

# Looking for BFKL resummation and saturation at the LHC

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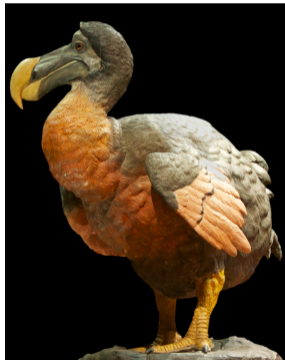
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DiffLowx 2024

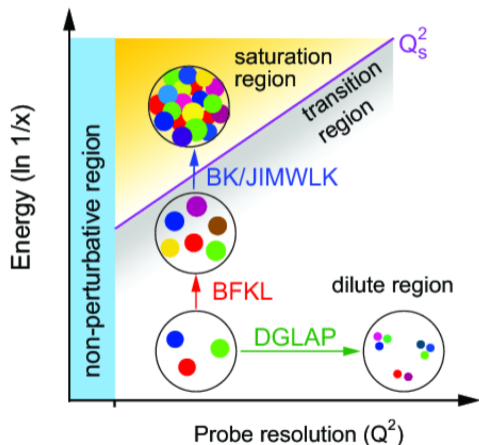


September 8-14, Palermo, Sicily, Italy

- Vector meson production (in collaboration with J. Penttala)
- Have we seen saturation in data at the LHC?
- Jet production in the very forward direction

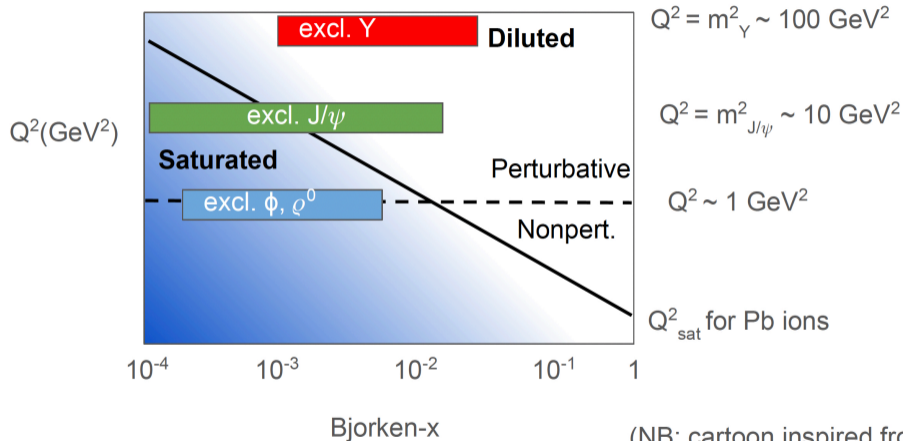


# Looking for BFKL resummation /saturation effects



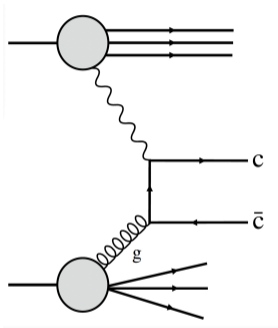
- DGLAP (Dokshitzer Gribov Lipatov Altarelli Parisi): Evolution in resolution  $Q^2$ , resums terms in  $\alpha_S \log Q^2 \rightarrow$  resolving "smaller" partons at high  $Q$
- BFKL (Balitski Fadin Kuraev Lipatov (BFKL): Evolution in energy  $x$ , resums terms in  $\alpha_S \log 1/x \rightarrow$  Large parton densities at small  $x$
- Saturation region at very small  $x$
- Important to understand QCD evolution, parton densities

# Looking for saturation effects: vector meson channel



(NB: cartoon inspired from Wei's [plot](#))

