

# Pulse characterisation techniques for multi-pulse laser plasma wakefield accelerators

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Position: 4<sup>th</sup> year PhD student

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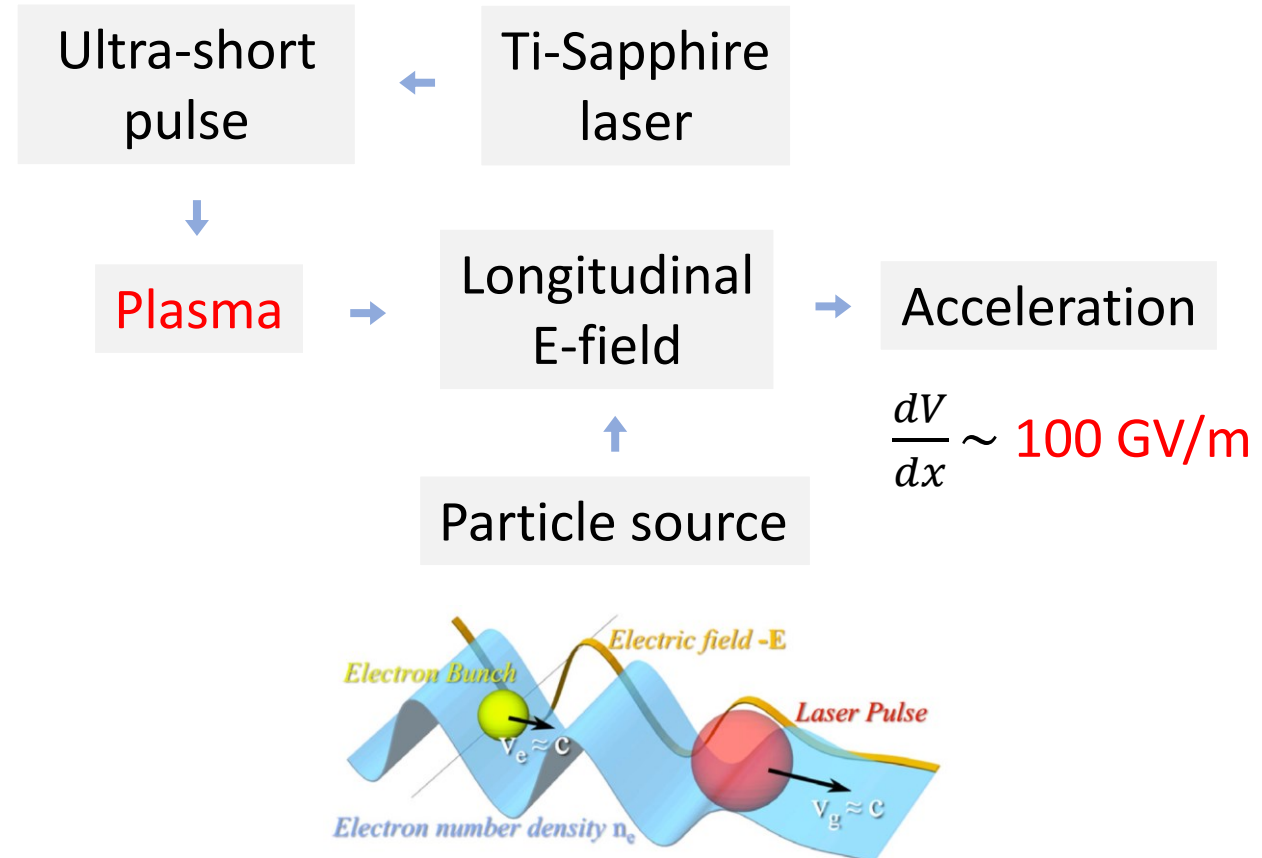
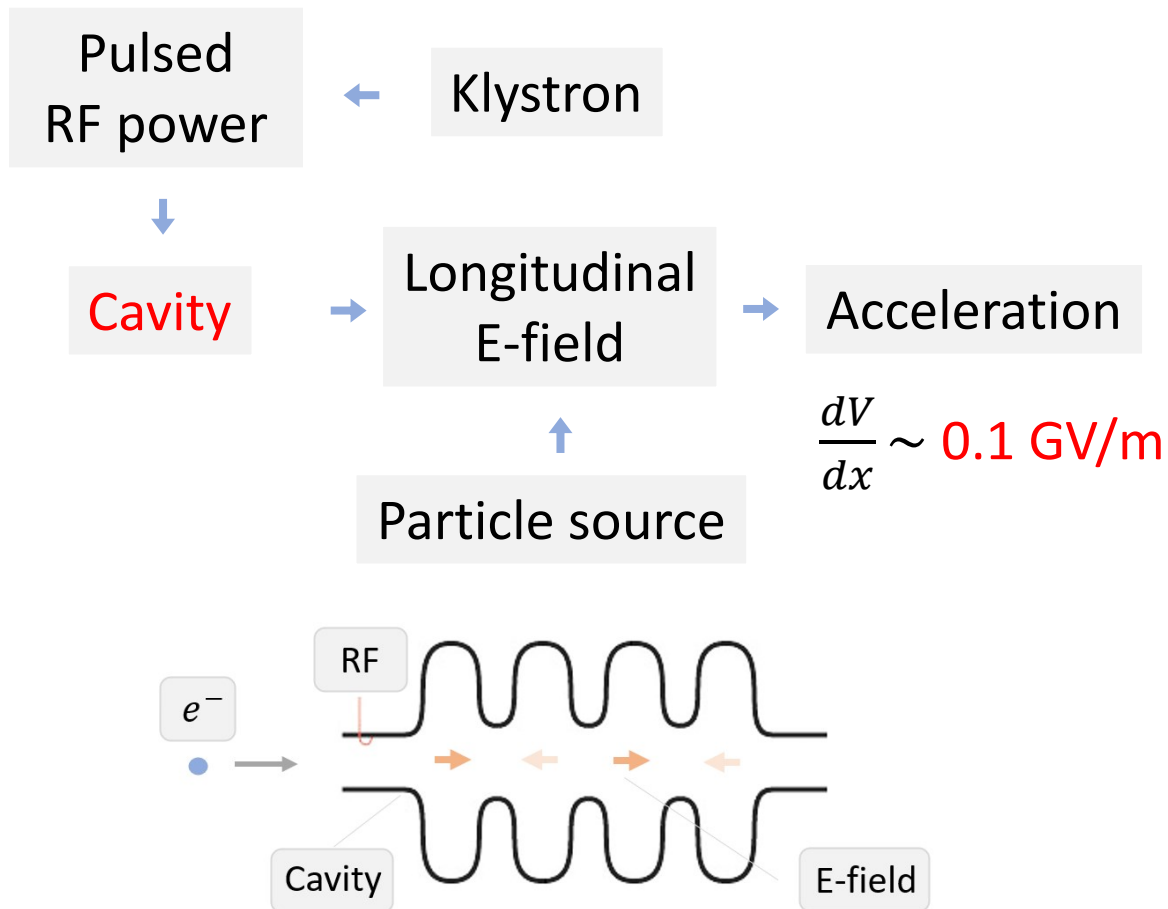


