

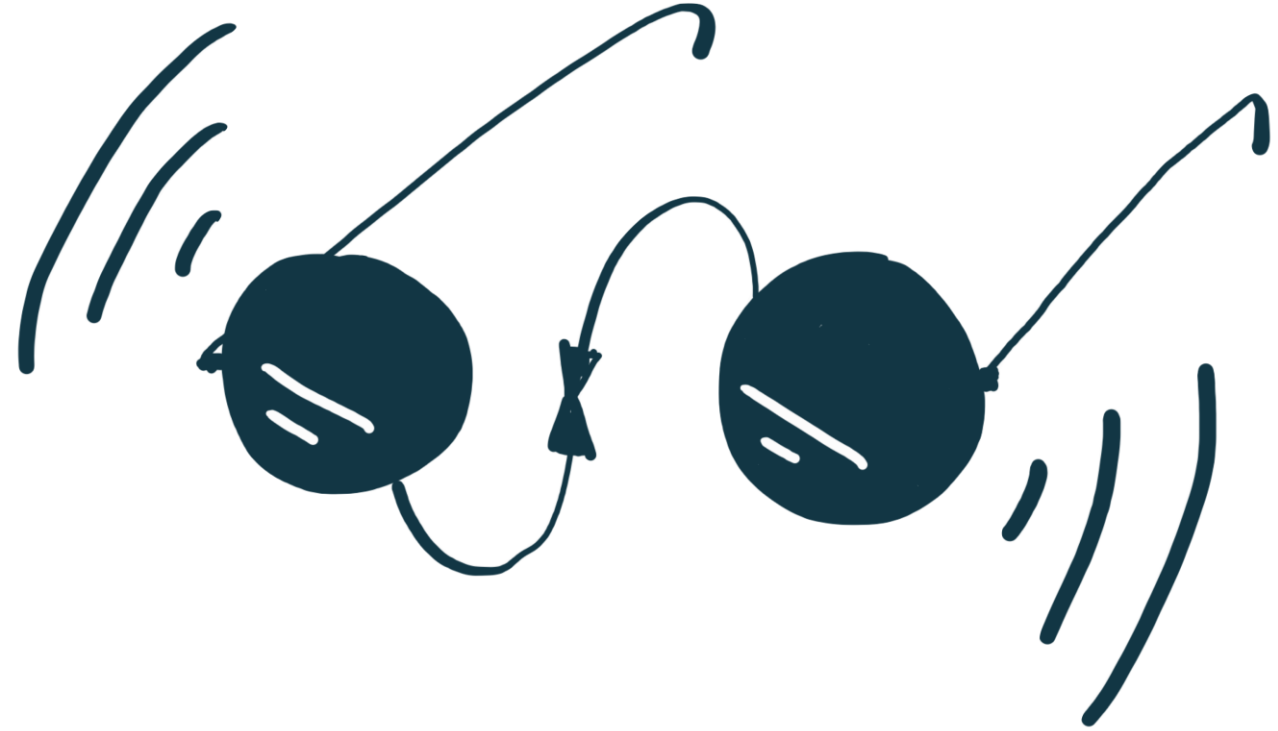
BAUSCIA

An antenna for high frequency gravitational waves

Matteo Borghesi

Contributors (Milano-Bicocca):

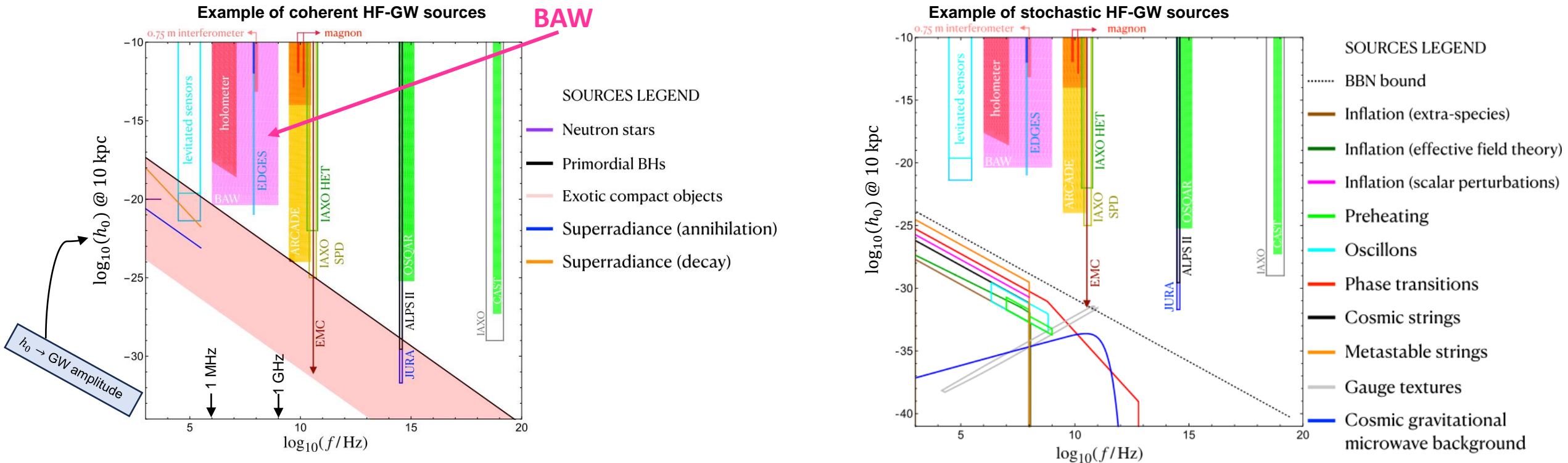
G. Albani, M. Borghesi, M. Benaglia, G. Conenna, T. Tabarelli de Fatis, F. De Guio, M. Faverzani, E. Ferri, A. Ghezzi, R. Gerosa, B. Giacomazzo, A. Giachero, M. Malberti, A. Nucciotti, G. Pessina.



Why high frequency gravitational waves?

- There are many potential GW sources at frequency higher than those covered by interferometers.

Aggarwal, N., Aguiar, O.D., Bauswein, A. *et al.* Challenges and opportunities of gravitational-wave searches at MHz to GHz frequencies. *Living Rev Relativ* 24, 4 (2021).
<https://doi.org/10.1007/s41114-021-00032-5>

