

New Constraints on Gauged $U(1)_{L_\mu - L_\tau}$ Models via Z-Z' Mixing

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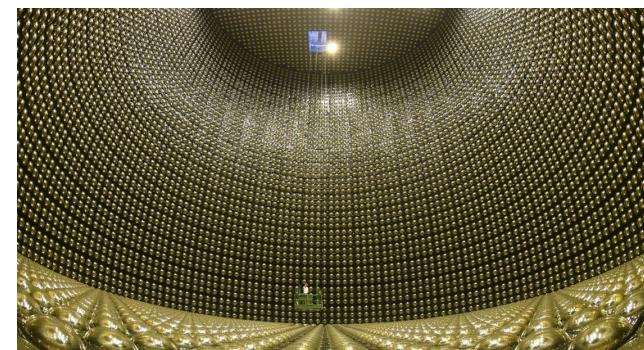
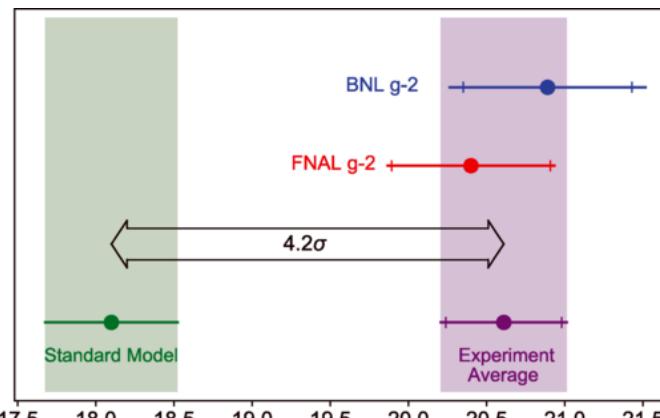
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Based on [arXiv : 2401.17613]

working with K. Asai(ICRR), S. Okawa(KEK), and K. Tsumura(Kyushu U.).

Background

- The discrepancy of muon g-2 between the SM and experimental results.
→ $U(1)_{L_\mu - L_\tau}$ gauge models can explain.
- The recent experiments of the neutrino oscillation become more precise.
→ Simple $U(1)_{L_\mu - L_\tau}$ gauge models seem hard to describe the neutrino physics.



Cited from <https://www-sk.icrr.u-tokyo.ac.jp/sk/>

Purpose

- To find the $U(1)_{L_\mu - L_\tau}$ gauge models which are consistent to the latest neutrino experiments.
- To get new (model dependent) constraints on the $U(1)_{L_\mu - L_\tau}$ gauge models.

Cited from NuFIT v5.2

		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 6.4$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.303^{+0.012}_{-0.012}$	$0.270 \rightarrow 0.341$	$0.303^{+0.012}_{-0.011}$	$0.270 \rightarrow 0.341$
	$\theta_{12}/^\circ$	$33.41^{+0.75}_{-0.72}$	$31.31 \rightarrow 35.74$	$33.41^{+0.75}_{-0.72}$	$31.31 \rightarrow 35.74$
	$\sin^2 \theta_{23}$	$0.451^{+0.019}_{-0.016}$	$0.408 \rightarrow 0.603$	$0.569^{+0.016}_{-0.021}$	$0.412 \rightarrow 0.613$
	$\theta_{23}/^\circ$	$42.2^{+1.1}_{-0.9}$	$39.7 \rightarrow 51.0$	$49.0^{+1.0}_{-1.2}$	$39.9 \rightarrow 51.5$
	$\sin^2 \theta_{13}$	$0.02225^{+0.00056}_{-0.00059}$	$0.02052 \rightarrow 0.02398$	$0.02223^{+0.00058}_{-0.00058}$	$0.02048 \rightarrow 0.02416$
	$\theta_{13}/^\circ$	$8.58^{+0.11}_{-0.11}$	$8.23 \rightarrow 8.91$	$8.57^{+0.11}_{-0.11}$	$8.23 \rightarrow 8.94$
	$\delta_{CP}/^\circ$	232^{+36}_{-26}	$144 \rightarrow 350$	276^{+22}_{-29}	$194 \rightarrow 344$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.41^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.03$	$7.41^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.03$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.507^{+0.026}_{-0.027}$	$+2.427 \rightarrow +2.590$	$-2.486^{+0.025}_{-0.028}$	$-2.570 \rightarrow -2.406$

Minimal $U(1)_{L_\mu - L_\tau}$ gauge model

- Fields : SM + three right-handed neutrino N_i + one scalar field.
- Symmetry : SM gauge $\times U(1)_{L_\mu - L_\tau}$ gauge.

Lepton	$(\ell_e \ \ell_\mu \ \ell_\tau)$	$(e_R \ \mu_R \ \tau_R)$	$(N_e \ N_\mu \ N_\tau)$
$U(1)_{L_\mu - L_\tau}$ charge	(0 +1 -1)	(0 +1 -1)	(0 +1 -1)
Scalar	Φ_{+1} SU(2) doublet	Φ_{-1} SU(2) doublet	σ SU(2) singlet
charge	+1	-1	+1

Results for Analysis of Neutrino Mass Matrix Structure

- Model independent result set by neutrino mass matrix.
- Each models have their own mass matrix structure.

Our work
(previous work [Phys. Rev. D 99 (2019) 05502])

Model	Normal ordering	Inverted ordering
$\text{SM} + N_i + \sigma_{+1}$	Viable in 2σ (Viable at 3σ)	Excluded (Excluded)
$\text{SM} + N_i + \Phi_{+1}$	Excluded (Excluded)	Viable at 3σ (Excluded)
$\text{SM} + N_i + \Phi_{-1}$	Excluded (Excluded)	Excluded (Excluded)

→ Are there any other constraints on the viable model?

Z-Z' Mixing

- The additional $U(1)_{L_\mu - L_\tau}$ gauge symmetry induces Z-Z' mixing.

