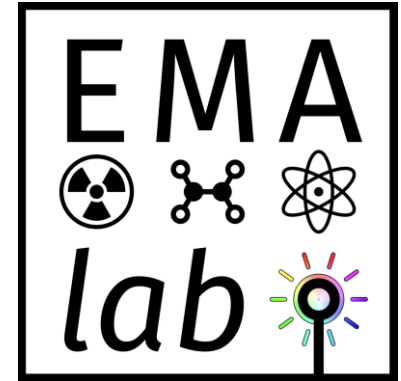
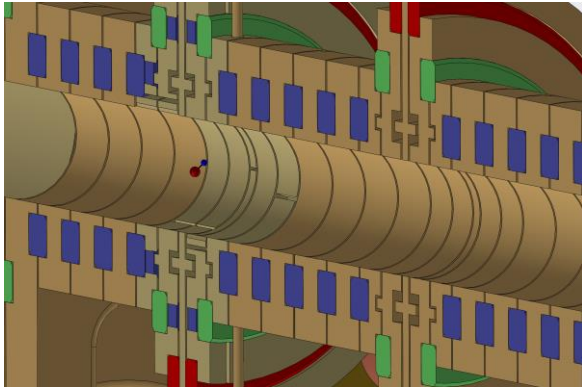


Measuring Electroweak Nuclear Properties using a Single Molecule in a Penning Trap

Scott Moroch— MIT Department of Physics

ECCTI Conference — 08/07/24



- Motivation
- Probing Electroweak Nuclear Structure using Molecules
- NEPTUNE project at MIT
- Status and Outlook

- **Motivation**
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$$H = H_S + H_{EM} + H_W$$

$\sigma(10^{-6})$

Electroweak Structure of Nuclei

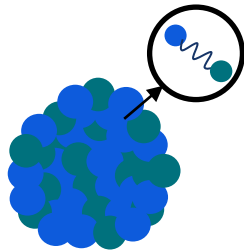


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Nuclear Physics

Electroweak effects have been measured only in a single system (Cesium) with low precision



P-odd forces

Single atomic measurement in tension with accelerator experiments

Electroweak Structure of Nuclei

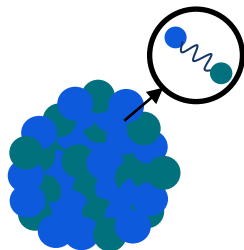


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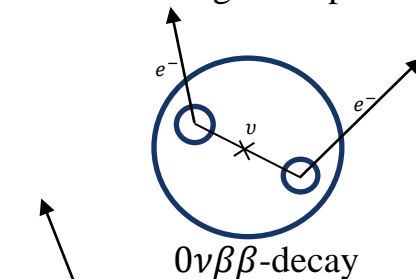


P-odd forces

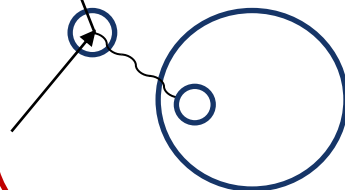
Single atomic measurement in tension with accelerator experiments

New Physics Searches

Electroweak forces are critical for understanding BSM processes



$0\nu\beta\beta$ -decay



WIMP Detection

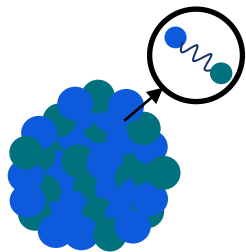
Electroweak Structure of Nuclei



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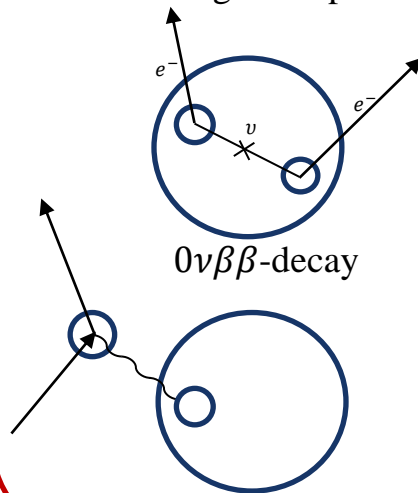


P-odd forces

Single atomic measurement in tension with accelerator experiments

New Physics Searches

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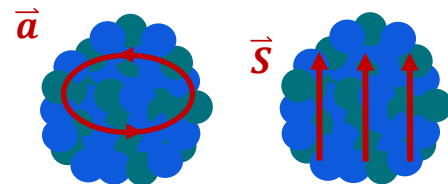


WIMP Detection

Fundamental Symmetries

CP violation is a critical ingredient to understand the observed matter – antimatter asymmetry

$$H_W = H_{PV} + H_{CPV} + ?$$



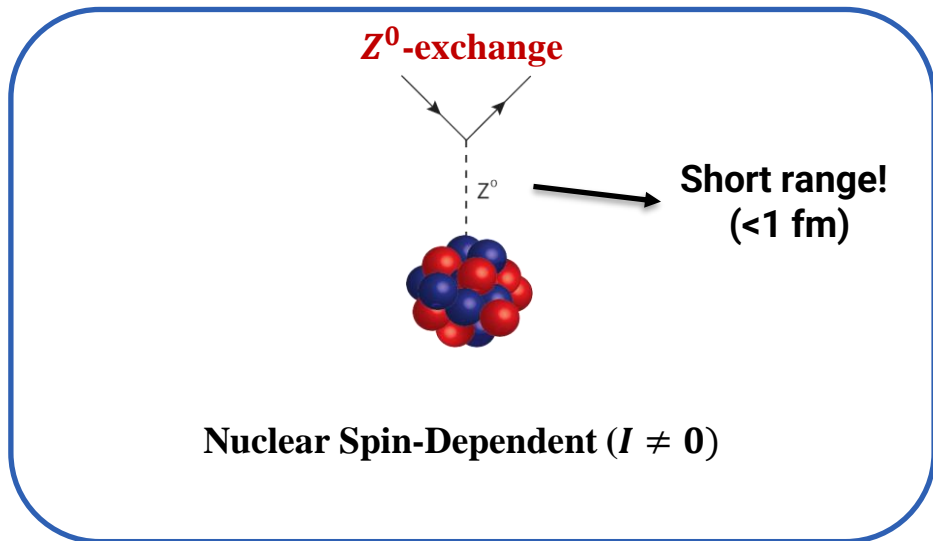
P-odd forces

CP-odd forces

Searches for new sources of CP violation

Weak Interaction in Atomic System

- Weak Interaction in atomic/molecular systems arises from two dominant contributions

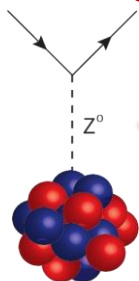


Weak Interaction in Atomic System



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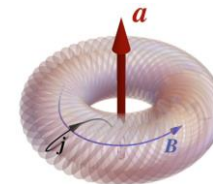
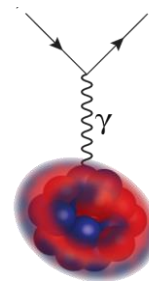
Z^0 -exchange



**Short range!
(<1 fm)**

Nuclear Spin-Dependent ($I \neq 0$)

Nuclear Anapole Moment



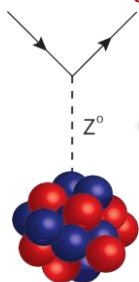
Nucleon-nucleon, weak interactions within the nucleus give rise to a toroidal magnetic field

Weak Interaction in Atomic System



- Weak Interaction in atomic/molecular systems arises from two dominant contributions

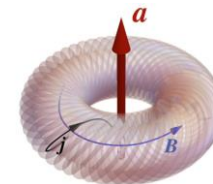
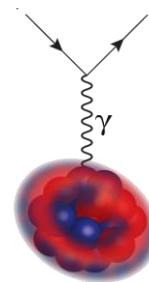
Z^0 -exchange



Short range!
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Nuclear Spin-Dependent ($I \neq 0$)

Nuclear Anapole Moment



Nucleon-nucleon, weak interactions within the nucleus give rise to a toroidal magnetic field

$$H \sim (\eta_Z + \eta_{NAM}) \vec{\alpha} \cdot \vec{I} \delta^3(\vec{r})$$

$$\downarrow \sim A^{2/3}$$

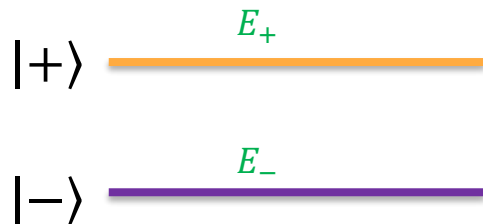
Figure from: M. S. Safronova, et. al. Rev. Mod. Phys., 90:025008, Jun 2018.

