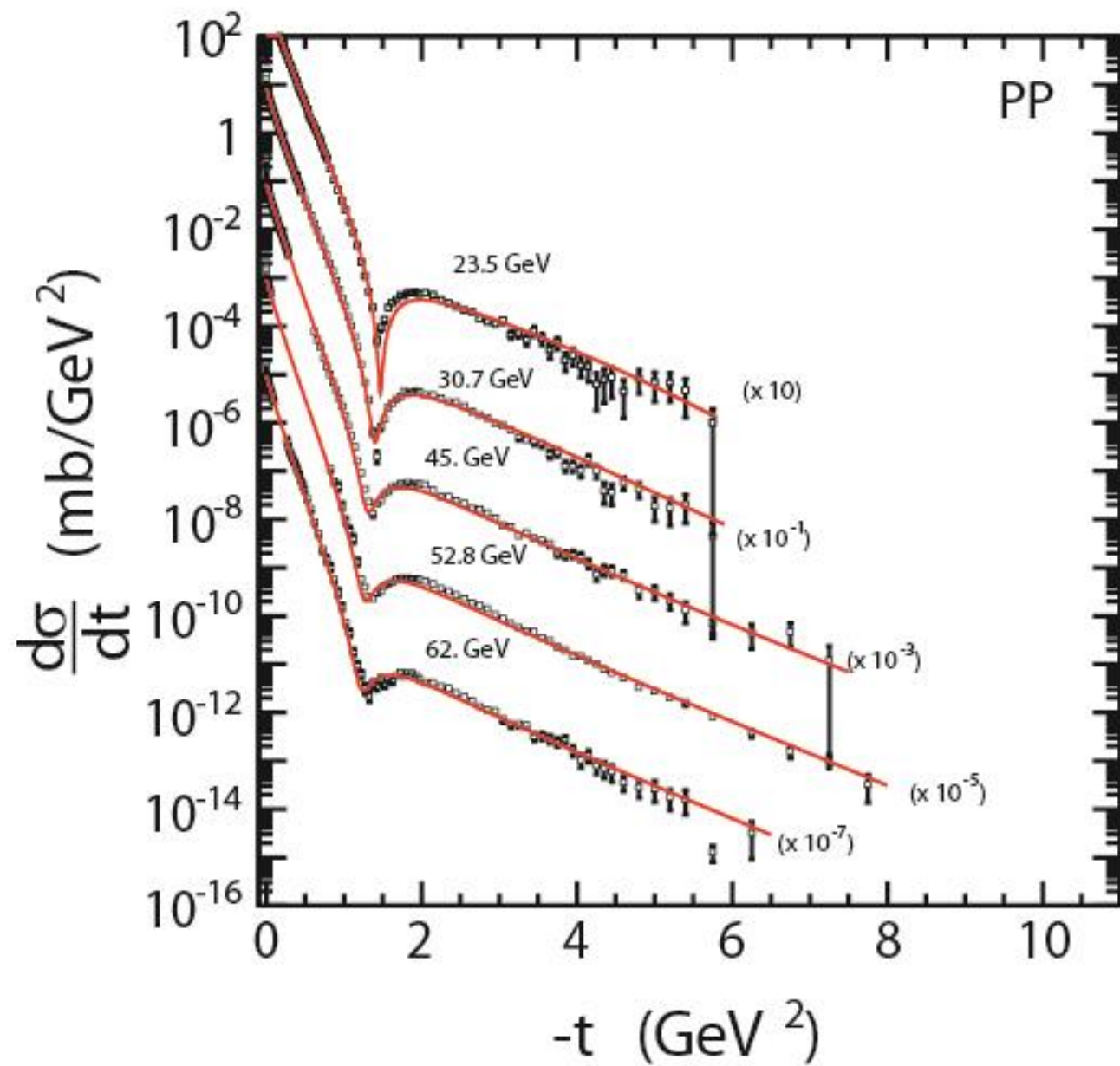
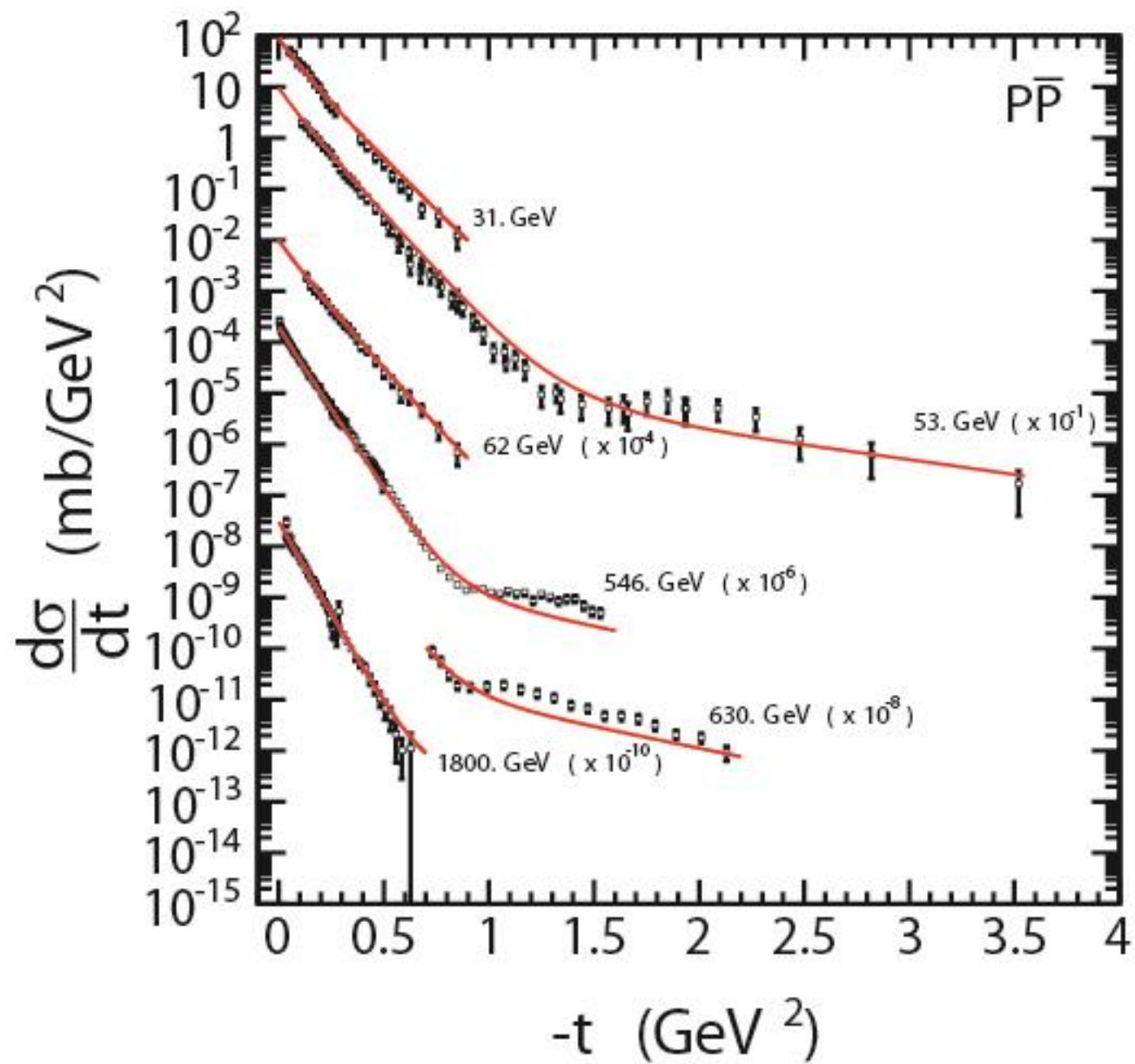