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# Outline

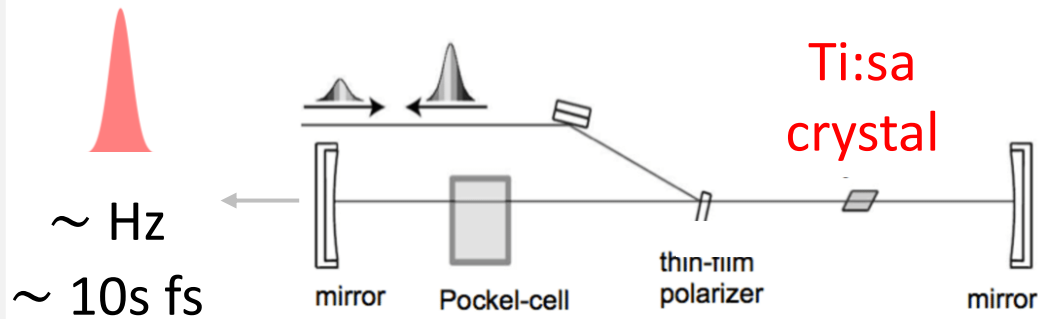
- Introduction
  - Conventional accelerators versus laser-driven plasma wakefield accelerators
  - Why pulse trains?
- Concepts of plasma accelerators driven by laser pulse trains
  - Multi-pulse laser plasma wakefield accelerators
  - Plasma-modulated plasma accelerators
  - Pulse train generation techniques
- Pulse characterization techniques
  - Representation of short pulses and pulse trains
  - Overview of characterisation techniques
  - FROG and SEA-TADPOLE
- Implementation of pulse characterization techniques
  - Development of FROG for MP-LWFA
  - Development of FROG + SEA-TADPOLE for P-MoPA
- Conclusion

# Conventional accelerators versus laser-driven plasma wakefield accelerators

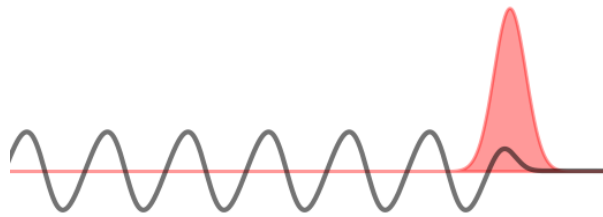


# Why pulse trains?

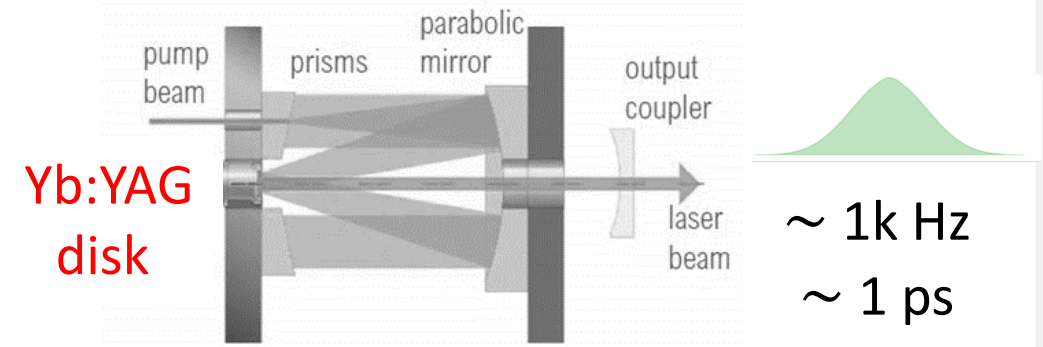
Inefficient laser systems (QD ~ 35%)



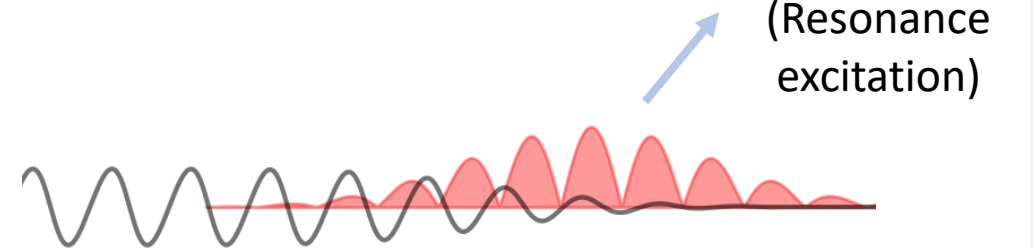
Conventional LWFA



Efficient laser systems (QD ~ 9%)