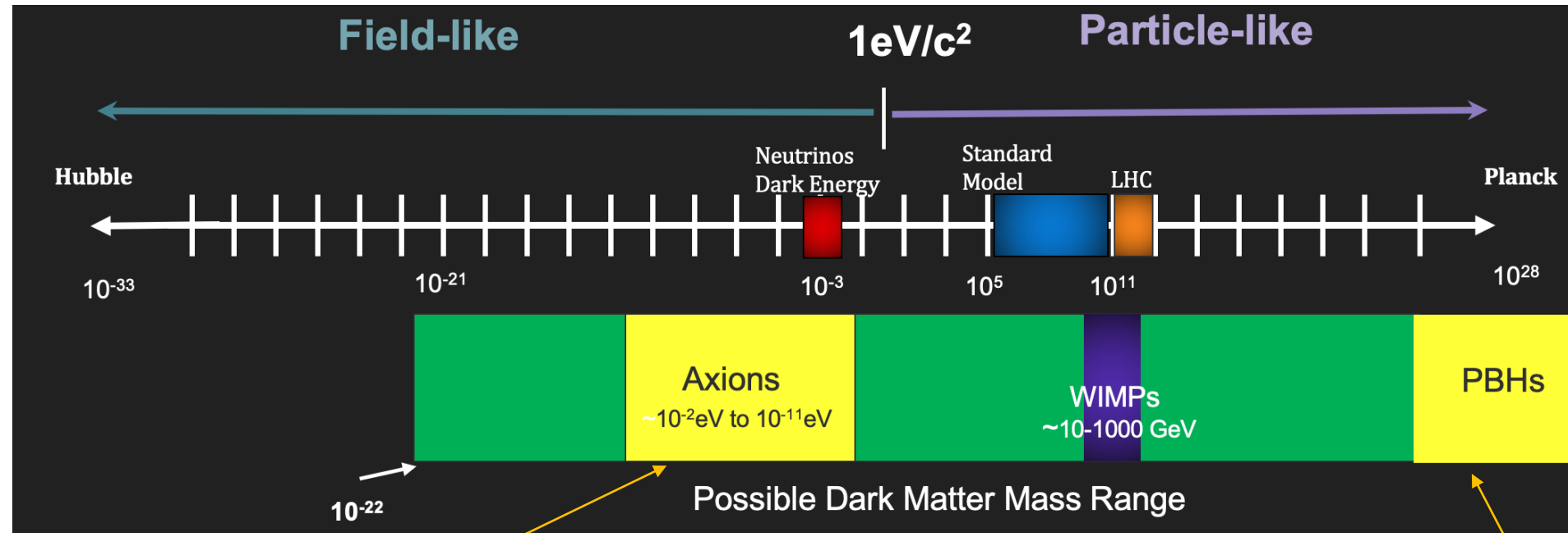


- The identity of dark matter is still unknown. It may hide in HF-GW?

A glimpse of HF-GW DM sources (I)

- With HF-GW we can probe very different mass range of DM!

Cartoon from [Andrew Geraci's talk at Challenges and opportunities of HFGW, Trieste 2019](#)



Black hole superradiance

- QCD **axion** annihilations to gravitons in cloud around black holes.
- Requires detection sensitivity around 10-100 kHz
Coverable with customized BAW

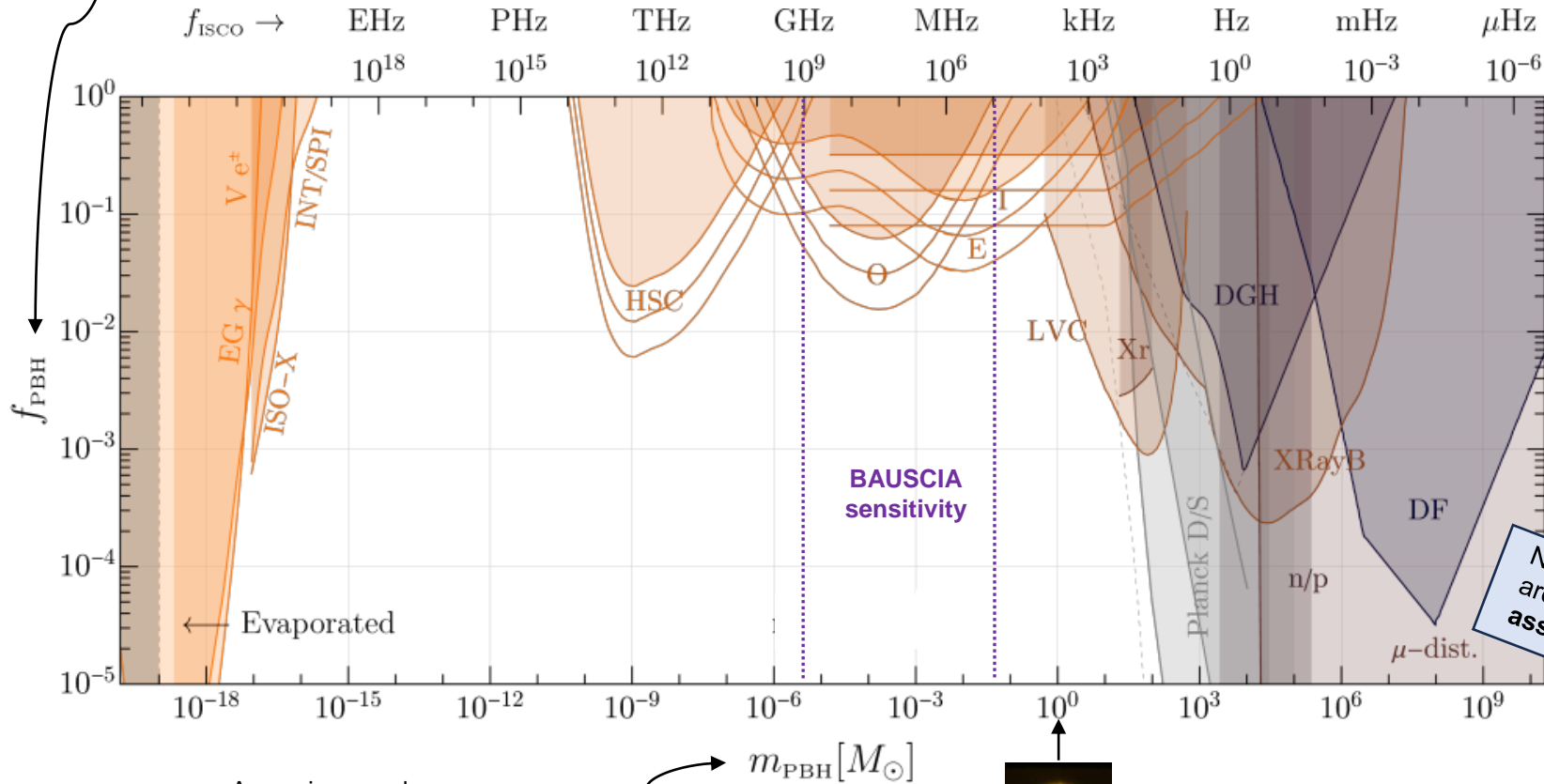
Light Primordial Black Holes (PBH)

- Primordial black holes (**PBH**) can contribute up to about 10% of the dark matter at planetary masses (see next slide).
GW emission coverable by existing BAW

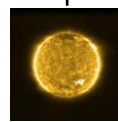
A glimpse of HF-GW DM sources (II)

Fraction of dark matter composed of PBH

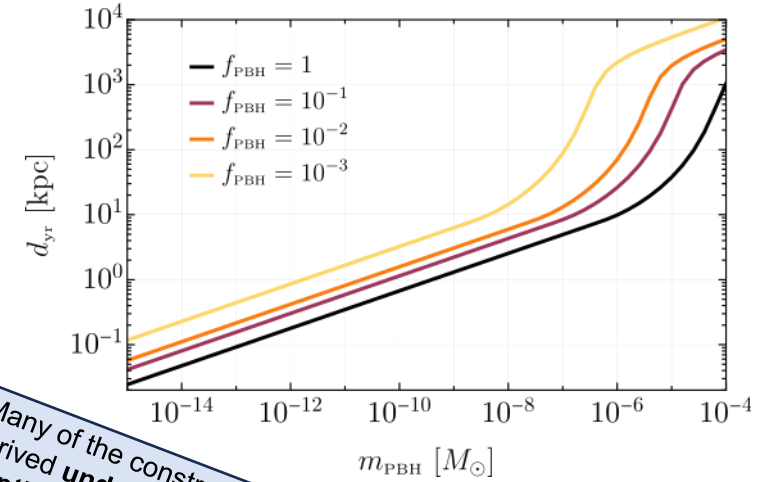
Most stringent constraints on the PBH abundance



