



Hadron Spectroscopy with Strangenes

April 3rd - 5th, 2024 University of Glasgow, Glasgow, UK

Strangeonium at BESIII

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on behalf of the **BESIII Collaboration**

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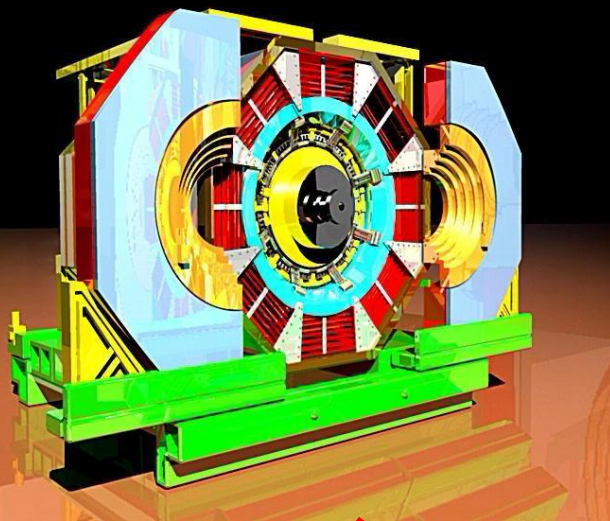


The experimental scenario

BESIII @ BEPC-II

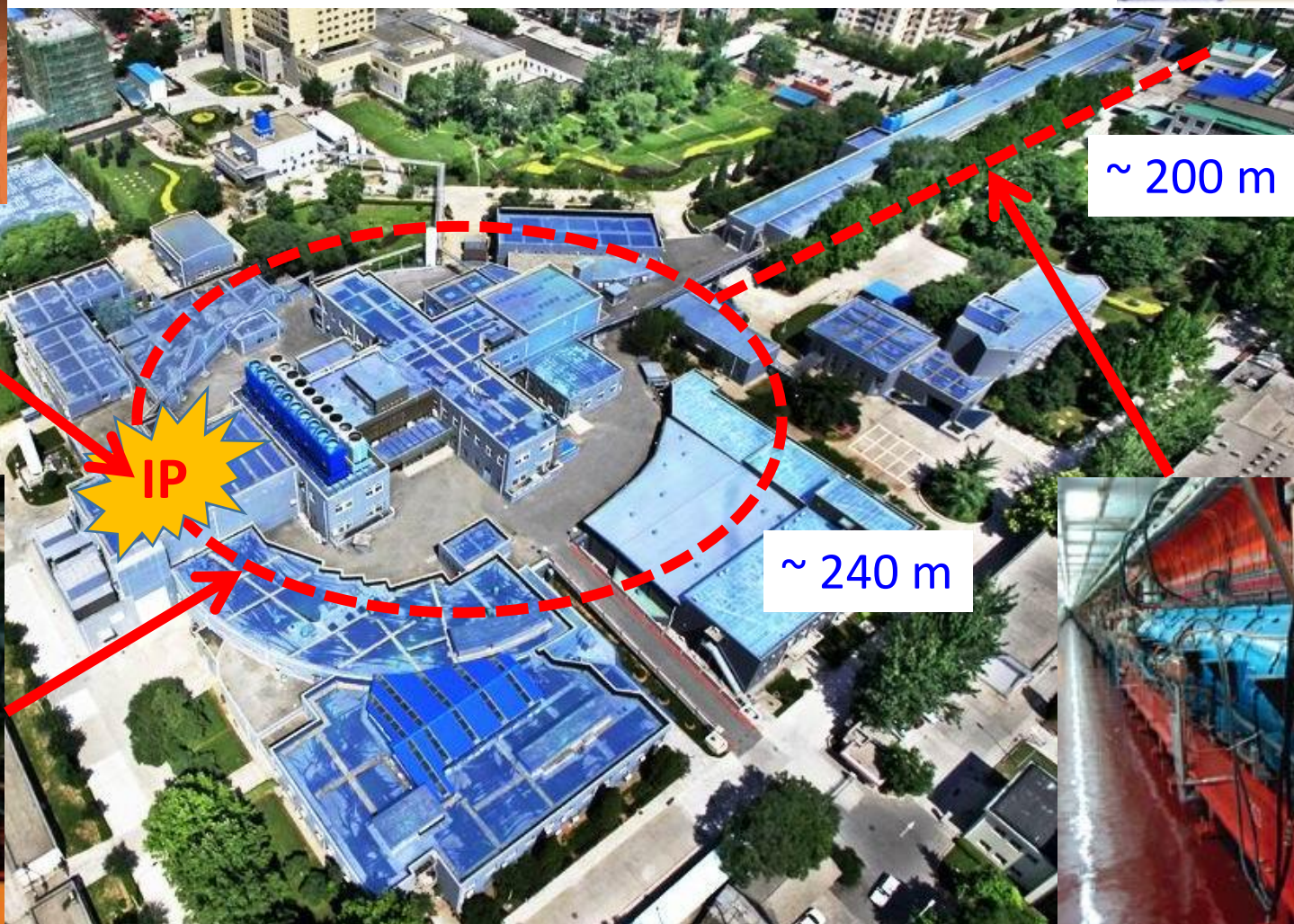
- BEPCII: τ -charm factory
- Center of Mass Energy: 2 – 4.95 GeV
- Achieved design Luminosity $L_{\text{design}} = 1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

2016/04/05 22:29:47		
Luminosity	10.00	$E_{32}/\text{cm}^2/\text{s}$
	e^+	e^-
Energy [GeV]	1.8831	1.8831
Current [mA]	849.18	852.31
Lifetime [hr]	1.53	2.30
Inj. Rate [mA/min]	0.00	0.00



BESIII
experiment

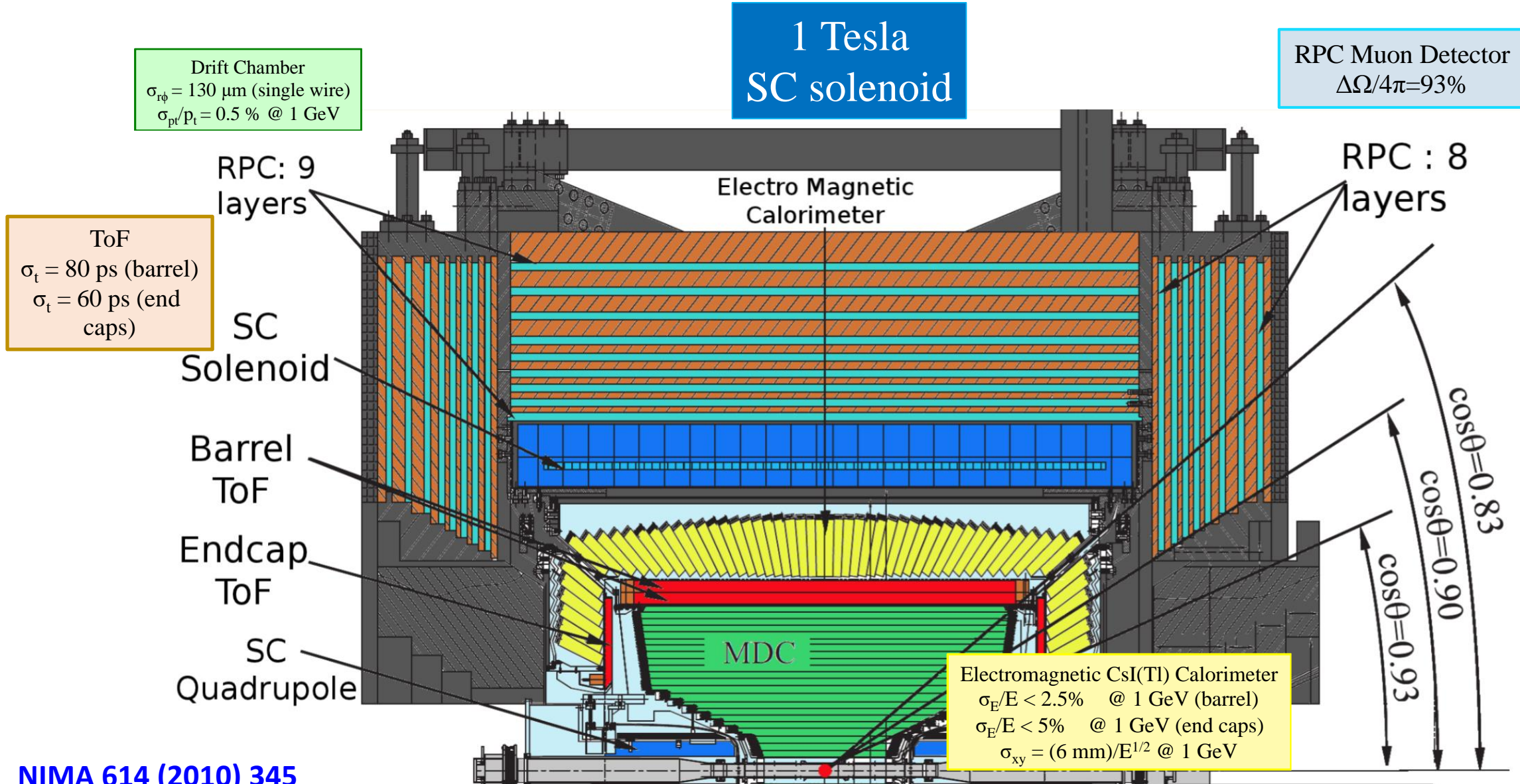
BEPC-II
 e^+e^- storage ring



injection LINAC



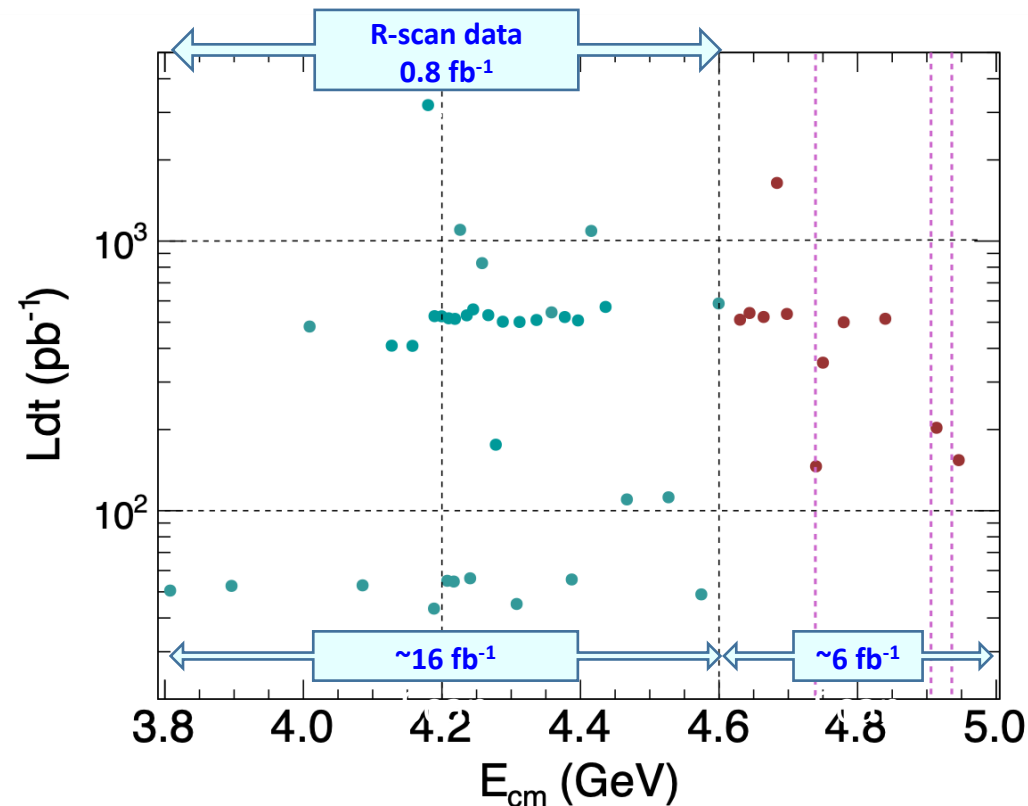
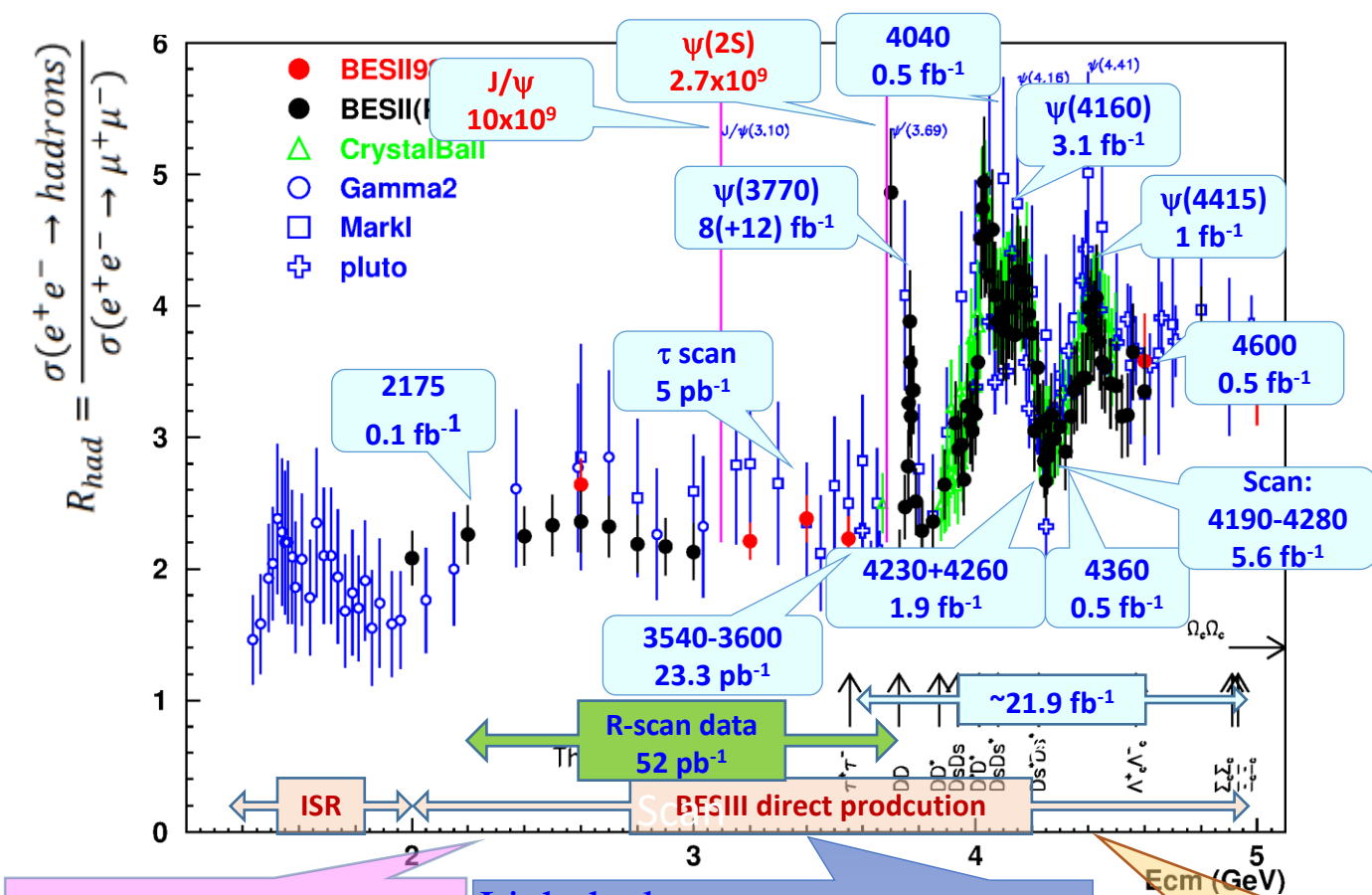
BESIII Spectrometer



NIMA 614 (2010) 345

Excellent scenario for XYZ Physics

World's largest data samples directly produced from e^+e^- collision @ J/ψ and $\psi(2S)$



Hadron form factors
Y(2175)
Zs states?
QCD test

Light hadron spectroscopy
Glueballs, hybrids, multi-quark states
Rare decays
Tau Physics

XYZ
D and Ds Physics
(f_D and f_{D_s} , mixing, CP)
Charmed baryons

XYZ data:

- 46 energy points (21.9 fb^{-1})
- 29 energy points with $L_i > 0.4 \text{ fb}^{-1}$

Small scan sample:

- 104 energy points (0.8 fb^{-1})

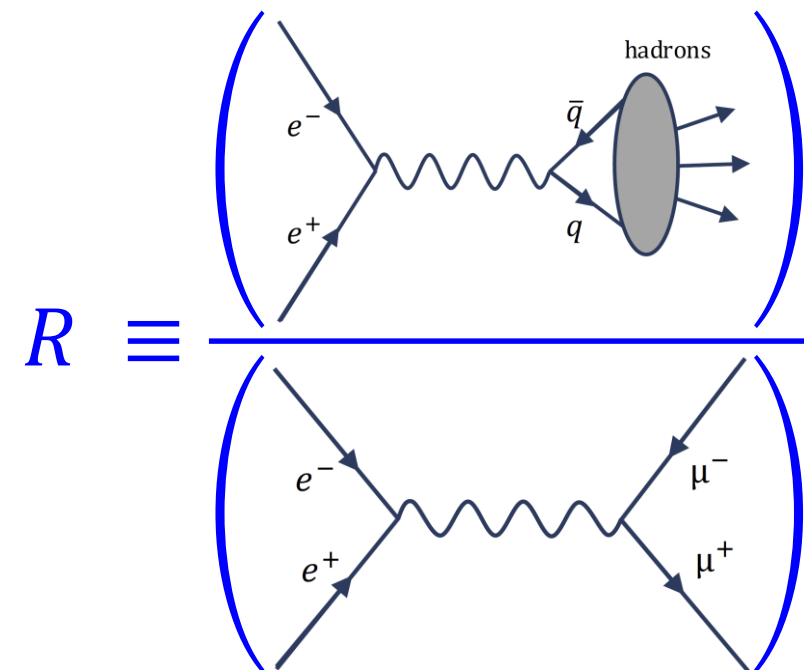
R value

Definition of R value

- *R value*

- LO production cross section ratio of hadrons and muon pairs in e^+e^- annihilations

$$R \equiv \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-)} \equiv \frac{\sigma_{\text{had}}^0}{\sigma_{\mu\mu}^0}$$



- σ_{had}^0

- important input to current tests of Standard Model
- critical to determine:
 - QED running coupling constant
 - anomalous magnetic moment of the muon

- $\sigma_{\mu\mu}^0$

- QED

$$\sigma_{\mu\mu}^0(s) = \frac{4\pi\alpha^2}{3s} \frac{\beta_\mu(3 - \beta_\mu^2)}{2} \quad \beta_\mu = \sqrt{1 - 4m_\mu^2/s}$$

