The Particle World

CERN Summer School Lectures 2023

David Tong









Further Reading

Particle Physics

CERN Lectures

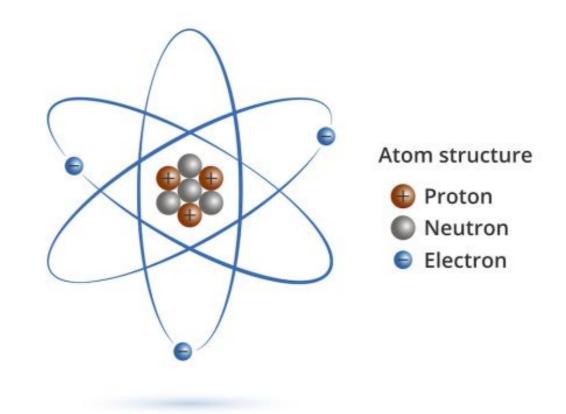
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http://www.damtp.cam.ac.uk/user/tong/particle.html d.tong@damtp.cam.ac.uk

around 240 pages! (Sorry)

What are we made of?



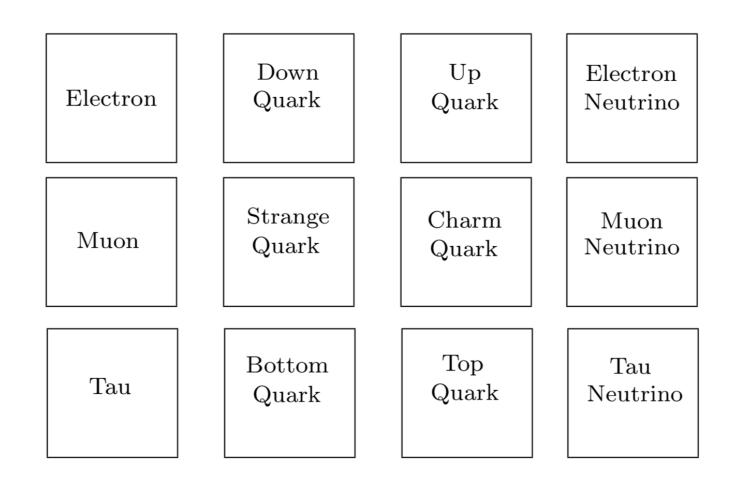
"If we consider protons and neutrons as elementary particles, we would have three kinds of elementary particles [p,n,e].... This number may seem large but, from that point of view, two is already a large number."