Assuming equal mass merger and narrow mass distribution



Size of the region containing O(1) merger event per year



NB: Many of the constraints are derived under specific assumptions

Hunt for light primordial black hole dark matter with ultrahigh-frequency gravitational waves
Gabriele Franciolini, Anshuman Maharana, and Francesco Muia
Phys. Rev. D **106**, 103520 – Published 17 November 2022

Few things to keep in mind

Amplitudes of the “plus” and “cross” polarization of the wave

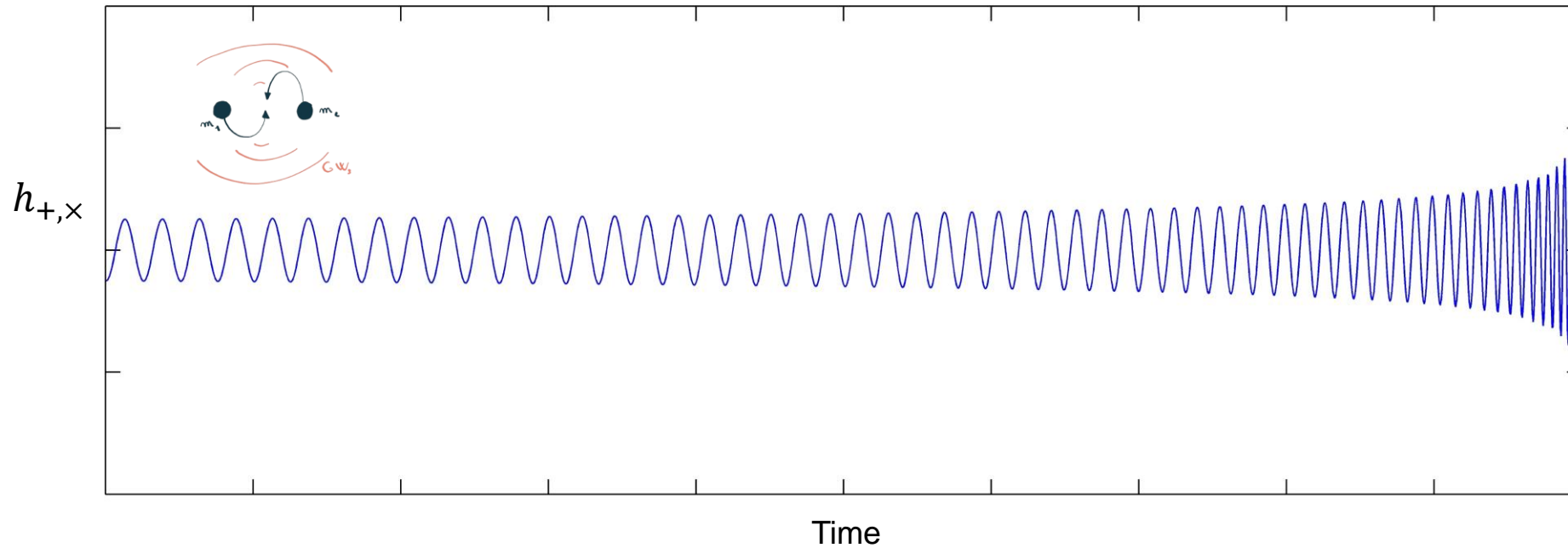
$$h_{+, \times}(t) \propto \frac{1}{d_L} \left(\frac{GM_c}{c^2} \right)^{\frac{5}{3}} \left(\frac{\pi f_{gw}}{c} \right)^{\frac{2}{3}} \cos(2\pi f_{gw}t + \phi)$$

Distance from the observer

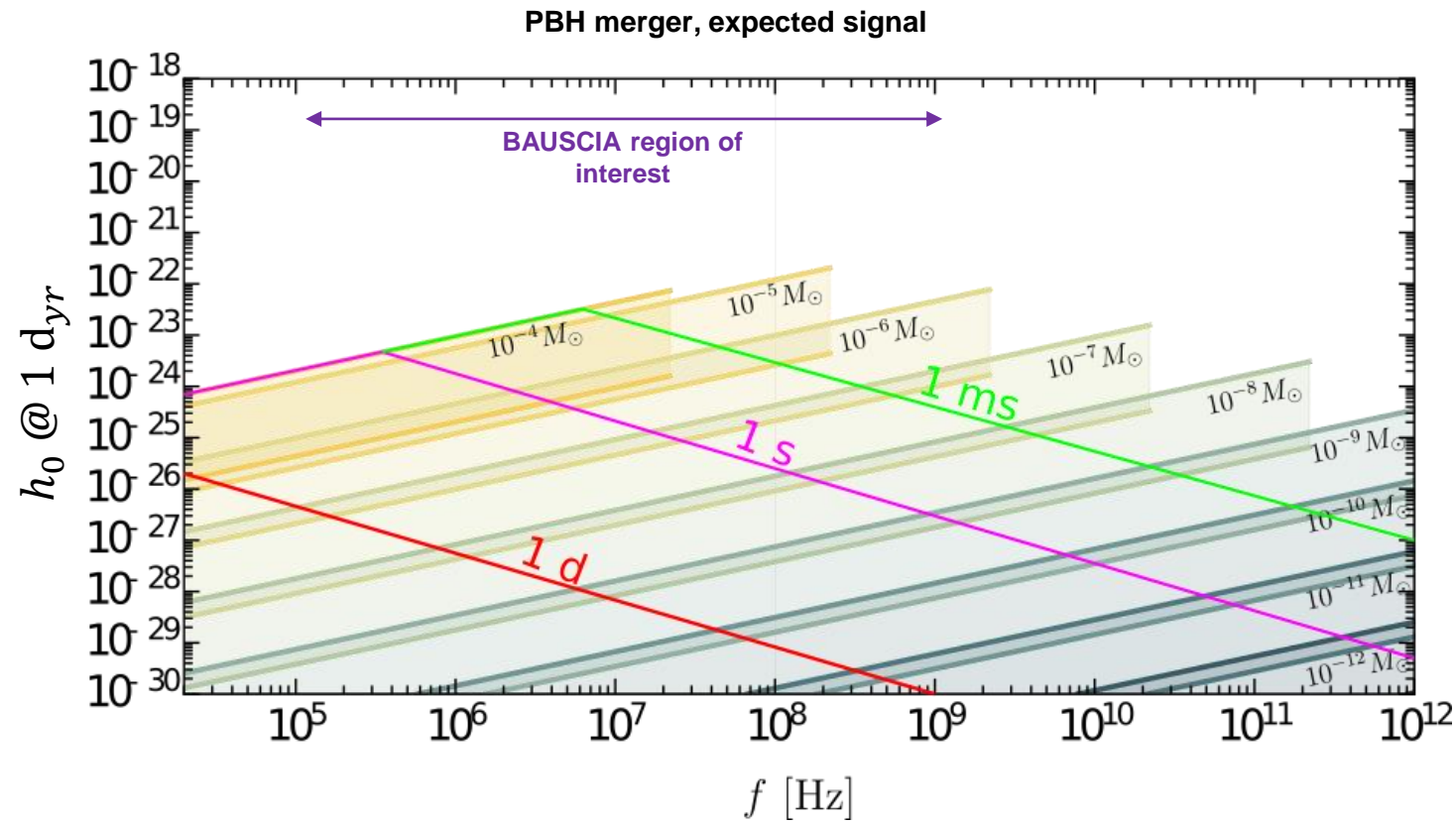
$$M_c = M_c(m_1, m_2)$$

$$f_{gw}(t) \propto \left(\frac{1}{t_{coal} - t} \right)^{3/8} \left(\frac{GM_c}{c^3} \right)^{-5/8}$$

