



Snapshotting Quantum Dynamics at Multiple Time Points

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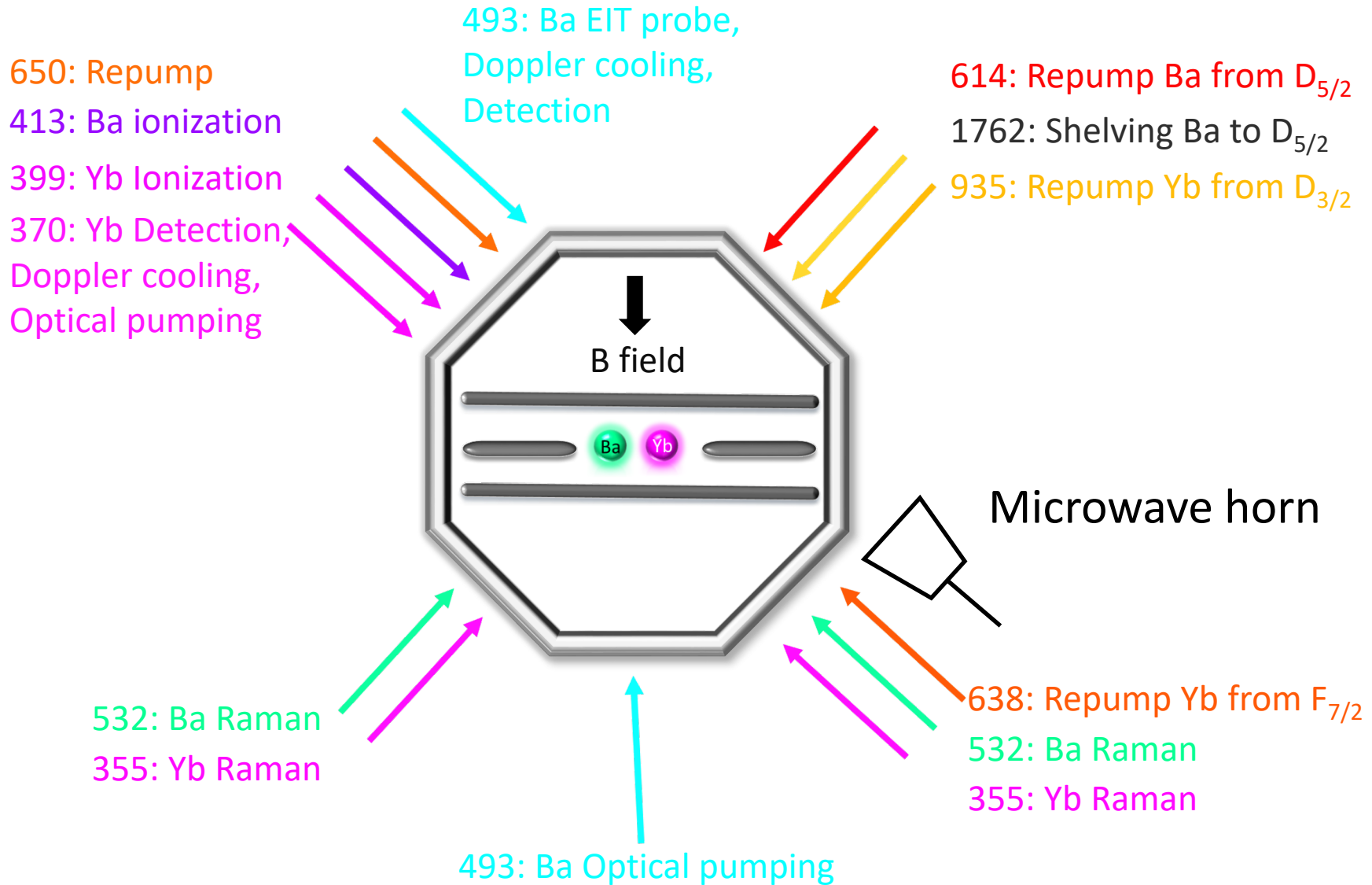
Kihwan Kim's team @ BAQIS

Outline

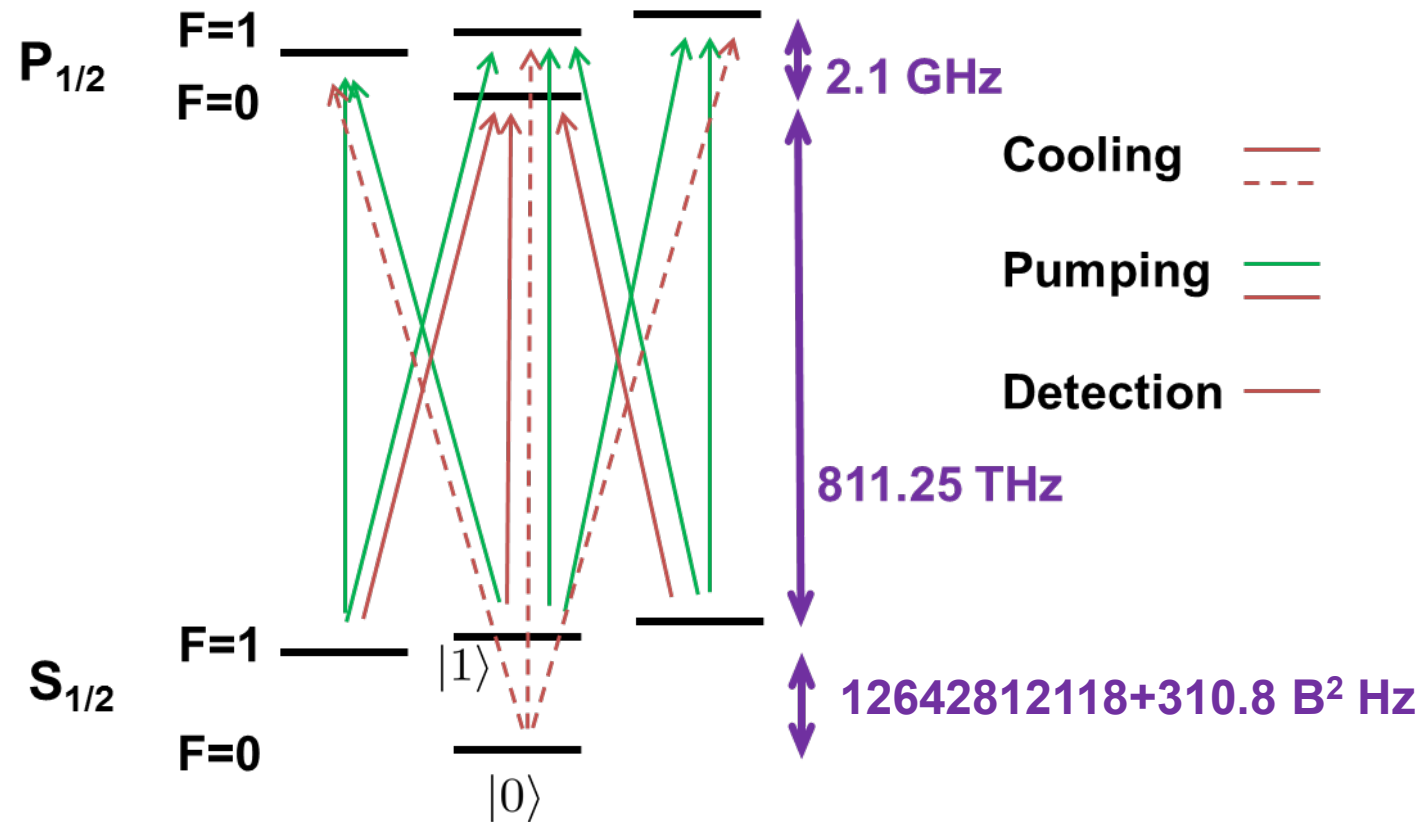
1. $^{171}\text{Yb}^+ - ^{138}\text{Ba}^+$ Ion trap system
2. Snapshotting quantum dynamics at multiple time points
3. Summary

