Global analysis and LHC study of a vector-like extension of the Standard Model with extra scalars

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Based on

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in collaboration with

Antonio E. Cárcamo Hernández, Kamila Kowalska, Huchan Lee

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The model was studied for the first time in

1

S.F.King, JHEP 09, 069 (2018)



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and then later again with different type of experimental motivations

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- A.C.Hernández, S.F.King, H.Lee, Phys. Rev. D 105, 015021 (2022)

- H.Lee, A.Cárcamo Hernández, 2207.01710 (2022)

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However, many things were not entirely correct ...



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However, many things were not entirely correct ...



In this work, we **re-assess** the previous analysis and add some **new results**.

The model

Particle Content

| Field | $ Q_{iL}$ | u_{iR} | d_{iR} | L_{iL} | e_{iR} | Q_{4L} | u_{4R} | d_{4R} | L_{4L} | e_{4R} | $ u_{4R}$ | $ \widetilde{Q}_{4R}$ | \widetilde{u}_{4L} | \widetilde{d}_{4L} | \widetilde{L}_{4R} | \widetilde{e}_{4L} | $\widetilde{\nu}_{4L}$ | ϕ | H_u | H_d |
|--------------------|---------------|----------------|---------------|----------------|----------|---------------|----------------|---------------|----------------|----------|-----------|------------------------|----------------------|----------------------|----------------------|----------------------|------------------------|--------|---------------|----------------|
| $\mathrm{SU}(3)_C$ | 3 | $ar{3}$ | $ar{3}$ | 1 | 1 | 3 | $ar{3}$ | $ar{3}$ | 1 | 1 | 1 | 3 | 3 | 3 | 1 | 1 | 1 | 1 | 1 | 1 |
| $\mathrm{SU}(2)_L$ | 2 | 1 | 1 | 2 | 1 | 2 | 1 | 1 | 2 | 1 | 1 | 2 | 1 | 1 | 2 | 1 | 1 | 1 | 2 | 2 |
| $\mathrm{U}(1)_Y$ | $\frac{1}{6}$ | $-\frac{2}{3}$ | $\frac{1}{3}$ | $-\frac{1}{2}$ | 1 | $\frac{1}{6}$ | $-\frac{2}{3}$ | $\frac{1}{3}$ | $-\frac{1}{2}$ | 1 | 0 | $-\frac{1}{6}$ | $\frac{2}{3}$ | $-\frac{1}{3}$ | $\frac{1}{2}$ | -1 | 0 | 0 | $\frac{1}{2}$ | $-\frac{1}{2}$ |
| $\mathrm{U}(1)_X$ | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | -1 | 1 | -1 | -1 |

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The model

Particle Content

| Field | $ Q_{iL}$ | u_{iR} | d_{iR} | L_{iL} | e_{iR} | Q_{4L} | u_{4R} | d_{4R} | L_{4L} | e_{4R} | ν_{4R} | $ \widetilde{Q}_{4R}$ | \widetilde{u}_{4L} | \widetilde{d}_{4L} | \widetilde{L}_{4R} | \widetilde{e}_{4L} | $\widetilde{\nu}_{4L}$ | ϕ | H_u | H_d |
|--------------------|---------------|----------------|---------------|----------------|----------|---------------|----------------|---------------|----------------|----------|------------|------------------------|----------------------|----------------------|----------------------|----------------------|------------------------|--------|---------------|----------------|
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| $\mathrm{SU}(2)_L$ | 2 | 1 | 1 | 2 | 1 | 2 | 1 | 1 | 2 | 1 | 1 | 2 | 1 | 1 | 2 | 1 | 1 | 1 | 2 | 2 |
| $\mathrm{U}(1)_Y$ | $\frac{1}{6}$ | $-\frac{2}{3}$ | $\frac{1}{3}$ | $-\frac{1}{2}$ | 1 | $\frac{1}{6}$ | $-\frac{2}{3}$ | $\frac{1}{3}$ | $-\frac{1}{2}$ | 1 | 0 | $-\frac{1}{6}$ | $\frac{2}{3}$ | $-\frac{1}{3}$ | $\frac{1}{2}$ | -1 | 0 | 0 | $\frac{1}{2}$ | $-\frac{1}{2}$ |
| $\mathrm{U}(1)_X$ | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | -1 | 1 | -1 | -1 |



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Mass of 3rd generation fermions

$$m_t \approx \frac{1}{\sqrt{2}} \frac{y_{43}^u x_{34}^Q v_\phi v_u}{\sqrt{(x_{34}^Q v_\phi)^2 + 2(M_4^Q)^2}}$$



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$$m_c \approx \frac{y_{24}^u x_{42}^u v_\phi v_u}{2 M_4^u}$$



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Mass of 3rd generation fermions

Mass of 2nd generation fermions

$$m_t \approx \frac{1}{\sqrt{2}} \underbrace{\frac{y_{43}^u x_{34}^Q v_{\phi} v_u}{\sqrt{(x_{34}^Q v_{\phi})^2 + 2(M_4^Q)^2}}}_{\text{Need to be O(1) to fit}} \qquad m_c \approx \frac{\frac{y_{24}^u x_{42}^u v_{\phi} v_u}{\sqrt{2M_4^u}}}{\sqrt{(x_{34}^Q v_{\phi})^2 + 2(M_4^Q)^2}}$$
Need to be O(1) to fit the experimental value

