



Implications of $B \rightarrow Kv\bar{v}$ under Rank-One Flavor Violation hypothesis

Claudio Toni

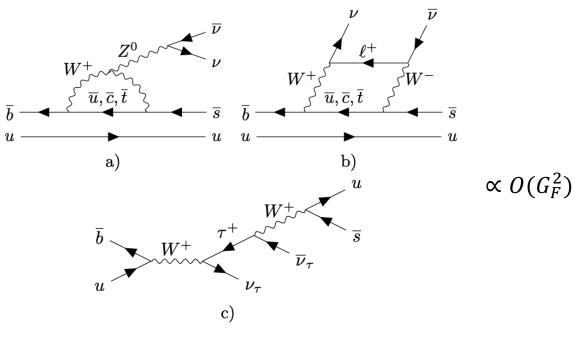
based on the work w/ David Marzocca, Marco Nardecchia and Alfredo Stanzione arxiv:2404.06533, submitted to JHEP

Zurich, «The Flavour Path to New Physics» workshop, 5 June 2024

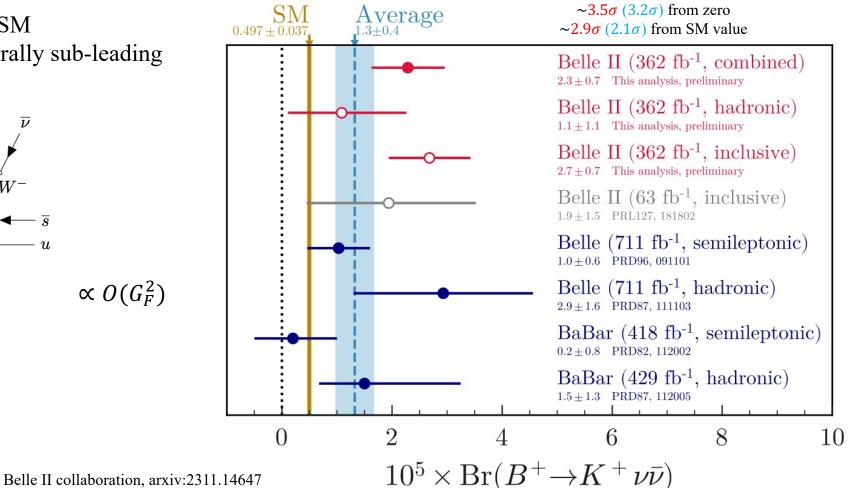
 $d_i \rightarrow d_i \nu \bar{\nu}$ searches and Belle II excess

FCNC decays with neutrinos are potentially powerful probe of BSM physics as:

- they are significantly suppressed in SM
- Iong-distance contributions are generally sub-leading



First exp. evidence of $B^+ \to K^+ \nu \bar{\nu}!$



Belle II excess as an hint of NP

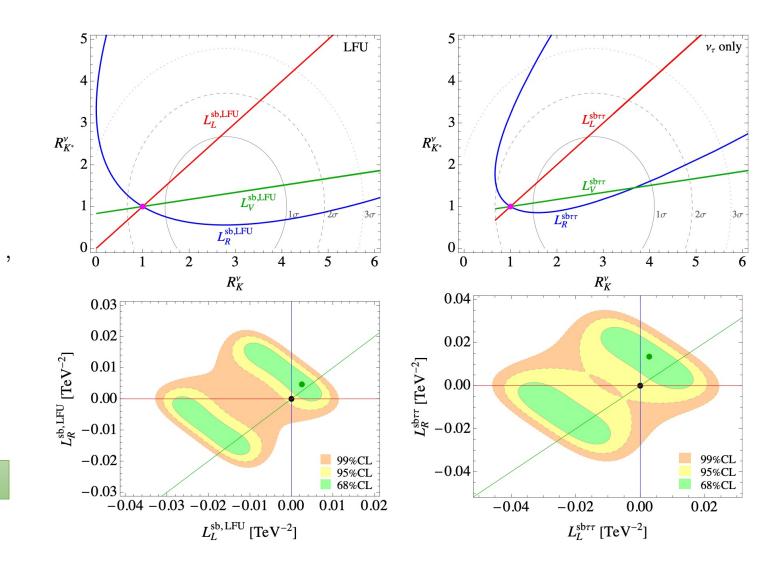
NP assumed to be heavy (for the complementary case, see next talk by Martin Novoa-Brunet)

BSM effects encoded in EFT operators

$$\mathcal{L}_{\text{LEFT}}^{bs\nu\nu} = \sum_{\alpha\beta} \left[L_R^{sb\alpha\beta} (\bar{s}_R \gamma_\mu b_R) (\bar{\nu}_L^\alpha \gamma^\mu \nu_L^\beta) + (L_L^{sb\alpha\beta} + L_L^{sb, \text{SM}} \delta^{\alpha\beta}) (\bar{s}_L \gamma_\mu b_L) (\bar{\nu}_L^\alpha \gamma^\mu \nu_L^\beta) \right]$$
$$L_V^{sb\alpha\beta} = L_R^{sb\alpha\beta} + L_L^{sb\alpha\beta},$$
$$R_{K^{(*)}}^\nu = \frac{\mathcal{B}(B \to K^{(*)} \nu \bar{\nu})}{\mathcal{B}(B \to K^{(*)} \nu \bar{\nu})_{\text{SM}}}$$

Effective scale of NP from the fit $\sim O(10 \text{ TeV})$

The chiral structure of NP depends on $R_{K^*}^{\nu}$ value!



