

QCD/top physics in the era of future accelerators

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Introduction

✓ We had a lot of related talks ...

Stefano Forte, Stefan Kluth, Fulvio Piccinini

✓ Will not discuss EW physics (see talk by Fulvio Piccinini)

✓ This talk is about trying to guess what QCD may look like at FCCee

✓ ... we can start by looking at the LHC today and extrapolate

✓ The situation at present is pretty amazing: we have many, more-precise calculations for a more complicated machine (LHC) than for e^+e^- !

✓ A brief LHC status:

✓ Fully differential NNLO for $2 \rightarrow 2$ and $2 \rightarrow 3$.

✓ N³LO already exists for $2 \rightarrow 1$ processes.

On a 10-year timescale we can expect N³LO calculations for the LHC, produced at scale

✓ These developments directly translate to e^+e^- :

✓ There are not as many e^+e^- implementations currently simply because there is no pressing need for them.

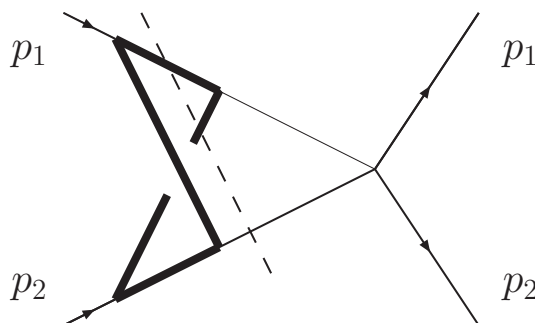
- ✓ The bottleneck at the LHC currently, and for the foreseeable future, is the calculation of multiloop amplitudes (translates directly to e^+e^-).
- ✓ Progress in multiloop amplitudes
 - ✓ Definition of the set of functions needed to describe such processes
 - ✓ Example 1: the description of massless $2 \rightarrow 3$ processes at NNLO required a new set of functions, the pentagon functions
 - Papadopoulos, Tommasini, Wever '15
 - Gehrmann, Henn, Lo Presti '16 '18
 - ✓ They evolved in a set which is fully useable for practical calculations
 - Chicherin, Sotnikov '20
 - ✓ Approach currently being generalized up to $V+4j$ at 2 loops
 - Abreu, Chicherin, Ita, Page, Sotnikov, Tschernow, Zoia

✓ Example 2: Elliptic functions

✓ These appear in multiscale problems

✓ first such collider example was the NLO $t\bar{t}$ total inclusive cross-section).

Czakon, Mitov '08



✓ These functions need to be systematized in order to have efficient algebra. Tremendous work ongoing.

✓ Computing amplitudes will become particularly tricky for multiscale processes (like different masses)

✓ Likely only fully numeric calculations are feasible. But this is OK: for example, $t\bar{t}$ @LHC@2 loops is known numerically and not yet fully analytically.

Chen, Czakon, Poncelet '17

✓ Finally, even one-loop amplitudes for N^3 LO calculation will require additional improvements

- ✓ What can we conclude from the discussion up to here?

By the time FCCee becomes operational many/most e^+e^- processes will have NNLO or N³LO precision