- Motivation
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Weak-Induced State Mixing

- Consider any system in the absence of the Weak Interaction

The eigenstates of the Hamiltonian are states of **well-defined Parity**



$$H = \begin{pmatrix} E_- & 0 \\ 0 & E_+ \end{pmatrix}$$

Weak-Induced State Mixing

Consider this system in the presence of the **Weak Force**

Weak Force violates parity: $H(\vec{r}) \neq H(-\vec{r})$

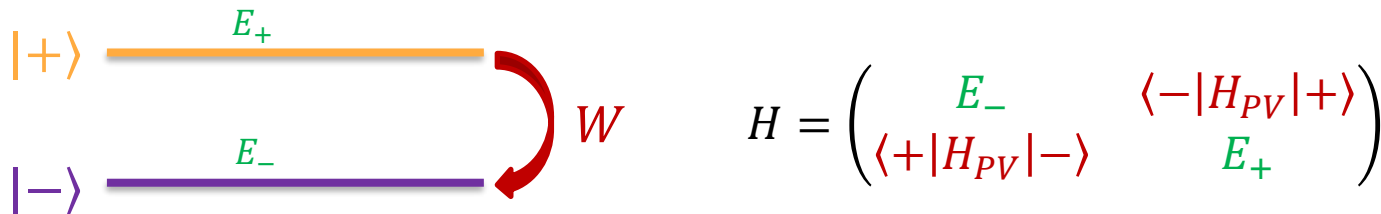
The eigenstates of the Hamiltonian are **not** states of well-defined Parity

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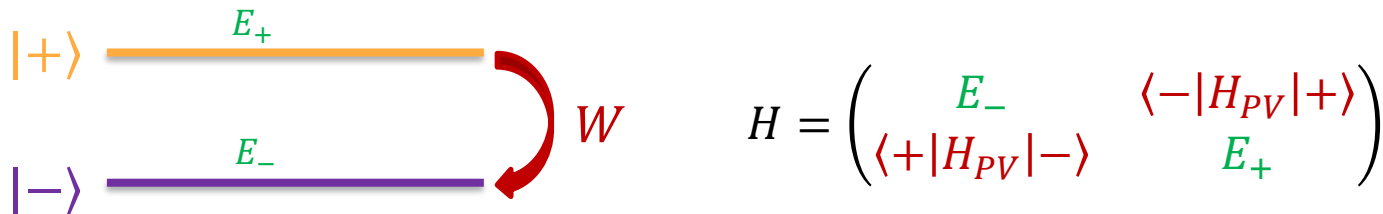


Weak-Induced State Mixing

Consider this system in the presence of the **Weak Force**

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The eigenstates of the Hamiltonian are **not** states of well-defined Parity



Perturbation theory

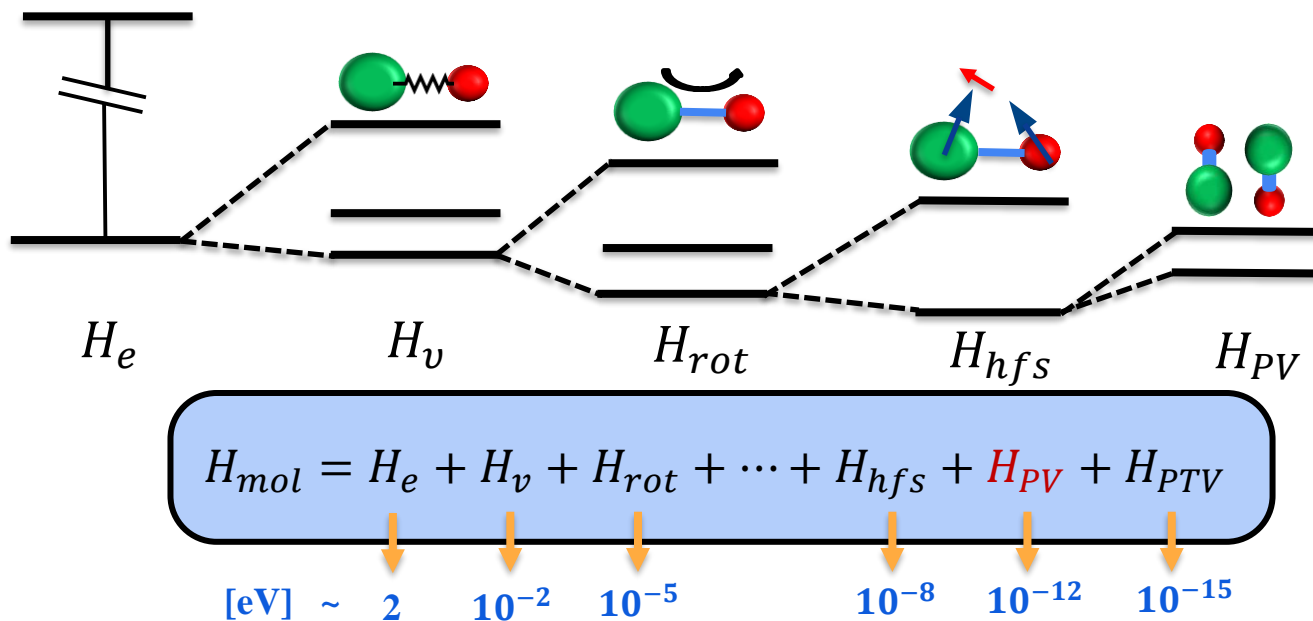
$$|+\prime\rangle = |+\rangle + \frac{\langle + | H_{PV} | - \rangle}{E_+ - E_-} |-\rangle$$

Mixing: $\frac{1}{\Delta}$

We want a system with a small Δ !

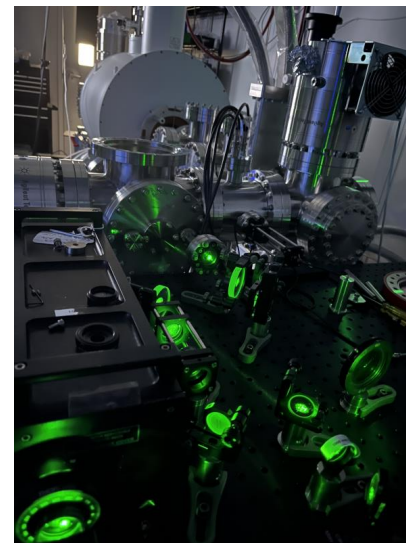
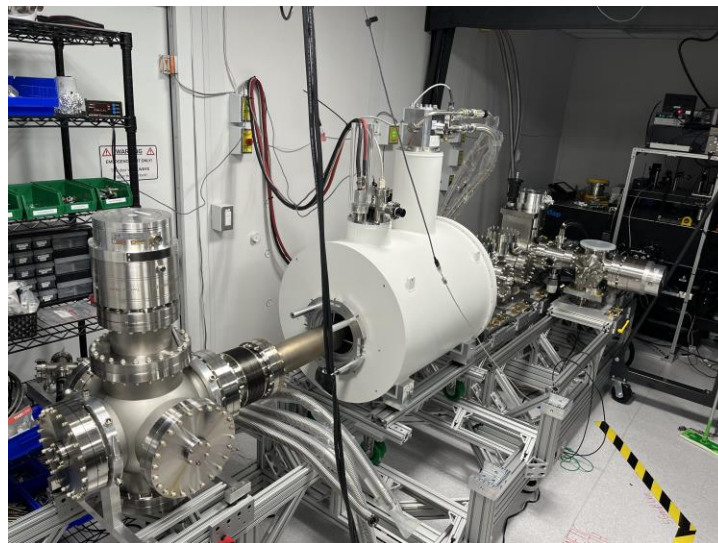
Why Molecules?