$B^+ \to K^+ \nu \bar{\nu}$ and ROFV

NP generically induces more EFT operators

$$\mathcal{L}_{\text{LEFT}}^{bs\nu\nu,\text{BSM}} \subset \mathcal{L}_{\text{LEFT}}^{\text{NP}} = \sum_{ij\alpha\beta} \left[L_L^{ij\alpha\beta} (\bar{d}_L^i \gamma_\mu d_L^j) (\bar{\nu}_L^\alpha \gamma^\mu \nu_L^\beta) + L_R^{ij\alpha\beta} (\bar{d}_R^i \gamma_\mu d_R^j) (\bar{\nu}_L^\alpha \gamma^\mu \nu_L^\beta) \right]$$

Identifying correlations among observables is crucial to establish the existence and the nature of BSM physics behind the measured anomalies!

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Rank-One Flavor Violation (ROFV)

NP couples along a specific direction \hat{n} in the $U(3)_q$ quark flavor space

This scenario is naturally realized in many wellmotivated BSM models:

- Single leptoquark mediator
- \rightarrow Z' coupled to one flavor in the interaction basis
- Vector-like quark mixes with SM quarks
- > NP coupled linearly to SM quarks

 $\mathcal{L} \supset \lambda_i ar{q}^i \mathcal{O}_{\mathrm{NP}} + \mathrm{h.c.}$

$B^+ \to K^+ \nu \bar{\nu}$ and ROFV

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Rank-One Flavor Violation (ROFV)

NP couples along a specific direction \hat{n} in the $U(3)_q$ quark flavor space

$$\hat{n}_{i} = \begin{pmatrix} \hat{n}_{1^{\text{st}}} \\ \hat{n}_{2^{\text{nd}}} \\ \hat{n}_{3^{\text{rd}}} \end{pmatrix} = \begin{pmatrix} e^{i\alpha_{db}} \sin \theta \cos \phi \\ e^{i\alpha_{sb}} \sin \theta \sin \phi \\ \cos \theta \end{pmatrix}$$

$$L_{L,R,V}^{ij\alpha\beta} = C_{L,R,V} \times \hat{n}_i \hat{n}_j^* \times \begin{cases} \delta^{\alpha\beta} & \text{for LFU} ,\\ \delta^{\tau\alpha} \delta^{\tau\beta} & \text{for only tau flavour ,} \end{cases}$$

ROFV in LEFT

The combination relevant for $B^+ \rightarrow K^+ \nu \bar{\nu}$ is fixed to the best-fit value

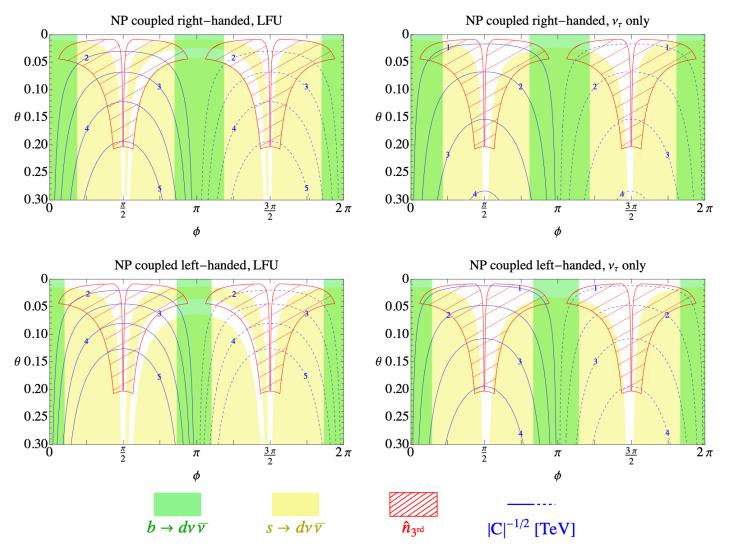
 $C_{L,R,V} \cos \theta \sin \theta \sin \phi = L_{L,R,V}^{sb} \Big|_{\text{best-fit}}$ $| \mathbf{LFU} | \nu_{\tau} \text{ only}$ $\mathbf{RH} | L_R^{sb,\text{LFU}} \approx (11.5 \text{ TeV})^{-2} | L_R^{sb\tau\tau} \approx (7.7 \text{ TeV})^{-2}$

 $\mathbf{LH} \mid L_L^{sb, \text{LFU}} \approx (14.2 \,\text{TeV})^{-2} \mid L_L^{sb\tau\tau} \approx (9.2 \,\text{TeV})^{-2}$

 $\alpha_{sb} = \alpha_{db} = 0$

Regions of the (ϕ, θ) plane excluded at 95% C.L.