# Forward jets, $J/\psi$ , $c$ and $b$ productions: observables for saturation

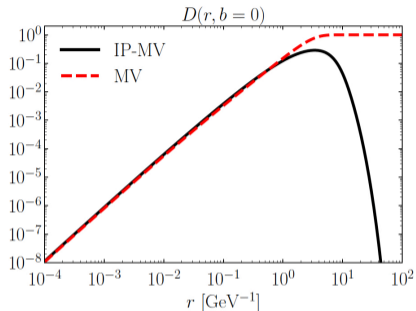
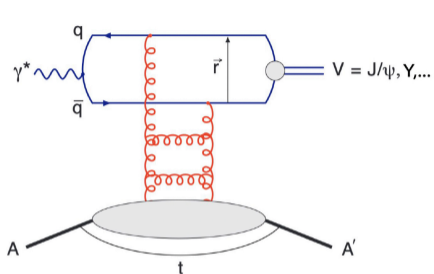


- What do we need to see saturation at the LHC?
- $\gamma Pb$   $c$ ,  $b$ ,  $J/\psi$  are ideal probes for low- $x$  physics

$$x = \frac{m_{c\bar{c}}}{\sqrt{s_{NN}}} \exp(-y_c)$$

- We can reach low  $x$  values of  $10^{-4}$  or smaller
- We need a low scale (to be below  $Q_S$ ), and this is why  $c$  or  $b$  where one can go to very low  $p_T$  or  $J/\psi$  (low mass vector mesons) are ideal while still being in the perturbative region
- $d\sigma/dW$  is the best observable while  $d\sigma/dy$  presents the difficulties to mix up low and high  $x$

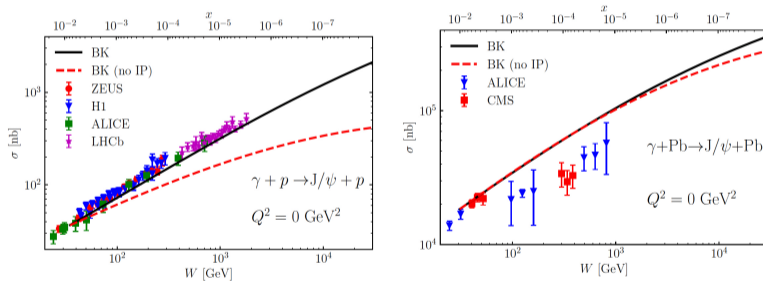
# Looking for saturation: vector meson production



- Compute exclusive vector meson production in  $\gamma p$  (HERA, EIC and pPb LHC) and  $\gamma Pb$  (EIC and Pb Pb LHC) where we probe the gluon density in p or Pb
- Saturation effects are expected to happen in Pb Pb, not in p Pb
- Computation: Factorize the  $\gamma \rightarrow q\bar{q}$  part from the coupling to the proton: cross section proportional to  $(xG)^2$  at LO
- Take into account  $b$  impact parameter dependence in dipole amplitude

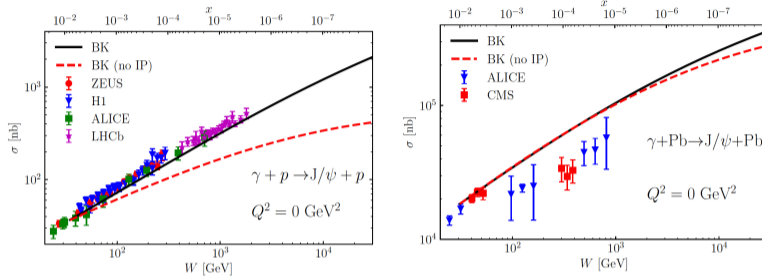
# High energy evolution

$$\partial_Y D(\mathbf{x}_0, \mathbf{x}_1, Y) = \int d^2\mathbf{x}_2 K_{\text{BK}}(\mathbf{x}_0, \mathbf{x}_1, \mathbf{x}_2) \left[ D(\mathbf{x}_0, \mathbf{x}_2, Y) + D(\mathbf{x}_2, \mathbf{x}_1, Y) - D(\mathbf{x}_0, \mathbf{x}_1, Y) - D(\mathbf{x}_0, \mathbf{x}_2, Y)D(\mathbf{x}_2, \mathbf{x}_1, Y) \right]$$



