



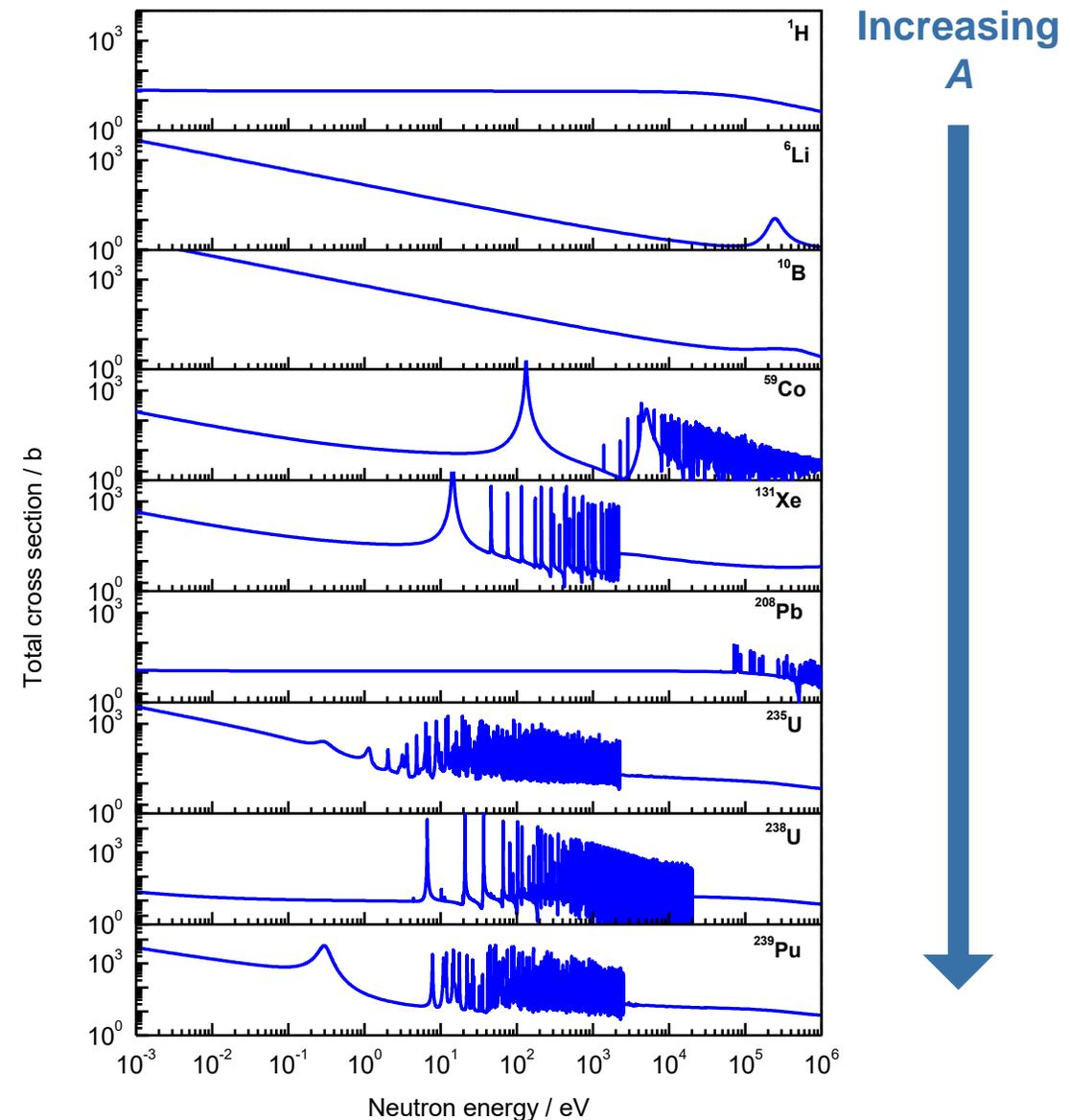
# Low energy ( $\leq 20\text{MeV}$ ) neutron interactions

# Outline

- Some neutron physics and neutron interactions below 20 MeV (small reminder above 20 MeV in passing)
- Group-wise treatment:
  - Legacy treatment
- Point-wise treatment:
  - Introduced in v4-3.0
  - Default from v4-4.0  
for DEFAULTS: NEW-DEFA, PRECISION, DAMAGE
- *Reminder: lethargy units*

# Why neutrons?

- Even when not studying a neutronics problem, neutrons can be generated as secondary particles
- They can induce significant backgrounds in detectors, e.g. via neutron capture or recoil generation
- Important for shielding considerations: high penetration (and even multiplication)
- They can activate/damage materials
- Significant even at very low energies (transport down to  $10^{-14}$  GeV in FLUKA): high-energy secondaries can be produced by near zero-energy neutrons
- Interaction probability varies wildly with neutron energy and target nucleus →
  - ...and cannot be theoretically predicted
- A special treatment is clearly required



P. Schillebeeckx et al., "Neutron Resonance Spectroscopy for the Characterisation of Materials and Objects", Report EUR 26848 EN (2014)  
[DOI: 10.2787/98278](https://doi.org/10.2787/98278)

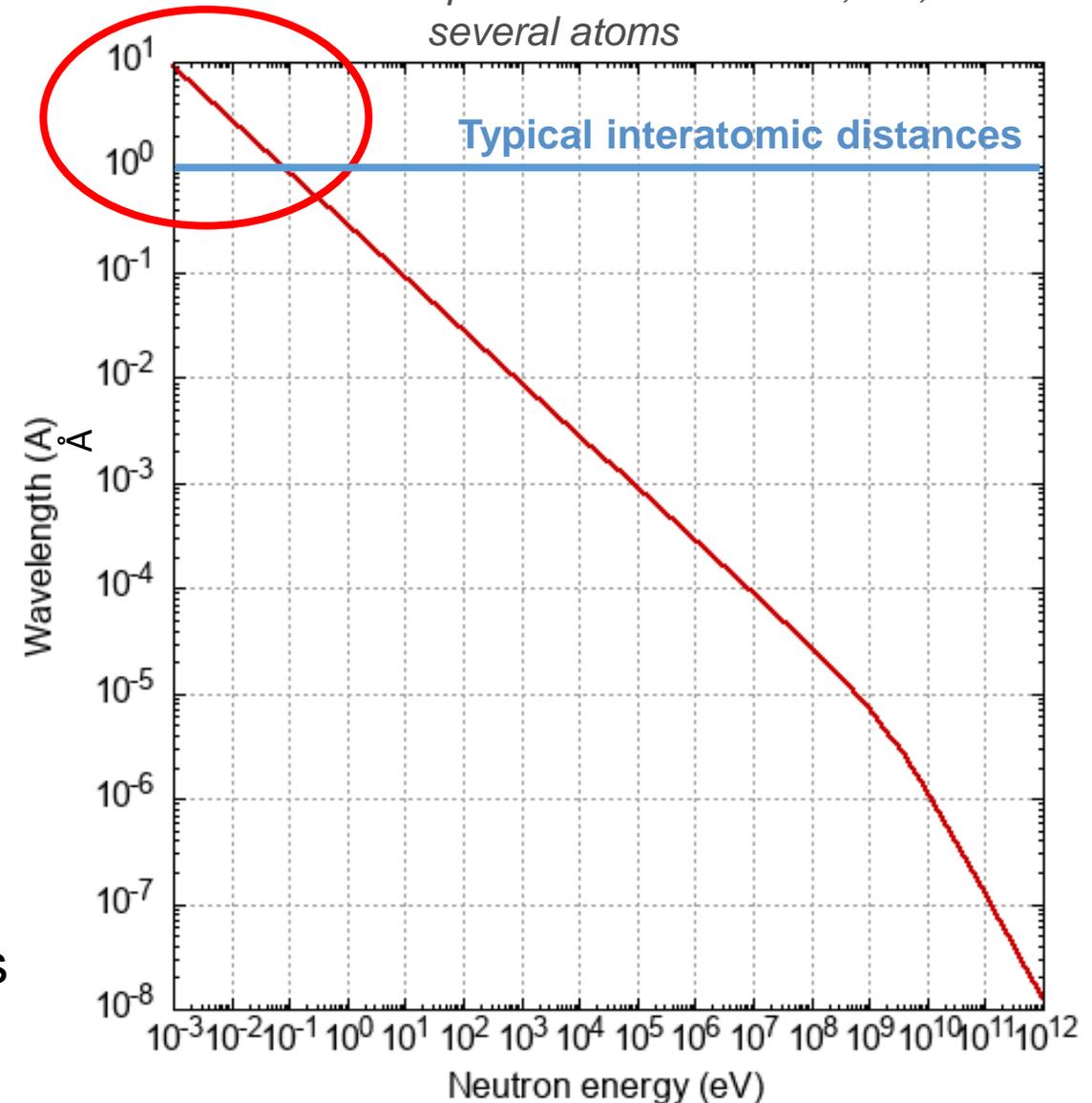
# Low-energy neutron interactions

# Neutron (n) interaction generalities

*Below 0(1) eV, neutron wavelength spreads over several Å, i.e., over several atoms*

- Neutrons **do not feel the Coulomb force**:
  - No Coulomb scattering on atoms
  - No interaction with target electrons (no  $dE/dx$ )
  - No Bremsstrahlung
- They **feel the strong force** (nuclear interaction):
  - Elastic scattering: (n,el)
  - Capture: (n, $\gamma$ )
  - Fission: (n,f)
  - Inelastic channels: (n,n'),(n,p),(n,2n),(n,d),(n,a)...
- Below  $\sim$ eV energies, they:
  - become sensitive to local atomic arrangement
  - scatter coherently on molecules / crystal lattice
  - thermal scattering laws  $S(\alpha,\beta,T)$
- Spin-1/2: neutrons probe magnetic/spin densities in matter\*

\* usually not accounted for in MC codes



# Neutron interactions in FLUKA - in a nutshell

- Above 20 MeV, neutrons are treated in FLUKA on equal footing with other hadrons:
  - **Nuclear elastic** scattering: based on the Ranft model (*J. Ranft, Part. Acc. 3 129-161, 1972*)
  - **Nuclear inelastic** interactions: FLUKA's hadron-nucleus reaction model (PEANUT)
- Below 20 MeV (“**low energy neutrons**” in FLUKA slang), cross sections exhibit a rich structure of **resonances**:
  - No effective model to capture/describe resonances in a systematic way
  - One must resort to evaluated nuclear data (for both group- and point-wise approaches, see below)
- Neutron **decay** (mean life-time of 879.6 s, *i.e.* about 15 min):  $n \rightarrow p + e^- + \bar{\nu}_e$
- **Gravitational** effects\* (meV n over 100s of m, e.g. in time-of-flight experiments)

\* not modelled in FLUKA

# Neutron moderation

- Neutrons are “**moderated**” (*i.e.* their kinetic energy is progressively reduced) through successive scattering with the surrounding nuclei in which a fraction of the energy is transferred to the nucleus
- An ideal neutron **moderator** has **low atomic mass** (to maximise energy transfer per collision), a **high neutron scattering cross section** (to maximise collisions), a **low neutron capture cross section** (to reduce depletion of the neutron population) and is resistant to high levels of radiation
  - Typically in reactors: light/heavy water ( $^1\text{H}$  and  $^2\text{H}$ ) (and  $^{16}\text{O}$  present), carbon (graphite)  $^{12}\text{C}$
- Eventually, neutrons are “**thermalised**”

# Neutron thermalisation

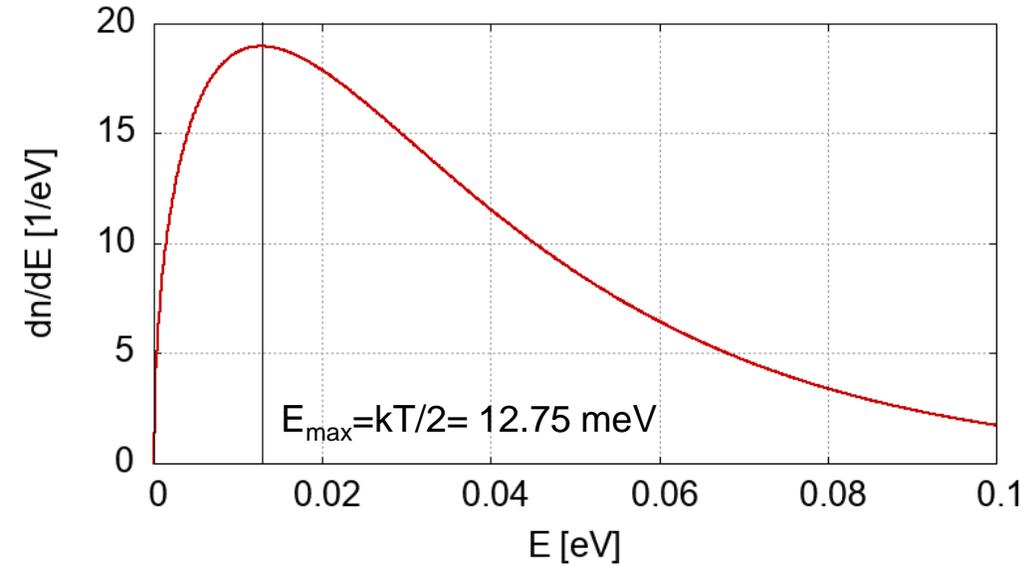
- Thermal motion energy:  $O(kT)$
- **At 296 K,  $kT=25.5$  meV**
- At/near these energies, neutrons collide elastically (losing or gaining energy) in a “gas” of nuclei, eventually reaching **thermal equilibrium**
- The energy distribution of non-relativistic classical particles in thermodynamic equilibrium at temperature  $T$  is given by the **Maxwell-Boltzmann distribution**:

$$\frac{dn}{dE} = 2\sqrt{\frac{E}{\pi}} \left(\frac{1}{kT}\right)^{3/2} e^{-E/kT} \quad \operatorname{argmax}(E) = \frac{kT}{2}$$

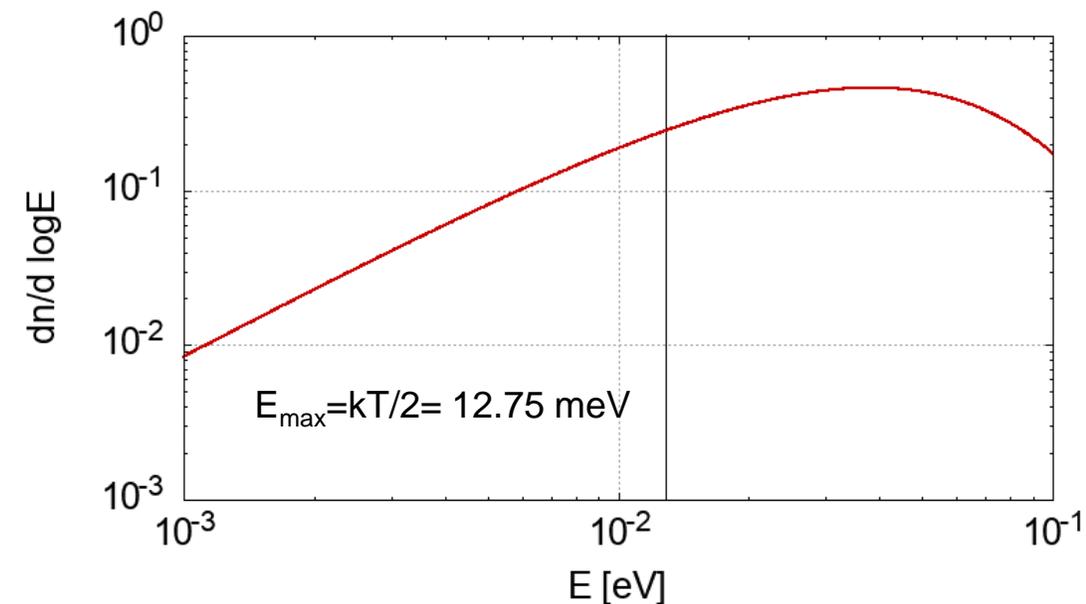
- In **lethargy representation\***, maximum shifts to higher energies