The 2 contributions need to be of the same order

Mass of 3rd generation fermions

Mass of 2nd generation fermions





Mass of 3rd generation fermions

Mass of 2nd generation fermions



$$V = \mu_u^2 (H_u^{\dagger} H_u) + \mu_d^2 (H_d^{\dagger} H_d) + \mu_{\phi}^2 (\phi^* \phi) - \frac{1}{2} \mu_{sb}^2 (\phi^2 + \phi^{*2}) + \frac{1}{2} \lambda_1 (H_u^{\dagger} H_u)^2 + \frac{1}{2} \lambda_2 (H_d^{\dagger} H_d)^2 + \lambda_3 (H_u^{\dagger} H_u) (H_d^{\dagger} H_d) + \lambda_4 (H_u^{\dagger} H_d) (H_d^{\dagger} H_u) - \frac{1}{2} \lambda_5 (\epsilon_{ij} H_u^i H_d^j \phi^2 + H.c.) + \frac{1}{2} \lambda_6 (\phi^* \phi)^2 + \lambda_7 (\phi^* \phi) (H_u^{\dagger} H_u) + \lambda_8 (\phi^* \phi) (H_d^{\dagger} H_d)$$

3 massive CP-Even

Spectrum: 2 massive CP-Odd + 1 Goldstone

1 massive charged + 1 Goldstone

$$V = \mu_u^2 (H_u^{\dagger} H_u) + \mu_d^2 (H_d^{\dagger} H_d) + \mu_{\phi}^2 (\phi^* \phi) - \frac{1}{2} \mu_{sb}^2 (\phi^2 + \phi^{*2}) + \frac{1}{2} \lambda_1 (H_u^{\dagger} H_u)^2 + \frac{1}{2} \lambda_2 (H_d^{\dagger} H_d)^2 + \lambda_3 (H_u^{\dagger} H_u) (H_d^{\dagger} H_d) + \lambda_4 (H_u^{\dagger} H_d) (H_d^{\dagger} H_u) - \frac{1}{2} \lambda_5 (\epsilon_{ij} H_u^i H_d^j \phi^2 + H.c.) + \frac{1}{2} \lambda_6 (\phi^* \phi)^2 + \lambda_7 (\phi^* \phi) (H_u^{\dagger} H_u) + \lambda_8 (\phi^* \phi) (H_d^{\dagger} H_d)$$

3 massive CP-Even **Spectrum:** 2 massive CP-Odd + 1 Goldstone 1 massive charged + 1 Goldstone

Alignment limit:

 $\lambda_2 = \lambda_3 + \tan^2 \beta (\lambda_1 - \lambda_3) \qquad \qquad \lambda_8 = -\tan \beta (\lambda_7 \tan \beta + \lambda_5)$

$$V = \mu_u^2 (H_u^{\dagger} H_u) + \mu_d^2 (H_d^{\dagger} H_d) + \mu_{\phi}^2 (\phi^* \phi) - \frac{1}{2} \mu_{sb}^2 (\phi^2 + \phi^{*2}) + \frac{1}{2} \lambda_1 (H_u^{\dagger} H_u)^2 + \frac{1}{2} \lambda_2 (H_d^{\dagger} H_d)^2 + \lambda_3 (H_u^{\dagger} H_u) (H_d^{\dagger} H_d) + \lambda_4 (H_u^{\dagger} H_d) (H_d^{\dagger} H_u) - \frac{1}{2} \lambda_5 (\epsilon_{ij} H_u^i H_d^j \phi^2 + H.c.) + \frac{1}{2} \lambda_6 (\phi^* \phi)^2 + \lambda_7 (\phi^* \phi) (H_u^{\dagger} H_u) + \lambda_8 (\phi^* \phi) (H_d^{\dagger} H_d)$$

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Alignment limit:

 $\lambda_{2} = \lambda_{3} + \tan^{2} \beta (\lambda_{1} - \lambda_{3}) \qquad \qquad \lambda_{8} = -\tan \beta (\lambda_{7} \tan \beta + \lambda_{5})$ $\lambda_{3} \approx \lambda_{1} + \mathcal{O}(1/\tan^{2} \beta) \qquad \qquad \lambda_{7} \sim \mathcal{O}(1/\tan^{2} \beta) \qquad \qquad \lambda_{5} \sim \mathcal{O}(1/\tan \beta)$

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$$V = \mu_u^2 (H_u^{\dagger} H_u) + \mu_d^2 (H_d^{\dagger} H_d) + \mu_{\phi}^2 (\phi^* \phi) - \frac{1}{2} \mu_{sb}^2 (\phi^2 + \phi^{*2}) + \frac{1}{2} \lambda_1 (H_u^{\dagger} H_u)^2 + \frac{1}{2} \lambda_2 (H_d^{\dagger} H_d)^2 + \lambda_3 (H_u^{\dagger} H_u) (H_d^{\dagger} H_d) + \lambda_4 (H_u^{\dagger} H_d) (H_d^{\dagger} H_u) - \frac{1}{2} \lambda_5 (\epsilon_{ij} H_u^i H_d^j \phi^2 + H.c.) + \frac{1}{2} \lambda_6 (\phi^* \phi)^2 + \lambda_7 (\phi^* \phi) (H_u^{\dagger} H_u) + \lambda_8 (\phi^* \phi) (H_d^{\dagger} H_d)$$

"Boundedness from below"

5



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"Boundedness from below"

