

Exploring the effect of rotation on the deconfinement phase transition in hybrid stars

Christoph Gärtlein¹, O.Ivanytskyi, D.Blaschke, V. Sagun, I.Lopes

¹Univ. Lisbon, Univ. Coimbra, Univ. Wrocław



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EREP, Coimbra

- 1 Introduction
- 2 Hybrid star equation of state
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Are Neutron Stars (NSs) worth to discuss in a Relativity Meeting?

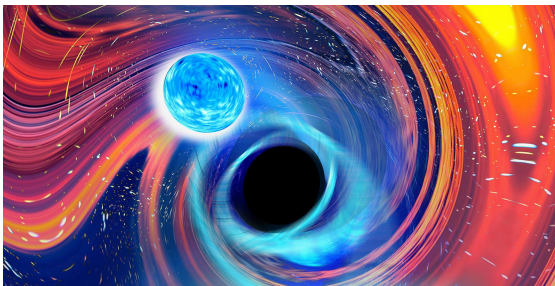
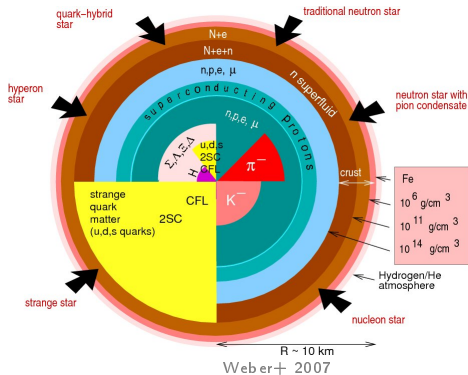


Illustration of NS-BH merger

Compactness of objects $\mathcal{C} = M/R$

- Black Holes (BHs) \Rightarrow Schwartzschild radius $\Rightarrow \mathcal{C} = 1/2$
- maximum mass NSs $\Rightarrow \mathcal{C} \approx 0.2 - 0.3$

What are these compact objects made of?



- different possible composition of Neutron Stars (NS)
- one possibility: Quark Gluon Plasma in the core (including phase transition)

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How to build up an NS with Equations of State?

What do we need to obtain possible NS configurations?

⇒ Tolmann-Oppenheimer-Volkoff Equations
(spherical symmetric and gravitational equilibrated objects)

$$\frac{dp}{dr} = -(\varepsilon + p) \frac{m + 4\pi r^3}{r^2 - 2rm}$$

$$\frac{dm}{dr} = 4\pi r^2 \varepsilon$$

static

⇒ need $p(\varepsilon)$ ⇒ need full EoS ⇒ hybrid EoS

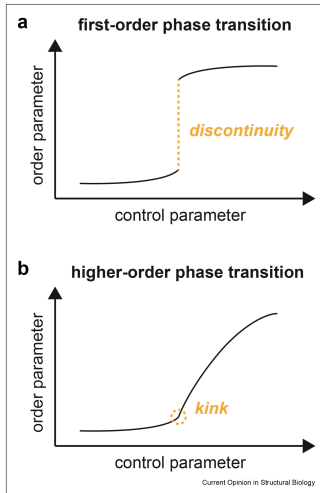
How to build up an NS with Equations of State?

Assumption: We work with a **First order Phase Transition** between Hadronic and Quark Gluon Plasma Phase

- Hadronic Phase: **DD2npY-T model** including n , p , e , μ and hyperonic degrees of freedom [Shahrbaf,Blaschke+\(2022\)](#)
- Quark matter: confining relativistic density functional approach [Ivanytskyi,Blaschke \(2022\)](#)

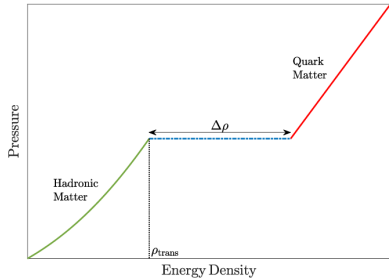
⇒ encoded in underlying Lagrangian

Interlude on phase transitions



Erdel 2023

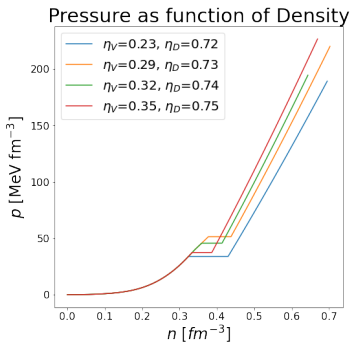
Short answer: Discontinuity of order parameter \Rightarrow First order phase transition