NP should be third family aligned
 NP lies at few TeV
 LFU slightly disfavored



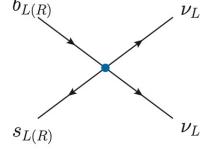
 $\hat{n}_{3^{\mathrm{rd}}} \sim (\mathcal{O}(V_{td}), \mathcal{O}(V_{ts}), \mathcal{O}(1))$

Going to the SMEFT

In SMEFT new correlations arise due to the SM structure:

- \succ rare decays $B_s(K_{L,S}) \rightarrow \mu^+ \mu^-$
- > meson-mixing constraints
- \succ high- p_T dilepton tails
- \succ Higgs and EW fit

$$\mathcal{O}_{lq}^{(1)\alpha\beta ij} = \left(\bar{l}_{L}^{\alpha}\gamma_{\mu}l_{L}^{\beta}\right)\left(\bar{q}_{L}^{i}\gamma^{\mu}q_{L}^{j}\right)$$
$$\mathcal{O}_{lq}^{(3)\alpha\beta ij} = \left(\bar{l}_{L}^{\alpha}\gamma_{\mu}\sigma_{a}l_{L}^{\beta}\right)\left(\bar{q}_{L}^{i}\gamma^{\mu}\sigma_{a}q_{L}^{j}\right)$$
$$\mathcal{O}_{ld}^{\alpha\beta ij} = \left(\bar{l}_{L}^{\alpha}\gamma_{\mu}l_{L}^{\beta}\right)\left(\bar{d}_{R}^{i}\gamma^{\mu}d_{R}^{j}\right)$$

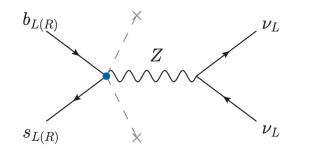


 $l_L^{lpha} = (
u_L^{lpha}, \ell_L^{lpha}) \qquad \qquad q_L^i = (V_{ji}^* u_L^j, d_L^i)^t$

Up to dimension six, there are 6 relevant SMEFT operators

$$\begin{split} L_L^{ij\alpha\beta} &= C_{lq}^{(1)\alpha\beta ij} - C_{lq}^{(3)\alpha\beta ij} + C_{Hq}^{(1)ij} \delta_{\alpha\beta} + C_{Hq}^{(3)ij} \delta_{\alpha\beta} ,\\ L_R^{ij\alpha\beta} &= C_{ld}^{\alpha\beta ij} + C_{Hd}^{ij} \delta_{\alpha\beta} \,. \end{split}$$

$$\begin{split} \mathcal{O}_{Hq}^{(1)ij} &= \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \left(\bar{q}_{L}^{i} \gamma^{\mu} q_{L}^{j} \right) \;, \\ \mathcal{O}_{Hq}^{(3)ij} &= \left(H^{\dagger} \sigma_{a} \overleftrightarrow{D}_{\mu} H \right) \left(\bar{q}_{L}^{i} \gamma^{\mu} \sigma_{a} q_{L}^{j} \right) \;, \\ \mathcal{O}_{Hd}^{ij} &= \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \left(\bar{d}_{R}^{i} \gamma^{\mu} d_{R}^{j} \right) \;. \end{split}$$

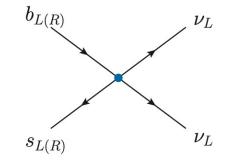


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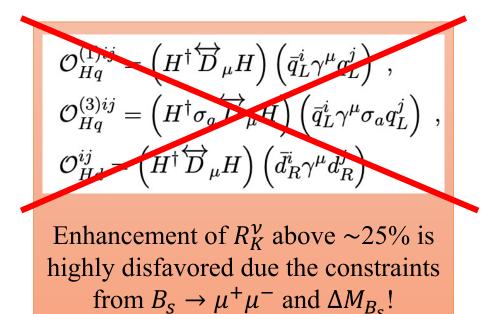
$$\mathcal{O}_{lq}^{(1)\alpha\beta ij} = \left(\bar{l}_{L}^{\alpha}\gamma_{\mu}l_{L}^{\beta}\right)\left(\bar{q}_{L}^{i}\gamma^{\mu}q_{L}^{j}\right)$$
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$$\mathcal{O}_{ld}^{\alpha\beta ij} = \left(\bar{l}_{L}^{\alpha}\gamma_{\mu}l_{L}^{\beta}\right)\left(\bar{d}_{R}^{i}\gamma^{\mu}d_{R}^{j}\right)$$



 $l_L^{lpha} = (
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Single-mediator models

$$\mathcal{O}_{lq}^{(1)\alpha\beta ij} = \left(\bar{l}_{L}^{\alpha}\gamma_{\mu}l_{L}^{\beta}\right)\left(\bar{q}_{L}^{i}\gamma^{\mu}q_{L}^{j}\right)$$
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$$\mathcal{O}_{ld}^{\alpha\beta ij} = \left(\bar{l}_{L}^{\alpha}\gamma_{\mu}l_{L}^{\beta}\right)\left(\bar{d}_{R}^{i}\gamma^{\mu}d_{R}^{j}\right)$$

Loop-level mediators are expected to have light and relatively strongly coupled states, disfavored by direct searches at the LHC