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}Z'^{\mu\nu}Z'^{\mu\nu} + \frac{1}{2}\frac{\varepsilon}{\cos\theta_W}B_{\mu\nu}Z'^{\mu\nu}$$
$$\mathcal{L}_{\varepsilon_Z} = \frac{1}{2} \begin{pmatrix} Z_\mu & Z'^\mu \end{pmatrix} \begin{pmatrix} 1 & -\varepsilon_Z \\ -\varepsilon_Z & m_{Z'}^2/m_Z^2 \end{pmatrix} \begin{pmatrix} Z^\mu \\ Z'^\mu \end{pmatrix}$$

$$\varepsilon_Z \equiv \frac{m_{Z'}}{m_Z} \delta$$

$$\mathcal{L} \supset Z'^\mu (g_{Z'} J^\mu_{L_\mu - L_\tau} + \varepsilon e J^\mu_{\text{em}} + \varepsilon_Z g_Z J^\mu_{\text{NC}})$$

$\rightarrow G_F$ and $\sin^2\theta_W$ are changed.

(Now we ignore the kinetic mixing $\varepsilon \sim g_{Z'}/70$ which is much smaller than ε_Z in our interest parameter space.)

Atomic Parity Violation (APV)

- The weak charge of Cs is given by the measurements of APV;

$$Q_W^{\text{exp}}(^{133}_{55}\text{Cs}) = -72.94(43)$$

- The weak charge of Cs based on SM is changed by Z-Z' mixing;

$$Q_W(^{133}_{55}\text{Cs}) \simeq Q_W^{\text{SM}}(^{133}_{55}\text{Cs}) (1 + \delta^2)$$

→ $|\delta|^2 \lesssim 5.7 \times 10^{-3}$ (90% CL)

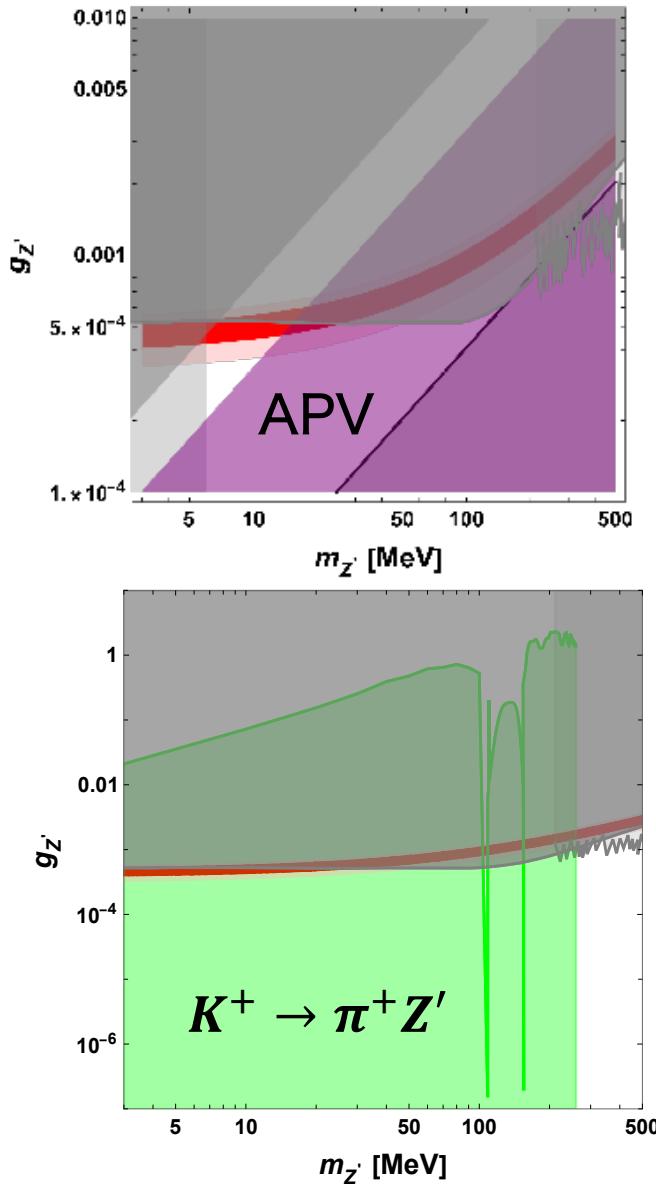
Flavor Changing Meson Decay

- Flavor changing meson decays provide a good probe of a light Z' boson.
- Branching ratio of $K^+ \rightarrow \pi^+ Z'$ is written by;

$$\text{Br}(K^+ \rightarrow \pi^+ Z') \simeq 1.6 \times 10^{-4} |\delta|^2$$

→ $|\delta| \lesssim 2.5 \times 10^{-4} \sqrt{\frac{\text{Br}(K^+ \rightarrow \pi^+ Z')_{\text{exp}}}{1 \times 10^{-11}}}$

Constraint on Model with Φ_{+1}



In this model $\delta = \frac{1}{v} \frac{m_{Z'}}{g_{Z'}} .$

Cs APV :

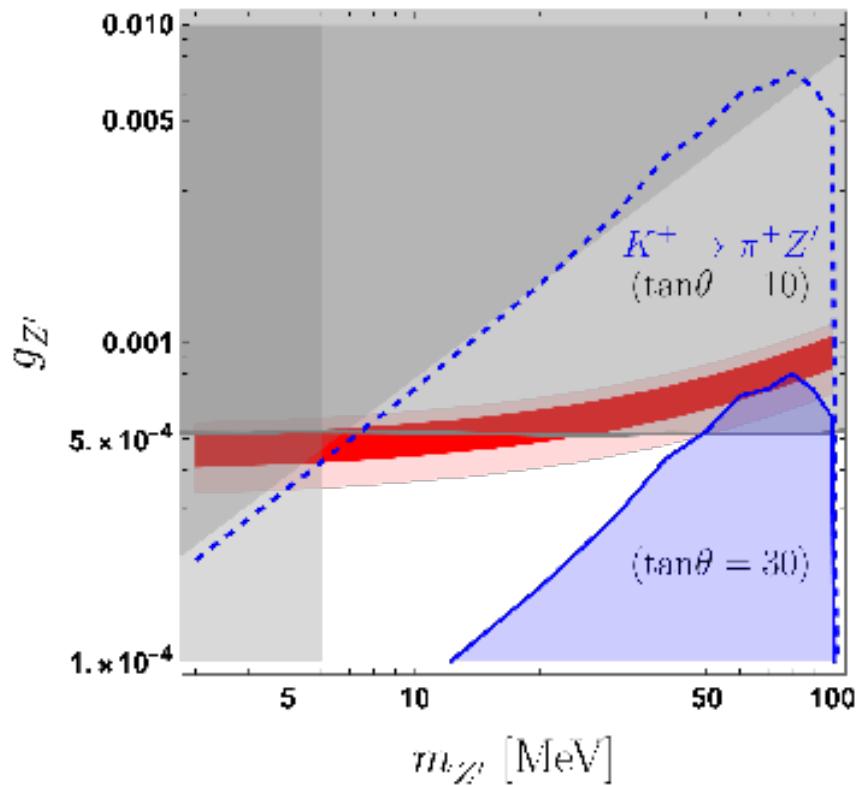
$$g_{Z'} \gtrsim 5.4 \times 10^{-4} \left(\frac{m_{Z'}}{10 \text{ MeV}} \right)$$