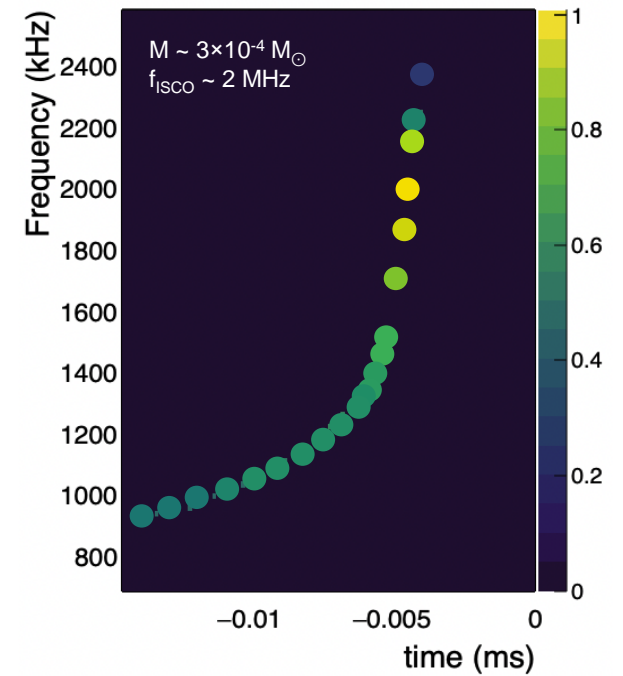
Time evolution of the GW amplitude (inspiral phase of a binary system)



A glimpse of HF-GW DM sources (III)

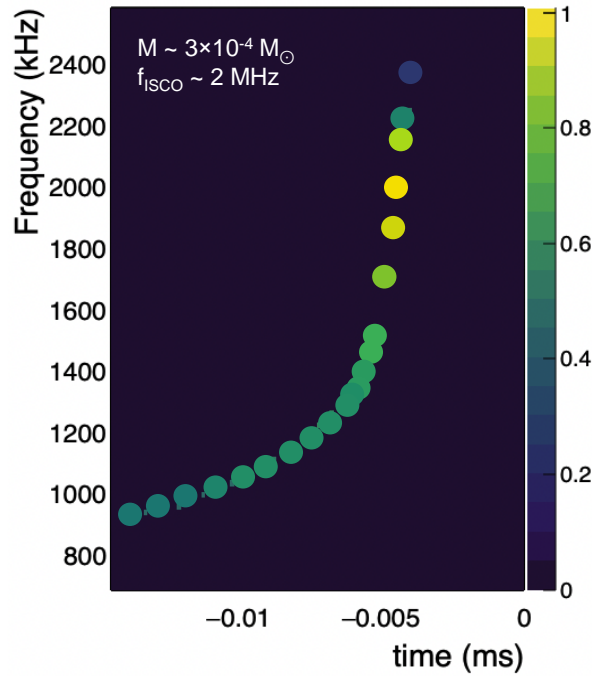


Example of a merger event near f_{ISCO} frequency

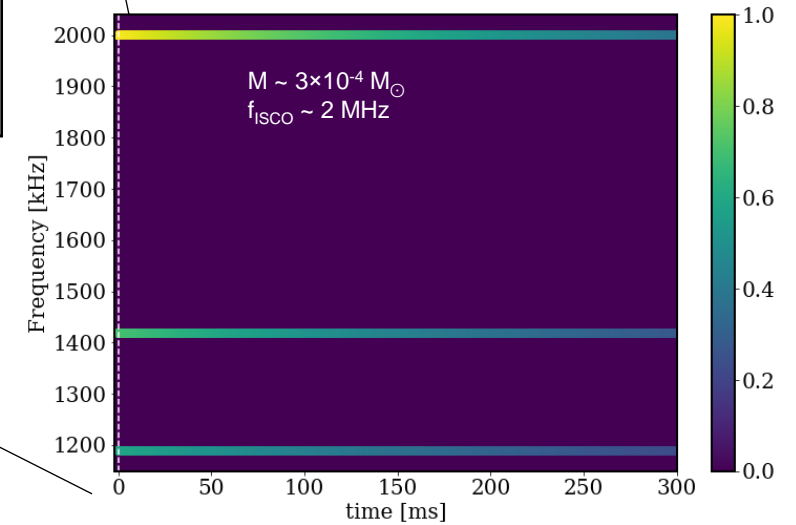
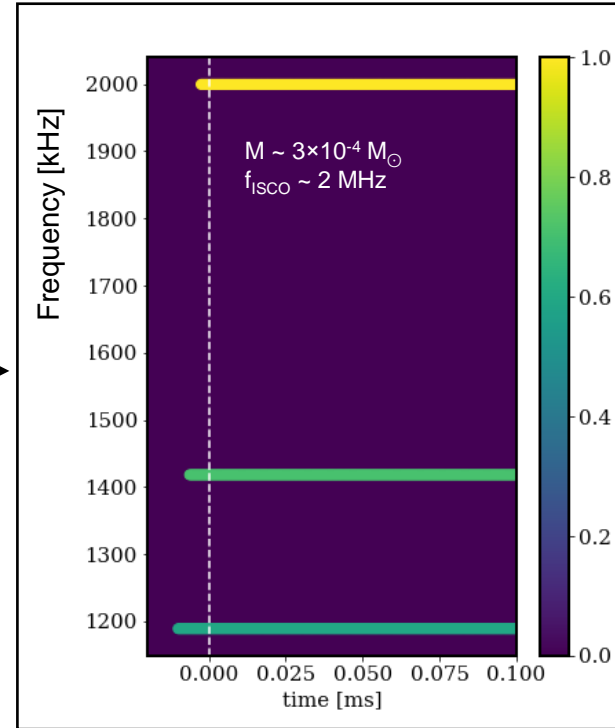


A glimpse of HF-GW DM sources (III)