			\mathbf{Spin}	$G_{ m SM}$	Interaction term	SMEFT coeff.
			$V' \mid 1$	$({\bf 1},{\bf 3},0)$	$\left[g_q^{ij}(ar q_L^i\gamma^\mu\sigma_a q_L^j) ~+~ g_\ell^{lphaeta}(ar l_L^lpha\gamma^\mu\sigma_a l_L^eta) ight]V_{a\mu}^\prime$	$C_{lq}^{(3)}$
Colorle	ess vector mediators	$ \langle$	$Z'_L \mid 1$	$({f 1},{f 1},0)$	$\left[g^{ij}_q(ar q^i_L\gamma^\mu q^j_L)~+~g^{lphaeta}_\ell(ar l^lpha_L\gamma^\mu\sigma_a l^eta_L) ight]Z'_{L\mu}$	$C_{lq}^{(1)}$
			Z'_R 1	$({f 1},{f 1},0)$	$\left[g^{ij}_q(ar{d}^i_R\gamma^\mu d^j_R)~+~g^{lphaeta}_\ell(ar{l}^lpha_L\gamma^\mu\sigma_a l^eta_L) ight]Z'_{R\mu}$	C_{ld}
			$S_1 \mid 0$	$(ar{3},1,1/3)$	$\lambda_{ilpha}^{*}(\overline{q_{L}^{i,c}}\epsilon l_{L}^{lpha})S_{1}$	$C_{lq}^{(1)} = -C_{lq}^{(3)}$
_			$S_3 \mid 0$	$(ar{3},3,1/3)$	$\lambda_{ilpha}^{st}(\overline{q_L^{i,c}}\epsilon\sigma_a l_L^{lpha})(S_3)_a$	$C_{lq}^{(1)} = 3C_{lq}^{(3)}$
	Leptoquarks	$ \prec$	$U_3 \mid 1$	$({\bf 3},{\bf 3},2/3)$	$\lambda_{ilpha}(\overline{q_L^i}\gamma_\mu\sigma_a l_L^lpha)(U_3^\mu)_a$	$C_{lq}^{(1)} = -3C_{lq}^{(3)}$
			$ ilde{R}_2 ig 0$	$({\bf 3},{\bf 2},1/6)$	$\lambda_{ilpha}\overline{d^i_R}(l^lpha_L\epsilon ilde R_2)$	C_{ld}
			V_2 1	$(ar{3}, 2, 5/6)$	$\lambda_{ilpha}^{st}\overline{d_{R}^{i,c}}\gamma_{\mu}(l_{L}^{lpha}\epsilon V_{2}^{\mu})$	C_{ld}

Single-mediator models

$egin{split} \mathcal{O}_{lq}^{(1)lphaeta ij} &= \left(ar{l}_L^lpha \gamma_\mu l_L^eta ight) \left(ar{q}_L^i \gamma^\mu q_L^j ight) \ \mathcal{O}_{lq}^{(3)lphaeta ij} &= \left(ar{l}_L^lpha \gamma_\mu \sigma_a l_L^eta ight) \left(ar{q}_L^i \gamma^\mu \sigma_a q_L^j ight) \ \mathcal{O}_{ld}^{lphaeta ij} &= \left(ar{l}_L^lpha \gamma_\mu l_L^eta ight) \left(ar{d}_R^i \gamma^\mu d_R^j ight) \end{split}$	cons mix	r-quark operators, strained by meson- ing, arise from the e interaction terms	$\mathcal{O}_{qq}^{(3)ijkl} = \begin{pmatrix} \bar{q}_L^i \\ \mathcal{O}_{dd}^{ijkl} = \begin{pmatrix} \bar{d}_L^j \end{pmatrix}$	$ \begin{pmatrix} \bar{q}_L^i \gamma_\mu q_L^j \end{pmatrix} \begin{pmatrix} \bar{q}_L^k \gamma^\mu q_L^l \end{pmatrix} , \\ \gamma_\mu \sigma_a q_L^j \end{pmatrix} \begin{pmatrix} \bar{q}_L^k \gamma^\mu \sigma_a q_L^l \end{pmatrix} , \\ \bar{q}_R^i \gamma_\mu d_R^j \end{pmatrix} \begin{pmatrix} \bar{d}_R^k \gamma^\mu d_R^l \end{pmatrix} , \\ \left(\bar{q}_L^i \gamma_\mu q_L^j \right) \begin{pmatrix} \bar{d}_R^k \gamma^\mu d_R^l \end{pmatrix} , $
	Spin $ $ C	$F_{\rm SM} \mid$ Int	teraction term	SMEFT coeff.
	$V' \mid 1 \mid (1,$	$\left. {f 3},0 ight) ~~\left ~\left[g_q^{ij}(ar q_L^i\gamma^\mu\sigma_a q_\mu^j) ight) ight ight.$	$(g_L^j) + g_\ell^{lphaeta}(ar l_L^lpha\gamma^\mu\sigma_a l_L^eta) \Big] V_{a\mu}'$	$C_{lq}^{(3)}$
Colorless vector mediators	$Z'_L \mid 1 \mid (1,$	$\left. {f 1},0 ight) ~~ ight ~~ \left[g_q^{ij} (ar q_L^i \gamma^\mu q_L^j$	$) ~+~ g_\ell^{lphaeta}(ar l_L^lpha\gamma^\mu\sigma_a l_L^eta)\Big]Z'_{L\mu}$	$C_{lq}^{\left(1 ight) }$
	$Z'_R \left 1 \right $ (1,	$\left. {f 1},0 ight) ~~\left ~~ \left[g_q^{ij} (ar d_R^i \gamma^\mu d_R^j$	$g_{\ell}^{lphaeta} \;+\; g_{\ell}^{lphaeta}(ar{l}_{L}^{lpha}\gamma^{\mu}\sigma_{a}l_{L}^{eta})\Big]Z_{R\mu}^{\prime}$	C_{ld}
	$S_1 \mid 0 \mid (ar{3}, ar{3})$	(., 1/3)	$\lambda_{ilpha}^{*}(\overline{q_{L}^{i,c}}\epsilon l_{L}^{lpha})S_{1}$	$C_{lq}^{(1)} = -C_{lq}^{(3)}$
	$S_3 \mid 0 \mid (\bar{3}, 3)$	$\left \lambda_{ic}^{*} \right = \lambda_{ic}^{*}$	$_{lpha}(\overline{q_{L}^{i,c}}\epsilon\sigma_{a}l_{L}^{lpha})(S_{3})_{a})_{a}$	$C_{lq}^{(1)} = 3C_{lq}^{(3)}$
Leptoquarks	$U_3 \mid 1 \mid (3,3)$	$\left \lambda_{ilpha} \right = \lambda_{ilpha}$	$(\overline{q_L^i}\gamma_\mu\sigma_a l_L^lpha)(U_3^\mu)_a$	$ig C^{(1)}_{lq} = -3 C^{(3)}_{lq}$
	$ ilde{R}_2 ig 0 ig (3, 2)$	2,1/6)	$\lambda_{ilpha}\overline{d^i_R}(l^lpha_L\epsilon ilde R_2)$	C_{ld}
	$V_2 \mid 1 \mid (\bar{3}, 2)$	$\lambda_{i}^{2}, 5/6)$ λ_{i}^{2}	$_{ilpha}^{*}\overline{d_{R}^{i,c}}\gamma_{\mu}(l_{L}^{lpha}\epsilon V_{2}^{\mu})$	C_{ld}