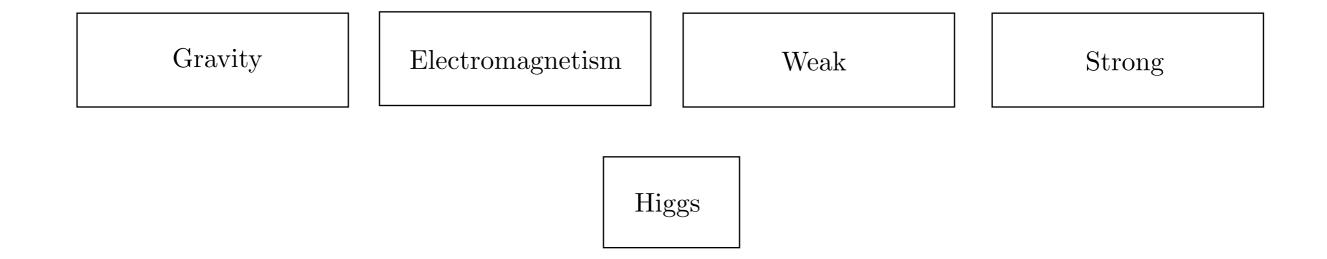
Paul Dirac 1933 Solvay Conference

The Standard Model

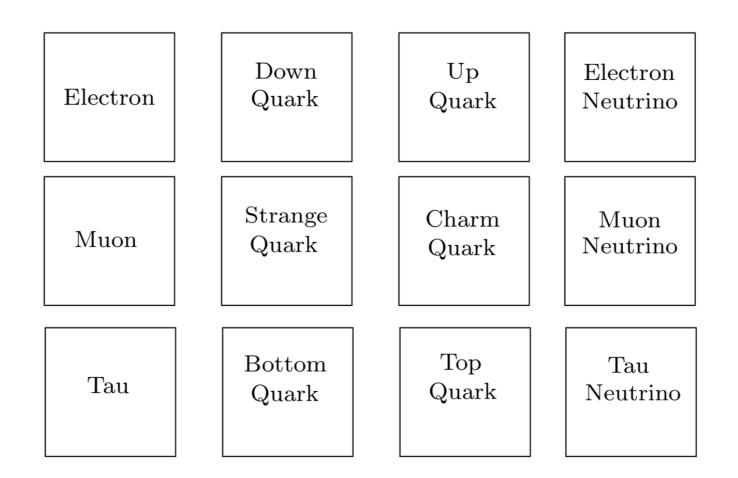
12 particles + 4 forces + Higgs boson

The Standard Model

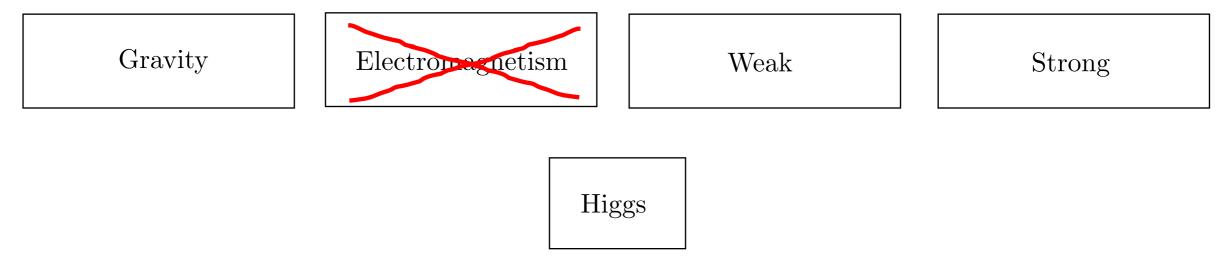




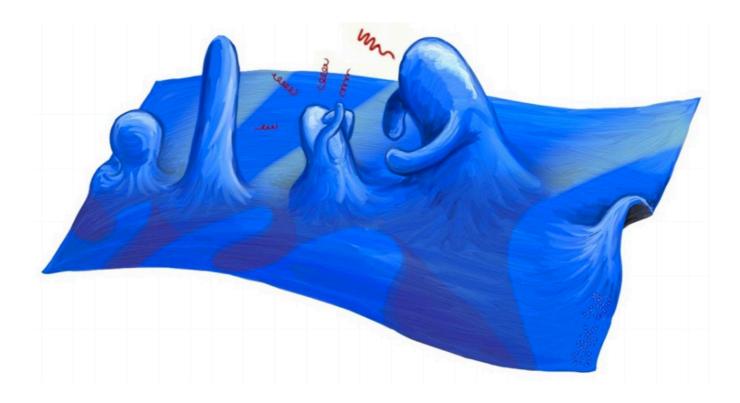
The Standard Model



Hypercharge

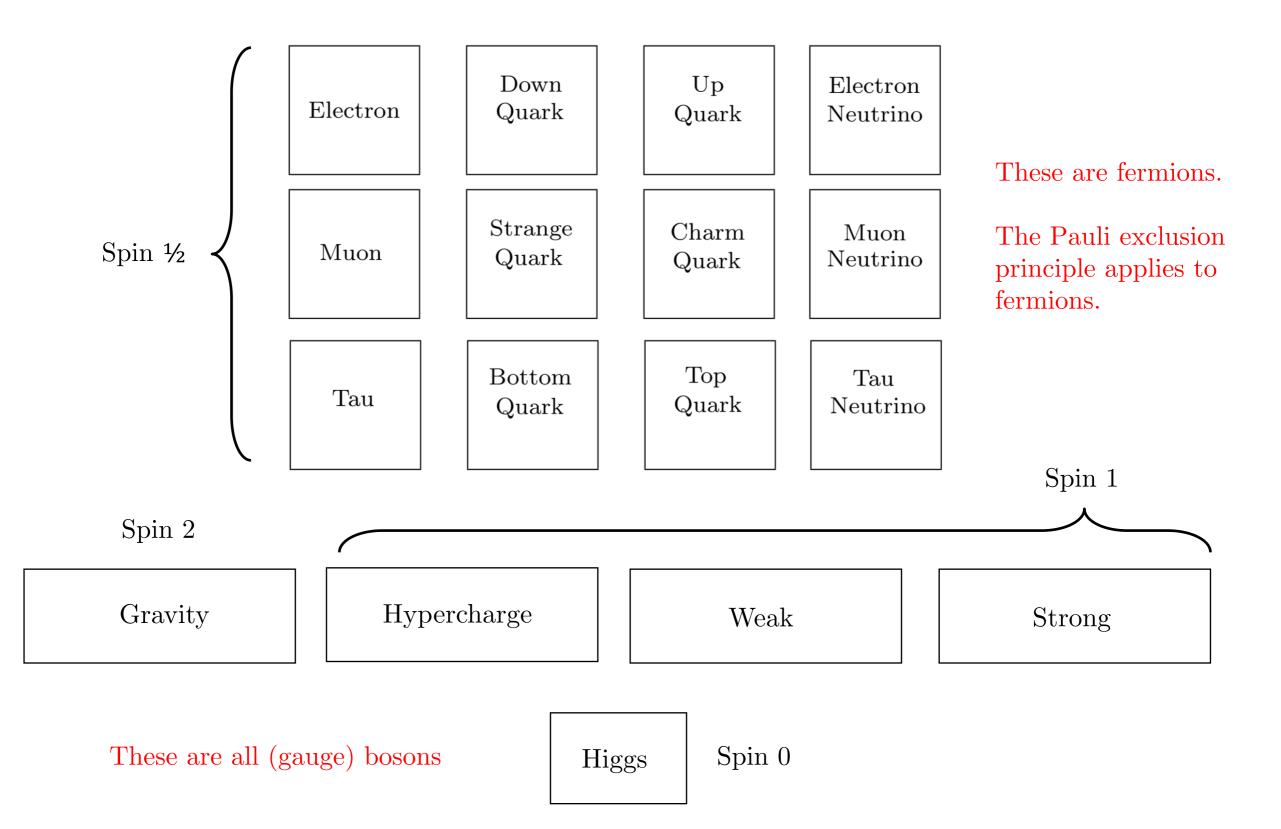


Our First Unification: Fields



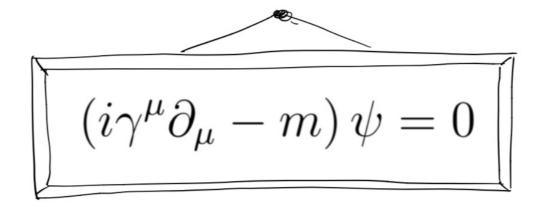
- Particles are excitations of underlying quantum fields
- Forces are also due to fields and have associated particles
 - Electromagnetism = photon
 - Strong = gluon
 - $\bullet \quad Weak = W \ and \ Z \ bosons$
 - Gravity = graviton

Intrinsic Angular Momentum = Spin



A Remarkable Fact

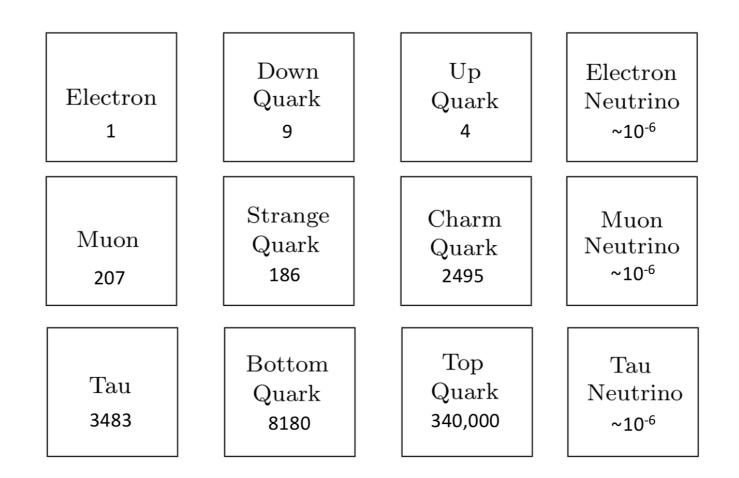
All spin $\frac{1}{2}$ particles are described by the same equation, discovered by Dirac



Here m is the mass.

Consequence: all matter particles come with anti-particles

Mass



An aside: In the Standard Model, the masses of all particles are determined by the strength of interaction with the Higgs field.

Units for Mass

We measure mass in terms of energy, using $E=mc^2$. The unit of choice is the electronvolt

 $1 \text{ eV} \approx 1.6 \times 10^{-19} \text{ J}$

Or MeV = 10^{6} eV or GeV = 10^{9} eV or TeV = 10^{12} eV.

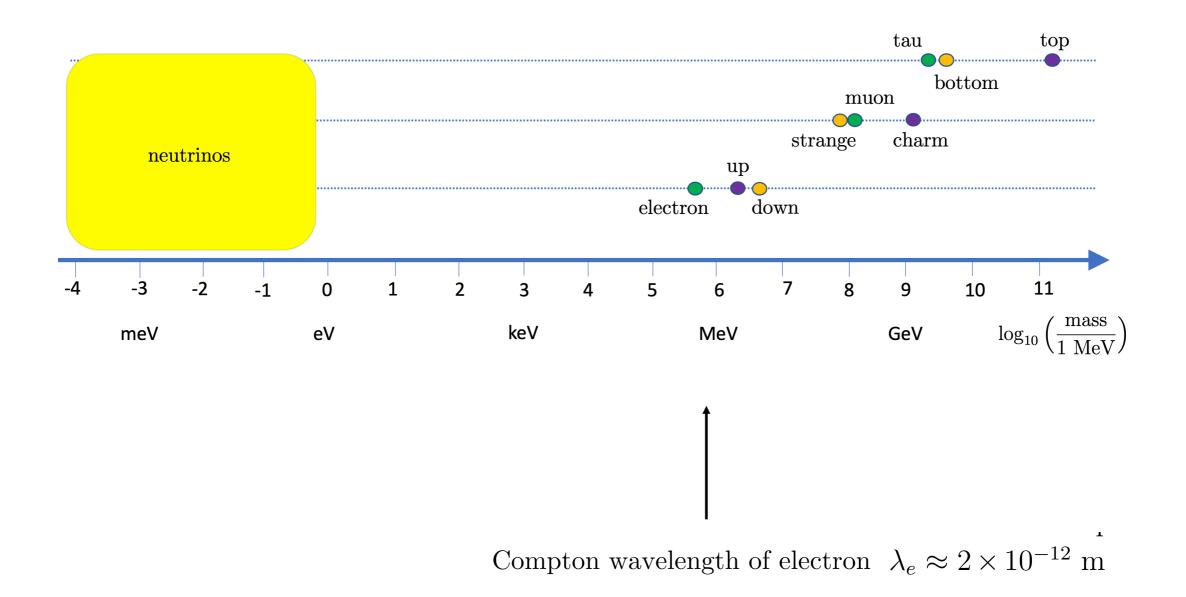
More confusingly, we also measure distance in terms of inverse energy, using