$^{171}\text{Yb}^+ - ^{138}\text{Ba}^+$ ion trap system

$^{171}\text{Yb}^+ - ^{138}\text{Ba}^+$ Ion trap system

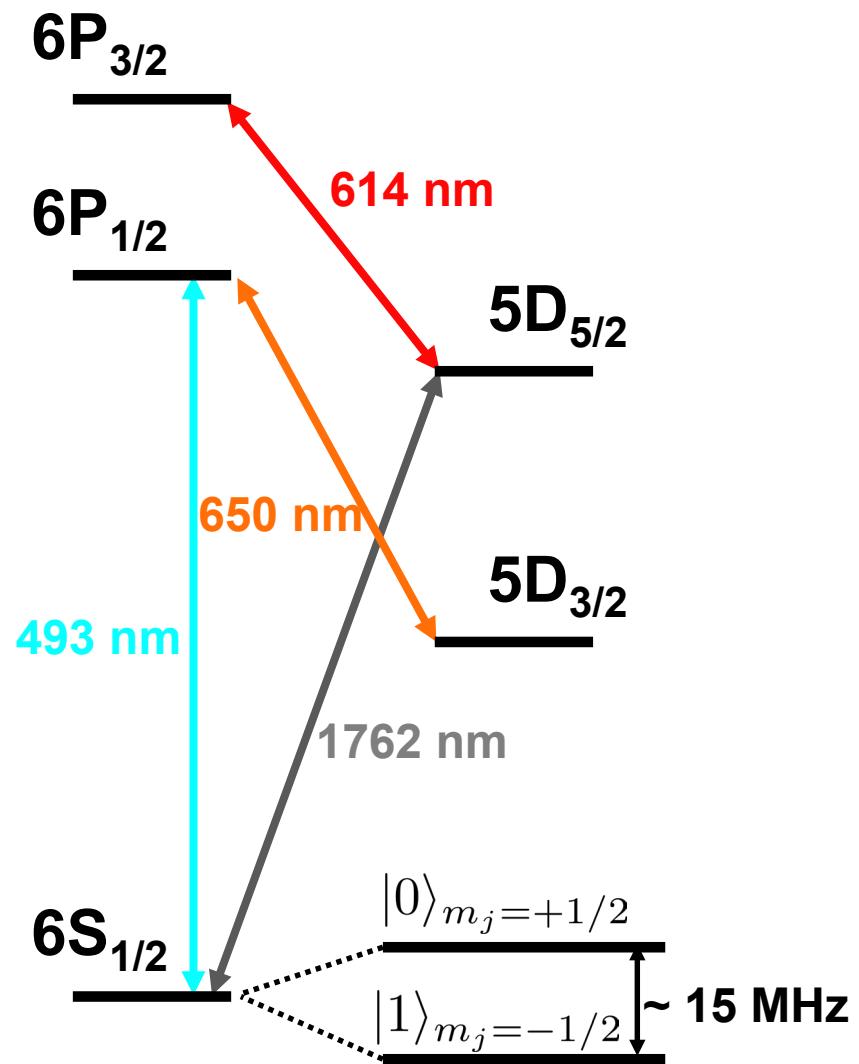


$^{171}\text{Yb}^+$ ion

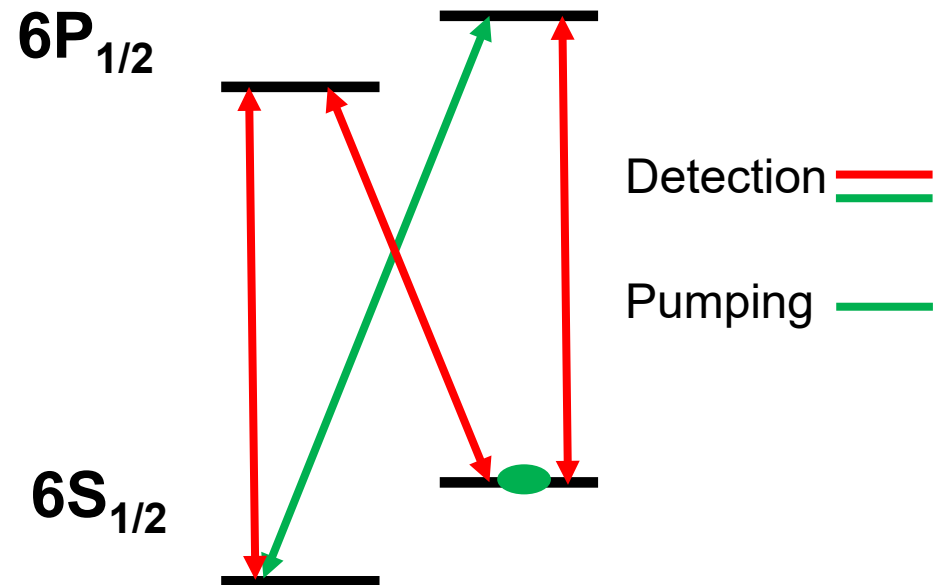


$^{171}\text{Yb}^+$ Energy levels

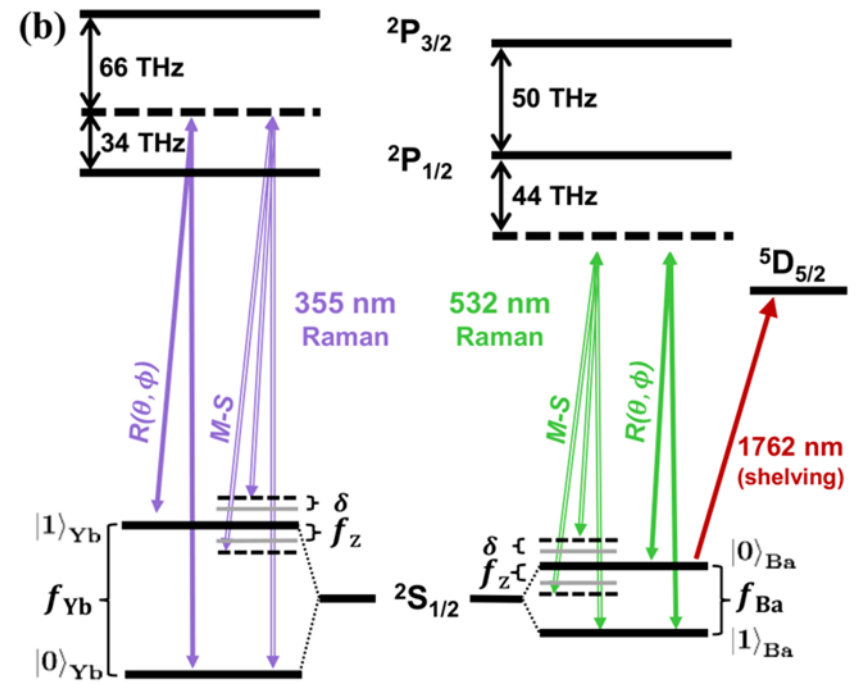
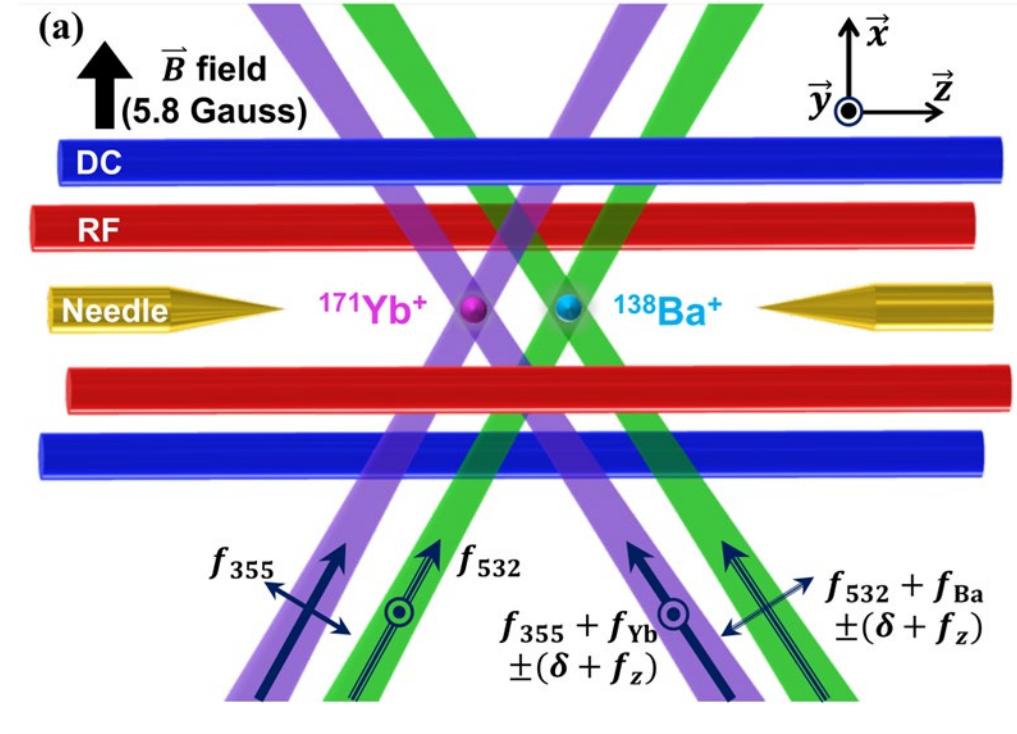
$^{138}\text{Ba}^+$ ion



$^{138}\text{Ba}^+$ Energy levels



Raman lasers



Snapshotting Quantum Dynamics at Multiple Time Points

Why quantum statistic at multiple time points important?


- 1、 Describe system properties beyond the weak perturbation with linear approximation ^[1]
- 2、 Difference between classical and quantum statistics^[2]
Bell inequality and Leggett-Garg inequality all related to quantum statistics
- 3、 Witness of nonclassicality^[3]:
Negativity in Quasi-probability distribution (QPD)

[1] M. S. Green, J. Chem. Phys. 22, 398 (1954).

[2] A. J. Leggett and A. Garg, Phys. Rev. Lett. 54, 857 (1985).

[3] R. W. Spekkens, Phys. Rev. Lett. 101, 020401 (2008).

How to measure MTP quantum statistic?

- 1、 Sequential projective measurement:
destroy the coherence
 - 2、 Weak measurement:
information gain **VS** disturbance^[1]
- 
- Measurement
back-action

[1] T. A. Brun, Am. J. Phys. 70, 719 (2002).

Our solution:

Ancilla-assisted measurement
&
post processing

- Back-action can be canceled
- Independent of the system's dynamics
- Simultaneously extract exponentially many quantum statistics.