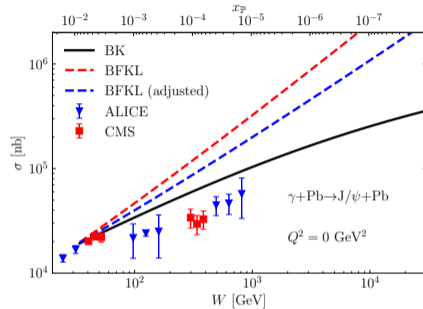
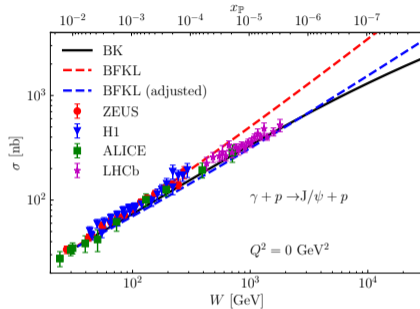
- Use Balitsky Kovchegov (BK) equation to describe the dipole evolution (so including saturation effects)

# High energy evolution



- Huge difference between taking into account  $b$  impact parameter dependence or not for  $\gamma p$  (Penttala, Salazar)
- Much smaller differences for  $\gamma Pb$ : nucleus much larger than proton and neglecting impact parameter dependence is more justified
- Possibility to determine effects of saturation by neglecting the gluon recombination term in BK: equivalent of linear BFKL equation

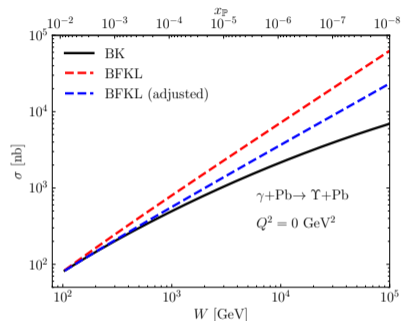
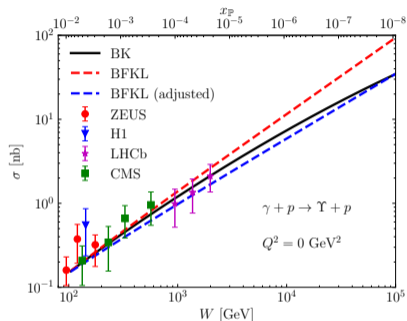
# Looking for saturation: $J/\psi$ vector meson production



- BFKL and BK CGC predictions after taking into account  $b$ -dependence (J. Penttala, C. R.)
- $J/\psi$  production in  $pPb$ : small differences between BK and BFKL, BK slightly favored
- Large differences between BK and BFKL in PbPb collisions

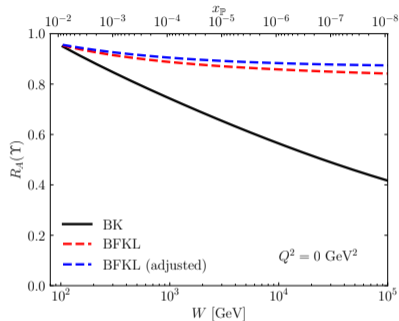
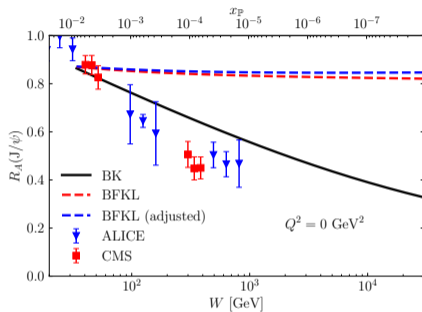