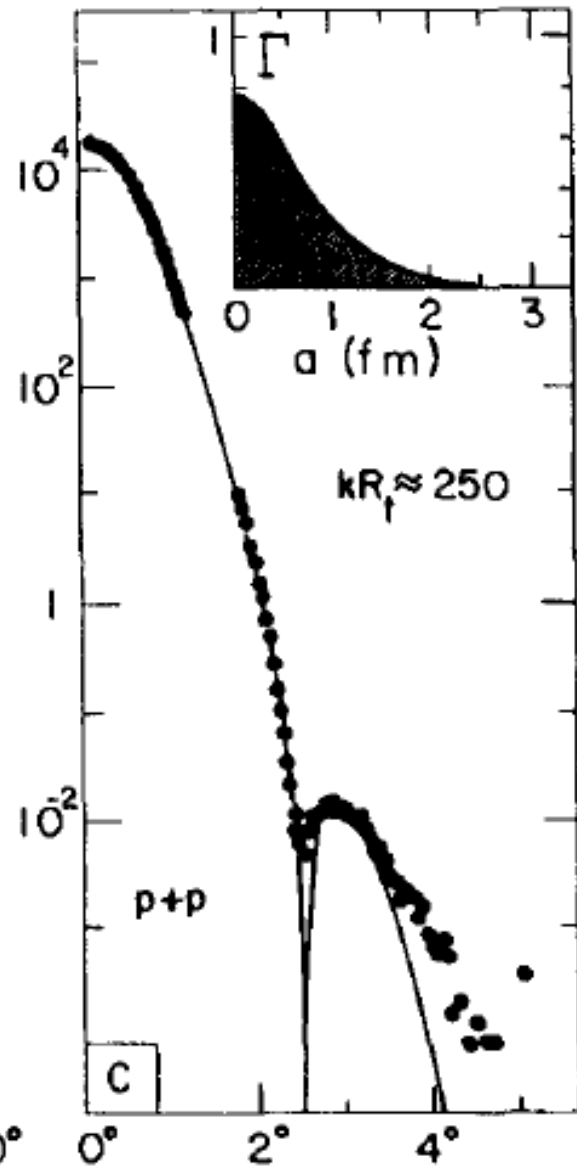
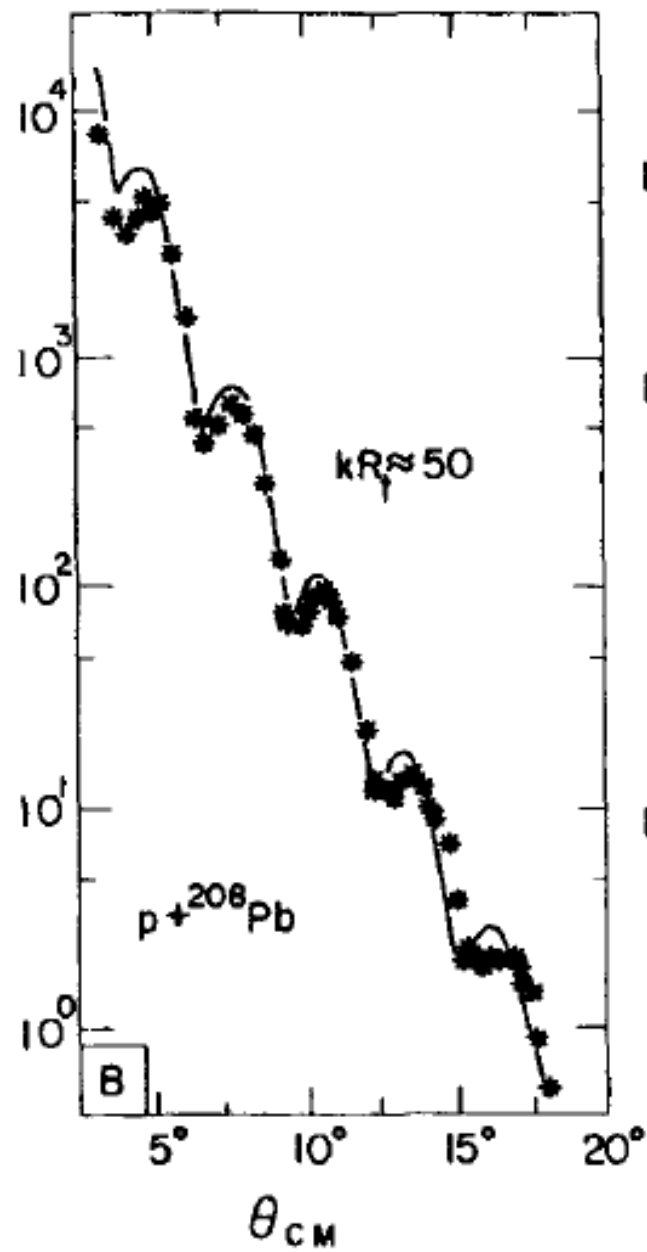
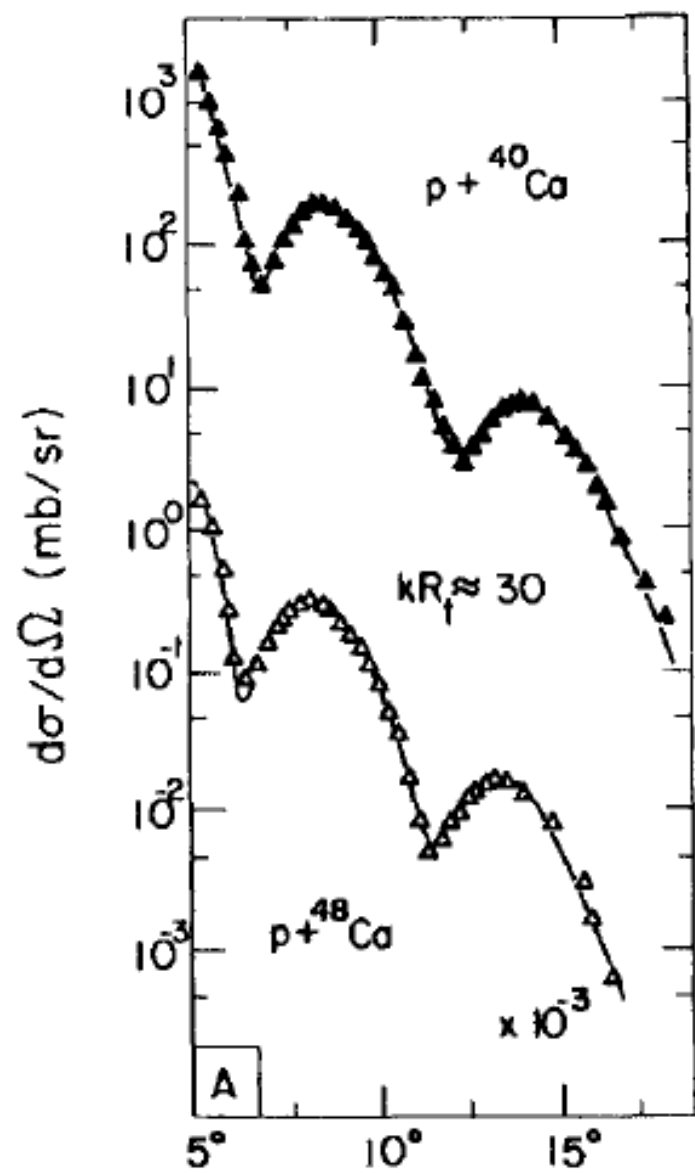
Palermo, September 2024

Structures in diffractive dissociation at the LHC

*László Jenkovszky (Kiev, Budapest), Rainer Schicker (Heidelberg),
István Szanyi (Budapest, Gyöngyös)*







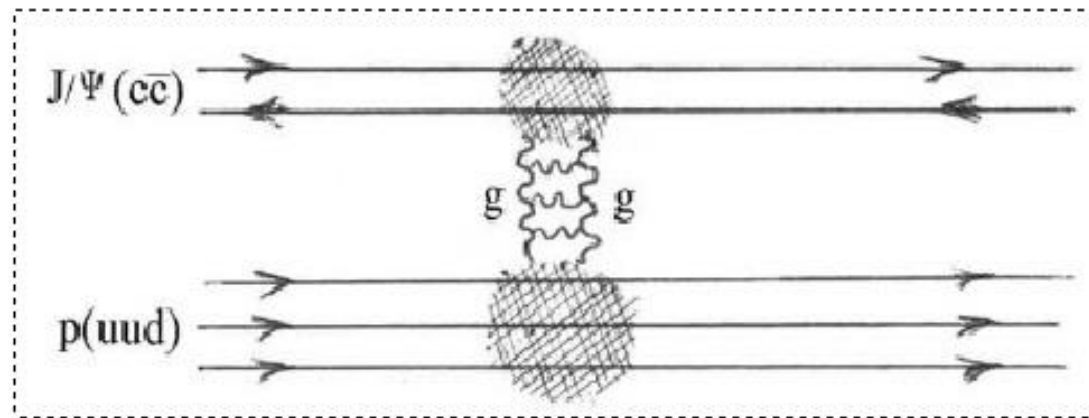
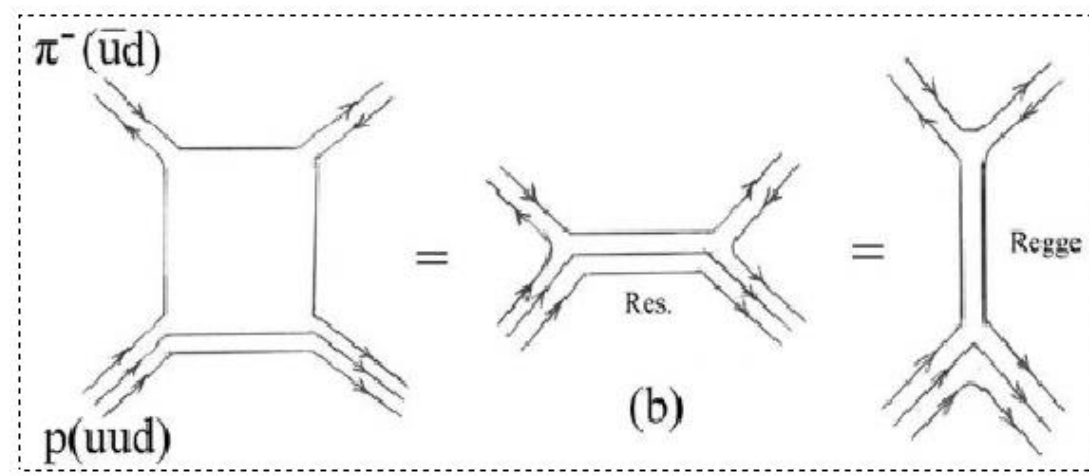
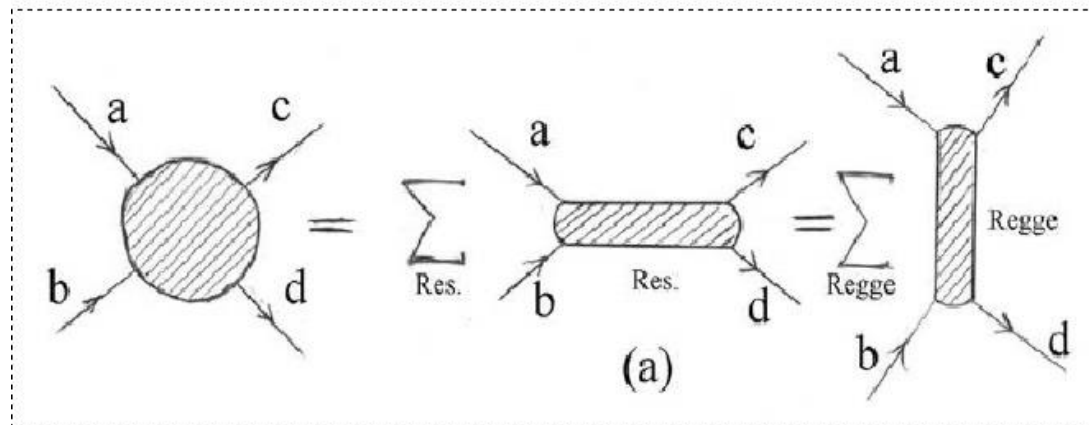