- Small energy splitting between rotational levels in a molecule → five order of magnitude enhancement to PV effects, relative to atoms



- Motivation
- Probing Electroweak Nuclear Structure using Molecules
- **NEPTUNE project at MIT**
- Status and Outlook

Nuclear Electroweak Measurements in a Penning Trap Using Near-Degenerate Energy States of Molecules



Accepted Paper

Electroweak nuclear properties from single molecular ions in a Penning trap

Phys. Rev. Lett.

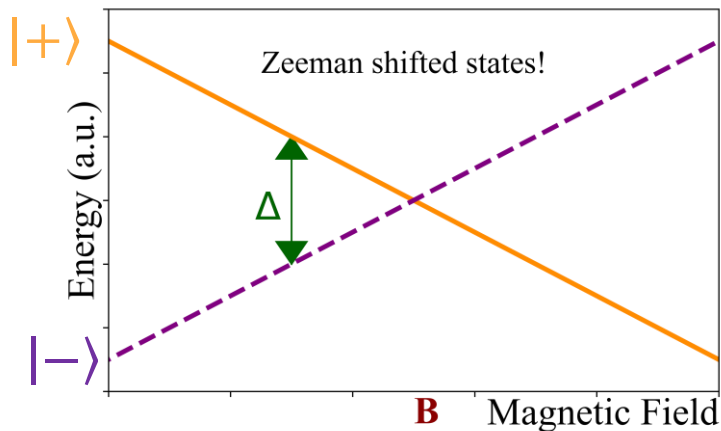
J. Karthein, S. M. Udrescu, S. B. Moroch, I. Belosevic, K. Blaum, A. Borschevsky, Y. Chamorro, D. DeMille, J. Dilling, R. F. Garcia Ruiz, N. R. Hutzler, L. F. Pařteka, and R. Ringle

Accepted 18 April 2024

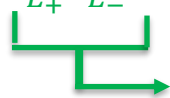
Measurements in a Penning Trap



Zeeman Shifting Molecular States



$$|+\prime\rangle = |+\rangle + \frac{\langle +|H_{PV}|- \rangle}{E_+ - E_-} |-\rangle$$

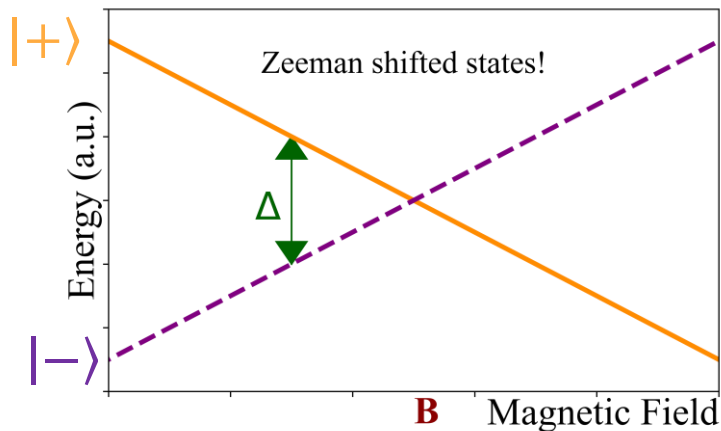


10^{11} enhancement
of PV effects in
Molecules!

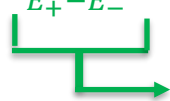
Measurements in a Penning Trap



Zeeman Shifting Molecular States



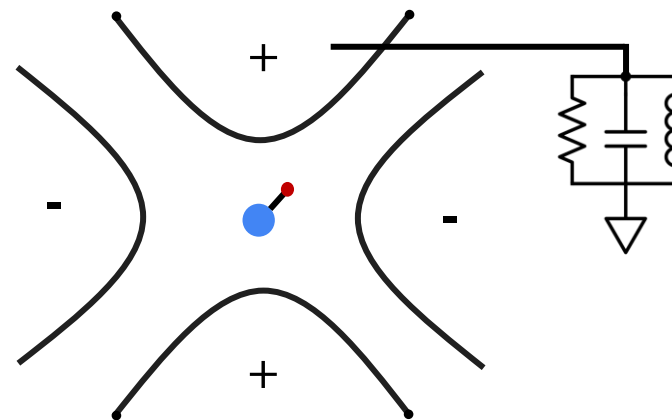
$$|+' \rangle = |+\rangle + \frac{\langle + | H_{PV} | - \rangle}{E_+ - E_-} |-\rangle$$



10^{11} enhancement
of PV effects in
Molecules!

Motional Cooling and Coherence Time

Resistive and sympathetic cooling techniques enable low motional temperatures (≤ 4 K)



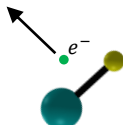
Coherence times of ms, compared to μs in a neutral beam experiment

Experimental Procedure

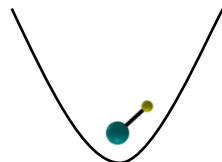
Molecule Formation



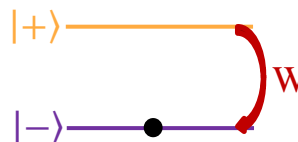
Ionization



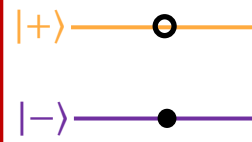
Trapping



Tuning

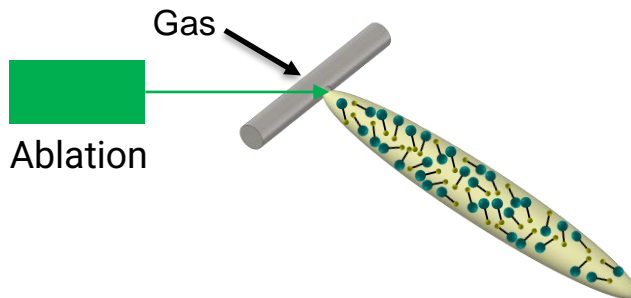


Counting



Molecule Formation

Supersonic expansion molecular source for producing rotationally cold molecules ($N < 20$)