*\* recall the scoring lecture, and see later*

Maxwell-Boltzmann distribution at 296 K



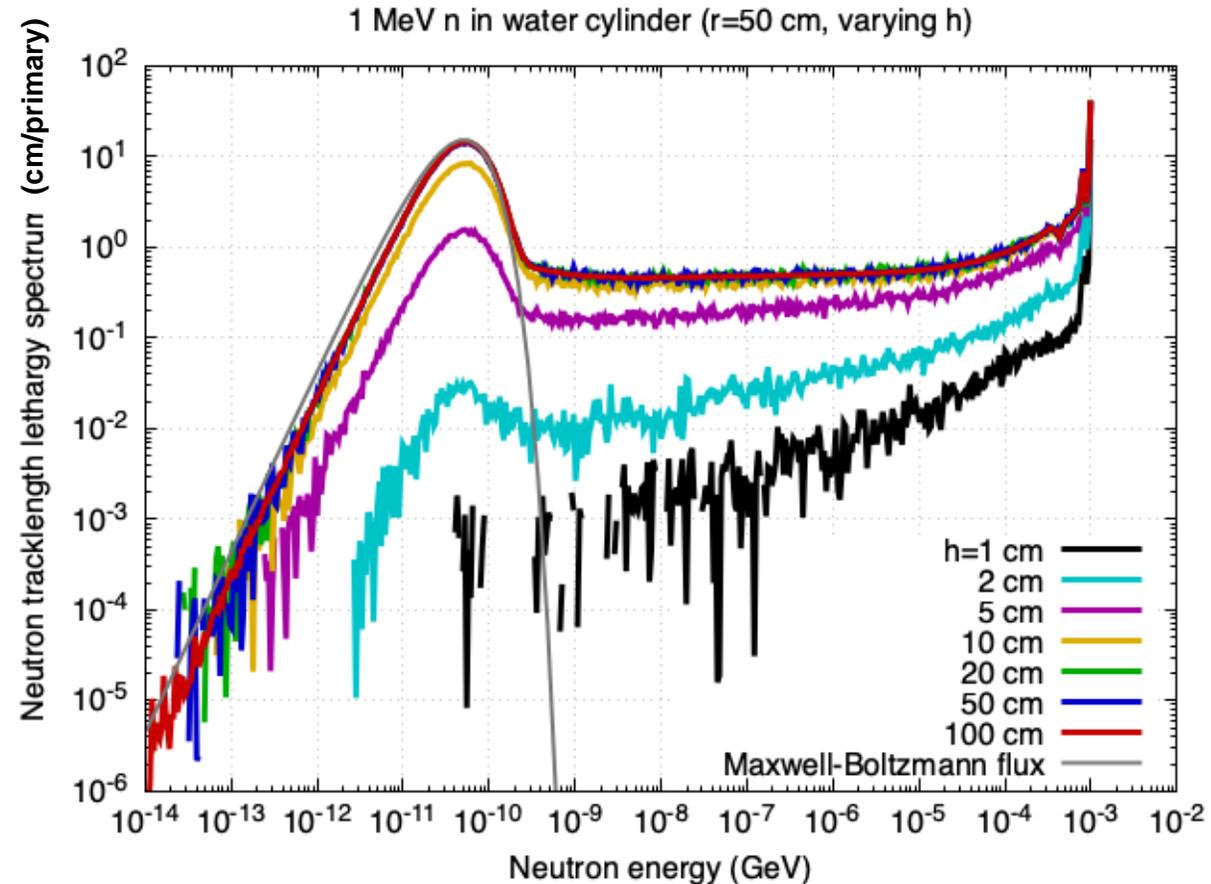
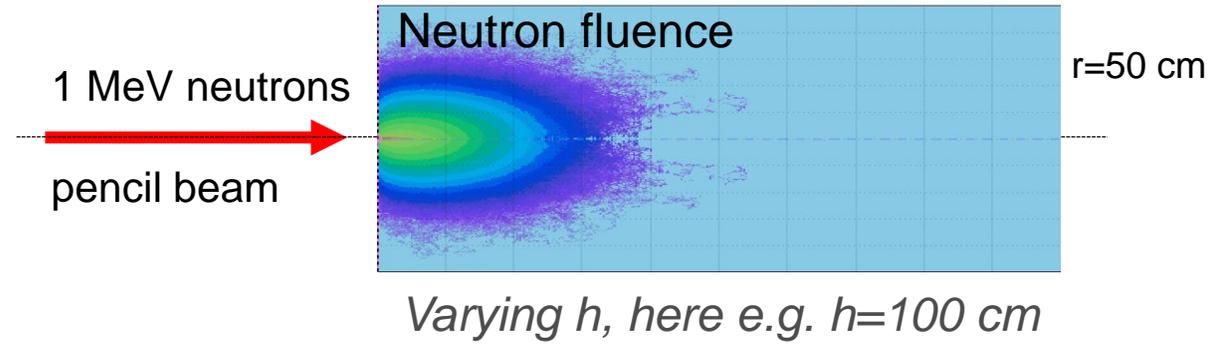
Maxwell-Boltzmann distribution at 296 K (lethargy)



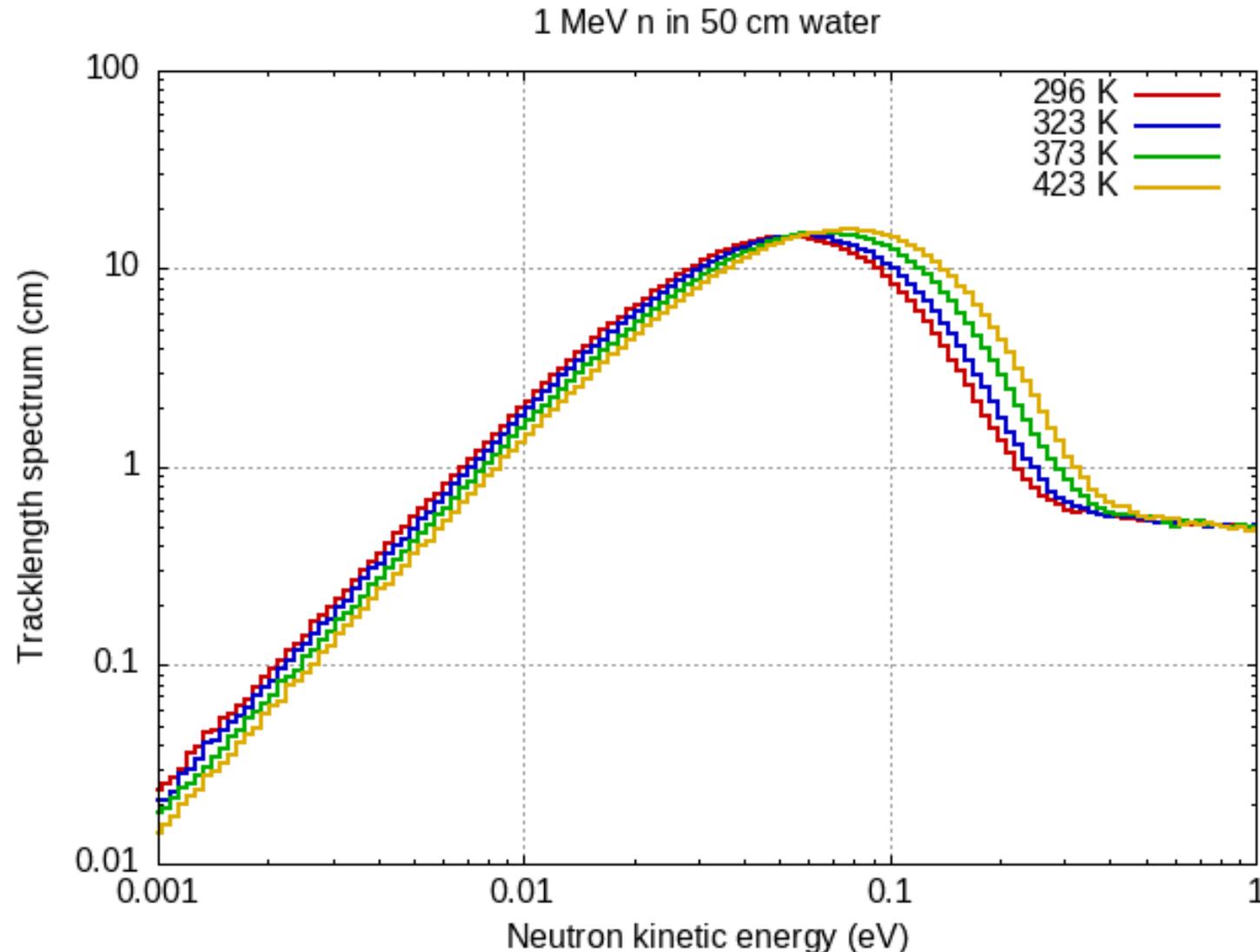
# Thermalisation in H<sub>2</sub>O

- Example: n pencil beam, E=1 MeV, impinging on a water cylinder (r=50 cm, varying h)
  - $\lambda_{(n,el)}(1 \text{ MeV}) = 3.5 \text{ cm}$  (in water)
  - **For  $h \ll \lambda_{(n,el)}$ , n barely scatter**
  - **For  $h \sim \lambda_{(n,el)}$ , n start to scatter elastically:**
    - Change direction (possibly staying longer in the cylinder)
    - Lose energy: possibly probing energy ranges where (n,el) cross section drastically increases
  - **For  $h \gg \lambda_{(n,el)}$ :**
    - Intensive elastic scattering
    - Thermal equilibrium: Maxwell-Boltzmann flux\*:
- $$\frac{d\Phi}{dE} = \frac{dn}{dE} v(E) = 2^{3/2} \frac{E}{\sqrt{m\pi}} \left( \frac{1}{kT} \right)^{3/2} e^{-E/kT}$$
- (n, $\gamma$ ) on either <sup>1,2</sup>H or <sup>16,17,18</sup>O eventually consumes the neutron flux in favor of MeV photons

\* Small detail discussed later: S( $\alpha,\beta,T$ )



# Thermalisation at different temperatures



- The thermal peak indeed shifts linearly with the temperature
- Energies below about O(1) eV are loosely called “**thermal**”

# Neutron reactions of interest

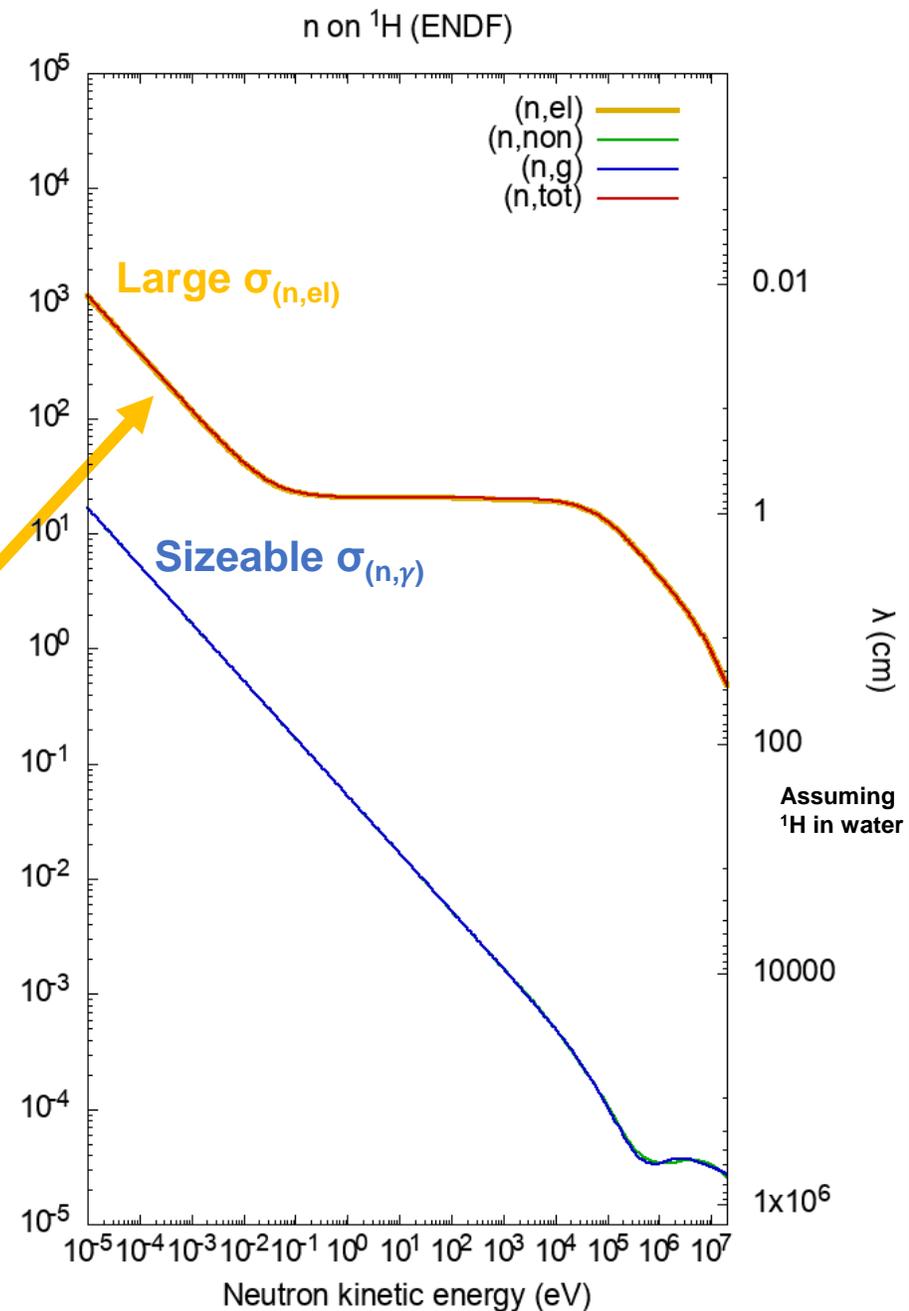
$^1\text{H}(n,\text{el})$  |  $^2\text{H}(n,\text{el})$  |  $^{10}\text{B}(n,\alpha)$  |  $^{\text{nat}}\text{Cd}(n,\gamma)$  |  $^{235}\text{U}(n,\text{f})$

# $^1\text{H}(n,\text{el})$

- Maximum energy transfer from  $n$  to  $^1\text{H}$ , i.e. a proton (for  $E_{\text{kin}} \ll m_n$ ):

$$E_{\text{rec,max}} = \frac{4m_p m_n E_{\text{kin}}}{(m_p + m_n)^2} \approx E_{\text{kin}}$$

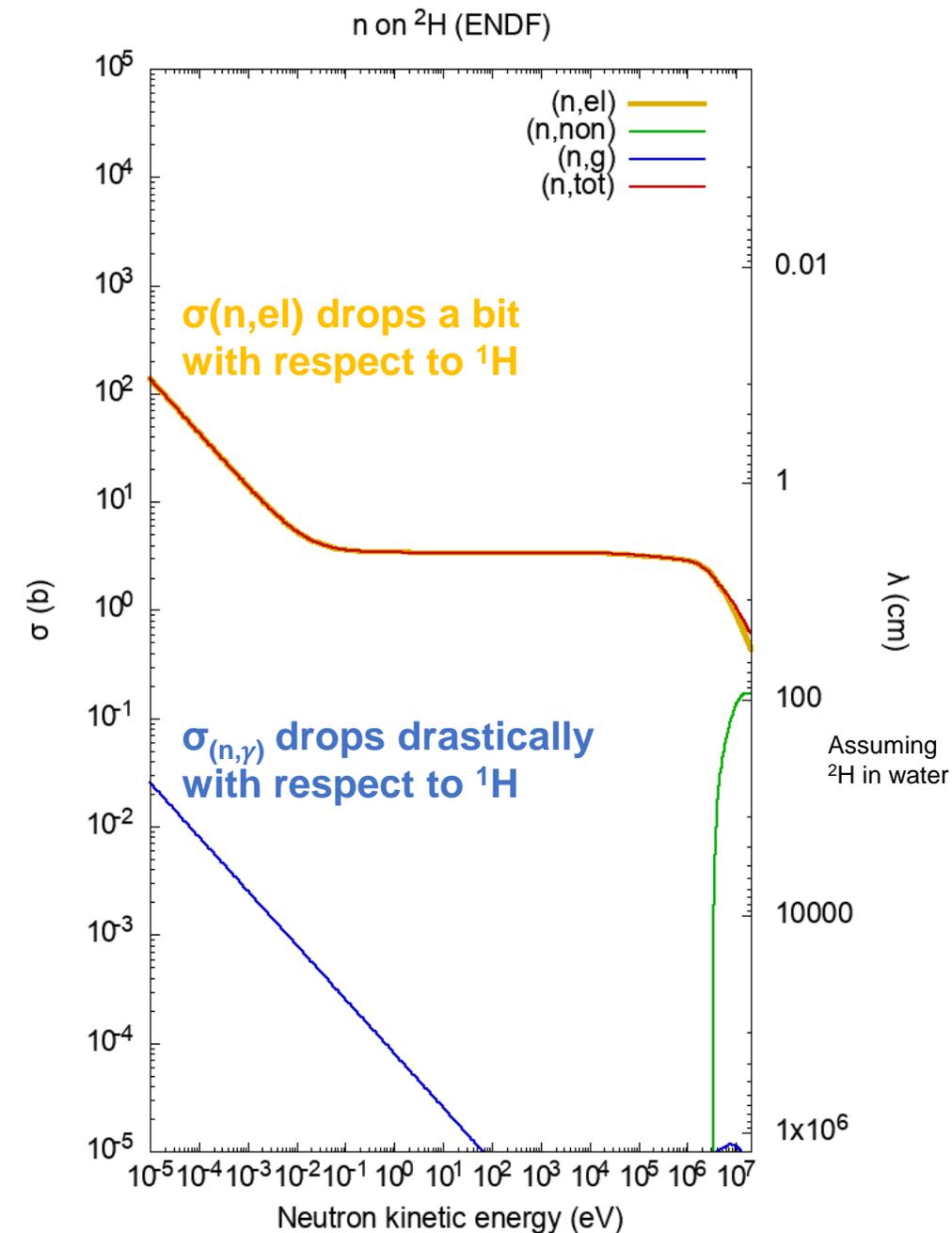
- (not necessarily the most likely energy transfer!)
- In few collisions,  $n$  have the chance to transfer a large fraction of kinetic energy to target  $^1\text{H}$
- $n$  energy quickly drops below the eV domain, where  $\sigma_{(n,\text{el})}$  increases drastically as  $1/v$ , i.e.  $1/\sqrt{E}$
- At these energies,  $\sigma_{(n,\gamma)}$  becomes sizeable: capture depletes the neutron flux generating MeV photons (!)
- One must track neutrons down to thermal energies