Train of pulses



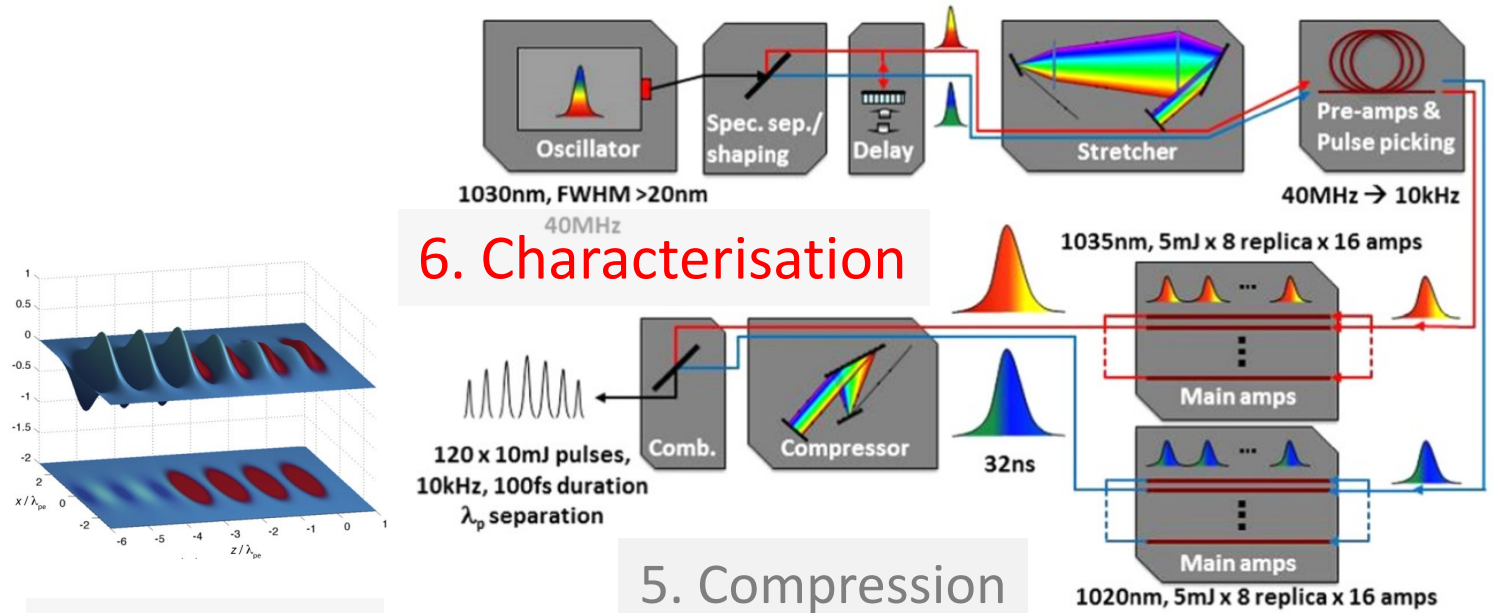
— Wakefields ■ Laser pulse

# Multi-pulse LWFA (MP-LWFA)

1. Fibre laser

2. Shaping

3. Pulse picking



6. Characterisation

5. Compression

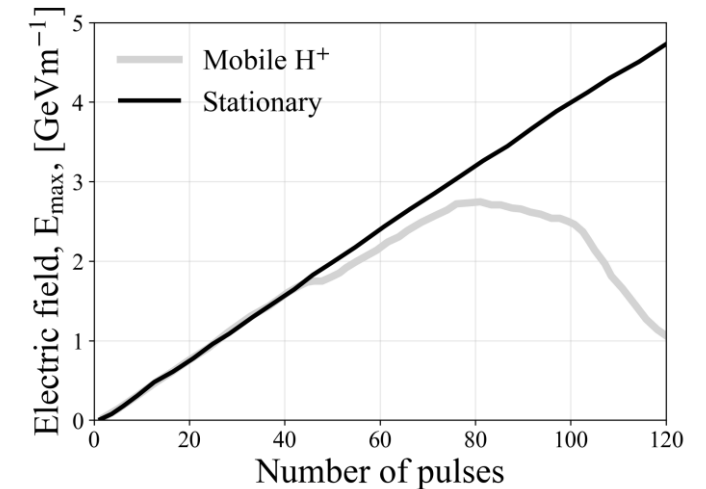
4. Amplification

7. Excitation

Simulation: 2D PIC

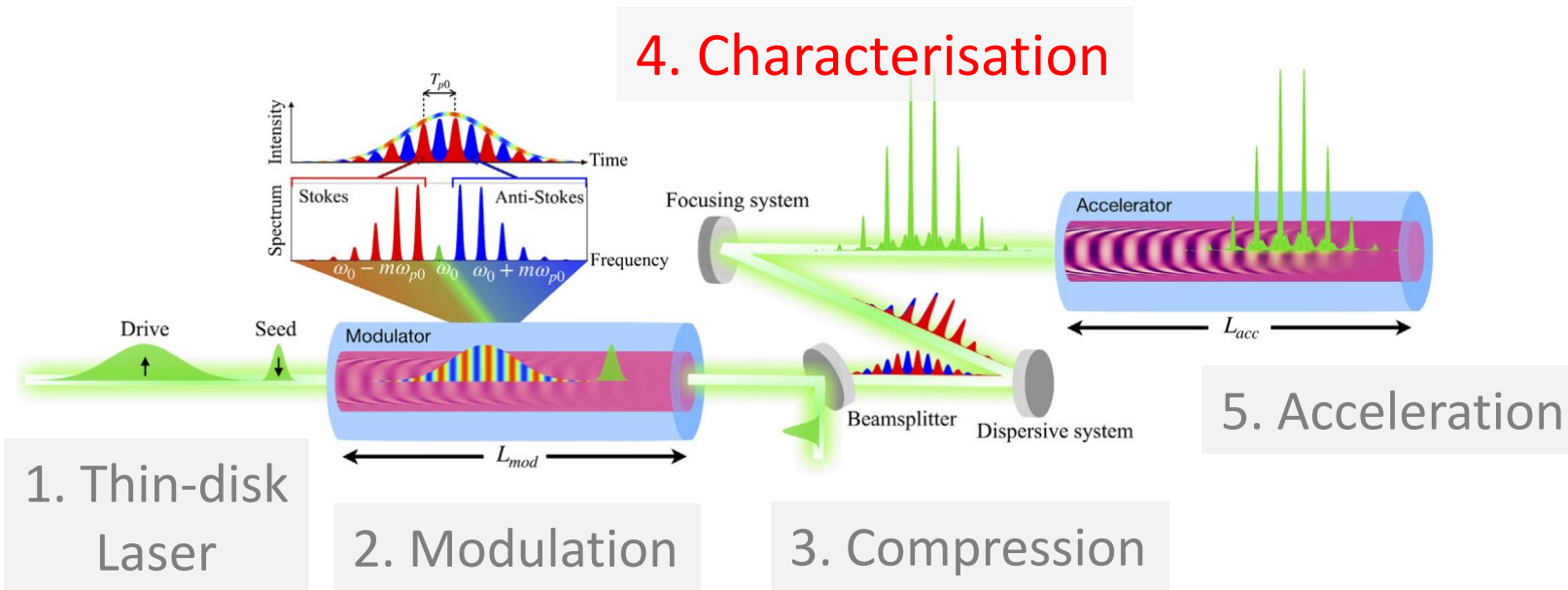
Pulse energy: 10 mJ

Pulse duration: 100 fs



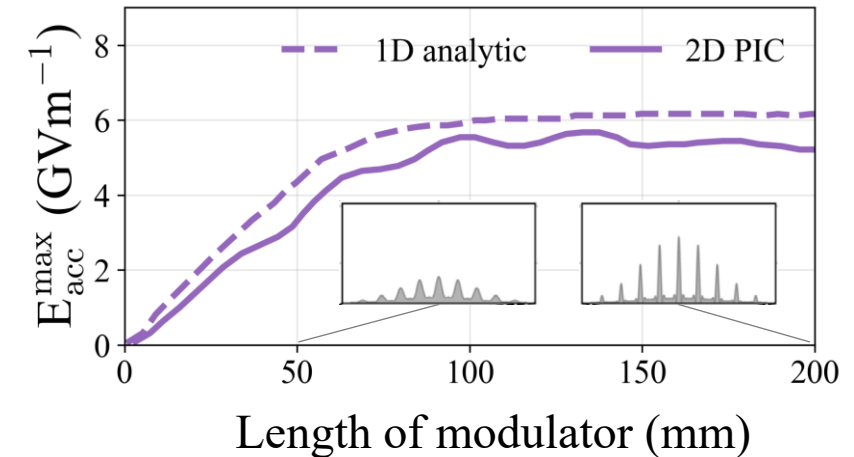
80 low energy short pulses  
Achieve 3 GV/m!