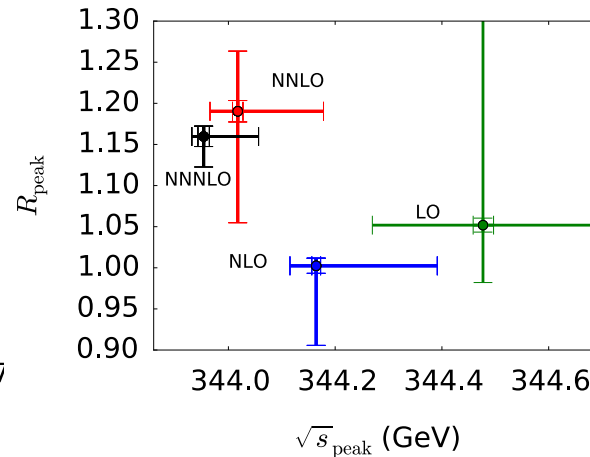
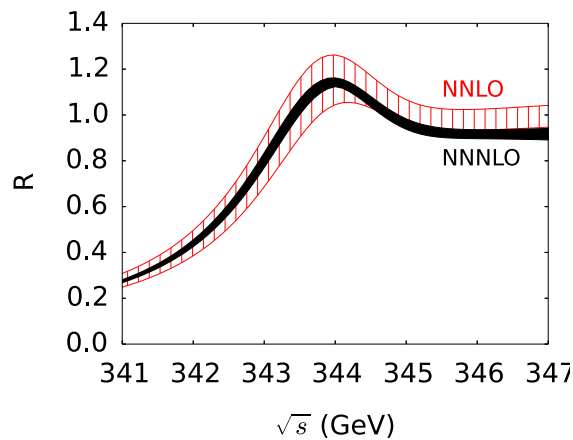
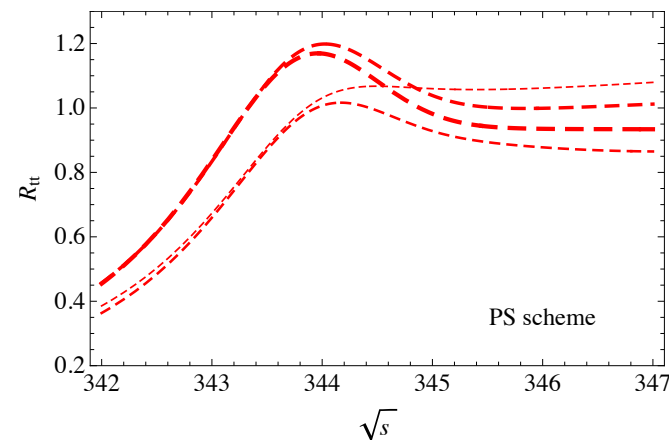
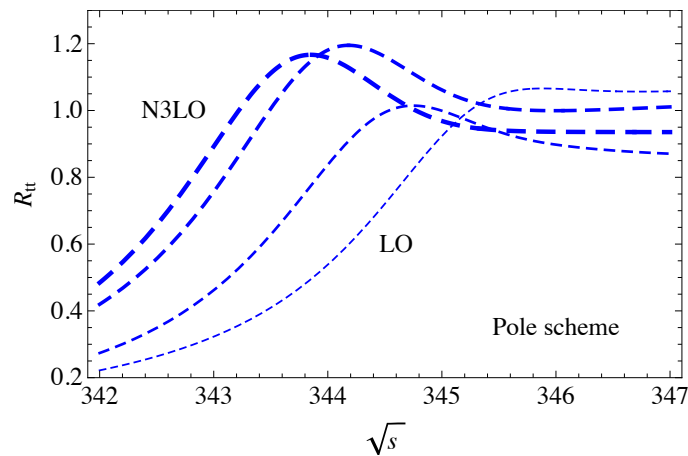
- ✓ One should expect fully differential calculations, not just inclusive observables
- ✓ This will be a huge progress relative to where we are today for e^+e^-

Overview of e^+e^- processes and their current status

Top quark pair production

- ✓ A major aim and potential major achievement for the FCCee
- ✓ A threshold scan allows a very precise measurement of the top quark mass, width and even its mass scheme.
- ✓ Theory known at N³LO in QCD

Beneke et al, '15



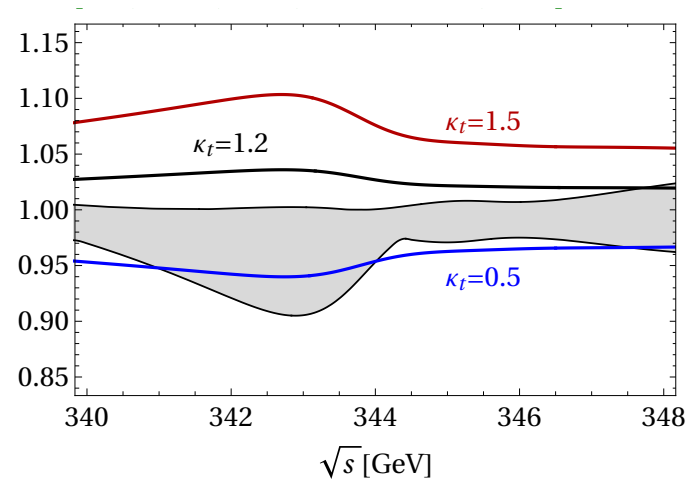
Top quark pair production

- ✓ Top Yukawa can also be constrained indirectly (albeit weakly).