QED running electromagnetic coupling constant $\Delta\alpha(s)$

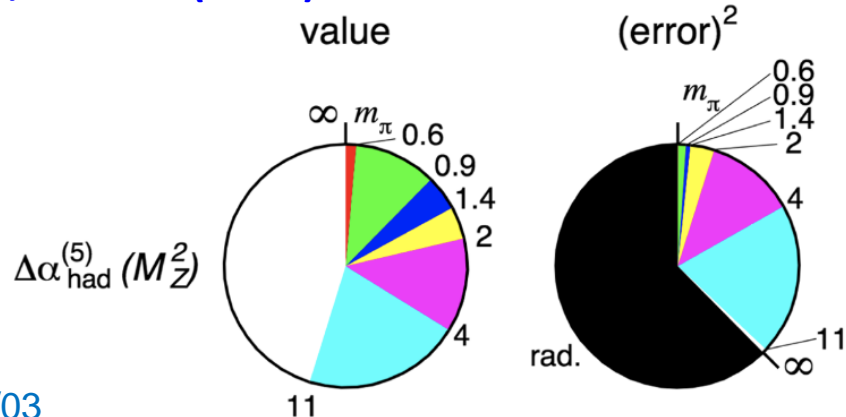
• $\Delta\alpha(s)$

$$\Delta\alpha(s) = 1 - \frac{\alpha(0)}{\alpha(s)} = \Delta\alpha_{lepton}(s) + \Delta\alpha_{had}^{(5)} + \Delta\alpha_{top}(s)$$

- $\Delta\alpha_{lepton}(s)$ determined analytically by perturbation theory
- $\Delta\alpha_{top}(s)$ negligible in BESIII energy range ($10^{-7} \sim 10^{-10}$) due to the large top quark mass
- $\Delta\alpha_{had}^{(5)}(s)$ Hadronic Vacuum Polarization (HVP) contribution
 - inferred from **R value**
 - optical theorem \rightarrow dispersion integral
 - $\Delta\alpha_{had}^{(5)}(s)$ limits precision Physics (EW fit) at m_Z : the 5 light quarks contribution is not computable by p-QCD at lower energies [$\alpha(m_Z^2)$ essential for EW precision Physics]

$$\Delta\alpha_{had}^{(5)}(s) = -\frac{\alpha s}{3\pi} \text{Re} \int_{E_{th}}^{\infty} ds' \frac{R(s')}{s'(s' - s - i\varepsilon)}$$

PRD 97, 114025 (2019)



$\Delta\alpha_{had}^{(5)}(s)$ is sensitive with the R-value on a wide energy range

Fundamental input

EPJ 80, 241 (2020)

Source	Contribution ($\times 10^{-4}$)
$\Delta\alpha_{lepton}(M_Z^2)$	314.979 ± 0.002
$\Delta\alpha_{had}^{(5)}(M_Z^2)$	276.0 ± 1.0
$\Delta\alpha_{top}(M_Z^2)$	-0.7180 ± 0.0054

Muon anomalous magnetic moment a_μ

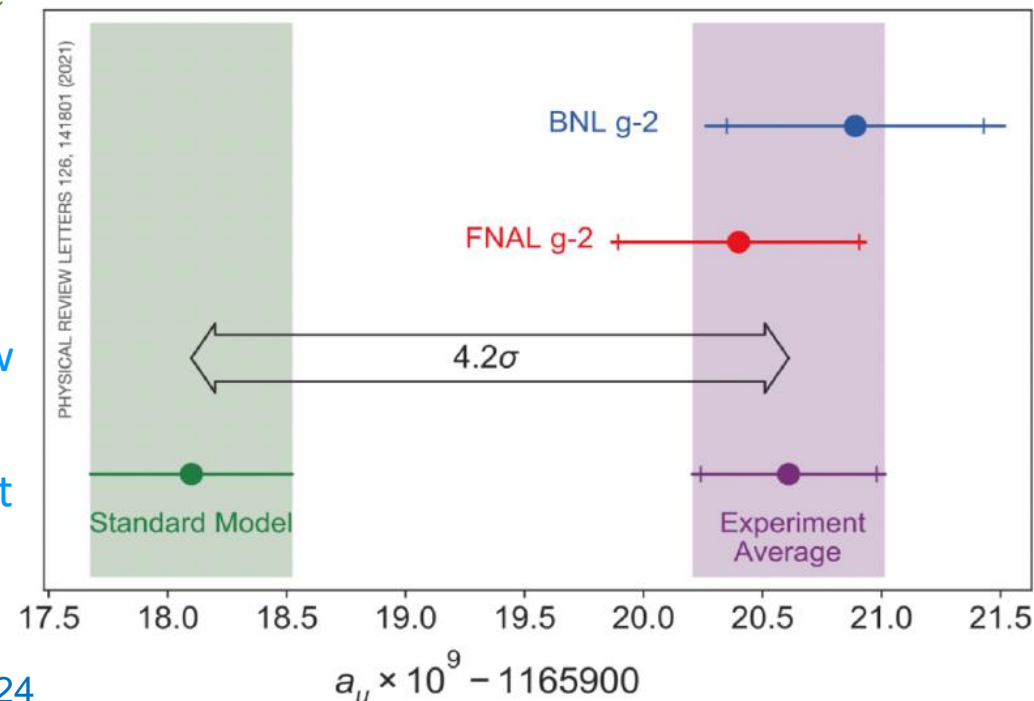
- magnetic moment of the muon: $\vec{\mu} = g_\mu \frac{e}{2m_\mu} \vec{S}$
- provides sharp test of EM theory and possible hints of BSM
- Dirac: $g_\mu = 2 \rightarrow$ Quantum Field Theory: $a_\mu = \frac{|g_\mu - 2|}{2}$ (**Muon Anomaly**)
- **Anomalous Magnetic Moment:** large discrepancy SM vs experimental data, **4.2 σ (BSM?)**

- SM: $a_\mu^{SM} = a_\mu^{QED} + a_\mu^{QCD} + a_\mu^{weak}$
PRD 97, 114025 (2019)

- Experimental average (BNL and FNAL)
PRL 126, 141801 (2021)

- hadronic contributions dominate a_μ^{SM} uncertainties
 - **Hadronic Light-by-Light Scattering (HLbL):** irreducible, now
 - **Hadronic Vacuum Polarisation (HVP):** a_μ^{LO-HVP} from dispersion integral exploiting R-value as experimental input

$$a_\mu^{LO-HVP} = \left(\frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^{\infty} ds \frac{R(s)K(s)}{s^2}$$



Literature

- **existing R-values experimental data:**

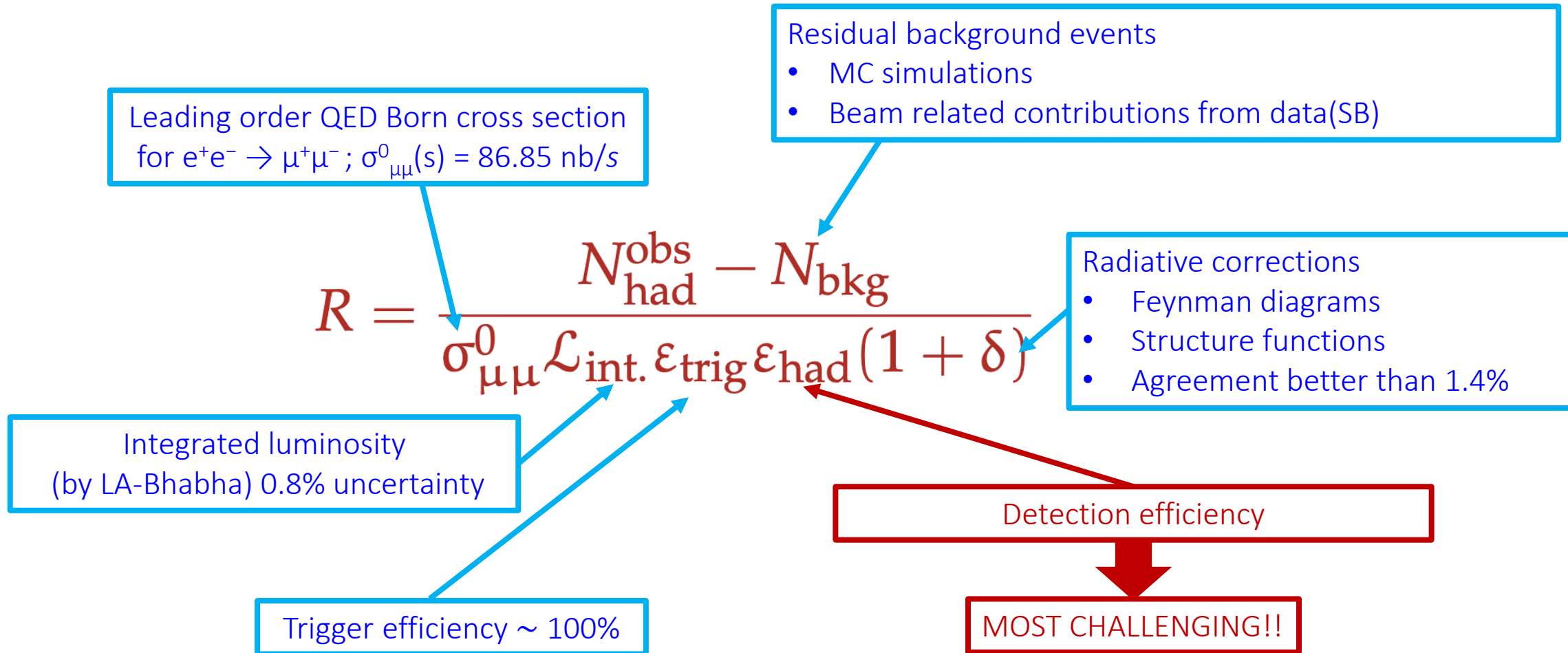
- ~20 experimental Collaborations measured R-value, ~10 in the lower energy region
- best accuracy (~ 3.3%) for R measurements achieved in the 2 ÷ 5 GeV range by BESII and KEDR at a few energy points
- systematic uncertainties dominate all R measurements

- **BESIII new R-values experimental data:**

PRL 128, 062004 (2022)

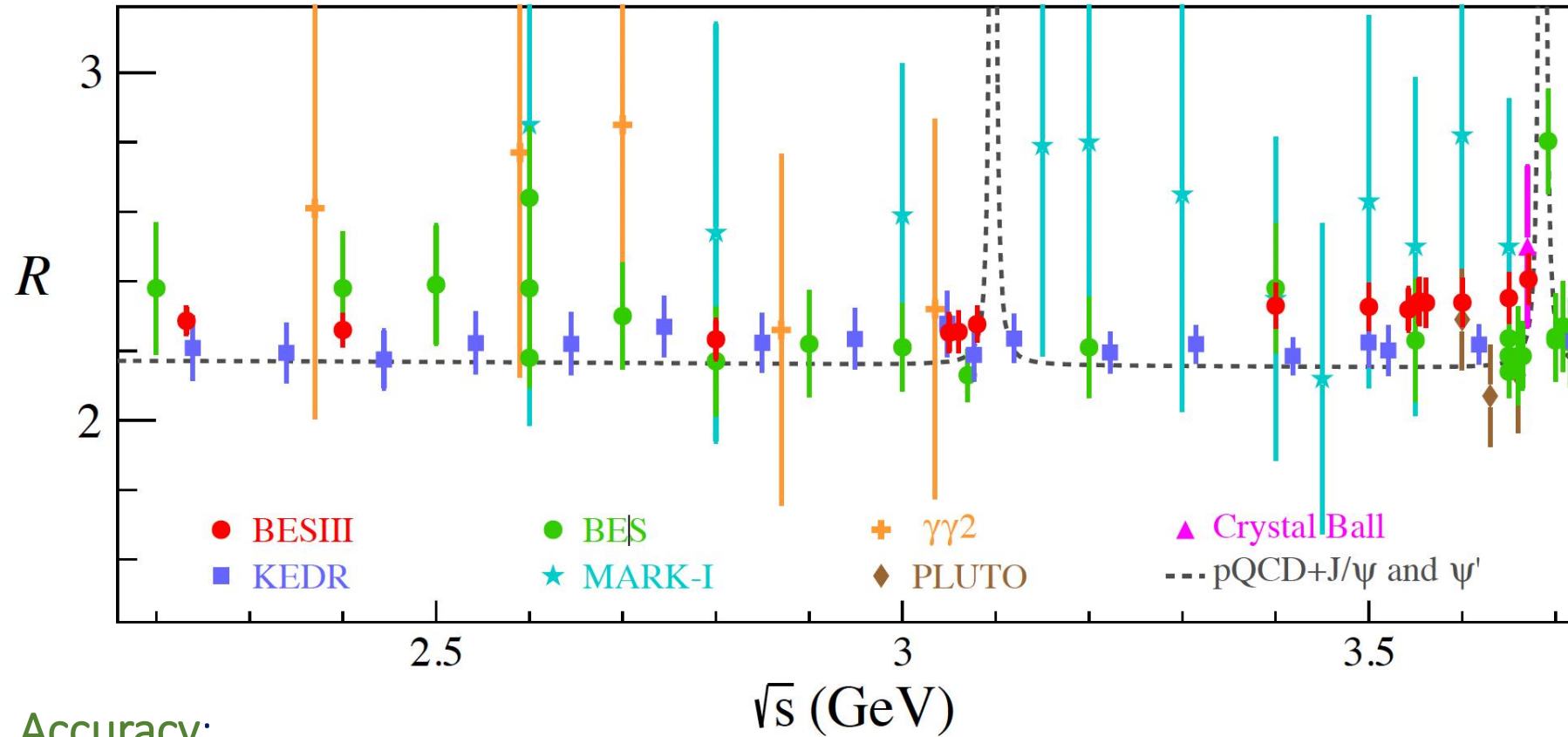
- inclusive R value measurement in 2.2 ÷ 3.7 GeV range (14 energy points, total of 52 pb⁻¹)
- Expected dominant backgrounds
 - beam associated
 - QED background events (e^+e^- , $\mu^+\mu^-$, $\tau^+\tau^-$, $\gamma\gamma$, ...)

New BESIII R-value data: determination of R



Exploiting two different signal simulations models!

BESIII experimental R data in the range 2.2 ÷ 3.7 GeV

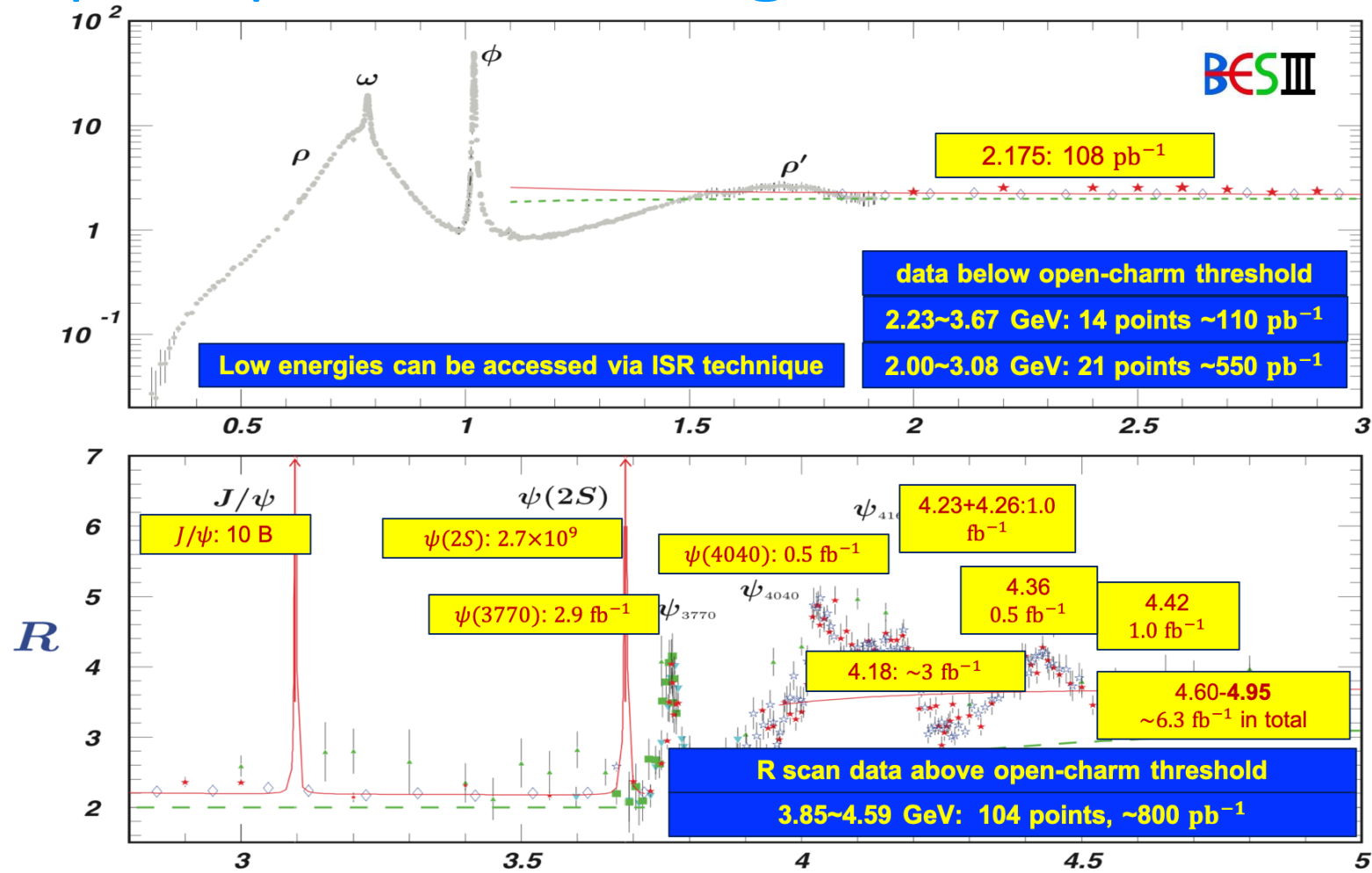


BESIII

14 energy points
total of 52 pb⁻¹

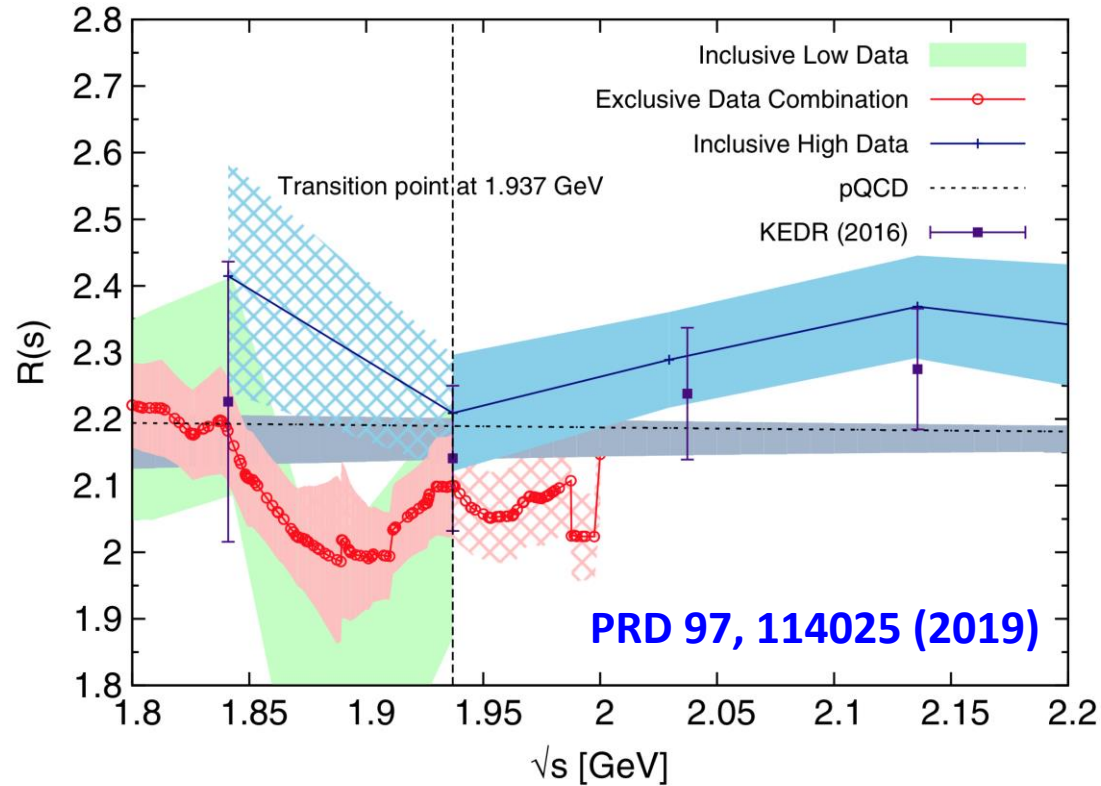
- **Accuracy:**
 - <2.6% below 3.1 GeV, 3.0% above
 - dominated by systematic uncertainties (statistic uncertainties: ~ 0.35%)
- **Average R value:**
 - larger than the pQCD prediction by **2.7 σ**
 - higher than KEDR by **1.7 σ** between 3.4 and 3.6 GeV.