5

 $\lambda_{8} + \sqrt{\lambda_{2}\lambda_{6}} > 0 \qquad -\frac{1}{4} \frac{(\operatorname{Re}\lambda_{5})^{2} + (\operatorname{Im}\lambda_{5})^{2}}{\lambda_{a}} + \lambda_{4} > 0$ $\lambda_{7} + \sqrt{\lambda_{1}\lambda_{6}} > 0 \qquad 4\lambda_{b}^{2} - (\operatorname{Re}\lambda_{5})^{2} + \operatorname{Re}\lambda_{5}\operatorname{Im}\lambda_{5} > 0$ $\lambda_3 + \sqrt{\lambda_2 \lambda_1} > 0$ $\lambda_3 + \lambda_4 + \sqrt{\lambda_2 \lambda_1} > 0$ $4\lambda_b^2 - (\mathrm{Im}\lambda_5)^2 + \mathrm{Re}\lambda_5\mathrm{Im}\lambda_5 > 0$ These conditions were These were already implemented in not considered in 2HDM Type II previous works previous work

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| Parameter | case A | case B | case C | case D | case E |
|-----------------------|---------|---------|---------|---------|---------|
| $v_u = v_1$ | 245.925 | 245.936 | 245.951 | 245.917 | 245.948 |
| $v_d = v_2$ | 6.086 | 5.595 | 4.921 | 6.387 | 5.077 |
| $v_{\phi} = v_3$ | -57.761 | -36.470 | -57.919 | -30.746 | -17.146 |
| $\tan\beta = v_u/v_d$ | 40.410 | 43.957 | 49.977 | 38.503 | 48.441 |
| λ_1 | 0.063 | 0.064 | 0.066 | 0.064 | 0.065 |
| λ_2 | -7.978 | 8.414 | -2.000 | 2.948 | 10.382 |
| λ_3 | -6.344 | -2.675 | 6.242 | -1.724 | -0.706 |
| λ_4 | 1.859 | 2.158 | -3.633 | 10.837 | -2.796 |
| λ_5 | -11.384 | -11.070 | 9.009 | -11.460 | -12.000 |
| λ_6 | 2.888 | 1.228 | 0.866 | 1.351 | 1.324 |
| λ_7 | -0.282 | -0.252 | 0.180 | -0.298 | -0.248 |
| λ_8 | -1.363 | -1.346 | -10.845 | -11.510 | 7.033 |

A.Cárcamo Hernández, S.F.King, H.Lee, Phys. Rev. D 103, 115024 (2021)

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| Small vev for the singlet | Parameter | case A | case B | case C | case D | case E |
|---------------------------|-----------------------|---------|---------|---------|---------|---------|
| Rig values of tap bota | $v_u = v_1$ | 245.925 | 245.936 | 245.951 | 245.917 | 245.948 |
| Big values of tall beta | $v_d = v_2$ | 6.086 | 5.595 | 4.921 | 6.387 | 5.077 |
| The scalar potential is | $v_{\phi} = v_3$ | -57.761 | -36.470 | -57.919 | -30.746 | -17.146 |
| not bounded from below | $\tan\beta = v_u/v_d$ | 40.410 | 43.957 | 49.977 | 38.503 | 48.441 |
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Small vev for the singlet

Big values of tan beta

The scalar potential is not bounded from below

Almost non-perturbative quartic couplings

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| $v_u = v_1$ | 245.925 | 245.936 | 245.951 | 245.917 | 245.948 |
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Small vev for the singlet

Big values of tan beta

The scalar potential is not bounded from below

Almost non-perturbative quartic couplings

Their perturbativity condition is given by $g, y(\mathrm{NP}) < \sqrt{4\pi}$ $\lambda(\mathrm{NP}) < 4\pi$

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$$\Delta a_{\mu} = \sum_{i,j} \left\{ -\frac{m_{\mu}^2}{16\pi^2 M_{\phi_i}^2} \left(|y_L^{ij}|^2 + |y_R^{ij}|^2 \right) [Q_j \mathcal{F}_1(x_{ij}) - Q_i \mathcal{G}_1(x_{ij})] - \frac{m_{\mu} M_{\psi_j}}{16\pi^2 M_{\phi_i}^2} \operatorname{Re} \left(y_L^{ij} y_R^{ij*} \right) [Q_j \mathcal{F}_2(x_{ij}) - Q_i \mathcal{G}_2(x_{ij})] \right\}$$

$$\Delta a_{\mu} = (2.49 \pm 0.48) \times 10^{-9}$$

Discrepancy is now at $\sim 5.1 \sigma$

7



Bennet et al, Phys. Rev. D 73 (2006) 072003 (hep-ex/0602035) Muon g-2 Collaboration, Phys. Rev. Lett. 126 (2021) 141801 Muon g-2 Collaboration, arXiv: 2308.06230

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$$\Delta a_{\mu} = \sum_{i,j} \left\{ -\frac{m_{\mu}^{2}}{16\pi^{2}M_{\phi_{i}}^{2}} \left(|y_{L}^{ij}|^{2} + |y_{R}^{ij}|^{2} \right) [Q_{j}\mathcal{F}_{1}\left(x_{ij}\right) - Q_{i}\mathcal{G}_{1}\left(x_{ij}\right)] - \frac{m_{\mu}M_{\psi_{j}}}{16\pi^{2}M_{\phi_{i}}^{2}} \operatorname{Re}\left(y_{L}^{ij}y_{R}^{ij*}\right) [Q_{j}\mathcal{F}_{2}\left(x_{ij}\right) - Q_{i}\mathcal{G}_{2}\left(x_{ij}\right)] \right\}$$

$$\Delta a_{\mu} = (2.49 \pm 0.48) \times 10^{-9}$$
Discrepancy is now at ~5.1 σ

$$\downarrow$$
Lattice
???