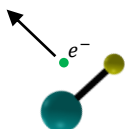
Experimental Procedure



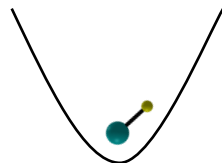
Molecule Formation



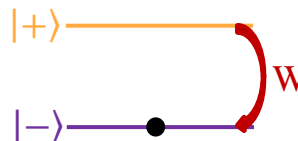
Ionization



Trapping



Tuning

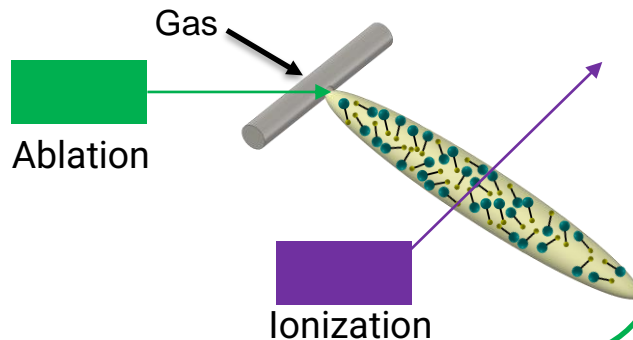


Counting



Resonant Photoionization

Resonantly ionize the molecules using a multi-step process

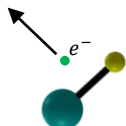


Experimental Procedure

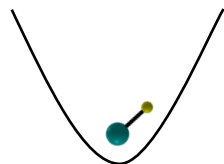
Molecule Formation



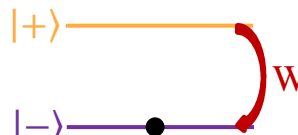
Ionization



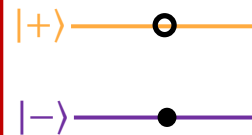
Trapping



Tuning

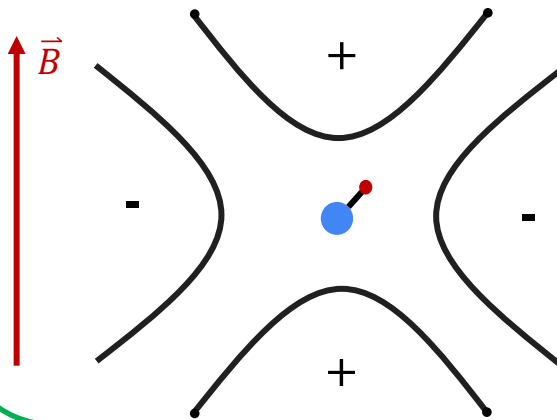


Counting



Trapping

Decelerate, trap and cool the molecules

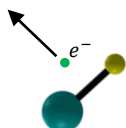


Experimental Procedure

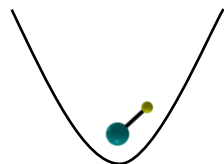
Molecule Formation



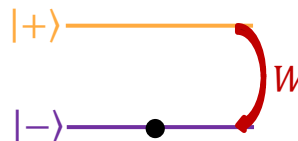
Ionization



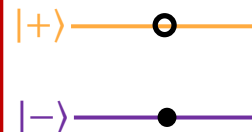
Trapping



Tuning

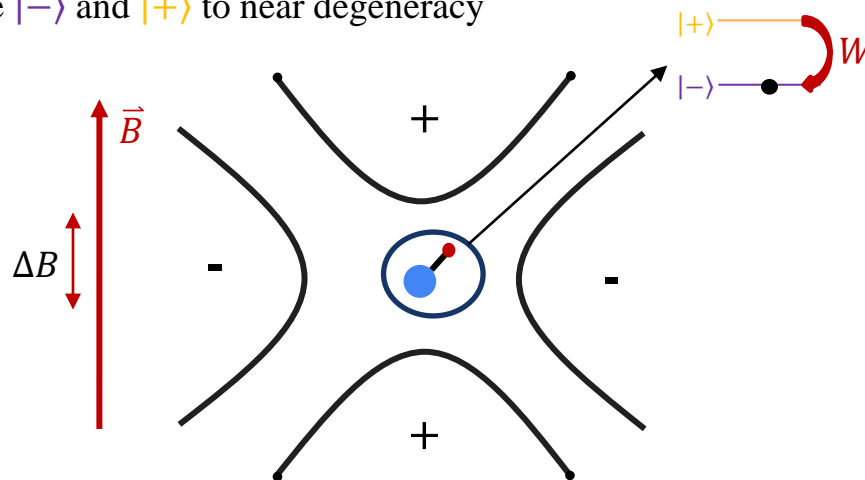


Counting



Tune Levels to Degeneracy

Drive $|- \rangle$ and $|+ \rangle$ to near degeneracy

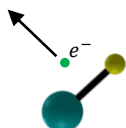


Experimental Procedure

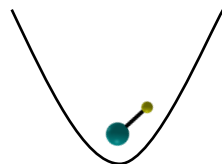
Molecule Formation



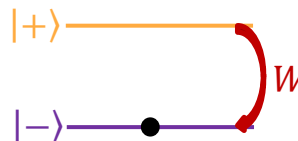
Ionization



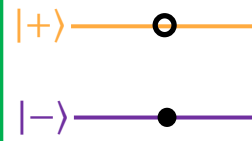
Trapping



Tuning

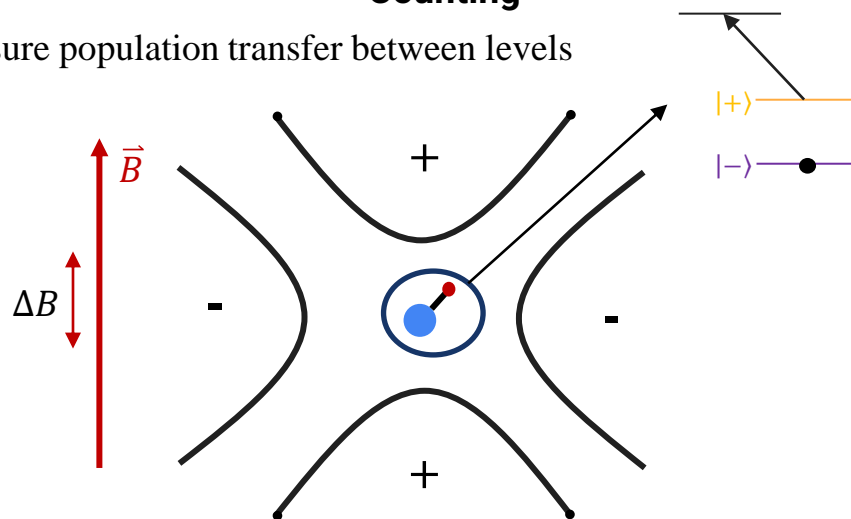


Counting



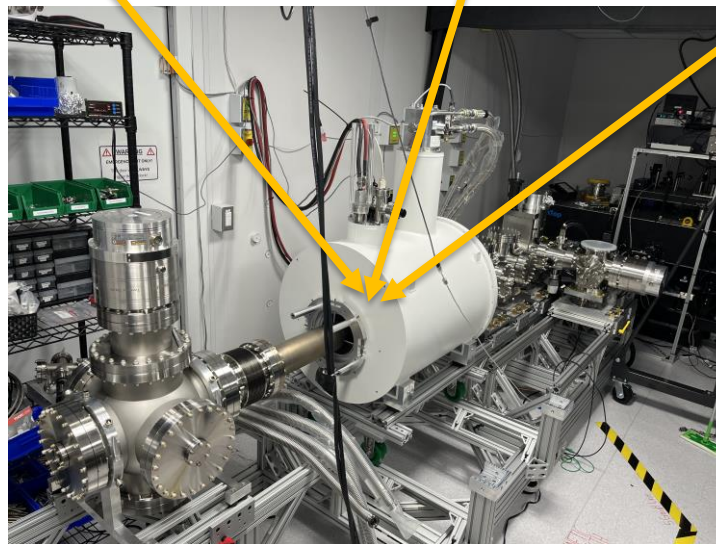
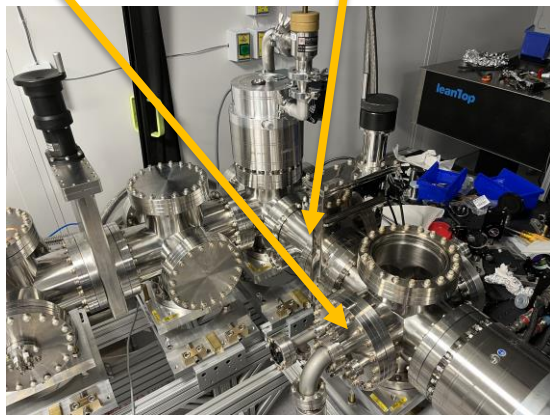
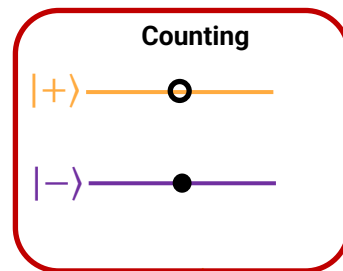
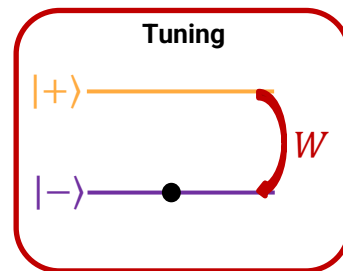
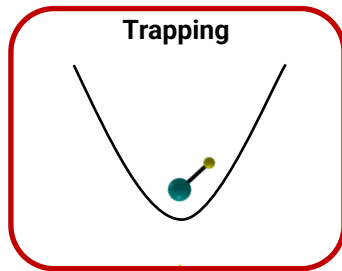
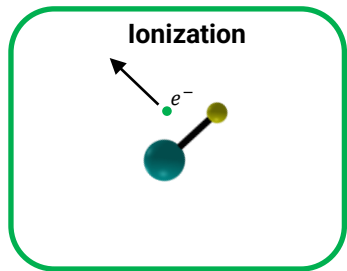
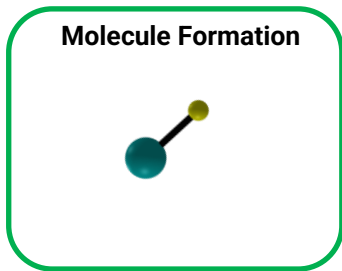
Counting