BESIII perspectives: large statistics available



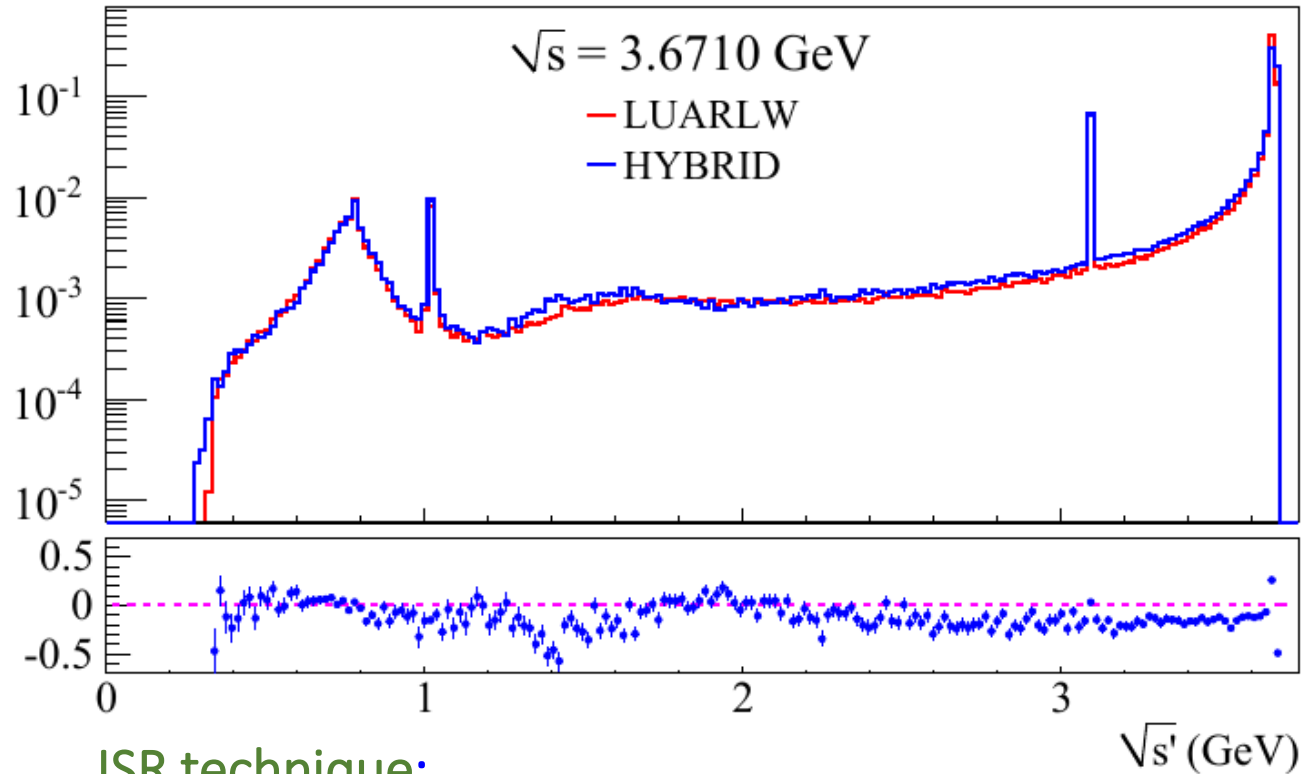
- BESIII has collected data from 2.00 to 4.95 GeV suitable for R measurements:
130 scan data points $>10^5$ hadrons
- R measurement both in the continuum and open-charm regions with high accuracy: significant impact

BESIII perspectives: exploring different methods



Exclusive vs inclusive measurements:

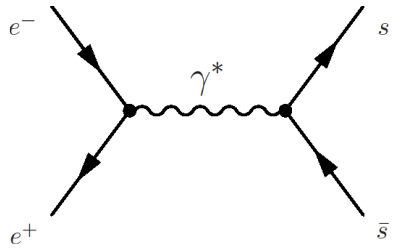
- Inclusive R measurements above 2.0 GeV
- Exclusive R measurement below 2.0 GeV
- Tension in the transition region!



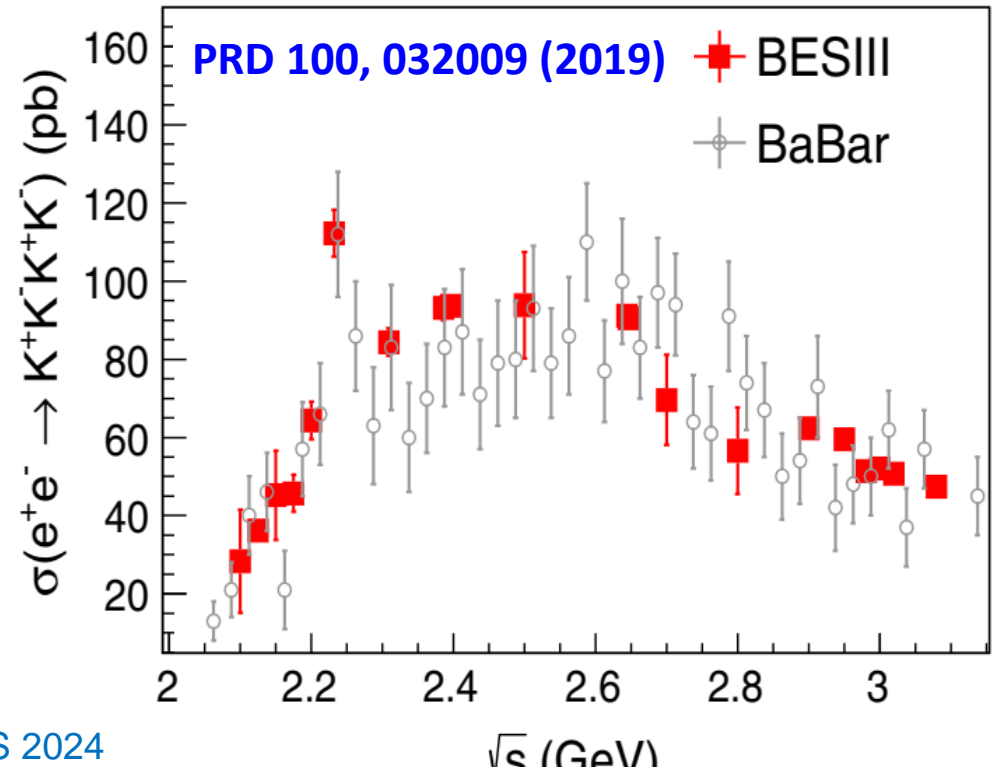
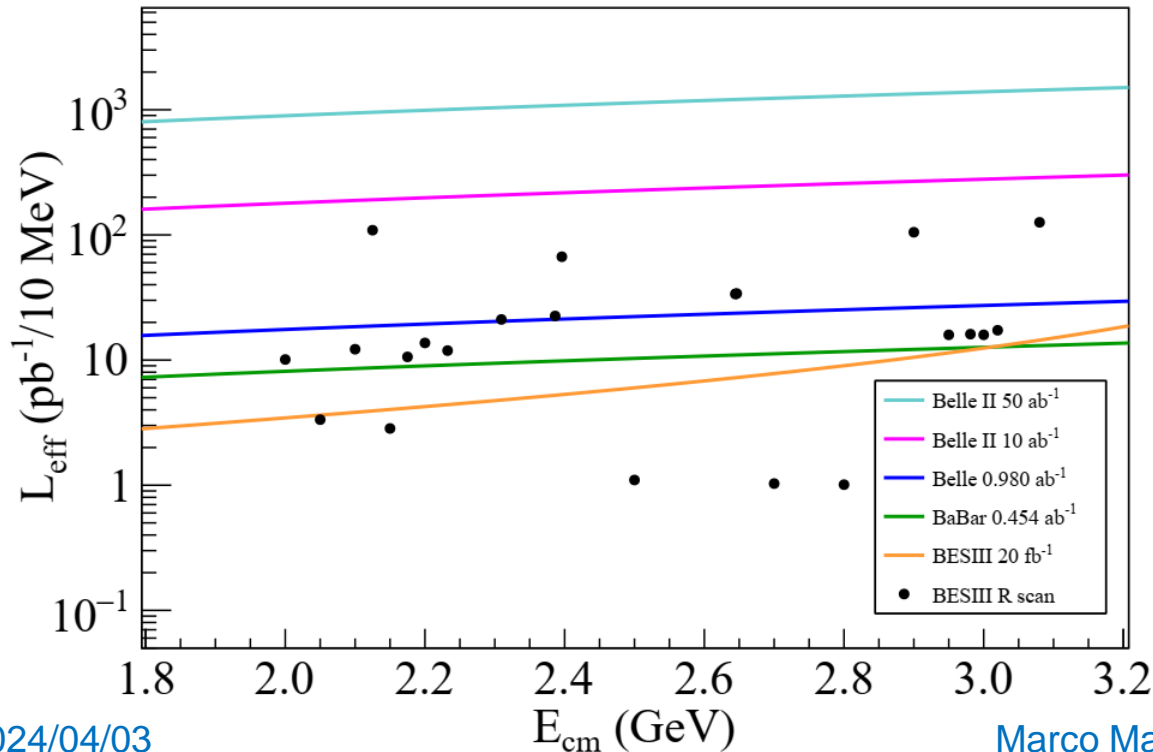
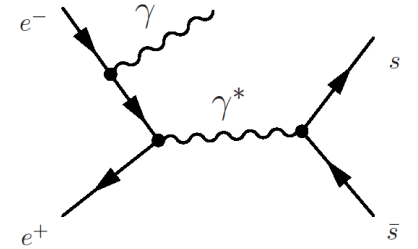
ISR technique:

- exploits large charmonia data (e.g. $\psi(3770)$)
- allows measurement from threshold to continuum
- less dependent on MC event generator
- better detection efficiency respect to scan
- allows comparison btw inclusive and exclusive measurements

Energy scan vs ISR



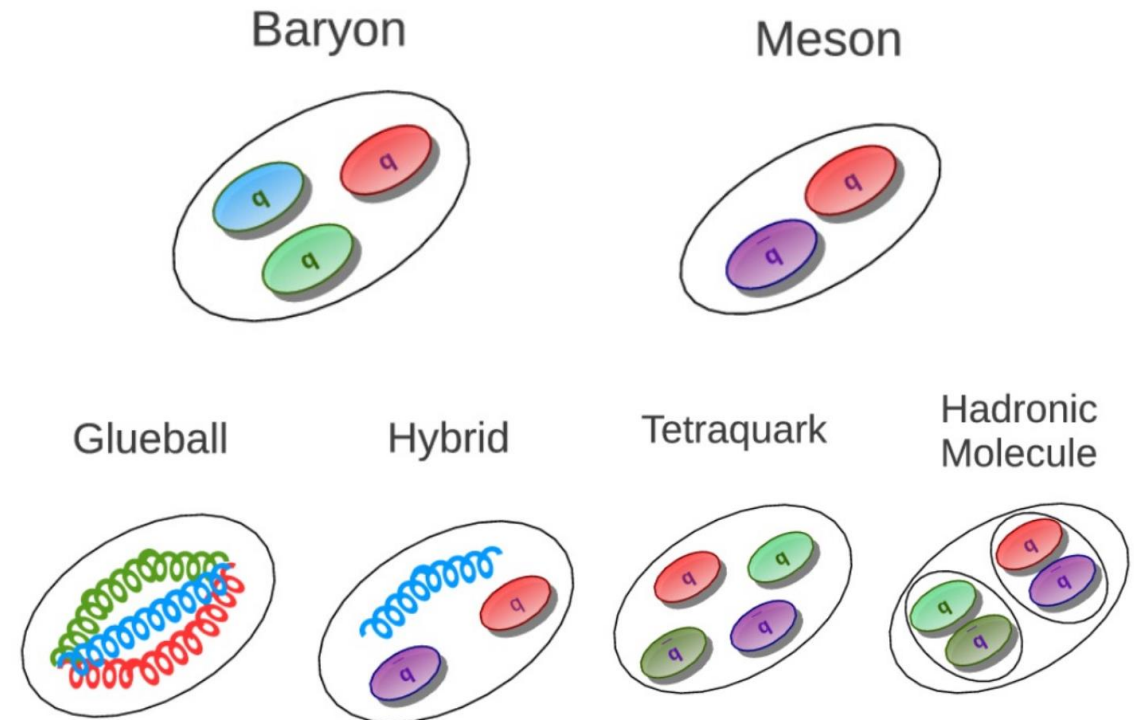
	Energy Scan	Initial State Radiation
\sqrt{s}	discrete	fixed
\mathcal{L}	low at each beam energy	high at one beam energy
σ	$\frac{d\sigma_{p\bar{p}}}{d(\cos\theta)} = \frac{\pi\alpha^2\beta C}{2q^2} [G_M ^2(1 + \cos^2\theta) + \frac{4m_p^2}{q^2} G_E ^2 \sin^2\theta]$	$\frac{d^2\sigma_{p\bar{p}\gamma}}{dq^2 d(\cos\theta_\gamma)} = \frac{1}{s} W(s, x, \theta_\gamma) \sigma_{p\bar{p}}(q^2)$ $W(s, x, \theta_\gamma) = \frac{\alpha}{\pi x} \left(\frac{2-2x+x^2}{\sin^2\theta_\gamma} - \frac{x^2}{2} \right)$
q^2	single at each beam energy	from threshold to s



Hadron Spectroscopy

QCD Exotics

- Non-exotic hadrons: mesons ($q\bar{q}$), baryons (qqq)
- QCD allows for exotic hadrons:
 - multi-quark states
 - strong evidence in heavy quark sector
 - <https://qwg.ph.nat.tum.de/exoticshub/>
 - hybrids
 - Glueballs
- BESIII is an ideal scenario for light QCD Exotics
 - Charmonium decays \rightarrow “gluon-rich processes”
 - clean high statistics data sample
 - kinematic constraints and $I(J^{PC})$ filter

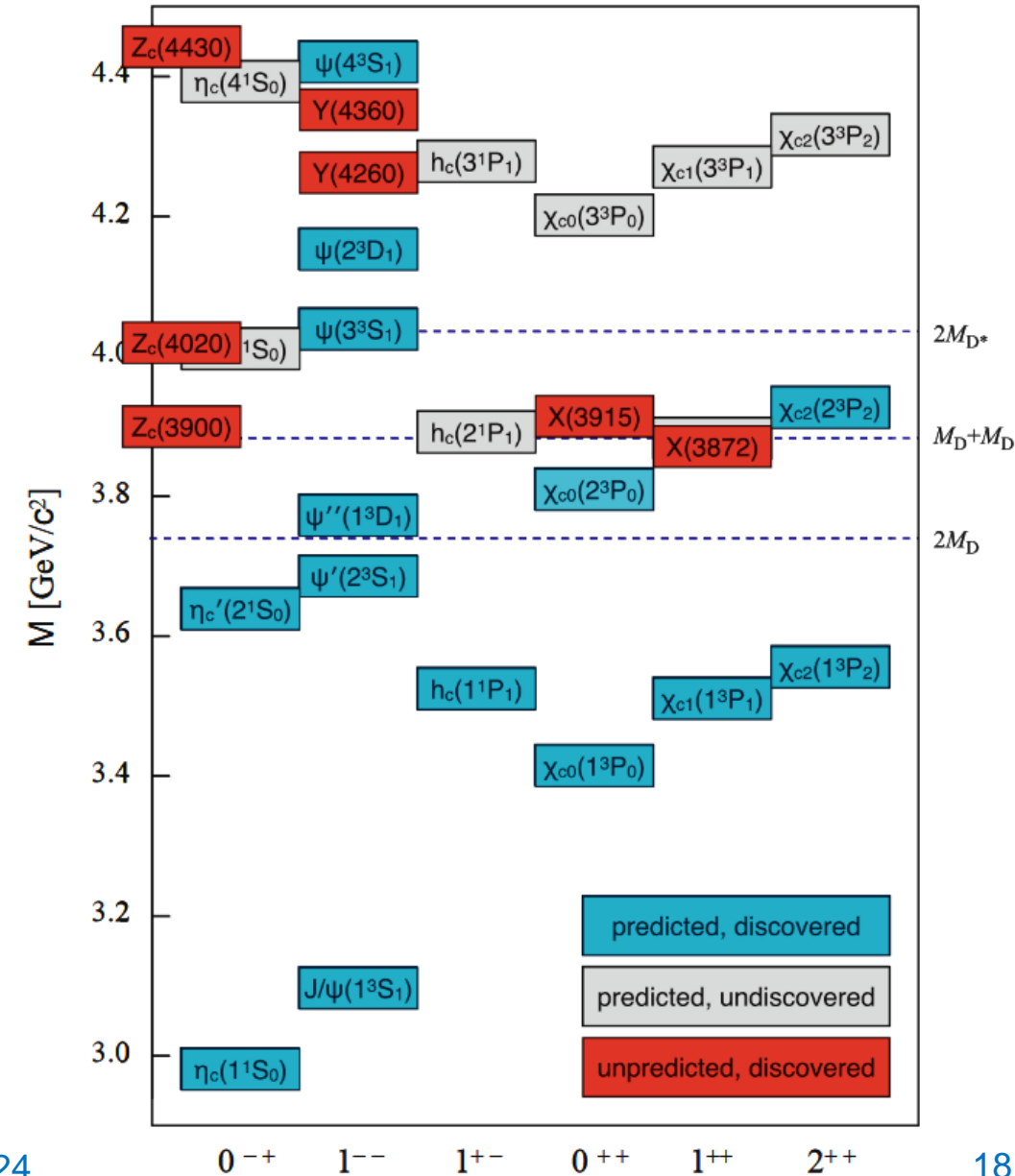


Charmonium Spectroscopy

- XYZ states: do not fit in the naïve quark model
 - X: neutral non-vector states
 - Y: neutral vector states
 - Z: charged, clearly multi-quark states

Ideal background for exotica!