$$\lambda = \frac{\hbar c}{E}$$

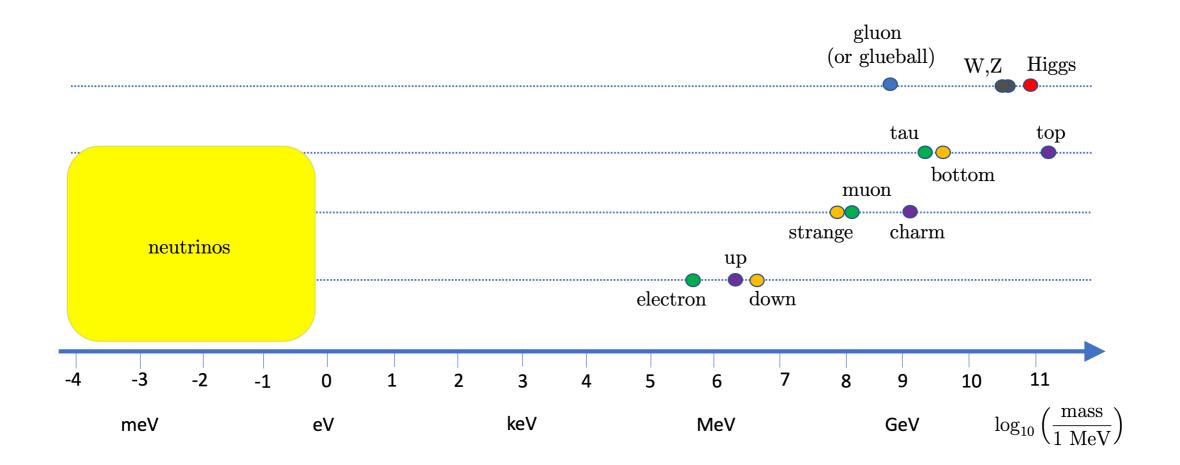
For a particle of mass E, this is the "Compton wavelength", or the size of the particle.

Note: heavier particles are smaller!

The Masses of Particles



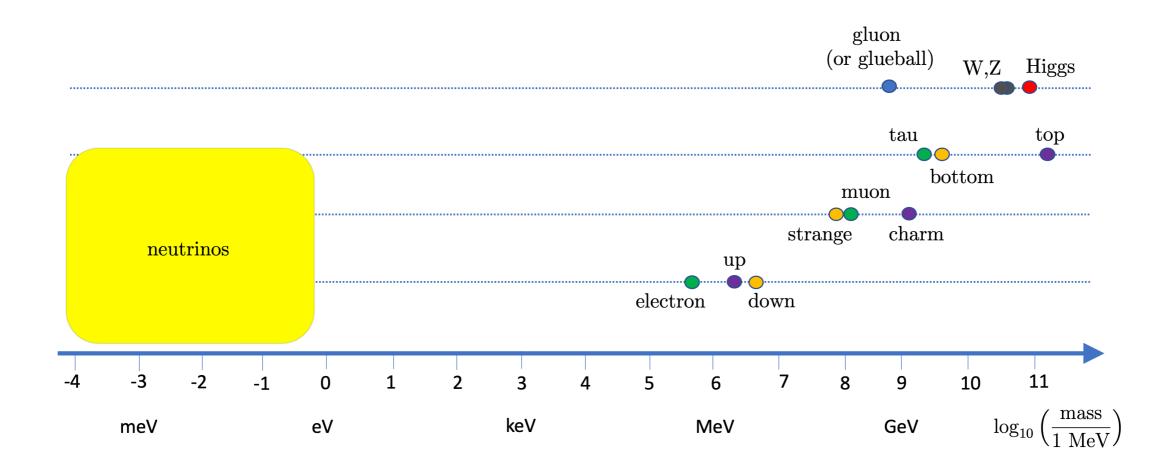
The Masses of Particles



Note: photon and graviton both massless.

(The gluon is a little subtle...see later.)

The Masses of Particles



<u>The biggest</u>

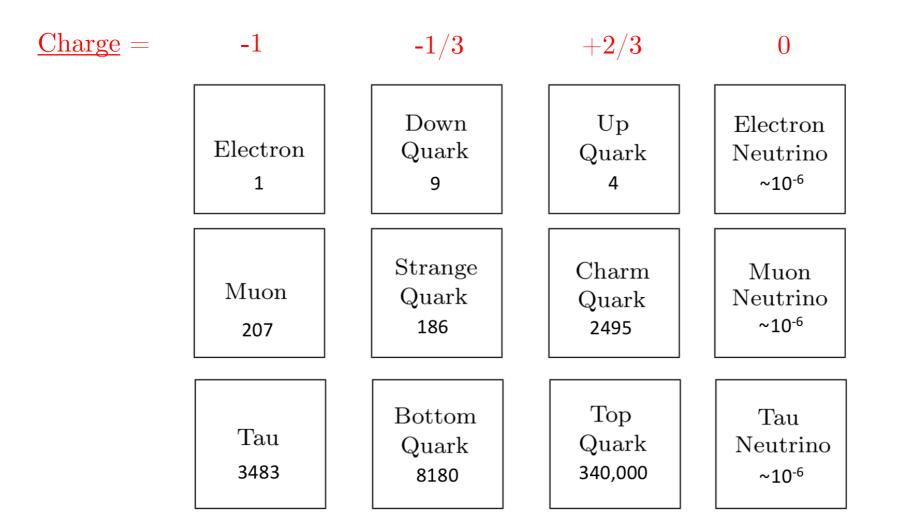
 $H \approx 2 \times 10^{-33} \text{ eV}$

 $L_{\rm universe} \approx 9 \times 10^{26} {\rm m}$

The smallest

$$M_{\rm pl} = \sqrt{\frac{\hbar c}{8\pi G}} \approx 2 \times 10^{18} \text{ GeV}$$
$$L_{\rm pl} = \sqrt{\frac{8\pi\hbar G}{c^3}} \approx 8 \times 10^{-35} \text{ m}$$