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Bennet et al, Phys. Rev. D 73 (2006) 072003 (hep-ex/0602035) Muon g-2 Collaboration, Phys. Rev. Lett. 126 (2021) 141801 Muon g-2 Collaboration, arXiv: 2308.06230

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We define the cutoff energy for the model by requiring that any New Physics wrt the model is at such an energy scale that the corrections to g-2 are negligible.

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By requiring that such correction is smaller than 3σ and in the most pessimistic scenario

$$y_L(\Lambda) = y_R(\Lambda) = \sqrt{4\pi}$$

9



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$$\Delta a_{\mu}^{\Lambda} \sim \frac{1}{16\pi^2} \frac{m_{\mu} v}{\Lambda^2} y_L(\Lambda) y_R(\Lambda)$$



By requiring that such correction is smaller than 3σ and in the most pessimistic scenario

$$y_L(\Lambda) = y_R(\Lambda) = \sqrt{4\pi}$$

$$g, y(\text{NP}) < \sqrt{4\pi}$$

$$\lambda(\text{NP}) < 4\pi$$

 $\longrightarrow \Lambda \gtrsim 50 \text{ TeV}$

 $y_L(\Lambda) = y_R(\Lambda) = \sqrt{4\pi}$

We define the cutoff energy for the model by requiring that any New Physics wrt the model is at such an energy scale that the corrections to g-2 are negligible.

$$\Delta a_{\mu}^{\Lambda} \sim \frac{1}{16\pi^2} \frac{m_{\mu} v}{\Lambda^2} y_L(\Lambda) y_R(\Lambda)$$



By requiring that such correction is smaller than 3σ and in the most pessimistic scenario

$$\longrightarrow \Lambda \gtrsim 50 \text{ TeV}$$

$$g, y(\text{NP}) < \sqrt{4\pi} \qquad g, y(\text{NP}) \lesssim 1$$
$$\lambda(\text{NP}) < 4\pi \qquad \lambda(\text{NP}) \lesssim 2$$

All benchmark point from previous works are this way excluded.

| | Contributions to $\Delta a_{\mu} \times 10^9$ | | | | | | | | | | | | | |
|--|---|---------|-----|---|---------|---------|-----|--|--|--|--|--|--|--|
| | Charged | scalars | | | CP-even | scalars | | | | | | | | |
| Loop | BP1 | BP2 | BP3 | Loop | BP1 | BP2 | BP3 | | | | | | | |
| $h^{\pm}, N_{1,2}$ $h^{\pm}, N_{3,4}$ | | | | | | | | | | | | | | |
| $h^{\pm}, N_{\rm tot}$ | | | | h_2, E_1 | | | | | | | | | | |
| | CP-odd | scalars | | h_2, E_2 | | | | | | | | | | |
| $a_1, E_1 \\ a_1, E_2$ | | | | $ \begin{array}{c c} h_3, E_1 \\ h_3, E_2 \end{array} $ | | | | | | | | | | |
| a_2, E_1 | | | | h, E_{tot} | | | | | | | | | | |
| a_2, E_2 | | | | | То | tal | | | | | | | | |
| $a, E_{\rm tot}$ | | | | Δa_{μ} | | | | | | | | | | |

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| | | | Contributions to | $\Delta a_{\mu} \times 10^9$ | | | |
|--|---------------------------------|---------------------------------|-----------------------------|------------------------------|--------|-------------|-----------------------|
| | Chargeo | d scalars | | | CP-eve | n scalars | |
| Loop | BP1 | BP2 | BP3 | Loop | BP1 | BP2 | BP3 |
| $h^{\pm}, N_{1,2}$ $h^{\pm}, N_{3,4}$ | | | | h_1, E_1 h_1, E_2 | | | |
| $h^{\pm}, N_{\rm tot}$ | | | | h_2, E_1 | | | |
| | CP-odd | scalars | | h_{2}, E_{2} | | | |
| $a_1, E_1 \\ a_1, E_2$ | | | | h_3, E_1 h_3, E_2 | | | |
| a_2, E_1 | | | | $h, E_{\rm tot}$ | | | |
| a_2, E_2 | | | | | Πγ | <u>stal</u> | γ |
| $a, E_{\rm tot}$ | | | | Δa_{μ} | | | , , , , , |
| Contril diagra alread | outions ms have y in prev | given b e been o vious wo | y these computec orks |) + | E 1 | | |

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| | | (| Contributions t | to $\Delta a_{\mu} \times 10^9$ | | | |
|--|--------------------------------|--|-------------------------|--|--------------|-----------|----------|
| | Charged | l scalars | | | CP-ever | ı scalars | |
| Loop | BP1 | BR2 | ВР3 ∥ | Loop | BP1 | BP2 | BP3 |
| $h^{\pm}, N_{1,2}$ $h^{\pm}, N_{3,4}$ | | | | $egin{array}{l} h_1, E_1 \ h_1, E_2 \end{array}$ | | | |
| $h^{\pm}, N_{\rm tot}$ | | | | h_2, E_1 | | | |
| | CP-odd | scalars | | h_2, E_2 | | | |
| $a_1, E_1 \\ a_1, E_2$ | | | \downarrow | h_3, E_1 h_3, E_2 | | | |
| a_2, E_1 | | | | $h, E_{ m tot}$ | | | |
| a_2, E_2 | | | | | To | tal | γ |
| $a, E_{\rm tot}$ | | | | Δa_{μ} | \backslash | | ، ب |
| Contril diagra consid | outions m have ered in j | given by not bee previous | / this en s works | | μ | N1 2 | |

