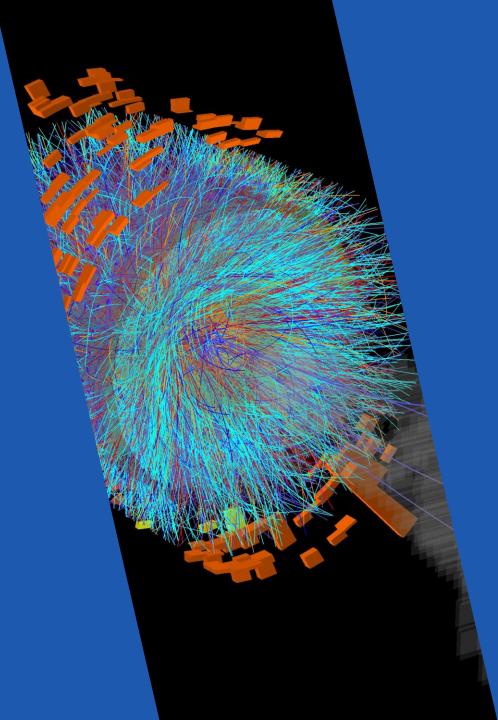


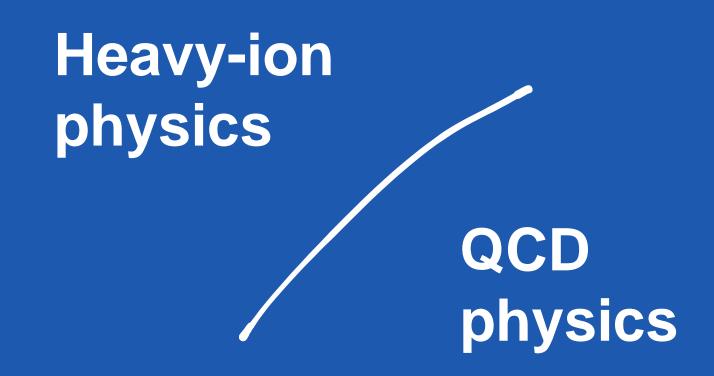
CERN Summer Student Lectures 2024

Heavy lons 1/3

Francesca Bellini

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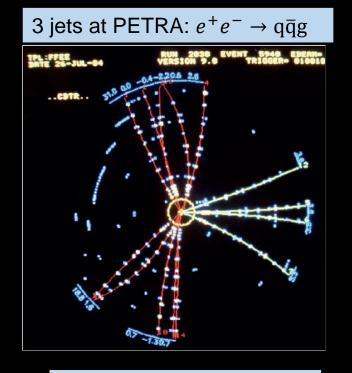


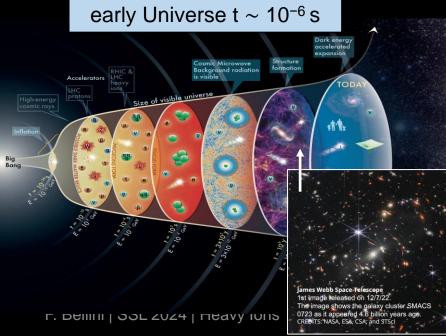


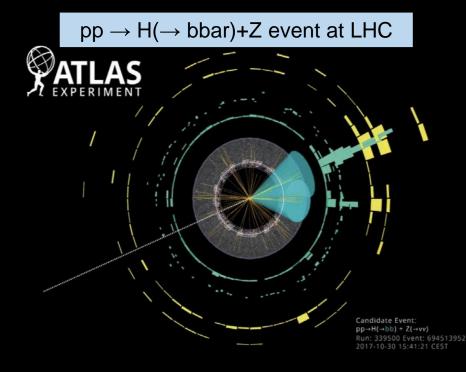
In these lectures:

- Basic concepts of QCD and heavy-ion physics
- Experimental principles
- Production and characterization of the QGP at the LHC
- The HIP programme at the LHC: present and future

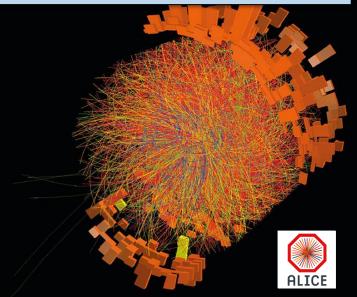
Take home message in blue background slides



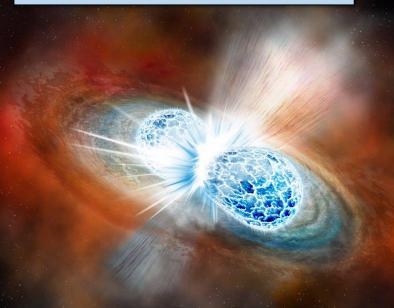




One central Pb-Pb collision at LHC



neutron stars and NS mergers



(extra)ordinary matter



neutron-

g

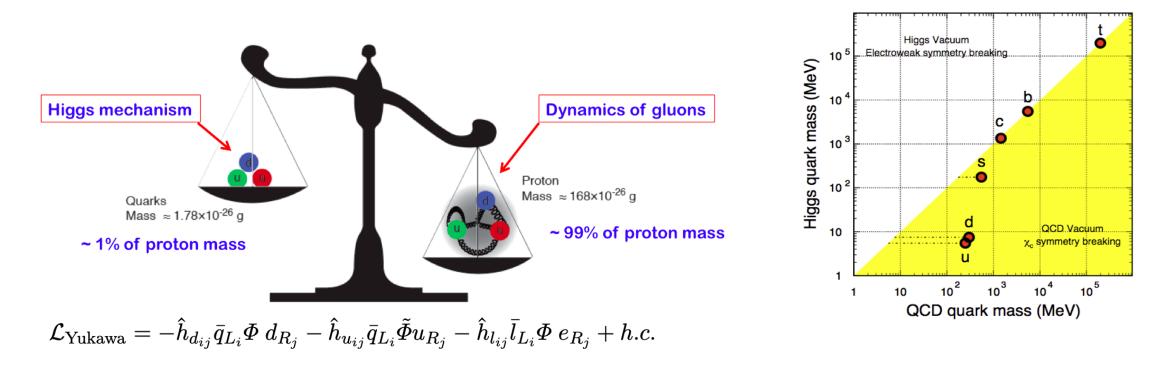
Artist's impression of

Why studying QCD 1/3

Because we have mass



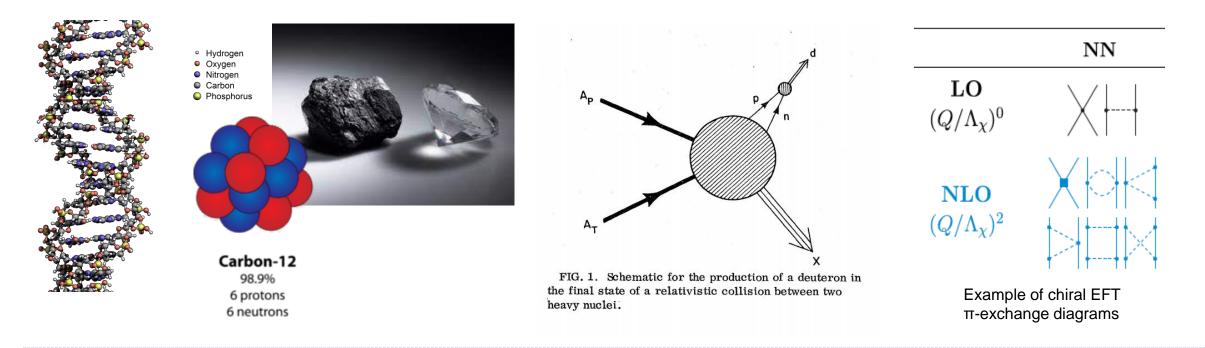
- → Mass is concentrated in atomic nuclei, i.e. in protons and neutrons but the mass of protons and neutrons is much larger than the sum of the masses of the valence quarks that come from the Higgs mechanism
- \rightarrow Most of the hadron mass comes from the strong interaction among color charges!



Why studying QCD 2/3

Because we are made of **bound (=strongly-interacting!) objects**

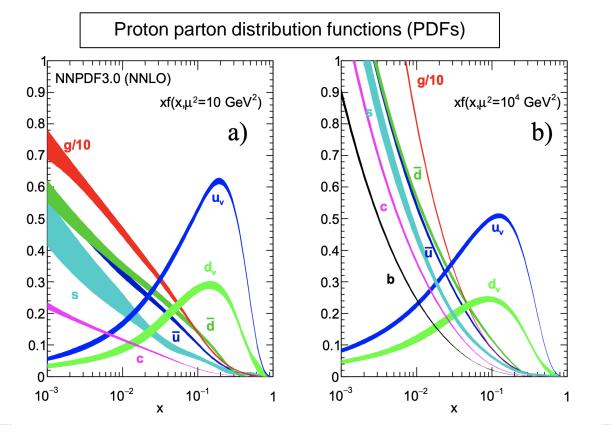
- → Nuclear many-body theories attempt to describe how the nuclear structure emerges from the basic properties of the strong interaction... but *«the description of all but the lightest nuclei at the QCD level is inefficient at best, and impossible at worst»* [H. Hergert (2020), Front. Phys. 8:379]
- \rightarrow We have effective field theories but not yet a complete understanding!

