

# Exploring high-multiplicity events in high-energy proton-proton collisions

PRC 106 (2022) 6, 065206 / EPJA 60 (2024) 3, 54 / PRD 109 (2024) 9, 094035

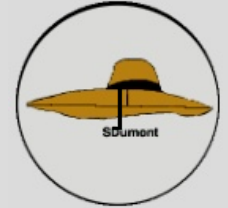
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LNCC/SDumont  
UFGD



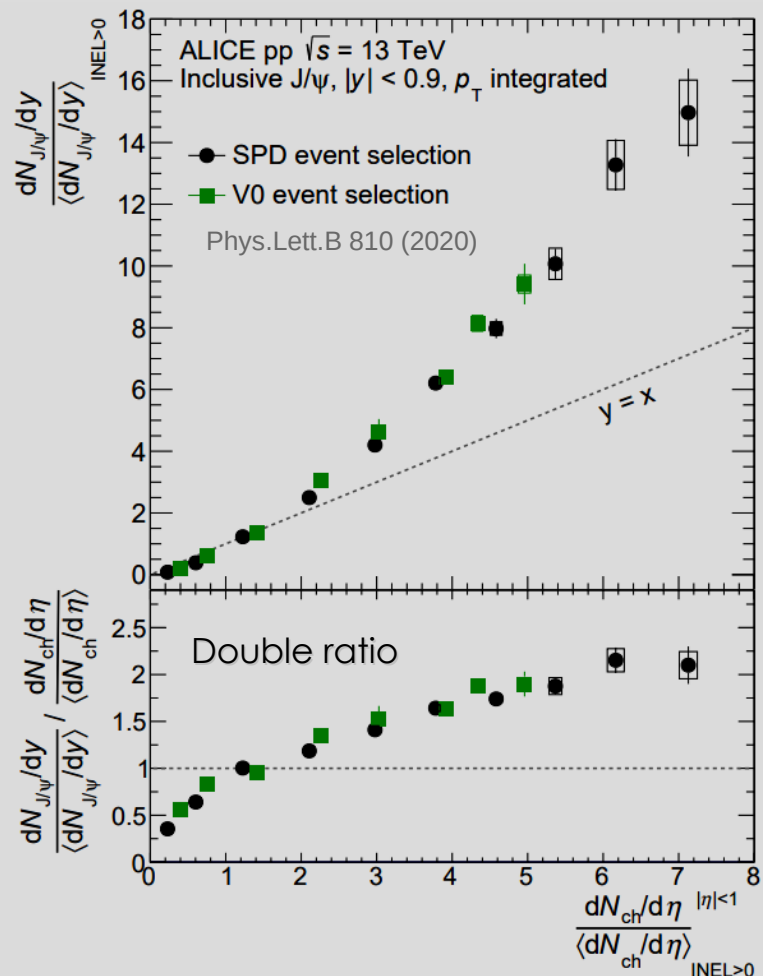
Partial support: 2017/05685-2  
& 2021/04924-9

Diffraction and Low-x 2024 8 – 14, Sept, 2024

Multiplicity: counting of (produced) particles

Recent experimental results: **stronger increase in identified particle multiplicities when compared to the minimum-bias case**

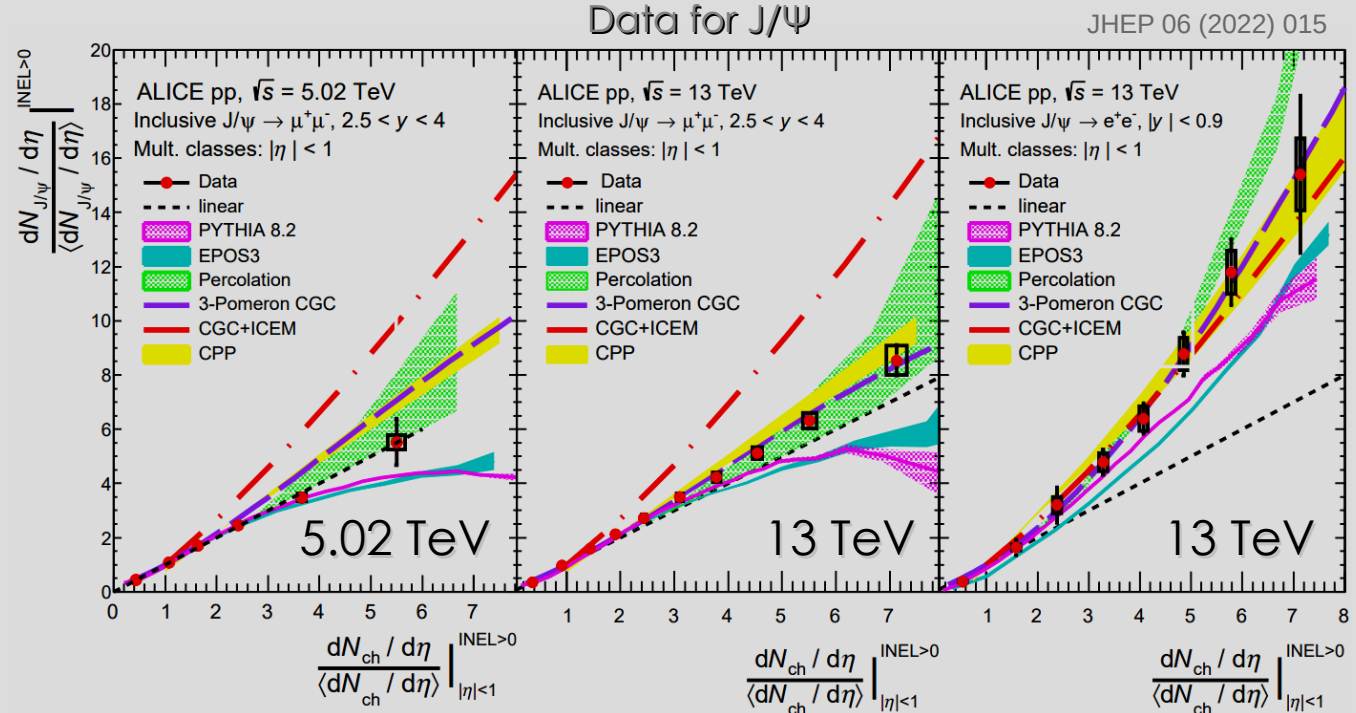
Two questions may be addressed



1. Comparison with available models: **no unified agreement w.r.t. data**

2. Beyond a quantitative description: **what causes this change in behavior?**

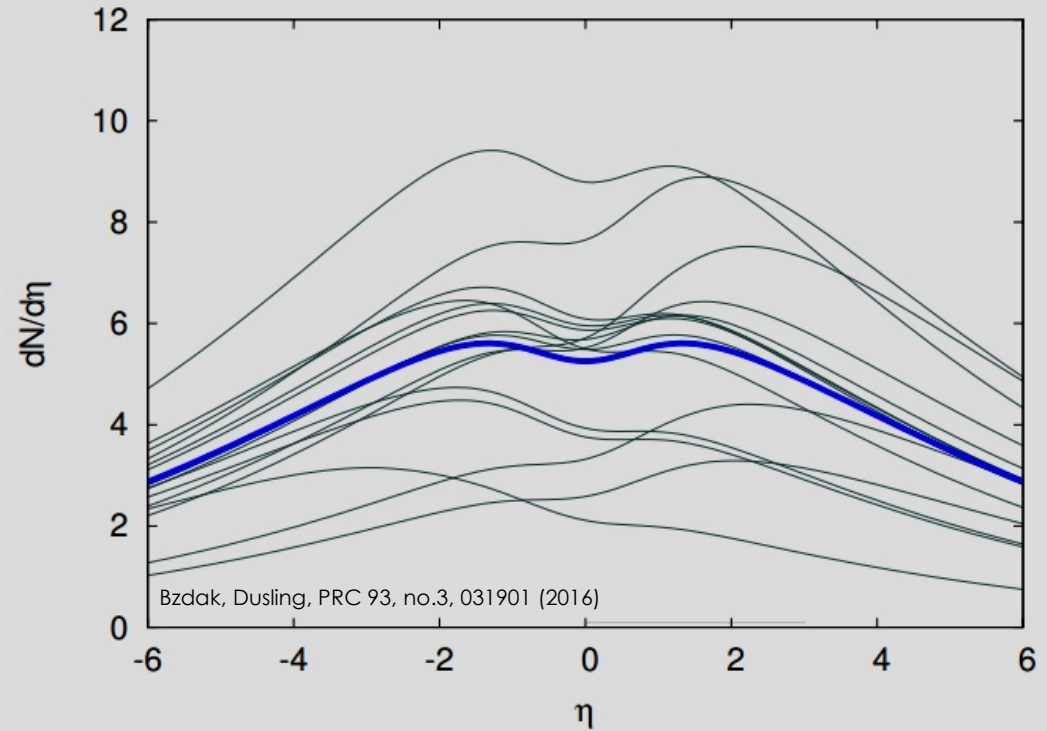
**Is it an initial-state effect?**  
**A final-state effect?**  
**A mixture of both?**