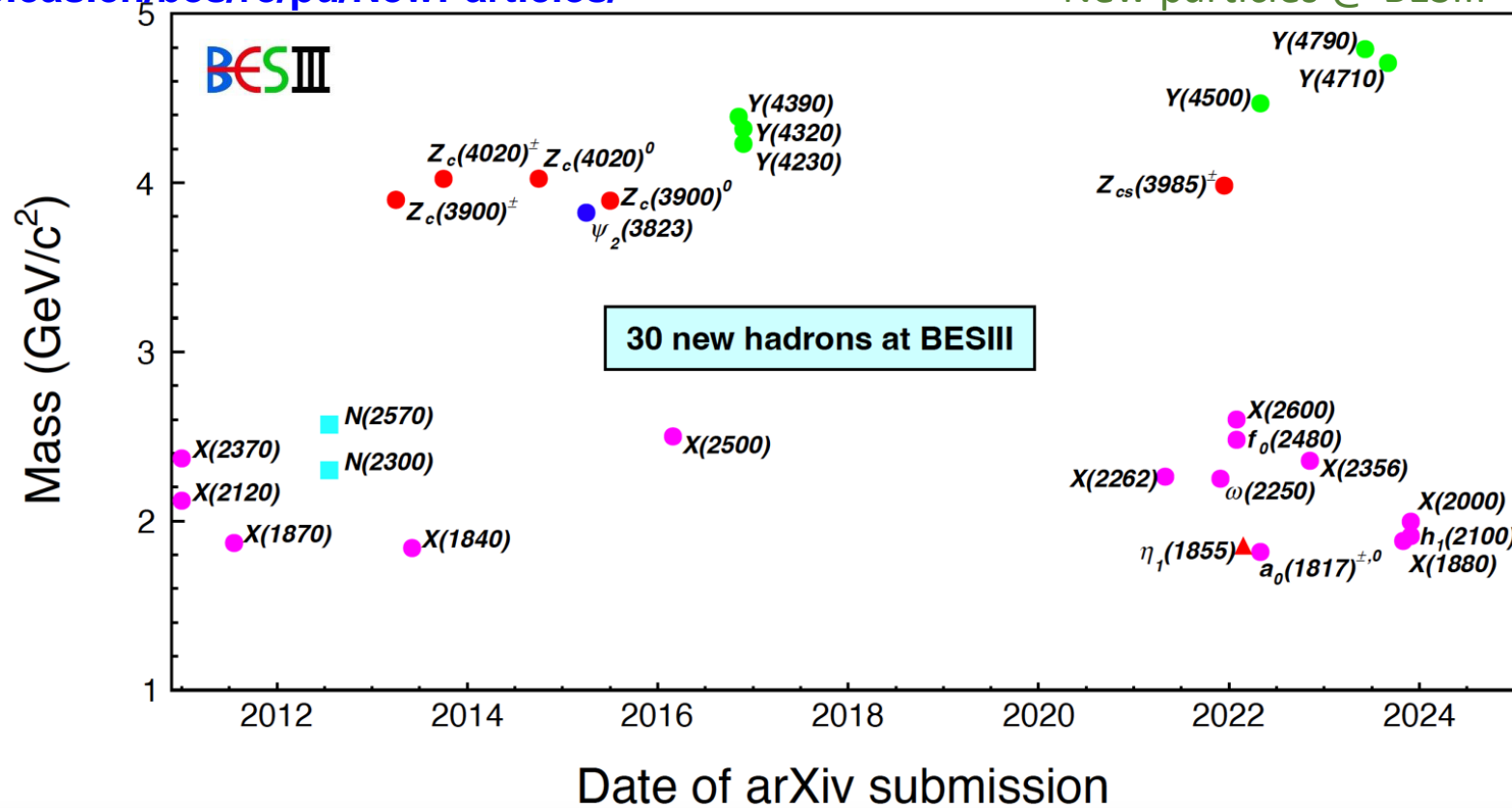
Picture cred: R. Mitchell and M. Kuessner



New discoveries

<http://english.ihep.cas.cn/bes/re/pu/NewParticles/>

New particles @ BESIII



manifestly exotic

- quark content more than $q\bar{q}$ or qqq
- \bar{q} not accessible for ordinary mesons or baryons

cryptically exotic

- overpopulation of states
- M/Γ not fitting in spectra
- production and/or decay patterns incompatible with standard baryons/mesons

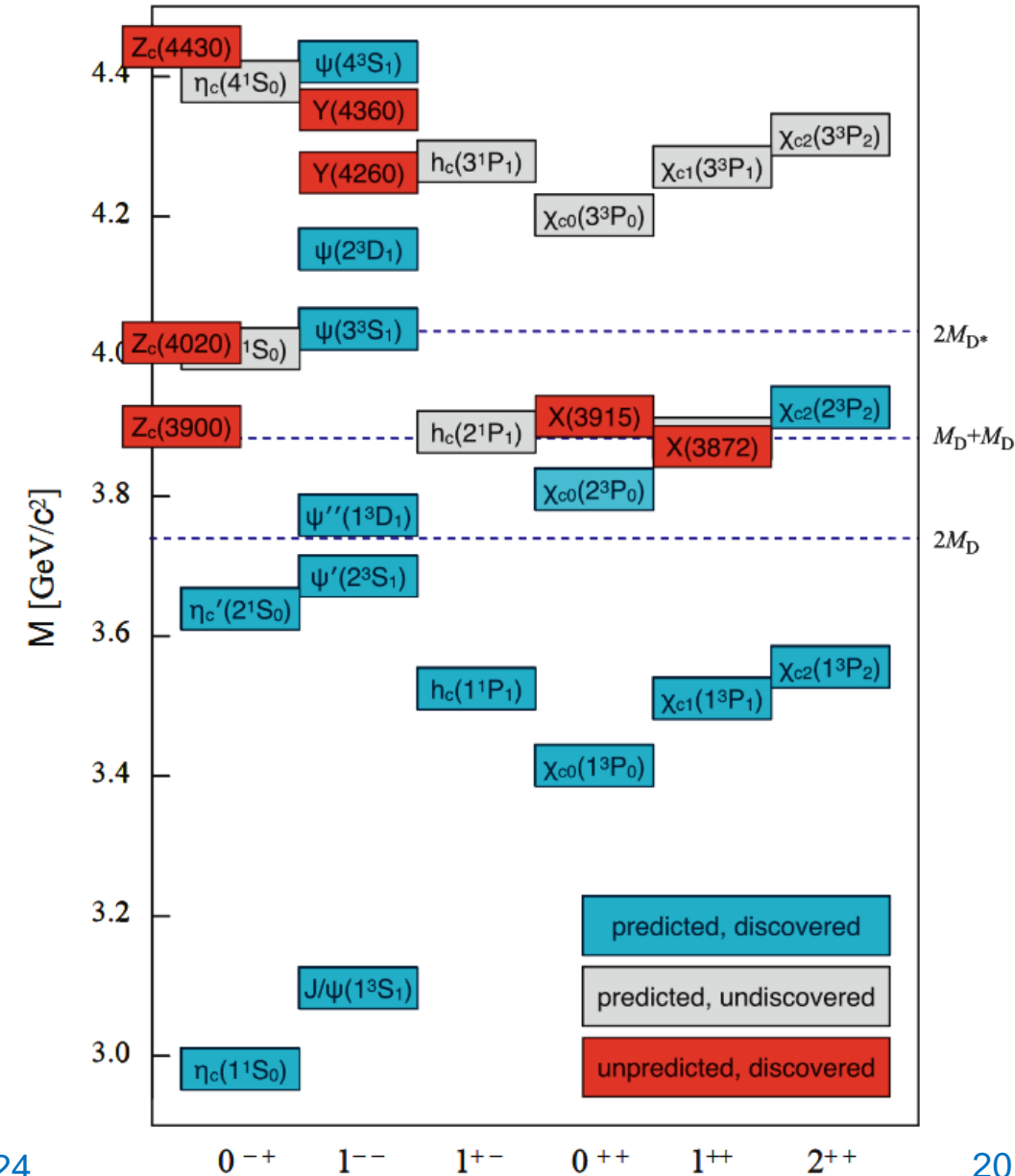
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Ideal background for exotica!

Wide focus on exotic states with charm and bottom quark but also...

Picture cred: R. Mitchell and M. Kuessner



Charmonium Spectroscopy

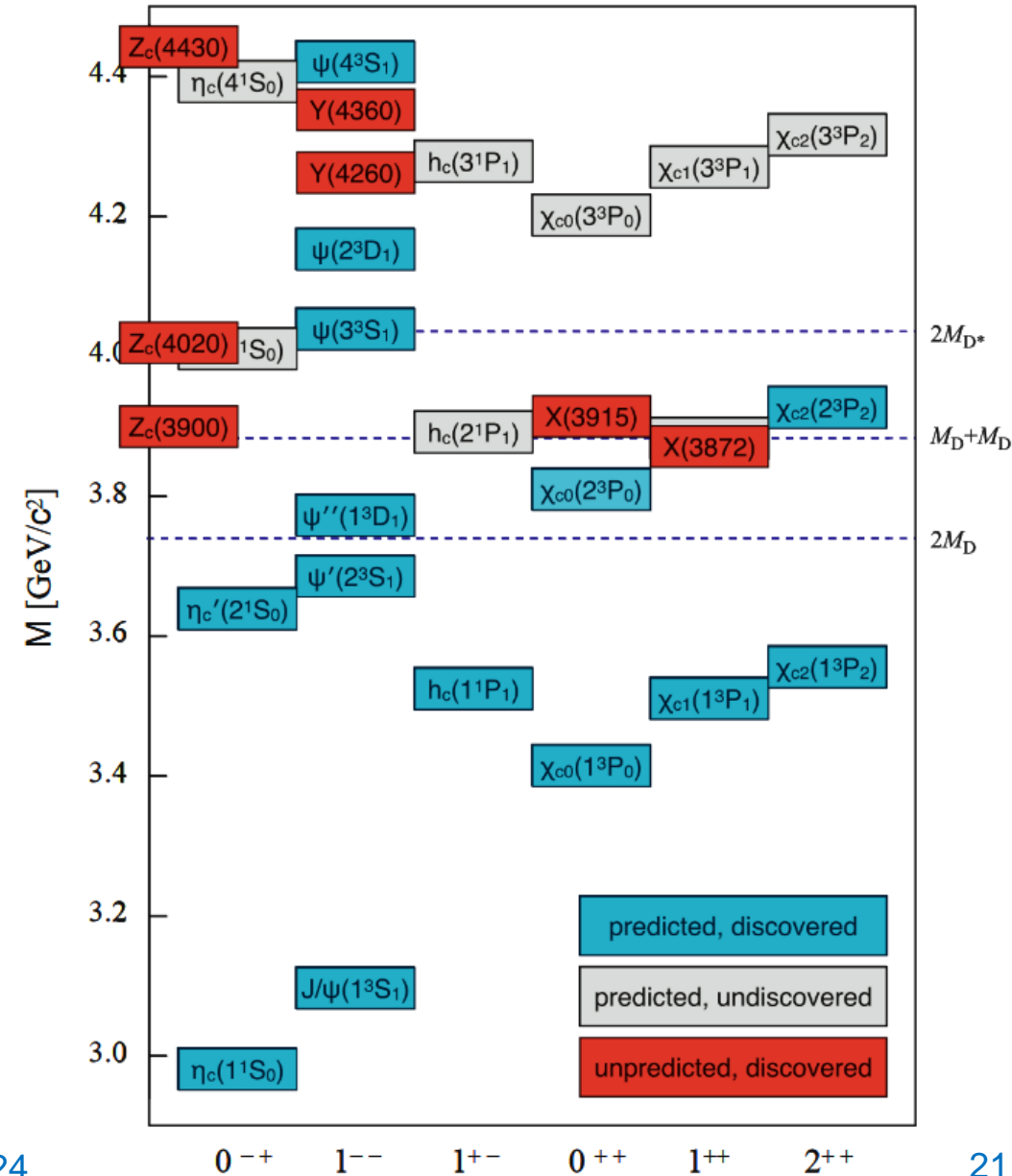
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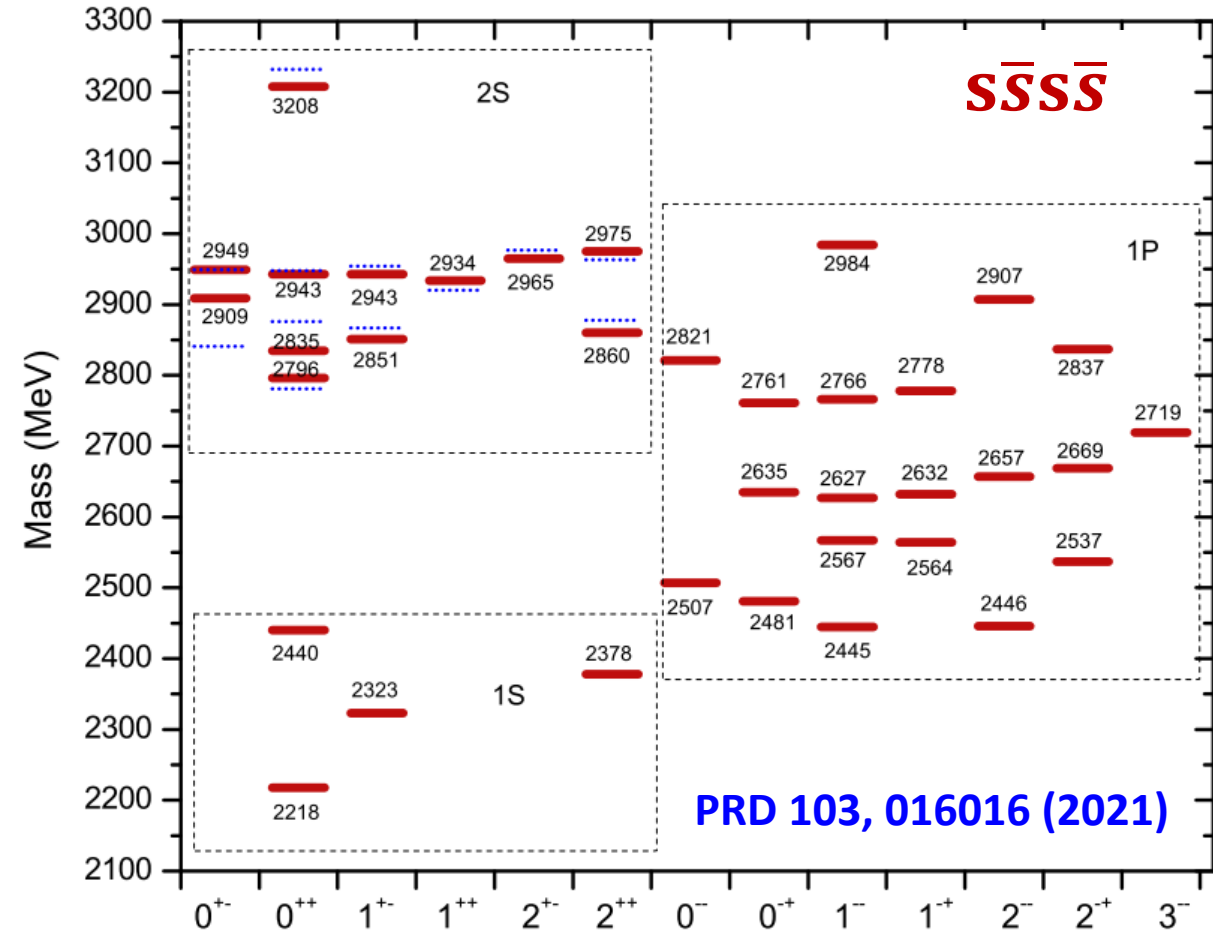
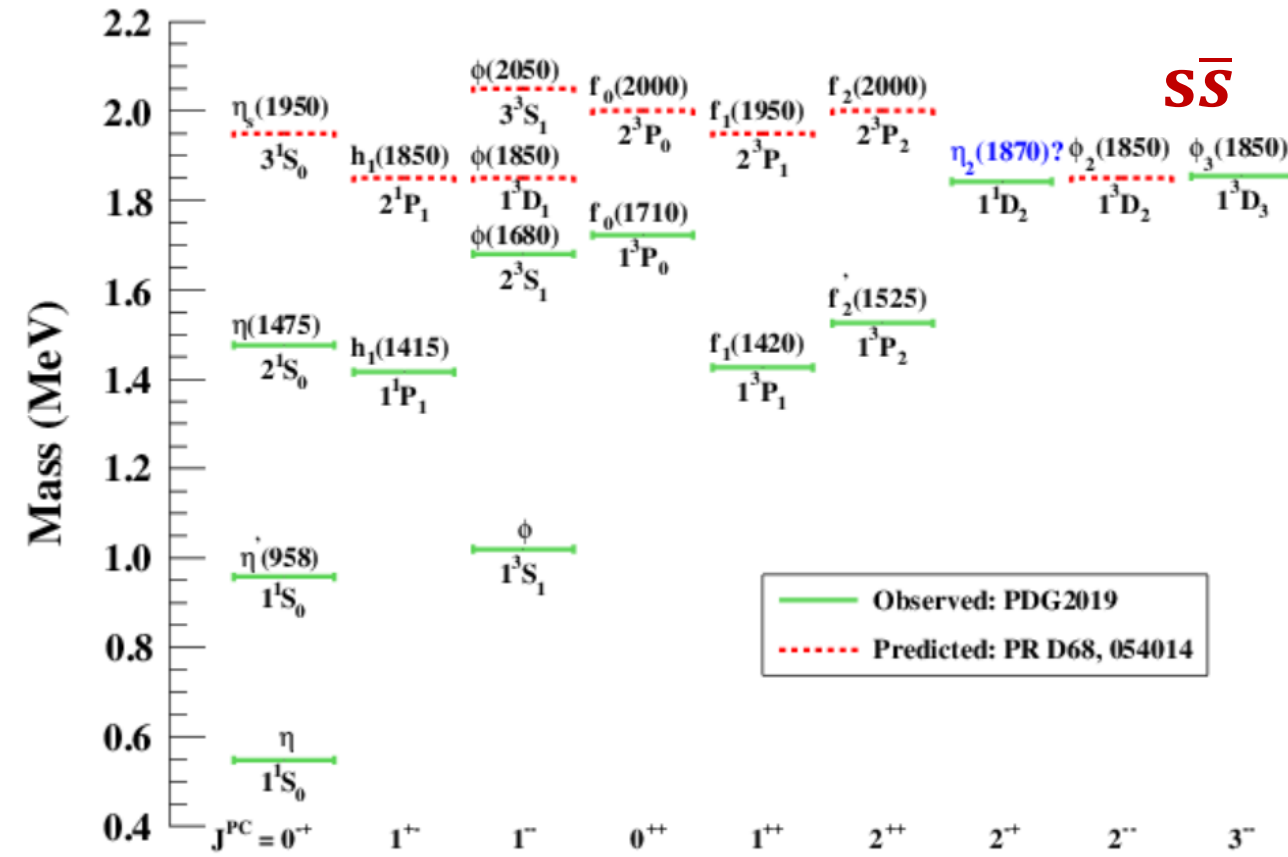
Wide focus on exotic states with charm and bottom quark but also...