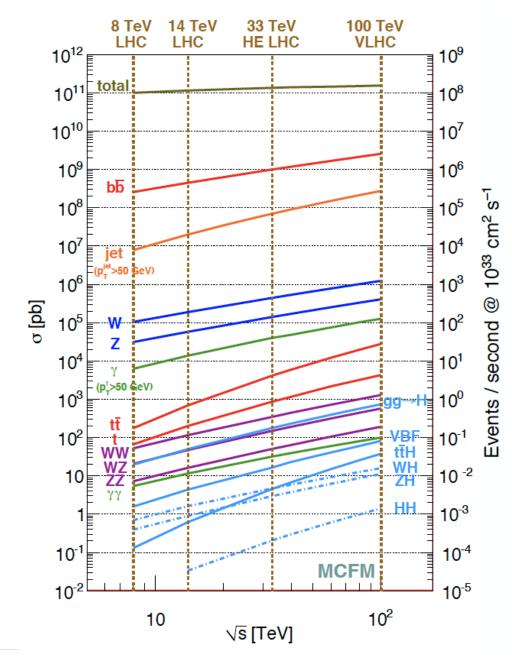


Why studying QCD 3/3

At hadron colliders we need knowledge of

- the projectile/target PDFs
- The physical background for Standard Model precision measurements and BSM searches





Recall: fundamental properties of QCD

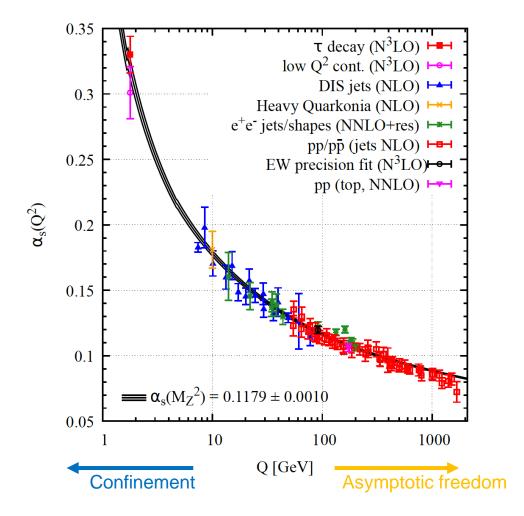
Quarks and gluons exist in nature as confined in colorless hadrons: ordinary matter at room temperature. → confining property of QCD

The strong coupling, i.e. the effective strength of the interaction, becomes weaker for processes involving larger quadrimomentum exchange.

 \rightarrow asymptotic freedom

Chiral symmetry in QCD:

- Spontaneously broken in the chiral limit
- Explicitly broken by non-zero quark masses
- → the mass of hadrons is a consequence of the strong interaction acting among their constituents.



The QCD phase transition (a very simplified picture)

At low temperature and "normal" density, i.e. us in this room at T \sim 1/40 eV, colored partons are confined in hadrons with chiral symmetry being broken (giving 99% mass to the proton!)

Idea developed back in the 1970's:

by **heating** hadronic matter up to high T and **compressing** it at high pressures, we can observe a **phase transition** from **confined** matter to a deconfined state made of colored quarks and gluons

What are the critical conditions at which the QCD phase transition occurs?

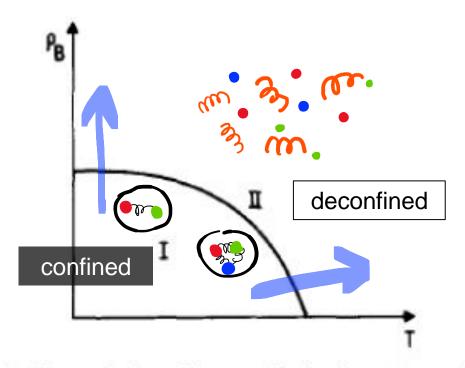


Fig. 1. Schematic phase diagram of hadronic matter. ρ_B is the density of baryonic number. Quarks are confined in phase I and unconfined in phase II.

N. Cabibbo, G. Parisi, Phys. Lett. B59 (1975) 67 J.C. Collins, M.J. Perry, Phys. Rev. Lett. 34 (1975) 1353

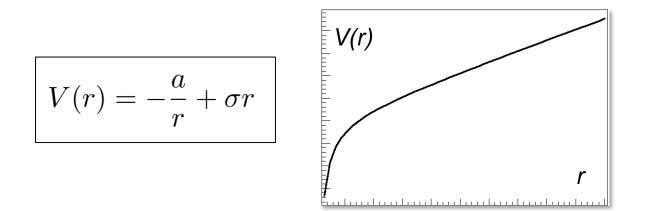
Understanding confinement

Properties of the QCD vacuum:

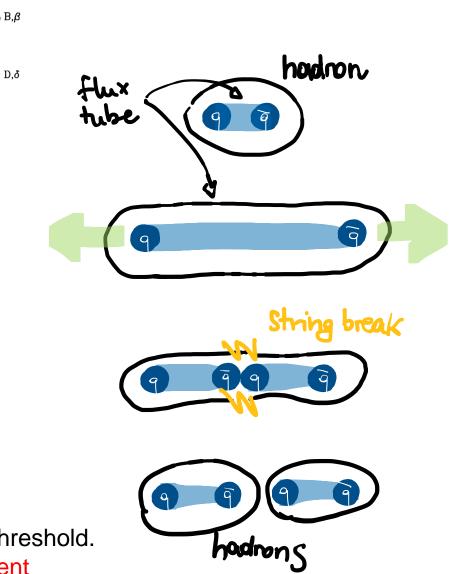
- Gluon-gluon self-interaction (non-abelian)
- QCD field lines compressed in flux tube (or "string")

C.Y

The q-qbar potential is of the form (Cornell potential):

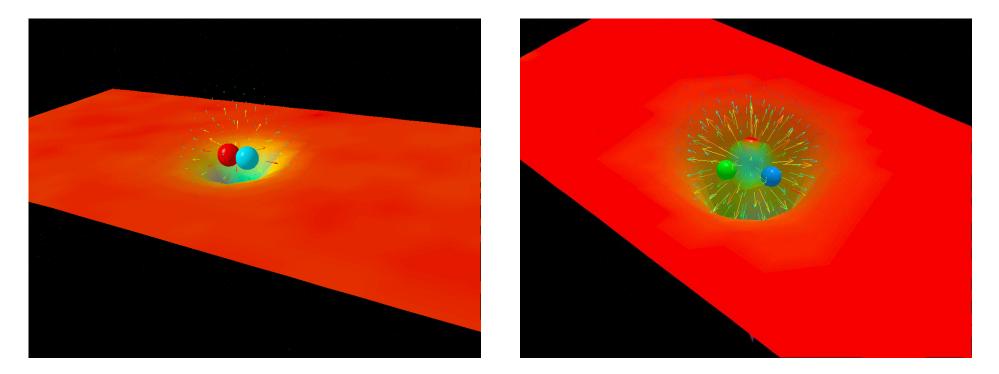


- The potential grows with distance.
- If pulled apart, the energy in the string increases
- A new q-qbar pair is created once the energy is above production threshold.
- No free quark can be obtained by breaking a flux tube \rightarrow confinement



QCD flux tubes in lattice QCD

The animations represent confinement of quarks in mesons and baryons as due to flux tubes. The colorscaled surface represent the QCD vacuum action density, which gets suppressed in the region among the (two or three) quarks (coloured spheres). A linear confinement potential is felt between quarks in baryons as well as mesons.



Animations from: <u>http://www.physics.adelaide.edu.au/theory/staff/leinweber/VisualQCD/ImprovedOperators/index.html</u> F. Bissey, et al, Phys. Rev. D **76**, 114512 (2007) [arXiv:hep-lat/0606016]

The MIT Bag model

A simple phenomenological model, describes confinement by assuming that hadrons are confined in bubbles of perturbative (= empty) vacuum and are surrounded by QCD vacuum (a fluid of gg pairs) exerting pressure.

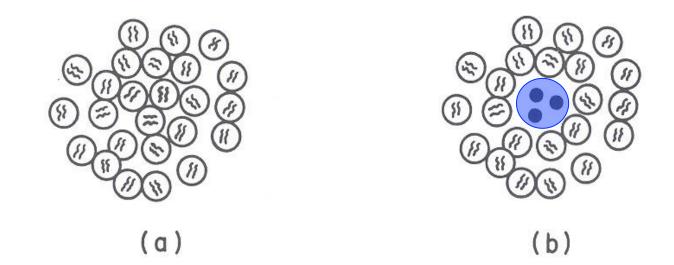


FIG. 9. The QCD vacuum state is depicted in (a). It is a random distribution of cells that contain a gluon pair in a color and spin singlet state. Quarks (in a color singlet configuration) displace these cells, creating a region (or "bag") of "empty" vacuum, as shown in (b).

A. Chodos, R. L. Jaffe, K. Johnson, C. B. Thorn, and V. F. Weisskopf, Phys. Rev. D 9, 3471; T. DeGrand, R.L. Jaffe, K. Johnson, J. Kiskis, Phys. Rev. D12 (1975) 2060

The MIT Bag model (2)

Inside the bag, quarks have very small masses and the interaction is weak

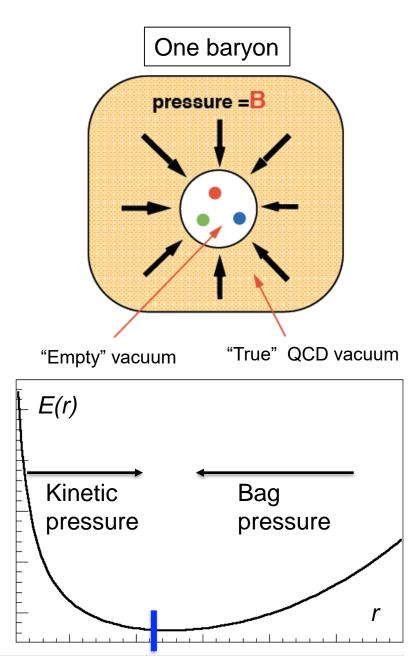
Outside the bag, quarks are not allowed to propagate, no colored partons, but quark and gluon condensates

The equilibrium between the kinetic pressure of the quarks inside the hadron vs the pressure of the surrounding QCD vacuum ("bag pressure", *B*) defines the radius *R* of the hadron.