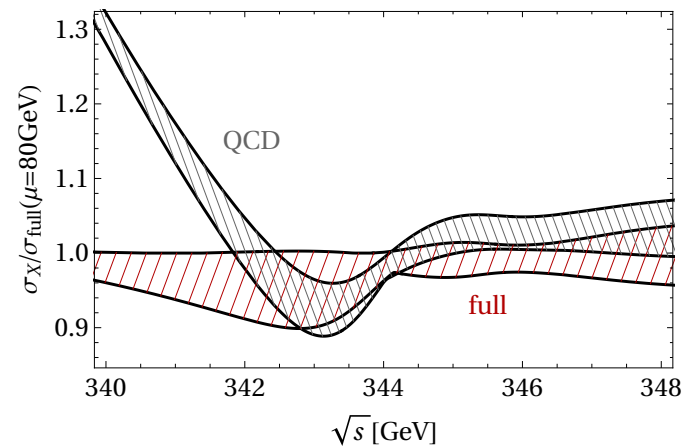
Nice connection to the talk by Gauthier Durieux

- ✓ Sensitivity to the top Yukawa coupling

Beneke et al, '17



- ✓ And NNLO EW corrections (EW+QED+non-resonant):



Top quark pair production

- ✓ Further prospects for $t\bar{t}$ at threshold:
 - ✓ A main remaining uncertainty is ISR
 - ✓ Going beyond N³LO will likely require a multi-decade effort...
- ✓ Continuum top pair production
 - ✓ Essentially available only at NLO via MadGraph5 aMC@NLO, Whizard, ...
 - ✓ No reason not to have full NNLO at present
- ✓ Note: the state of continuum b and c production is similar.
 - ✓ Single inclusive production at high p_T is known at NNLO (will revisit later in this talk)

Jet production and α_s

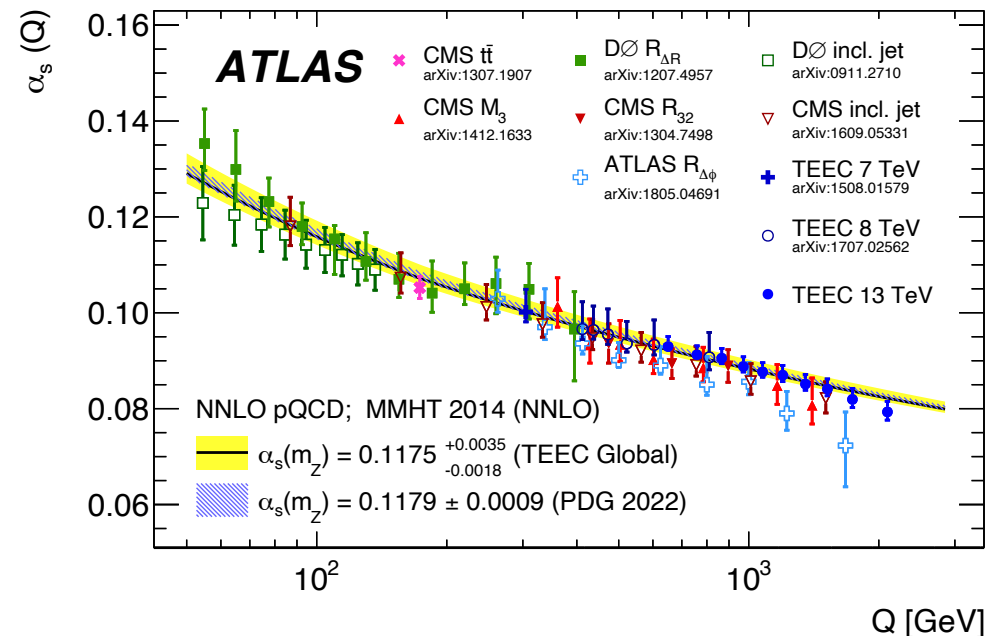
- ✓ 3-jet production at the LHC is known at NNLO (in full color)
- ✓ 3-jet is also known for e^+e^- at NNLO
 - Gehrmann-De Ridder, Gehrmann, Glover, Heinrich '07
 - Weinzierl '08
 - Del Duca, Duhr, Kardos, Somogyi, Szor, Trocsanyi, Tulipant '16
- ✓ 4-jet at NNLO is doable (integrals were just derived for the LHC)
- ✓ Studies of jet substructure, jet algorithms, including flavor, has advanced tremendously during the lifetime of the LHC.
- ✓ Ultimately, N³LO for 3 jet production at e^+e^- will likely be possible within a decade or so.