Proton-proton collisions:  
average result is symmetric,  
as expected

Event-by-event color charge  
fluctuations may produce  
asymmetric collisions

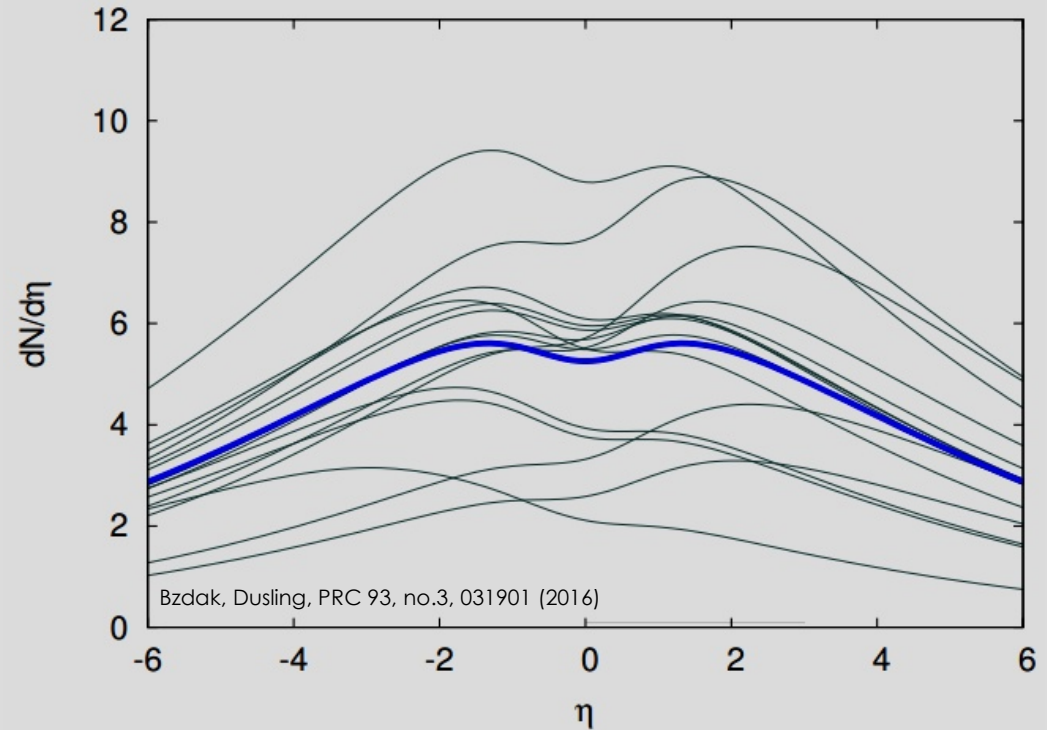
Could be the case for  
multiplicities larger than  
average, excluding highest  
multiplicities



Will make two assumptions:

1. The production mechanism is the same for low and high multiplicities events

2. Final multiplicity proportional to the initial partonic configuration: high multiplicity events have larger  $Q_s$  than minimum bias events



$$\frac{dN_h}{dyd^2p_T} = \frac{K}{(2\pi)^2} \int_{x_F}^1 \frac{dz}{z^2} \left[ f_{q/p}(x_1, \mu^2) \tilde{N}_F \left( \frac{p_T}{z}, x_2 \right) D_{h/q} (z, \mu_{FF}^2) + f_{g/p}(x_1, \mu^2) \tilde{N}_A \left( \frac{p_T}{z}, x_2 \right) D_{h/g} (z, \mu_{FF}^2) \right]$$

Dipole scattering amplitude

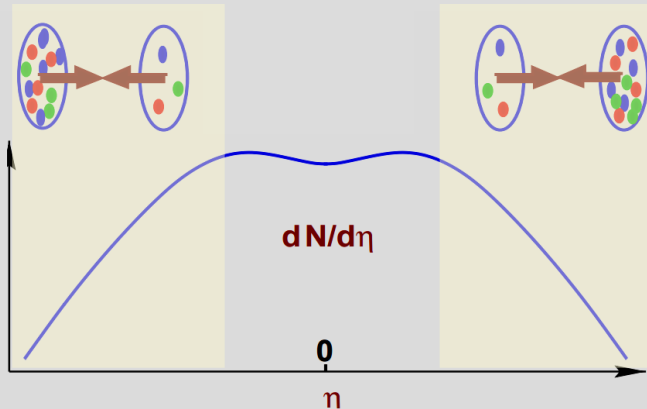
“Hybrid formalism”  
(collinear + TMD)

$$\tilde{N}_{A,F}(x, p_T) = \int d^2r e^{ip_T \cdot \vec{r}} [1 - \mathcal{N}_{A,\mathcal{F}}(x, r)]$$

$$x_{1,2} = (p_T/\sqrt{s})\exp(\pm y)$$

Employed to describe particle production @ RHIC, LHC

Dumitru, Hayashigaki, Jalilian-Marian, NPA 765, 464-482 (2006); Boer, Utermann, Wessels, PRD 77, 054014 (2008); Betemps, Goncalves, JHEP 09, 019 (2008); Albacete, Marquet, PLB 687, 174-179 (2010); Altinoluk, Kovner, PRD 83, 105004 (2011); Albacete, Dumitru, Fujii, Nara, NPA 897, 1-27 (2013); Chirilli, Xiao, Yuan, PRL 108, 122301 (2012); Kang, Vitev, Xing, PRL 113, 062002 (2014); Altinoluk, Armesto, Beuf, Kovner, Lublinsky, PRD 91, no.9, 094016 (2015); Iancu, Mueller, Triantafyllopoulos, JHEP 12, 041 (2016); Durães, AVG, Goncalves, Navarra, PRC 94, no.2, 024917 (2016); Ducloué et. al, PRD 97, no.5, 054020 (2018); Ducloué, Lappi, Zhu, PRD 95, no.11, 114007 (2017); Carvalho, AVG, Goncalves, Navarra, PRD 96, no.9, 094002 (2017); Liu, Ma, Chao, PRD 100, no.7, 071503 (2019); Iancu, Mulian, JHEP 03, 005 (2021); Shi, Wang, Wei, Xiao, PRL 128, no.20, 202302 (2022)



# Particle production @ CGC EFT

Final states:  $FS = K_S^0, h^+ + h^-$

$$\sigma(pp \rightarrow FS + X) \propto \sum_i f_i(x_1) \otimes \tilde{\mathcal{N}}_F(x_2) \otimes D_{i/h} + g(x_1) \otimes \tilde{\mathcal{N}}_A(x_2) \otimes D_{g/h}$$

Photon production,  $q + g \rightarrow q + \gamma$  [QCD "Compton" scattering]

Collinear + TMD factorization for all processes here

$$\sigma(pp \rightarrow \gamma + X) \propto \sum_i f_i(x_1) \otimes \tilde{\mathcal{N}}_F(x_2) \quad \text{No FF!}$$

D-meson production,  $c + g \rightarrow D^0 + X + \{g + p \rightarrow Q\bar{Q}\} \rightarrow D^0 + X$

$$\sigma(pp \rightarrow D^0 + X) \propto c(x_1) \otimes \tilde{\mathcal{N}}_F(x_2) \otimes D_{c/D} + g(x_1) \otimes k_T^2 \tilde{\mathcal{N}}_A(x_2) \otimes D_{c/D}$$

CGC EFT provides a unified description of these processes!

$$\frac{\partial \mathcal{N}(r, Y)}{\partial Y} = \int d^2 r_1 K(r, r_1, r_2) [\mathcal{N}(r_1, Y) + \mathcal{N}(r_2, Y) - \mathcal{N}(r, Y) - \mathcal{N}(r_1, Y) \mathcal{N}(r_2, Y)]$$

$$\mathcal{N}_F(r, x) \equiv \mathcal{N}(r, x)$$

Balitsky, Kovchegov: NPB 463 (1996) 99, PRL 81 (1998) 2024, PRD 60 (1999) 014020, PLB 518 (2001) 235, NPB 629 (2002) 290, PRD 60 (1999) 034008, PRD 61 (2000) 074018

Running coupling BK: provides the small-x evolution **given an initial condition**

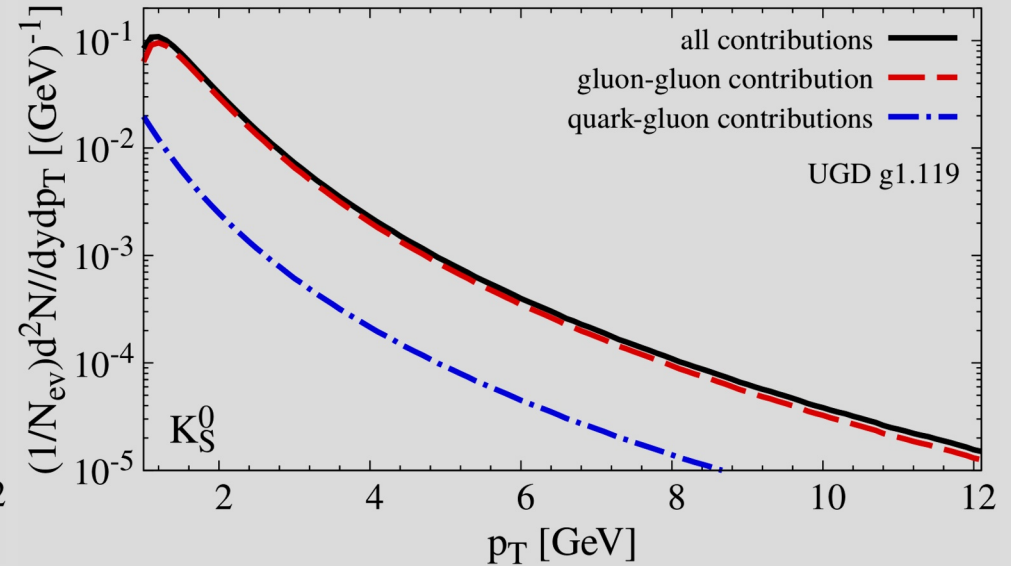
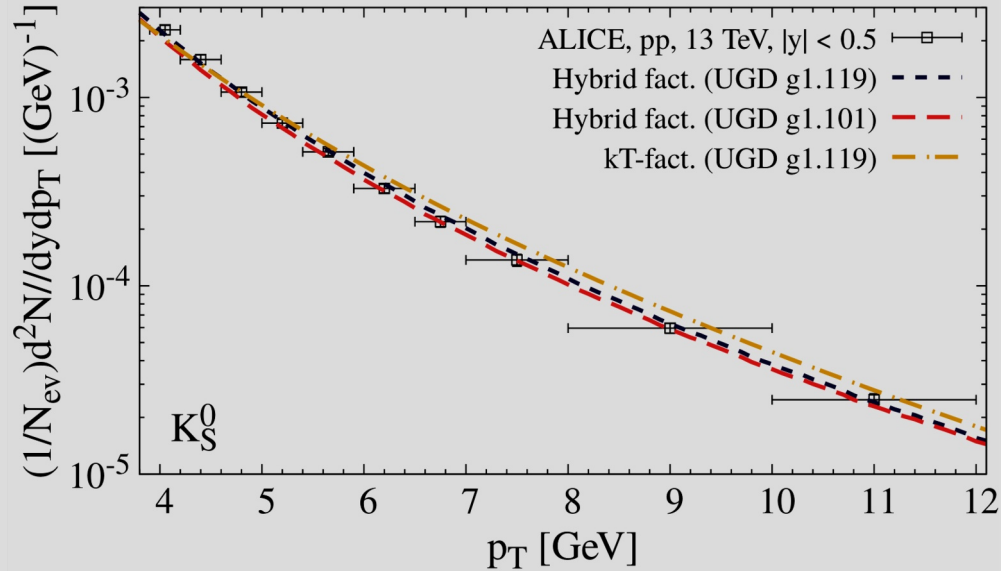
$$\mathcal{N}_F(r, x_0) = 1 - \exp \left[ - \frac{(r^2 Q_{s0, \text{proton}}^2)^\gamma}{4} \ln \left( \frac{1}{\Lambda r} + e \right) \right] \quad \text{MV-like ic}$$

