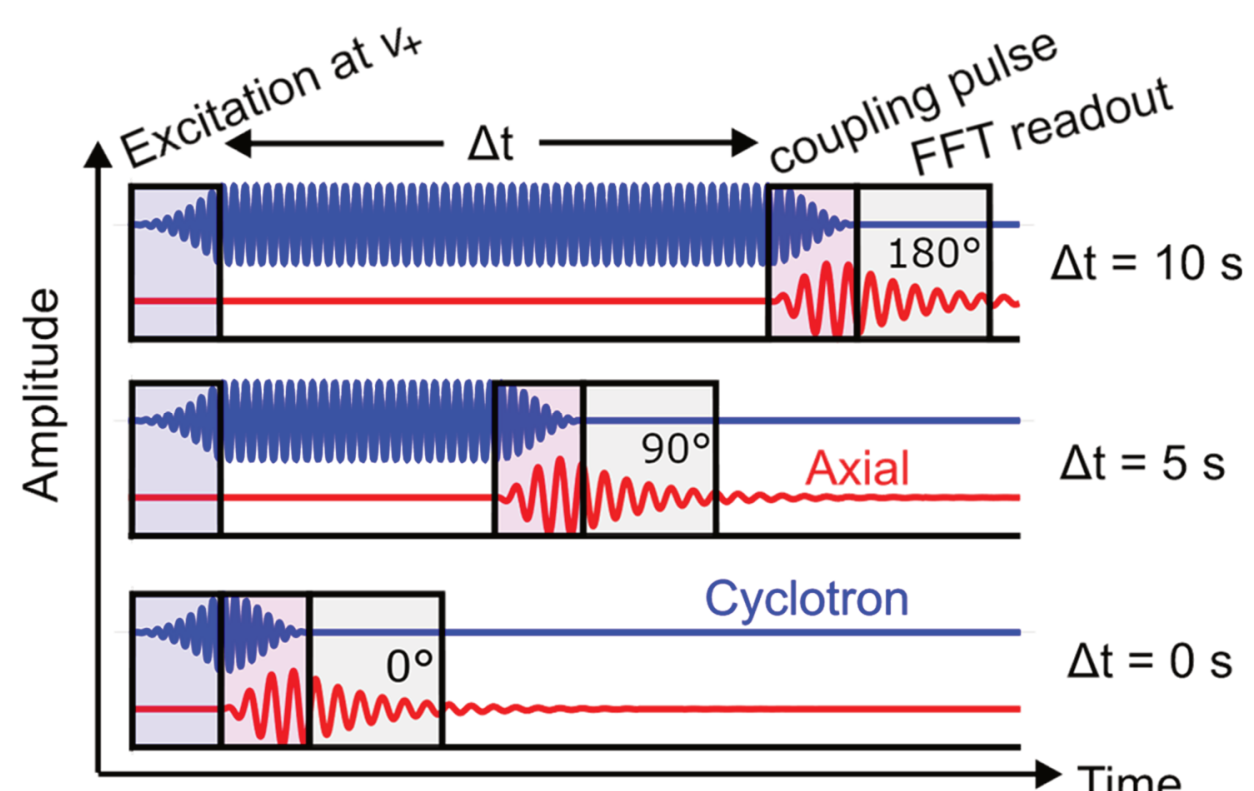


(optimal conditions) $\sigma_{+,PK} \approx 0.24 \text{ ppb} \sim 1/T$ (evolve) [6]
(current progress) $\sigma_{+,PK} \approx 3 \text{ ppb}$ (AD limited)

