

# Inclusive $J/\psi$ production in forward proton-proton and proton-lead collisions at high energy

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arXiv:2409.01791 (2024)

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# Outline

Based on *Gimeno-Estivill, Lappi, Mäntysaari (2024) arXiv:2409.01791*

- $J/\psi$  production in Color Glass Condensate (CGC) + Non-relativistic QCD (NRQCD)
  - Correlators of Wilson Lines
  - Target parametrization constrained by DIS HERA data
  
- Results compared to LHCb and ALICE data + previous  $J/\psi$  phenomenology in CGC+NRQCD
  - $J/\psi$  cross section in p+p and p+Pb
  - Nuclear modification factor  $R_{pPb}$

# Gluon saturation

- High-energy (small- $x$ ) regime  $\rightarrow$  strong increase in gluon density
- Forward rapidity ( $y \gg 1$ ) in pA and pp collisions

$$x_p \propto e^y \lesssim 1 \rightarrow \text{dilute projectile}$$

$$x_A \propto e^{-y} \ll 1 \rightarrow \text{dense gluon target}$$

- Massive quarks  $c\bar{c} : J/\psi$

$$M_{J/\psi} \sim Q_s \rightarrow \text{sensitive to saturation}$$

$$v \ll 1, \alpha_s(M_{J/\psi}) \ll 1 \rightarrow \text{perturbative expansion in non-relativistic QCD}$$

# Inclusive $J/\psi$ production

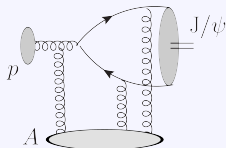
Color Glass Condensate (CGC) + Non-Relativistic QCD (NRQCD)

$$\frac{d\sigma_{J/\psi}}{d^2\mathbf{p}dy} = \sum_{\kappa} \frac{d\hat{\sigma}_{c\bar{c}}^{\kappa}}{d^2\mathbf{p}dy} \langle \mathcal{O}_{\kappa}^{J/\psi} \rangle$$

short-distance cross sections

$\otimes$

long-distance matrix elements (LDME)



## LDME

- Values from cross section/polarization fit to Tevatron  $J/\psi$  data
- Ordered in powers of velocity

*Chao et al. (2012)*<sup>⌘</sup>

$$\langle \mathcal{O}^{J/\psi} (^3S_1^{[1]}) \rangle \sim 1$$

$$\langle \mathcal{O}^{J/\psi} (^1S_0^{[8]}) \rangle \sim v^3$$

$$\langle \mathcal{O}^{J/\psi} (^3S_1^{[8]}) \rangle \sim v^4$$

$$\langle \mathcal{O}^{J/\psi} (^3P_0^{[8]}) \rangle \sim v^4$$

$$\kappa = 2s+1 L_J^{[c]}$$

s: spin

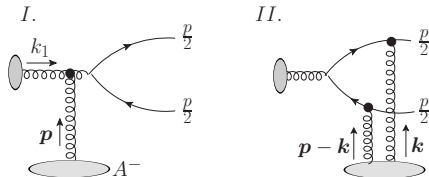
L: orbital angular momentum

J: total angular momentum

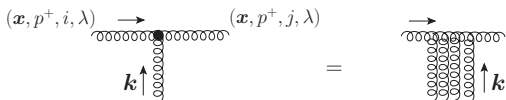
c: color

*Bodwin, Braaten, Lepage (1994)*<sup>⌘</sup>

- Dilute-dense collision in the proton collinear limit ( $k_1 \rightarrow 0$ )
- Target: classical gluon field  $A^-$



- Eikonal interaction parton-nucleus: Wilson Line  $V(\mathbf{x})$

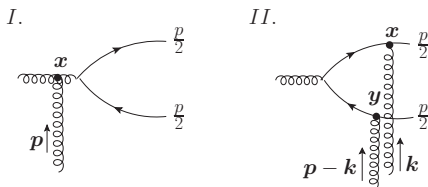


$\lambda$ : polarization,  $i, j$ : color

## Wilson Line

$$V_{F,A}(\mathbf{x}) = \mathcal{P} \exp \left( -ig \int dx^+ A_a^-(x^+, \mathbf{x}) t^a \right)$$