$$\mathcal{N}_F(r, x_0) = 1 - \exp \left[ - \frac{r^2 Q_{s0, \text{proton}}^2}{4} \right] \quad \text{GBW-like ic}$$

Albacete, Armesto, Milhano, Salgado, PRD 80, 034031 (2009)  
 Albacete, Armesto, Milhano, Quiroga-Arias, Salgado, EPJC 71, 1705 (2011)  
 Albacete, Dumitru, Fujii, Nara, NPA 897, 1-27 (2013)



Lima, AVG, Goncalves, PRC 106 (2022) 6, 065206



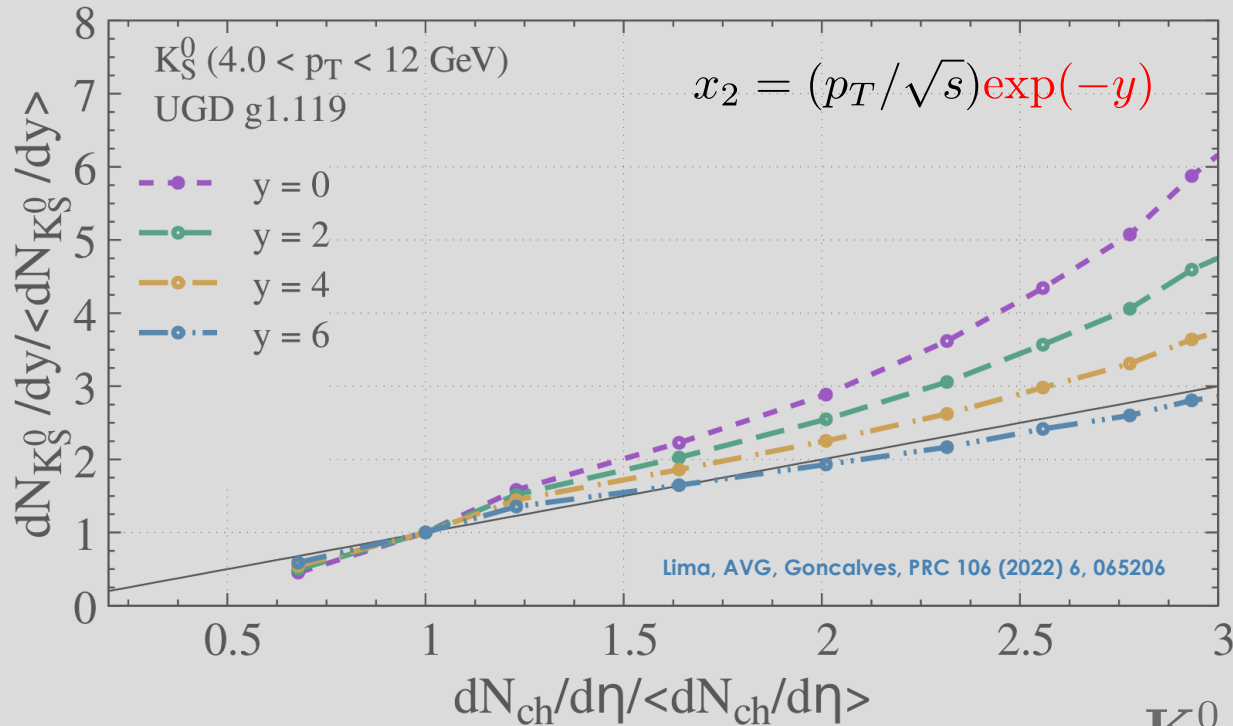
Good description of  $p_T$ -spectrum of  $K_S^0$  for kt-fact. & hybrid form.

**Gluon**-initiated interactions are dominant

**Quark**-initiated channel is sub-dominant

For now on, only results with hybrid formalism for identified final states

# Application to selected particles: $K_S^0$



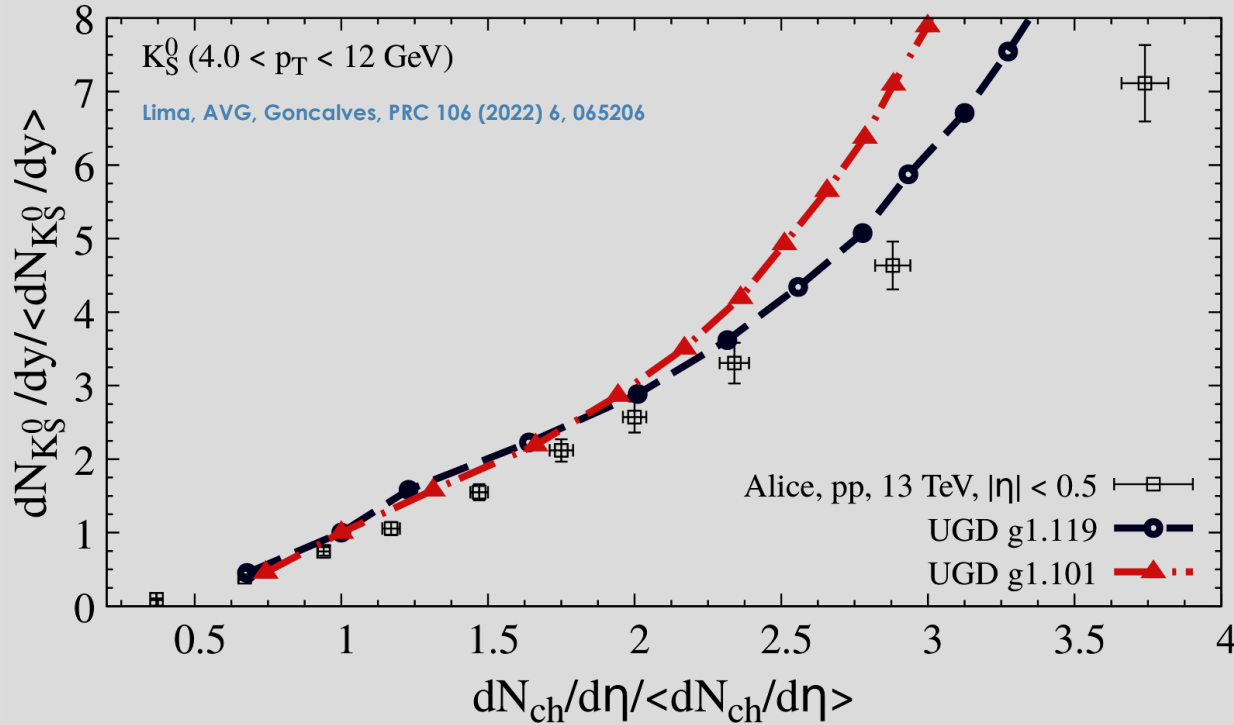
$Q_s(x_2)$  increases: high- $p_T$  kaons are affected in the same way as charged particles

Results depend on  $p_T$  cuts as well [backup slides]

$$K_S^0 : 4 < p_T < 12 \text{ GeV}$$

$$N_{ch} : 0.1 < p_T < 12 \text{ GeV}, |\eta| < 0.5$$

# Application to selected particles: $K_S^0$

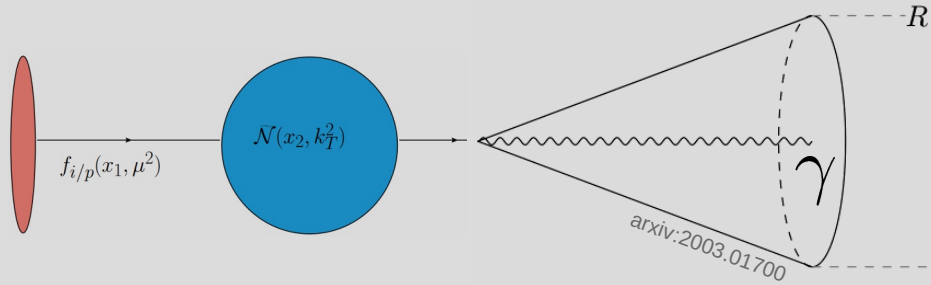


Hybrid formalism captures the qualitative behavior seen in data up to:  $N_{ch}/\langle N_{ch} \rangle \sim 2.5$

Highest multiplicities not described: missing saturation effects on projectile? Medium modification effects?