# Plasma-modulated plasma accelerators (P-MoPA)



Oscar. Jakobsson et al., Physical Review Letters 127, 184801 (2021).

Simulation: 2D PIC  
 Pulse energy: 600 mJ  
 Pulse duration: 1 ps



Single long pulse  
 (9 short pulses)  
 Achieves 6 GV/m !

# Pulse train generation techniques

## MP-LWFA concept

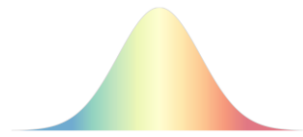
Broadband

Single short pulse



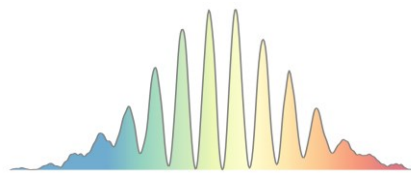
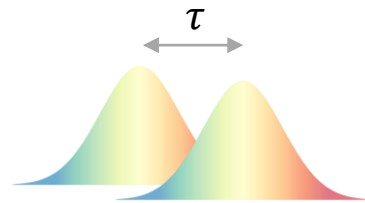
Pulse stretching

Grating pair compressor



Delay time control

Michelson interferometer



## P-MoPA concept

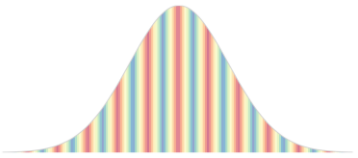
Narrow band

Single long pulse



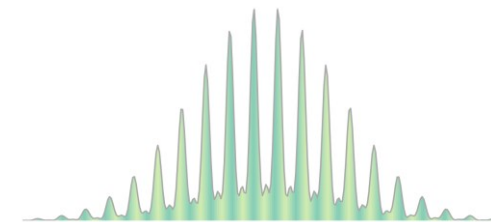
Phase modulation

Plasma wakefield



Dispersion Control

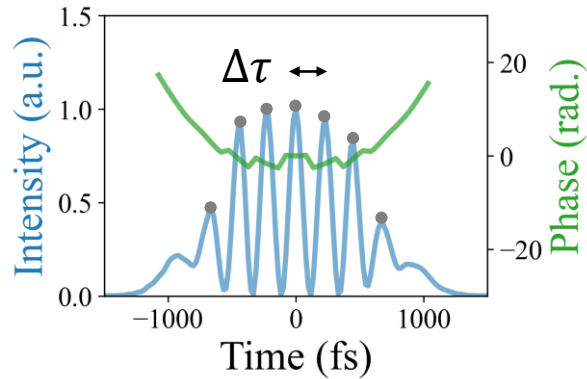
Dispersive optics



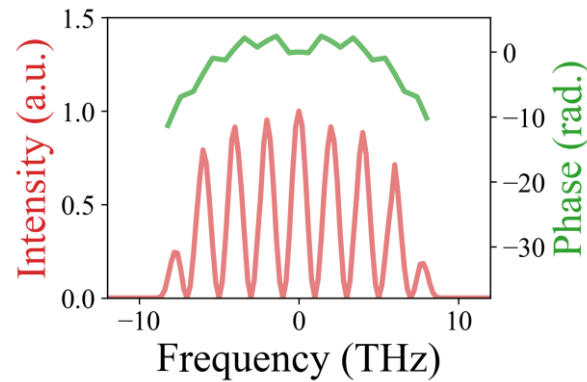
# Structure of pulse trains

MP-LWFA

Time domain

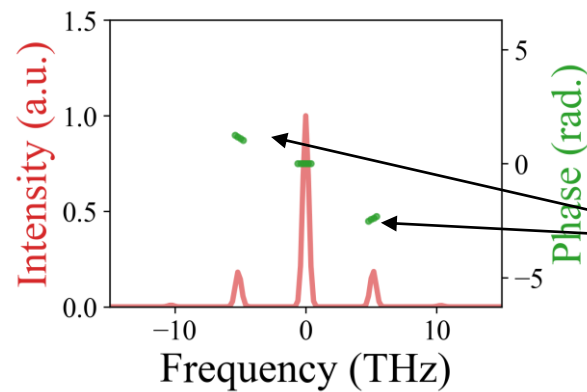
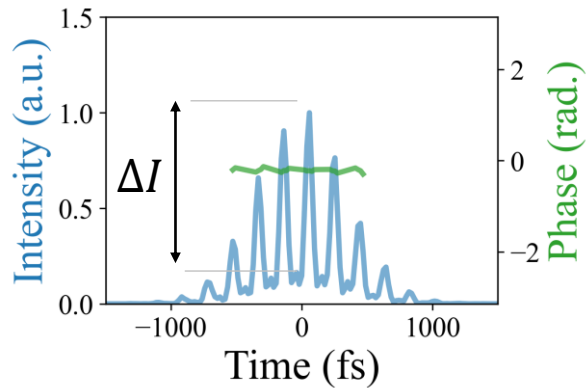