# Short-distance coefficients in CGC



Color octet states: *I* & *II*

$$\frac{d\hat{\sigma}}{d^2\mathbf{p} dy} \propto \alpha_s x_p f_{p/g}(x_p, \mu^2) \int_{\mathbf{b}} \int_{\mathbf{k}} \mathcal{N}(\mathbf{k}) \mathcal{N}(\mathbf{p} - \mathbf{k}) \tilde{\Gamma}_8^\kappa(\mathbf{p}, \mathbf{k})$$

$$\mathcal{N}(\mathbf{k}) = \int_{\mathbf{r}} e^{i\mathbf{k}\mathbf{r}} D_{\mathbf{r}}$$

Color singlet states: *II*

$$\frac{d\hat{\sigma}}{d^2\mathbf{p} dy} \propto \alpha_s x_p f_{p/g}(x_p, \mu^2) \int_{\mathbf{x}, \mathbf{x}', \mathbf{y}', \mathbf{y}} e^{-i\mathbf{p}\mathbf{\Delta}} \left( Q_{\mathbf{x}, \mathbf{x}', \mathbf{y}', \mathbf{y}} - D_{\mathbf{r}} D_{\mathbf{r}'} \right) \tilde{\Gamma}_1^\kappa(\mathbf{r}, \mathbf{r}')$$

$$D_{\mathbf{r}} \sim \langle \text{Tr}[V_{\mathbf{F}}(\mathbf{0}) V_{\mathbf{F}}^\dagger(\mathbf{r})] \rangle$$

$$Q_{\mathbf{x}, \mathbf{x}', \mathbf{y}', \mathbf{y}} \sim \langle \text{Tr}[V_{\mathbf{F}}(\mathbf{x}) V_{\mathbf{F}}^\dagger(\mathbf{x}') V_{\mathbf{F}}(\mathbf{y}') V_{\mathbf{F}}^\dagger(\mathbf{y})] \rangle$$

Dipole size:  $\mathbf{r} = \mathbf{x} - \mathbf{y}$  (conjugate amplitude:  $\mathbf{r}' = \mathbf{x}' - \mathbf{y}'$ )

Impact parameter:  $\mathbf{b} = (\mathbf{x} + \mathbf{y})/2$

Shift center of dipoles:  $\mathbf{\Delta} = (\mathbf{x}' + \mathbf{y}' - \mathbf{x} - \mathbf{y})/2$

# Color Structure

## Dipole

$$D_{\mathbf{x}-\mathbf{y}} = \frac{1}{N_c} \langle \text{Tr}[V_F(\mathbf{x}) V_F^\dagger(\mathbf{y})] \rangle$$

- Proton target: rcBK with initial condition: MV model parametrization fit to HERA DIS data
- Nuclear target:  $\mathbf{b}$ -dependent initial condition from the optical Glauber model
- rcBK evolution for each  $\mathbf{b}$

*Lappi, Mäntysaari (2014)*

→ For nucleus target no free parameters besides Woods-Saxon nuclear density

## Quadrupole

$$Q_{\mathbf{x},\mathbf{x}',\mathbf{y}',\mathbf{y}} = \frac{1}{N_c} \langle \text{Tr}[V_F(\mathbf{x}) V_F^\dagger(\mathbf{x}') V_F(\mathbf{y}') V_F^\dagger(\mathbf{y})] \rangle$$