masse →	2.4 MeV	1.27 GeV	171.2 GeV
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
nom →	u up	c charm	t top
Quarks	4.8 MeV	104 MeV	4.2 GeV
	$-\frac{1}{3}$	$-\frac{1}{3}$	$\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	d down	s strange	b bottom

Picture cred: R. Mitchell and M. Kuessner



Strangeonium Spectroscopy



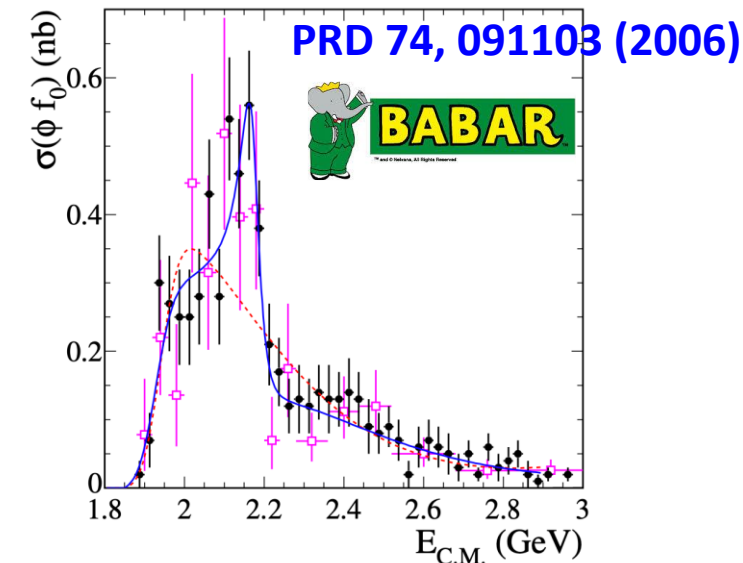
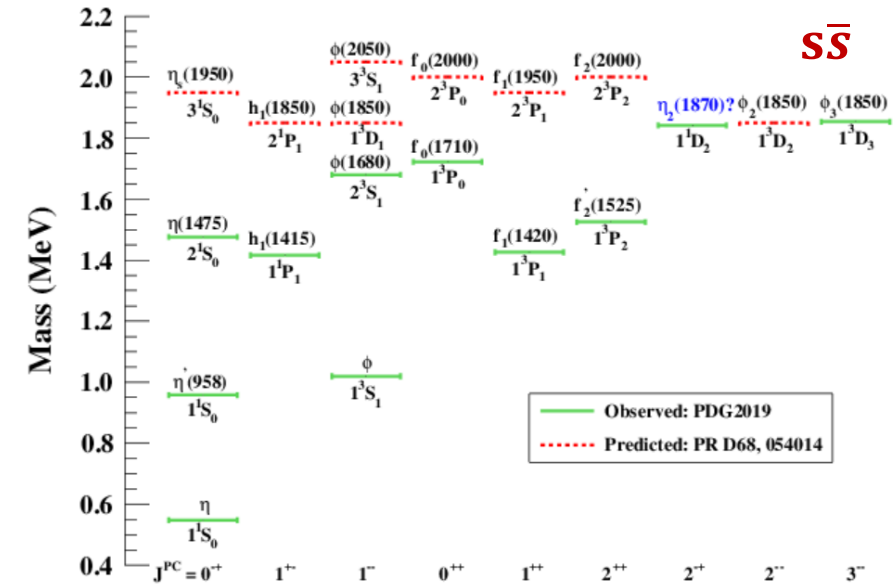
- exotic states with (just) light quarks
 - $s\bar{s}$ spectrum far from being well known
 - hybrid $s\bar{s}g$
 - tetraquark $s\bar{s}s\bar{s}/s\bar{s}u\bar{u}/s\bar{s}d\bar{d}$, ...
 - rich $s\bar{s}s\bar{s}$ spectrum spectrum

$\phi(2170) / Y(2175)$

- $\phi(2170) / Y(2175)$:
 - first observed by **BABAR** in ϕf_0 [PRD 74, 091103 (2006)]
 - later confirmed:
 - BESIII** [PRL 100, 102003 (2008)]
 - Belle** [PRD 80, 031101 (2009)]
 - $s\bar{s}$ is terra incognita:
 - low BR
 - wide Γ
 - a bridge among lighter and heavier quark states [EPJ C72, 2008 (2012)]

$$e^+e^- \Rightarrow \begin{cases} Y(2175) \rightarrow \phi(1020)\pi^+\pi^- & \text{strange,} \\ Y(4260) \rightarrow J/\psi\pi^+\pi^- & \text{charm,} \\ Y(10860) \rightarrow \Upsilon(1S, 2S)\pi^+\pi^- & \text{bottom,} \end{cases}$$

1. produced in e^+e^- collisions hence 1^{--} states
2. observed di-pion transitions in the three cases
3. observed anomalous phenomena in e^+e^- collisions at the relevant energies

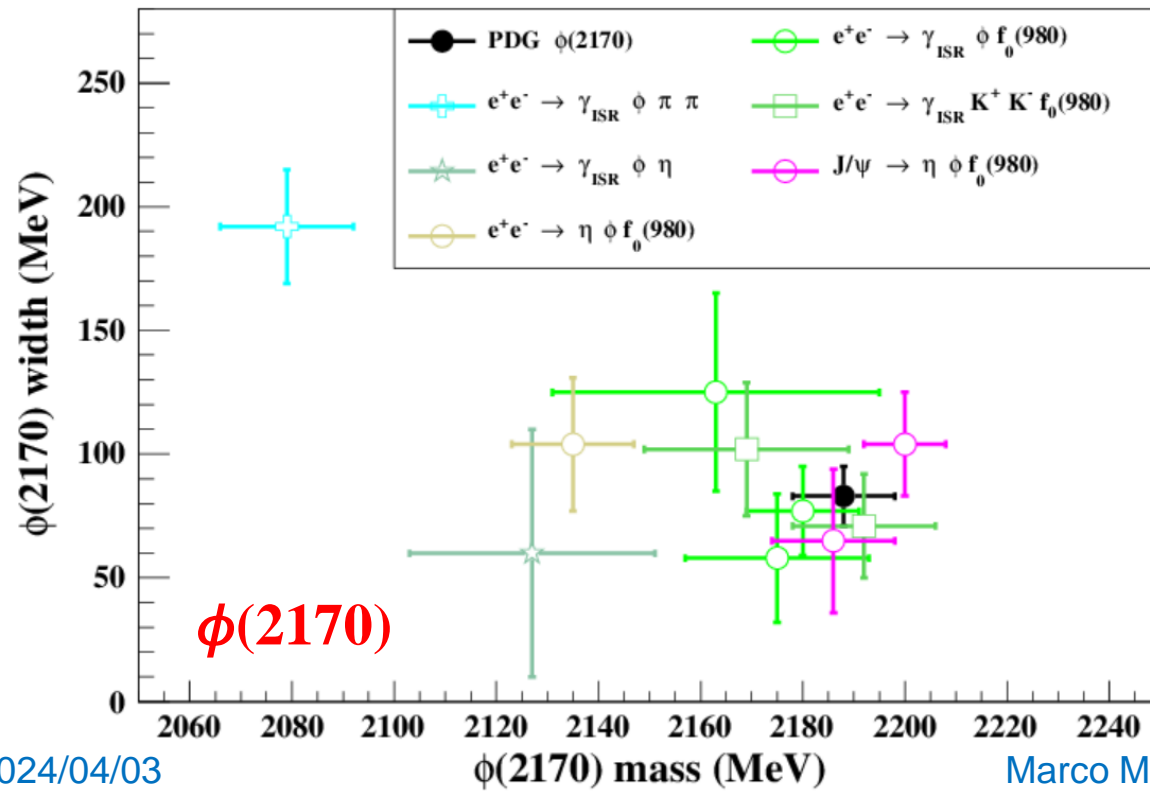


$\phi(2170) / \Upsilon(2175)$

PDG2018

$\phi(2170)$ DECAY MODES

Mode	Fraction (Γ_i/Γ)
Γ_1 $e^+ e^-$	seen
Γ_2 $\phi \eta$	
Γ_3 $\phi \pi \pi$	
Γ_4 $\phi f_0(980)$	seen
Γ_5 $K^+ K^- \pi^+ \pi^-$	
Γ_6 $K^+ K^- f_0(980) \rightarrow K^+ K^- \pi^+ \pi^-$	seen
Γ_7 $K^+ K^- \pi^0 \pi^0$	
Γ_8 $K^+ K^- f_0(980) \rightarrow K^+ K^- \pi^0 \pi^0$	seen
Γ_9 $K^{*0} K^\pm \pi^\mp$	not seen
Γ_{10} $K^*(892)^0 \bar{K}^*(892)^0$	not seen



- **experimental scenario:**

- **limited decay modes**
- **mass and width inconsistencies**

- **$\phi(2170)$ interpretations:**

- 2^3D_1 or 3^3S_1 $s\bar{s}$
 - $s\bar{s}g$ hybrid
 - **tetraquark**
 - **molecular $\Lambda\bar{\Lambda}$ state**
 - $\phi f_0(980)$ resonance with FSI
 - **three body ϕKK system**
- needing better knowledge of $\rho^*/\omega^*/\phi^*$ @ ~ 2.2 GeV

BESIII R scan: probing vector states

- published/submitted paper:

1. $e^+e^- \rightarrow K^+ K^-$: PRD 99, 032001 (2019)
2. $e^+e^- \rightarrow \phi K^+ K^-$: PRD 100, 032009 (2019)
3. $e^+e^- \rightarrow K^+ K^- \pi^0 \pi^0$: PRL 124, 112001 (2020)
4. $e^+e^- \rightarrow \phi \eta'$: PRD 102, 012008 (2020)
5. $e^+e^- \rightarrow \omega \eta$, $e^+e^- \rightarrow \omega \pi^0$: PLB 813, 136059 (2021)
6. $e^+e^- \rightarrow \phi \eta$: PRD 104, 032007 (2021)
7. $e^+e^- \rightarrow K_S K_L$: PRD 104, 032007 (2021)
8. $e^+e^- \rightarrow \eta' \pi^+ \pi^-$: PRD 104, 092014 (2021)
9. $e^+e^- \rightarrow \omega \pi^0 \pi^0$: PRD 105, 032005 (2022)
10. $e^+e^- \rightarrow K^+ K^- \pi^0$: JHEP 07, 045 (2022)
11. $e^+e^- \rightarrow \omega \pi^+ \pi^-$: JHEP 01, 111 (2023)
12. $e^+e^- \rightarrow \phi \pi^+ \pi^-$: PRD 108, 032011 (2023)
13. $e^+e^- \rightarrow \pi^+ \pi^- \pi^0$: arXiv:2401.14711
14. $e^+e^- \rightarrow \eta \pi^+ \pi^-$: PRD 108, L111101 (2023)
15. $e^+e^- \rightarrow K_S K_L \pi^0$: JHEP 01, 180 (2024)

- ongoing analyses:

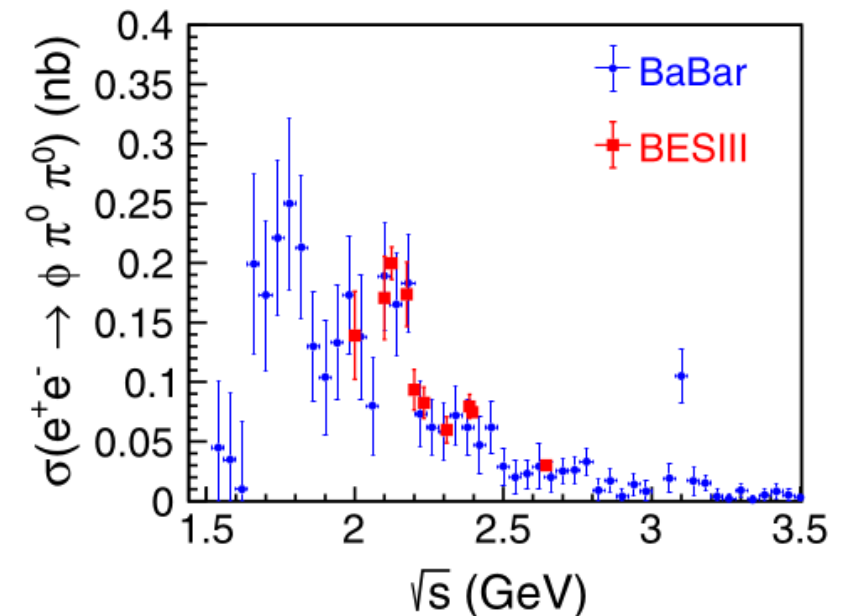
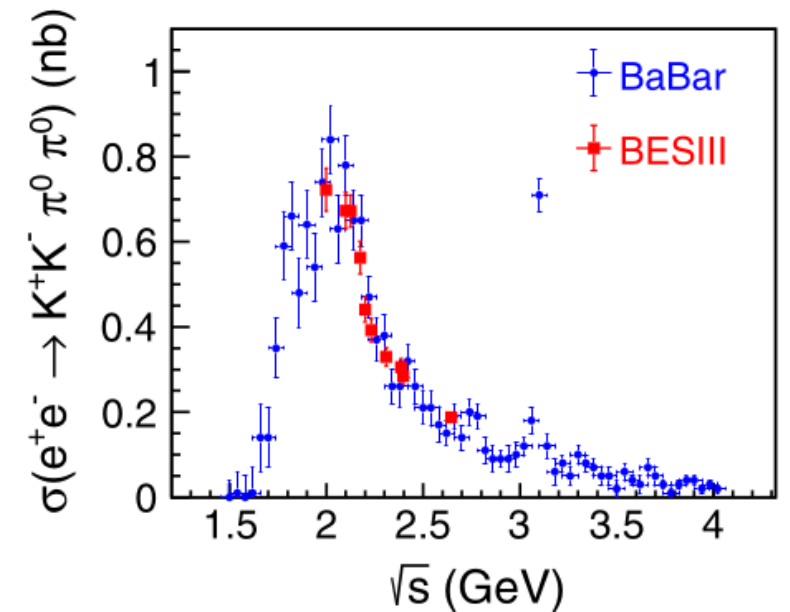
1. $e^+e^- \rightarrow \omega \eta'$
2. $e^+e^- \rightarrow \omega K^+ K^-$
3. $e^+e^- \rightarrow \gamma \eta'$
4. $e^+e^- \rightarrow K_S K^\pm \pi$
5. $e^+e^- \rightarrow \omega \eta \pi$
6. $e^+e^- \rightarrow K^+ K^- \pi^+ \pi^-$
7. $e^+e^- \rightarrow f_1(1285) \pi^+ \pi^-$
8. $e^+e^- \rightarrow \omega \pi^+ \pi^- \pi^0$
9. $e^+e^- \rightarrow \pi^+ \pi^- 2\pi^0$

$\phi(2170) / Y(2175): e^+ e^- \rightarrow K^+ K^- \pi^0 \pi^0$

- $e^+ e^- \rightarrow K^+ K^- \pi^0 \pi^0$ [PRD 124, 112001 (2020)]
 - PWA on 300 pb^{-1} data between 2.00 and 2.644 GeV
 - cross sections consistent with BABAR data, more precise
 - $M = (2126.5 \pm 16.8 \pm 12.4) \text{ MeV}/c^2$
 - $\Gamma = (106.9 \pm 32.1 \pm 28.1) \text{ MeV}$
 - statistical significance: 6.3σ ; $J^{PC} = 1^{--}$
 - simultaneous fit on 4 channels

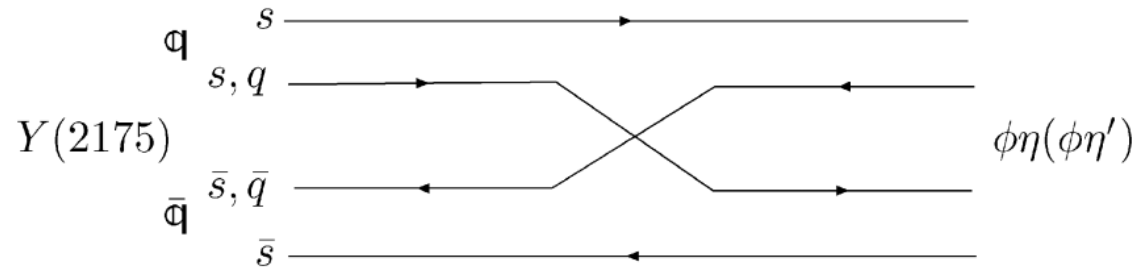
Channel		$\mathcal{B}_r \Gamma_R^{e^+ e^-}$ (eV)	ϕ (rad)	significance (σ)
$K^+(1460)K^-$		3.0 ± 3.8	5.6 ± 1.5	4.4
$K_1^+(1400)K^-$	Solution 1	4.7 ± 3.3	3.7 ± 0.4	4.8
	Solution 2	98.8 ± 7.8	4.5 ± 0.3	
$K_1^+(1270)K^-$	Solution 1	7.6 ± 3.7	4.0 ± 0.2	1.4
	Solution 2	152.6 ± 14.2	4.5 ± 0.1	
$K^{*+}(892)K^{*-}(892)$		0.04 ± 0.2	5.8 ± 1.9	1.2

- consistent with $\phi(2170)$
- not consistent with 3^3S_1 or 2^3D_1 (K^*K^* decay favoured)
- not consistent with $s\bar{s}g$ (comparing dominant decays)

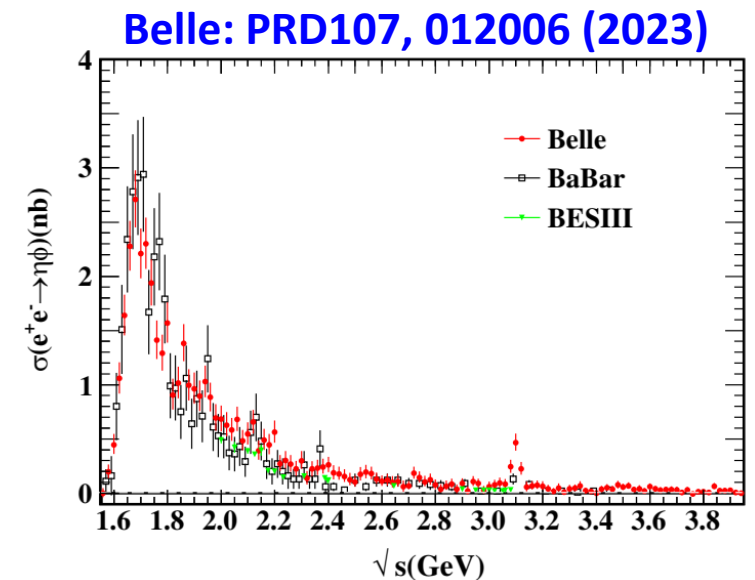
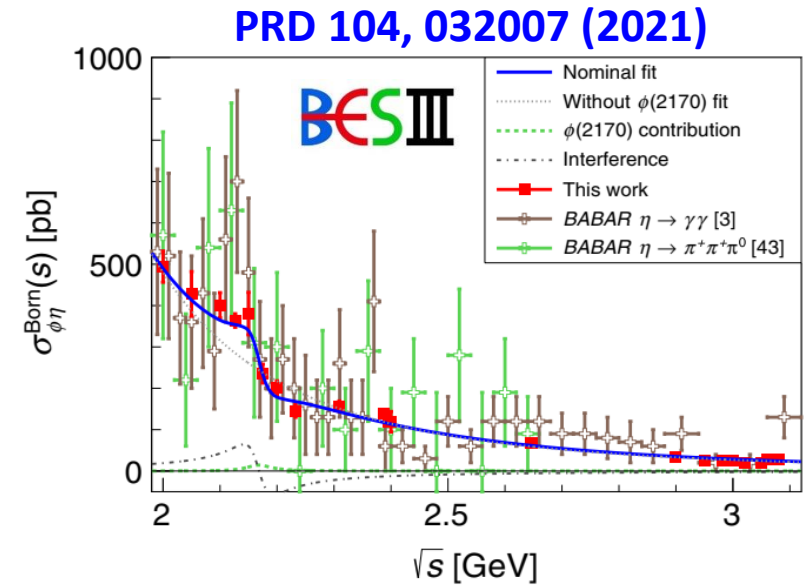