# $^2\text{H}(n,e)$

- We already saw: compounds containing  $^1\text{H}$  are good neutron moderators
- But  $^1\text{H}$  has a sizeable  $(n,\gamma)$  cross section. At thermal energies:
  - $\sigma_{(n,\gamma)}/\sigma_{(n,e)} \sim 10^{-2}$  for  $^1\text{H}$
  - $\sigma_{(n,\gamma)}/\sigma_{(n,e)} \sim 10^{-4}$  for  $^2\text{H}$
- For applications requiring a high thermal neutron flux, it is advantageous to employ  $^2\text{H}$  (fewer neutrons captured on the way to thermalisation)
- $^2\text{H}$  still has good moderator properties:

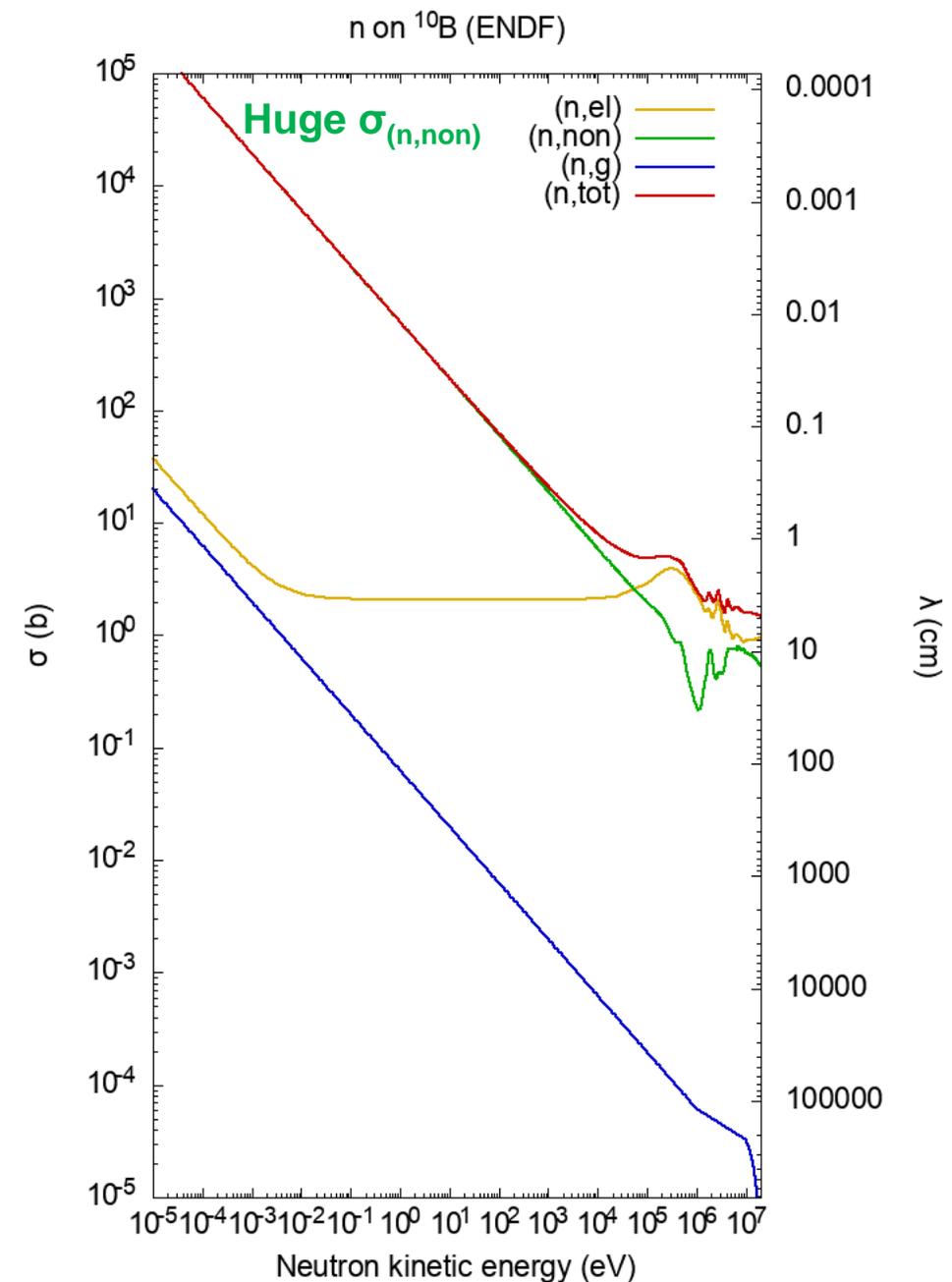
$$E_{\text{rec,max}} = \frac{4m_d m_n E_{\text{kin}}}{(m_d + m_n)^2} \approx \frac{8}{9} E_{\text{kin}}$$



# $^{10}\text{B}(n,\alpha)$

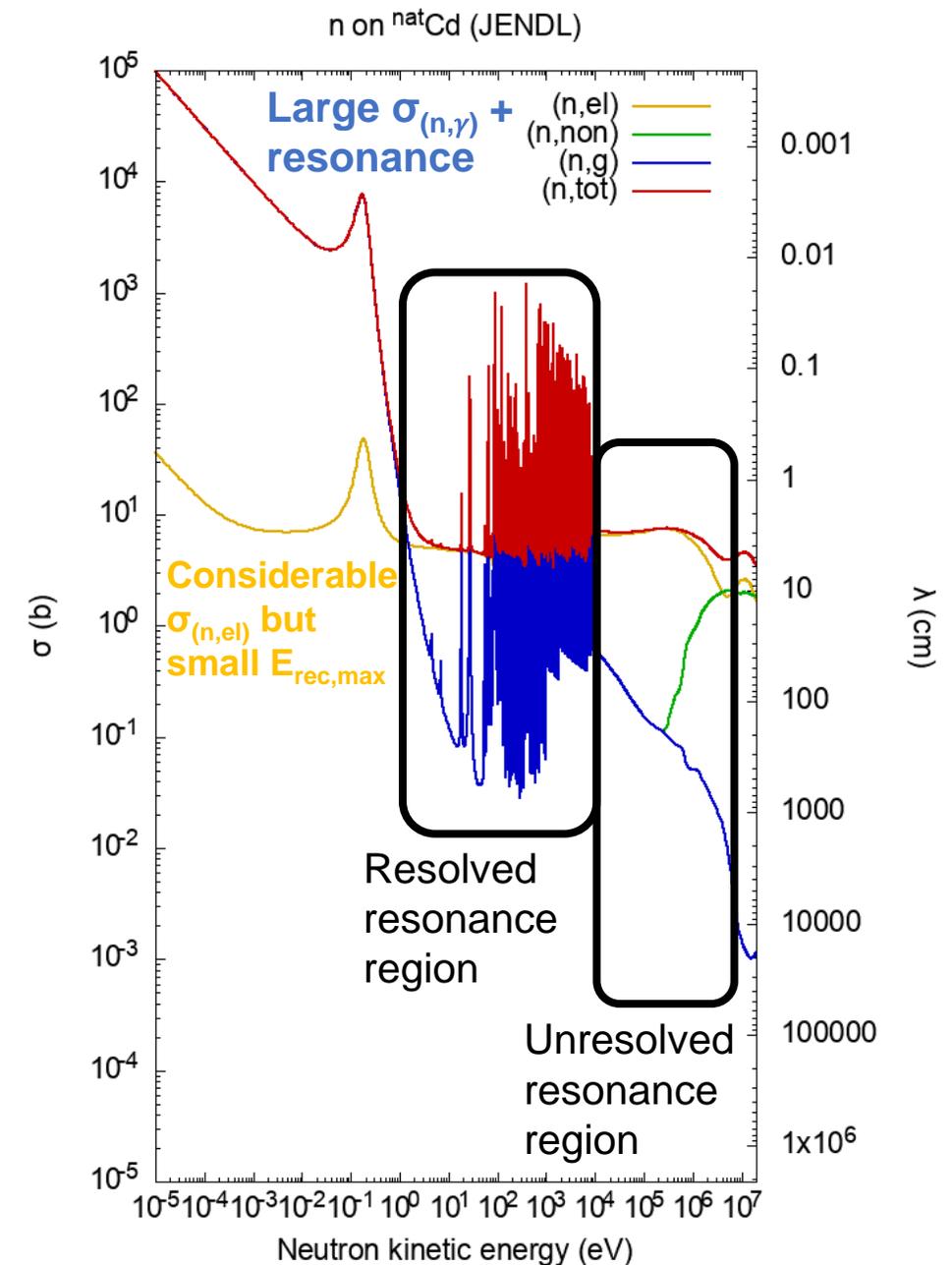
- $\sigma_{(n,\text{el})}$  is only slightly lower than for  $^1,^2\text{H}$ 
  - But:  $E_{\text{rec,max}}(n \text{ on } ^{10}\text{B}) \ll E_{\text{kin}}$
  - $^{10}\text{B}$  is not as effective a moderator as  $^1,^2\text{H}$
- However, the  $^{10}\text{B}(n,\alpha)$  channel has a very large  $\sigma$ :  
$$^{10}\text{B} + n \rightarrow ^7\text{Li} + \alpha + \gamma$$
  - $\sigma \sim 10^3 - 10^5 \text{ b}$ , i.e. mean free paths  $\ll 100 \mu\text{m}$
  - $^7\text{Li}$  and  $\alpha$  have short range ( $< 10 \mu\text{m}$ )
- Basis for various applications:
  - boron neutron capture\* therapy (BNCT)
  - boron rods in nuclear power plants to control n flux
  - borated moderators: reduction of neutron fluence and of MeV photon background from neutron capture in  $^1\text{H}$

*\*should rather be "absorption"*



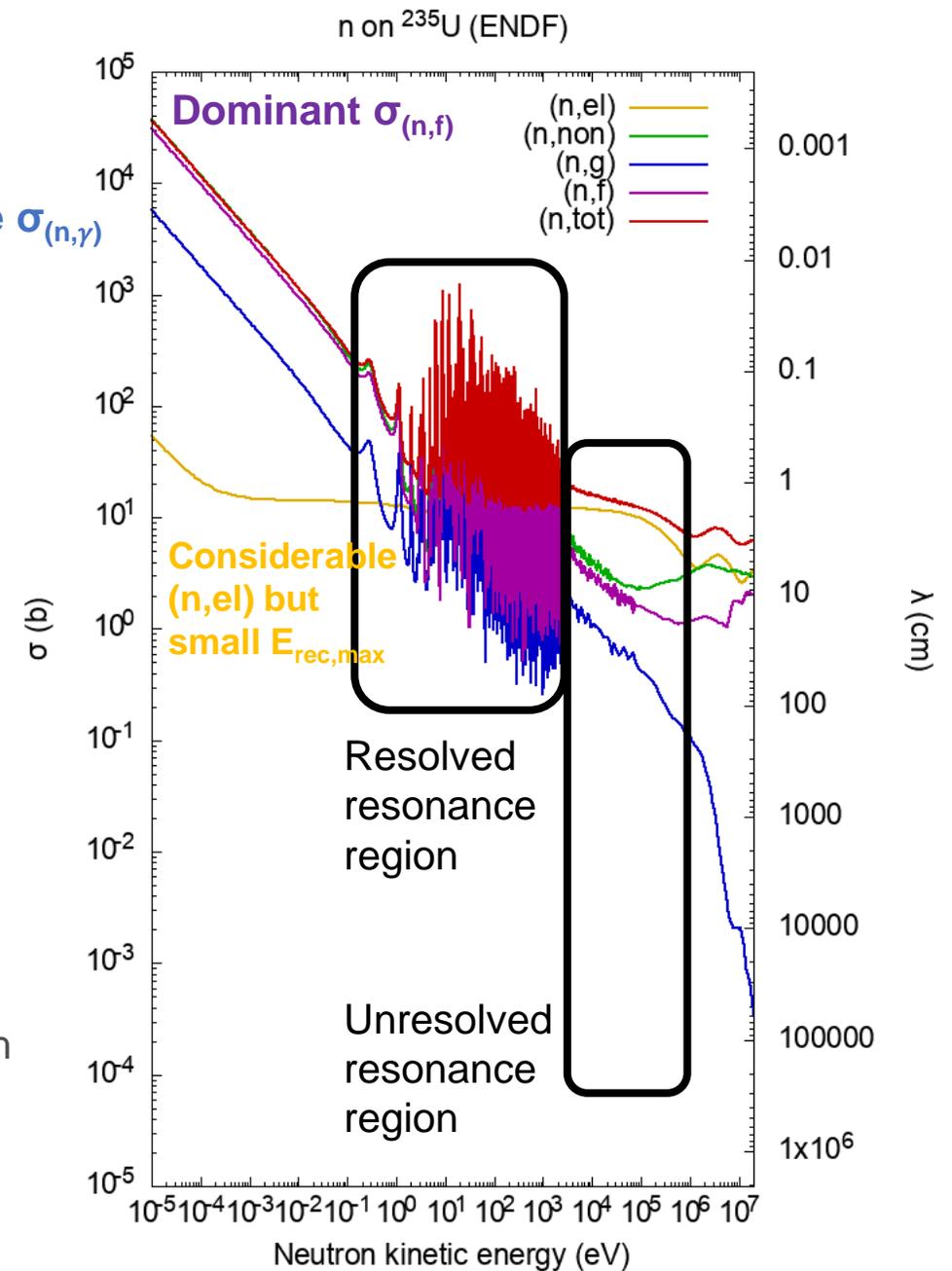
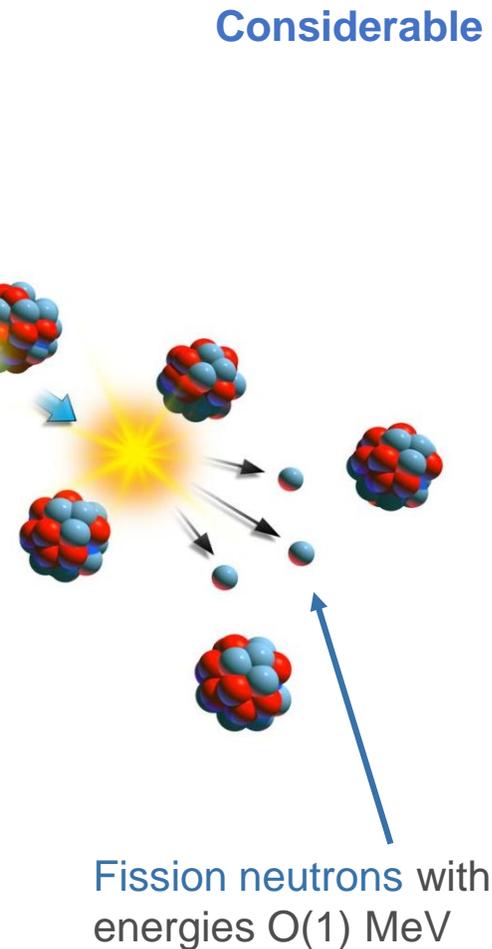
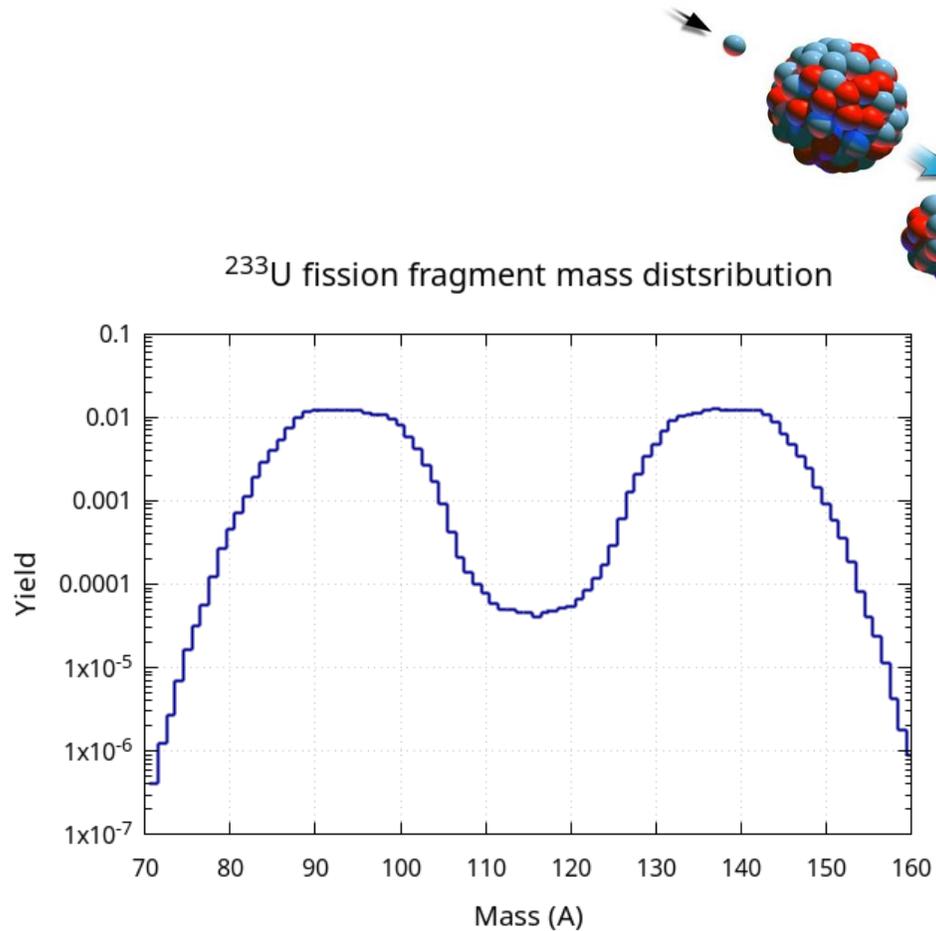
# $^{nat}\text{Cd}(n,\gamma)$