TABLE I: Two-component duality

$\mathcal{I}m A(a + b \rightarrow c + d) =$	R	Pomeron
s -channel	$\sum A_{Res}$	Non-resonant background
t -channel	$\sum A_{Regge}$	Pomeron ($I = S = B = 0; C = +1$)
Duality quark diagram	Fig. 1b	Fig. 2
High energy dependence	$s^{\alpha-1}, \alpha < 1$	$s^{\alpha-1}, \alpha \geq 1$

$$\sigma_t(s) = \frac{4\pi}{s} \text{Im}A(s, t=0); \quad \frac{d\sigma}{dt} = \frac{\pi}{s^2} |A(s, t)|^2; \quad n(s);$$

$$\sigma_{el} = \int_{t_{min} \approx -s/2 \approx \infty}^{t_{thr.} \approx 0} \frac{d\sigma}{dt} dt; \quad \sigma_{in} = \sigma_t - \sigma_{el}; \quad B(s, t) = \frac{d}{dt} \ln\left(\frac{d\sigma}{dt}\right);$$

$$A_{pp}^{\bar{p}}(s, t) = P(s, t) \pm O(s, t) + f(s, t) \pm \omega(s, t) \rightarrow_{LHC} \approx P(s, t) \pm O(s, t),$$

where P , O , f , ω are the Pomeron, odderon and non-leading Reggeon contributions.

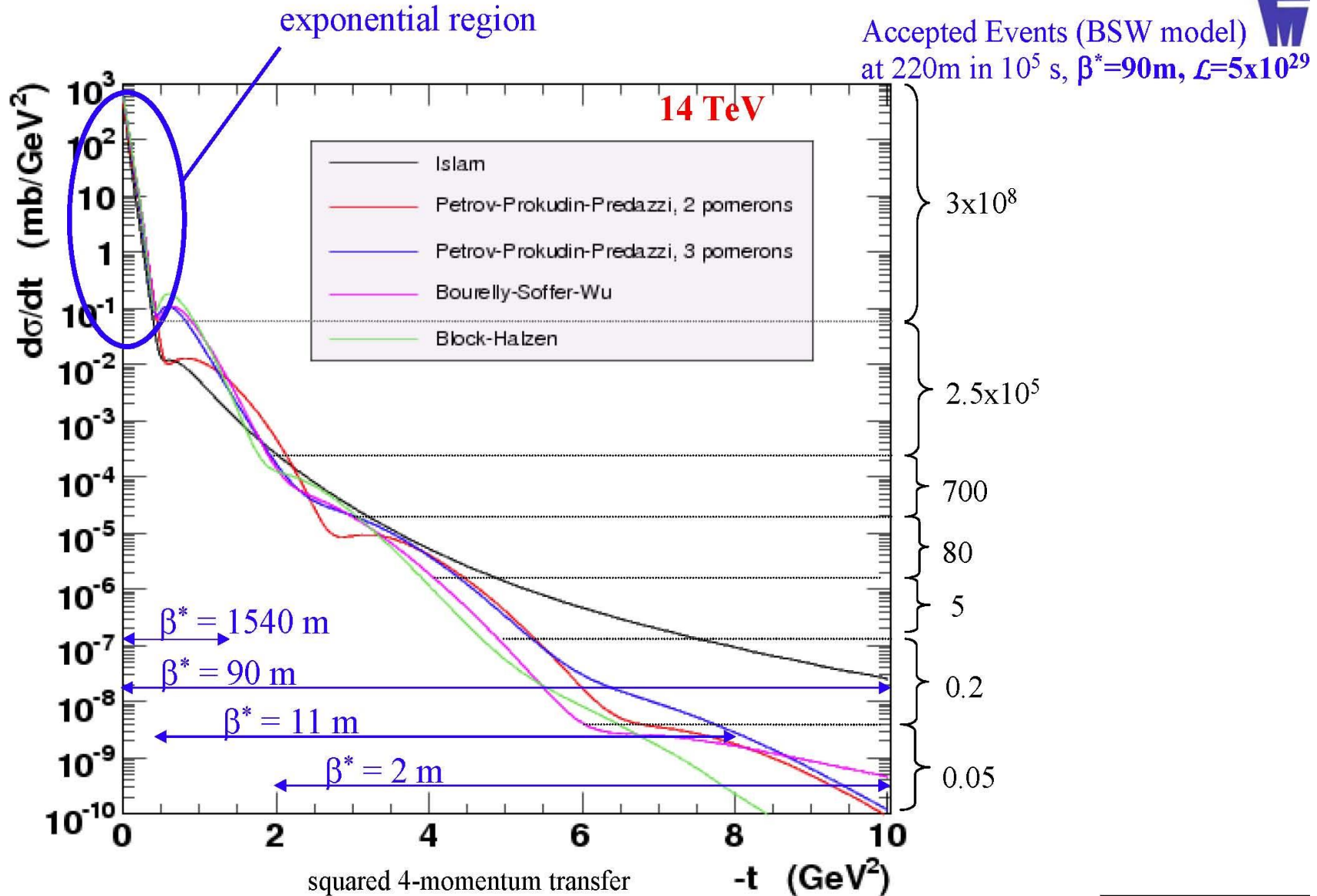
$\alpha(\mathbf{0}) \setminus \mathbf{C}$	+	-
1	P	O
1/2	f	ω

NB: The S-matrix theory (including Regge pole) is applicable to asymptotically free states only (not to quarks and gluons)!