Frequency domain



Pulse spacing:  $\Delta\tau$   
 Number of pulses: ●  
 Oscillating spectrum

P-MOPA



Pulse contrast:  $\Delta I$   
 Spectral phase: —  
 Phase jumps

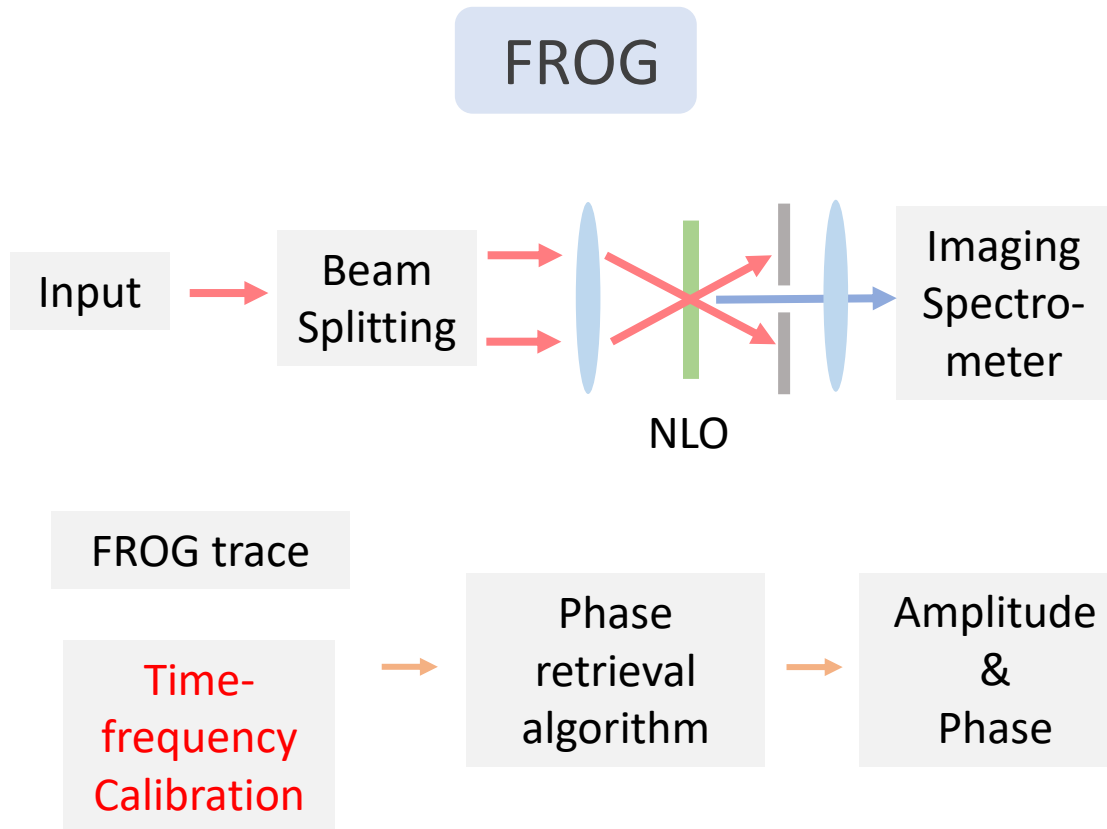


# Pulse characterisation techniques

	Techniques	Measured signal	Measured phase
<b>Time-frequency correlation</b>	Frequency-resolved optical gating (FROG)	Self-referenced Spectrogram $I(\tau, \omega)$	$\psi(\omega) = \sum_{n=2}^{\infty} \frac{1}{n!} \frac{\partial^n \psi(\omega)}{\partial \omega^n} \omega^n$
	Cross-correlation frequency-resolved optical gating (XFROG)	Cross-referenced Spectrogram $I(\tau, \omega)$	$\psi(\omega) = \sum_{n=2}^{\infty} \frac{1}{n!} \frac{\partial^n \psi(\omega)}{\partial \omega^n} \omega^n$
<b>Spectral interferometry</b>	Spatial Encoded Arrangement for Temporal Analysis by Dispersing a Pair of Light E-fields (SEA-TADPOLE)	Cross-referenced Interferogram $I(\omega, x)$	$\Delta\psi(\omega) = \psi_t(\omega) - \psi_r(\omega)$
	Spectral phase interferometry for direct electric-field reconstruction (SPIDER)	Self-referenced Interferogram $I(\omega)$	$\frac{\partial \psi}{\partial \omega} = \frac{\psi(\omega - \Omega) - \psi(\omega)}{\Omega}$

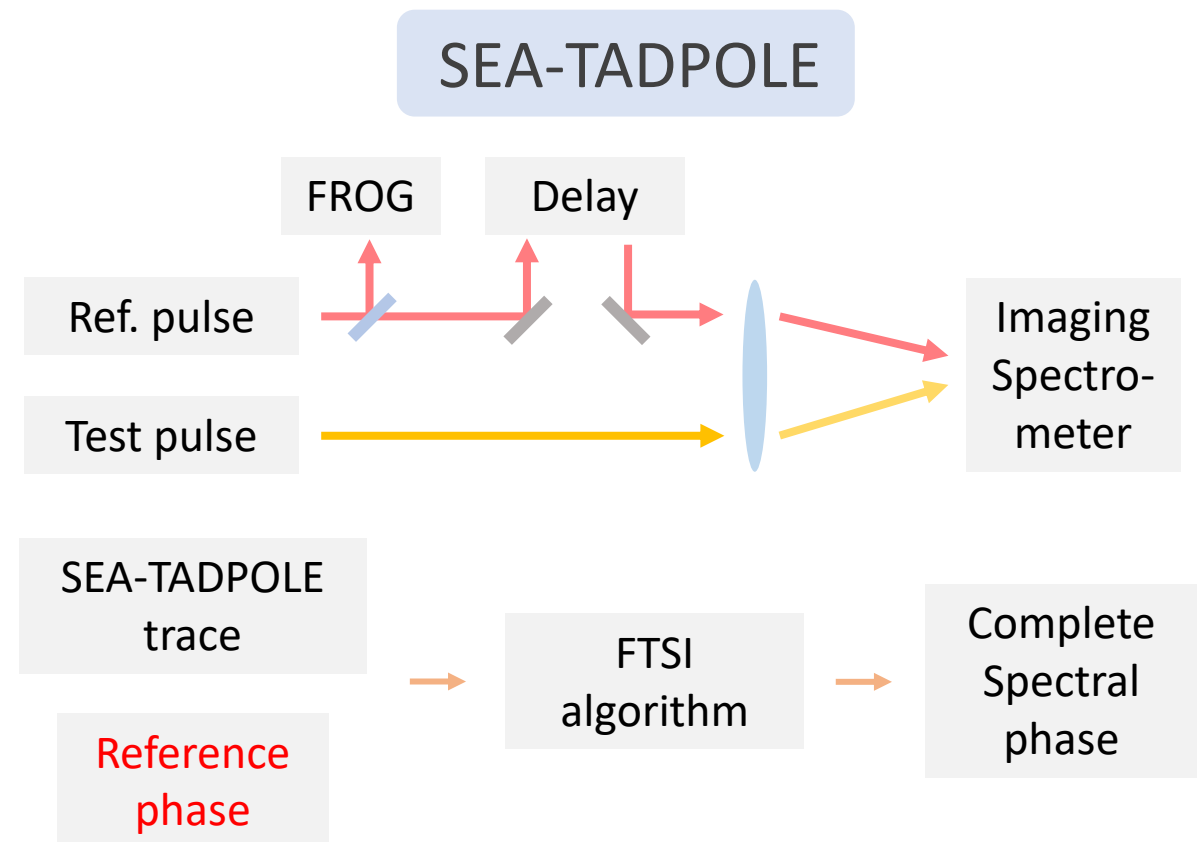
# FROG and SEA-TADPOLE

## FROG



Rick Trebino et al., J. Opt. Soc. Am. A, Vol. 10, No. 5 (1993).  
Spangenberg et al., Physical Review A 91, 021803(R) (2015).

## SEA-TADPOLE

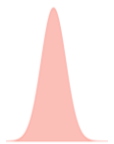


Pamela Bowlan et al., Optics Express, Vol. 14, No. 24 (2006).