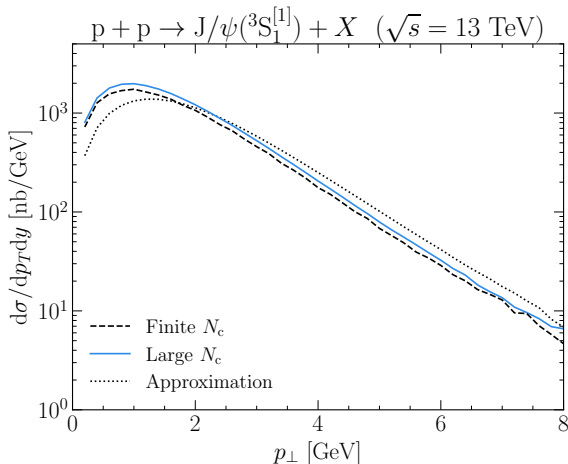
- Explicit expression in the Gaussian approximation for finite and large  $N_c$

*Dominguez, Marquet, Xiao, Yuan (2011)*

→ Quantification of finite- $N_c$  corrections +  $J/\psi$  phenomenology with explicit  $Q$

# Results: finite- $N_c$ corrections quadrupole

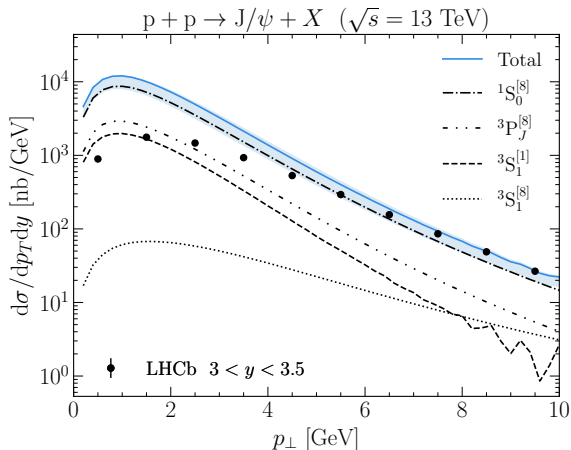
Color singlet state in proton-proton collisions at  $y = 3.25$



- Finite- $N_c$  corrections are small  $\mathcal{O}(1/N_c^2) \sim 12\%$
- Approximated quadrupole (Ma, Venugopalan\*) different by a factor of 2

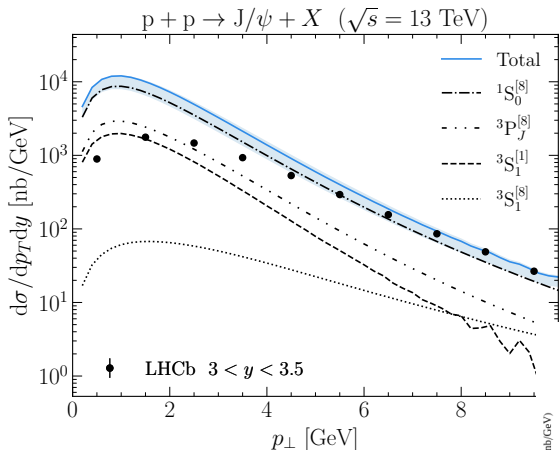


# $J/\psi$ production in proton-proton collisions



- Correct description at high- $p_{\perp}$
- Low- $p_{\perp}$   
→ Need Sudakov correction
- Dominant octet state  $1S_0^{[8]}$
- Color singlet state  $3S_1^{[1]} \sim 15\%$

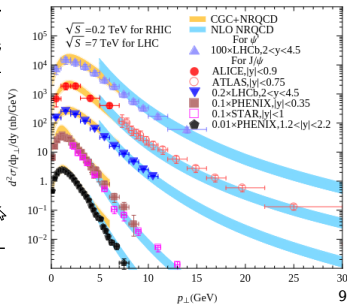
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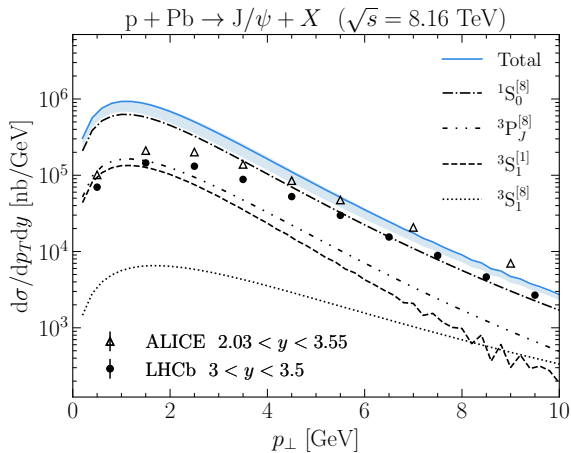
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Ma, Venugopalan (2014)