Considerations in Phase Method Implementation

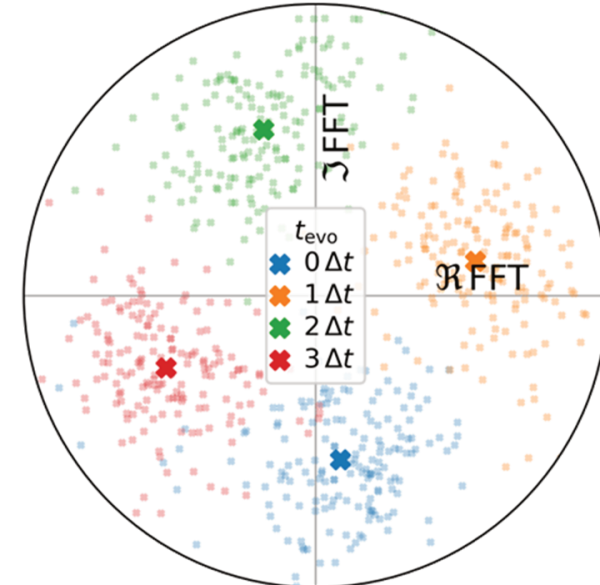
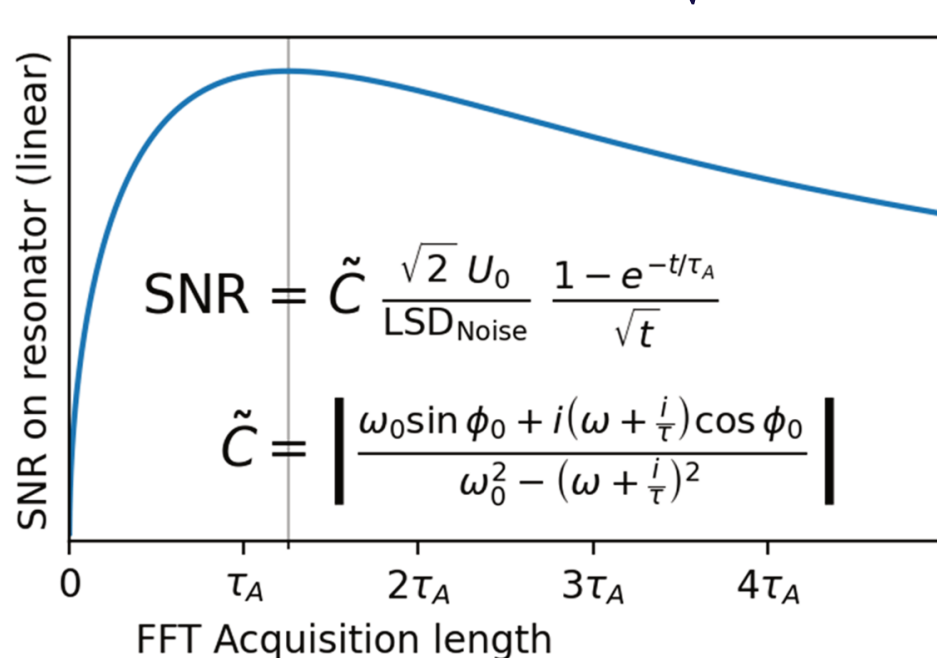
Timing Sequence

- excite ω_+ , evolve, couple at $\omega_+ - \omega_z$, acquire, cool
- $\phi(t_{evo}) = \omega_+ t_{evo} + \phi_0$ (ϕ_0 unknown, but constant)
- locked phases $\rightarrow 1/T_{pulse} | f_{L,O}, 1/T_{pulse} | f_{S,FFT}$