- $\sigma_{(n,\text{el})}$  is slightly lower than for  $^1,^2\text{H}$ , but  $E_{\text{rec,max}}(n \text{ on } ^{nat}\text{Cd}) \ll E_{\text{kin}}$
- $^{nat}\text{Cd}$  is less effective than  $^1,^2\text{H}$  as a moderator
- $(n,\gamma)$  dominates at energies below 1 eV:
  - Resonance (thousands of barns!) at  $\sim 0.2$  eV
  - Mean free paths  $\ll 100 \mu\text{m}$  (!)
- neutrons with energies below eV are promptly converted into photons of O(100 keV)-O(10 MeV)
- Resonances:
  - Present in neutron cross sections in all but the lightest nuclei
  - Resolved vs unresolved resonance region



# $^{235}\text{U}(n,f)$

- For heavy targets (n,f) tends to dominate at thermal energies

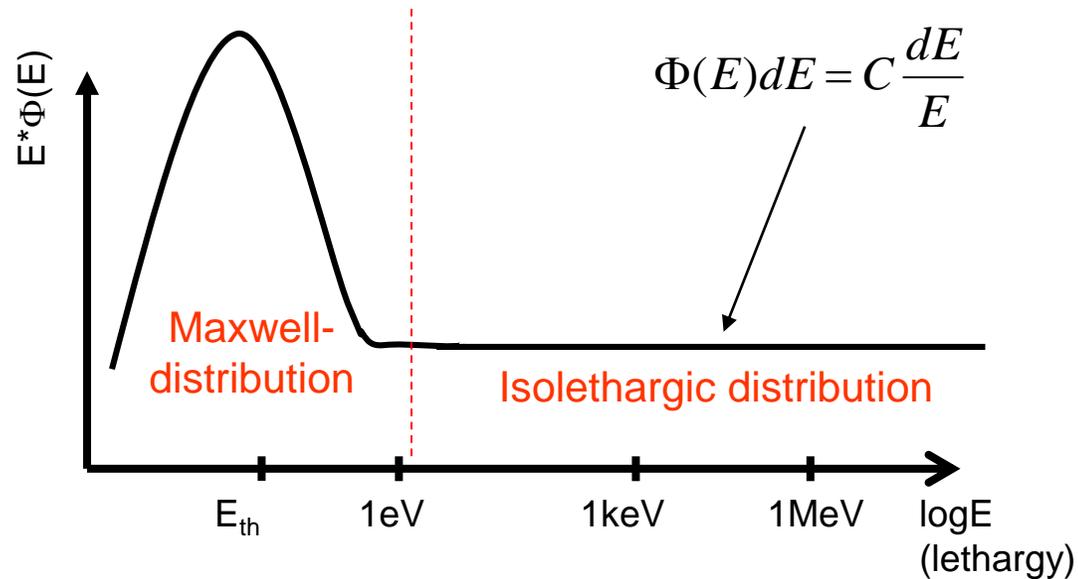


# Group-wise treatment of neutron interactions below 20 MeV in FLUKA

The legacy approach

# Group-wise approach

- Energy scale is divided into  $i=1, \dots, 260$  fixed bins (**groups**)
- At each group, cross sections from evaluated nuclear databases (ENDF, JEFF, JENDL...) are averaged over a typical neutron fluence:



$$\langle \sigma_i \rangle = \frac{\int_{E_{i,low}}^{E_{i,high}} \sigma(E) \Phi(E) dE}{\int_{E_{i,low}}^{E_{i,high}} \Phi(E) dE}$$

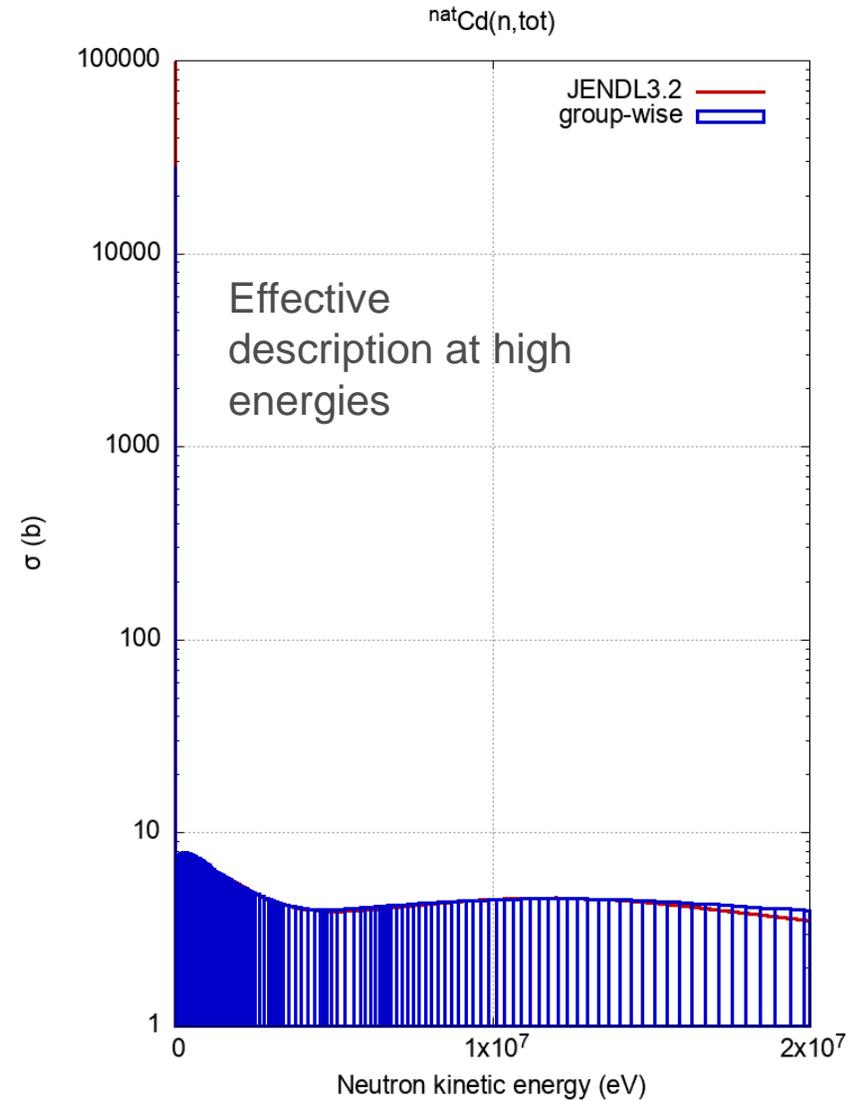
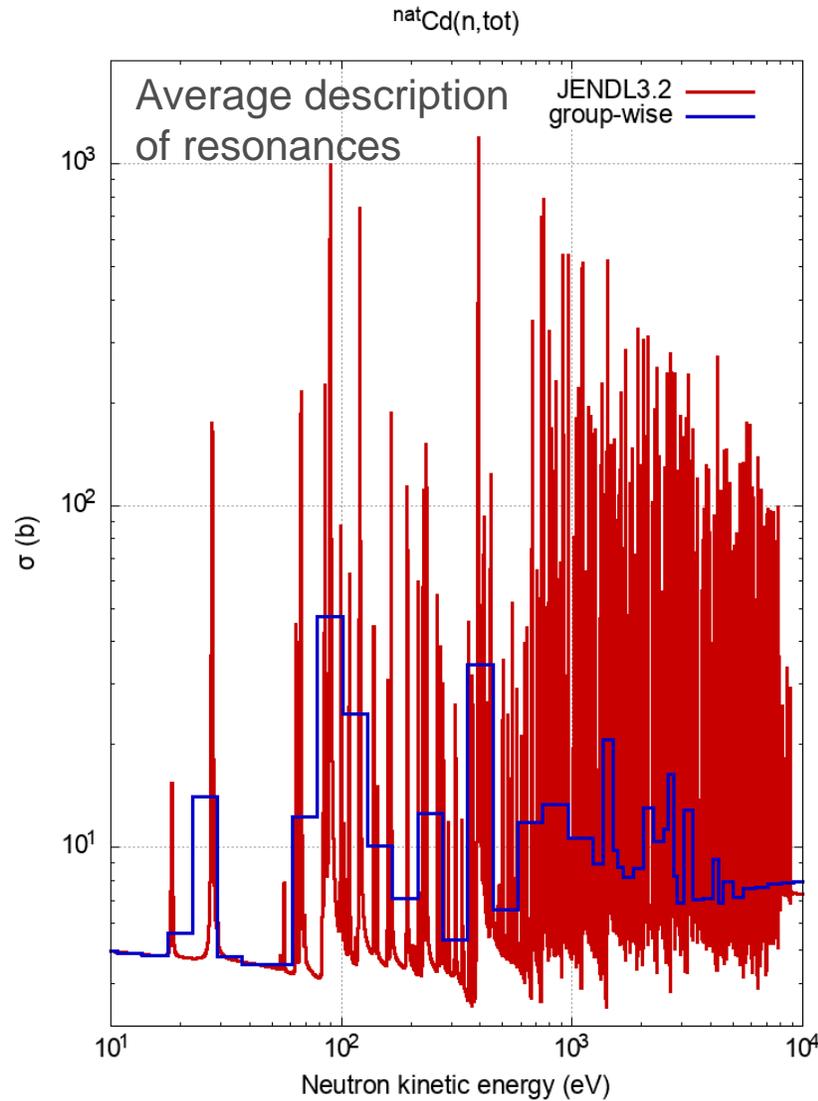
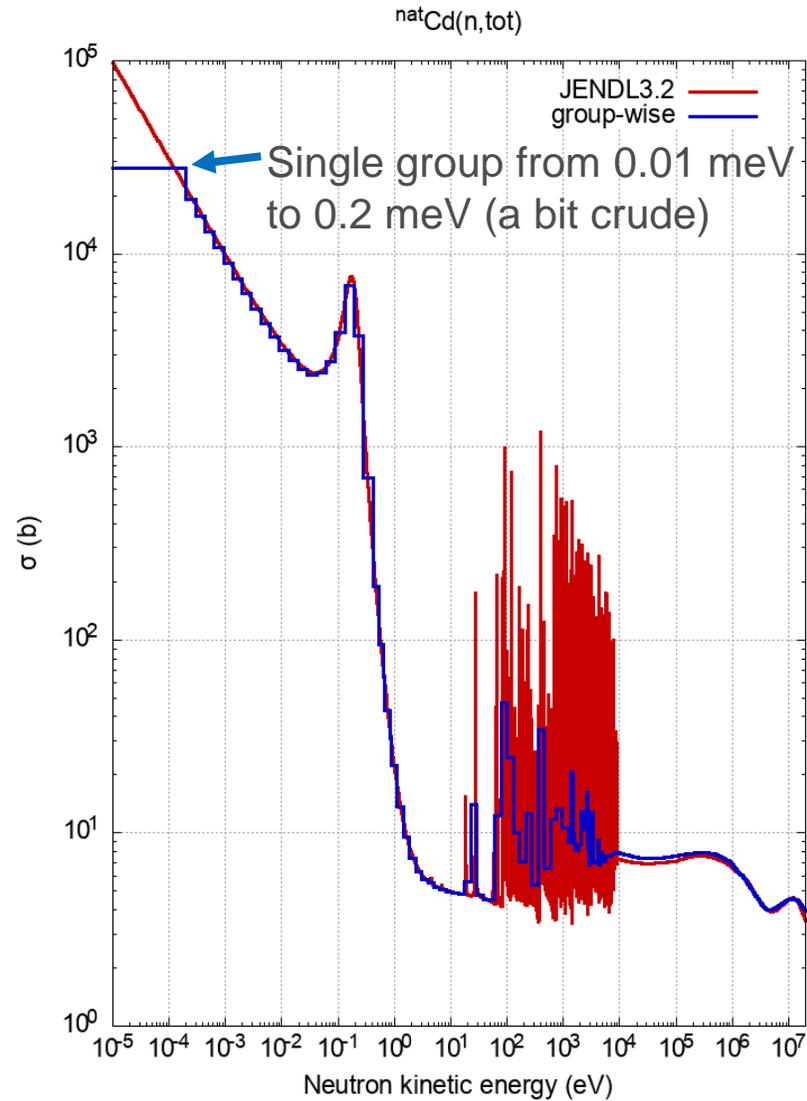
- Energy (**continuous variable**) becomes a group index  $g$  (**discrete variable**)
- Effect: continuous cross sections become histograms

# Low-energy neutron groups in FLUKA

- Highest energy group index: 1
- Lowest energy group index: 260
- All energy-resolved quantities involving low-energy neutrons default to this fixed binning
- This affects USRTRACK, USRBDX, USRYIELD, USRCOLL