$K^+ \rightarrow \pi^+ Z'$:

$$g_{Z'} \gtrsim 1.6 \times 10^{-1} \sqrt{\frac{1 \times 10^{-11}}{\text{Br}(K^+ \rightarrow \pi^+ Z')_{\text{exp}}}} \left(\frac{m_{Z'}}{10 \text{ MeV}} \right)$$

- The gray shaded region are excluded by the well-known constraints (from BABAR, NA64 μ , white dwarf cooling, and effective number of neutrinos).
- The red region gives the proper correction to muon g-2.
- There is **no region** which gives proper correction to muon g-2.

Constraint on Model with Φ_{+1} and a SU(2) singlet scalar σ_{+1}



In this model, $\delta = \frac{\text{sign}(Q_\Phi)}{1 + \tan^2 \theta} \frac{1}{v} \frac{m_{Z'}}{g_{Z'}}$.

$\tan\theta \equiv \frac{v_\sigma}{v_\Phi}$ ($v_{\Phi(\sigma)}$ means VEV of $\Phi(\sigma)$).

Cs APV : much smaller than the flavor changing meson decay.

$$g_{Z'} \gtrsim \frac{5.4 \times 10^{-4}}{1 + \tan^2 \theta} \left(\frac{m_{Z'}}{10 \text{ MeV}} \right)$$

$K^+ \rightarrow \pi^+ Z'$:

$$g_{Z'} \gtrsim \frac{1.6 \times 10^{-1}}{1 + \tan^2 \theta} \sqrt{\frac{1 \times 10^{-11}}{\text{Br}(K^+ \rightarrow \pi^+ Z')_{\text{exp}}} \left(\frac{m_{Z'}}{10 \text{ MeV}} \right)}$$

- Model gives proper correction to the muon g-2 discrepancy when $\tan\theta \equiv \frac{v_\sigma}{v_2} \gtrsim 10$.

Conclusion

- We revisited the minimal $U(1)_{L_\mu - L_\tau}$ gauge model based on the latest NuFITv5.2 data. As the results, the model with $SU(2)$ doublet scalar Φ_{+1} was viable at 3σ in case of Inverted ordering while the model was excluded in the previous work.
- Considering the constraints from Z - Z' mixing (APV and flavor changing meson decay process), the model with Φ_{+1} is completely excluded in the region which give the explanation to muon g-2.
- The model with Φ and σ is viable when $\tan \theta \equiv \frac{v_\sigma}{v_2} \gtrsim 10$.

BACKUP

NuFITv4.0

		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 9.3$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.310^{+0.013}_{-0.012}$	$0.275 \rightarrow 0.350$	$0.310^{+0.013}_{-0.012}$	$0.275 \rightarrow 0.350$
	$\theta_{12}/^\circ$	$33.82^{+0.78}_{-0.76}$	$31.61 \rightarrow 36.27$	$33.82^{+0.78}_{-0.75}$	$31.62 \rightarrow 36.27$
	$\sin^2 \theta_{23}$	$0.582^{+0.015}_{-0.019}$	$0.428 \rightarrow 0.624$	$0.582^{+0.015}_{-0.018}$	$0.433 \rightarrow 0.623$
	$\theta_{23}/^\circ$	$49.7^{+0.9}_{-1.1}$	$40.9 \rightarrow 52.2$	$49.7^{+0.9}_{-1.0}$	$41.2 \rightarrow 52.1$
	$\sin^2 \theta_{13}$	$0.02240^{+0.00065}_{-0.00066}$	$0.02044 \rightarrow 0.02437$	$0.02263^{+0.00065}_{-0.00066}$	$0.02067 \rightarrow 0.02461$
	$\theta_{13}/^\circ$	$8.61^{+0.12}_{-0.13}$	$8.22 \rightarrow 8.98$	$8.65^{+0.12}_{-0.13}$	$8.27 \rightarrow 9.03$
	$\delta_{\text{CP}}/^\circ$	217^{+40}_{-28}	$135 \rightarrow 366$	280^{+25}_{-28}	$196 \rightarrow 351$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.39^{+0.21}_{-0.20}$	$6.79 \rightarrow 8.01$	$7.39^{+0.21}_{-0.20}$	$6.79 \rightarrow 8.01$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.525^{+0.033}_{-0.031}$	$+2.431 \rightarrow +2.622$	$-2.512^{+0.034}_{-0.031}$	$-2.606 \rightarrow -2.413$

From <http://www.nu-fit.org/?q=node/177>

Neutrino Mass Matrix

- In general,

$$\mathcal{M}_{\nu_L} = U_{\text{PMNS}} \text{ diag}(m_1 m_2 m_3) U_{\text{PMNS}}^T \equiv \mathcal{M}_{\nu_L}^{\text{gen}}.$$

$$U_{\text{PMNS}} \equiv \begin{pmatrix} V_{11} & V_{12} & V_{13} \\ V_{21} & V_{22} & V_{23} \\ V_{31} & V_{32} & V_{33} \end{pmatrix} \begin{pmatrix} 1 & & \\ & e^{\frac{i\alpha_2}{2}} & \\ & & e^{\frac{i\alpha_3}{2}} \end{pmatrix}.$$

m_i :light neutrino mass α_i :Majorana phase

V_{ij} :matrix component including mixing angles and CP phase

- Through the seesaw mechanism

$$\mathcal{M}_{\nu_L} \simeq -\mathcal{M}_D \mathcal{M}_R^{-1} \mathcal{M}_D^T.$$

→ Some equations arise by comparing these.