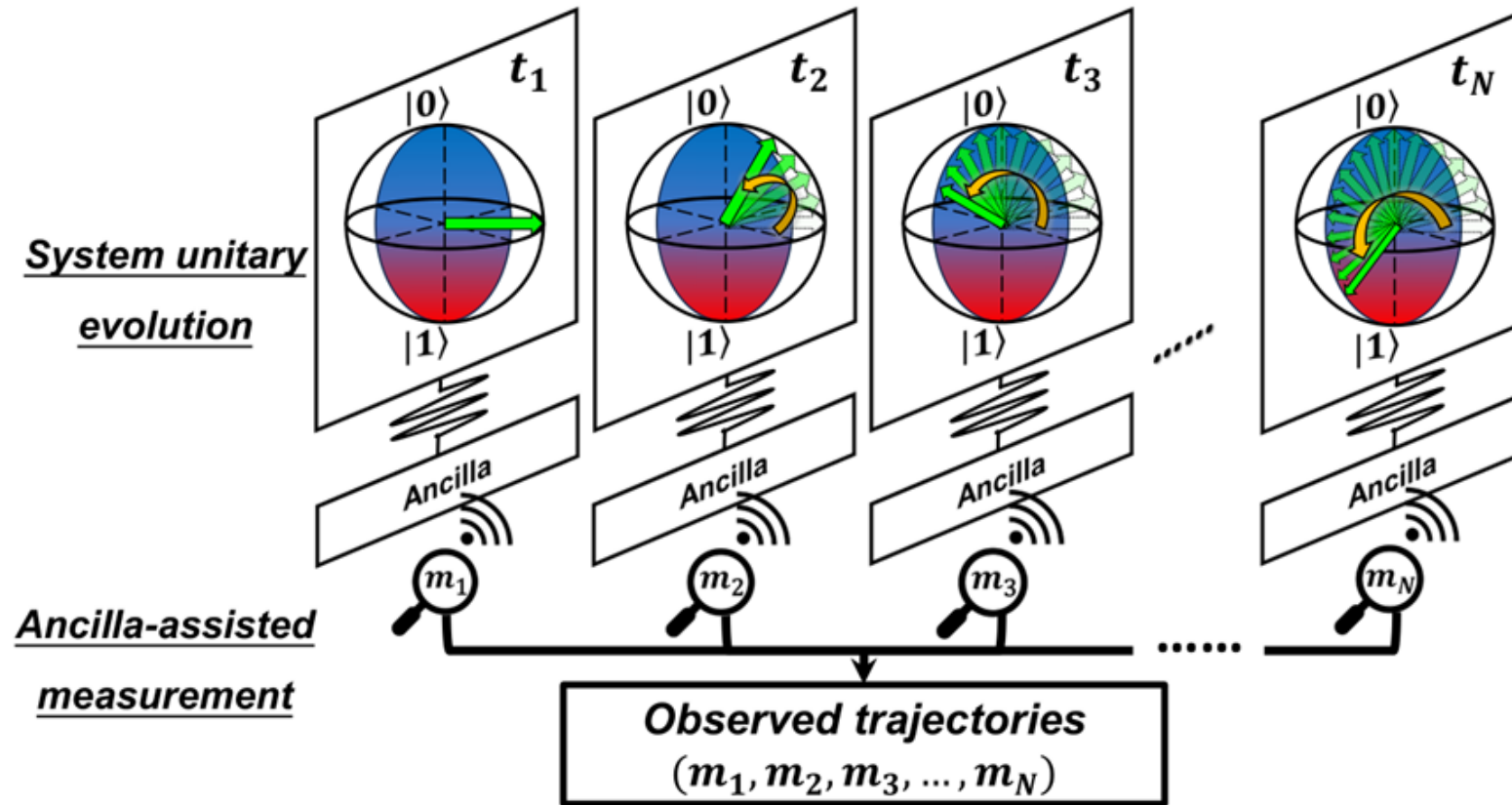


Myungshik Kim
Imperial College London

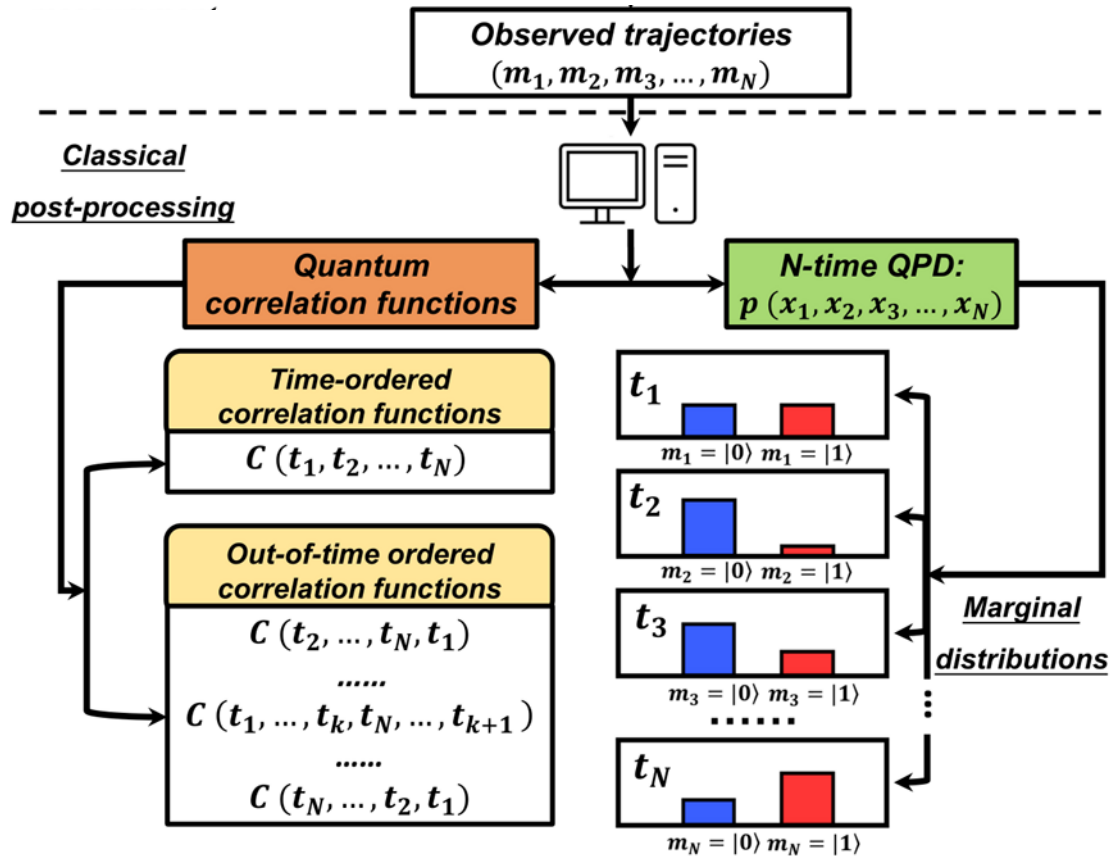


Hyukjoon Kwon
KIAS

Protocol



Protocol



MTP quantum correlation function:

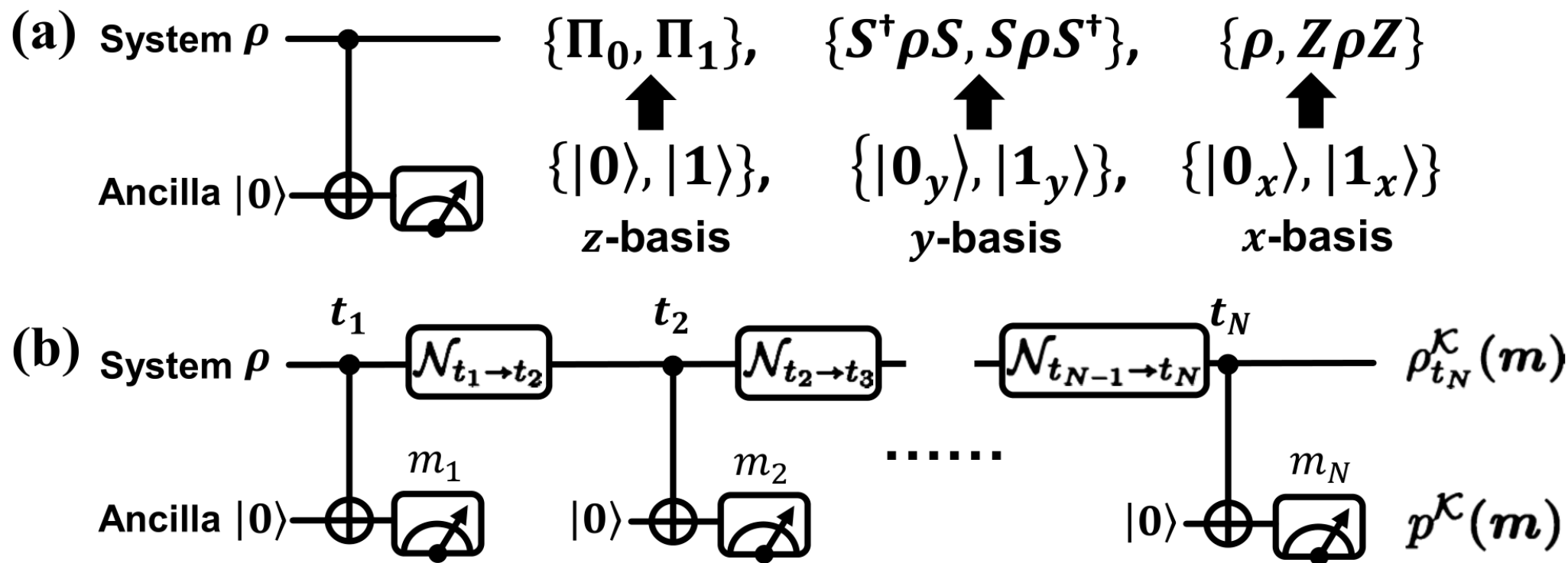
$$C_A(t) := \text{Tr}[\rho A^{(0)}(t_0) A^{(1)}(t_1) \cdots A^{(N)}(t_N)].$$

Quasi-probability distribution (QPD):

$$Q_i(t) := \text{Tr} \left[\rho \Pi_{i_0}^{(0)}(t_0) \Pi_{i_1}^{(1)}(t_1) \cdots \Pi_{i_N}^{(N)}(t_N) \right]$$