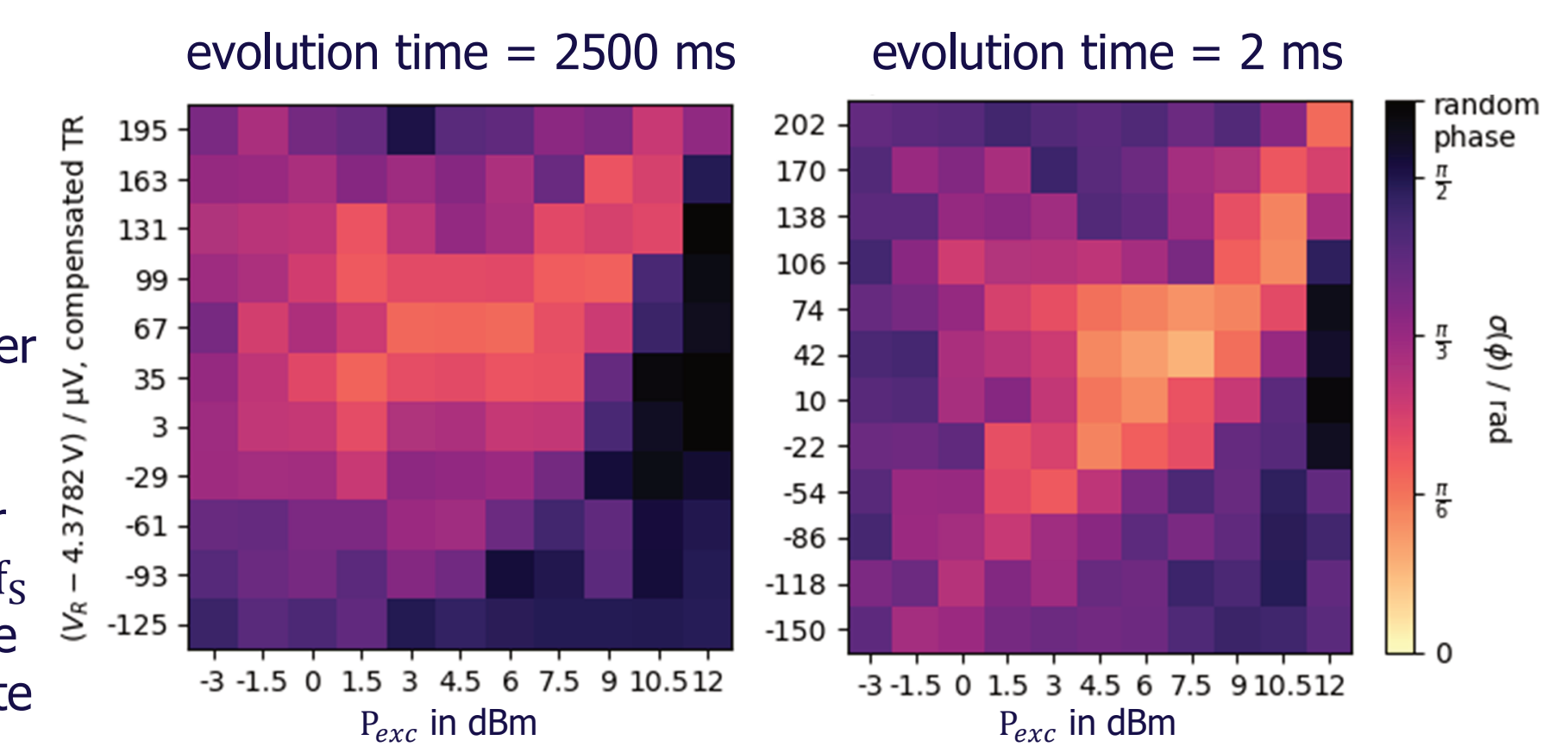
FFT Acquisition

- axial signal decays exponentially, noise const.
 - $\tau_A = 180 \text{ ms} \rightarrow t_{opt} = 225 \text{ ms} \approx 256 \text{ ms}$
 - expected maximum SNR of approximately 5
- unwindowed FFT minimizes NENBW
- axial peak centered in one bin for maximum SNR
- SNR proportional to $\sqrt{f_s}$