Two Zero Texture (Minor) Structure Mass Matrix

- Classification of structures;

$$\mathbf{B}_3: \begin{pmatrix} * & 0 & * \\ 0 & 0 & * \\ * & * & * \end{pmatrix}, \mathbf{B}_4: \begin{pmatrix} * & * & 0 \\ * & * & * \\ 0 & * & 0 \end{pmatrix}, \mathbf{C}: \begin{pmatrix} * & * & * \\ * & 0 & * \\ * & * & 0 \end{pmatrix}$$

- Through the seesaw mechanism, the neutrino mass matrix (or its inverted one) often has such structure.

- Two components of \mathcal{M}_{ν_L} are zero → **Two zero texture**
- Two components of $\mathcal{M}_{\nu_L}^{-1}$ are zero → **Two zero minor**

The mass matrix with such structures
give us two equations. → Predictions

Light Neutrino Mass

$$m_3 = \sqrt{\frac{\Delta m_{31}^2}{1 - \frac{1}{|R_3(\theta_{12}, \theta_{13}, \theta_{23}, \delta_{CP})|^2}}}$$

Neutrino mass
in case of NO.

$$m_1 = \sqrt{m_3^2 - \Delta m_{31}^2}$$

$$m_2 = \sqrt{m_1^2 + \Delta m_{21}^2} = \sqrt{m_3^2 + \Delta m_{21}^2 - \Delta m_{31}^2}$$

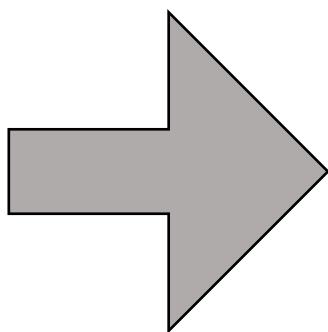
- These masses can be described in terms of θ_{23} .

($\theta_{12}, \theta_{13}, \Delta m_{21}^2, \Delta m_{31}^2$ are fixed as best fit value of NuFITv5.2)

Analysis of SM+N_i+Φ₊₁ Model

- **B₃ texture** : $(\mathcal{M}_{\nu_L})_{[1,2],[2,2]} = 0$

$$\left\{ \begin{array}{l} (\mathcal{M}_{\nu}^{\text{gen}})_{12} = m_1 V_{11} V_{21} + m_2 e^{i\alpha_2} V_{12} V_{22} + m_3 e^{i\alpha_3} V_{13} V_{23} = 0 \quad (= (\mathcal{M}_{\nu})_{12}). \\ (\mathcal{M}_{\nu}^{\text{gen}})_{22} = m_1 V_{21}^2 + m_2 e^{i\alpha_2} V_{22}^2 + m_3 e^{i\alpha_3} V_{23}^2 = 0 \quad (= (\mathcal{M}_{\nu})_{22}). \end{array} \right.$$



$$\left\{ \begin{array}{l} e^{i\alpha_2} \equiv \frac{m_1}{m_2} R_2(\theta_{12}, \theta_{13}, \theta_{23}, \delta) \equiv \frac{R_2}{|R_2|} \\ e^{i\alpha_3} \equiv \frac{m_1}{m_3} R_3(\theta_{12}, \theta_{13}, \theta_{23}, \delta) \equiv \frac{R_3}{|R_3|} \end{array} \right.$$

V_{ij} : components of PMNS matrix , θ_{ij} : mixing angle, δ : CP phase,
 α : Majorana phase

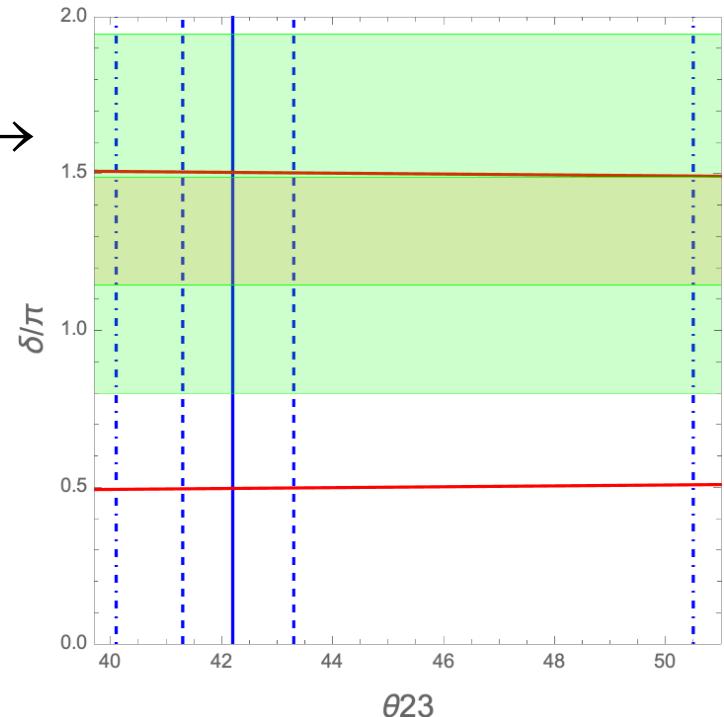
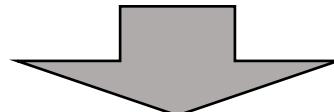
- To rewrite mass-squared difference in case of Normal ordering(NO)

$$\left\{ \begin{array}{l} \Delta m_{31}^2 = m_3^2 - m_1^2 = m_1^2(|R_3|^2 - 1) \\ \Delta m_{21}^2 = m_2^2 - m_1^2 = m_1^2(|R_2|^2 - 1) \end{array} \right.$$

↓

$$(|R_2|^2 - 1) = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} (|R_3|^2 - 1) \rightarrow$$