$\phi(2170) / Y(2175): e^+ e^- \rightarrow \phi\eta, \phi\eta'$

- $e^+ e^- \rightarrow \phi\eta$ [PLB 669, 160 (2008): significant contribution]

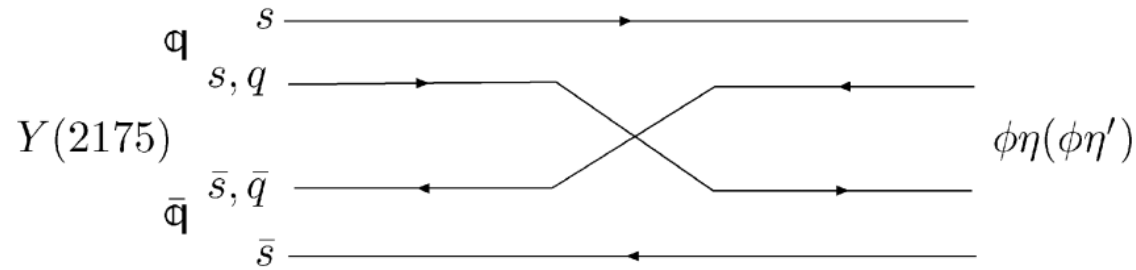


- 715 pb^{-1} data between 2.00 and 3.08 GeV
- $M = (2163.5 \pm 6.2 \pm 3.0) \text{MeV}/c^2$
- $\Gamma = (31.1_{-11.6}^{+21.1} \pm 1.1) \text{MeV}$
- statistical significance: $> 10.9 \sigma$; $J^{PC} = 1^{--}$
- ω^* OZI suppressed, ρ^* suppressed by isoscalar mode

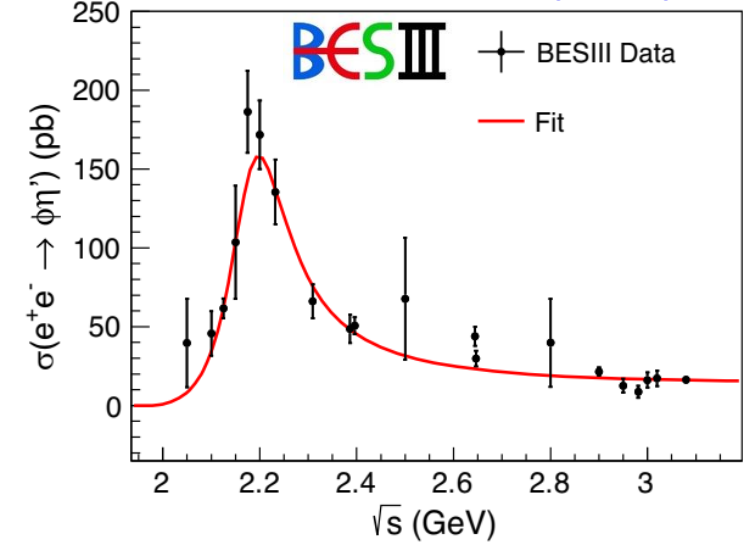


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PRD 102, 012008 (2020)

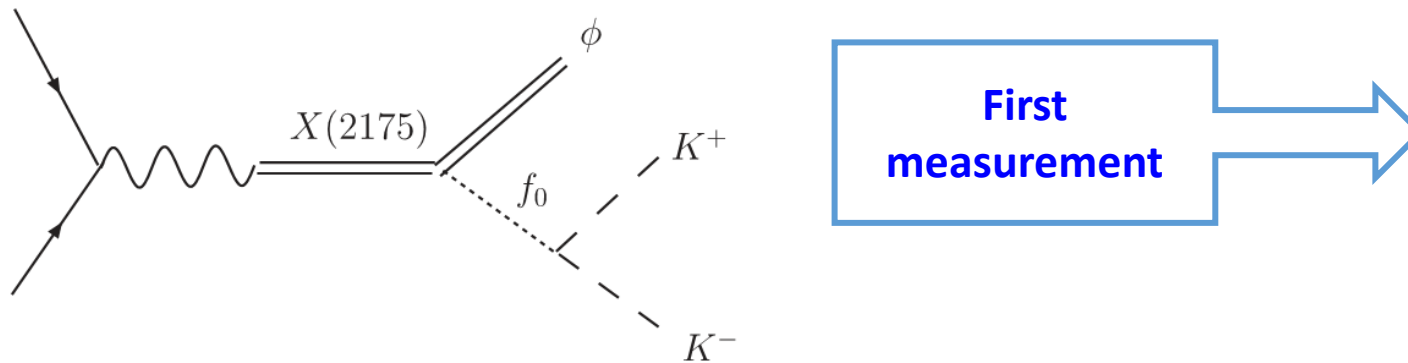


- 640 pb^{-1} data between 2.05 and 3.08 GeV
- cross sections consistent with BABAR, more precise
- $M = (2177.5 \pm 4.8 \pm 19.5) \text{ MeV}/c^2$
- $\Gamma = (149.0 \pm 15.6 \pm 8.9) \text{ MeV}$
- statistical significance: $> 10 \sigma$; $J^{PC} = 1^{--}$
- $\frac{\mathcal{B}(e^+ e^- \rightarrow \phi\eta)}{\mathcal{B}(e^+ e^- \rightarrow \phi\eta')} = 0.23 \pm 0.10 \pm 0.18 \ll \mathbf{s\bar{s}g}$ hybrid model predictions [PRD59,034016; PLB650,390]
- $2^3D_1 \mathbf{s\bar{s}}$ disfavoured by resonance parameters, $3^3S_1 \mathbf{s\bar{s}}$ disfavoured by larger predicted Γ

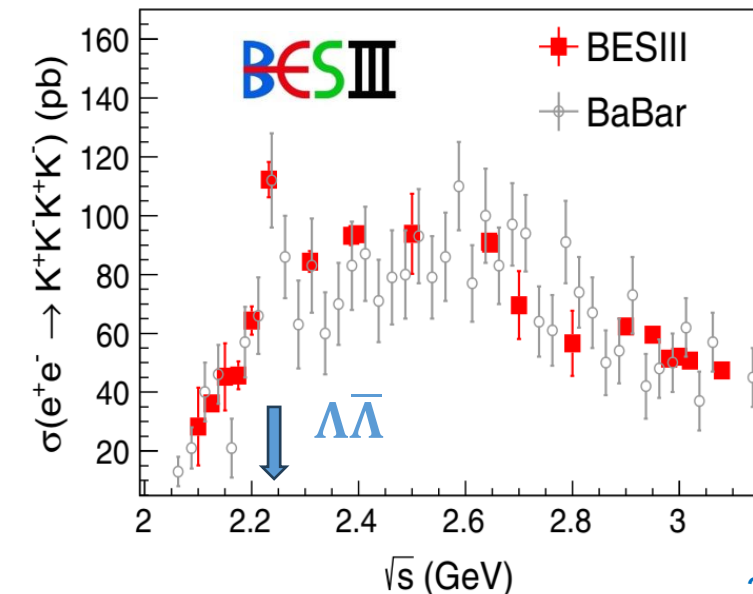
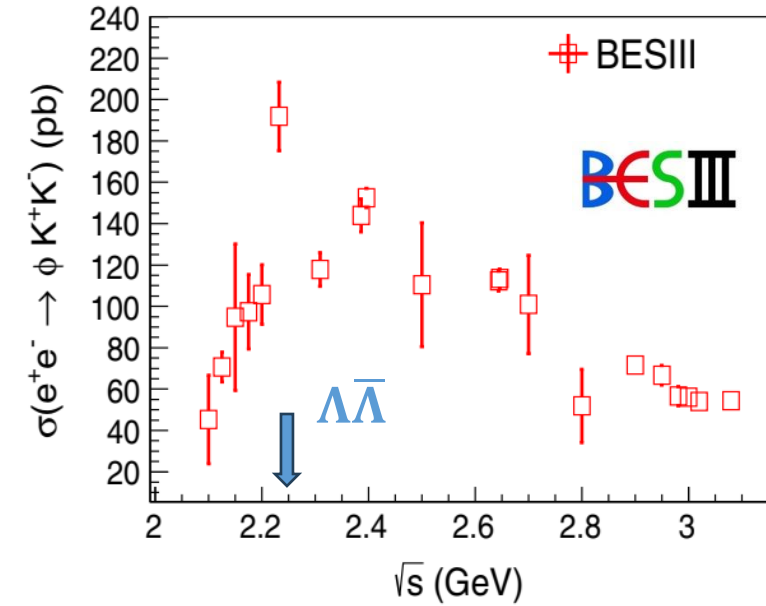
$\phi(2170) / Y(2175): e^+ e^- \rightarrow \phi K^+ K^-, K^+ K^- K^+ K^-$

PRD 100, 022009 (2019)

- $e^+ e^- \rightarrow \phi(2170) \rightarrow \phi K^+ K^-$



- $\phi(2170)$ is predicted to be a $\phi K^+ K^-$ resonance [PRD 79 034018 (2009)]
- 650 pb^{-1} data between 2.00 and 3.08 GeV
- cross sections consistent with BABAR, more precise
- similar enhancement @ 2.2324 GeV, near $\Lambda\bar{\Lambda}$ threshold
- hint for a narrow resonance ($\Gamma < 20 \text{ MeV}$) at $\Lambda\bar{\Lambda}$ threshold

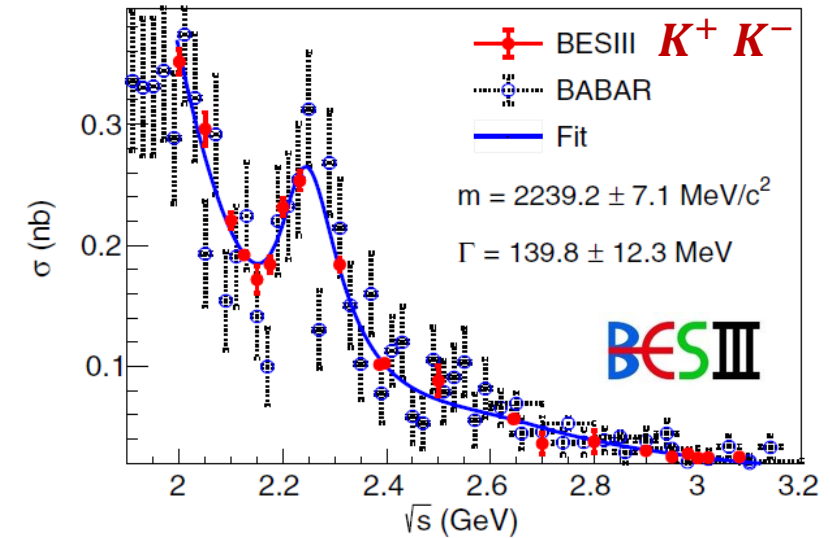


$\phi(2170) / Y(2175): e^+ e^- \rightarrow K^+ K^-, K_S K_L$

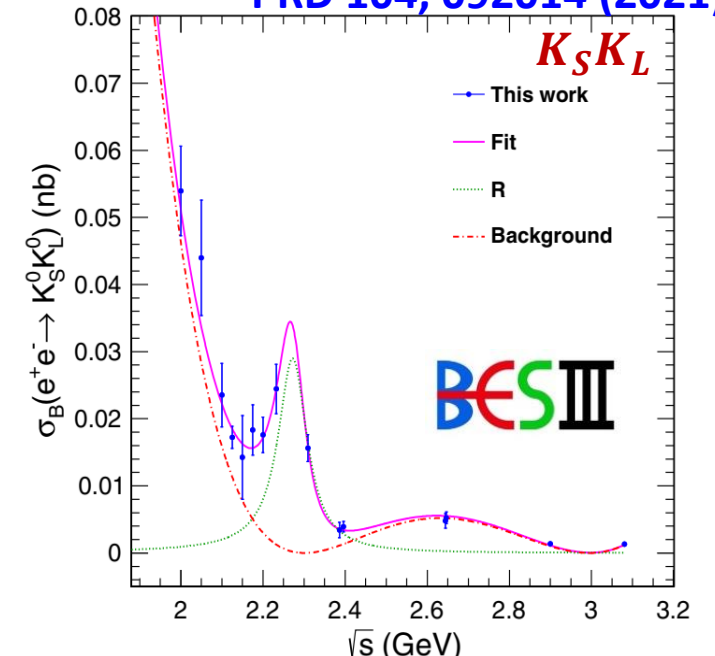
PRD 99, 032001 (2019)

- $e^+ e^- \rightarrow K^+ K^-, K_S K_L$
- 582 pb^{-1} data between 2.00 and 3.08 GeV
- one resonance at $K^+ K^-$ and $K_S K_L$

	$K^+ K^-$	$K_S K_L$
Mass (MeV/c^2)	$2239.2 \pm 7.1 \pm 11.3$	$2273.7 \pm 5.7 \pm 19.3$
Width (MeV)	$139.8 \pm 12.3 \pm 20.6$	$86 \pm 44 \pm 51$
$\Gamma_{ee} \text{Br}$ (eV)		$0.9 \pm 0.6 \pm 0.7$



PRD 104, 092014 (2021)

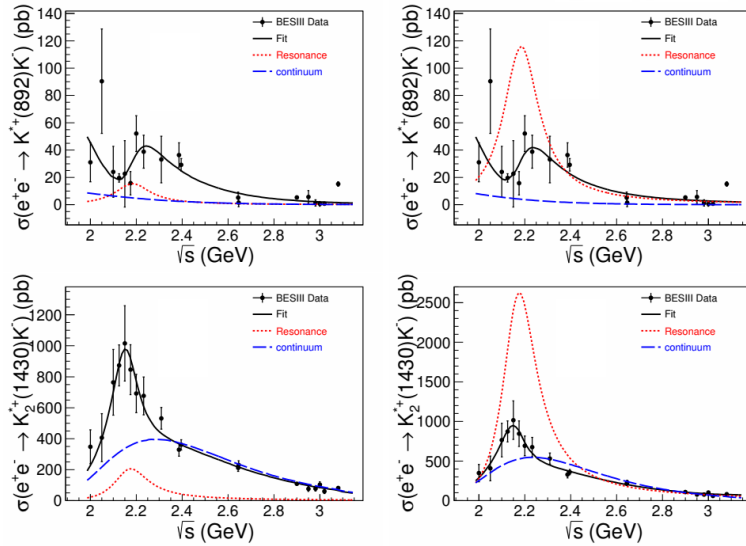


- Dominant KK mode @ $\phi(2170)$?
 - Iso-scalar: ω^*/ϕ^* ; iso-vector: ρ^*
 - Extract isospin component

$\phi(2170) / \Upsilon(2175): e^+e^- \rightarrow K^+K^-\pi^0$

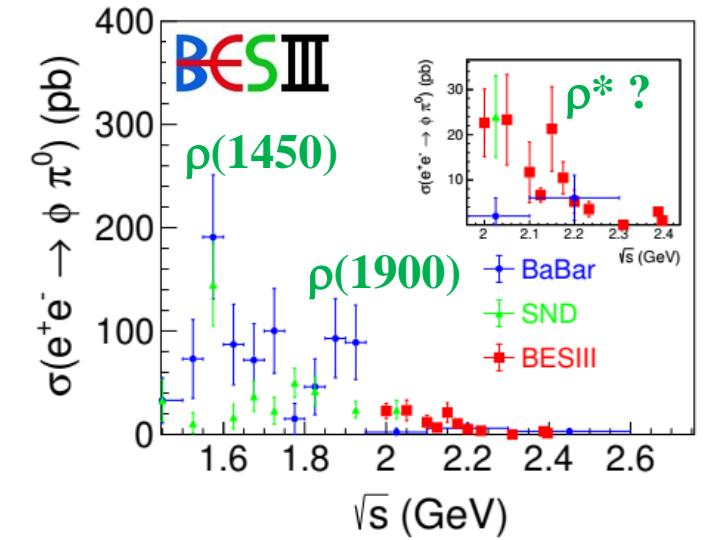
JHEP 07, 045 (2022)

BESIII



	$K_2^*(1430)K$	$K^*(892)K$
Mass (MeV/c ²)	$2190 \pm 19 \pm 37$	
Width (MeV)	$191 \pm 28 \pm 60$	
$\Gamma_{ee} Br$ (eV)	12.6 ± 2.4	1.0 ± 0.3
	161.1 ± 20.6	7.1 ± 0.9

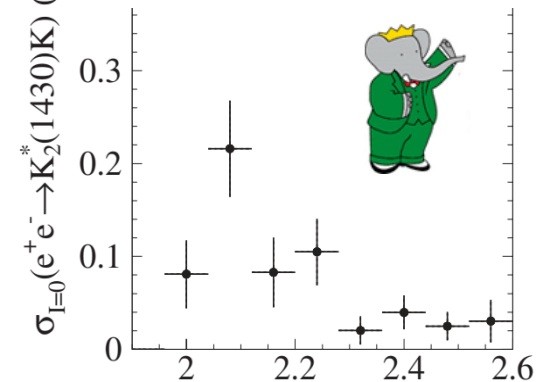
$$\frac{\mathcal{B}(\phi(2170) \rightarrow K_2^+(1430)K^-)}{\mathcal{B}(\phi(2170) \rightarrow K^+(892)K^-)} = \frac{12.6 \pm 4.5}{(22.7 \pm 4.1)}$$



$e^+e^- \rightarrow K^+K^-\pi^0$

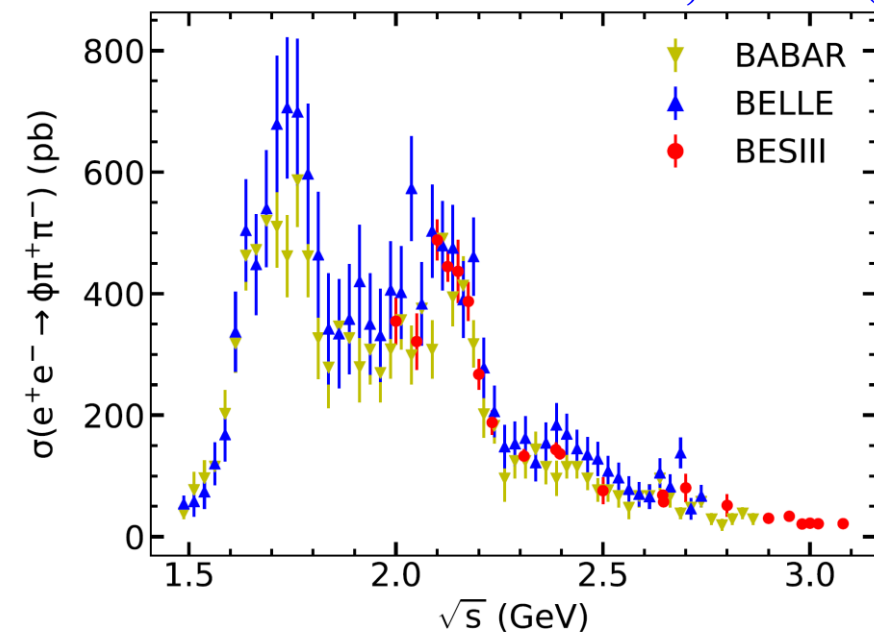
- 648 pb⁻¹ data between 2.00 and 3.08 GeV
- cross sections consistent with BABAR, more precise
- resonance in $K_2^*(1430)K / K^*(892)$, statistical significance: $> 7.1 \sigma$
- compatible with $\phi(2170)$ in $K_2^*(1430)K$ (BABAR hint @ 2.1 GeV)
- vector state in $\phi\pi^0$: ρ^* OZI-suppressed, ω/ϕ^* isospin violating
- resonance in $\phi\pi^0$ @ 2.1 GeV?