5. $U_3 \sim (\mathbf{3}, \mathbf{3}, 2/3)$

It can not accommodate the Belle II excess with 1σ

1
 2



4. $Z' \sim (1, 1, 0)$ and $V' \sim (1, 3, 0)$

Disfavored as meson-mixing arises already at tree-level

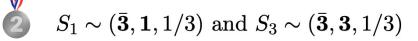
5. $U_3 \sim (\mathbf{3}, \mathbf{3}, 2/3)$

 $V_2 \sim (\bar{\mathbf{3}}, \mathbf{2}, 5/6)$ Good fit but stringent PU bound on coupling

- 4. $Z' \sim (1, 1, 0)$ and $V' \sim (1, 3, 0)$
- 5. $U_3 \sim (\mathbf{3}, \mathbf{3}, 2/3)$

2

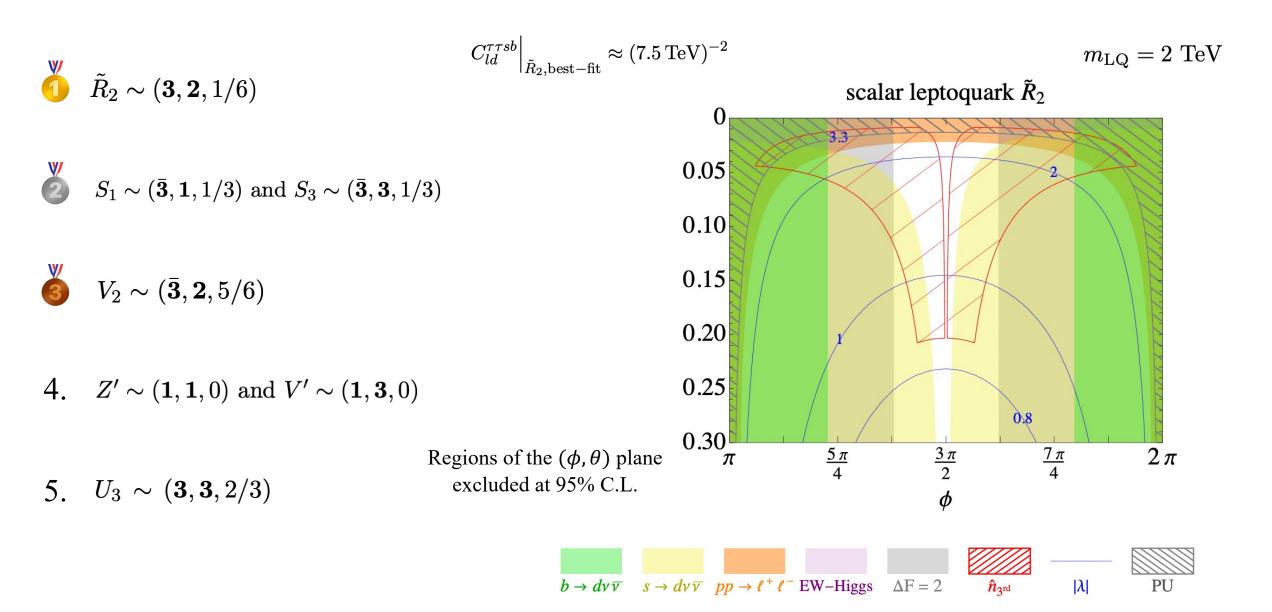




Slightly disfavored as they coupled to LH quarks

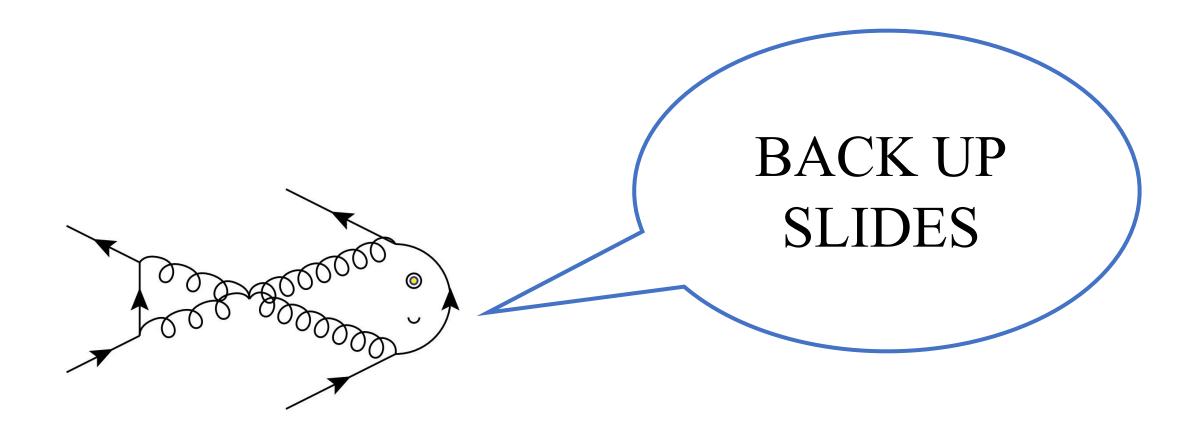
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- 4. $Z' \sim (1, 1, 0)$ and $V' \sim (1, 3, 0)$
- 5. $U_3 \sim (\mathbf{3}, \mathbf{3}, 2/3)$