Measure population transfer between levels

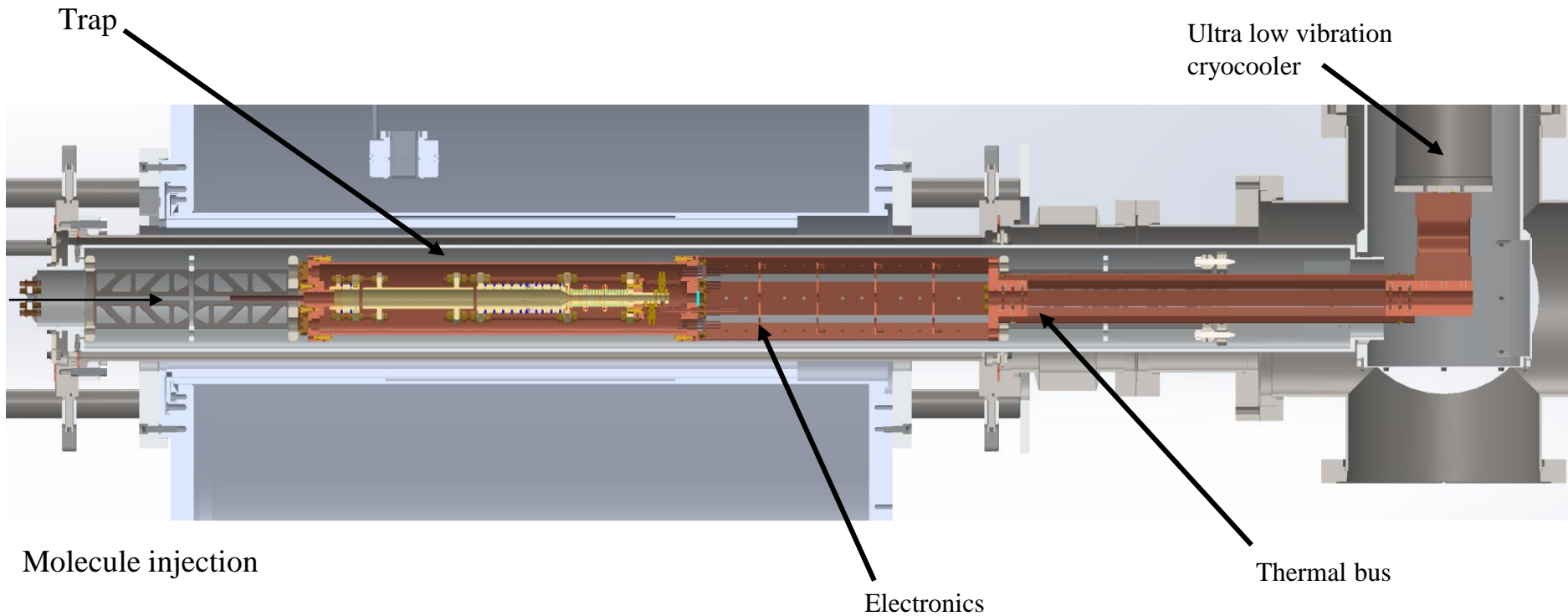


- Motivation
- Probing Electroweak Nuclear Structure using Molecules
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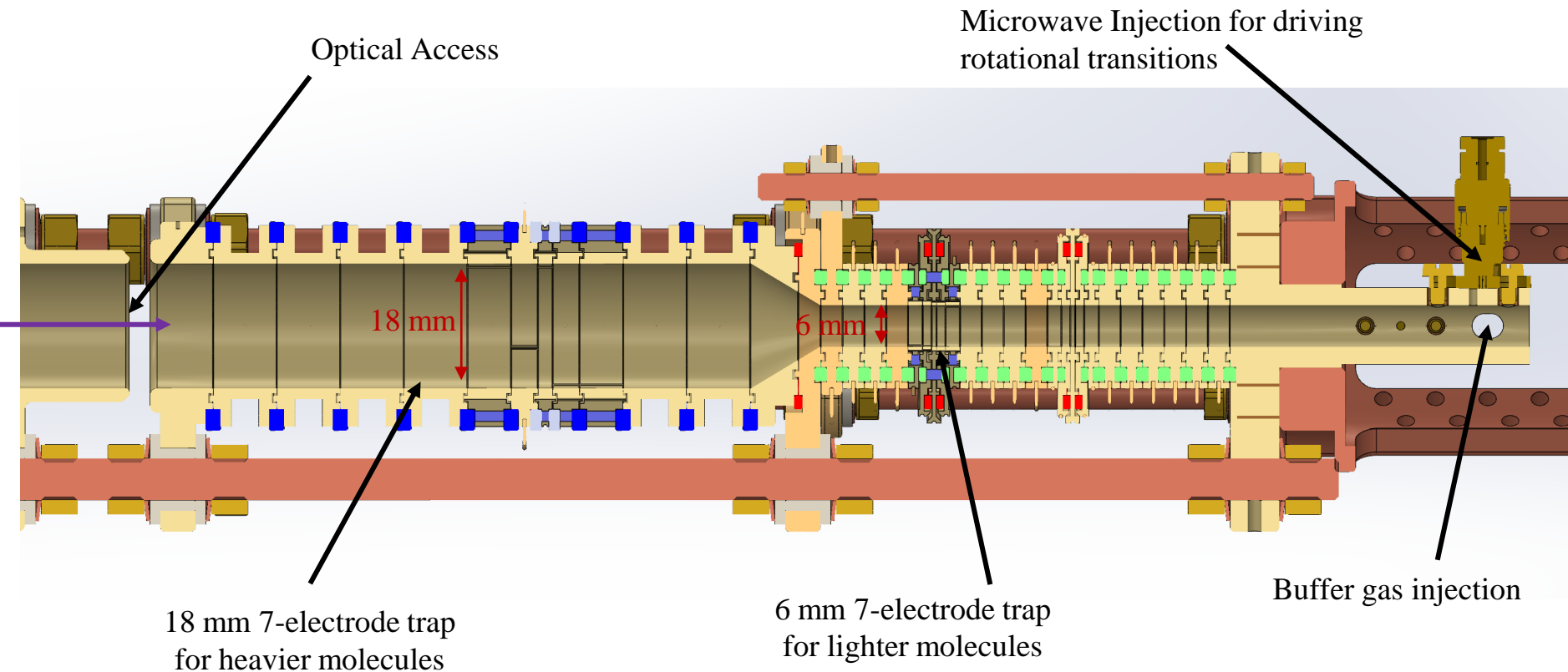
Experiment Status



Penning Trap Design



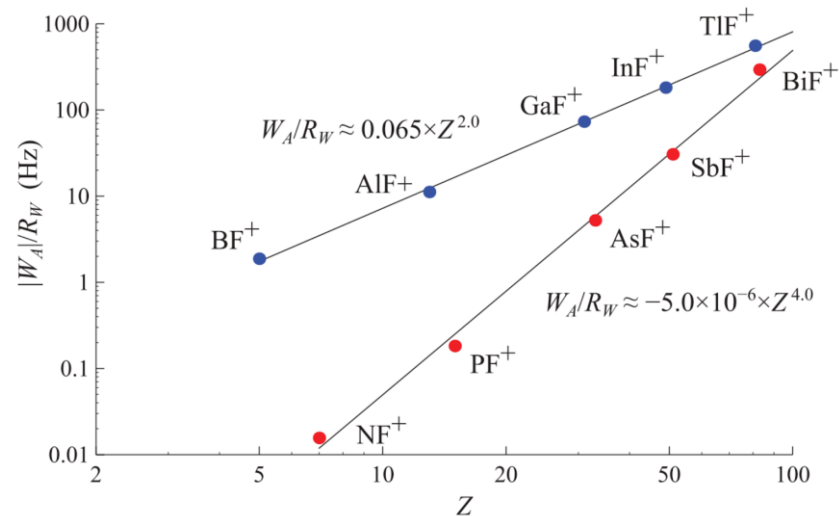
Penning Trap



Future Outlook



- To extract nucleon-nucleon electroweak interactions – must disentangle different contributions
- Rely on the scaling of different effects and studying in different nuclei
- Once demonstrated the experiment can be implemented at a radioactive ion beam facility
- Generating and cooling single molecular ions is much simpler than neutral molecules