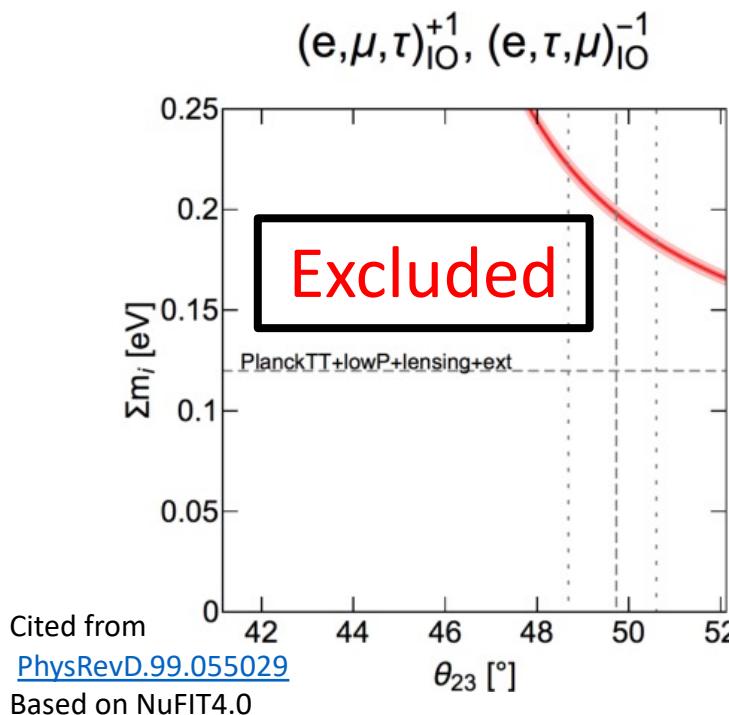
By fixing $\theta_{12}, \theta_{13}, \Delta m_{21}^2, \Delta m_{31}^2$ as the best-fit value of NuFITv5.2,
 θ_{23} -dependence of δ are found.



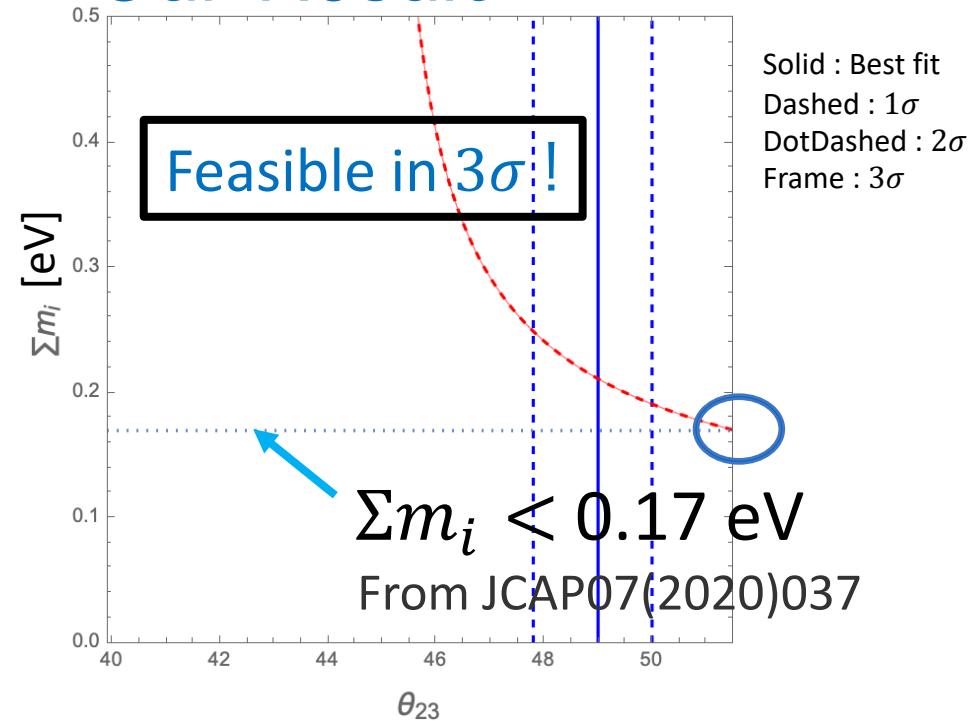
Neutrino mass and Majorana phase can be written by θ_{23} !

Result of Analysis (B_3 Texture)

- Previous Work



- Our Result

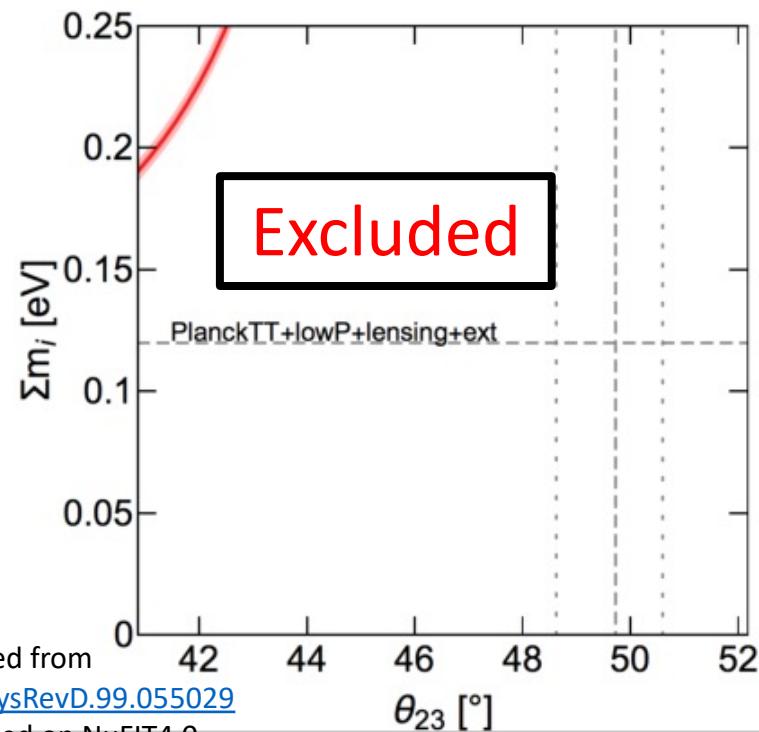


- B_3 -type mass matrix in Inverted ordering is revived.
- The range of θ_{23} shift to left in the latest NuFITv5.2.
- The mass sum constraint is relaxed because of being had considered mass ordering in the analysis.