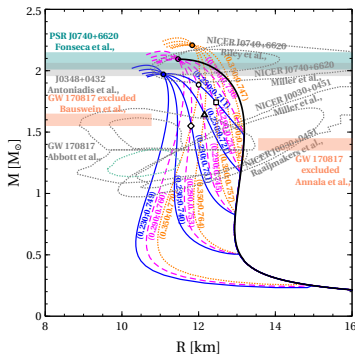
Jump in energy density for hybrid EoS

- sharp interface between two phases

From EoSs to M-R curves



TOV



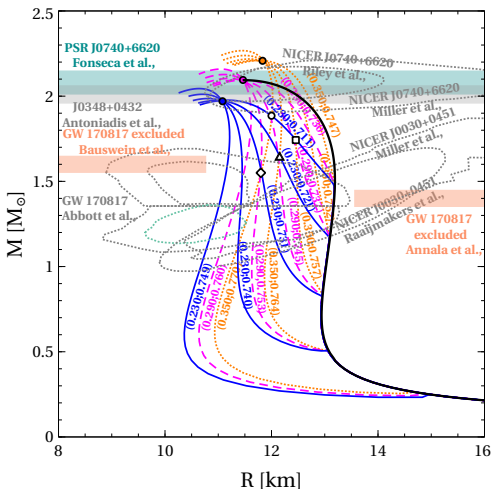
TOV equations:

$$\frac{dp}{dr} = -(\varepsilon + p) \frac{m + 4\pi r^3}{r^2 - 2rm},$$

$$\frac{dm}{dr} = 4\pi r^2 \varepsilon$$

Remember interesting properties as

- Special Points (SPs) and
- the deconfinement phase transition



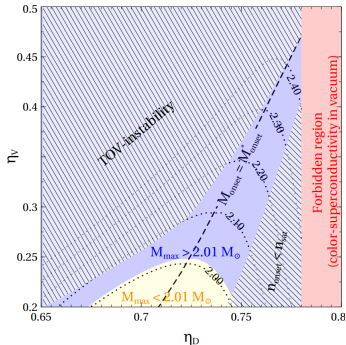
Gärtlein+ 2023

Summary of published paper

- ① Hybrid EoS with specific quark matter description

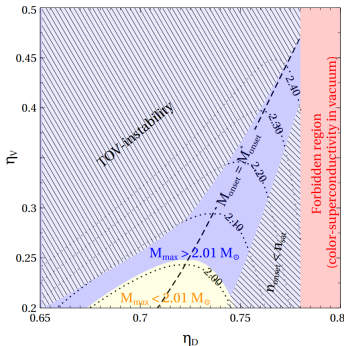
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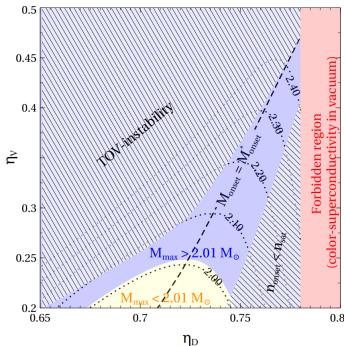
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- corresponding M-R curves with properties as Special point (empirical relation)

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- [10.1103/PhysRevD.108.114028](https://arxiv.org/abs/10.1103/PhysRevD.108.114028)

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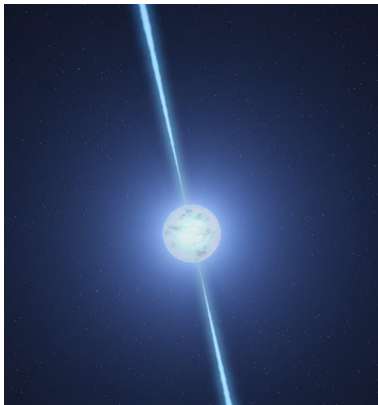
What about rotating NSs?

Do they exist and if yes...

- How to observe them?
- How do they behave under rotation?
- Do characteristics change “dramatically” under rotations?