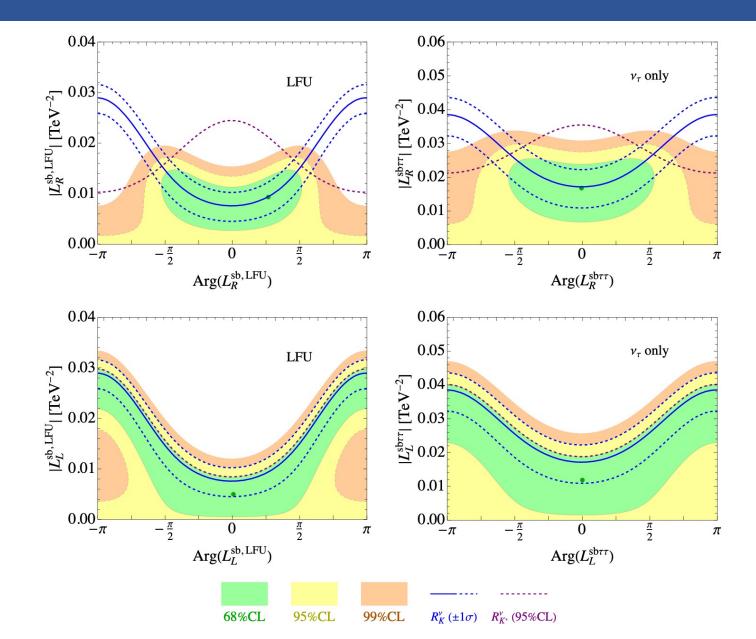








LEFT fits

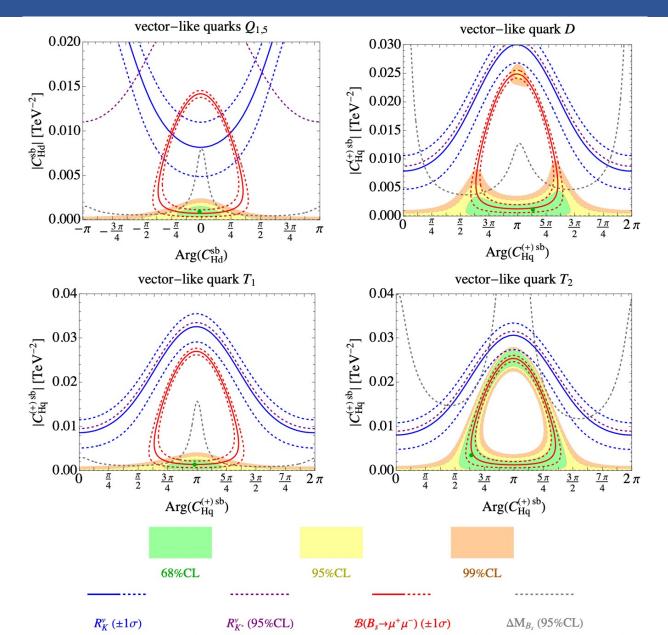


Higgs-quark operators

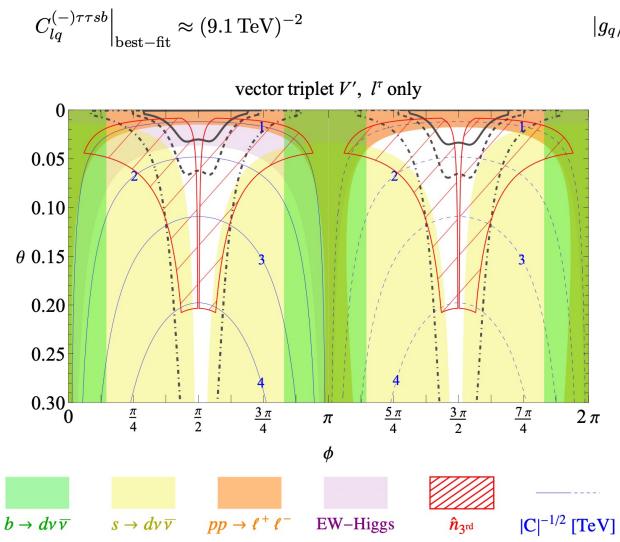
$$\begin{split} \mathcal{O}_{Hq}^{(1)ij} &= \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \left(\bar{q}_{L}^{i} \gamma^{\mu} q_{L}^{j} \right) \;, \\ \mathcal{O}_{Hq}^{(3)ij} &= \left(H^{\dagger} \sigma_{a} \overleftrightarrow{D}_{\mu} H \right) \left(\bar{q}_{L}^{i} \gamma^{\mu} \sigma_{a} q_{L}^{j} \right) \;, \\ \mathcal{O}_{Hd}^{ij} &= \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \left(\bar{d}_{R}^{i} \gamma^{\mu} d_{R}^{j} \right) \;. \end{split}$$

Simplified model	Spin	SM irrep	SMEFT couplings
D	1/2	(3 , 1 ,-1/3)	$C_{Hq}^{(1)} = C_{Hq}^{(3)}$
T_1	1/2	(3 , 3 ,-1/3)	$C_{Hq}^{(1)} = -3C_{Hq}^{(3)}$
T_2	1/2	(3 , 3 , 2/6)	$C_{Hq}^{(1)} = 3C_{Hq}^{(3)}$
Q_1	1/2	(3, 2, 1/6)	C_{Hd}
Q_5	1/2	(3, 2, -5/6)	C_{Hd}

Enhancement of R_K^{ν} above ~25% is highly disfavored due the constraints from $B_s \rightarrow \mu^+ \mu^-$ and $\Delta M_{B_s}!$

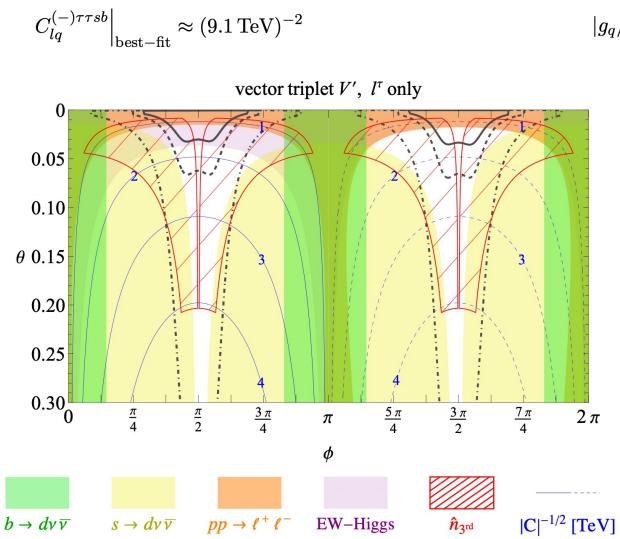


Colorless vectors



 $|g_q/g_\ell| = 0.1$ (solid), 0.05(dashed) and 0.01(dot-dashed)

Colorless vectors



 $|g_q/g_\ell| = 0.1$ (solid), 0.05(dashed) and 0.01(dot-dashed)

$$M_{V'} \lesssim 1391 \text{ GeV} \left(\frac{|g_q/g_\ell|^{\max}}{0.05} \right)^{1/2} |\sin \theta \cos \theta \sin \phi|^{\frac{1}{2}}$$

 $pprox 762 \text{ GeV} \left(\frac{|g_q/g_\ell|^{\max}}{0.05} \right)^{1/2} \left| \frac{\theta}{0.3} \right|^{1/2},$