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| Contributions to $\Delta a_{\mu} \times 10^9$ | | | | | | | | | | | | | |
|---|--------|-----------|--------|------------------|--------|--------|--------|--|--|--|--|--|--|
| | Charge | d scalars | | CP-even scalars | | | | | | | | | |
| Loop | BP1 | BP2 | BP3 | Loop | BP1 | BP2 | BP3 | | | | | | |
| $h^{\pm}, N_{1,2}$ | -1.076 | -0.792 | -0.942 | $\ h_1, E_1$ | -0.003 | -0.001 | -0.009 | | | | | | |
| $h^{\pm}, N_{3,4}$ | 3.300 | 2.898 | 3.153 | h_1, E_2 | 0.003 | 0.001 | 0.009 | | | | | | |
| $h^{\pm}, N_{\rm tot}$ | 2.225 | 2.106 | 2.211 | h_2, E_1 | -0.409 | -0.520 | -0.969 | | | | | | |
| | CP-odd | scalars | | h_2, E_2 | 0.437 | 0.548 | 0.994 | | | | | | |
| a_1, E_1 | 0.425 | 0.528 | 0.938 | $\ h_3, E_1$ | 0.018 | 0.115 | 0.076 | | | | | | |
| a_1, E_2 | -0.544 | -0.611 | -1.529 | h_3, E_2 | -0.017 | -0.127 | -0.076 | | | | | | |
| a_2, E_1 | -0.033 | -0.135 | -0.071 | $h, E_{\rm tot}$ | 0.032 | 0.027 | 0.025 | | | | | | |
| a_2, E_2 | 0.110 | 0.196 | 0.621 | Total | | | | | | | | | |
| $a, E_{\rm tot}$ | -0.015 | -0.023 | -0.041 | Δa_{μ} | 2.215 | 2.101 | 2.196 | | | | | | |

The deviation from the experimental measurement of g-2 can be explained within this model.

The main contribution to g-2 in mediated by **charged scalars** and **neutrinos**!

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VL Quarks

 $U_1 \rightarrow \sim 1500 \qquad \text{GeV}$ $D_1 \rightarrow \sim 1500 \qquad \text{GeV}$ $U_2 \rightarrow \sim 1700\text{-}1900 \qquad \text{GeV}$ $D_2 \rightarrow \sim 2900\text{-}3600 \qquad \text{GeV}$

VL Leptons

 $\begin{array}{l} N_{1,2} \rightarrow \sim 200 \quad \text{GeV} \\ N_{3,4} \rightarrow \sim 500\text{-}600 \quad \text{GeV} \\ E_1 \quad \rightarrow \sim 500\text{-}600 \quad \text{GeV} \\ E_2 \quad \rightarrow \sim 550\text{-}650 \quad \text{GeV} \end{array}$

CP-Even Scalars

CP-Odd Scalars

 $a_1 \rightarrow \sim 400 \quad \text{GeV}$ $a_2 \rightarrow \sim 450\text{-}600 \quad \text{GeV}$

Charged Scalars

h_± → ~400 GeV

$\begin{array}{ll} h_1 \rightarrow & 125 & \text{GeV} \\ h_2 \rightarrow \sim 400 & \text{GeV} \end{array}$

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h₃ → ~600-800 GeV

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VL Leptons

 $\begin{array}{l} N_{1,2} \rightarrow \sim 200 \quad \text{GeV} \\ N_{3,4} \rightarrow \sim 500\text{-}600 \quad \text{GeV} \\ E_1 \quad \rightarrow \sim 500\text{-}600 \quad \text{GeV} \\ E_2 \quad \rightarrow \sim 550\text{-}650 \quad \text{GeV} \end{array}$

CP-Even Scalars

11

CP-Odd Scalars

 $h_1 \rightarrow 125$ GeV $a_1 \rightarrow \sim 400$ GeV $h_2 \rightarrow \sim 400$ GeV $a_2 \rightarrow \sim 450-600$ GeV $h_3 \rightarrow \sim 600-800$ GeV $a_2 \rightarrow \sim 450-600$ GeV

Charged Scalars

h_± → ~400 GeV

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Almost degenerative because depend on the mass of the VL doublet

VL Leptons

 $\begin{array}{l} N_{1,2} \rightarrow \sim 200 \quad \text{GeV} \\ N_{3,4} \rightarrow \sim 500\text{-}600 \quad \text{GeV} \\ E_1 \quad \rightarrow \sim 500\text{-}600 \quad \text{GeV} \\ E_2 \quad \rightarrow \sim 550\text{-}650 \quad \text{GeV} \end{array}$

CP-Even Scalars

11

CP-Odd Scalars

 $h_1 \rightarrow 125$ GeV $h_2 \rightarrow \sim 400$ GeV $h_3 \rightarrow \sim 600-800$ GeV $a_1 \rightarrow \sim 400 \quad \text{GeV}$ $a_2 \rightarrow \sim 450\text{-}600 \quad \text{GeV}$