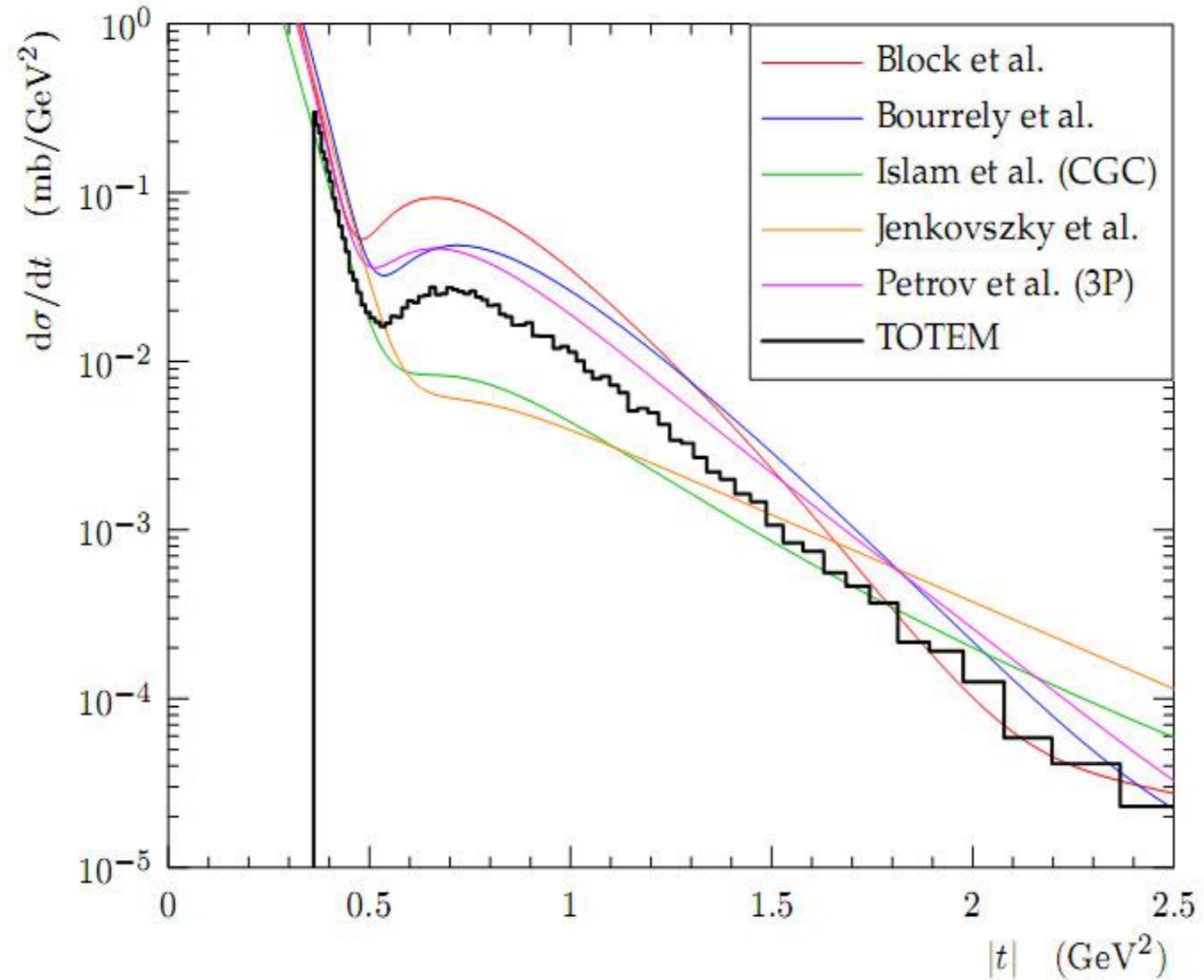
The differential cross section of elastic (EL) proton-proton scattering is:

$$\frac{d\sigma_{EL}}{dt} = A_{EL}\beta^2(t)|\eta(t)|^2 \left(\frac{s}{s_0}\right)^{2\alpha_P(t)-2},$$

where A_{EL} is a free parameter including normalization. The proton-pomeron coupling is: $\beta^2(t) = e^{bt}$, where b is a free parameter, $b \approx 1.97 \text{ GeV}^{-2}$. The pomeron trajectory is $\alpha_P(t) = 1 + \epsilon + \alpha' t$, where $\epsilon \approx 0.08$ and $\alpha' \approx 0.3 \text{ GeV}^{-2}$. The signature factor is $\eta(t) = e^{-i\frac{\pi}{2}\alpha(t)}$; its contribution to the differential cross section is $|\eta(t)|^2 = 1$, therefore we ignore it in what follows.



CERN LHC, TOTEM Collab., June 26, 2011:



The Pomeron is a dipole in the j -plane

$$A_P(s, t) = \frac{d}{d\alpha_P} \left[e^{-i\pi\alpha_P/2} G(\alpha_P) \left(s/s_0 \right)^{\alpha_P} \right] = \quad (1)$$

$$e^{-i\pi\alpha_P(t)/2} \left(s/s_0 \right)^{\alpha_P(t)} \left[G'(\alpha_P) + \left(L - i\pi/2 \right) G(\alpha_P) \right].$$

Since the first term in squared brackets determines the shape of the cone, one fixes

$$G'(\alpha_P) = -a_P e^{b_P[\alpha_P-1]}, \quad (2)$$

where $G(\alpha_P)$ is recovered by integration, and, as a consequence, the Pomeron amplitude can be rewritten in the following “geometrical” form

$$A_P(s, t) = i \frac{a_P s}{b_P s_0} \left[r_1^2(s) e^{r_1(s)[\alpha_P-1]} - \varepsilon_P r_2^2(s) e^{r_2(s)[\alpha_P-1]} \right], \quad (3)$$

where $r_1^2(s) = b_P + L - i\pi/2$, $r_2^2(s) = L - i\pi/2$, $L \equiv \ln(s/s_0)$.

$$A_{pp}^{p\bar{p}}(s, t) = P(s, t) \pm O(s, t) + f(s, t) \pm \omega(s, t) \xrightarrow{LHC} P(s, t) \pm O(s, t),$$

where P is the Pomeron contribution and O is that of the Odderon.

$$P(s, t) = i \frac{as}{bs_0} (r_1^2(s) e^{r_1^2(s)[\alpha_P(t)-1]} - \epsilon r_2^2(s) e^{r_2^2(s)[\alpha_P(t)-1]}),$$

where $r_1^2(s) = b + L - \frac{i\pi}{2}$, $r_2^2(s) = L - \frac{i\pi}{2}$ with $L \equiv \ln \frac{s}{s_0}$; $\alpha_P(t)$ is the Pomeron trajectory and a, b, s_0 and ϵ are free parameters.

P and f (second column) have positive C -parity, thus entering in the scattering amplitude with the same sign in pp and $\bar{p}p$ scattering, while the Odderon and ω (third column) have negative C -parity, thus entering pp and $\bar{p}p$ scattering with opposite signs, as shown below:

$$A(s, t)_{pp}^{\bar{p}p} = A_P(s, t) + A_f(s, t) \pm [A_\omega(s, t) + A_O(s, t)], \quad (1)$$

where the symbols P , f , O , ω stand for the relevant Regge-pole amplitudes and the super(sub)script, evidently, indicate $\bar{p}p(pp)$ scattering with the relevant choice of the signs in the sum.

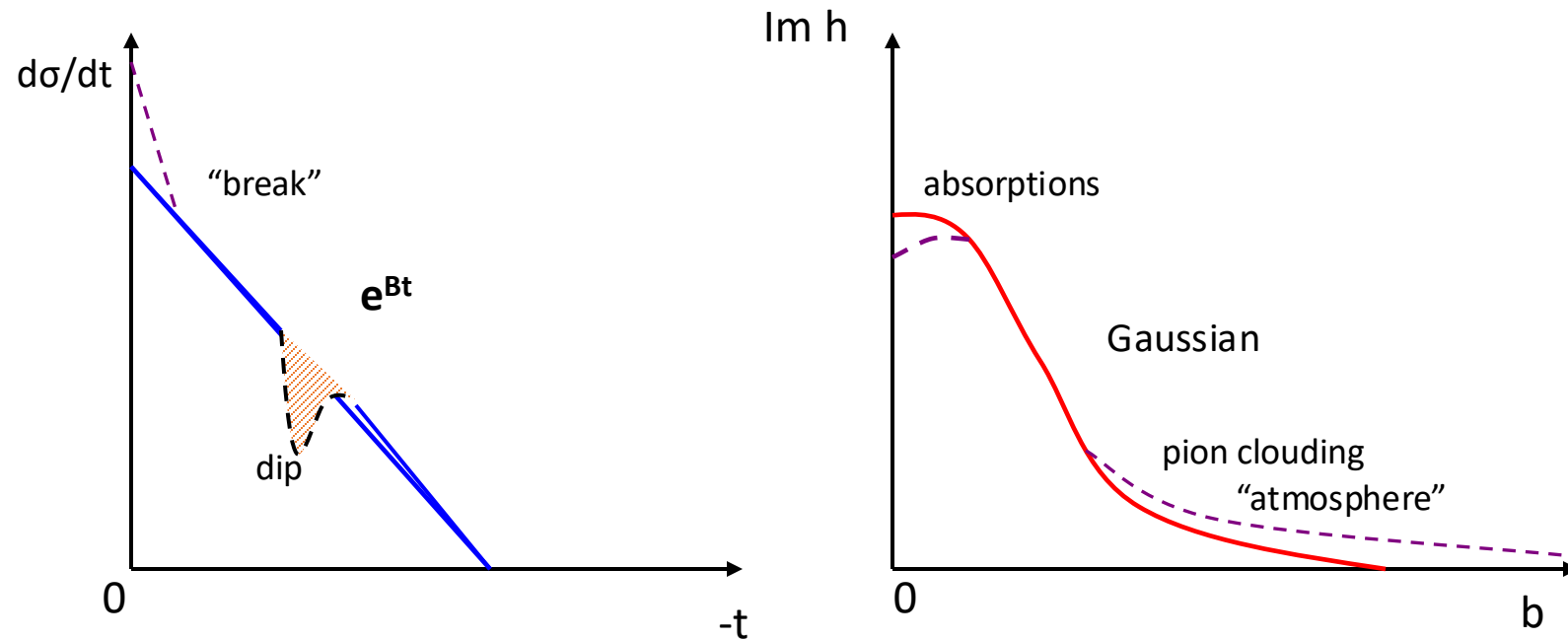
$$A_P(s, t) = \frac{d}{d\alpha_P} \left[e^{-i\pi\alpha_P/2} G(\alpha_P) \left(s/s_0 \right)^{\alpha_P} \right] =$$