$\Pi_{i_n}^{(n)}$ projection operators

Experiment circuit



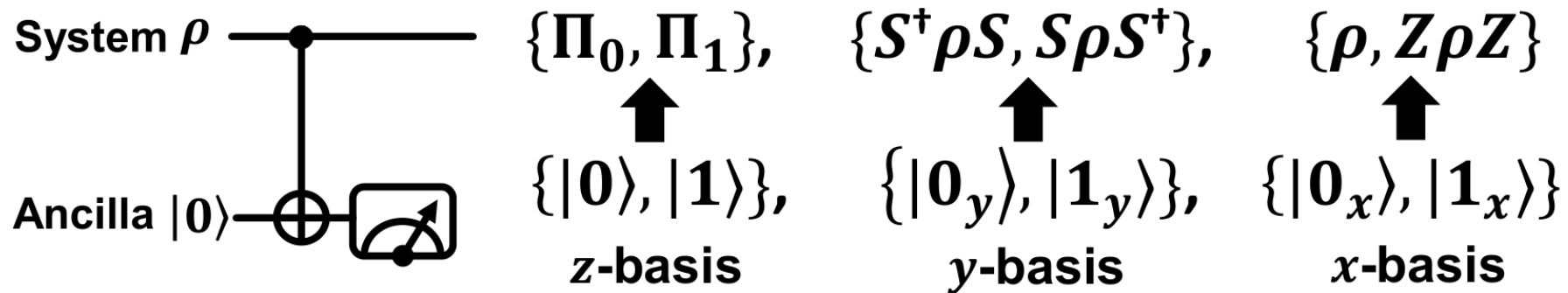
Example of post processing

$$Q_i(t) := \text{Tr} \left[\rho \Pi_{i_0}^{(0)}(t_0) \Pi_{i_1}^{(1)}(t_1) \cdots \Pi_{i_N}^{(N)}(t_N) \right] \quad \Pi_{i_n}^{(n)} \text{ projection operators}$$

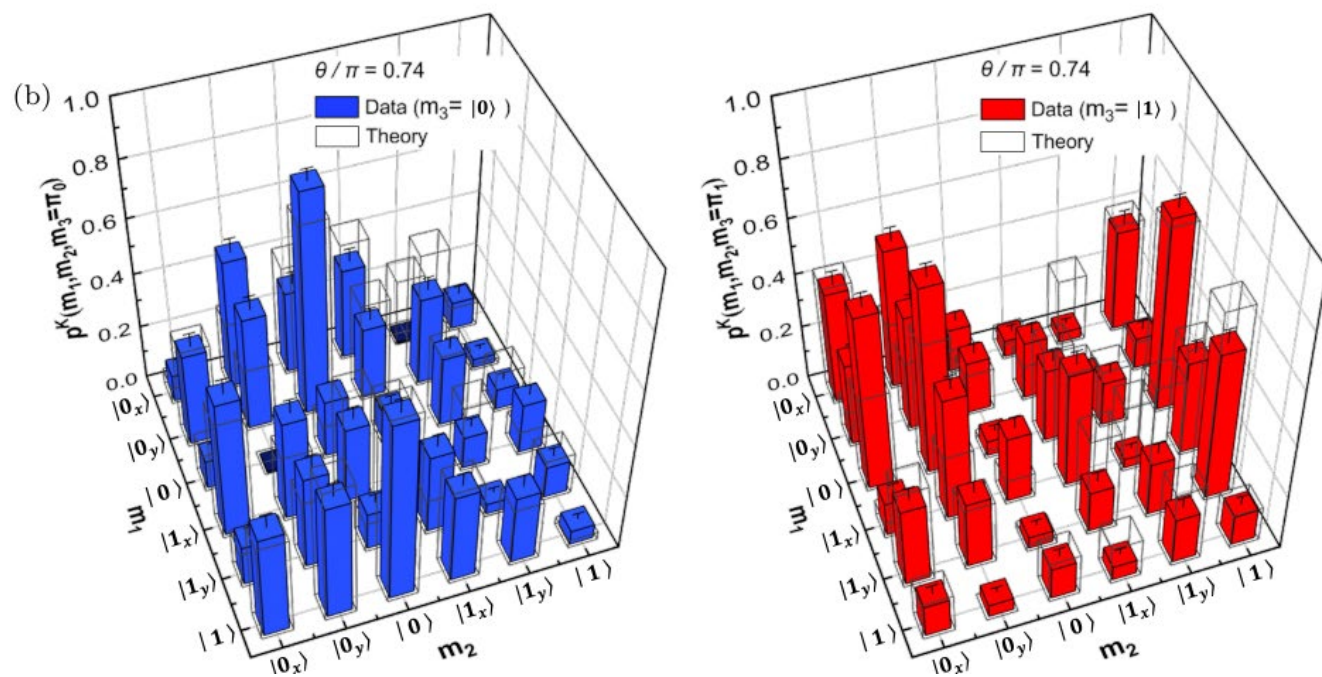
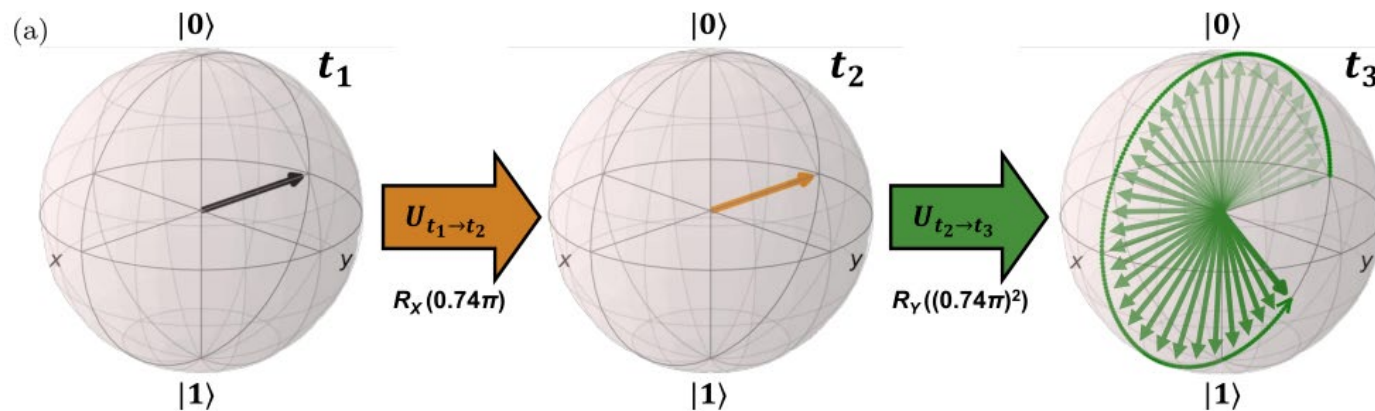
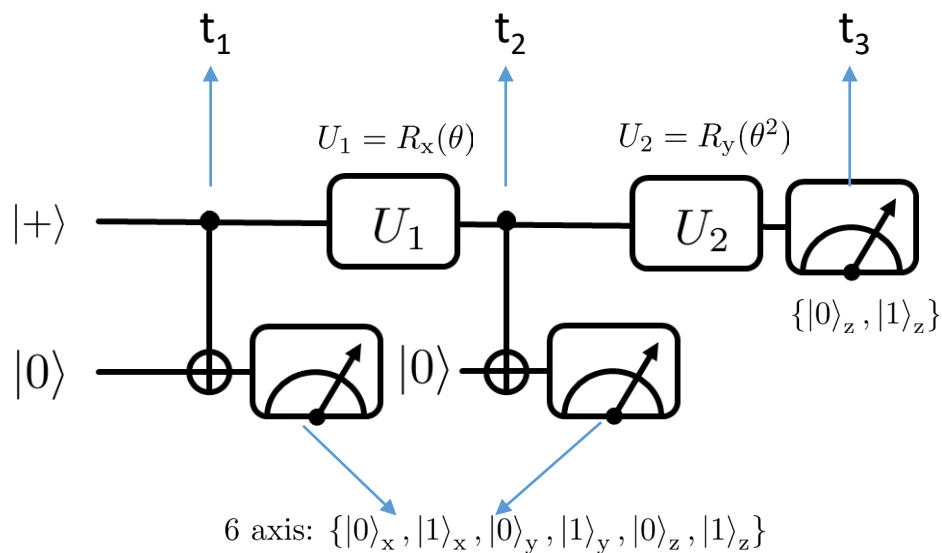
Two-point case