Electric Charge



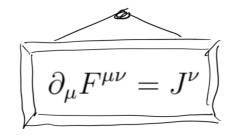
The electric charge characterizes the (relative) strength of the electromagnetic interaction

Electromagnetism (or QED)

or

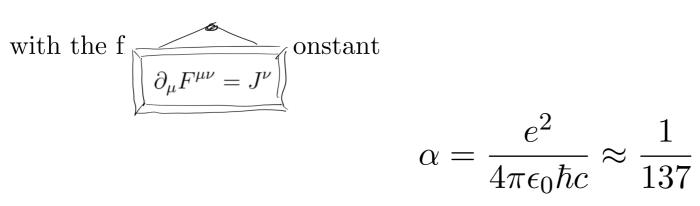
The Maxwell Equations

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0} \quad , \quad \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$
$$\nabla \cdot \mathbf{B} = 0 \quad , \quad \nabla \times \mathbf{B} = \mu_0 \left(\mathbf{J} + \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right)$$



This implies the Coulomb force which, in natural units, reads

$$F = \alpha \frac{Q_1 Q_2}{r^2}$$

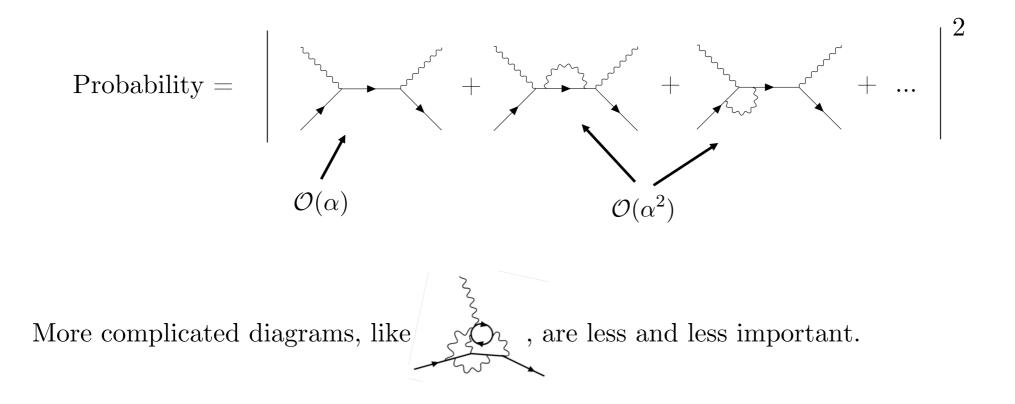


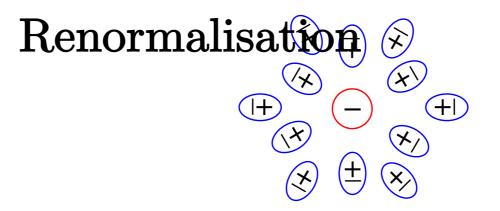
Feynman Diagrams

An important fact: quantum field theory is hard!

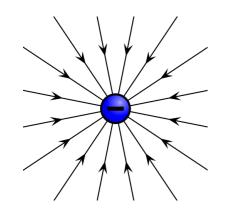
We are saved in QED because $\alpha\approx\frac{1}{137}\ll 1.$ This allows us to write down an approximate solution

e.g. what is the probability for a photon to scatter off an electron in some direction?



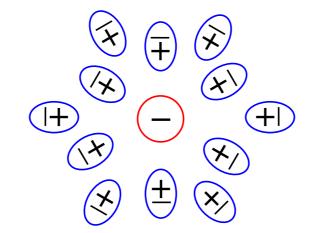


Look close at the electron.

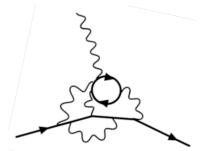


$$\mathbf{E} = \frac{e}{4\pi\epsilon_0 r^2} \hat{\mathbf{r}} \qquad \qquad \Box \searrow$$

Large energy density near electron, This allows for the creation of particle-anti-particle pairs

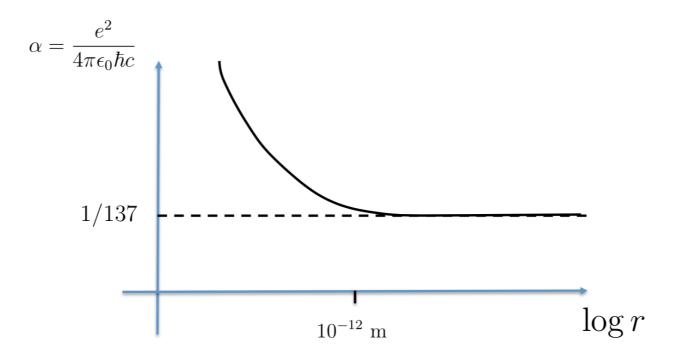


This is the physics behind the increasingly complicated diagrams like this



Renormalisation

As you look more closely, the charge of an electron gets bigger!



Constants of nature are not constant!

The Strong and Weak Force

Both nuclear forces have associated "electric" and "magnetic" fields

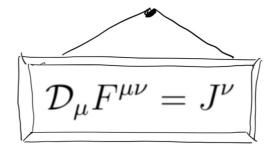
$$\mathbf{E} = (E_x, E_y, E_z) \qquad \mathbf{B} = (B_x, B_y, B_z)$$

But each component is now itself a matrix.

- $1 \ge 1$ matrix \implies Electromagnetism
- $2 \ge 2$ matrix \implies Weak force
- $3 \ge 3$ matrix \implies Strong force

or $U(1) \ge SU(2) \ge SU(3)$

These fields are governed by the Yang-Mills equations



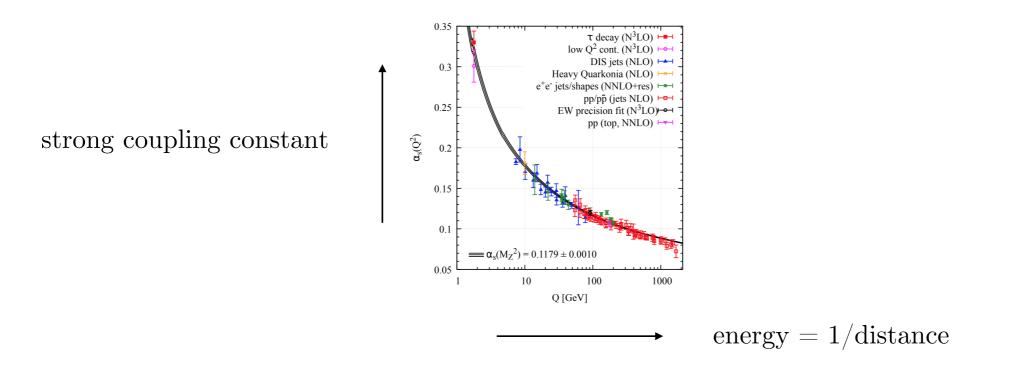
The Strong Force (or QCD)



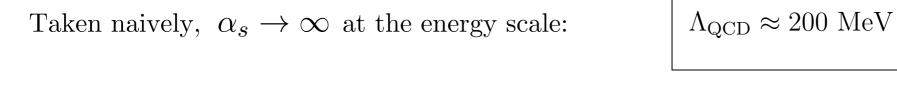
Each quark comes in three *colours*, which we take to be red, green and blue.