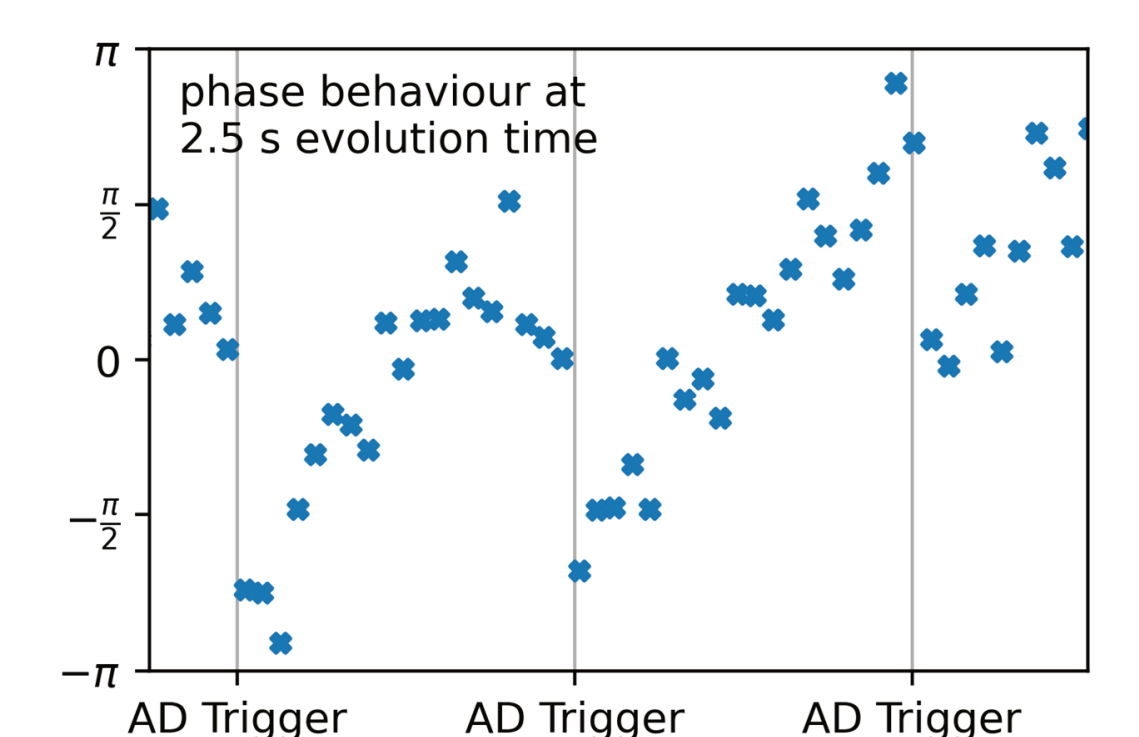
Optimizations

- in optimized 5-pole penning trap, TR determined in advance and $V_r = V_r(f_{z,resonator}, TR)$
- scan TR around canonical point to minimize phase scatter
- $X(z) = X_0 + X_1 z + X_2 z^2 + X_3 z^3 \dots$ compensated B_1, B_2, \dots and $\Phi_1, \Phi_3, \Phi_4, \dots$ minimizes phase scatter
- FFT acquisition start, length and f_s
- decreasing particle cool drive time increases phase measurement rate