# Pulse characterization technique for MP-LWFA

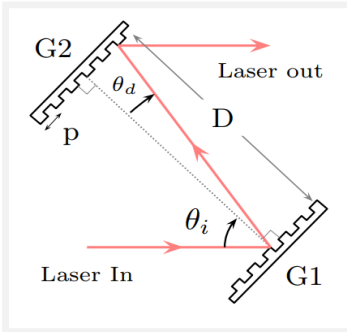
Ti-Sapphire Laser system

2 mJ,  
50 fs,  
at 790 nm,  
at 1 kHz



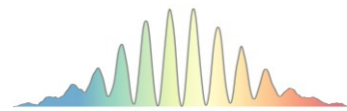
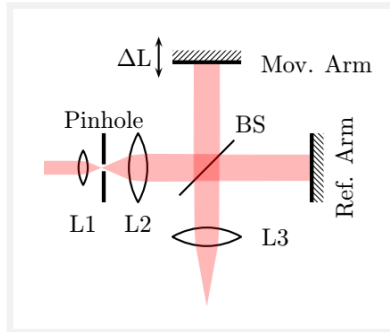
Broadband Short pulse

Grating pair Compressor



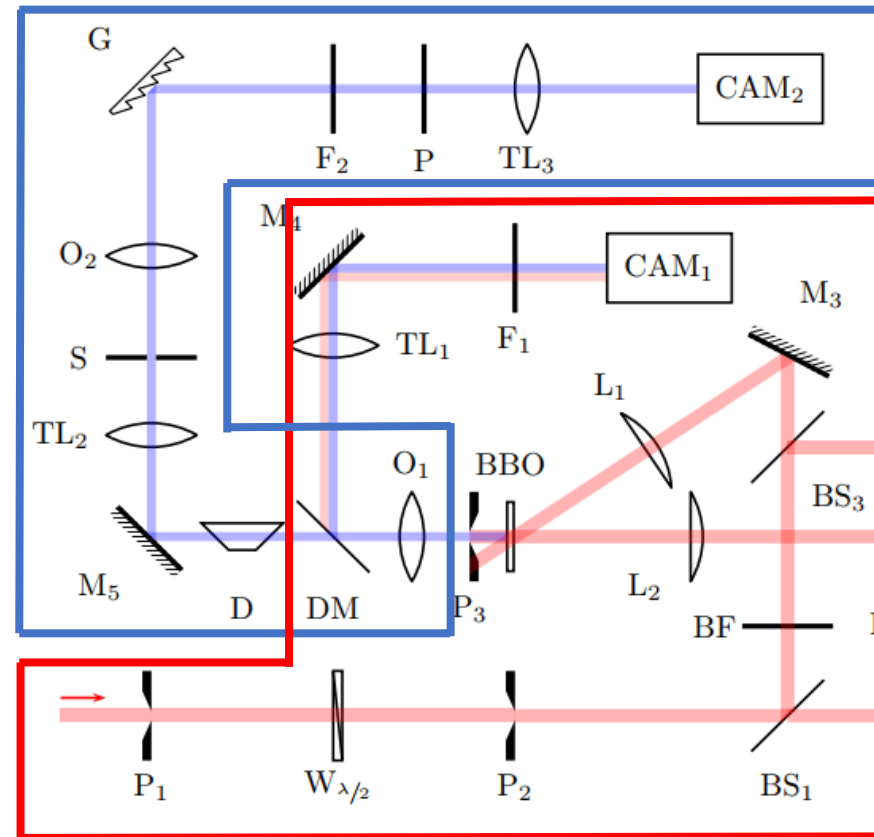
Stretching

Michelson Interferometer

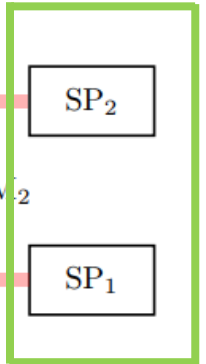


Temporal interference

High res. imaging spectrometer



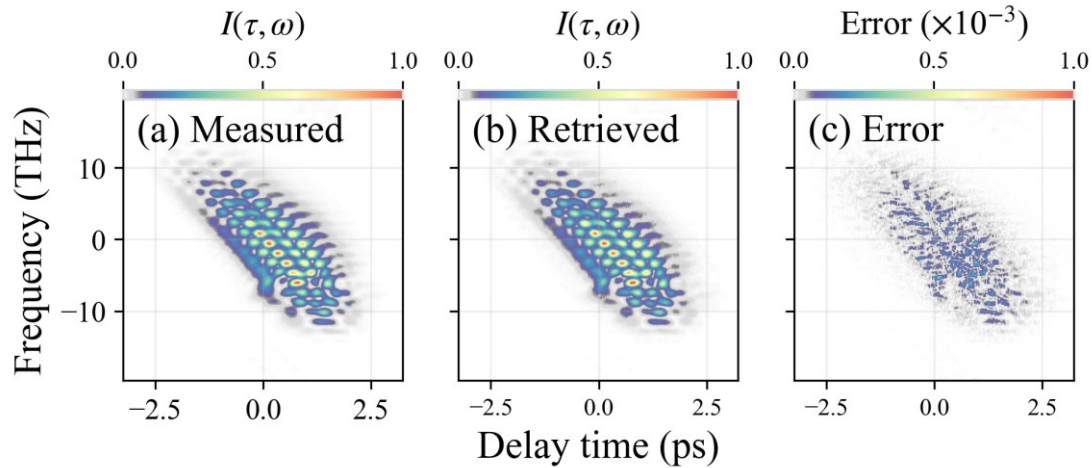
Line-array spectrometer



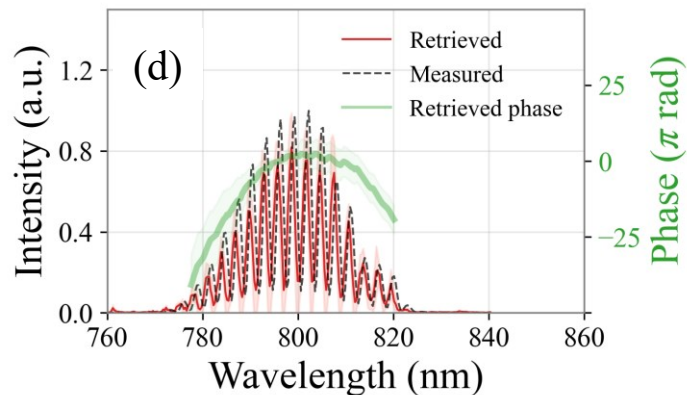
Self-referenced cross-correlator