# Looking for saturation: $\Upsilon$ vector meson production



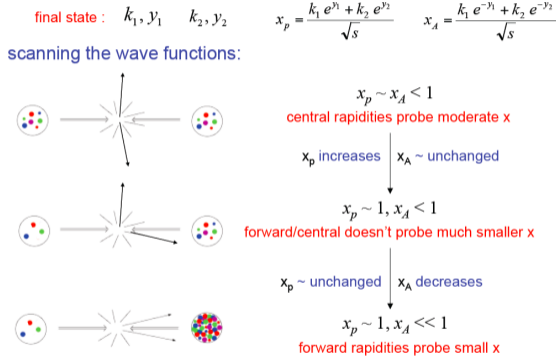
- $\Upsilon$  vector meson production: smaller differences between BFKL and BK in pPb or PbPb collisions
- Looking for additional observables: charm, etc

# Looking for saturation: $J/\psi$ and $\Upsilon$ nuclear suppression factor



- Large nuclear suppression factor for  $J/\psi$  in PbPb collisions
- Have we seen saturation in Pb Pb?
- Importance to have precise measurements of pp interactions as a reference at the same  $\sqrt{s}$

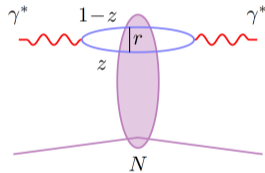
# Saturation at the LHC using forward jets: Use pA and AA data



- If we want to see saturation effects, we need a dense object (Pb) and to go to very low  $x$ : measure jets in very forward direction
- Saturation effects: Measure two jets in very forward calorimeter (CASTOR in CMS, FOCAL project in ALICE)
- Use pp and pA runs (inclusive measurements,  $p$  and Pb are destroyed most of the time)
- Possibility to look for quark gluon plasma formation using  $t\bar{t}$  production in PbPb

# Dipole amplitude from HERA data

$$\sigma_{T,L}(x, Q^2) = 2 \int dz \int d^2\mathbf{b} d^2\mathbf{r} \left| \Psi_{L,T}^\gamma(Q^2, \mathbf{r}) \right|^2 \mathcal{N}(\mathbf{r}, \mathbf{b}, x)$$
$$\Rightarrow \sigma_p \int dz \int d^2\mathbf{r} \left| \Psi_{L,T}^\gamma(Q^2, \mathbf{r}) \right|^2 \mathcal{N}(\mathbf{r}, x)$$



dipole-shockwave interaction schematic

- TMDs can be computed using either  $b$ -dependent or  $b$ -independent  $N$

- We use AAMQS parametrization (A non-linear QCD analysis of new HERA data at small- $x$ , ArXiv 1012.4408) (no impact parameter dependence)
- Factorisation of a photon into a  $q\bar{q}$  dipole from the  $q\bar{q}$  scattering off a dense nuclear target
- Balitsky Kovchegov equation to evolve the parton distributions at small  $x$
- IPSat model to describe the impact parameter dependence (no BK evolution)
- Our model: mixture of AAMQS and IPSat

## Dependence on impact parameter

$$S_{\perp} \mathcal{N}(\{G(r, x)\}) \rightarrow \int d^2 \mathbf{b} \mathcal{N}(\{G(r, x, b)\}) = \begin{cases} S_{\perp} \frac{\eta}{\sigma} \int d^2 \mathbf{b} (1 - \exp[\sigma G(r, x) T(\mathbf{b})]), & T(b) > T_{\min} \\ 0, & \text{otherwise} \end{cases}$$