If the hadron can be modeled as *N* massless Dirac fermions in a spherical cavity,

$$E = \frac{2.04N}{R} + \frac{4\pi}{3}R^3B$$

By asking $\partial E/\partial R = 0$ and $R(p) \sim 0.8$ fm $\rightarrow B_{MIT} \sim (200 \text{ MeV})^4$



Deconfinement

For a gas of massless, relativistic partons the pressure can be calculated from the Stefan-Boltzmann law

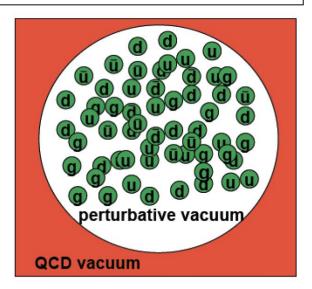
$$P = \left(n_g + \frac{7}{8}n_f\right)\frac{\pi^2 T^4}{90}$$

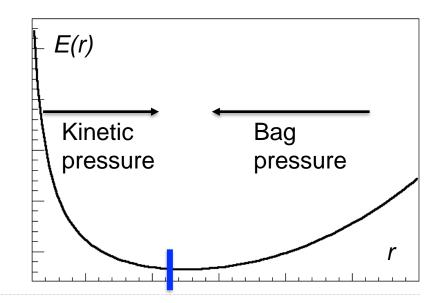
where the degrees of freedom of the system are $n_{\rm g} = 8$ gluons x 2 spin = 16 $n_{\rm f} = 2$ quark flavors x 2 spin x 3 colors + anti-q = 24

The systems gets **deconfined** if the kinetic pressure exceeds the bag pressure

P > B → T⁴ > (200 MeV)⁴ * 90 / (16+7/3) / π^2 → T_c > 141 MeV (critical temperature)

Above T_c , the system undergoes a phase transition to a state of matter where quark and gluons are (quasi) free, the Quark-Gluon Plasma





Recall: phase transitions

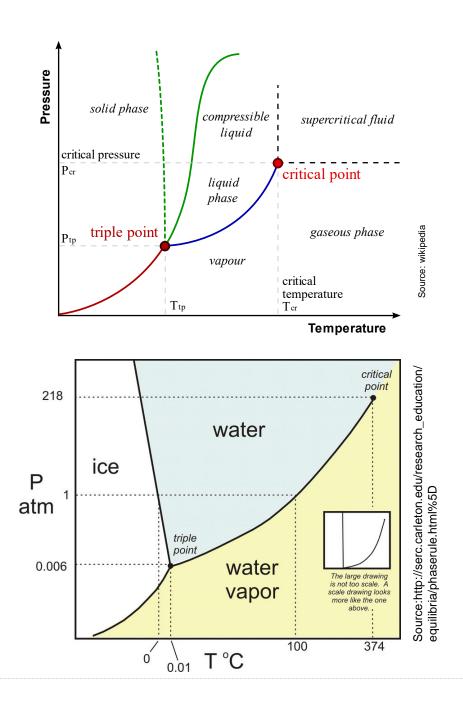
A **phase transition** is the transformation of a thermodynamic system from one phase (or state of matter) to another.

e.g. ice \Leftrightarrow water \Leftrightarrow vapour

e.g. confinement \Leftrightarrow deconfinement in QCD

During a phase transition, certain properties of the medium change, often discontinuously, as a result of external conditions e.g. pressure, temperature, ...

The measurement of these external conditions at which the transformation occurs is called the phase transition point.



The QCD phase diagram

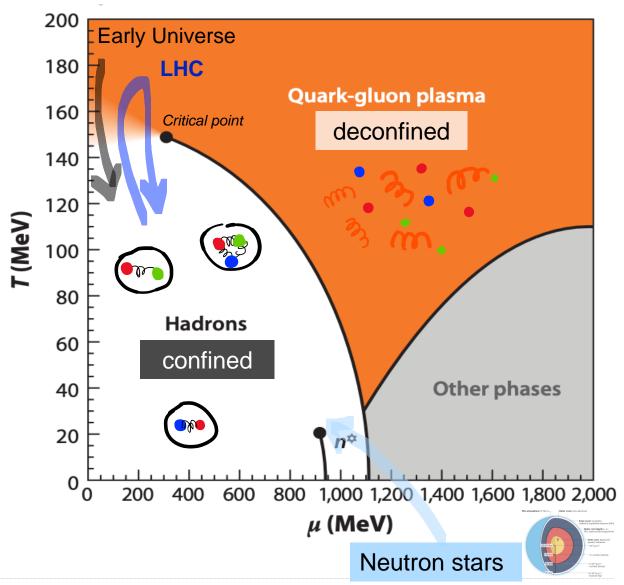
The phases of QCD matter can be summarized in a phase diagram as a function of two parameters:

temperature T and baryochemical potential μ_B

$$\mu_B = \frac{\partial E}{\partial n_B}, \quad n_B = n(B) - n(\overline{B})$$

 $\mu_{\rm B} = 0 \rightarrow$ antimatter / matter = 1 as at the LHC and in the Early Universe!

The quark-gluon plasma is the deconfined phase of strongly-interacting matter.



Which QCD energy regime are we dealing with?

Having in mind:

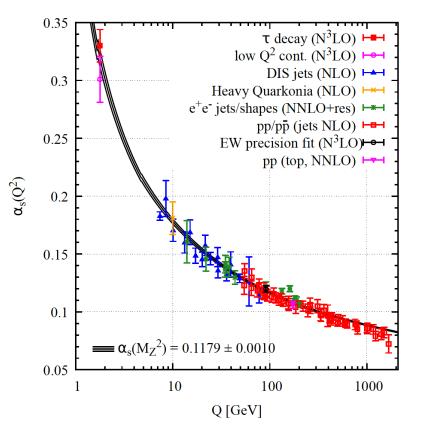
- MIT bag model estimate for the critical temperature: $T_c \sim 140 \text{ MeV}$
- $\Lambda_{\rm QCD}(m_{\rm Z,}\,N_{\rm f}=3)=244~{\rm MeV}$

But also that at T = 200 MeV, the typical kinetic energy

- for a non-relativistic particle is $E = 3/2 k_{\rm B}T = 300 \text{ MeV}$
- for a relativistic particle is $E = 3k_BT = 600 \text{ MeV}$

Low $Q \rightarrow \alpha_s$ is not small! \rightarrow The QCD transition is a non-perturbative QCD problem

- Need models to deal with (phenomenology)
- Use Lattice QCD for calculations from first principles



Lattice QCD basics

Lattice QCD (IQCD) is a well-established non-perturbative method to solve QCD starting from first principles, i.e. the QCD Lagrangian.

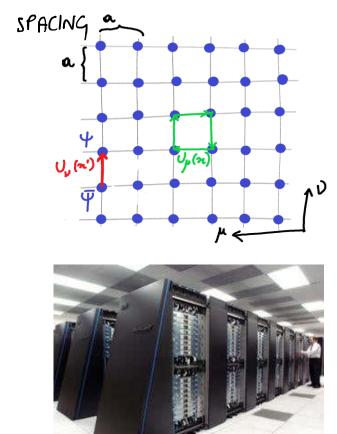


Image: Argonne Nat. Lab.

The Euclidean space-time is discretized in a 4D-hypercubic lattice with 3 real spatial and 1 imaginary time.

The finite lattice **spacing** *a* acts as an ultraviolet cutoff for the theory. The quark fields $\psi(x)$ are defined on lattice sites. The gluon fields $U_u(x)$ are defined as links between lattice sites.

The QCD Lagrangian in the Minkowski space is transformed into the action in Euclidean space and then the theory is solved by numerical integration.

F. Bellini | SSL 2024 | Heavy lons

Thermodynamics of QCD matter on the lattice

Thermodynamical properties of a quantum system can be calculated according to the principles of statistical mechanics from the **partition function**, **Z**.

$$Z = Tr \left[e^{-\beta (\hat{H} - \mu_i \hat{N}_i)} \right]$$

$$P = T \frac{\partial \log Z}{\partial V}; \qquad N_i = T \frac{\partial \log Z}{\partial \mu_i};$$

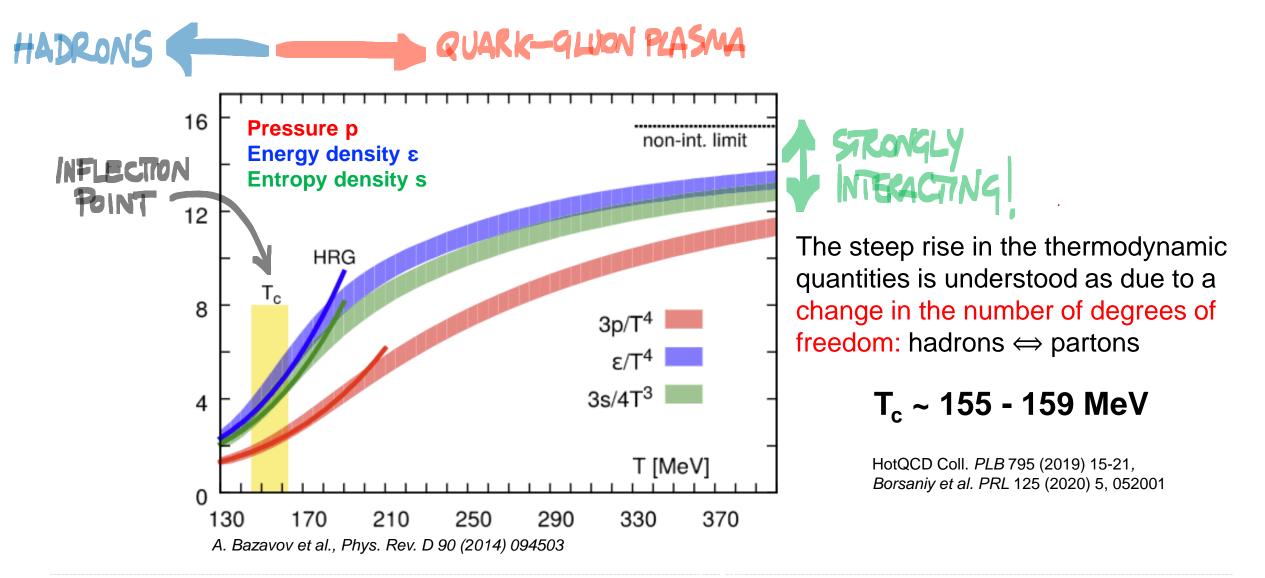
$$S = \frac{\partial T \log Z}{\partial T} \qquad E = -PV + TS + \mu_i N_i$$
heat both & particle reservation

A system of **QCD degrees of freedom** can be represented by a **grand canonical** (GC) ensemble, where a given volume element can exchange particles and heat with its surrounding (heat bath and particle reservoir).