- ✓ Measurements of the strong coupling constant at e^+e^- will offer exciting possibilities

reviewed in talk by Stefan Kluth

- ✓ A remark: FCCee will only give us access to α_s at scales $\sim M_Z$. This is unlike the LHC where the running of α_s has already been probed to 2 TeV or so with full NNLO precision.

ATLAS arXiv:2301.09351



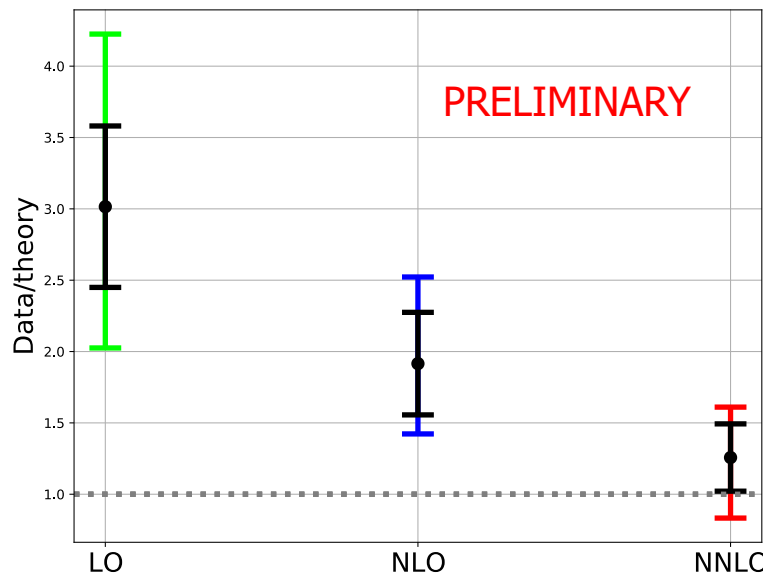
Two selected aspects
we can learn from at future e^+e^- colliders

Terra Z

- ✓ Precision remeasurement of SM parameters and processes is going to be essential for the future precision program we all hope for.
- ✓ It is just like building a house: it can be only as good as the foundation it sits on.
- ✓ Zoltan Ligeti gave an exhaustive introduction to this. Let me just add couple of more examples:
 - ✓ B and D fragmentation measurements from LEP are rather limited.
 - ✓ Only a mixture of B mesons available
 - ✓ Only a single D meson measurement available
 - ✓ Quality of available data is currently a major limiting factor on heavy flavor production
- ✓ Another potential great benefit: measurements at different c.m. energies
 - ✓ Measurements at higher energies (240GeV, 365 GeV) will be the first time we have high precision high-energy data to test precision DGLAP evolution for heavy flavors.
 - ✓ B fragmentation is currently restricted to $x > 0.1 \sim m_Z / (2m_B)$. Higher c.m. energies will allow access to fragmentation measurements with $x < 0.1$.
 - ✓ And a bigger lesson: acquiring confidence in treating small mass effects in unrelated processes (including muon colliders, how to properly treat the muon or electron mass – even in QED context, etc.).

Small mass effects

- ✓ Identified heavy flavor production (fragmentation) is among the basic processes QCD offers and has been measured at many colliders.
- ✓ e^+e^- the gold standard for such measurements (due to lack of pdf, clean environment and ease of directly relating the observable to the fragmentation function)
- ✓ Open B and D production have so far (in the last almost 30 years) been treated in FONLL (NLO+NLL).
- ✓ It has been a great success and a major step forward; its main limitation is a significant NLO scale uncertainty.
- ✓ NNLO calculations expected to improve this. Indeed, the Tevatron B-production anomaly completely disappears at NNLO