Analysis Result (NO)

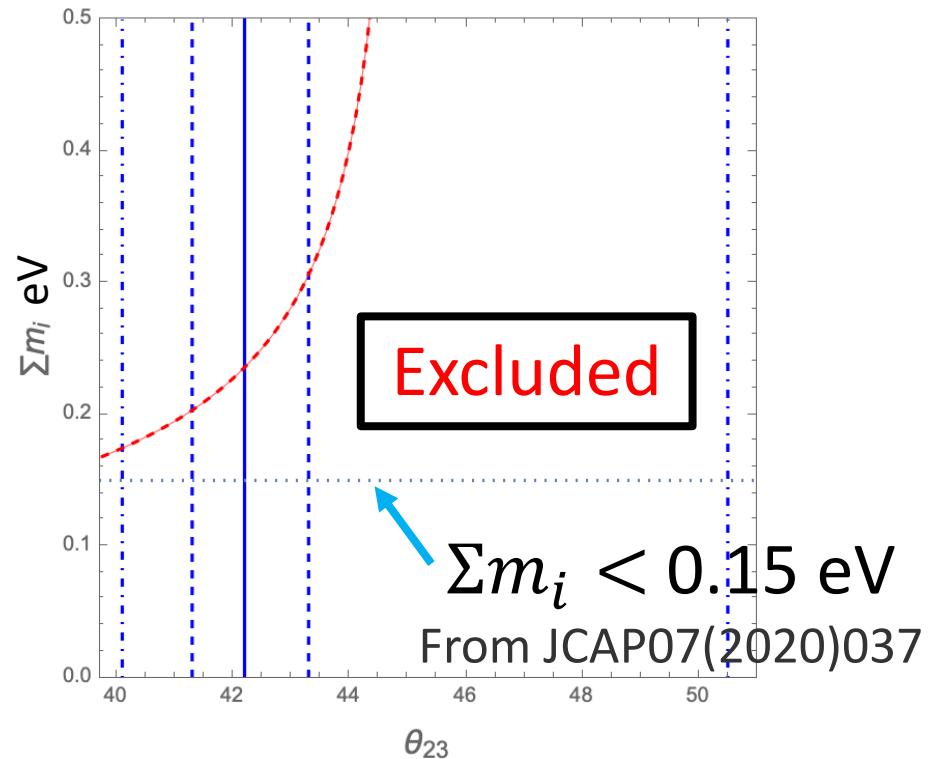
- Previous Work

$$(\mu, \tau, \nu)_\text{NO}^{+1}, (\mu, \tau, \nu)_\text{NO}^{-1}$$



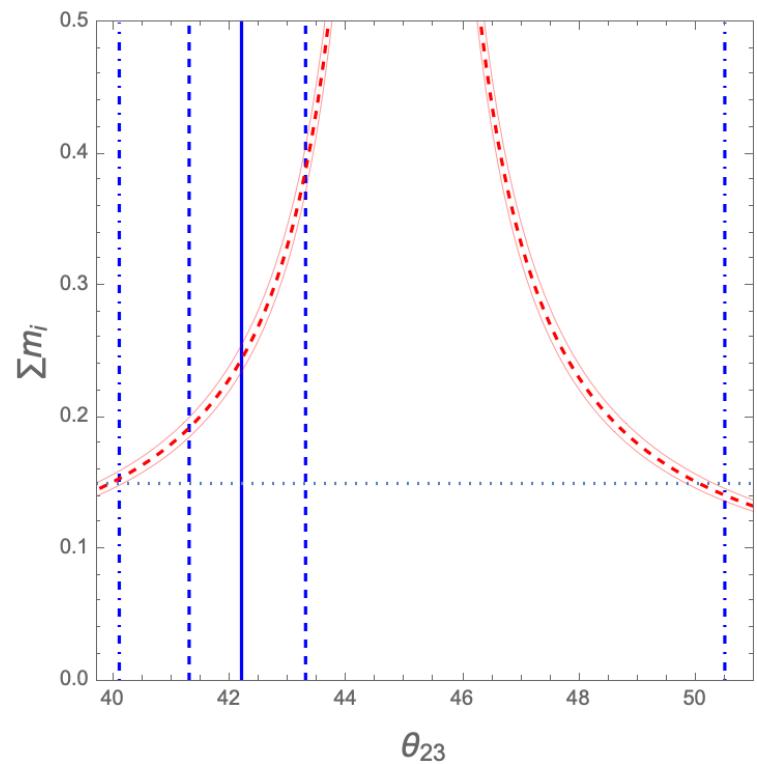
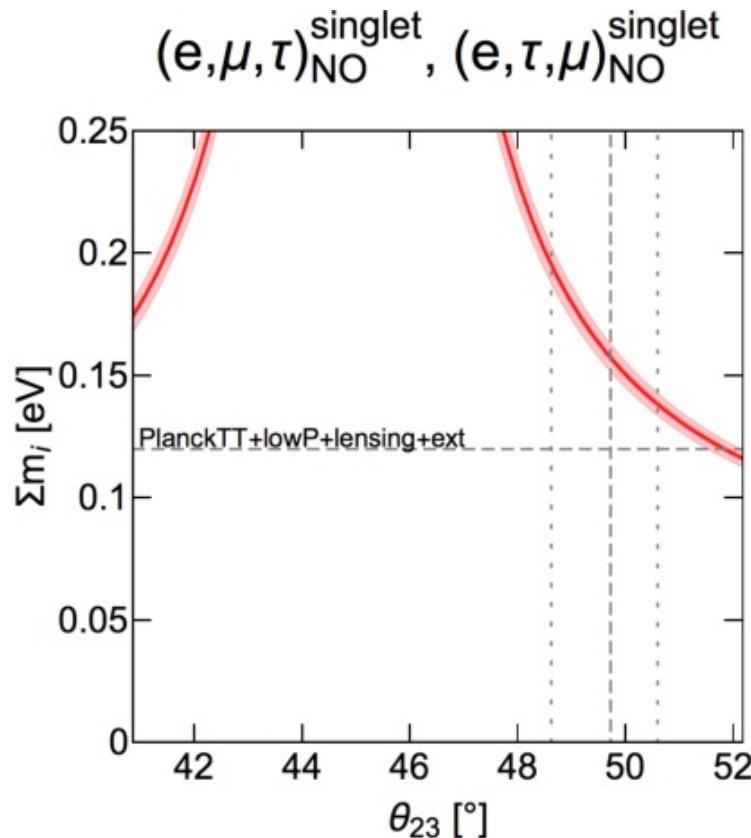
- Our Result