[Borschevsky, A. et al. PRA 86, 050501\(R\) \(2012\).](#)

- Electroweak properties of nuclei are poorly understood
- Molecules are very sensitive to parity-violating electroweak effects due to rotational levels
- We propose the use of a single ion in a Penning trap to measure these effects by the induced mixing between two states
- Experimental procedure is applicable across the nuclear chart

NEPTUNE Collaboration



Prof. Ronald Garcia Ruiz (MIT)



Silviu Udrescu (MIT)



Scott Moroch (MIT)



Haruka Kakioka (MIT)



Dr. Jonas Karthein (MIT)



Prof. David DeMille (UChicago)



Prof. Nick Hutzler (Caltech)



Prof. Jens Dilling (Duke/ORNL)



Prof. Klaus Blaum (MPIK)



Dr. Ryan Ringle (FRIB)



Dr. Xing Fan
(Northwestern/Harvard)

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F. Pastrana



D. Gonzales



J. Munoz



M. Fulghieri



F. Shungo

Postdoctoral Researchers



S. Wilkins



J. Karthein



S. Ebadi



S. Jadbabaie



A. Belly

PI

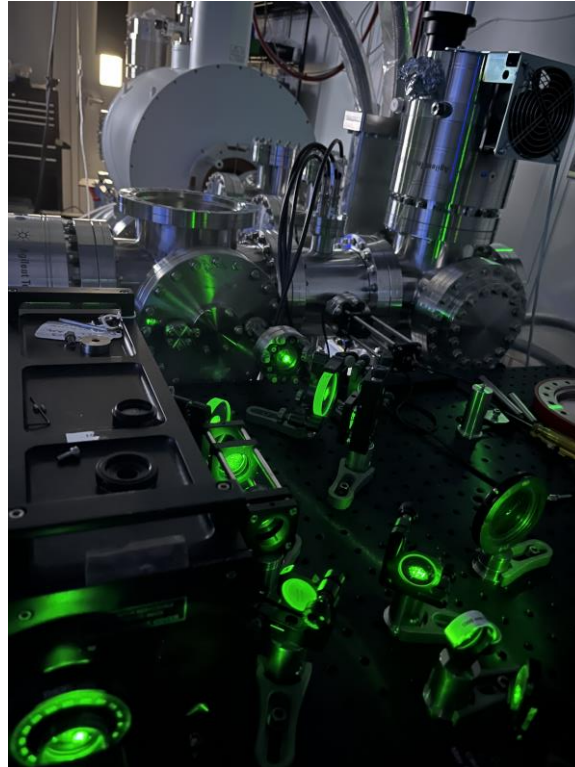


R.F. Garcia Ruiz



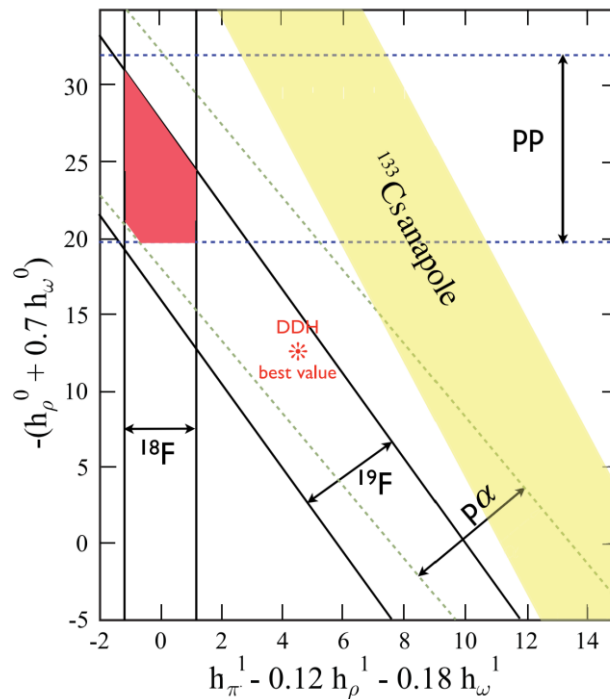
Bates
Lab

Questions?



Backup Slides

Cesium Anapole Measurement



Details on Opposite Parity Mixing



- The QED Lagrangian governing AMO physics commute with P
- Considering this effect alone atoms conserve parity:
 - Easily seen by looking at an electric dipole E1 transition:

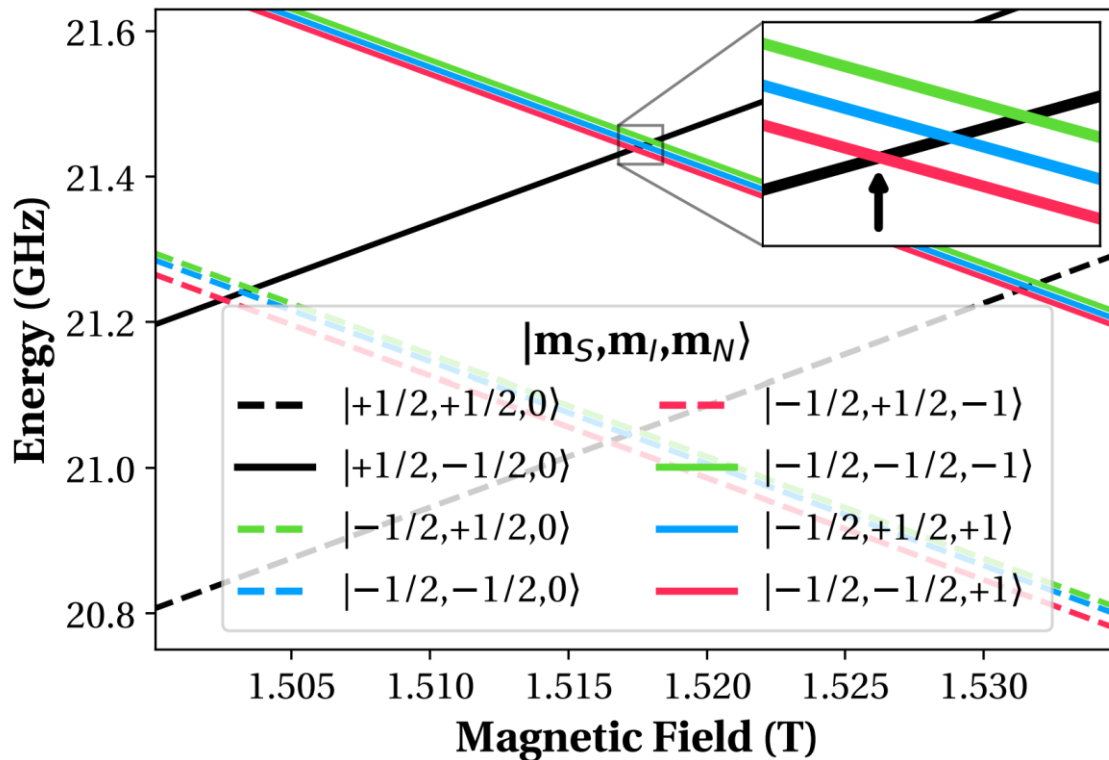
$$T_{fi}^{E1} = \langle \psi_f | D | \psi_i \rangle$$

- Insert the identity: $1 = P^\dagger P$

$$\begin{aligned} T_{fi}^{E1} &= \langle \psi_f | P^\dagger P D | \psi_i \rangle \\ &= -\Pi_f \Pi_i T_{fi}^{E1} \end{aligned}$$