Need a way to check what is the reason!

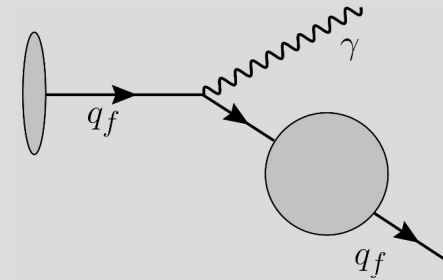
# Application to selected particles: **isolated** photons



Negligible dependence of isolation radius, will show results for  $R = 0.1$  fm

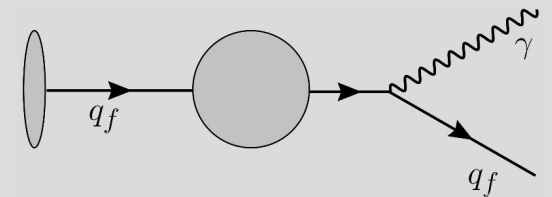
**Not affected by fragmentation processes**

(photons from fragmentation suppressed by angular exclusion)



$\gamma$  – bremsstrahlung off an eikonal parton through the low- $x$  color field

Qualitative description of  $p_T$ -spectra [backup slides]

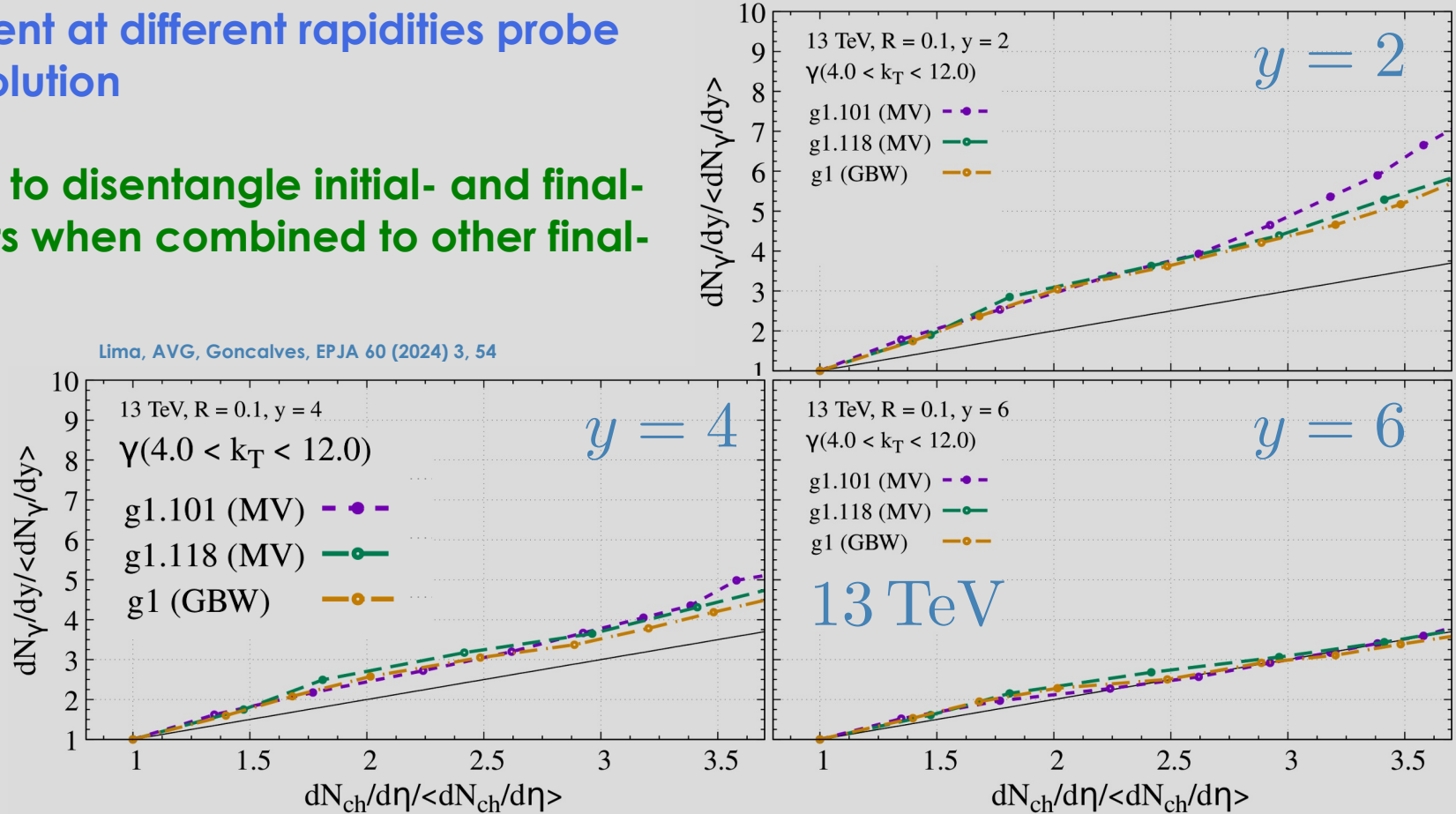


# Application to selected particles: isolated photons

Measurement at different rapidities probe small-x evolution

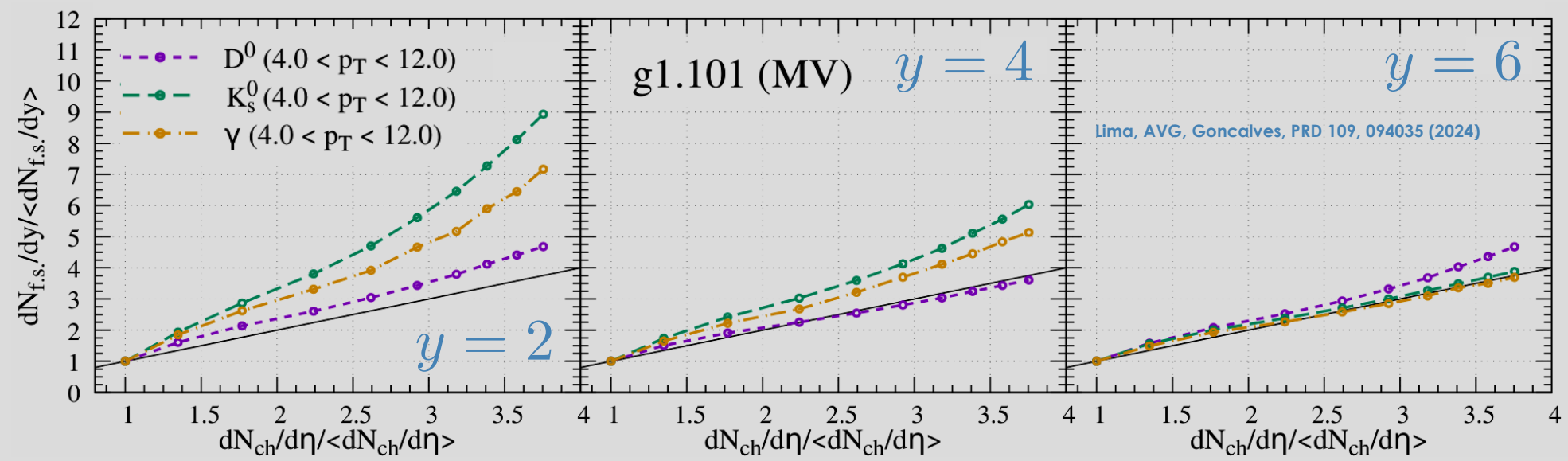
Could help to disentangle initial- and final-state effects when combined to other final-states

Lima, AVG, Goncalves, EPJA 60 (2024) 3, 54



# Application to selected particles: $D^0$ mesons

$$c + g \rightarrow D^0 + X + \{g + p \rightarrow Q\bar{Q}\} \rightarrow D^0 + X$$



Universal, final-state independent curve at (ultra-)forward rapidities If high multiplicity events are mainly a product of initial-state effects

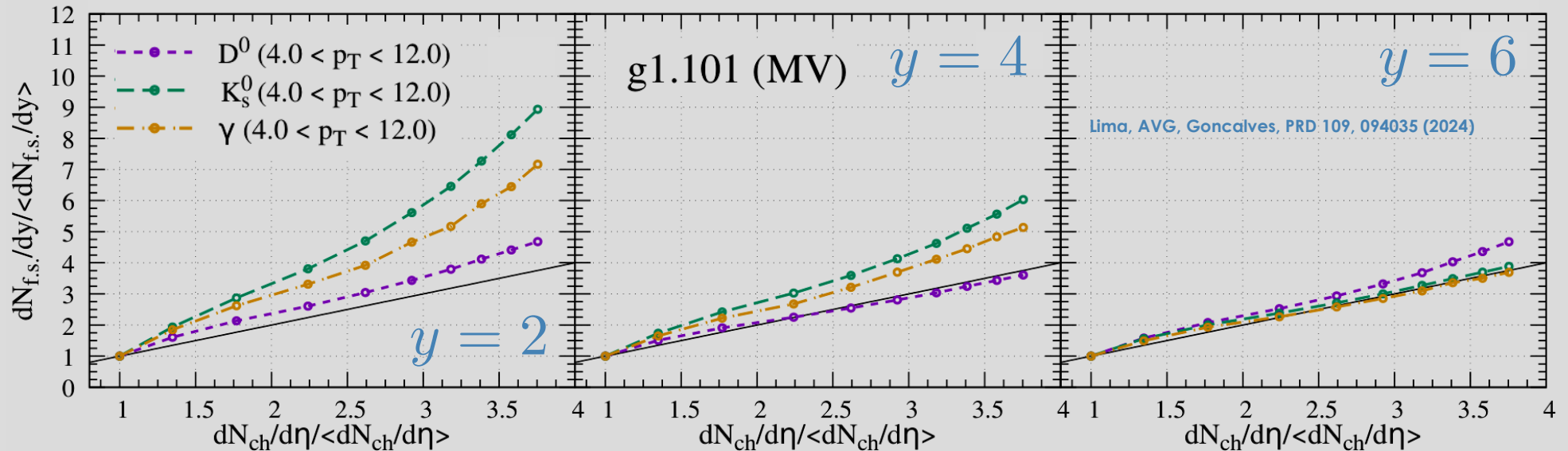
Result will not be universal if final-state effects play a role in such events