PRD 77, 092002 (2008)



$\phi(2170) / \Upsilon(2175): e^+e^- \rightarrow \phi\pi^+\pi^-$ PRD 108, 032011 (2023)

- $e^+e^- \rightarrow \phi\pi^+\pi^-$
 - 651 pb⁻¹ data between 2.05 and 3.08 GeV
 - cross sections consistent with BABAR, more precise
 - $M = (2178 \pm 20 \pm 5) \text{MeV}/c^2$
 - $\Gamma = (140 \pm 36 \pm 16) \text{MeV}$
 - statistical significance: $> 10 \sigma$; $J^{PC} = 1^{--}$
 - Belle data: structure @ 2.4 GeV with 1.5σ
 - no resonance observed @ 2.4 GeV but...
 - ...resonance observed @ 2.4 GeV in $K^+K^-f_0(980)$
 - PWA is needed



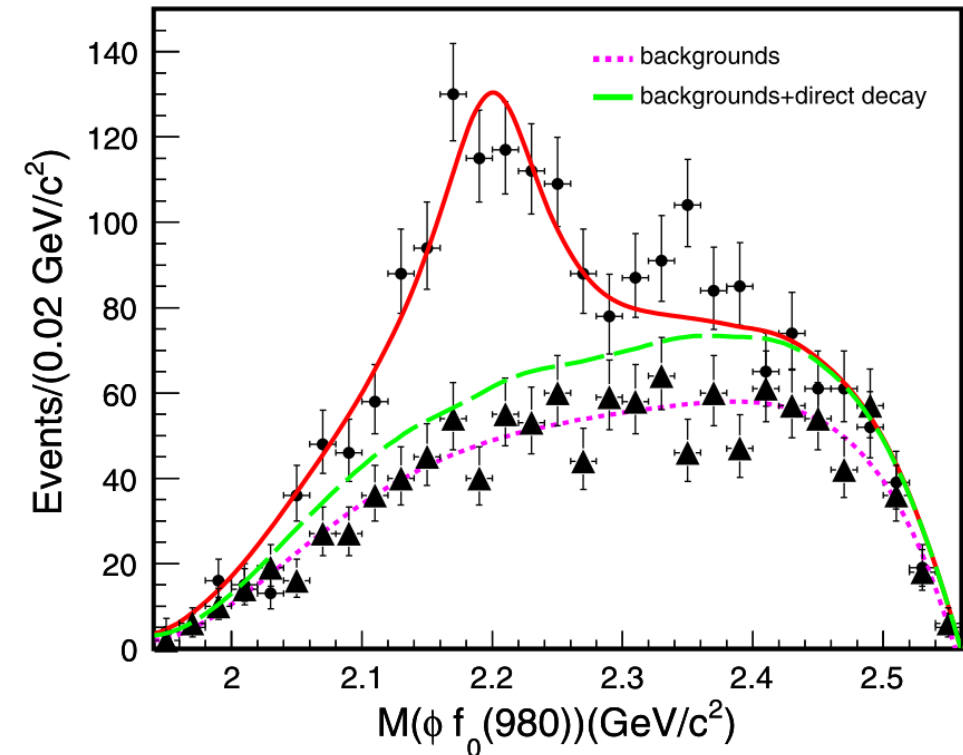
$\phi f_0(980)$	Mass (MeV)	Width (MeV)
BaBar (2006)	$2175 \pm 10 \pm 15$	$58 \pm 16 \pm 20$
BES (2008)	$2186 \pm 10 \pm 6$	$65 \pm 23 \pm 17$
Belle (2009)	2163 ± 32	125 ± 40
BaBar (2012)	$2172 \pm 10 \pm 8$	$96 \pm 19 \pm 12$
BESIII (2015)	$2200 \pm 6 \pm 5$	$104 \pm 15 \pm 15$
BESIII (2019)	$2135 \pm 8 \pm 9$	$104 \pm 24 \pm 12$
PDG2022	2160 ± 7	$100 \pm 31 \pm 23$

$\phi(2170) / Y(2175): J/\psi \rightarrow \eta\phi\pi^+\pi^-$

• $e^+ e^- \rightarrow J/\psi \rightarrow \eta Y(2175), Y(2175) \rightarrow \phi f_0(980), f_0(980) \rightarrow \pi^+\pi^-$

- $2.25 \cdot 10^8 J/\psi \rightarrow \eta\phi\pi^+\pi^-$
- invariant mass spectrum of $\phi f_0(980)$
- $M = (2200 \pm 6 \pm 5) \text{MeV}/c^2$
- $\Gamma = (104 \pm 15 \pm 15) \text{MeV}$
- statistical significance: $> 10 \sigma$
- $\mathcal{B}(J/\psi \rightarrow \eta Y(2175), Y(2175) \rightarrow \phi f_0(980), f_0(980) \rightarrow \pi^+\pi^-) = (1.20 \pm 0.14 \pm 0.37) \times 10^{-4}$

PRD 91, 052017 (2015)



Summary

Conclusions

- High accuracy **R-value measurements**
- Impressive record of **new particles** discovered at BESIII
- Ideal experimental scenario for **Hadron Spectroscopy**
- Unique access to **nucleon, hyperon and hadronic structure**
- **New exciting results expected:**
 - high statistics datasets in wide energy range already collected
 - other approaches to be explored

Stay tuned!

Thank you!

Backup

BESIII detector performance

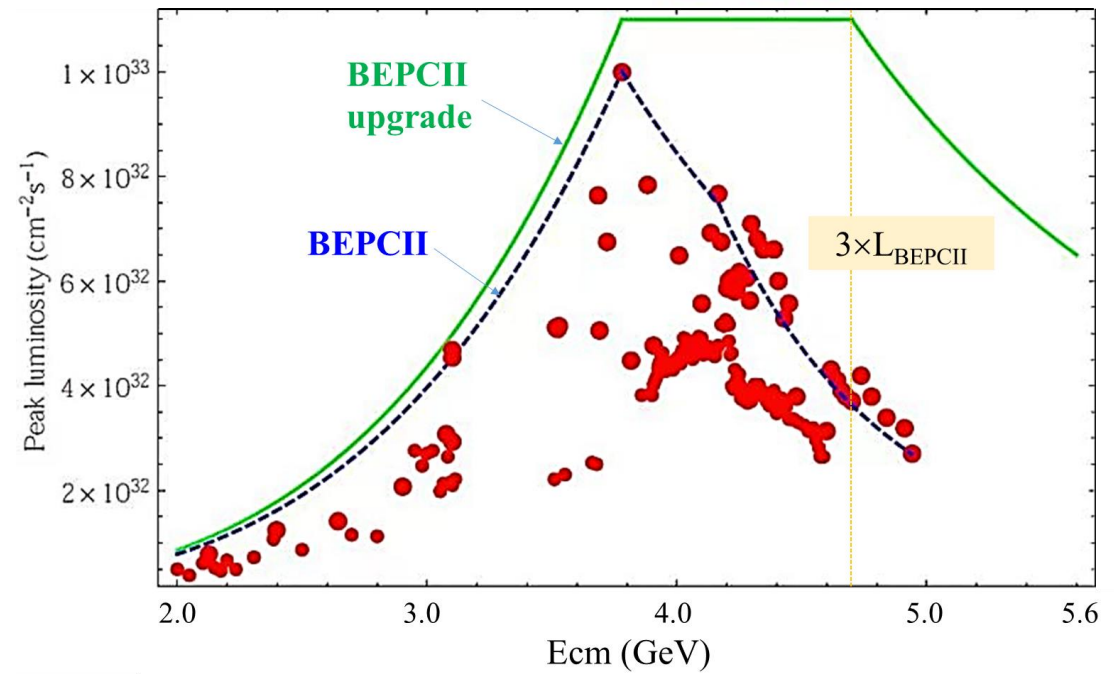
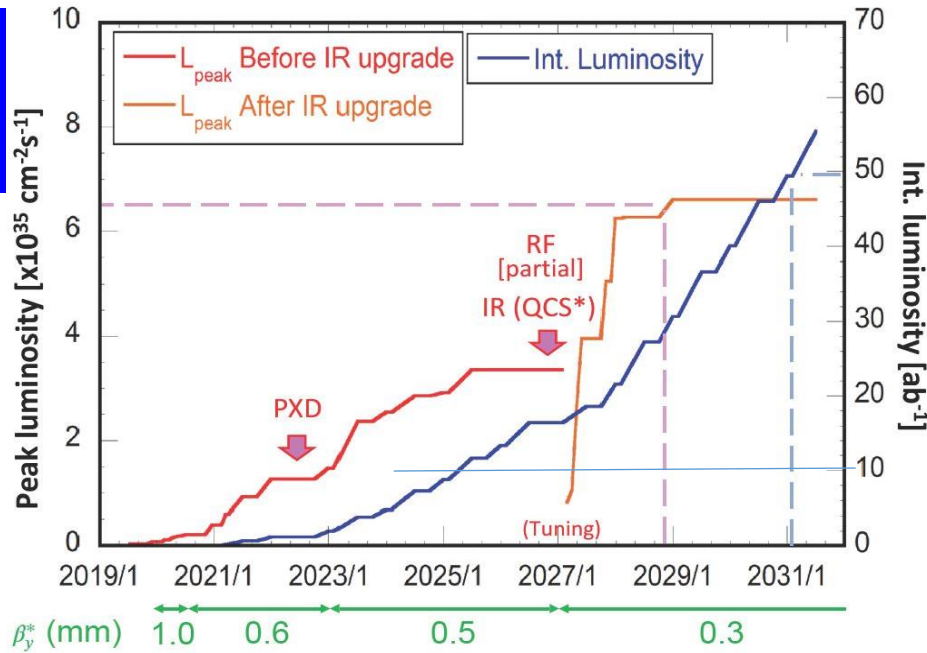
Experiments	MDC	MDC	EMC
	Spatial resolution	dE/dx resolution	Energy resolution
CLEOc	110 μm	5%	2.2-2.4 %
Babar	125 μm	7%	2.67 %
Belle	130 μm	5.6%	2.2 %
BESIII	115 μm	<5% (Bhabha)	2.4%

Experiments	TOF
	Time resolution
CDFII	100 ps
Belle	90 ps
BESIII	68 ps (BTOF) 60 ps (ETOF)

The near future

The logo for BES III, featuring the letters 'B', 'E', 'S', and 'III' in a stylized font. 'B' is blue, 'E' is red, 'S' is green, and 'III' is black.The logo for Belle II, featuring a large yellow stylized 'B' on a blue square background with the text 'Belle II' in white below it.The logo for LHCb, featuring the text 'LHCb' in white on a light blue background, with 'LHCb' repeated in a darker blue background below it, crossed by a red diagonal line.

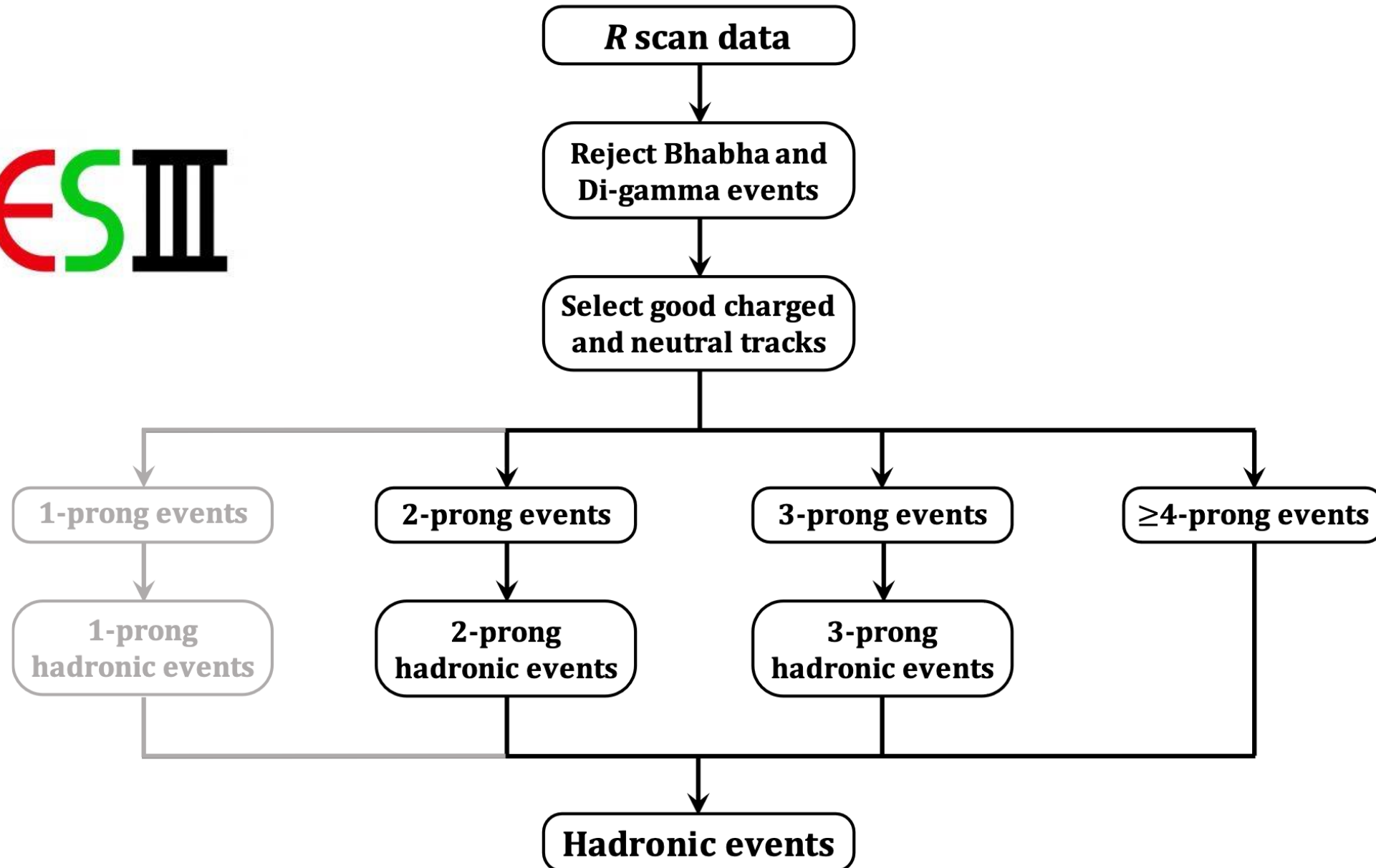
The near future



	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	203+
				Run III						Run IV			Run V		
	LS2						LS3					LS4			
LHCb 40 MHz UPGRADE I	$L = 2 \times 10^{33}$					LHCb Consolidate: UPGRADE Ib			$L = 2 \times 10^{33}$ 50 fb^{-1}			LHCb UPGRADE II		$L = 1-2 \times 10^{34}$ 300 fb^{-1}	
ATLAS Phase I Upgr	$L = 2 \times 10^{34}$					ATLAS Phase II UPGRADE			HL-LHC $L = 5 \times 10^{34}$					HL-LHC $L = 5 \times 10^{34}$	
CMS Phase I Upgr	300 fb^{-1}					CMS Phase II UPGRADE								3000 fb^{-1}	