(Note: a better counting is that each generation contains 1+3+3+1=8 particles.)

Why is the Strong Force Strong?



At high energy, say E=100 GeV, we have $\alpha_s \approx 0.1$. But the strong force gets stronger as we go to larger distances. (Asymptotic freedom.)



This corresponds to a distance scale $R_{\rm QCD} = \frac{1}{\Lambda_{\rm QCD}} \approx 5 \times 10^{-15} \text{ m}$

Confinement

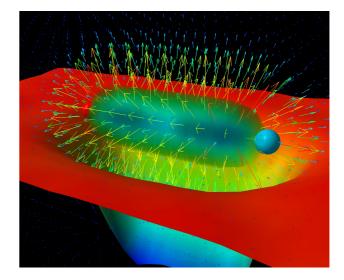
At short distances, $F(r) \sim \frac{\alpha_s}{r^2}$ but at long distances F(r) becomes constant.

In terms of the potential energy, $V(r) \sim -\frac{\alpha_s}{r}$ at short distances, but at long distances

$$V(r) \sim \Lambda_{\rm QCD}^2 r$$

This is *confinement*. We don't see isolated quarks.

Also, the force carrying field is not massless. The gluons stick together to form glueballs, with mass around $m_{\rm gluon} \approx \Lambda_{\rm QCD}$. This is the "mass gap" problem.



Hadrons (Stuff Made of Quarks)

• Baryons: three quarks. For example

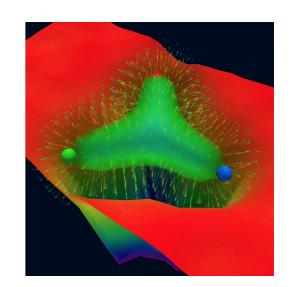
n (ddu) $m_n \approx 939.57 \text{ MeV}$ p (uud) $m_p \approx 938.28 \text{ MeV}$

A puzzle: $m_{down} = 5$ MeV and $m_{up} = 2$ MeV. Where does the mass come from?

• Mesons: quark-anti-quark pair. For example, pions

 $\pi^{+} (\bar{d}u) \qquad m \approx 139 \text{ MeV}$ $\pi^{0} \frac{1}{\sqrt{2}} (\bar{u}u - \bar{d}d) \qquad m \approx 135 \text{ MeV}$ $\pi^{-} (\bar{u}d) \qquad m \approx 139 \text{ MeV}$

Note: Pions have spin 0 and so should be thought of as "force carrying" particles! So ...



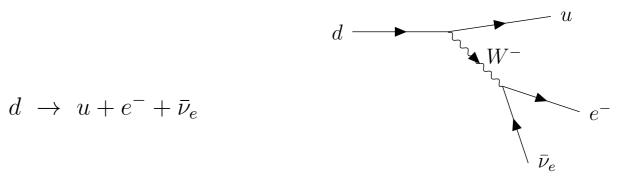
Decay

All hadrons other than the proton are unstable. They decay.

The most famous weak decay is how we first discovered the weak force

$$n \rightarrow p + e^- + \bar{\nu}_e$$

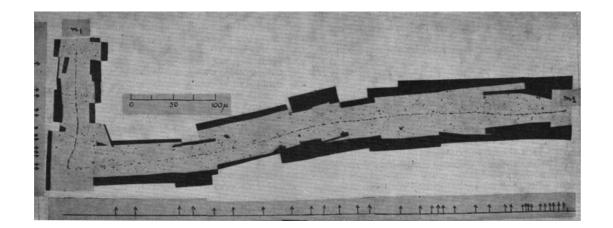
Or, if you look more closely,

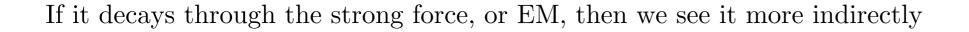


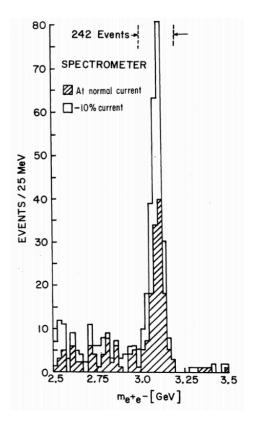
Particles vs Resonances

- Strong decay: $\sim 10^{-22}$ to 10^{-24} seconds.
- Electromagnetic decay: $\sim 10^{-16}$ to 10^{-21} seconds.
- Weak decay: $\sim 10^{-7}$ to 10^{-13} seconds.

If a particle decays through the weak force, we can take a photograph of it!

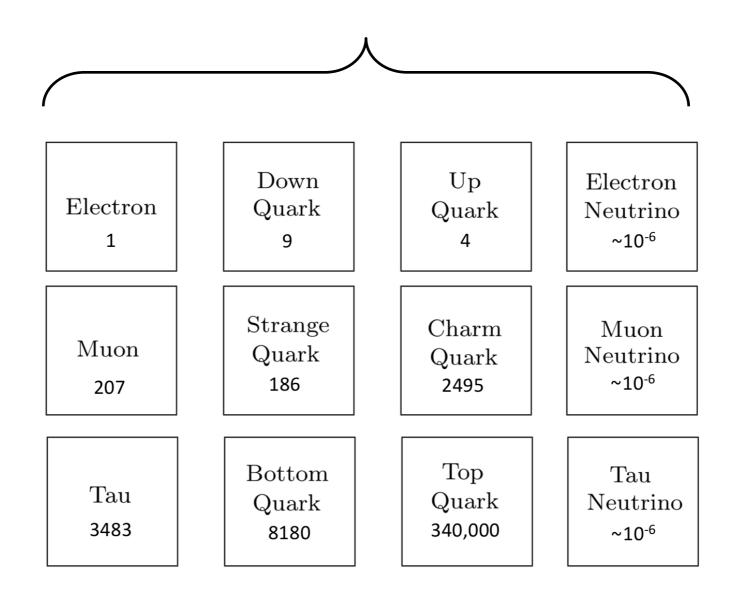






The Weak Force

half of each particle!