$$\text{Tr} \left[U_{t_1 \rightarrow t_2} \rho(t_1) \Pi_{i_1} U_{t_1 \rightarrow t_2}^\dagger \Pi_{i_2} \right] \quad \text{Heisenberg picture}$$

$$\rho \Pi_x = \frac{\rho - Z\rho Z + \Pi_x \rho \Pi_x - i(-1)^x S \rho S^\dagger + i(-1)^x S^\dagger \rho S}{4}$$

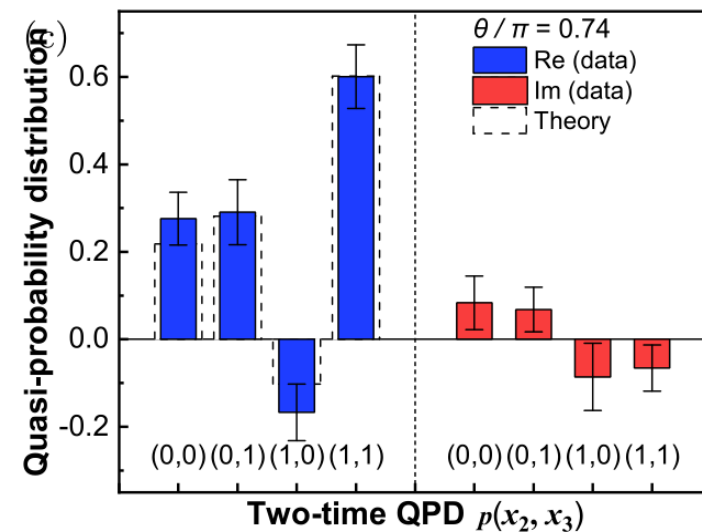
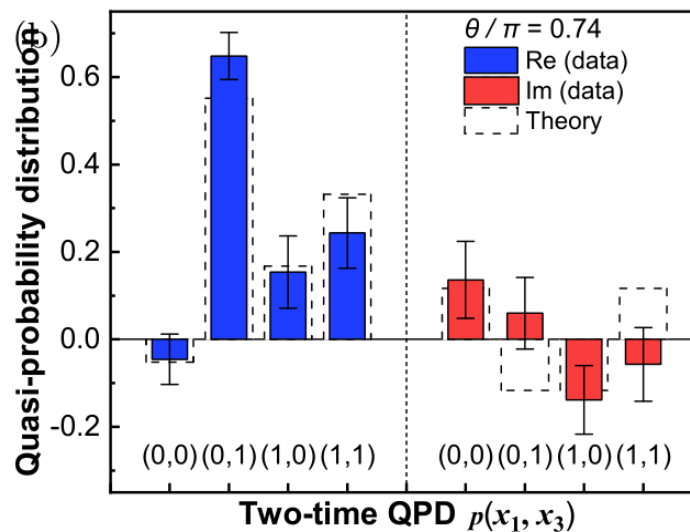
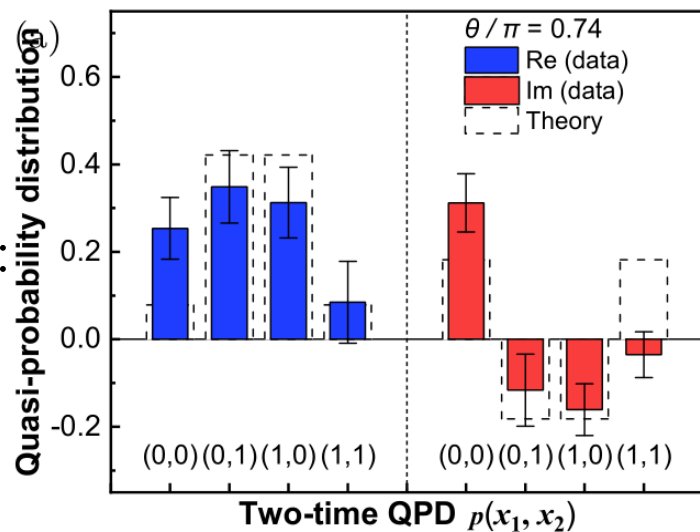


Experiment circuit and raw data

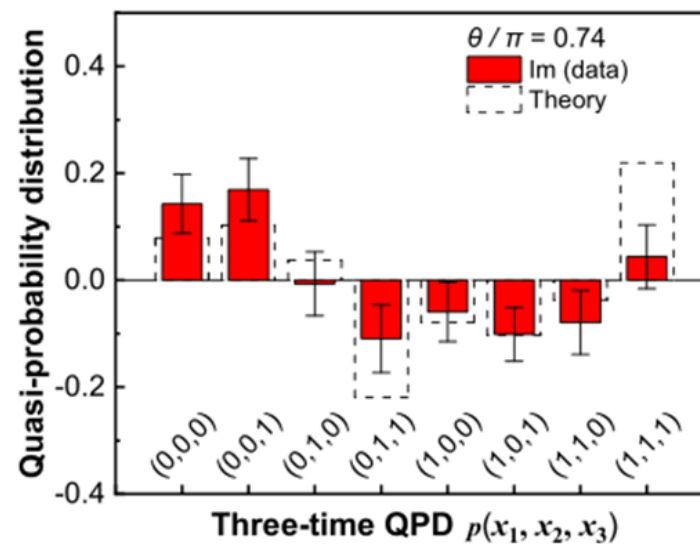
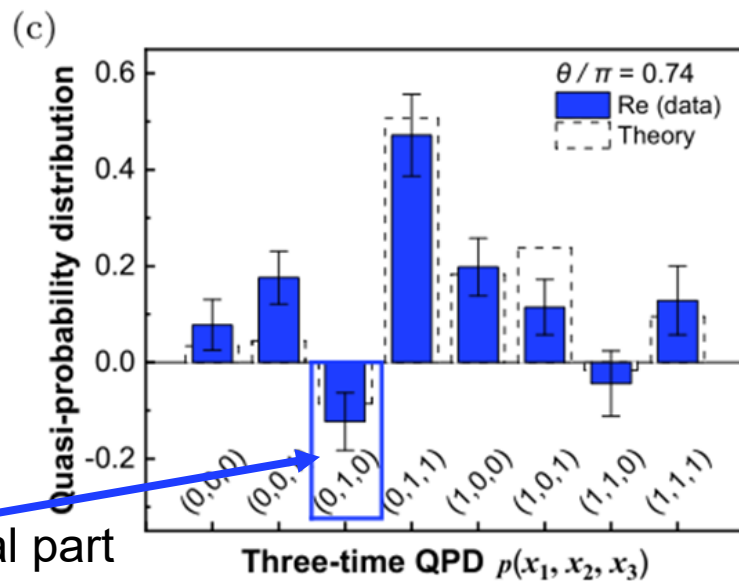