Czakon, Generet et al, to appear

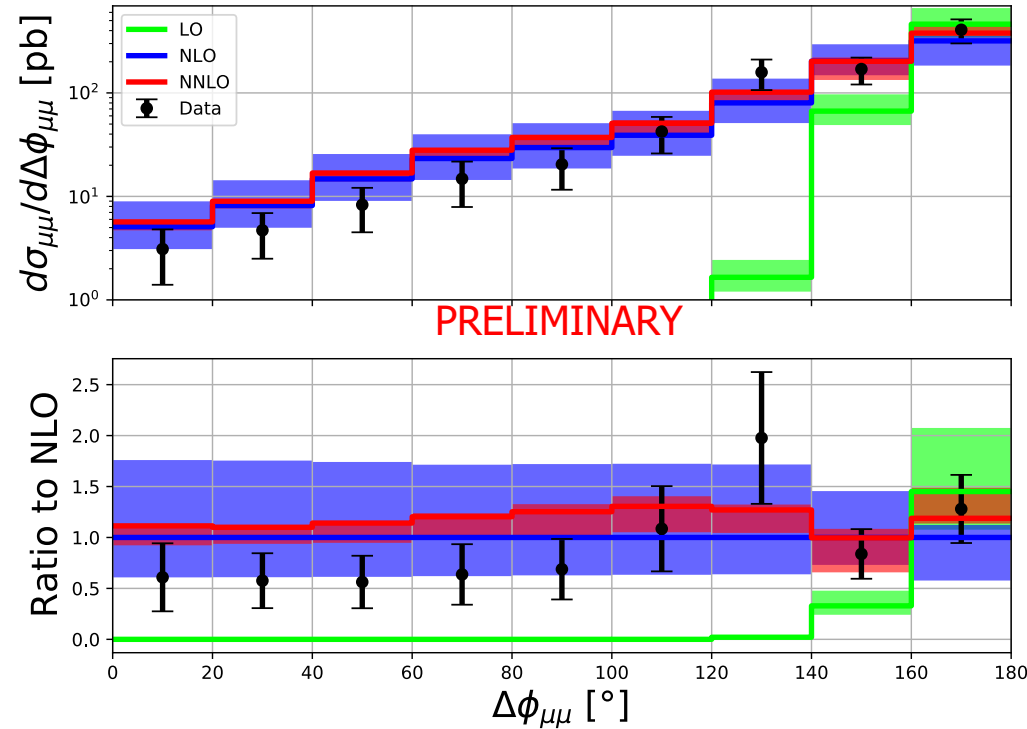
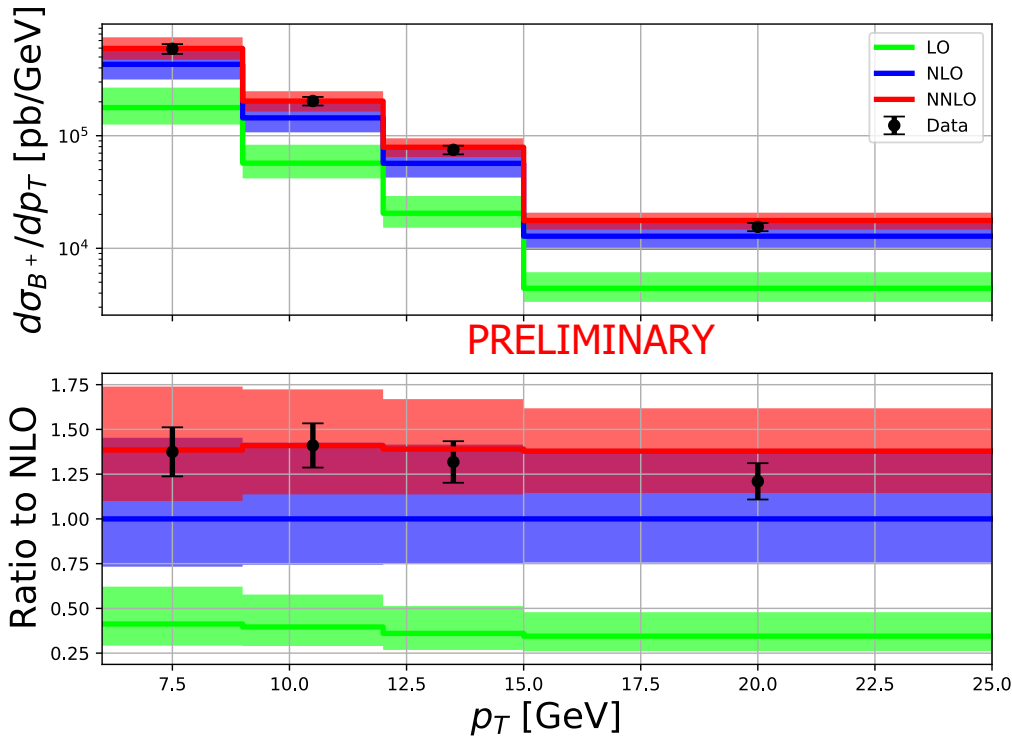
Tevatron fiducial x-section for
bb **at quark level**