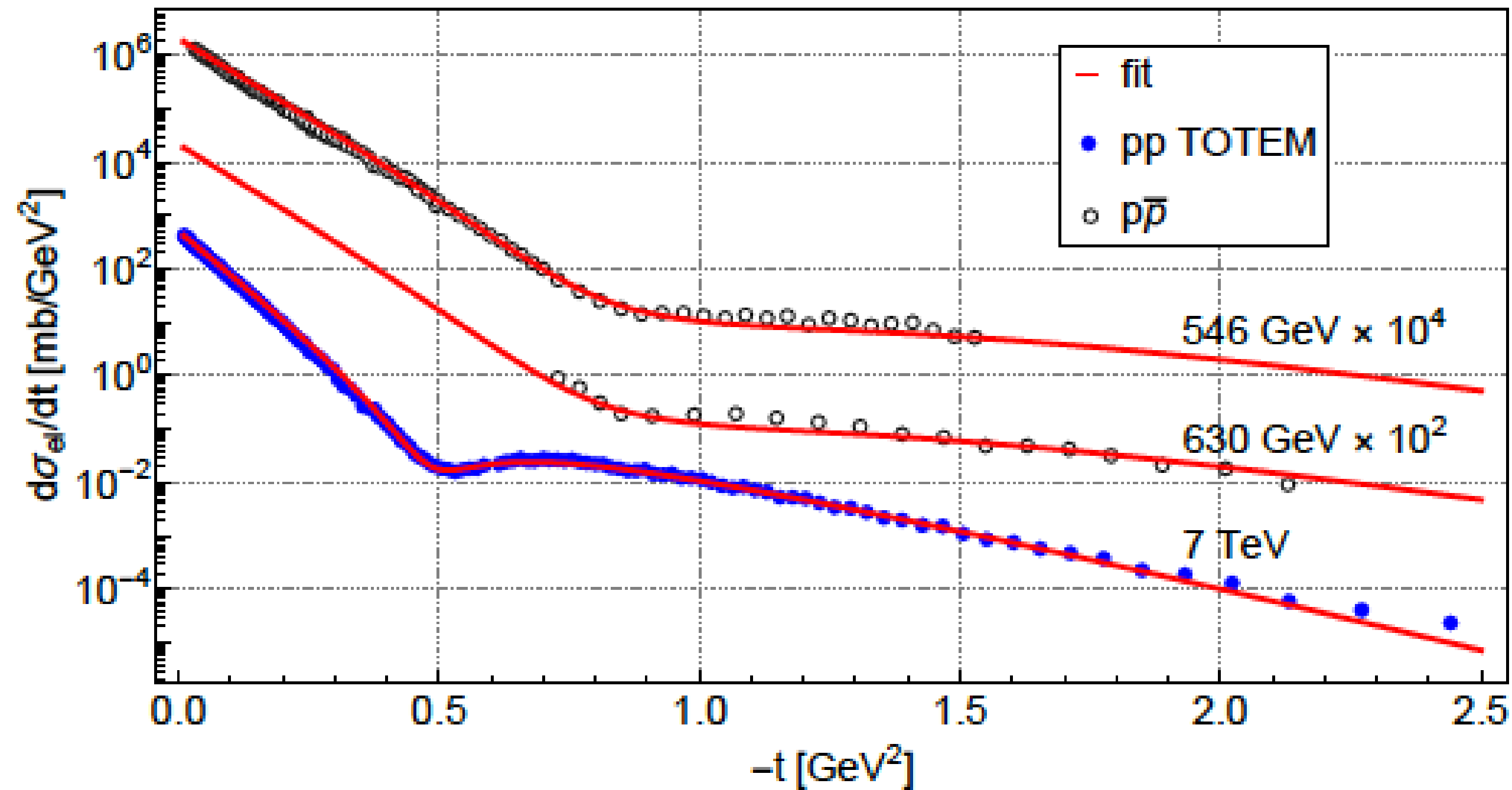
$$e^{-i\pi\alpha_P(t)/2} \left(s/s_0 \right)^{\alpha_P(t)} \left[G'(\alpha_P) + \left(L - i\pi/2 \right) G(\alpha_P) \right].$$

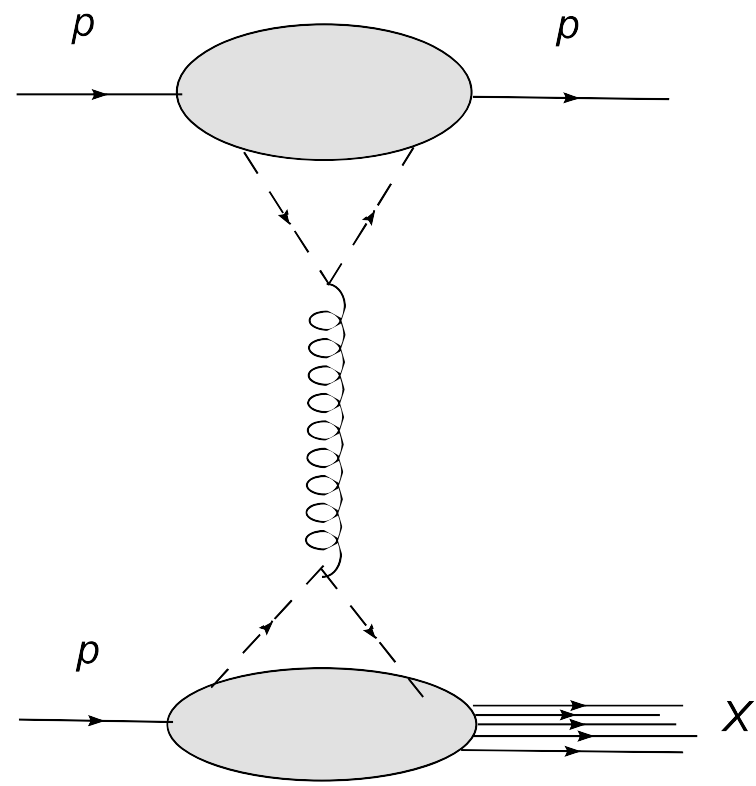
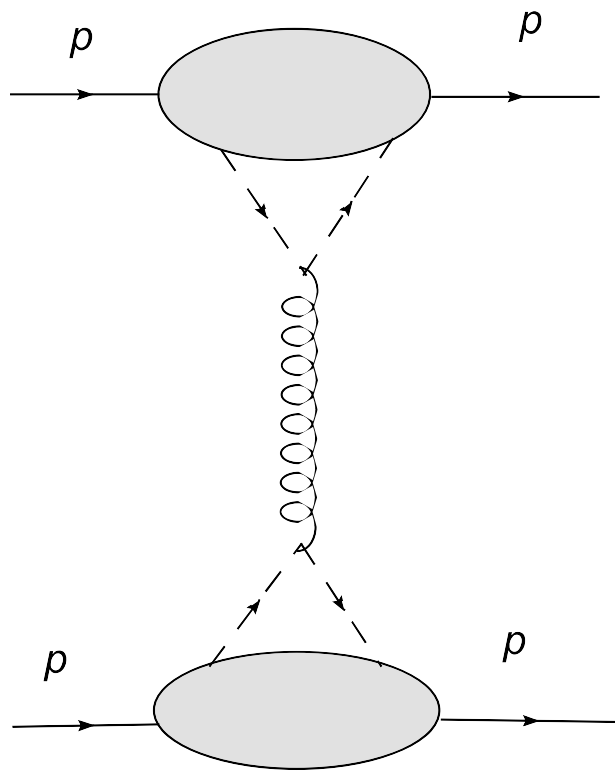
Geometrical scaling (GS), saturation and unitarity

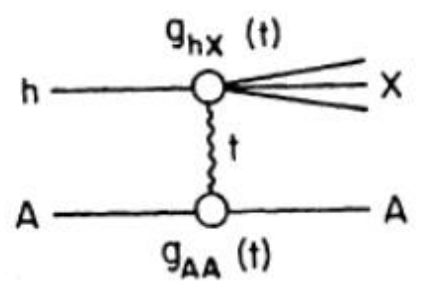
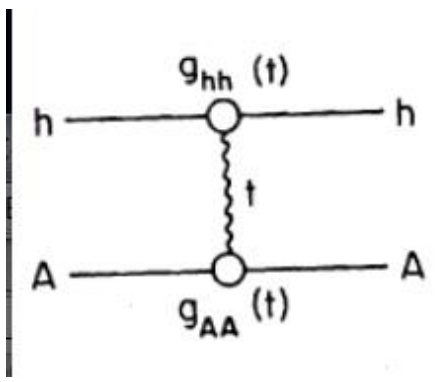
1. On-shell (hadronic) reactions ($s, t, Q^2=m^2$);