Example of a merger event near f_{ISCO} frequency

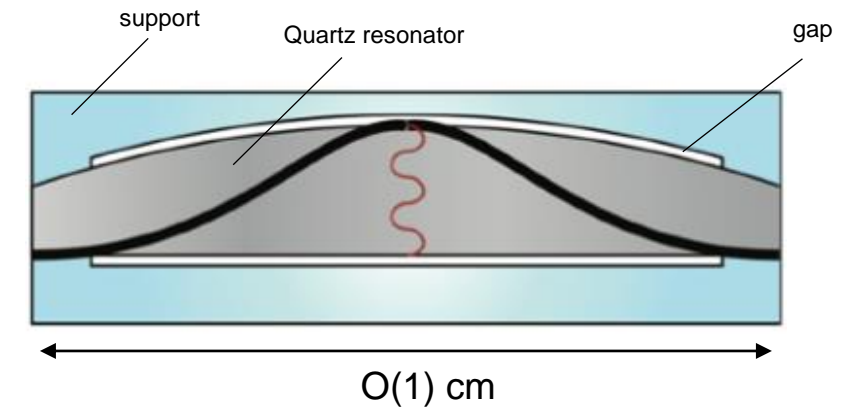


1 Resonant mass
BAUSCIA-like detector



Bulk Acoustic Wave (BAW) Device

- Bulk Acoustic Wave Sensors for a High Frequency Antenna (BAUSCIA, in Milan's dialect)
- GW tidal forces stretches and squeeze the mass: **resonance mass detector**
- Length variation only **detectable at the resonant frequency** of the vibration mode(s)
- **MAGE**: existing experiment. In 2021 it detected two signals of uncertain origin



M. Goryachev et al, "Rare events detected with a Bulk Acoustic Wave High Frequency Gravitational Wave Antenna", [PRL 127, 07102 \(2021\)](#)

PRO:

- High narrow band sensitivity through **high quality factor (Q)**
- Internal transducer: **piezoelectric**
 - Only odd overtones audible
- **Wide frequency range of high Q modes**
 - Three family types with different velocities
 - 2 transverse (B,C) and 1 longitudinal (A)
 - multiple overtones and vibration modes
- **Scalable** technology, established > 70 years for precision clock applications

$$f_{n,k} = n \frac{v_k}{2\Delta s} \quad (k = A, B, C)$$

Resonant frequency

Sound velocity of the k mode

Harmonic number

BAW thickness

BAW Detection concept

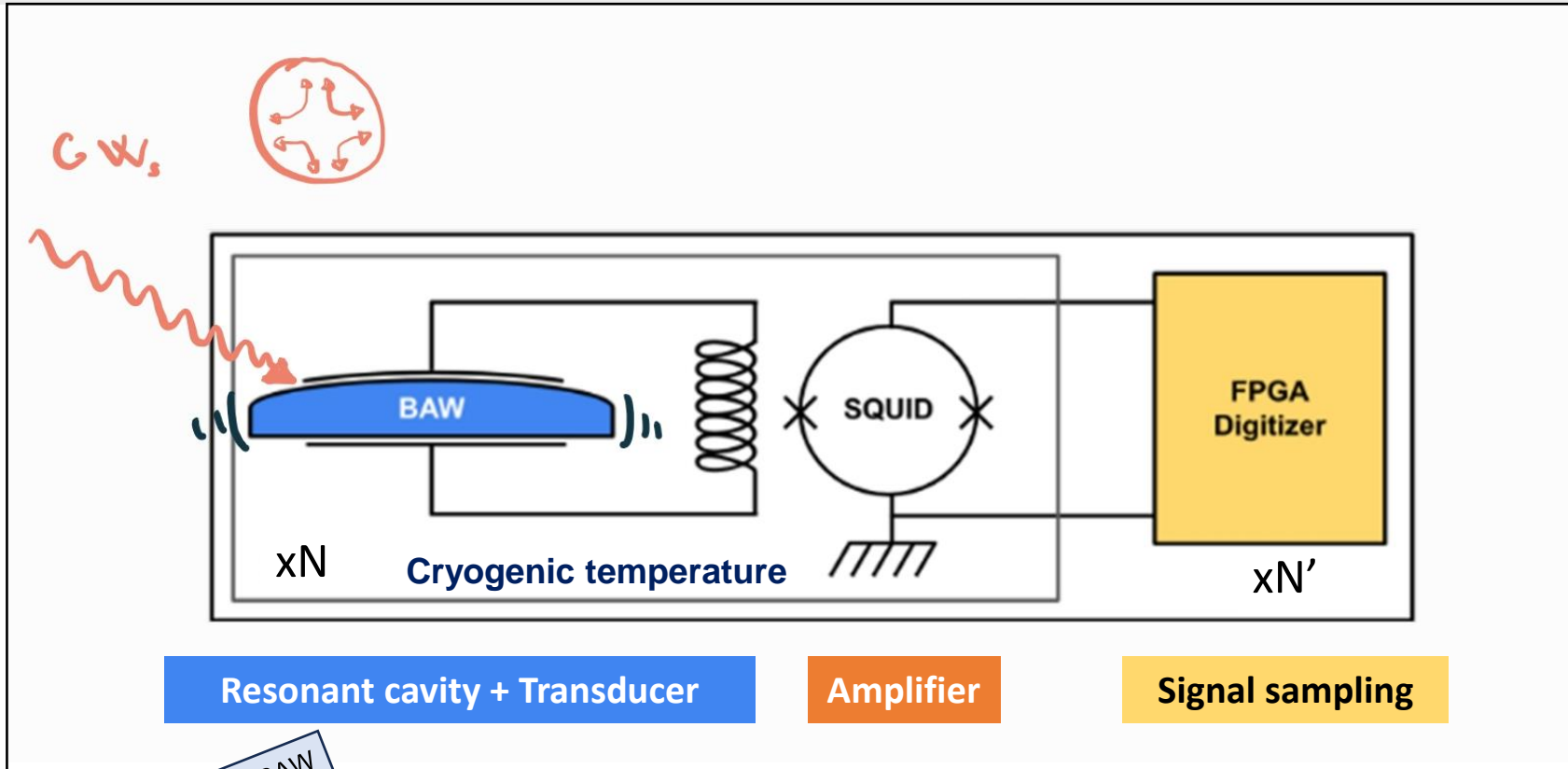
displacement

current

voltage

data

$$h(t) \longrightarrow u(t) + n \longrightarrow i(t) + n \longrightarrow A(i(t) + n) + n_A \longrightarrow A(i(\tau) + n) + n_A$$



Noise is dominated by BAW thermal noise.