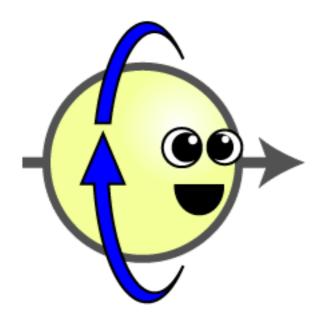
Parity Violation

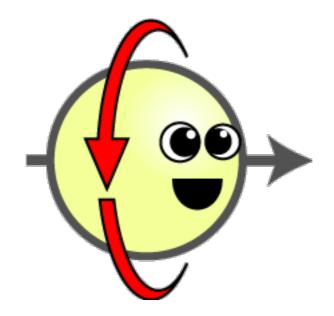




60 Co $\rightarrow ^{60}$ Ni + $e^- + \bar{\nu}_e + 2\gamma$

Chiral Fermions





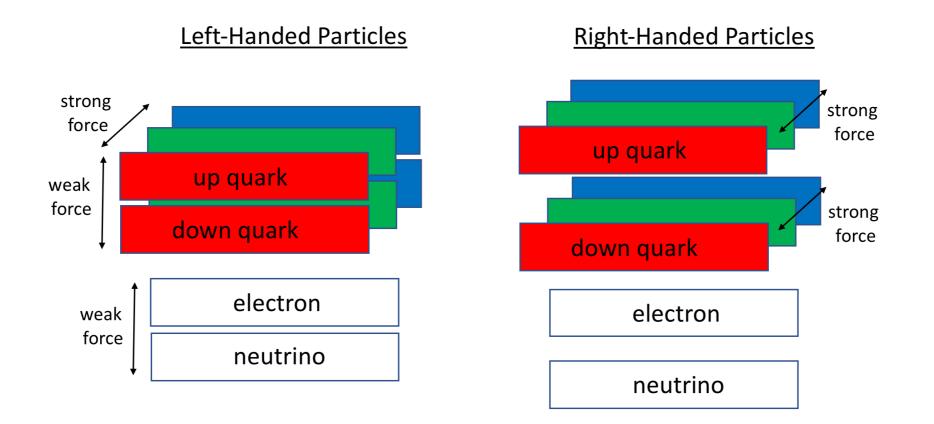
left-handed fermion

right-handed fermion

Left-handed particles experience the weak force, right-handed do not.

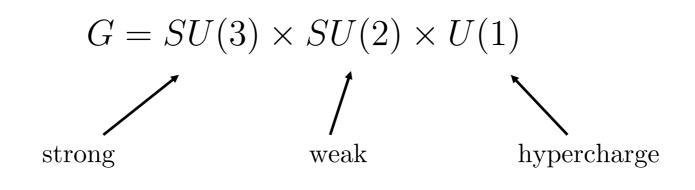
The Forces of the Standard Model

Each generation splits into 8x2 sets of particles



Note: We don't yet know if the right-handed neutrino exists.

The Structure of the Standard Model



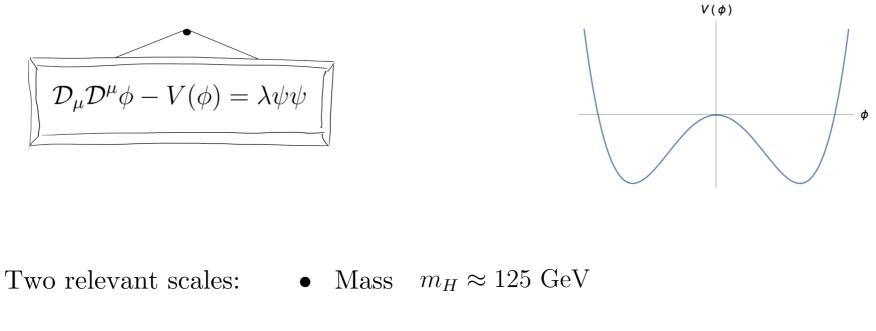
Particles		Strong	Weak	Hypercharge
Left-handed	quarks	yes	yes	+1/6
	leptons	no	yes	-1/2
Right-handed	up quark	yes	no	+2/3
	down quark	yes	no	-1/3
	electron	no	no	-1
	neutrino	no	no	0

A perfect jigsaw: Anomaly cancellation means that it could hardly be any other way!

The Higgs Field

This is both the simplest and most complicated field in the Standard Model!

Particle	Strong	Weak	Hypercharge
Higgs	no	yes	+1/2



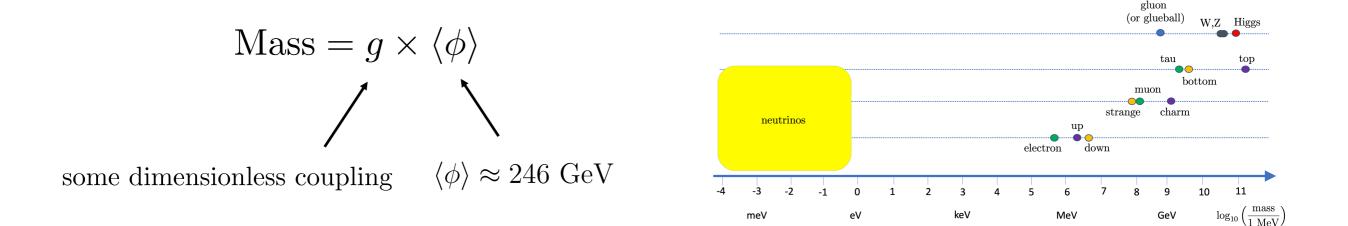
• Condensate $\langle \phi \rangle \approx 246 \text{ GeV}$

It is the condensate that gives the Higgs its Midas touch: everything that it touches gets a mass

How Particles Get a Mass

In the Standard Model, all fermions and gauge bosons are obliged to be fundamentally massless

They get a mass by interaction with the Higgs.



- The Higgs gives mass to the W-boson and Z-boson and all fermions.
- The photon remains massless: it is the one that got away!
- Recall: the mass of the proton and neutron do not come from the Higgs!

One Last Thing: Quark Mixing

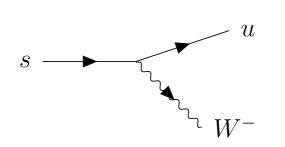
There is a misalignment between the interactions with the Higgs and the interaction with the weak force.

It turns out that you can choose to have the up-sector aligned. But then the down sector is not. The result is a superposition of particles.

$$\begin{pmatrix} d'\\s'\\b' \end{pmatrix} = \begin{pmatrix} V_{ud} \ V_{us} \ V_{ub}\\V_{cd} \ V_{cs} \ V_{cb}\\V_{td} \ V_{ts} \ V_{tb} \end{pmatrix} \begin{pmatrix} d\\s\\b \end{pmatrix}$$
These particles interact with weak force

These particles interact with Higgs, and so definite mass.

This is how, for example, mesons with strange quarks decay



One Last Thing: and Lepton Mixing

There is a similar statement for neutrinos

$$\begin{pmatrix} \nu_{e} \\ \nu_{\mu} \\ \nu_{\tau} \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_{1} \\ \nu_{2} \\ \nu_{3} \end{pmatrix}$$

These particles interact with weak force and are produced in, say, beta decay

These particles have definite mass. These are energy eigenstates that travel unchanged through space.