- Some parameters from interpolation between PDF and uGD

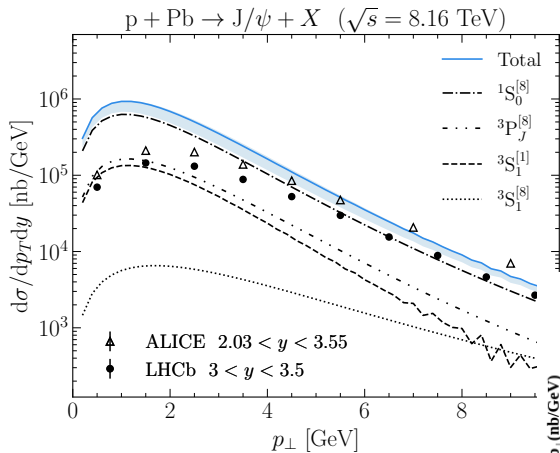


# $J/\psi$ production in proton-nucleus collisions

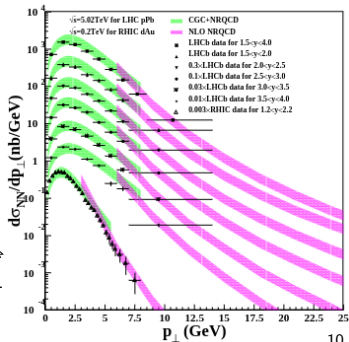


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# $J/\psi$ production in proton-nucleus collisions



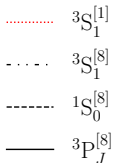
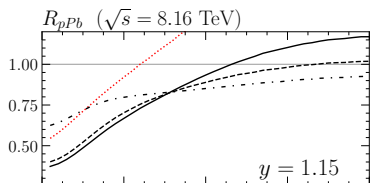
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Ma, Venugopalan (2015)<sup>✉</sup>

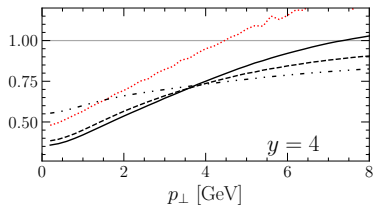
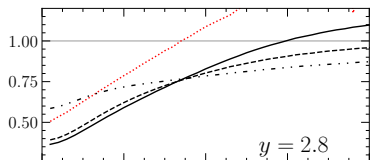
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# Nuclear modification ratio individual channels

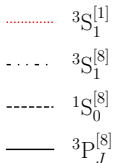
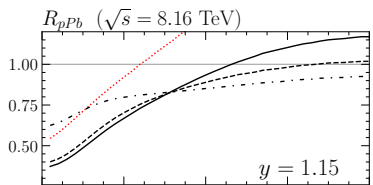


$$R_{pPb} = \frac{d\sigma_{pPb}}{Ad\sigma_{pp}}$$

- $R_{pPb} \rightarrow 1$  by construction at high- $p_{\perp}$
- Cronin enhancement color singlet  $3S_1^{[1]}$