MTP QPD

Two time points:

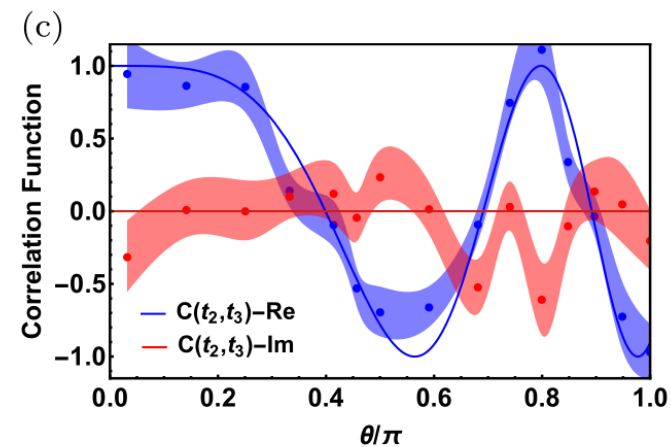
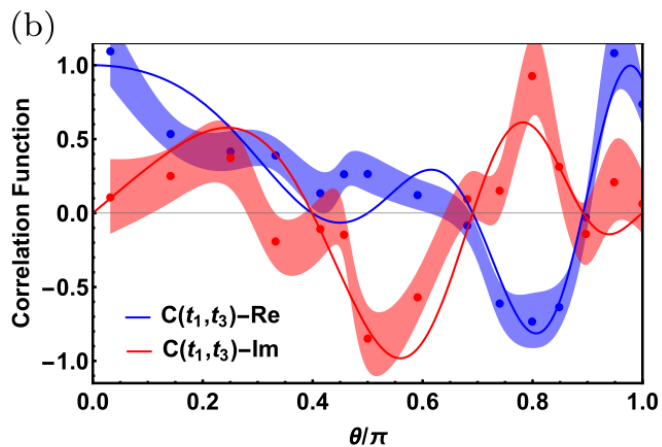
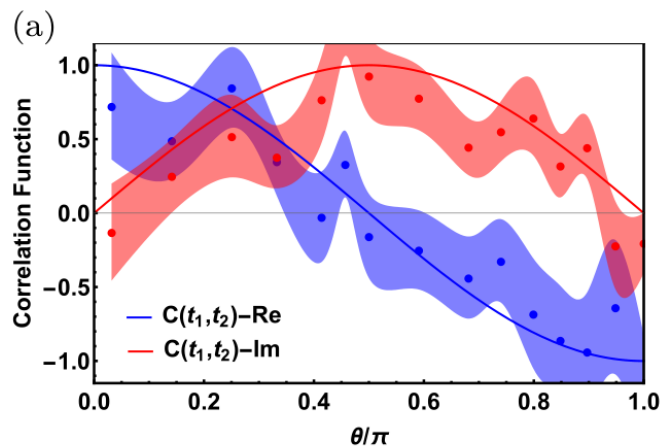


Three time points:

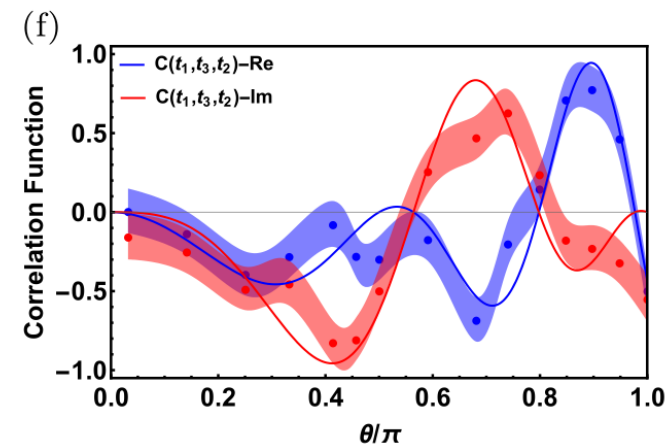
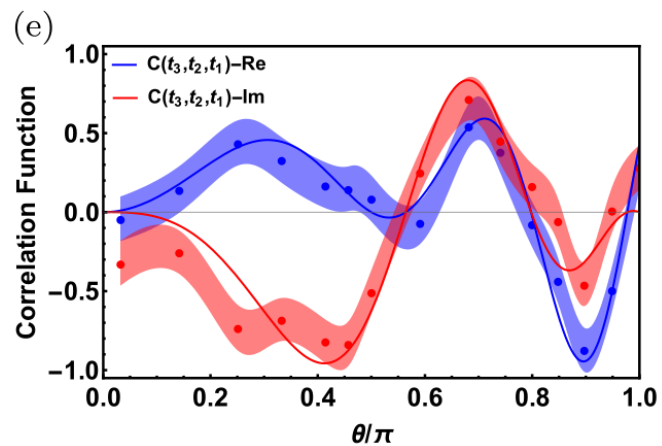
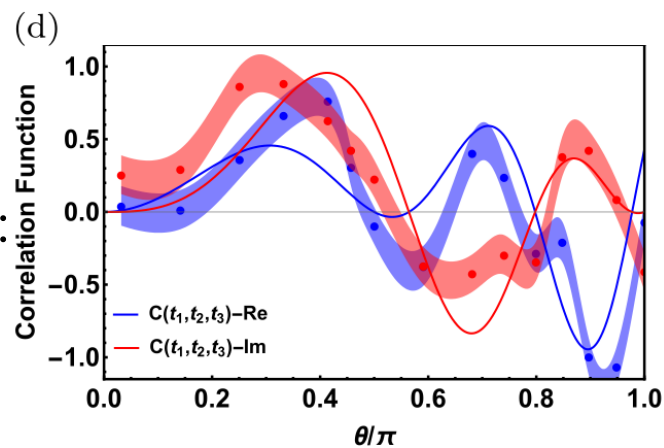


MTP Correlation function

Two time points:

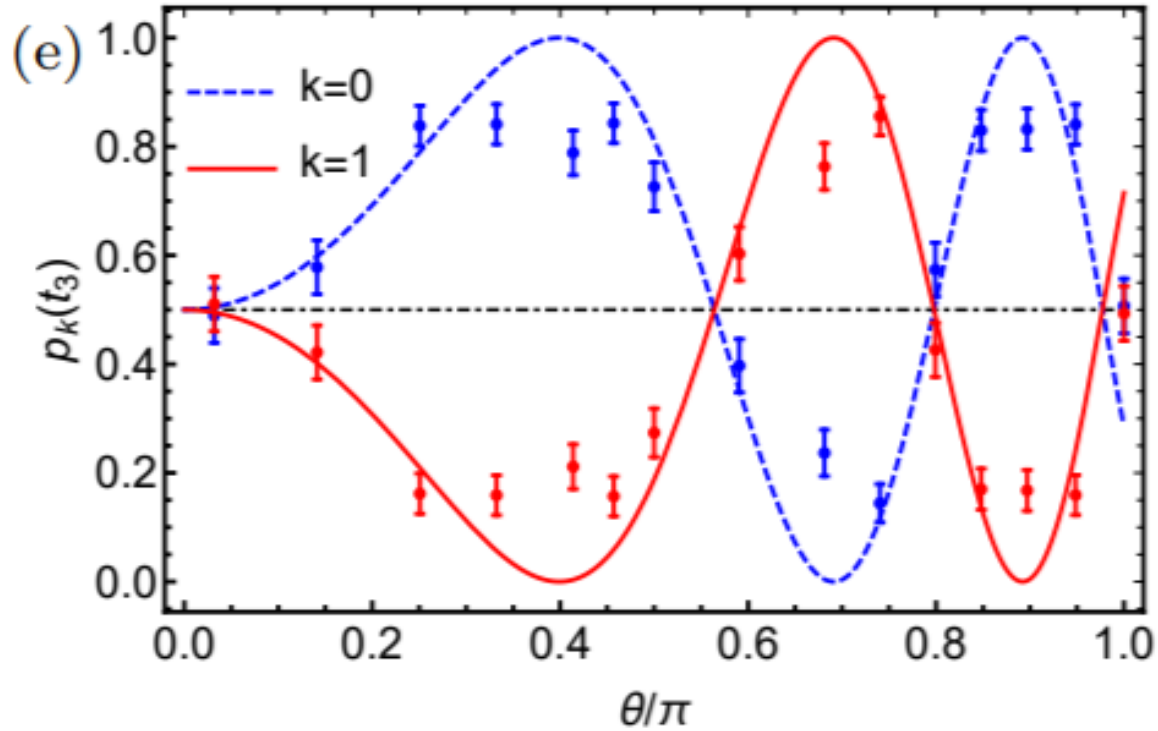


Three time points:



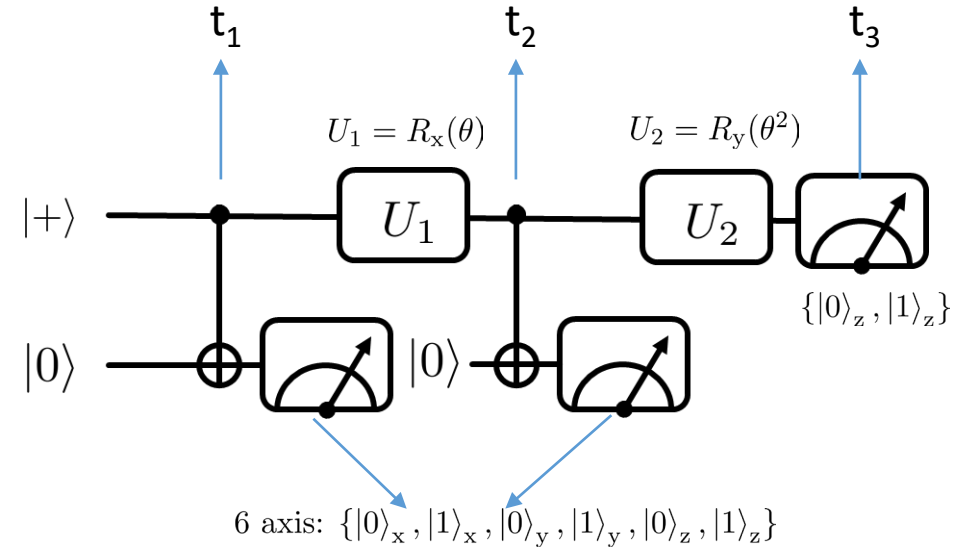
Out-of-time ordered

Marginal distribution at t_3



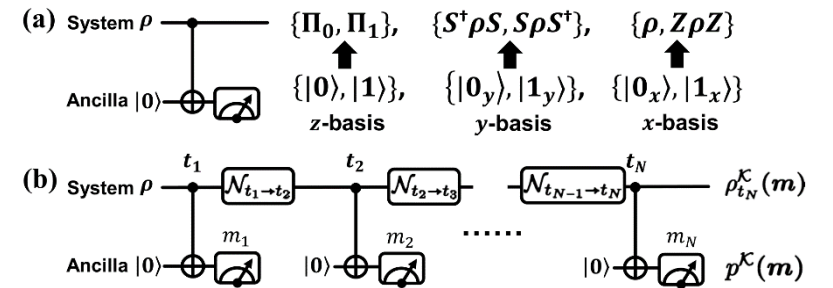
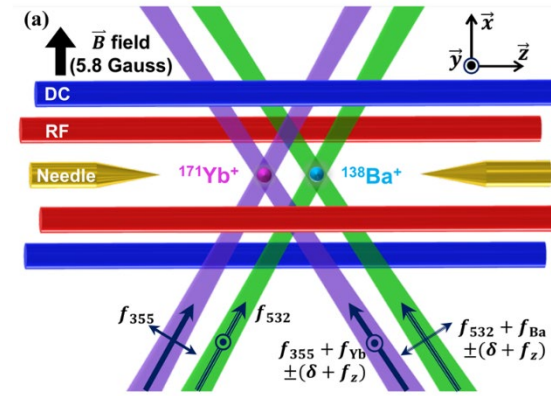
marginal distribution

$$\sum_{x_k} p(x_1, \dots, x_N) = p(x_1, \dots, x_{k-1}, x_{k+1}, \dots, x_N)$$



Summary

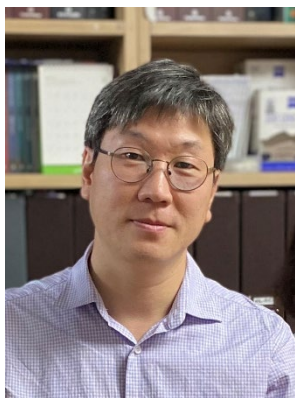
- 1、 $^{171}\text{Yb}^+ - ^{138}\text{Ba}^+$ hybrid system.
- 2、 Ancilla-assisted measurement & Post processing



Advantage of our method:

- 1、 Only need one ancilla qubit for many-time point measurement (reuse).
- 2、 Independent of the system's dynamics, even in the case of an open system.
- 3、 Only need a short-time system-ancilla interaction
- 4、 Simultaneously extract exponentially many correlation functions.

Team leader:



Kihwan Kim

- Tsinghua University
- Beijing Academy of Quantum Information Sciences

Theory support:



Myungshik Kim
Imperial College London

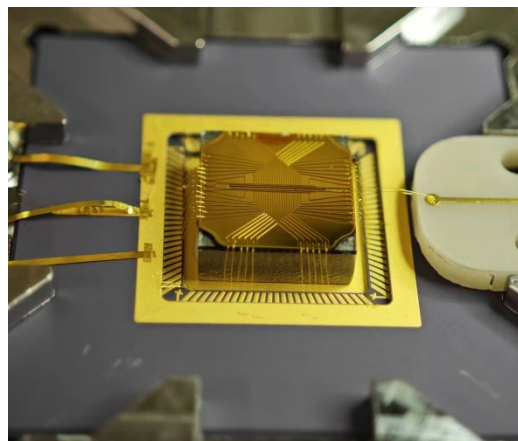


Hyukjoon Kwon
KIAS

Thank you

Surface trap based on fused silica :

- Yb⁺-Ba⁺ Hybrid system
- QCCD
- Qubit reuse



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