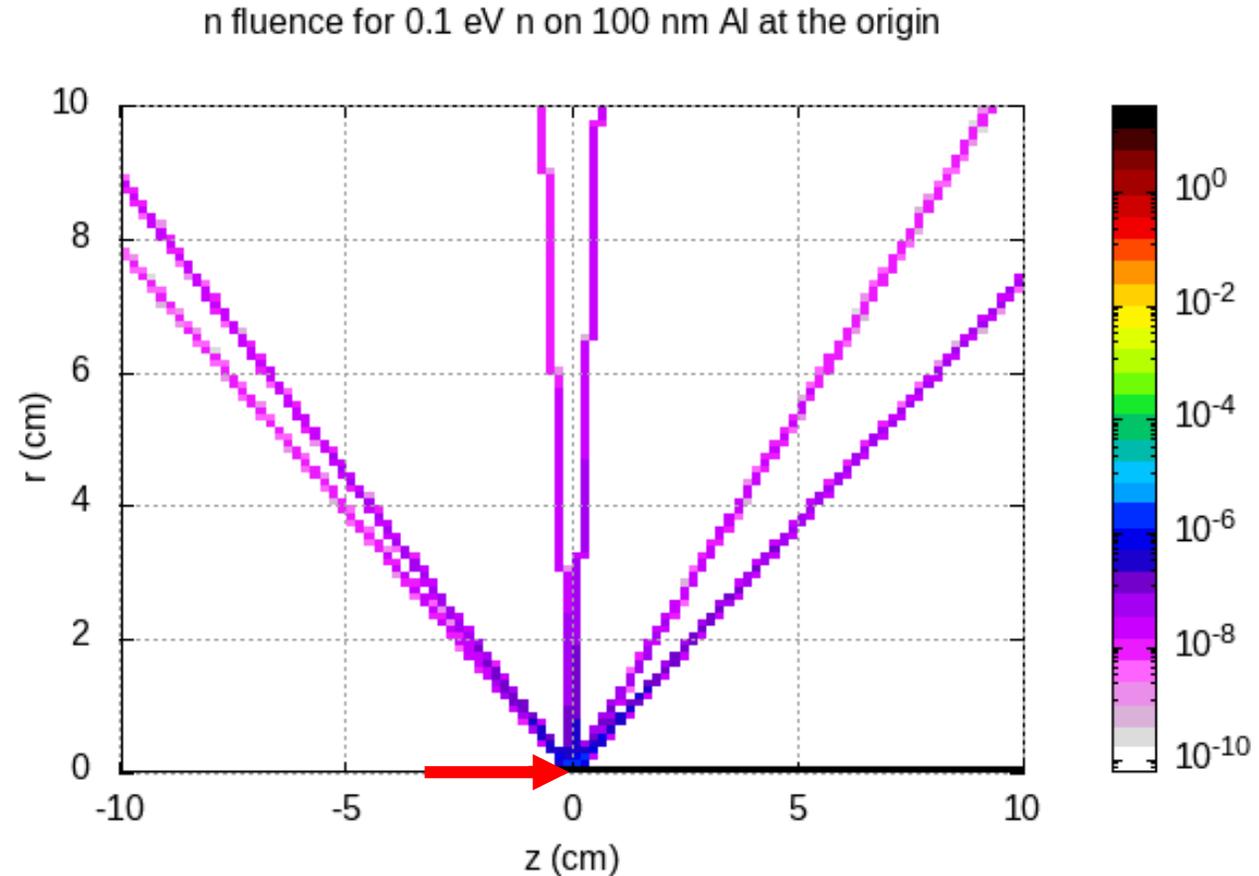
#	Group	Elow (GeV)	Ehigh(GeV)
	1	1.9640E-02	2.0000E-02
	2	1.9155E-02	1.9640E-02
	3	1.8683E-02	1.9155E-02
	4	1.8221E-02	1.8683E-02
	5	1.7771E-02	1.8221E-02
	6	1.7333E-02	1.7771E-02
	7	1.6905E-02	1.7333E-02
	8	1.6487E-02	1.6905E-02
	9	1.6080E-02	1.6487E-02
	10	1.5683E-02	1.6080E-02
	(...)		
	250	6.2118E-12	9.0994E-12
	251	4.2405E-12	6.2118E-12
	252	2.8948E-12	4.2405E-12
	253	1.9761E-12	2.8948E-12
	254	1.3490E-12	1.9761E-12
	255	9.2092E-13	1.3490E-12
	256	6.2867E-13	9.2092E-13
	257	4.2917E-13	6.2867E-13
	258	2.9297E-13	4.2917E-13
	259	2.0000E-13	2.9297E-13
	260	1.0000E-14	2.0000E-13

# Group-wise cross sections



# Angular distributions

- (n,e) and reaction channels with secondary neutrons are described in terms of an **up/down-scattering matrix**  $M_{gg'}$ , providing the likelihood for a neutron to transition from group  $g$  to group  $g'$ :
  - $E_{g'} > E_g$ : up-scattering (thermal neutrons!)
  - $g' = g$ : in-scattering
  - $E_{g'} < E_g$ : downscattering
- Several  $g'$  may be accessible to a given  $g$
- For a given  $g \rightarrow g'$  transition, the **continuous distribution of polar scattering angles is discretised into 3 possible directions** (respecting first 6 moments of the original distribution)



*Two  $g \rightarrow g'$  transitions happened to be accessible here, hence two groups of 3 outgoing directions*

# Other aspects of FLUKA's group-wise treatment

- **Charged secondaries** from low-energy neutron interactions **are not produced**
  - Except for **few selected channels**, among which  $^1\text{H}(n,\text{el})$ ,  $^{10}\text{B}(n,\text{a})$ ,  $^{14}\text{N}(n,\text{p})$
  - Their energy is deposited locally via *kerma factors*
- Gamma generation from  $(n,\gamma)$  and  $(n,n')$  accounted for (42 groups, 1 keV - 50 MeV), correlated only for a few isotopes. Photon energy sampled uniformly in group, transport is done in EMF module
- **Uncorrelated sampling of residual nucleus** from average distribution
- Cross sections available at a few database temperatures (**no arbitrary material temperature**)
- The group-wise approach **is not applicable** to event-by-event analyses, detector simulations, applications sensitive to details of a particular cross section resonance, a specific temperature not contained in the database, etc.
- But it has its merits:
  - It is **fast** and has **small memory requirements**
  - It is sufficient for some applications, e.g. to score energy deposition in thick materials

# Group-wise low-energy neutron interactions in FLUKA

- Group-wise cross sections available for a series of materials:

[https://flukafiles.web.cern.ch/manual/chapters/low\\_energy\\_neutrons/multigroup\\_neutron\\_transport/neutron\\_cross\\_section\\_library/available\\_cross\\_sections.html](https://flukafiles.web.cern.ch/manual/chapters/low_energy_neutrons/multigroup_neutron_transport/neutron_cross_section_library/available_cross_sections.html)

Table 8 Available low-energy neutron groupwise cross sections

Material		Temp.	Source	RN	Name	Identifiers			GP
H	H <sub>2</sub> O bound natural Hydrogen	296 K	ENDF/B-VIIR0	✓	HYDROGEN	1	-2	296	✓
H	CH <sub>2</sub> bound natural Hydrogen	296 K	ENDF/B-VIIR0	✓	HYDROGEN	1	-3	296	✓
(…)									
Fe	Natural Iron	296 K	ENDF/B-VIR8	✓	IRON	26	-2	296	✓
Fe	Natural Iron	87 K	ENDF/B-VIR8	✓	IRON	26	-2	87	✓
Fe	Natural Iron	4 K	ENDF/B-VIR8	✓	IRON	26	-2	4	✓
Fe	Natural Iron	430 K	ENDF/B-VIR8	✓	IRON	26	-2	430	✓
(…)									
<sup>241</sup> Am	Americium 241	296 K	ENDF/B-VIIR0	✓	241-AM	95	241	296	✓
<sup>241</sup> Am	Americium 241	87 K	ENDF/B-VIIR0	✓	241-AM	95	241	87	✓
<sup>243</sup> Am	Americium 243	296 K	ENDF/B-VIIR0	✓	243-AM	95	243	296	✓
<sup>243</sup> Am	Americium 243	87 K	ENDF/B-VIIR0	✓	243-AM	95	243	87	✓

- Processed from ENDF, JENDL, JEFF
- Available at 296 K, and at a few fixed temperatures for selected materials

# Using FLUKA's group-wise library

- Every FLUKA material (except VACUUM and BLCKHOLE) must be assigned to a group-wise library material
- If 'FLUKA material name' = 'group-wise library material name', the association is automatic
- Otherwise, the **LOW-MAT** card must be used:

<b>MATERIAL</b>	Name: SODIU_87	#	p: 0.97
Z: 11	Am: 22.99	A:	dE/dx: ▼
<b>LOW-MAT</b>	Mat: SODIU_87 ▼	LowMat: 23Na. Sodium 23, 87K ▼	

- The first match of FLUKA material name to group-wise library material name present in the input is taken into account

# Point-wise treatment of neutron interactions below 20 MeV in FLUKA

General treatment introduced in FLUKA v4-3.0

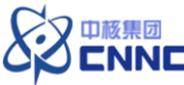
Default from v4-4.0 for DEFAULTs: NEW-DEFA, PRECISION, DAMAGE

See V. Vlachoudis et al., *Recent developments in the point wise neutron treatment for FLUKA v4*, EPJ WoC 284 (2023) 03021 [doi.org/10.1051/epjconf/202328403021](https://doi.org/10.1051/epjconf/202328403021)

# Point-wise interactions in FLUKA

- Nearly direct sampling from evaluated nuclear data libraries:

- **JEFF** (Joint Evaluated Fission and Fusion library): <https://www.oecd-nea.org/dbdata/jeff/>
- **ENDF** (Evaluated Nuclear Data Files): <https://www-nds.iaea.org/exfor/endl.htm>
- **JENDL** (Japanese Evaluated Nuclear Data Library): <https://www.ndc.jaea.go.jp/jendl/jendl.html>
- **CENDL** (Chinese Evaluated Nuclear Data Library): [https://en.cnc.com.cn/2020-06/17/c\\_501119.htm](https://en.cnc.com.cn/2020-06/17/c_501119.htm)
- **BROND** (Russian evaluated neutron data library): <https://vant.ippe.ru/en/brond-3-1>



- FLUKA's point-wise code implementation relies on the G4NDL data:



## **Evaluated neutron cross section libraries for the GEANT4 code (v2.0, 17/05/2018)**

**Emilio Mendoza and Daniel Cano-Ott, Centro de Investigaciones Energéticas, Medioambientales y Tecnológicas (CIEMAT), Spain**

# FLUKA point-wise data libraries

- Due to large size, the neutron data libraries are provided as **separate packages to download\***, installed in `${FlukaDir}/data/neutron/` :

BROND-2.2	ENDF-VII0	JEFF31N	JENDL-4.0
BROND-3.1	ENDF-VII.1	JEFF-3.2	JENDL-4.0u
CENDL-31	ENDF-VIII0	<b>JEFF-3.3</b>	JENDL-5.0
ENDF-VI8	JEFF30N	JENDL330	TENDL21

- The **default** point-wise library for FLUKA v4-4.0 is **JEFF-3.3**
- Older evaluations are also provided for comparison purposes
- Thermal Scattering Law  $S(\alpha,\beta,T)$  for several materials

\* <https://fluka.cern/download/neutron-data-libraries>

- **Directory structure:**

- **Elastic/**
  - CrossSection/
  - FS/
- **Capture/**
  - CrossSection/
- **Inelastic/**
  - ...
- **Fission/**
  - ...
- **ThermalScattering/**
  - Coherent/
  - Incoherent/
  - Inelastic/

Containing one file per isotope, per channel, cross section, and final state

# Point-wise interaction libraries used by FLUKA

- Interactions are divided into 4 kinds:
  - Elastic: (n,el)
  - Capture: (n, $\gamma$ )
  - Inelastic
    - Further subdivided into 36 channels, e.g. (n,n'), (n,p), (n,d), (n, $^3\text{He}$ ), (n, $\alpha$ )
  - Fission: (n,f)
    - Fission fragments from database if present, otherwise Wahl [1] systematics
- All isotopes have (n,el) and (n, $\gamma$ ), as well as inelastic channels (typically open at high energies, with a few exceptions)
- A few isotopes have a fission channel

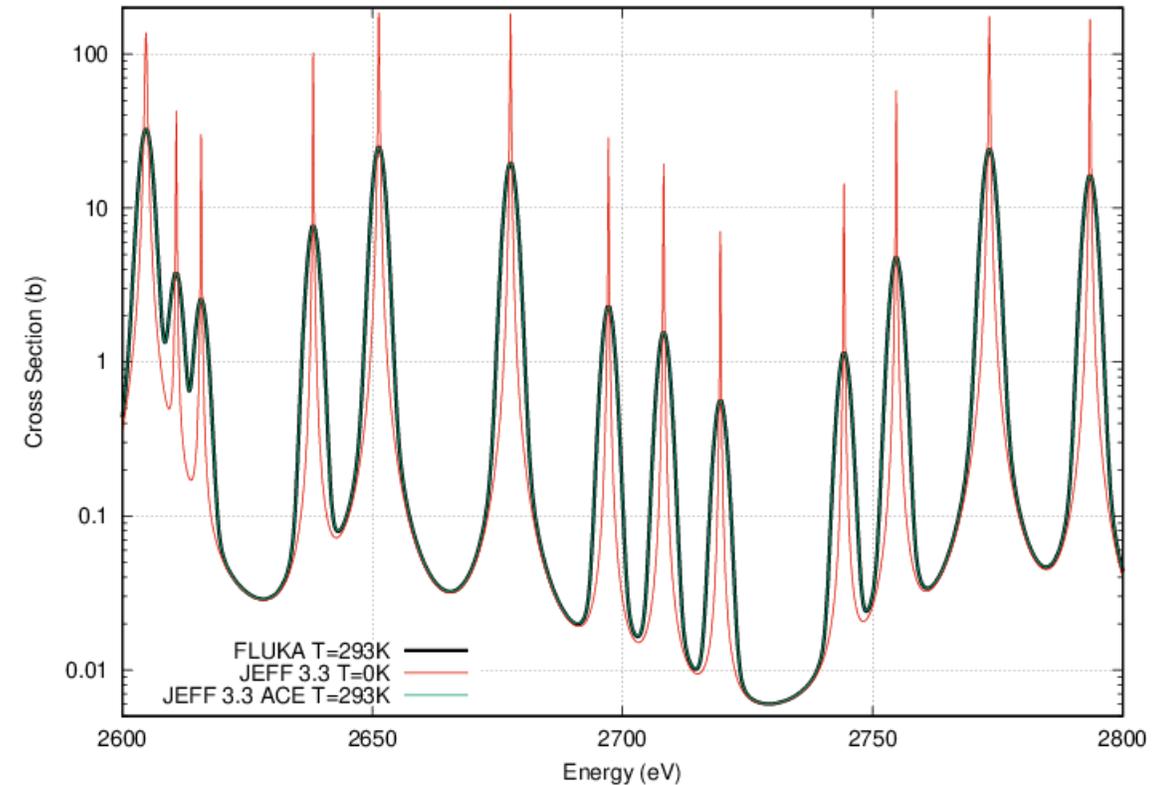
[1] A. Wahl, *Systematics of Fission-Product Yields*, LA-13928 May (2002)  
<http://cds.cern.ch/record/747754/files/34035670.pdf>

# Point-wise interactions in FLUKA: key features

- Nearly direct sampling from evaluated nuclear data libraries
- $(E_i, \sigma_i)$  tables with accuracy  $< 0.1\%$
- Modern C++ implementation
- Heavily optimised:
  - Caching a lot of necessary information (pre-tabulation of cumulative distributions)
  - Using adaptive algorithms to improve performance
  - Improved sampling of secondary distributions (using tight envelopes in case of rejection)
  - An innovative idea: a fast indexing of cross-sections using a cheap CPU  $\log_2$  approximation
  - Hierarchical sampling of channels
- Fast Doppler broadening at arbitrary temperature performed at initialisation
- “Fully” correlated emission of reaction products: N-body final states populated by subsequent 2-body emissions (the kinematics gradually constraining database distributions)

# Doppler broadening

- Integrated cross sections are Doppler-broadened to the temperature  $T$  required using an adaptive numerical integration
- Performed at initialisation
- Fast: CPU time reported in output file (see below)
- Always ensuring precision better than 0.1% (as provided in the initial data)