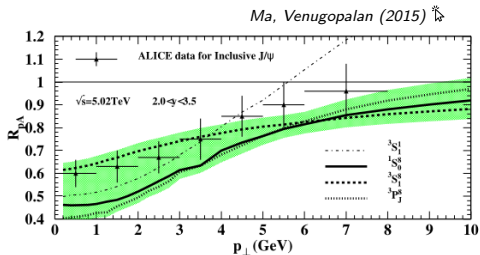
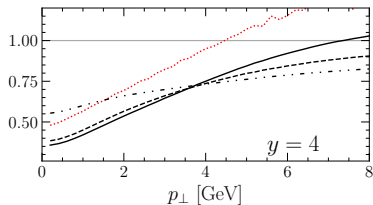
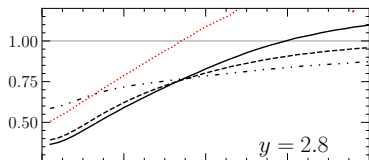


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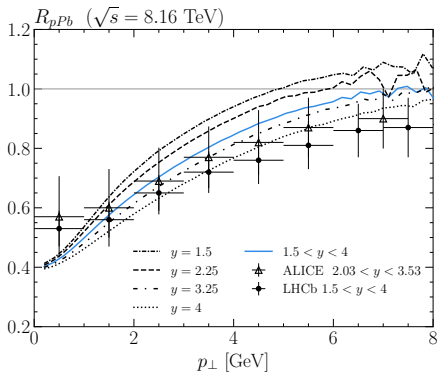


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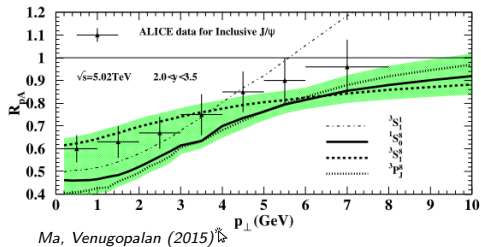
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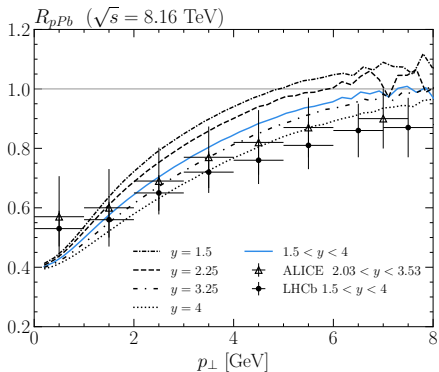
# Nuclear modification ratio vs $p_{\perp}$ and $y$



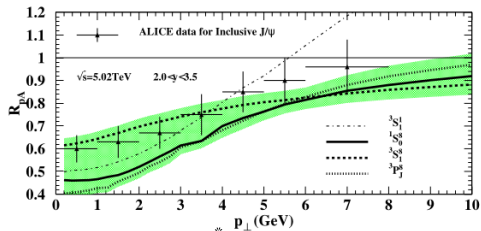
- Strong suppression at low  $p_{\perp}$
- Steeper  $p_{\perp}$ -dependence  $\rightarrow$  need NLO correction



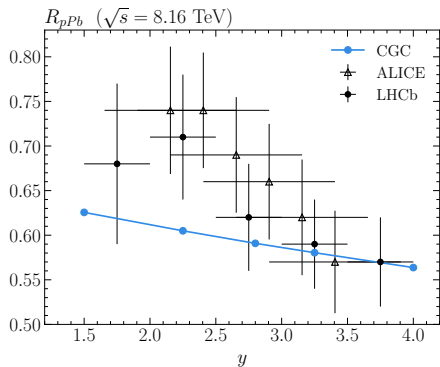
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Ma, Venugopalan (2015)





# Summary

- $J/\psi$  production in forward  $p+p$  and  $p+A$  in CGC+NRQCD
  - Explicit expression of the quadrupole
  - Description of the dense target in CGC constrained by DIS HERA data
  
- $R_{pPb}$  compatible with data, with a similar trend as the CGC+CEM calculation

*Ducloué, Lappi, Mäntysaari (2015)*
  
- Possible improvements
  - Sudakov correction at NLO
  - Fit initial conditions for BK equation including heavy quarks