BAUSCIA idea

“Broadband” sensitivity provided by:

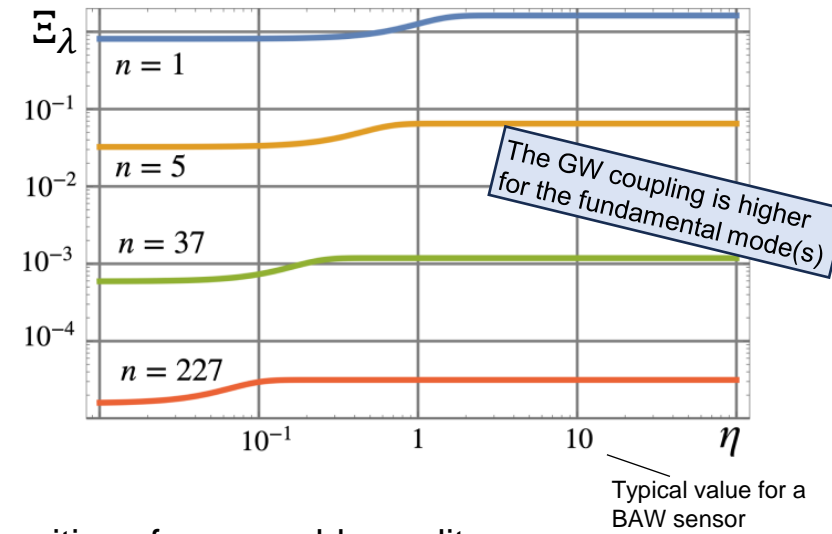
- Multiple **overtones** sensing per BAW
- **Array** of many **BAWs** tuned to different frequency
Requires specific R&D on BAWs

BAW HF-GW sensitivity

- The time component of the displacement (ξ_λ) follow the forced harmonic oscillator equation

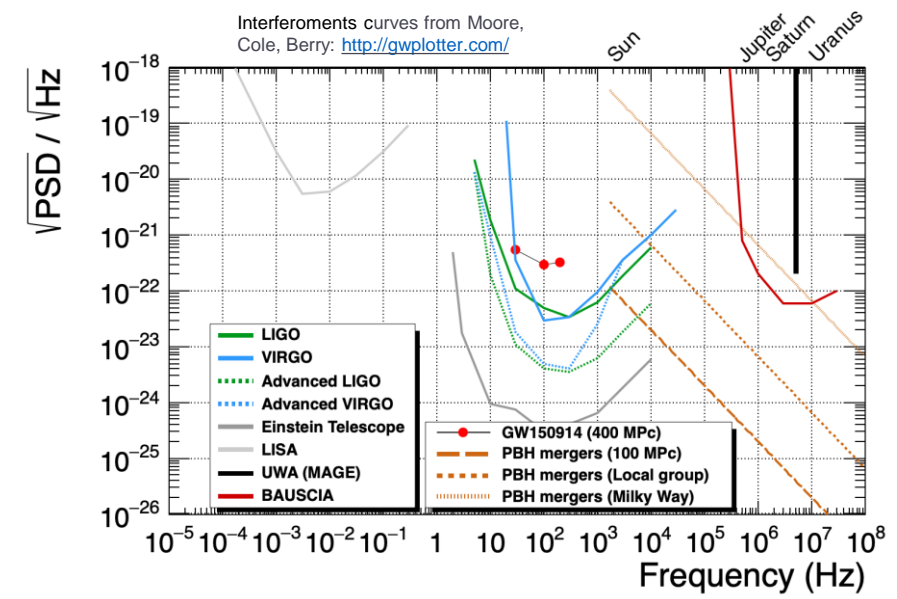
$$\ddot{\xi}_\lambda + \gamma_\lambda \dot{\xi}_\lambda + \omega_\lambda^2 \xi_\lambda = -c^2 \times (R_{i0j0}) \times \frac{\Delta s}{2} \times \Xi_\lambda$$

displacement ξ_λ Mode numbers ($\lambda = X, n, m, p$) GW (R_{i0j0}) BAW thickness $\frac{\Delta s}{2}$ GW-cavity coupling Ξ_λ



- Expected sensitivity (PRELIMINARY) scaling from the MAGE antenna to an array of multiple BAW cavities of comparable quality.

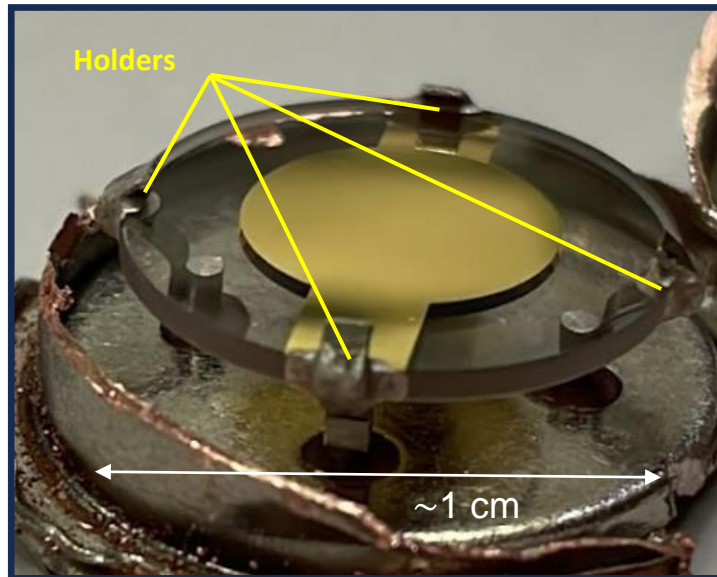
$$S_h^+(\omega = \omega_\lambda) = \sqrt{\frac{4 k_b T_\lambda \omega_\lambda}{Q_\lambda M_\lambda} \left(\frac{1}{\omega_\lambda^2 (\Delta s/2) \Xi_\lambda} \right)}$$



- Complementary to large interferometers
- Supplementary to MAGE

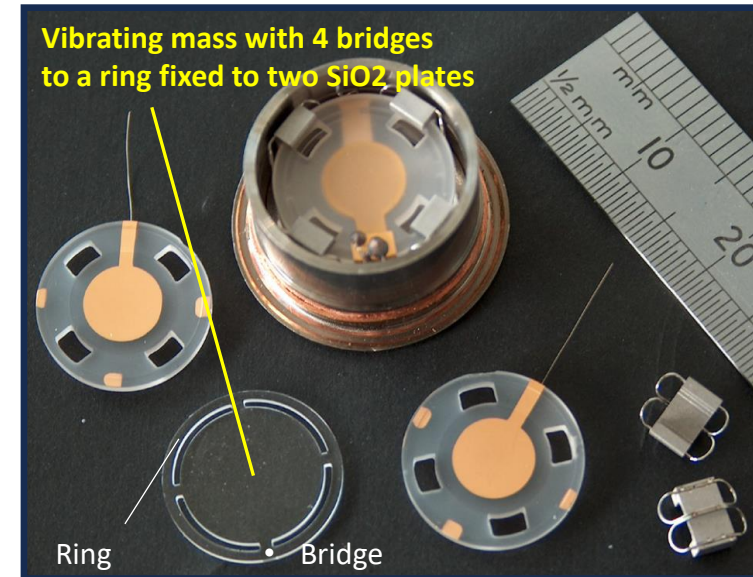
Off-the-shelf quartz cavities (Rakon XO)

- SiO₂ crystal with 4 rigid mounts
- Electrodes deposited on BAW (**suboptimal**)
- Optimized at room temperature for the 3rd Overtone of the C-mode (~5 MHz)
- Low Q at n = 1