- If the two states have the same parity then $T_{fi}^{E1} = 0$

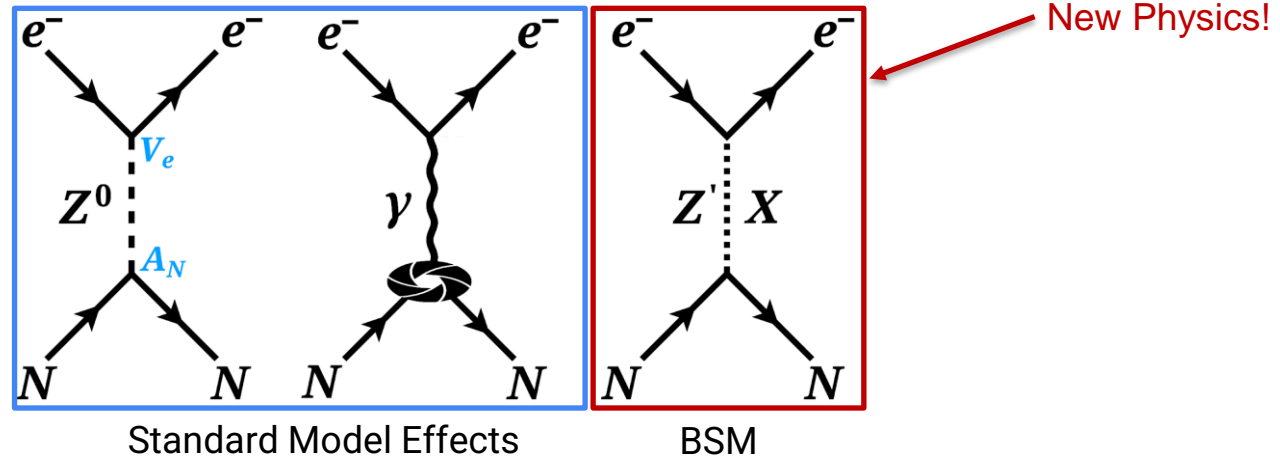
Level Structure



New Force Searches



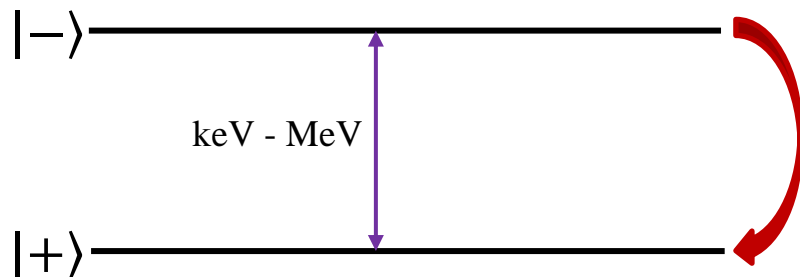
- Access to electroweak coupling parameters – few existing measurements with large uncertainties
- Constrain Standard Model contributions (Z-boson, Anapole moment, etc) – experiment provides avenue for 5th-force searches



NN Weak Interactions - Macroscopic



- The nucleus has excited states and weak interactions will mix these levels



- The Anapole moment emerges as a P-odd moment that can exist only in the presence of this mixing

$$\vec{a} = \langle JM' | \vec{a} | JM \rangle$$

$$\vec{a} = \frac{\langle J | \vec{a} \cdot \vec{J} | J \rangle}{J(J+1)}$$

NN Weak Interactions - Macroscopic



- In the absence of the weak interaction the $|JM\rangle$ states are states of definite parity and $\vec{a} = 0$
- In the presence of the weak interaction these states are mixed:

$$|J\rangle = |J; 0\rangle + \sum_{k \neq 0} \frac{\langle J; k | W | J; 0 \rangle}{E_0 - E_k} |J; k\rangle$$

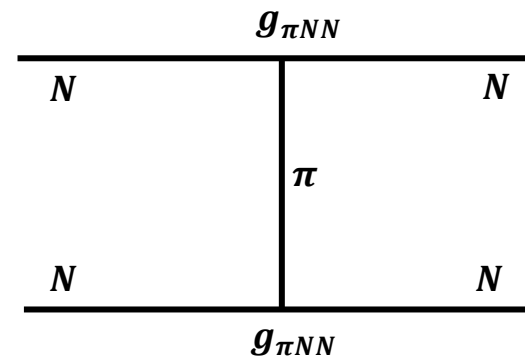
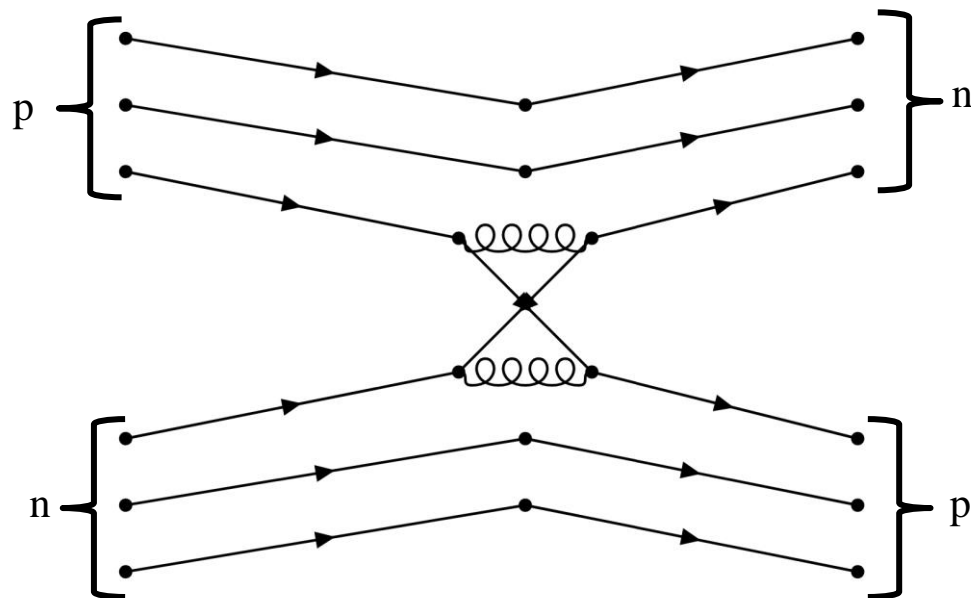
- Now the nucleus can acquire a non-zero anapole moment:

$$\langle a \rangle = 2 \operatorname{Re} \sum_{k \neq 0} \frac{\langle J; 0 | a | J; k \rangle \langle J; k | W | J; 0 \rangle}{E_0 - E_k}$$

NN Weak Interactions - Microscopic



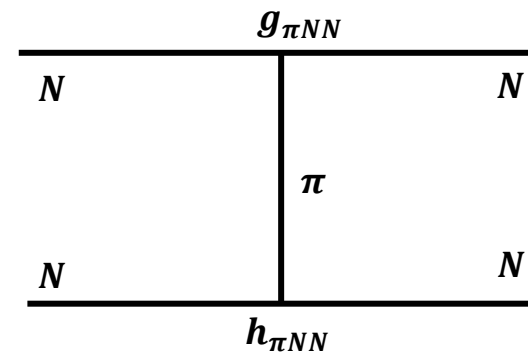
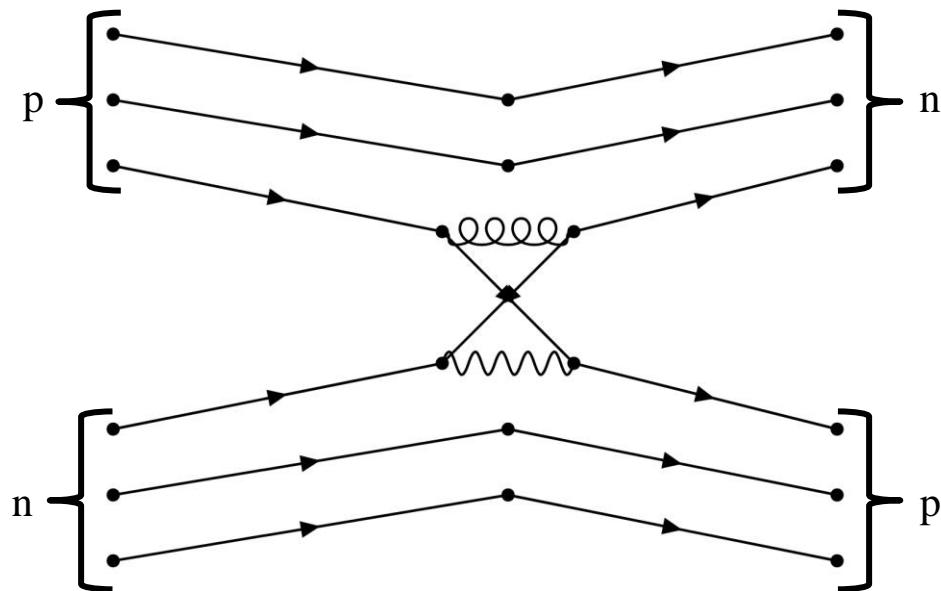
- Microscopically electroweak nuclear interactions arise at the individual quark-level