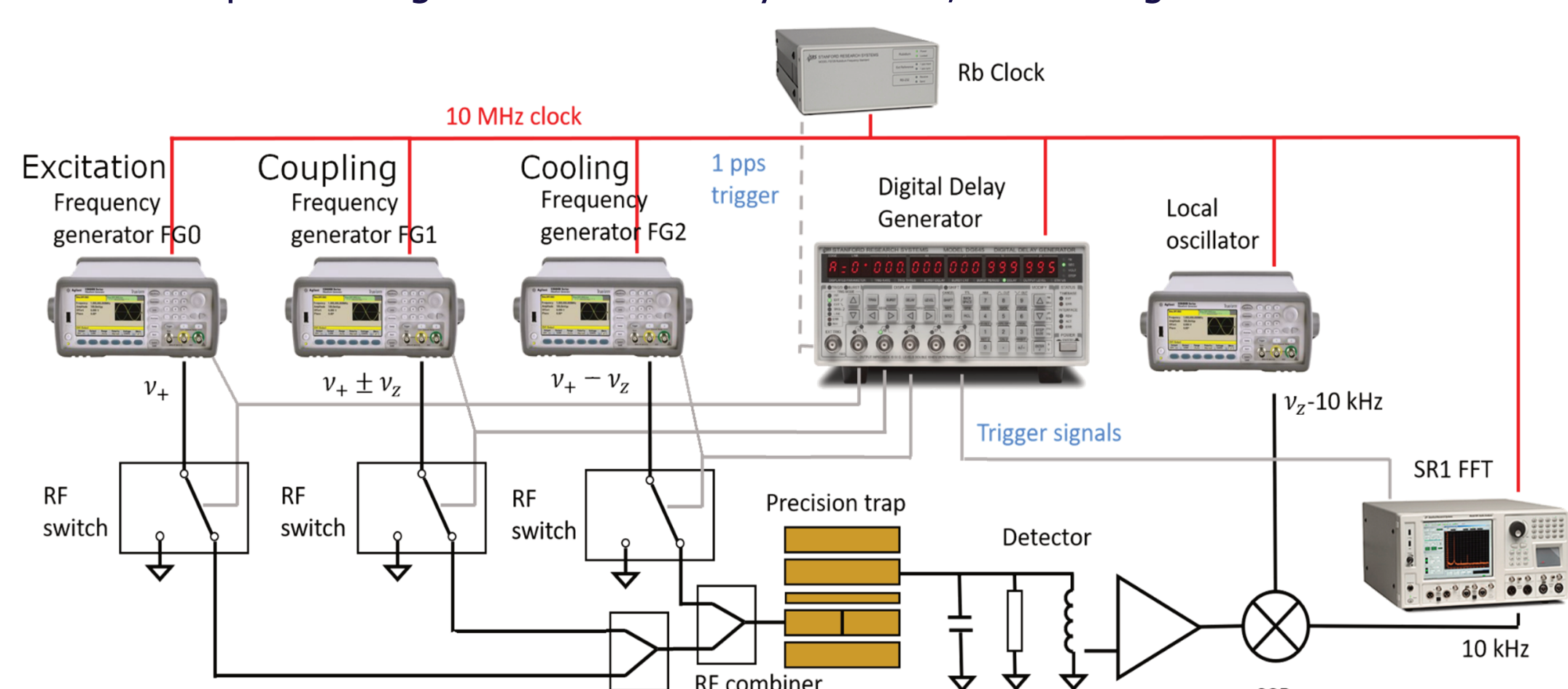
Limits

- systematic ω_+ shifts from $B_1, B_2, \dots \neq 0$
 - increases at higher E_+
- phase scatter after excitation $\sigma(E_+) \approx \sqrt{2E_{+,exc} E_+}$
 - increases with initial T_+ and $B_1, B_2, \dots \neq 0$
- acquisition noise phase scatter
 - decreases at higher E_+ and increases for $\Phi_1, \Phi_3, \Phi_4, \dots \neq 0$ due to axial peak broadening
- Magnetic Field Drift $\sim 40 \text{ ppb/day}$
- AD magnet ramping $\sim 400 \text{ ppb/min}$ when on!
 - repeating variations in measured phase currently limiting phase meas. to $\approx 3 \text{ ppb}$



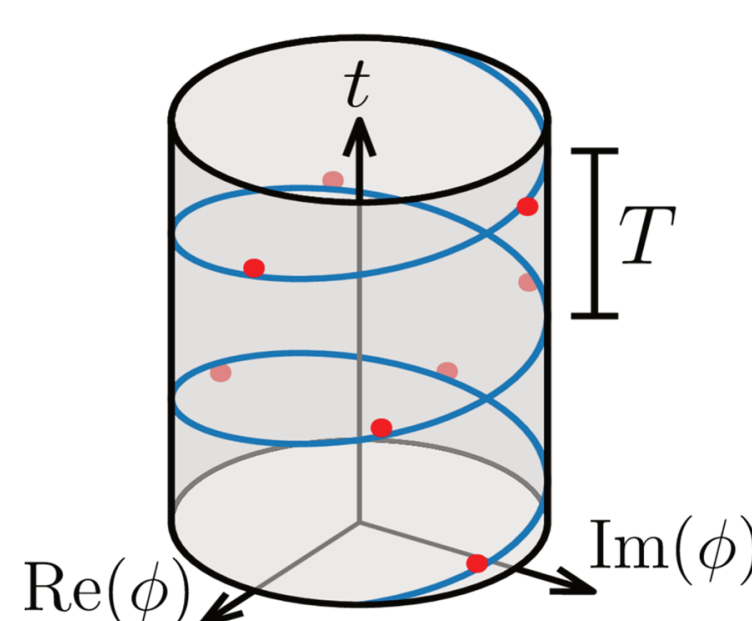
Implementation Diagram

- all instruments referenced to high precision Rb clock to avoid phase drifts
- drive outputs both gated and externally switched, minimizing crosstalk