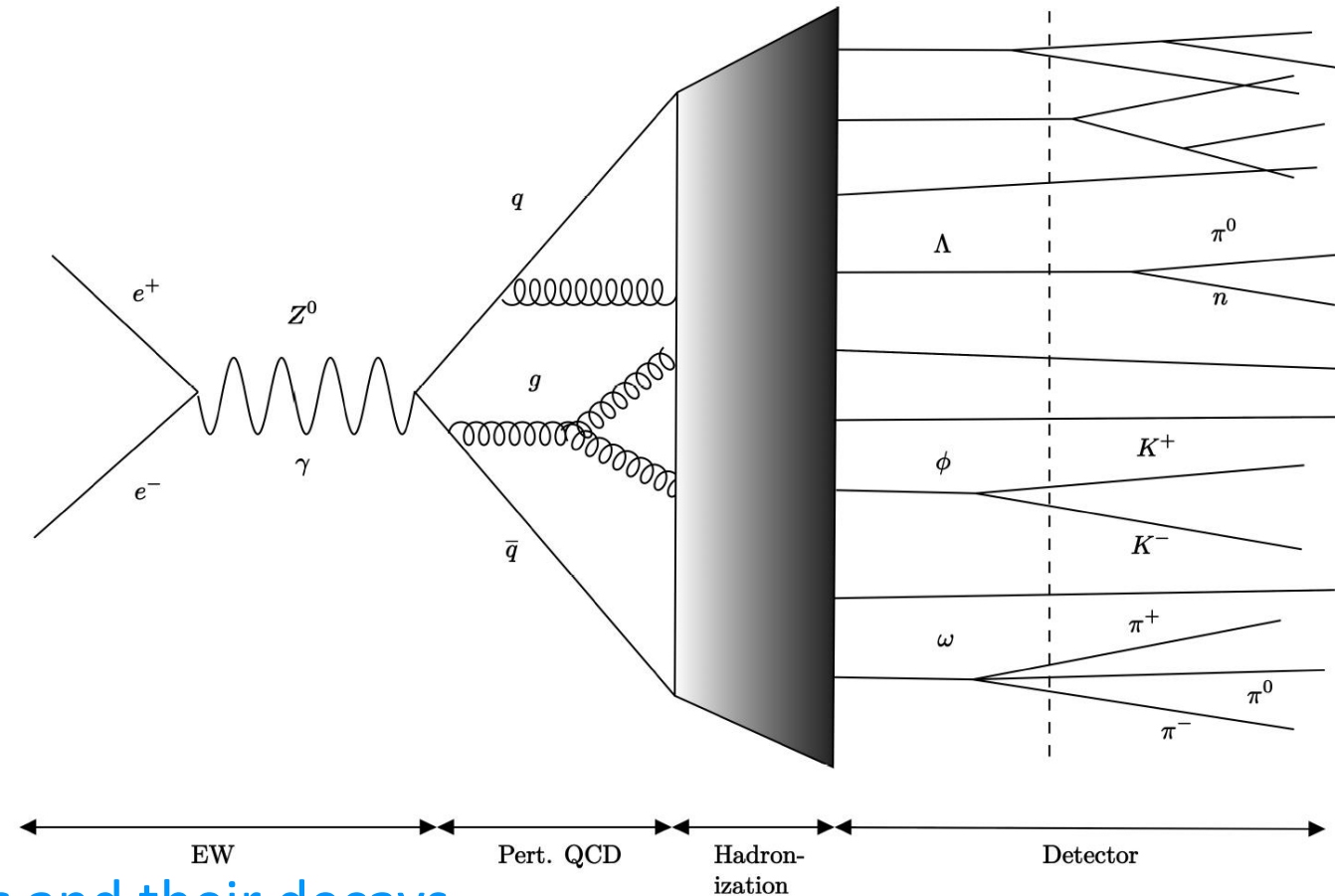
R value: experimental data

New BESIII R-value data: analysis strategy



Nominal signal simulation model: LUARLW

LUARLW



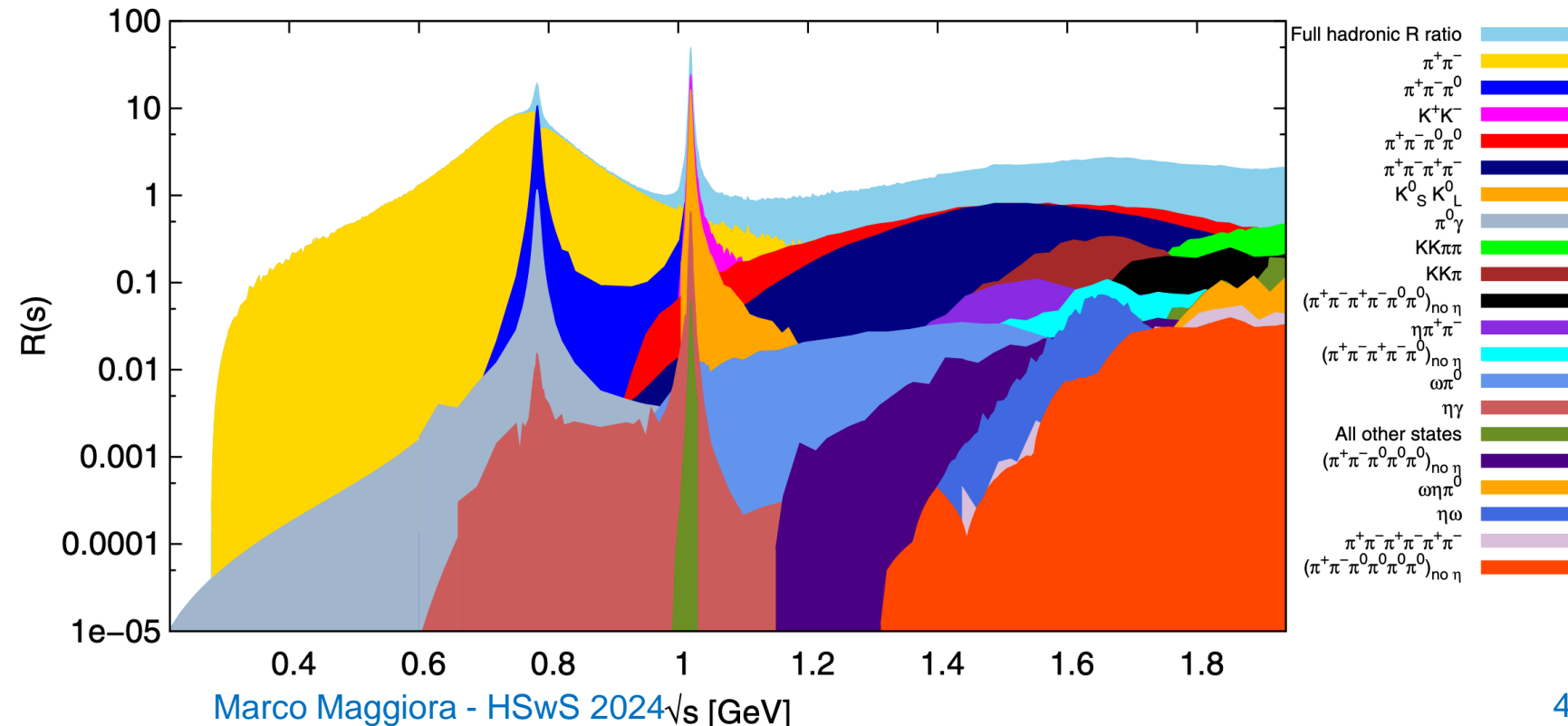
- self-consistent inclusive generator
- based on **JETSET** at low energies
- generation: continuum, resonant states and their decays
- Initial-State Radiation (**ISR**) processes implemented from $2m_\pi$ to \sqrt{s}
- kinematics of initial hadrons determined by **Lund** area law
- phenomenological parameters tuned to data
- adopted in **most previous R-measurements** (e.g. BESII and KEDR)

Alternative signal simulation model: HYBRID

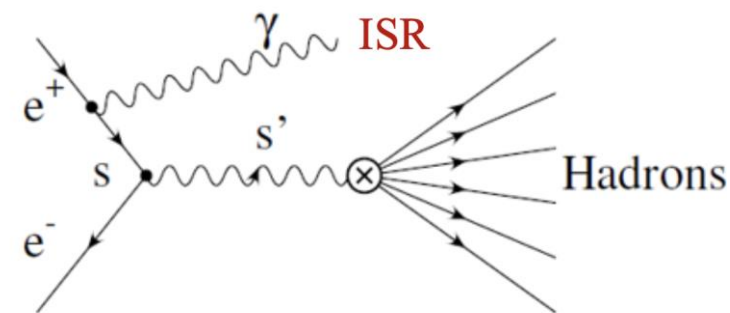
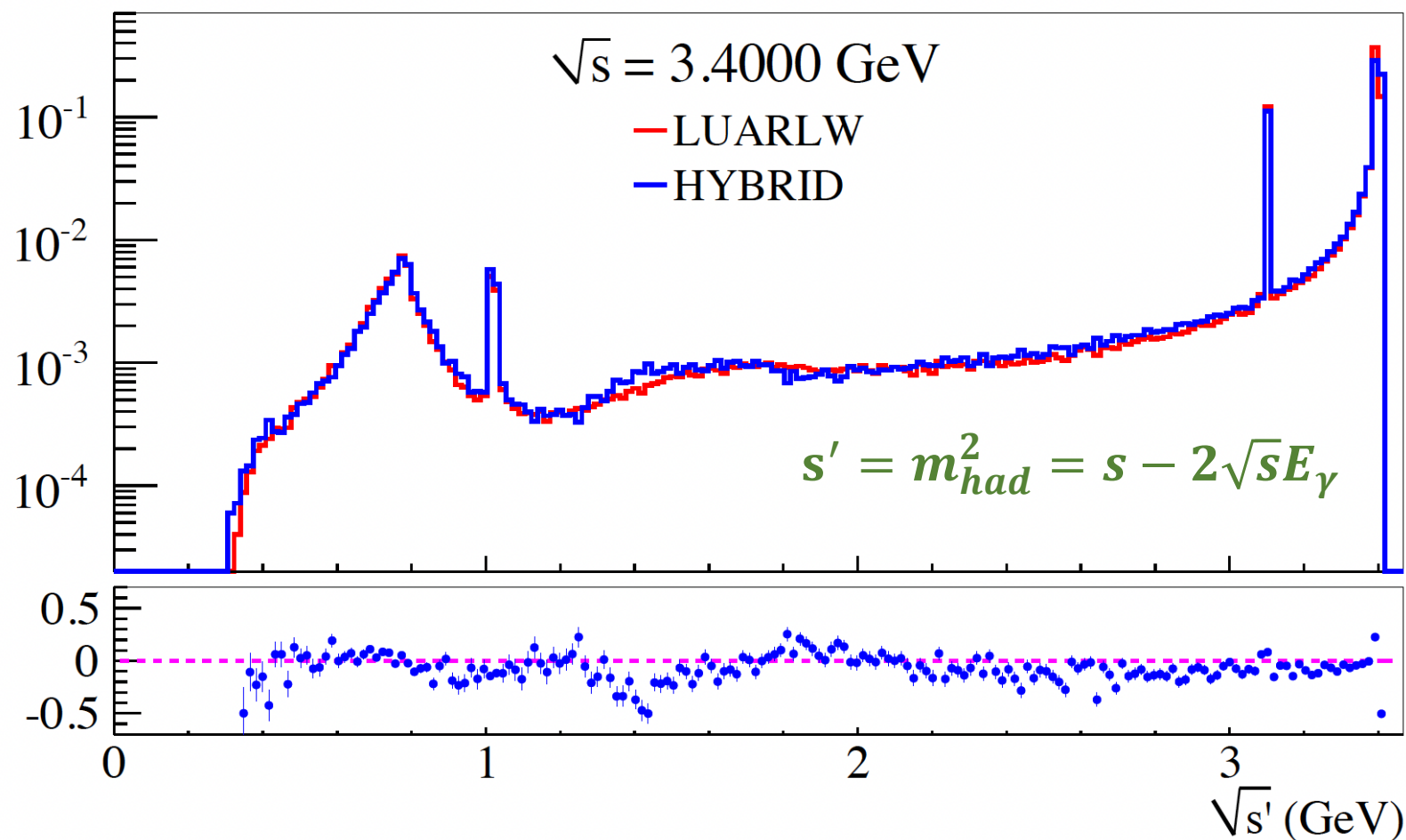
- **HYBRID**: as much experimental information as possible, combining **3** established models:
 - CONEXC (over 50 channels, experimental cross sections)
 - PHOKHARA (10 exclusive channels, hadronic models tuned to experimental data)
 - LUARLW (unknown processes)
- up-to-date experimental knowledge implemented
- alternative **ISR** and **VP** correction schemes from the nominal ones adopted

PRD 97, 114025 (2019)

HYBRID vs LUARLW: < 1.4%



Effective energy $\sqrt{s'}$ spectra: LUARLW vs HYBRID



maximum difference
of the calculated ISR correction
between HYBRID and LUARLW
is 1.4%,

- $\sqrt{s'}$ spectrum directly reflects the **fraction** of the ISR-returned processes
- LUARLW and HYBRID adopts two different ISR simulation schemes, and yet ...
- ... effective energy spectrum results are consistent

MC vs data consistency: LUARLW vs HYBRID

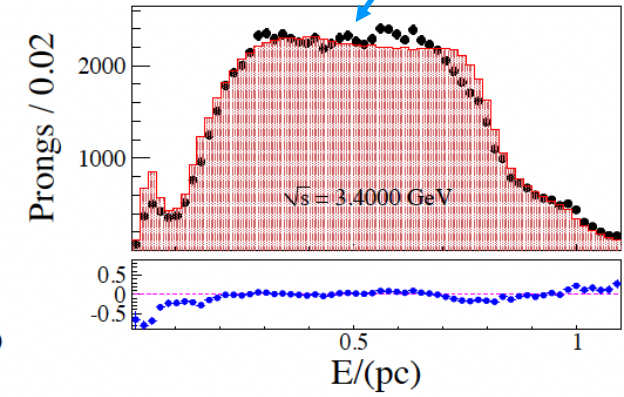
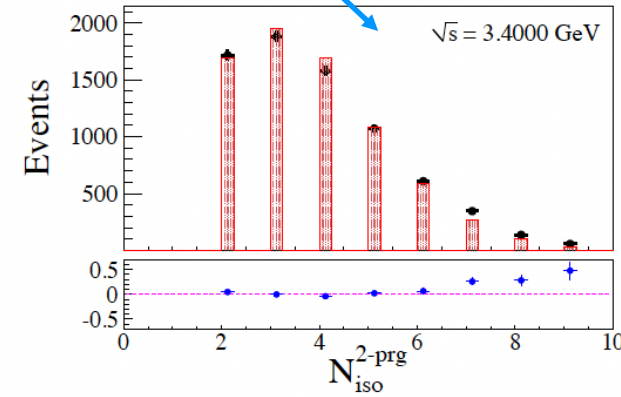
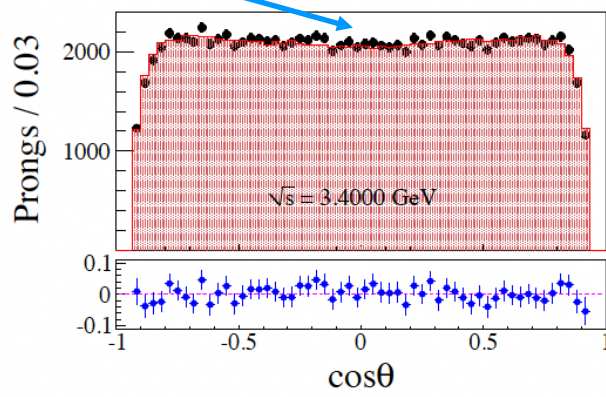
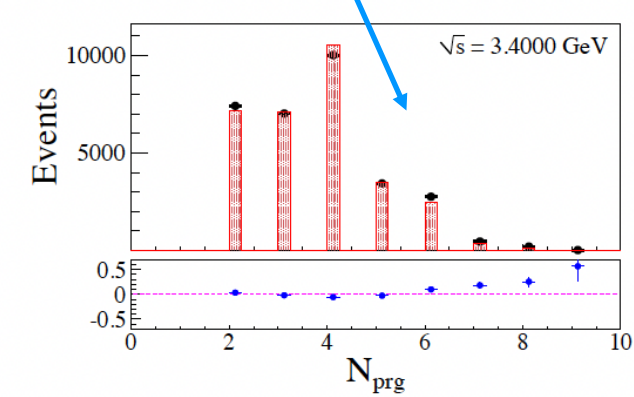
number of good charged tracks (prongs)

polar angle of charged tracks

number of isolated clusters in 2-prong events

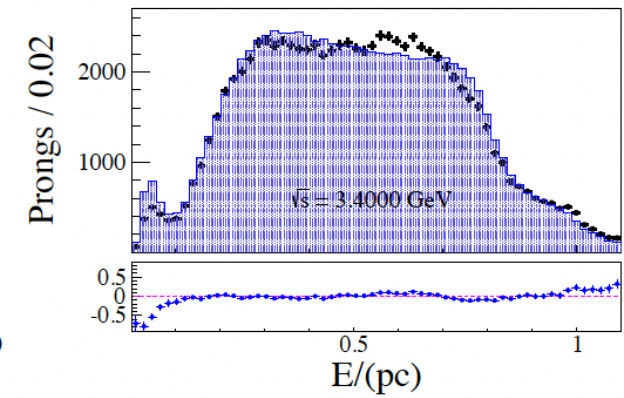
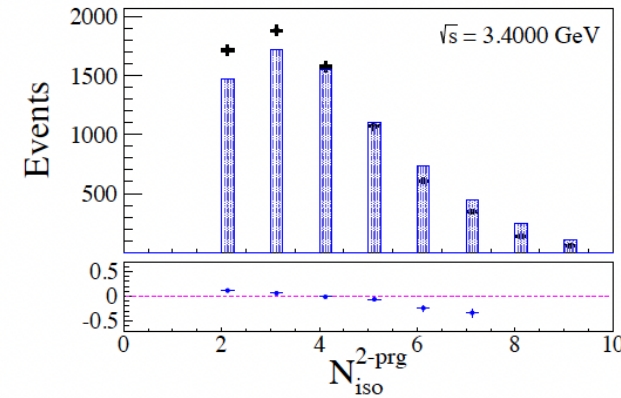
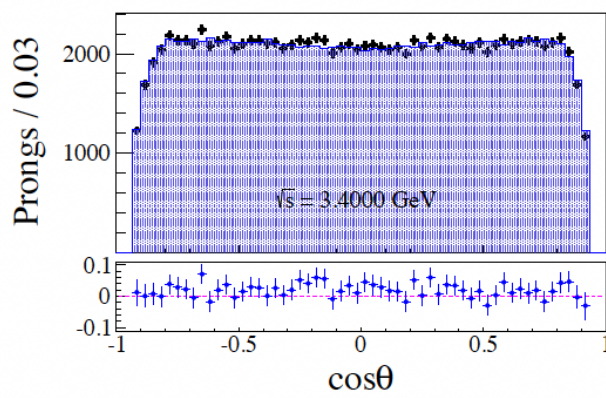
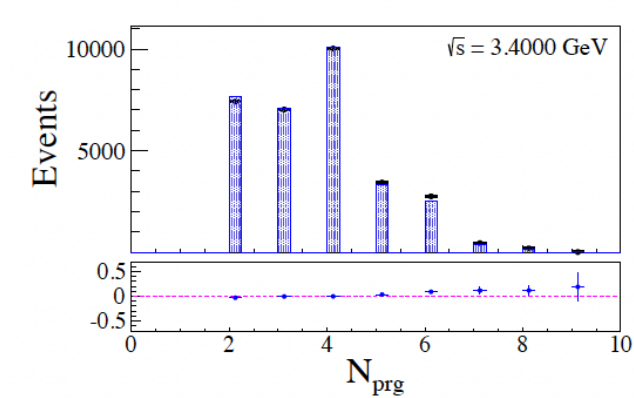
ratio of EMC deposited energy and momentum

LUARLW



@3.4 GeV

HYBRID



Both models show good agreement with data!

BESIII experimental R data in the range 2.2 ÷ 3.7 GeV

TABLE I. Summary of systematic uncertainties (in percent) at each c.m. energy, where the total uncertainty is the sum of the individual ones in quadrature. Uncertainties from the last four sources are correlated between the energy points.

\sqrt{s} (GeV)	Event selection	QED background	Beam background	Luminosity	Trigger efficiency	Signal model	ISR correction	Total
2.2324	0.41	0.23	0.28	0.80	0.10	0.60	1.15	1.62
2.4000	0.55	0.27	0.15	0.80	0.10	1.11	1.10	1.87
2.8000	0.58	0.28	0.34	0.80	0.10	1.97	1.06	2.48
3.0500	0.61	0.33	0.41	0.80	0.10	1.76	1.01	2.33
3.0600	0.60	0.34	0.48	0.80	0.10	1.84	1.00	2.39
3.0800	0.61	0.35	0.35	0.80	0.10	1.31	1.05	2.02
3.4000	0.65	0.33	0.16	0.80	0.10	1.86	1.24	2.49
3.5000	0.60	0.35	0.62	0.80	0.10	2.05	1.16	2.66
3.5424	0.61	0.37	0.01	0.80	0.10	2.05	1.14	2.58
3.5538	0.66	0.31	0.39	0.80	0.10	2.22	1.13	2.74
3.5611	0.74	0.34	0.34	0.80	0.10	2.28	1.12	2.81
3.6002	0.66	0.33	0.38	0.80	0.10	2.27	1.09	2.77
3.6500	0.53	0.35	0.69	0.80	0.10	2.28	1.13	2.83
3.6710	0.61	0.42	0.63	0.80	0.10	2.23	1.04	2.77



14 energy points
total of 52 pb⁻¹

- accuracy dominated by systematic uncertainties
- statistic uncertainties: ~ 0.35%