NN Weak Interactions - Microscopic



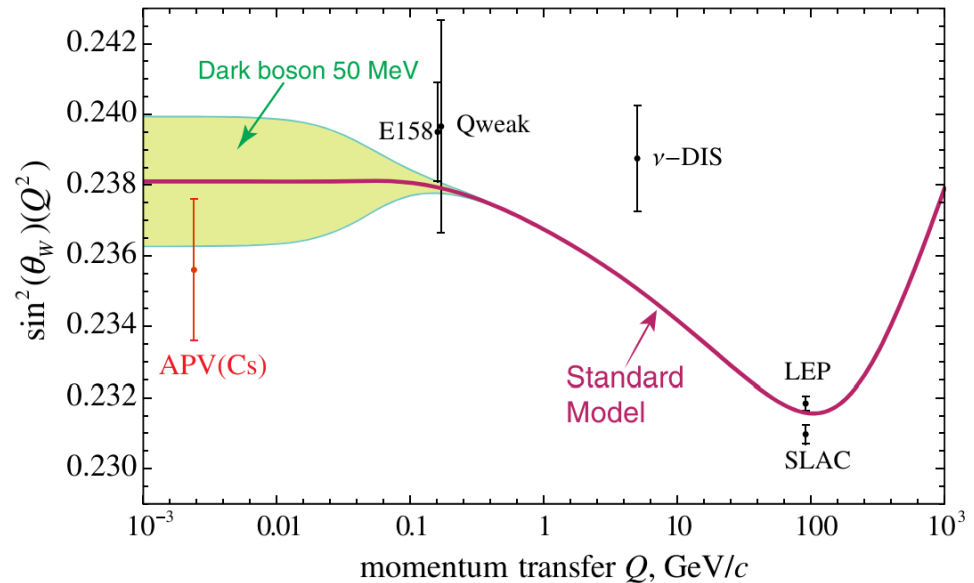
- Microscopically electroweak nuclear interactions arise at the individual quark-level



Nuclear Spin Independent PV



- Nuclear Spin-Independent Parity Violation measurements (Z exchange) in atoms provide a low-energy test of the Standard Model



- Consider the case of Cesium: ground state is $6S_{1/2}$
- Electric dipole transition to excited state of the same parity is forbidden:

$$\langle 6S_{1/2} | D | 7S_{1/2} \rangle = 0$$

- Weak interactions lead to small mixing between states of opposite parity giving a non-zero matrix element (10^{-11}):

$$E_{PV} = \langle \widetilde{6S_{1/2}} | D | \widetilde{7S_{1/2}} \rangle \neq 0$$

- In an interference technique an electric field is added to provide a strong E1 pathway with transition amplitude $\beta\mathcal{E}$
- The transition rate is proportional to the square of the transition amplitude: $E_{PV}^2 + (\beta\mathcal{E})^2 + (\beta\mathcal{E}E_{PV})$
- By reversing the electric field one can extract E_{PV}

- Since the weak interactions are essentially contact interactions we rely on molecular states with strong overlap of the electron with the nucleus
- We consider diatomic molecules with a single valence electron in a $^2\Sigma$ electronic state. This is the molecular equivalent of alkali atoms (in particular a Hund's case b)
- We have one nucleus with non-zero spin ($I = \frac{1}{2}$) that couples to the electron by NSD-PV interaction and a second nucleus with zero spin ($I = 0$)
- Lowest energy levels are described by the Hamiltonian:

$$H = B_e N^2 + \gamma \mathbf{N} \cdot \mathbf{S} + b \mathbf{I} \cdot \mathbf{S} + c (\mathbf{I} \cdot \mathbf{n}) \times (\mathbf{S} \cdot \mathbf{n})$$

- B_e - rotational constant
- γ - Spin-rotation constant
- b/c - Hyperfine constants
- $B_e \gg \gamma, b, c$ so N is a good quantum number and $E_N = B_e N(N + 1)$ and $P = (-1)^N$

- The magnetic field needed to bridge the rotational energy:

$$E_1 - E_0 \approx 2B_e$$

- The magnetic field decouples S, I and N such that the molecular states can be considered in the decoupled basis:

$$|\psi\rangle = |N, m_N\rangle |S, m_S\rangle |I, m_I\rangle$$

- The Zeeman effect is dominated by the coupling to the electron spin:

$$H_Z \cong -g\mu_B S \cdot B$$

- The state of opposite of interest are:

$$|\psi_{\uparrow}^+\rangle = |N = 0, m_N = 0\rangle |S = 1/2, m_S = 1/2\rangle |I = 1/2, m_I\rangle$$

$$|\psi_{\downarrow}^-\rangle = |N = 1, m_N\rangle |S = 1/2, m_S = -1/2\rangle |I = 1/2, m_I'\rangle$$

Rotational Cooling

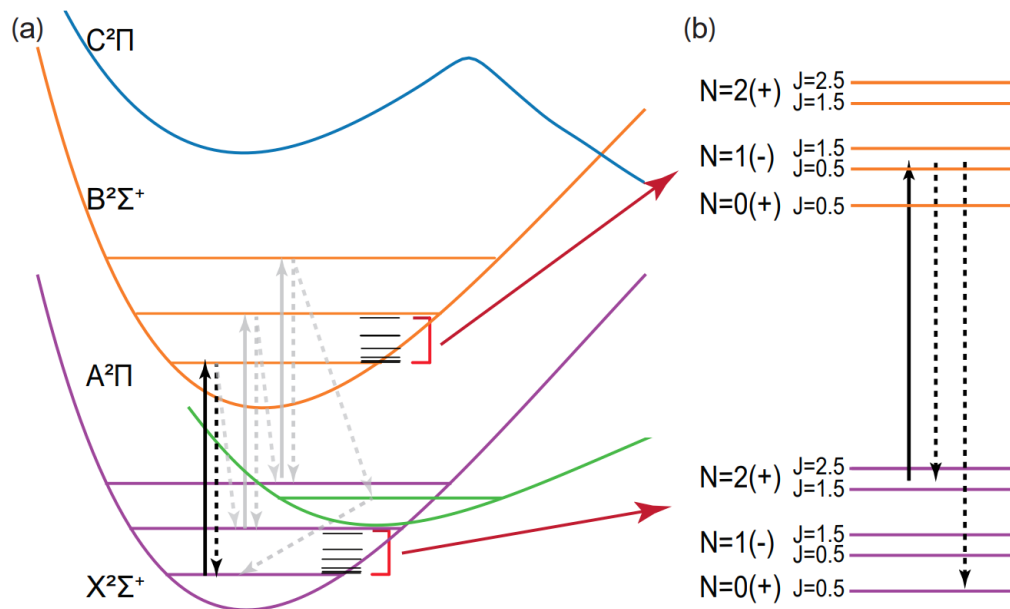


Figure from: Stollenwerk P.R. et al., Phys. Rev. Lett. 125 (2020)