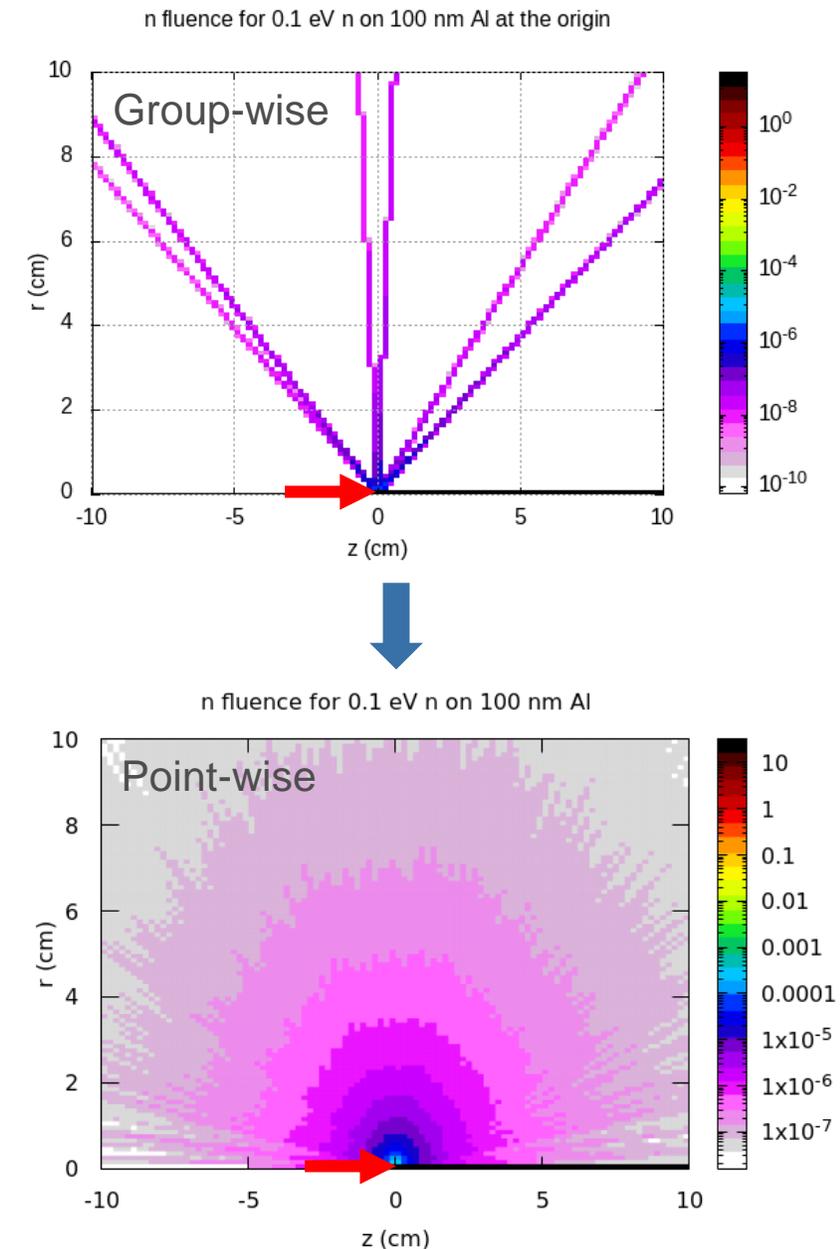


Online Doppler broadening example at 293 K for  $^{113}\text{Cd}(n,\gamma)$ :

- FLUKA
- JEFF (T=0 K)
- JEFF processed with NJOY

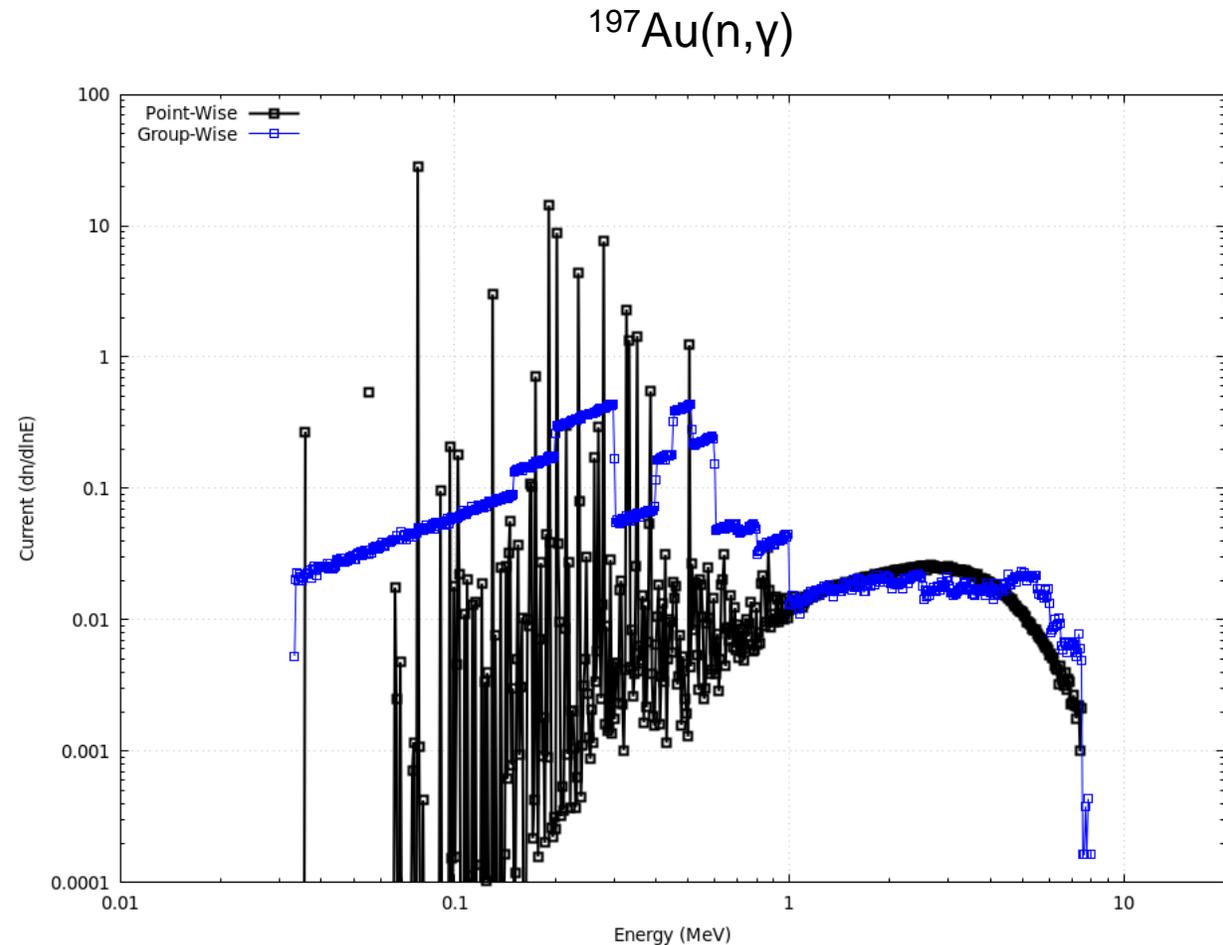
# Point-wise (n,eI) in FLUKA

- Continuous distribution of polar scattering angles  $\nabla$
- Above  $\sim 5$  eV the **target nucleus is effectively at rest**
- Below  $\sim 5$  eV the **target nucleus motion** is sampled from a Maxwell-Boltzmann distribution
- Recoils are explicitly calculated and pushed to the stack
- Below  $\sim$ eV, neutron wavelength spreads over several atoms. Neutron scattering cross sections are sensitive to the molecular/crystalline binding of the target nuclide.
  - E.g. H(n,eI) will be different depending on whether H is bound in H<sub>2</sub>, H<sub>2</sub>O, ZrH, etc.
- To account for binding effects, thermal scattering laws S( $\alpha,\beta,T$ ) are available upon user request for a handful of isotopes / materials (more below)



# Point-wise (n, $\gamma$ ) in FLUKA

- The neutron is absorbed leading to an excited nucleus  
→ standard FLUKA de-excitation module
- All known  $\gamma$  lines will be reproduced
- **Currently all isotopes de-excite to the ground state**
- Work is ongoing to properly use the probability to end in an isomeric state if the information is available in the database
- The recoil is properly generated

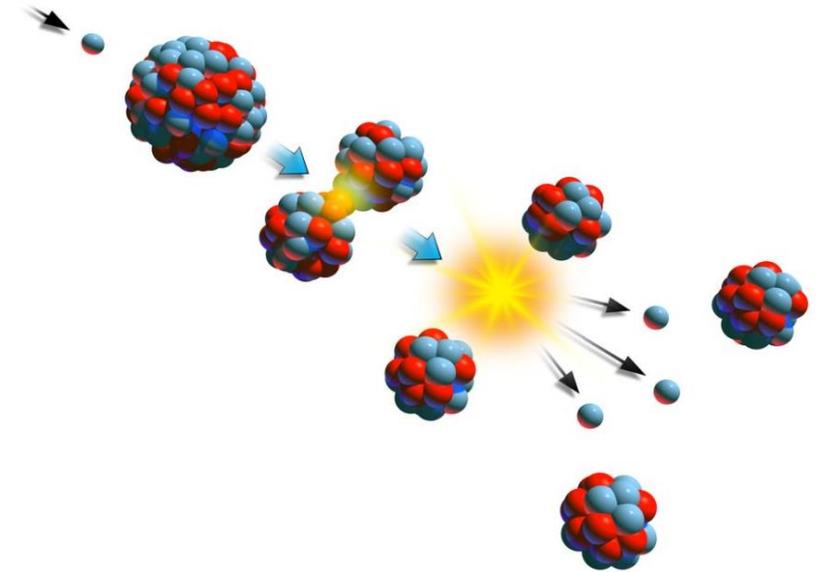


# Inelastic interaction channels

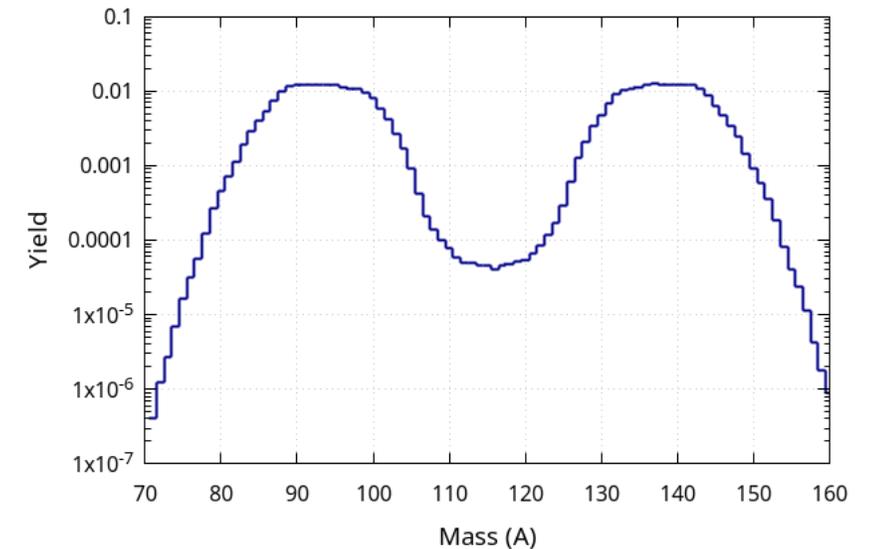
- FLUKA selects a sub-channel based on the cross section
- It then samples the secondaries (including the residual nucleus) according to database information on the final state
- It will sample the secondaries (except the photons) one-by-one from the database distributions, getting back the Energy and  $\cos\theta$  of the ejectile, either in LAB or in CMS
- Excited residual nucleus is **de-excited with the standard FLUKA modules** (see Hadronics lecture)

# Fission timeline

- Compound nucleus  $n+(Z,A) \rightarrow (Z,A+1)$
- ~10% neutrons emitted pre-scission if kinematically possible
- Scission  $\rightarrow$  Split into two or three fragments (only two in FLUKA)
- Excited fragments emit prompt neutrons proportionally to their neutron excess and gammas from the database distribution
- Fragments are sampled either from the database or from Wahl systematics
- Fragments can further emit delayed neutrons (not implemented!)
- Beta decay of fission fragments via a decay run
- Neutrino emission of fission fragments – not implemented



$^{233}\text{U}$  fission fragment mass distribution



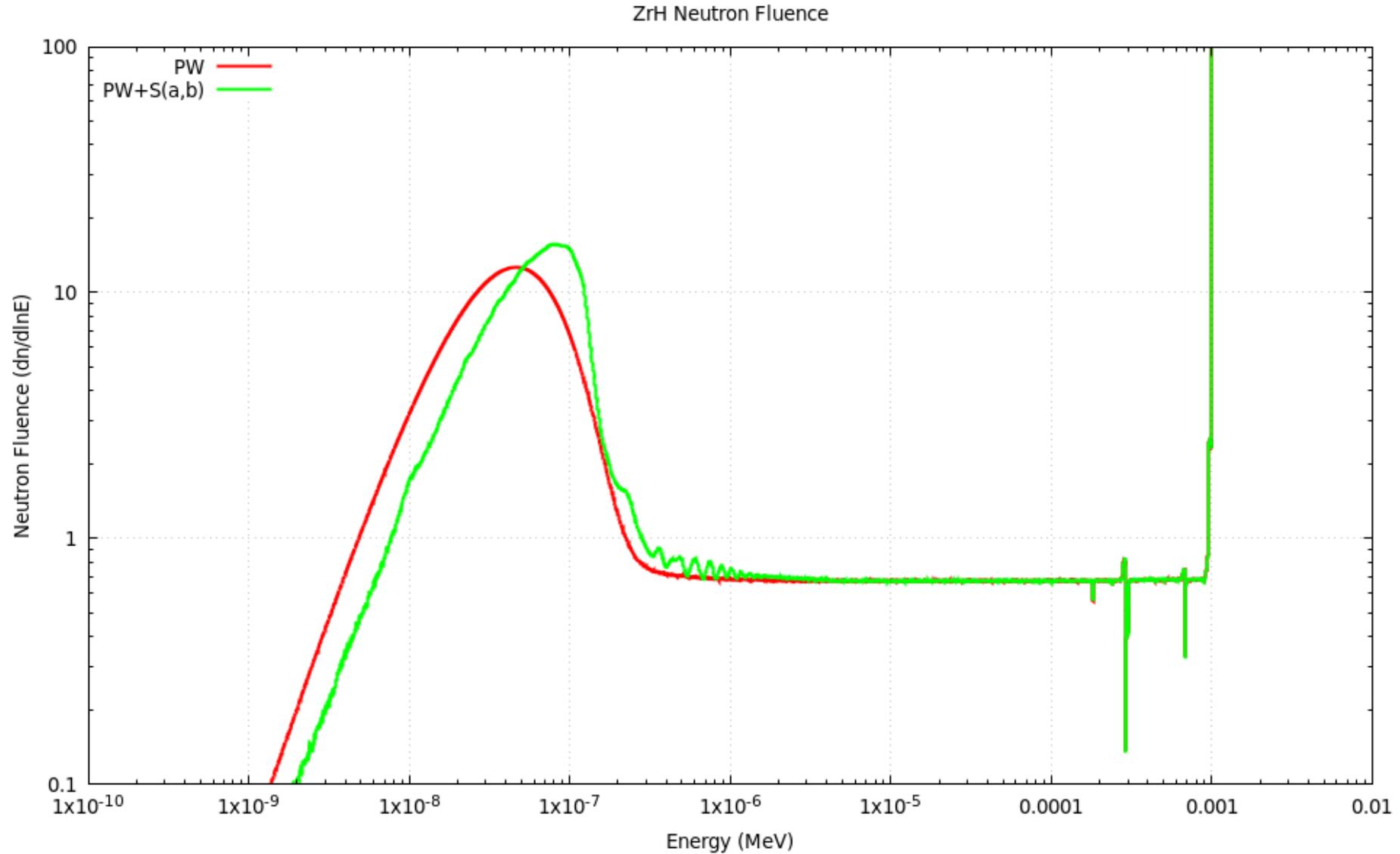
# Thermal Scattering Law $S(\alpha, \beta, T)$ (1/2)

- For thermal neutrons, generally with energies less than  $\sim 4$  eV, scattering cross sections are affected by the chemical/molecular/crystalline binding environment of the active target isotope
- If binding effects are not accounted for in a simulation, the reported results may be highly inaccurate
- Luckily NJOY can preprocess the Thermal Cross section data and prepare 3D tabulations with:
  - [Incoming neutron energy; Outgoing energy; Outgoing angular distribution]
  - [Incoming neutron energy; Bragg Edge; Outgoing angular distribution]