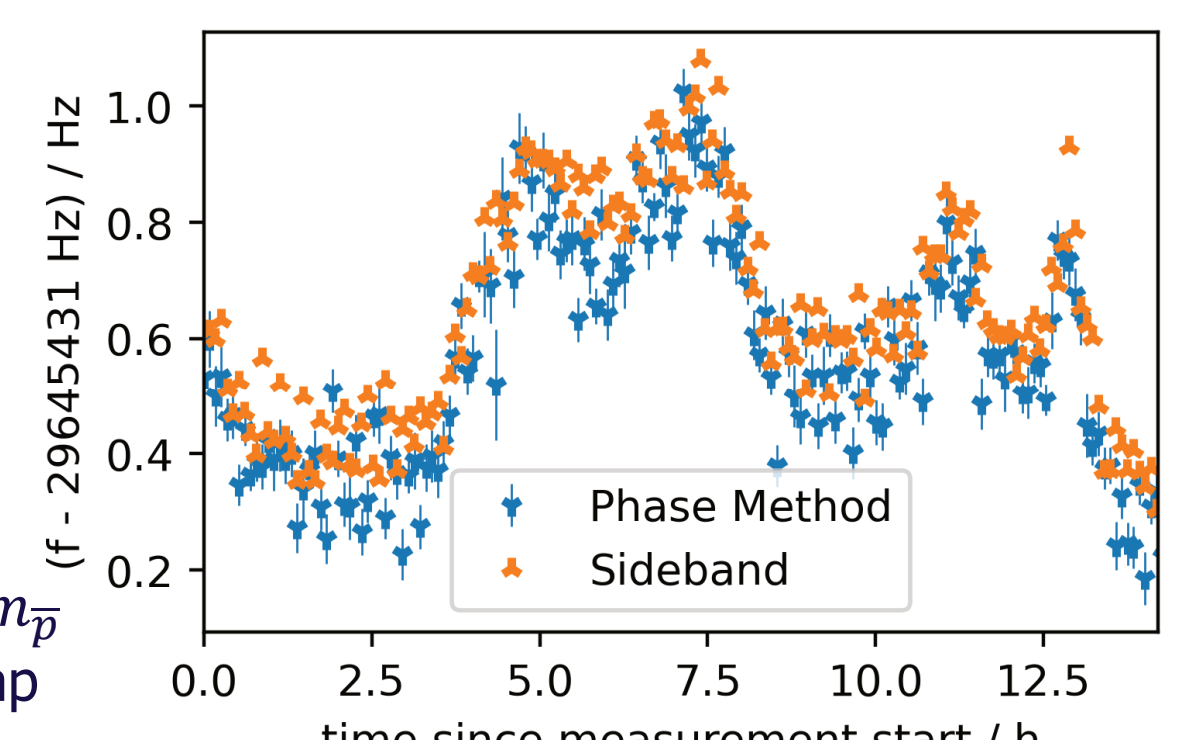
Phase Unwrapping

- $\phi \in \mathbb{R}/2\pi\mathbb{Z} \neq \mathbb{R} \rightarrow$ phase jumps
- remove jumps by unwrapping
 - unstable at low phase SNR
- Solution: treat phases in C
- Direct helix fit is susceptible to convergence into local minima
 - FFT for init. ω_+ estimation



Outlook

- upper SB coupling at $\omega_+ + \omega_z$ for increased SNR at the cost of even larger systematics (PnA [7])
- systematic corrections to reach consistency with sideband and peak methods
- subsequent improved measurements of g & $q\bar{p}/m\bar{p}$
- direct axial phase methods in high- B_2 analysis trap



References

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 [7] S. Sturm et al., PRL **107**, 143003 (2011)
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Acknowledgements

Financial support by RIKEN, the Max Planck Society, CERN, HHU Düsseldorf, Mainz, Hannover, Heidelberg, PTB Braunschweig, DFG, and the Max-Planck/RIKEN/PTB Center for Time, Constants and Fundamental Symmetries