Solid : Best fit
Dashed : 1σ
DotDashed : 2σ
Frame : 3σ

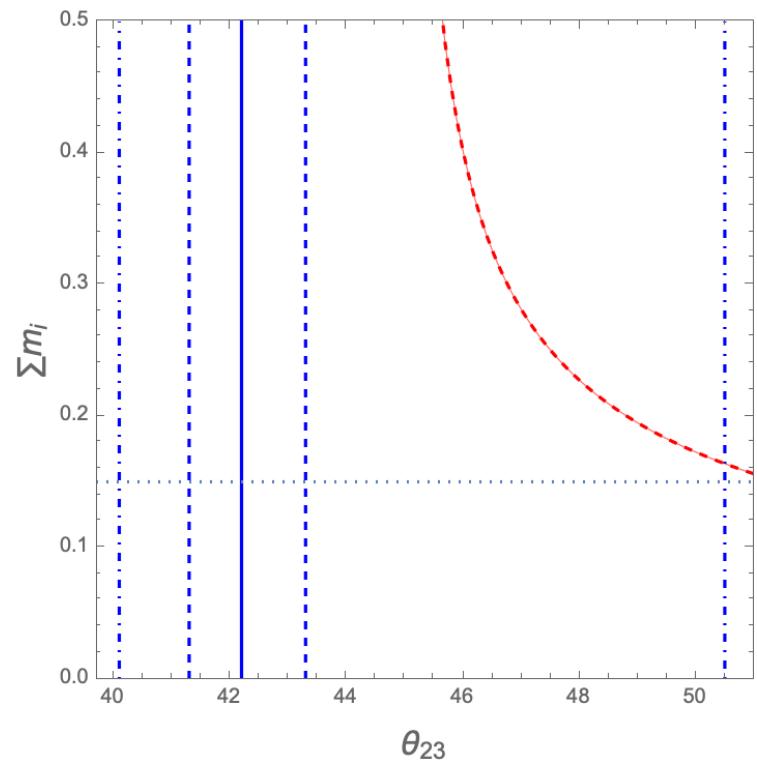
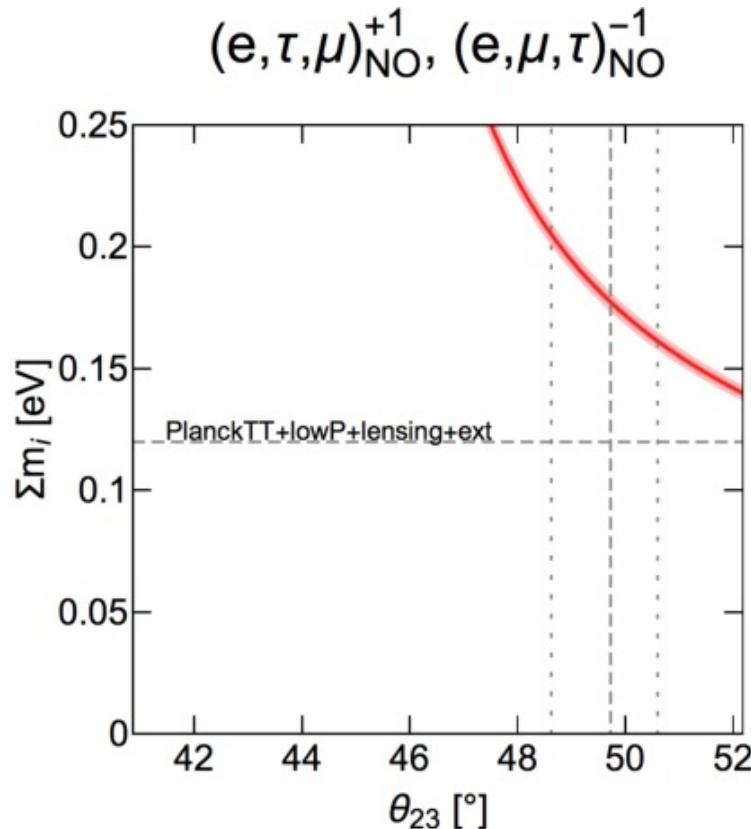


- The range of θ_{23} shift to left in the latest NuFITv5.2.
- The mass sum constraint are relaxed by considering mass ordering.