# Final remarks

Studied high-multiplicity p+p collisions for different final states in correlation to charged particles + explored different kinematical regions

Qualitative understanding of kaon production at moderated multiplicities

Possible advances in understanding the mechanism behind high-multiplicity events by simultaneous study of different final states



# Backup slides



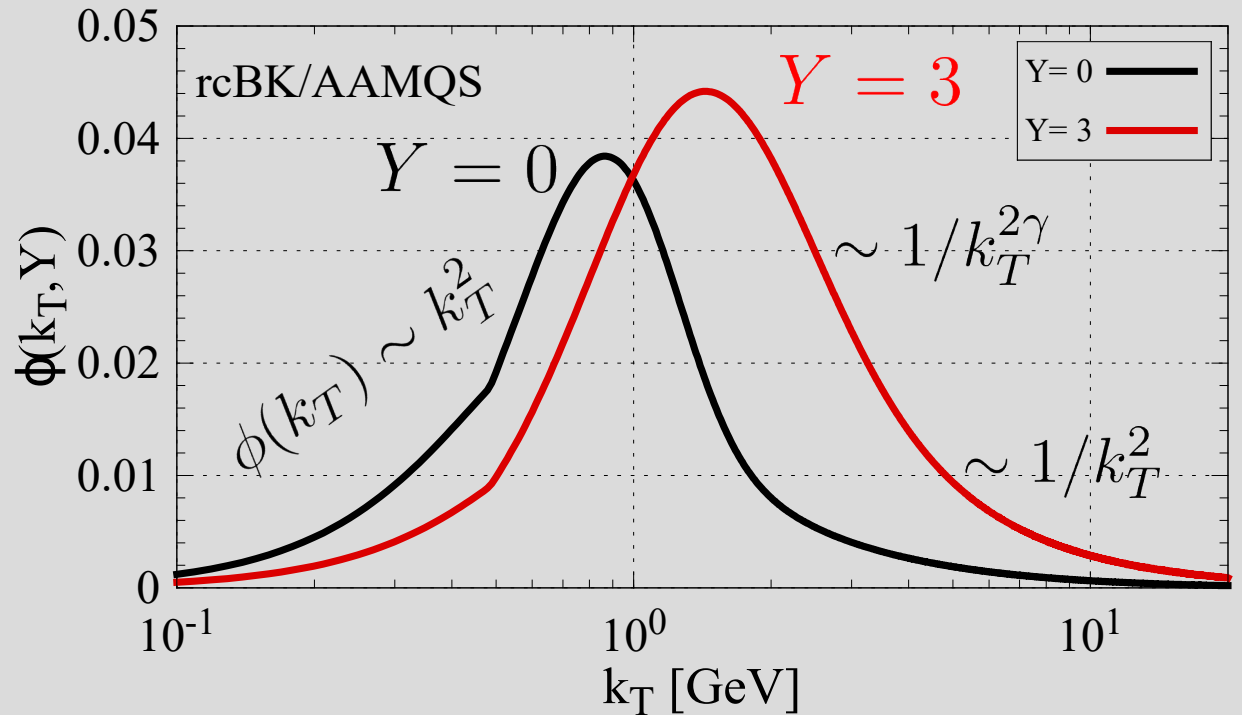
# Specifying the dipole scattering amplitude

$$\mathcal{N}_F(r, x_0) = 1 - \exp \left[ - \frac{(r^2 Q_{s0,proton}^2)^\gamma}{4} \ln \left( \frac{1}{\Lambda r} + e \right) \right]$$

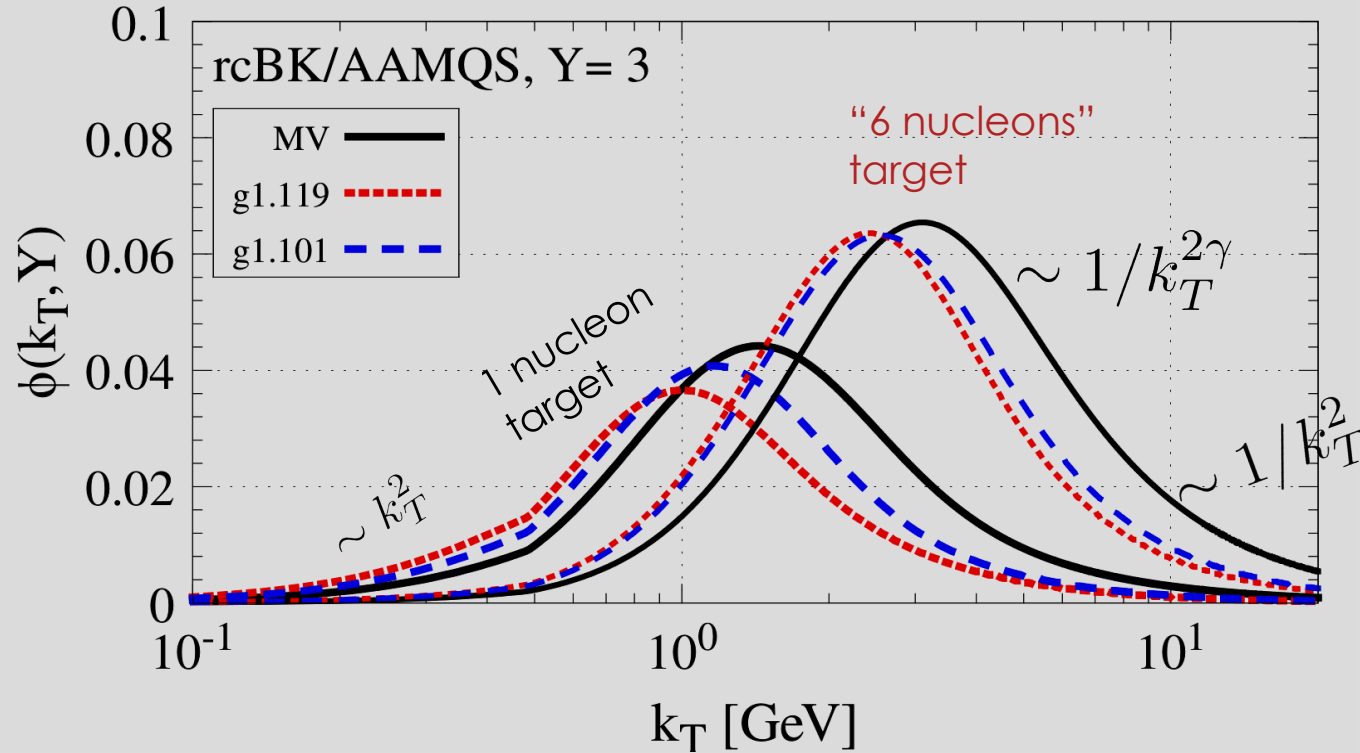
$\gamma = 1$  : MV model

$\gamma = 1 + \text{no log}$  : GBW model

$\gamma > 1$  : best fit of HERA data



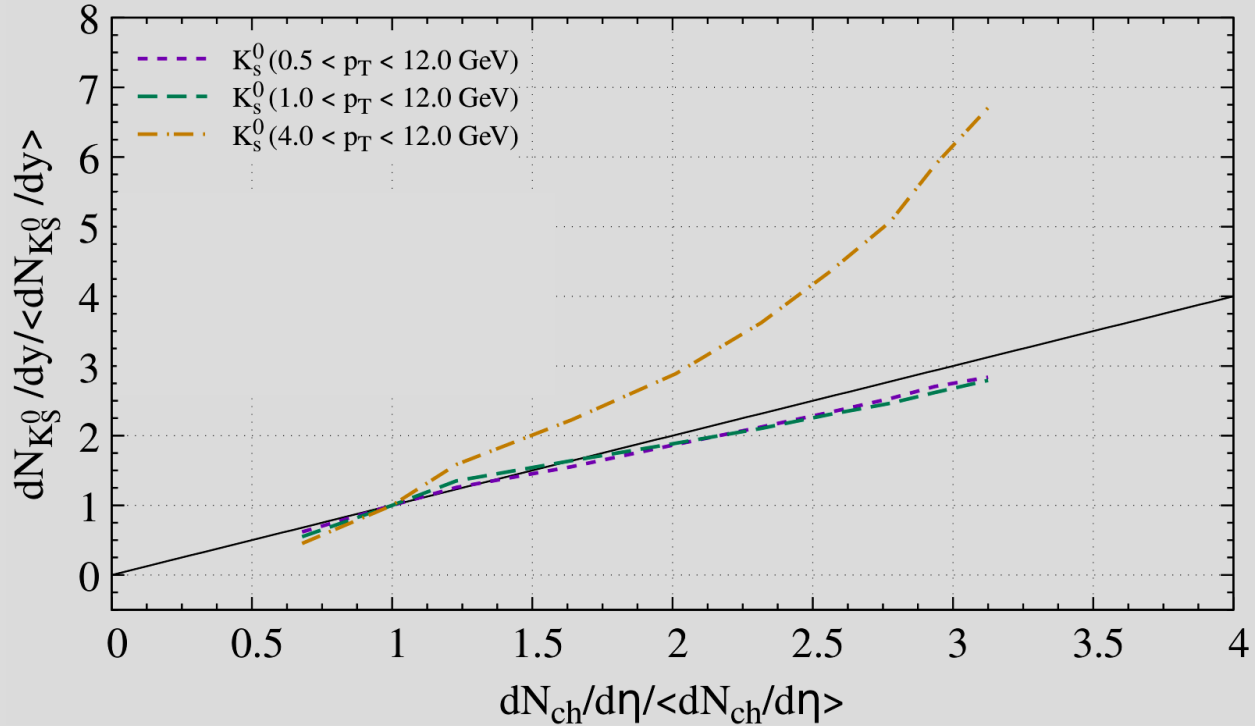
# Specifying the dipole scattering amplitude