On the lattice, the GC partition function can be used to extract the expectation value of the physical observables.

$$\begin{aligned} \mathcal{Z}(T,V,\vec{\mu}) &= \int \prod_{\mu} \mathcal{D}A_{\mu} \prod_{f=u,d,s...} \mathcal{D}\psi_{f} \mathcal{D}\bar{\psi}_{f} \, \mathrm{e}^{-S_{E}(T,V,\vec{\mu})} \\ \langle \mathcal{O} \rangle &= \frac{1}{Z(T,V,\vec{\mu})} \int \prod_{\mu} \mathcal{D}A_{\mu} \prod_{f} \mathcal{D}\psi_{f} \mathcal{D}\bar{\psi}_{f} \, \mathcal{O} \, \mathrm{e}^{-S_{E}(T,V,\vec{\mu})} \end{aligned}$$

Equation of State (EoS) from lattice QCD



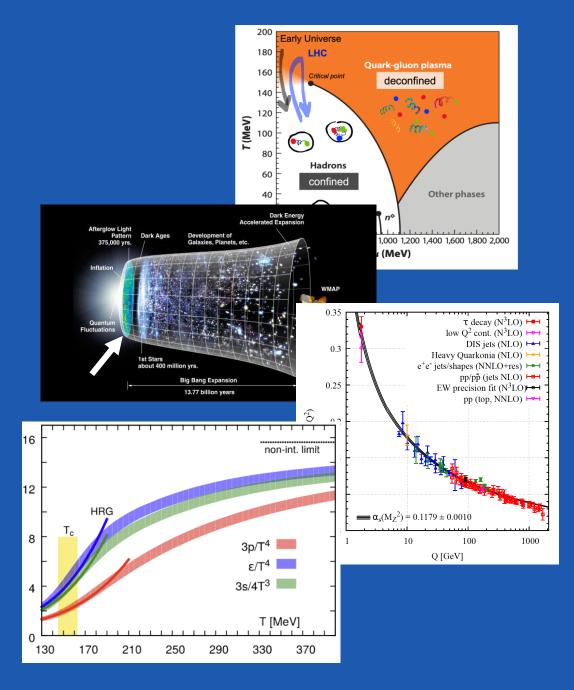
The QGP is a state of strongly-interacting matter resulting from the phase transition of nuclear/hadronic (color-neutral) matter under extreme conditions of pressure or temperature

 \rightarrow the Universe up to O(1-10µs) after the Big Bang

 \rightarrow the properties of the QGP emerge from the fundamental properties of the strong interaction

 \rightarrow physics of **condensed** QCD matter

Next: the experimental quest towards a **quantitative** characterization of the QGP

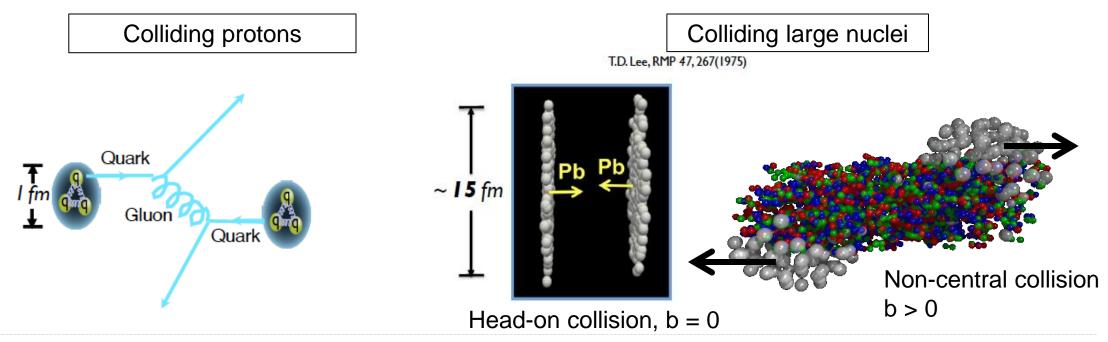


Experimental principles

QCD in extreme conditions in the laboratory

A QGP can be formed by compressing large amount of energy in a small volume

- \rightarrow collide **heavy nuclei** (multiple, ~simultaneous nucleon-nucleon collisions)
- \rightarrow control the energy deposited in the collision region by varying the collision system
 - nuclear species, p-Pb, pp
 - vary impact parameter (centrality)



Hadron and ion colliders

With symmetric proton beams with energy E, the centre-of-mass energy is $\sqrt{s} = 2E$.

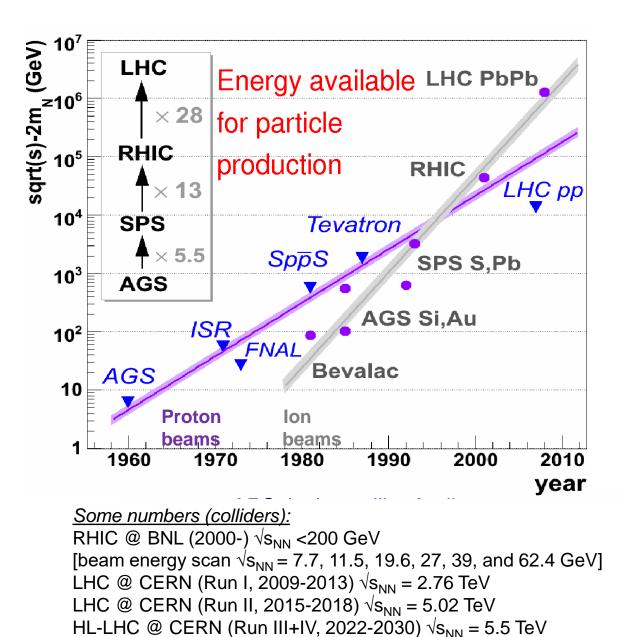
With heavy-nuclei, only protons can be accelerated, but neutrons are there too:

 $p_{\rm A} = Z/A p_{\rm proton}$

<u>At the LHC</u>, the rigidity of accelerated particles is fixed by the magnet field configuration ($B_{max} = 8.3 \text{ T}$).

For the ²⁰⁸Pb⁸²⁺ ions used at the LHC: $p_{Pb} = 82 / 208 p_{proton}$

 $p_{\text{proton}} = 6.5 \text{ TeV} (\text{Run 2}) \rightarrow p_{\text{Pb}} = 2.56 \text{ TeV}$ $\rightarrow \sqrt{s_{\text{NN}}} = 5.02 \text{ TeV} \rightarrow \sqrt{s} \sim 1.04 \text{ PeV}$



NICA @ JINR (2021) $3 < \sqrt{s_{NN}} < 11 \text{ GeV}$

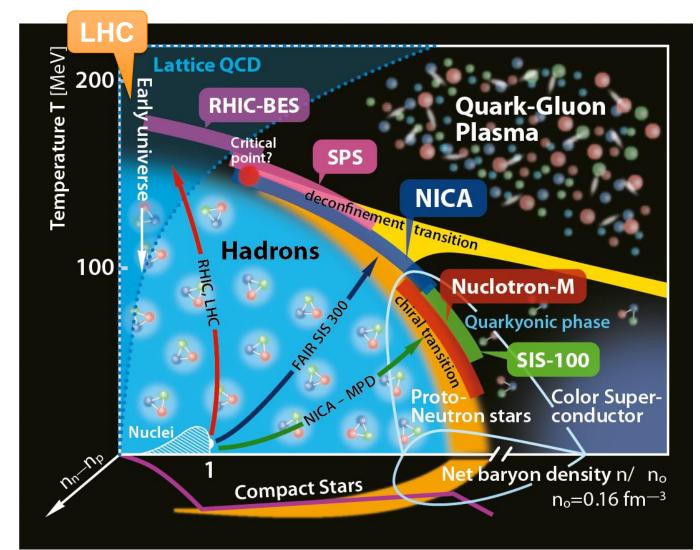
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Experimental exploration of the QCD phase diagram

RHIC and the LHC explore the region of the phase diagram for $\mu_{\rm B} \sim 0$

which is also the region of the phase diagram where lattice QCD calculations can be performed

Low energy (& high $\mu_{\rm B}$) are the conditions to study the 1st order transition and the search for the critical point, the key regime being 2.5 < $\sqrt{s_{\rm NN}}$ < 8 GeV



Heavy-ion physics worldwide: present / high energy

Operating since 1986

Circumference 6.9 Km

max p = 450 A/Z GeV

Ongoing: NA61/Shine

 $\sqrt{s_{NN}} < 20 \text{ GeV}$

CERN SPS



Super Proton Syncrotron and Large Hadron Collider, CERN (Switzerland/France)