Could also be inferred from
Catani(a), Devoto, Grazzini, Kallweit, Mazzitelli '20

Small mass effects

Czakon, Generet et al, to appear

✓ Full NNLO +resummation prediction for B mesons and their decays



✓ At future e^+e^- machine we should expect this observable to be known to N^3LO .

✓ Uncertainties dominated by measurements of input parameters and treatment of mass effects.

Small mass effects

✓ Example: fitting LEP data is not trivial

arXiv:2210.06078

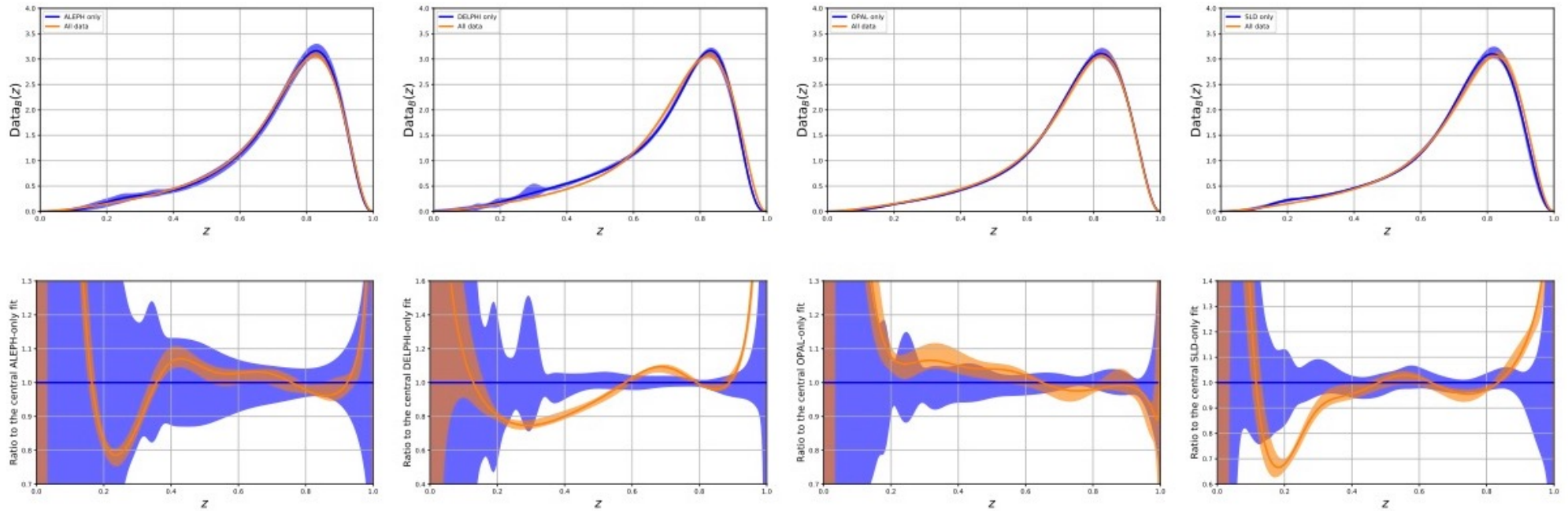


Figure 16. NPDF fits from one dataset at a time (blue) versus the combined fit (orange). The four datasets are (from left to right): ALEPH, DELPHI, OPAL and SLD.

HighTEA time

- ✓ A very legitimate question:
 - ✓ How do you make the above results available?
 - ✓ If I need a new prediction, where can I get it?
- ✓ There are just two options:
 - If there is a public code one can use it to compute what one needs
 - Problem 1: serious/huge CPU expense
 - Problem 2: is the user using the code correctly?
 - No public code: ask the authors. Hope they are free and have spare CPU to use...
- ✓ Can one bypass all of these problems at once?