Higher than average multiplicity events from collisions where (at least one of the) protons have larger  $Q_s$

Larger  $Q_s$ : UGD peak is shifted to the right

# Application to selected particles: $K_S^0$



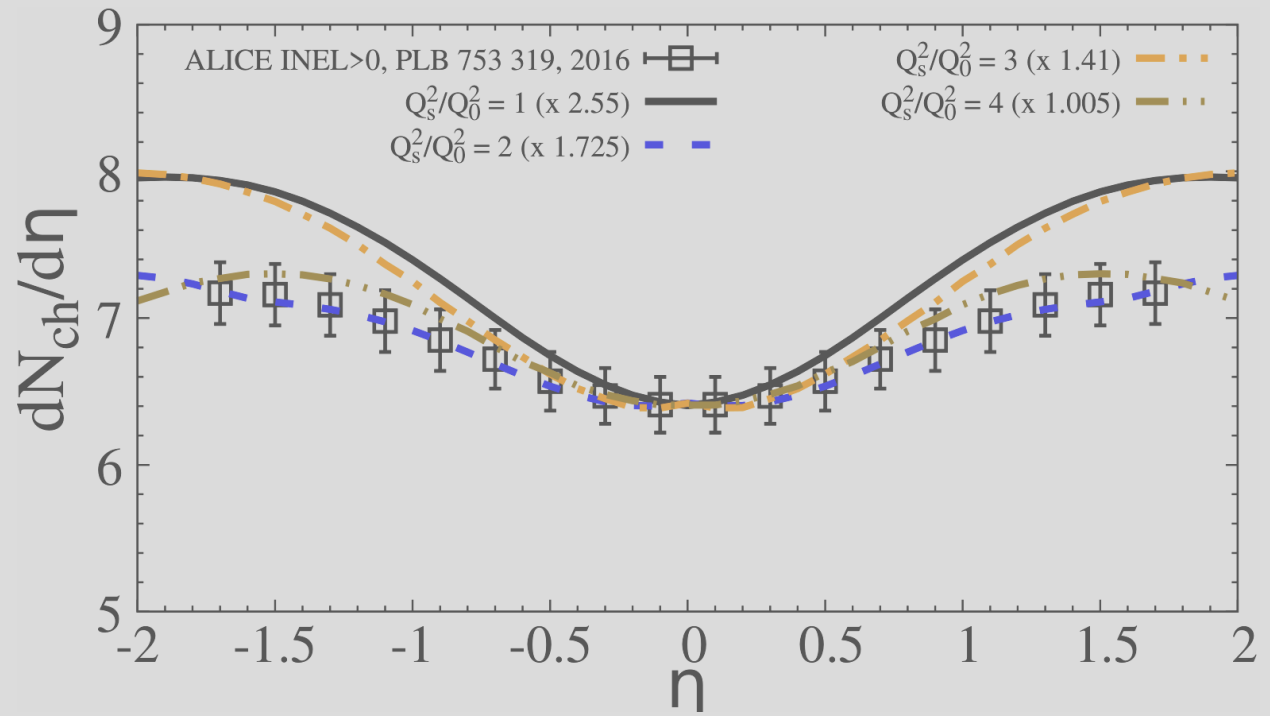
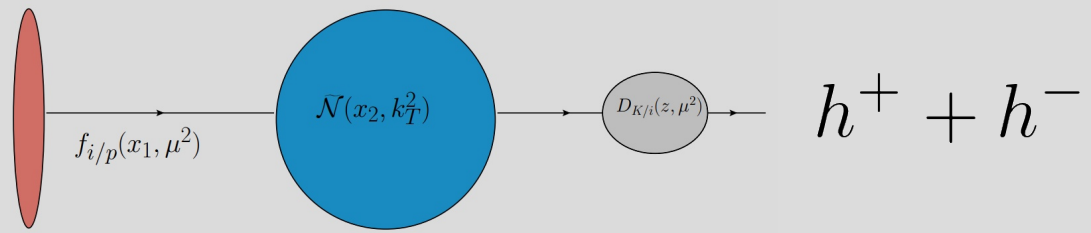
Dependence with  $p_T$  cuts

Ch. particles always in  
 $0.1 < p_T < 12$  GeV

Including low- $p_T$  particles  
 favors saturation effects

Larger  $p_T$  ranges require  
 larger  $Q_s(x)$  to be affected  
 in same way as charged  
 particles

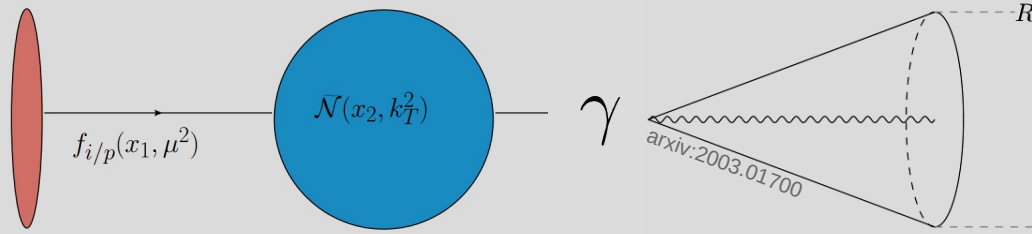
# Describing the charged particle multiplicity



Best description is provided when assuming a slightly larger saturation scale for the proton

Ratios do not depend on K-factor!

# Isolated photons in the hybrid formalism



$$\frac{dN^{pp \rightarrow \gamma X}}{d^2\mathbf{k}_T dy} = \sum_q \frac{e_q^2 \alpha_{em}}{\pi (2\pi)^3} \int d^2\mathbf{l}_T \int_{x_{min}} dx_p z^2 [1 + (1-z)^2] \frac{q(x_p, \mu^2)}{\mathbf{k}_T^2} \times \frac{(\mathbf{k}_T + \mathbf{l}_T)^2}{[z\mathbf{l}_T - (1-z)\mathbf{k}_T]^2} \int d^2\mathbf{b} S(\mathbf{k}_T + \mathbf{l}_T, \mathbf{b}, x_g) \theta[\sqrt{(y - y_q)^2 + \Delta\phi} - R]$$

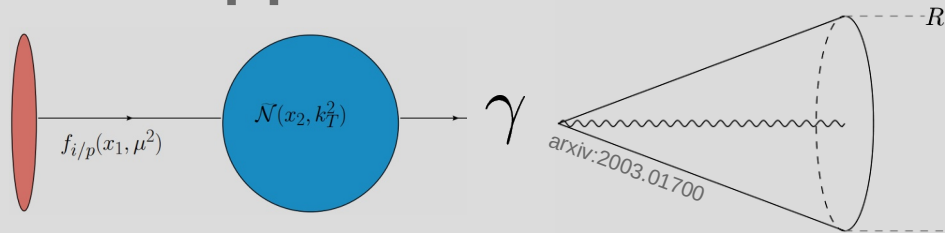
Ducloue, Lappi, Mantysaari, PRD 97(5), 054023 (2018)

$$S = 1 - \mathcal{N}$$

azimuthal angle between the scattering quark and the photon

$$x_g = \frac{|\mathbf{k}_T| e^{-y} + |\mathbf{l}_T| e^{-y_q}}{\sqrt{s}}, \quad y_q = \log \left( \frac{-e^y |\mathbf{k}_T| + x_p \sqrt{s}}{|\mathbf{l}_T|} \right), \quad z = \frac{|\mathbf{k}_T|}{x_p \sqrt{s} e^y}$$

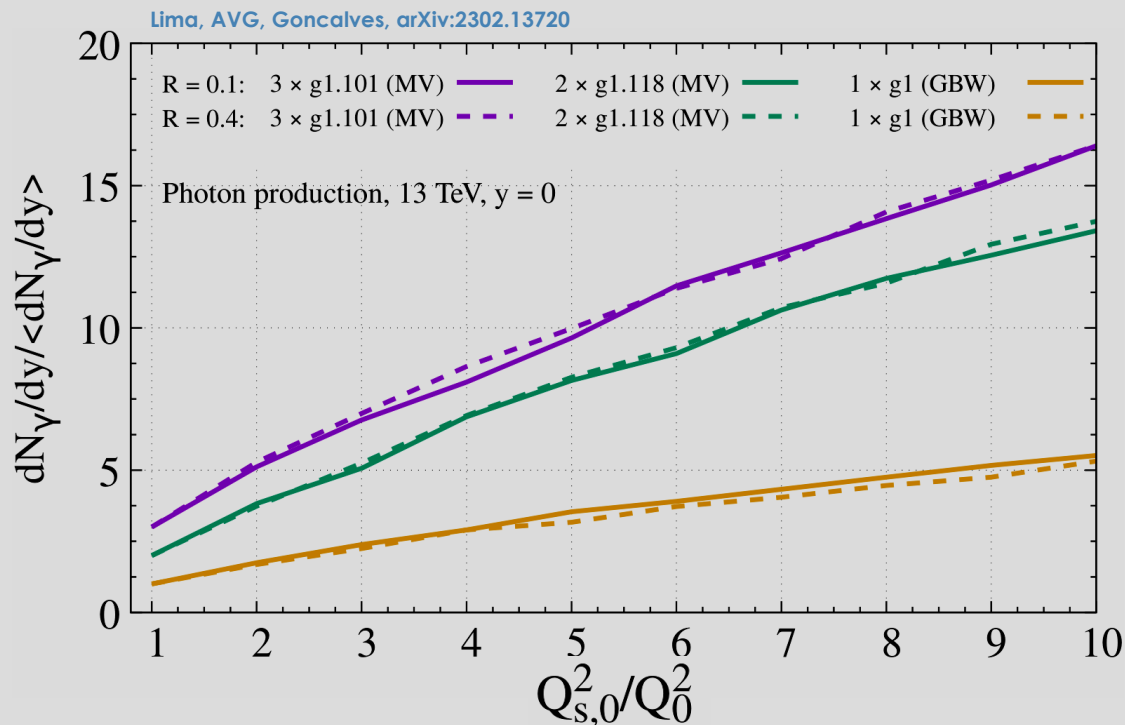
# Application to selected particles: isolated photons