# Thermal Scattering Law $S(\alpha, \beta, T)$ (2/2)

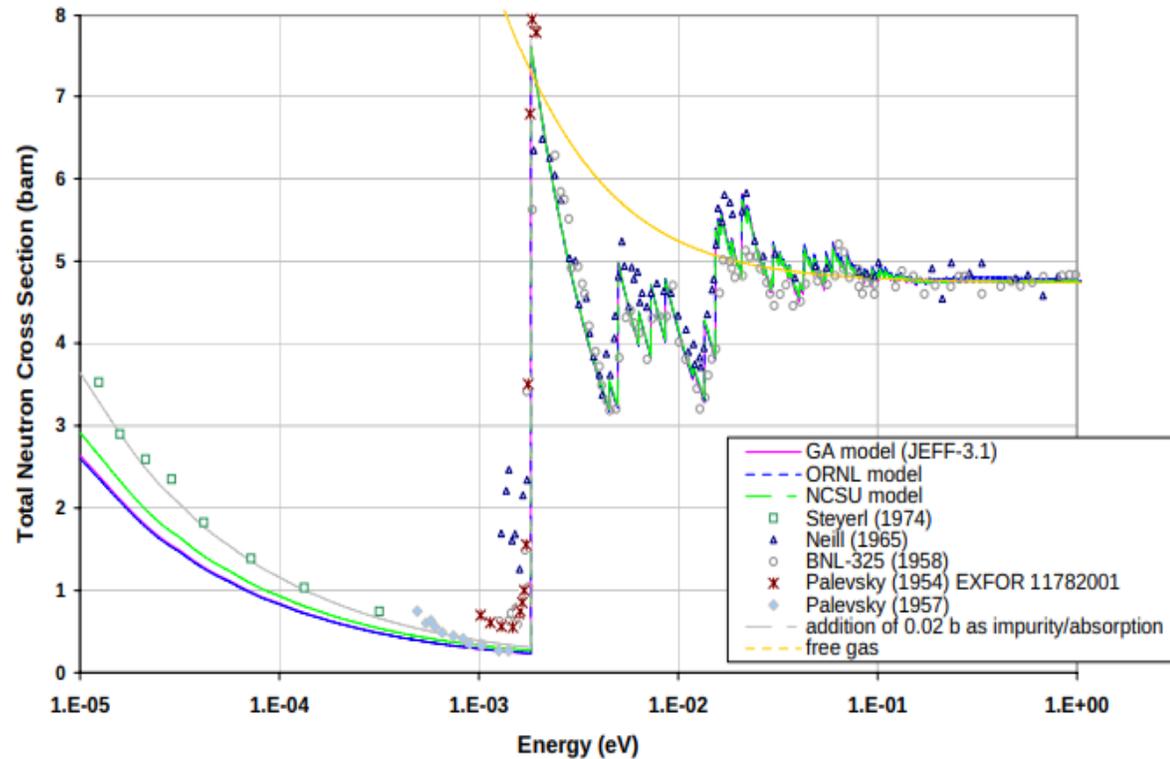
- Channels (nomenclature refers to state in which target system is left):
  - **Elastic** – the neutron energy remains the same, the angle changes
    - **Coherent** – discrete angles depending on the crystal direction vs neutron direction and Bragg edge selected, on crystal lattice
    - **Incoherent** – continuous distribution of angles mostly on hydrogenous materials
  - **Inelastic** – the scattering system is left in an excited state
- 58 materials available
  - `al_metal`, `be_beo`, `be_metal`, `benzen`, `d_heavy_water`, `d_ortho_d2`, `d_para_d2`, `fe_metal`, `graphite`, `h_l_ch4`, `h_ortho_h2`, `h_para_h2`, `h_polyethylene`, `h_s_ch4`, `h_water`, `h_zrh`, `o_beo`, `o_uo2`, `u_uo2`, `zr_zrh`, ...
- In addition, any  $S(\alpha, \beta, T)$  ACE library with point-wise data can be used
- At various fixed temperatures per material: 4 .. 800 K
- Must be requested explicitly on a per-isotope basis (see **LOW-PWXS** card below)
- Exception: H is always assumed bound to H<sub>2</sub>O

# Example $S(\alpha, \beta, T)$ on ZrH

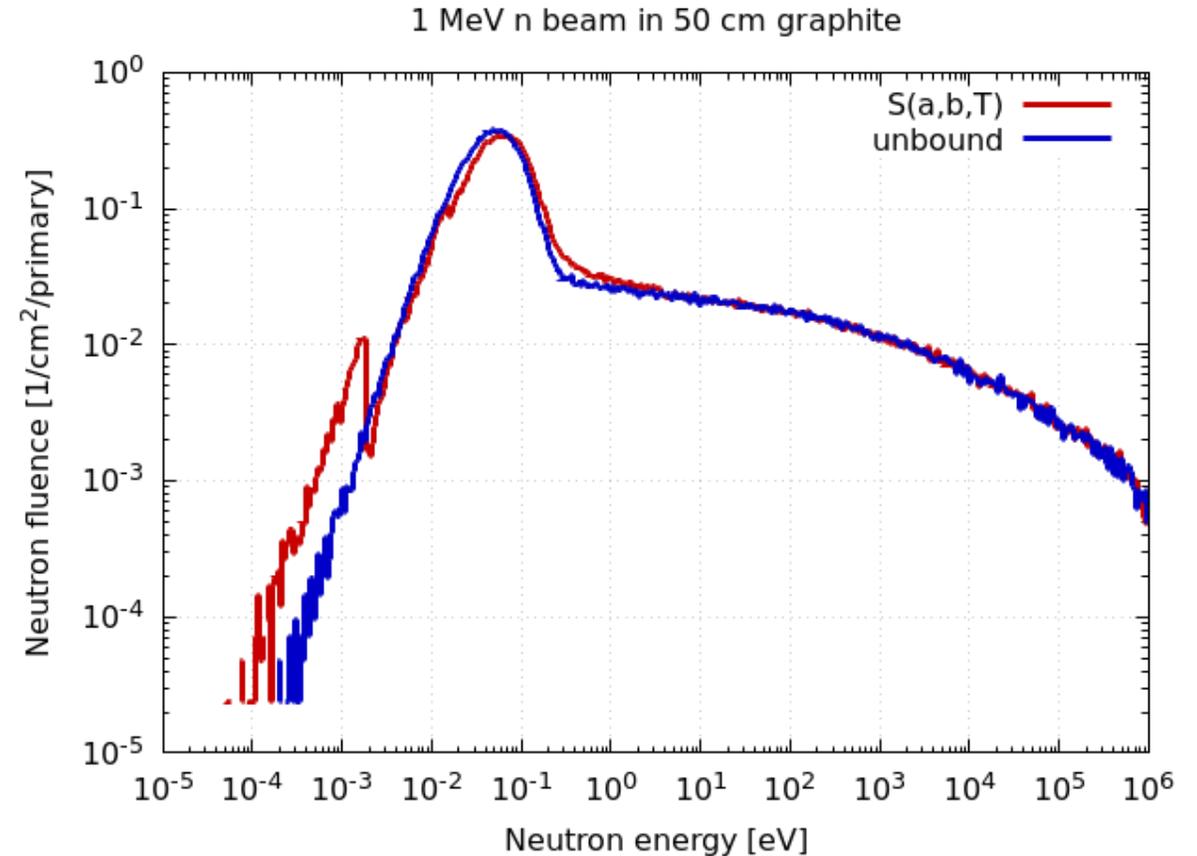


# Binding effects of n scattering in graphite

- First Bragg edge of graphite: 1.82 meV



<https://www-nds.iaea.org/publications/indc/indc-nds-0475.pdf>



<https://fluka-forum.web.cern.ch/t/4528/7>

# Usage: LOW-PWXS card

- **LOW-PWXS** card controls the new point-wise treatment in FLUKA
- **WHAT(1):**
  - **empty/0** = use PW treatment for this isotope (default)
  - **>0** Isotope code **Z\*10000 + A\*10 + iso**
  - **-1** = switch to OLD behavior, use GW/Old PW treatment for this isotope
- **WHAT(2):**
  - **S( $\alpha,\beta,T$ )** tabulation to associate with this isotope (list of isotopes in various binding environments)
- **WHAT(3):**
  - **Temperature in K** to Doppler broaden XS (default 296 K)
- **WHAT(4,5,6):**
  - **FLUKA material** range
- **SDUM:**
  - Select **database** to be used. Empty = **default** (For the present v4-4 default = JEFF-3.3)

# LOW-PWXS: examples

- Without any argument: enable PW treatment for all (available) isotopes

```
LOW-PWXS                               Mat: ▼                               to Mat: ▼                               Step:  
db: ▼                                  IAZ:                               S(α,β): ▼                               T:
```

- With WHAT(1) = -1 to use GW supplemented by PW for a handful of channels

```
LOW-PWXS                               Mat: ▼                               to Mat: ▼                               Step:  
db: ▼                                  IAZ: -1|                             S(α,β): ▼                               T:
```

- Example:

- Enable PW for HYDROGEN (natural 1H + 2H)  
Load from ENDF database  
Doppler broaden to 350 K  
Select the h\_water S(α,β,T) ONLY for 1H

```
LOW-PWXS                               Mat: HYDROGEN ▼                       to Mat: ▼                               Step:  
db: endf ▼                             IAZ: 10010                             S(α,β): h_water ▼                       T: 350|
```

# Scoring: USR{BDX, TRACK, YIELD, COLL}

## Group-wise:

- When scoring of low-energy neutrons is requested, FLUKA will use the FIXED energy group structure of 260 groups, independently of what is supplied in the card

## Point-wise:

- FLUKA will honor the user histogram settings:  
**ONLY IF** the materials of the regions involved have ALL constituents declared as point-wise
- Special attention to VACUUM which can be operationally declared as point or group-wise with the **LOW-PWXS** card
- E.g. USRBDX on a boundary between a point-wise material and VACUUM declared as group-wise, will still show group binning (!)

# FLUKA output

- Search for the section:  
Low energy neutron Point Wise materials
- For each FLUKA material that contains PW isotopes the natural composition, temperature, abundance, dataset used, and time for the Doppler broadening is printed
- When something goes wrong verify that what was asked was what you got

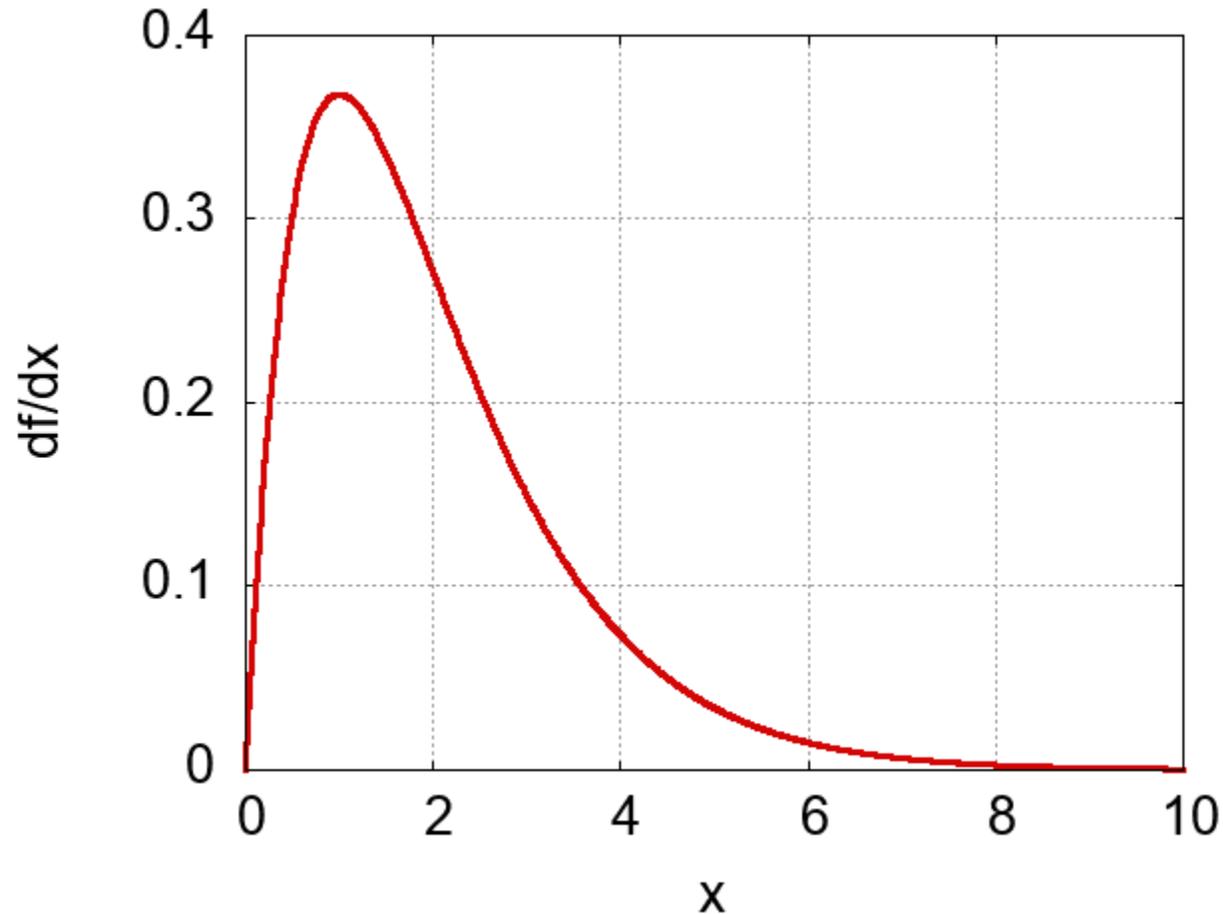
```
*** Low energy neutron Point Wise materials
### Material Z A m T(K) Dataset
3 HYDROGEN 1 1 0 296.0 default
  S(a,b) 1 1 0 h_water
6 CARBON 6 0 0 296.0 default
  12 0 0.9893
  13 0 0.0107
7 NITROGEN 7 0 0 296.0 default
  14 0 0.9963
  15 0 0.0037
8 OXYGEN 8 0 0 296.0 default
  16 0 0.9976
  18 0 0.0020
  17 0 0.0004
Doppler broadening Z= 1 A= 1 to T=296K time=0.018041s
Doppler broadening Z= 6 A= 12 to T=296K time=0.002211s
Doppler broadening Z= 6 A= 13 to T=296K time=0.002787s
Doppler broadening Z= 7 A= 14 to T=296K time=0.00405s
Doppler broadening Z= 7 A= 15 to T=296K time=0.001994s
Doppler broadening Z= 8 A= 16 to T=296K time=0.002313s
Doppler broadening Z= 8 A= 18 to T=296K time=0.002716s
Doppler broadening Z= 8 A= 17 to T=296K time=0.003154s
Doppler broadening Z=12 A= 24 to T=296K time=0.006679s
Doppler broadening Z=12 A= 26 to T=296K time=0.005807s
Doppler broadening Z=12 A= 25 to T=296K time=0.008832s
Doppler broadening Z=13 A= 27 to T=296K time=0.011427s
Doppler broadening Z=26 A= 56 to T=296K time=0.080996s
Doppler broadening Z=26 A= 54 to T=296K time=0.037268s
Doppler broadening Z=26 A= 57 to T=296K time=0.066767s
Doppler broadening Z=26 A= 58 to T=296K time=0.149089s
```

# Lethargy units

An important reminder from the scoring lecture

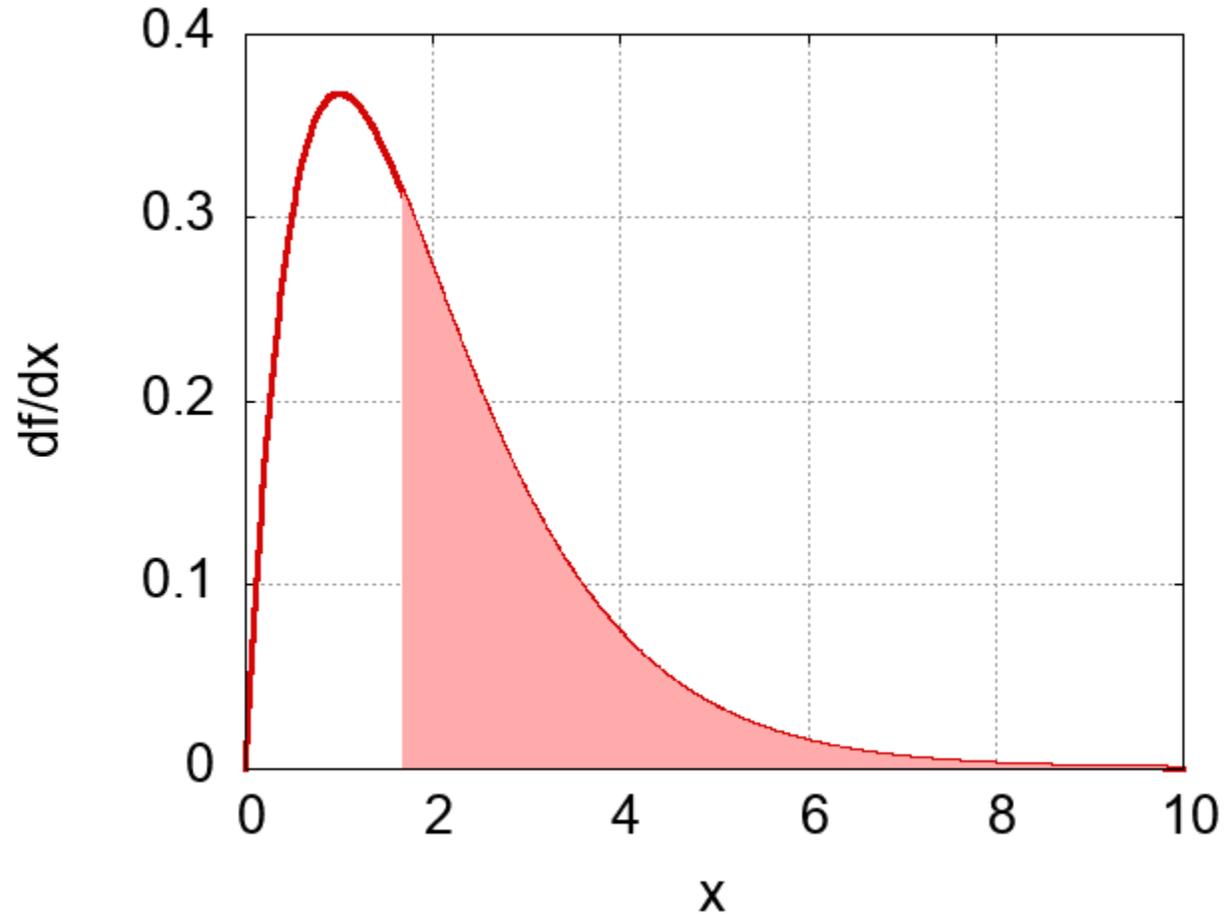
# An important reminder from the scoring lecture