Charged Scalars

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VL Leptons

$$\begin{array}{ccc} \mathsf{N}_{1,2} \to \sim 200 & \text{GeV} \\ \mathsf{N}_{3,4} \to \sim 500\text{-}600 & \text{GeV} \\ \mathsf{E}_1 \to \sim 500\text{-}600 & \text{GeV} \\ \mathsf{E}_2 \to \sim 550\text{-}650 & \text{GeV} \end{array} \right\} \approx \sqrt{(M_4^L)^2 + \frac{1}{2}(v_\phi x_{34}^L)^2}$$

GeV

CP-Even Scalars

 $h_2 \rightarrow \sim 400$ GeV

h₃ → ~600-800 GeV

 $h_1 \rightarrow 125$

11

CP-Odd Scalars

 $a_1 \rightarrow \sim 400 \quad \text{GeV}$ $a_2 \rightarrow \sim 450\text{-}600 \quad \text{GeV}$

Charged Scalars

h_± → ~400 GeV



VL Leptons



CP-Even Scalars

 $h_1 \rightarrow 125$ GeV

 $h_2 \rightarrow \sim 400$ GeV

h₃ → ~600-800 GeV

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CP-Odd Scalars

 $\begin{array}{ll} a_1 \rightarrow \sim 400 & \text{GeV} \\ a_2 \rightarrow \sim 450\text{-}600 & \text{GeV} \end{array}$

Charged Scalars $h_+ \rightarrow \sim 400 \text{ GeV}$

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VL Leptons

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Can be tested in Run 3

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Leptons

Quarks



Leptons

Quarks

Our leptons decay predominantly to muons, but there are **no** dedicated experimental analysis.



Leptons

Quarks

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Our leptons decay predominantly to muons, but there are **no** dedicated experimental analysis.

The best we can do is study:



ATLAS: JHEP 07, 118 (2023) CMS: Phys. Rev. D 100, 052003 (2019)

Leptons

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ATLAS: JHEP 07, 118 (2023) CMS: Phys. Rev. D 100, 052003 (2019)

BR(LL $\rightarrow \tau \tau$) < 10% and x-section is 3-4 orders of magnitude **smaller** than current bounds.

Leptons

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12

Quarks

Two possible channels can be studied:



ATLAS: Eur. Phys. J. C 83, 719 (2023) CMS: JHEP 07, 020 (2023)

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Can not be tested in Run 3

12

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Can be tested in Run 3

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Conclusions

- I have discussed a NP model which can explain SM fermion's **mass generation** (and mixings) in a completely new way (SM-like interactions are not allowed).
- We have re-assessed findings from previous works. The main result is a thorough study of the perturbativity of the model, investigated by requiring that the observable do not get corrections from possible UV completions.
- When imposing conditions on the parameter space (SM masses and couplings, vacuum stability, perturbativity) the number of free parameters gets drastically reduced, preventing the model from having a too big parameter space.
- We have presented (c.f. paper) **three benchmark points** which accommodate all the physical requirements and explain the deviation in the muon g-2.
- Incidentally, the perturbativity of the benchmark points is guaranteed up to a much higher energy scale (1000 TeV) than the theoretical value (50 TeV).
- The main contribution to **g-2** is the loop with **neutrino** and **charged scalar**.

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• The benchmark points can be **tested** at the LHC: discovery/exclusion.

CKM Mixing Matrix

Reduced CKM matrix

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$$V_{\rm CKM}^{3\times3} \approx \begin{pmatrix} 1 - x_{ud}^2/2 & x_{ud} & x_{ud}x_d \\ -x_{ud} & 1 - x_{ud}^2/2 & x_d - x_u \\ -x_u x_{ud} & x_u - x_d & 1 \end{pmatrix}$$

$$x_d = \frac{y_{24}^d x_{43}^d M_4^Q}{y_{43}^d x_{34}^Q M_4^d} = 0.017 \qquad x_u = \frac{y_{24}^u x_{43}^u M_4^Q}{y_{43}^u x_{34}^Q M_4^u} \approx -0.023 \qquad x_{ud} = \frac{y_{14}^d}{y_{24}^d} \approx 0.22$$

$$\frac{|V_{CKM}^{exp}| - |V_{CKM}^{3 \times 3}|}{\delta |V_{CKM}^{exp}|} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0.04 & 0 \\ 8.88 & 0.23 & 0.01 \end{pmatrix}$$

With only 1 VL family it is not possible to fit all the elements of the CKM matrix!

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$$M_{U_1} \approx \sqrt{(M_4^Q)^2 + \frac{1}{2}(v_\phi x_{34}^Q)^2 - \frac{(M_4^Q y_{43}^u v_u)^2}{(x_{34}^Q v_\phi)^2 + 2(M_4^Q)^2}}$$

$$M_{U_2} \approx \sqrt{(M_4^u)^2 + \frac{1}{2}(v_\phi x_{43}^u)^2 + \frac{1}{2}(v_\phi x_{42}^u)^2 + \frac{2(M_4^u y_{43}^u v_u)^2}{2(M_4^u)^2 + (v_\phi x_{43}^u)^2 + (v_\phi x_{42}^u)^2}}$$

$$M_{D_1} \approx \sqrt{(M_4^Q)^2 + \frac{1}{2}(v_\phi x_{34}^Q)^2} \qquad M_{D_2} \approx \sqrt{(M_4^d)^2 + \frac{1}{2}(v_\phi x_{43}^d)^2 + \frac{1}{2}(v_\phi x_{42}^d)^2}}$$

$$M_{E_1} \approx \sqrt{(M_4^L)^2 + \frac{1}{2}(v_\phi x_{34}^L)^2} \qquad M_{E_2} \approx \sqrt{(M_4^e)^2 + \frac{1}{2}(v_\phi x_{43}^e)^2 + \frac{1}{2}(v_\phi x_{42}^e)^2}}$$

$$M_{N_1} = M_{N_2} \approx M_4^\nu \qquad M_{N_3} = M_{N_4} \approx \sqrt{(M_4^L)^2 + \frac{1}{2}(v_\phi x_{34}^L)^2}$$