This gives rise to neutrino oscillations

The Mixing Matrices

For quarks, we have the CKM matrix

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| & |V_{ts}| & |V_{tb}| \end{pmatrix} \approx \begin{pmatrix} 0.97 & 0.22 & 0.004 \\ 0.22 & 0.97 & 0.04 \\ 0.009 & 0.04 & 0.999 \end{pmatrix}$$

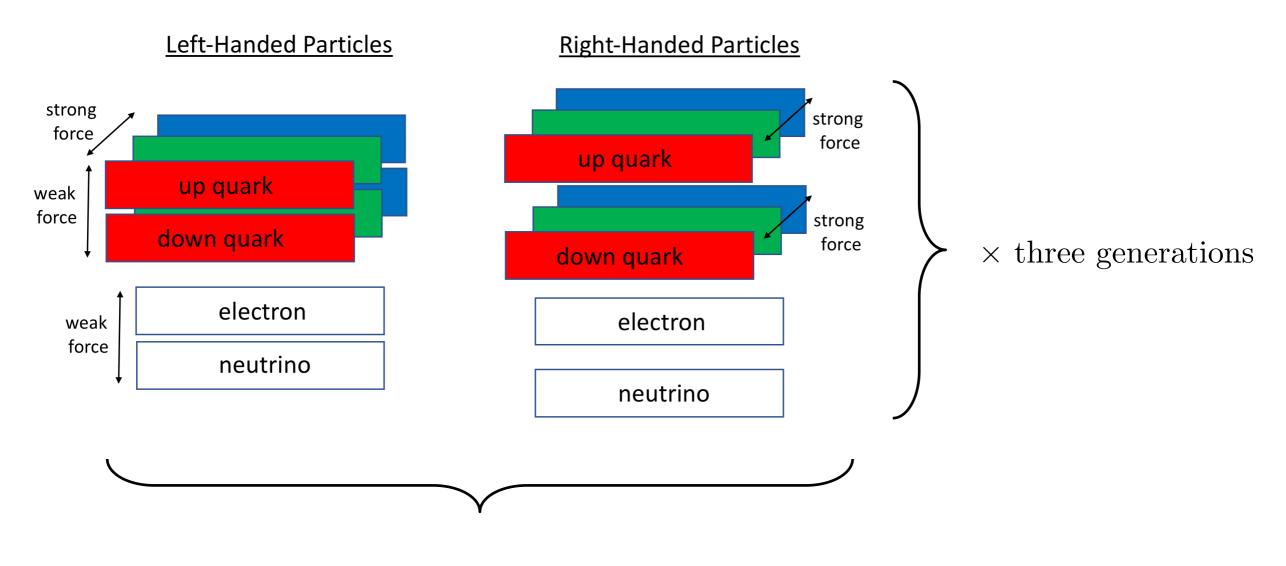
For neutrinos, we have the PMNS matrix

$$\begin{pmatrix} |U_{e1}| & |U_{e2}| & |U_{e3}| \\ |U_{\mu1}| & |U_{\mu2}| & |U_{\mu3}| \\ |U_{\tau1}| & |U_{\tau2}| & |U_{\tau3}| \end{pmatrix} \approx \begin{pmatrix} 0.8 & 0.5 & 0.1 \\ 0.3 & 0.5 & 0.7 \\ 0.4 & 0.6 & 0.6 \end{pmatrix}$$

We only know these parameters by experimental measurement. Why do they take these values? Why are the matrices so different?

Summary: The Greatest Theory of All Time

 $G = SU(3) \times SU(2) \times U(1)$



with all complications coming from interactions with Higgs!

What We Don't Know

- Things that the Standard Model gets wrong
- Questions that the Standard Model raises
- Things that the Standard Model doesn't explain

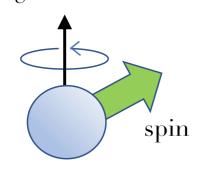
Does the Standard Model Get Anything Wrong?

Does the Standard Model Get Anything Wrong?

No.

Muon g-2

magnetic field



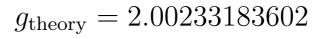
For the electron:

 $g_{\rm expt} = 2.0023193043617 \pm 3$

 $g_{\text{theory}} = 2.00231930436\dots$

For the muon:

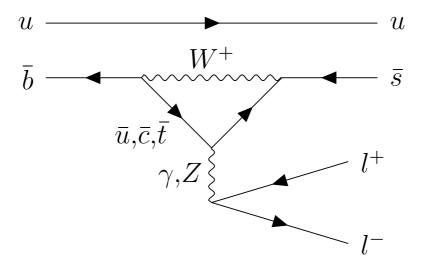
 $g_{\rm expt} = 2.00233184122$



Î

But...

B-anomalies and Lepton Universality



$$l = e$$
 vs $l = \mu$

The W-Boson Mass

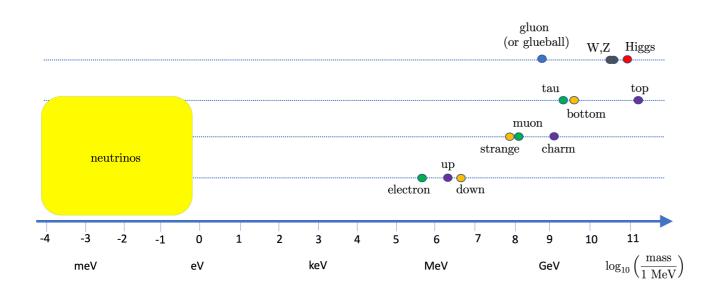
$M_{\rm Europe} = 80.37 \,\,{\rm GeV}$

$M_{USA} = 80.38 \text{ GeV}$

Questions Raised by the Standard Model

Why do parameters take certain values?

- 3 force strengths
- 2 parameters in the Higgs potential
- Loads of parameters in flavour physics



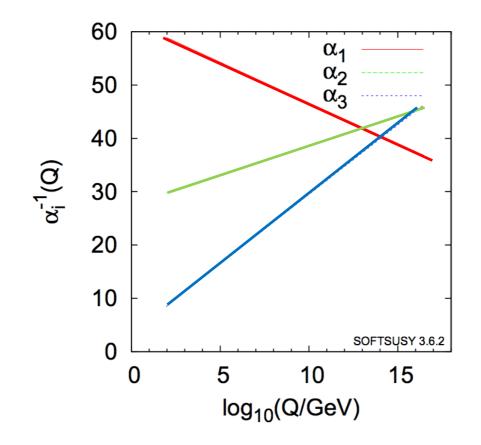
$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$	2	$\left(\begin{array}{cccc} 0.97 & 0.22 & 0.004 \\ 0.22 & 0.97 & 0.04 \\ 0.009 & 0.04 & 0.999 \end{array}\right)$
$ \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} $	\approx	$\left(\begin{array}{rrrr} 0.8 & 0.5 & 0.1 \\ 0.3 & 0.5 & 0.7 \\ 0.4 & 0.6 & 0.6 \end{array}\right)$

Strengths of Forces

At an energy of 100 GeV, we have

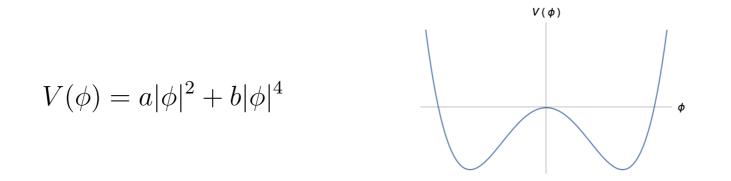
$$\alpha_{\rm QED} \approx \frac{1}{127}$$
 $\alpha_{\rm strong} \approx \frac{1}{10}$ $\alpha_{\rm weak} \approx \frac{1}{30}$

But each of these is a function of scale

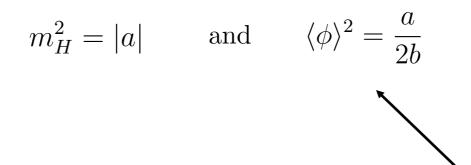


Unification or coincidence?