⇒ Consider a “phase diagram” of
rotating hybrid stars
 ω - M space

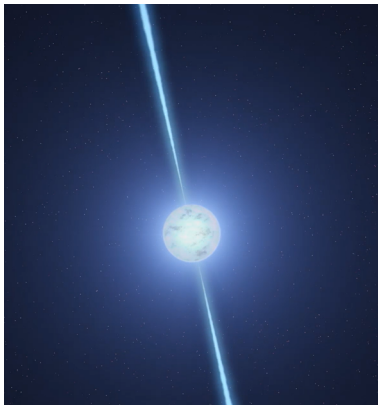
Justification



Pulsars - Showing a "beam of light"

- multiple detected pulsars including rotations over 700Hz \Rightarrow millisecond pulsars

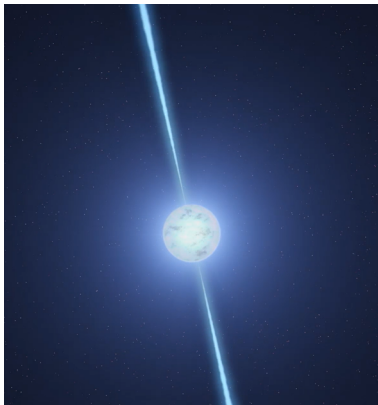
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Pulsars - Showing a "beam of light"

- multiple detected pulsars including rotations over 700Hz \Rightarrow millisecond pulsars
- changing of spherical shape (**flattening**) and frame-dragging
- phase transition inside and maximum mass \Rightarrow how does it change?

What does it mean mathematically?

- Rotational metric (ZAMO frame - observer at same ω)

$$ds^2 = -e^{2\nu} dt^2 + e^{2\psi} (d\phi - \omega dt)^2 + e^{2\lambda} (dr^2 + r^2 d\theta^2)$$

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- **process:**
 - input: EoS, central density ε_c , frequency ω
 - output: R , M , oblateness (R_p/R_e), etc.

Kepler frequency

NSs rotating at Kepler frequency

- hypothetical highest rotation of NSs
- higher rotations will lead to mass shedding

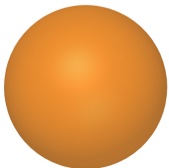
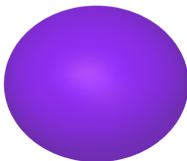
- $\omega_{Kepler} \propto \sqrt{\frac{M}{R^3}}$

- ω_{Kepler} will play the role of a phase boundary in our discussion

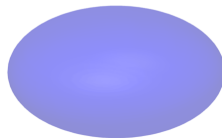
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Neutron stars under rotation

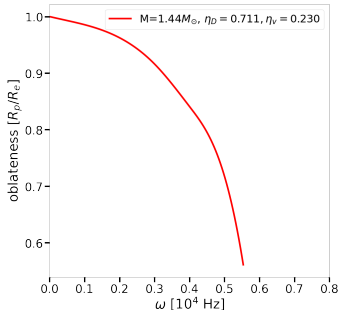
static case

 $\omega = 6 \text{ kHz}$ 

Kepler frequency

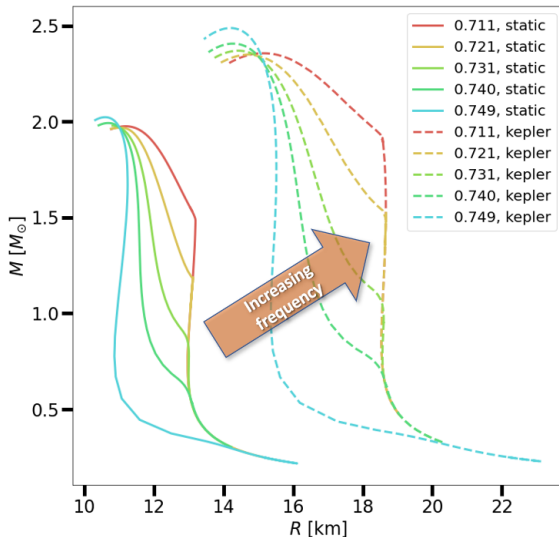


Neutron star under rotation



- oblateness as a function of the rotational frequency ω
- depending on EoS/couplings \Rightarrow oblateness goes down to ca. 55%

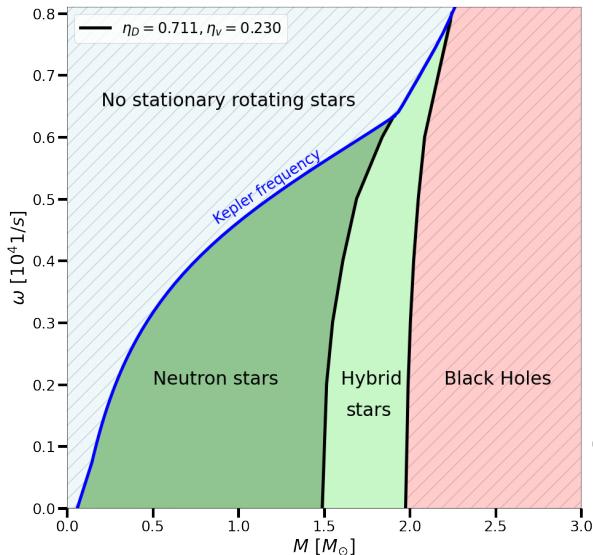
M-R curves and characteristics



- M-R curves are essentially shifted to higher radii and masses
- properties as SP and onset of deconfinement phase transition are shifted in a similar way
- SP still seems to exist!