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Parameter Space

| | | | | | Scalar sector | | | | |
|--|--|--|--|---|--|---|--|---|--|
| $\boxed{\frac{\tan\beta}{\lambda_4}}$ | [2, 50] [-2.0, +2.0] | $egin{array}{c} v_{\phi} \ \lambda_{5} \end{array}$ | [1000, 1500] [-0.2, 0.0] | $\begin{vmatrix} \mu_{sb}^2 \\ \lambda_6 \end{vmatrix}$ | $[4, 64] \times 10^4$ [-2.0, +2.0] | $\begin{vmatrix} \lambda_2 \\ \lambda_7 \end{vmatrix}$ | [-2.0, +2.0] [-0.01, +0.01] | $\begin{vmatrix} \lambda_3 \\ \lambda_8 \end{vmatrix}$ | [0.24, 0.28] [-1.0, +1.0] |
| | | | | • | Lepton sector | | | 1 | |
| $\begin{vmatrix} y^{e}_{24} \\ y^{e}_{34} \\ x^{L}_{34} \end{vmatrix}$ | $\begin{array}{c} [-0.7,+0.7] \\ [-1.0,+1.0] \\ [-1.0,+1.0] \end{array}$ | $\begin{vmatrix} y^{e}_{43} \\ x^{e}_{42} \\ x^{e}_{43} \end{vmatrix}$ | $\begin{array}{c} [-1.0,+1.0] \\ [-1.0,+1.0] \\ [-1.0,+1.0] \end{array}$ | $\begin{array}{c} y_{14}^{\nu} \\ y_{24}^{\nu} \\ y_{34}^{\nu} \end{array}$ | $[-1.0, +1.0] \times 10^{-10}$ $[-1.0, +1.0] \times 10^{-10}$ $[-1.0, +1.0] \times 10^{-10}$ | $egin{array}{c c} y_{14}^{\prime u} \ y_{24}^{\prime u} \ y_{34}^{\prime u} \end{array}$ | $\begin{array}{c} [-1.0,+1.0] \\ [-1.0,+1.0] \\ [-1.0,+1.0] \end{array}$ | $\begin{vmatrix} M_4^e \\ M_4^\nu \\ M_4^L \end{vmatrix}$ | $\pm [200, 1000]$ $\pm [200, 1000]$ $\pm [200, 1000]$ |
| | | | | | Quark sector | | | | |
| $\begin{vmatrix} y_{24}^{u} \\ y_{34}^{u} \\ x_{34}^{Q} \end{vmatrix}$ | $\begin{array}{c} [-1.0,+1.0] \\ [-1.4,+1.4] \\ [-1.0,+1.0] \end{array}$ | $\begin{vmatrix} y_{43}^{u} \\ x_{42}^{u} \\ x_{43}^{u} \end{vmatrix}$ | $\begin{array}{c} [-1.4,+1.4] \\ [-1.0,+1.0] \\ [-1.4,+1.4] \end{array}$ | $y^d_{14}\\y^d_{24}\\y^d_{34}$ | $egin{array}{l} [-0.7,+0.7] \ [-1.0,+1.0] \ [-1.0,+1.0] \end{array}$ | $\begin{vmatrix} y^d_{43} \\ x^d_{42} \\ x^d_{43} \end{vmatrix}$ | $\begin{array}{c} [-1.0,+1.0] \\ [-1.0,+1.0] \\ [-1.0,+1.0] \end{array}$ | $\begin{vmatrix} M_4^d \\ M_4^u \\ M_4^Q \end{vmatrix}$ | $\begin{array}{c} \pm \left[1200, 4000 \right] \\ \pm \left[1200, 4000 \right] \\ \pm \left[1200, 4000 \right] \end{array}$ |

Minimization of a χ^2 function to determine benchmark points.