$t \leftrightarrow b$ transformation: $h(s, b) = \int_0^\infty d\sqrt{-t}\sqrt{-t}A(s, t)$
and dictionary:









$$\frac{d^2\sigma}{dtdx} = \left| \begin{array}{c} h \\ \diagup \quad \diagdown \\ t \\ \diagdown \quad \diagup \\ p \end{array} \right|^2 = \begin{array}{c} \diagdown \quad \diagup \\ t=0 \\ \diagup \quad \diagdown \\ t \end{array} = \begin{array}{c} h \\ | \\ t=0 \\ | \\ p \end{array}$$

$$\sigma_{tot} = \left| \begin{array}{c} h \\ \bigcirc \\ \diagup \quad \diagdown \\ p \end{array} \right|^2 = \begin{array}{c} \diagdown \quad \diagup \\ \bigcirc \\ \diagup \quad \diagdown \end{array} = \begin{array}{c} h \\ | \\ t=0 \\ | \\ p \end{array}$$

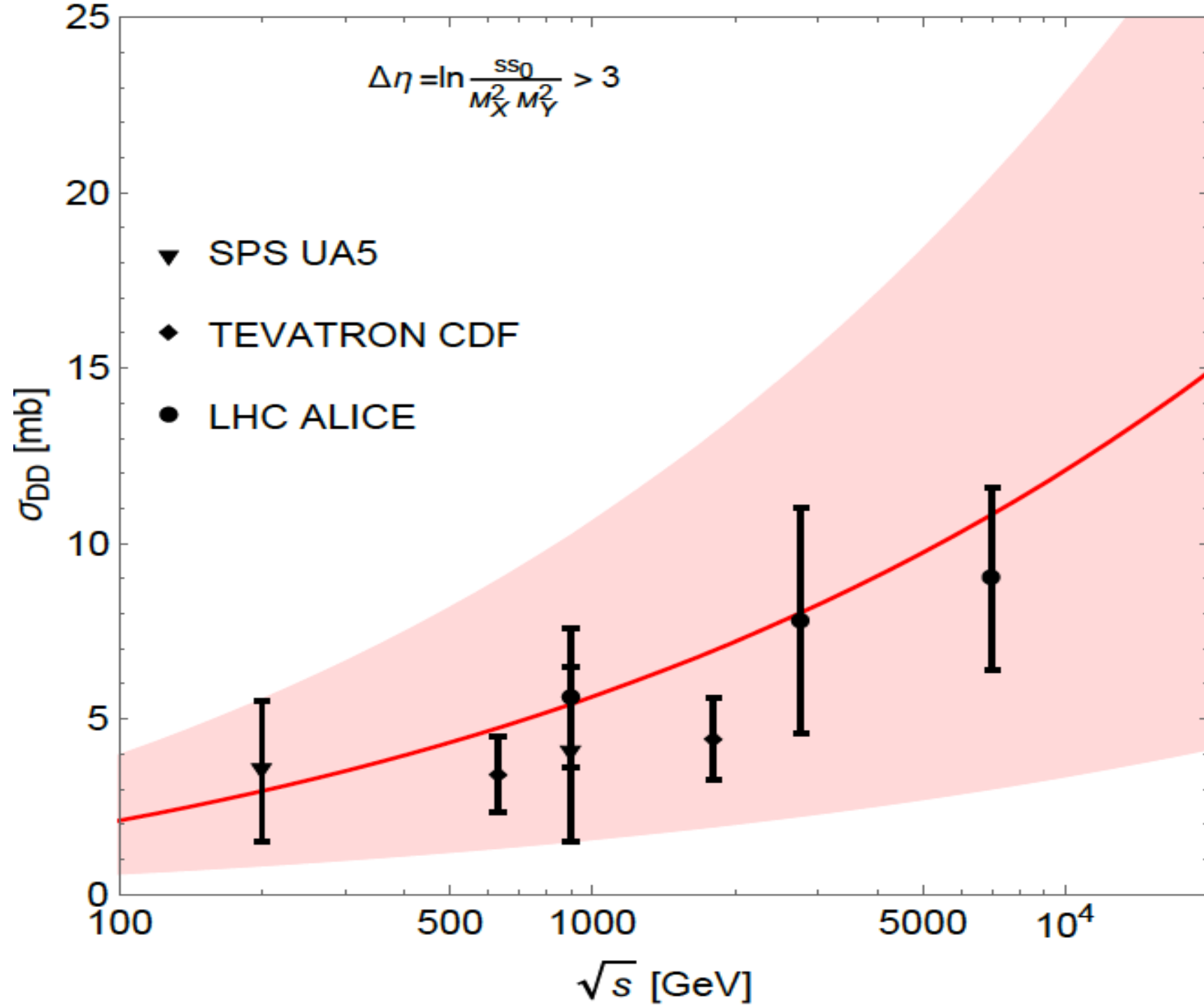
The differential cross section of proton-proton single diffraction (SD) is:

$$2 \cdot \frac{d^2 \sigma_{SD}}{dt dM_X^2} = A_{SD} \beta^2(t) \tilde{W}_2^{PP}(M_X^2, t) \left(\frac{s}{M_X^2} \right)^{2\alpha_P(t)-2},$$

where $\tilde{W}_2^{PP}(M_X^2, t) \sim F_2^P(M_X^2, t)$.

Similarly, the differential cross section of proton-proton double diffraction (DD) process is:

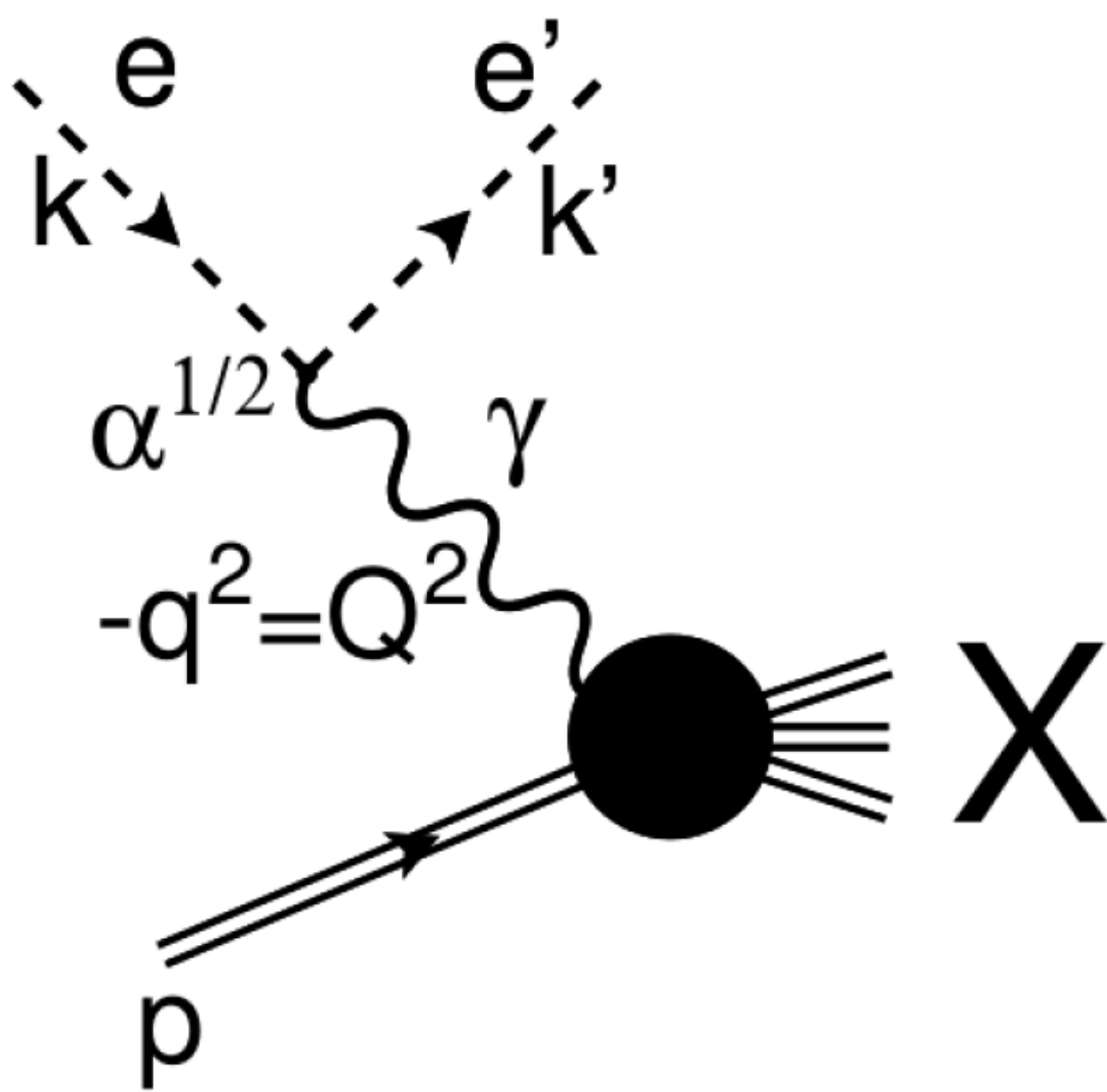
$$\frac{d^3 \sigma_{DD}}{dt dM_X^2 dM_Y^2} = A_{DD} \tilde{W}_2^{PP}(M_X^2, t) \tilde{W}_2^{PP}(M_Y^2, t) \left(\frac{ss_0}{M_X^2 M_Y^2} \right)^{2\alpha_P(t)-2}.$$



Similar to the case of elastic scattering, the double differential cross section for the SDD reaction, by Regge factorization, can be written as

$$\frac{d^2\sigma}{dt dM_X^2} = \frac{9\beta^4 [F^p(t)]^2}{4\pi \sin^2[\pi\alpha_P(t)/2]} (s/M_X^2)^{2\alpha_P(t)-2} \times \left[\frac{W_2}{2m} \left(1 - M_X^2/s\right) - mW_1(t + 2m^2)/s^2 \right], \quad (1)$$

where W_i , $i = 1, 2$ are related to the structure functions of the nucleon and $W_2 \gg W_1$. For high M_X^2 , the $W_{1,2}$ are Regge-behaved, while for small M_X^2 their behavior is dominated by nucleon resonances. The knowledge of the inelastic form factors (or transition amplitudes) is crucial for the calculation of low-mass diffraction dissociation.