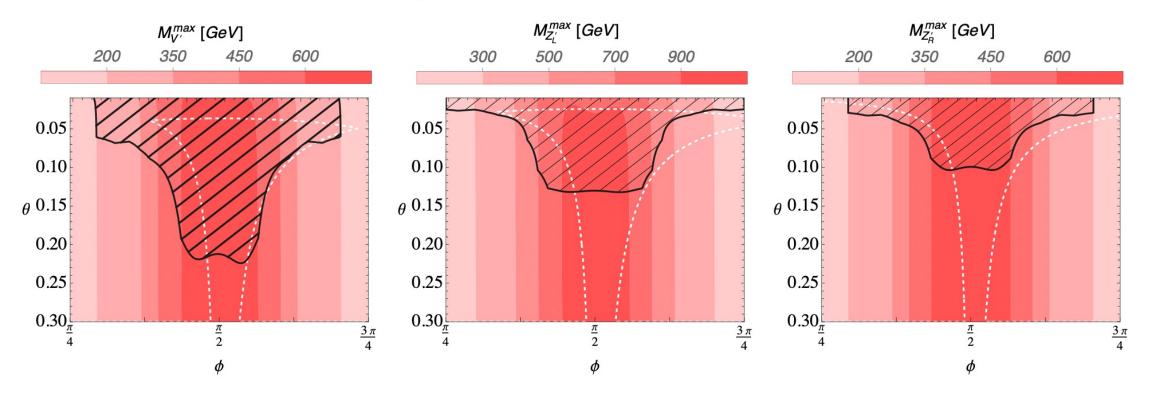
Colorless vectors

High-p_T dilepton tails bound does not hold anymore!
 We consider the constraints from direct searches

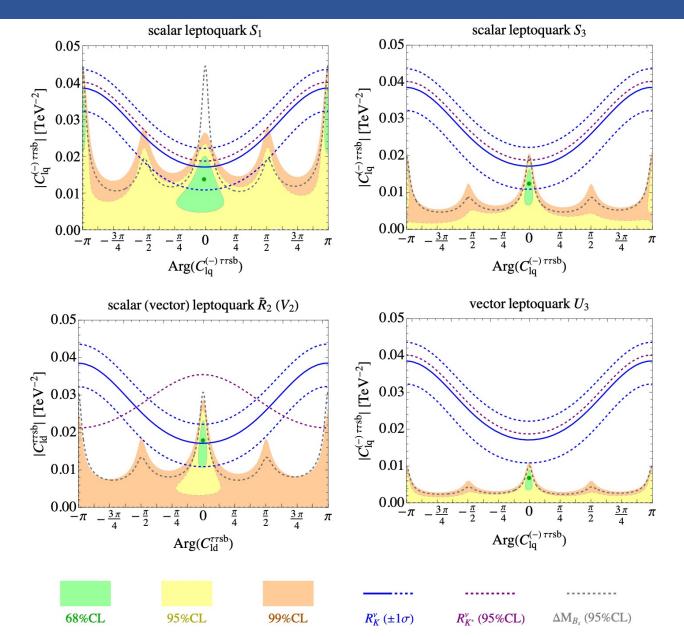
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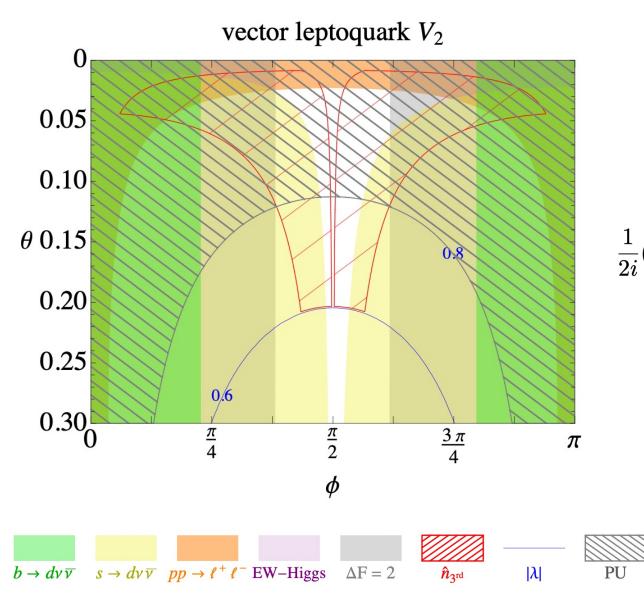
$$\sigma(pp \to V'^0 \to \tau^+ \tau^-) \approx \frac{4\pi^2}{3} \mathcal{B}(V'^0 \to \tau^+ \tau^-) \sum_{i,j=u,d,s,c,b} \frac{\Gamma(V'^0 \to q^i \bar{q}^j)}{M_{V'}} \frac{2}{s_0} \mathcal{L}_{q^i \bar{q}^j}(M_{V'})$$



Leptoquark fits



PU bound



$$a_{fi}^J = rac{1}{32\pi} \int_{-1}^1 \mathrm{d}\cos heta d_{\mu_i\mu_f}^J(heta) \mathcal{T}_{fi}(\sqrt{s},\cos heta)$$

$$\frac{1}{2i}(a_{fi}^J - a_{if}^{J*}) = \sum_{h} a_{hf}^{J*} a_{hi}^J , \qquad |a_{ii}^{J,\text{tree}}| \le \frac{1}{2}$$

$$|\lambda| \lesssim egin{cases} 3.2 & {
m for} \; S_1 \; , \ 3.3 & {
m for} \; ilde R_2 \; , \ 0.8 & {
m for} \; V_2 \; . \end{cases}$$

LNV scenario