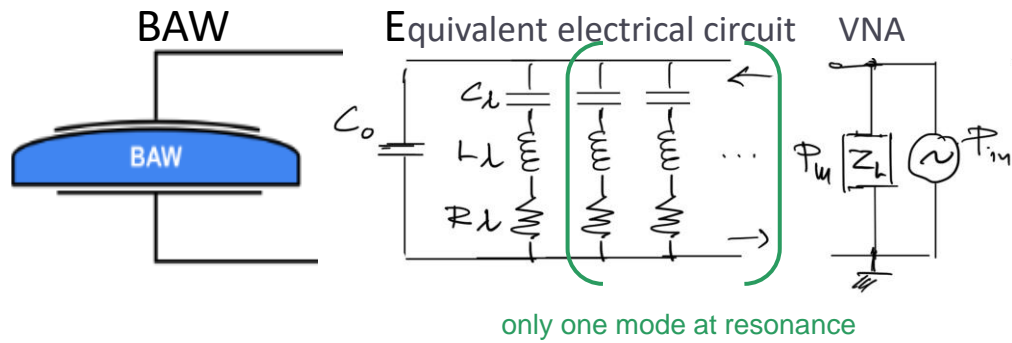
MAGE-like BAW

- Piano convex SiO₂ crystal
- Electrodes deposited on separated support plates (**low loss design**)

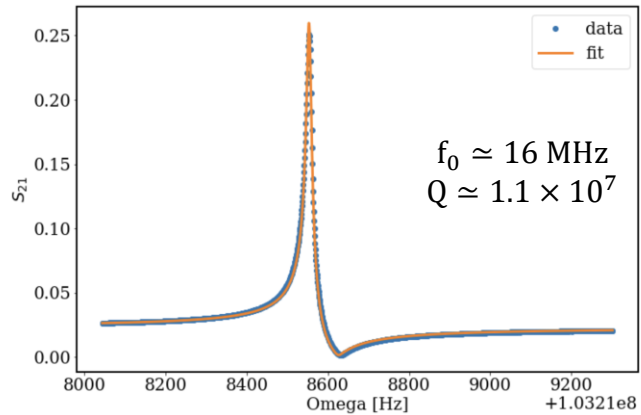


Both exhibit **Q factor > 10⁶** at cryogenic temperature (4K)

- Study of low temperature BAW behaviour

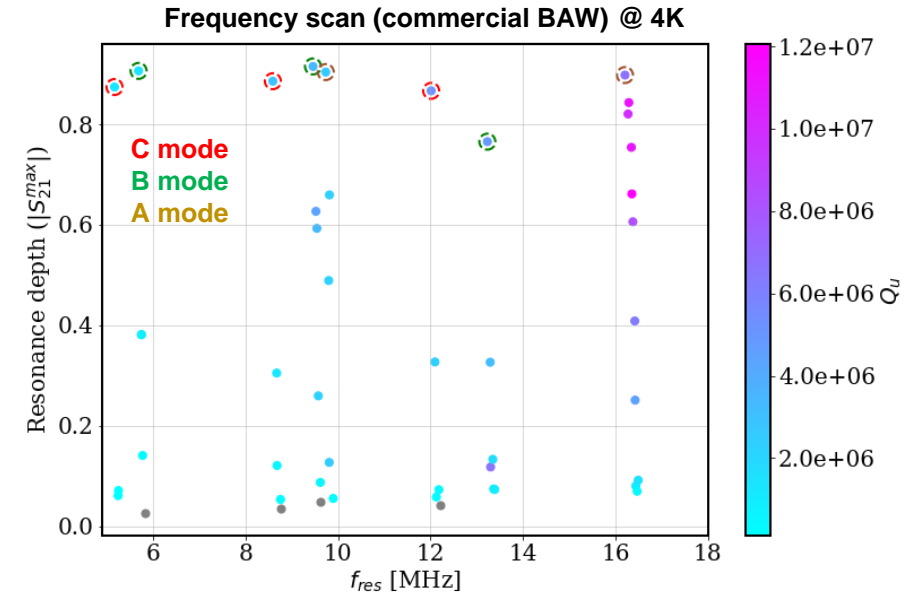
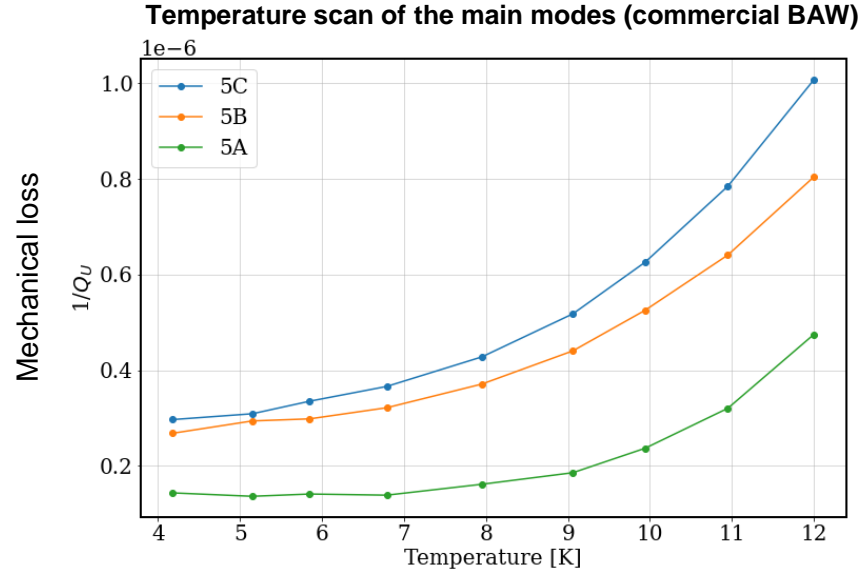


Example of a BAW Resonance fit



BAUSCIA will have its own
cryostat in the new cryogenic lab

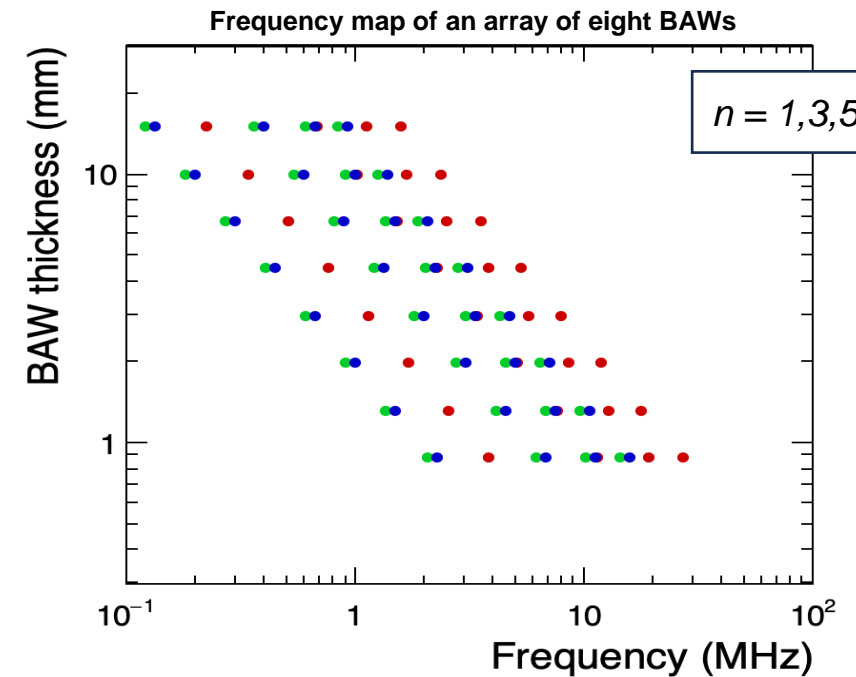
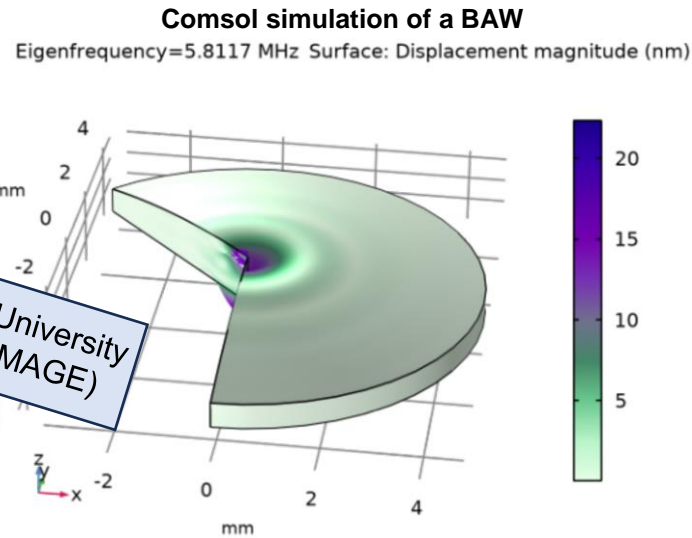
- Study of low temperature BAW behaviour