- We reintroduce the  $b$  dependence into the  $b$ -averaged dipole fits (parameters:  $\eta$ ,  $\sigma$ ,  $T_{\min}$ )
- For protons, choose (IPSat model hep-ph/0304189):

$$T_p(b) = \frac{\exp(-b^2/2B_G)}{2\pi B_G}$$

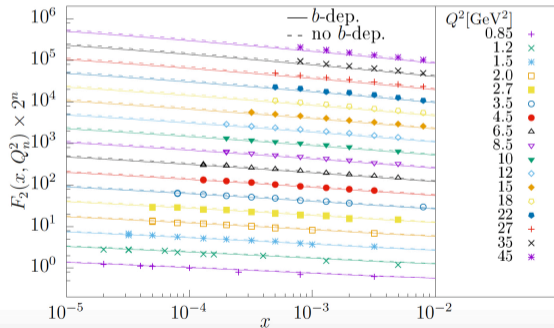
- For nuclei, sum of each proton and neutron gaussian thickness

$$T(b) = \sum_{i=1}^A T_{p/n}(b_i - b)$$

where the nucleon impact parameters ( $b_i$ 's) are generated stochastically

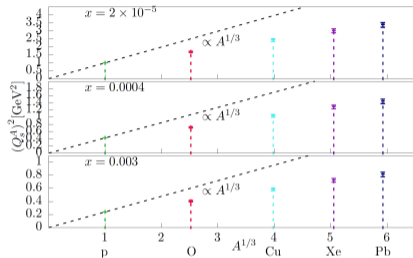
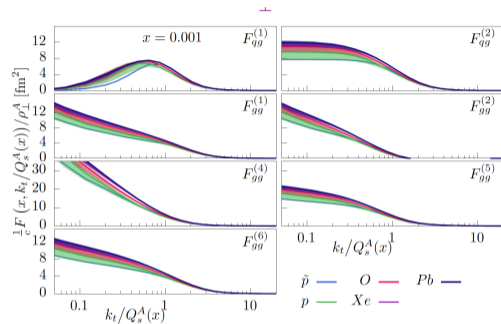
# Matching $b$ -dependent and independent proton TMDs: Recovering $F_2$ from HERA

$$F_2(x, Q^2) = \frac{Q^2}{4\pi^2\alpha_{em}} \left[ \sigma_T(x, Q^2) + \sigma_L(x, Q^2) \right]$$



- Cross check of our model: get a good description of  $F_2$  measurement at HERA
- Good description using either  $b$ -dependent or  $b$ -independent approaches, leads to same predictions

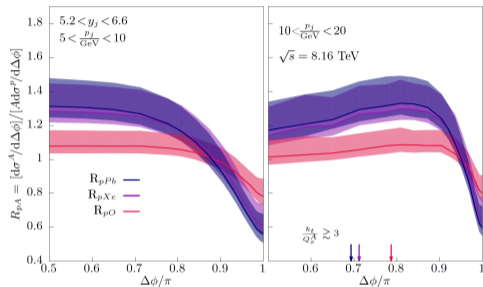
# Use of nuclear Transverse Momentum Distributions (TMDs)



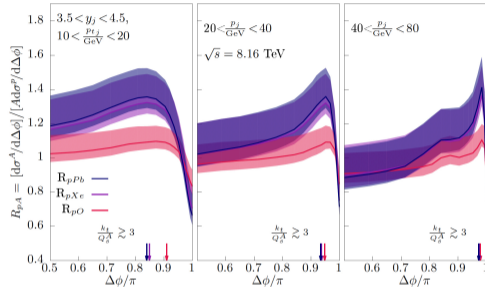
- Nuclear TMDs are calculated by swapping  $T_p$  and  $T_A$
- Comparison between the saturation scales given by our model (using the  $b$ -dependence) and the naive one with the usual  $A^{1/3}$  dependence: we get lower saturation scales

# Nuclear modification factor

Nuclear mod. fac. in very forward Castor/Focal kinematics



Nuclear mod. fac. in Forward CMS kinematics



- Nuclear modification factors for two detector configurations:

- CASTOR/FOCAL kinematics:  $5.2 < y_{jet}, < 6.6$  and  $p_T^{jet}$  5 to 10 GeV, or 10 to 20 GeV
- “Forward CMS” kinematics:  $3.5 < y_{jet}, < 4.5$  and  $p_T^{jet}$  10 to 20 GeV, 20 to 40 GeV or 40 to 80 GeV

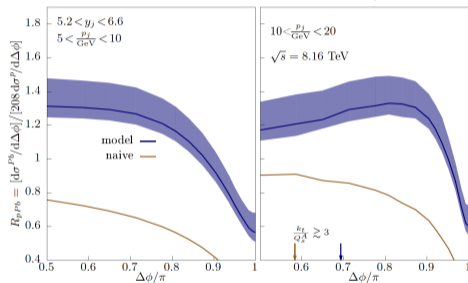
- As expected, decorrelation more pronounced for higher  $y$  and lower  $p_T$

- F. Deganutti, C. Royon, S. Schlichting, JHEP 01 (2024) 159

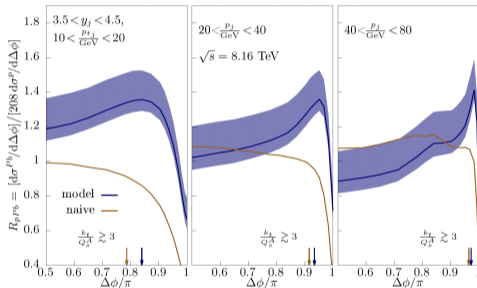


# Nuclear modification factor: model versus naive saturation scale

Nuclear mod. fac. in very forward Castor/Focal kinematics



Nuclear mod. fac. in Forward CMS kinematics

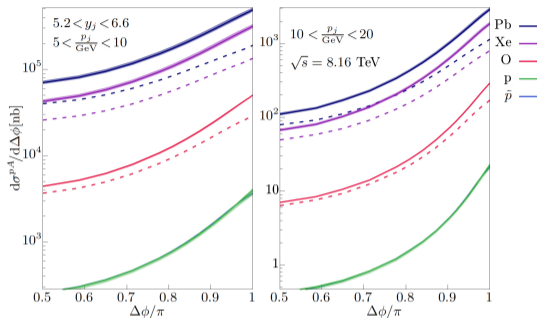


- As expected, large difference between model and naive saturation scales

- Saturation at the LHC: use dedicated observables allowing to access low mass, low  $x$  such as very forward jets, vector meson ( $J/\psi$ ),  $c$  and  $b$  production
- **Have we seen already saturation at the LHC in  $J/\psi$  production?**
- Predictions using impact parameter dependence on  $\Delta\phi$  decorrelation between jets in the very forward direction (FOCAL)

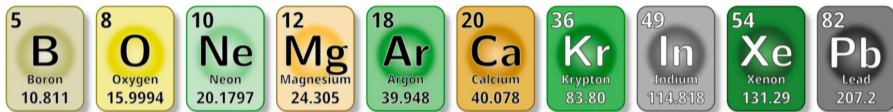


# Looking for saturation: very forward jet production



- Dedicated observables to look for saturation: particle/jet production in the forward region (F. Deganutti, C. Royon, S. Schlichting, JHEP 01 (2024) 159)
- Jet decorrelation predicted to be more pronounced for softer and higher rapidity jets
- Our model (including a full  $b$ -dependence calculation) predicts less decorrelation than using the naive scaling
- Can be tested using CASTOR (CMS) data or incoming FOCAL (ALICE) ones

# Using different heavy ions at the LHC?



- Possibility to use lighter heavy ions at the LHC beyond run 4
- This would mean starting around 2035, so in overlap with the EIC
- Is it potentially interesting to compare for instance very forward jets,  $c$  and  $b$  production,  $J/\psi$  and  $\Upsilon$  production at higher energies of the LHC to see probably no saturation effects for light ions, and saturation for heavy ions?
- How much lumi would be needed?
- Can we measure  $Q_s$  for different ions using these data (and compare to EIC)?