SM masses, CKM elements, g-2

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| Scalar sector | | | | | | | | | | | | | |
|-----------------|-------------------|------------------|--------------------|-------------|--------|--------|--------|--|--|--|--|--|--|
| | BP1 | BP2 | BP3 | | BP1 | BP2 | BP3 | | | | | | |
| $\tan\beta$ | 13 | 8 | 12 | λ_1 | 0.258 | 0.258 | 0.258 | | | | | | |
| v_u | 245.3 | 244.3 | 245.2 | λ_2 | 0.514 | 0.153 | 0.623 | | | | | | |
| v_d | 18.9 | 30.5 | 20.4 | λ_3 | 0.257 | 0.260 | 0.256 | | | | | | |
| v_{ϕ} | 1015 | 1077 | 1012 | λ_4 | 0.552 | 0.304 | 0.167 | | | | | | |
| μ_u^2 | -7.8×10^3 | $-6.6	imes10^3$ | -7.6×10^3 | λ_5 | -0.039 | -0.072 | -0.061 | | | | | | |
| μ_d^2 | $-8.2 	imes 10^3$ | $-8.6	imes10^4$ | $-3.4 	imes 10^4$ | λ_6 | 0.370 | 0.487 | 0.663 | | | | | | |
| μ_{ϕ}^2 | -4.9×10^4 | -9.4×10^4 | -2.3×10^5 | λ_7 | 0.001 | 0.002 | 0.002 | | | | | | |
| $\mu_{ m sb}^2$ | $1.4 	imes 10^5$ | $1.9 	imes 10^5$ | 1.1×10^5 | λ_8 | 0.254 | 0.423 | 0.417 | | | | | | |
| | | | Mass pa | rameters | | | | | | | | | |
| | BP1 | BP2 | BP3 | | BP1 | BP2 | BP3 | | | | | | |
| M_4^u | -1317 | 1405 | 1334 | M_4^e | -517 | -575 | 533 | | | | | | |
| M_4^d | -3644 | 3068 | -2882 | M_4^{ν} | 204 | -212 | 217 | | | | | | |
| M_4^Q | -1384 | 1443 | 1322 | M_4^L | -206 | -222 | -202 | | | | | | |

Benchmark Points

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| Quark sector | | | | | Lepton sector | | | |
|--------------|--------|--------|--------|----------------------|----------------------|---------------------|---------------------|--|
| | BP1 | BP2 | BP3 | | BP1 | BP2 | BP3 | |
| y_{24}^u | -0.051 | -0.049 | 0.050 | y_{24}^e | 0.028 | -0.015 | 0.022 | |
| y_{34}^u | -0.980 | 1.185 | -1.024 | y_{34}^{e} | -0.895 | 0.612 | 0.790 | |
| x_{34}^{Q} | 0.924 | -0.842 | -0.877 | x_{34}^{L} | 0.616 | -0.729 | 0.724 | |
| y_{43}^{u} | 1.382 | 1.093 | -1.337 | y_{43}^{e} | -0.223 | 0.144 | -0.191 | |
| x_{42}^{u} | 0.550 | 0.821 | -0.595 | x_{42}^{e} | 0.156 | 0.165 | 0.188 | |
| x_{43}^{u} | 1.286 | 1.261 | 1.263 | x^{e}_{43} | -0.168 | 0.228 | -0.205 | |
| y_{14}^{d} | -0.022 | 0.035 | 0.026 | y_{14}^{ν} | -2×10^{-11} | 5×10^{-11} | 3×10^{-11} | |
| y_{24}^{d} | 0.096 | 0.151 | -0.113 | y_{24}^{ν} | 3×10^{-11} | 8×10^{-12} | 6×10^{-11} | |
| y_{34}^{d} | -0.684 | 0.274 | 0.267 | y_{34}^{ν} | -5×10^{-11} | 9×10^{-11} | 9×10^{-11} | |
| y_{43}^{d} | -0.672 | -0.489 | 0.656 | $y_{14}^{\prime u}$ | -0.824 | -0.674 | -0.674 | |
| x_{42}^{d} | -0.371 | -0.110 | 0.225 | $y_{24}^{\prime u}$ | -0.895 | -0.874 | -0.896 | |
| x^{d}_{43} | -0.160 | 0.072 | -0.127 | $y_{34}'^{\nu}$ | 0.701 | 0.744 | -0.812 | |

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Mass Spectrum

| SM fermions | | | | | | | | | | | |
|----------------------------|-------|-------|-------|-------------------------------------|-------|-------|-------|--|--|--|--|
| | BP1 | BP2 | BP3 | | BP1 | BP2 | BP3 | | | | |
| m_c | 1.262 | 1.282 | 1.259 | m_{μ} | 0.110 | 0.110 | 0.110 | | | | |
| m_t | 172.7 | 172.8 | 172.6 | $m_{	au}$ | 1.864 | 1.756 | 1.765 | | | | |
| m_s | 0.089 | 0.093 | 0.091 | $m_{\nu_2} \left[10^{-10} \right]$ | 4.659 | 6.587 | 0.252 | | | | |
| m_b | 4.169 | 4.196 | 4.175 | $m_{\nu_3} \left[10^{-10} \right]$ | 8.253 | 18.38 | 20.95 | | | | |
| NP fermions | | | | | | | | | | | |
| Quark sector Lepton sector | | | | | | | | | | | |
| | BP1 | BP2 | BP3 | | BP1 | BP2 | BP3 | | | | |
| M_{U_1} | 1495 | 1561 | 1440 | M_{E_1} | 487 | 596 | 554 | | | | |
| M_{U_2} | 1708 | 1842 | 1704 | M_{E_2} | 543 | 615 | 570 | | | | |
| M_{D_1} | 1534 | 1579 | 1464 | $M_{N_{1,2}}$ | 205 | 214 | 218 | | | | |
| M_{D_2} | 3655 | 3070 | 2888 | $M_{N_{3,4}}$ | 488 | 598 | 556 | | | | |
| Scalars | | | | | | | | | | | |
| | BP1 | BP2 | BP3 | | BP1 | BP2 | BP3 | | | | |
| M_{h_1} | 125 | 125 | 125 | M_{a_1} | 362 | 411 | 433 | | | | |
| M_{h_2} | 362 | 412 | 435 | M_{a_2} | 532 | 614 | 469 | | | | |
| M_{h_3} | 617 | 752 | 824 | $M_{h^{\pm}}$ | 384 | 423 | 440 | | | | |

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