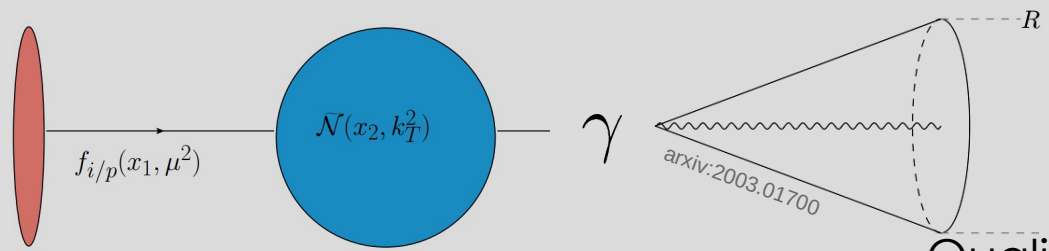
Negligible dependence of isolation radius

Similar dependence on  $p_T$  cuts (as seen in previous plots)

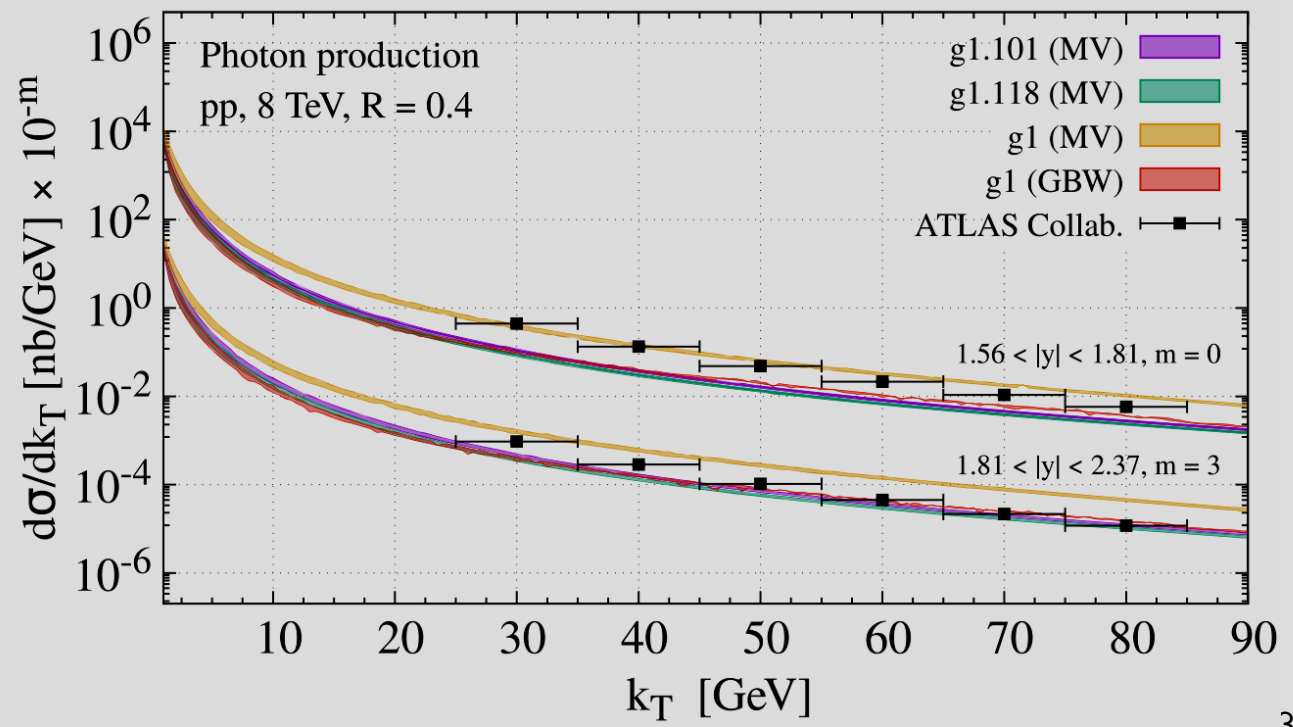
Can check the correlation to charged particles and different kinematical regions



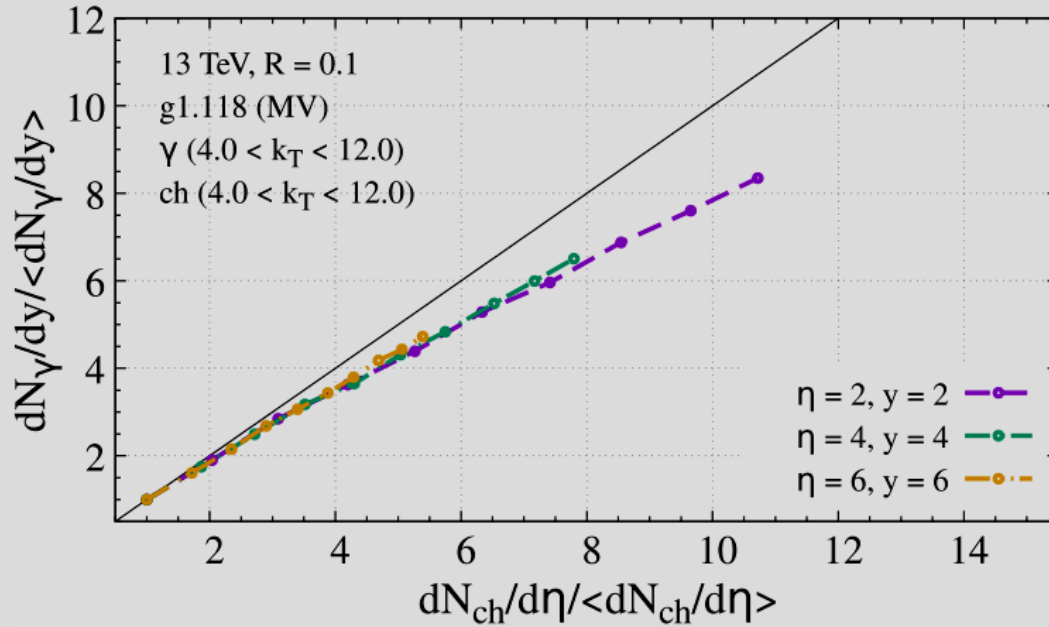
# Application to selected particles: isolated photons



Qualitative description of  $p_T$ -spectra



# Application to selected particles: isolated photons



Ch. particles and photons have similar  $Q_s$  dependence for same kinematical range

Ch. particles has faster increase compared to photons

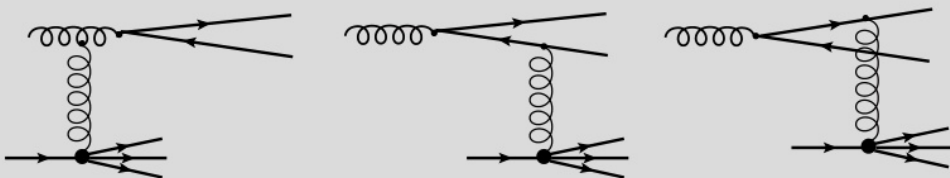
**Fig. 6** Correlation between the normalized isolated photon and charged particles yields in  $pp$  collisions at  $\sqrt{s} = 13$  TeV, derived that the distinct yields are integrated over the same transverse momentum range and are estimated at the same rapidity



Goncalves, **Kopeliovich**, Nemchik, Pasechnik, Potashnikova, PRD 96, 014010

$$\left. \frac{d\sigma_{pp \rightarrow D^0 X}}{dy d^2 p_T} \right|_{G.I.} = \int_{z_{\min}}^1 \frac{dz}{z^2} x_1 g(x_1, Q^2) \times \int_{\alpha_{\min}}^1 d\alpha \frac{d^3 \sigma_{gp \rightarrow c\bar{c}X}}{d\alpha d^2 q_T} D_{c/D}(z, \mu^2),$$

$$z_{\min} = \frac{\sqrt{m_D^2 + p_T^2}}{\sqrt{s}} e^y \quad \alpha_{\min} = \frac{z_{\min}}{z} \sqrt{\frac{m_c^2 z^2 + p_T^2}{m_D^2 + p_T^2}}.$$



interaction of a colorless three-body system  $gQ\bar{Q}$   
scattering off the color background field of the target proton

$$\frac{d^3 \sigma_{gp \rightarrow c\bar{c}X}}{d\alpha d^2 q_T} = \frac{1}{6\pi} \int \frac{d^2 \kappa_T}{\kappa_T^4} \alpha_s \mathcal{K}_{\text{dip}}(x_2, \kappa_T^2) \left\{ \left[ \frac{9}{8} \mathcal{H}_0(\alpha, \bar{\alpha}, \vec{q}_T) - \frac{9}{4} \mathcal{H}_1(\alpha, \bar{\alpha}, \vec{q}_T, \vec{\kappa}_T) + \mathcal{H}_2(\alpha, \bar{\alpha}, \vec{q}_T, \vec{\kappa}_T) + \frac{1}{8} \mathcal{H}_3(\alpha, \bar{\alpha}, \vec{q}_T, \vec{\kappa}_T) \right] + [\alpha \leftrightarrow \bar{\alpha}] \right\},$$

$$\mathcal{H}_0(\alpha, \bar{\alpha}, \vec{q}_T) = \frac{m_c^2 + (\alpha^2 + \bar{\alpha}^2) q_T^2}{(q_T^2 + m_c^2)^2},$$