- Consider the (unnormalised) distribution  $\frac{df}{dx} = x e^{-x}$ , where  $x$  is dimensionless:



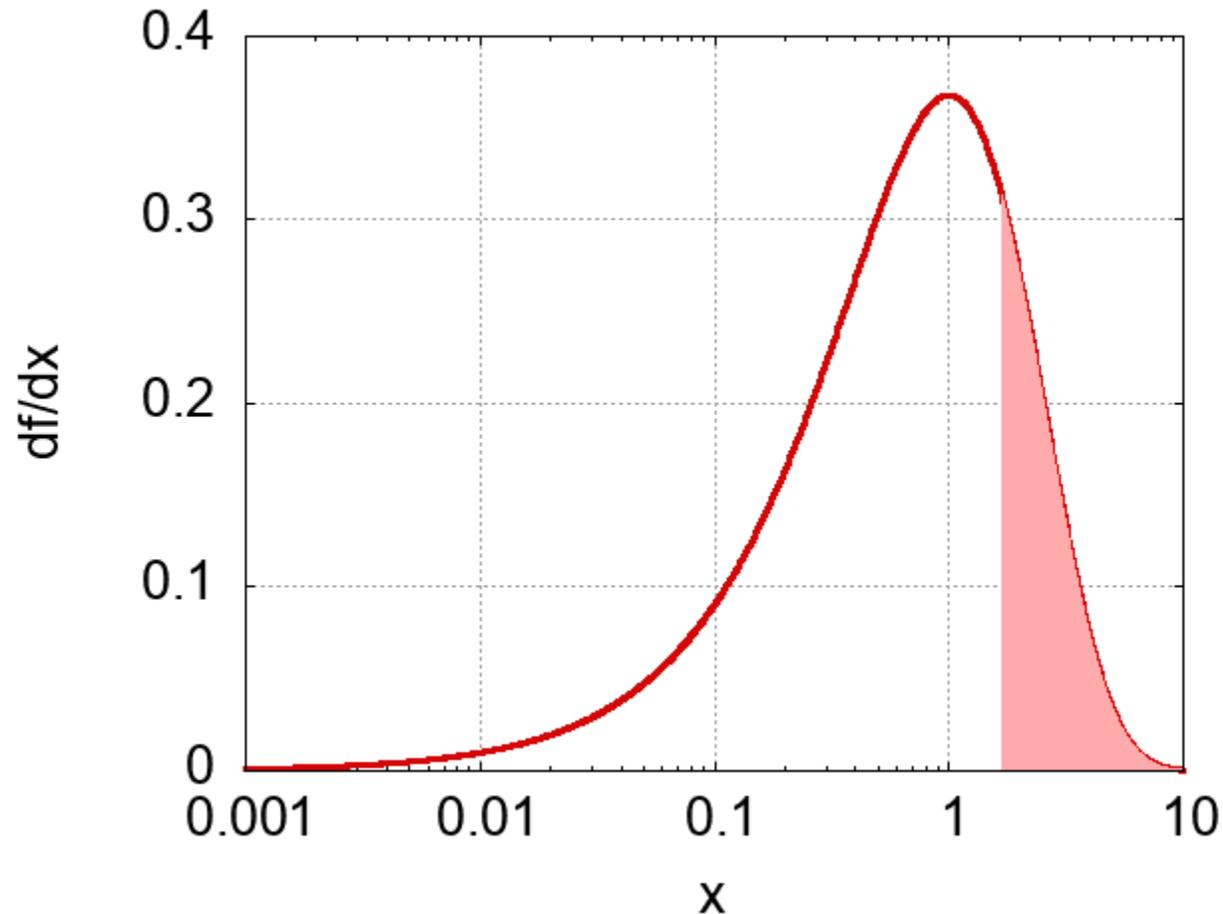
# An important reminder from the scoring lecture

- We now shade in 50% of the area under the curve:



# An important reminder from the scoring lecture

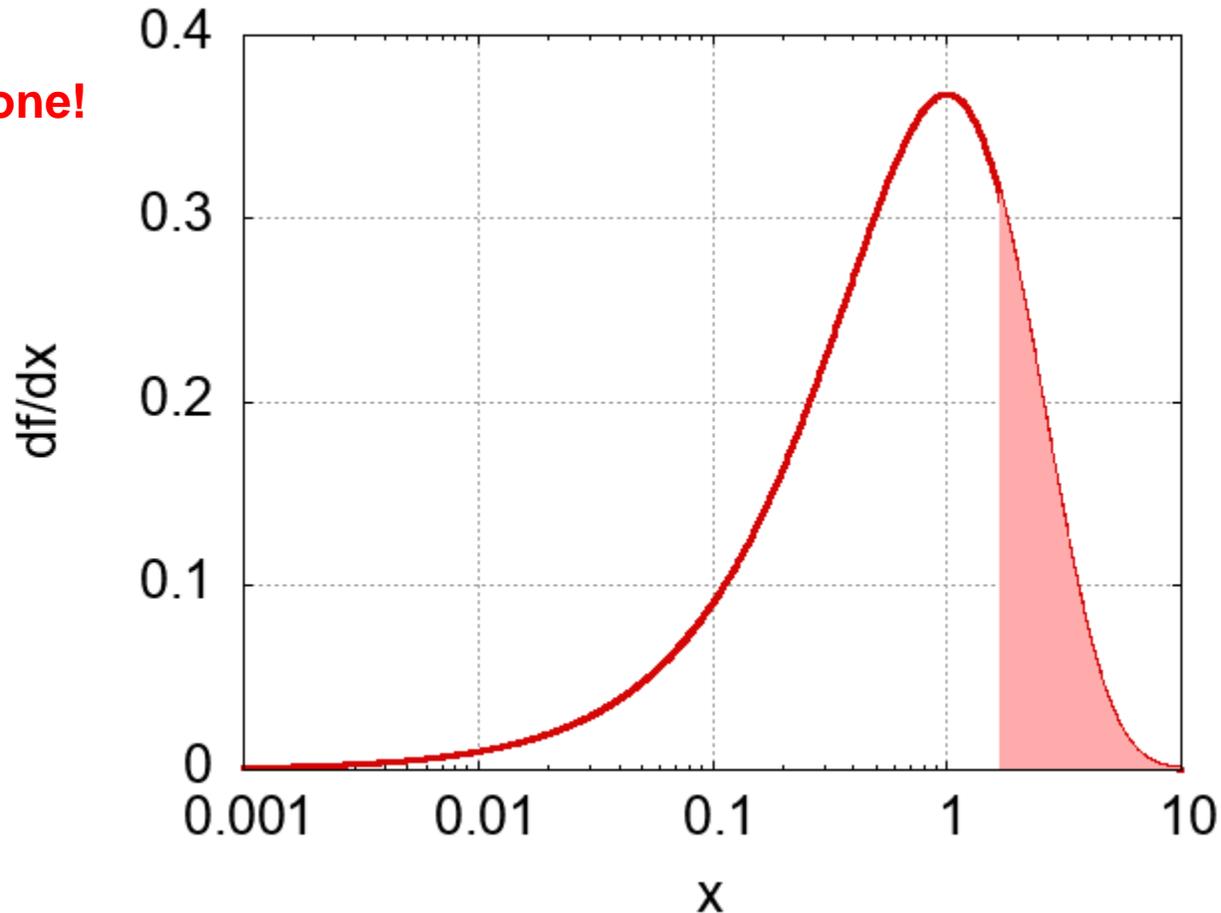
- Suppose you want to legitimately resolve what happens at small  $x$  in more detail
- So you naturally plot the **horizontal axis in logarithmic scale, don't you?**



# An important reminder from the scoring lecture

- Suppose you want to legitimately resolve what happens at small  $x$  in more detail
- So you naturally plot the **horizontal axis in logarithmic scale**:

Careful! Achtung! Attenzione!



**With this careless action  
you are severely  
distorting information!**

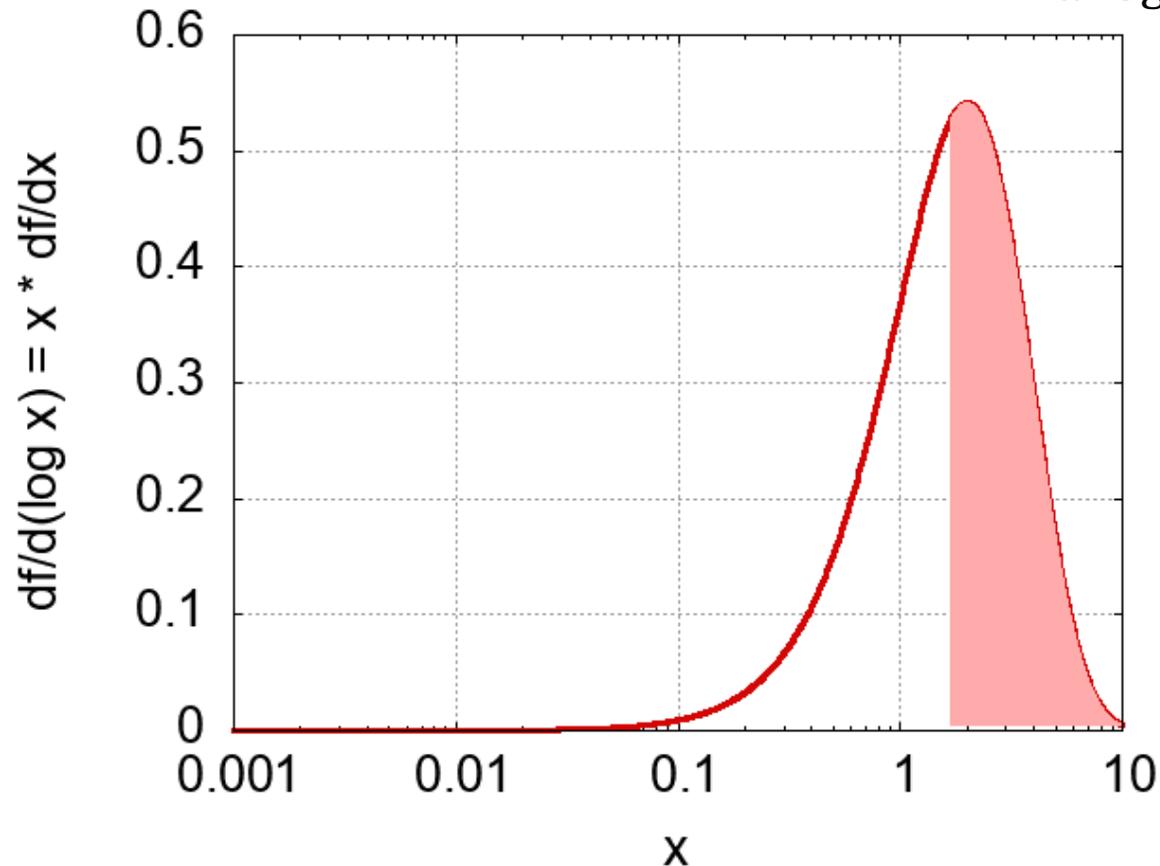
The shaded area appears almost irrelevant in front of the unshaded region, while in reality both regions represent 50% of the distribution (!!!)

# Lethargy units

- What happened? **You forgot a Jacobian:**  $\frac{df}{d \log(x)} = \frac{df}{dx} \frac{dx}{d \log(x)} = x \frac{df}{dx}$
- Embrace *lethargy\* units*, the proper representation of  $\frac{df}{d \log(x)}$ :

\* *neutronics* term  
(neutron lethargy)

*lethargy: slowness,  
sluggishness, from Greek  
lēthargīa (ληθαργία)*



In this representation,  
*integrals are respected*

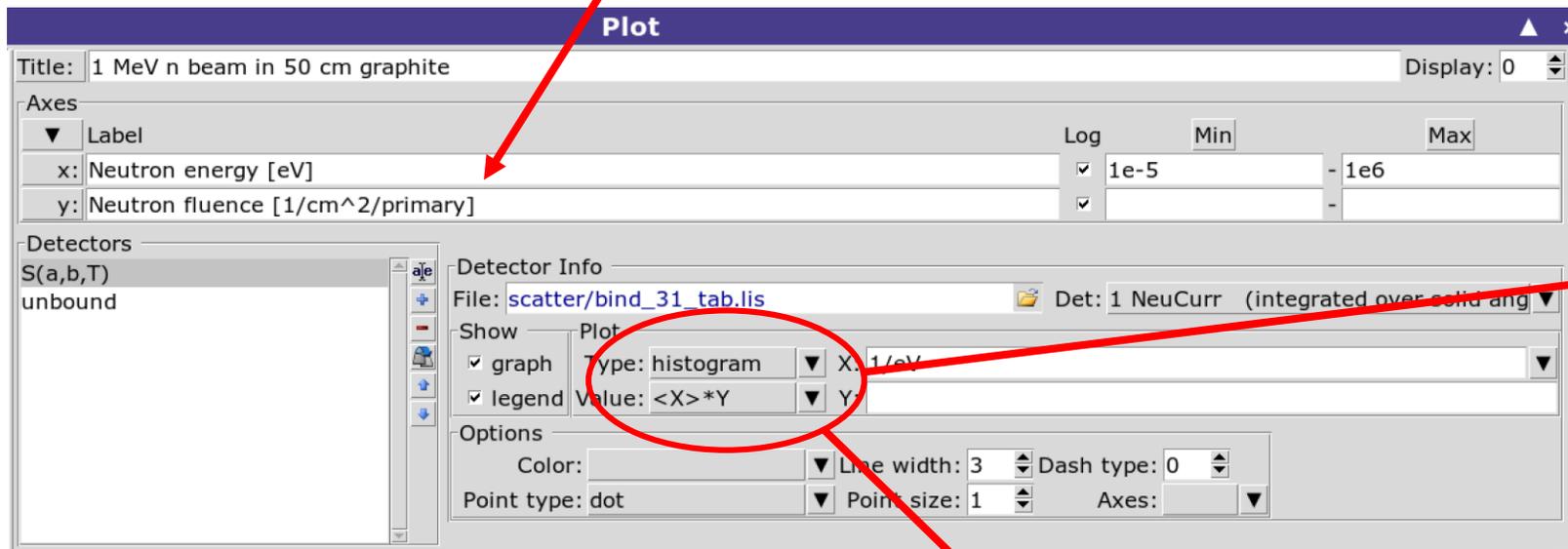
You are now representing  
information in a faithful  
way

(NB: taking a logarithmic  
scale in the vertical axis is  
harmless)

# Flair helps you out (but you are responsible for axis labels)

- Do you need to worry? Yes. Be fully conscious when you plot histograms and distributions with logarithmic abscissas (horizontal axes) – **needed for low energy n**

- $\frac{df}{d \log(E)} = E \frac{df}{dE}$  → Indeed, the resulting spectrum does not have units of “1/GeV”



Regardless of whether you request **lin** or **log** spacing in your scoring cards

- What about histograms? Which  $X$  is taken?  $X_i$ ?  $X_{i+1}$ ?

$$\log X = \frac{1}{2} (\log X_{i+1} + \log X_i) = \frac{1}{2} \log(X_{i+1} X_i) \quad \Rightarrow \quad X = [e^{\log(X_{i+1} X_i)}]^{1/2} = \sqrt{X_{i+1} X_i}$$

# Summary

- Low energy neutrons  $\leq 20\text{MeV}$  receive special treatment in FLUKA
- Two methods are available:
  - **Group-wise**: coarse, but fast treatment. Few isotopes/channels are in point-wise.
  - **Point-wise**: superior model, highly optimised, giving access to all latest available neutron data, explicit treatment of interactions in fully correlated way
- What to use:
  - Prefer the use of **point-wise**
    - **unless**: Speed is an issue and you are not interested in the detailed neutron treatment
    - **Warning**: Neutrons can be indirectly responsible for many effects (activation, damage, SEU)
    - When unsure, use point-wise to properly take all physical effects into account
  - Group-wise can work nicely for shielding applications
  - Optionally you can mix point- and group-wise treatment in the same problem