Similar to the case of elastic scattering, the Dipole SD amplitude is recovered by differentiation (for simplicity (we set $s_0 = 1 \text{ GeV}^2$)):

$$T_{DP} = \frac{d}{d\alpha} T(s, t, M^2) = e^{-i\pi\alpha/2} s^\alpha [G' F_2 + F_2' G + (L - i\pi/2) G F_2],$$

where $L = \ln(s/(1 \text{ GeV}^2))$ and the primes imply differentiation in $\alpha(t)$.

The extrema (dip(s) and bump(s)) are calculated by a standard procedure, i.e. by equating to zero the derivative of the cross section:

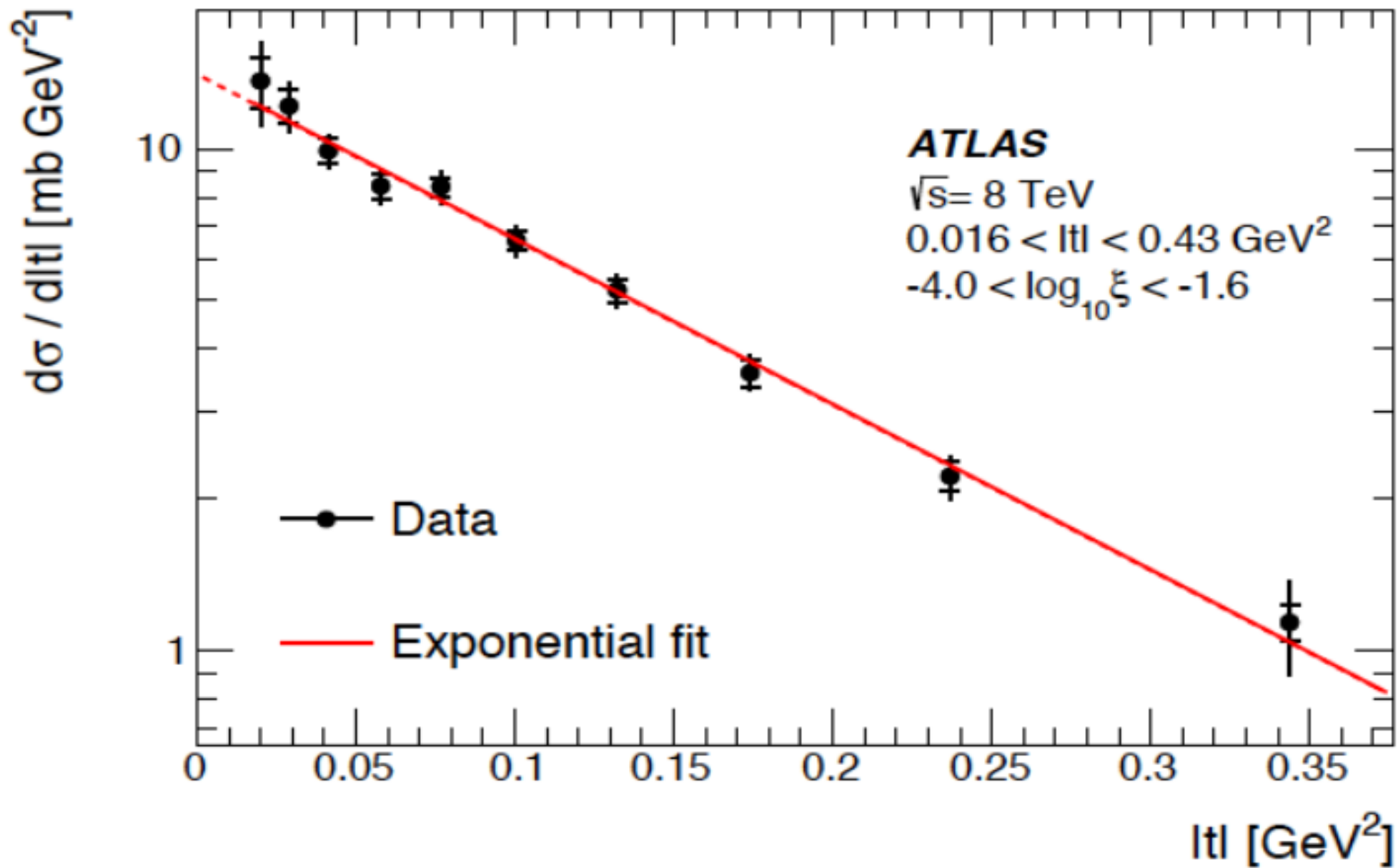
$$\frac{d|T_{SD}|^2}{d\alpha} = \frac{1}{2} \left(\frac{s^2}{s_0^2} \right)^\alpha \left[GF' + F(LG + G') \right] \left[8F'G' + 4G(2LF' + F'') \right. \\ \left. + F(4L^2 + \pi^2)G + 4(2LG' + G'') \right],$$

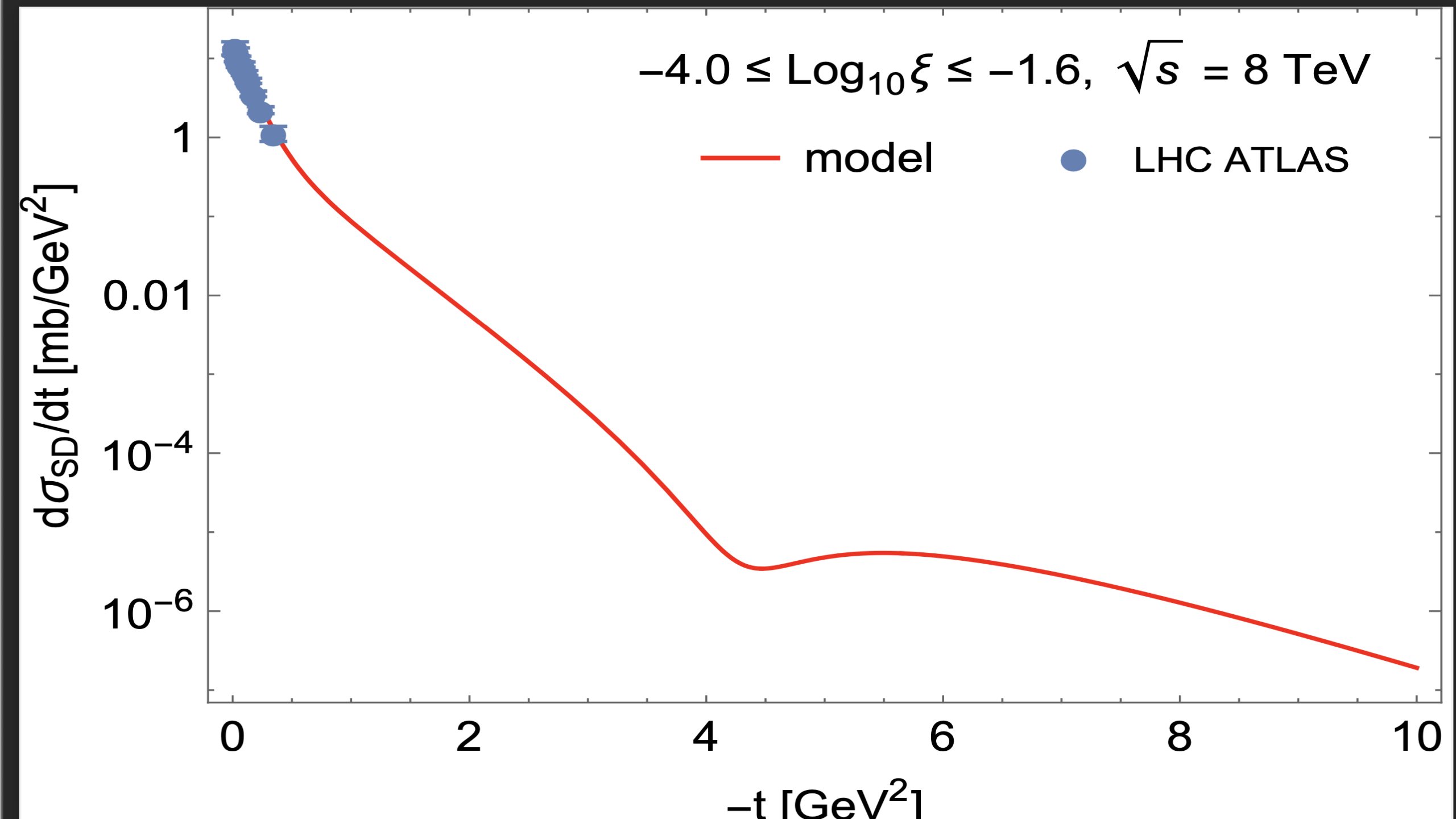
where $L = \ln(s/s_0)$ and the primes imply differentiation in $\alpha(t)$.