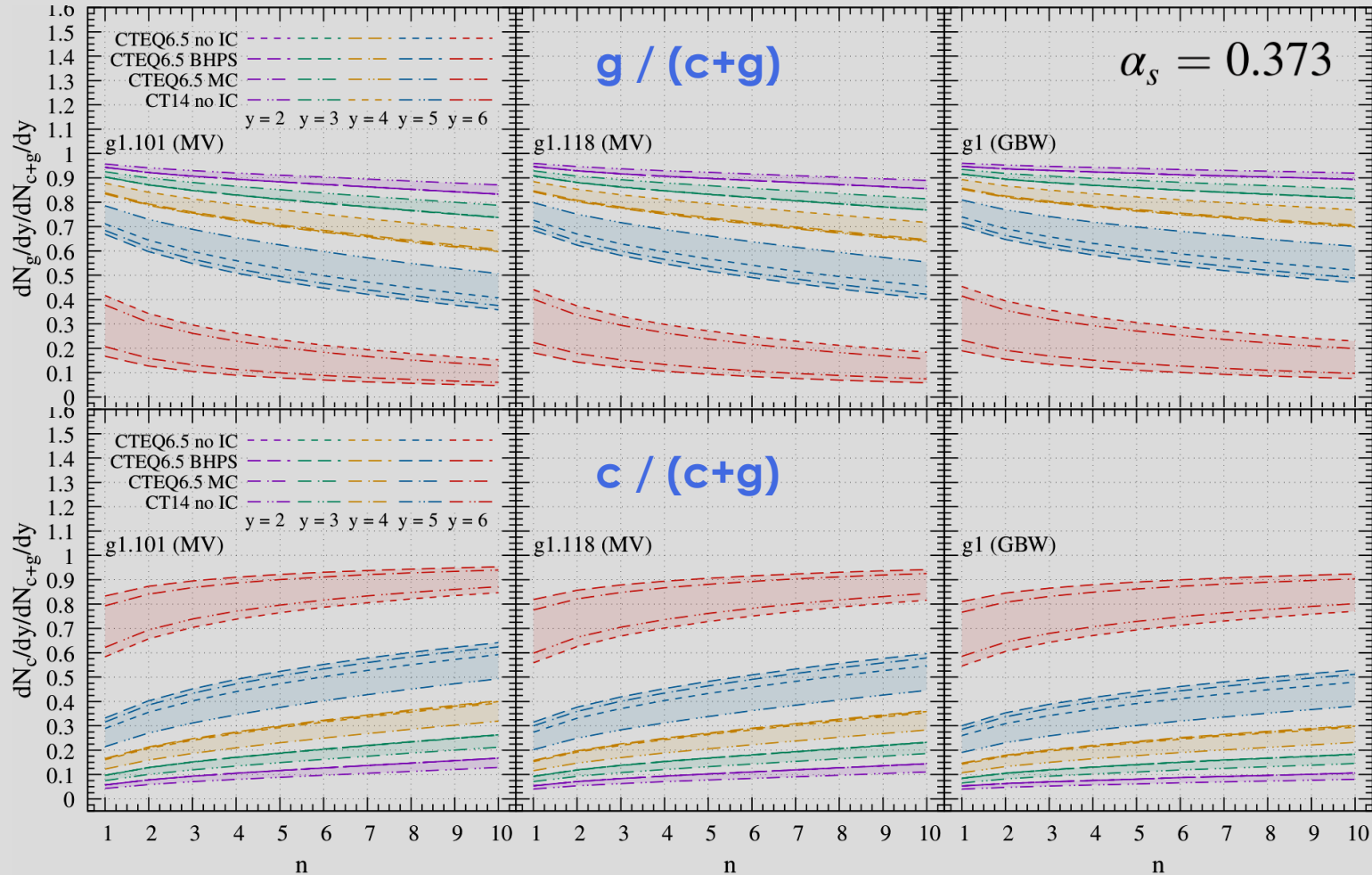
$$\mathcal{H}_1(\alpha, \bar{\alpha}, \vec{q}_T, \vec{\kappa}_T) = \frac{m_c^2 + (\alpha^2 + \bar{\alpha}^2) \vec{q}_T \cdot (\vec{q}_T - \alpha \vec{\kappa}_T)}{[(\vec{q}_T - \alpha \vec{\kappa}_T)^2 + m_c^2](q_T^2 + m_c^2)},$$

$$\mathcal{H}_2(\alpha, \bar{\alpha}, \vec{q}_T, \vec{\kappa}_T) = \frac{m_c^2 + (\alpha^2 + \bar{\alpha}^2) (\vec{q}_T - \alpha \vec{\kappa}_T)^2}{[(\vec{q}_T - \alpha \vec{\kappa}_T)^2 + m_c^2]^2},$$

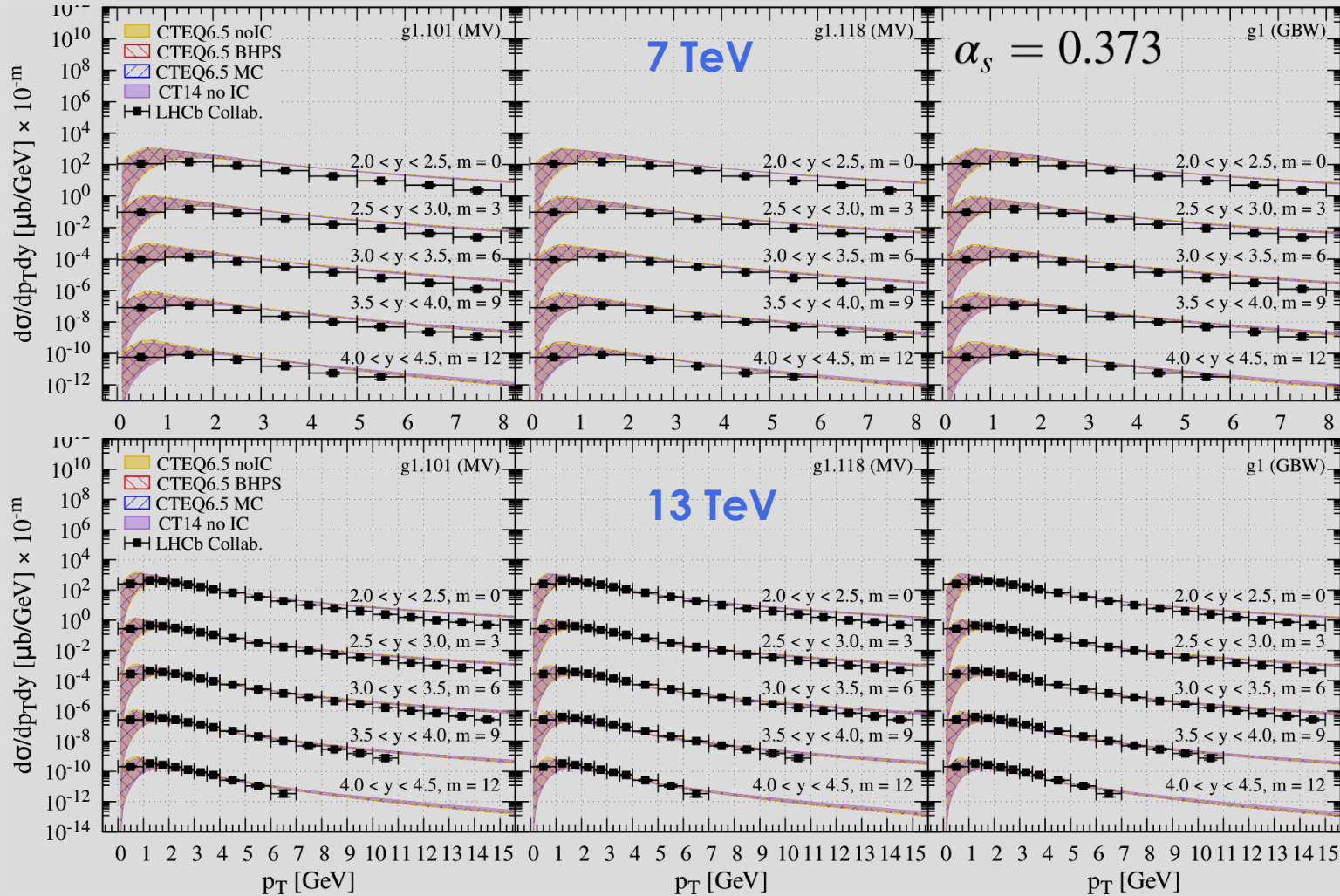
$$\mathcal{H}_3(\alpha, \bar{\alpha}, \vec{q}_T, \vec{\kappa}_T) = \frac{m_c^2 + (\alpha^2 + \bar{\alpha}^2) (\vec{q}_T + \alpha \vec{\kappa}_T) \cdot (\vec{q}_T - \bar{\alpha} \vec{\kappa}_T)}{[(\vec{q}_T + \alpha \vec{\kappa}_T)^2 + m_c^2][(\vec{q}_T - \bar{\alpha} \vec{\kappa}_T)^2 + m_c^2]}$$

$$x_{1,2} = \frac{M_{Q\bar{Q}}}{\sqrt{s}} e^{\pm y} \quad M_{Q\bar{Q}} \simeq 2\sqrt{m_Q^2 + p_T^2}.$$

# Application to selected particles: $D^0$ mesons



# Application to selected particles: $D^0$ mesons



# Application to selected particles: $D^0$ mesons