Inth are (M) in

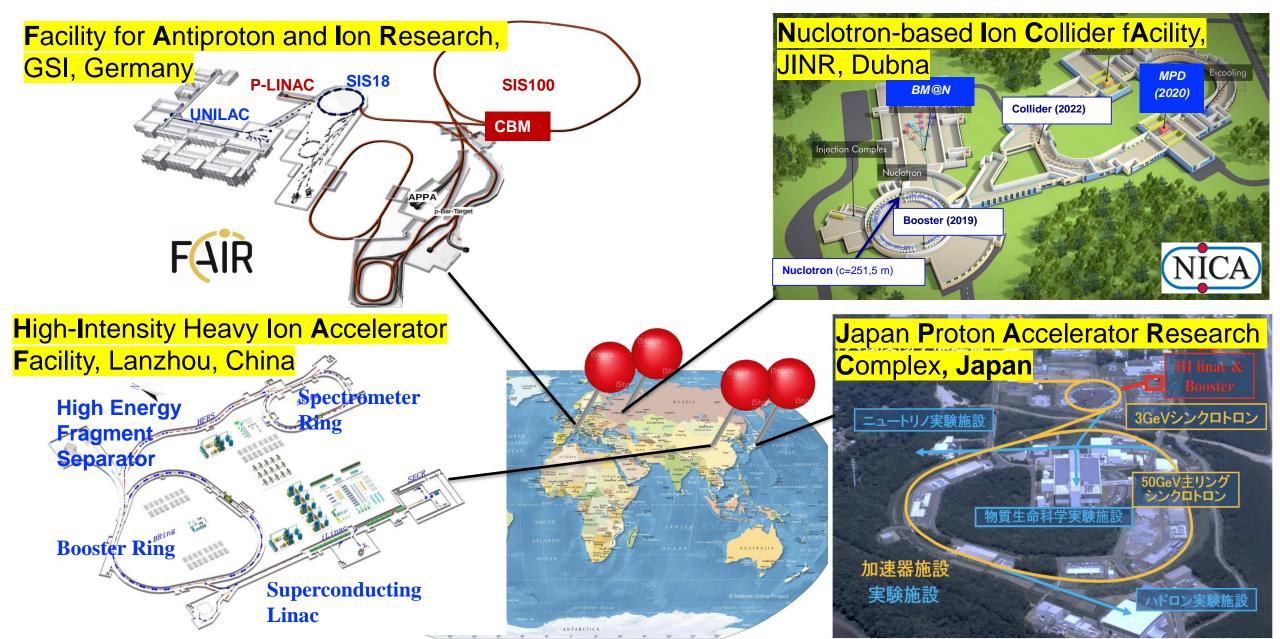
Brookhaven RHIC

- Operating since 2000
- Circumference 3.83 km, 2 rings
- Superconducting magnets
- $\sqrt{s_{NN}} = 3 200 \text{ GeV}$ in Au-Au
- Beam energy scan I: 2010-11
- Beam energy scan II: 2019-22
- Ongoing exp: STAR

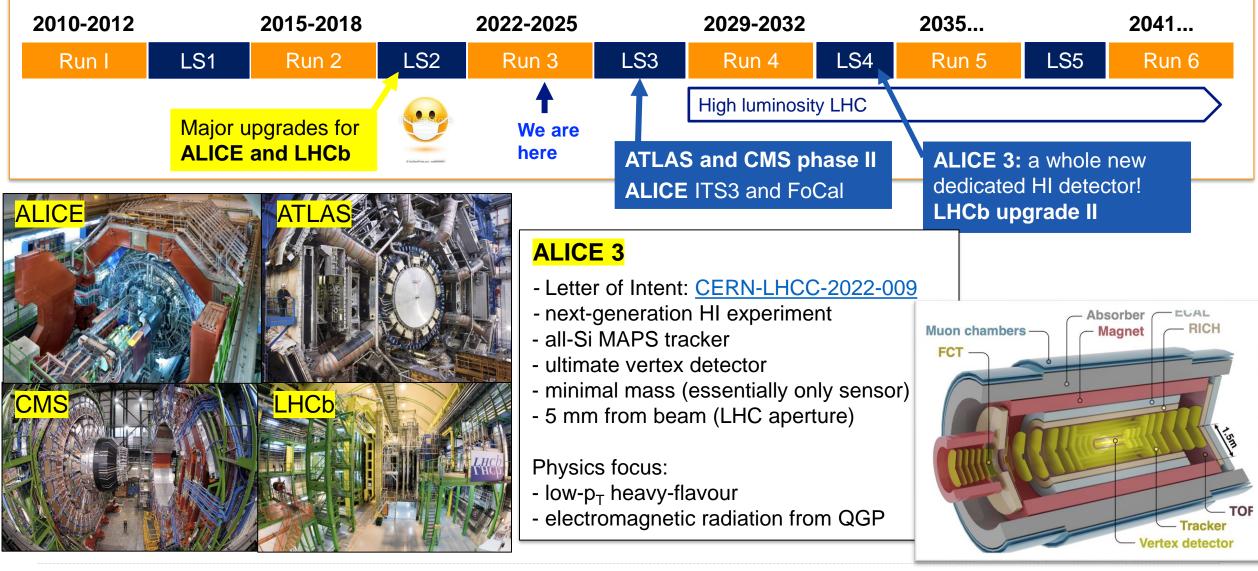
CERN LHC

- Operating since 2009
- Run III: started in 2022
- Circumference: 27 km
- B-field: 8 T, superconducting
- pp $\sqrt{s} = 0.9 13.6 \text{ TeV}$
- Pb-Pb $\sqrt{s_{NN}} = 2.76-5.5 \text{ TeV}$
- Main ongoing: ALICE, ATLAS, CMS, LHCb

Heavy-ion physics worldwide: future / low energy



Heavy-ion physics at the LHC



Guidance for the experimental study of the QGP

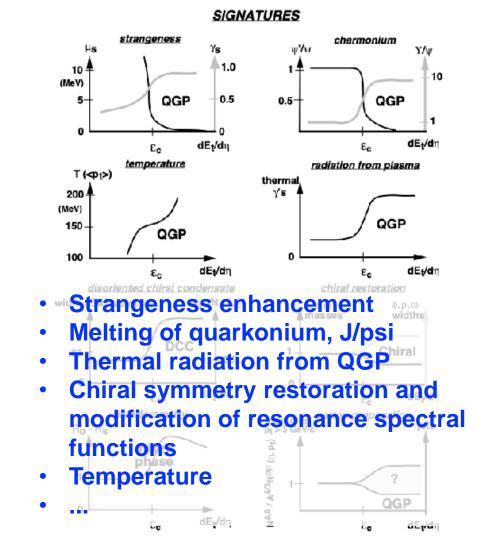
How can a QGP, once formed, be detected and investigated? How can the physical properties be determined?

Back in 1990's, some **"smoking gun"** observables were proposed, however these were not based on solid calculations (IQCD was still a "baby"...)

Today, we have several powerful theoretical tools at disposal:

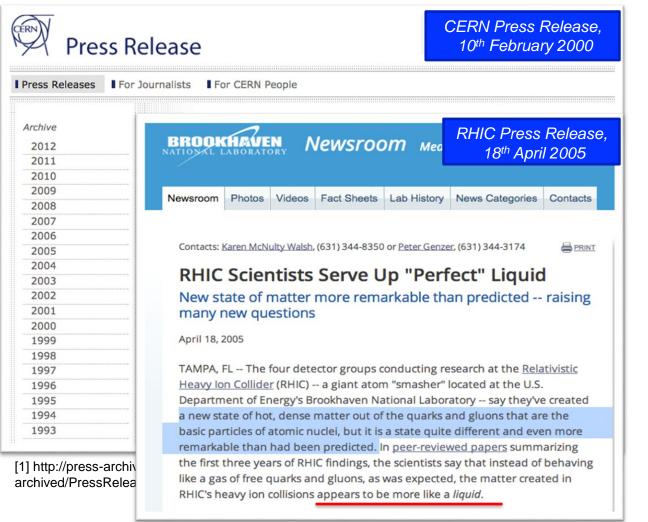
- Lattice QCD (the only one from first principles)
- Hydrodynamics and standard model of HIC
- Bayesian analysis
- Transport models

Remember: the QGP is not static but an evolving system!



J.Harris, B.Muller, Annu Rev. Part. Nucl. Physics 46 (1996) 71

QGP: from "discovery" to "measurement"



[2] http://www.bnl.gov/newsroom/news.php?a=1303

First "compelling" evidence of QGP at SPS

The "remarkable" evidence at RHIC that the hot matter formed is

- Extremely strongly interacting (sQGP)
- Absorbing energy of traversing partons
 → Almost opaque medium
- Reacting to pressure gradients by flowing with very small shear viscosity

→ Almost perfect liquid

At the LHC the increased beam energies and the state-of-the-art experiments allow the measurement of a hotter, larger and longer-lived QGP with increased precision

Experimental characterisation of the QGP

1. Thermodynamics and global properties

- Energy density
- Temperature
- Lifetime and size

2. Hydrodynamics and transport properties

- Shear viscosity η/s
- Bulk viscosity ζ/s

3. Hadron formation and flavour equilibration

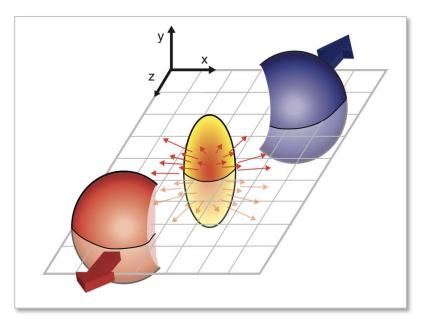
- Formation of hadrons and bound states
- Chemistry / flavour composition and hadron rates
- Charm equilibration

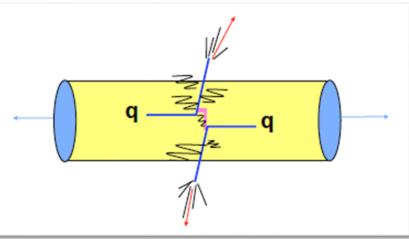
4. Interaction of partons in a colored medium

- Energy loss of partons / jet quenching
- Transport coefficients
- Diffusion

5. Influence of deconfined medium on the strong force

Color screening

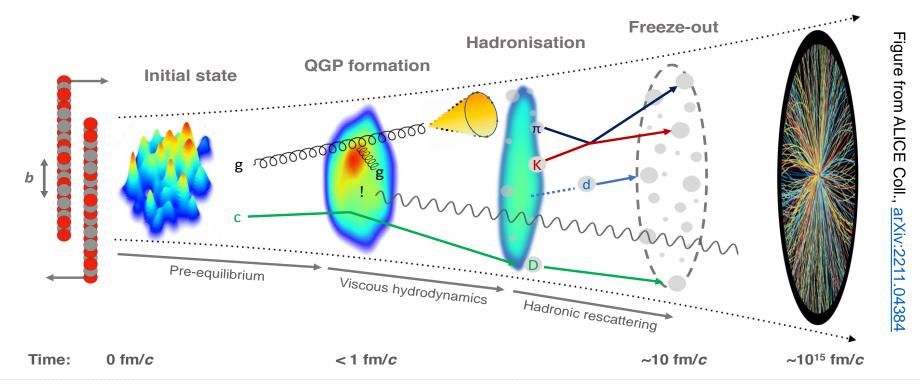




The "little bang" in the laboratory

"Little bangs" of heavy nuclei can be studied similarly as the Early Universe **No direct observation of the QGP is possible**