The Higgs Potential



Naively



This then sets the scale for the masses of all other particles

$$m_H \approx 125 \text{ GeV}$$
 and $\langle \phi \rangle \approx 246 \text{ GeV}$ $\square > a \approx -(125)^2 \text{ GeV}^2$ and $b \approx 0.13$

Remarkably, the coefficient a is the only dimensionful parameter in the Standard Model!

The Hierarchy Problem

The equation $m_H^2 = |a|$ is sadly too naive. There are quantum corrections that give

$$m_H^2 \approx \left| a + \mathcal{O}(\Lambda_{\rm UV}^2) \right|$$

This should be thought of as the biggest scale in the game...maybe the Planck scale?

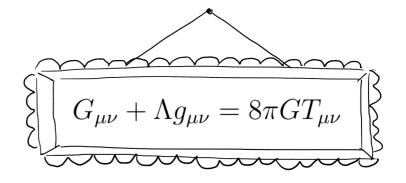
Why should the coefficient a be so finely tuned to the higher energy scale? This is the problem of naturalness.

Things Still to Explain

- (Gravity)
- Dark Matter
- Dark Energy
- Early Universe

Gravity

Standard Model + General Relativity = Job Done. (Almost)



In contrast to the other forces, gravity has a dimensionful coupling constant

$$G = \frac{\hbar c}{8\pi M_{\rm pl}^2}$$
 with $M_{\rm pl} \approx 10^{18} \,\,{\rm GeV}$

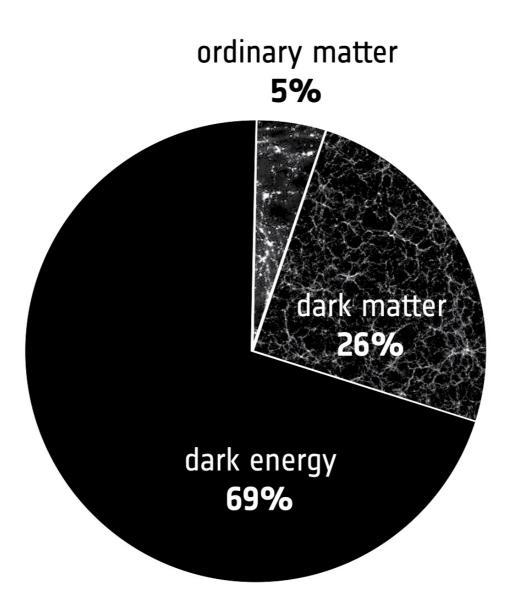
This means that

Strength of Gravity
$$\sim \left(\frac{E}{M_{\rm pl}}\right)^2 \sim GE^2$$

This is perfectly fine for any experiments that we can currently perform. But... • Black holes

• Big Bang

The Dark Universe



The Cosmological Constant

The energy density of the vacuum – or cosmological constant – acts as dark energy

Observed:
$$\rho_{\Lambda} \approx (10^{-3} \text{ eV})^4$$

Value of Standard Model: $\rho_{\rm SM} = (10^{12} \text{ eV})^4$

A solution (of sorts!):

 $\rho_{\Lambda} = \rho_{\rm SM} + \text{something else}$

This is the second, much more acute, hierarchy problem in physics.

Dark Matter

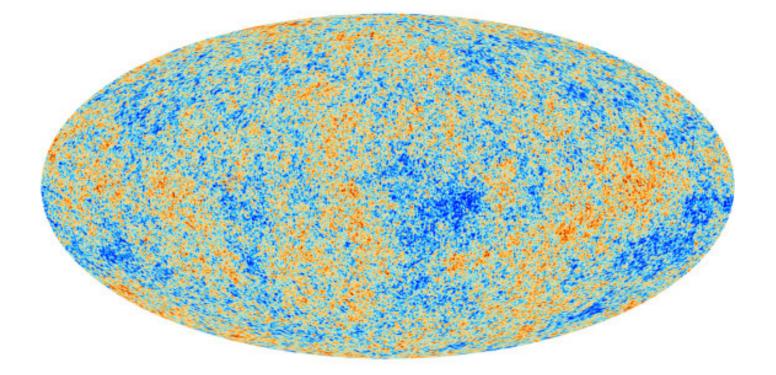
Whenever we weigh galaxies, or galaxy clusters, they always have more matter than we can see.



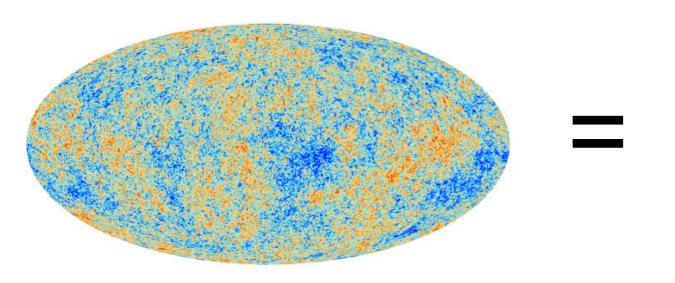
Further evidence comes from early universe cosmology.

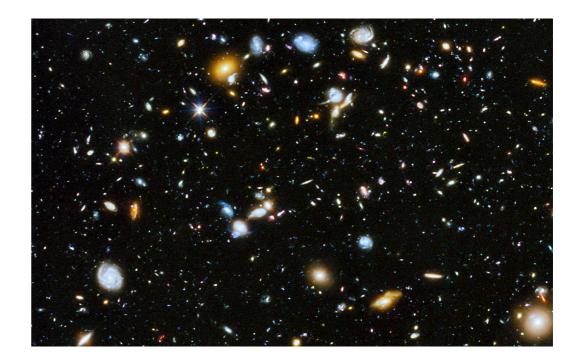
Big question: does it interact with Standard Model other than through gravity?

The CMB

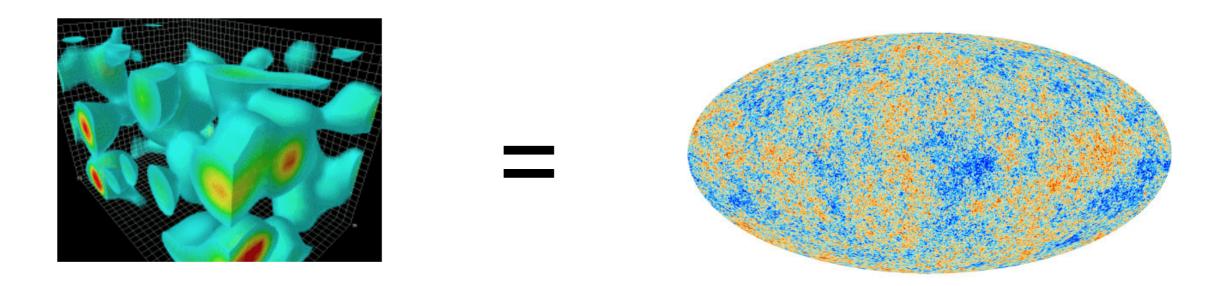


Structure Formation





Inflation



Big Question: What quantum field are we looking at? And how can we see it now?

Summary

Still lots of work to be done!