# Experimental pulse retrieval results

## FROG Trace

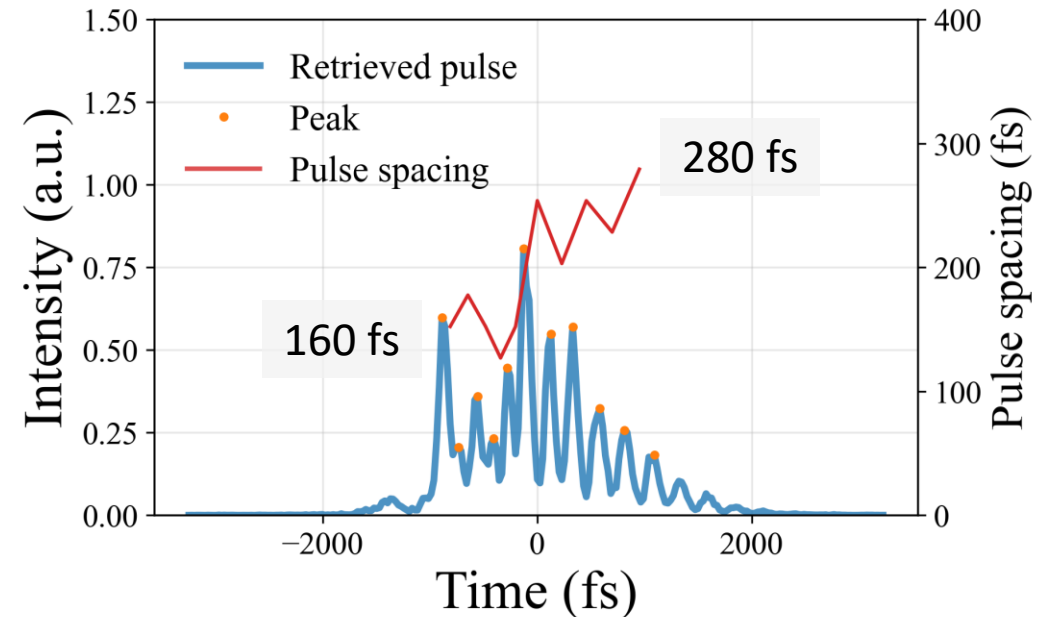


## Spectrum



FROG Error:  $9 \times 10^{-3}$   
RMS Intensity error:  
14 %

## Pulse structure



- Number of pulses:  $\sim 11$
- Time bandwidth product:  $\sim 13$
- Avg. pulse spacing:  $\sim 200$  fs
- Non-uniformity detected.

# Pulse characterisation technique for P-MoPA

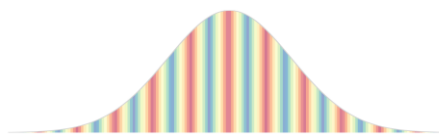
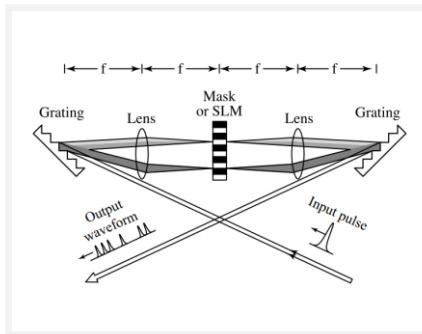
Ti-Sapphire Laser system

2 mJ,  
50 fs,  
at 790 nm,  
at 1 kHz



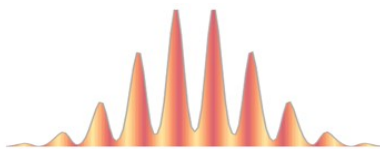
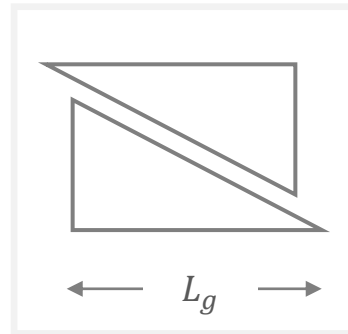
Broadband Short pulse