 \rightarrow use particles that decouple from the system at different phases of the evolution as probes



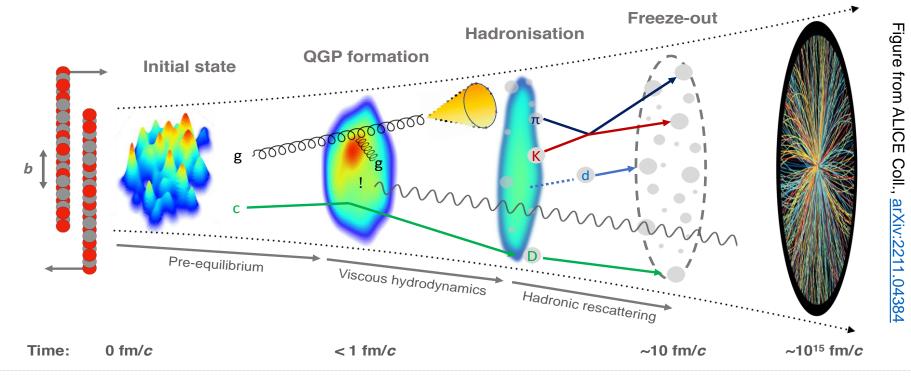
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The "little bang" in the laboratory

Charm and beauty quarks (\rightarrow open HF, quarkonia), high-p_T partons (\rightarrow jets)

produced in the early stages in hard processes, traverse the QGP interacting with its constituents

- \rightarrow rare, calibrated probes, pQCD
- \rightarrow in-medium interaction (energy loss) and transport properties
- \rightarrow in-medium modification of the strong force and of fragmentation



The "little bang" in the laboratory

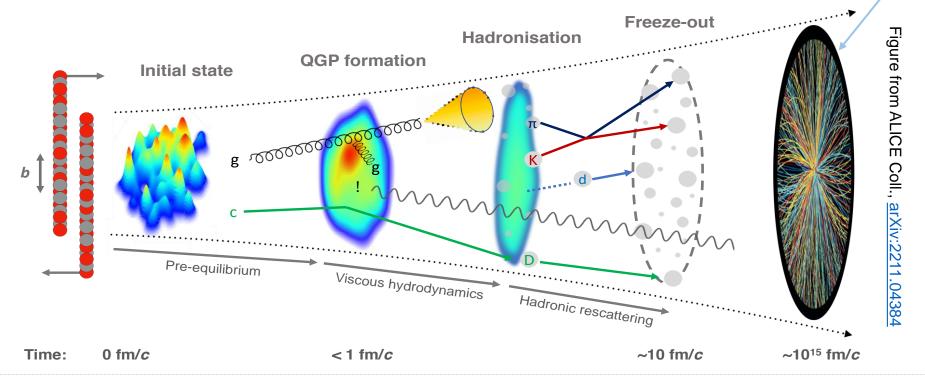
Low-p_T particles, light flavour hadrons (u,d,s, +nuclei)

produced from hadronization of the strongly-interacting, thermalized QGP constitute the bulk of the system

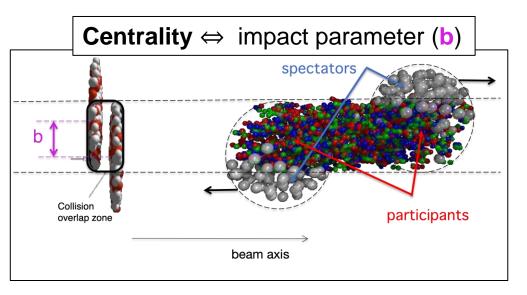
 \rightarrow non-perturbative regime

\rightarrow thermodynamical, hydrodynamical and transport properties

>2k charged particles per unit of rapidity in 5% most central Pb-Pb: 98% with $p_T < 2$ GeV/c, 90% pions



Centrality



Centrality = fraction of the total hadronic cross section of a nucleus-nucleus collision, typically expressed in percentile, and related to the **impact parameter** (b)

Correlation observed between number of particles produced at forward and at mid-rapidity \rightarrow Centrality is determined by counting the number of particles (multiplicity) or measuring the energy deposition in a region of phase space *independent* from the measurement.



Central collisions (e.g. 0-5%)

- \rightarrow smaller impact parameter
- \rightarrow larger overlap region
- \rightarrow more participants
- \rightarrow more binary collisions
- \rightarrow more particles produced

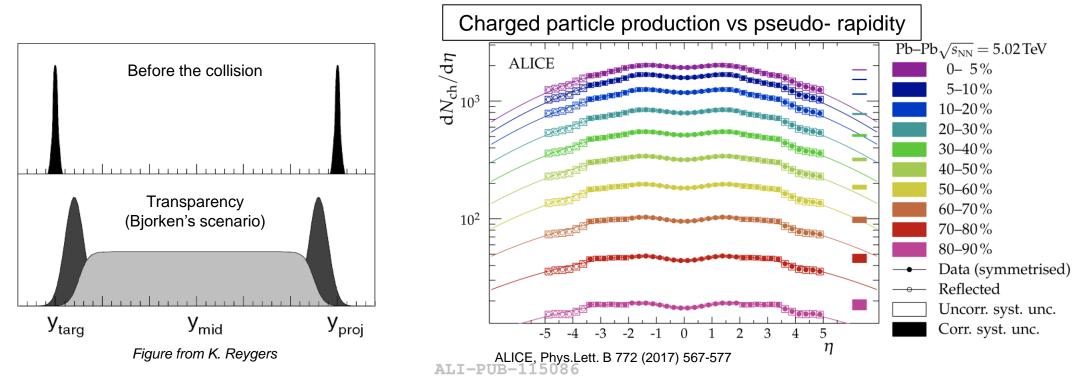
Peripheral collision (e.g. 80-90%)

- \rightarrow larger impact parameter
- \rightarrow smaller overlap region
- \rightarrow less participants
- \rightarrow less binary collisions
- \rightarrow less particles produced

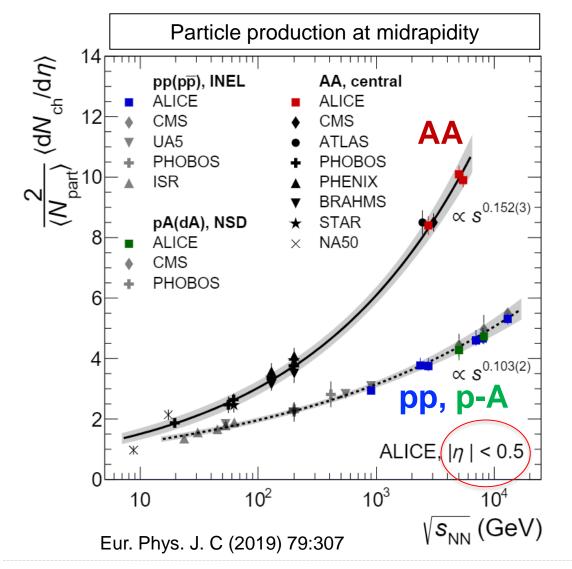
High energy HI collisions – the midrapidity region

In **high-energy** collisions (RHIC, LHC), the beams have large rapidity difference before the collision. After the collision nuclei slow down to lower γ and y, particles are produced with a "plateau" in the central rapidity region \rightarrow **Transparency regime**

The baryon number carried out by the colliding nuclei is outside the centre-of-mass rapidity region, $y_{CM} = 0$. The **midrapidity region** is the hottest region, where particle production is maximal and the highest temperatures are reached.

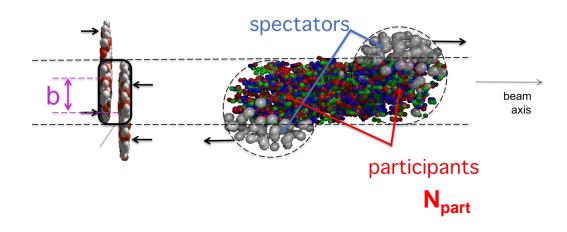


Charged particle production in central HI collisions



Particle production per participant in HI collisions follows a steeper power law than in pp, pA and increases by 2-3x from RHIC to the LHC

Heavy-ion collisions are more efficient in transferring energy from beam- to mid- rapidity than pp



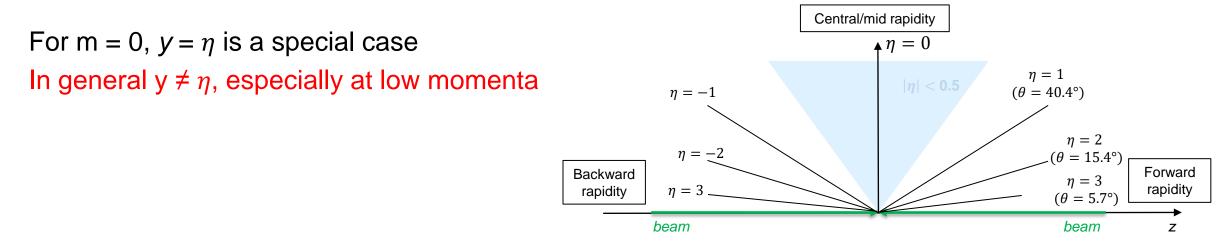
Pseudorapidity

The rapidity can be approximated by **pseudo-rapidity** in the ultra-relativistic limit in which *p>>m*:

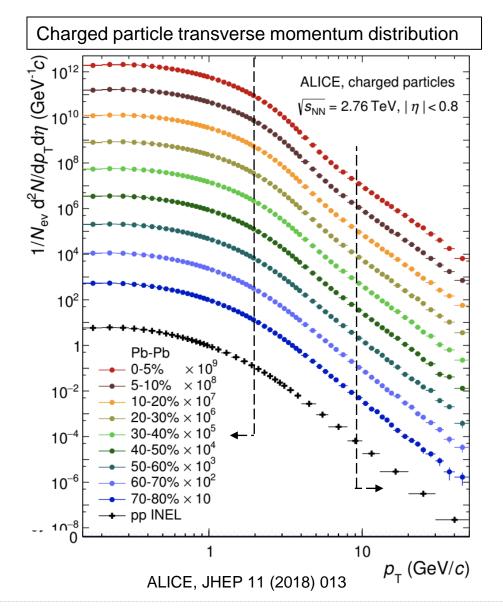
$$y = \frac{1}{2} \ln \frac{E + p \cos \vartheta}{E - p \cos \vartheta} \overset{p \gg m}{\approx} \frac{1}{2} \ln \frac{1 + \cos \vartheta}{1 - \cos \vartheta} = \frac{1}{2} \ln \frac{2 \cos^2 \frac{\vartheta}{2}}{2 \sin^2 \frac{\vartheta}{2}} = -\ln \left[\tan \frac{\vartheta}{2} \right] =: \eta$$
$$\cos(2\alpha) = 2 \cos^2 \alpha - 1 = 1 - 2 \sin^2 \alpha$$

Where ϑ is the angle between the direction of the beam and the particle. The relation to transverse and longitudinal momenta are

$$p = p_T \cdot \cosh \eta, \qquad p_L = p_T \cdot \sinh \eta$$



Key observable: particle "spectrum"

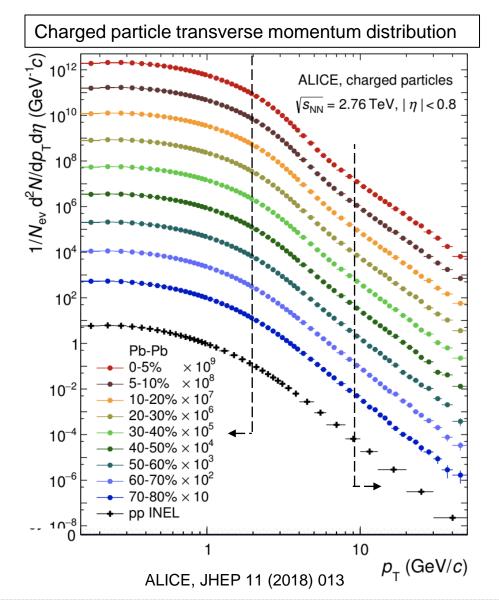


Particle "**spectra**": $d^2N/(dydp_T) = yield per event per (pseudo)rapidity unit per transverse momentum unit$

~95% of the produced charged particles are "soft", i.e. have $p_T < 2$ GeV/c.

Low/high- p_T ends of the spectra are due to different hadron formation mechanisms

Features of particle spectra



Low p_T (< 2 GeV/c)

- Particle spectra are described by a Boltzmann distribution → "thermal", ~ exp(-1/k_BT)
- "Bulk" dominated by light flavor particles produced by hadronization of the QGP
- Non-perturbative QCD regime

Mid p_T (2 to 8 GeV/c)

- Interplay of parton fragmentation and recombination of partons from QGP

High p_T (> 8-10 GeV/c)

- Particle spectra described by a power law
- Dominated by parton fragmentation (jets!)
- Perturbative QCD regime

Heavy-ion and high-energy physics have different goals and thus different detector requirements.

Observables:

- soft (low p_T) and hard (high p_T) probes
- hadron production rates (needs PID)
- flow (needs acceptance coverage)
- photon/W/Z (calorimetry)
- jets (coverage, high p_T)

In HI physics also emphasis on:

- midrapidity measurements
- identification of hadron species
- soft (non-perturbative) regime, i.e. low p_T
- minimum bias events

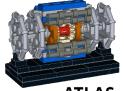
Complementarity of the LHC experiments



- ALICE
 - Low p_T

- PID

Low material budget next to IP



ATLAS/CMS

- ATLAS
- Wide pseudorapidity coverage
- High p_{T,} jets



LHCb

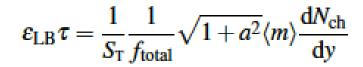
- Forward pseudorapidity
- PID
- Fixed target

LHCb

Determination of the initial energy density

Measurement of the multiplicity dN_{ch}/dy and the $\langle p_T \rangle$, or of the transverse energy, can be used to determine the initial energy density available in the collision.

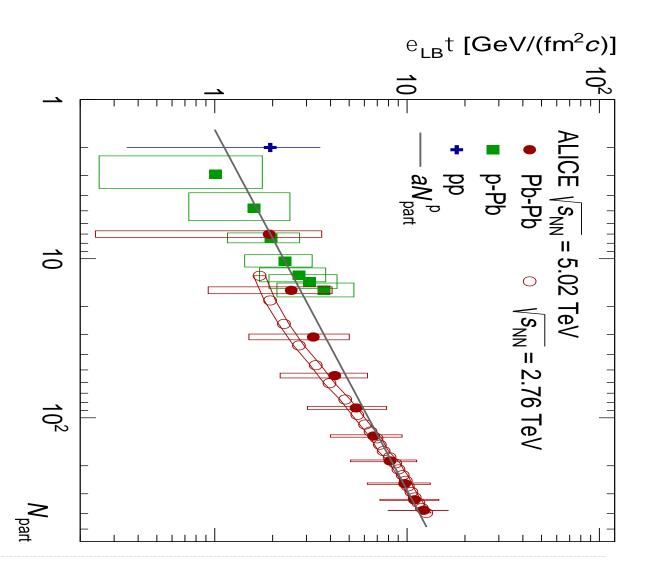
J. D. Bjorken, Phys. Rev. D 27 (1983) 140–151.



 S_T = Transverse area from Glauber model $f_{total} = 0.55 \pm 0.01$ = fraction of charged particles $\sqrt{(1+a^2)}$ <m> = effective transverse mass

$\varepsilon_{\text{LB}}\tau_0$ (0-5%) = (12.5 ± 1.0) GeV/fm²/c

For τ_0 ~1fm/c, ~20x the energy density of a hadron! Well above the critical energy density for the phase transition to occur!



Formation of quark-gluon plasma at the LHC

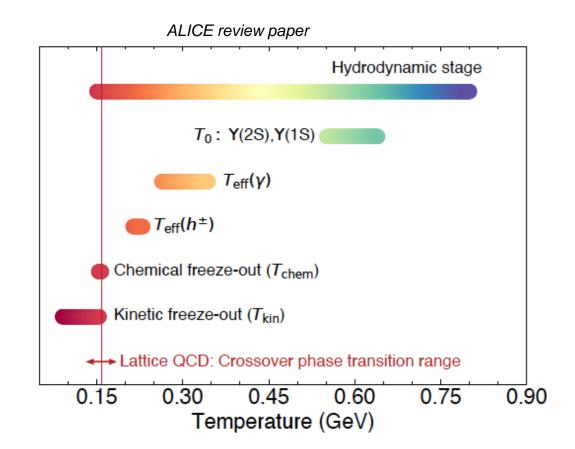
The conditions to form a QGP are met and exceeded in heavy-ion collisions at the LHC.

The **initial energy density** estimated in central collisions is \sim 12 GeV/fm³ at the early time of 1 fm/c

 \rightarrow ~70x the density of atomic nuclei

The **initial QGP temperature** is up to 5 times higher than the QCD decofinement temperature predicted by ab-initio lattice QCD calculations, $T_{pc} = 155-159$ MeV

The matter created has the largest temperature and energy density ever observed!

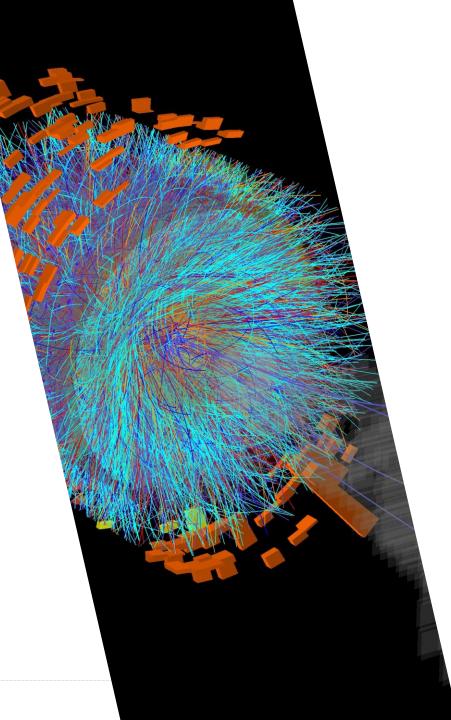


Bonus material

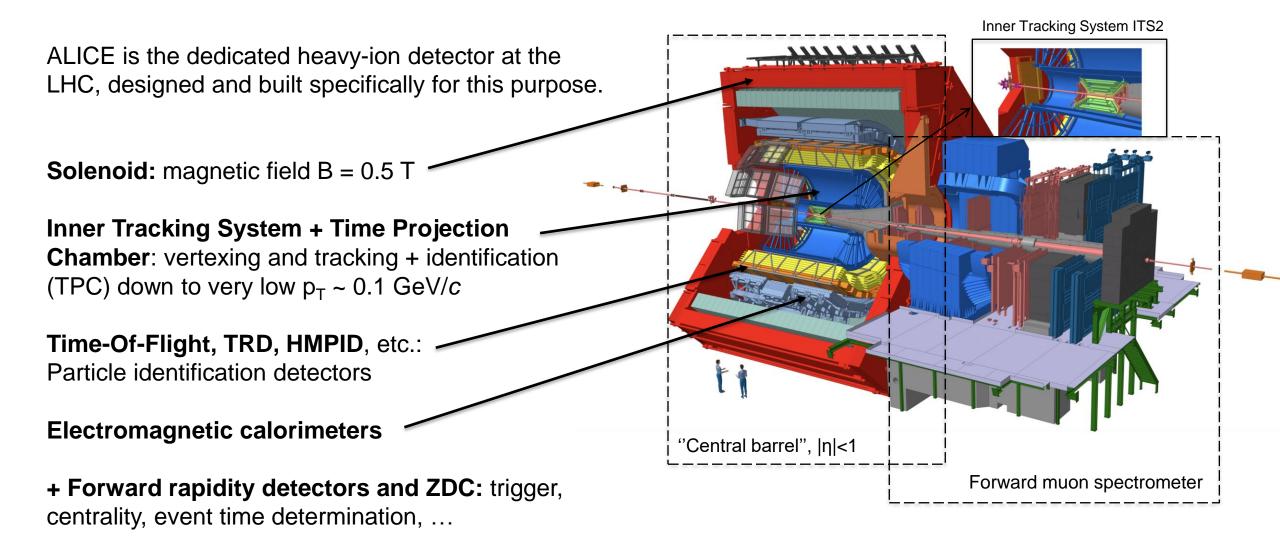
Further readings:

- [review] ALICE Collaboration, The ALICE experiment -- A journey through QCD, arXiv:2211.04384
- [future] CERN Yellow Report on QCD with heavy-ion beams at the HL-LHC, arXiv:1812.06772
- [future] Letter of intent for ALICE 3: A next generation heavy-ion experiment at the LHC, arXiv:2211.02491

+ many more reviews on specific topics can be found on arXiv

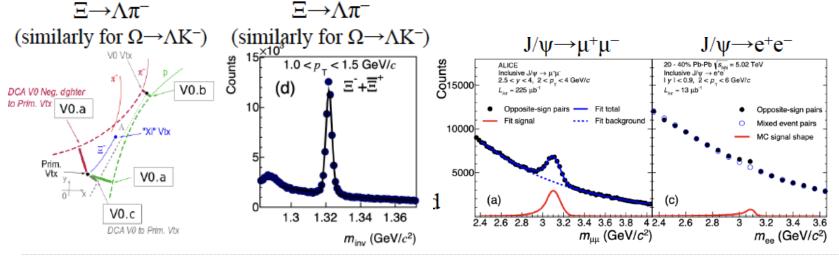


Characteristics of a heavy-ion detector: ALICE

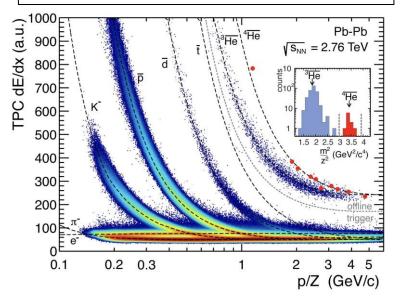


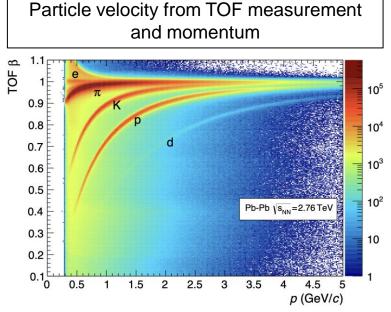
Particle identification

- Direct identification: π, K, p, light (anti)nuclei
- Electron identification using calorimeters and transition radiation detectors
- Strange and heavy-flavour hadrons:
 - reconstruction of secondary vertex and weak decay topology
 + PID + invariant mass reconstruction
- Photons detected in calorimeters and through pair production
- Quarkonia through leptonic decays



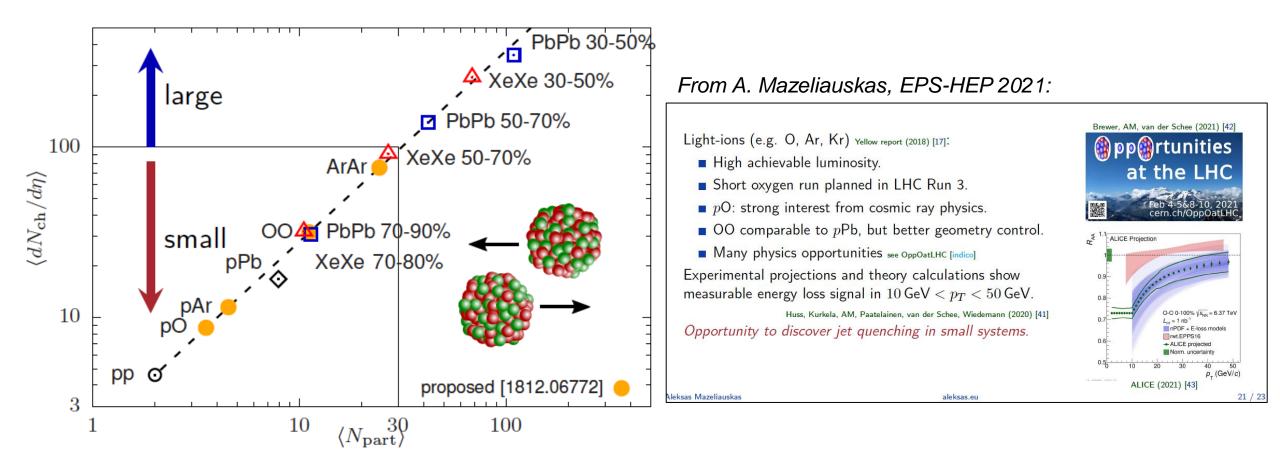
Energy loss of long lived particles in TPC



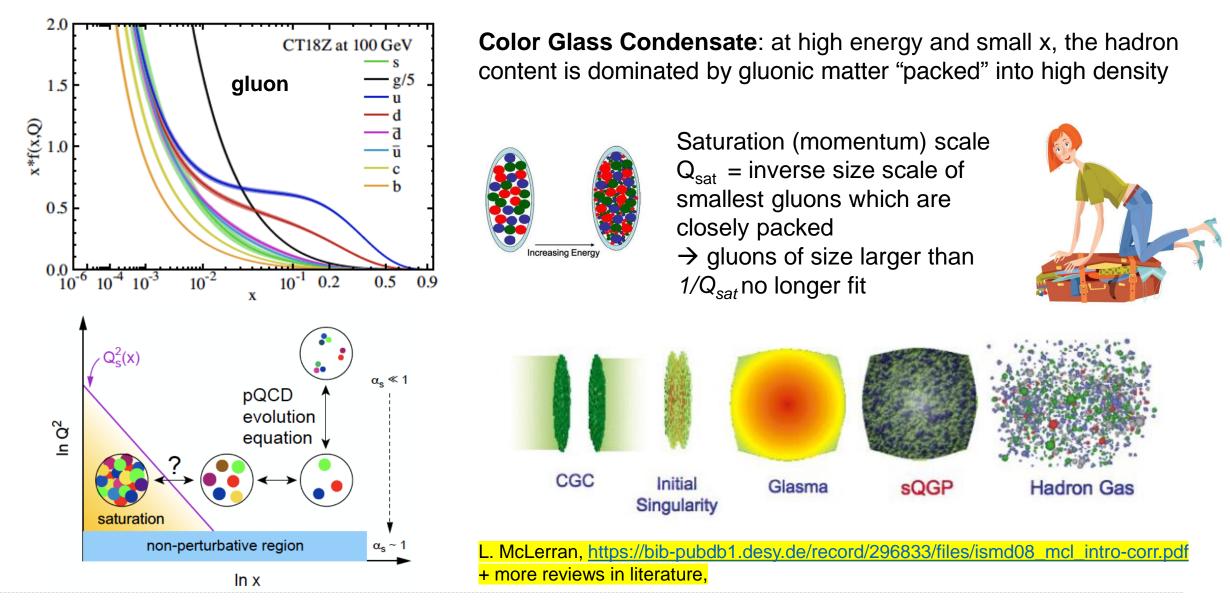


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Light ions at the LHC



Initial stage of heavy ion collisions



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Glauber model

Nucleus-nucleus interaction as **incoherent** superposition of nucleon-nucleon collisions calculated in a probabilistic approach [*M. L. Miller et al., An. Rev. Nucl. Part. Sci. 57* (2007) 205-243]

- nucleons in nuclei are considered as point-like and non-interacting
- nuclei (and nucleons) have straight-line trajectories (no deflection)

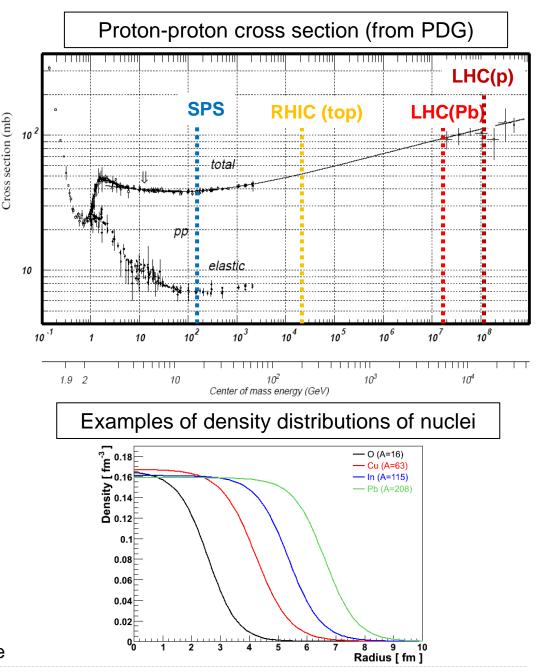
Input:

- Nucleon-nucleon inelastic cross section
- Nuclear density distribution, e.g. Fermi

 $\rho(r) = \rho_0 \frac{1 + w(r/R)^2}{1 + \exp\left(\frac{r-R}{a}\right)}$

 ρ^{0} = density in the nucleus center R = nucleus radius a = skin depth w = deviations from spherical shar

 $\ensuremath{\mathrm{w}}$ = deviations from spherical shape



Glauber model (2)

Output:

- Interaction probability
- Number of elementary nucleon-nucleon collisions (N_{coll})
- Number of participant nucleons (N_{part})
- Number of spectator nucleons
- Size of the nuclei overlap region

These variables are fundamental to study the scaling properties of observables in HIC – **Rule of thumb**:

- *N*_{part} scaling of soft particle production
 → bulk of the system
- N_{coll} scaling of high p_T particle production \rightarrow hard partons produced early in the collision