Gärtlein+ 2024, still in preparation

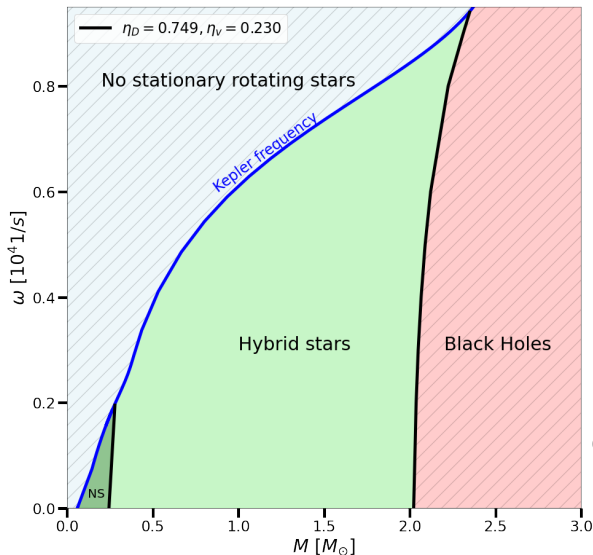
Phase diagram ω - M



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Still in preparation

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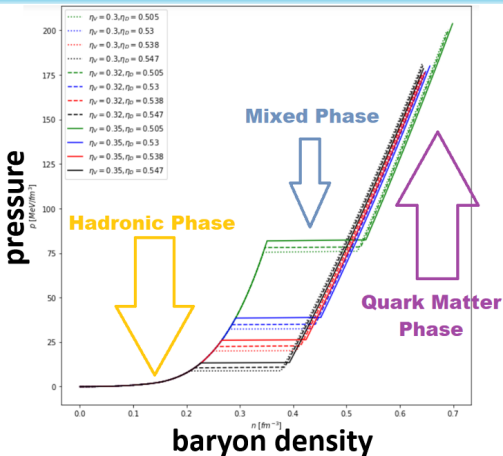
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- 5 phase diagram predicts composition of hybrid stars \Rightarrow parameter space (η_V, η_D) needs to be more restricted
- 6 observation of rotating stars can put constraints on internal composition

Thanks!

Maxwell construction



- typical plateau of first order phase transition
- **But:** inside star, no shell of mixed phase \Rightarrow narrow

Relativistic density functional for quark matter EOS

$$\mathcal{L} = \bar{q}(i\not{\partial} - \hat{m})q + \mathcal{L}_{PS} + \mathcal{L}_V + \mathcal{L}_D$$

- **Pseudoscalar interaction \Rightarrow chiral dynamics**

$$\mathcal{L}_{PS} = G_0 \left[(1 + \alpha) \langle \bar{q}q \rangle_0^2 - (\bar{q}q)^2 - (\bar{q}i\vec{\tau}\gamma_5 q)^2 \right]^{\frac{1}{3}}$$

- **Vector interaction \Rightarrow repulsion**

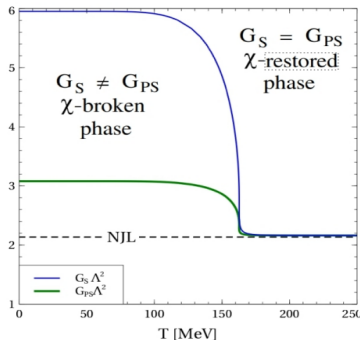
$$\mathcal{L}_V = -G_V (\bar{q}\gamma_\mu q)^2$$

- **Diquark pairing \Rightarrow color superconductivity**

$$\mathcal{L}_D = G_D \sum_{A=2,5,7} (\bar{q}i\gamma_5\tau_2\lambda_A q^c)(\bar{q}^c i\gamma_5\tau_2\lambda_A q)$$

- **Comparison to NJL model**

- medium dependent scalar G_S and pseudoscalar G_{PS} couplings
- high vacuum quark mass \Rightarrow phenomenological confinement
- quark correlations \Rightarrow mesons: $\pi, \sigma = \text{---} \circ \text{---}$



Details in:

Ivanytskyi, Blaschke, PRD (2022)

Ivanytskyi, Blaschke, Particles (2022)