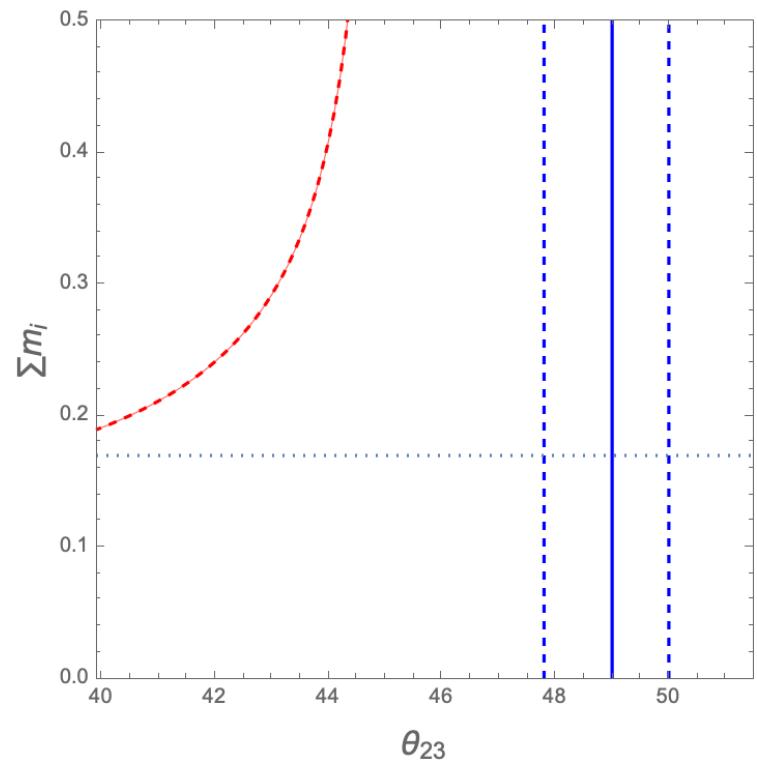
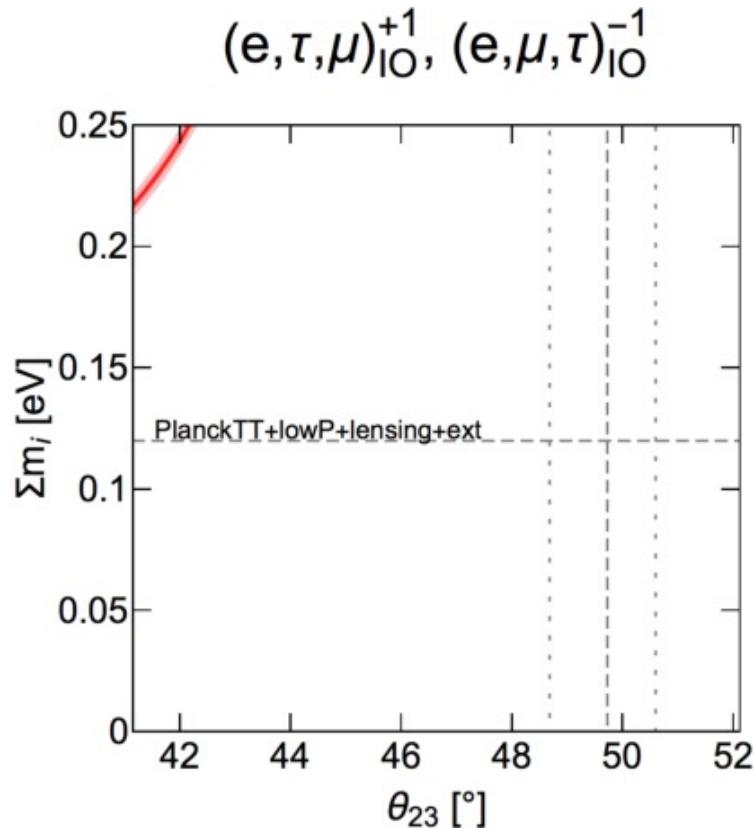
C Minor (NO)



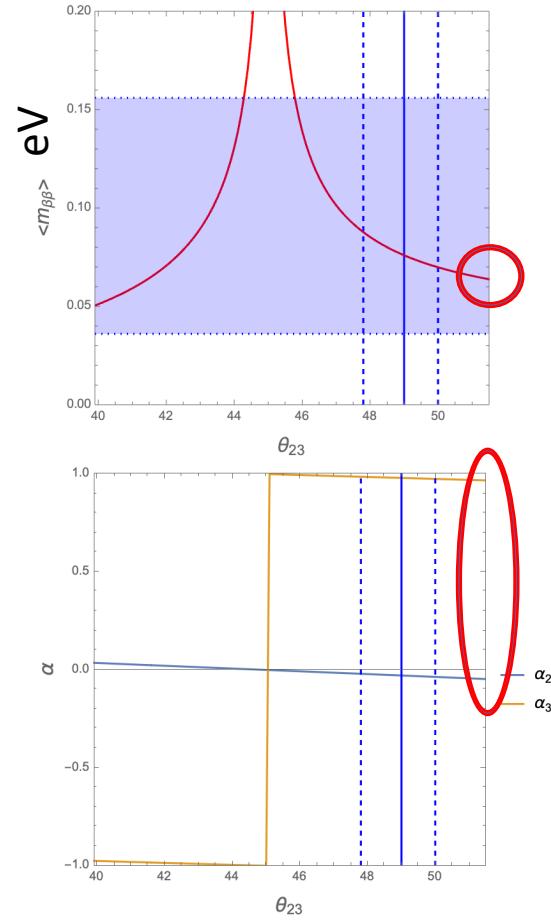
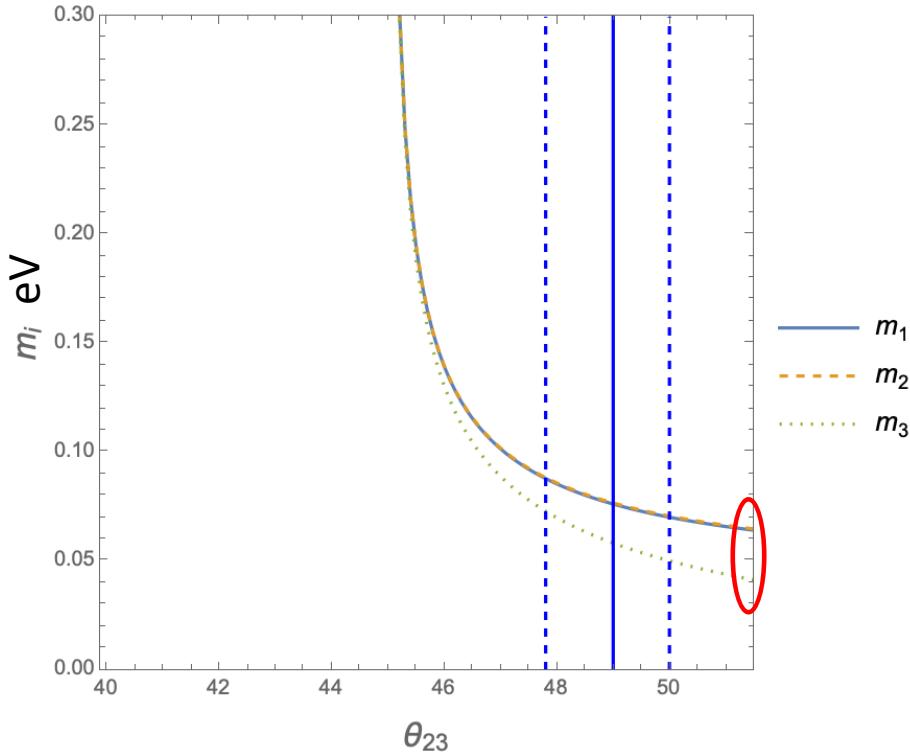
B4 Texture (NO)



B4 Texture (IO)



Result of analysis 2



	m_1 [eV]	m_2 [eV]	m_3 [eV]	α_2/π	α_3/π	$\langle m_{\beta\beta} \rangle$ [eV]
B_3 texture (IO)	0.064	0.065	0.041	-0.05	0.96	0.064