- Mechanical loss comparable to device in use at MAGE
- Ready to **setup a GW detector** to supplement MAGE measurement
 - Readout SQUIDs expected by late spring 2024
 - Expected sensitivity sufficient to compare measurements

NEXT steps: BAWs optimization

- **BAW with customized shape (curvature) and thickness**
 - Design to minimize mechanical losses for $n=1$



- **Material type and quality**
 - SiO_2 , LiNbO_3 (*), etc. in discussion with crystal manufactures

(*) See, e.g., [M. Kemp et al. Nature Comm. 1715 \(2019\)](#) for a LiNbO_3 bar of 10 cm (40 kHz) showing $Q \sim 10^6$

- **High Frequency Gravitational Waves** can provide sensitivity to **dark matter searches** complementary to other research lines
- **Broad range sensitivity** requires many BAWs of different thickness
 - Sensitivity scales as $\sim 1/n$ ($n =$ overtone)
 - Optimal sensitivity as $n=1$
- (**Easy**) We are setting up a **HF-GW detection site at Milano-Bicocca** with off-the-shelf BAWs
 - Expected sensitivity comparable to MAGE
- (**Hard**) We will design (and measure) **custom BAWs cavities** optimized for GW detection.

Further details:

- “Bulk Acoustic Wave Devices”, talk at the [Ultrahigh Frequency Gravitational Waves workshop: where to next?](#)

BACKUP

- GWs act on resonant mass (**BAW**) as a driving force, resulting in a **driven harmonic oscillator**.

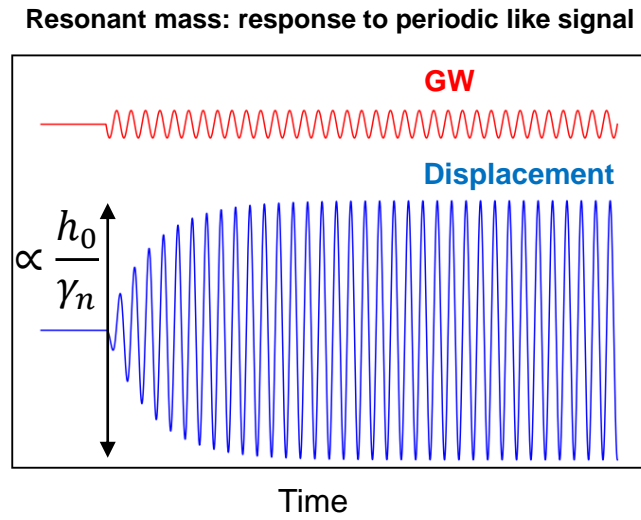
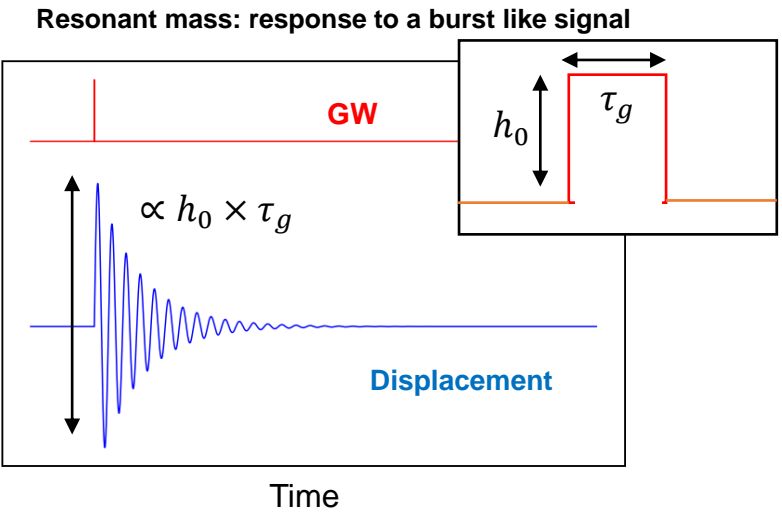
$$\ddot{\xi}_n + \gamma_n \dot{\xi}_n + \omega_n^2 \xi_n = C_n \times \frac{2L}{\pi^2} \ddot{h}_{yy}^{TT}$$

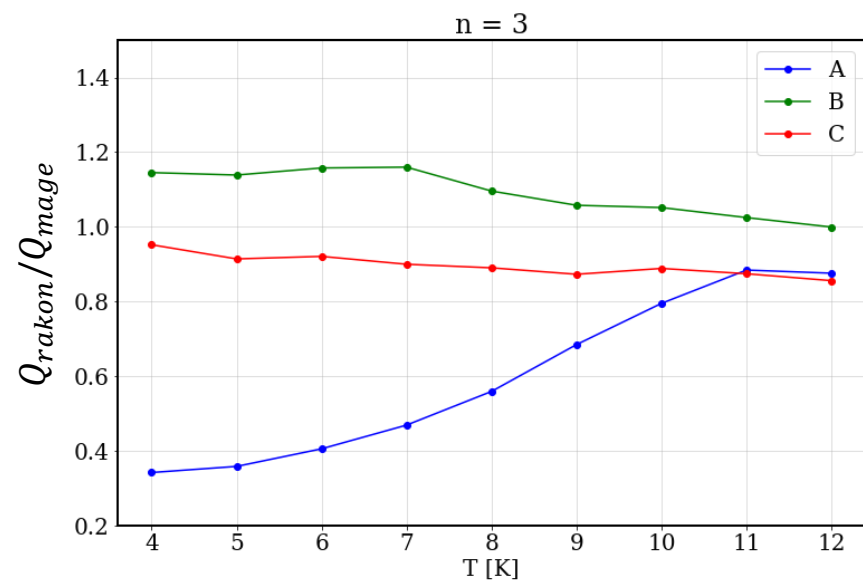
Displacement

Dissipation factor of the mode n

Resonance frequency of the mode n

The effect of GW can be described in terms of a **Newtonian force**
(If the linear size of the detector is less than the reduced wavelength of the GW)





Two detected signal from MAGE, uncertain origin