MCFM
MATRIX

YES!

- ✓ The answer can be found here:

<https://www.precision.hep.phy.cam.ac.uk/hightea/>

✓ Dedicated website

<https://www.precision.hep.phy.cam.ac.uk/hightea/>



HighTEA

(High-energy Theory Event Analyzer for collider processes)

- Publication (to appear)
- For the impatient: [running HighTEA via Jupyter Notebook on Google Colab](#)

The modern way of doing physics

This site is the public face of a novel approach for distributing and analyzing the results of fixed order NNLO calculations for LHC processes. Here are the main topics:

- [The basic idea](#)
- [How it works](#)
- [Features](#)
- [Ways to access the library](#)
- [Our team](#)
- [Disclaimer](#)

The basic idea

The idea behind HighTEA is very simple: existing calculations use Monte Carlo (MC) methods to integrate over the available phase space. Such MC samplings, called *events*, are usually binned in histograms and then discarded.

While very powerful, such an approach to doing high-precision NNLO calculations has a serious drawback: it lacks

CAVENDISH HEP SEMINAR

Tue 02 May 11:00: The Force Awakens: searching for new sources of CP violation in the electroweak sector

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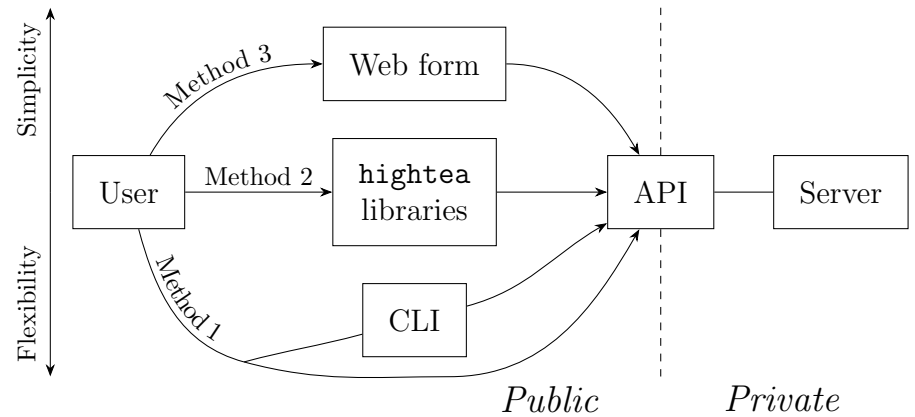
European Research Council

Established by the European Commission

Czakov, Kassabov, Mitov, Poncelet, Popescu 2023

- ✓ What is HighTEA? A library of precomputed events + all the required infrastructure.
 - ✓ No specialized knowledge needed to fully use it
 - ✓ It allows the user to compute any infrared safe n-dimensional differential distribution in any process which has already been added to the library
 - ✓ The output of a HighTEA computation is a histogram, and the input is the histogram's specification.
 - ✓ Users can define their own kinematic variables and scales.
 - ✓ No need for major computing infrastructure (typically, a large cluster). Example: A quick calculation takes 50k CPUh; the most demanding ones – over 10M CPUh.
 - ✓ Predictions derived from HighTEA are very fast (~minutes).
 - ✓ All one needs is a computer (or a smart phone) and a free Google account.
- ✓ HighTEA's limitations
 - ✓ Only processes already included can be computed
 - ✓ Fixed statistics: fine bins will result in large MC uncertainty (estimate always provided)
 - ✓ Fixed parameters like LHC energy and particle masses.

✓ HighTEA's logic:



✓ Next:

- ✓ A webform (restricted functionality): <https://www.hep.phy.cam.ac.uk/hightea/webform/>
- ✓ Our Library implemented in Jupyter notebooks on Google Colab. Has full functionality. One needs a device and a free Google account <https://colab.research.google.com/github/HighteaCollaboration/hightea-examples/blob/master/Start.ipynb>

Conclusions

- ✓ Steady progress on NNLO and already N³LO calculations for the LHC
- ✓ Future FCCee program will benefit from these developments
- ✓ Expect fully differential NNLO and N³LO to be the standard for FCCee
- ✓ We need FCCee, among others, for (much) more precise measurements of basic SM parameters and processes.
 - ✓ This will be critical for the success of the future precision program.