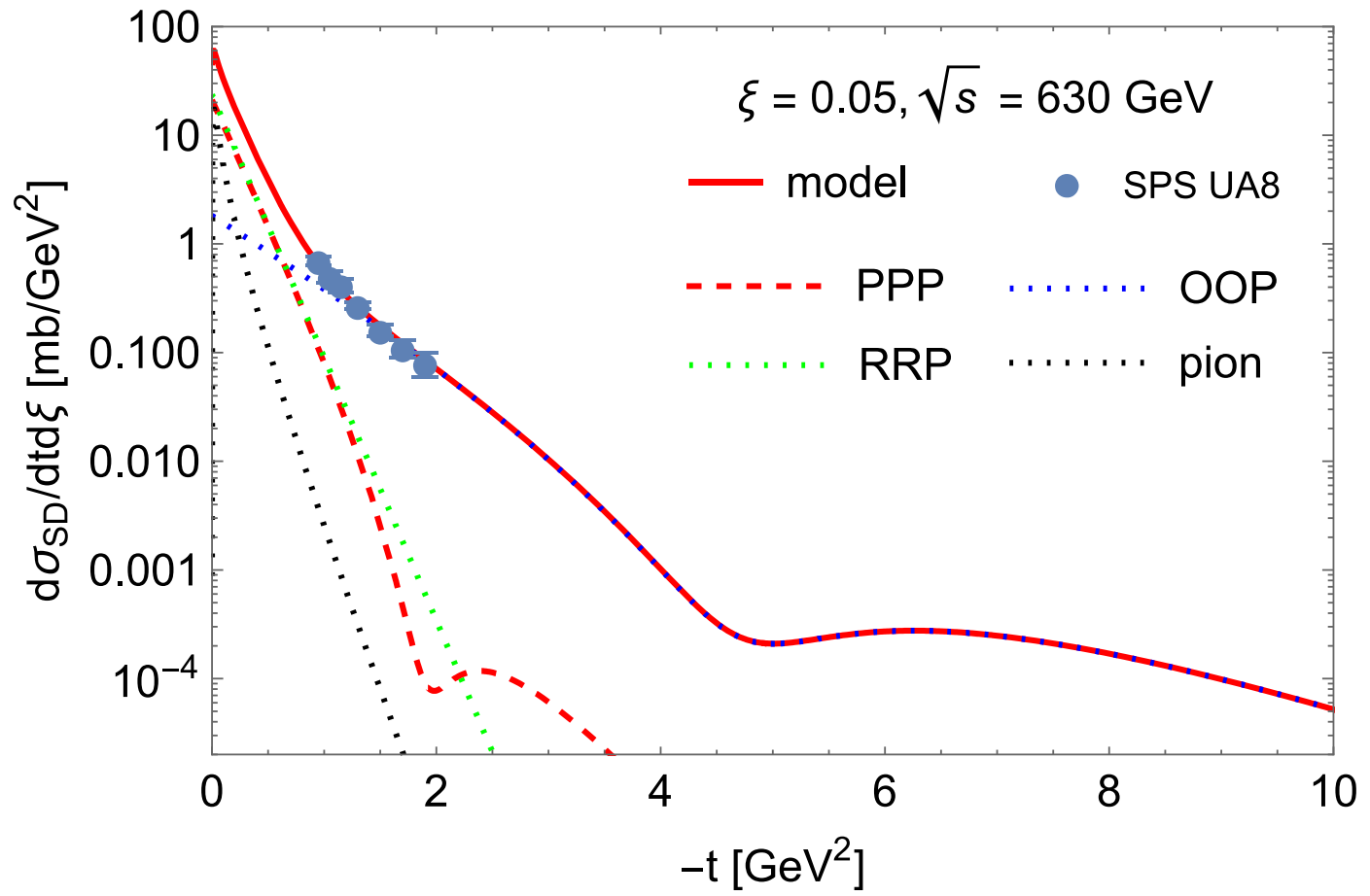
Similar to the case of elastic scattering, the Dipole SD amplitude is recovered by differentiation (for simplicity (we set $s_0 = 1 \text{ GeV}^2$)):

$$T_{DP} = \frac{d}{d\alpha} T(s, t, M^2) = e^{-i\pi\alpha/2} s^\alpha [G' F_2 + F_2' G + (L - i\pi/2) G F_2], \quad (19)$$

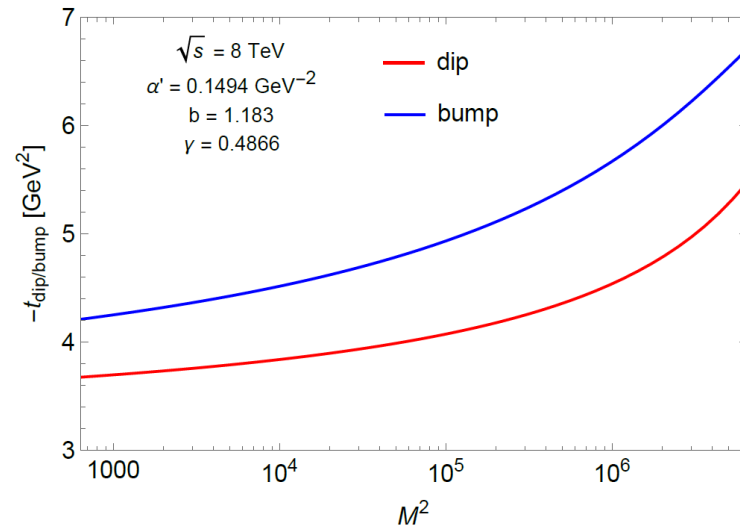
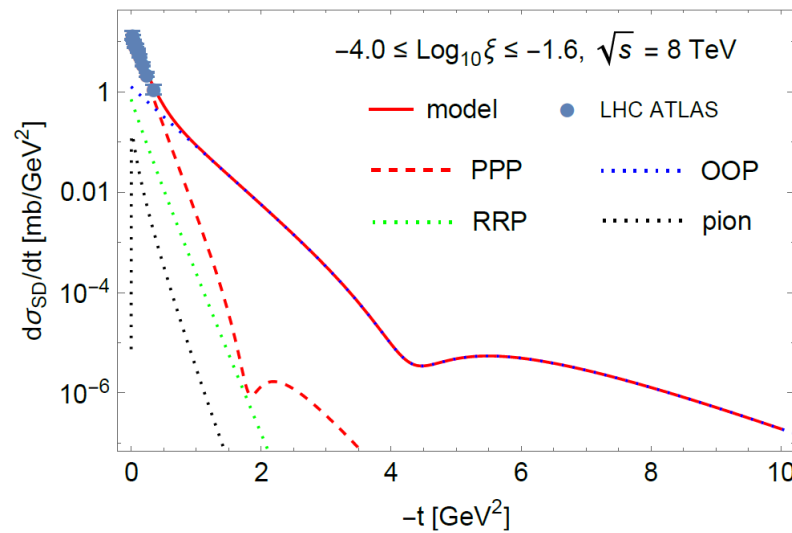
where $L = \ln(s/(1 \text{ GeV}^2))$ and the primes imply differentiation in $\alpha(t)$.







dip-bump in $-t$ at LHC



$$\begin{aligned}
 & -t_{\text{dip}}^{\text{SS}} = \frac{1}{\alpha_{\text{bb}}} \ln \frac{b + U_{\text{SS}}}{\mathcal{N} U_{\text{SS}}} \\
 & -t_{\text{bump}}^{\text{SS}} = \frac{1}{\alpha_{\text{bb}}} \ln \frac{4(b + U_{\text{SS}})^2 + i^2}{\mathcal{N} b (4U_{\text{SS}}^2 + i^2)} \\
 & U_{\text{SS}} = \ln(ss'/M^2)
 \end{aligned}$$

Conclusions

Theoretical and experimental search for structures in proton diffractive dissociation at the LHC kinematical region (and elsewhere) provide new perspectives in high-energy physics.

Make your prediction, do your measurements!

Thank you for your attention!