4-f pulse shaper

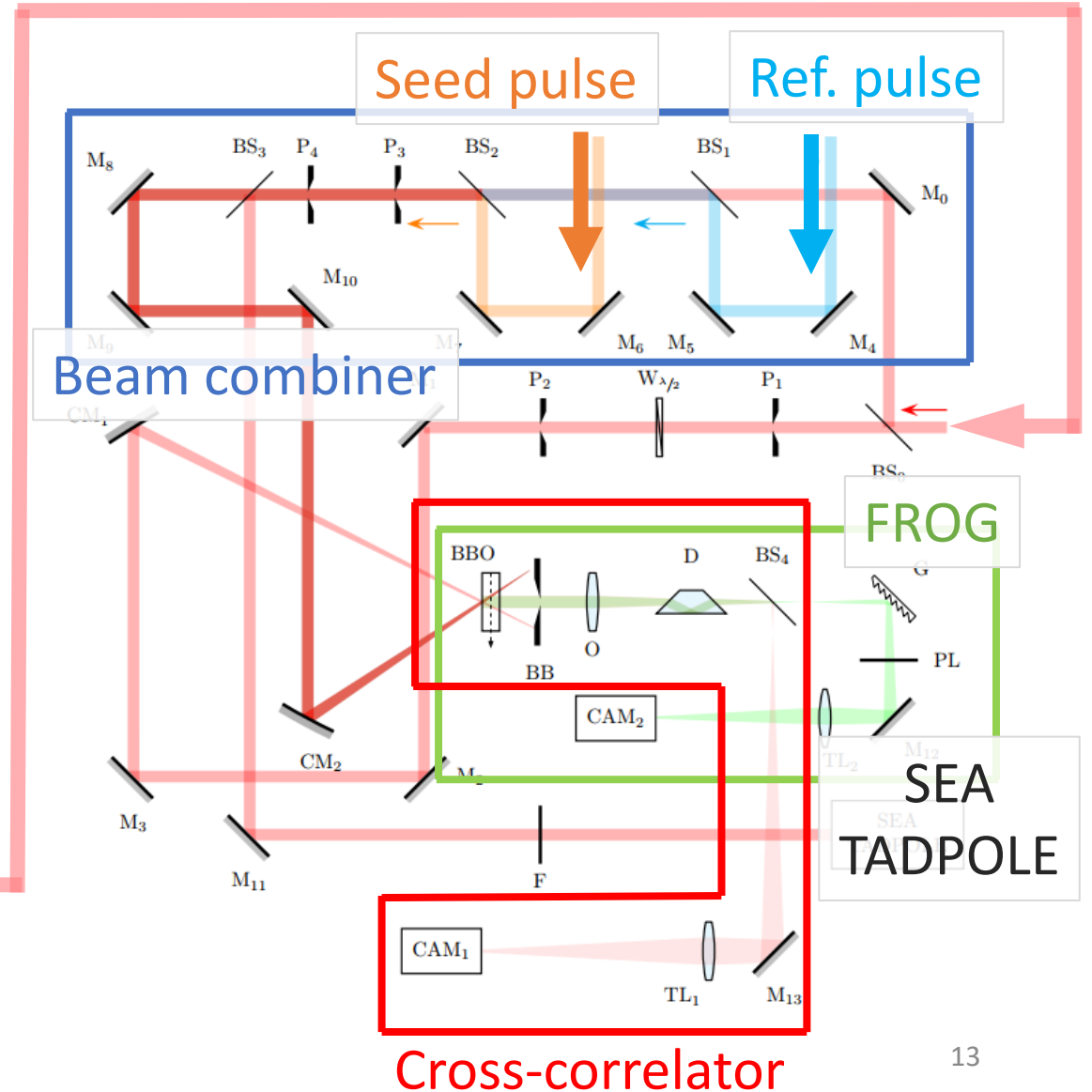


Spectral masking Phase modulation

Prism pair Compressor



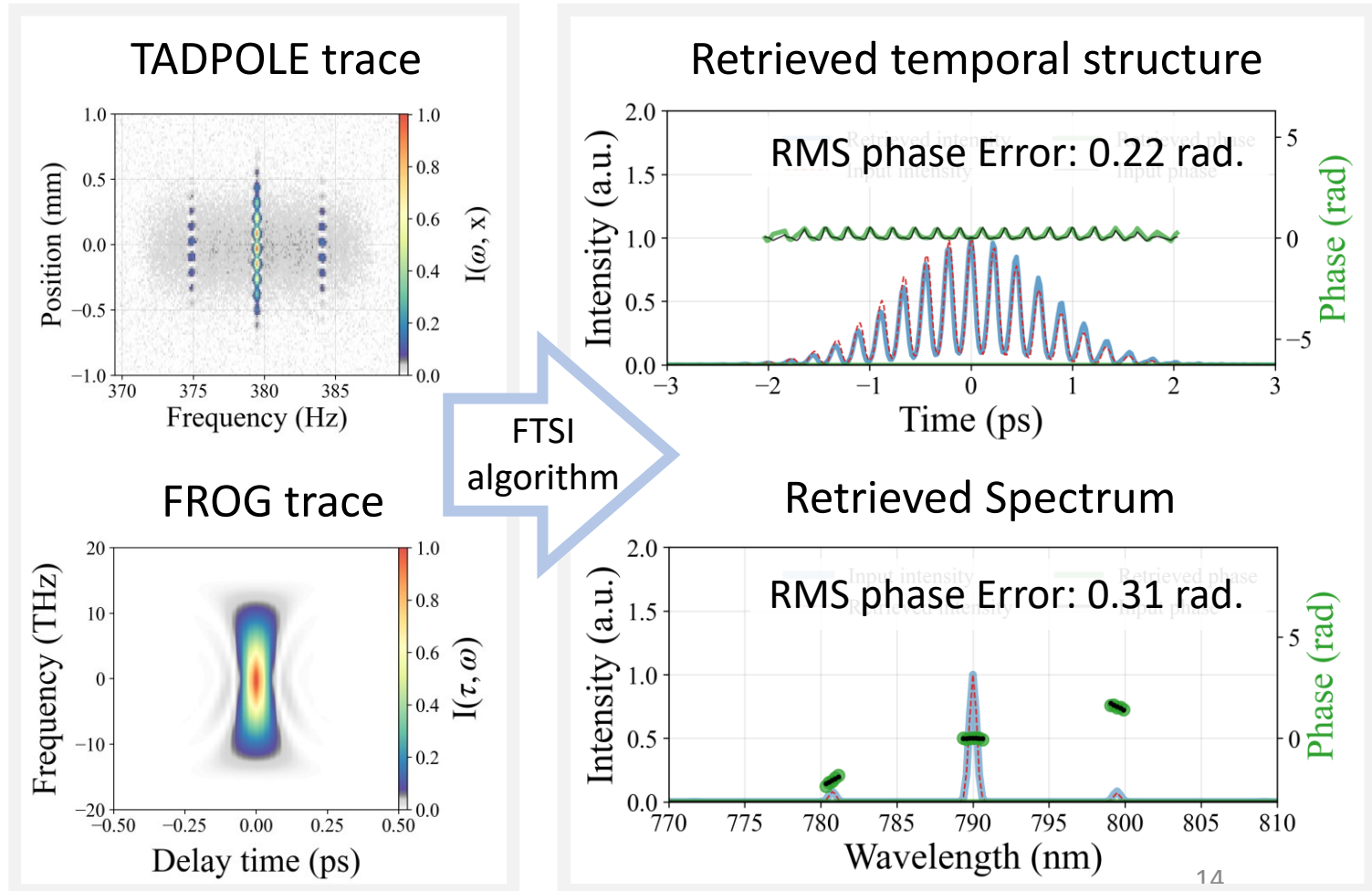
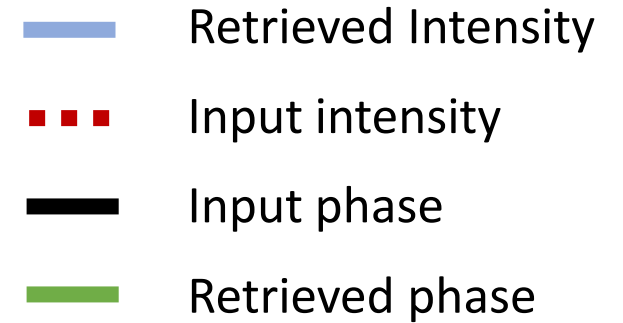
Pulse Compression



# Pulse retrieval simulation

## Simulation conditions

- Plasma density  $n$ :  $2.5e17 \text{ cm}^{-3}$
- Plasma modulation  $\delta n/n$ : 2%
- Channel length  $L_c$  : 5 cm
- Glass length  $L_g$  : 8 cm
- Centre wavelength of pulse  $\lambda_0$  : 790 nm
- Seed pulse duration: 50 fs
- Drive pulse duration: 1.4 ps
- Spectral SNR : 20 dB (white noise)
- Sensor SNR: 43 dB (Gaussian noise)
- Uncertainty of gas density: 5 %
- RMS Timing jitter: 200 fs



# Conclusion

- LWFA driven by pulse trains allows use of new laser technology with high rep. rates (kHz) and high wall-plug efficiency (>16%).
- Pulse characterisation is crucial for pulse train optimisation in MP-LWFA/P-MoPA.
- Multi-pulse trains can be diagnosed by FROG. Entire temporal structure of pulse trains can be retrieved.
- Characterisation of plasma modulated pulse trains require FROG and spectral interferometry (SEA-TADPOLE). Complete intensity and phase can be retrieved with smooth reference phase.

# Back-up slides



# Representation of ultra-short pulses

Spectrum + **Spectral phase**  $\xrightarrow{\text{iFT}}$  Temporal structure  
(Time-frequency relation)

Frequency domain

$\downarrow$  iFT

Time domain

